

# Halo structure involving core excitation in $^{15}\text{C}$

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# Introduction

## Investigation for halo nuclei in larger mass region

- Rms matter radius of  $^{22}\text{C}$  derived from reaction cross section measurement

$$^{22}\text{C}: 5.4 \pm 0.9 \text{ fm}$$

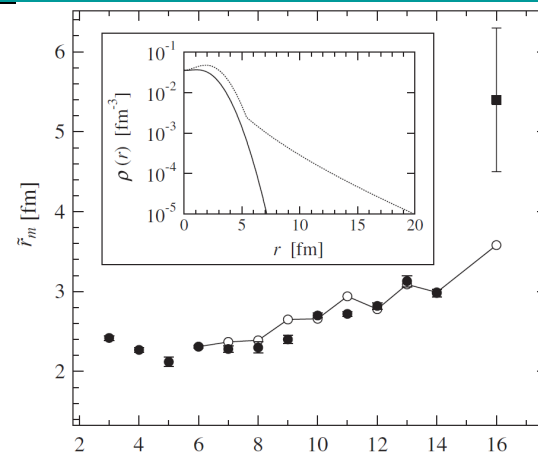
K. Tanaka et al. PRL104,062701 (2010)

Assumption of inert core is valid in heavier nuclei?

- Implication of core excitation in  $^{11}\text{Be}$  from observation of charge radius  $r_m^N$

- Approximately 0.1 fm larger than  $^{10}\text{Be}$
- Development of  $2\alpha$  cluster core? Recoil effect?

W. Nörtershäuser et al. PRL102,062503 (2009)



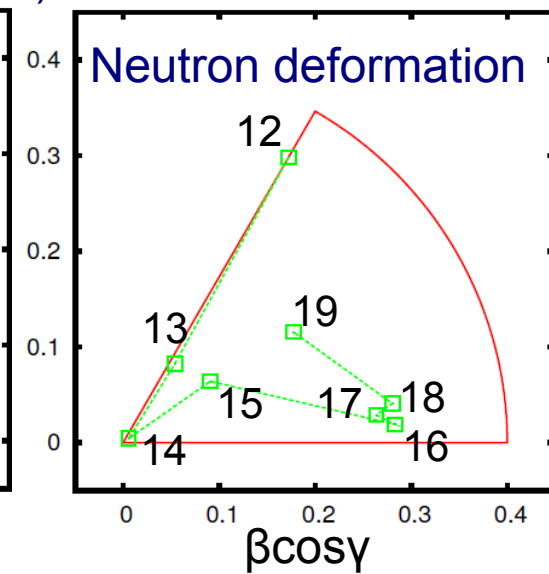
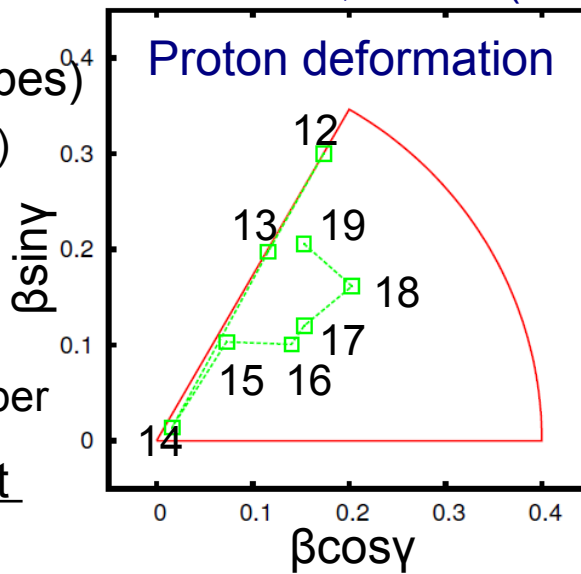
## Theoretical expectation (C isotopes)

MAMD: MV1+G3RS ( $V_{\text{ls}} = 1800 \text{ MeV}$ )

