

# Recent progress in many-body models based on the covariant DFT

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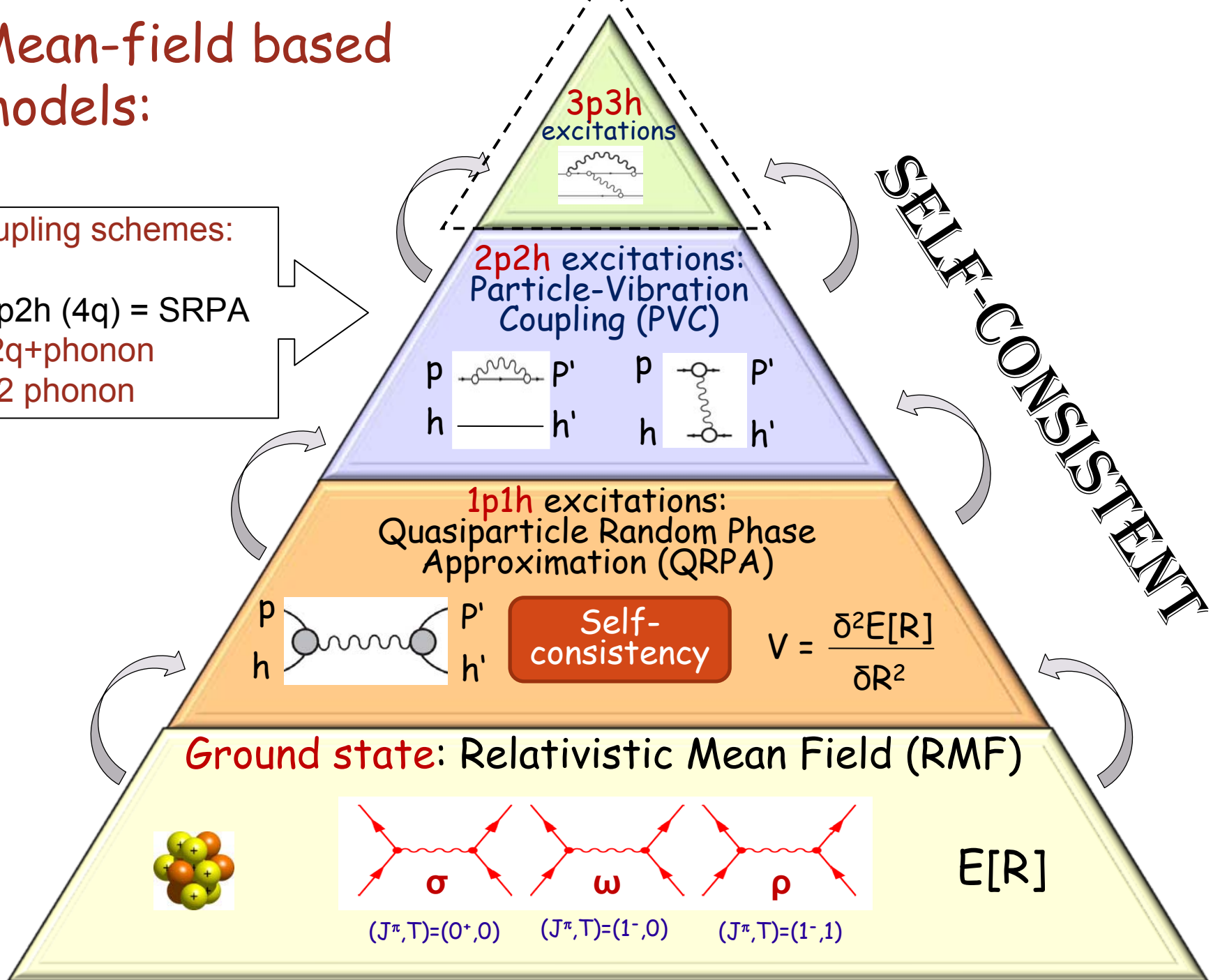
# OUTLINE

- ❖ Introduction
- ❖ Theory:
  - Relativistic mean field (RMF) model
  - Relativistic quasiparticle random phase approximation (RQRPA)
  - Quasiparticle time blocking approximation (QTBA)
  - Particle-vibration coupling (PVC) model
  - Mode-coupling model
- ❖ Applications:
  - Nuclear single-particle structure
  - Nuclear low-energy response
- ❖ Conclusions and outlook

# Mean-field based models:

## Coupling schemes:

- I. 2p2h (4q) = SRPA
- II. 2q+phonon
- III. 2 phonon



# Relativistic mean field

$$E_{RMF}[\hat{\rho}, \phi] = Tr[(\boldsymbol{\alpha}\mathbf{p} + \beta m)\hat{\rho}] + \sum_m \left\{ Tr[(\beta\Gamma_m\phi_m)\hat{\rho}] \mp \int \left[ \frac{1}{2}(\nabla\phi_m)^2 + U(\phi_m) \right] d^3r \right\}$$

$$\begin{cases} \mathcal{H}_{RHB}|\psi_k^\eta\rangle = \eta E_k|\psi_k^\eta\rangle, & \eta = \pm 1 \\ -\Delta\phi_m(\mathbf{r}) + U'(\phi_m(\mathbf{r})) = \mp \sum_k V_k^\dagger(\mathbf{r})\beta\Gamma_m V_k^*(\mathbf{r}) \end{cases}$$

← Nucleons  
← Mesons

no sea

RHB  
Hamiltonian

$$\hat{\mathcal{H}}_{RHB} = \frac{\delta E_{RHB}}{\delta \mathcal{R}} = \begin{pmatrix} h^{\mathcal{D}} - m - \lambda & \Delta \\ -\Delta^* & -h^{\mathcal{D}*} + m + \lambda \end{pmatrix}$$

Dirac  
Hamiltonian

$$h^{\mathcal{D}} = \boldsymbol{\alpha}\mathbf{p} + \beta(m + \sum_m \Gamma_m\phi_m(\mathbf{r}))$$

$\tilde{\Sigma}(\mathbf{r})$

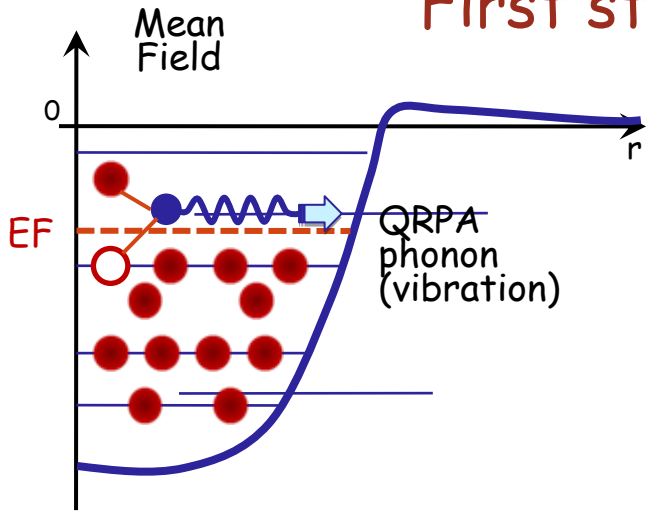
RMF  
self-  
energy

$$|\psi_k^+(\mathbf{r})\rangle = \begin{pmatrix} U_k(\mathbf{r}) \\ V_k(\mathbf{r}) \end{pmatrix}$$

