



RICH COLLABORATION

Justus-Liebig-Universität Gießen

Bergische Universität Wuppertal

PNPI Gatchina

Gesellschaft für Schwerionenforschung GSI

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- ① Motivation & Introduction
 - i. The CBM Experiment
 - ii. The RICH Concept
 - iii. RICH Prototype & Electronics
- ② Radiation Hardness of the Photon Detector
- ③ Geometry Optimisation & PMT Shielding Box
- ④ Mirror & PMT Holding Structure
- ⑤ Summary

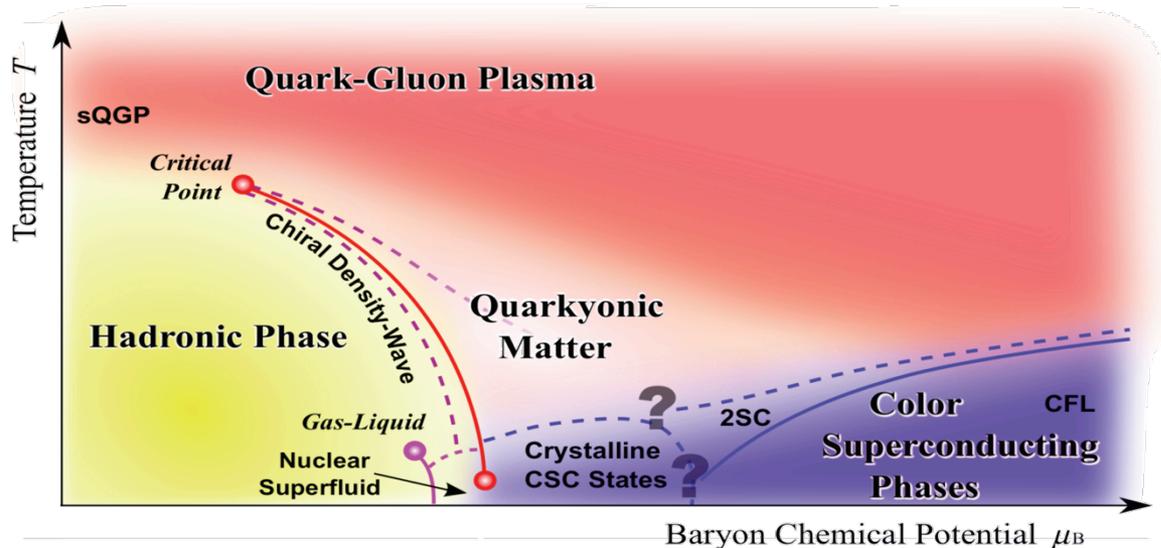
MOTIVATION

Heavy-Ion Collisions: study the properties of nuclear matter under extreme conditions and map the **QCD phase diagram**

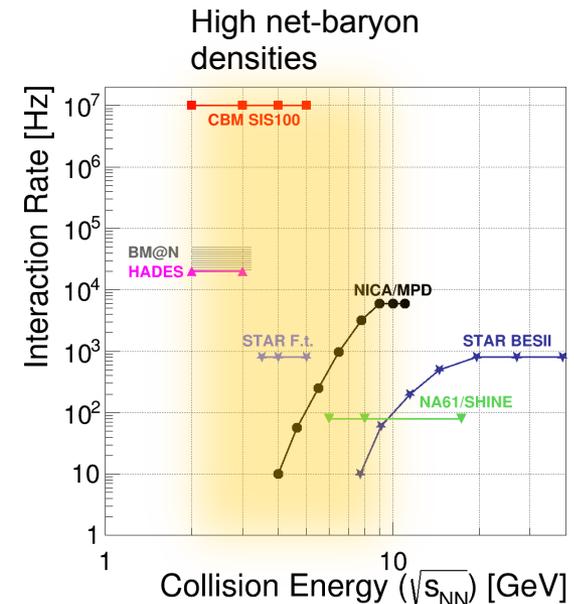
Different $T-\mu_B$ regimes:

- **High T , low μ_B :** lattice QCD and high quality data RHIC and LHC
- **Low T , high μ_B :** largely unknown structures:
 - ① New phases besides QGP and HG (Quarkyonic)
 - ② Nature of phase transitions
 - ③ Existence and location of CP

→ new experimental campaign in Dubna, RHIC, SPS, J-PARC, and FAIR(**CBM**)



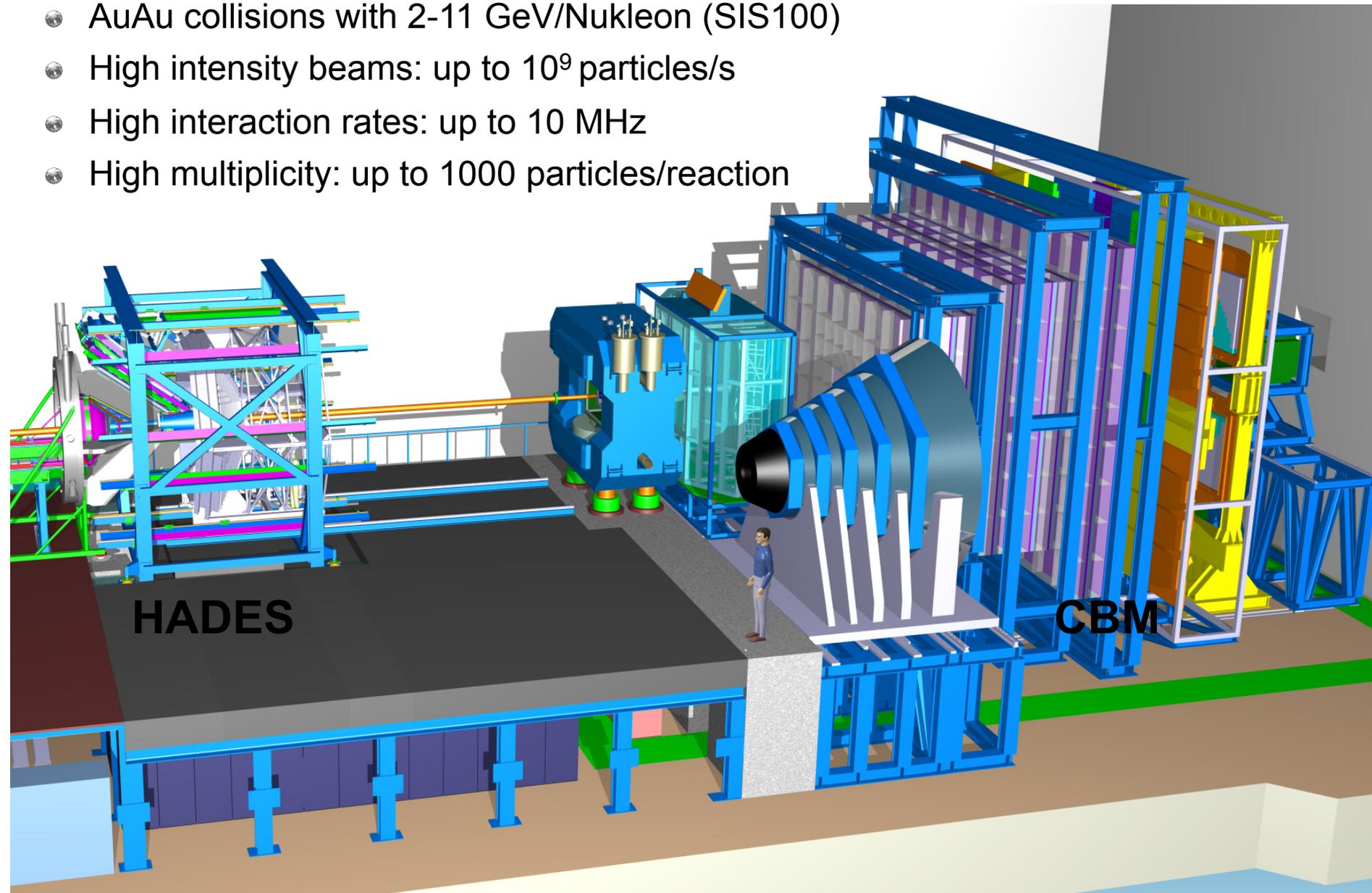
K. Fukushima and T. Hatsuda, Rept. Prog. Phys. 74 (2011) 014001



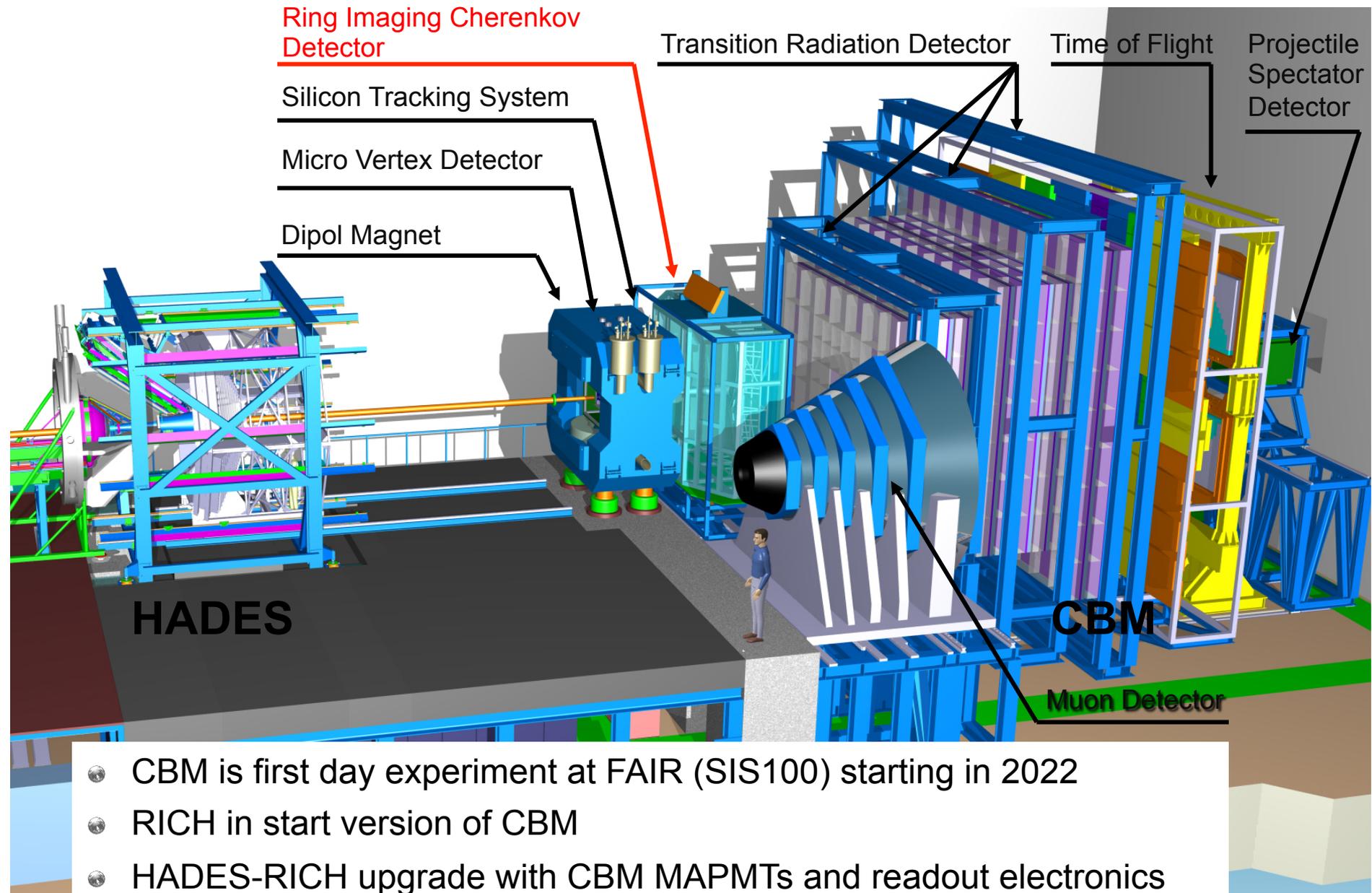
arXiv:1607.01487

THE CBM EXPERIMENT @ FAIR

- AuAu collisions with 2-11 GeV/Nukleon (SIS100)
- High intensity beams: up to 10^9 particles/s
- High interaction rates: up to 10 MHz
- High multiplicity: up to 1000 particles/reaction



THE CBM EXPERIMENT @ FAIR



THE RICH CONCEPT

Aim: **efficient** and **clean** electron identification for momenta below 8GeV/c

Challenges: ① high rates and high particle density ② located directly behind magnet

Strategy: build a **stable**, **robust** and **fast** detector relying on components from industry

$$P_{th} = \frac{m}{125}, \delta_{CO_2} = 4.3 \times 10^{-4}$$
$$e^- \quad 17.4 \text{ GeV} \quad K^{\pm} \quad 17 \text{ GeV}$$
$$\pi^{\pm} \quad 4.6 \text{ GeV} \quad p \quad 3.2 \text{ GeV}$$

RADIATOR

- CO_2 : $Y_{th} = 33$, $p_{\pi,th} = 4.65 \text{ GeV}/c$
- Length=1.7 m, $V \approx 30 \text{ m}^3$



MIRROR

- SIMAX-glass with Al+MgF₂ coverage
- $R = 3\text{m}$, $d \leq 6\text{mm}$, 11.8 m^2
- 72 tiles of $40 \times 40 \text{ cm}^2$

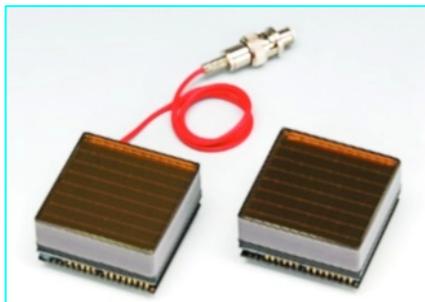
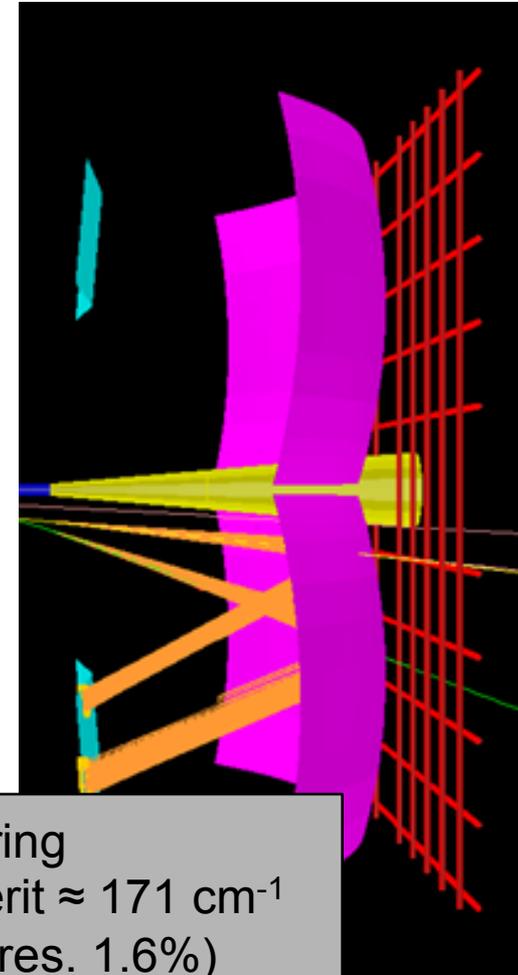


