

ExtreMe Matter Institute EMMI

EMMI Workshop

Bound states and particle interactions in the 21st century

University of Trieste, Italy, July 3 – 6, 2023

Meson–baryon scattering and $\Lambda(1405)$ in baryon chiral perturbation theory

Xiu-Lei Ren (任修磊)



In collaboration with:

E. Epelbaum (RUB), J. Gegelia (RUB), and U.-G. Meißner (Bonn)

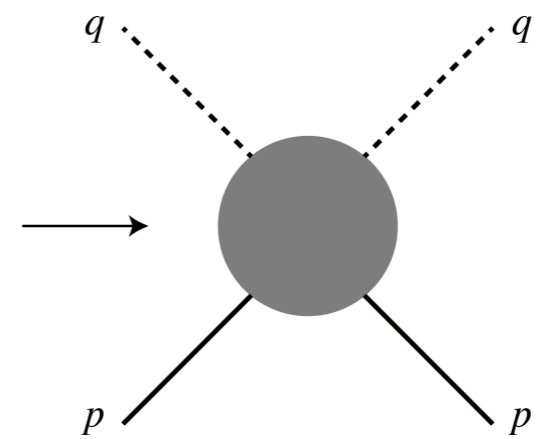
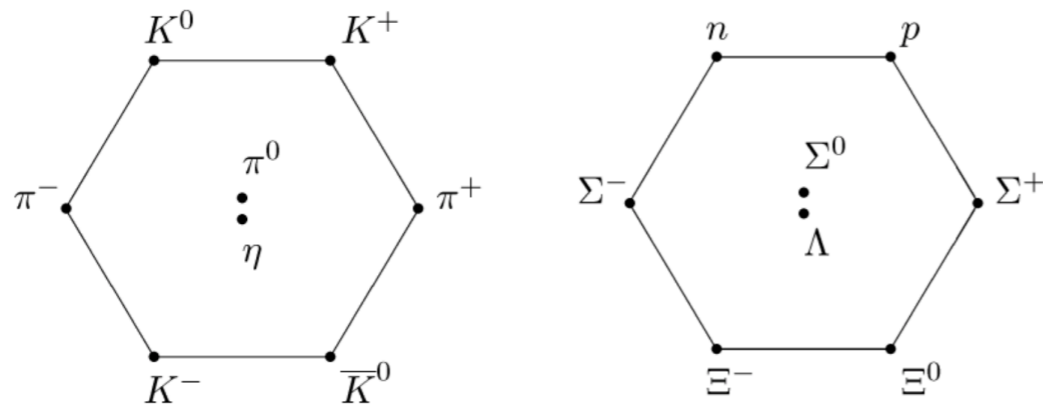
2023.7.6

OUTLINE

- Introduction
- Theoretical framework
- Results and discussion
- Summary

Meson-baryon scattering

Simple process: lowest-lying MB scattering



Interesting phenomena

- πN scattering: 30K data points of GWU

✓ Sigma term $\sigma_{\pi N}$, key input of neutralino-nucleon cross section

M. Hoferichter, et al., PRL115,092301(2015) J.R. Ellis, et al., PRD77(2008)065026

- $\bar{K}N$ interaction is important in strangeness nuclear physics

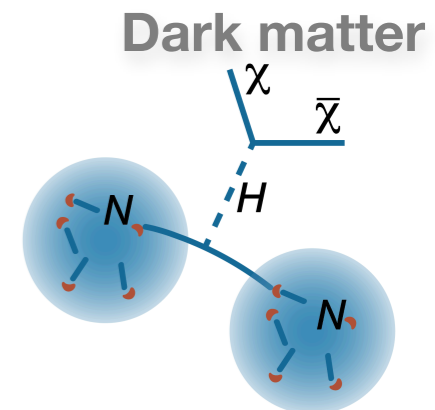
✓ Interaction is strongly attractive, generating $\Lambda(1405)$ resonance

✓ $\bar{K}NN, \bar{K}NNN$, multi-antikaonic nuclei **J-PARC, FINUDA@DAΦNE, etc**

✓ Kaon-condensate (?) in the interior of neutron star *S.Pal et al., NPA674(2000)553*