Eigenstates

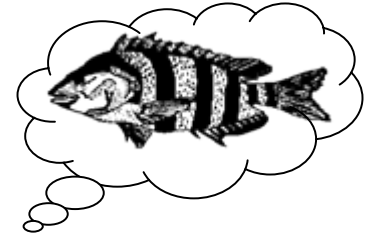
$$|\psi_k^-(\mathbf{r})\rangle = \begin{pmatrix} V_k^*(\mathbf{r}) \\ U_k^*(\mathbf{r}) \end{pmatrix}$$

# First step beyond relativistic mean field:



Coupling to vibrations

First order coupling:  
self-energy diagram "fish"



$$\Sigma^e = \text{fish diagram}$$

The diagram shows a horizontal line with two vertices. A wavy line (phonon) connects the two vertices, forming a loop. The vertices are labeled p and p'.

One-body propagation:

$$p_1 \text{---} p_2 = p_1 \text{---} p_2 + p_1 \text{---} p \text{---} \Sigma^e \text{---} p' \text{---} p_2$$

The diagram shows a Dyson equation for the one-body propagator. It starts with a solid line from p1 to p2, which is equal to the sum of a direct solid line from p1 to p2 and a term involving a solid line from p1 to p, a blue circle representing the self-energy Σ^e, and a solid line from p' to p2.

(Dyson equation)

p

h

$$\Sigma_{p'p''}^e = \text{diagrams}$$

$$\Sigma_{h'h''}^e = \text{diagrams}$$

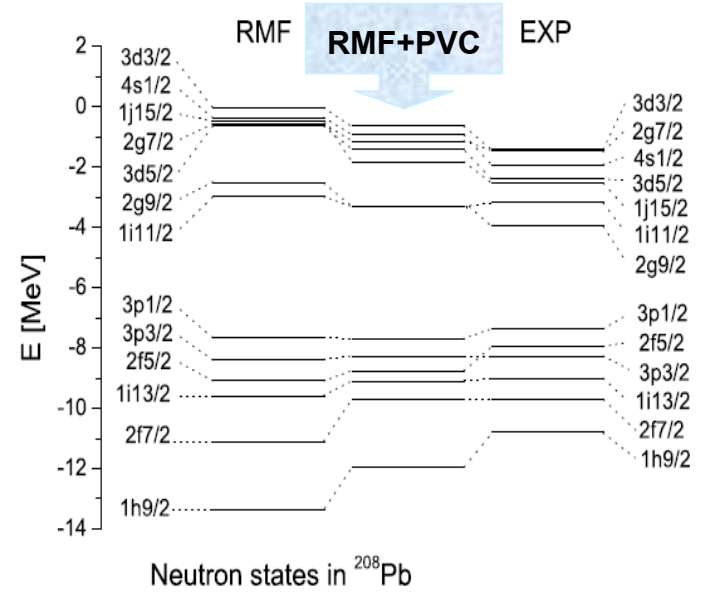
Time's arrow ----->

Detailed description: This block contains two sets of self-energy diagrams. The top set is for a proton (p) and the bottom set is for a hole (h). Each set shows three diagrams representing different interaction channels (μ, α, h). A red dashed arrow at the bottom indicates the direction of time.

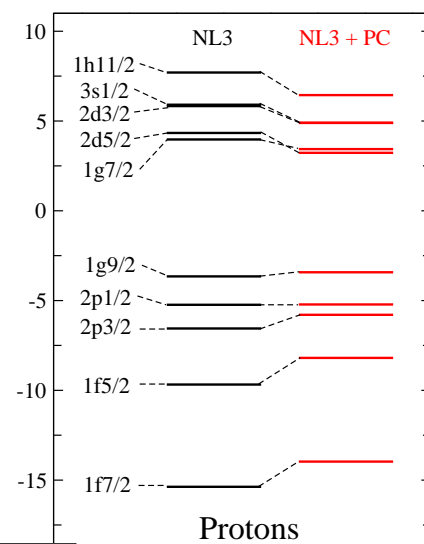
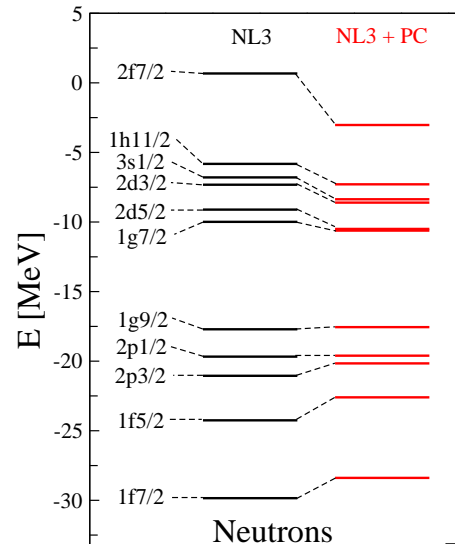
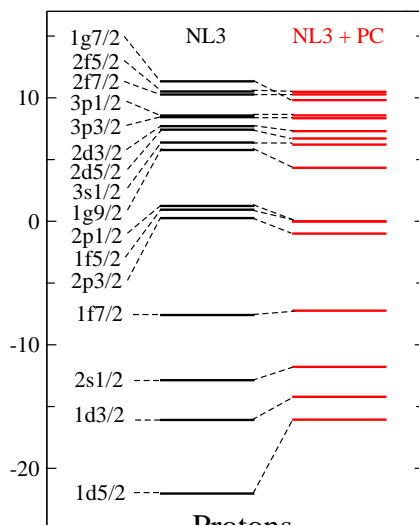
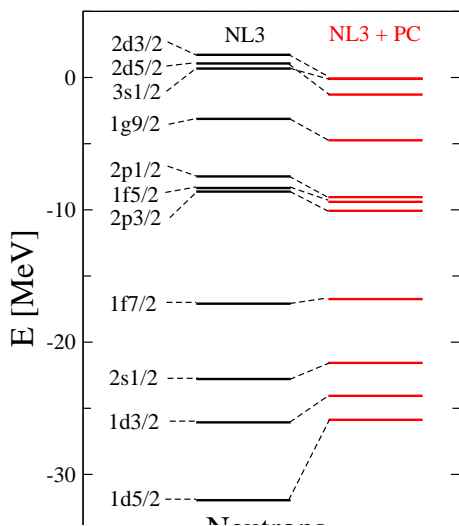
Splitting and shift of single-quasiparticle levels  
& distribution of single-particle strength  
» spectroscopic factors

Not complete: pairing vibrations  
have to be studied!