PHOTO DETECTOR

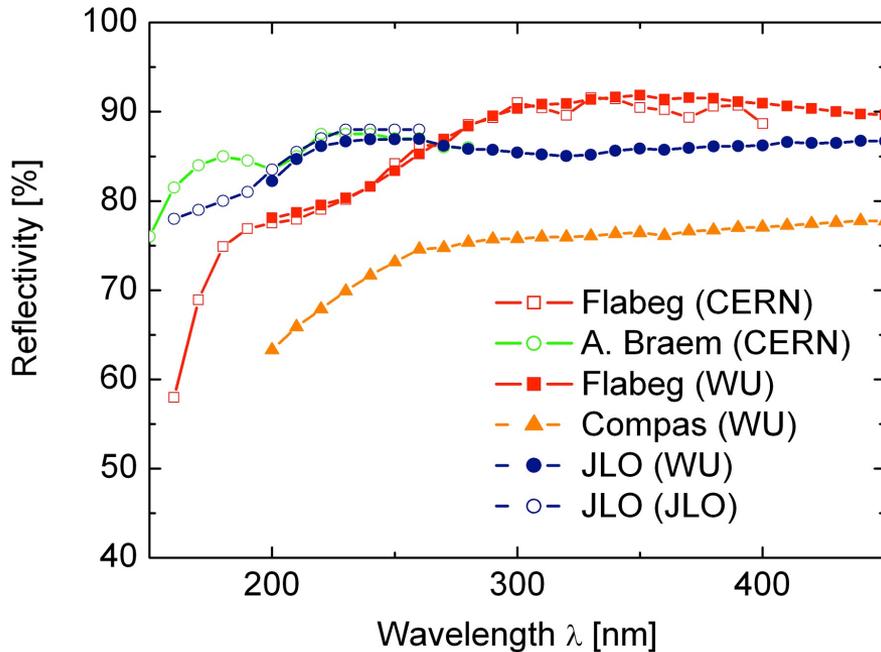
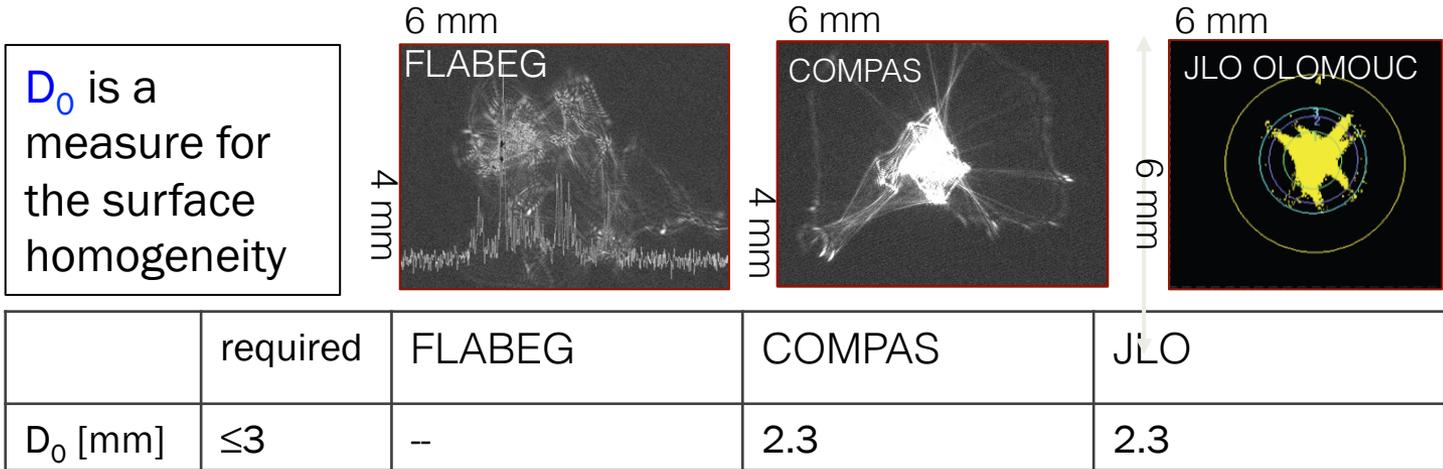
- 2.4 m^2 , 55k Ch.
- MAPMT: H12700 series
- Enhance sensitivity in the UV with WLS

- 28 photons/ring
- Figure of Merit $\approx 171 \text{ cm}^{-1}$
- $r_e = 4.56 \text{ cm}$ (res. 1.6%)



MIRRORS

Mirrors from three manufacturers were tested upon **surface homogeneity** and **reflectivity**



Best results with JL OLOMOUC

PHOTON DETECTORS (MAPMT)

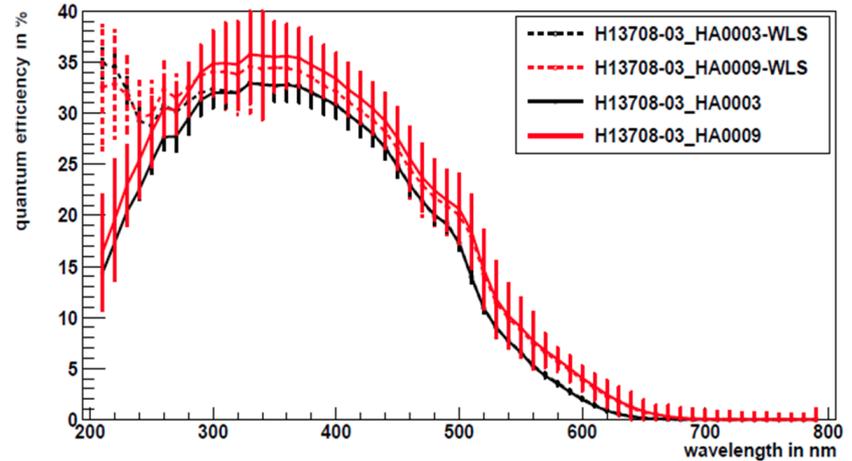
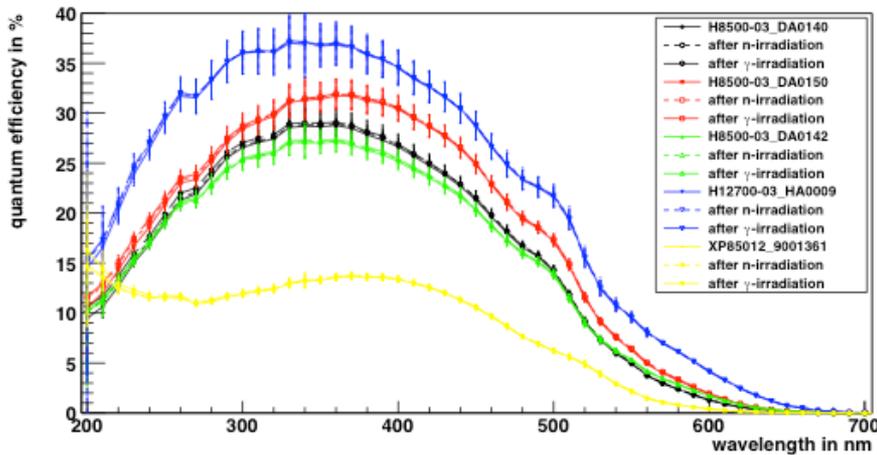
HAMAMATSU: Multi-anode Photomultiplier Tubes (MAPMT)

- ① **H10966**: 8-dyn., SBA photo cathode good QE but bad single photon response
- ② **R11265**: 12-dyn., SBA photo cathode best results but small & expensive
- ③ **H8500**: 12-dyn., BA photo cathode best choice

- ④ **H12700**:
 - 10-dyn., dyn. system as in R11265,
 - geometry of H8500,
 - advanced BA photo cathode
 - 1100 pcs ordered in Sept 2015
 - Up to now about 500 pcs delivered

- Pixel resolution
- Single photon response
- Noise
- Quantum efficiency w/ & w/o
WaveLength-Shifting films

WLS: NIM A 783 (2015) 43-50



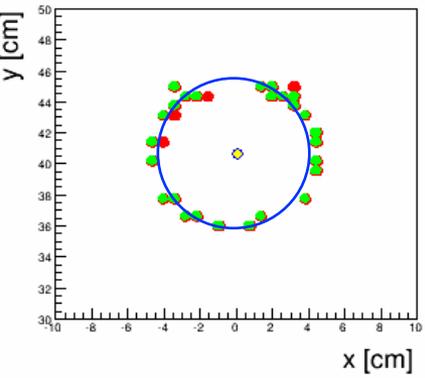
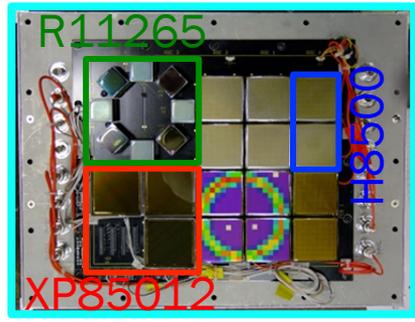
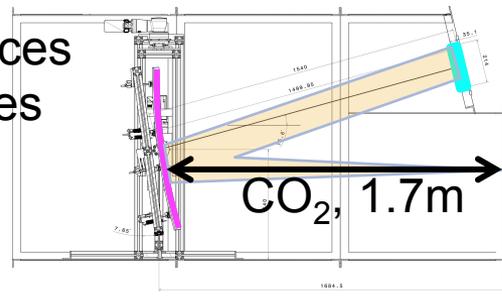
PHOTONIS (XP85012): Micro Channel Plate (MCP)

Poster: J. Förtsch (B4)

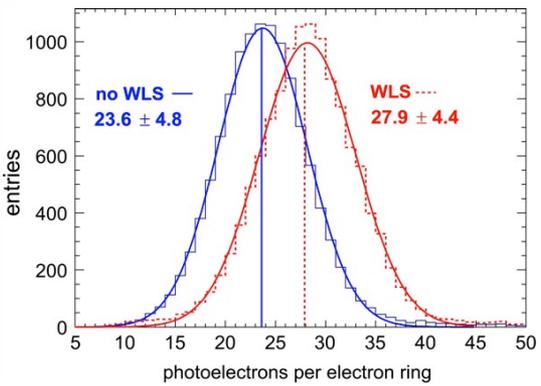
THE RICH PROTOTYPE

Laterally scaled prototype: Modules have the same dimensions and properties as foreseen in the RICH concept.

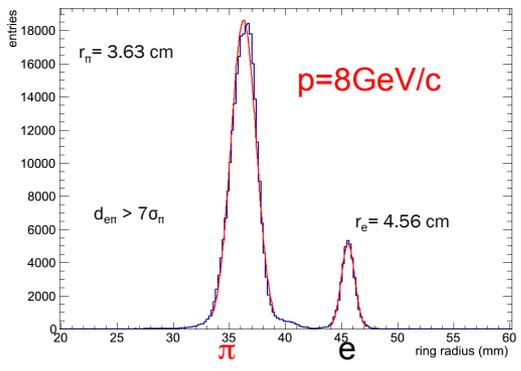
- ① Verified RICH concept & gained experiences
- ② Determined components & fixed tolerances
- ③ Tested software and gas system
- ④ Test of electronics and DAQ



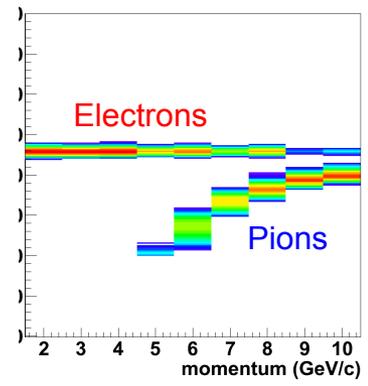
Single (fitted) ring



of hits per ring



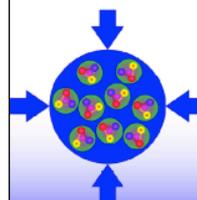
ring radius



Pion suppression factor = 3500 @ p=8 GeV/c

Poster: S. Lebedev (A25)

Poster: E. Ovcharenko (A11)



Compressed Baryonic Matter Experiment

Technical Design Report for the CBM

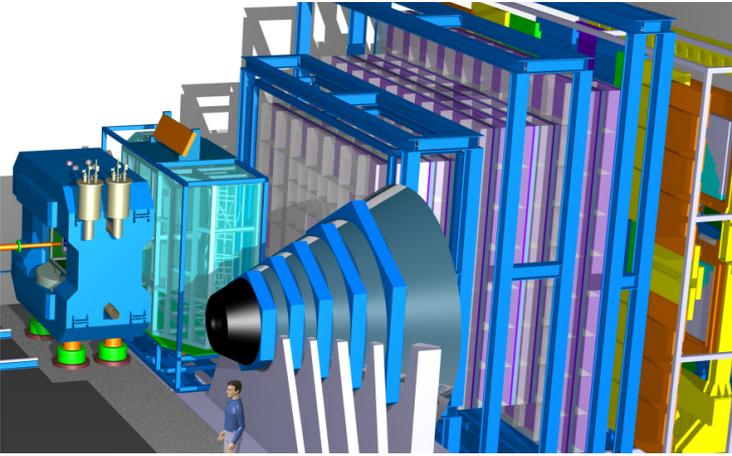
Ring Imaging Cherenkov (RICH) Detector

The CBM Collaboration



April 2013

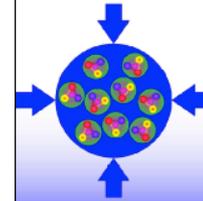
CONCEPT APPROVED



Besides electronics ...
Three issues kept open:

RICH is located ...

- ① not far from IP → high radiation environment
→ Test PMTs upon radiation hardness
- ② directly behind the magnet → stray field
→ re-optimize geometry to escape the field influence; shielding box
- ③ in front of other sub-detectors (TRD, TOF)
→ Holding structure with low radiation length

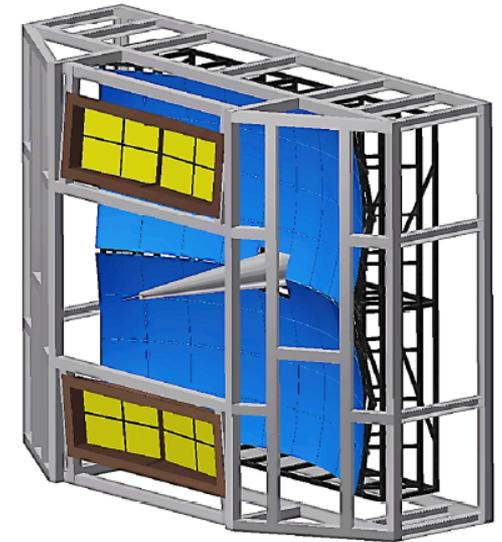


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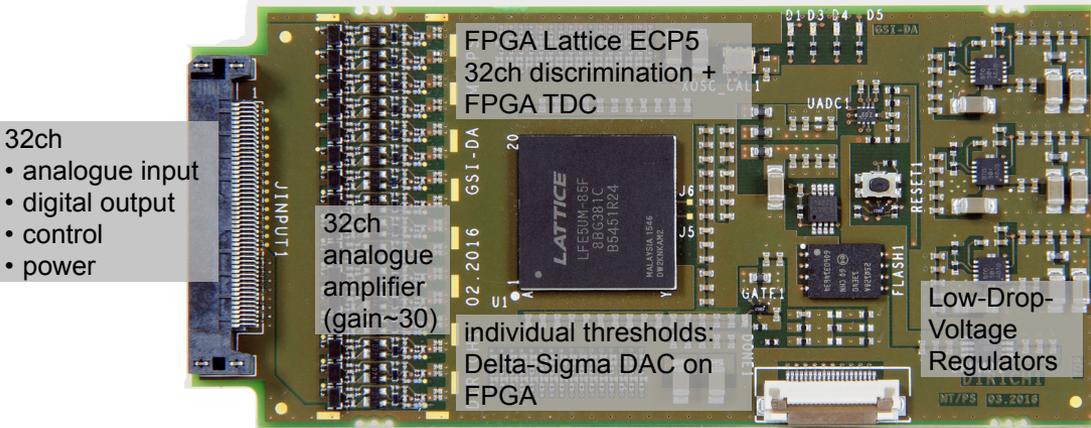
Ring Imaging Cherenkov (RICH) Detector

The CBM Collaboration



April 2013

READOUT CONCEPT



DiRICH:

- Combined development between PANDA, HADES, and CBM
- FPGA-TDC readout based on HADES TRB3 board
- **Excellent time resolution:** limits by sensor
- **Limited amplitude information** via Time-over-Threshold

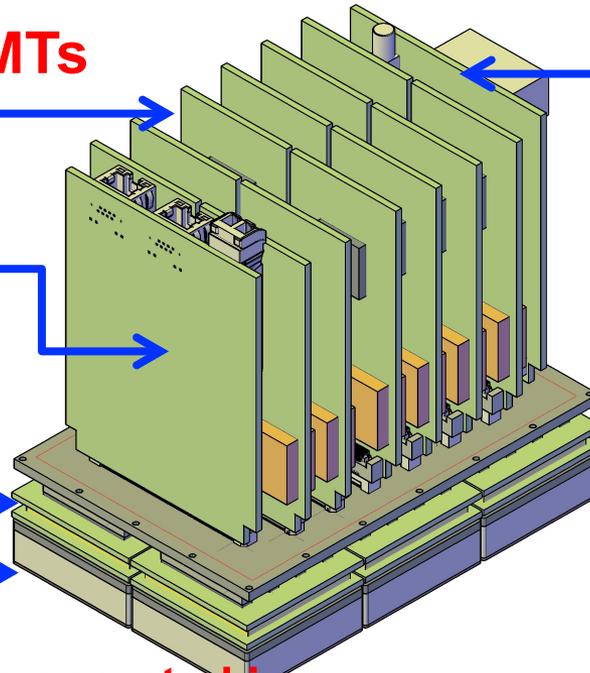
Modules with 2x3 PMTs

12x DiRICH

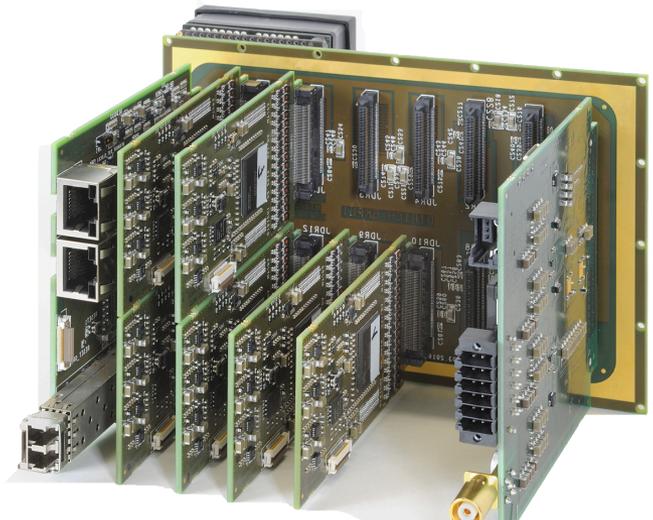
Data combiner module

Backplane

6x H12700 MAPMTs



Power module



Photos: G. Otto (GSI)