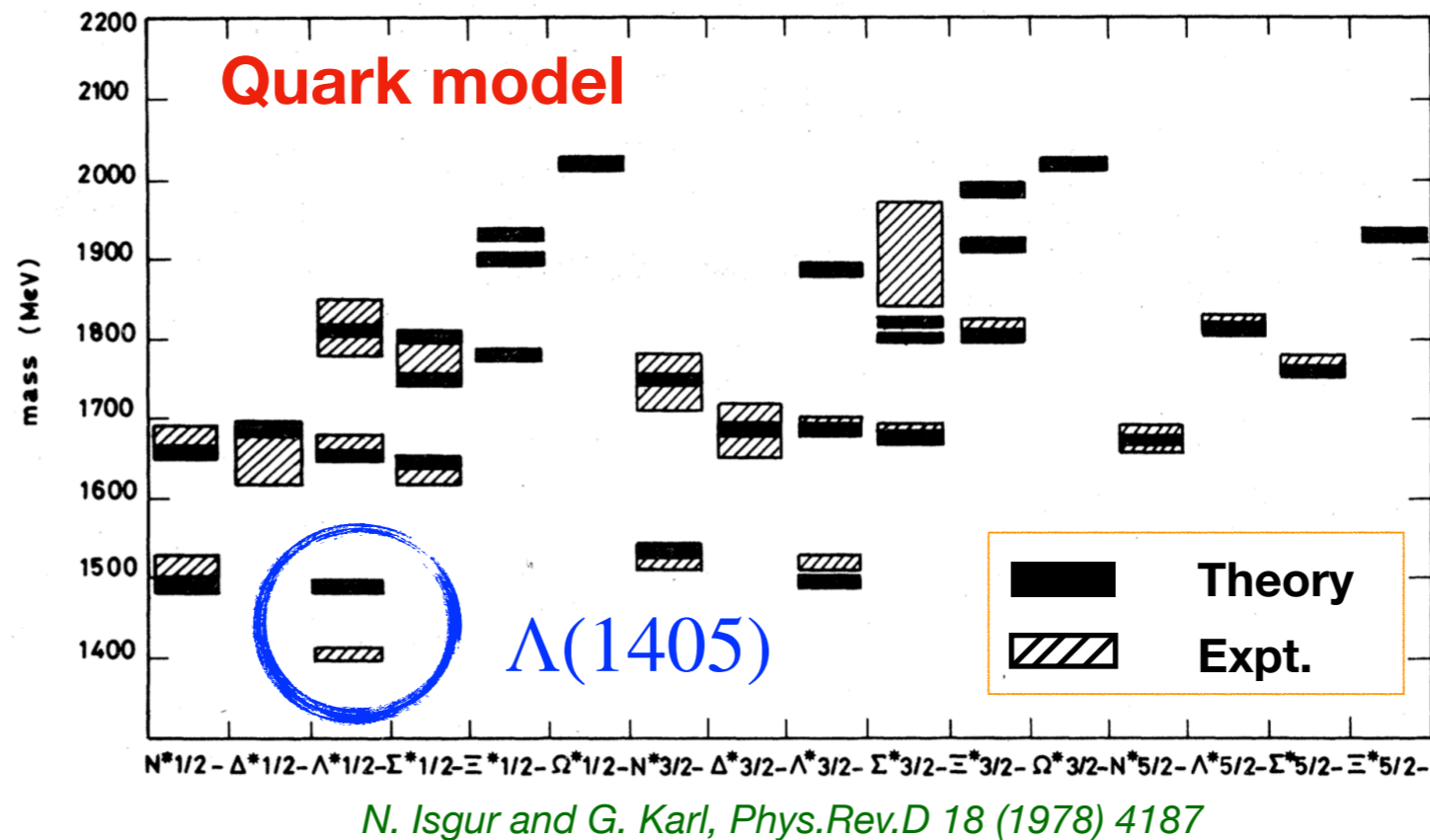
see Oton Vázquez Doce's talk @ Monday

- Deepen understanding of SU(3) dynamics in nonperturbative QCD



$\Lambda(1405)$ resonance

- $\Lambda(1405)$ state is an exotic candidate

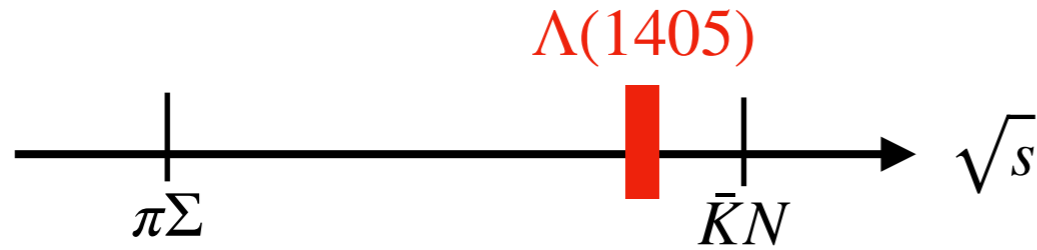


- Variety of theoretical studies

- QCD sum rules *L.S. Kisslinger, EPJA2011...*
- Phenomenological potential model *A. Cieplý, NPA2015...*
- Skyrme model *T. Ezoë, PRD2020...*
- Hamiltonian effective field theory *Z.-W. Liu, PRD2017...*
- Chiral unitary approach *N.Kaiser, NPA1995; E.Oset, NPA1998; J.A.Oller & U.-G.Meißner, PLB2001...*

Structure of $\Lambda(1405)$ resonance

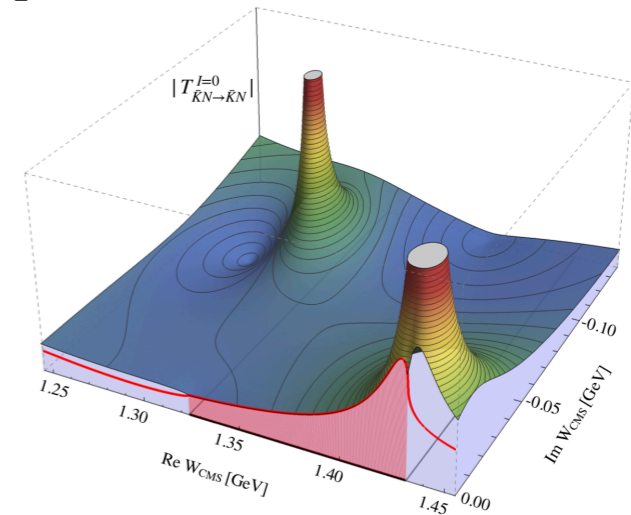
Double-pole predicted by **chiral unitary approach**



Pole positions

PDG(2022) Review 83

approach	pole 1 [MeV]	pole 2 [MeV]
Refs. [14, 15], NLO	$1424_{-23}^{+7} - i 26_{-14}^{+3}$	$1381_{-6}^{+18} - i 81_{-8}^{+19}$
Ref. [17], Fit II	$1421_{-2}^{+3} - i 19_{-5}^{+8}$	$1388_{-9}^{+9} - i 114_{-25}^{+24}$
Ref. [18], solution #2	$1434_{-2}^{+2} - i 10_{-1}^{+2}$	$1330_{-5}^{+4} - i 56_{-11}^{+17}$
Ref. [18], solution #4	$1429_{-7}^{+8} - i 12_{-3}^{+2}$	$1325_{-15}^{+15} - i 90_{-18}^{+12}$



Citation: R.L. Workman et al. (Particle Data Group), Prog.Theor.Exp.Phys. **2022**, 083C01 (2022) and 2023 update

$\Lambda(1405) \ 1/2^-$

$I(J^P) = 0(\frac{1}{2}^-)$ Status: ****

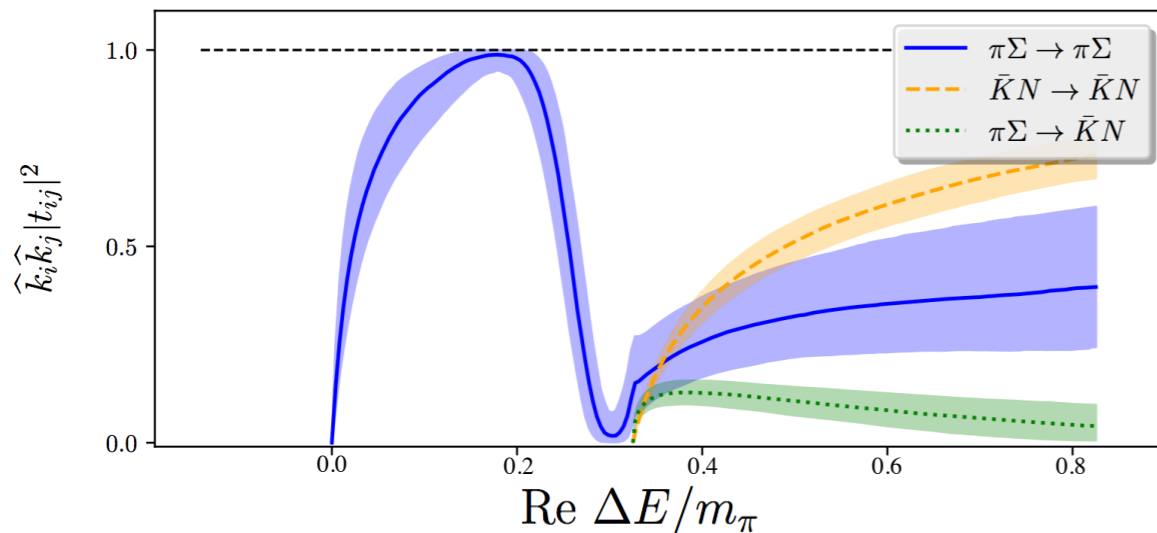
$\Lambda(1380) \ 1/2^-$

$J^P = \frac{1}{2}^-$ Status: **

✓ pole 2: needs further studies to fix its position

Double-pole structure is verified by LQCD

Daniel Mohler's @ Meson 2023



$m_\pi = 200 \text{ MeV}, m_K = 480 \text{ MeV}$

(preliminary) result for the poles is

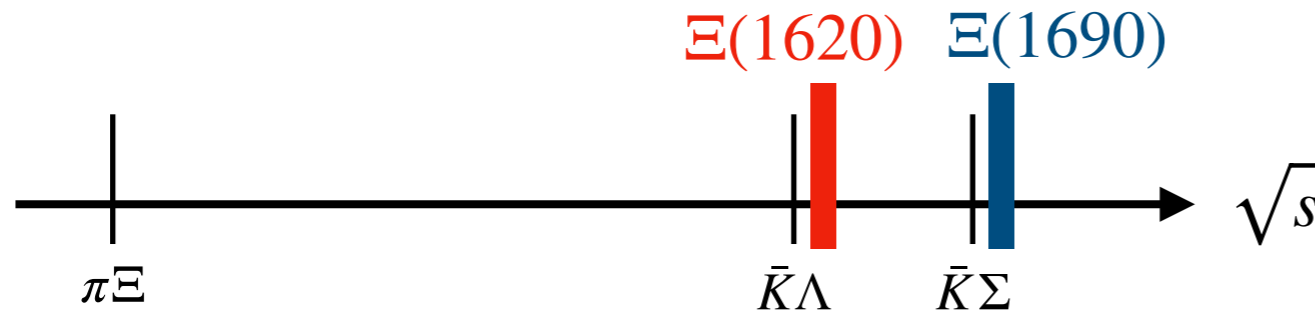
Pole II $1395(9)_{\text{stat}}(2)_{\text{model}}(16)_a \text{ MeV}$