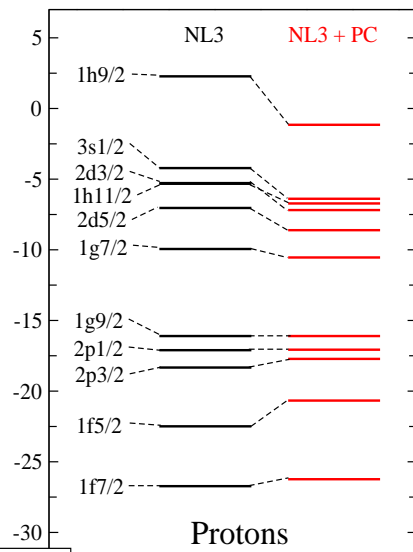
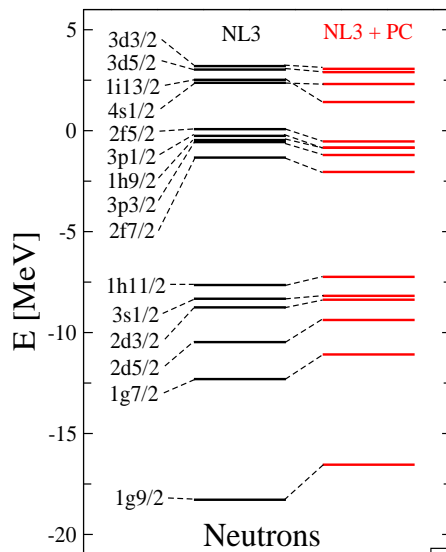
E. L., P. Ring,  
PRC 73, 044328 (2006)



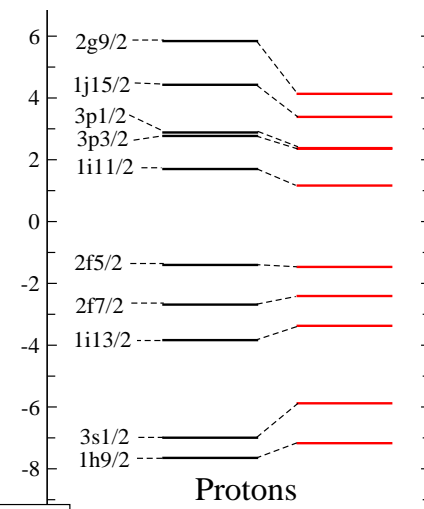
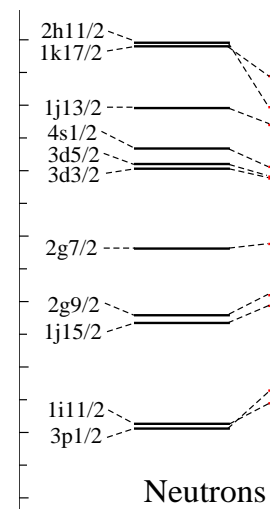
# Single-particle spectra of doubly-magic nuclei



$^{100}\text{Sn}$



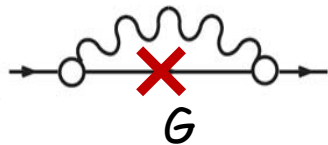



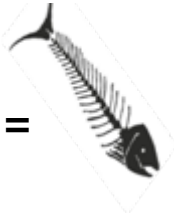
$^{132}\text{Sn}$



$^{292}_{120}\text{Sn}$

# Nuclear response function

Functional derivative  
of the nucleon  
self-energy

$i \frac{\delta}{\delta G}$   =  $i \frac{\delta \Sigma^e}{\delta G}$  =   
 $i \frac{\delta}{\delta G}$   =  = 

Nuclear response function  $R$ :  
two-body propagation  
in the nuclear medium

Bethe-Salpeter equation  
(BSE) in the p-h channel

2p2h:  
Energy-  
dependent

1p1h:  
static

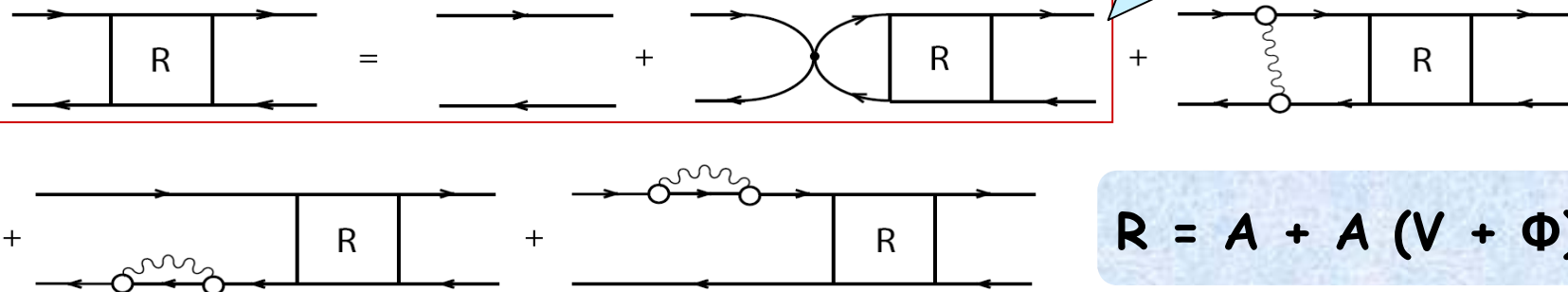
$$U^e = i \frac{\delta \Sigma^e}{\delta G}$$

$$V = \frac{\delta \Sigma}{\delta \rho}$$

Bethe-Salpeter equation  
is solved in the  
particle-hole (1p1h) basis:  
all the job on complex  
configurations is done by  
intermediate summations.

NO huge matrices!

QRPA

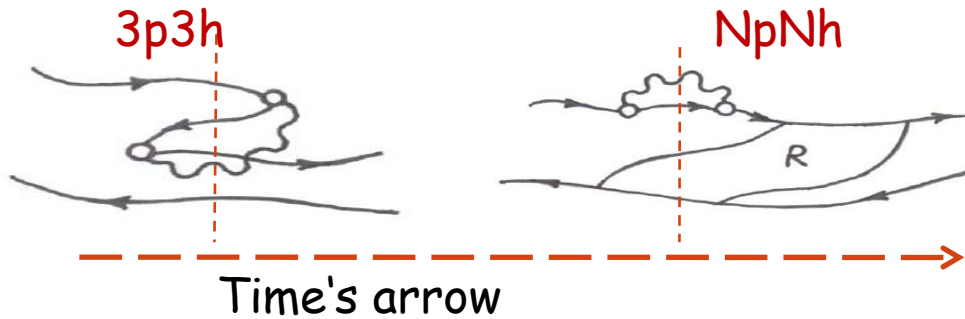
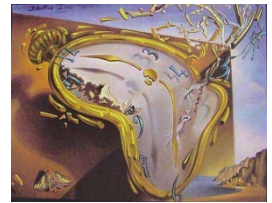


$$R = A + A (V + \Phi) R$$



# Time blocking\*

**Problem:**  
'Melting' diagrams



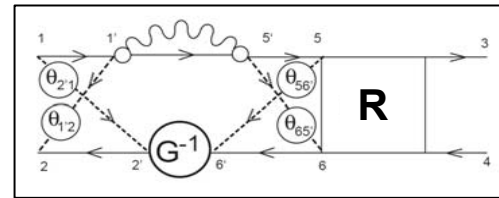
**Unphysical result:**  
negative cross sections