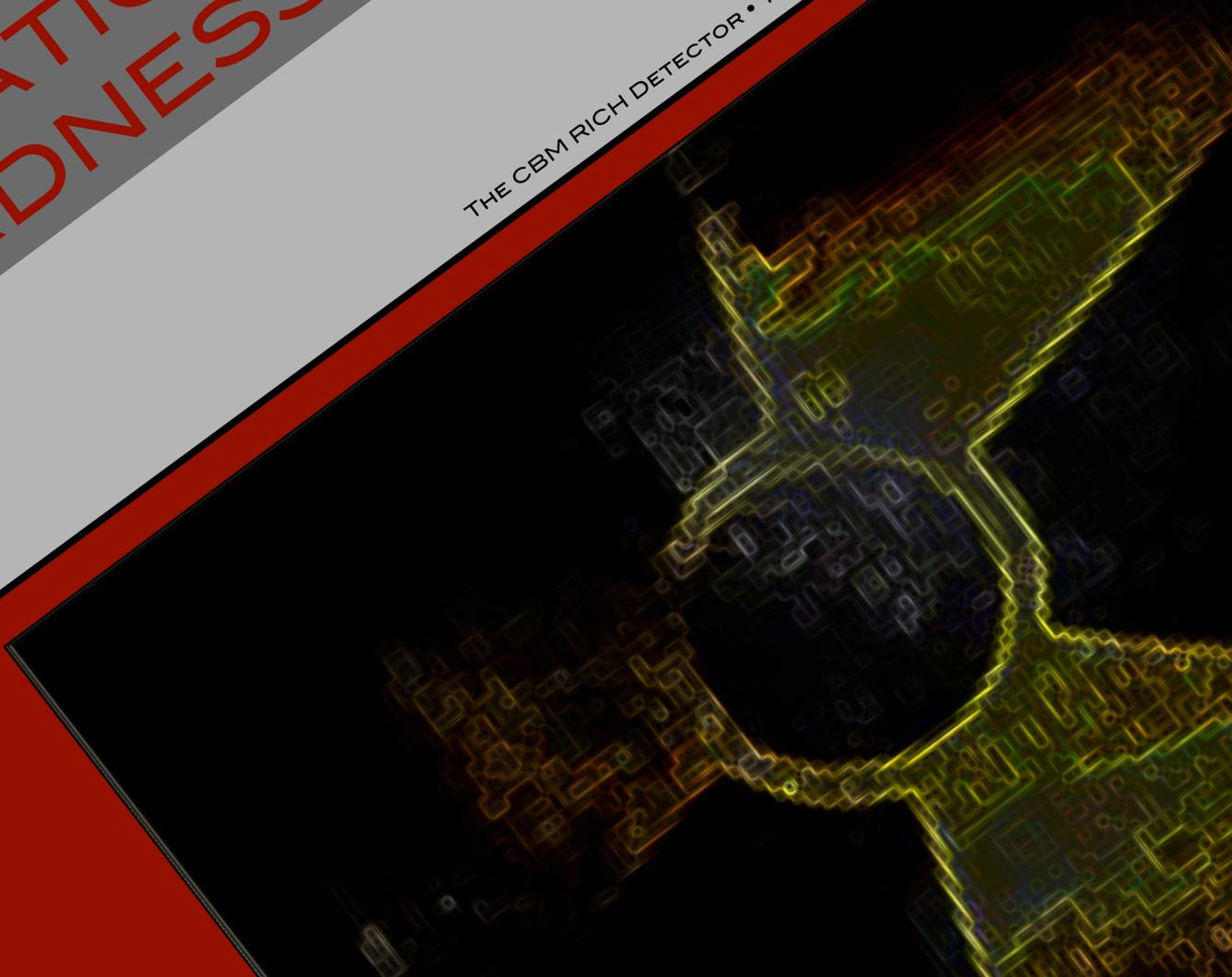
PMTs and readout will be operated in upgraded HADES RICH starting 2018

Poster: C. Pauly (A19)

RADIATION HARDNESS

THE CBM RICH DETECTOR • TARIQ MAHMOUD • RICH2016 • 05.09.2016

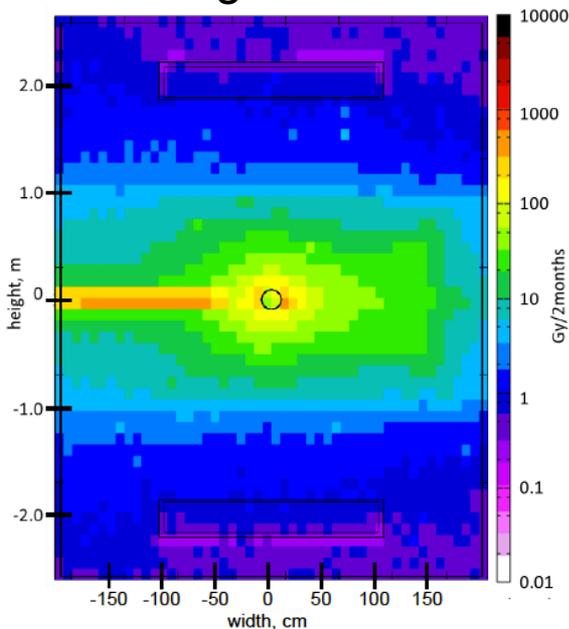
13



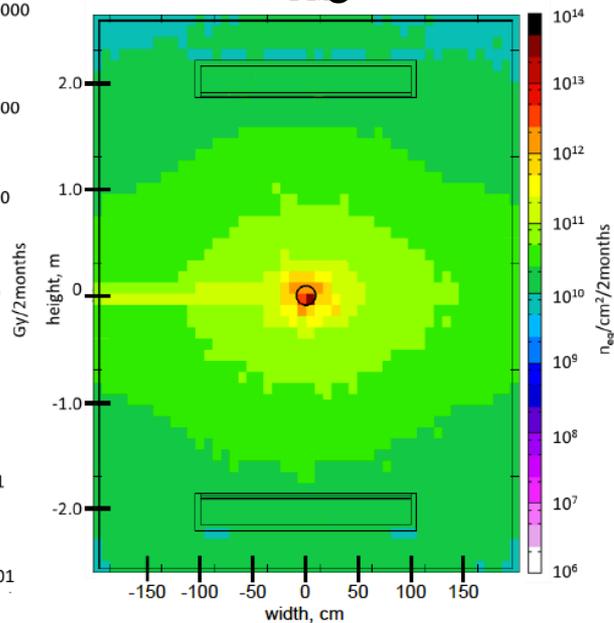
RADIATION DOSE AT PMT VICINITY

Simulations with FLUKA

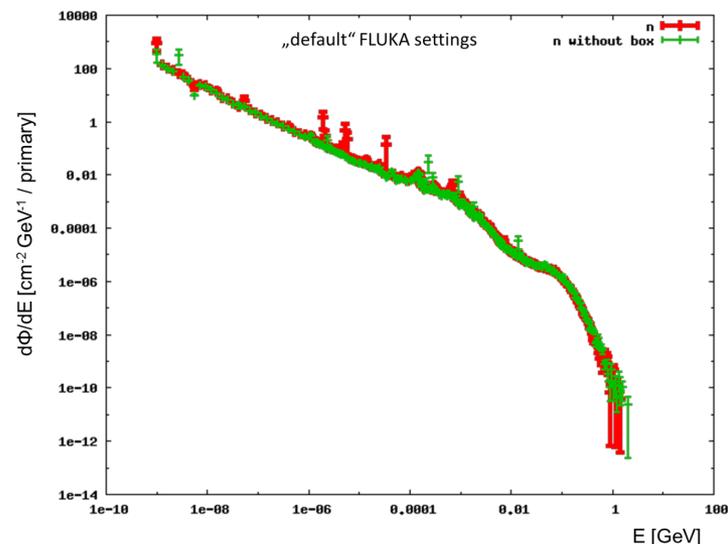
Ionising radiation



Non-ionising radiation



Mainly thermal neutrons are expected



Expected dose rate at PMT plane

per 2 months operation at maximum intensity ...
with 35 AGeV AuAu collisions:

IR ~5 Gy

NIR $\sim 5 \times 10^{10}$ n_{eq} / cm² (mainly thermal neutrons)



PMT sensors should survive 1×10^{12} n_{eq} / cm² and 100 Gy

(CBM life time: dose rate about 20x higher)

POTENTIAL DAMAGE

| PMT component | Effect |
|---------------------|--|
| PMT entrance window | loss of transmittance → loss of hits |
| WLS | change of structure → loss of hits |
| Whole PMT | activation of material (ca. 70% kovar) → higher dark rate, lower QE, loss of gain and detection efficiency |

Kovar: 54% Fe + 20 % Ni + 17% Co ($\rho = 8 \text{ g/cm}^3$)

Irradiate samples and compare results before and after irradiation

SAMPLES & DOSES

None ionizing radiation: TRIGA nuclear reactor, Jozef Stefan Institute, Ljubljana:

high flux of thermal neutrons

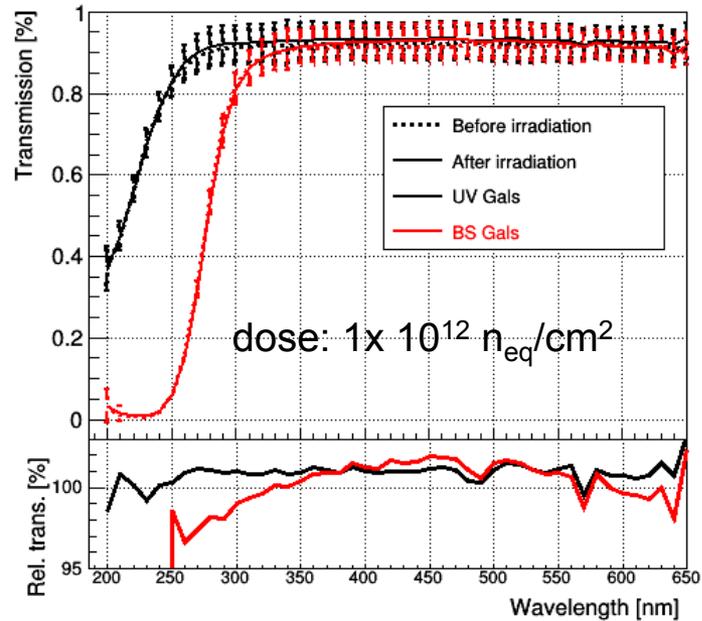
Ionizing radiation: ^{60}Co source, *Strahlencentrum* Giessen: gammas of 1.2 MeV-1.3 MeV

| Sample | Neutron dose [$n_{\text{eq}}/\text{cm}^2$] | Gamma dose [Gy] |
|-------------------|--|-----------------|
| BS-window 1 | 1×10^{12} | |
| UV-window 1 | 1×10^{12} | |
| BS-window 2 | --- | 20-32000 |
| UV-window 2 | --- | 20- 32000 |
| Quartz with WLS 1 | $(1-3) \times 10^{11}$ | --- |
| Quartz with WLS 2 | --- | ~ 50 & 100 |
| H12700 | 3×10^{11} | 145,7 |
| H8500-D | 1×10^{11} | 45,8 |
| H8500-D | 3×10^{10} | 12,5 |
| H8500-D | 1×10^{10} | |
| MCP | 1×10^{11} | 145,7 |

ENTRANCE WINDOW

Measured transmittance of BS and UV glass samples **before and after irradiation**

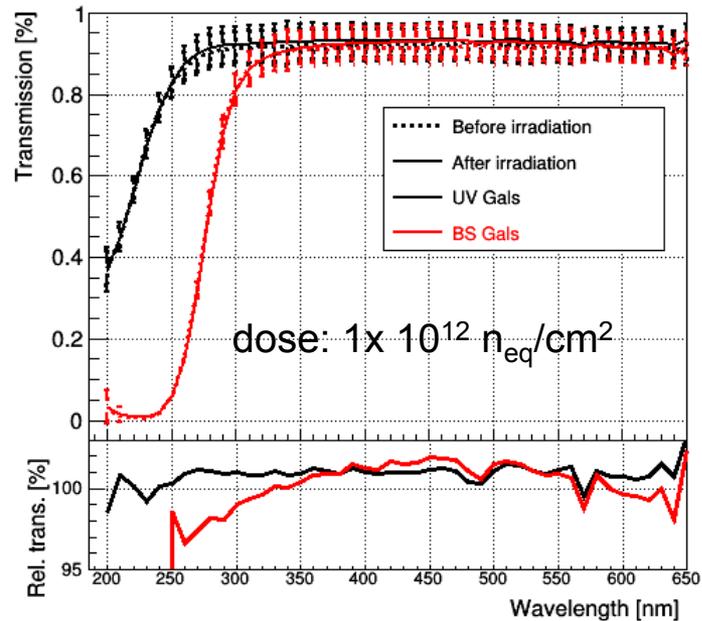
- For both samples the most noticeable **loss of transmittance** occurs **in the UV region**
- The reduction is **more pronounced for the BS** sample



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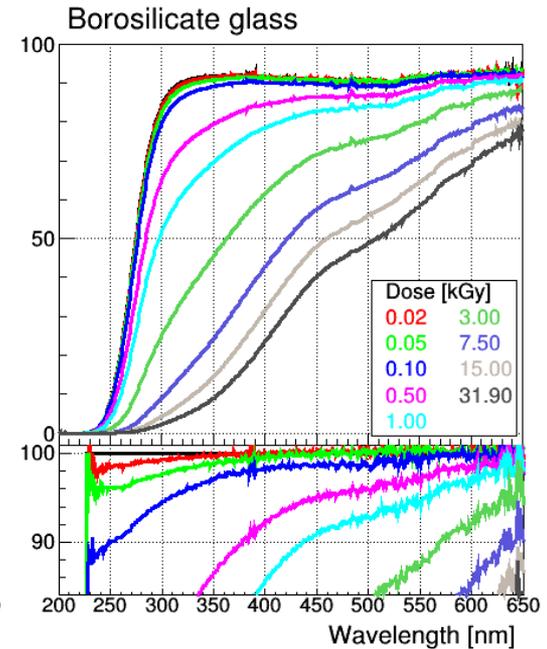
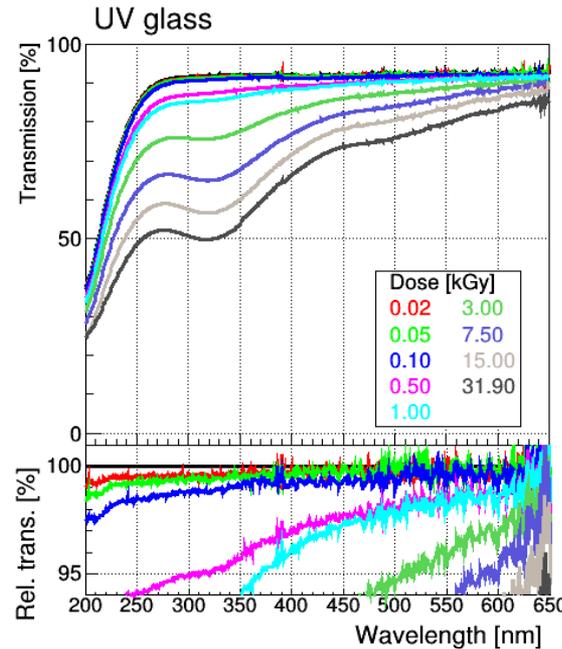
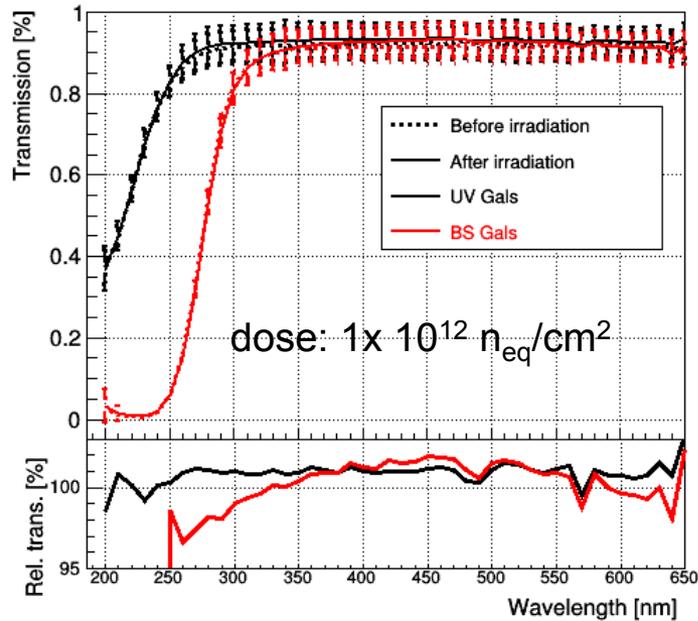
Neutron irradiation

None of the samples is affected with neutron irradiation up to $1 \times 10^{12} \text{ n}_{\text{eq}}/\text{cm}^2$

ENTRANCE WINDOW

Measured transmittance of BS and UV glass samples **before and after irradiation**

