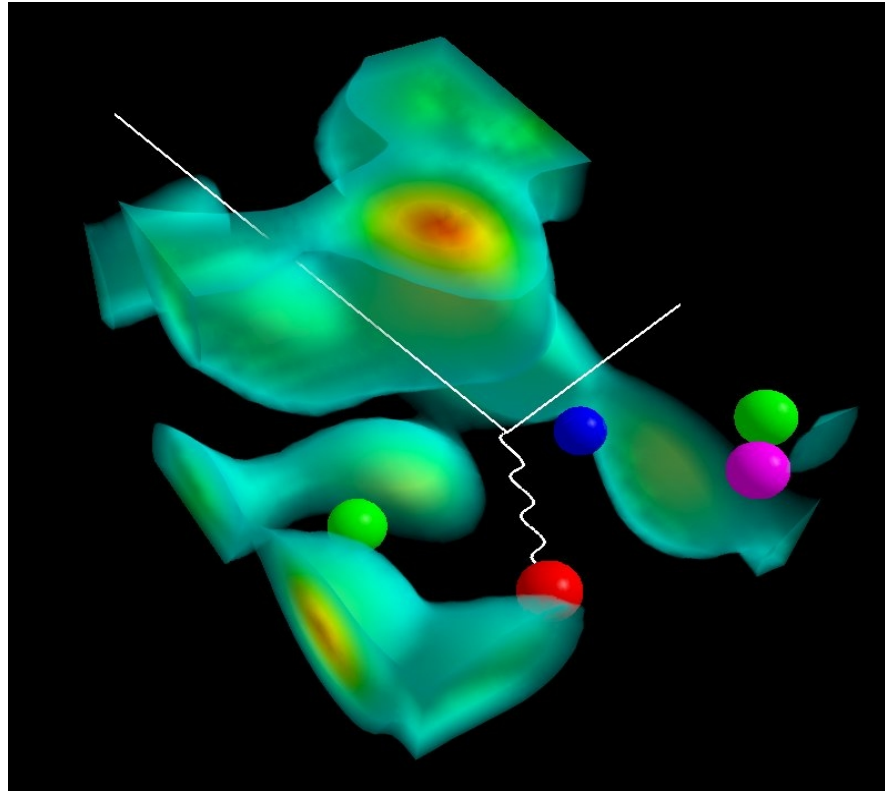


# New Developments in Low Energy QCD



**Anthony W. Thomas**

**International Conference on Exotic Atoms and Related Subjects**  
**Stefan-Meyer-Institute for Subatomic Physics, Wien**  
**15<sup>th</sup> September 2021**

# Outline

- I. New Insight into the Quark Model
  - The  $\Lambda(1405)$  IS a  $K\bar{b}$ -N bound state
  - The Roper IS generated by  $\pi N$ - $\sigma N$ - $\pi\Delta$  rescattering
  - The Quark Model is not so bad!
- II. Kaonic H and D
- III. Nuclei from Quarks
  - start from a QCD-inspired model of *hadron* structure
  - develop a quantitative theory of nuclear structure
- IV. Search for observable effects of the change in hadron structure in-medium

# Spectroscopy

- how do excited states emerge from QCD ?
- what are the fundamental degrees of freedom ?
- Lattice QCD provides extremely valuable information

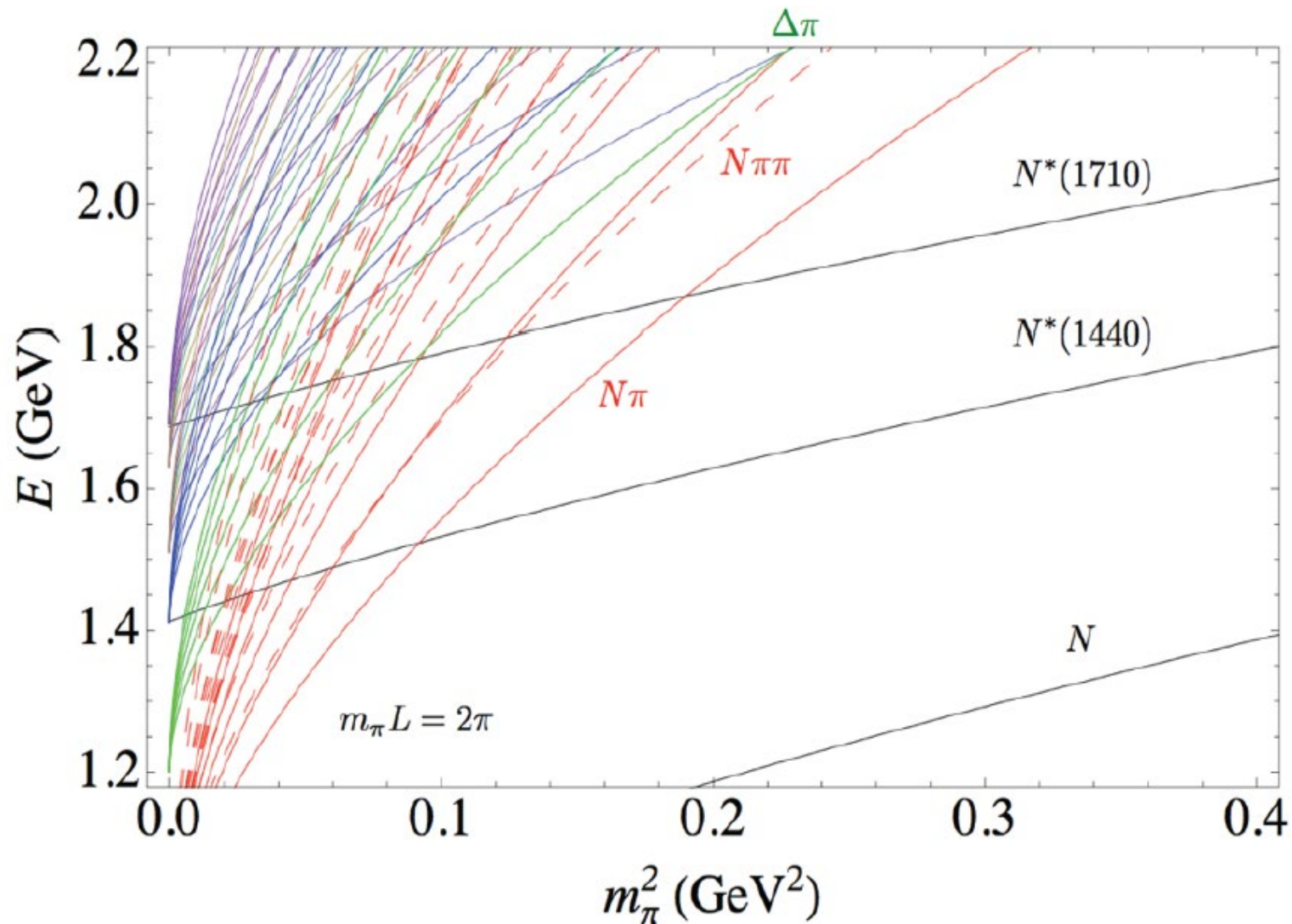
# **Resonances are very complicated – and the lattice is not**

- **Everything is stable – an eigenstate of the QCD Hamiltonian**
- **Whereas real resonances decay like crazy.....**
- **Lüscher has a method to derive phase shifts at discrete energies when there is one open channel**
- **That approach has been generalized to coupled channels by Hansen and Sharpe (Phys.Rev. D86 (2012) 016007) and Lellouch and Lüscher (Comm.Math.Phys., 219 (2011) 31) BUT it becomes very complicated**

**Interesting cases have many open channels**

- at least at realistic quark masses**

# In General: Multiple open channels



and then there is:  $\sigma N$ ,  $\omega N$ ,  $\rho N$  etc....

# The $\Lambda(1405)$

- 50 years after speculation by Dalitz *et al.*, we have unambiguous evidence that it is a  $\bar{K}$ -N bound state!
- Rather than the Lüscher method we apply **Hamiltonian Effective Field Theory**
  - shown to be equivalent for phase shifts\*
  - BUT also provides information on eigenstates
- Carry out a Hamiltonian analysis of lattice data
- Examine the **strange magnetic form factor** of  $\Lambda(1405)$

\* Wu et al., Phys. Rev. C 90 (2014) 5, 055206

# First calculation after QCD incorporating chiral symmetry

PHYSICAL REVIEW D

VOLUME 31, NUMBER 5

1 MARCH 1985

## *S*-wave meson-nucleon scattering in an SU(3) cloudy bag model

E. A. Veit\* and B. K. Jennings

*TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia, Canada V6T 2A3*

A. W. Thomas

*Physics Department, University of Adelaide, Adelaide, South Australia 5001*

R. C. Barrett

*Physics Department, University of Surrey, Guildford GU2 5XH, United Kingdom*

(Received 8 June 1984)

The cloudy bag model (CBM) is extended to incorporate chiral  $SU(3) \times SU(3)$  symmetry, in order to describe *S*-wave  $KN$  and  $\bar{K}N$  scattering. In spite of the large mass of the kaon, the model yields reasonable results once the physical masses of the mesons are used. We use that version of the CBM in which the mesons couple to the quarks with an axial-vector coupling throughout the bag volume. This version also has a meson-quark contact interaction with the same spin-flavor structure as the exchange of the octet of vector mesons. The present model strongly supports the contention that the  $\Lambda^*(1405)$  is a  $\bar{K}N$  bound state.

