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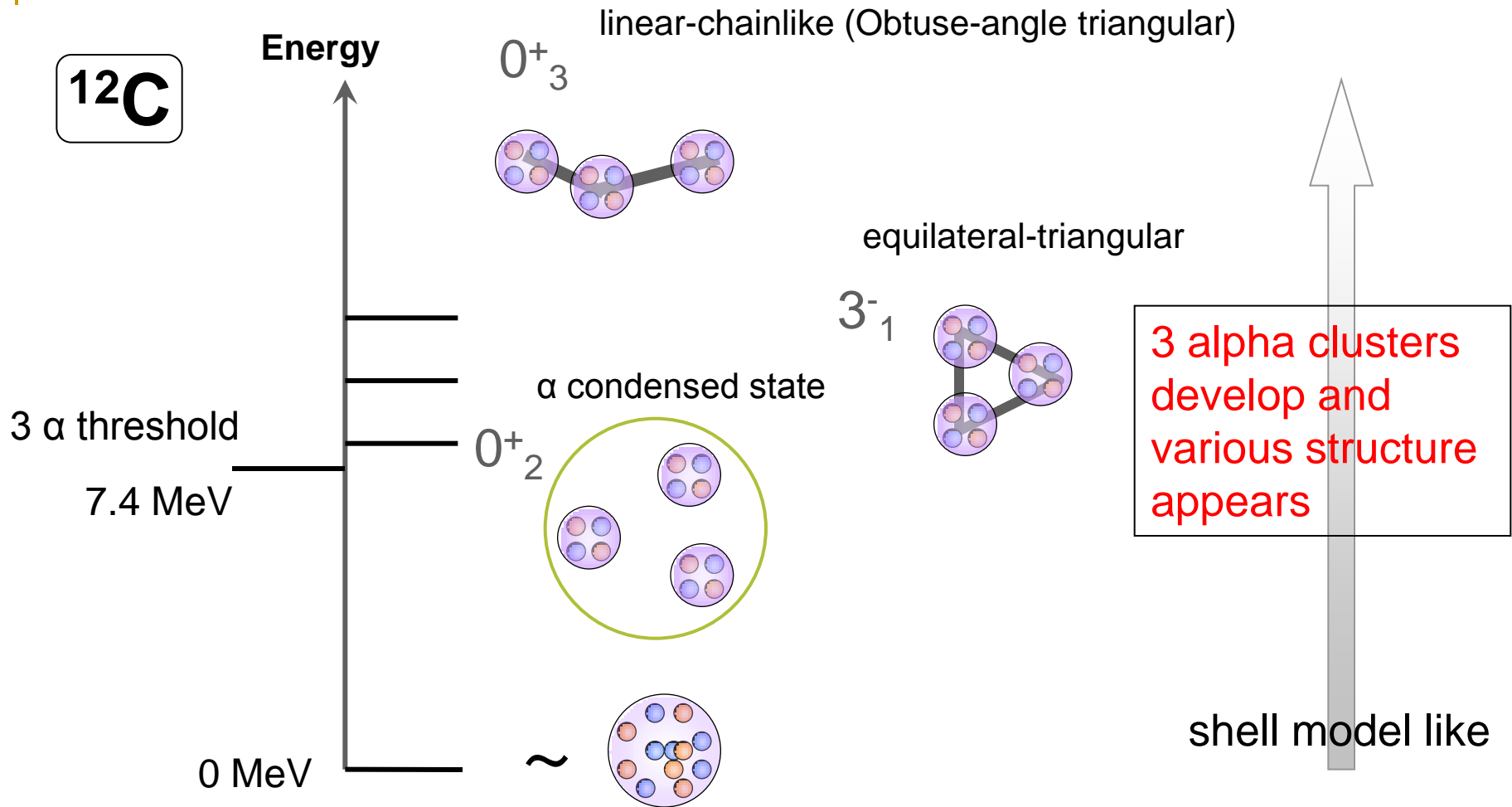
# Cluster structures of excited states in $^{14}\text{C}$

