



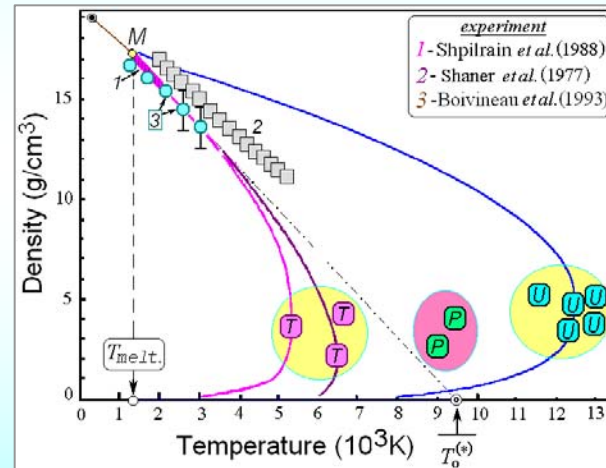
*EMMI: Cosmic Matter in the Laboratory*

Plasma Physics *with Intense Laser and Heavy Ion Beams*

3rd Workshop: Moscow, May 20-21, 2010



# Heavy Ion *and* Laser Heating *in resolution of* Uranium Critical Point Location Problem



Igor Iosilevskiy

*Joint Institute for High Temperature (Russian Academy of Science)  
Moscow Institute of Physics and Technology (State University)*



Support: RAS Scientific Program "Physics of Extreme State of Matter"  
MIPT Research-Education Center "Physics of Extreme State of Matter"



# Historical comments

Boris Sharkov, Meeting in ITEPh, 1997; EMMI-Workshop, 20 May, 2010; . . . .

! - Brilliant perspectives with HIB energy deposition,  $\Delta E \sim 100$  kJ/g. . . but now:  $\Delta E \sim 1$  kJ/g

? - What could we do with  $\Delta E \sim 1$  kJ/g and  $t_{\text{HIB}} \sim 100$  ns ?

Igor Iosilevskiy, Meeting in ITEP, 1997

Igor Iosilevskiy, Meeting at HIF, 2002

Igor Iosilevskiy, Meeting in GSI, 2007

Igor Iosilevskiy, Meeting in GSI, 2009

? ? ? Meeting in GSI, 20..??

? - What could we do with  $\Delta E \sim 1$  kJ/g and  $t_{\text{HIB}} \sim 100$  ns ?

Study of thermophysical properties for WDM

- What to study
- How to arrange HIB energy deposition
- How to arrange measurements

# HIB for thermophysical investigations

- What to study
- How to arrange HIB energy deposition
- How to arrange measurements

## Basic point

- Careful choice of investigated substance and physical problem

## Criteria

- great uncertainty
- great applied importance
- fundamental physics

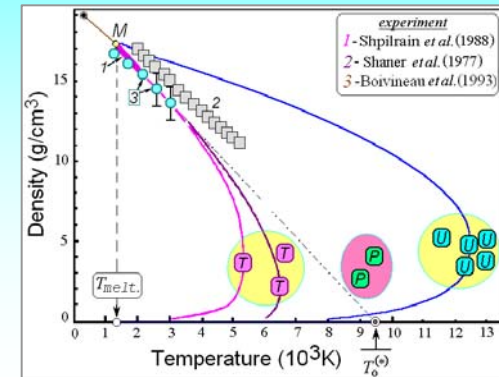
? - What substance - ? What property - ? What parameters - ?

# Low energy deposition – what could we study via HIB ?

## Two outstanding goals

### – Uranium Critical Point Location Problem

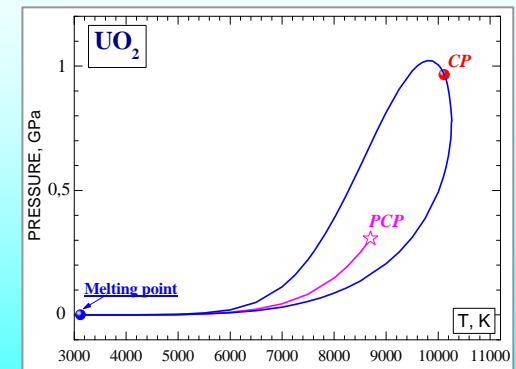
- applied importance
- phenomenology
- fundamental physical problem

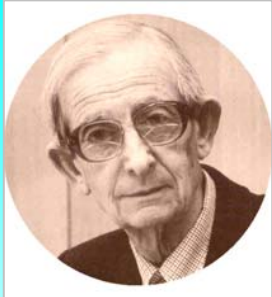


### – Non-congruent Phase Transitions in High Energy Density Matter

(uranium-bearing fuels (UO<sub>2</sub>, UC, UN ...) and other mixed substances)

- applied importance
- phenomenology
- fundamental physical problem





## «Extreme State of Matter»

Int. Conference "Equation of State"

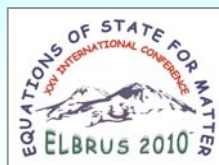
Russia, Elbrus, 1990 -2010

Int. Conference "Khariton's Science Readings"

Russian Federal Nuclear Center, Sarov, 2005 -2010

Int. Conference "Zababakhin's Science Readings"

Russian Federal Nuclear Center, Snezhinsk, 2005 -2010



# Uranium Critical Point Location Problem

- Applied importance
- Phenomenology
- Fundamental physical problem

In cooperation with:

Victor Gryaznov (*IPCP RAS*) and Artem Ukrainets & Katya Romadinova (*MIPT*)

# Uranium Critical Point Location Problem

## Uncertainty

*Recommendations of IVTAN-Database (1982)*

Critical Point Parameters

Cr	9620	968	0.023
Mo	11150	546	0.0365
W	13400	337	0.043
V	12500	1078	0.027
Nb	19040	1252	0.030
Ta	20570	13500	0.036
Ti	11790	763	0.037
Zr	16250	752	0.051
Hf	18270	938	0.046
Sc	8350	408	0.048
Y	10800	374	0.068
La	11060	335	0.078
Th	14950	488	0.072
U	11630	611	0.045
UO <sub>2</sub>	7580	122.6	0.163
UF <sub>6</sub>	504.5	4.59	0.255
Pu	10000	324.2	0.081
PuO <sub>2</sub>	7620	101	0.202
Li	3680	60	0.055
Na	2503	25.64	0.111
NaCl	3400	35	0.266
K	2280	15.8	0.202
KCl	3200	22	0.415
Rb	2106	13.22	0.246
Cs	2043	11.75	0.308

Discussion: I. Iosilevskiy & V. Gryaznov, *Journ. of Nuclear Materials*, **344** (2005)

# Critical Point Parameters

## Recommendations of IPCP RAS-GSI Database

	<i>Pressure</i> $P_c$ kbar	<i>Temperature</i> $T_c$ K	<i>Density</i> $\rho_c$ g/cm <sup>3</sup>	<i>Entropy</i> $S_c$ J/gK
<i>Be</i>	2.87	8877	0.398	13.18
<i>Mg</i>	2.46	3957	0.553	3.789
<i>Na</i>	0.47	2473	0.240	3.281
<i>Zr</i>	9.88	14860	1.634	1.693
<i>Hf</i>	11.74	15810	3.610	0.885
<i>V</i>	9.19	9915	1.631	2.718
<i>Nb</i>	11.06	19180	1.701	2.023
<i>Ta</i>	9.93	13530	4.263	0.923
<i>Cr</i>	9.91	7797	2.660	2.332
<i>Mo</i>	7.59	10180	3.690	1.520
<i>W</i>	11.80	15750	4.854	0.837
<i>Fe</i>	11.31	8787	2.183	2.496
<i>Co</i>	5.55	9157	1.890	2.458
<i>Ni</i>	10.42	7547	2.092	2.518
<i>Zn</i>	3.28	3079	2.381	1.468
<i>Cd</i>	0.87	2510	2.283	0.840
<i>Ag</i>	10.64	7053	3.279	1.118
<i>Au</i>	6.14	8515	6.061	0.624
<i>Re</i>	15.91	18710	6.024	0.824
<i>Ir</i>	13.40	16220	6.061	0.780
<i>Pt</i>	6.21	11430	5.236	0.807
<i>Sn</i>	2.39	8175	1.592	1.123
<i>Pb(VI)</i>	2.25	4869	2.937	0.529
<i>U</i>	7.70	9637	4.505	0.727