**Solution:**

Time-projection operator:

$$\delta_{\sigma_1 - \sigma_2} \theta(\sigma_1 t_{2'1}) = 1 \rightarrow \theta_{2'1} \rightarrow 2'$$

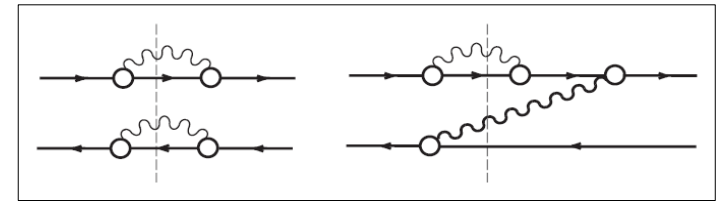
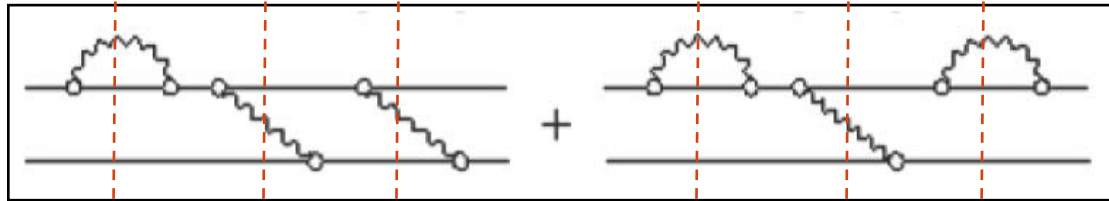
$$\delta_{\sigma_2 - \sigma_1} \theta(\sigma_1 t_{1'2}) = 2 \leftarrow \theta_{1'2} \leftarrow 1'$$



Partially fixed

Allowed terms: 1p1h, 2p2h

Blocked terms: 3p3h, 4p4h, ...



Time's arrow

Time blocking approximation = one-fish approximation!

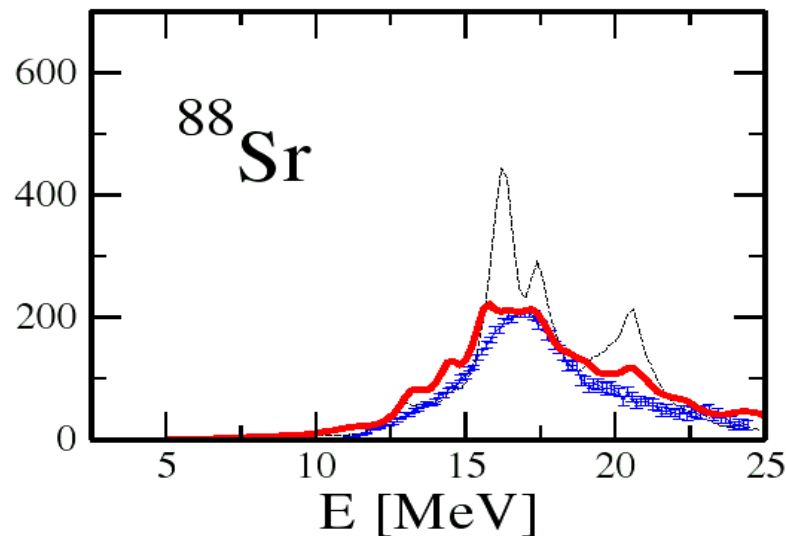
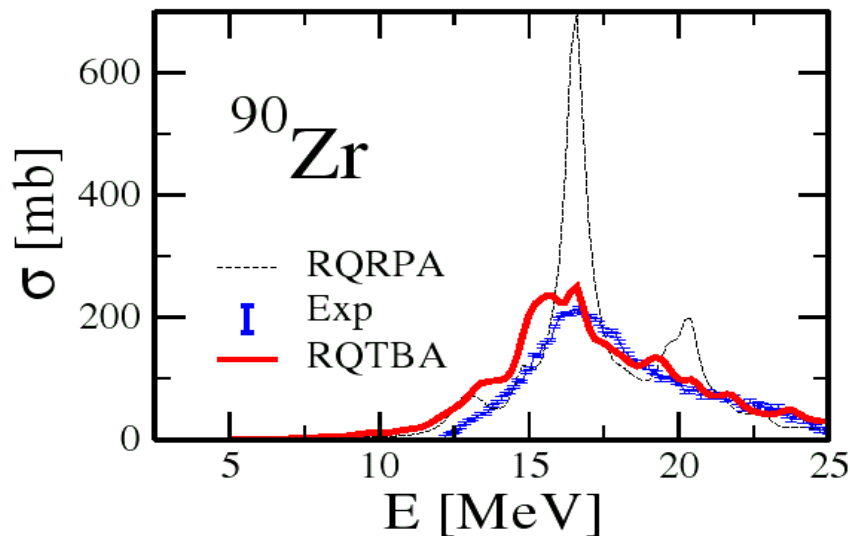
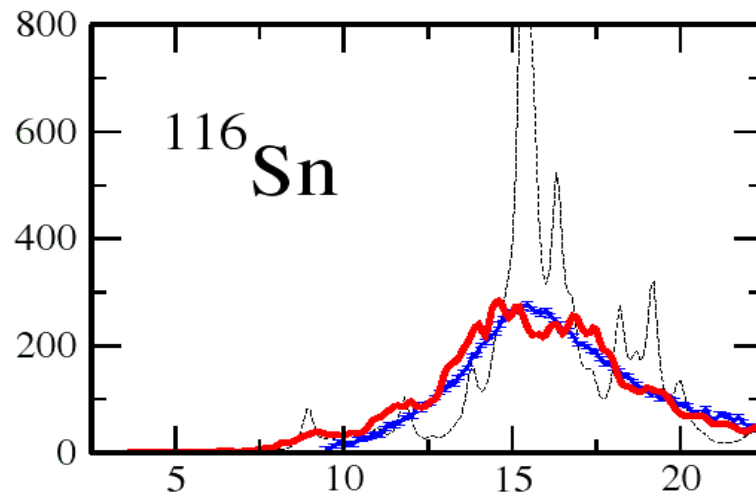
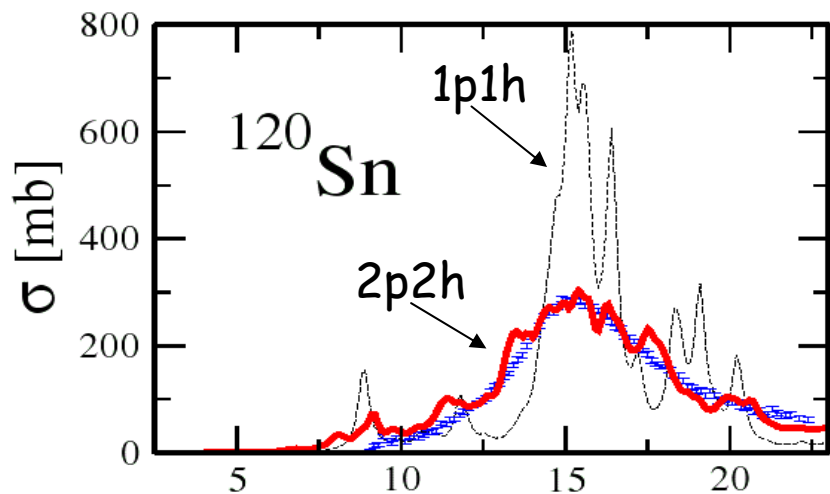
\*V.I. Tselyaev, Yad. Fiz. 50,1252 (1989).  
S.S. Wu, Scientia Sinica 16, 347 (1973).  
F.J.W. Hahne and W.D. Heiss,  
Z. Phys. A 273, 269 (1975).