- For both samples the most noticeable **loss of transmittance** occurs in the **UV region**
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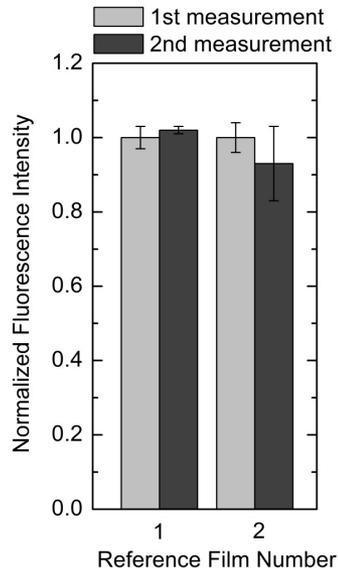
Neutron irradiation

None of the samples is affected with neutron irradiation up to $1 \times 10^{12} \text{ n}_{\text{eq}}/\text{cm}^2$

Gamma irradiation

- After 100 Gy the UV window loses less than 3% of its transparency (200nm)
- After irradiation of 3 kGy the UV glass loses only 16% of its transparency but the BS glass is opaque

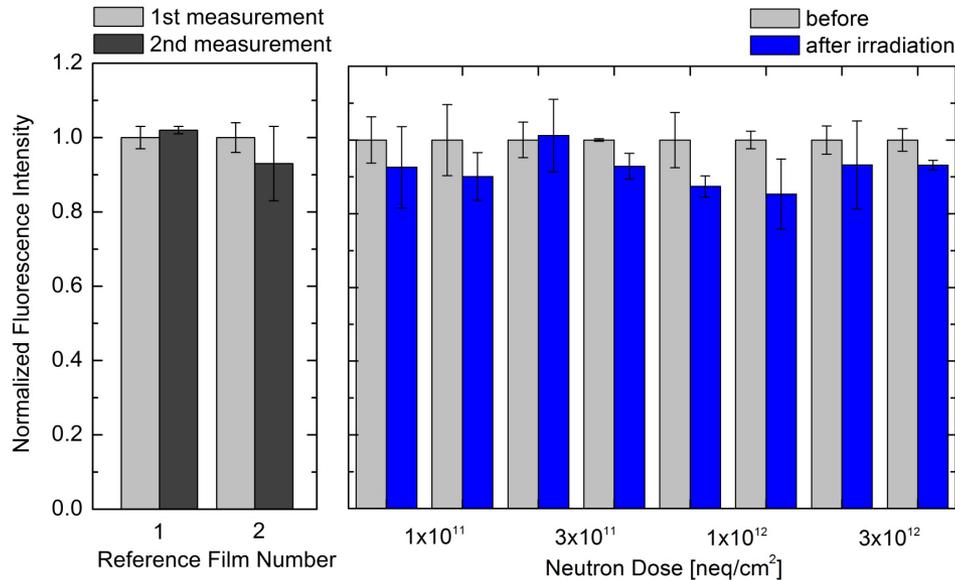
WAVELENGTH SHIFTING FILM



Without radiation:

Up to **10% fluctuation** between different measurements with the same sample

WAVELENGTH SHIFTING FILM



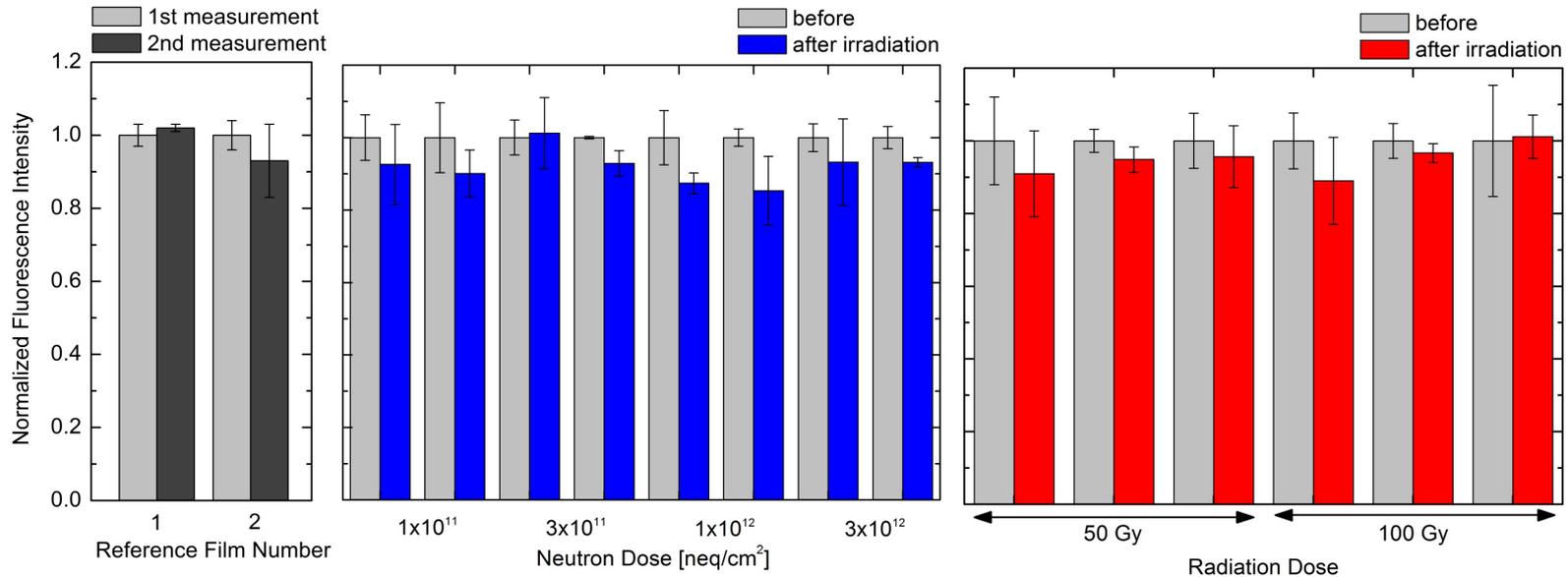
Without radiation:

Up to **10% fluctuation** between different measurements with the same sample

Neutron irradiation (four doses):

- Up to **10% fluctuation** between irradiated and non-irradiated samples
- No dependence on irradiation dose

WAVELENGTH SHIFTING FILM



Without radiation:

Up to **10% fluctuation** between different measurements with the same sample

Neutron irradiation (four doses):

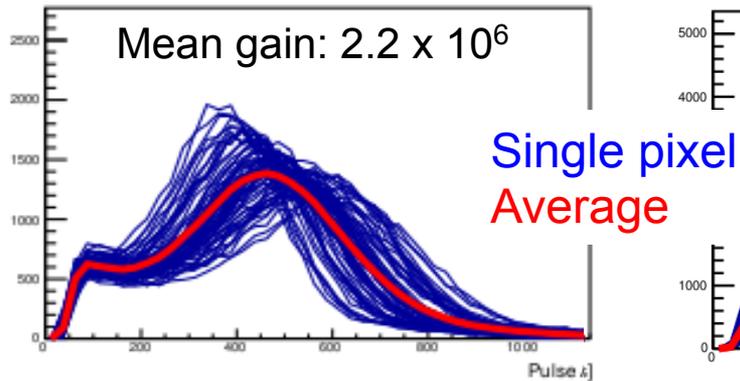
- Up to **10% fluctuation** between irradiated and non-irradiated samples
- No dependence on irradiation dose

Gamma irradiation (two doses)

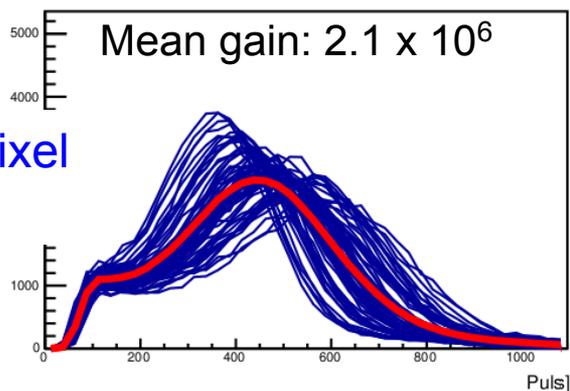
- Up to **10% fluctuation** between irradiated and non-irradiated samples
- No dependence on irradiation dose

SING. PH. SPECTRA & DETEC. EFFICIENCY

Before irradiation



After n-and γ -irradiation



H12700

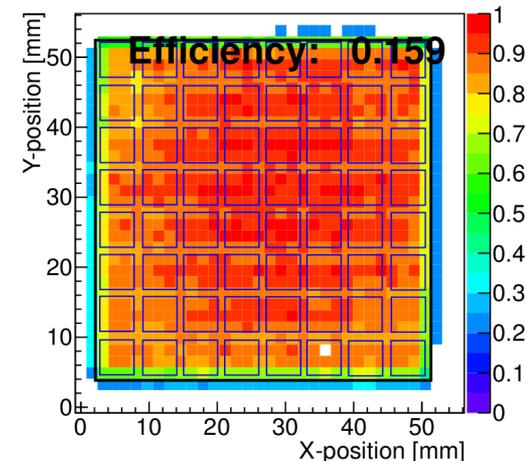
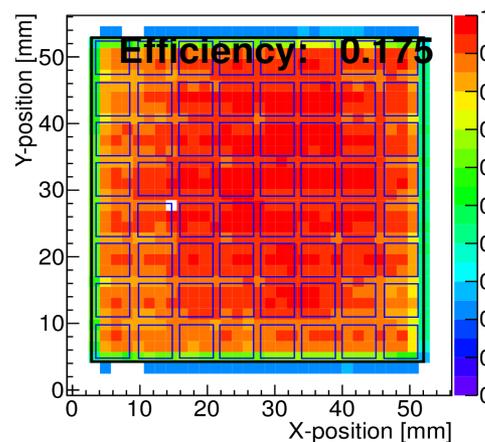
n-dose = $3 \times 10^{11} n_{eq}/cm^2$
gamma-dose = 145,7 Gy

Single photon spectra:

- Neither the n- nor the gamma-irradiation affects the single photon spectrum
- Sensors survive: $1 \times 10^{12} n_{eq}/cm^2$ and 100 Gy

Single photon detection efficiency:

- No effect from n-irradiation
- About 6% loss of efficiency by gamma-irradiation. *Probably* caused by the UV window

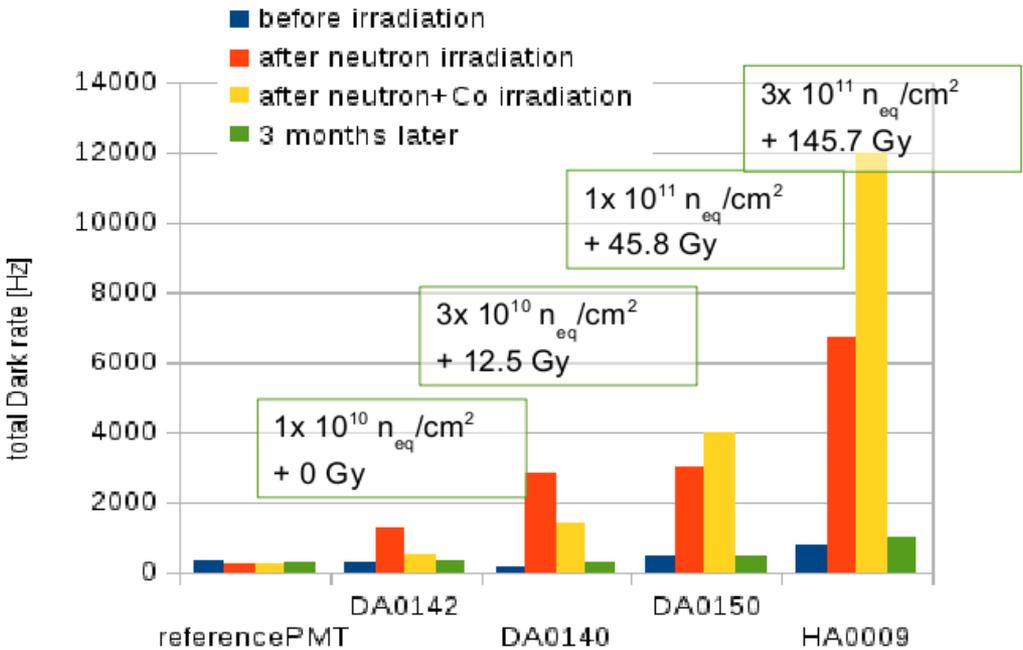


GAMMA SPECTROSCOPY

Gamma spectroscopy results measured **24h** after irradiation:

H8500

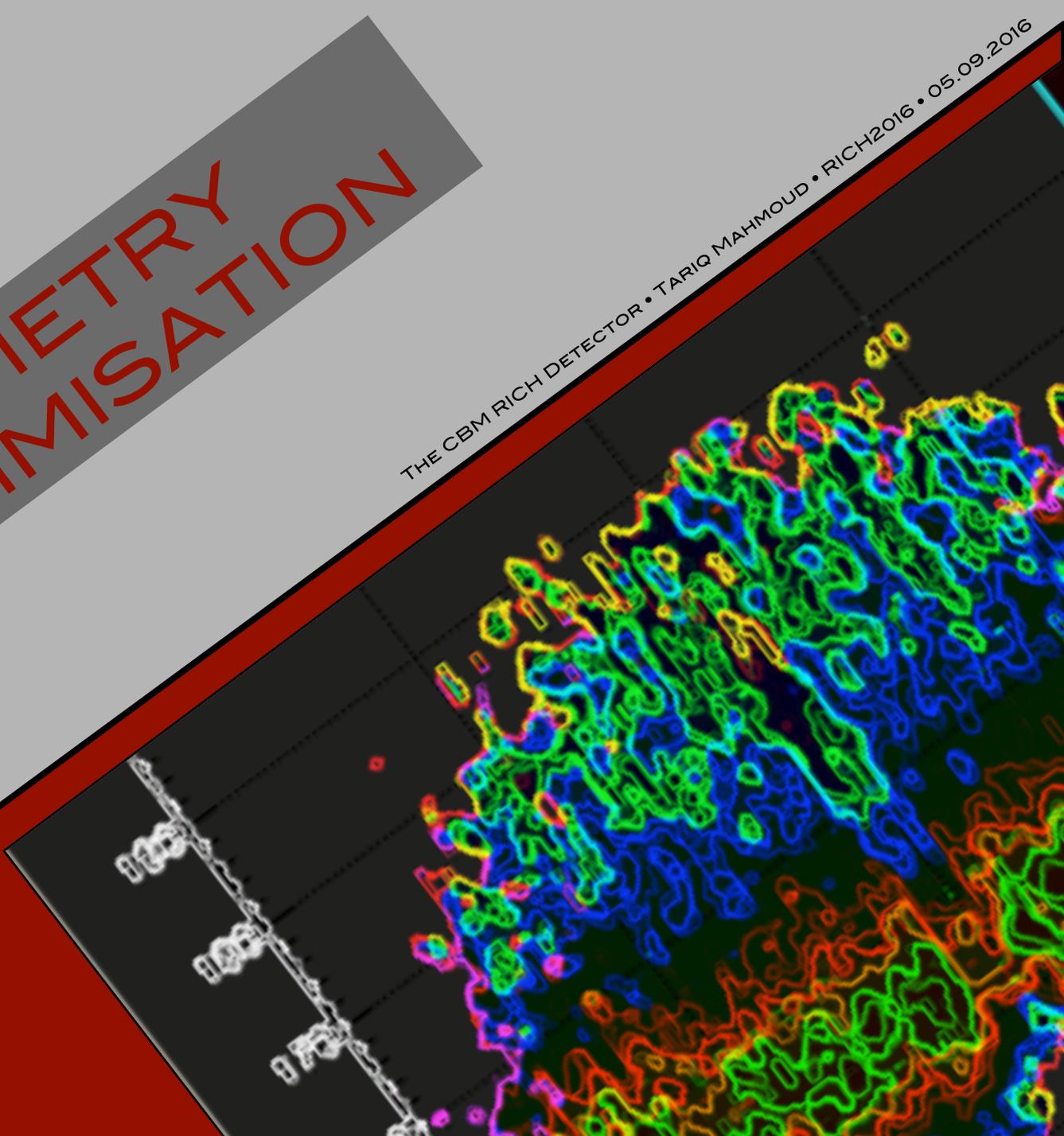
| Radionuclide | Activity [Bq] | Half-life | Used in |
|--------------|---|--------------|----------------------|
| Br-82 | 1.70×10^3 ($\pm 3.4 \times 10^2$) | 1.5 d | Voltage Divider PCB |
| Au-198 | 6.63×10^2 ($\pm 1.4 \times 10^2$) | 2.7 d | Gold-plated contacts |
| Na-24 | 2.46×10^2 ($\pm 5.1 \times 10^1$) | 15 h | Glass window |
| Co-58 | 3.03×10^1 ($\pm 7.3 \times 10^0$) | 71.3 d | Kovar metal case |
| Co-60 | 7.13×10^1 ($\pm 1.5 \times 10^1$) | 5.3 y | Kovar metal case |



GEOMETRY OPTIMISATION

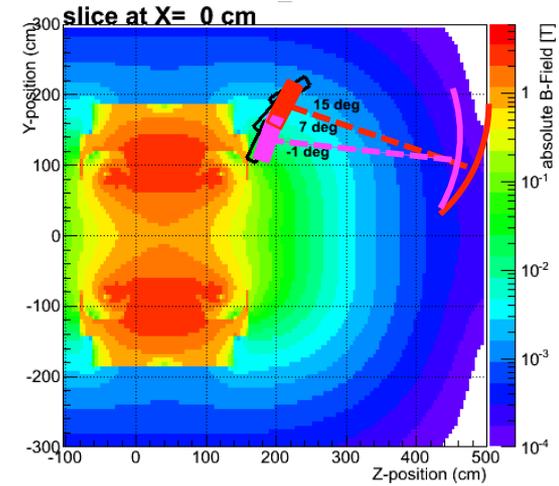
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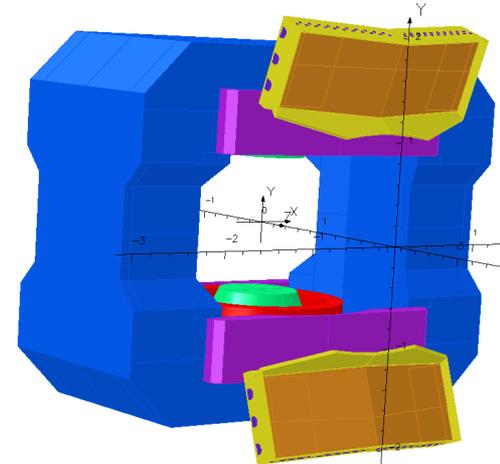


GEOMETRY OPTIMISATION (I)

- ① **Stray field** at the PMT position is about **100mT!**
- ② **Rotation** of the mirrors by 10° outwards and ...