$^{12}\text{C}$  is very soft against oblate deformation

→ Development of oblate deformation of proton change with neutron number

Core excitation can be important in halo nuclei



# Introduction

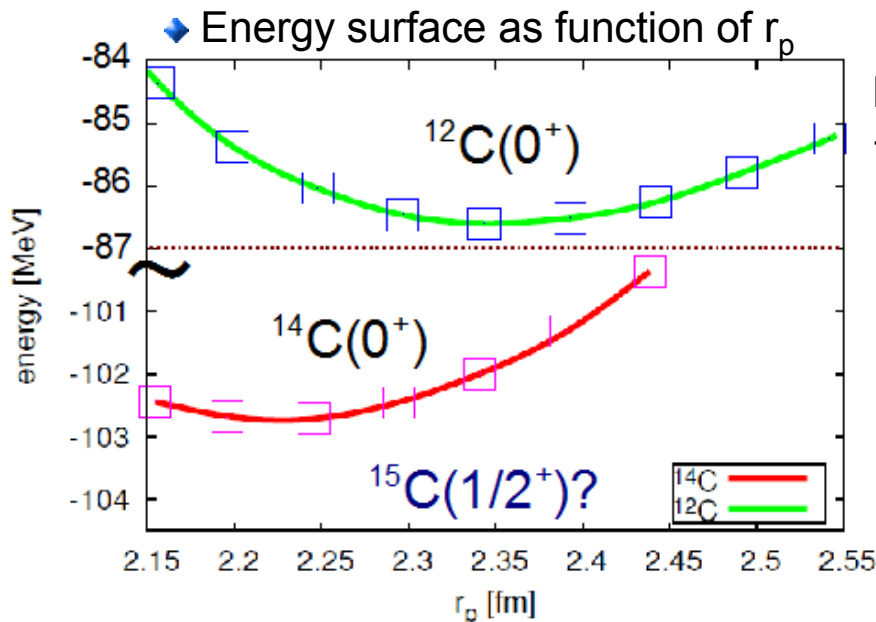
## In this work,

Structure of  $^{15}\text{C}$  is investigated  
to discuss importance of core excitation in halo nuclei

- $^{15}\text{C}$ :
- ◆ Small one neutron separation energy  $S_n = 1.218$  MeV
  - ◆ Narrow longitudinal momentum distribution for  $^{15}\text{C} \rightarrow ^{14}\text{C}$
  - ◆ Large s-wave spectroscopic factor

- $^{15}\text{C}$  is One neutron halo nucleus?
- Inversion of  $1/2^+$  state (ground state) and  $5/2^+$  state (Ex 0.74 MeV)

● Importance of core excitation can be seen in energy surface as function of proton radius



MAMD: Volkov No.2  
+G3RS ( $V_{ls} = 900$  MeV)

◆  $^{12}\text{C}$  has flat energy surface  
in wide  $r_p$  range due to development  
of  $3\alpha$  cluster structure

◆ Development of  $3\alpha$  cluster structure  
suppressed in  $^{14}\text{C}$

◆ By adding one more neutron?

- ◆ Description of core excitation  
(development of  $3\alpha$  cluster structure is expected) → AMD
- ◆ Simultaneous description of  
halo structure and core excitation → Extended framework of AMD

## AMD wave function

$$\Phi_{int} = \frac{1}{\sqrt{A!}} \det[\varphi_1, \varphi_2, \dots, \varphi_A],$$

### Improved nucleon wave function

$$\varphi_i(\mathbf{r}) = \phi_i(\mathbf{r}) \chi_i \tau_i \quad \phi_i(\mathbf{r}) = \exp \left[ -\nu \left( \mathbf{r} - \frac{\mathbf{Z}_i}{\sqrt{\nu}} \right)^2 \right]$$

$$\varphi_i(\mathbf{r}) = \left( \sum_{\alpha} C_i^{\alpha} \phi_i^{\alpha}(\mathbf{r}) \right) \chi_i \tau_i \quad \phi_i^{\alpha}(\mathbf{r}) = \exp \left[ -\nu_i^{\alpha} \left( \mathbf{r} - \frac{\mathbf{Z}_i^{\alpha}}{\sqrt{\nu_i^{\alpha}}} \right)^2 \right]$$