After  
D. Varentsov  
*FAIR-Russia School*  
*Moscow, 2009*

# Uranium Critical Point Location

*fifty years old problem*

List of Uranium  
CP parameters  
estimations

$T_c \approx 12'000 \text{ K}$		<i>(the early estimation)</i>			Braut (1957)	
$T_c$ [K]	$p_c$ , bar	$\rho_c$ g/cm <sup>3</sup>	$Z_c$	$\rho_s/\rho_c$ (*)	References	
6'618	4160	4.12	0.437	4.60	Young D. (1977)	
7'533	798	1.03	0.295	18.4	Gates D. et al. (1960)	
6'200–7'663	-	-	-	-	Goldstein R.(1989) Hess H.(1995)	
8'317–9'112	-	-	-	-	Guldberg C. (1890).	
8'730	2360	5.17	0.150	3.67	Martynyuk M. (1989).	
9'000 ( $z_c = 3$ )	5000	2.60	0.6	7.42	Likalter A. (1997)	
9'400 ( $z_c = 3$ )	6000	2.59	0.706	7.32	Likalter A. (1985 - 1996)	
11'630	6110	5.30	0.284	3.58	Fortov V. et al. (1975)	
11'679–12'995	-	-	-	-	Kopp I. (1967) Lang G. (1977)	
12'400	4800	3.55	0.312	5.34	Morris E. (1964)	
12'434	4950	3.78	0.302	5.02	Gathers-Shaner-Young (1974)	
12'500	-	-	-	-	Grosse A. (1961)	
13'034	5136	4.03	0.280	4.71	Hornung K. (1975)	
13'043	8'487	5.17	0.361	3.66	Young D. & Alder B. (1971)	
9'636	7'700	4,50	Wide-range EOS	Bushman - Lomonosov		
7'000	1'712	3,30	Extrapolation of Liquid $\rho(T)$	Apfelbaum - Vorob'ev (2009)		
5'500–6'500	100 – 1'000	<i>(estimation – thermal EOS calibration)</i>		Iosilevskiy (1990)		
6'840	4'440	<i>(Plasma model – thermal calibration)</i>		Iosilevskiy & Gryaznov		
12'800	8'450	<i>(Plasma model – caloric calibration)</i>		SAHA-code, JNM, (2005)		

Table from:  
H. Hess,  
H.Schneidenbach  
Z. Metallkd. (2001)  
Vapor Pressure and  
Critical Data for  
Uranium

Additions IL



# Uncertainty in high-temperature density-temperature diagram

Shpilrain *et al.* (1988)  
 Static experiment: -  $\rho_{liquid}$  ( $1400 < T < 2100$  K)  
 high accuracy - 0.5 %

**Thermal variants** T  
 Yound & Shaner (1977)  
 Gathers *et al.* (1986)  
 Iosilevskiy (1991)  
 Iosilevskiy & Gryaznov (SAHA-T)

---

Correlation  
 $T_c \Leftrightarrow$  Thermal expansion

**Caloric variants** U  
 Brout (1957)  
 Grosse (1961)  
 Morris (1964)  
 Yound & Alder (1971)  
 Gathers *et al.* (1974)  
 Fortov *et al.* (1975)  
 Hornung (1975).....  
 Iosilevskiy & Gryaznov (code SAHA-E)