Position optimisation



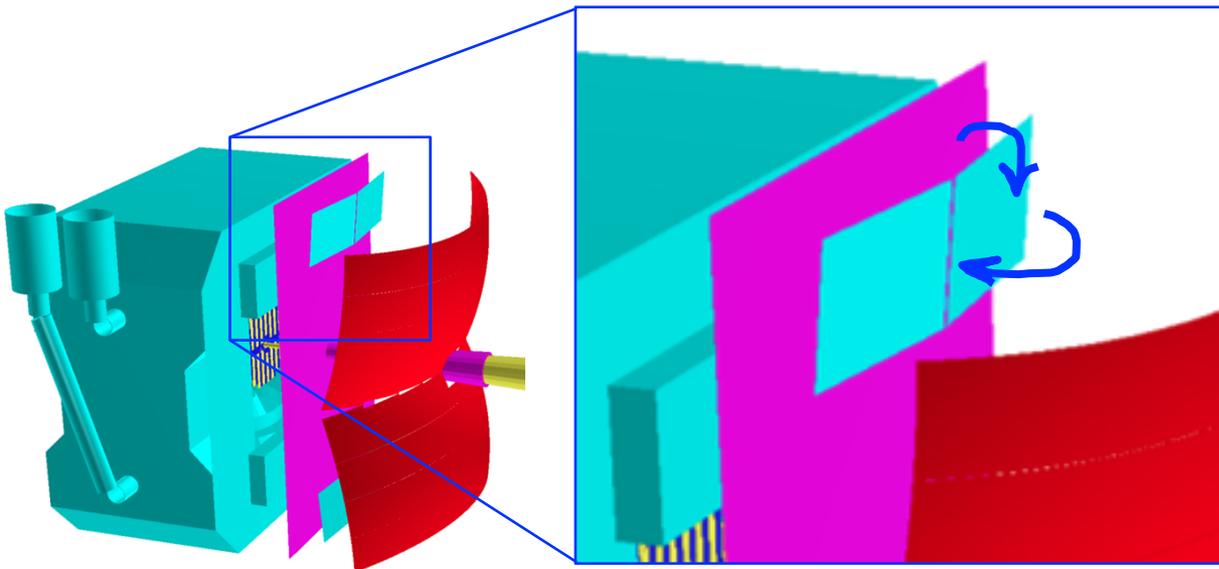
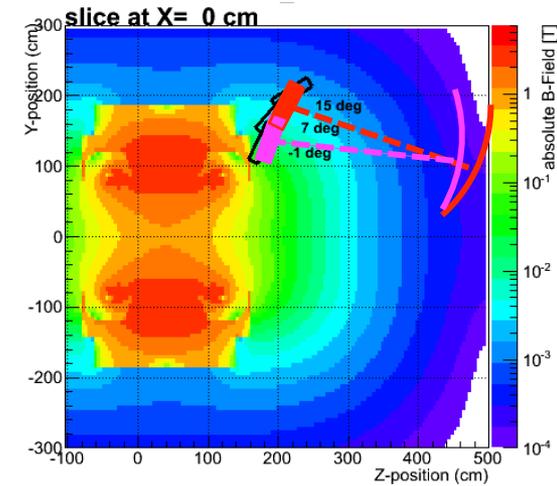
- ③ **Shielding** the PMT plane with steal

GEOMETRY OPTIMISATION (I)

- ① **Stray field** at the PMT position is about **100mT!**
- ② **Rotation** of the mirrors by 10° outwards and ...

- **Optimisation** of position and dimensions of the PMT-plane
- **Segmentation** of the PMT-plane to cope with the electronics concept within the CBM acceptance \rightarrow

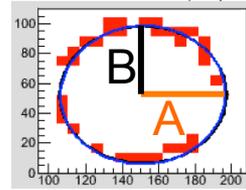
7 x 7 modules (14 x 21 MPTs \rightarrow 742 mm x 1113 mm)



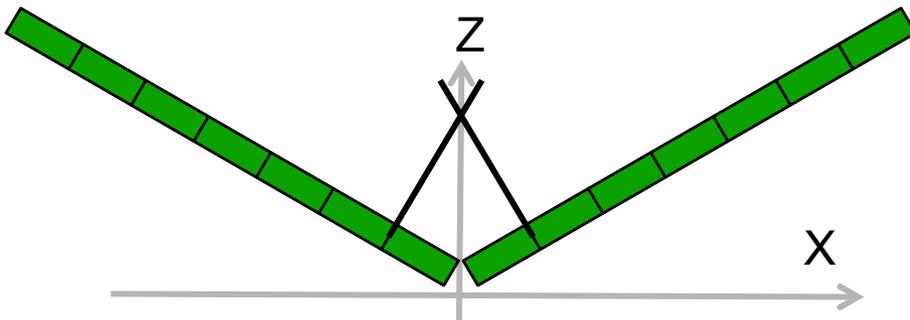
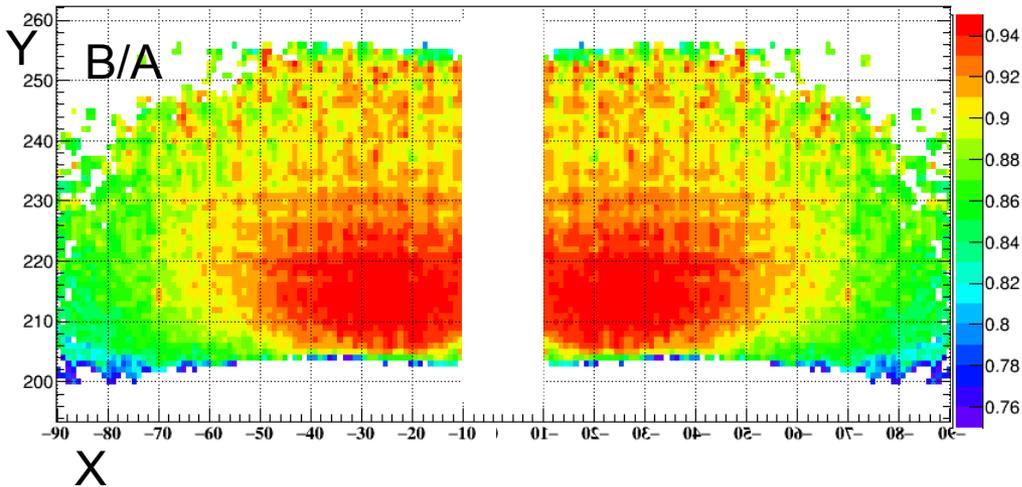
- In a first step for a **two-wings geometry**
- In a second step for a **curved geometry**

GEOMETRY OPTIMISATION (II)

Best position in space is that with **the highest resolution** of an elliptic fit upon the rings and **the highest B/A**

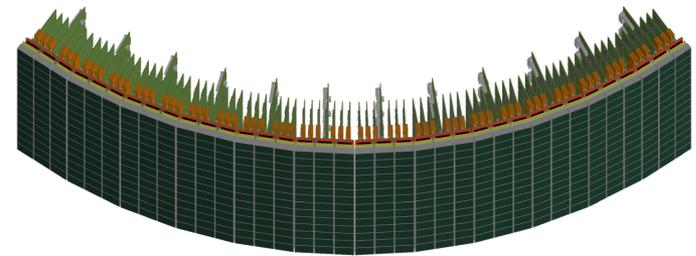


① Two wing geometry



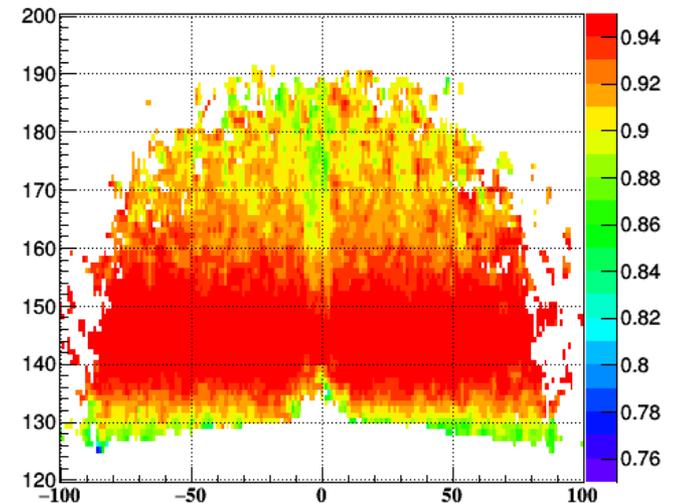
Loss of efficiency

② Curved geometry



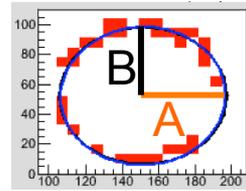
BoA: $\Delta_y = 0$, $\Delta_z = -20$, $\theta_x = 18$, $r_y = 1650$

Aa = 0.36, Ba = 0.36, BoA = 0.93, dR = 0.28, Eff = 92.86,

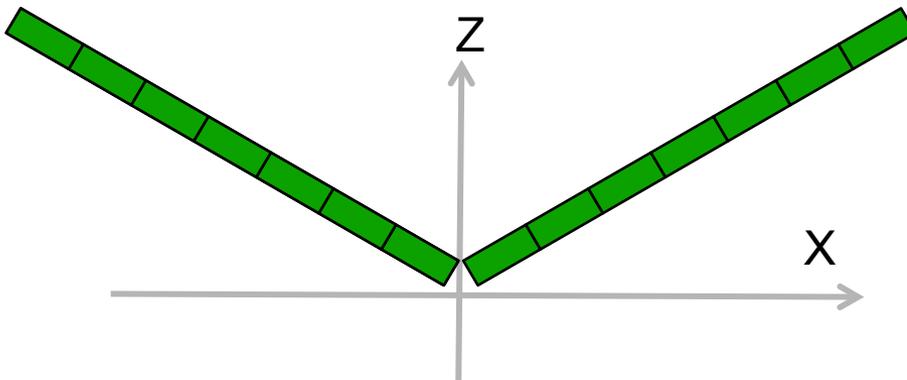
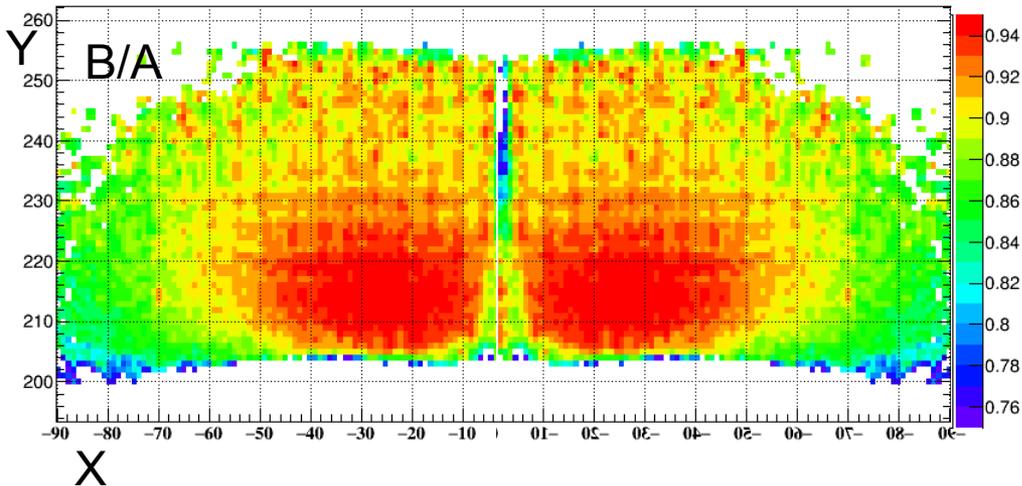


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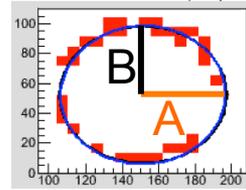


① Two wing geometry

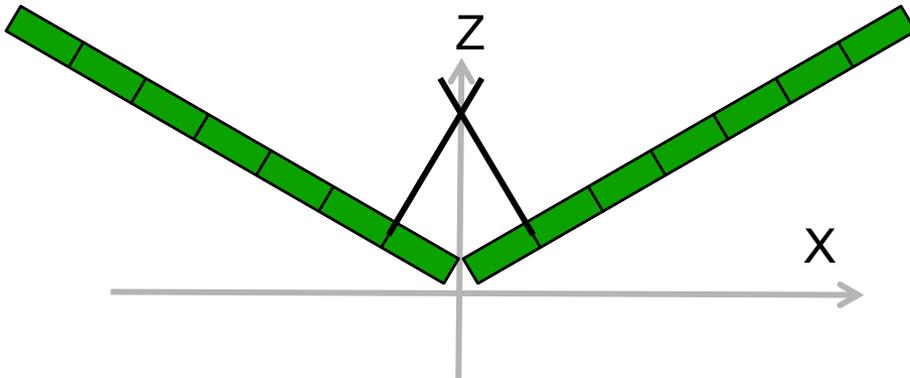
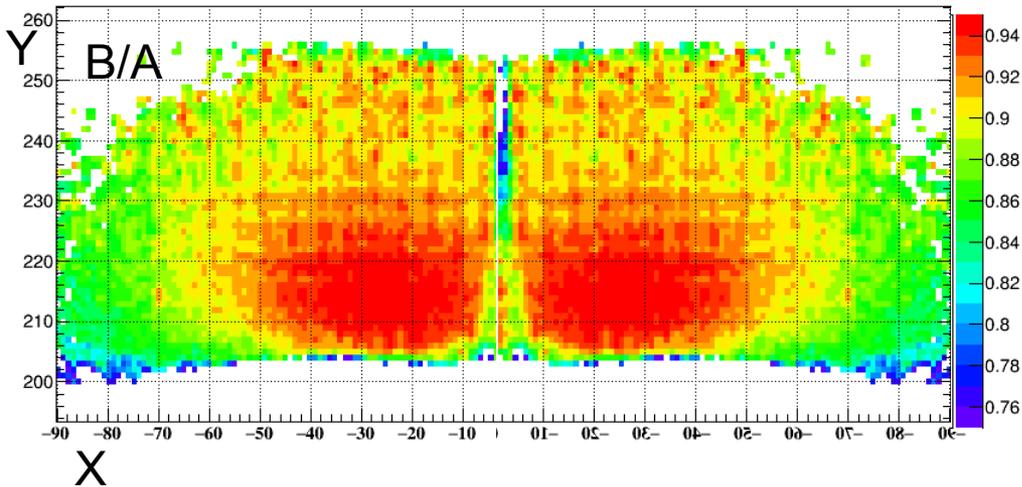


GEOMETRY OPTIMISATION (II)

Best position in space is that with **the highest resolution** of an elliptic fit upon the rings and **the highest B/A**

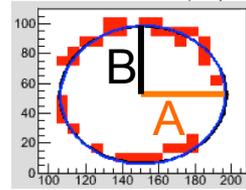


① Two wing geometry

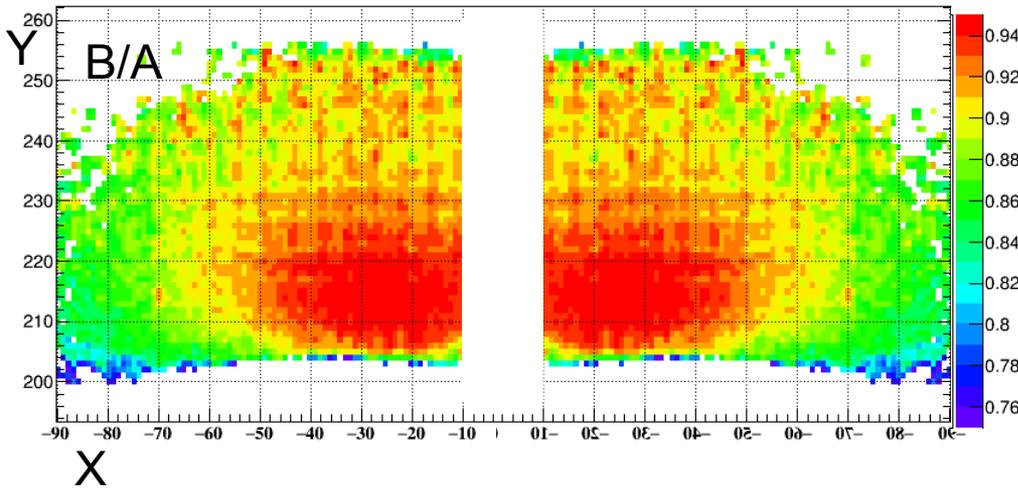


GEOMETRY OPTIMISATION (II)