• Separation of the integrations in the BSE kernel

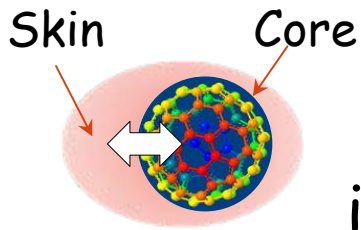
• R has a simple-pole structure (spectral representation)  
»» Strength function is positive definite!



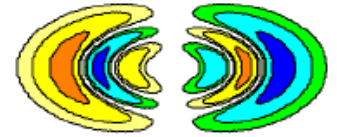
# Giant Dipole Resonance within Relativistic Quasiparticle Time Blocking Approximation (RQTBA)\*



\*E. L., P. Ring, and V. Tselyaev,  
Phys. Rev. C 78, 014312 (2008)



# Pygmy dipole resonance



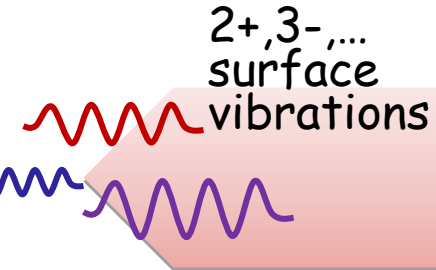
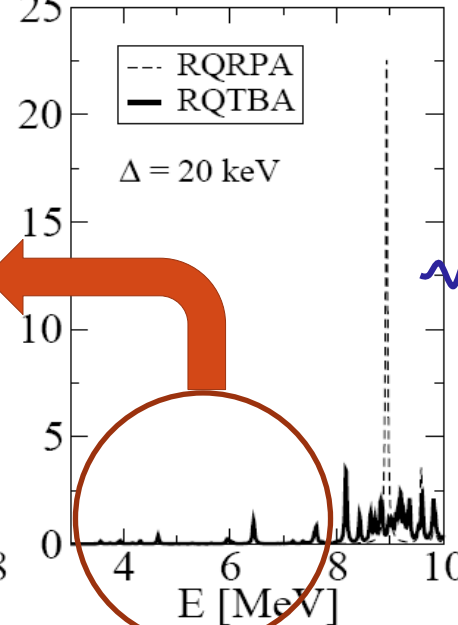
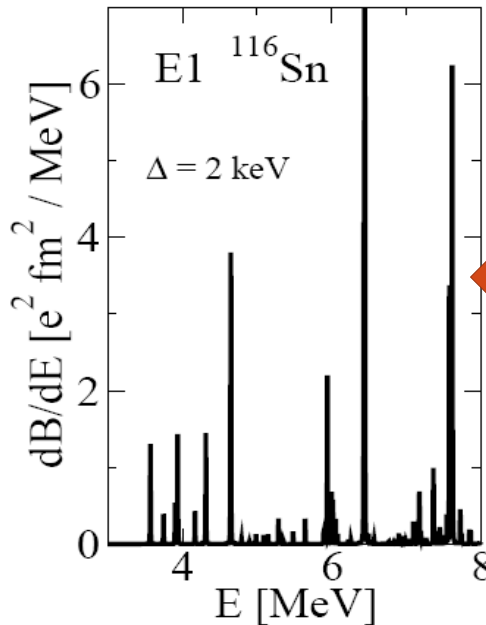
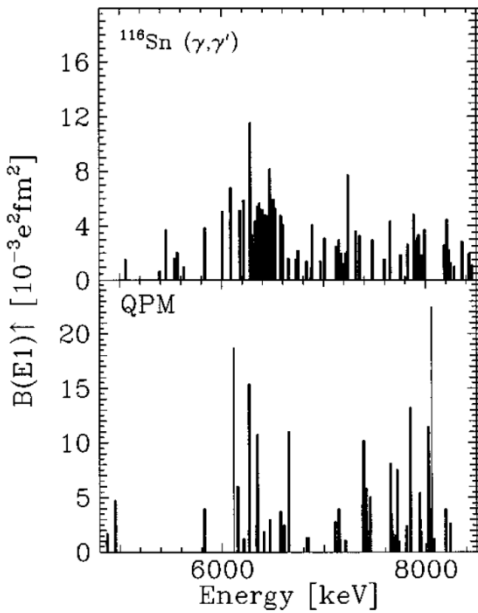
in the mode coupling interpretation

## Low-lying dipole strength in $^{116}\text{Sn}$

Experiment\*

Fine structure

Gross structure



QPM up to 3p3h  
(V.Yu. Ponomarev)