Pole I $1456(14)_{\text{stat}}(2)_{\text{model}}(16)_a \text{ MeV}$

$- i \times 11.7(4.3)_{\text{stat}}(4)_{\text{model}}(0.1)_a \text{ MeV}$

$S=-2$: $\Xi(1620)$, $\Xi(1690)$ resonances

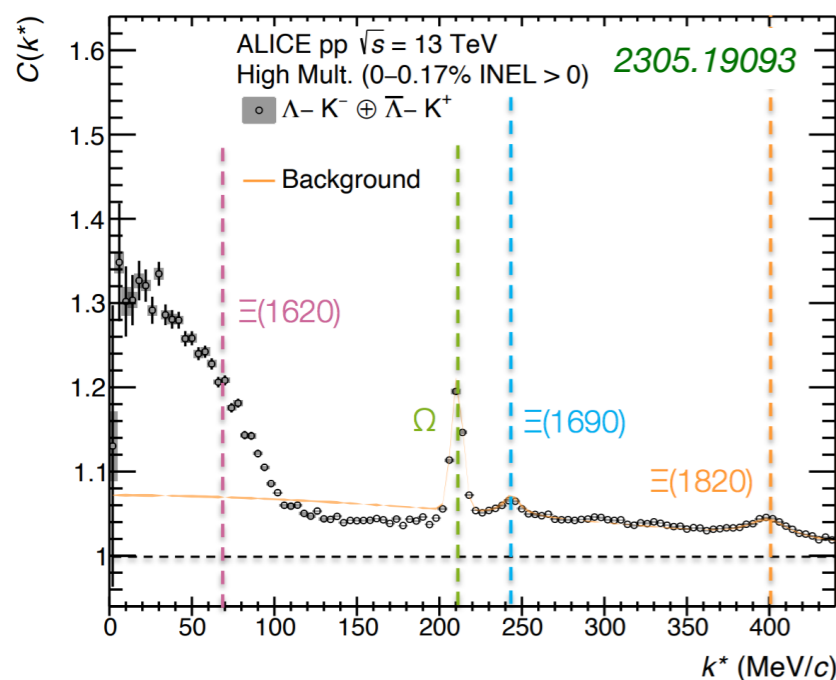
□ Dynamically generated in UChPT



- WT terms: A. Ramos, et al., PRL(2002), M. Lutz, J. Nieves ...
- NLO: A. Feijoo, et al., PLB(2023)

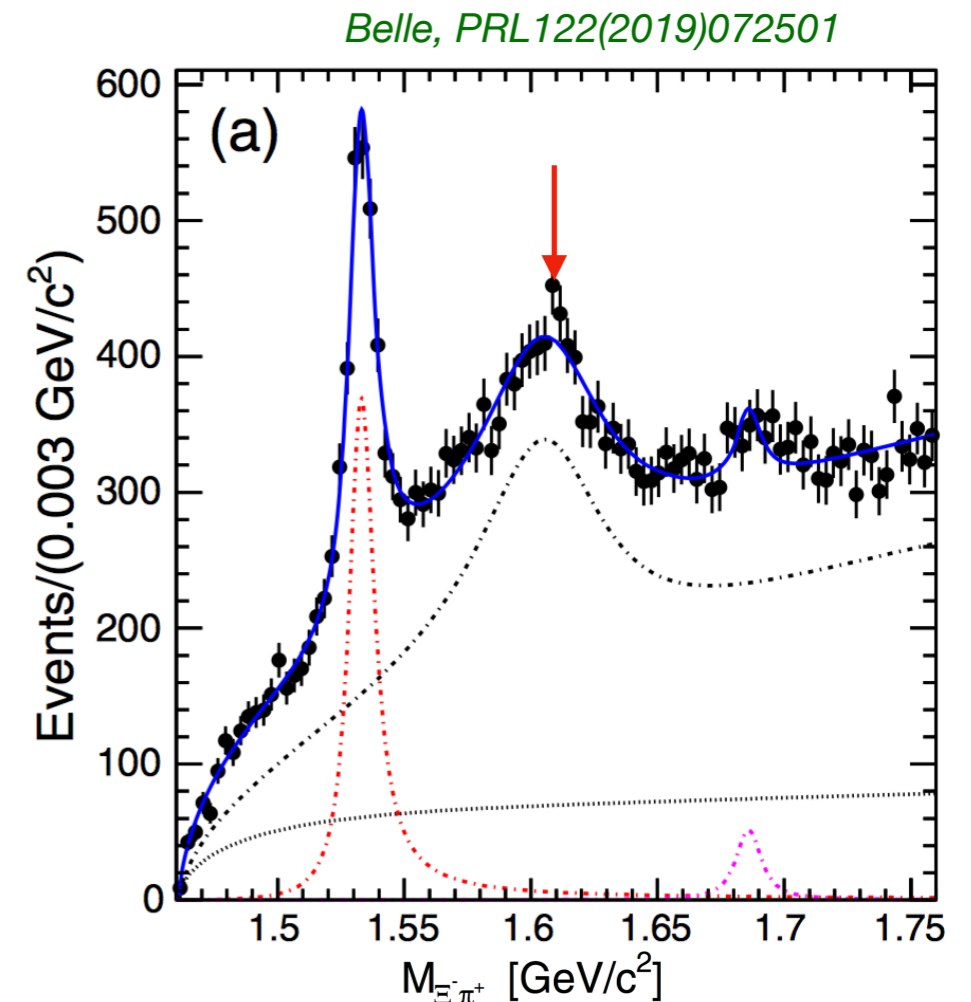
see Angels Ramos's talk @ today

□ Femtoscopy @ ALICE



- **First evidence** of $\Xi(1620)$ in the ΛK decay channel
- Femtoscopic data + **UChPT@NLO**
 - ✓ $\Xi(1620)$: mainly molecular state of $\bar{K}\Sigma$
 - ✓ $\Xi(1690)$: virtual state, mainly coupled to $\bar{K}\Sigma$

see Dimitar Mihaylov's talk @ Monday



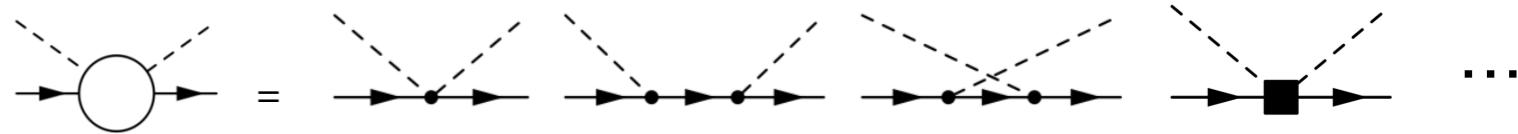
Chiral Unitary approach

□ Chiral symmetry of low-energy QCD + Unitary Relation

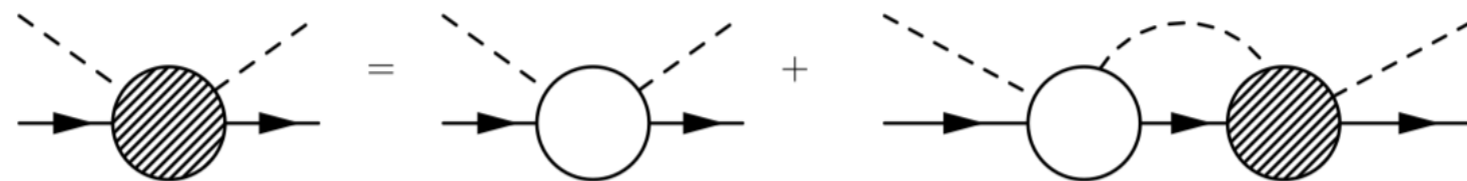
J.A.Oller et al., PPNP45(2000)157-242; T.Hyodo et al., PPNP120 (2021)103868 ...

□ Interaction kernel V : calculate in ChPT order by order

- Leading, next-to-leading order, ...