The same type of nucleon wave function is used in FMD

- $\alpha=2$  for  $|N-Z|$  neutron wave function  
 $\alpha=1$  for  $N=Z$  nucleon wave function ( $i=1-12:\alpha=1, i=13-15:\alpha=2$ )

## ■ Variational function

$$\Phi^\pm = P^\pm \Phi_{int} = \frac{(1 \pm P_x)}{2} \Phi_{int}$$

## ■ Hamiltonian

$$\hat{H} = \hat{T} + \hat{V}_{nucl} + \hat{V}_c - \hat{T}_g \quad \hat{V}_{nucl} ; \text{Volkov No.2} \\ + \text{G3RS force } (V_0=900 \text{ MeV})$$

## ■ Energy variation

$$E^\pm = \frac{\langle \Phi^\pm | \hat{H} | \Phi^\pm \rangle}{\langle \Phi^\pm | \Phi^\pm \rangle}$$

## ■ GCM

### ● Generator coordinate; proton and neutron radii

- ◆ Proton radius: Description of core excitation
- ◆ Neutron radius: Description of halo

$$\Psi_n^{J^\pm} = \sum_i c_i^n \Phi_{MK_i}^{J^\pm}(r_i^p, r_i^n) \quad \Phi_{MK}^{J^\pm}(r^p, r^n) = \hat{P}_{MK}^J \Phi^\pm(r^p, r^n)$$

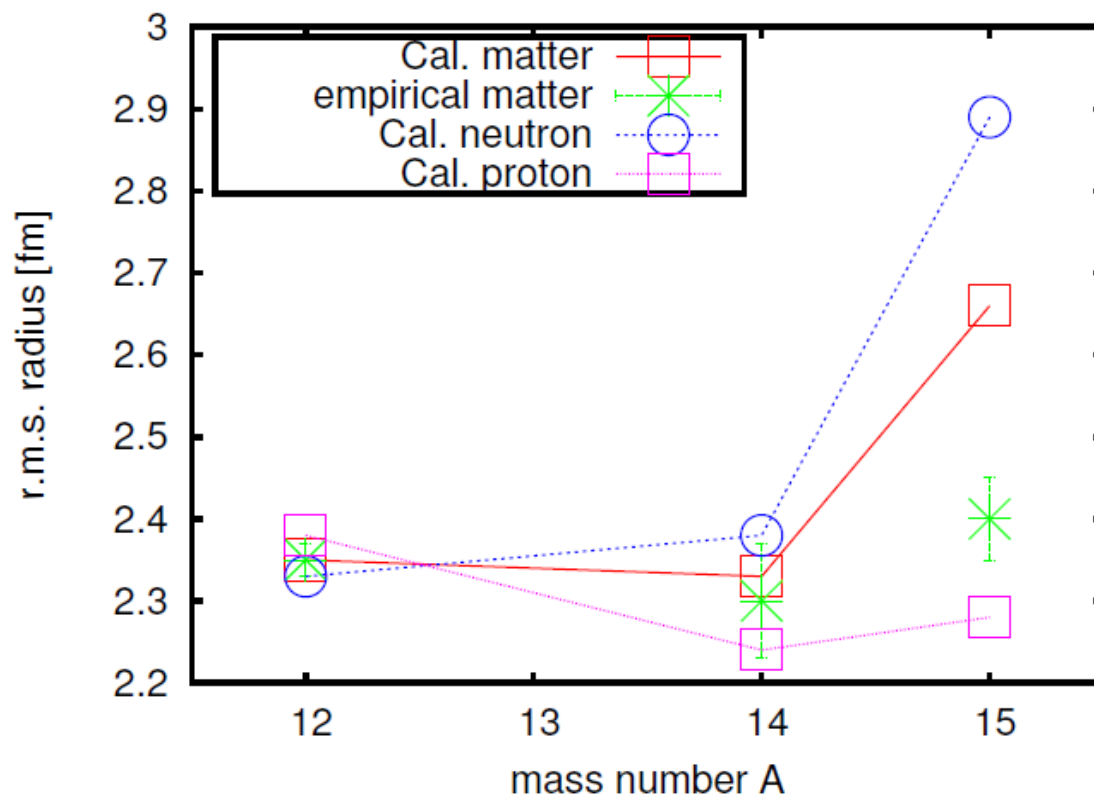
- ◆  $r^p = 2.15 \sim 2.45$  fm (intervals of 0.05 fm)
- ◆  $r^n = r^p + 0.15 \sim r^p + 0.95$  (intervals of 0.1 fm)