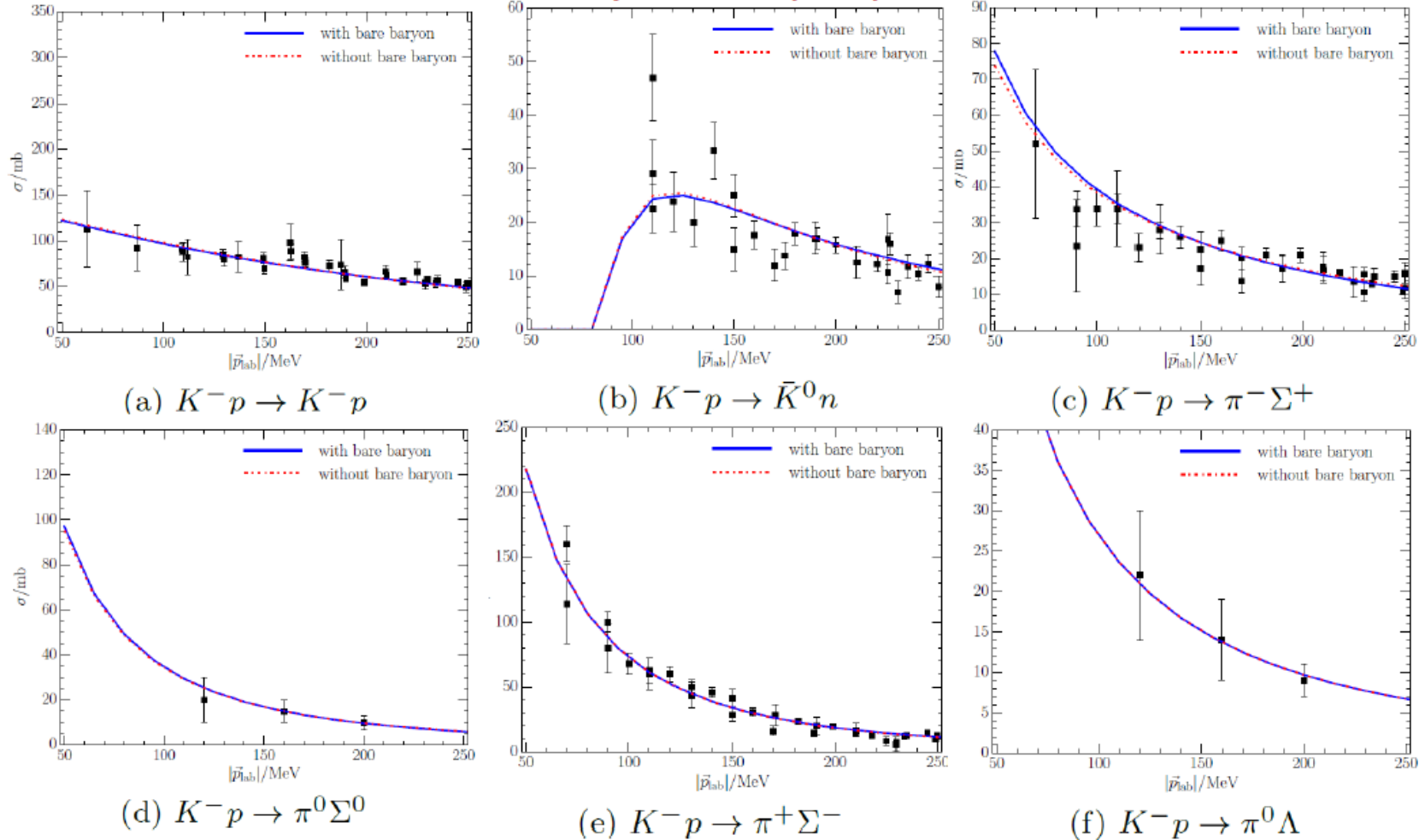
Reached a similar conclusion

But now we can use QCD itself



# Hamiltonian fits existing data

Zhan-wei Liu etc. Phys.Rev. D95 (2017) no.1, 014506

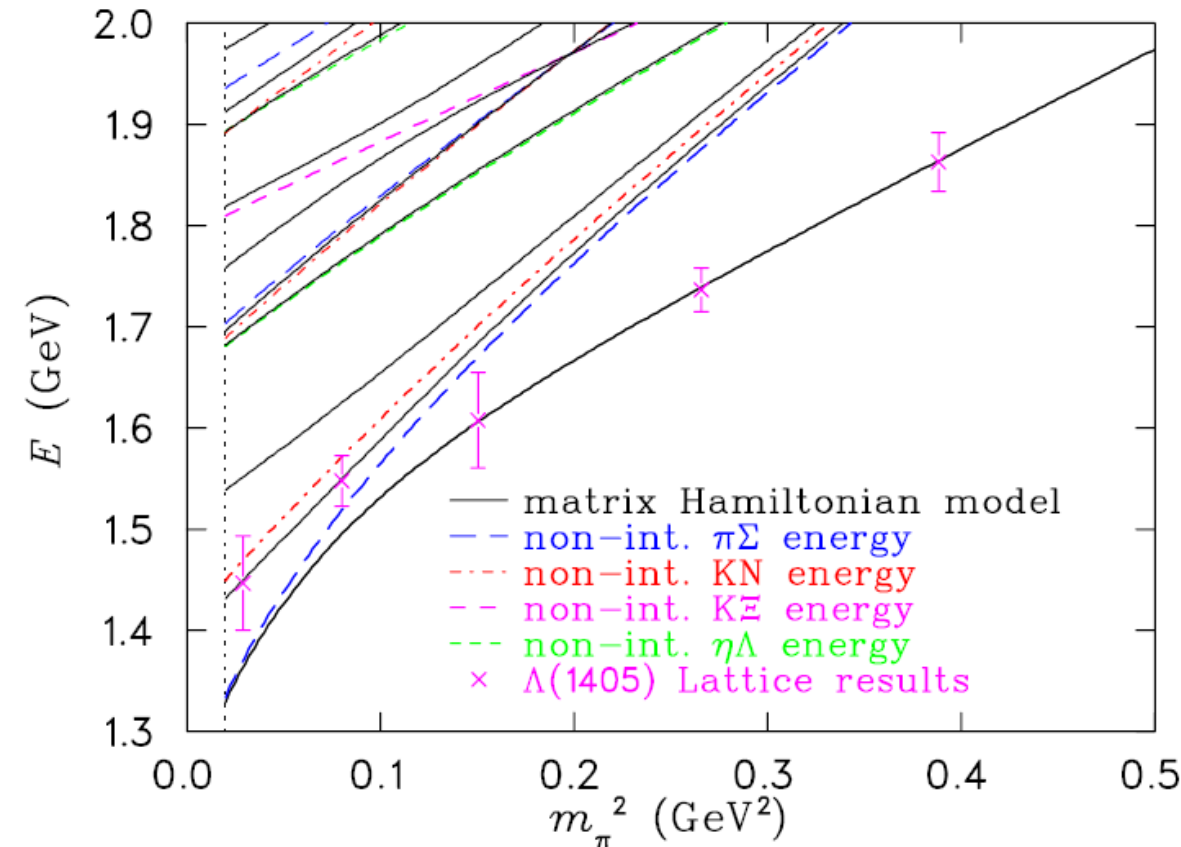


Include  $\pi\Sigma$ ,  $K\bar{p}N$ ,  $\eta\Lambda$  and  $K\Xi$  channels

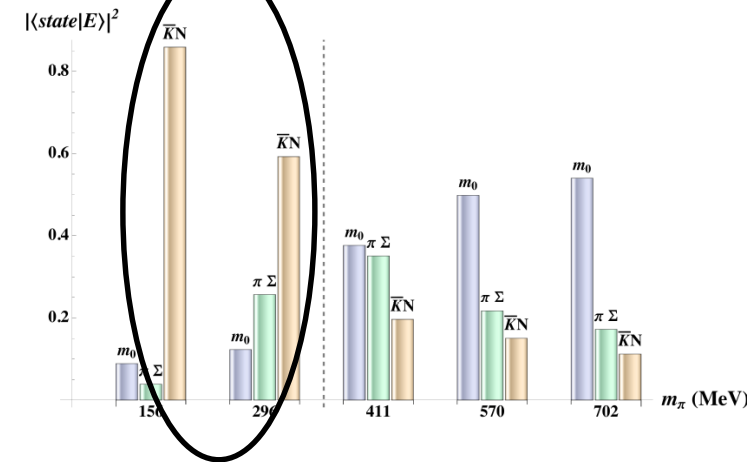
Similar work by Valencia, Bonn, Jlab and other groups

# Low lying negative parity state : $\Lambda(1405)$

Clear evidence that it is a  $\bar{K}N$  bound state



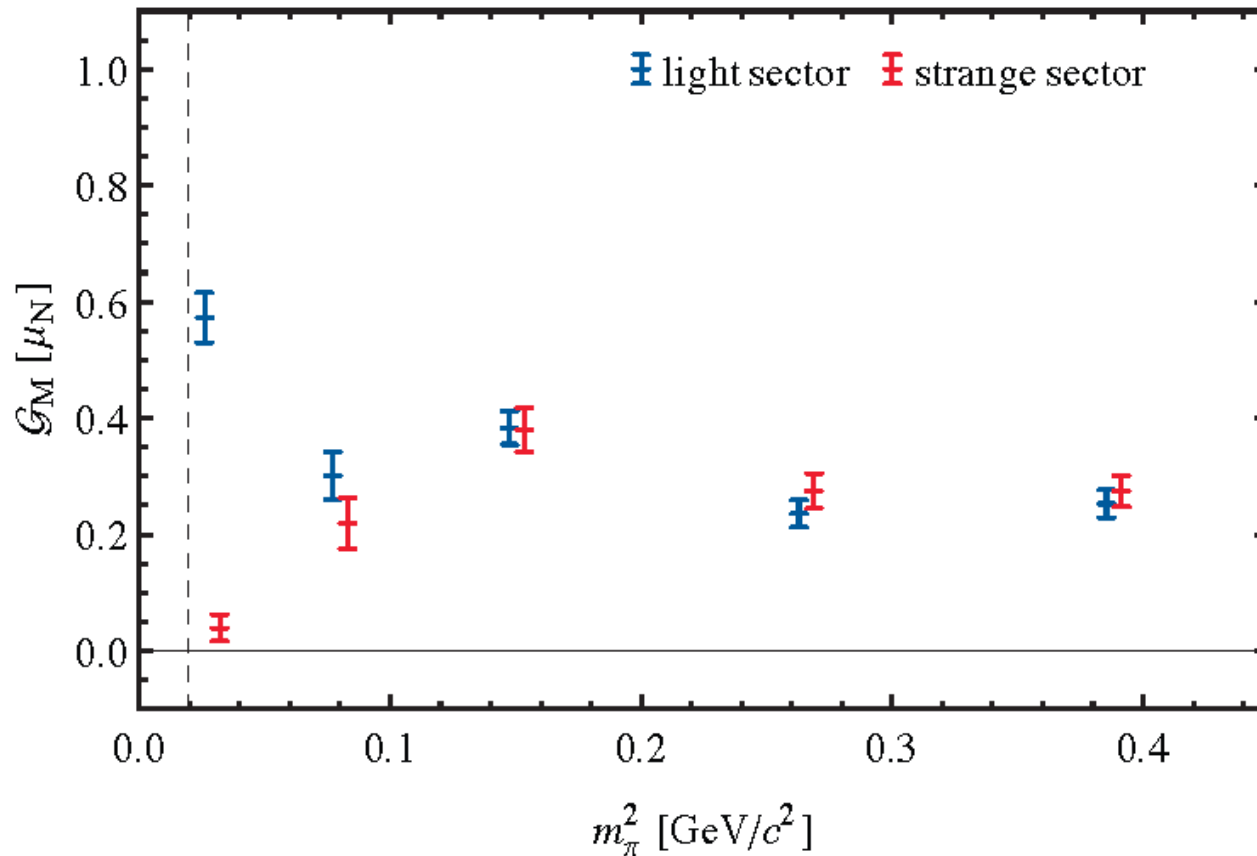
Hamiltonian approach allows one to examine the eigenstates:



Hall, Leinweber, Menadue, Young, AWT  
– Phys. Rev. Lett. 114 (2015) 13

# Lattice Magnetic Form Factor Calculations

- Calculation of the individual quark contributions to the magnetic form factor confirms that it is a  $\bar{K}N$  bound state