□ Scattering T -matrix: solve scattering equations



- Lippmann-Schwinger equation or Bethe-Salpeter equation

$$T(p', p) = V(p', p) + i \int \frac{d^4 k}{(2\pi)^4} V(p', k) G(k) T(k, p)$$

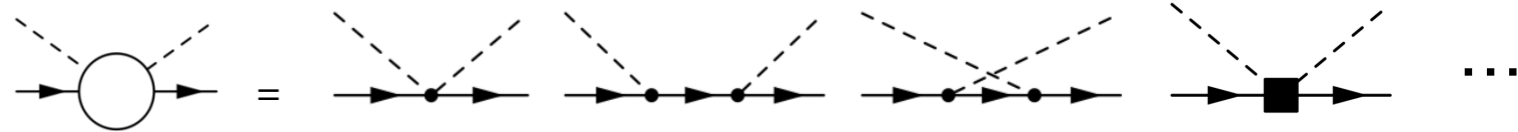
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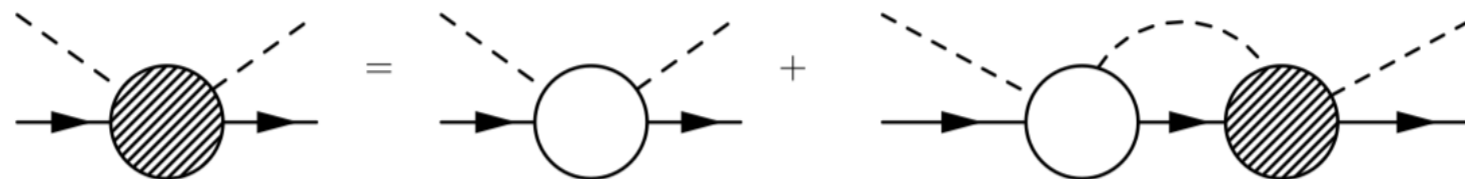
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$$T(p', p) = V(p', p) + i \int \frac{d^4 k}{(2\pi)^4} V(p', k) G(k) T(k, p)$$

- On-shell factorization $\rightarrow V(p', p) + V(p', p) \left(i \int \frac{d^4 k}{(2\pi)^4} G(k) \right) T(p', p)$

Neglecting off-shell effect

\rightarrow cause troubles in the study of three-body interaction?

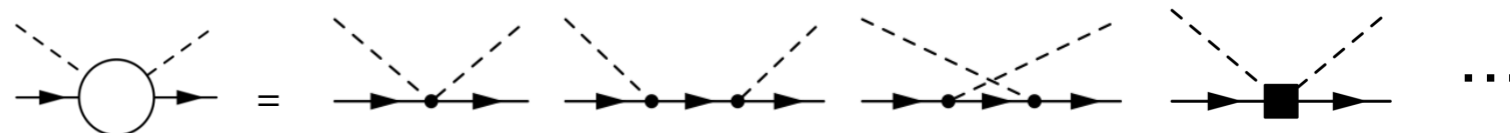
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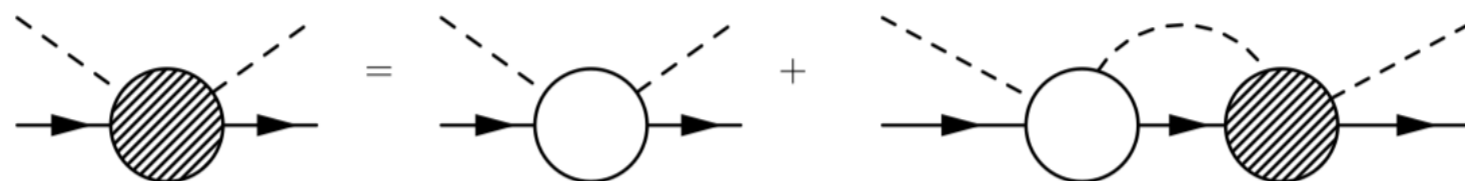
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- Finite cutoff or subtraction constant to renormalize the loop integral

$$G^R(E, \Lambda) \text{ or } G^R(E, \alpha_i)$$

Cutoff/Model dependence

In this work

- Facing the rapid progress of precision experiments, **a model-independent formalism would be needed** ALICE, AMADEUS, J-PARC, STAR...
- We tentatively propose **a renormalized framework** for meson-baryon scattering using **time-ordered perturbation theory** with the covariant chiral Lagrangians
 - Obtain the potential and scattering equation on an equal footing
 - Include the **off-shell effects of potential** and utilize the **subtractive renormalization** to obtain the **renormalizable T-matrix**
 - Apply to the pion-nucleon scattering at LO
 - Extend to $S = -1$ sector and investigate the $\Lambda(1405)$ state

XLR, E. Epelbaum, J. Gegelia and U.-G. Meißner,
Eur. Phys. J. C80 (2020) 406; Eur. Phys. J. C81 (2021) 582; work in progress

Theoretical framework

Time-ordered perturbation theory

□ Definition

S. Weinberg, Phys.Rev.150(1966)1313

G.F. Sterman, "An introduction to quantum field theory", Cambridge (1993)

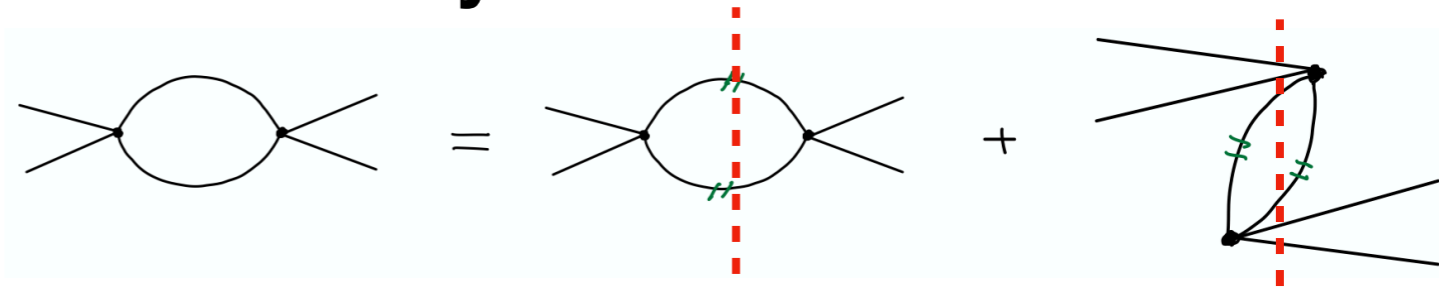
- Re-express the Feynman integral in a form that **makes the connection with on-mass-shell (off-energy shell) state explicit.**

✓ Instead the propagators for internal lines as the energy denominators for intermediate states

- **TOPT or old-fashioned perturbation theory**

□ Advantages

- Explicitly show the unitarity
- Easily to tell the contributions of a particular diagram



□ Obtain the rules for time-ordered diagrams

- Perform Feynman integrations over the zeroth components of the loop momenta
- Decompose Feynman diagram into sums of time-ordered diagrams
- Match to the rules of time-ordered diagrams

Diagrammatic rules in TOPT

XLR, PoS(CD2021)007

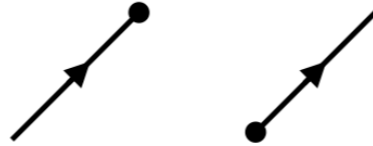
▶ External lines

Spin 0 boson (in, out)



1

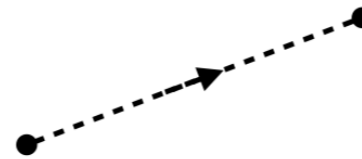
Spin 1/2 fermion (in, out)