## Binding energy and radius

### Binding energy

	Cal. (MeV)	Exp.(MeV)
$^{14}\text{C}(0^+)$ :	-105.6	-105.28
$^{15}\text{C} 1/2^+$ :	-106.7	-106.50
Ex. $5/2^+$ :	2.0	0.74

### Radius

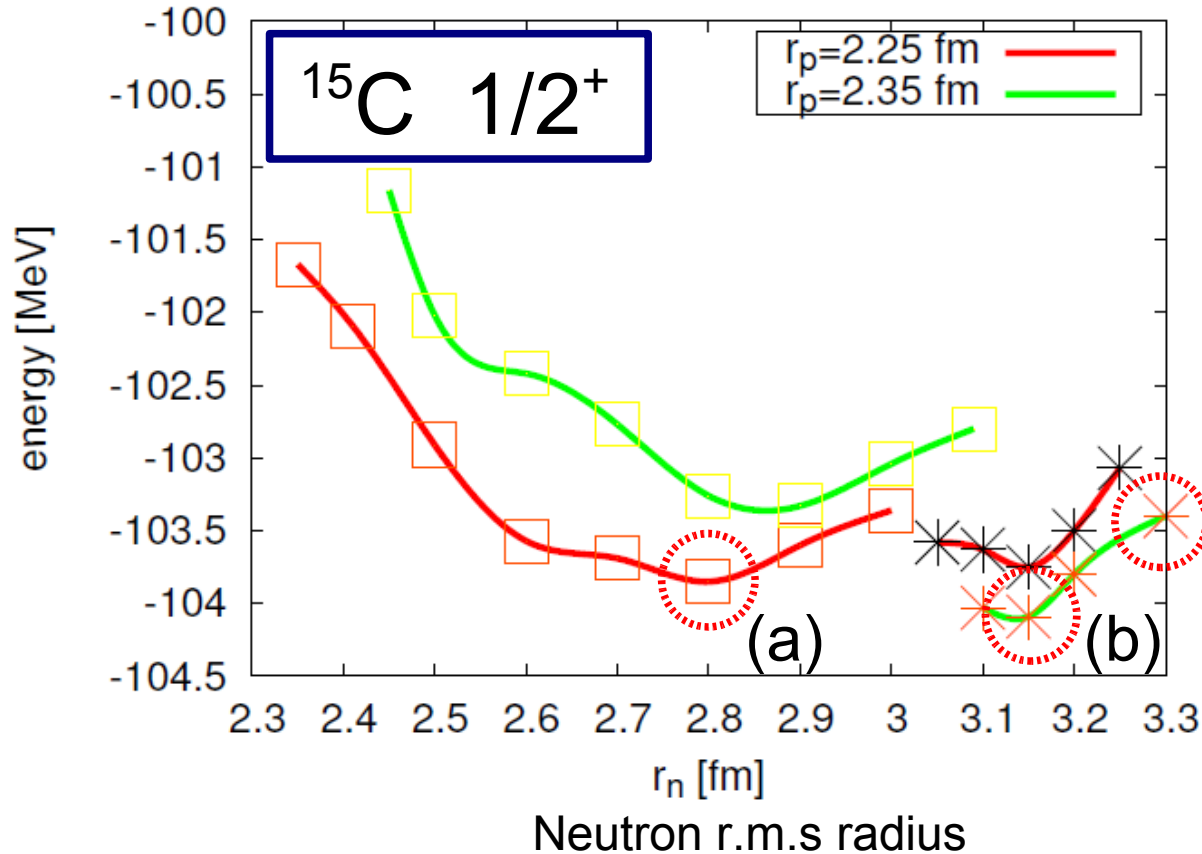


◆ Ground state spin-parity and binding energies are reproduced

◆ Large neutron radius  
→ Development of halo structure

◆  $^{15}\text{C}$  has larger proton radius than  $^{14}\text{C}$   
→ core excitation?