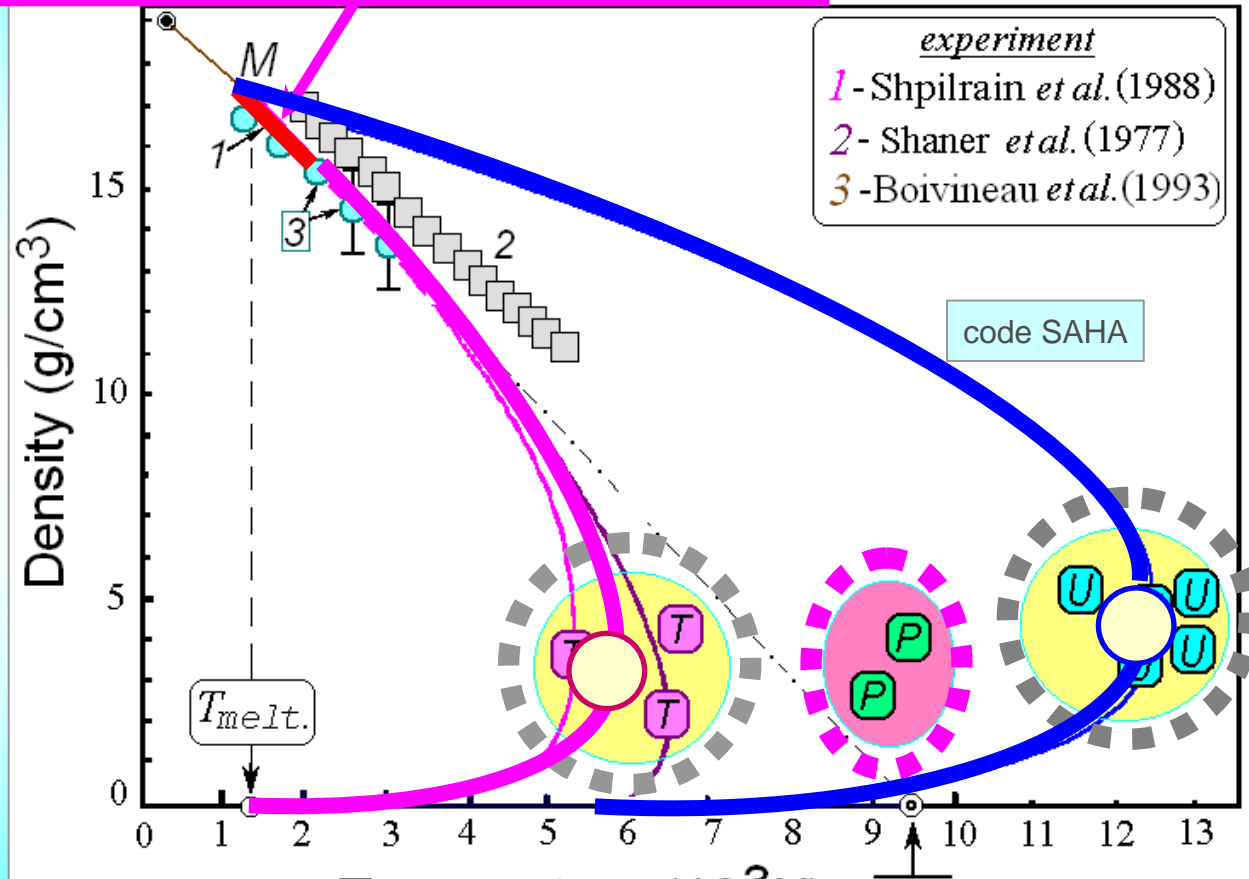
---

Correlation  
 $T_c \Leftrightarrow$  Vaporization heat

**Plasma Hypothesis** P  
 Likalter (1981)  
 Likalter + Hess (1997)

---

Correlation  
 $T_c \Leftrightarrow$  Ionization Potential



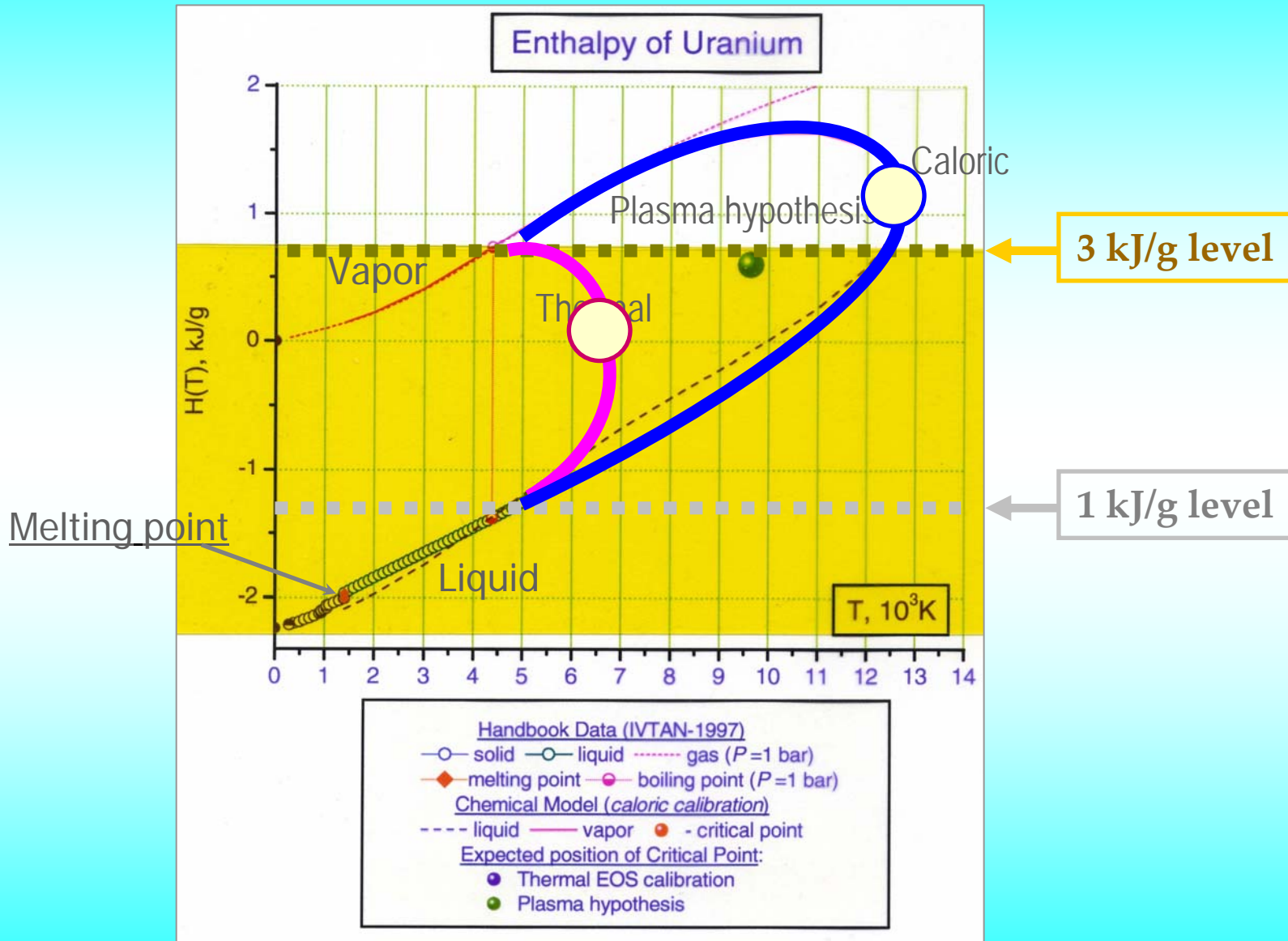
*experiment*  
 1 - Shpilrain *et al.* (1988)  
 2 - Shaner *et al.* (1977)  
 3 - Boivineau *et al.* (1993)

Extrapolation: (i) Guggenheim's formula, (ii) Law of Correspondent States (Iosilevskiy, 1990), (iii) SAHA-code (Iosilevskiy & Gryaznov, 2005)

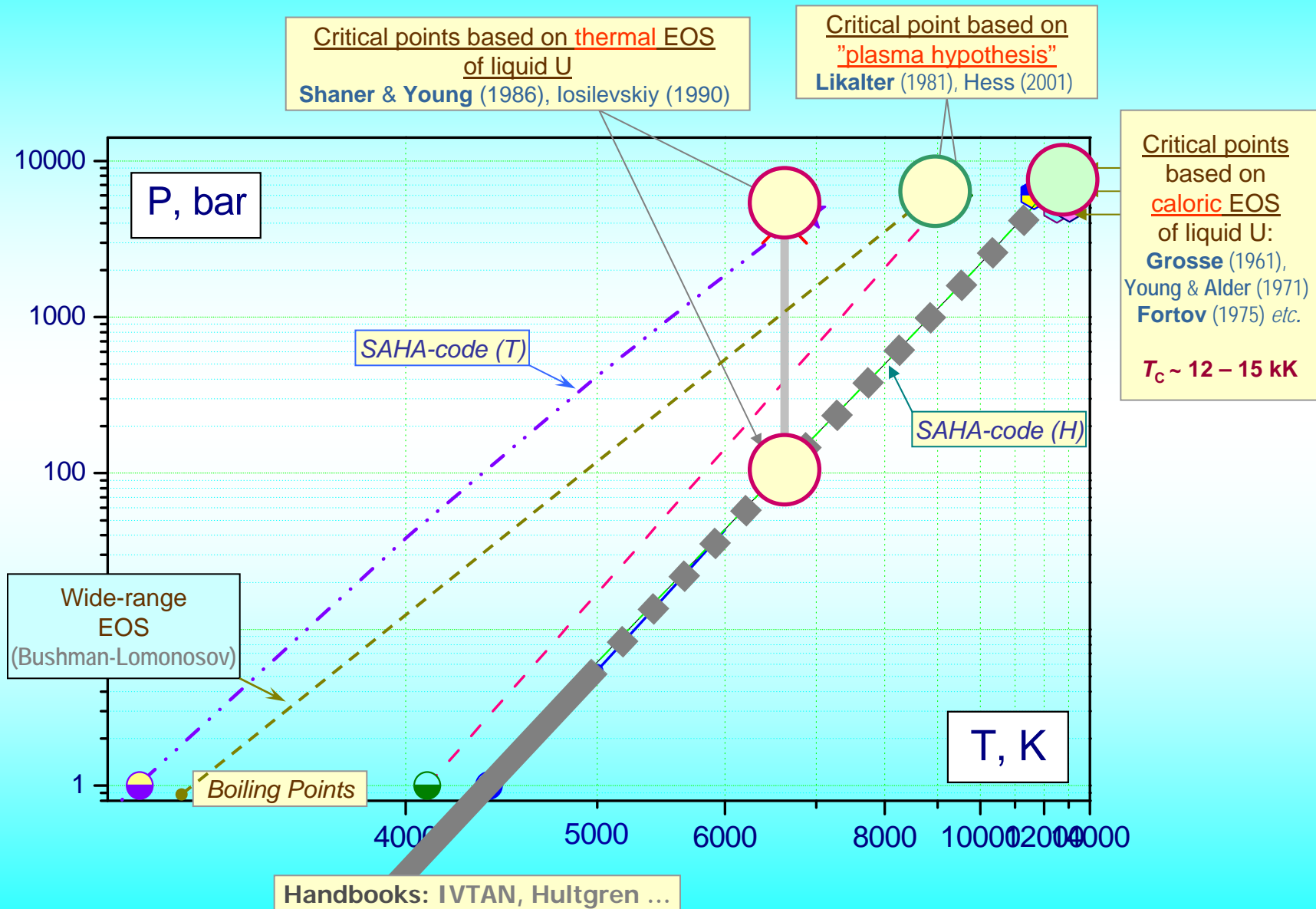
(i) 
$$\frac{\rho_{l,v}}{\rho_c} = 1 + b_1 \left(1 - \frac{T}{T_c}\right) \pm b_2 \left(1 - \frac{T}{T_c}\right)^\beta$$

(ii) 
$$\left(\frac{\rho(T/T_{cr})}{\rho_{cr}}\right)_U = \left(\frac{\rho(T/T_{cr})}{\rho_{cr}}\right)_{C_s}$$

# Uncertainty in high-temperature caloric phase diagram



# Uncertainty in Uranium Critical Pressure



SAHA-code: I. Iosilevskiy & V. Gryaznov, *Journal of Nuclear Materials*, **344** (2005)

# The Problem:

## Experimental data:

Liquid density  $\rho(T)$  - ( $T < 5$  kK)  
Liquid enthalpy  $H(T)$  - ( $T < 5$  kK)  
Vapor pressure  $P_s(T)$  - ( $T < 5$  kK)

## Semi-empirical rules:

Convexity of liquid density  $\rho_L(T)$   
Quasi-linear vapor pressure  $\ln P_s(T^{-1})$   
Universal evaporation enthalpy  $\Delta H(T)$

*Incompatible*

## Dilemma:

Access semi-empirical rules  
*and*  
Deny experimental data

*or*

Access experimental data  
*and*  
Violate semi-empirical rules

*Hypothetical resolution ?*

# In Search *of* Resolution *for* Uranium Critical Point Location Problem

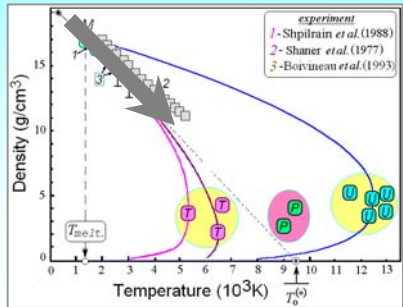
Low temperature

? Wrong experiment

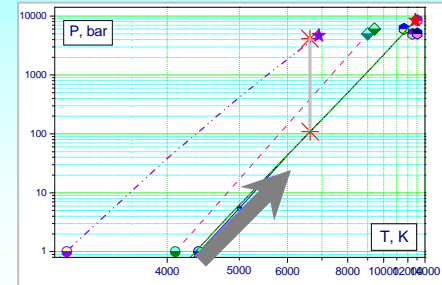


High temperature

wrong extrapolation ?



liquid density  $\rho(T)$  - ?  
liquid enthalpy  $H(T)$  - ?  
vapor pressure  $P_s(T)$  - ?



