

# DILEPTON PRODUCTION CROSS SECTION IN PP COLLISIONS AT $T_{\text{LAB}} = 3.5 \text{ GeV}$

M. I. Krivoruchenko  
ITEP, Moscow

- ▼ TÜBINGEN/ITEP MODEL - INTRODUCTION
- ▼ THRESHOLD OF PARTIAL WIDTHS IN DILEPTON CHANNELS  
 $M\Gamma_{\nu \rightarrow e^+e^-}(M)$ , production cross section and  
constraints for  $1/g_{\nu}(M)$
- ▼ ETA-MESON CONTRIBUTION

---

Ad.Hoc Workshop on NN collisions with HADES  
Darmstadt, 12 August 2011

# TÜBINGEN/ITEP MODEL - INTRODUCTION

---

Dilepton production cross section can be calculated using the inclusive vector meson production cross sections:

$$\frac{d\sigma(s, M)^{pp \rightarrow e^+ e^- X}}{dM^2} = \sum_M \frac{d\sigma(s, M)^{pp \rightarrow MX'}}{dM^2} B(M)^{M \rightarrow e^+ e^- X}.$$

where

$$B(M)^{M \rightarrow e^+ e^- X} = \frac{\Gamma(M)^{M \rightarrow e^+ e^- X}}{\Gamma_{tot}^M(M)}$$

In order to disentangle various contributions, we decompose the cross section into the pole and background parts:

$$d\sigma(s, M)^{pp \rightarrow MX} = d\sigma(s, M)_P^{pp \rightarrow VX} + d\sigma(s, M)_B^{pp \rightarrow MX}$$

$$d\sigma(s, \mu)^{pp \rightarrow MX} = \sigma(s)^{pp \rightarrow MX} \frac{1}{\pi} \frac{\mu \Gamma_{tot}^M(\mu) d\mu^2}{(\mu^2 - m_M^2)^2 + (\mu \Gamma_{tot}^M(\mu))^2} \\ \times \sum_{n=0}^{N_\pi} w_n C_n \Phi_{3+n}(\sqrt{s} \dots)$$

where

$$\Phi_{3+n}(\sqrt{s} \dots) = \Phi(\sqrt{s}, m_N, m_N, \mu, \underbrace{\mu_\pi, \dots, \mu_\pi}_{+ \text{ pions } \dots}),$$

$$\sum_{n=0}^{N_\pi} w_n = 1,$$



$$C_n^{-1} = \int_{\mu_{TH}^2}^{(\sqrt{s} - 2m_N - n\mu_\pi)^2} \frac{1}{\pi} \frac{\mu \Gamma_{tot}^M(\mu) d\mu^2}{(\mu^2 - m_M^2)^2 + (\mu \Gamma_{tot}^M(\mu))^2} \Phi_{3+n}(\sqrt{s} \dots).$$

The **binomial distribution** is based on the idea of a Bernoulli trial.

Applying for pion multiplicity

$$W_n = \frac{N_\pi!}{n!(N_\pi - n)!} p^n (1 - p)^{N_\pi - n}$$

The maximum number of pions

$$N_\pi = \left[ (\sqrt{s} - 2m_N - m_M) / \mu_\pi \right]$$

To fix  $W_n$  (i.e. parameter  $p$ ) one has to know **two** cross sections.

Examples:

$$\sigma(s)^{pp \rightarrow NNM} \quad \& \quad \sigma(s)^{pp \rightarrow NNM\pi},$$

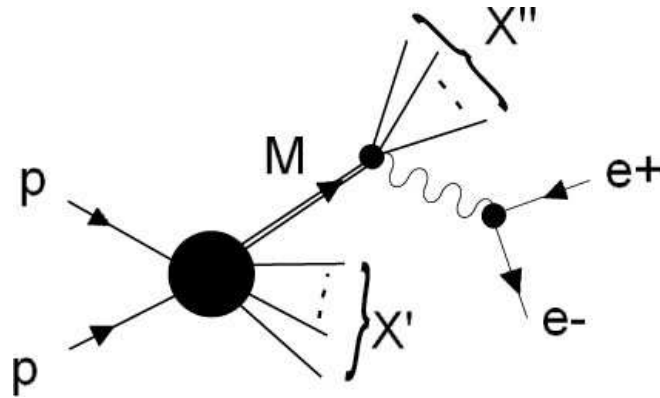
$$\sigma(s)^{pp \rightarrow MX} \quad \& \quad \sigma(s)^{pp \rightarrow NNM}.$$

In the last case

$$\frac{\sigma(s)^{pp \rightarrow NNM}}{\sigma(s)^{pp \rightarrow NNM\pi}} = (1 - p)^{N_\pi}.$$

## Phenomenology:

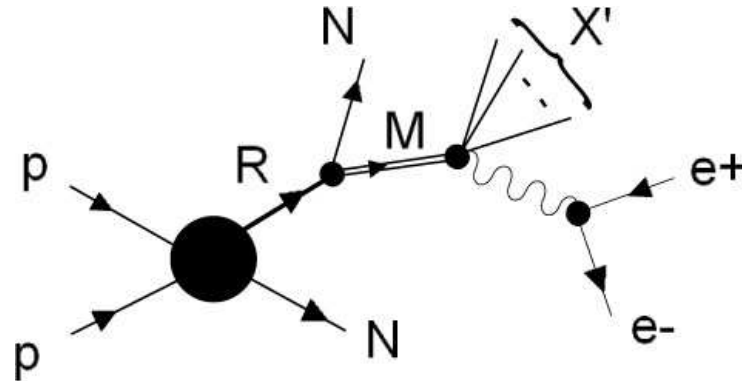
$$\frac{d\sigma(s, M)^{NN \rightarrow e^+ e^- X}}{dM^2} = \sum_M \int d\mu^2 \frac{d\sigma(s, \mu)^{NN \rightarrow MX'}}{d\mu^2} \frac{dB(\mu, M)^{M \rightarrow e^+ e^- X''}}{dM^2}$$



$\mu$ - invariant mass of  $M$ ,  $M$  - invariant mass of  $e^+e^-$ ,  
 $X'' =$  mesons,  
 $X' = NN +$  pions.