Only an  $L=0$   $\bar{K}N$  state gives vanishing strange moment

Hall *et al.*, Phys. Rev. D 95 (2017) 5, 054510

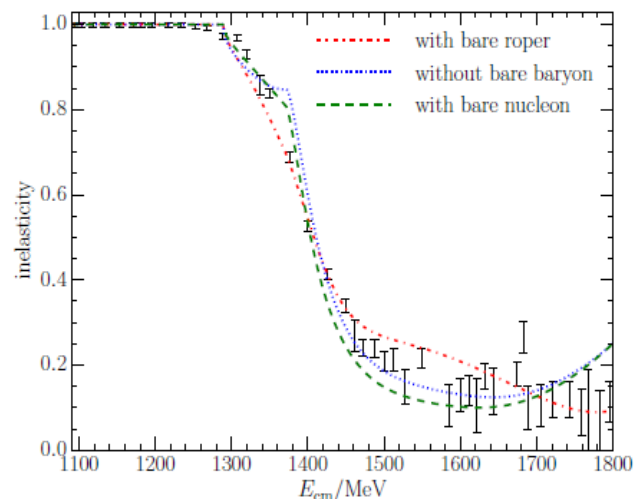
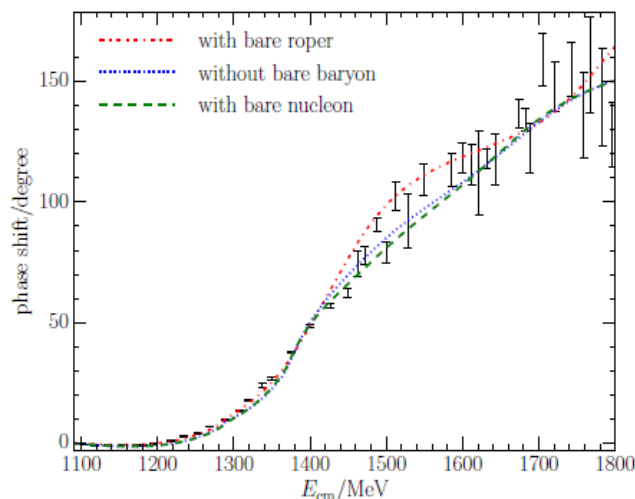
**Note that Lattice QCD allows us  
to study hadron structure IN QCD as a  
function of quark mass – a powerful tool**

# Roper Resonance

Again this has long been a challenge for the quark model, as it is the 1<sup>st</sup> positive parity excited state and lies below the N(1535), the 1<sup>st</sup> negative parity state

Bare Roper Case:  $m_0 = 2.03$  GeV

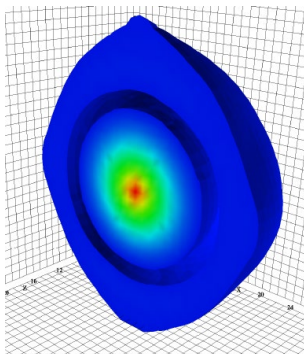
- Consider  $\pi N$ ,  $\pi\Delta$  and  $\sigma N$  channels, dressing a bare state.
- Fit to phase shift and inelasticity



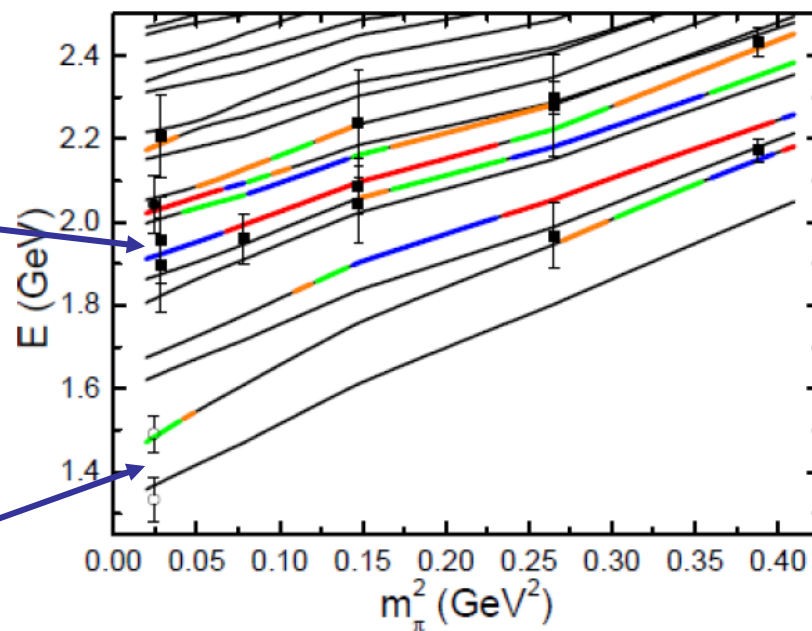
- Fit yields a pole at  $1380 - i87$  MeV.
- Compare PDG estimate  $1365 \pm 15 - i95 \pm 15$  MeV.

# Comparison of HEFT Results with Lattice Energy Levels

- Blue indicates high “bare state” (i.e. 3-quark) content. This matches the lowest state found with a 3-quark interpolating field



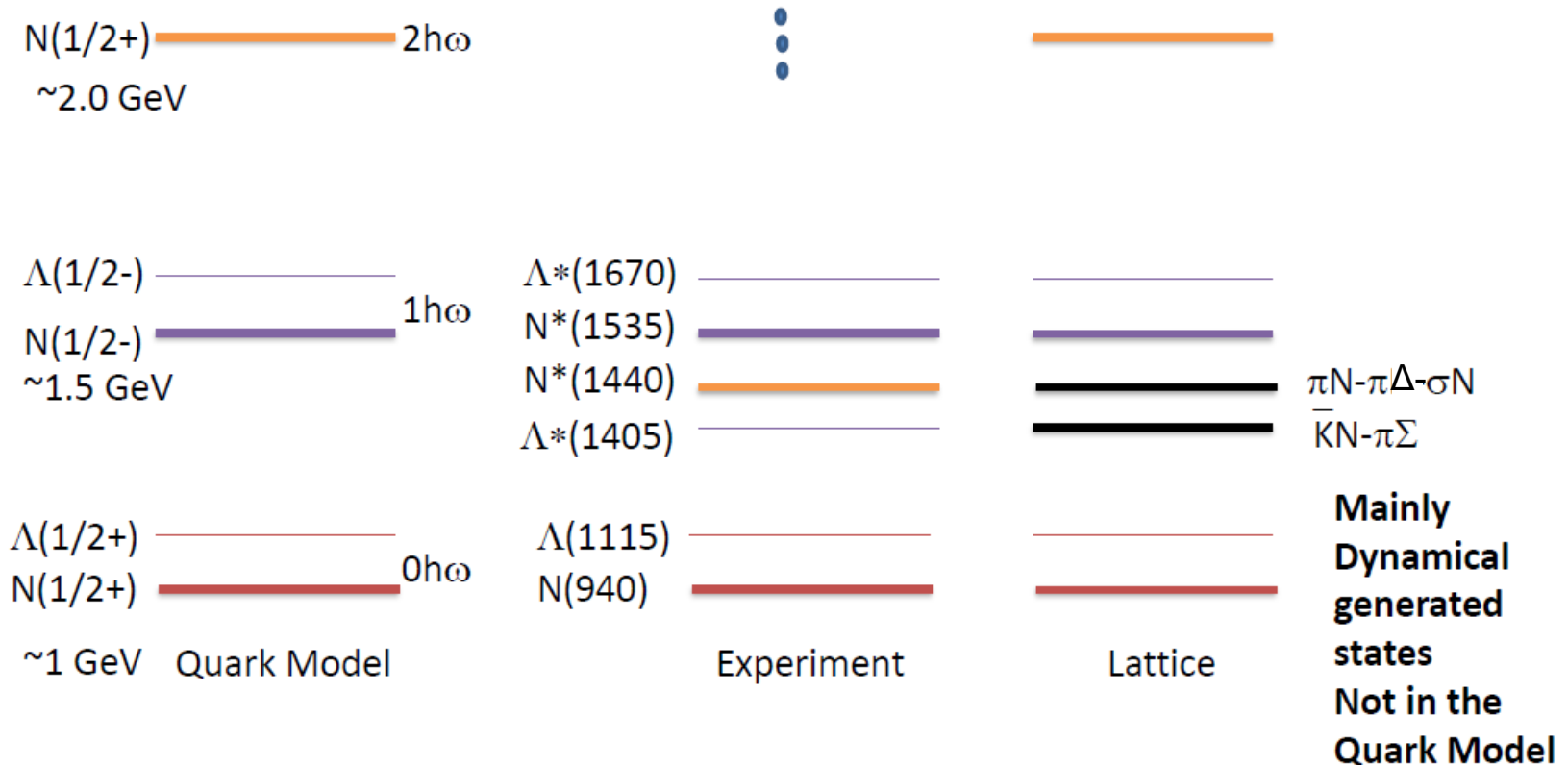
- Lattice calculations of Lang et al., Phys. Rev. D 95, 014510 (2017), using baryon-meson interpolating fields, especially  $N\sigma$
- Matched by Hamiltonian levels but with little or no 3-quark content



The first scenario with a bare state for P11 around the pole at 2.0 GeV can fit both Lattice data and experimental data well, it indicates that  $N^*(1440)$  seems a molecule state, and first radial excitation of nucleon should be around 2.0 GeV.

**Clear conclusion is that the Roper is  
dynamically generated by coupling  
to the  $N\sigma$  and  $\Delta\pi$  channels**

# Once the nature of key states becomes clear the quark model makes sense





# Test $\Lambda(1405)$ Solution in Kaonic Atoms

Using the Hamiltonian discussed earlier (with  $\Lambda(1405)$  a  $\bar{K}$ -N bound state) compare with the kaonic hydrogen binding found by the SIDDHARTA experiment\*

$$\epsilon_{1S}^p = 283 \pm 36(\text{stat}) \pm 6(\text{sys}) \text{ eV},$$

$$\Gamma_{1S}^p = 541 \pm 89(\text{stat}) \pm 22(\text{sys}) \text{ eV}$$

The result is excellent agreement with the calculation:

$$a_{K^-n} = 0.27 + 0.52i \text{ fm}, \quad a_{\bar{K}^0n} = -0.75 + 0.80i \text{ fm},$$

$$a_{\bar{K}^0n \rightarrow K^-p} = 1.02 - 0.28i \text{ fm}.$$

which yields (Liu *et al.*, Phys. Lett. B808 (2020) 135652)

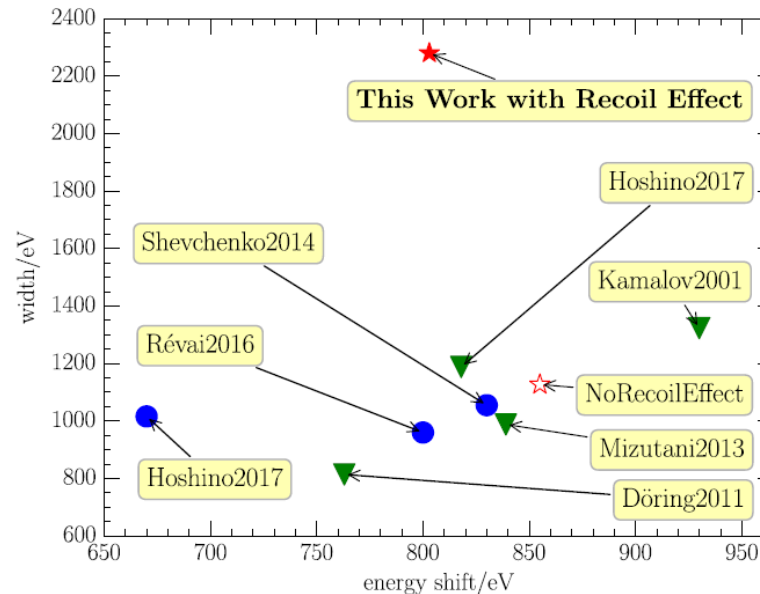
$$\epsilon_{1S}^p = 307 \text{ eV}, \quad \Gamma_{1S}^p = 533 \text{ eV}$$

\* Bazzi *et al.*, Nucl. Phys. A881 (2012) 88

# Kaonic Deuterium

This was also applied to kaonic deuterium using an approximate solution of the Faddeev equations

Result was a surprisingly large width



Z.-W. Liu et al. / *Physics Letters B* 808 (2020) 135652

Result challenged by Barnea and collaborators...  
Await results from experiments of Zmeskal,  
Pochodzalla et al. at J-PARC and Frascati

# A new paradigm for nuclear structure

– what is the atomic nucleus?