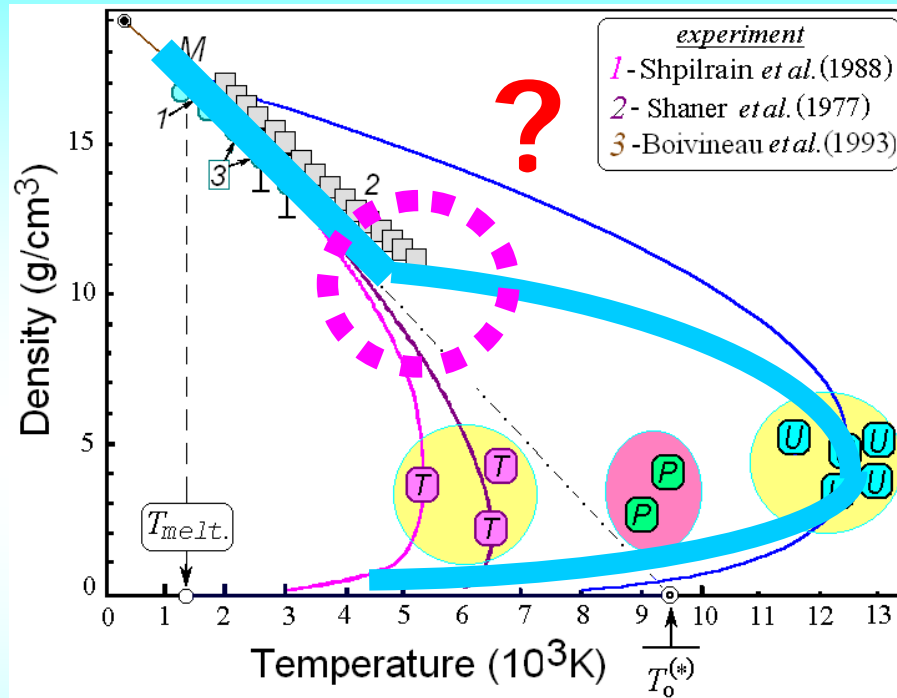
**! unbelievable !**

We have enough reason to expect

**Violation of semi-empirical rule(s)**

# Hypothetical violation of semi-empirical rule(s)

## Lost of convexity for $\rho_L(T)$ ?



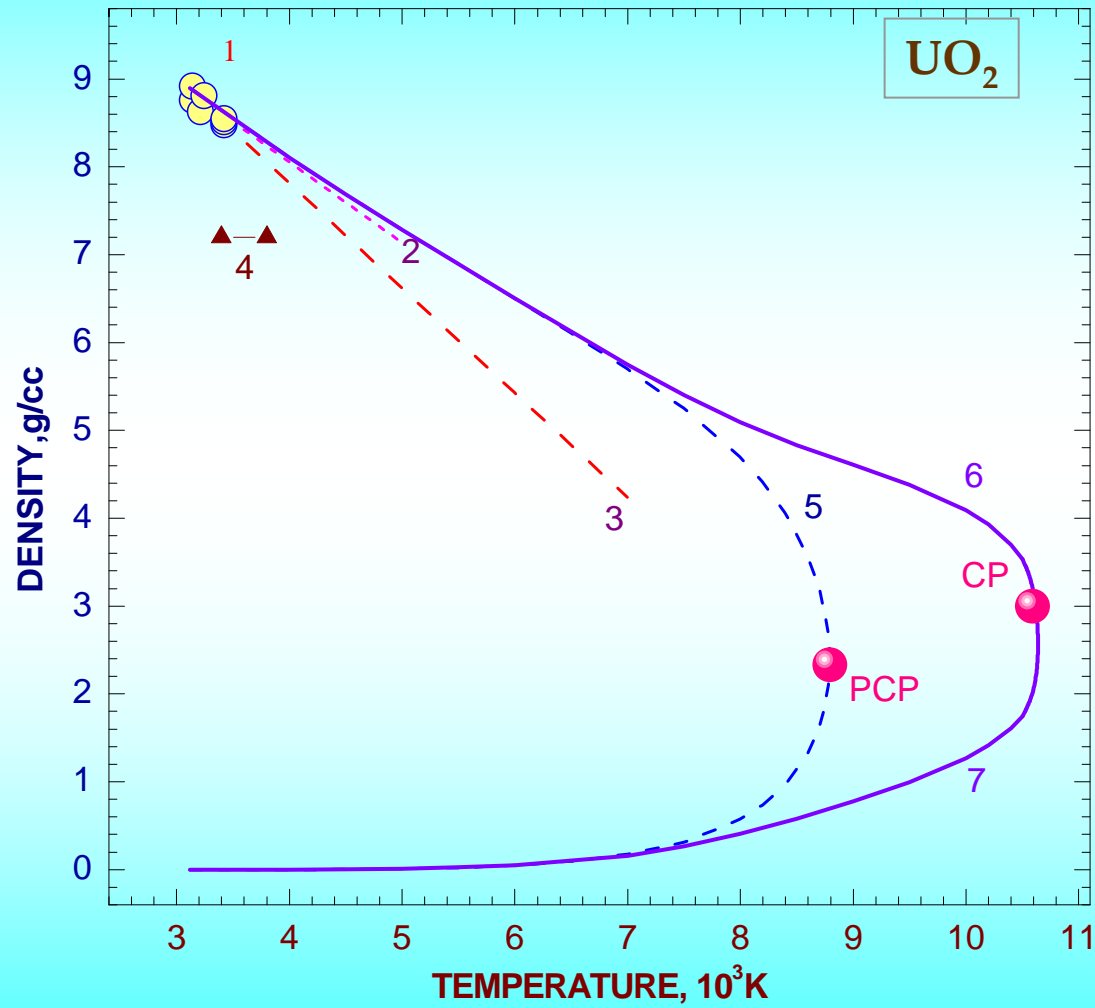
? What physical reason can approve this violation ?



Elbrus\_1990-2010

# Exception

## Non-congruent evaporation !



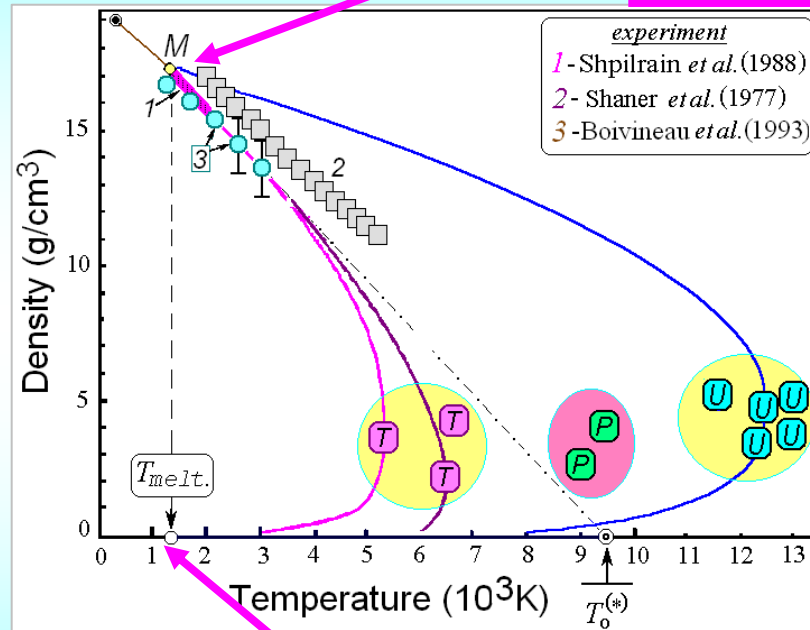
Iosilevskiy I, Hyland G., Ronchi C., Yakub E. "An Advanced Equation of State of UO<sub>2</sub> up to the Critical Point" - *Trans. Amer. Nucl. Soc.* **81** 122 (1999)// - *Int. Journ. Thermophys.* **22**, 1253 (2001)// *Contrib. Plasma Phys.* **43**, (2003)

