

From a first order transition in QCD with up, down and strange quarks to a dark QCD matter scenario

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- ✓ Chiral extrapolation for baryon masses and a first order transition
- ✓ A generalized Higgs potential for dark QCD matter
- ✓ Dark QCD matter in a Higgs bubble
- ✓ Summary and outlook

The chiral Lagrangian with baryon fields

$$\Phi = \sqrt{2} \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & K^0 \\ K^- & \bar{K^0} & -\frac{2}{\sqrt{6}} \eta \end{pmatrix}$$

Goldstone boson octet ($J^P = 0^-$)

baryon octet ($J^P = \frac{1}{2}^+$)

$$B = \begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}} \Lambda \end{pmatrix}$$

✓ Leading order terms

covariant derivative $\partial_\mu = \partial_\mu + \dots$

$$\begin{aligned} \mathcal{L} = & \text{tr} \left\{ \bar{B} (i \partial \cdot \gamma - M_{[8]}) B \right\} + \textcolor{blue}{F} \text{tr} \left\{ \bar{B} \gamma^\mu \gamma_5 [i \textcolor{blue}{U}_\mu, B] \right\} + \textcolor{blue}{D} \text{tr} \left\{ \bar{B} \gamma^\mu \gamma_5 \{i \textcolor{blue}{U}_\mu, B\} \right\} \\ & - \text{tr} \left\{ \bar{B}_\mu \cdot ((i \partial \cdot \gamma - M_{[10]}) g^{\mu\nu} - i (\gamma^\mu \partial^\nu + \gamma^\nu \partial^\mu) + \gamma^\mu (i \partial \cdot \gamma + M_{[10]}) \gamma^\nu) B_\nu \right\} \\ & + \textcolor{blue}{C} \left(\text{tr} \left\{ (\bar{B}_\mu \cdot i \textcolor{blue}{U}^\mu) B \right\} + \text{h.c.} \right) + \textcolor{blue}{H} \text{tr} \left\{ (\bar{B}^\mu \cdot \gamma_\nu \gamma_5 B_\mu) i \textcolor{blue}{U}^\nu \right\} \end{aligned}$$

- $\textcolor{blue}{U}_\mu = \frac{1}{2} u^\dagger (\partial_\mu e^{i \frac{\Phi}{f}}) u^\dagger - \frac{i}{2} u^\dagger (\textcolor{red}{v}_\mu + \textcolor{red}{a}_\mu) u + \frac{i}{2} u (\textcolor{red}{v}_\mu - \textcolor{red}{a}_\mu) u^\dagger \quad \text{with} \quad u = e^{i \frac{\Phi}{2f}}$
- from $B \rightarrow B' + e + \bar{\nu}_e$: $\textcolor{blue}{F} \simeq 0.45$ and $\textcolor{blue}{D} \simeq 0.80$
- from large- N_c : $\textcolor{blue}{H} = 9 \textcolor{blue}{F} - 3 \textcolor{blue}{D}$ and $\textcolor{blue}{C} = 2 \textcolor{blue}{D}$

Chiral symmetry breaking terms

$$\begin{aligned}\mathcal{L}_\chi^{(2)} = & 2 \textcolor{blue}{b}_0 \operatorname{tr} (\bar{B} B) \operatorname{tr} (\textcolor{blue}{\chi}_+) + 2 \textcolor{blue}{b}_D \operatorname{tr} (\bar{B} \{\textcolor{blue}{\chi}_+, B\}) + 2 \textcolor{blue}{b}_F \operatorname{tr} (\bar{B} [\textcolor{blue}{\chi}_+, B]) \\ - & 2 \textcolor{blue}{d}_0 \operatorname{tr} (\bar{B}_\mu \cdot B^\mu) \operatorname{tr} (\textcolor{blue}{\chi}_+) - 2 \textcolor{blue}{d}_D \operatorname{tr} ((\bar{B}_\mu \cdot B^\mu) \textcolor{blue}{\chi}_+)\end{aligned}$$

$$\textcolor{blue}{\chi}_+ = \chi_0 - \frac{1}{8f^2} \{\Phi, \{\Phi, \chi_0\}\} + \mathcal{O}(\Phi^4)$$

quark mass matrix

$$\chi_0 \sim \begin{pmatrix} m_u & 0 & 0 \\ 0 & m_d & 0 \\ 0 & 0 & m_s \end{pmatrix}$$

✓ Relevance of low-energy parameters

- quark-mass dependence of the baryon masses \leftrightarrow lattice QCD
- meson-baryon scattering \leftrightarrow resonances in QCD
- nucleon sigma terms, $\langle N | \bar{u} u | N \rangle$, $\langle N | \bar{d} d | N \rangle$ and $\langle N | \bar{s} s | N \rangle$
relevant in WIMP scenarios – ATLAS

see e.g. arXiv:1805.09795

Quark-mass dependence of the baryon masses

✓ A challenge

- 'poor' convergence in the heavy-baryon formulation of χ PT
e.g. $M_{\Xi} = (1018 + 1311 - 1007) \text{ MeV} = 1322 \text{ MeV}$
- conventional χ PT inconsistent with three-flavor QCD lattice simulations

✓ One-loop depends sensitively on internal masses

$$\Sigma_B(p) = \sum_{Q \in [8]} \sum_{R \in [8], [10]} \quad \begin{array}{c} \text{---} \\ p, B \end{array} \quad \begin{array}{c} \text{---} \\ k, Q \end{array} \quad \begin{array}{c} \text{---} \\ p-k, R \end{array} \quad \begin{array}{c} \text{---} \\ p, B \end{array} \quad + \dots$$

- chiral expansion in terms of physical meson and baryon masses
- reorganize conventional χ PT keeping its model independence
- renormalization scale and reparametrization invariance