$u(\mathbf{p}), \bar{u}(\mathbf{p}')$

▶ Internal lines

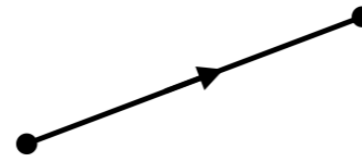
Spin 0 (anti-)boson



$$\frac{1}{2\epsilon_q}$$

$$\epsilon_q \equiv \sqrt{\mathbf{q}^2 + M^2}$$

Spin 1/2 fermion



$$\frac{m}{\omega_p} \sum u(\mathbf{p})\bar{u}(\mathbf{p}) \quad \omega_p \equiv \sqrt{\mathbf{p}^2 + m^2}$$

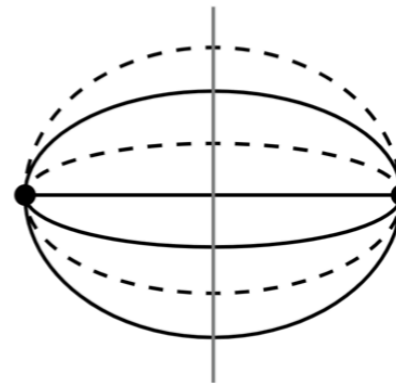
anti-fermion



$$\frac{m}{\omega_p} \sum u(\mathbf{p})\bar{u}(\mathbf{p}) - \gamma_0$$

▶ Intermediate state

A set of lines between two vertices



$$\frac{1}{E - \sum_i \omega_{p_i} - \sum_j \epsilon_{q_j} + i\epsilon}$$

▶ Interaction vertices: the standard Feynman rules

- Take care of zeroth components of integration momenta

✓ particle $p^0 \rightarrow \omega(p, m)$

✓ antiparticle $p^0 \rightarrow -\omega(p, m)$

Meson-baryon scattering in TOPT

Interaction kernel / potential V

- **Define:** sum up the one-meson and one-baryon **irreducible diagrams**
- **Power counting:** Q/Λ_χ systematic ordering of all graphs

Scattering equation

$$\boxed{T} = \boxed{V} + \boxed{V} \boxed{G} \boxed{T}$$

- Coupled-channel integral equation for T-matrix

$$T_{M_j B_j, M_i B_i}(\mathbf{p}', \mathbf{p}; E) = V_{M_j B_j, M_i B_i}(\mathbf{p}', \mathbf{p}; E) + \sum_{MB} \int \frac{d^3 \mathbf{k}}{(2\pi)^3} V_{M_j B_j, MB}(\mathbf{p}', \mathbf{k}; E) G_{MB}(E) T_{MB, M_i B_i}(\mathbf{k}, \mathbf{p}; E)$$

- **Meson-baryon Green function in TOPT**

$$G_{MB}(E) = \frac{m}{2\omega(k, M) \omega(k, m)} \frac{1}{E - \omega(k, M) - \omega(k, m) + i\epsilon}$$

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$$G_{MB}(E) = \frac{m}{2\omega(k, M) \omega(k, m)} \frac{1}{E - \omega(k, M) - \omega(k, m) + i\epsilon}$$

Potential and scattering equation are obtained on an equal footing!

Baryon–baryon scattering in TOPT

□ Baryon-baryon scattering equation

$$\boxed{T} = \boxed{V} + \boxed{V} \boxed{G} \boxed{T}$$

- Potential V : sum up the two-baryon irreducible time-ordered diagrams
- **Two-baryon Green function**

$$G_{ij}^{BB}(E) = \frac{m_i m_j}{\omega(k, m_i) \omega(k, m_j)} \frac{1}{E - \omega(k, m_i) - \omega(k, m_j) + i\epsilon}$$

- ✓ Generalized Kadyshevsky propagator of NN scattering *V. Kadyshevsky, NPB (1968)*
- ✓ SELF-CONSISTENTLY obtained in TOPT
- **Successfully applied to the NN and YN interactions**
 - V. Baru, E. Epelbaum, J. Gegelia, XLR, Phys. Lett. B 798, 134987 (2019)*
 - XLR, E. Epelbaum, J. Gegelia, Phys. Rev. C 101, 034001 (2020)*
 - XLR, E. Epelbaum, J. Gegelia, Phys. Rev. C 106, 034001 (2022) / in preparation*

MB and BB scatterings in TOPT

	Meson-baryon scattering	Baryon-baryon scattering
Potential TOPT diagrams		
Green function	$G^{MB}(E) = \frac{m}{2\omega_M \omega_m} \frac{1}{E - \omega_M - \omega_m + i\epsilon}$	$G_{ij}^{BB}(E) = \frac{m_i m_j}{\omega_{m_i} \omega_{m_j}} \frac{1}{E - \omega_{m_i} - \omega_{m_j} + i\epsilon}$

Unify the description of SU(3) meson-baryon and baryon-baryon scatterings within our TOPT framework

Results and discussion

Leading order potential

□ Chiral effective Lagrangian

$$\mathcal{L}_{\text{LO}} = \frac{F_0^2}{4} \langle u_\mu u^\mu + \chi_+ \rangle + \langle \bar{B} (i\gamma_\mu \partial^\mu - m) B \rangle + \frac{D/F}{2} \langle \bar{B} \gamma_\mu \gamma_5 [u^\mu, B]_\pm \rangle$$

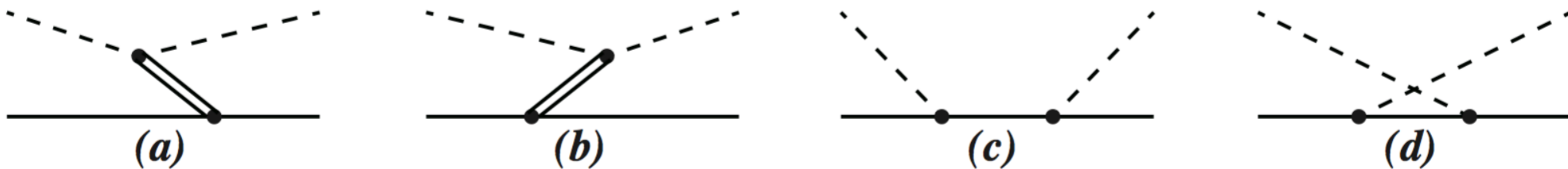
$$- \frac{1}{4} \left\langle V_{\mu\nu} V^{\mu\nu} - 2\dot{M}_V^2 \left(V_\mu - \frac{i}{g} \Gamma_\mu \right) \left(V^\mu - \frac{i}{g} \Gamma^\mu \right) \right\rangle + g \langle \bar{B} \gamma_\mu [V^\mu, B] \rangle$$

- **Vector mesons included as explicit degrees of freedom**

- ✓ One-vector meson exchange potential instead the Weinberg-Tomozawa term

- ✓ **Improve the ultraviolet behaviour without changing the low-energy physics**

□ Time ordered diagrams



- **LO potential in TOPT**

- ✓ Dirac spinor is decomposed as $u_B(p, s) = u_0 + [u(p) - u_0] \equiv (1, 0)^\dagger \chi_s + \text{high order}$

$$V_{M_j B_j, M_i B_i}^{(a+b)} = -\frac{1}{32F_0^2} \sum_{V=K^*, \rho, \omega, \phi} C_{M_j B_j, M_i B_i}^V \frac{\dot{M}_V^2}{\omega_V(q_1 - q_2)} (\omega_{M_i}(q_1) + \omega_{M_j}(q_2))$$

$$\times \left[\frac{1}{E - \omega_{B_i}(p_1) - \omega_V(q_1 - q_2) - \omega_{M_j}(q_2)} + \frac{1}{E - \omega_{B_j}(p_2) - \omega_V(q_1 - q_2) - \omega_{M_i}(q_1)} \right]$$

$$V_{M_j B_j, M_i B_i}^{(c)} = \frac{1}{4F_0^2} \sum_{B=N, \Lambda, \Sigma, \Xi} C_{M_j B_j, M_i B_i}^B \frac{m_B}{\omega_B(P)} \frac{(\boldsymbol{\sigma} \cdot \mathbf{q}_2)(\boldsymbol{\sigma} \cdot \mathbf{q}_1)}{E - \omega_B(P)}$$

$$V_{M_j B_j, M_i B_i}^{(d)} = \frac{1}{4F_0^2} \sum_{B=N, \Lambda, \Sigma, \Xi} \tilde{C}_{M_j B_j, M_i B_i}^B \frac{m_B}{\omega_B(K)} \frac{(\boldsymbol{\sigma} \cdot \mathbf{q}_1)(\boldsymbol{\sigma} \cdot \mathbf{q}_2)}{E - \omega_{M_i}(q_1) - \omega_{M_j}(q_2) - \omega_B(K)}$$