T. Suhara (Kyoto Univ.)

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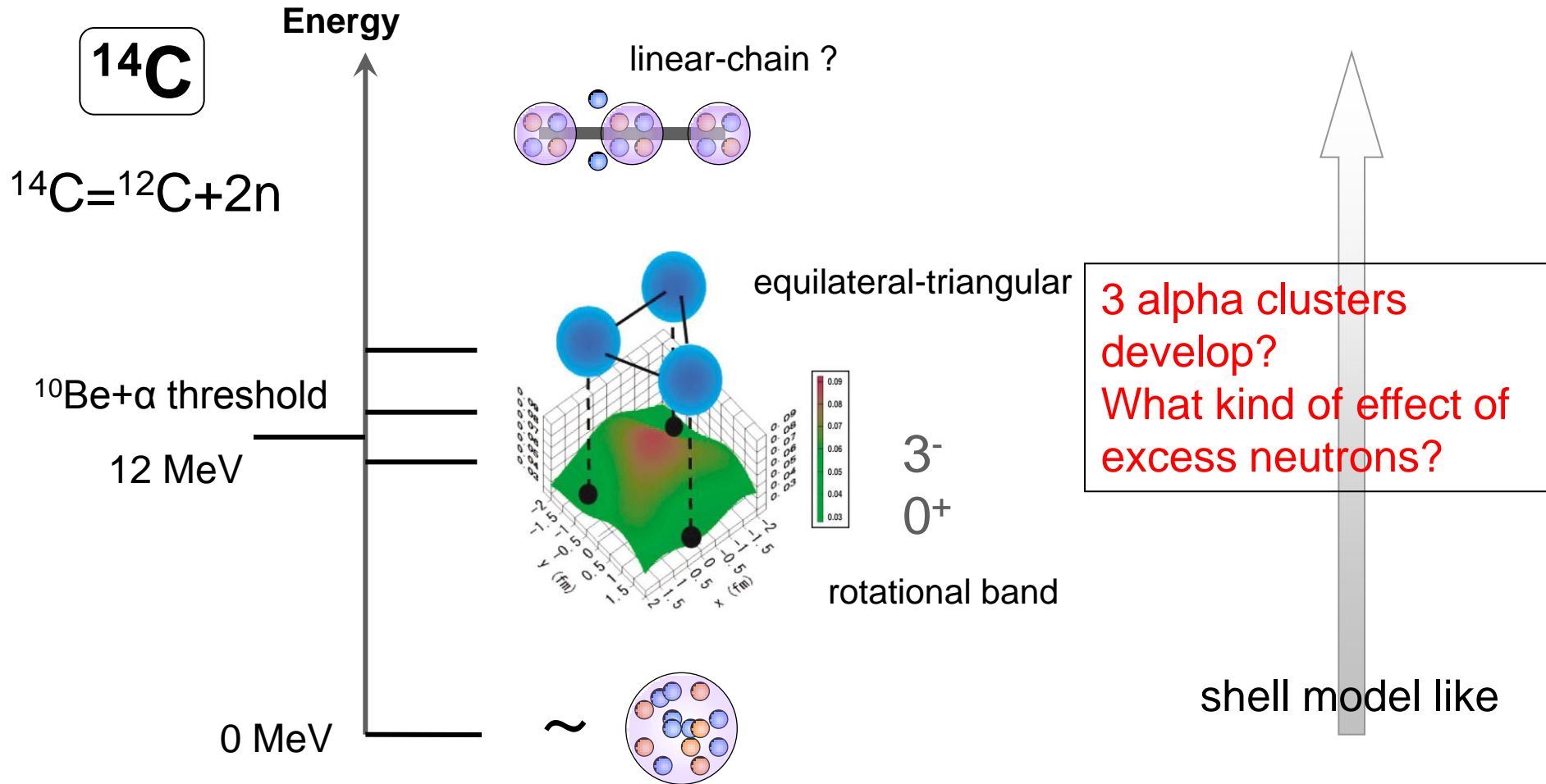
Y. Kanada-En'yo (Kyoto Univ.)

# 1. Introduction



- E. Uegaki, et al. Prog. Theor. Phys. **57**, 1262 (1977)  
M. Kamimura, et al. J. Phys. Soc. Jpn. **44** (1978), 225.  
A. Tohsaki, et al. Phys. Rev. Lett. **87**, 192501 (2001)  
T. Neff, et al. Nuc. Phys. **A738**, 357 (2004)  
Y. Kanada-En'yo, Prog. Theor. Phys. **117**, 655 (2007) etc

# 1. Introduction



# 1. Introduction

## Aim

- To know what kind of structures appear in  $^{14}\text{C}$

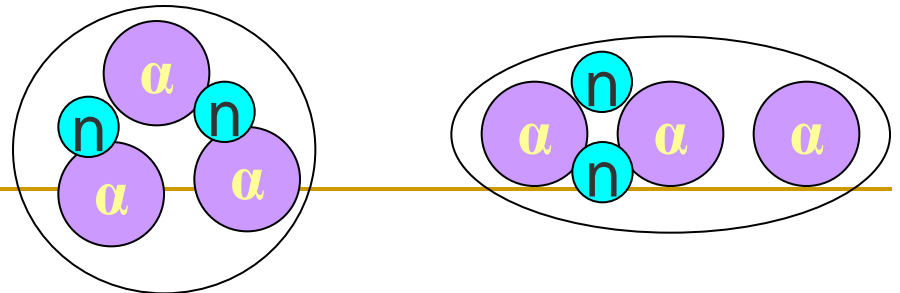
It is expected that various structure appear from an analogy of  $^{12}\text{C}$ .

- Do  $\alpha$  clusters appear or disappear?
- If  $\alpha$  clusters appear, what kind of structure do they have?  
Equilateral-triangular, Linear-chain, ...
- What kind of effect do excess neutrons give structure?

## Methods

$\beta$ - $\gamma$  constraint AMD (Antisymmetrized Molecular Dynamics)  
Superposition (GCM)

T. Suhara and Y. Kananda-En'yo, Prog. Theor. Phys. 123, 303 (2010).



## 2. Methods ( $\beta$ - $\gamma$ constraint AMD)

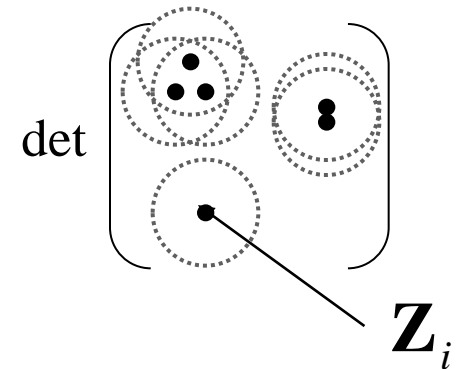
### AMD (Antisymmetrized Molecular Dynamics)

a wave function of A-body system

$$\Phi_{\text{AMD}} = \det[\varphi_1, \varphi_2, \dots, \varphi_A]$$

$$\varphi_i = \phi(\mathbf{Z}_i) \chi(\xi_i)$$

$$\left[ \begin{array}{l} \text{spatial} \\ \phi(\mathbf{Z}_i) \propto \exp\left[-\nu\left(\mathbf{r} - \frac{\mathbf{Z}_i}{\sqrt{\nu}}\right)^2\right] \\ \text{spin and isospin} \\ \chi(\xi_i) = \begin{pmatrix} \xi_{i\uparrow} \\ \xi_{i\downarrow} \end{pmatrix} \times (\text{p or n}) \end{array} \right.$$



Set of variational parameters

$$\mathbf{Z} = \{\mathbf{Z}_i, \xi_i\}$$

$$\left\{ \begin{array}{l} \mathbf{Z}_i : \text{center of Gaussian wave packets} \\ \xi_i : \text{spin direction} \end{array} \right.$$

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## 2. Methods ( $\beta$ - $\gamma$ constraint AMD)

### Parity and angular momentum projections

$$P^\pm = \frac{1 \pm P}{2}$$

$$P_{MK}^J = \frac{2J+1}{8\pi^2} \int d\Omega D_{MK}^{J*}(\Omega) R(\Omega)$$

We projected AMD wave functions onto parity and angular momentum eigenstates .