# Quark Structure matters/doesn't matter

- Nuclear femtography: the science of mapping the quark and gluon structure of *atomic nuclei* is just beginning
- “Considering quarks is in contrast to our **modern understanding of nuclear physics...** the basic degrees of freedom of QCD (quarks and gluons) have to be considered only at higher energies. The *energies relevant for nuclear physics are only a few MeV*”

# What do we know?

- Since 1970s: Dispersion relations → intermediate range NN attraction is a strong Lorentz scalar
- In relativistic treatments (RHF, RBHF, QHD...) this leads to mean scalar field on a nucleon ~300 to 500 MeV!!

# Just one example of very large scalar mean-fields

1970

R. BROCKMANN AND R. MACHLEIDT

TABLE II. Results of a relativistic Dirac-Brueckner calculation in comparison to the potential  $B$ . As a function of the Fermi momentum  $k_F$ , it is listed: the energy per nucleon vector potentials  $U_S$  and  $U_V$ , and the wound integral  $\kappa$ .

$k_F$ (fm <sup>-1</sup> )	$\mathcal{E}/A$ (MeV)	Relativistic		$U_V$ (MeV)	$\kappa$ (%)
		$\tilde{M}/M$	$U_S$ (MeV)		
0.8	-7.02	0.855	-136.2	104.0	23.1
0.9	-8.58	0.814	-174.2	134.1	18.8
1.0	-10.06	0.774	-212.2	164.2	16.1
1.1	-11.18	0.732	-251.3	195.5	12.7
1.2	-12.35	0.691	-290.4	225.8	11.9
1.3	-13.35	0.646	-332.7	259.3	12.5
1.35	-13.55	0.621	-355.9	278.4	13.0
1.4	-13.53	0.601	-374.3	293.4	13.8
1.5	-12.15	0.559	-413.6	328.4	14.4
1.6	-8.46	0.515	-455.2	371.0	15.8

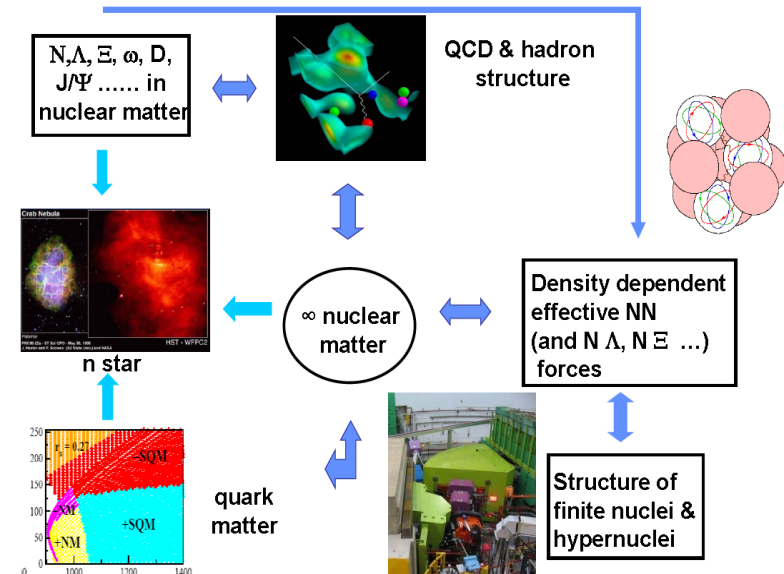
# What do we know?

- Since 1970s: Dispersion relations → intermediate range NN attraction is a strong Lorentz scalar
- In relativistic treatments (RHF, RBHF, QHD...) this leads to mean scalar field on a nucleon  $\sim 300$  to  $500$  MeV!!
- *This is not small* – up to half the nucleon mass
  - death of “wrong energy scale” arguments
- Largely cancelled by large vector mean field BUT these have totally different dynamics:  $\omega^0$  just shifts energies,  $\sigma$  seriously modifies internal hadron dynamics
- Latter cannot be accurately captured by EFT with N and  $\pi$

# Suggests a different approach : QMC Model

(Guichon, Saito, Tsushima et al., Rodionov et al., Stone  
- see Saito *et al.*, Prog. Part. Nucl. Phys. 58 (2007) 1 and  
Guichon *et al.*, Prog. Part. Nucl. Phys. 100 (2018) 262-297 for reviews)

- Start with quark model (MIT bag/NJL...) for all hadrons
- Introduce a relativistic Lagrangian with  $\sigma$ ,  $\omega$  and  $\rho$  mesons coupling to non-strange quarks
- Hence, initially only 4 parameters  
 $(m_\sigma, g^{\sigma, \omega, \rho}_q)$ 
  - determine by fitting to:  
 $\rho_0$ ,  $E/A$  and symmetry energy
  - same in dense matter & finite nuclei
- Must solve self-consistently for the internal structure of baryons in-medium  $\equiv$  3-body forces with NO new parameters





# Application to nuclear structure

# QMC $\pi 3$

- **Just 5 parameters\***:  $m_\sigma$ , quark couplings to  $\sigma$ ,  $\omega$  and  $\rho$  and  $\lambda_3$  - the strength of  $\sigma^3$  term

- Tensor term included: 
$$H_{\sigma,\omega,\rho}^J = \left( \frac{G_\sigma (1 - dv_0)^2}{4m_\sigma^2} - \frac{G_\omega}{4m_\omega^2} \right) \sum_m \vec{J}_m^2 - \frac{G_\rho}{4m_\rho^2} \sum_{m,m'} S_{m,m'} \vec{J}_m \cdot \vec{J}_{m'},$$

and 
$$H_S^J = -\frac{G_\sigma - G_\omega}{16M^2} \sum_m \vec{J}_m^2 + \frac{G_\rho}{16M^2} \sum_{mm'} S_{m,m'} \vec{J}_m \cdot \vec{J}_{m'}.$$

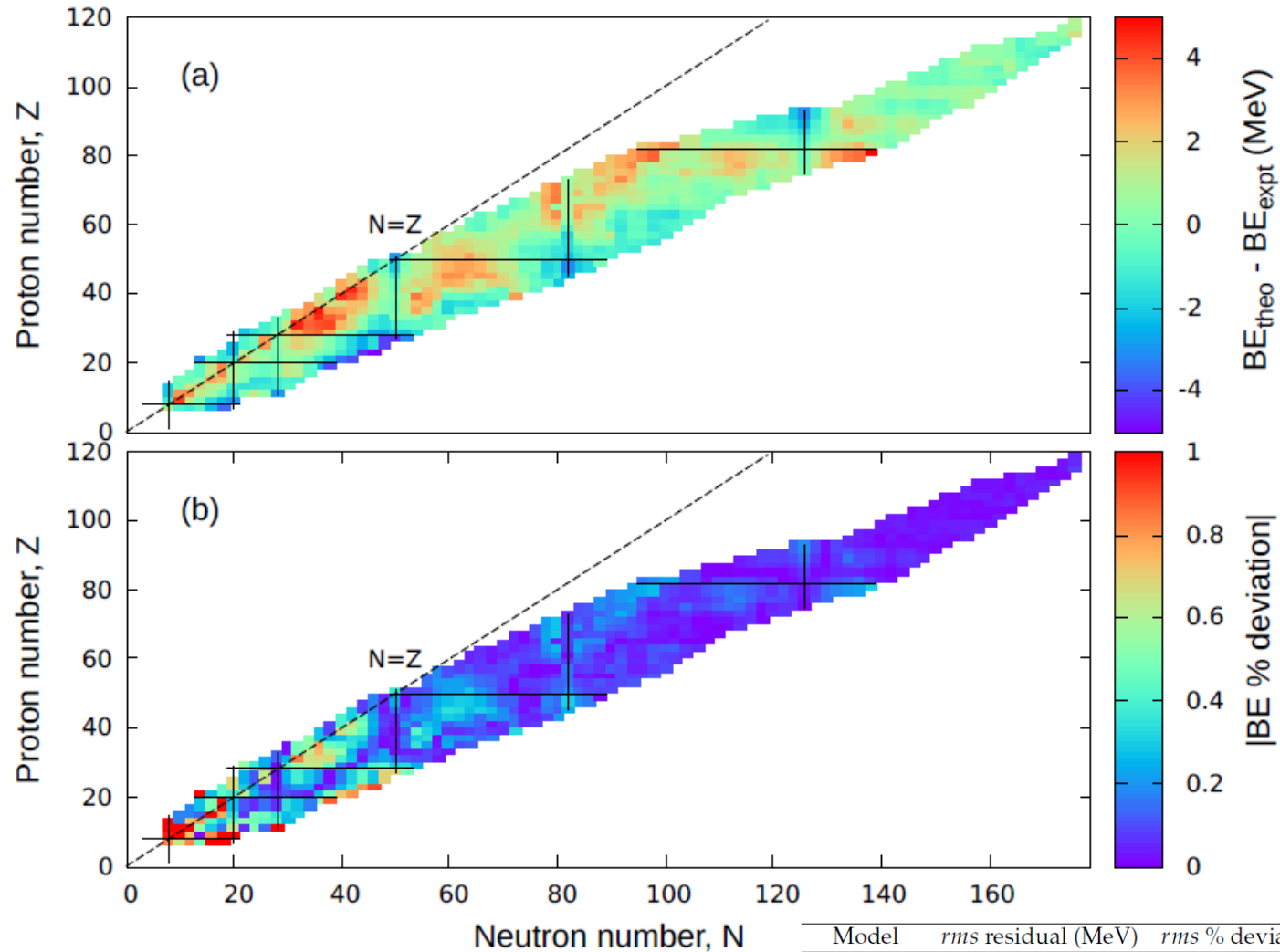
with 
$$\vec{J}_m = i \sum_{i \in F_m} \sum_{\sigma\sigma'} \vec{\sigma}_{\sigma'\sigma} \times [\vec{\nabla} \phi^i(\vec{r}, \sigma, m)] \phi^{i*}(\vec{r}, \sigma', m), \quad \vec{J} = \vec{J}_p + \vec{J}_n,$$

- Pairing interaction (simple BCS) derived in the model

$$V_{\text{pair}}^{\text{QMC}} = - \left( \frac{G_\sigma}{1 + d' G_\sigma \rho(\vec{r})} - G_\omega - \frac{G_\rho}{4} \right) \delta(\vec{r} - \vec{r}')$$