Ultraviolet Behavior

□ One-loop integral $V G V$

$$I_{VGV} = \int \frac{d^3k}{(2\pi)^3} V(p', k) G(k) V(k, p) \begin{cases} V = V_{\text{VME}}, & I_{VGV} \xrightarrow{k \rightarrow \infty} \int d^3k \frac{1}{k} \frac{1}{k^3} \frac{1}{k} \\ V = V_{\text{WT}}, & I_{VGV} \xrightarrow{k \rightarrow \infty} \int d^3k k \frac{1}{k^3} k \end{cases}$$

- Scattering amplitude from the VME potential is **cutoff independent!**

$$T_{\text{VME}} = V_{\text{VME}} + V_{\text{VME}} G T_{\text{VME}}$$

Renormalizable

Ultraviolet Behavior

□ One-loop integral $V G V$

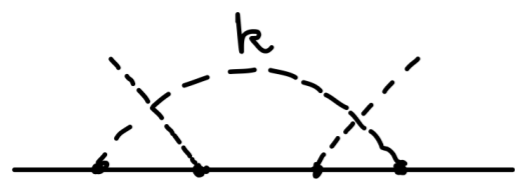
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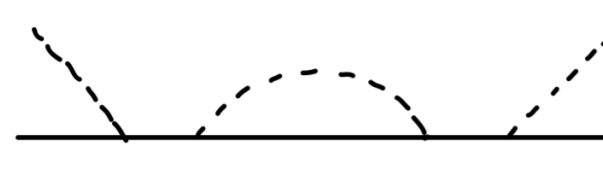
Renormalizable

□ Iteration of the crossed-Born term is also renormalizable



$$\rightarrow \int d^3k \frac{\boldsymbol{\sigma} \cdot \mathbf{p}' \boldsymbol{\sigma} \cdot \hat{\mathbf{k}}}{k} \frac{1}{k^3} \frac{\boldsymbol{\sigma} \cdot \mathbf{p} \boldsymbol{\sigma} \cdot \hat{\mathbf{k}}}{k}$$

□ Only divergence is from the iteration of the Born term



$$\rightarrow \int d^3k \boldsymbol{\sigma} \cdot \mathbf{p}' \boldsymbol{\sigma} \cdot \hat{\mathbf{k}} k \frac{1}{k^3} k \boldsymbol{\sigma} \cdot \mathbf{p} \boldsymbol{\sigma} \cdot \hat{\mathbf{k}}$$

Quadratical divergence

Subtractive renormalization

- LO potential: one-baryon irreducible and reducible parts

$$V_{\text{LO}} = V_I \left(\text{---} \diagup \text{---} \quad \text{---} \diagdown \text{---} \quad \text{---} \cdot \text{---} \right) + V_R \left(\text{---} \cdot \text{---} \right)$$

- LO T-matrix

$$T_{\text{LO}} = V_{\text{LO}} + V_{\text{LO}} G T_{\text{LO}} \quad \Rightarrow \quad \begin{cases} T_{\text{LO}} = T_I + (1 + T_I G) T_R (1 + G T_I) \\ T_I = V_I + V_I G T_I \\ T_R = V_R + V_R G (1 + T_I G) T_R \end{cases}$$

- Irreducible part: $T_I \xrightarrow{\Lambda \sim \infty} \text{Finite}$
- Reducible part: $T_R \xrightarrow{\Lambda \sim \infty} \text{Divergent}$

✓ Potential can be rewritten as separable form

$$V_R(p', p; E) = \xi^T(p') C(E) \xi(p) \quad C(E): \text{constant} \quad \xi^T(q) := (1, q)$$

✓ T_R can be rewritten as $T_R(p', p; E) = \xi^T(p') \chi(E) \xi(p) \quad \chi(E) = [C^{-1} - \xi G \xi^T - \xi G T_I^S G \xi^T]^{-1}$

D.B.Kaplan, et al., NPB478,629(1996); E. Epelbaum, et al., EPJA51,71(2015)

✓ Using **subtractive renormalization**, replacing Green function $G^{Rn} = G(E) - G(m_B)$

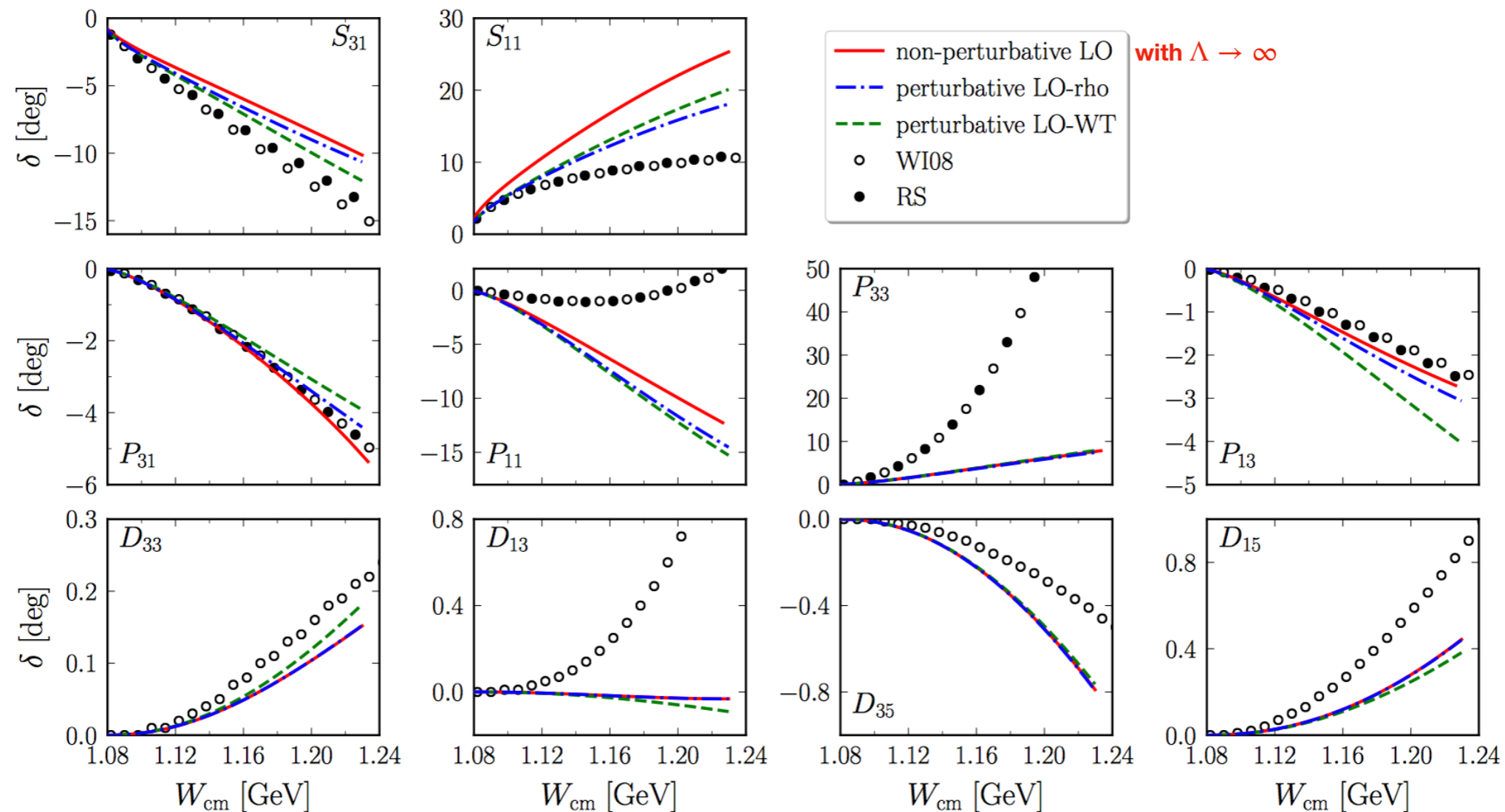
E. Epelbaum, et al., EPJA56(2020)152

Renormalized LO T-matrix

$$T_{\text{LO}}^{Rn} = T_I + \left(\xi^T + T_I G^{Rn} \xi^T \right) \chi^{Rn}(E) \left(\xi + \xi G^{Rn} T_I \right)$$

