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purpose:

understand the Equation of state (EOS) = p(e) of neutron stars (NS)

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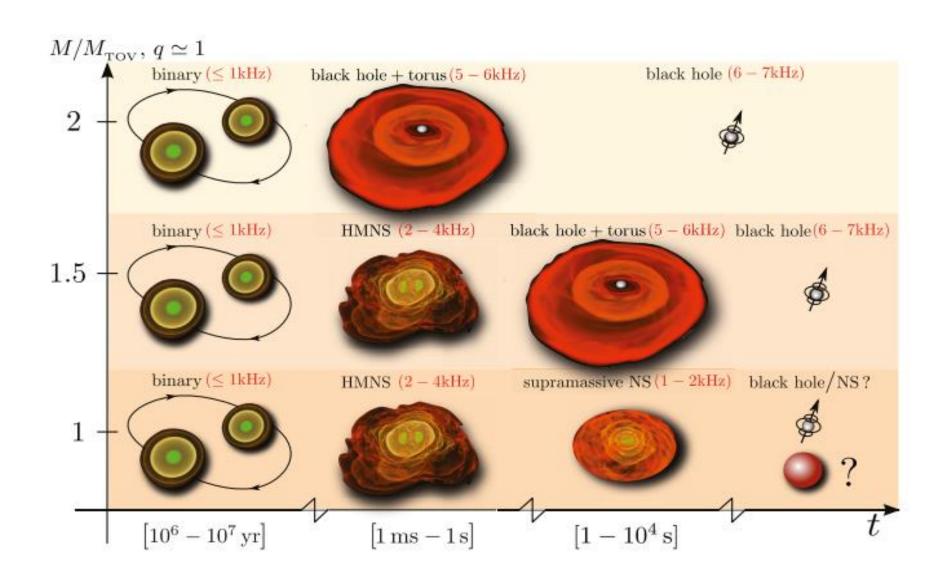
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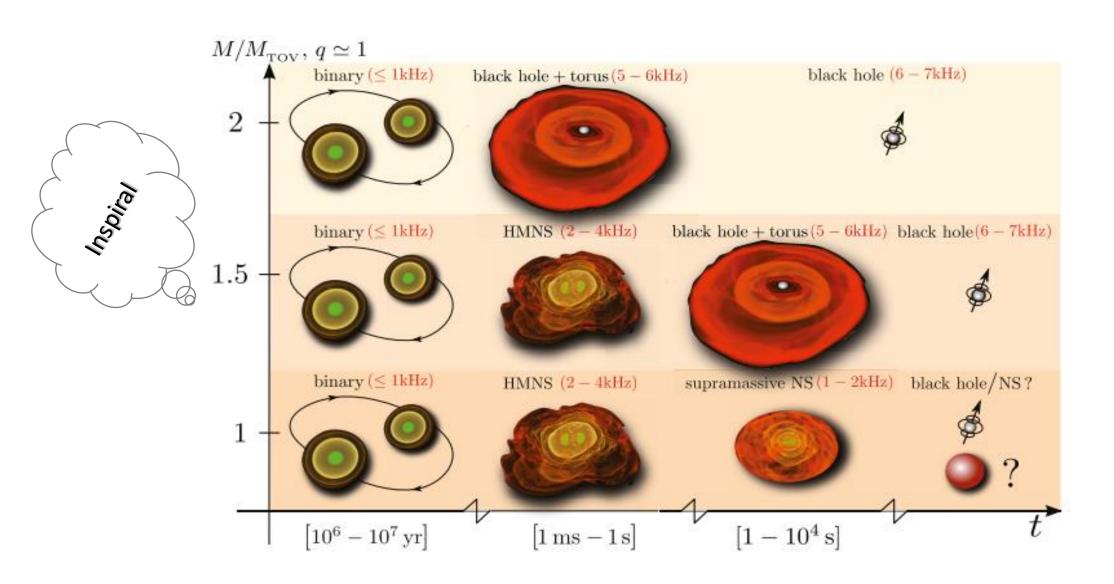
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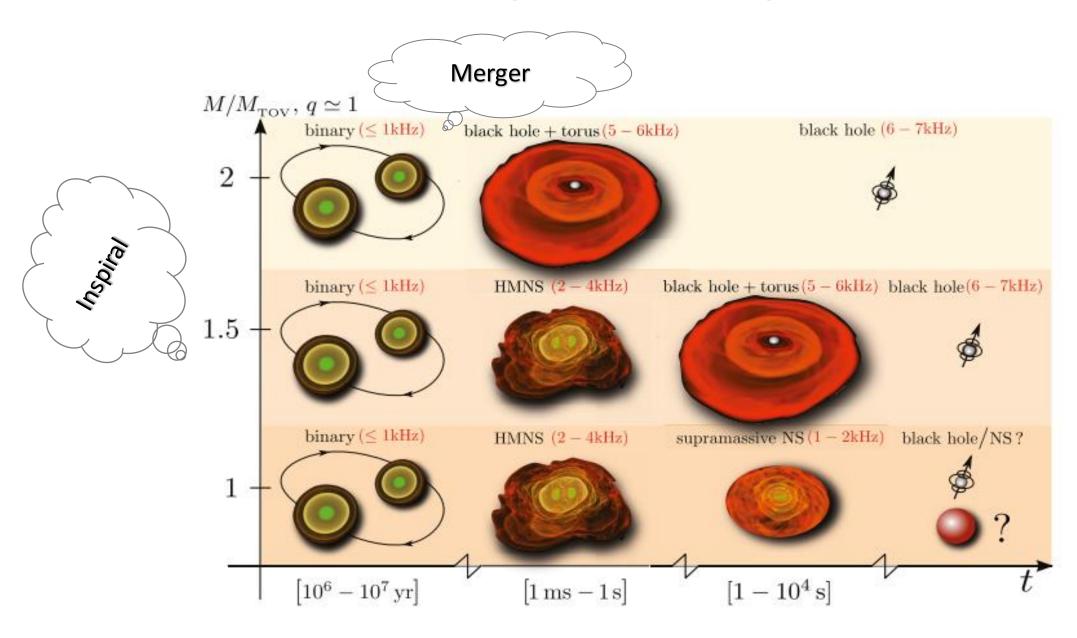
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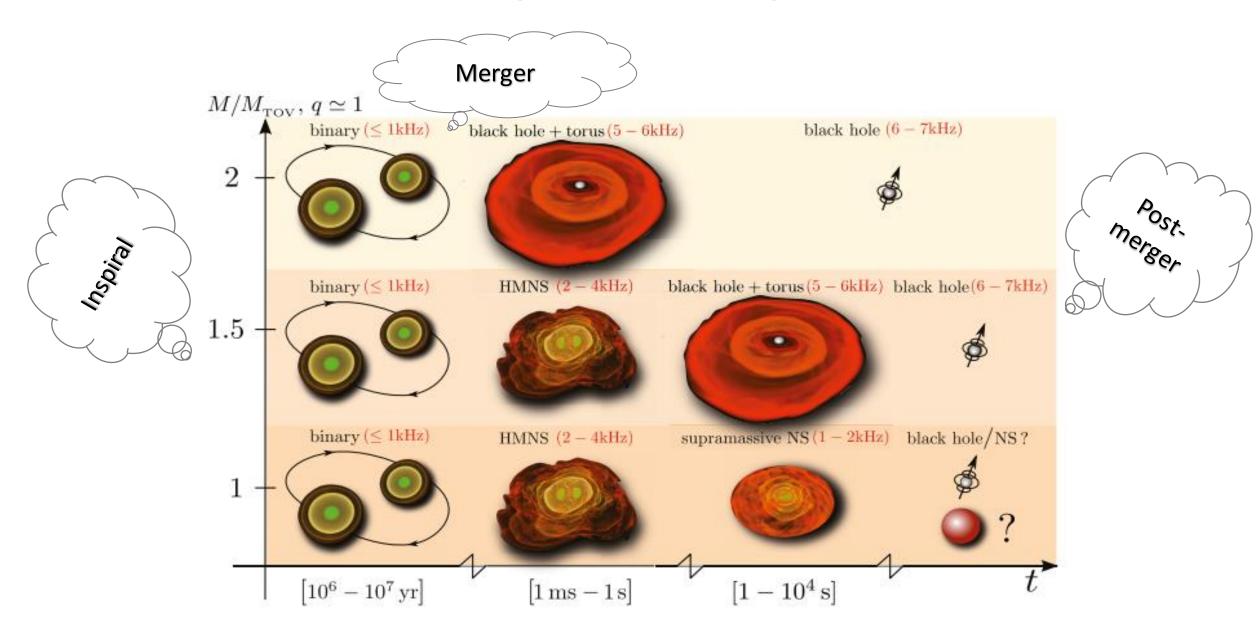