# What physical reason can approve the lost of convexity for $\rho(T)$ two-phase boundary in uranium ?



$Z = 3$

$\text{U}^{+3} + 3e^-$   
 $\Gamma_D \approx 3300 // n_e \lambda_e^3 \approx 900$



$\text{U}^{+1} + e^-$   
 $\Gamma_D \approx 80 // n_e \lambda_e^3 \approx 10$

$Z = 1$

$Z = 0$

**NB !**

Drastic change of effective ion-ionic interaction during thermal expansion of liquid uranium and decrease of electronic degeneracy

Drastic change of phase behavior of evaporating uranium ( $\rho$ - $T$  diagram)



# Uranium Critical Point Location Problem

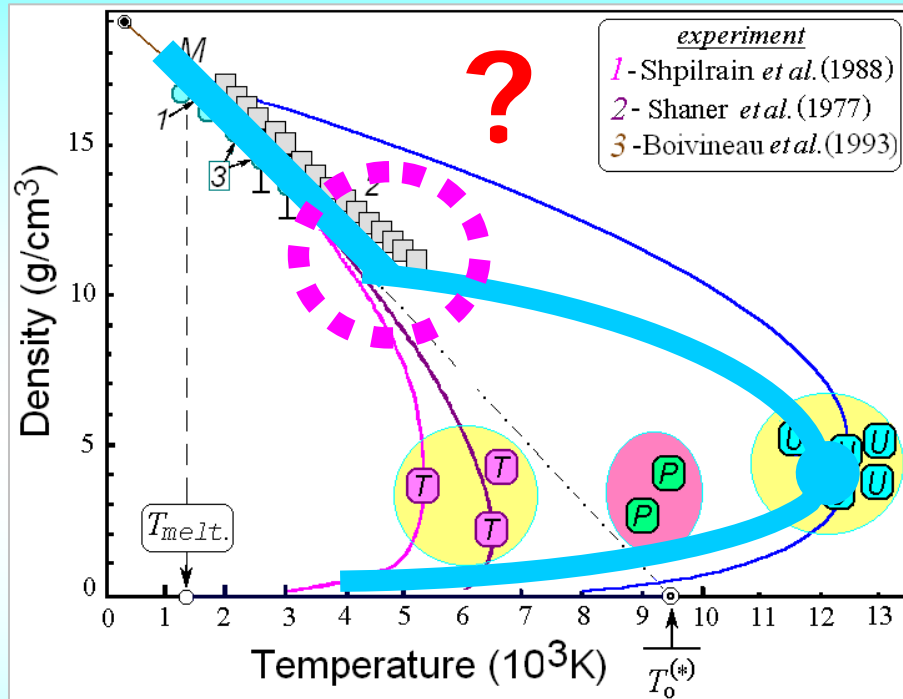
## Hypothetical resolution - I

### Discussion:

*I. Iosilevskiy & Int. Conference: Subsecond Thermophysics, Moscow, 2008// FAIR-Russia School, Moscow, 2009*

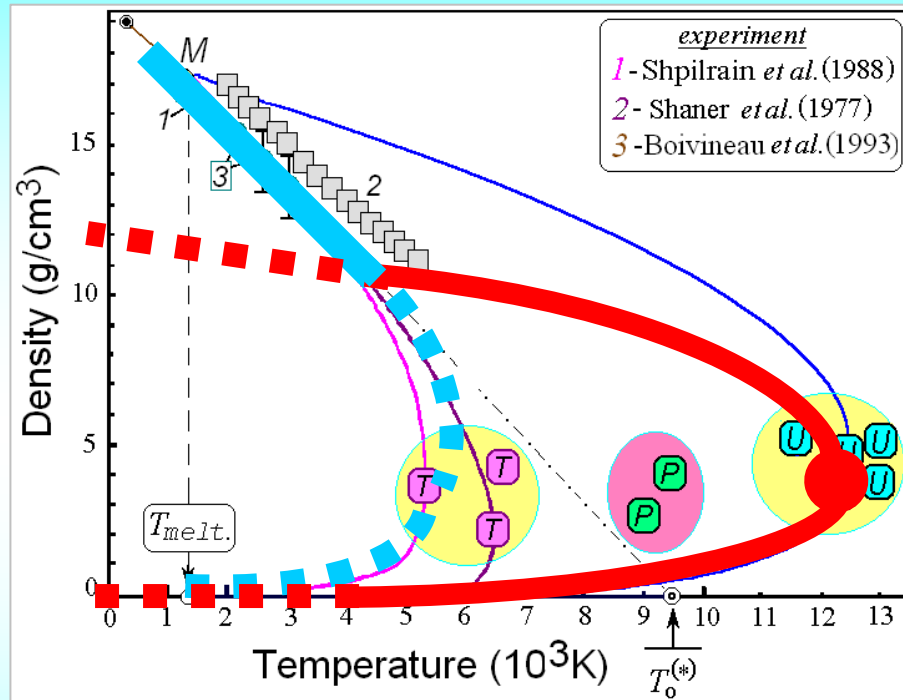
# Hypothetical resolution of uranium critical point location problem

?  $\rho$ - $T$  phase boundary consists of **TWO** fragments ?



# Hypothetical resolution of uranium critical point location problem

?  $\rho$ - $T$  phase boundary consists of **TWO** fragments ?



«high-density phase»  $\Leftrightarrow$  «low-density phase»

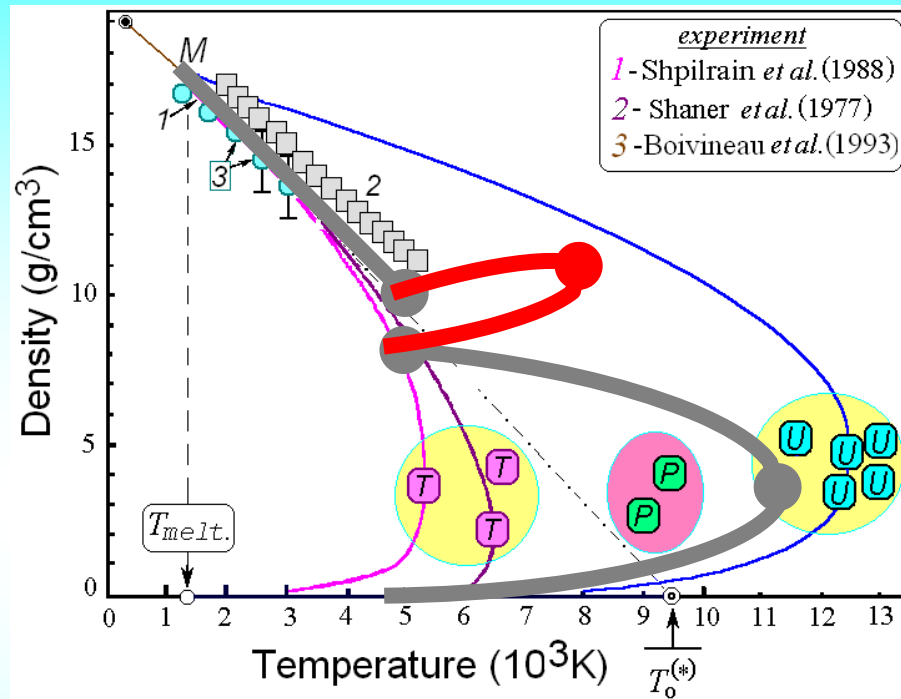
*More exotic and hypothetical*

## Hypothetical resolution - II

Transition from the “high-density phase”  
to the “low-density phase”  
**must not be continuous**