## Resonance model:

$$\frac{d\sigma(s, M)^{NN \rightarrow e^+ e^- X}}{dM^2} = \sum_R \int_{(m_N + M)^2}^{(\sqrt{s} - m_N)^2} d\mu^2 \frac{d\sigma(s, \mu)^{NN \rightarrow NR}}{d\mu^2} \times \sum_M \frac{dB(\mu, M)^{R \rightarrow MN \rightarrow e^+ e^- X' N}}{dM^2}$$



$\mu$ - invariant mass of  $R$ ,  $M$  - invariant mass of  $e^+ e^-$ ,  
 $X'$  = mesons

subthreshold

$$\sigma(s)^{excl.} = \sigma(s)^{NN \rightarrow RN \rightarrow e^+ e^- NX'N} = w_0 \sigma(s)^{NN \rightarrow e^+ e^- X},$$

$$\sigma(s)^{excl.+n\pi} = w_n \sigma(s)^{NN \rightarrow e^+ e^- X},$$

$$\sigma(s)^{incl.} = \sum_{n=0}^{N_\pi} \sigma(s)^{excl.+n\pi} = \sigma(s)^{NN \rightarrow e^+ e^- X}.$$

We used suppression factor  $0 < S_F < 1$  such that

$$d\sigma(s, M)^{excl.} = S_F d\sigma(s, M)^{NN \rightarrow RN \rightarrow e^+ e^- NX'N} \\ + (1 - S_F) w_0 d\sigma(s, M)^{NN \rightarrow e^+ e^- X},$$

$S_F = 0$  around the peak and  $S_F = 1$  at small invariant masses

# THRESHOLD OF PARTIAL WIDTHS IN DILEPTON CHANNELS

---

Multichannel Breit-Wigner formula:

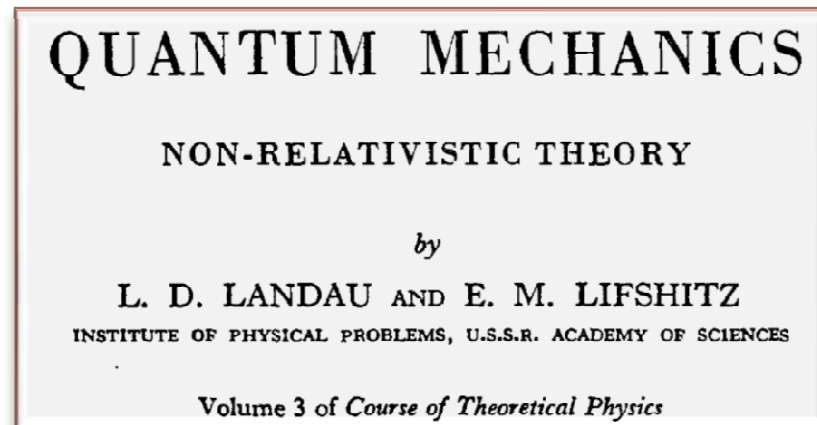
$$f_{ab}^{(l)} = \frac{1}{2ik_a} (e^{2i\delta_a} - 1) \delta_{ab} - \frac{1}{2\sqrt{(k_a k_b)}} e^{i(\delta_a + \delta_b)} \frac{\Gamma M_{ab}}{E - E_0 + \frac{1}{2}i\Gamma}$$

where

$$M_{ab} = \pm \sqrt{(\Gamma_a \Gamma_b) / \Gamma}$$



from § 145 of



Every channel has its own threshold



Every channel has its own threshold, e.g.,

$$\omega \rightarrow \pi^+ \pi^- \pi^0, \quad \sqrt{s_{TR}} = 3\mu_\pi,$$

$$\omega \rightarrow e^+ e^- \pi^0, \quad \sqrt{s_{TR}} = \mu_\pi + 2m_e,$$

$$\omega \rightarrow e^+ e^-, \quad \sqrt{s_{TR}} = 2m_e.$$

$$\begin{aligned} \frac{d\sigma(s, M)^{NN \rightarrow e^+ e^- X}}{dM^2} &= \sum_M \int d\mu^2 \frac{d\sigma(s, \mu)^{NN \rightarrow MX'}}{d\mu^2} \frac{dB(\mu, M)^{M \rightarrow e^+ e^- X}}{dM^2} \\ &= \sum_M \int \sigma(s)^{NN \rightarrow MX'} \frac{1}{\pi} \frac{\mu \Gamma_{tot}^M(\mu) d\mu^2}{(\mu^2 - m_M^2)^2 + (\mu \Gamma_{tot}^M(\mu))^2} \\ &\quad \times \frac{d}{dM^2} \frac{\Gamma(\mu, M)^{M \rightarrow e^+ e^- X}}{\Gamma_{tot}^M(\mu)} \end{aligned}$$

Every channel has its own threshold, e.g.,

$$\omega \rightarrow \pi^+ \pi^- \pi^0, \quad \sqrt{s_{TR}} = 3\mu_\pi,$$

$$\omega \rightarrow e^+ e^- \pi^0, \quad \sqrt{s_{TR}} = \mu_\pi + 2m_e,$$

$$\omega \rightarrow e^+ e^-, \quad \sqrt{s_{TR}} = 2m_e.$$

$$\begin{aligned} \frac{d\sigma(s, M)^{NN \rightarrow e^+ e^- X}}{dM^2} &= \sum_M \int d\mu^2 \frac{d\sigma(s, \mu)^{NN \rightarrow MX'}}{d\mu^2} \frac{dB(\mu, M)^{M \rightarrow e^+ e^- X}}{dM^2} \\ &= \sum_M \int \sigma(s)^{NN \rightarrow MX'} \frac{1}{\pi} \frac{\mu \Gamma_{tot}^M(\mu) d\mu^2}{(\mu^2 - m_M^2)^2 + (\mu \Gamma_{tot}^M(\mu))^2} \\ &\quad \times \frac{d}{dM^2} \frac{\Gamma(\mu, M)^{M \rightarrow e^+ e^- X}}{\Gamma_{tot}^M(\mu)} \end{aligned}$$