Binary NSs merger

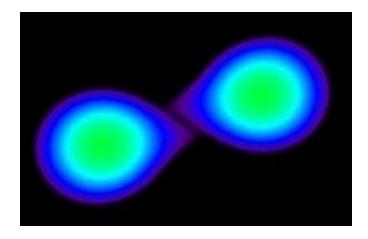






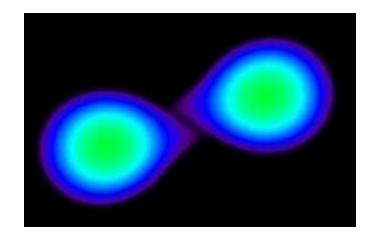


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- Tidal deformation: equatorial plane



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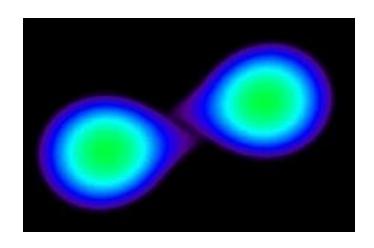




Shock at NSs interface and radial oscillations

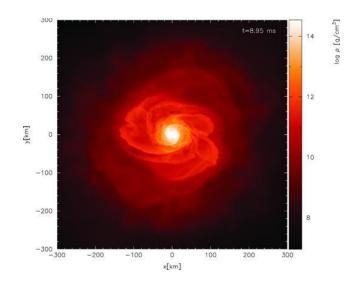
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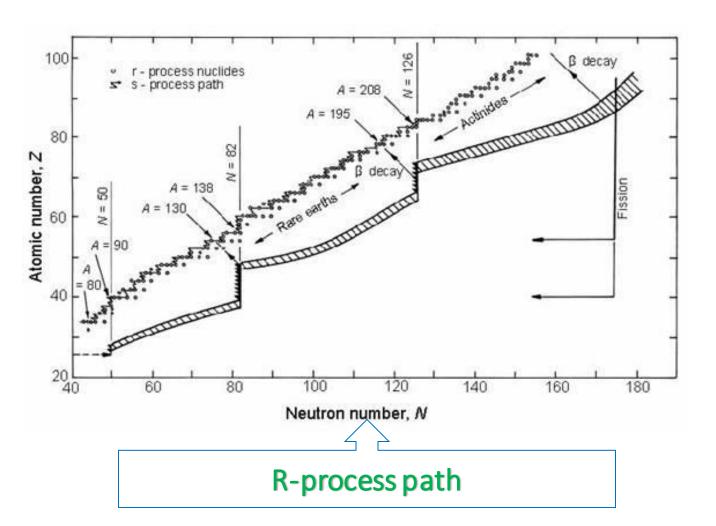