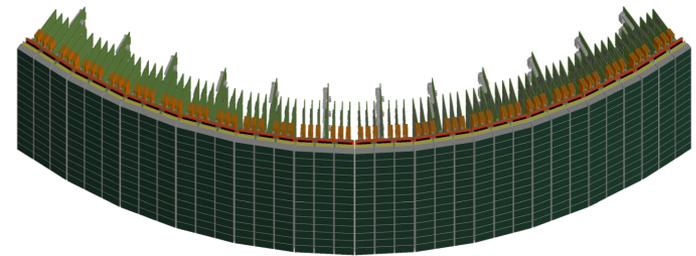
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① Two wing geometry

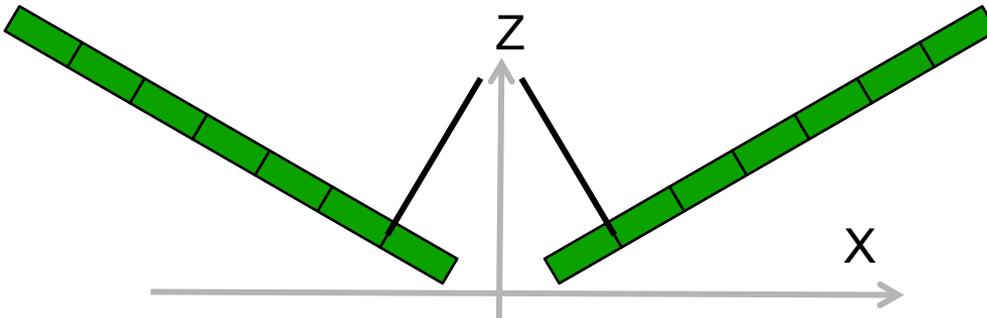
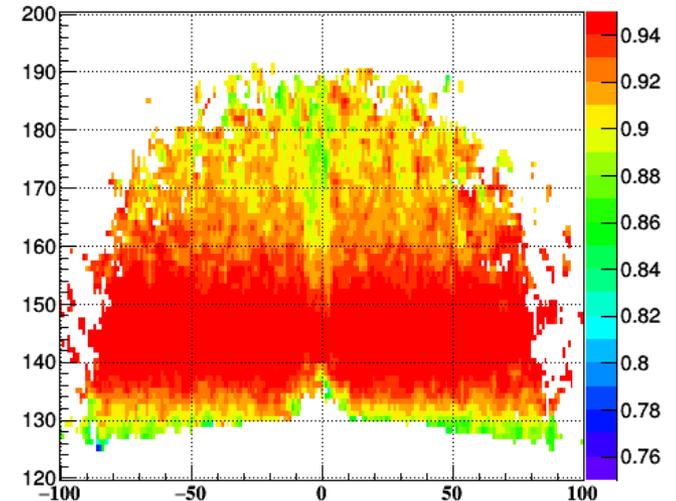


② Curved geometry



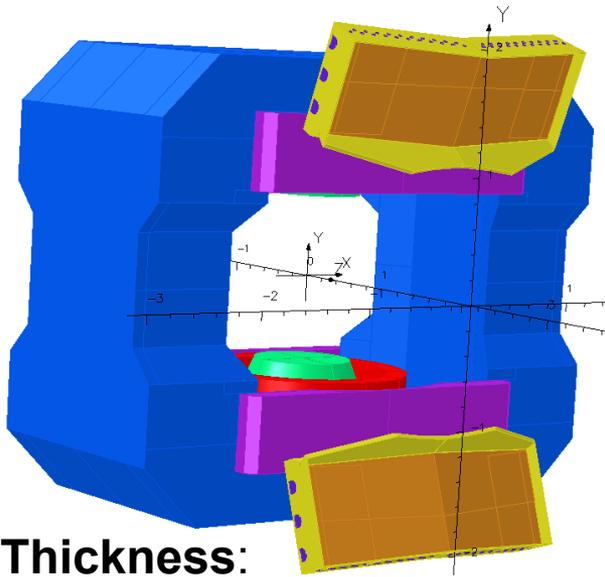
BoA: $\Delta_y = 0$, $\Delta_z = -20$, $\theta_x = 18$, $r_y = 1650$

Aa = 0.36, Ba = 0.36, BoA = 0.93, dR = 0.28, Eff = 92.86,



Loss of efficiency

SHIELDING BOX



Thickness:

back & inner side: 3 cm

inner side extension: 3.5 cm

right, left, and outer sides: 1 cm

Volume:

$V = 0.1087 \text{ m}^3 \rightarrow \text{weight}=850 \text{ kg}$

Holes on:

right and left sides for services

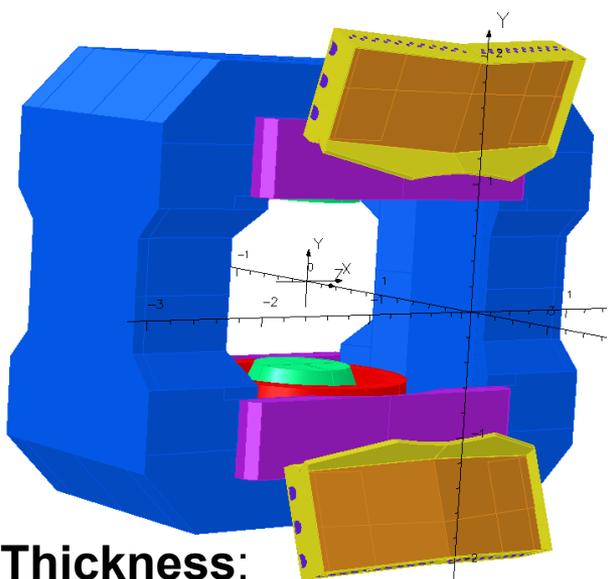
outer sides for cooling

Space to PMT-plane:

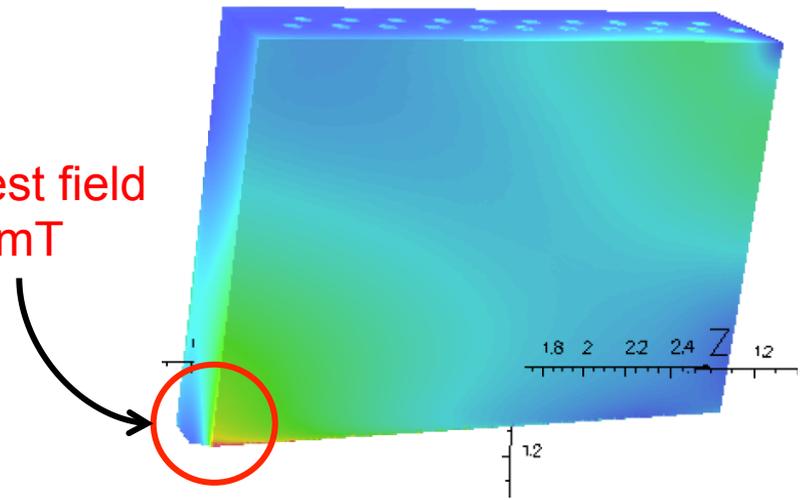
right, left, and outer sides: 5 cm

inner side: 2 cm

SHIELDING BOX



highest field
ca. 1mT



Thickness:

- back & inner side: 3 cm
- inner side extension: 3.5 cm
- right, left, and outer sides: 1 cm

Volume:

$V = 0.1087 \text{ m}^3 \rightarrow \text{weight}=850 \text{ kg}$

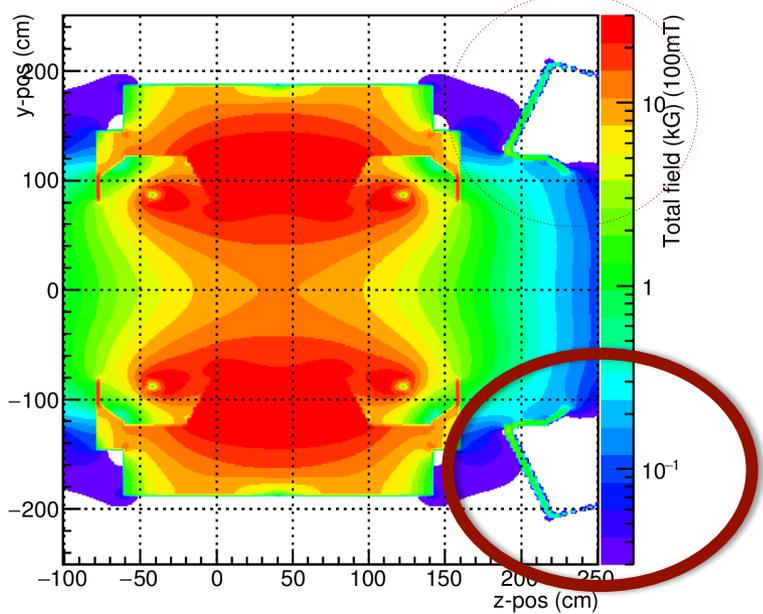
Holes on:

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Space to PMT-plane:

- right, left, and outer sides: 5 cm
- inner side: 2 cm

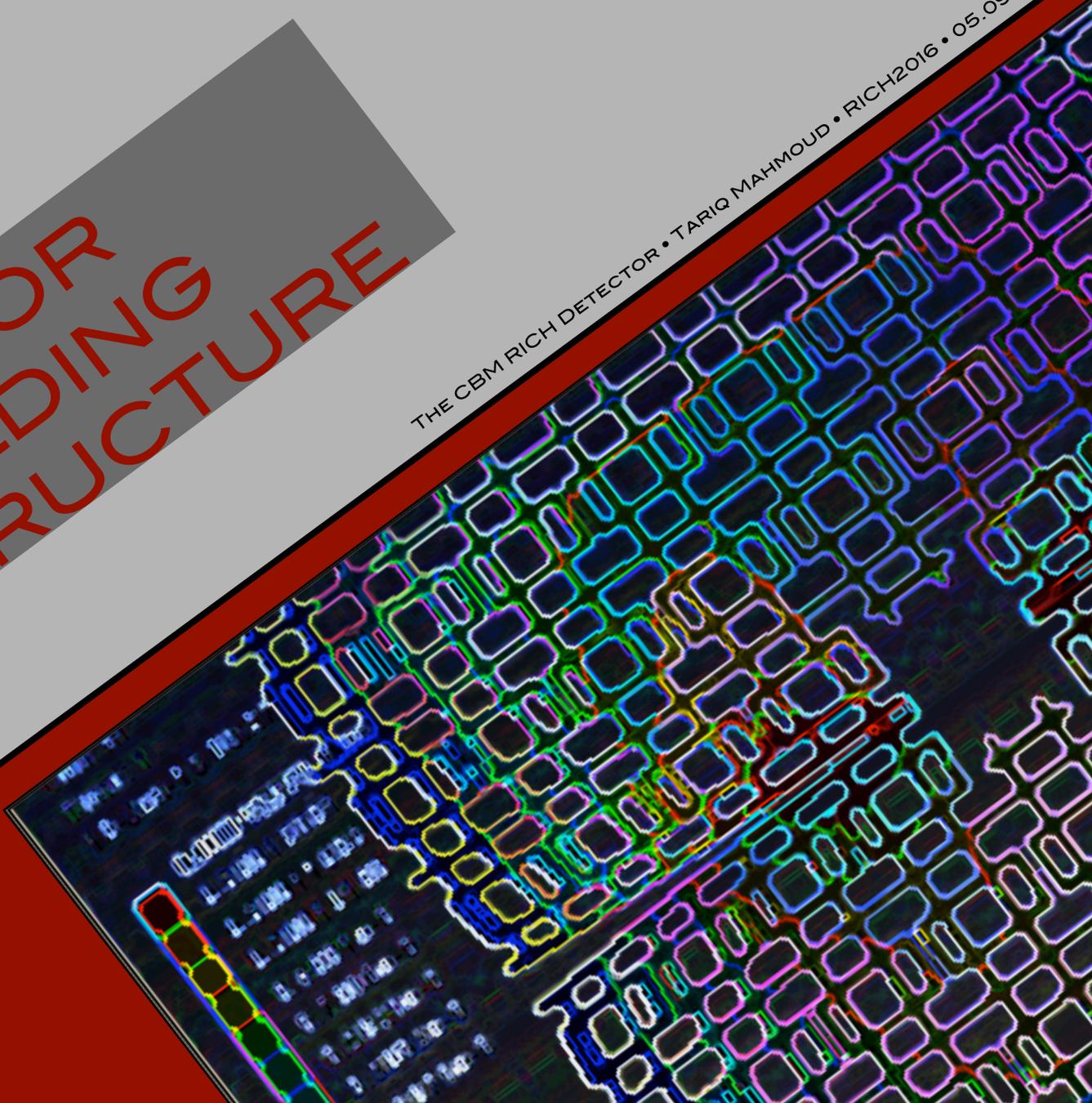
NewRICH_mmod8l25m11June1_Cs3 yz projection



MIRROR HOLDING STRUCTURE

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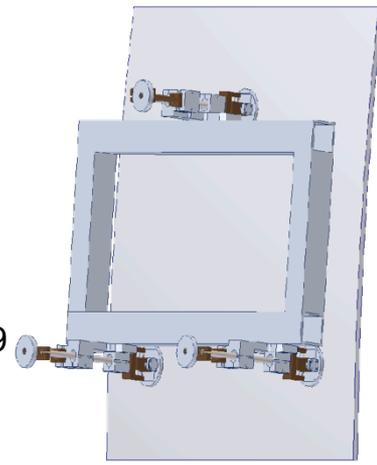
MIRROR MOUNT STRUCTURE (I)

- Ensure **high mechanical stability** WITH **low material budget**

- **Basic structure:**

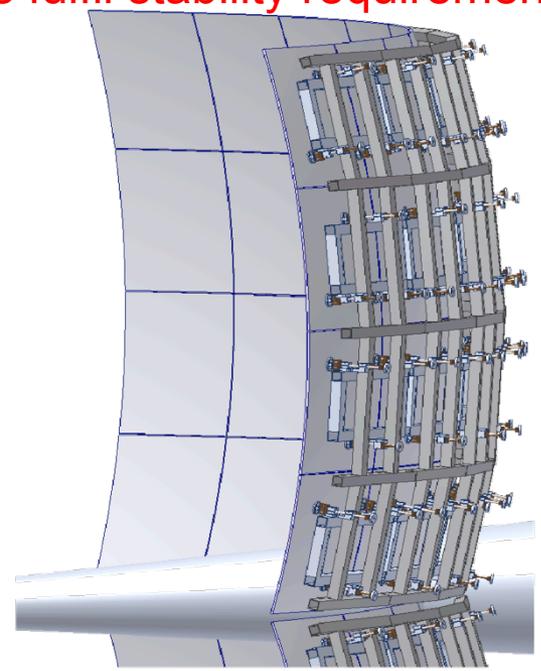
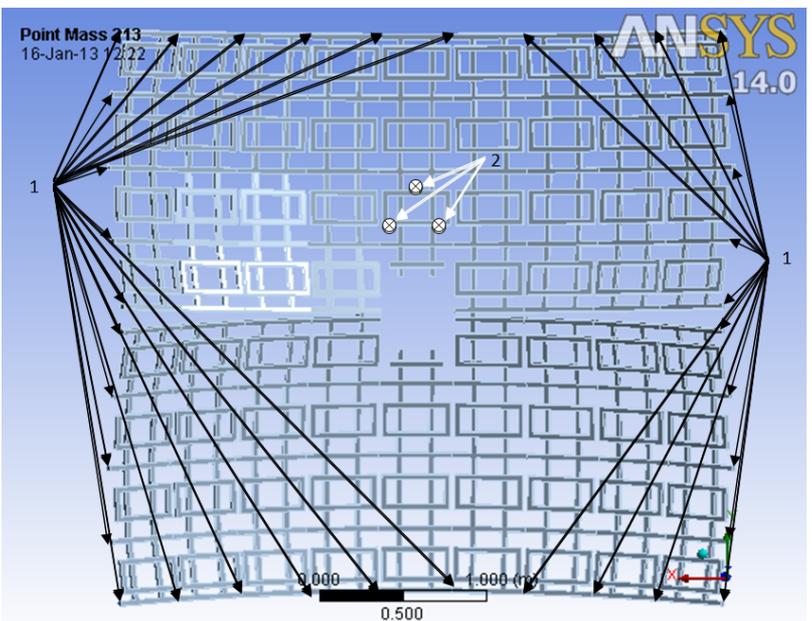
- mount mirror tile to an aluminium rectangle with three actuators
- 4 rows → 4 “belts” with 9 cells each
- Weight = 197 kg + mounts, **$X_0 \sim 6.35\%$ ***

* relative to X_0 of an aluminum volume covering the CBM acceptance with 9 cm thickness.