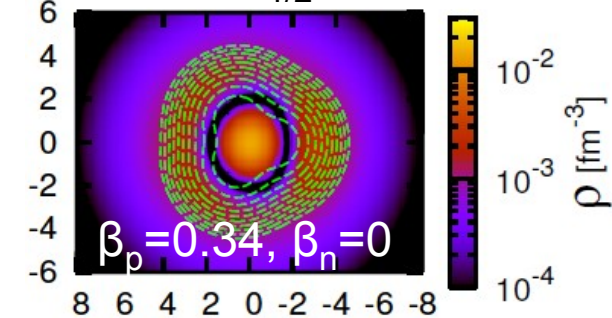
# Energy surface of $1/2^+$ state



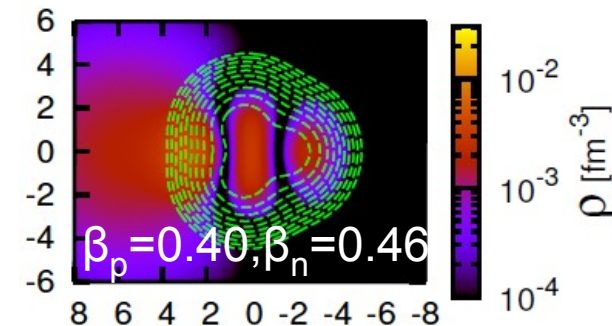
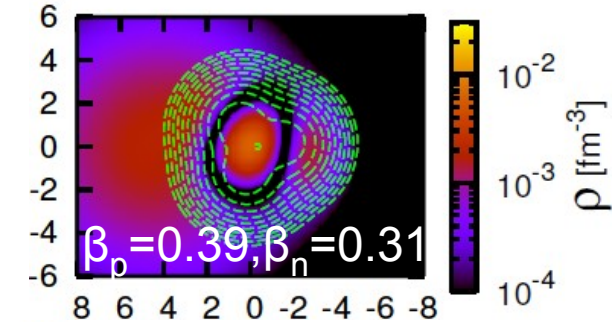
- Structure change around 3.0 fm  $\rightarrow$  Conf. (a) and (b)
- Conf. (b) has deeper energy than Conf. (a) at  $r_p=2.35 \text{ fm}$

Color plot:  
Density distribution of the most weakly-bound neutron  
Contour line:  
Density distribution of  $^{14}\text{C}$