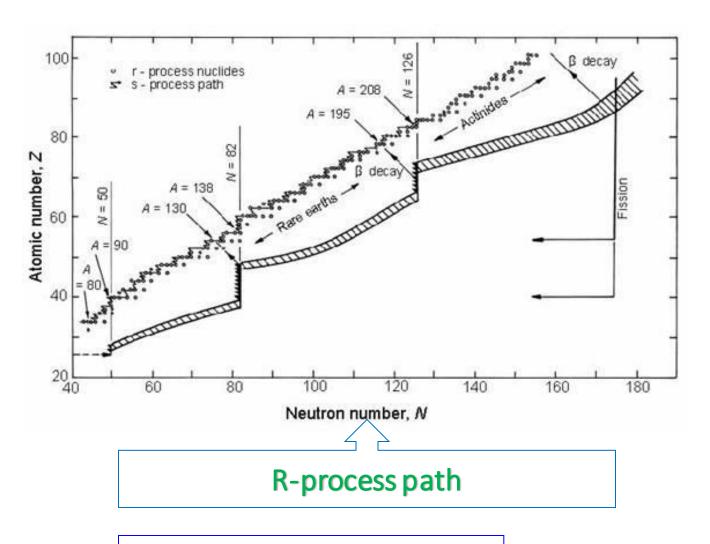


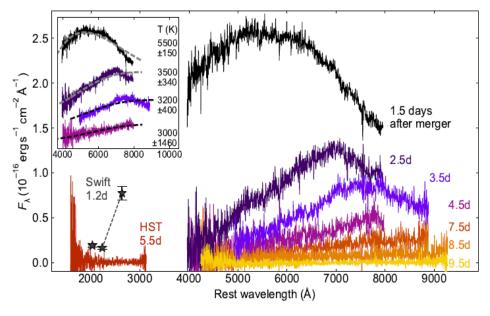
Shock at NSs interface and radial oscillations

- \triangleright Disk: $10^{-3} M_{\odot} < M_{disk} < 0.03 M_{\odot}$
- Viscous or neutrino heating









Nicholl et al. [arXiv:astro-ph.HE/1710.05456]

$$t_{peak} \propto \left(\frac{kM_{ej}}{v}\right)^{1/2} \qquad L_{peak} \propto \left(\frac{vM_{ej}}{k}\right)^{1/2}$$

kilonova signal

$$T_{peak} \propto \left(vM_{ej}\right)^{-1/8} k^{-3/8}$$

Merger of compact objects August 2017

Limit on $\widecheck{\Lambda}$ from the inspiral phase

$$2 < M_{max} < 2.2 M_{\odot}$$
 , $R_{1.5} < 13.5 \ km$

Limit on ejecta from the Kilonova signal

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* $11.5 < R_{1.5} < 13~km$: hyperons and delta from $1.5 M_{\odot}$, hybrid stars

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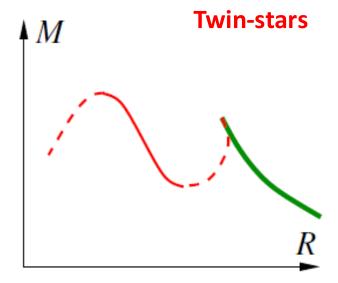
Radii measurements from x-ray binaries ≈ 11 km

• $R_{1.5} < 11.5 \ km$: only disconnected solutions of the TOV

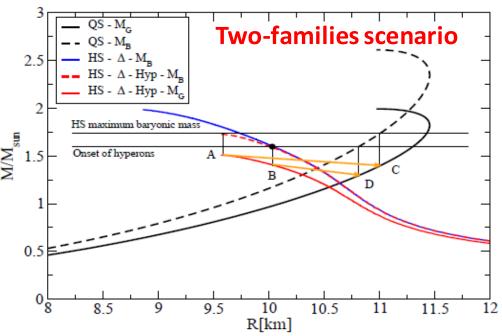


Two different configurations

- 1. Hadronic Matter
- 2. Partially or totally deconfined quark matter

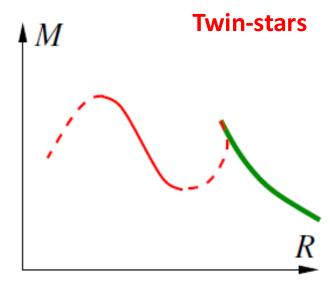


- 1 order phase transition
- The quark stars have the **smallest** radii



A. Drago, A. Lavagno, and G. Pagliara, Phys. Rev. D89,043014 (2014), 1309.7263

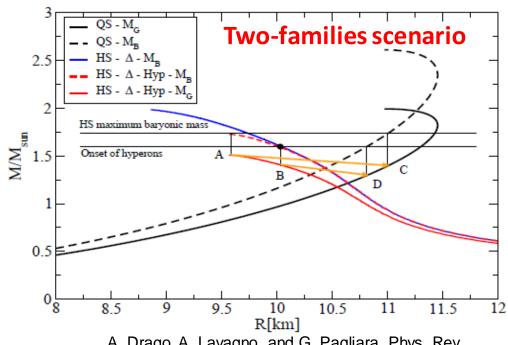
- Witten hyphotesis
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Strange quark matter