Pion–Nucleon scattering

□ Description phase shifts of pion-nucleon scattering



- Rho-meson-exchange contribution is similar as WT term.
 - Phase shifts from non-perturbative renormalized amplitude are only slightly different from the ones of the perturbative approach.
- ✓ Our non-perturbative treatment is valid, since ChPT has good convergence in SU(2) sector

XLR, E. Epelbaum, J. Gegelia and U.-G. Meißner, Eur. Phys. J. C80 (2020) 406

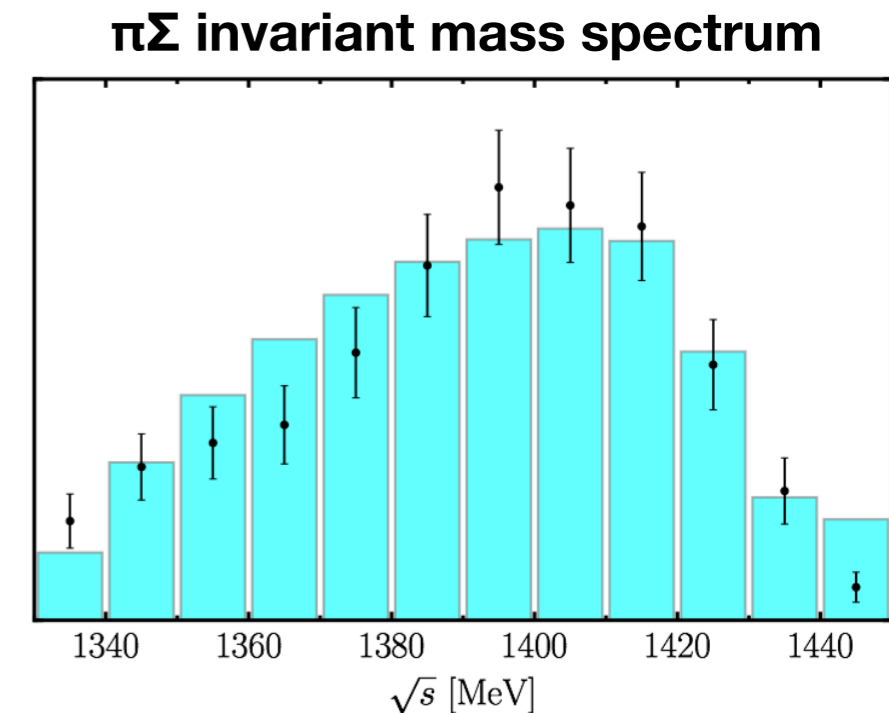
S = -1 meson-baryon scattering

- Four coupled channels $\bar{K}N, \pi\Sigma, \eta\Lambda, K\Xi$
 - Solve the scattering equation in isospin basis by taking into account **the off-shell effects of potential**
 - **Use subtractive reormalization and take $\Lambda \rightarrow \infty$** to obtain the renormalized T-matrix

No free parameters needed to be fitted!

- Two pole positions of $\Lambda(1405)$

		lower pole	higher pole
This work	$F_0 = F_\pi$	$1337.7 - i79.1$	$1430.9 - i8.0$
(LO)	$F_0 = 103.4$	$1348.2 - i120.2$	$1436.3 - i0.7$
NLO	<i>Y. Ikeda, NPA(2012)</i>	$1381_{-6}^{+18} - i81_{-8}^{+19}$	$1424_{-23}^{+7} - i26_{-14}^{+3}$
	<i>Z.-H. Guo, PRC(2013)-Fit II</i>	$1388_{-9}^{+9} - i114_{-25}^{+24}$	$1421_{-2}^{+3} - i19_{-5}^{+8}$
	<i>M. Mai, EPJA(2015)-sol-2</i>	$1330_{-5}^{+4} - i56_{-11}^{+17}$	$1434_{-2}^{+2} - i10_{-1}^{+2}$
	<i>M. Mai, EPJA(2015)-sol-4</i>	$1325_{-15}^{+15} - i90_{-18}^{+12}$	$1429_{-7}^{+8} - i12_{-3}^{+2}$



- **Consistent with M. Mai EPJA(2015), in particular for the lower pole**

Coupling strengths for $\Lambda(1405)$

- On-shell scattering T-matrix can be approximated by

$$T_{ij} \simeq 4\pi \frac{g_i g_j}{z - z_R}$$

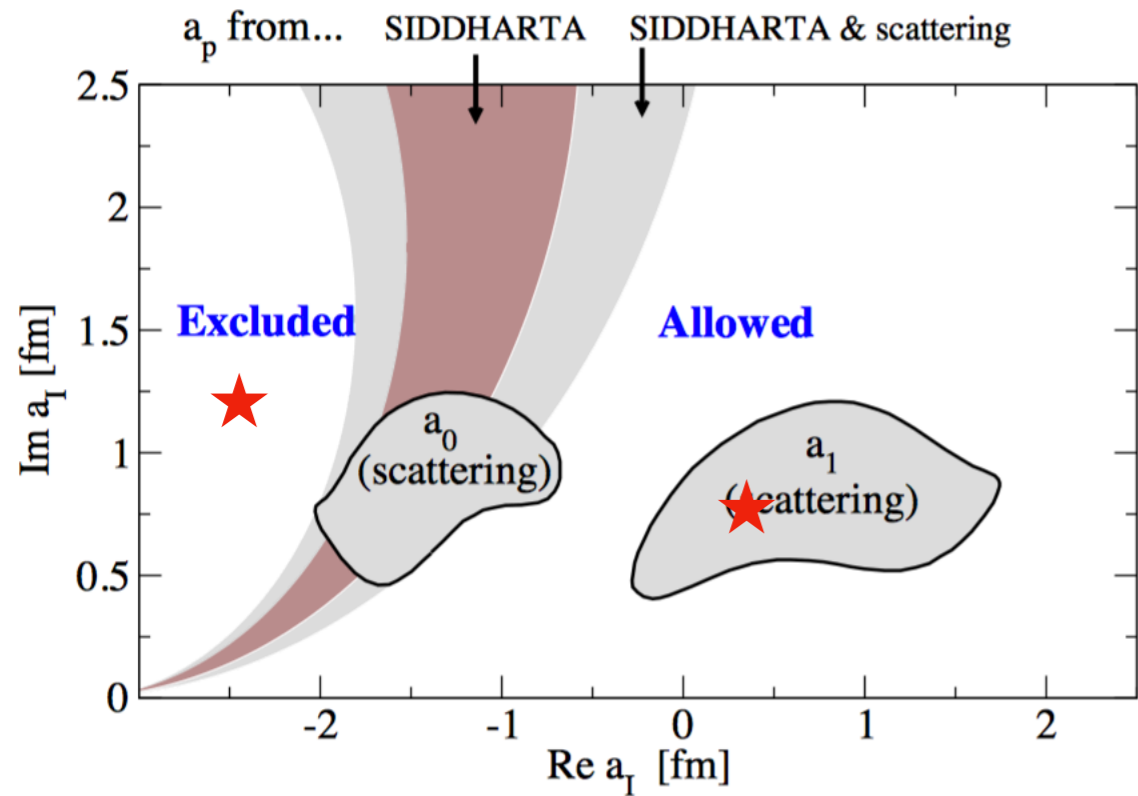
- g_i (g_j): coupling strength of the initial (final) transition channel