**Additional phase transition ?**

# Additional phase transition ?



*Very exotic but not fantastic !*

**! Only 1 – 2 kJ/g is needed !**

# Fundamental Physical Problem

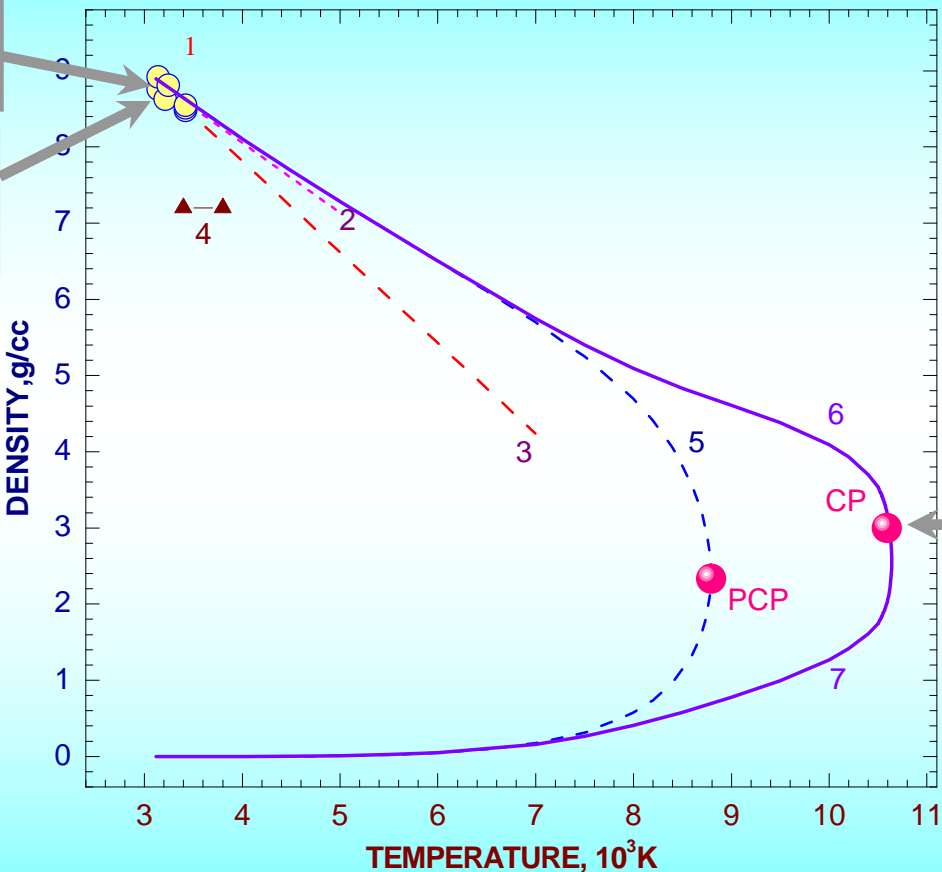
**Phase transition in a system  
*with*  
varying mean-particle interaction**

Non-congruent evaporation in  $\text{UO}_2 \rightleftharpoons$  the same physical problem

Phase transition in the system with varying composition

*Molecular model*  
 $\text{UO}_2 \rightleftharpoons \text{UO}_2$

*Ionic model*  
 $\text{U}^{+4} \rightleftharpoons \text{O}^{-2}$



*Ion-molecular mixture*  
 $\text{U} \rightleftharpoons \text{O} \rightleftharpoons \text{UO}$   
 $\text{UO}^+ \rightleftharpoons \text{UO}_2^+$   
 $\text{O}^- \rightleftharpoons \text{UO}_2^- \rightleftharpoons \text{UO}_3^-$

Phase transition in the system  
 with varying mean-particle interaction !

# Fundamental Physical Problem

## *What could we do ?*

- Study via simplified analytical plasma models

One-component plasma model on uniformly-compressible compensating background {OCP(~)}

- Study via direct numerical simulation

FT-DFT\_MD // Monte-Carlo // . . . .

- Experimental study:

Exploding wires, . . . . *etc*

**Heavy Ion Beam**

**Surface Laser Heating**



# HIB for thermophysical investigations

## – How to arrange HIB energy deposition

### Priorities

- Uniformity of heated material
- Thermodynamic equilibrium

## – How to arrange measurements

### Priorities

- Direct measurement of thermodynamic parameters  
without intermediate hydrodynamic re-calculations
- Energy deposition control

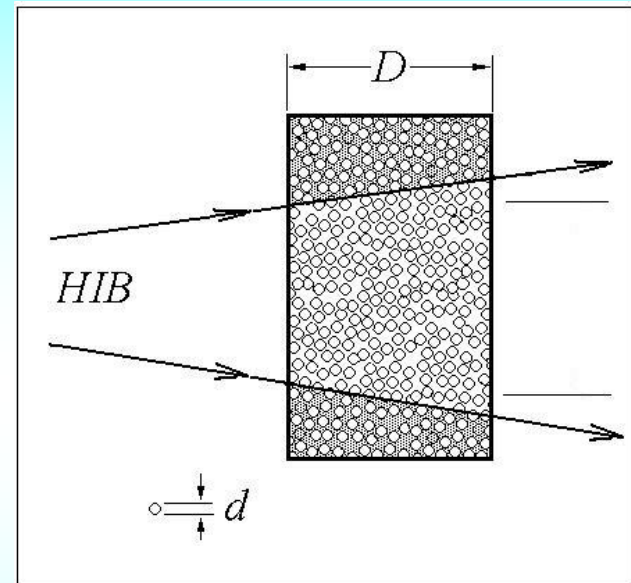
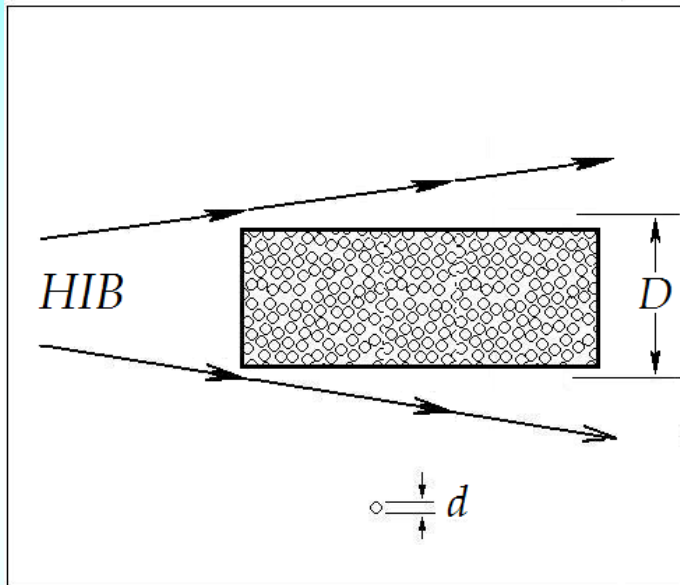
**HIB heating of highly dispersive materials –  
– very promising for thermophysical investigations (\*)**

\* Iosilevskiy I. // Int. Conf. *Intense Ion Beam Interaction with Ionized Matter* // Moscow, ITEP Publishing (1999)

\* Iosilevskiy I., Gryaznov V. // XIV Int. Conf. *Heavy Ion & Inertial Fusion* // Moscow, ITEP Publishing (2002)

# How to arrange HIB energy deposition

- HIB heating of highly dispersive porous materials –  
– very promising for thermophysical investigations (\*)



## Advantages:

- uniform quasi-free equilibrium expansion of each grain
- no fast hydrodynamic movement
- surface thermodynamic parameters are equal to the bulk ones
- porosity ( $\rho_{00}/\rho_0$ ) is well-controlled parameter

\* Iosilevskiy I. // Int. Conf. *Intense Ion Beam Interaction with Ionized Matter* // Moscow, ITEP Publishing (1999)

\* Iosilevskiy I., Gryaznov V. // XIV Int. Conf. *Heavy Ion & Inertial Fusion* // Moscow, ITEP Publishing (2002)

# Moment "X"

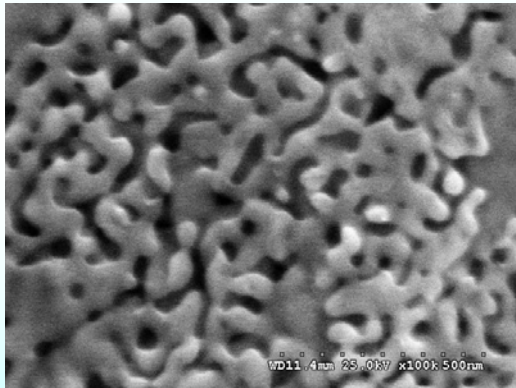
\* \* \* \* \*

## Basic idea

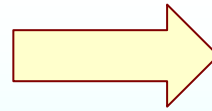
**Critical event** – Exhausting of free volume for grain's thermal expansion

**!!** In this moment we obtain:

- **Uniform** and **homogeneous** state of investigated material
- **Known density** (*due to porosity and initial density control*)



|← 1 μm →|



**!!** It means :

- **End** of free quasi-**isobaric** expansion
- Fast **increasing** of bulk **pressure**
- **Start** of stressed quasi-**isochoric** expansion

**Pressure Jump**

# Moment "X"

\* \* \* \* \*

## Pressure Jump

### !! If we catch this moment

and if we know:

- temperature (*surface*)
- energy deposition (*beam control*)
- density (*porosity control*)

### !! We obtain:

- Density of expanded liquid  $\rho(T)_{liquid}$  (*or*  $\rho(H)_{liquid}$ )
- Thermal (*or caloric*) expansion coefficient