- > u, d, s quarks, gluons and electrons
- ➤ Witten: absolutely stable ———— energy per baryon < 930 MeV
- > it can exist in lumps from few fm to 10 km (quark star)



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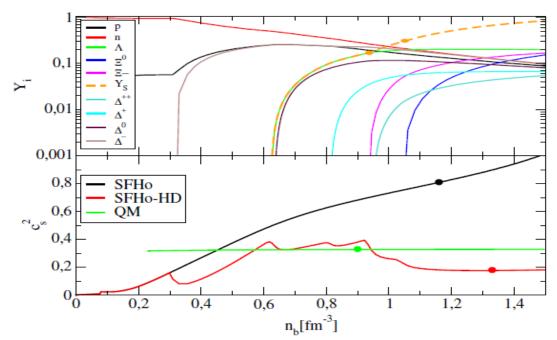
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Two-families scenario...

Appearance of hyperons and Δ -resonances Softening of the EOS

1. Hadronic stars: $M_{max} \sim 1.5 M_{\odot}$, $R \sim 10 km$

2. Quark stars: $M_{max} \sim 2 M_{\odot}$, R > 11 km



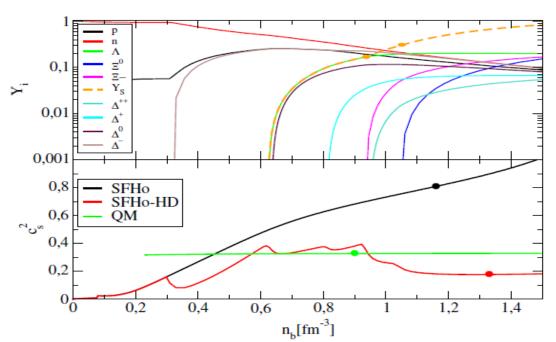
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$$Y_S = \frac{n_{\Lambda} + 2(n_{\Xi^0} + n_{\Xi^-})}{n_b}$$

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R. De Pietri, A. Drago, A. Feo, G. Pagliara, M. Pasquali, S. Traversi, and G. Wiktorowicz, "Merger of compact stars in the two-families scenario," 2019

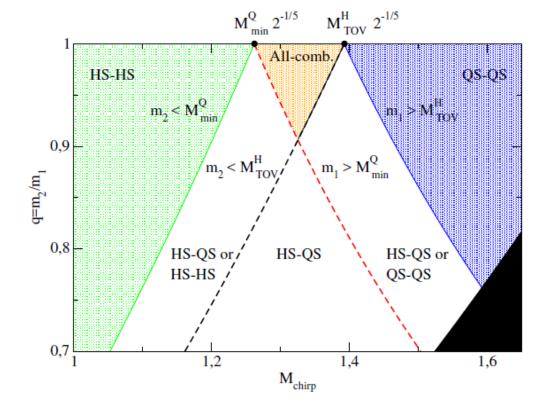
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$$d_S \leq n_0^{-1/3}$$

$$Y_s \approx 0.2 - 0.3$$

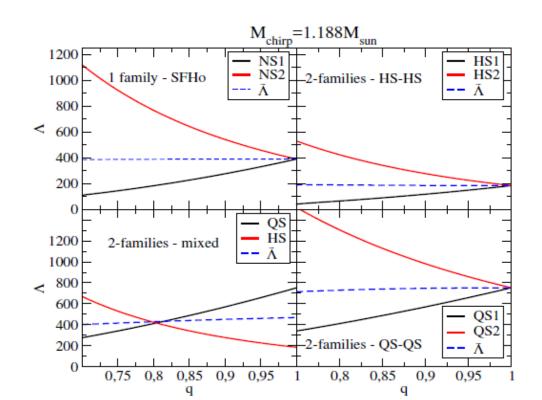
Classification of the mergers

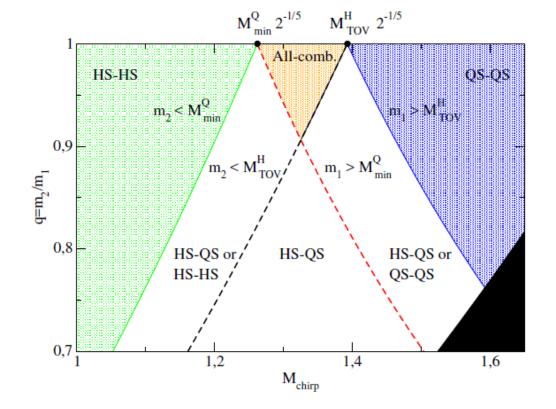
- 1. Hadronic-Hadronic (HS-HS)
- 2. Hadronic-Quark (HS-QS)
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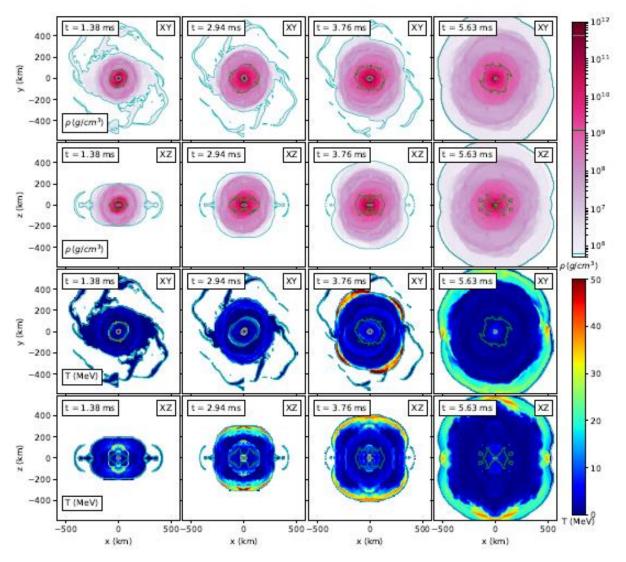