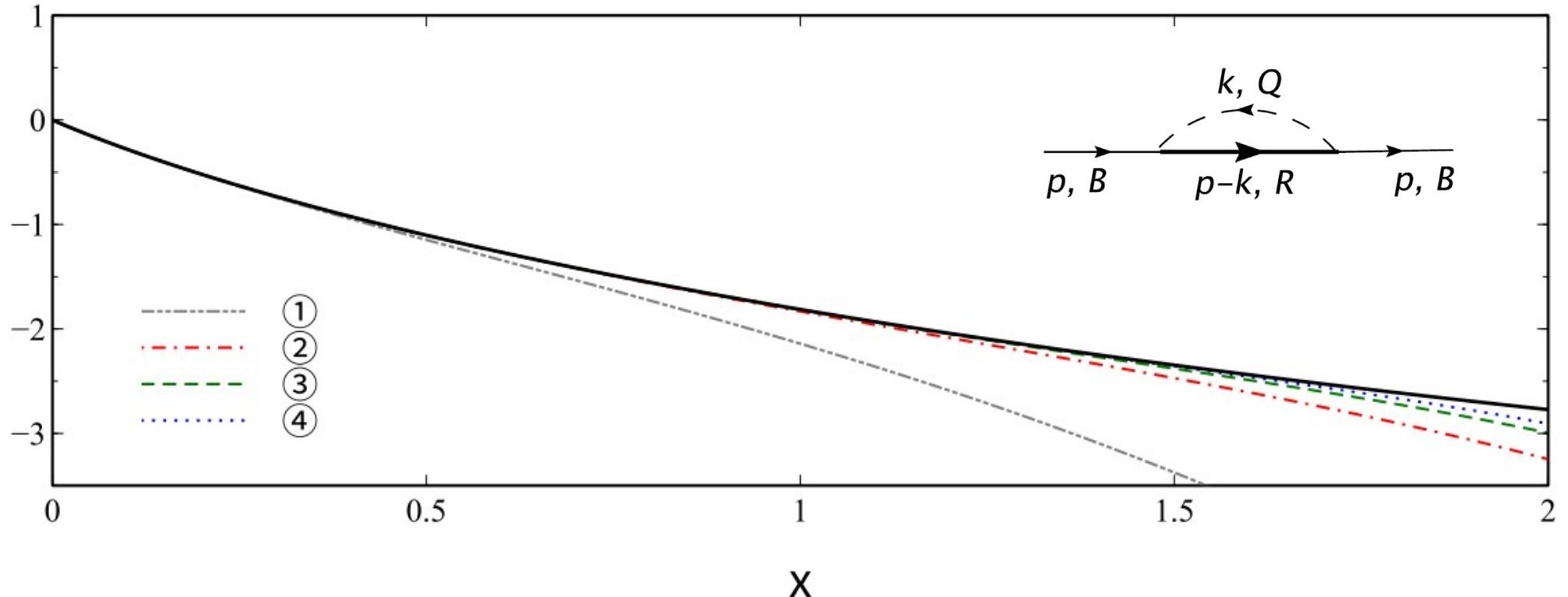
Phys. Rev. D51 (1995) 3697

Phys. Rev. D85 (2012) 034001

Phys. Rev. D86 (2012) 091502

Phys. Rev. D90 (2014) 054505

Chiral expansion of the scalar loop function $(4\pi)^2 \bar{I}_{QR}$



✓ Convergence study for $M_R = M_B$ and $x = m_Q/M_R$

- $(4\pi)^2 \bar{I}_{QR} = -\pi \sqrt{x^2} f_1(x^2) + x^2 f_2(x^2) - \frac{1}{2} x^2 f_3(x^2) \log x^2$
 - the functions $f_n(x^2)$ are analytic in x^2 for $|x| < 2$
- $$f_n(x^2) = 1 + \#x^2 + \#x^4 + \dots$$
- good convergence even for $m_K = M_N$ with $x \simeq 1!$

Quark-mass dependence of the baryon masses

✓ Good convergence of reordered chiral expansion

- use physical meson and baryon masses
- the full one-loop contributions can be decomposed into chiral moments
- taking empirical masses the N⁴LO effects are less than 8 MeV

✓ Baryon masses determined by a non-linear system

$$M_B - \Sigma_B(M_B) = \begin{cases} M_{[8]} & \text{for } B \in [8] \\ M_{[10]} & \text{for } B \in [10] \end{cases}$$

$$\Sigma_B(p) = \sum_{Q \in [8]} \sum_{R \in [8], [10]} \frac{\text{---}}{p, B} \frac{\text{---}}{p-k, R} \frac{\text{---}}{p, B} + \dots$$