Every channel has its own threshold, e.g.,

$$\omega \rightarrow \pi^+ \pi^- \pi^0, \quad \sqrt{s_{TR}} = 3\mu_\pi,$$

$$\omega \rightarrow e^+ e^- \pi^0, \quad \sqrt{s_{TR}} = \mu_\pi + 2m_e,$$

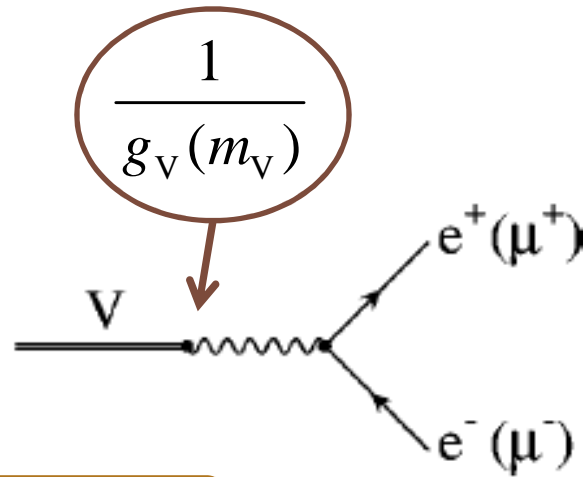
$$\omega \rightarrow e^+ e^-, \quad \sqrt{s_{TR}} = 2m_e.$$

$$\begin{aligned} \frac{d\sigma(s, M)^{NN \rightarrow e^+ e^- X}}{dM^2} &= \sum_M \int d\mu^2 \frac{d\sigma(s, \mu)^{NN \rightarrow MX'}}{d\mu^2} \frac{dB(\mu, M)^{M \rightarrow e^+ e^- X}}{dM^2} \\ &= \sum_M \int \sigma(s)^{NN \rightarrow MX'} \frac{1}{\pi} \frac{\mu \Gamma_{tot}^M(\mu) d\mu^2}{(\mu^2 - m_M^2)^2 + (\mu \Gamma_{tot}^M(\mu))^2} \end{aligned}$$

in various event generators

$$\times \frac{d}{dM^2} \frac{\Gamma(\mu, M)^{M \rightarrow e^+ e^- X}}{\Gamma_{tot}^M(m_M)??}$$

Direct decay modes



$$M\Gamma_{V \rightarrow e^+e^-}(M) \equiv \mathfrak{I}\Sigma_V(M^2)$$

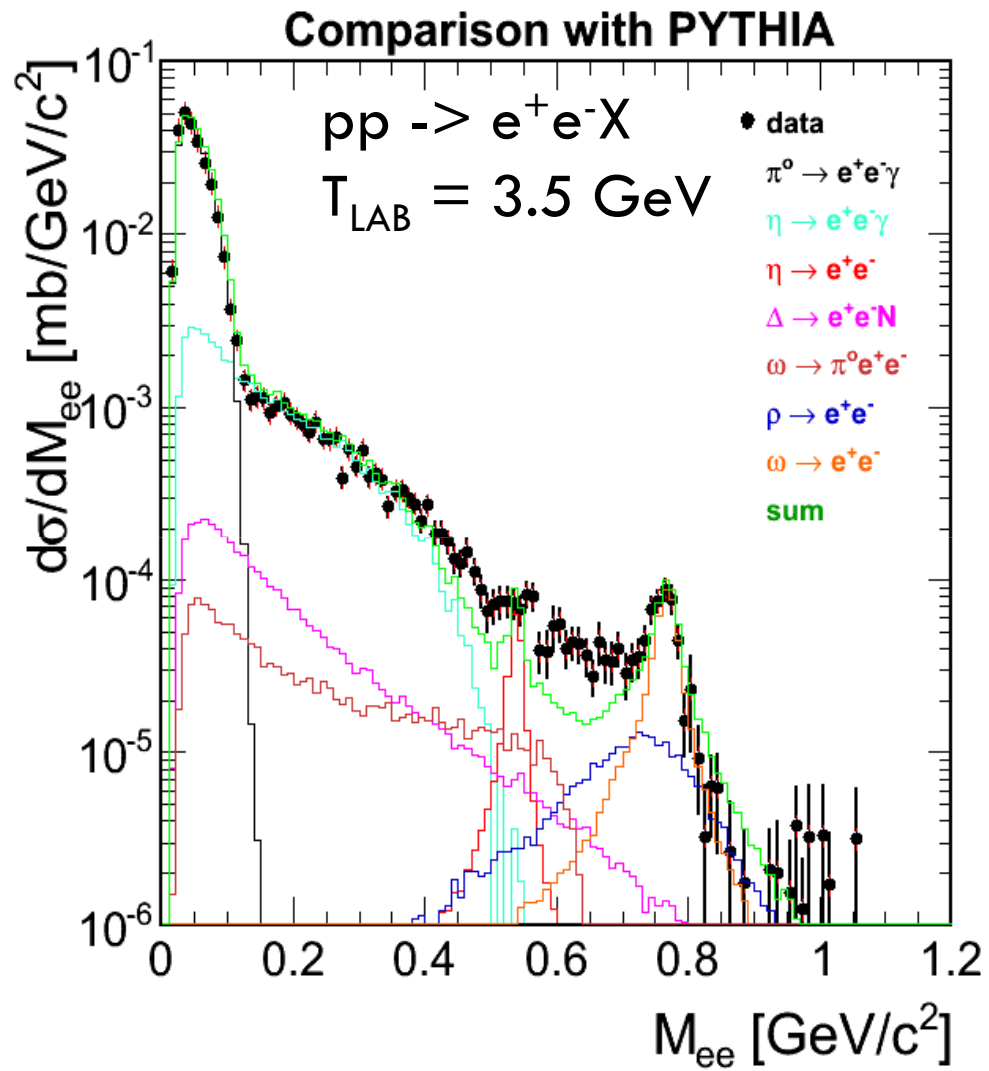
← Self energy

$$= m_V \Gamma_{V \rightarrow e^+e^-}(m_V)$$

$$\times \frac{M^2 + 2m_e^2}{m_V^2 + 2m_e^2} \left( \frac{m_V}{M} \right)^4 \frac{\Phi_2(M, m_e, m_e)}{\Phi_2(m_V, m_e, m_e)}$$