GW170817

HS-QS compatible with the limits on $\check{\Lambda}$

Kilonova?

- the radii of the two compact objects are both rather small, the system is asymmetric and the threshold mass is large
- Issue: fate of quark matter
 Strangelets evaporation?



Astrophys. J. 881, 122 (2019)

Previous studies: strangelets evaporation in cosmological context

C. Alcock and E. Farhi, Phys. Rev. D32, 1273 (1985)

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Lumps of strange matter with baryon number A:

- 3A quarks in quark-matter phase
- radius $\approx A^{1/3}$
- mass = eA where e $\approx 860 880 \text{ MeV}$ ionization energy $\approx 50 70 \text{ MeV}$

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The universe cools down from 100 to 1 MeV in 1s: is that time enough to evaporate the lumps?

$$\frac{dA}{dt} = \left[\frac{m_n T_s^2}{2\pi^2} e^{-I/T_s} - N_n \left(\frac{T_s}{2\pi m_n} \right)^{1/2} \right] (f_n + f_p) \sigma_0 A^{2/3}$$

- m_n : mass of the neutron
- *I* : ionization energy
- T_s : temperature of the strangelets
- N_n : density of the environment
- $\sigma_0 A^{2/3}$: geometric cross section
- $f_{n,p}$: absorpion efficiencies

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Fragmentation of strangelets to infer the typical size

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Fragmentation

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$$l_k = \left(\frac{\mu^3}{\rho^3 \epsilon}\right)^{1/4}$$

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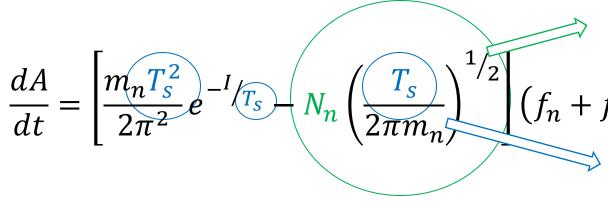
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❖ Shock waves ☐ larger energies and smaller length scales
⇒ small strangelets



re-absorption of neutrons from the environment

cooling of the strangelet due to evaporation

$$\frac{dA}{dt} = \left[\frac{m_n T_s^2}{2\pi^2}e^{-I/T_s} - N_n \left(\frac{T_s}{2\pi m_n}\right)^{1/2}\right] (f_n + f_p)\sigma_0 A^{2/3}$$
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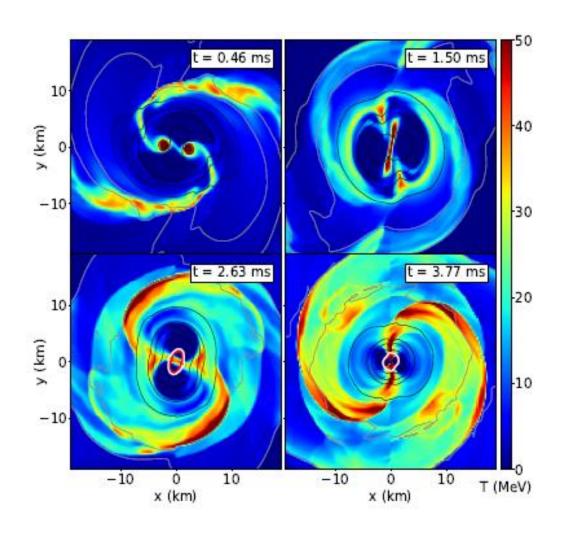
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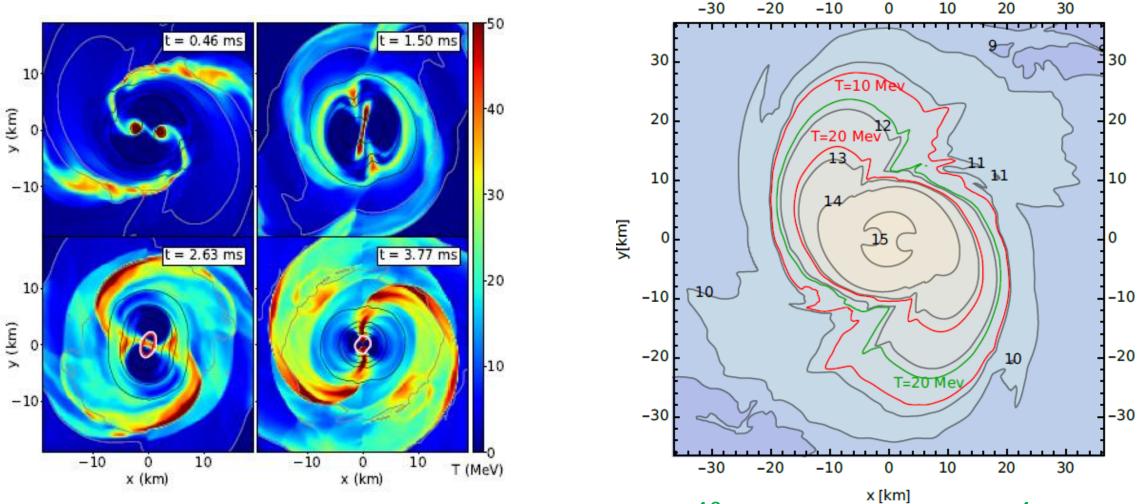