RQTBA 2p2h

RQRPA 1p1h vs  
RQTBA 2p2h

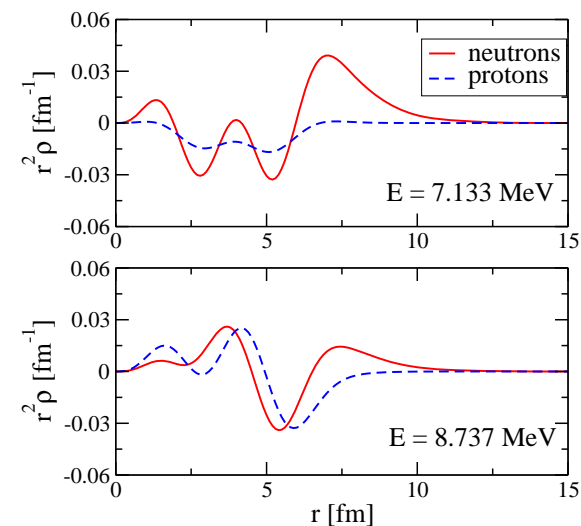
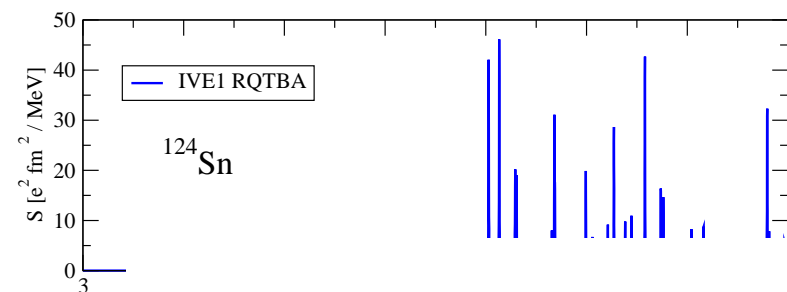
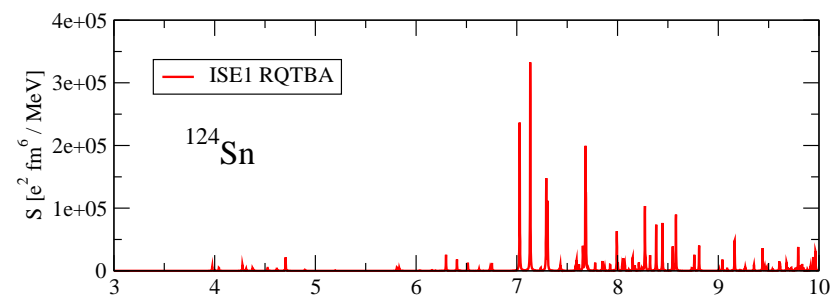
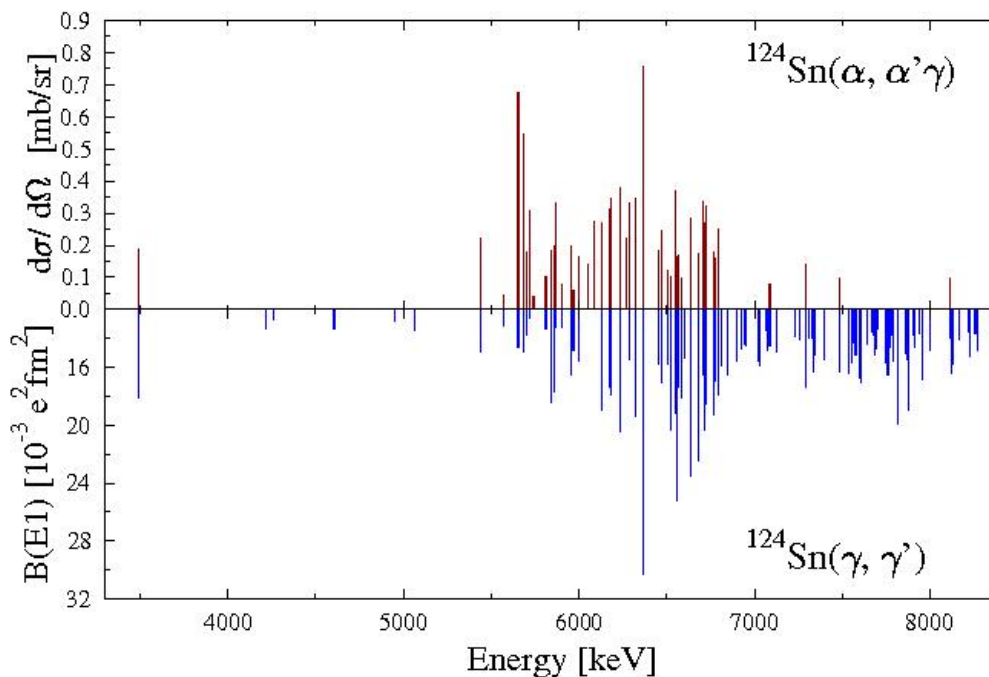
\* K. Govaert et al.,  
PRC 57, 2229 (1998)

<b>Integral</b>	
<b>5-8 MeV:</b>	
	$\Sigma B(E1)\uparrow [e^2 \text{ fm}^2]$
Exp.	0.204(25)
QPM	0.216
RQTBA	0.27

# Structure of the pygmy dipole resonance in $^{124}\text{Sn}$ (preliminary)

Experiment (J. Enders, D. Savran et al.)

Theory: RQTBA



Hadron vs Coulomb  
excitation

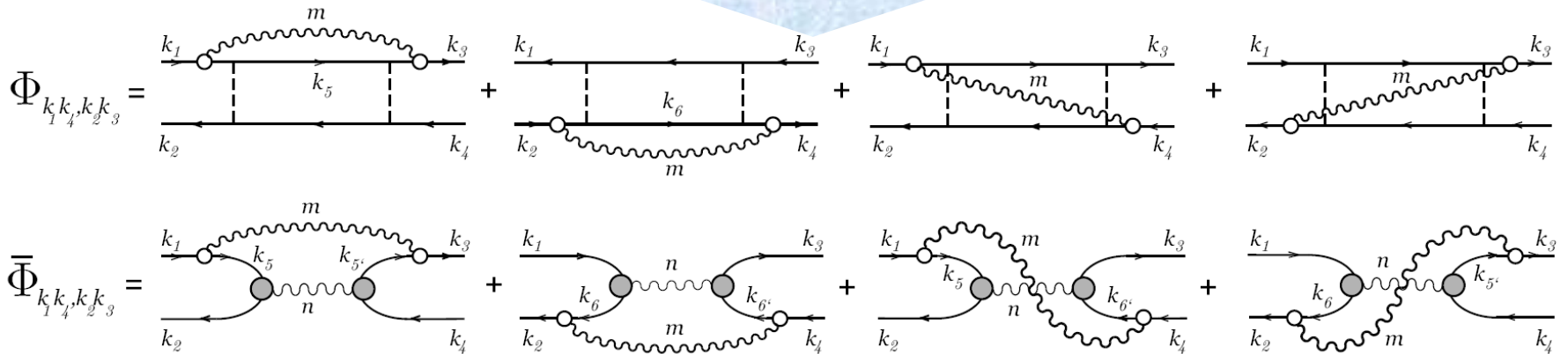
Transition  
densities

# From "2q+phonon" to "2 phonons"

P. Schuck, Z. Phys. A 279, 31 (1976)  
 V.I. Tselyaev, PRC 75, 024306 (2007)

& Mode Coupling Theory  
 Time Blocking Approximation

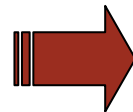
Replacement of the uncorrelated propagator inside the  $\Phi$  amplitude by QRPA response



Nuclear response:  $R = A + A (V + \bar{\Phi}) R$

Poles may appear at lower energies:

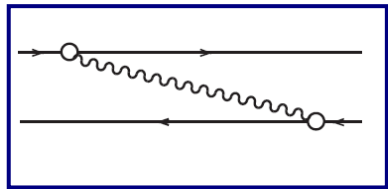
'2q+phonon' response:  
 $\Phi_{ij'i'j'}(\omega) \sim \sum_{\mu k} \alpha_{ijk\mu} / (\omega - E_{i'} - E_k - \Omega_{\mu})$