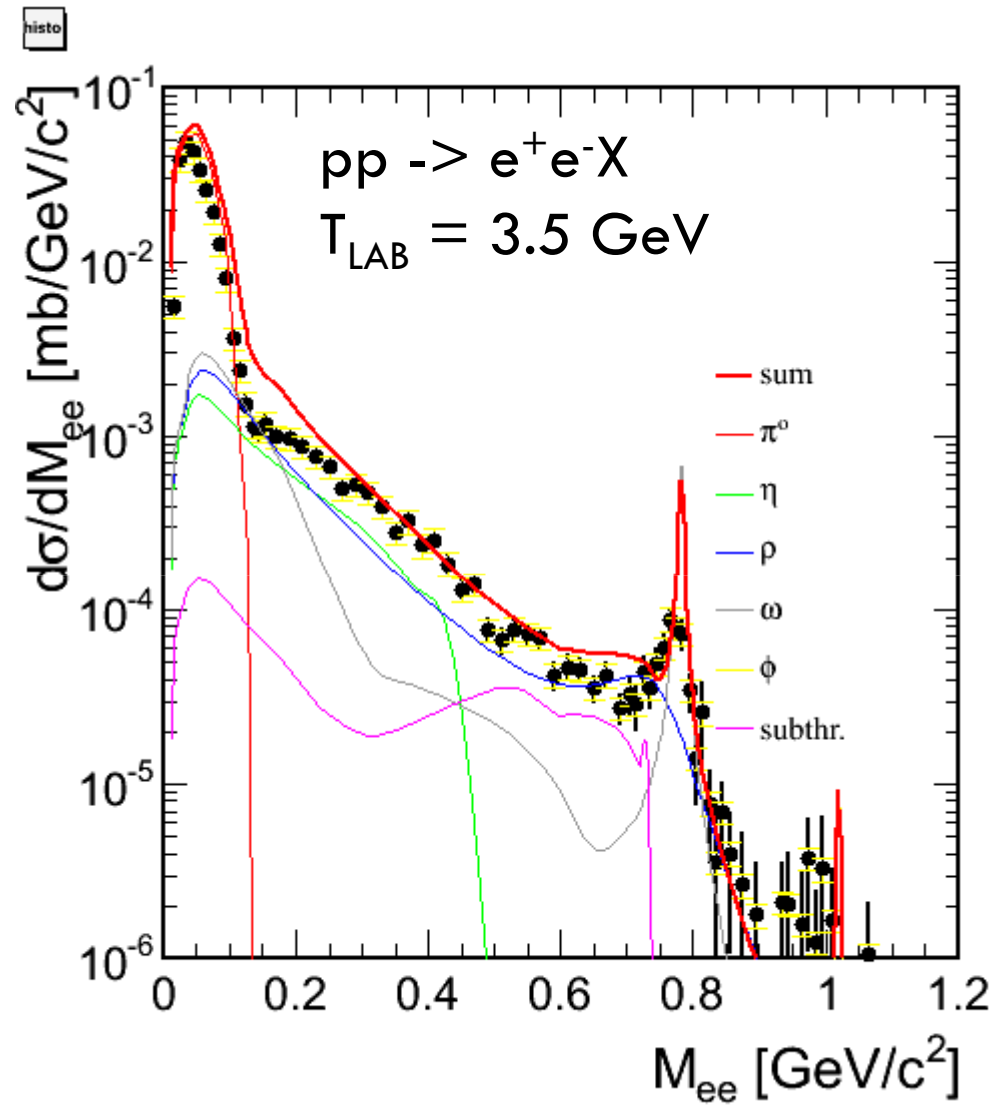
The width grows as  $1/M^3$  at small invariant masses

$$m_V \Gamma_{V \rightarrow e^+e^-}(m_V) \sim \frac{1}{g_V^2(m_V)} \rightarrow \frac{1}{g_V^2(M)} = \text{but assumed constant}$$