In this study, we performed the variation for the parity projected wave function. After the variation, we project the obtained wave function onto the total-angular-momentum eigenstates.

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## 2. Methods ( $\beta$ - $\gamma$ constraint AMD)

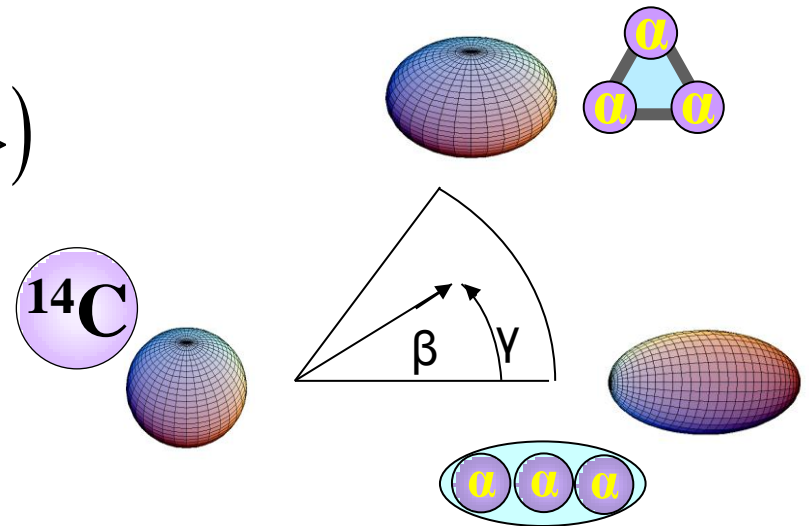
### Constraints

The quadrupole deformation ( $\beta$ ,  $\gamma$ )

$$\beta \cos \gamma = \frac{\sqrt{5\pi}}{3} \frac{2 \langle z^2 \rangle - \langle x^2 \rangle - \langle y^2 \rangle}{R^2}$$

$$\beta \sin \gamma = \sqrt{\frac{5\pi}{3}} \frac{\langle x^2 \rangle - \langle y^2 \rangle}{R^2}$$

$$R^2 = \frac{5}{3} (\langle x^2 \rangle + \langle y^2 \rangle + \langle z^2 \rangle)$$



## 2. Methods

### Effective Hamiltonian

$$H^{\text{eff}} = \sum_i t_i - T_{\text{CM}} + \sum_{i<j} v_{ij}^{\text{central}} + \sum_{i<j} v_{ij}^{\text{LS}} + \sum_{i<j} v_{ij}^{\text{Coulomb}}$$

The central force : The Volkov No.2

$$v_{ij}^{\text{central}} = \left( v_1 \exp\left[-\left(\frac{r_{ij}}{a_1}\right)^2\right] + v_2 \exp\left[-\left(\frac{r_{ij}}{a_2}\right)^2\right] \right) X_{ij}$$

$$X_{ij} = W + BP_{\sigma} - HP_{\tau} - MP_{\sigma}P_{\tau} \quad (W = 0.4, M = 0.6, B = H = 0.125)$$

$$v_1 = -60.65[\text{MeV}], a_1 = 1.80[\text{fm}], v_2 = 61.14[\text{MeV}], a_2 = 1.01[\text{fm}]$$

The LS force : The LS part of the G3RS

$$v_{ij}^{\text{LS}} = \left( u_1 \exp\left[-\left(\frac{r_{ij}}{a_1}\right)^2\right] + u_2 \exp\left[-\left(\frac{r_{ij}}{a_2}\right)^2\right] \right) P(S=1)P(T=1)\mathbf{L} \cdot \mathbf{S}$$