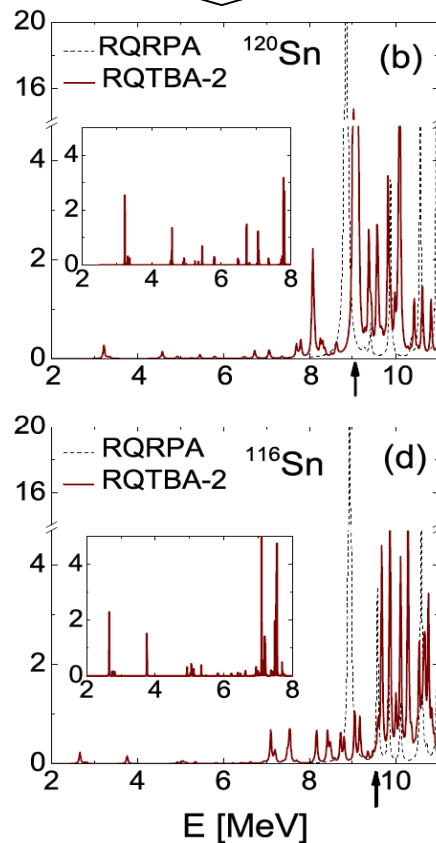
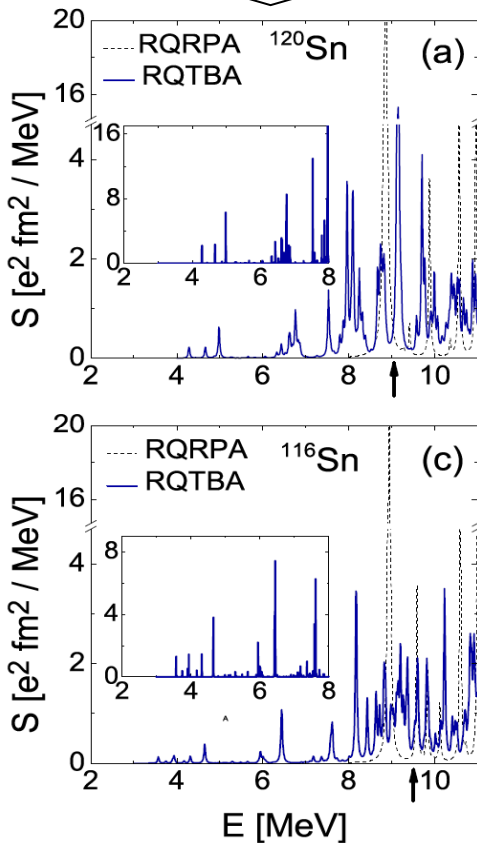
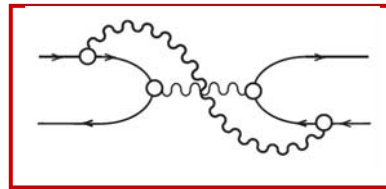
'2 phonon' response:  
 $\Phi_{ij'i'j'}(\omega) \sim \sum_{\mu\nu} \alpha_{ij'i'j'} / (\omega - \Omega_{\nu} - \Omega_{\mu})$