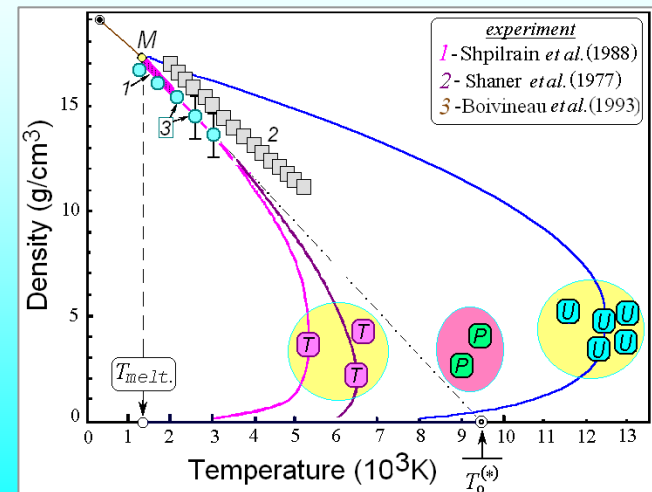
$$\alpha_P = (\partial\rho/\partial T)_P \quad \alpha_P^* = (\partial\rho/\partial U)_P$$

\* \* \* \* \*

- Heat capacity  $C_P = (\partial U/\partial T)_P$

### !! Hypothetically:

- sound speed,
- vapor pressure,
- electro-conductivity ... *etc.*



# Quasi-static heating of a stack target

$t < t_x$ : quasi-static heating of a stack of foils

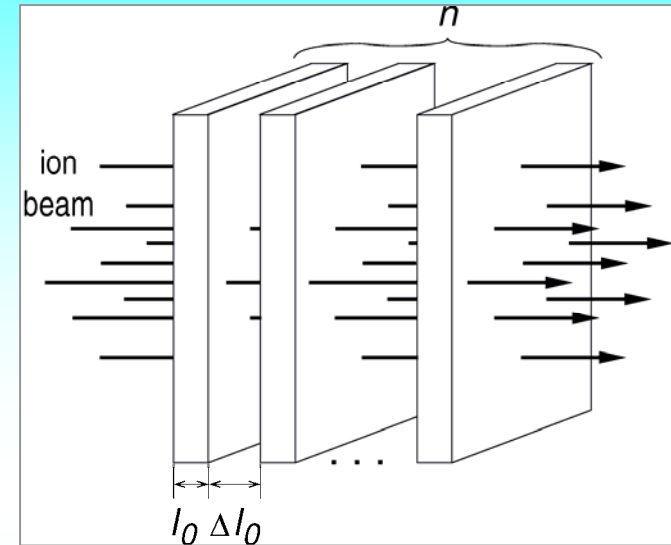
•  $\rho, P, \varepsilon$  (and  $T$ ) are spatially uniform  $u_l = \frac{1}{2} \alpha l q$

• expansion velocity

$l$  – foil thickness,  $q$  – heating rate,

$$\alpha = \left( \frac{\partial P}{\partial \varepsilon} \right) \left( \frac{\partial P}{\partial \ln \rho} \right)^{-1}$$

• kinetic energy  $E_{kin} \ll \varepsilon$



Thermal (not hydrodynamic) expansion if the foils are thin:  
 $\Delta\rho/\rho \ll 1$  over  $t_s = l/c_s$  (sound propagation time)

mean density:  $\rho_{00} = \rho_0 \frac{l_0}{l_0 + \Delta l_0}$

at  $t = t_x$ :  $l = l_0 + \Delta l_0$

$t = t_x$ : the foils merge, weak shocks are generated

$t > t_x$ : expansion velocity is determined by shock hydrodynamics

1D target expansion in planar geometry;  $t_x$  can be detected by measuring the surface velocity

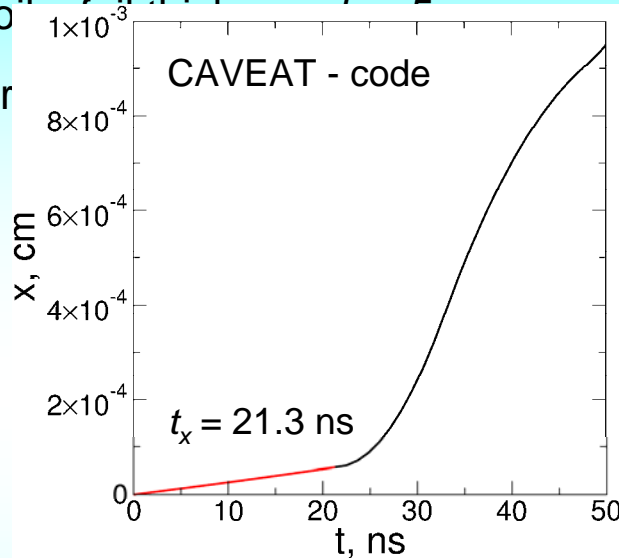
# Hydrodynamic simulation

foils made of Al:  $\rho_0 = 2.7 \text{ g/cm}^3$ ,  $c_s = 5 \cdot 10^5 \text{ cm/s}$ ,  $\Gamma = 2.5$

Position of the target surface

$n = 10$  foils

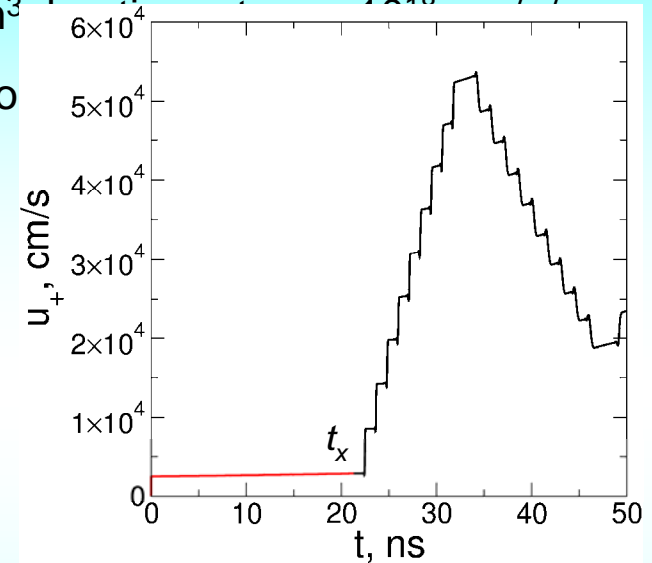
sound pr



$2.2 \text{ g/cm}^3$

expansio

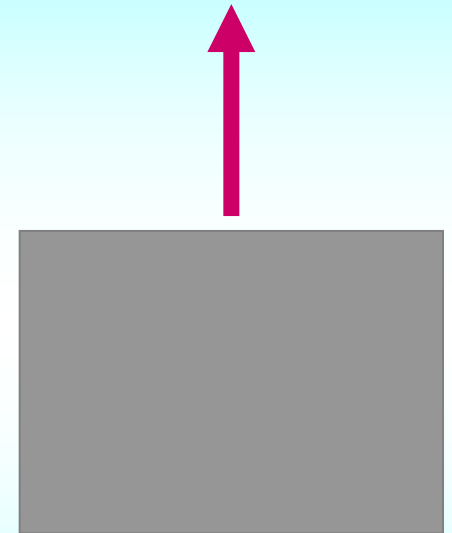
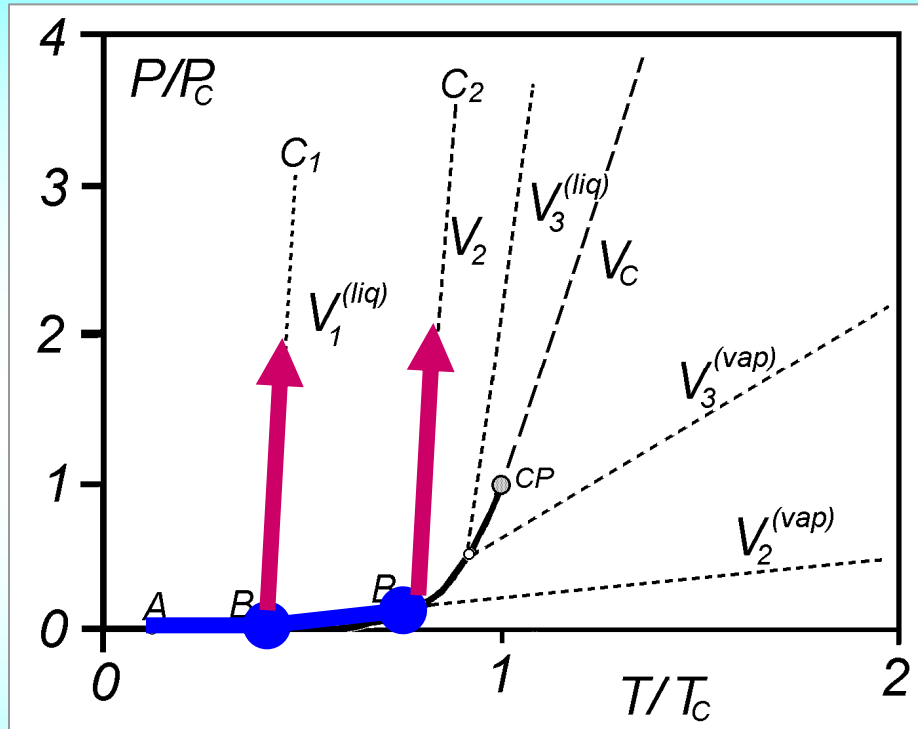
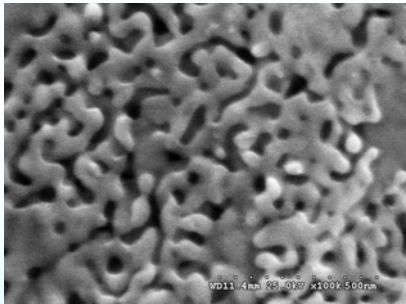
Expansion velocity