- Simulations with ANSYS: **maximal deformation: 153 μm**

- Prototype was build and tested: **design and materials fulfil stability requirements**



MIRROR MOUNT STRUCTURE (II)

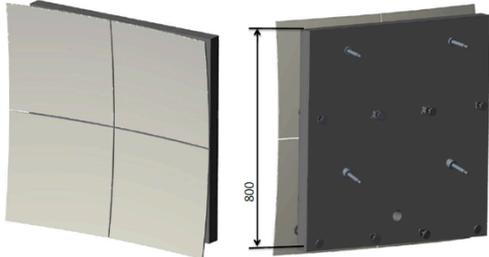
Reduce material budget: → considered three new types of designs.

V1: Foam structure
 Not sure that the design will keep the geometry over time

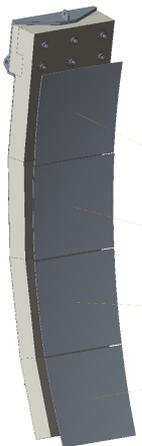
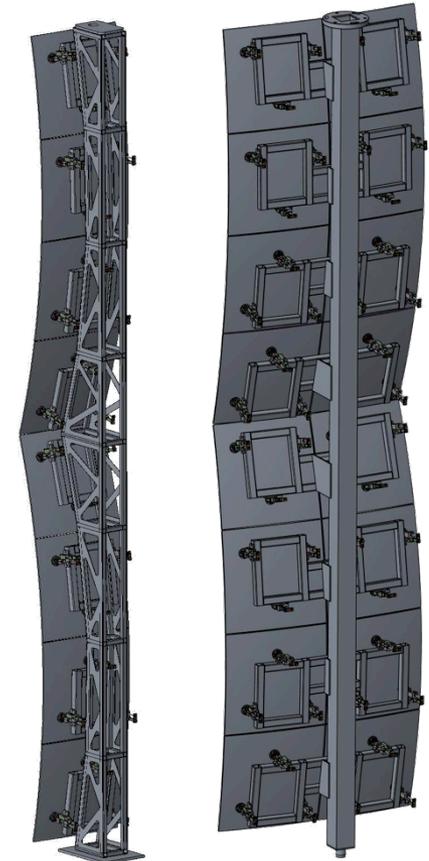
V2: Frame from light Al profile plus welding
 Difficulties in manufacturing

V3: "Pillar" design
 Two mirror columns per pillar

Module 2x2



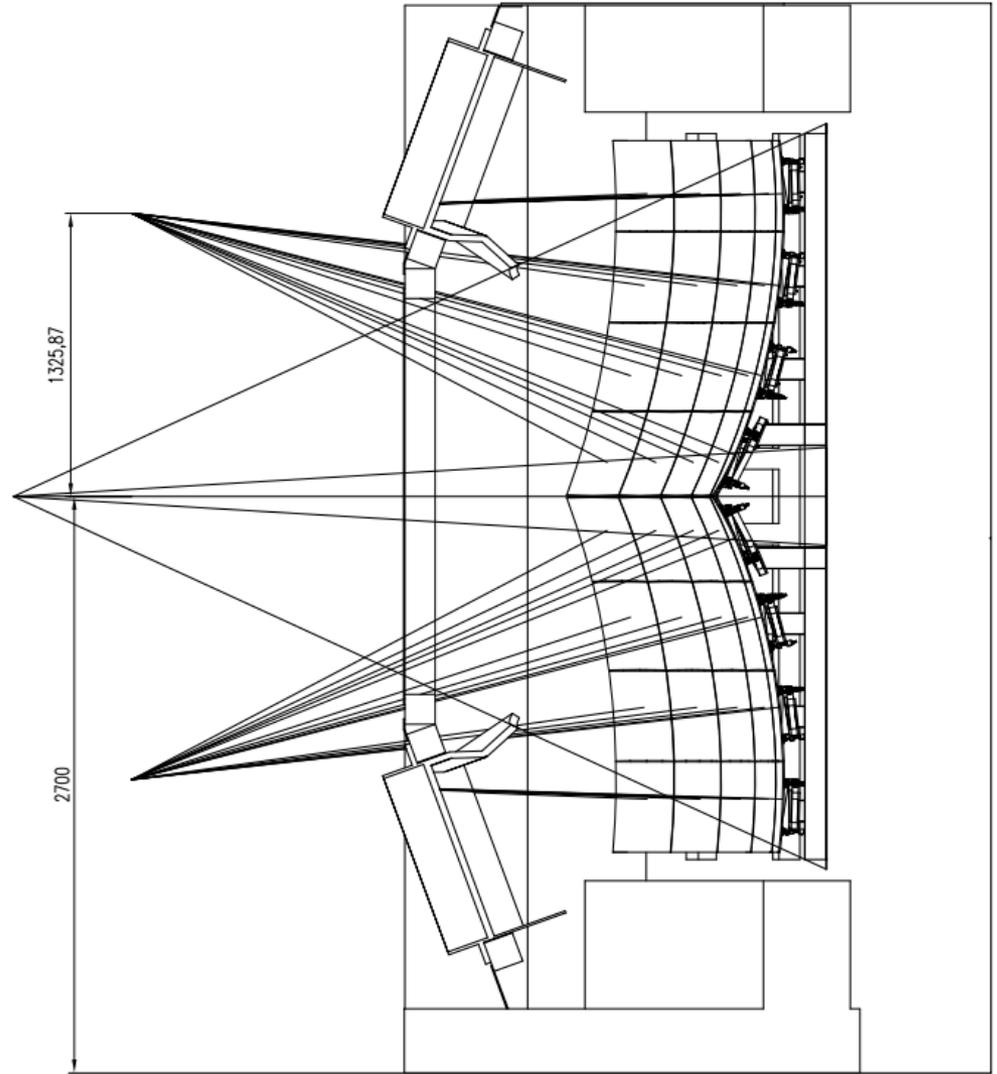
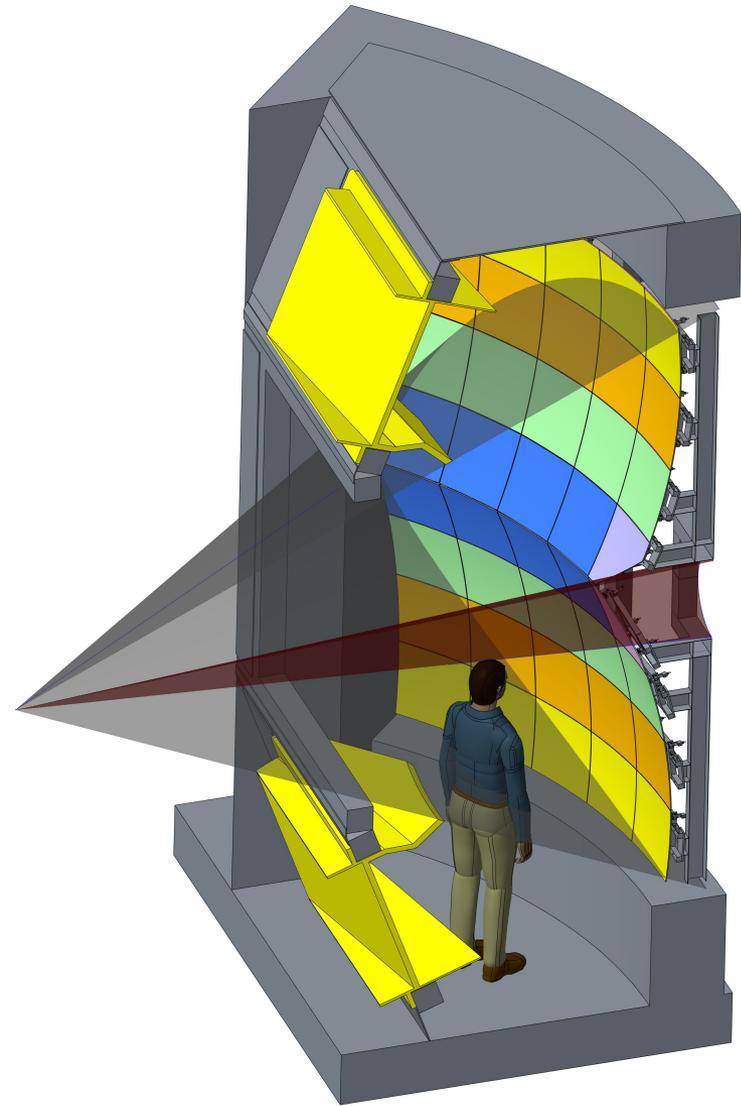
The mass of the mirrors ~10 kg
 The mass of the foam ~ 3-6 kg



| | Weight [kg] | X_0 [%] |
|--------------|--------------|-----------|
| Basic design | 197 + mounts | ~ 6.35 |
| V1 | | ~ 3.8 |
| V2 | 140 + mounts | ~ 4.8 |
| V3 | 125 + mounts | ~ 4.4 |

Potential reduction of X_0 with carbon fibre pillars

GEOMETRY OVERVIEW



Building the mirror structure and the shielding box does not pose any challenge

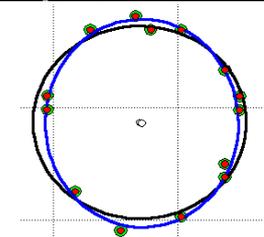
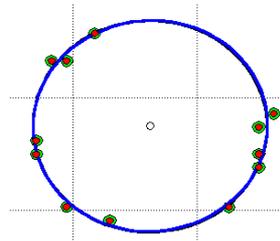
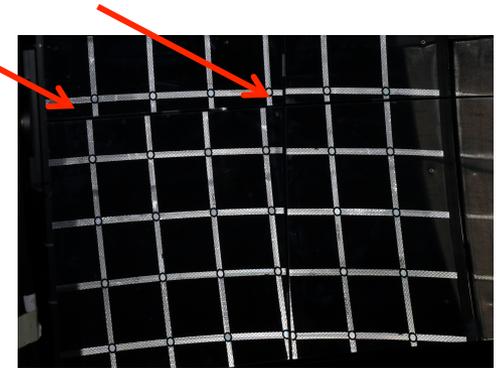
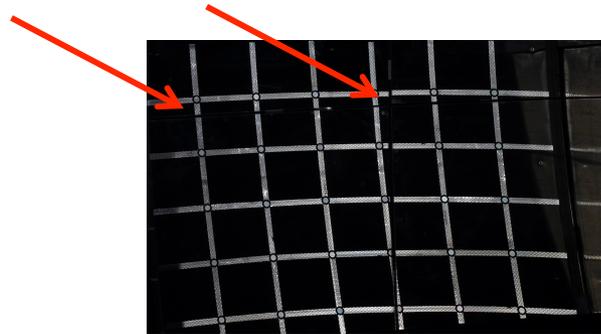
MIRROR ALIGNMENT

- ① Alternating usage of RICH with MUCH
 - potential mirror misalignment
 - development of a mirror alignment system

- ② **CLAM method:**

retro-reflective grid at entrance illuminated by LED,
reflection “seen” via mirror and recorded with a camera
→ determine misalignment

COMPASS experiment, Nucl.
Instr. Meth. Phys. Res. A 553
(2005) 135



- ③ **“Two ring centres”**: calculate difference between fitted and extrapolated ring centres
HERA experiment, Nucl. Instr. Meth. Phys. Res. A 433 (1999) 408
→ correct for the misalignment

Poster: J. Bendarouach (A3)

SUMMARY

- ① The RICH concept was approved and accepted by the FAIR council
- ② Open items were studied carefully:
 - i. RICH **geometry optimised** to escape the influence of the stray field; **shielding box designed**
 - ii. **PMTs tested on their radiation hardness** for the duration of the CBM life time
 - iii. PMTs ordered and being delivered and tested
 - iv. **Mirror holding structure developed** to ensure mechanical stability with low material budget
 - v. Common readout development with PANDA and HADES: **first readout board ready**
- ③ Mirror alignment system established
- ④ **Software developed** and refined accordingly
- ⑤ **Electronics and WLS tested** in beam time
- ⑥ Cooperation with HADES: **HADES-RICH upgrade for SIS18** (2018-2020) with ~400 CBM-MAPMTs & electronics

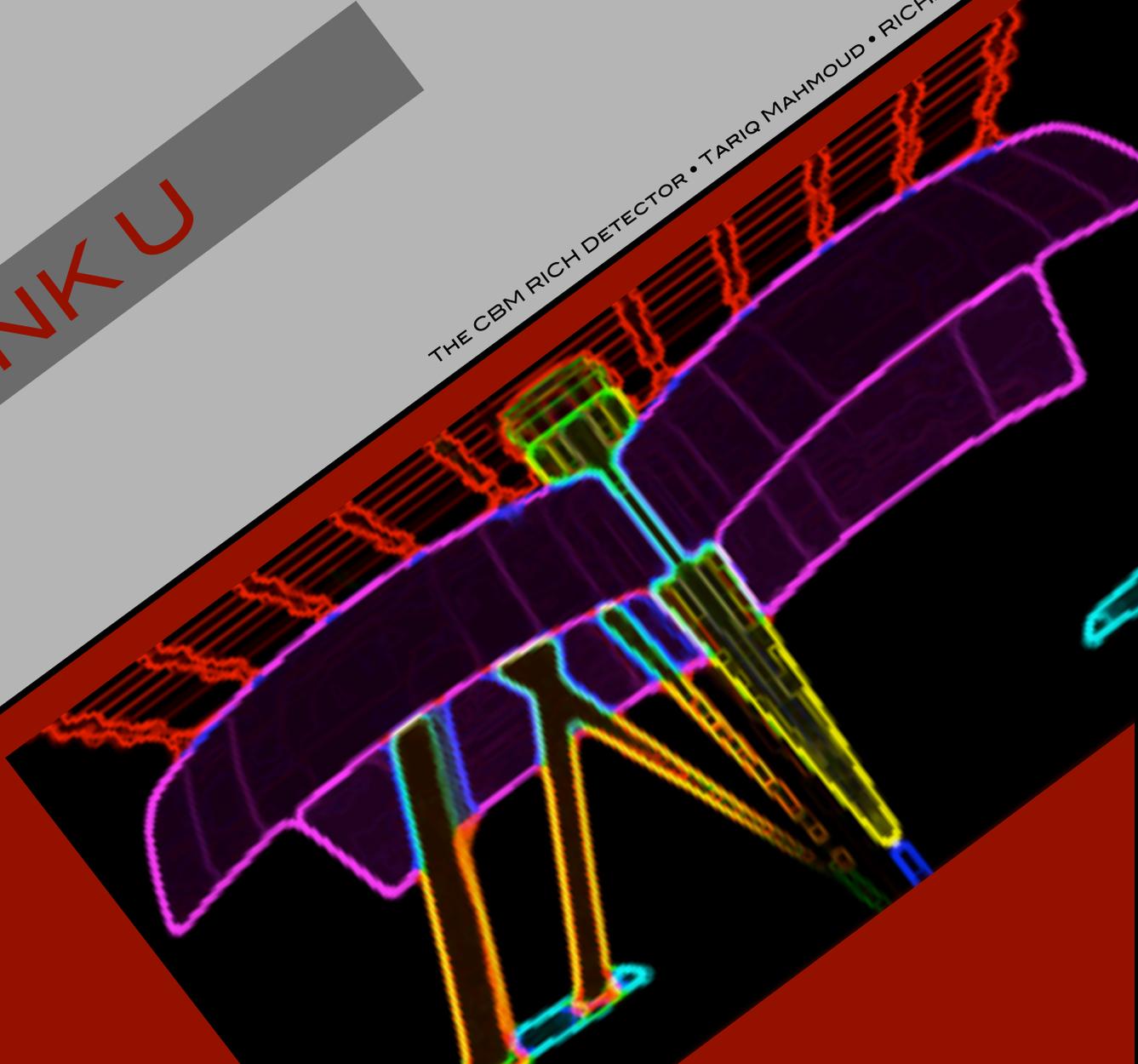
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- ④ **Software developed** and refined accordingly **Poster: S. Lebedev (A25)**
- ⑤ **Electronics and WLS tested** in beam time **Poster: E. Ovcharenko (A11)**
- ⑥ Cooperation with HADES: **HADES-RICH upgrade for SIS18** (2018-2020) with ~400 CBM-MAPMTs & electronics **Poster: C. Pauly (A19)**