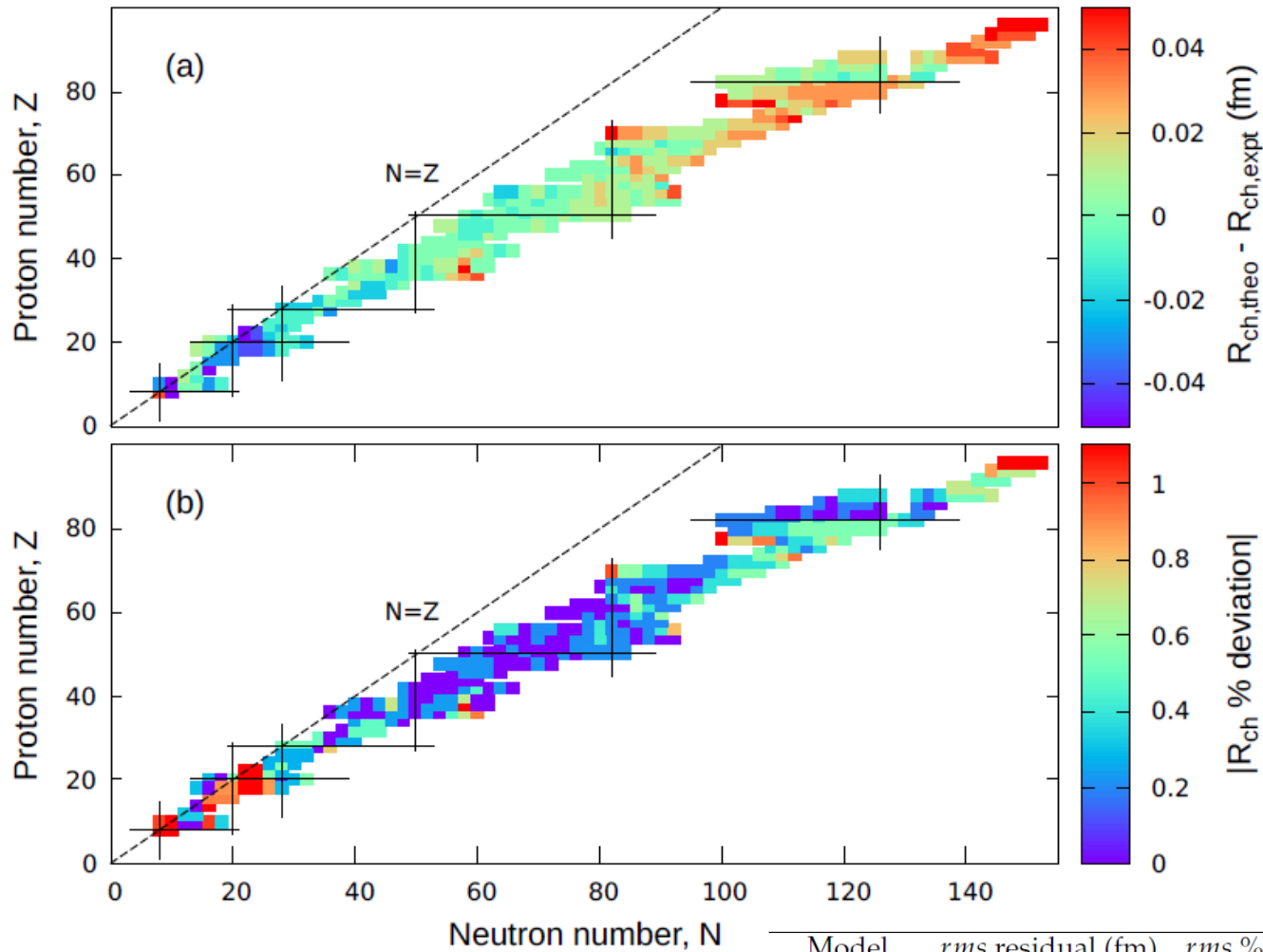
\* cf. Over 20 in FRDM and typically 16 (11+5) in Skyrme forces

# Binding Energies – All Known Even-Even Nuclei



Model	$rms$ residual (MeV)	$rms$ % deviation
QMC $\pi$ -III	1.59	0.29
QMC $\pi$ -II	2.34	0.39
QMC $\pi$ -I	2.78	0.50
QMC-I	3.84	0.69
SV-min	3.64	0.38
UNEDF1	2.06	0.55
DD-ME $\delta$	2.41	0.42
FRDM	0.89	0.18

# Charge Radii



Model	$rms$ residual (fm)	$rms$ % deviation
QMC $\pi$ -III	0.024	0.50
QMC $\pi$ -II	0.029	0.66
QMC $\pi$ -I	0.028	0.65
QMC-I	0.030	0.66
SV-min	0.024	0.61
UNEDF1	0.029	0.65
DD-ME $\delta$	0.035	0.78

# Separation energies: Drip Lines

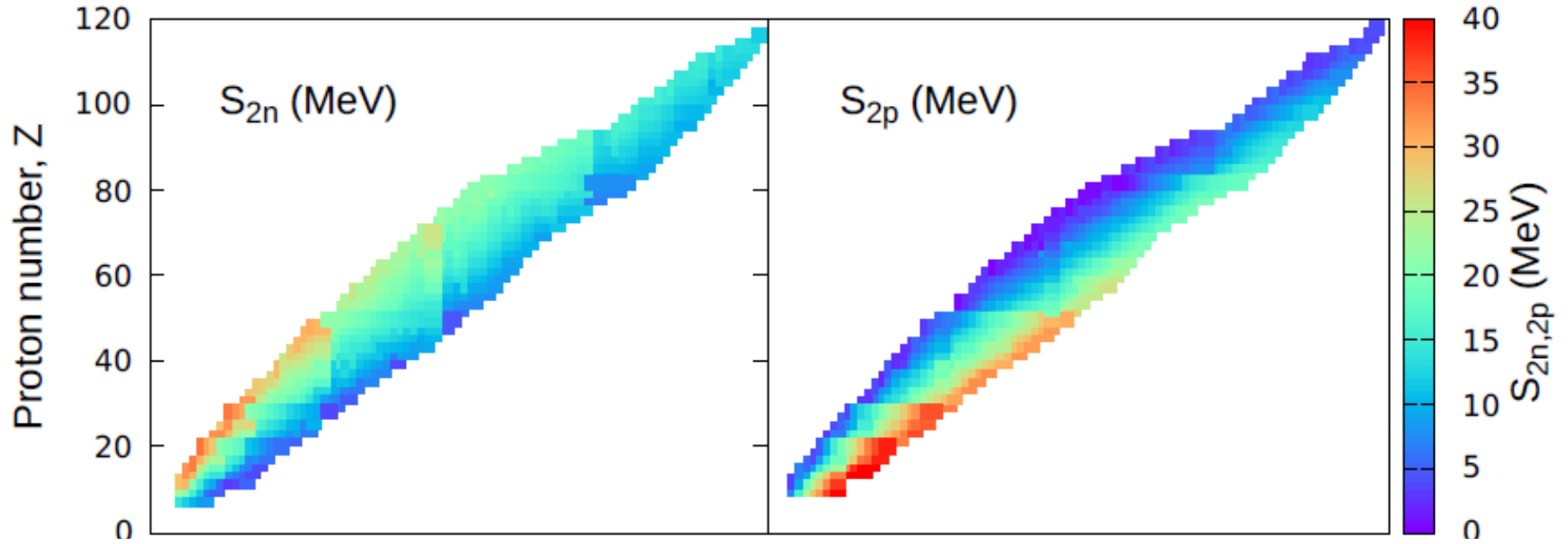


TABLE 7.3: Comparison of *rms* residuals for separation energies (in MeV) from QMC and from other nuclear models.

Model	$S_{2n}$	$S_{2p}$	$\delta_{2n}$	$\delta_{2p}$	$Q_\alpha$
QMC $\pi$ -III	0.97	0.95	1.24	1.28	1.07
QMC $\pi$ -II	1.03	1.08	1.20	1.25	1.19
SV-min	0.77	0.82	0.87	1.00	0.79
UNEDF1	0.74	0.82	0.85	0.90	0.80
DD-ME $\delta$	1.01	1.05	1.12	1.11	1.30
FRDM	0.50	0.55	0.61	0.75	0.61

# Deformation

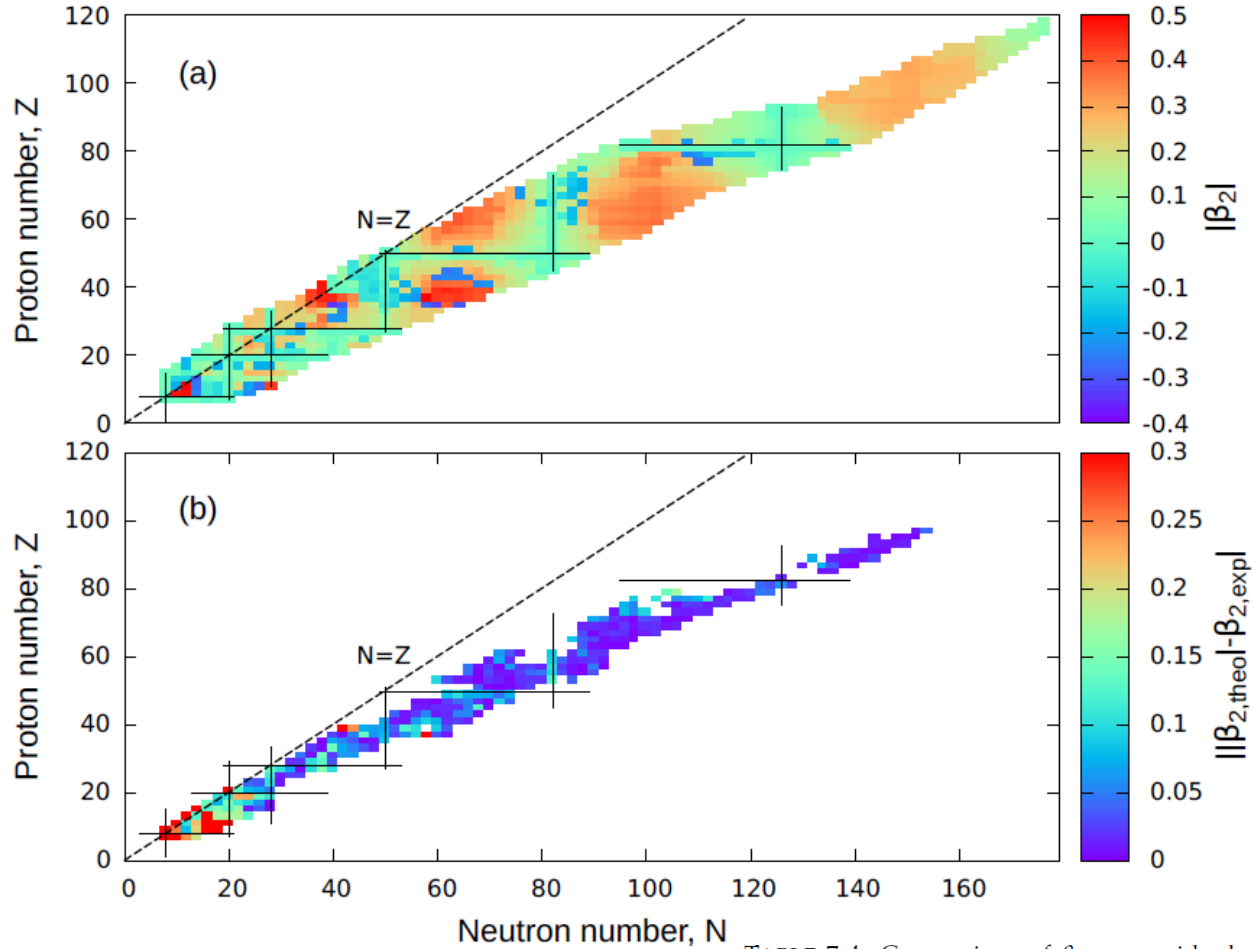


TABLE 7.4: Comparison of  $\beta_2$  *rms* residuals and *rms* % deviations from QMC $\pi$ -III and from other nuclear models. There are a total of 324 even-even nuclei with available data for  $\beta_2$  included for comparison.