- Conf. (a):  $1s_{1/2}$  orbit

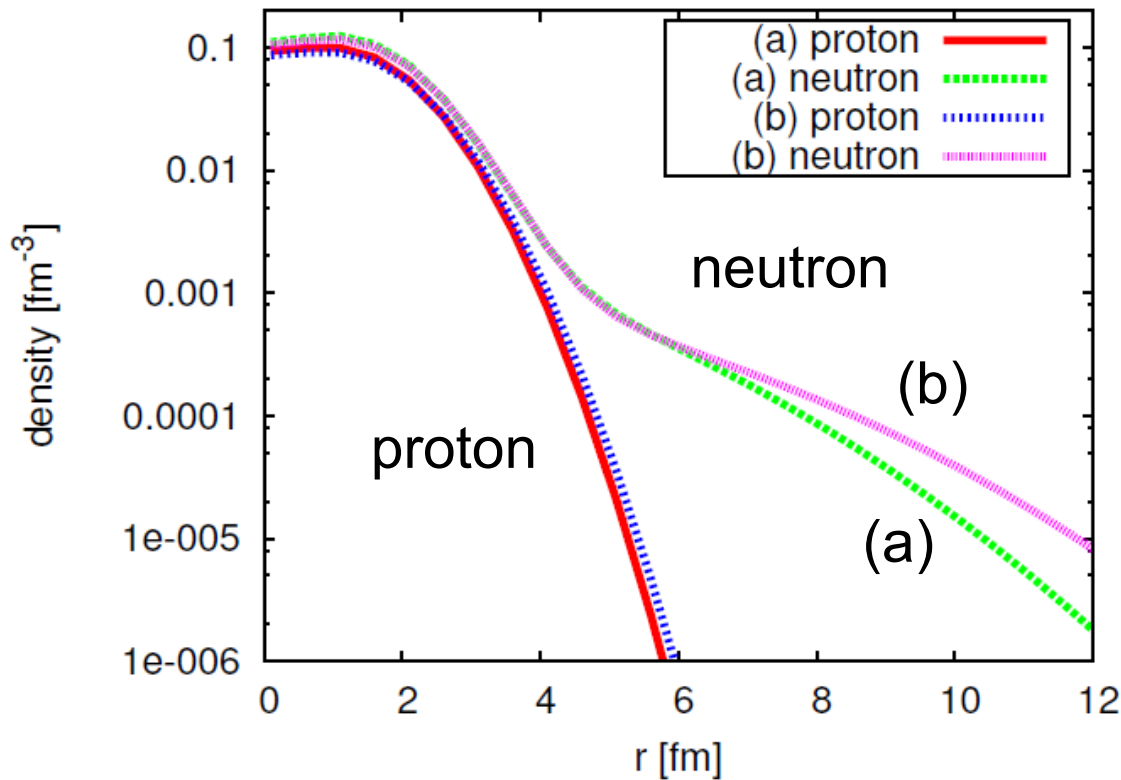


- Conf. (b): prolate deformation

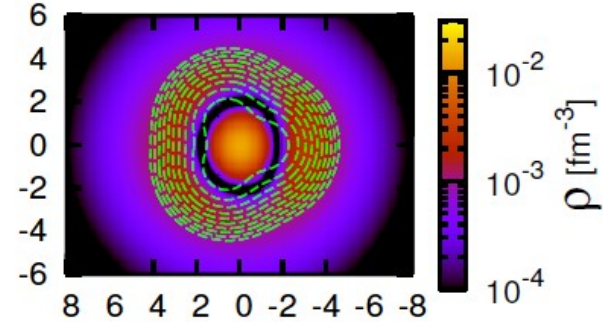


# Radial density distribution of $1/2^+$ state

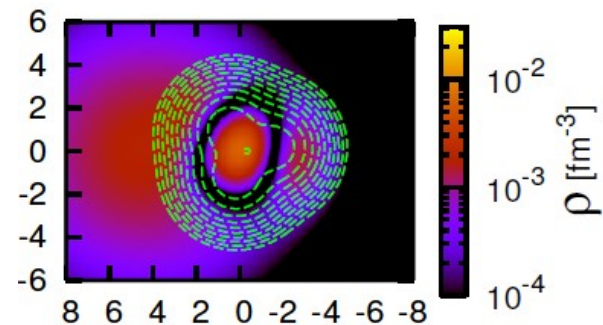
$^{15}\text{C}$   $1/2^+$



◆ Conf. (a):  $1s1/2$  orbit



◆ Conf. (b): prolate deformation

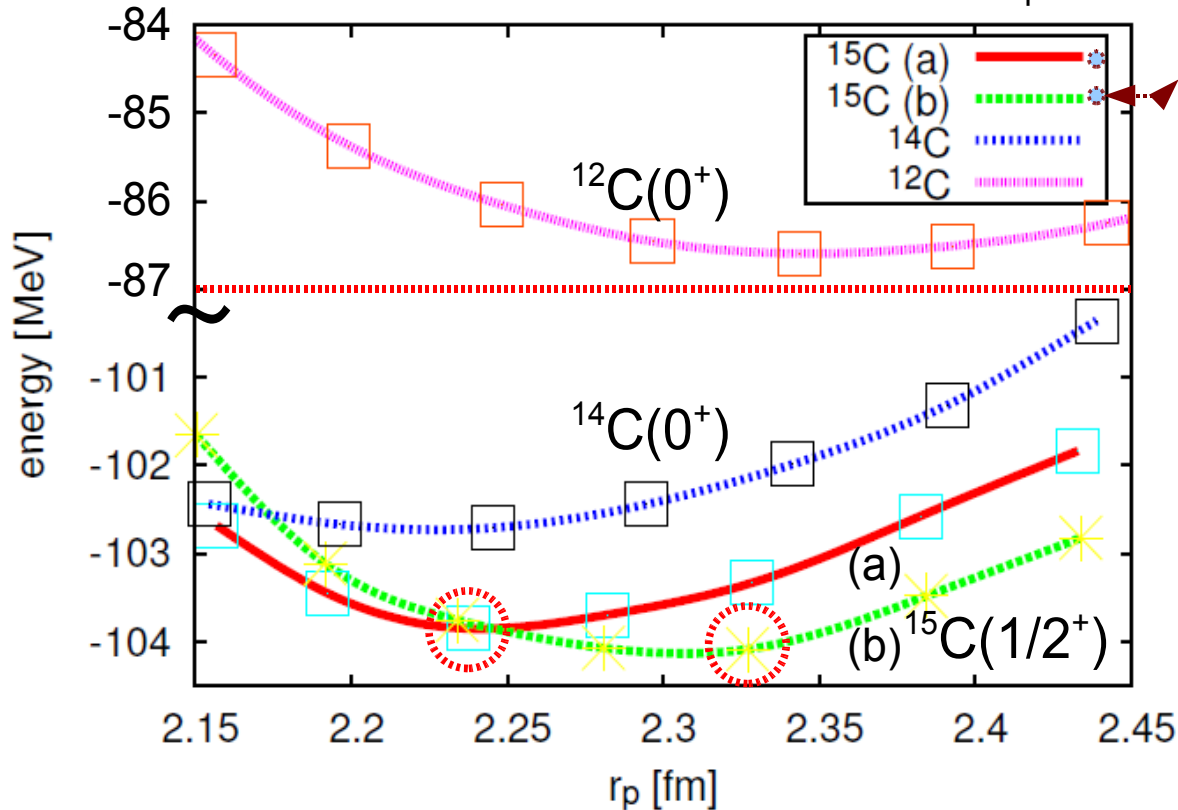