A. Rustamov, GSI, Darmstadt, April 18, 2011

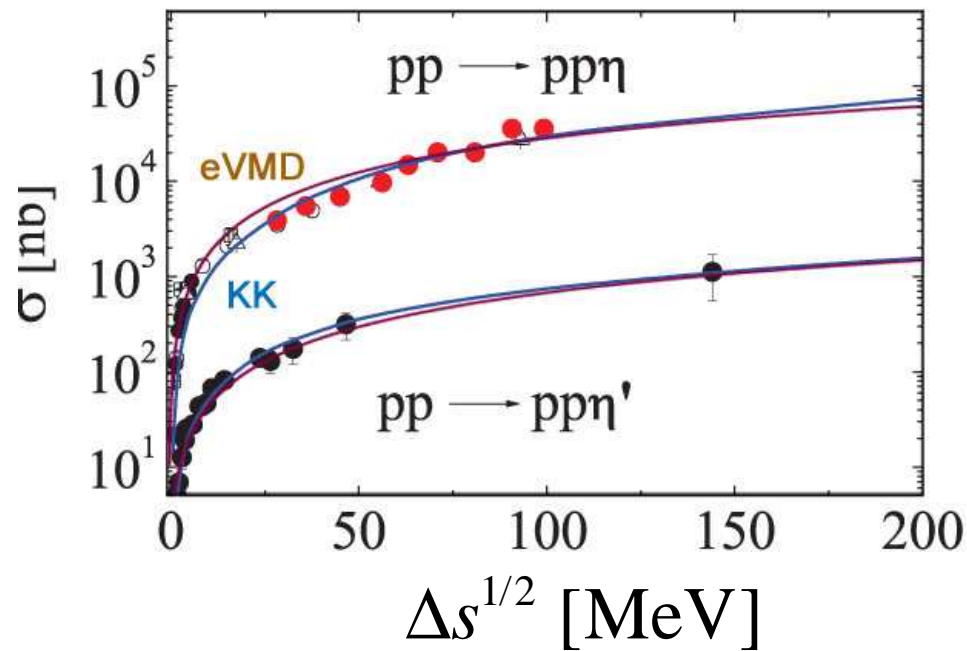
# Comparison with Tübingen/ITEP model



MIK, June 2011

[without smearing]

# ETA-MESON CONTRIBUTION



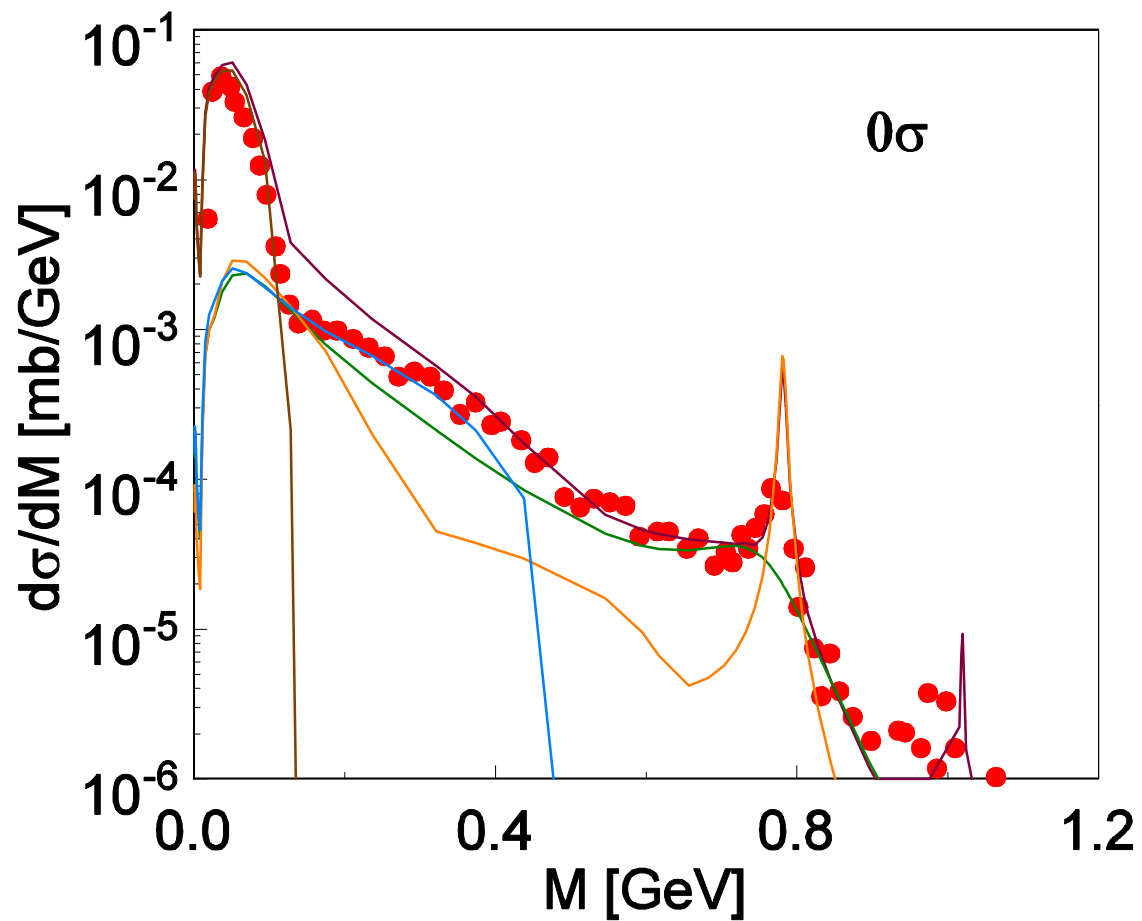
Comparison with  
Kaptari and Kampfer, 2007

Ad.Hoc fit: 
$$\xi = \frac{s}{s_0}, \quad \begin{cases} a = 0.50 \text{ mb,} \\ b = 1.21, \\ c = 1.93. \end{cases}$$