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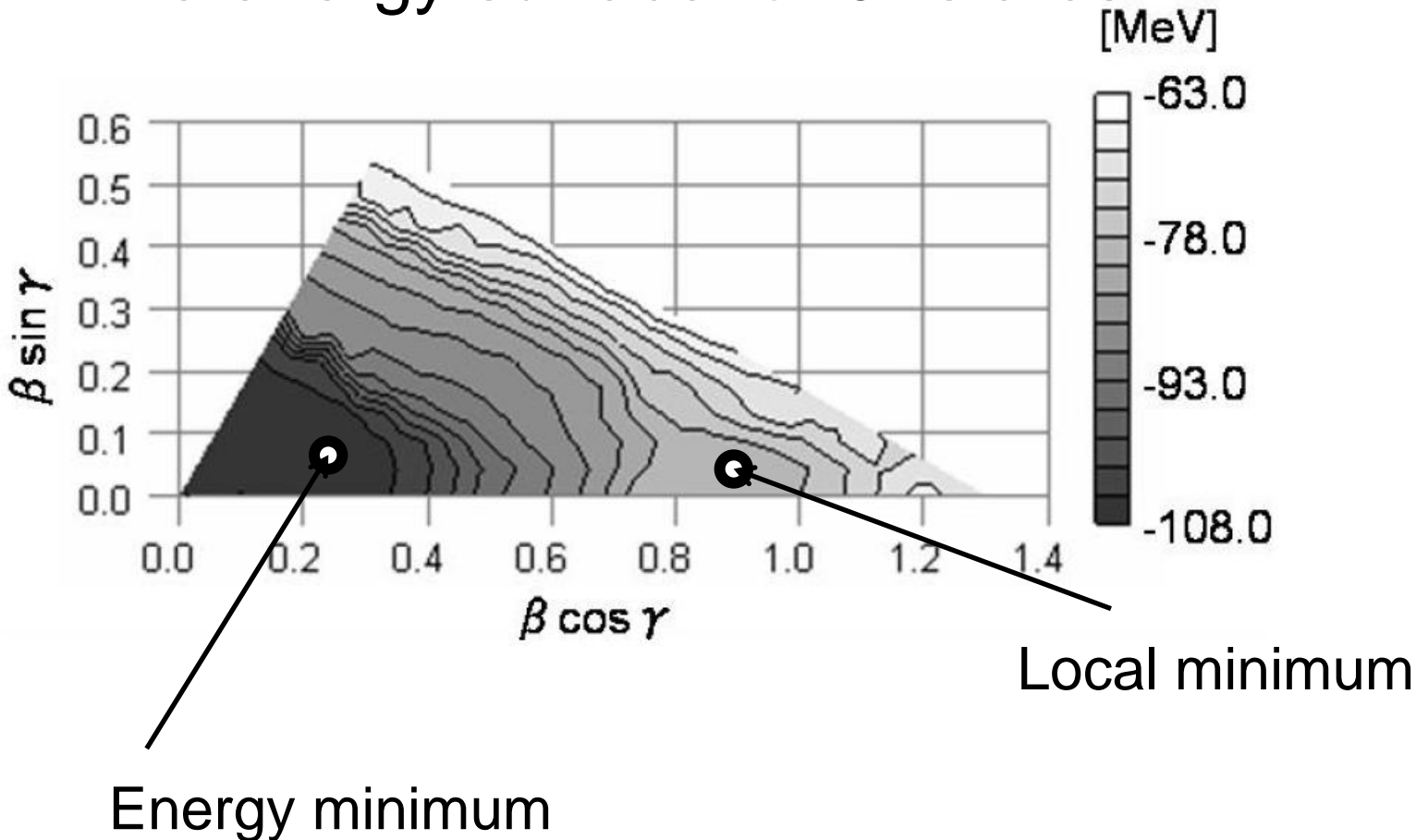
$$P(S=1) = \frac{1+P_{\sigma}}{2}, P(T=1) = \frac{1+P_{\tau}}{2}$$

$$u_1 = 1600[\text{MeV}], a_1 = 0.447[\text{fm}], u_2 = -1600[\text{MeV}], a_2 = 0.600[\text{fm}]$$



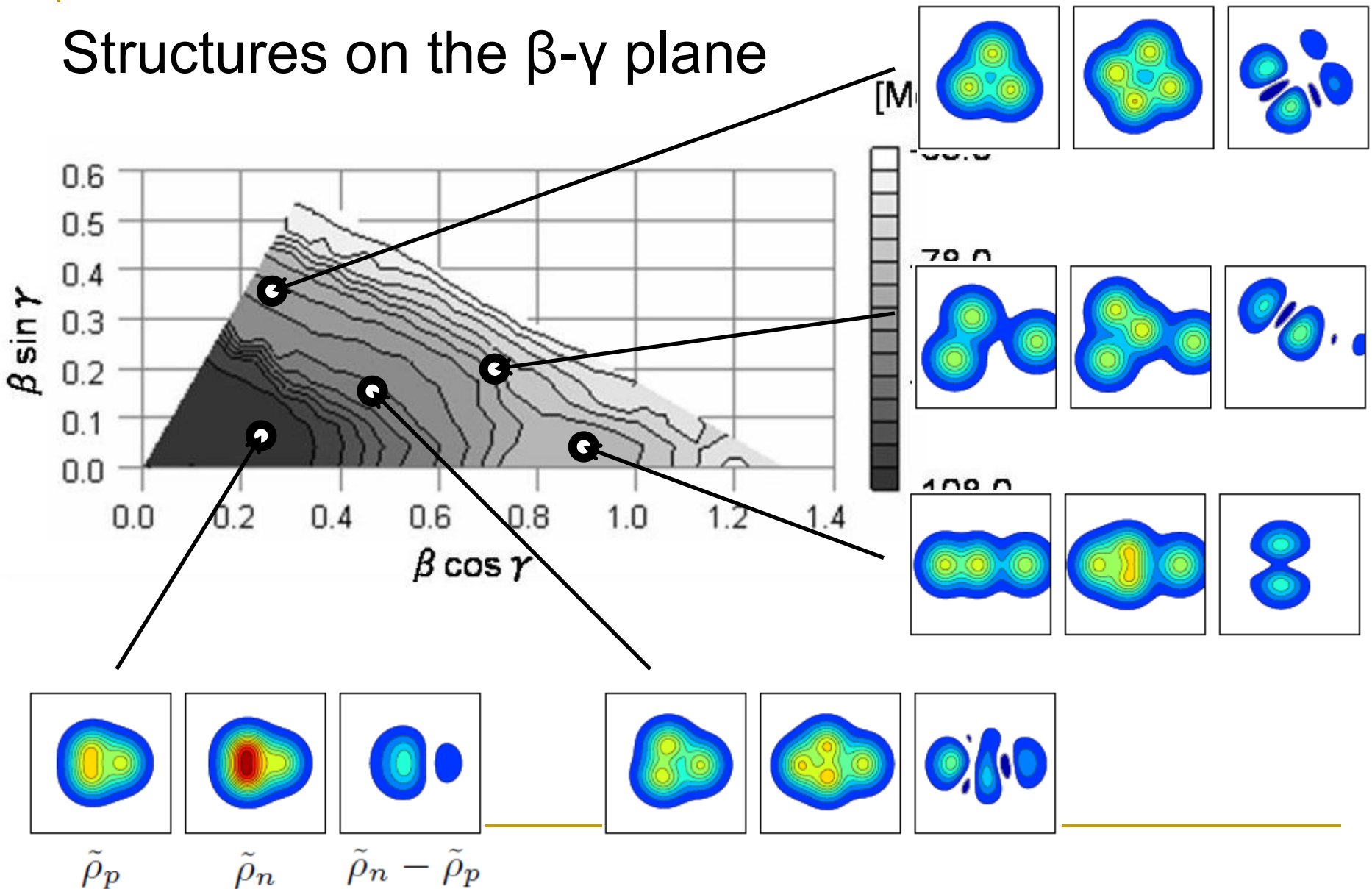
### 3. Results (+ parity states)