	Lower pole		Higher pole	
	g_i	$ g_i $	g_i	$ g_i $
$\pi\Sigma$	$1.83 + i1.90$	2.64	$-0.38 + i0.84$	0.92
$\bar{K}N$	$-1.59 - i1.47$	2.17	$2.16 - i0.83$	2.31
$\eta\Lambda$	$-0.19 - i0.67$	0.69	$1.59 - i0.36$	1.63
$K\Xi$	$0.72 + i0.81$	1.08	$-0.10 + i0.34$	0.35

- Two poles of $\Lambda(1405)$ have different coupling nature
 - ✓ Lower pole couples predominantly to the $\pi\Sigma$ channel
 - ✓ Higher pole couples strongly to the $\bar{K}N$ channel

$\bar{K}N$ scattering observables

- Scattering length: constrained by scattering + SIDDHARTA kaonic deuterium data



M. Döring and U.-G. Meißner, Phys. Lett. B 704, 663 (2011)

Our LO prediction (isospin basis)

- Isospin $I=0$

$$a_0 = -2.50 + i 1.37 \text{ fm}$$

outside the allowed region

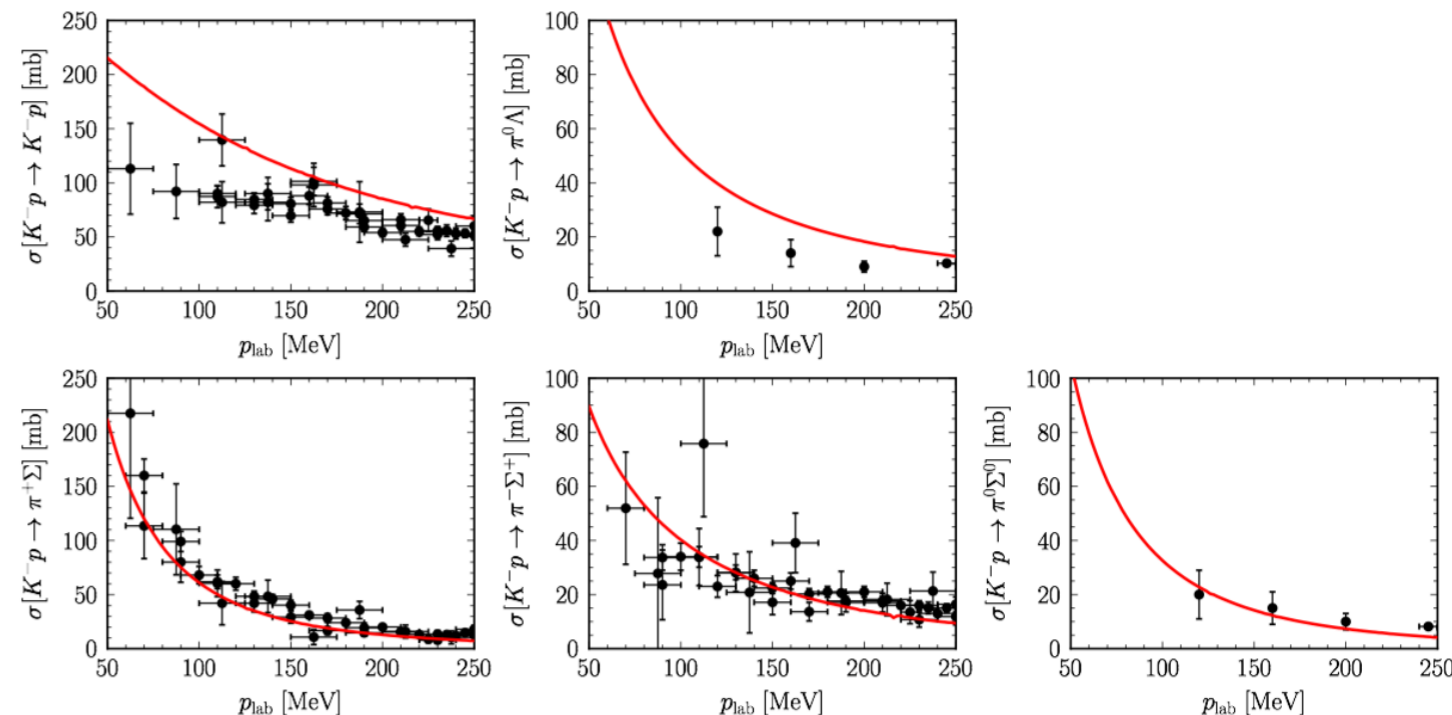
- Isospin $I=1$

$$a_1 = 0.33 + i 0.72 \text{ fm}$$

within the allowed region

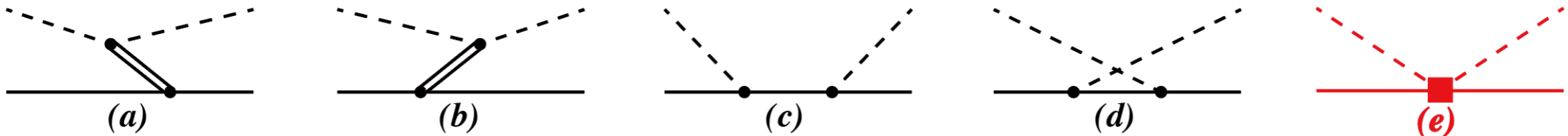
- Total cross section of K^-p

- Our LO prediction covers well $K^-p \rightarrow \pi^{\pm,0}\Sigma^{\pm,0}$ cross section
- slightly larger than the data of $K^-p \rightarrow K^-p, \pi^0\Lambda$



Higher order studies

- Maintain the scattering T-matrix renormalizable
 - Take LO potential non-perturbatively, use the subtractive renormalization
 - **Beyond LO correction is perturbatively included**
- Such as the NLO calculation



$$V = V_{\text{LO}} + V_{\text{NLO}} \longrightarrow T = T_{\text{LO}} + T_{\text{NLO}}$$

$$T_{\text{LO}} = T_I + (\xi^T + T_I G^{Rn} \xi^T) \chi^{Rn}(E) (\xi + \xi G^{Rn} T_I)$$

$$T_{\text{NLO}} = (1 + GT_{\text{LO}}) V_{\text{NLO}} (1 + GT_{\text{LO}})$$

- T-matrix in the particle basis

- **S=-1 sector, 10 coupled channels:** $K^-p, \bar{K}^0n, \pi^0\Lambda, \pi^0\Sigma^0, \pi^+\Sigma^-, \pi^-\Sigma^+, \eta\Lambda, \eta\Sigma^0, K^+\Xi^-, K^0\Xi^0$
- Fit: cross section, decay ratios, energy shift and width of kaonic hydrogen from SIDDHARTA + **Femtoscopic data**

Summary

- **A renormalized framework** for MB scattering is proposed
 - Time-ordered perturbation theory + Covariant chiral Lagrangians
 - **Take into account the off-shell effects of potential**
 - **Use subtractive renormalization**
 - ✓ **achieve T-matrix is cutoff-independent**
 - Apply to πN scattering and extend to the $S=-1$ sector at LO
 - Obtain the two-pole structure of $\Lambda(1405)$

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- We are working on the $S = -2$ sector at LO
 - Very preliminary result:
 - $\Xi(1620)$ is not found at second Riemann sheet, while $\Xi(1690)$ is survive
- Next-leading order study is planed

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Thank you for your attention!

Back up