$$\sigma_{pp \rightarrow \eta X}(T) = a(\xi - 1)^b \xi^c$$

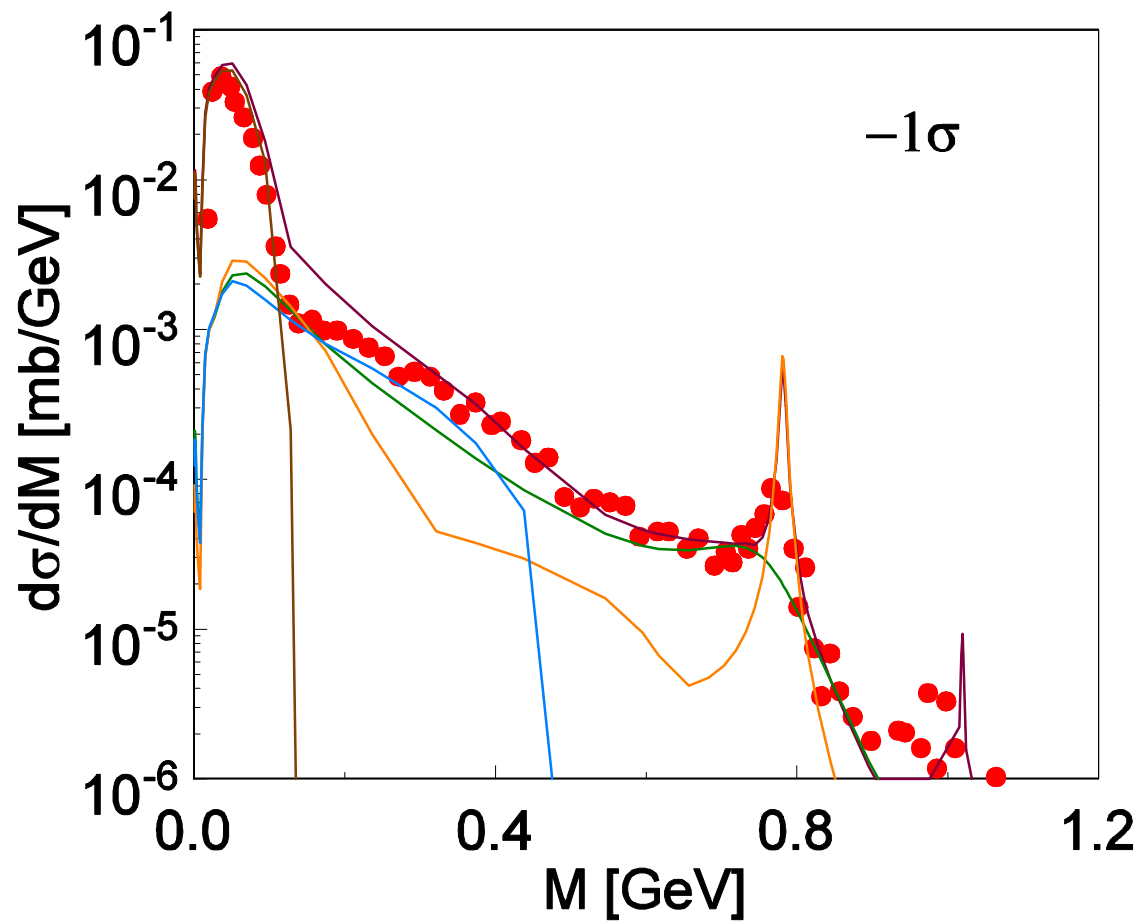
$$\begin{aligned} \sigma_{pp \rightarrow \eta X}(T = 3.5 \text{ GeV}) \\ = 0.94 \text{ mb } (-1 \sigma) \end{aligned}$$

Sensitivity of the HADES data to the  $\eta$ -meson  
according to Tübingen/ITEP model