The energy surface for  $0^+$  states



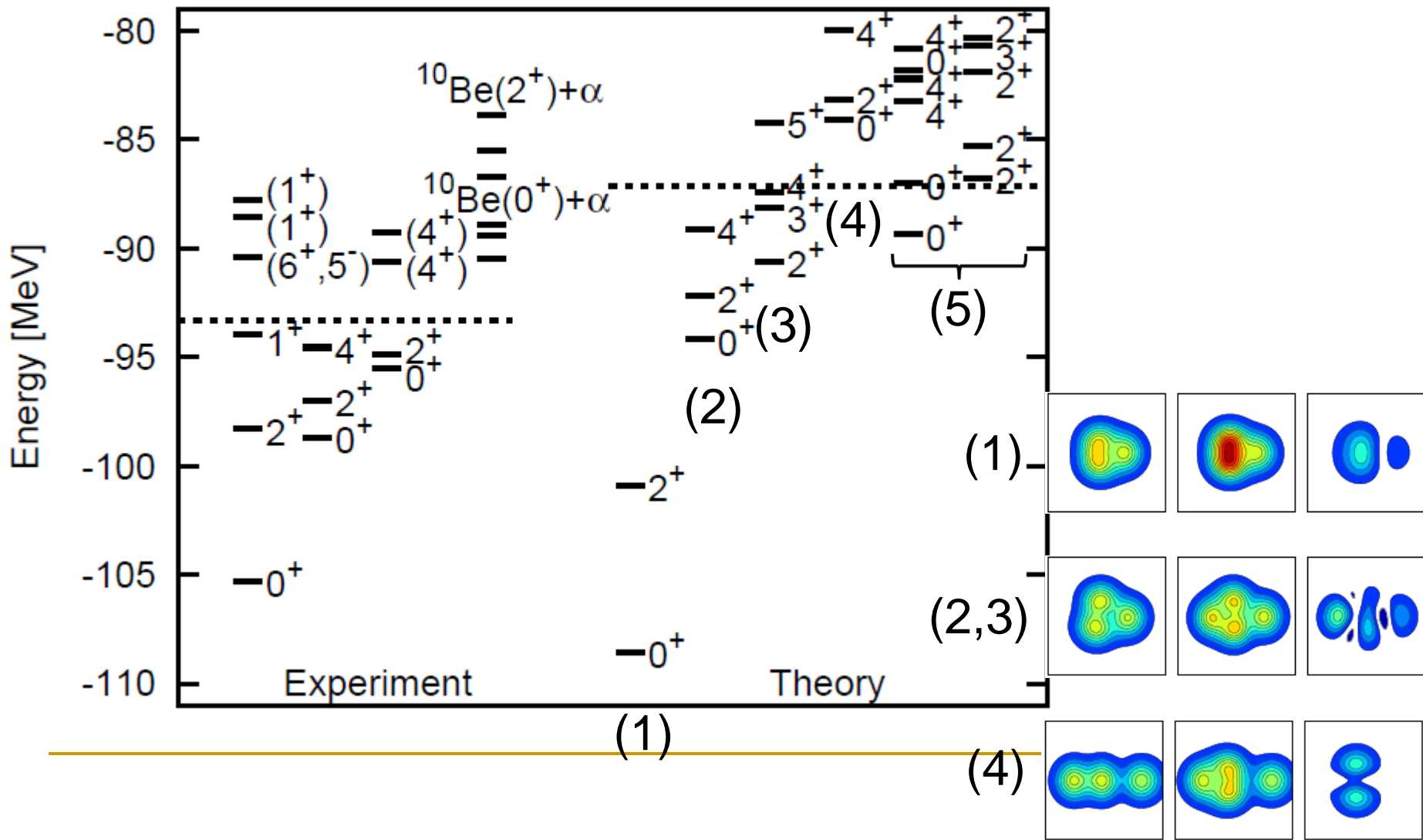
### 3. Results (+ parity states)