Model	<i>rms</i> residual	<i>rms</i> % deviation
QMC $\pi$ -III	0.11	28
SV-min	0.16	59
UNEDF1	0.15	53
DD-ME $\delta$	0.14	40
FRDM	0.11	30

# The Superheavy Region

## First study:

PHYSICAL REVIEW C **100**, 044302 (2019)

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**Physics of even-even superheavy nuclei with  $96 < Z < 110$  in the quark-meson-coupling model**

J. R. Stone\*

*Department of Physics (Astro), University of Oxford, Keble Road OX1 3RH, Oxford, United Kingdom  
and Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA*

K. Morita†

*Department of Physics, Kyushu University, Nishi-ku, Fukuoka 819-0395, Japan  
and RIKEN Nishina Center, RIKEN, Wako-shi, Saitama 351-0198, Japan*

P. A. M. Guichon‡

*CEA/IRFU/SPhN Saclay, F91191, France*

A. W. Thomas§

*CSSM and CoEPP, Department of Physics, University of Adelaide, SA 5005, Australia*

**Updated and expanded here (Martinez *et al.*, to be published)**

# Binding Energies

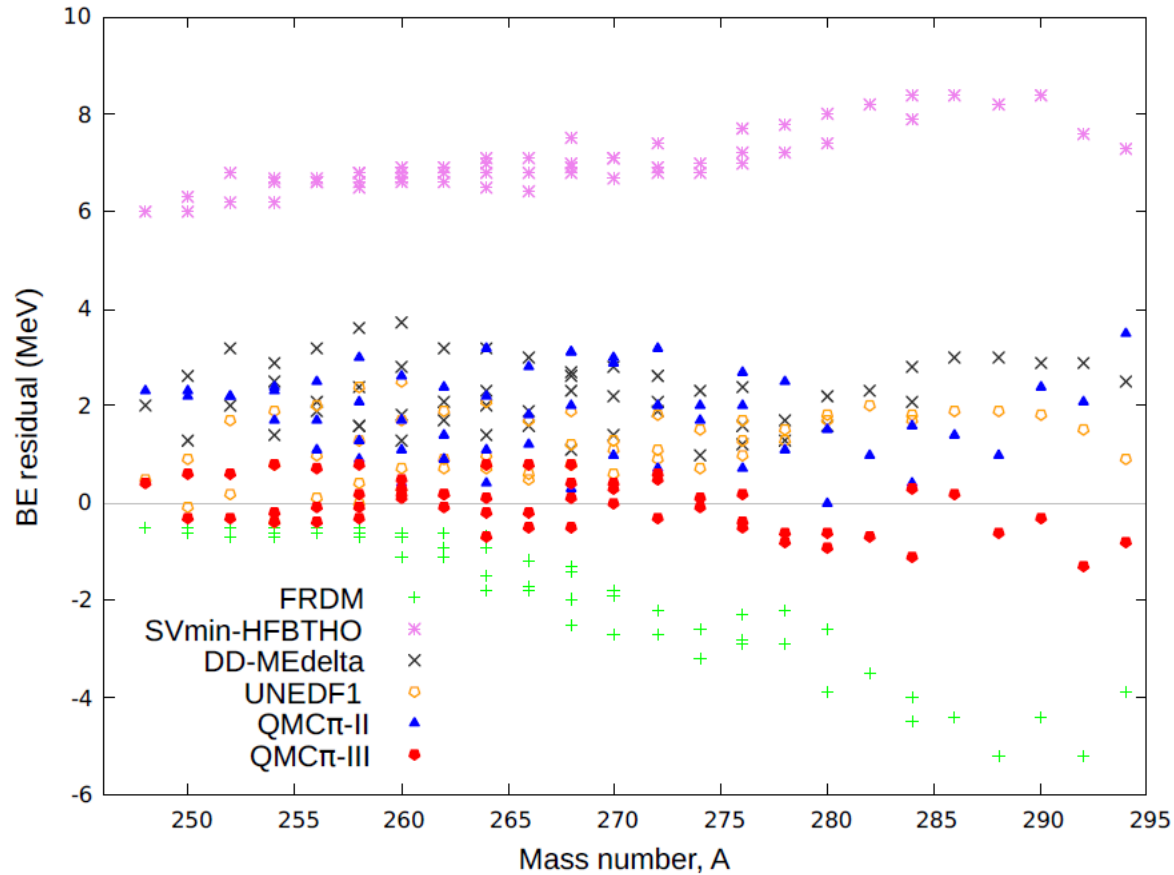


TABLE 6.1: Comparison of *rms* percent deviations and *rms* residuals from QMC and from other nuclear models for SHE with available data.

	<i>rms</i> % deviation	<i>rms</i> residual (MeV)
QMC $\pi$ -III	0.03	0.52
QMC $\pi$ -II [54]	0.11	2.04
QMC $\pi$ -I [53]	0.12	2.42
QMC-I [8]	0.08	1.50
FRDM [23]	0.11	2.25
SV-min [24]	0.36	6.99
UNEDF1 [28]	0.07	1.31
DD-ME $\delta$ [66]	0.12	2.28

Outstanding agreement



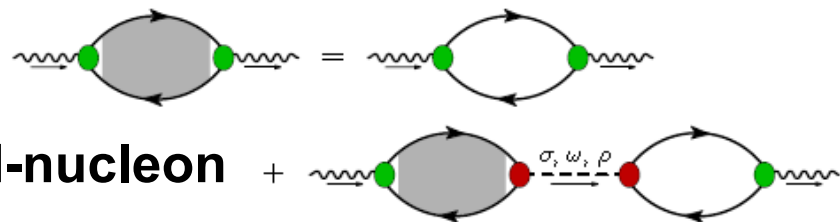
# Summary: Finite Nuclei

- The effective force was *derived* at the quark level *based upon the changing structure of a bound nucleon*
- Has many less parameters but reproduces nuclear properties at a level comparable with the best phenomenological Skyrme forces
- Looks like standard nuclear force
- BUT underlying theory also predicts modified internal structure and hence modified
  - DIS structure functions
  - elastic form factors.....

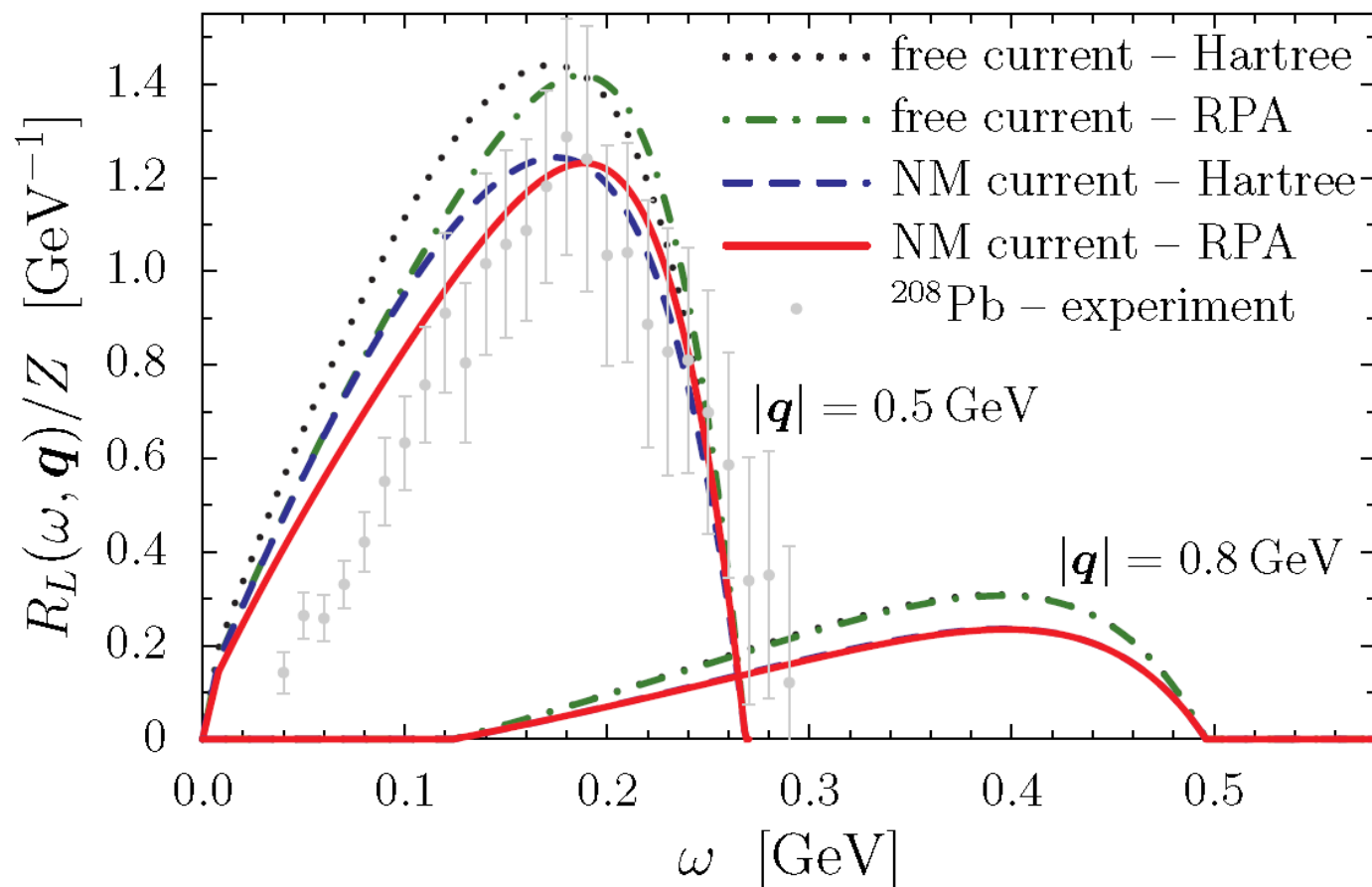
# Modified Electromagnetic Form Factors In-Medium

# Response Function

$$\frac{d^2\sigma}{d\Omega d\omega} = \sigma_{\text{Mott}} \left[ \frac{q^4}{|q|^4} R_L(\omega, |q|) + \left( \frac{q^2}{2|q|^2} + \tan^2 \frac{\theta}{2} \right) R_T(\omega, |q|) \right]$$