k, Q

- numerical challenge

Low-energy parameters from lattice QCD simulations

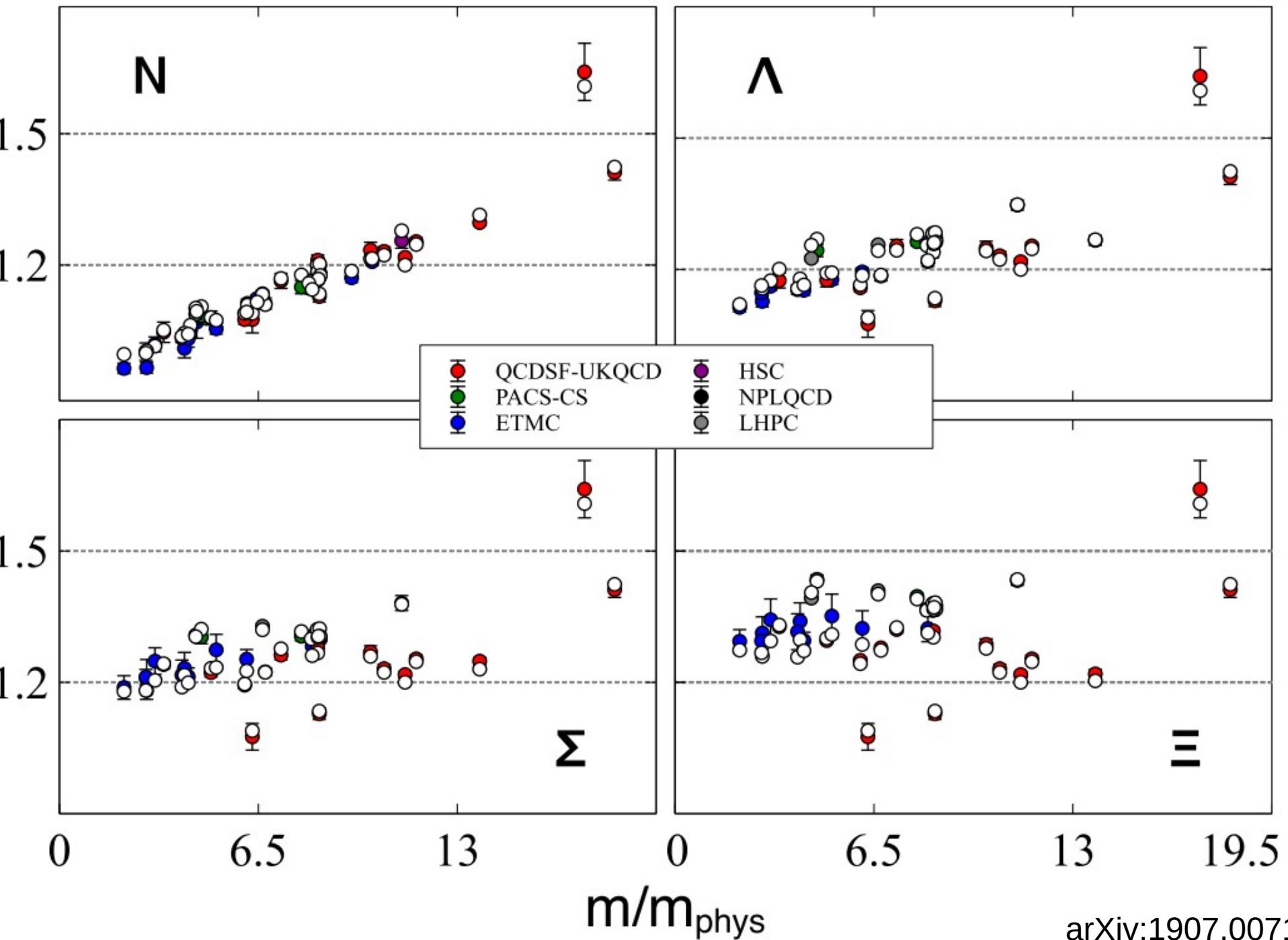


QCD Lattice simulations

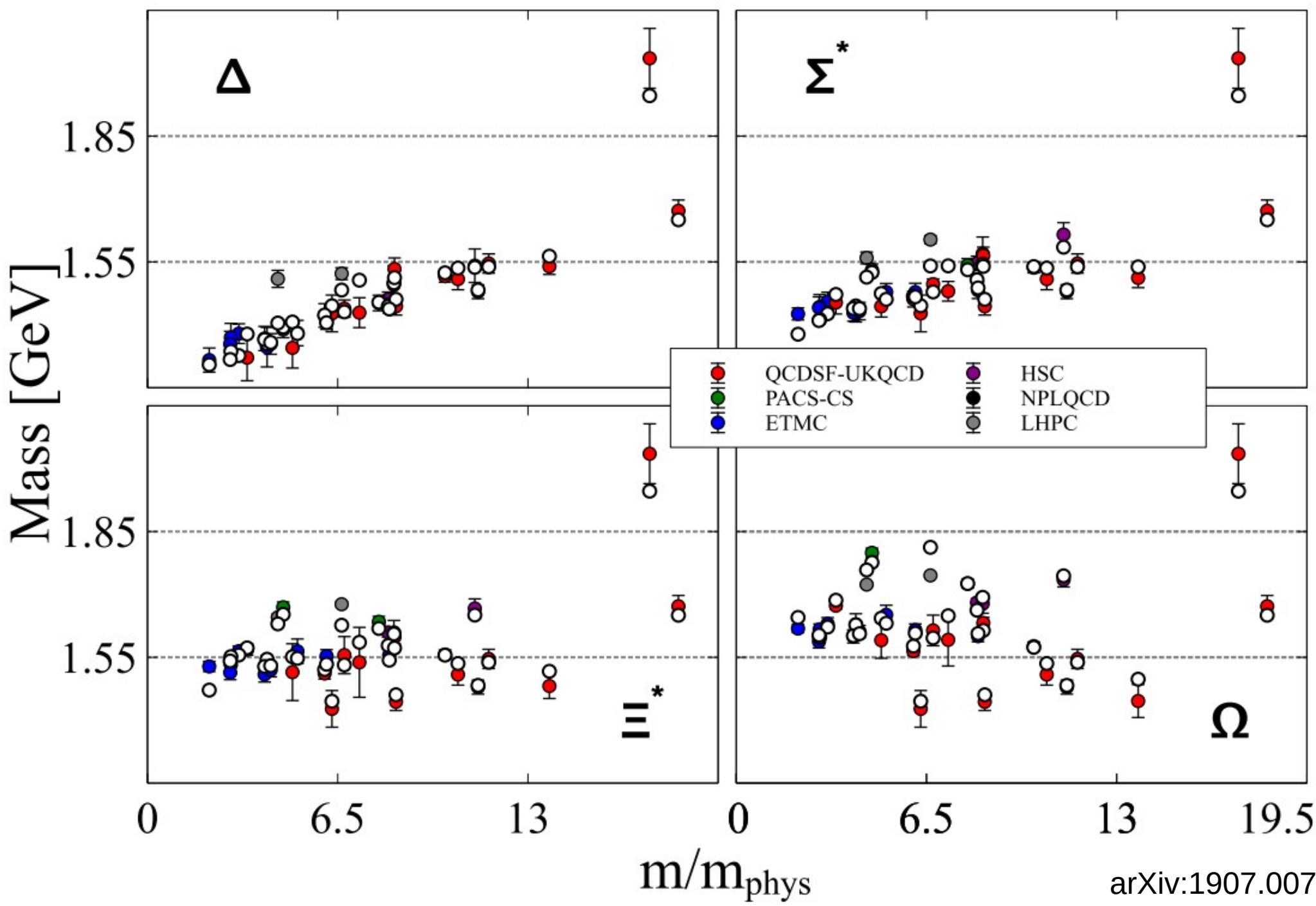
- consider data from PACS-CS, HSC, LHPC, NPLQCD, QCDSF-UKQCD and ETMC
- finite volume effects are considered
- data are not always at physical strange-quark mass
- there are about 300 data points with $m_\pi, m_K < 600$ MeV
- physical baryon octet and decuplet masses are always reproduced
→ global lattice scale setting
- lattice spacing effects are ignored in this work
- assume an ad-hoc size for the systematic error of about 10 MeV
- achieve a data reproduction with $\chi^2/N \simeq 1$

Quark-mass dependence of the baryon octet masses

Mass [GeV]