## Structures on the $\beta$ - $\gamma$ plane



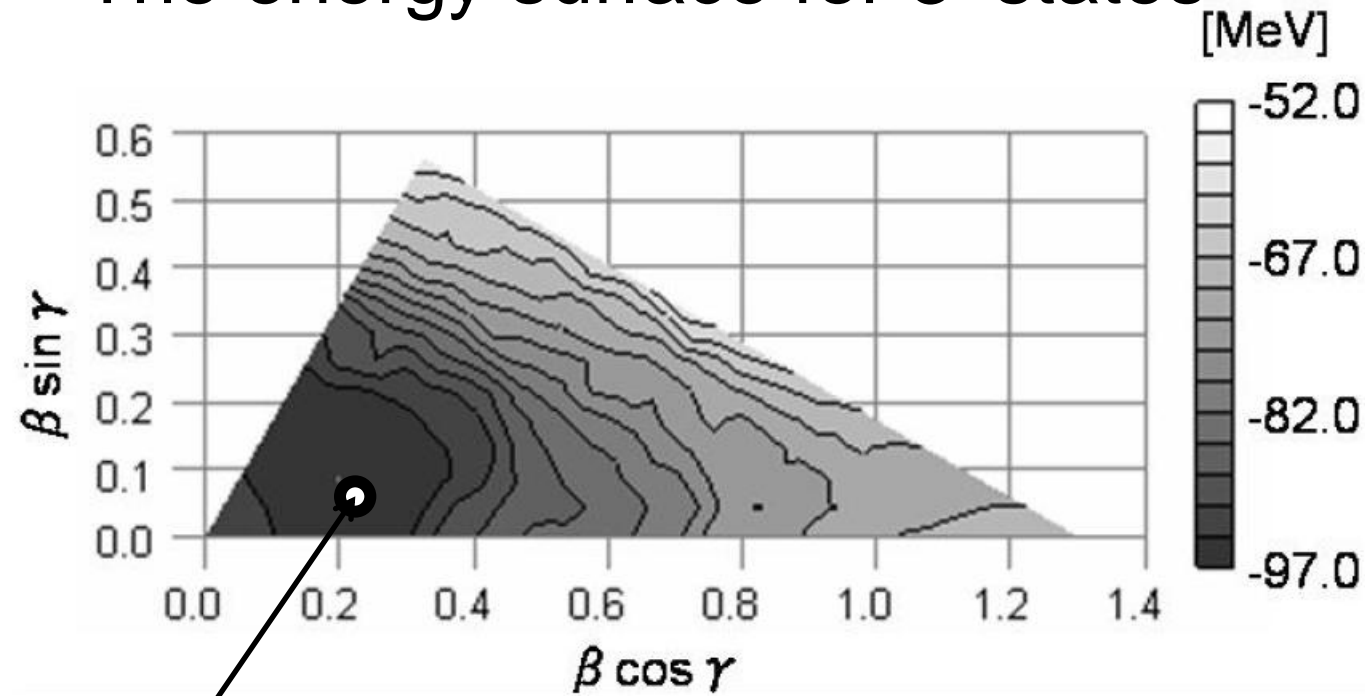
### 3. Results (+ parity states)