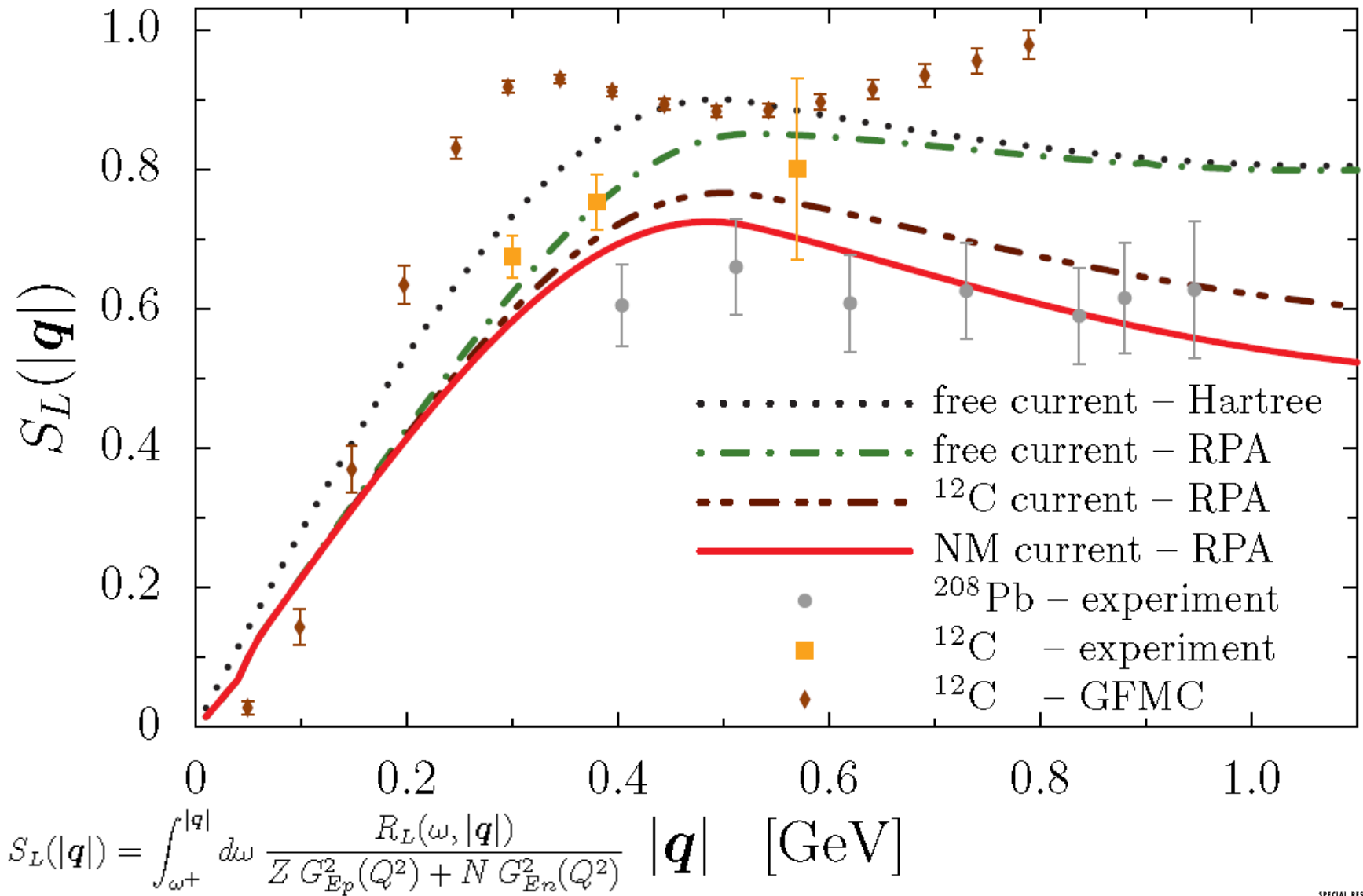


**RPA correlations repulsive**  
**Significant reduction in Response**  
**Function from the modification of bound-nucleon**



**Cloët, Bentz & Thomas, PRL 116 (2016) 032701**

# Comparison with Unmodified Nucleon & Data



**Data: Morgenstern & Meziani**

**Calculations: Cloët, Bentz & Thomas (PRL 116 (2016) 032701)**

# Summary

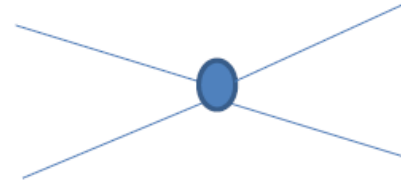
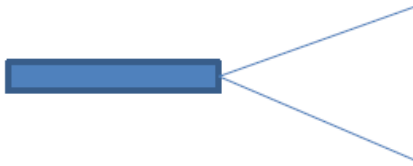
- **New techniques applied to lattice QCD provide hitherto unimagined insights into hadron structure**
- **The quark model has new life**
- **Exotic atoms, e.g. Kbar and hyperon, provide valuable information**
- **There is much more to nuclear structure than EFT can give (powerful though it is)**
- **Hadron structure changes in nuclear matter: leading to a new paradigm for nuclear structure**
- **Experimental tests underway**



# N(1535) is a 3-quark state

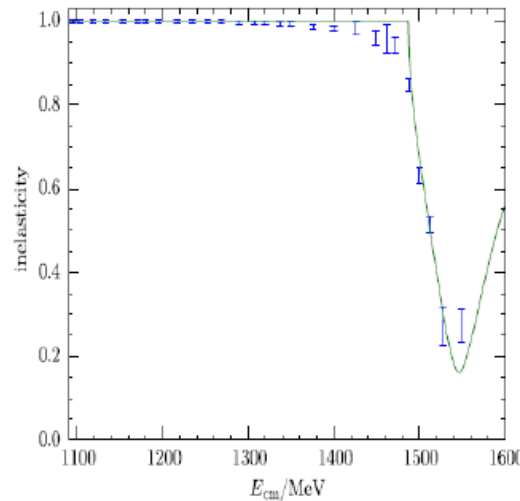
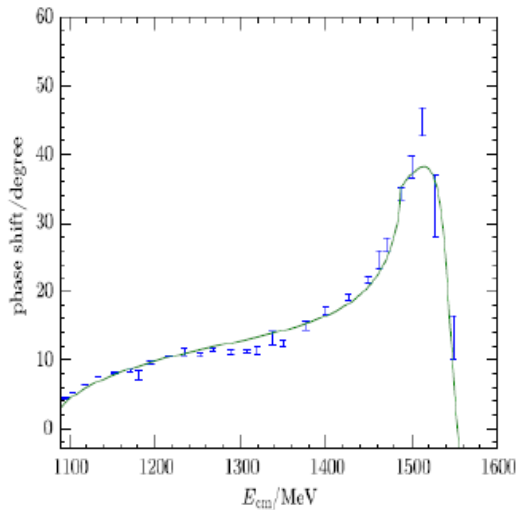
Zhan-wei Liu et al. Phys.Rev.Lett. 116 (2016) no.8, 082004

- 2 Channels:  $\pi N$  and  $\eta N$



$$G_{iN}^2(k) = \left( 3g_{N_0^*iN}^2 / 4\pi^2 f^2 \right) \omega_i(k) u^2(k)$$

$$\frac{3g_{\pi N}^S \tilde{u}(k) \tilde{u}(k')}{4\pi^2 f^2}$$



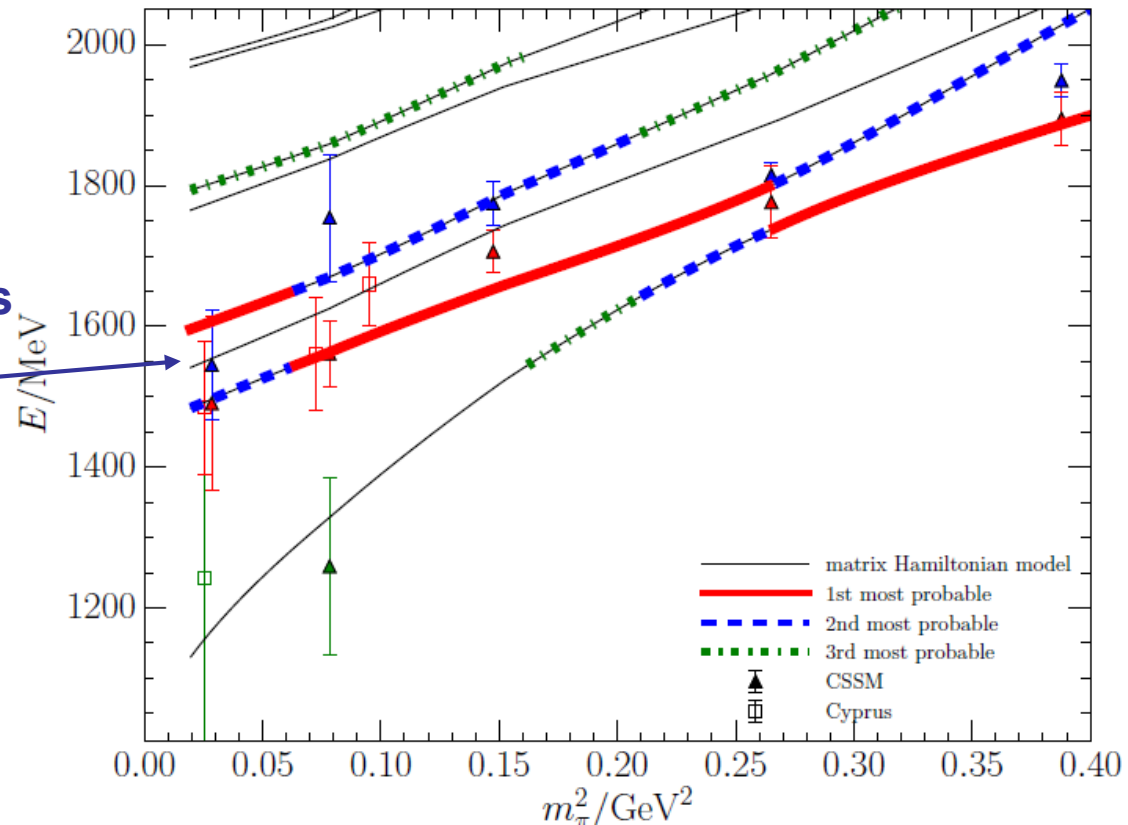
$$\begin{aligned} g_{\pi N}^S &= -0.0608 \pm 0.0004 \\ m_0 &= 1601 \pm 14 \text{ MeV} \\ g_{N_0^* \pi N} &= 0.186 \pm 0.006 \\ g_{N_0^* \eta N} &= 0.185 \pm 0.017, \\ \chi_{\text{DOF}}^2 &= 6.8 \\ 1531 \pm 29 - i88 \pm 2 \text{ MeV} \end{aligned}$$

Liu et al., PRL 116 (2016) 082004

# N(1535) is a 3-quark state

## Hamiltonian Model $N^*$ Spectrum: 3 fm

Hamiltonian eigenstates dominated by 3-quark state match the lattice result with 3-quark interpolating field



Liu *et al.*, PRL 116 (2016) 082004



# Special Mentions.....



**Guichon**



**Tsushima**



**Saito**



**Stone**



**Krein**



**Matevosyan**



**Cloët**



**Whittenbury**



**Simenel**



**Bentz**



**Martinez**



**Motta**



**Antic**



**Kalaitzis**

# Latest papers

- **QMC  $\pi^3$ ;**  
**Martinez et al., Phys Rev C102 (2020) 034304**
- **Review:**  
**Guichon et al., PPNP 100 (2018) 262**
- **SHE:**  
**Stone et al., arXiv: 1901.06064**
- **Systematic application to finite nuclei:**  
**Stone et al., Phys Rev Lett 116 (2016) 092501**

# Key papers on QMC

- **Many-body forces:**

1. Guichon, Matevosyan, Sandulescu, Thomas, Nucl. Phys. A772 (2006) 1.
2. Guichon and Thomas, Phys. Rev. Lett. 93 (2004) 132502

- **Built on earlier work on QMC: e.g.**

3. Guichon, Phys. Lett. B200 (1988) 235
4. Guichon, Saito, Rodionov, Thomas, Nucl. Phys. A601 (1996) 349

- **Major review of applications of QMC to many nuclear systems:**

5. Saito, Tsushima, Thomas, Prog. Part. Nucl. Phys. 58 (2007) 1-167 (hep-ph/0506314)
6. Guichon et al., Prog. Part. Nucl. Phys. 100 (2018) 262