Quark-mass dependence of the baryon decuplet masses



Quark-mass dependence of the baryon masses

✓ Baryon masses as a function of $m_u = m_d = m$ shown

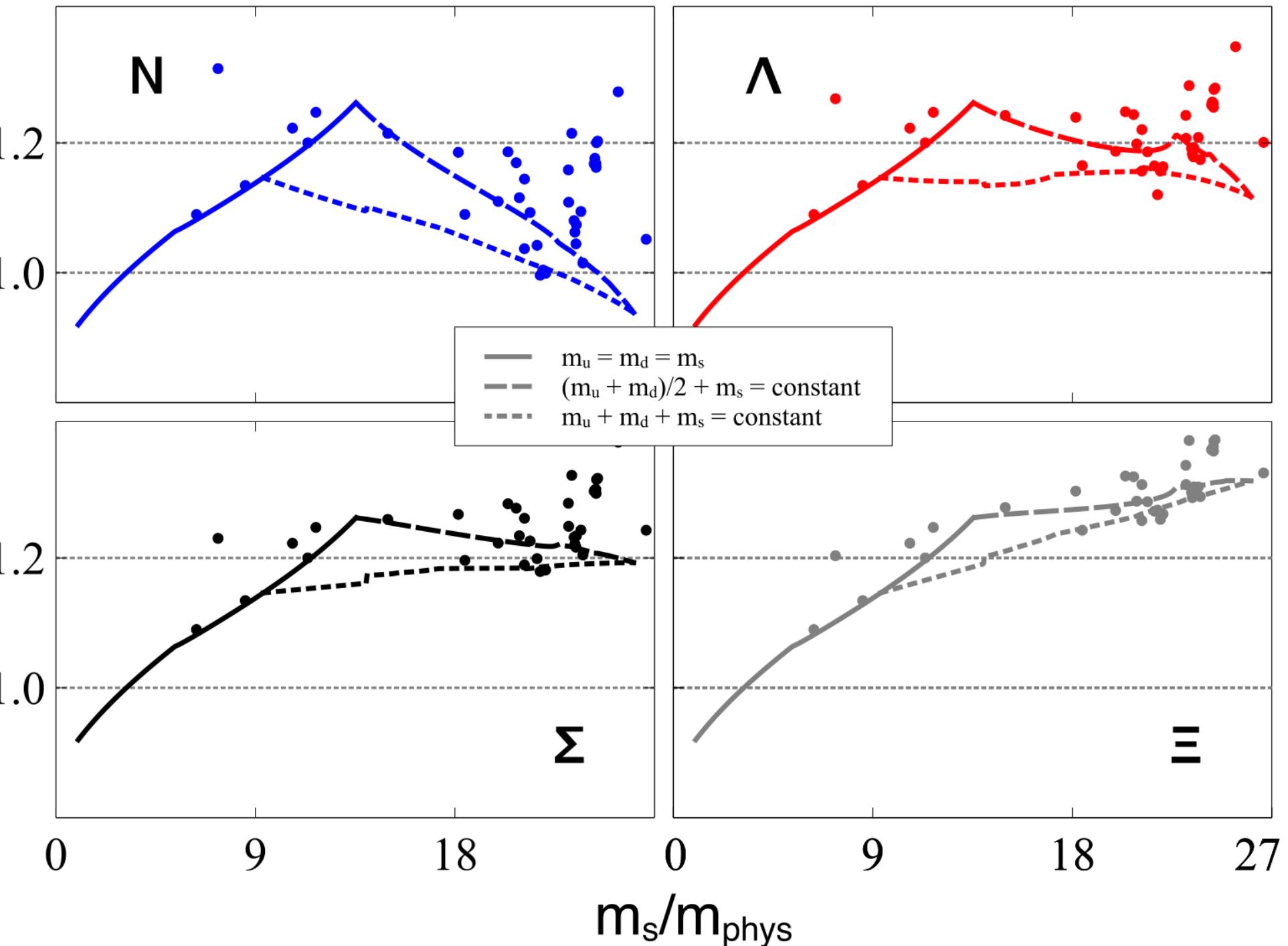
- unphysical strange quark mass as chosen by the lattice group

✓ Baryon masses on different m_s trajectories

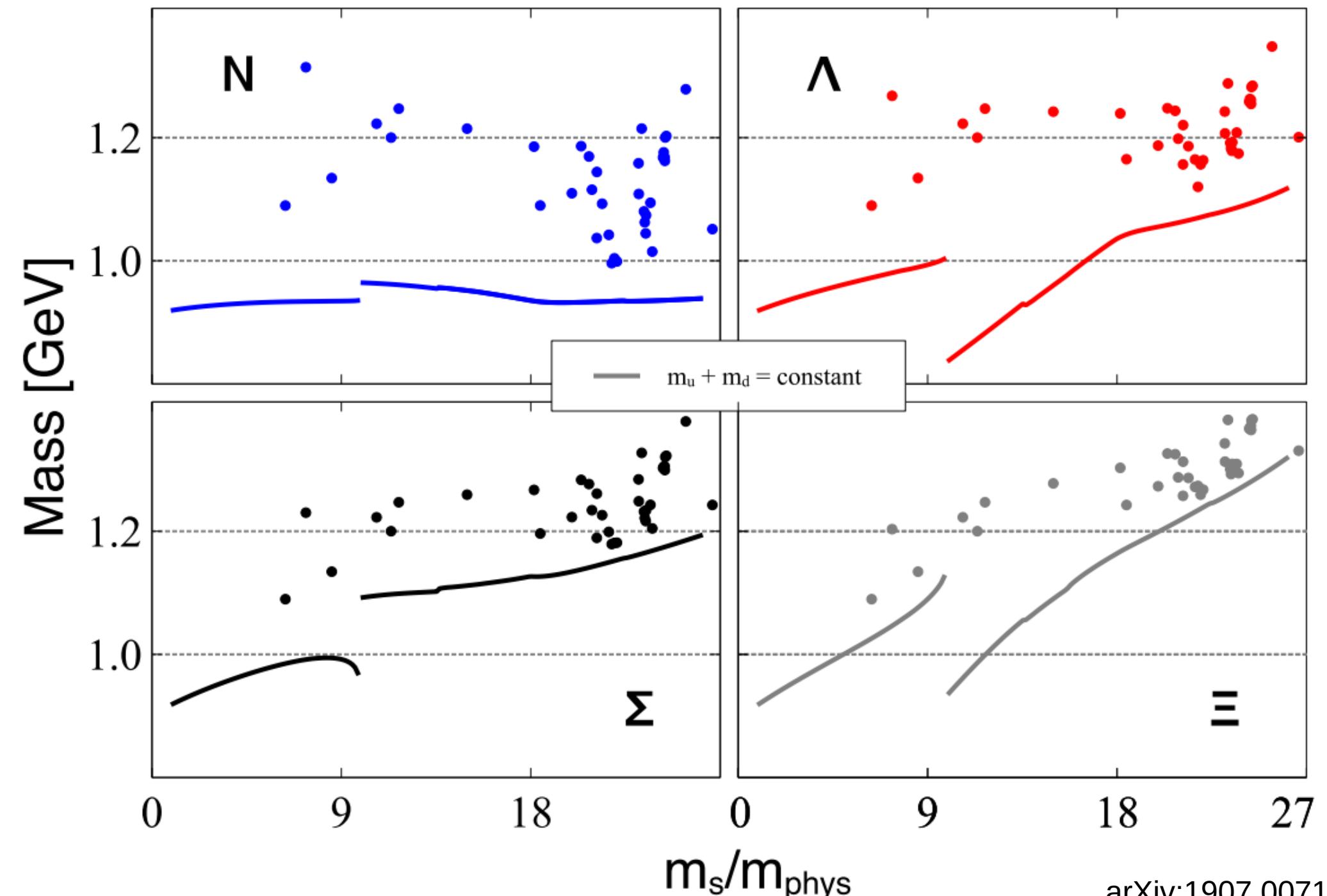
- flavour symmetric case :: $m_u = m_d = m_s$
- fan plot :: $m_u + m_d + m_s$ fixed
- kaon mass :: at $(m_u + m_d)/2 + m_s \sim m_K^2$ fixed
- pion mass :: $m_u + m_d \sim m_\pi^2$ fixed