The “homogenization” time  $t_x$  can be detected by measuring the surface velocity

Thermophysical investigations via HIB  
(*novel regimes*)

# Tracing of the Boiling Curve



$0 < t < t^*$  – Quasi-free “isobaric” expansion



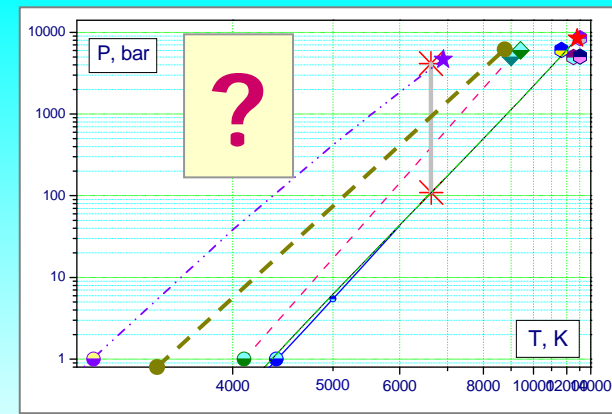
Moment “X”:  $\rho = \rho^*$

$t > t^*$  – Isochoric Heating + Hydrodynamic Expansion

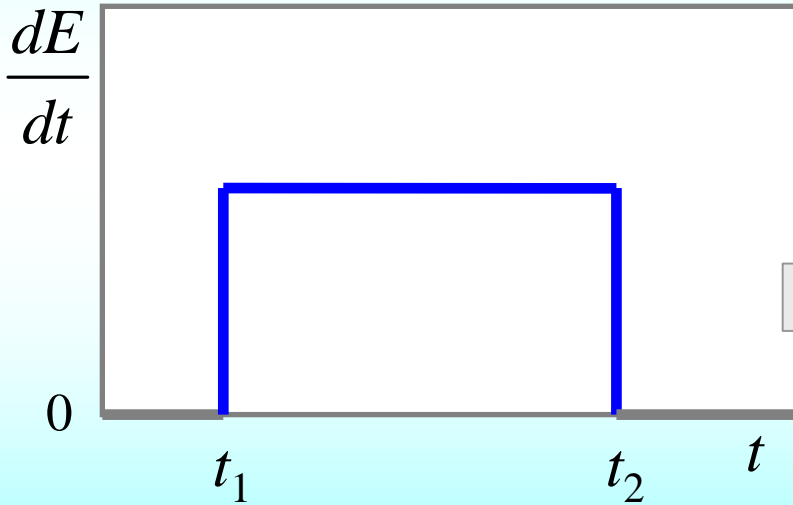
Goal for experimenters: – to catch the pressure jump moment!

# Measurement of Uranium Vapor Pressure in Experiment with Surface Laser Heating

$$P = \text{const (in buffer gas)}$$

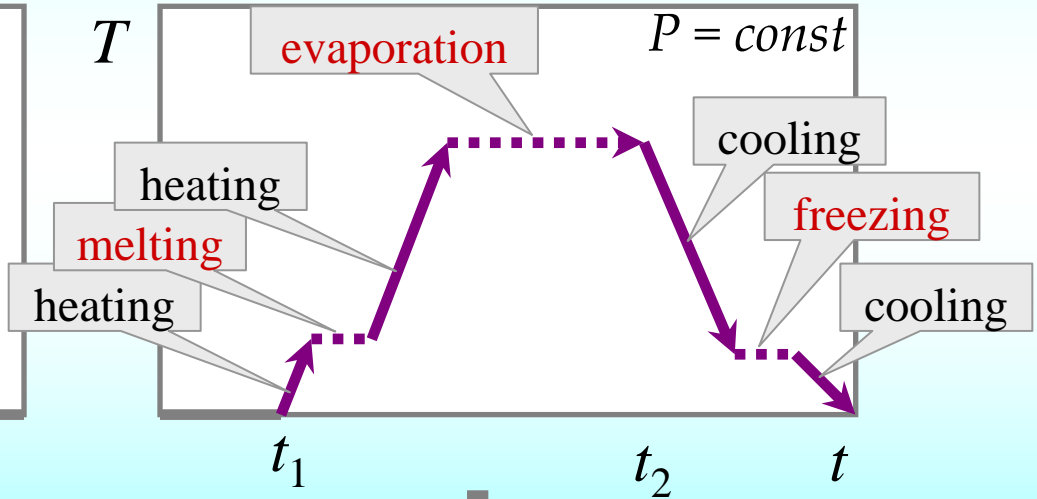


*Laser impulse*



$$P = 1 - 1000 \text{ bar}$$

*Schematic thermogram*



$$T_{\text{melt}}(P) \quad T_{\text{boil}}(P)$$





## Conclusions *and* Perspectives

In the case of **uranium** we meet **fundamental physical problem**:

- *Phase transition in a system with mean-particle interaction strongly dependent on density (and temperature)*

- It is **promising** to investigate this problem analytically via **simplified plasma models**

- It is **promising** to investigate this problem in **direct numerical simulation** in frames of ***ab initio*** approaches

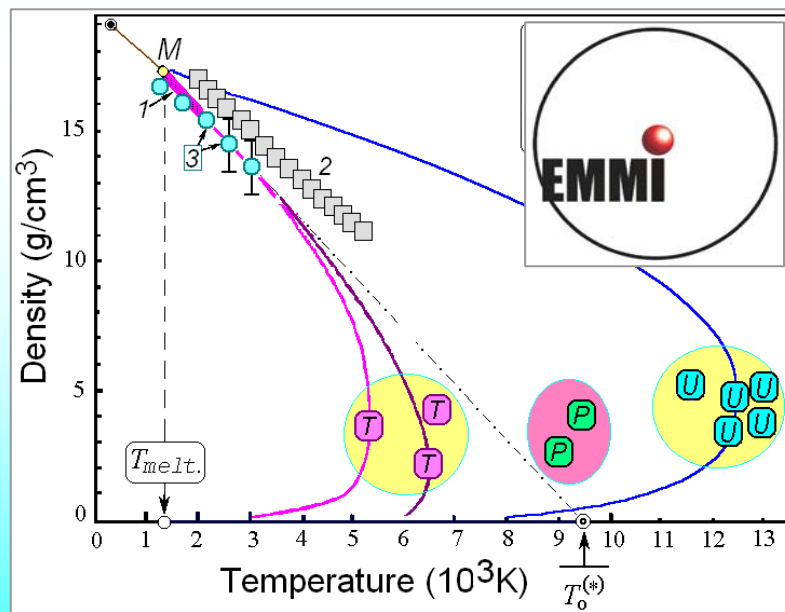
- It is **promising** to investigate non-congruent phase transitions **experimentally**. in particular with **intense laser** and **heavy ion** heating

**! Only 1 – 3 kJ/g is needed !**



Features of phase transitions in cosmic matter and laboratory

# Thank you!



Support: RAS Scientific Program "Physics of Extreme State of Matter"  
MIPT Research-Education Center "Physics of Extreme State of Matter"