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$$4\pi r_s^2 \left[\frac{7\pi^2}{160} \right] \left[T_u^4 p(r_s, T_u) - T_s^4 p(r_s, T_s) \right] = \frac{dA}{dt} (I + 2T_s)$$

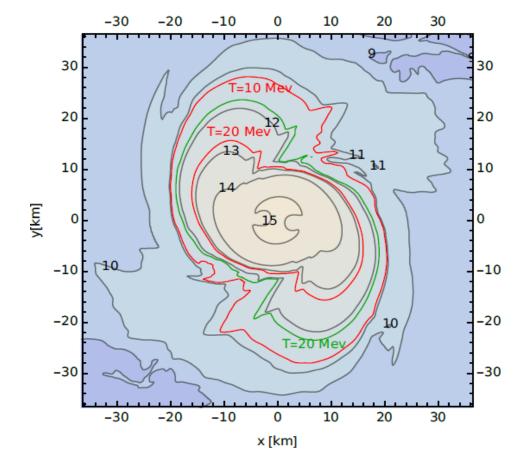
$$\nu \text{ absorption} \qquad \nu \text{ emission} \qquad \text{evaporation}$$
Energy gained Energy loss



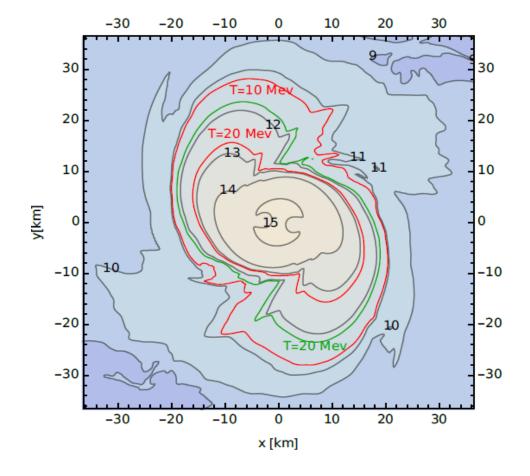


Outside the contours all the strangelets with $A \leq 10^{40}$ evaporate in few $10^{-4}s$

green contour: $T_u = 20 \ MeV$, re-heating source = neutrinos $T_s < T_u$, $\rho \sim 6 \cdot 10^{11} \ g/_{cm^3}$

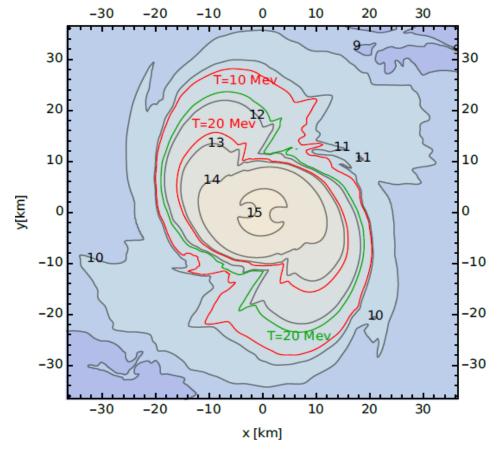


red contours: $T_u = T_s = 10,20 \ MeV$, more efficient re-heating source $T_s = T_u$, $\rho \sim 1.6 \cdot 10^{11} \ g/_{cm^3}$, $\rho \sim 5.9 \cdot 10^{12} \ g/_{cm^3}$



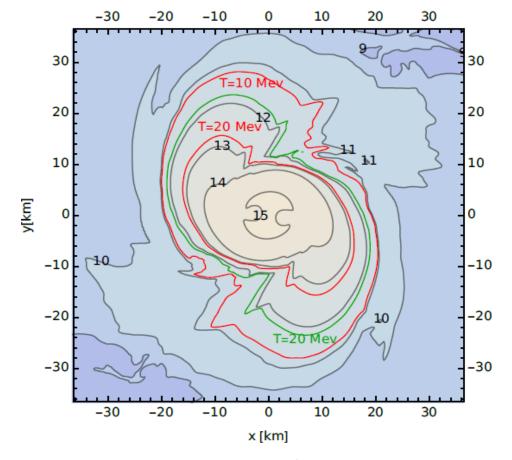
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distances $\sim 20,30 \ km$ from the center of the merger