Baryon masses on different m_s trajectories

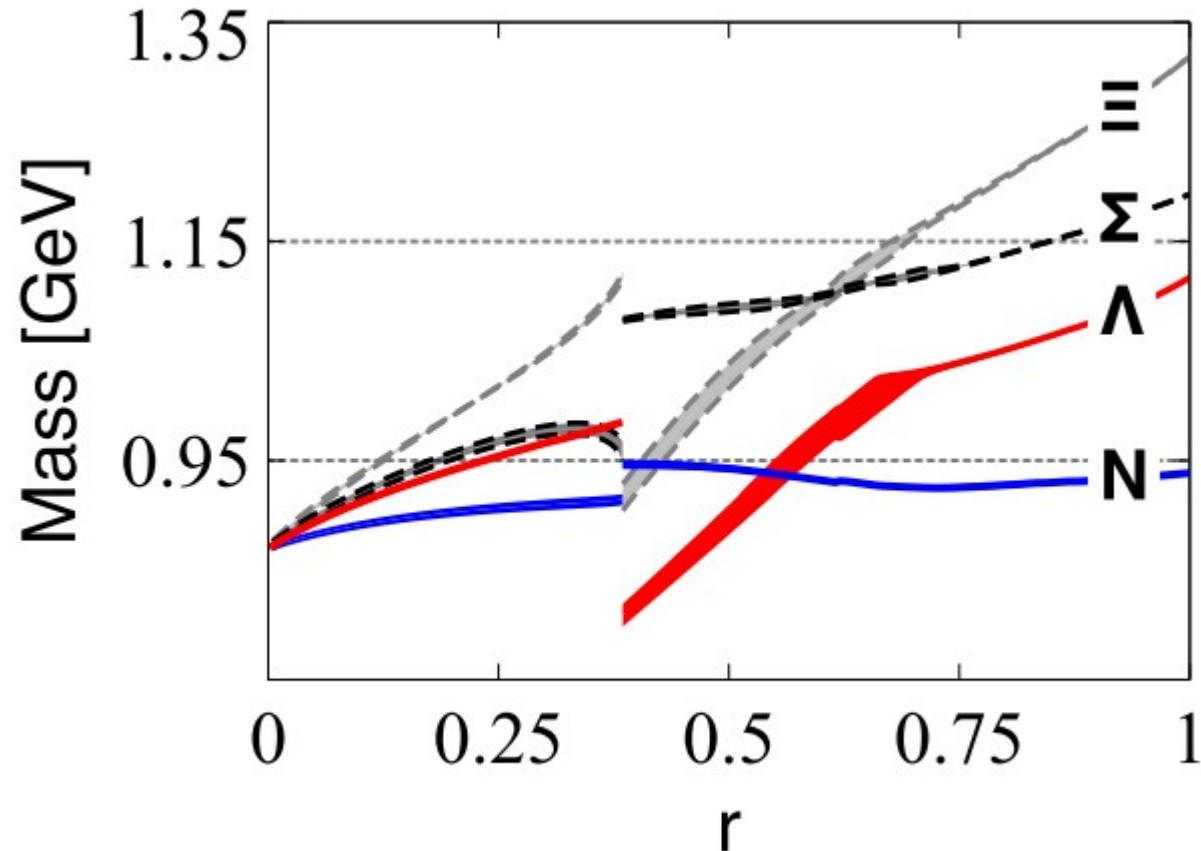
Mass [GeV]