# Two-phonon effects in dipole spectra

2q+phonon



2 phonon



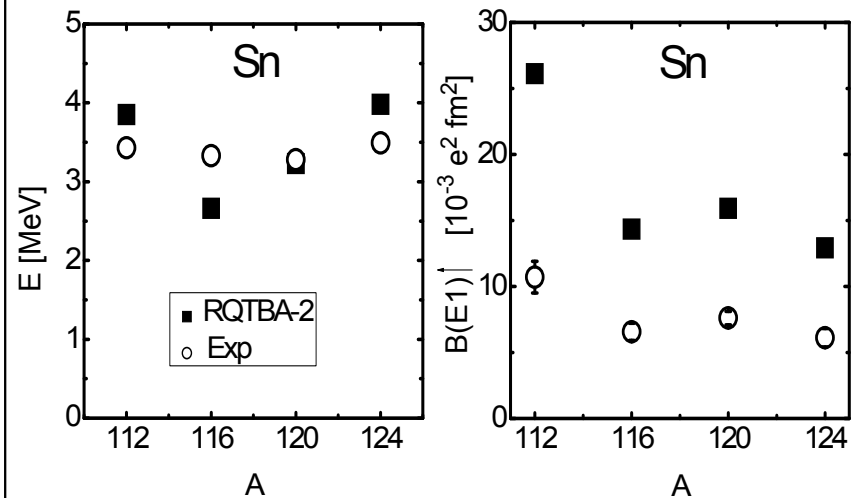
First two-phonon state  $1^-_1$

$$3^- \otimes 2^+$$

$$E(1^-_1) \approx E(2^+_1) + E(3^-_1)$$

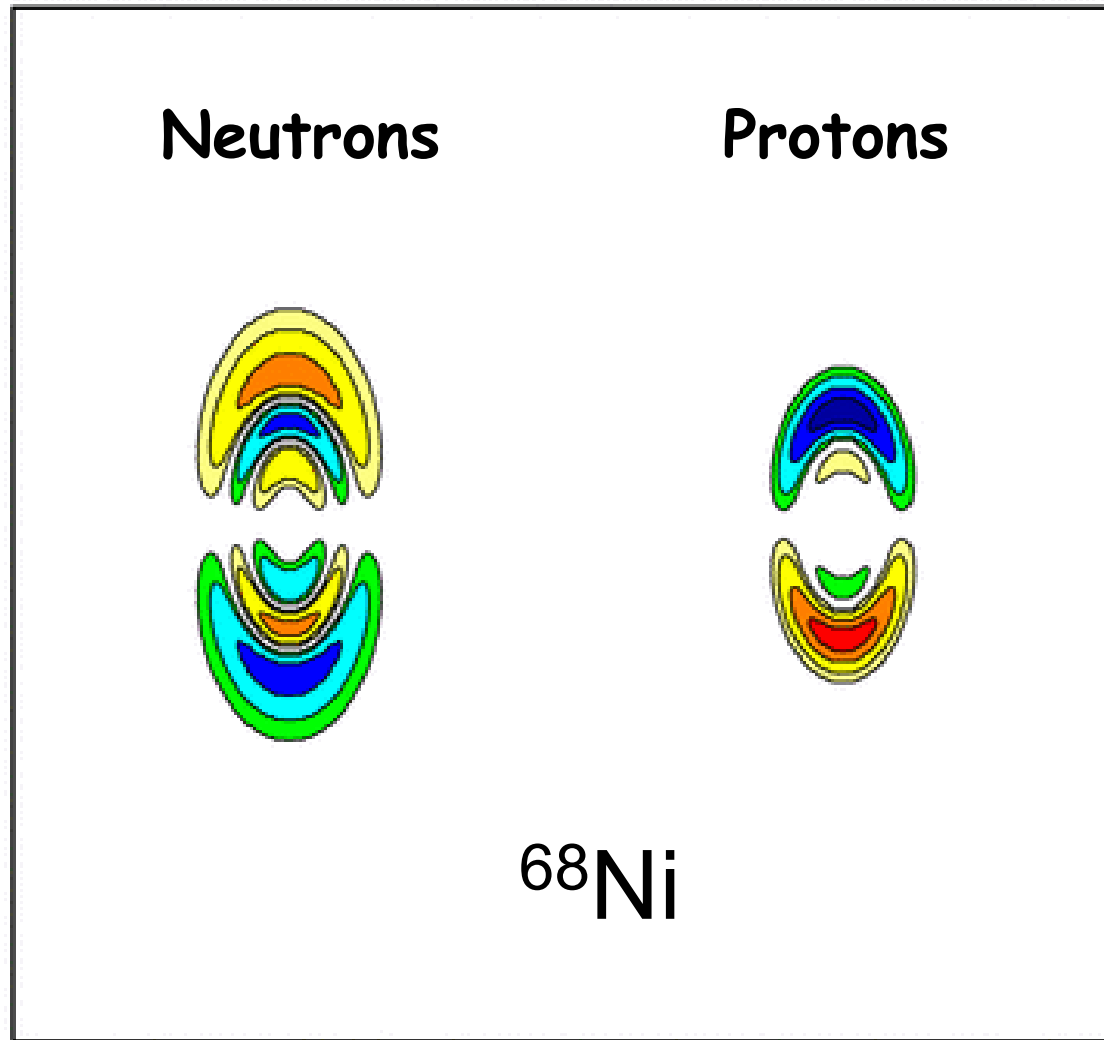
$E(1^-_1)$

$B(E1) \uparrow$

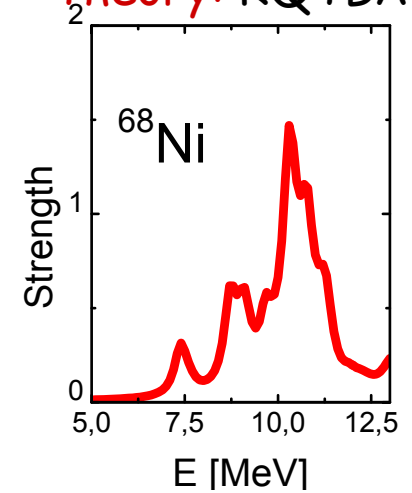


\*E.L., P.Ring, V.Tselyaev, arXiv:0910.4343, PRL (2010).  
 \*\*I.Pysmenetska et al., PRC73 (2006) 017302.

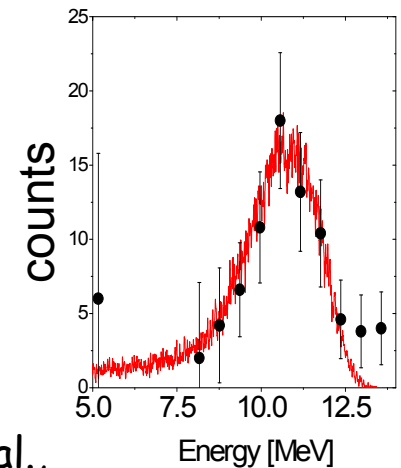
# Neutron-rich nuclei: neutron skin oscillations



Theory: RQTBA-2



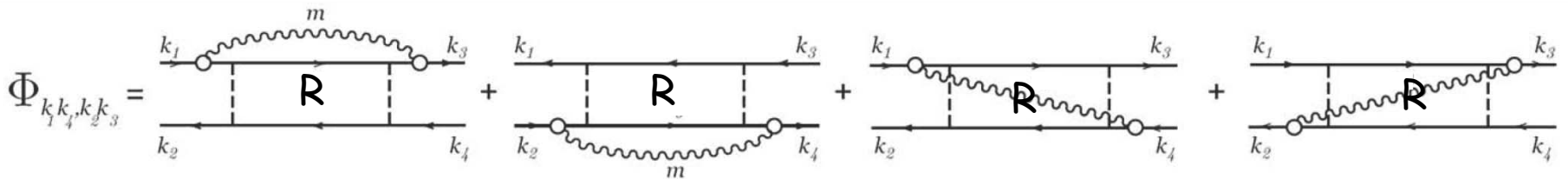
Experiment\*:  
Coulomb excitation  
of  $^{68}\text{Ni}$  at 600 A MeV



\*O. Wieland et al.,  
PRL 102, 092502 (2009)

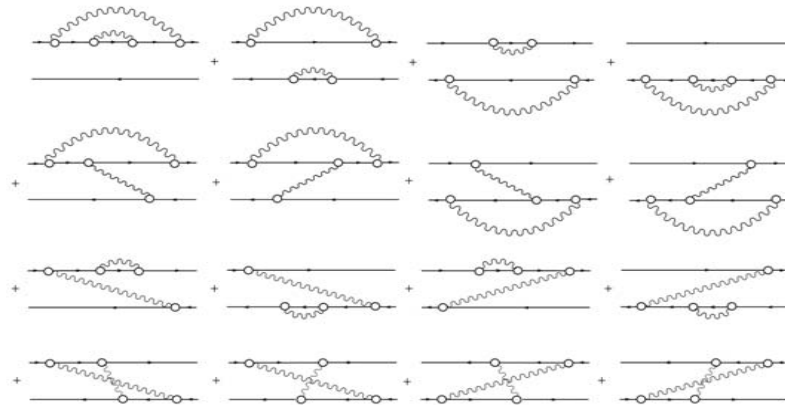
Next-order RQTBA for **3p-3h** configurations:  
iterative procedure for multiphonon response

$$R^{(n+1)} = GG + GG [V + \Phi(R^{(n)})] R^{(n+1)}$$



Nested configurations

$\gamma^4$  terms in  $\Phi$ -amplitude:



**3p3h**: two-fish approximation, ...

# Summary & Outlook

## Present status:

Microscopic approaches based on the covariant DFT with consistent treatment of many-body correlations by the **parameter-free** Green's function techniques have been developed

**2q+phonon** and **2phonon** coupling schemes have been studied within the same framework

Giant resonances' shapes, low-energy fraction of the pygmy dipole resonance and two-phonon states in medium-mass and heavy spherical nuclei including neutron-rich ones are reproduced well **within the fully consistent scheme**

## Open problems & perspectives:

**Static part:** improvements in the RMF functional in both ph- and pp-channels

**Dynamic part:** inclusion of the next orders of many-body correlations, explicit single-particle continuum

**Spatial symmetry:** deformation



# Thanks for collaboration:

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**Gabriel Martínez-Pinedo** (GSI)

**Thomas Rauscher** (Basel University)

**Peter Ring** (Technische Universität München)

**Friedrich-Karl Thielemann** (Basel University)

**Victor Tselyaev** (St. Petersburg State University)

**Dario Vretenar** (University of Zagreb)