Evaporation raises the strangeness fraction on the surface

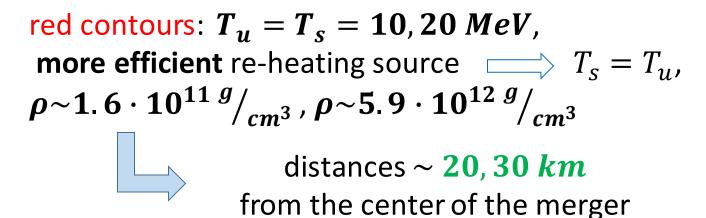
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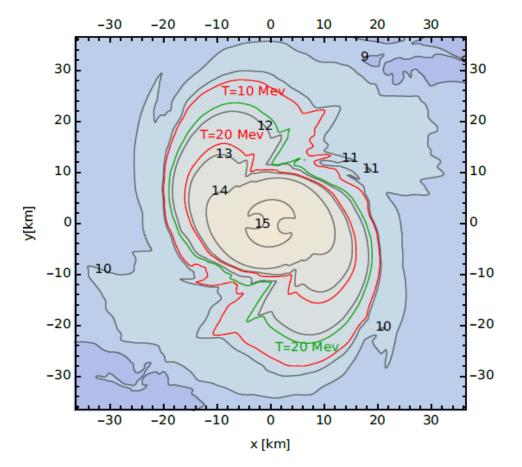


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Weak reactions need time to reequilibrate $\frac{dA}{dt} < kG_F^2 \mu_q^5 \sin \theta_c^2 A$





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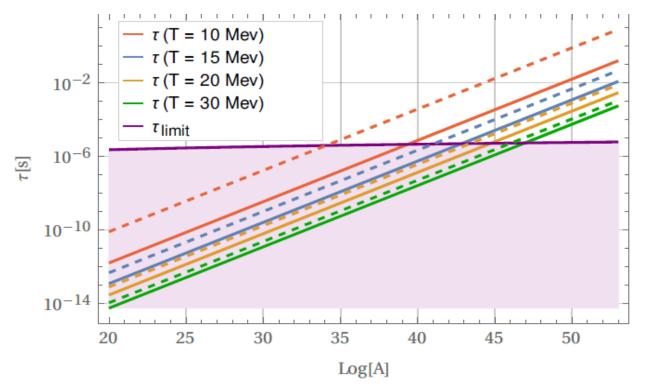


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Negligible lower limit on the timescale $\tau > 10^{-6} - 10^{-5} s$

> cold

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- > neutrinos are the only source of re-heating
- > low density region

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The density is dominated by **evaporated neutrons**

$$N_n(T_S) = \frac{11\pi^2(T_u^4 - T_S^4)}{360T_S}$$

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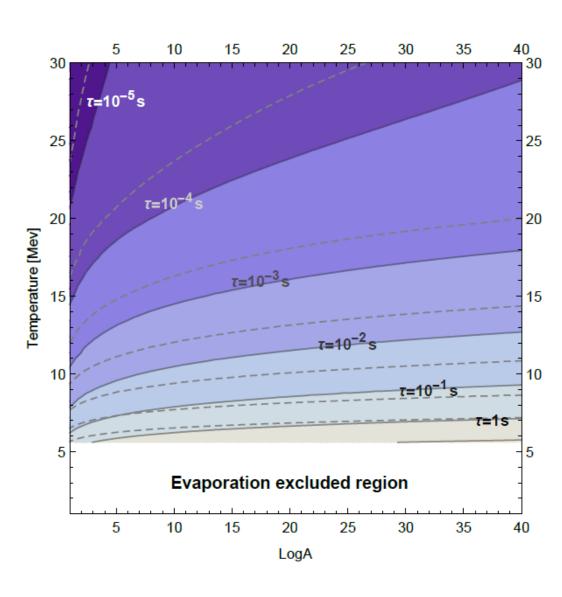


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- To evaporate $A \sim 10^{30}$ in few $10^{-3}s$ we need $T \sim 13 \; MeV$



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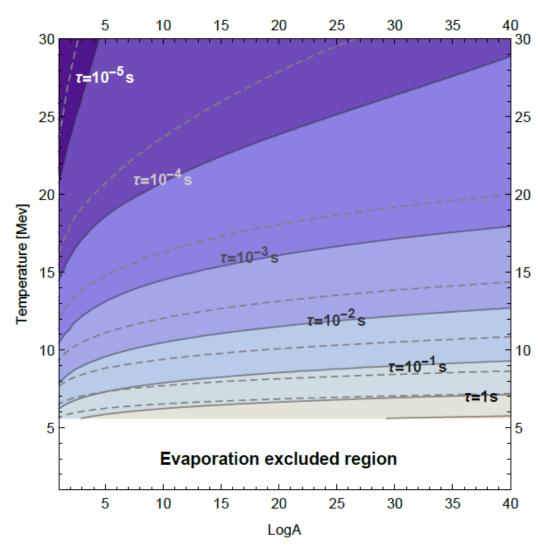


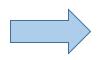
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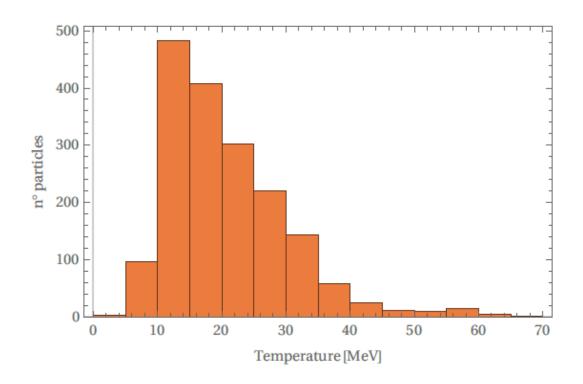