# References to: Covariant Version of QMC

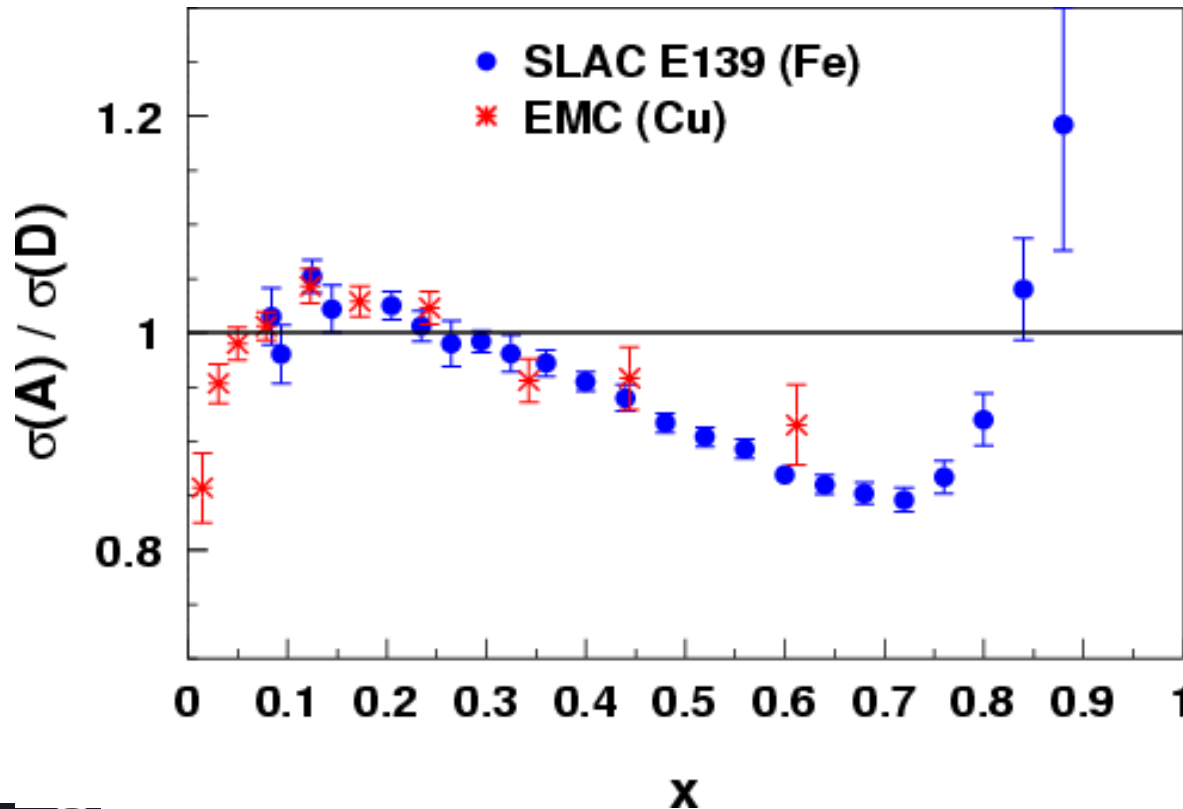
- **Basic Model: (Covariant, chiral, confining version of NJL)**
- **Bentz & Thomas, Nucl. Phys. A696 (2001) 138**
- **Bentz, Horikawa, Ishii, Thomas, Nucl. Phys. A720 (2003) 95**
- **Applications to DIS:**
- **Cloet, Bentz, Thomas, Phys. Rev. Lett. 95 (2005) 052302**
- **Cloet, Bentz, Thomas, Phys. Lett. B642 (2006) 210**
- **Applications to neutron stars – including SQM:**
- **Lawley, Bentz, Thomas, Phys. Lett. B632 (2006) 495**
- **Lawley, Bentz, Thomas, J. Phys. G32 (2006) 667**

# Nuclear DIS Structure Functions: The EMC Effect

To address questions like this one **MUST** start  
with a theory that quantitatively describes  
nuclear structure and allows calculation of  
structure functions  
– very, very few examples.....

# The EMC Effect: Nuclear PDFs

- Observation stunned and electrified the HEP and Nuclear communities 37 years ago
- What is it that alters the quark momentum in the nucleus?



J. Ashman *et al.*, Z. Phys. C57, 211 (1993)

J. Gomez *et al.*, Phys. Rev. D49, 4348 (1994)

# Theoretical Understanding

- Still numerous proposals but few consistent theories
- Initial studies used MIT bag<sup>1</sup> to estimate effect of self-consistent change of structure in-medium  
– but better to use a covariant theory
- For that Bentz and Thomas<sup>2</sup> re-derived change of nucleon structure in-medium in the NJL model
- This set the framework for sophisticated studies by Bentz, Cloët and collaborators over the last decade

<sup>1</sup> Thomas, Michels, Schreiber and Guichon, Phys. Lett. B233 (1989) 43

<sup>2</sup> Bentz and Thomas, Nucl. Phys. A696 (2001) 138

# EMC Effect for Finite Nuclei

(There is also a spin dependent EMC effect - as large as unpolarized)

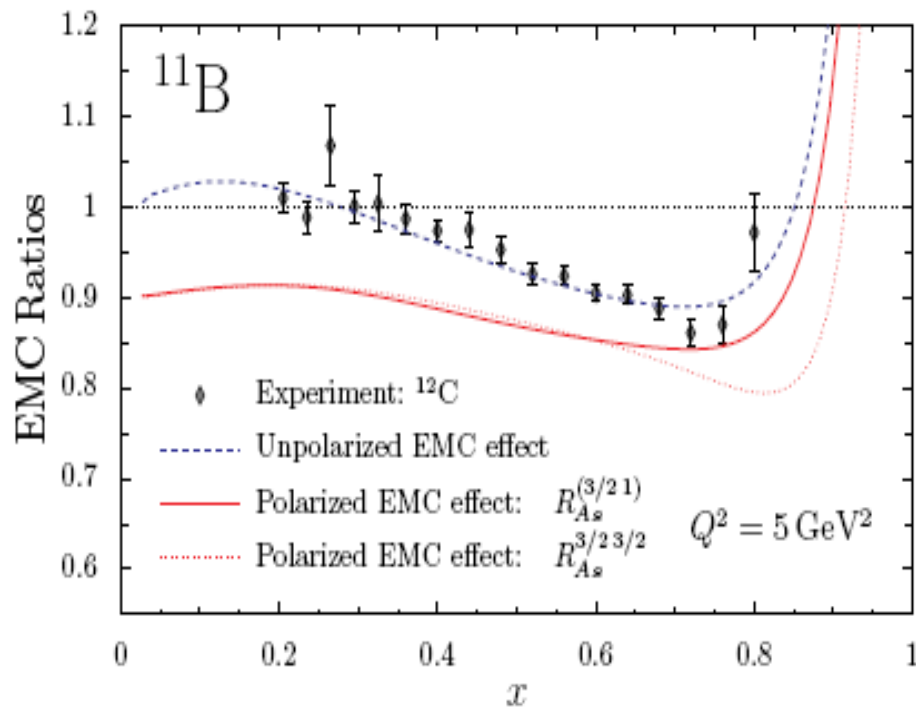


FIG. 7: The EMC and polarized EMC effect in  $^{11}\text{B}$ . The empirical data is from Ref. [31].

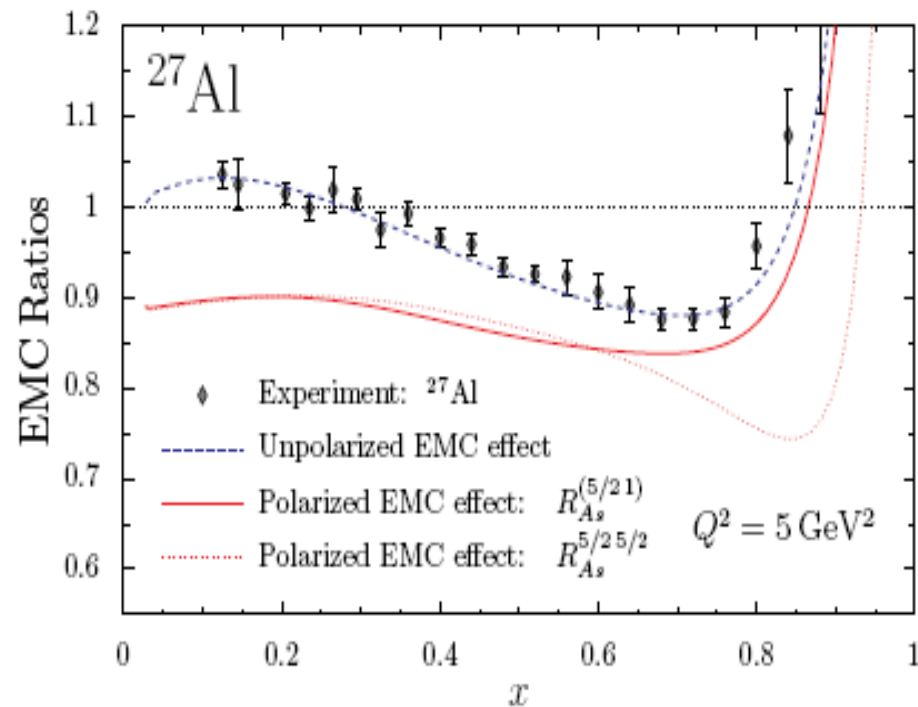
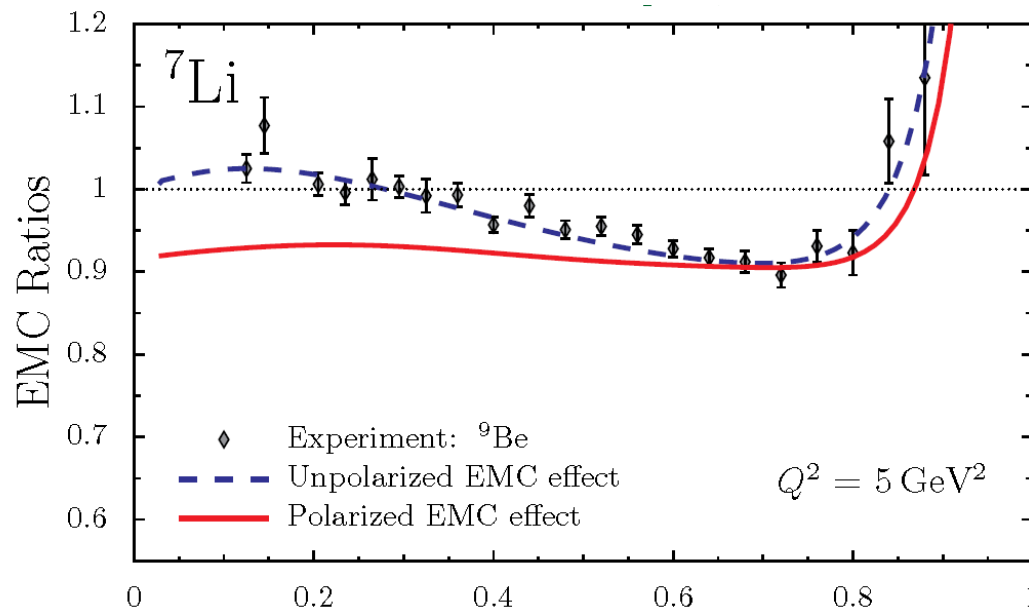


FIG. 9: The EMC and polarized EMC effect in  $^{27}\text{Al}$ . The empirical data is from Ref. [31].



# Approved JLab Experiment

- Effect in  ${}^7\text{Li}$  is slightly suppressed because it is a light nucleus and proton does not carry all the spin (simple WF:  $P_p = 13/15$  &  $P_n = 2/15$ )
- Experiment now approved at JLab [E12-14-001] to measure spin structure functions of  ${}^7\text{Li}$  (GFMC:  $P_p = 0.86$  &  $P_n = 0.04$ )



**Spin EMC measurement is critical as the proposed explanation in terms of SRC through the tensor force gives NO spin EMC effect (arXiv:1809.06622)**