1st order transition at physical $m_u = m_d$



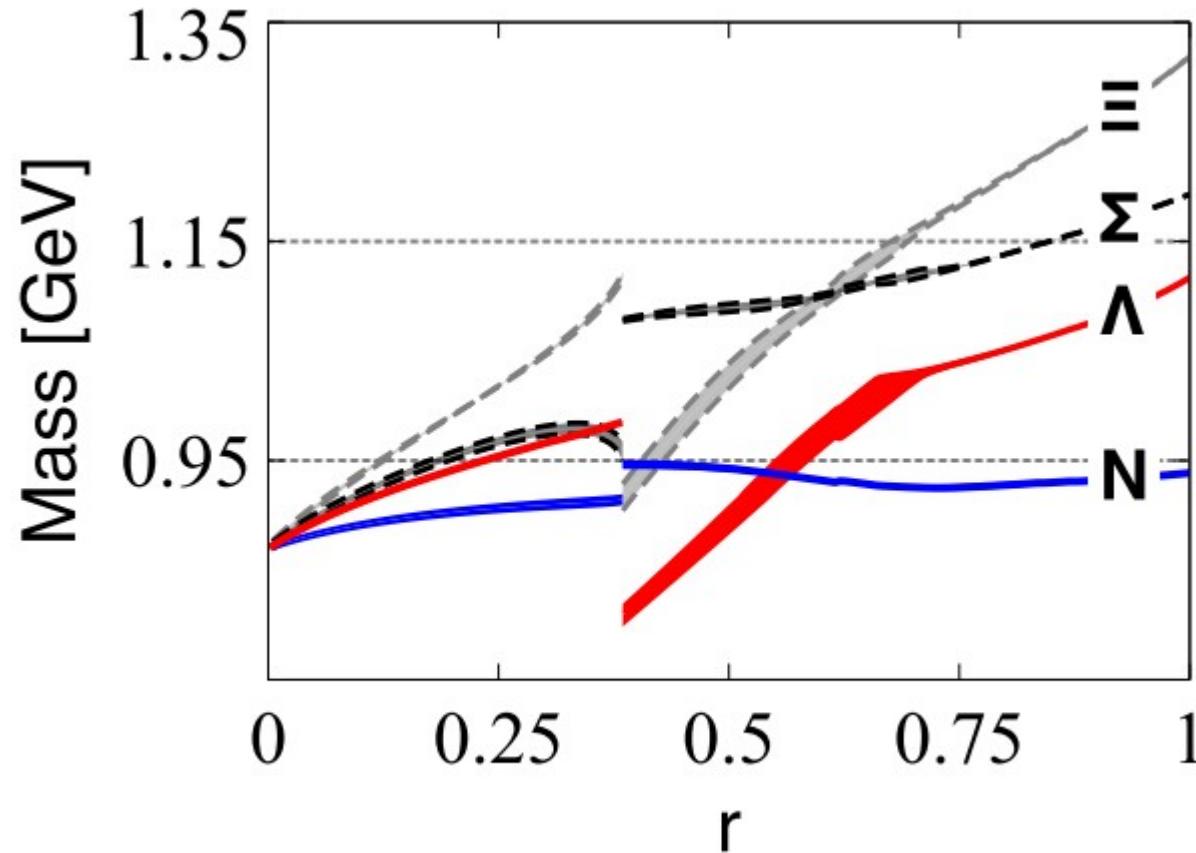
Baryon masses depend on the Higgs field



- quark masses in QCD are proportional to $v \sim r$

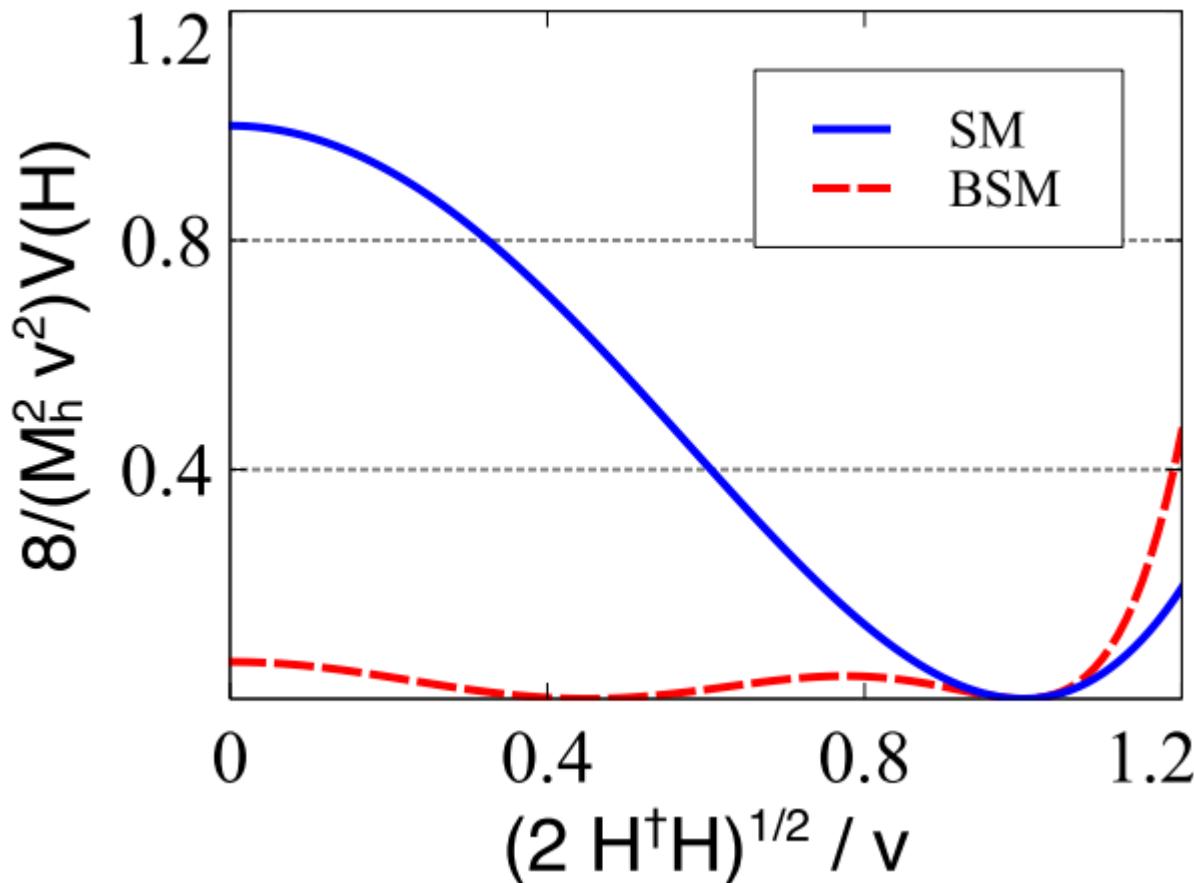
$$V(H) = \frac{M_h^2}{2 v^2} \left(H^\dagger H - \frac{v^2}{2} \right)^2 \quad \text{from Standard Model}$$

Baryon masses depend on the Higgs field



- is such a first order transition of physical relevance?
- lattice QCD simulations should see that transition
- in the standard model $r = 1$:: physics beyond the SM?

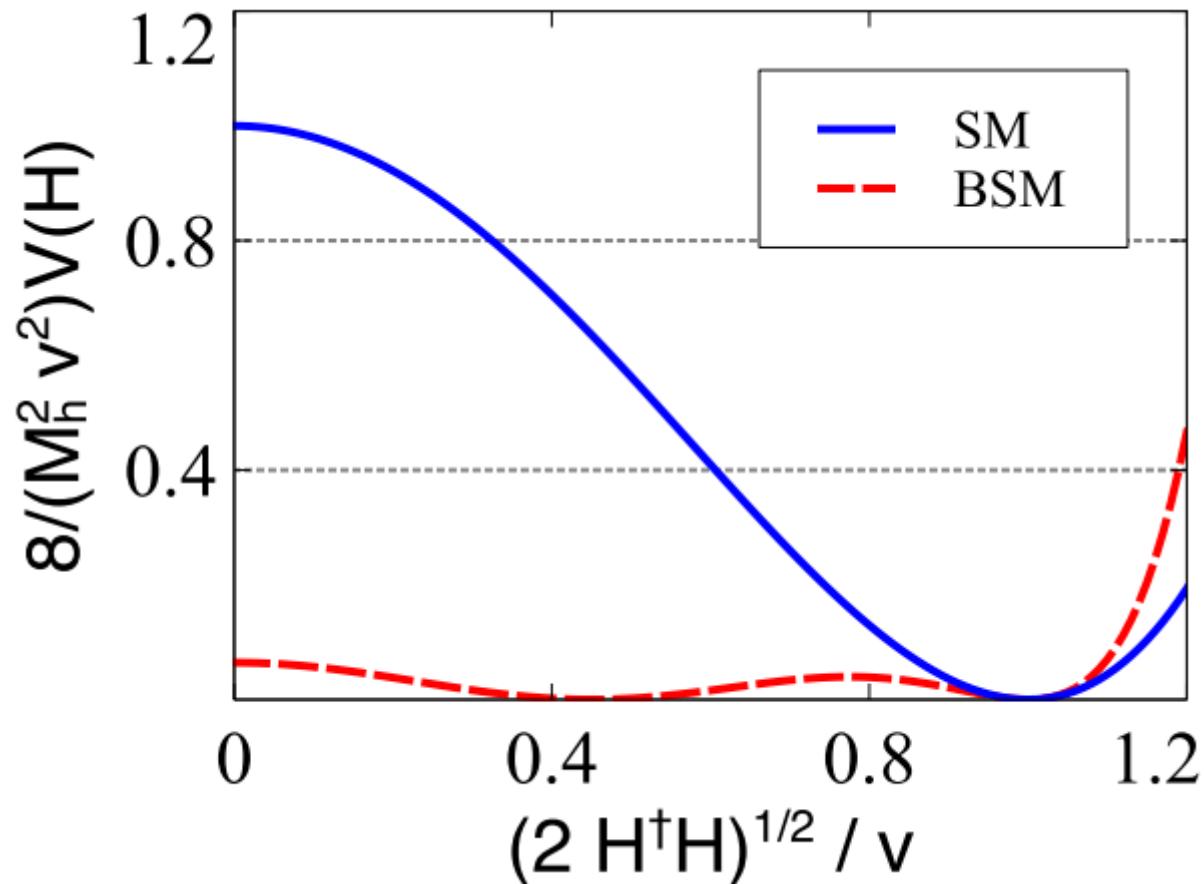
A generalization of the Higgs potential with two minima



$$V_{\text{BSM}}(H) = \frac{2 M_h^2}{v^6 (1 - r^2)^2} \left(H^\dagger H - \frac{v^2}{2} \right)^2 \left(H^\dagger H - \frac{v_a^2}{2} \right)^2 ,$$