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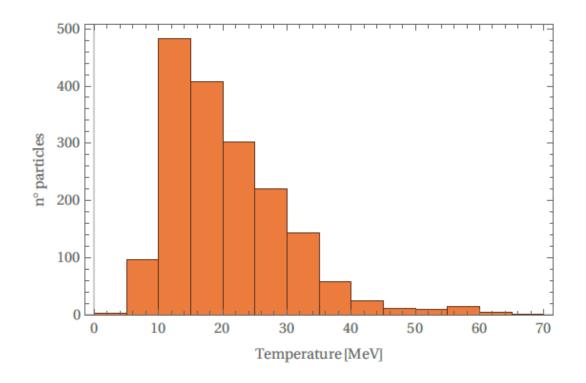


Some fragments with $A \sim 10^{30}$ could survive



From quark – star quark star simulation:

(A. Bauswein, R. Oechslin, and H.-T. Janka, Phys. Rev. D 81 (2010) 024012)



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How many strangelets ... ?

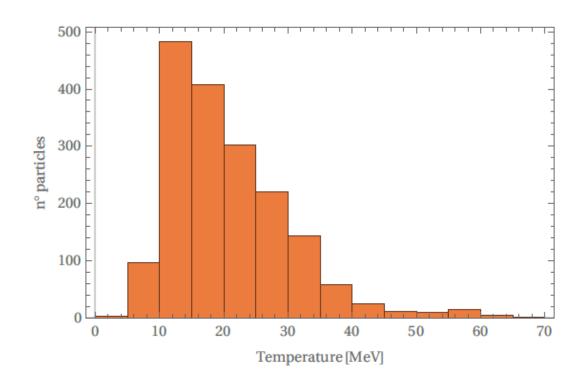
$$ightharpoonup$$
 keep $T>13~MeV$ for $t>8~ms$ or $T>16~MeV$ for $t>1~ms$ evaporated

- do not fulfill any of the two conditions remain
- have a temperature that is still increasing at end of the simulation

increasing

	100 %	99.9 %	99 %	total evaporated
	evaporated	evaporated	evaporated	mass
I=50 MeV	0.64-0.73	0.83-0.91	0.85 - 0.92	0.88-0.94
I=70 MeV	0.57 - 0.65	0.78 - 0.86	0.81 - 0.88	0.83-0.90

$$\nu$$
-heating: \approx 70% evaporate $T_u = T_s$: 94% evaporate (total ejecta = 6.6 \cdot 10⁻³ M_{\odot})



From quark – star quark star simulation:

(A. Bauswein, R. Oechslin, and H.-T. Janka, Phys. Rev. D 81 (2010) 024012)

How many strangelets ... ?

$$ightharpoonup$$
 keep $T > 13~MeV$ for $t > 8~ms$ or $T > 16~MeV$ for $t > 1~ms$ evaporated

- do not fulfill any of the two conditions remain
- have a temperature that is still increasing at end of the simulation

increasing

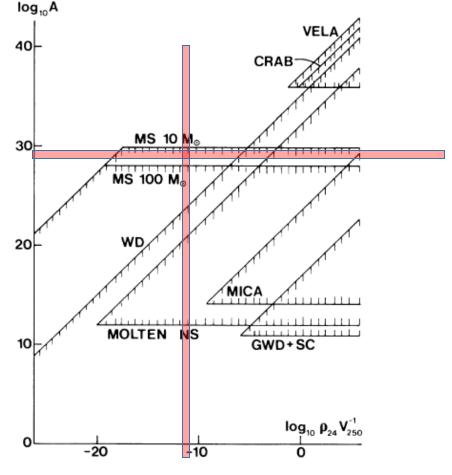
	100 %	99.9 %	99 %	total evaporated
	evaporated	evaporated	evaporated	mass
I=50 MeV	0.64-0.73	0.83-0.91	0.85 - 0.92	0.88-0.94
I=70 MeV	0.57 - 0.65	0.78 - 0.86	0.81 - 0.88	0.83-0.90

 ν -heating: \approx 70% evaporate $T_u = T_s$: 94% evaporate (total ejecta = $6.6 \cdot 10^{-3} M_{\odot}$)

Some strangelets evaporate partially: ≈90% of the mass evaporates

Conclusions

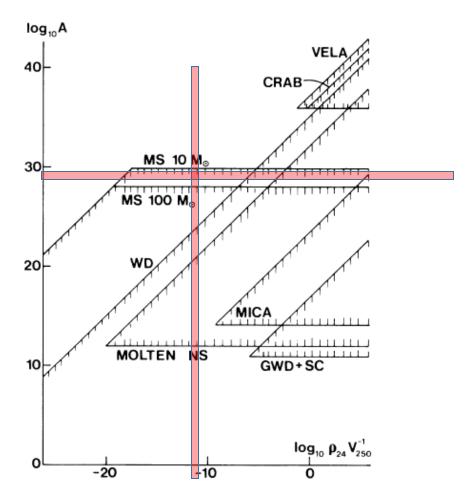
- Most of the strangelets ejected during the merger evaporate
- * non-evaporating strangelets are massive $A \sim 10^{30}$ and their number is small and so they are very unlikely to be detected in experiments
- evaporation is dominated by neutrons and therefore the initial electron fraction of the material is really low: same KN as NS-NS



J. Madsen, "Astrophysical Limits on the Flux of Quark Nuggets," Phys. Rev. Lett., vol. 61, pp. 2909–2912, 1988

Conclusions

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THANK YOU