## Energy levels



### 3. Results (- parity states)

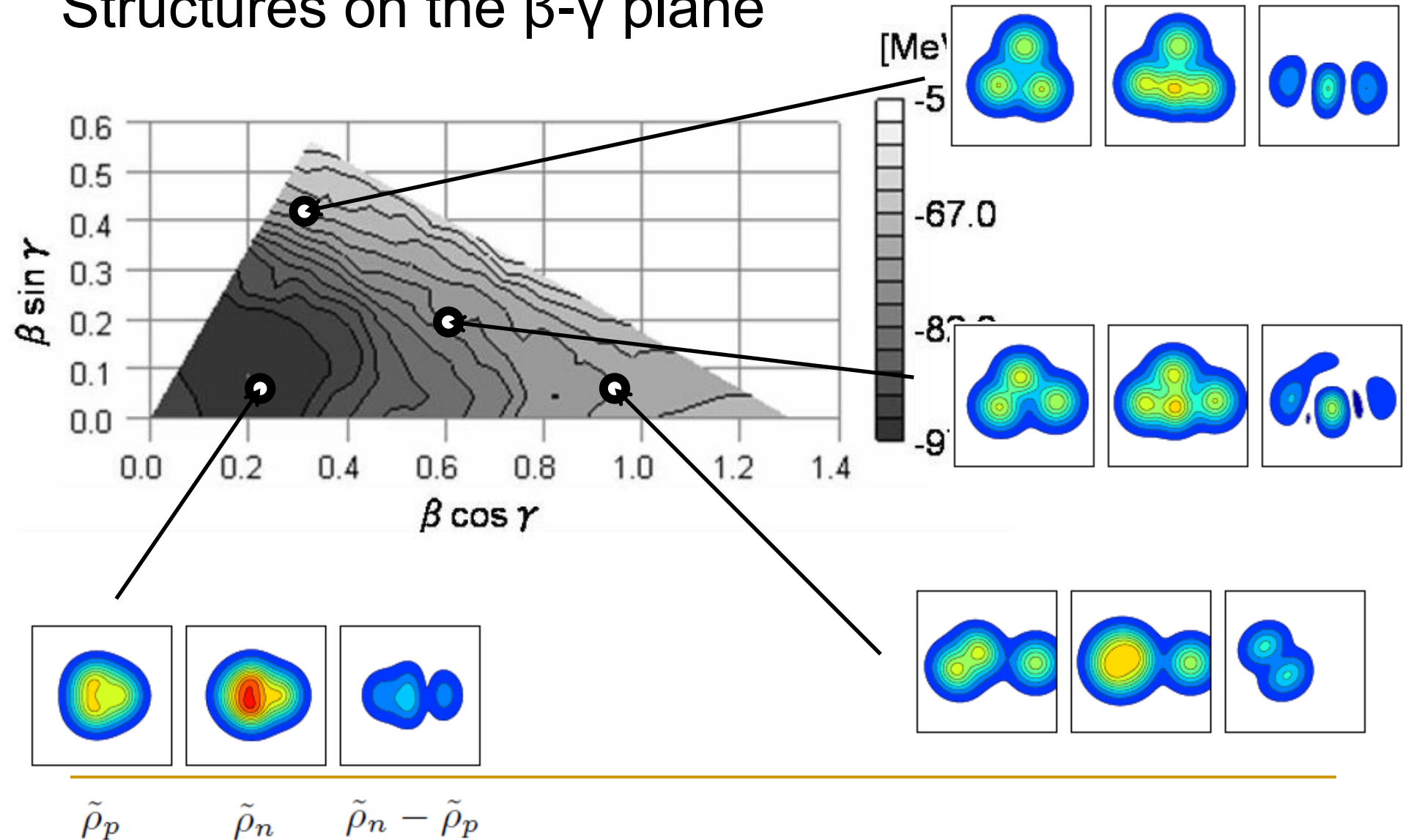
The energy surface for  $3^-$  states



Energy minimum

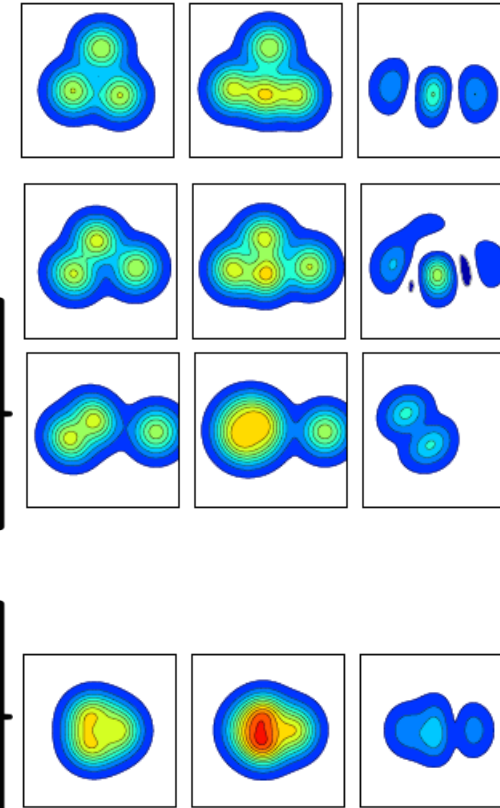
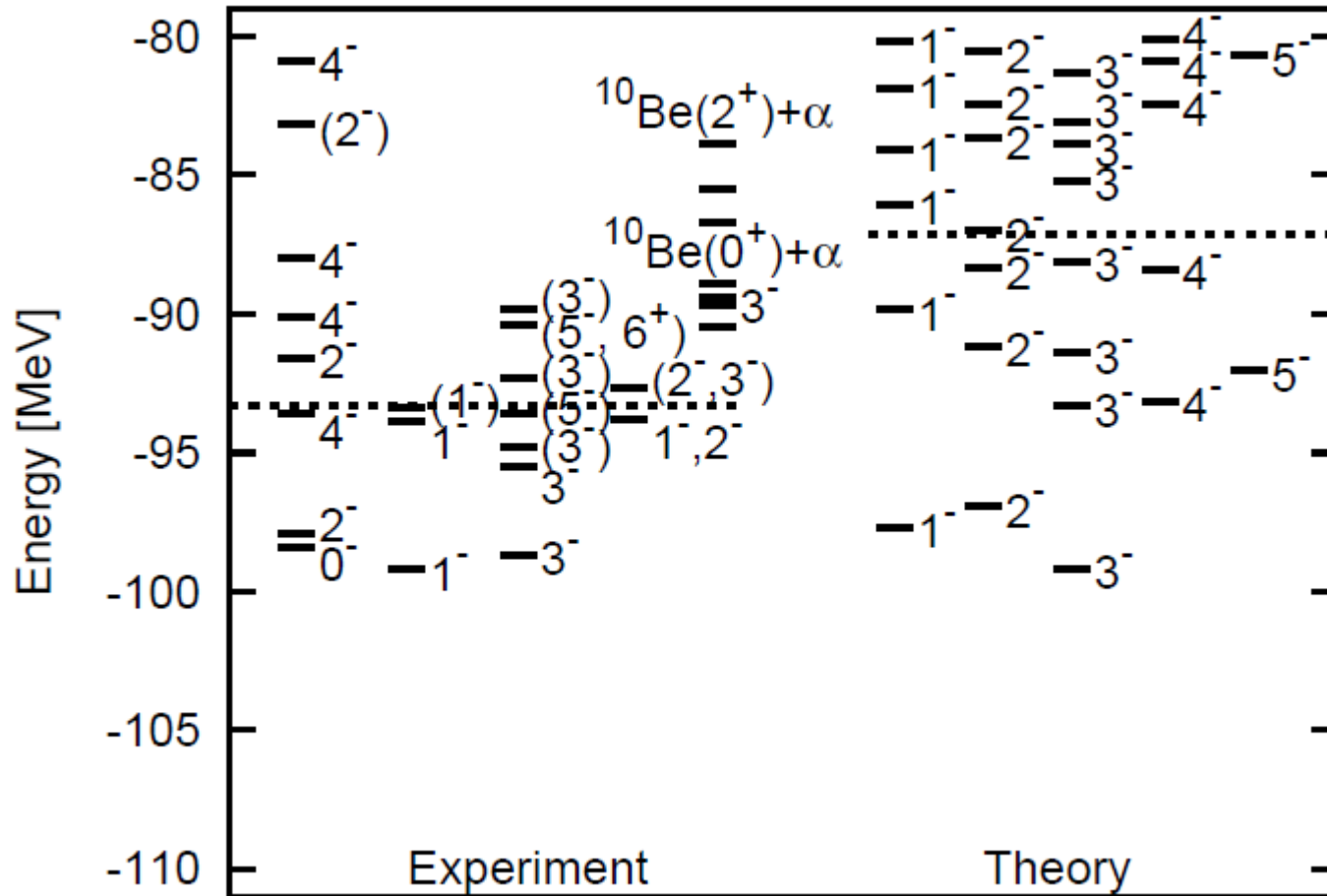
### 3. Results (- parity states)