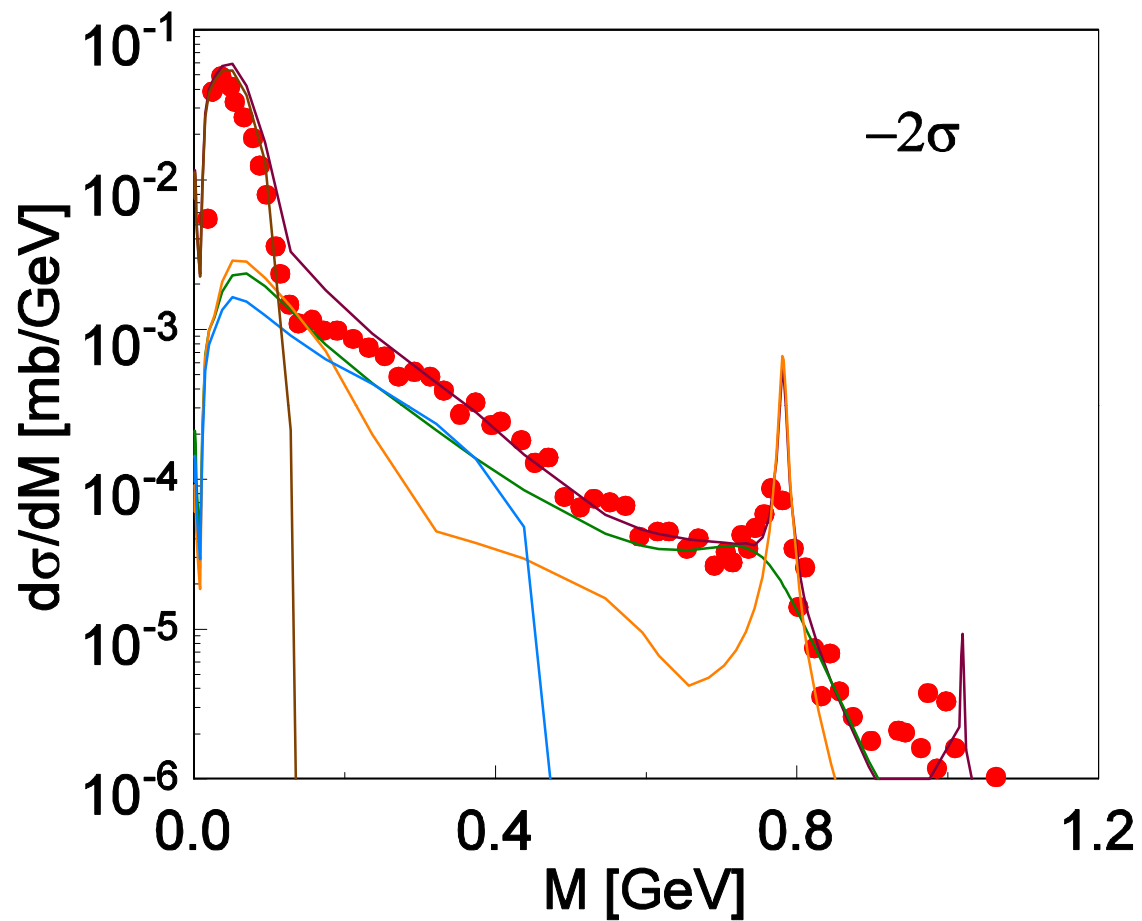




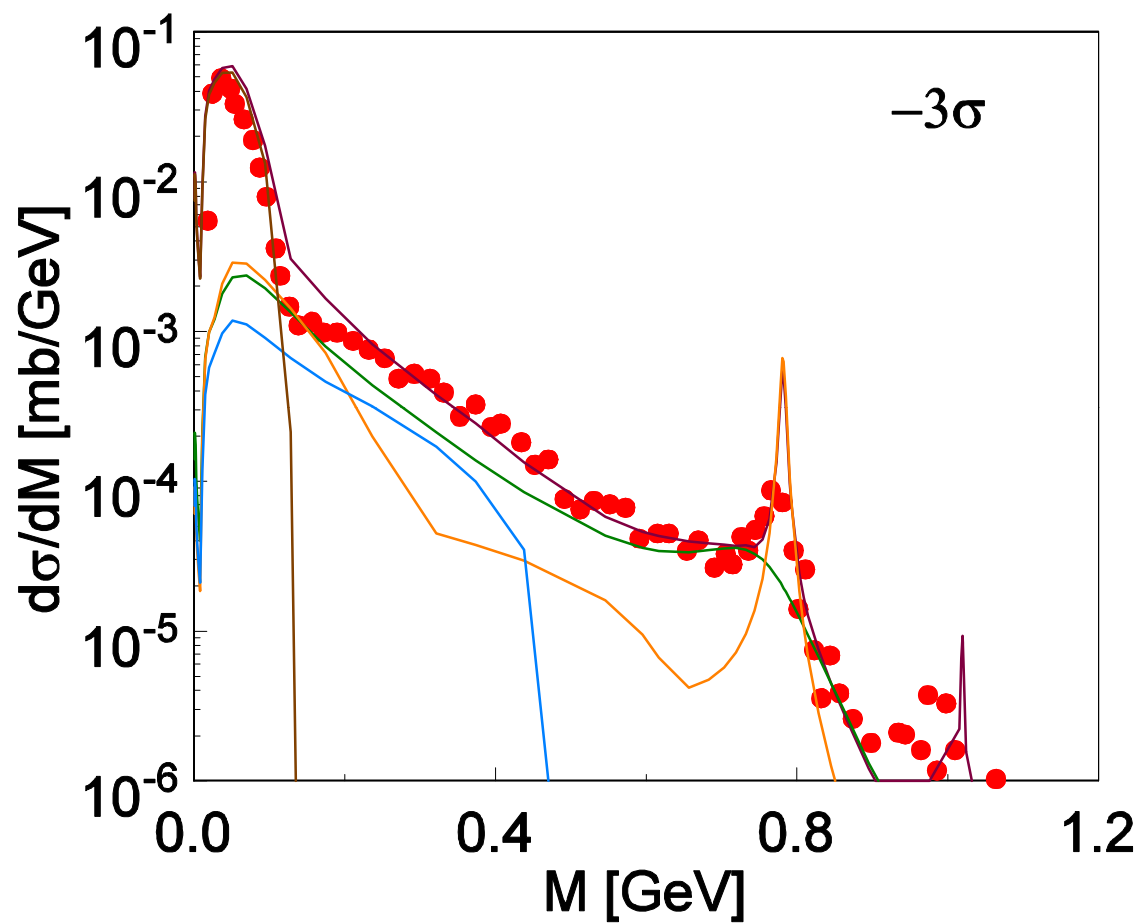
Sensitivity of the HADES data to the  $\eta$ -meson  
according to Tübingen/ITEP model



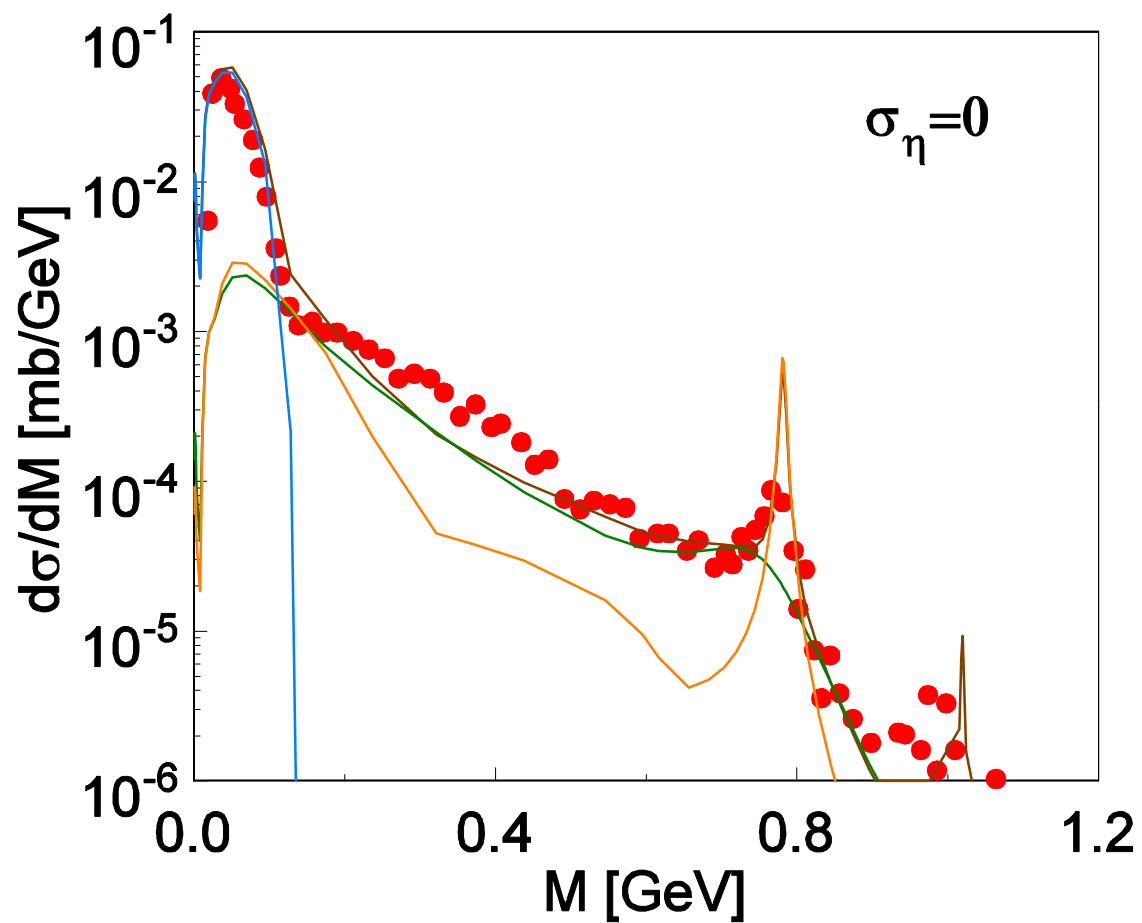
Sensitivity of the HADES data to the  $\eta$ -meson  
according to Tübingen/ITEP model