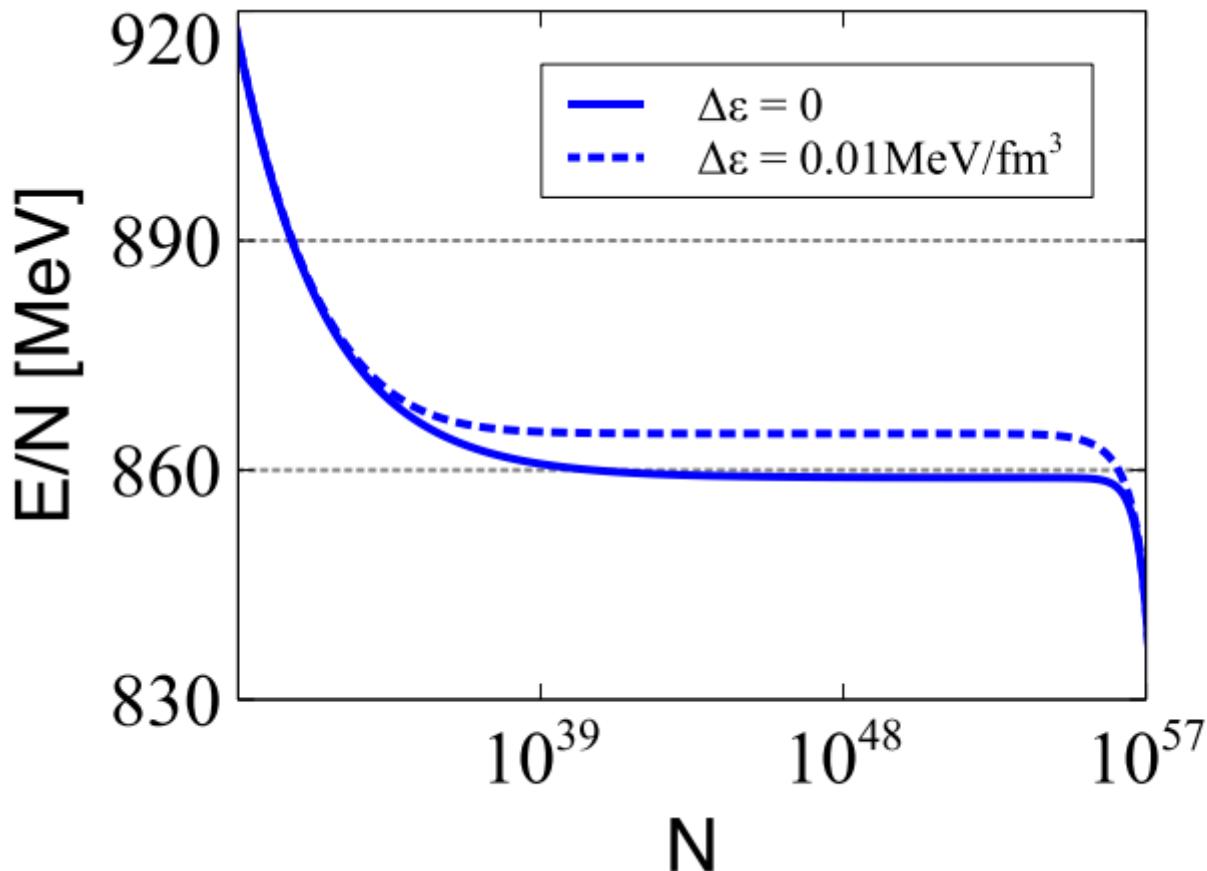
and $r = v_a/v = m_s/m_s^{\text{phys}}$,

A generalization of the Higgs potential with two minima



- current data from CERN do not rule out such a potential
- 3-Higgs coupling $\kappa_\lambda \simeq 6$ versus $\kappa_\lambda = 1$ from SM
- 2σ range $-5.0 < \kappa_\lambda < 12.1$ from ATLAS