THANK U

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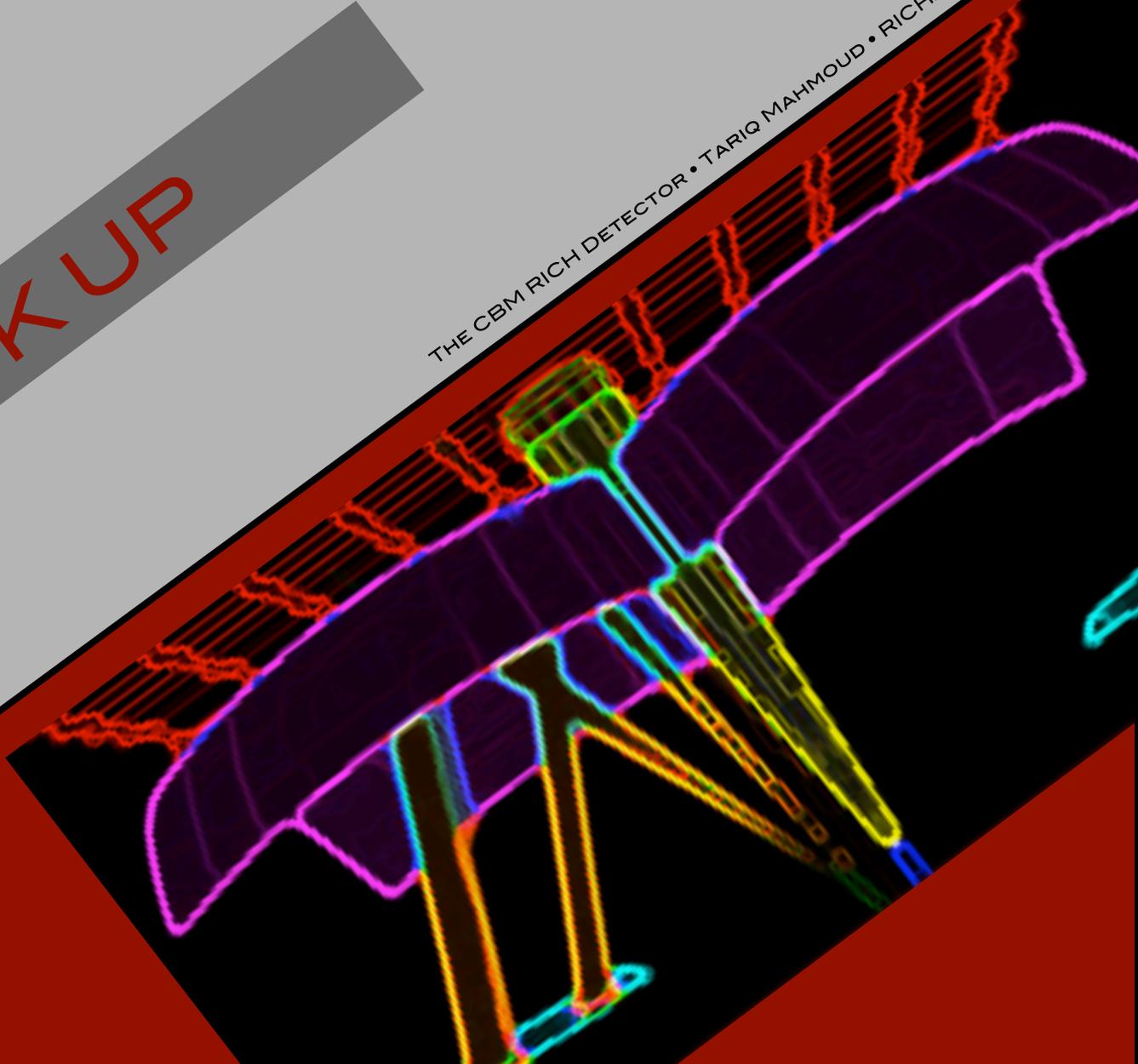
41



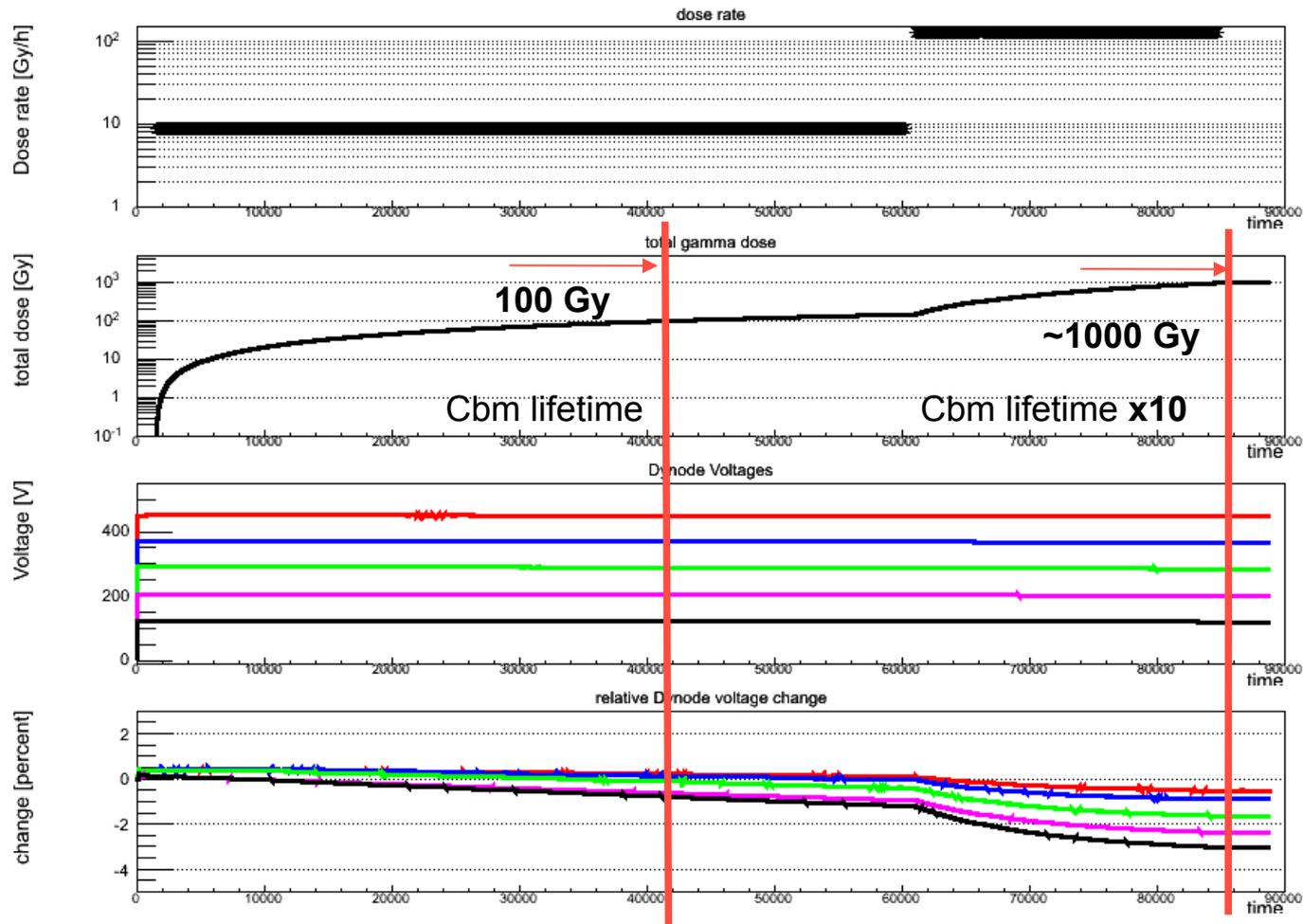
BACK UP

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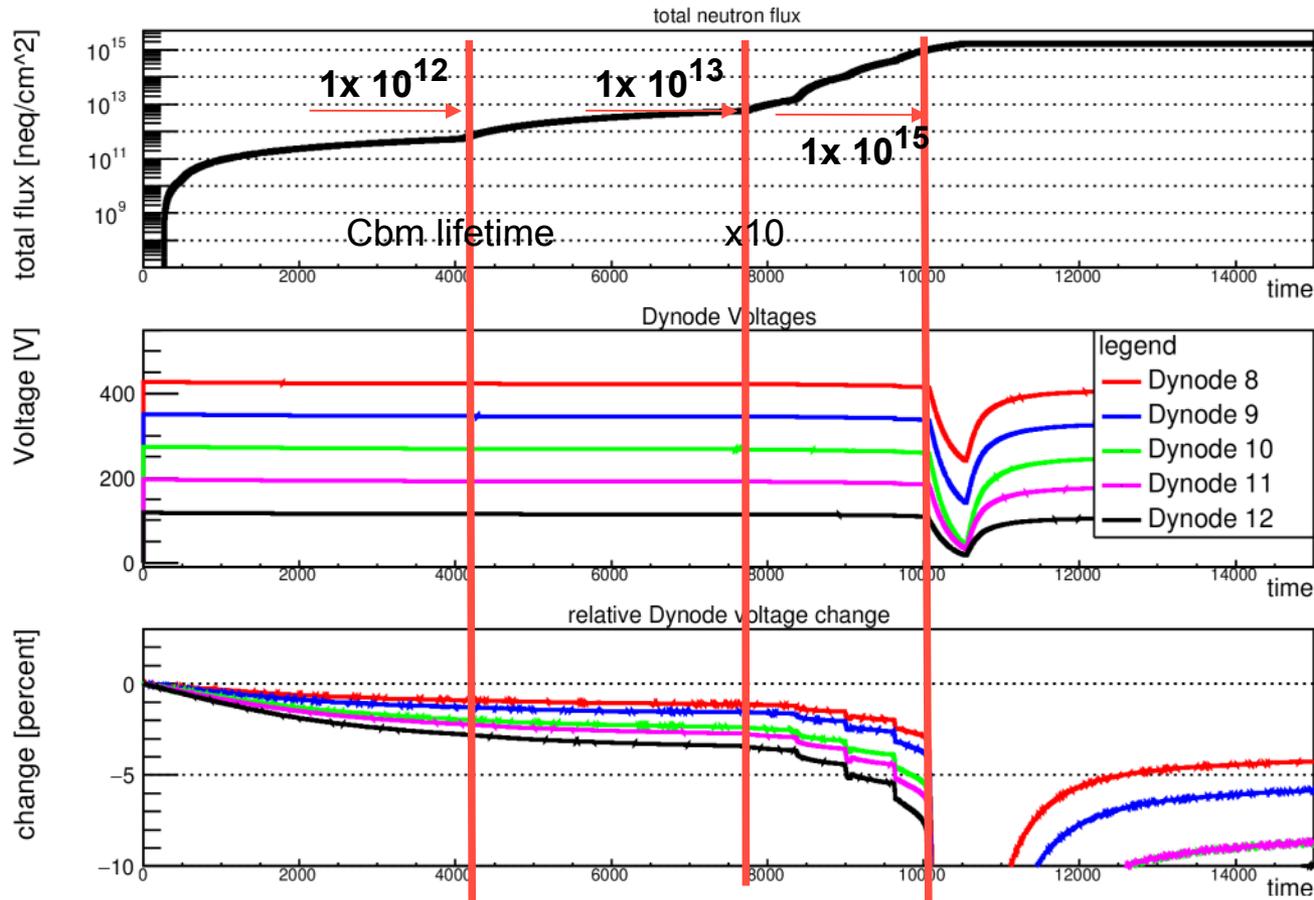


PMT VOLTAGE DIVIDER (GAMMA)



✧ No effect on voltage divider after 10x of the CBM life time from the γ -irradiation.

PMT VOLTAGE DIVIDER (NEUTRONS)



✧ Only after 1000x of the CBM the n-irradiation damages the PMT voltage divider.

RADIATOR

CBM RICH

Goal: separate electrons from pions with momenta up to 8 GeV →

Physics requirements:

need gas radiator (low n)
→ CO₂ or N₂

| | N ₂ | CO ₂ | C ₄ F ₁₀ | Aerogil | C ₅ F ₁₀ | Quartz |
|------------------------------|----------------|-----------------|--------------------------------|---------|--------------------------------|--------------------|
| δ [10 ⁻⁴] | 2.98 | 4.3 | 14 | 300 | 2700 | 4700 |
| $p_{th}(e)$ [GeV] | 0.02 | 0.017 | 0.01 | 0.002 | 7•10 ⁻⁴ | 5•10 ⁻⁴ |
| $p_{th}(\pi)$ [GeV] | 5.72 | 4.76 | 2.64 | 0.57 | 0.19 | 0.14 |

Practical considerations

$$\delta = n - 1$$

| | Radiator length [m] | Full length [m] | Mirror radius [m] | Mirror size [m ²] | Photon detector plane [m ²] | # of channels |
|-----------------|---------------------|-----------------|-------------------|-------------------------------|---|---------------|
| CO ₂ | 1.76 | 2.1 | 3 | 11.8 | 3.7 | 55k |
| N ₂ | 2.5 | 2.9 | 4.5 | 22.8 | 9 | 200k |

→ take CO₂

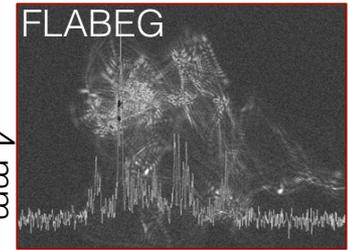
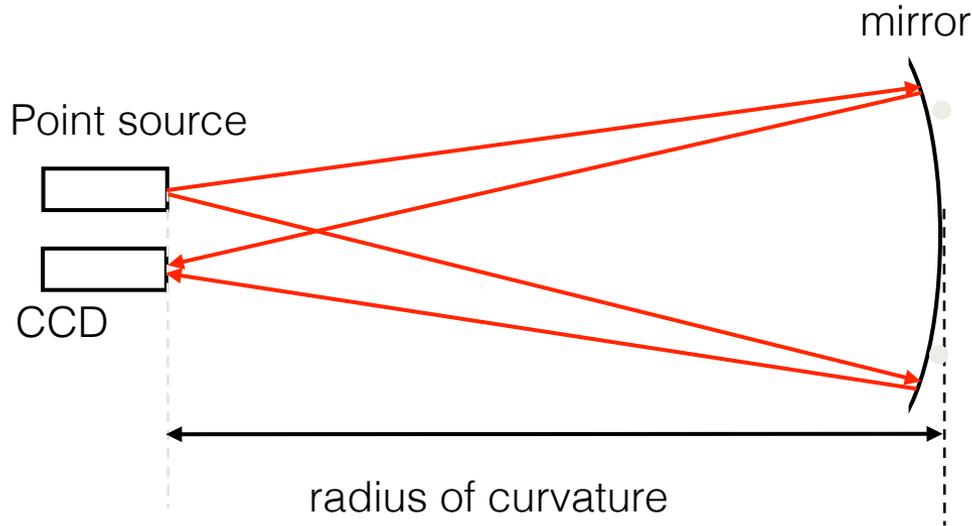
$$n_{CO_2} = 1.0004489 \rightarrow p_{th} = 33.37 * m/c^2$$

$$p_{th}(e^-) = 17 \text{ MeV}/c$$

$$p_{th}(\pi) = 4658 \text{ MeV}/c$$

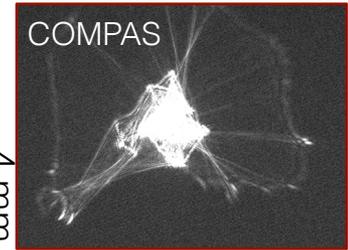
$$p_{th}(K) = 16474 \text{ MeV}/c$$

SURFACE HOMOGENEITY



4 mm

6 mm

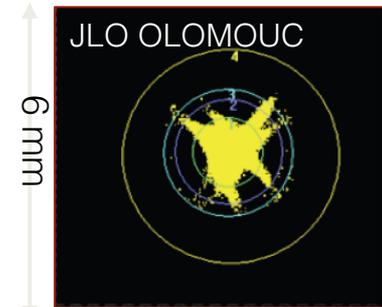


4 mm

6 mm

Homogeneity:

- D_0 as a measure of the mirror homogeneity.
- Reflect a point-like source on the mirror and record its image.
- Ideally the image is also point-like. In Reality, inhomogeneity causes a non-homogenous spot (picture).
- D_0 is the diameter, of a circle, which contains 95% of the reflected light



6 mm

6 mm

| | required | FLABEG | COMPAS | JLO OLOMOUC |
|------------|----------|----------|--------|-------------|
| D_0 (mm) | ≤ 3 | Very bad | 2.3 | 2.3 |

RESOLUTION

$$\sigma = \frac{\sqrt{\sigma_{mirror}^2 + \sigma_{disp}^2 + \sigma_{pixel}^2 + \sigma_{MS}^2 + \sigma_B^2}}{\sqrt{N}}$$

Cherenkov angle resolution for N photons

σ_{mirror} due to mirror quality. It is negligible.

σ_{disp} due to chromatic dispersion. Can be estimated to 1 mrad.

σ_{pixl} due pixel size. It is about 1 mrad.

P. Glässel. In: Nucl. Instr. Meth. A 433 17 (1999)

$$\sigma_{MS} = \frac{2}{3} MeV/c \cdot \sqrt{\frac{L}{X_0}} \cdot \frac{1}{p} = 0.874 MeV/c \cdot \frac{1}{p}$$

$$\sigma_B = 55.1 \frac{MeV}{Tm} \cdot \frac{LB_T}{p} \quad B_T = 0.077 Tm$$

| | | | |
|----------------------|-----|-----|-----|
| p [GeV] | 0.4 | 1 | 8 |
| σ_{MS} [mrad] | 2.2 | 0.9 | 0.1 |
| σ_B [mrad] | 18 | 7.2 | 0.9 |

$$\sigma(p = 8 GeV, N = 20) = 0.38 mrad$$

For a $\sigma = 0.572$ mrad (2% resolution), pions and electrons are separated by 5 sigma up to about 11 GeV/c.