## Structures on the $\beta$ - $\gamma$ plane



### 3. Results (- parity states)

## Energy levels



### 3. Results (- parity states)

## Parity partner

$$|\text{Linear - chain } +\rangle = \left| \begin{array}{c} \alpha \quad n \quad \alpha \\ \alpha \quad \alpha \end{array} \right\rangle + \left| \begin{array}{c} \alpha \quad \alpha \quad n \quad \alpha \\ \alpha \quad \alpha \end{array} \right\rangle$$

~~$$|\text{Linear - chain } -\rangle = \left| \begin{array}{c} \alpha \quad n \quad \alpha \\ \alpha \quad \alpha \end{array} \right\rangle - \left| \begin{array}{c} \alpha \quad \alpha \quad n \quad \alpha \\ \alpha \quad \alpha \end{array} \right\rangle$$~~

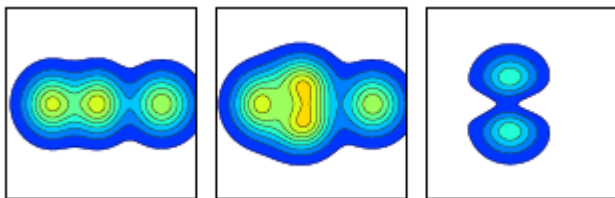
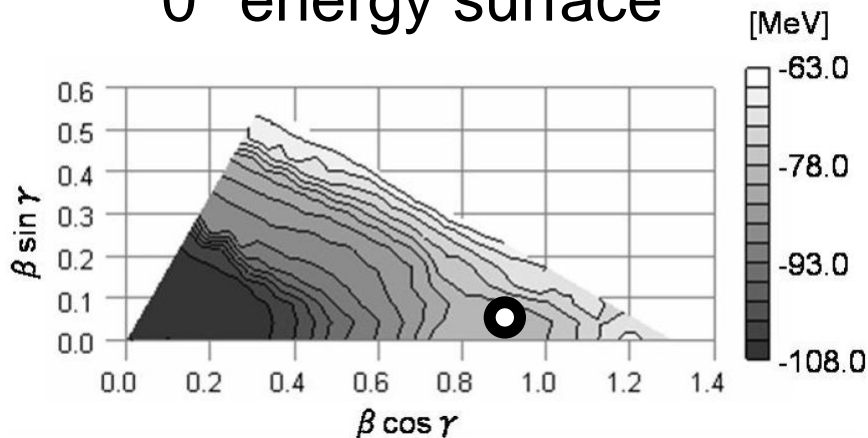
### 3. Results (- parity states)

## Parity partner

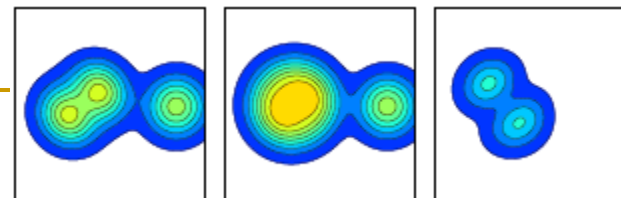
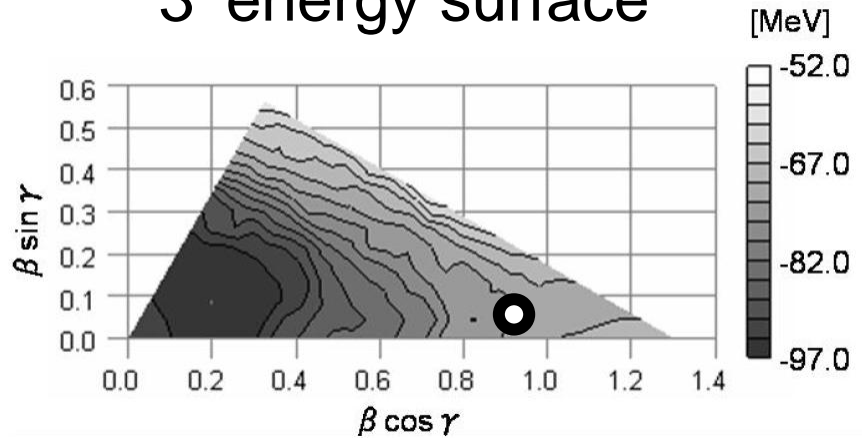
$$|\text{Linear - chain } +\rangle = \left| \begin{array}{c} \alpha \quad n \quad \alpha \\ \alpha \quad \alpha \end{array} \right\rangle + \left| \begin{array}{c} \alpha \quad \alpha \quad n \quad \alpha \\ \alpha \quad n \quad \alpha \end{array} \right\rangle$$

~~$$|\text{Linear - chain } -\rangle = \left| \begin{array}{c} \alpha \quad n \quad \alpha \\ \alpha \quad \alpha \end{array} \right\rangle - \left| \begin{array}{c} \alpha \quad \alpha \quad n \quad \alpha \\ \alpha \quad n \quad \alpha \end{array} \right\rangle$$~~

$0^+$  energy surface



$3^-$  energy surface





## 5. Summary

We investigated  $^{14}\text{C}$  with  $\beta$ - $\gamma$  constraint AMD+GCM.

- Various excited states with the developed  $3\alpha$  cluster core structures are suggested in  $^{14}\text{C}$ .
- In the positive-parity states, triaxial deformed and linear-chain structures are found to construct excited bands.
- The linear-chain band has  $^{10}\text{Be}+\alpha$  correlation.
- In the negative-parity states, the parity-partner of linear-chain state disappears because  $^{10}\text{Be}$  cluster rotates easily.

## Future Work

- Estimating decay widths to  $^{10}\text{Be}(0^+_{1})+\alpha$  and  $^{10}\text{Be}(2^+_{1})+\alpha$   
Excited states with  $^{10}\text{Be}+\alpha$  correlation are the candidates for the states which were observed recently in  $^{10}\text{Be}+\alpha$  decays.
- Further neutron-rich C isotopes