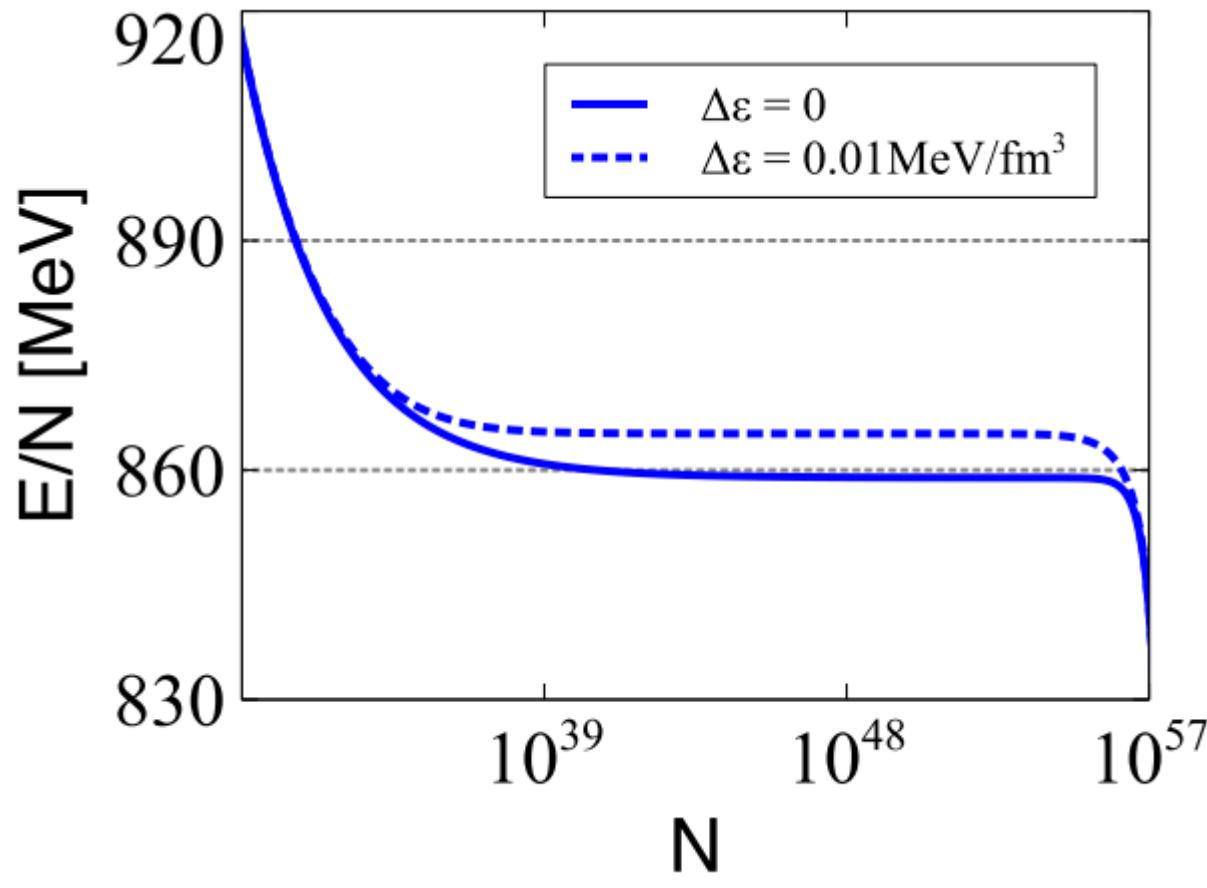
Dark QCD matter in a Higgs bubble



$$N_{\text{Sun}} \simeq M_{\text{Sun}}/M_N \\ \simeq 1.2 \times 10^{57}$$

- consider Λ baryons with $M_\Lambda \simeq 860 \text{ MeV}$ in 'false' vacuum
- total energy per particle E/N smaller than M_N for large N
- dark matter in a Higgs bubble is stable

Dark QCD matter in a Higgs bubble

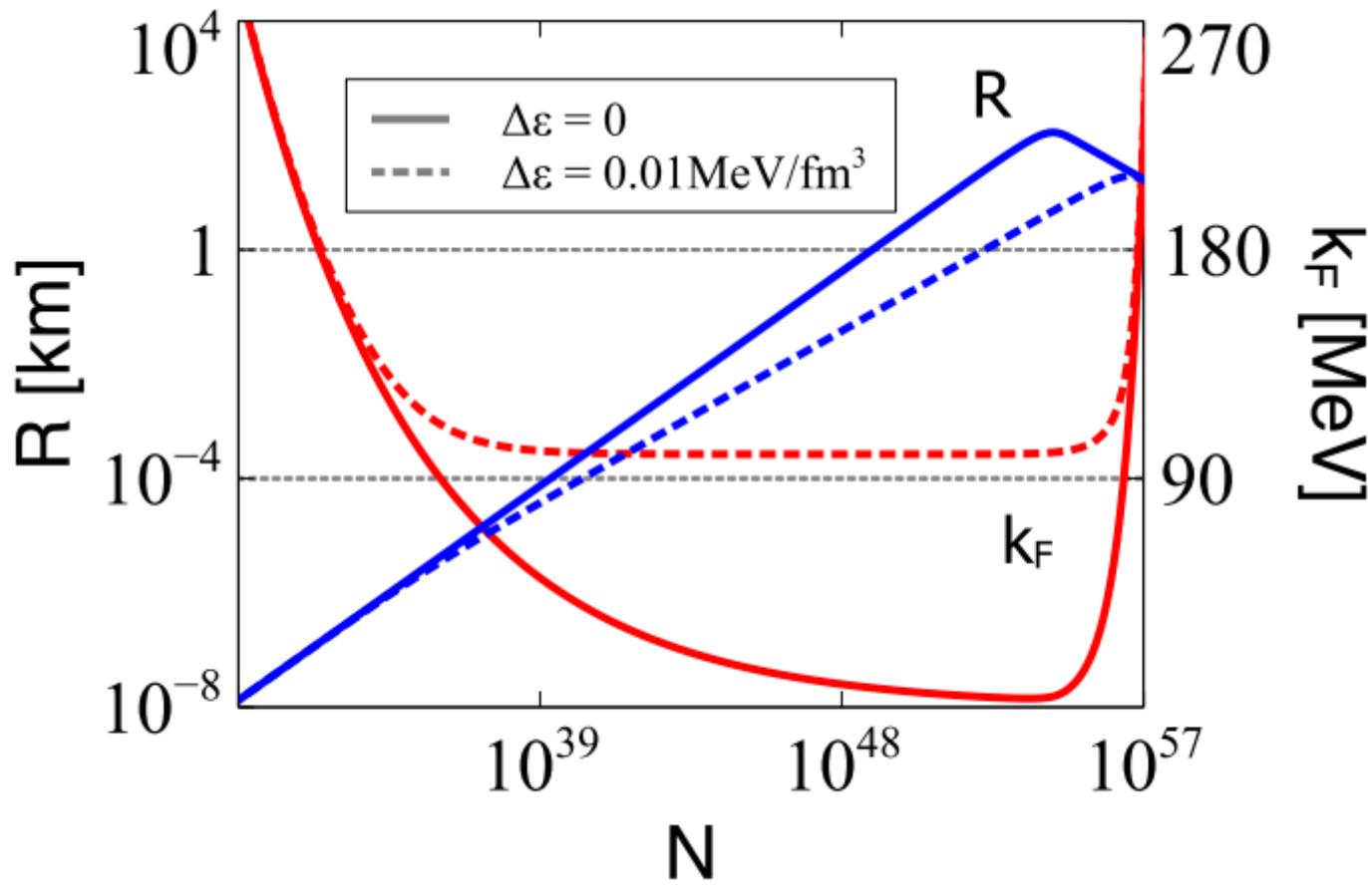


$$N_{\text{Sun}} \simeq M_{\text{Sun}}/M_N \\ \simeq 1.2 \times 10^{57}$$

$$N = \frac{4(R k_F)^3}{9\pi}$$

- volume effects: fermi gas + gravitation + $\Delta\epsilon$
- surface effects: value of Higgs field changes from v_a to v
- large amount of energy stored in Higgs shell

Radius and density of the Higgs bubble



$$\rho = k_F^3 / (3\pi^2)$$

$$N = \frac{4(Rk_F)^3}{9\pi}$$

- predict maximum radius of Higgs bubble
- for $N > 10^{57}$ sensitive to EOS of Λ 's in the bubble

Summary & Outlook

✓ Chiral extrapolation of baryon octet and decuplet masses

- resummed χ PT : use on-shell masses in the loops
 - solve system of coupled and non-linear equations
 - chiral expansion with up, down and strange quarks is well convergent
 - reproduce the QCD Lattice data set at $m_{\pi,K} < 600$ MeV
 - predict a large number of low-energy constants for the chiral Lagrangian of QCD
- predict first order transition for the baryon masses
 - the nature of the baryonic ground state in QCD depends on the quark masses
 - the nature of the baryonic ground state depends on the choice of Higgs field

✓ A dark matter scenario with Λ baryons in a Higgs bubble

- Generalize the Higgs potential to support two degenerate minima
 - large fraction of (dark) baryonic matter in Higgs bubbles (here $M_\Lambda < M_N$)
 - derive a maximum radius of such bubbles (< 800 km)
- future request: derive equation of state of Λ baryons in the Higgs bubble ...
- possibility of strange dark matter objects with masses larger than neutron stars

thanks to collaborators: Yonggoo Heo and Xiao-Yu Guo