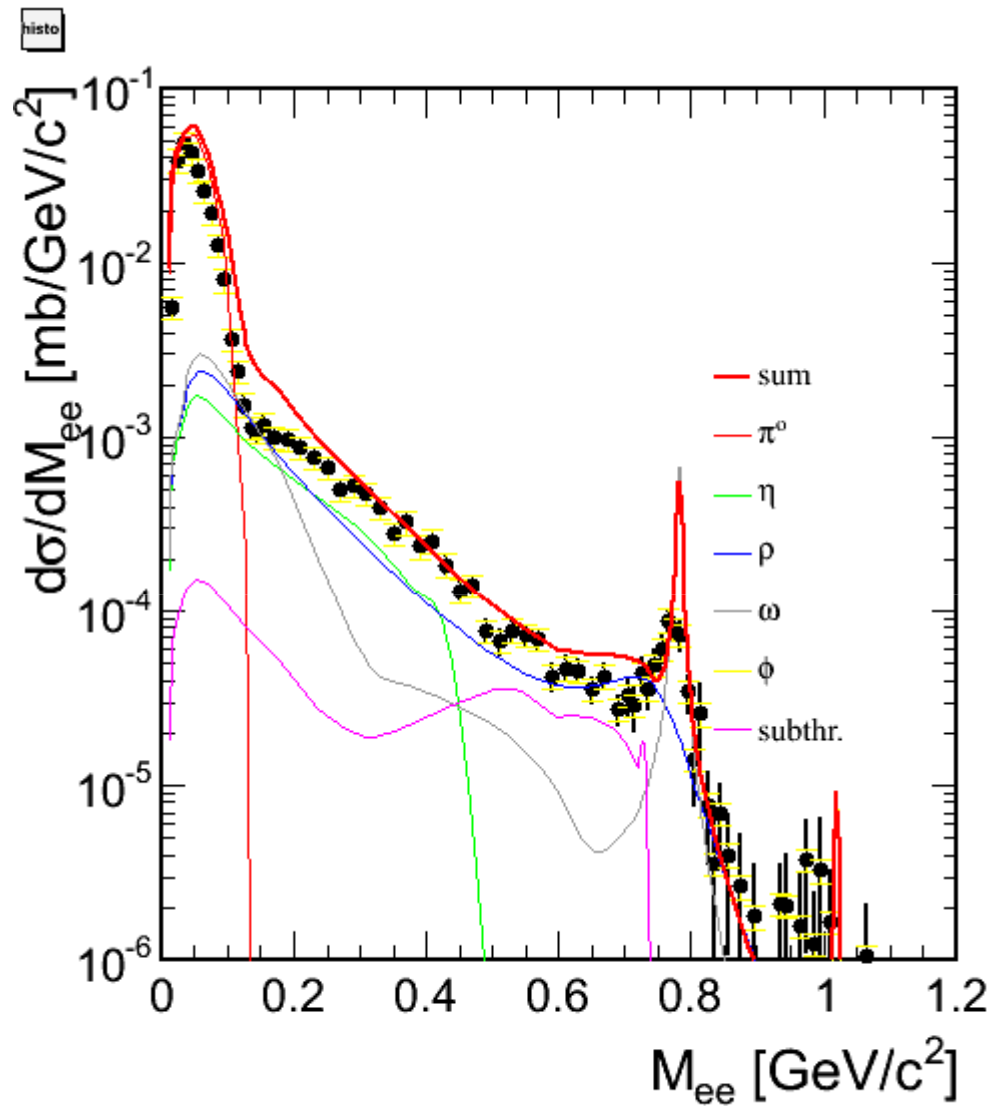


Sensitivity of the HADES data to the  $\eta$ -meson  
according to Tübingen/ITEP model



Sensitivity of the HADES data to the  $\eta$ -meson  
according to Tübingen/ITEP model





Comparison with  
the HADES data gives  
constraint:

$$\frac{1}{g_V^2(M)} = O(1) \text{ at } M \rightarrow 0.$$

Possible option:

$$\frac{1}{g_V^2(M)} \sim |\Psi_{q\bar{q}}(0)|^2 \sim M^3 \quad (?)$$

# CONCLUSIONS

---

- ▼ TÜBINGEN/ITEP MODEL IS IN REASONABLE AGREEMENT WITH HADES DATA AT 3.5 GEV
- ▼ THRESHOLD OF PARTIAL WIDTHS IN THE DILEPTON CHANNELS IS TWICE THE ELECTRON MASS
- ▼ FROM THE LOW-M BEHAVIOR  $1/g_V(M) = O(1)$  for  $M \rightarrow 0$
- ▼ THE HADES DATA ARE NOT VERY SENSITIVE TO ETA-MESON WHEN THE DILEPTON THRESHOLDS ARE SET CORRECTLY