- ◆ Both Conf. (a) and Conf. (b) have halo like spatial extension of neutron density distribution

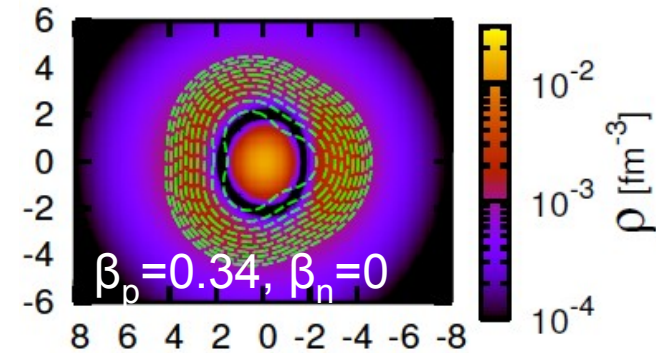


# Energy surface of $1/2^+$ state

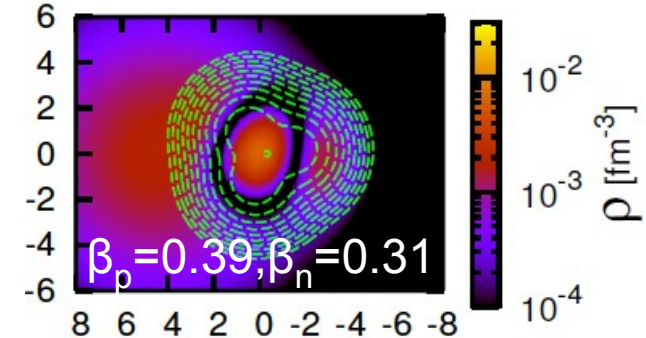
Horizontal axis: proton r.m.s radius  $r_p$   
 Optimal  $r_n$  values are chosen for each  $r_p$



◆ Conf. (a):  $1s_{1/2}$  orbit



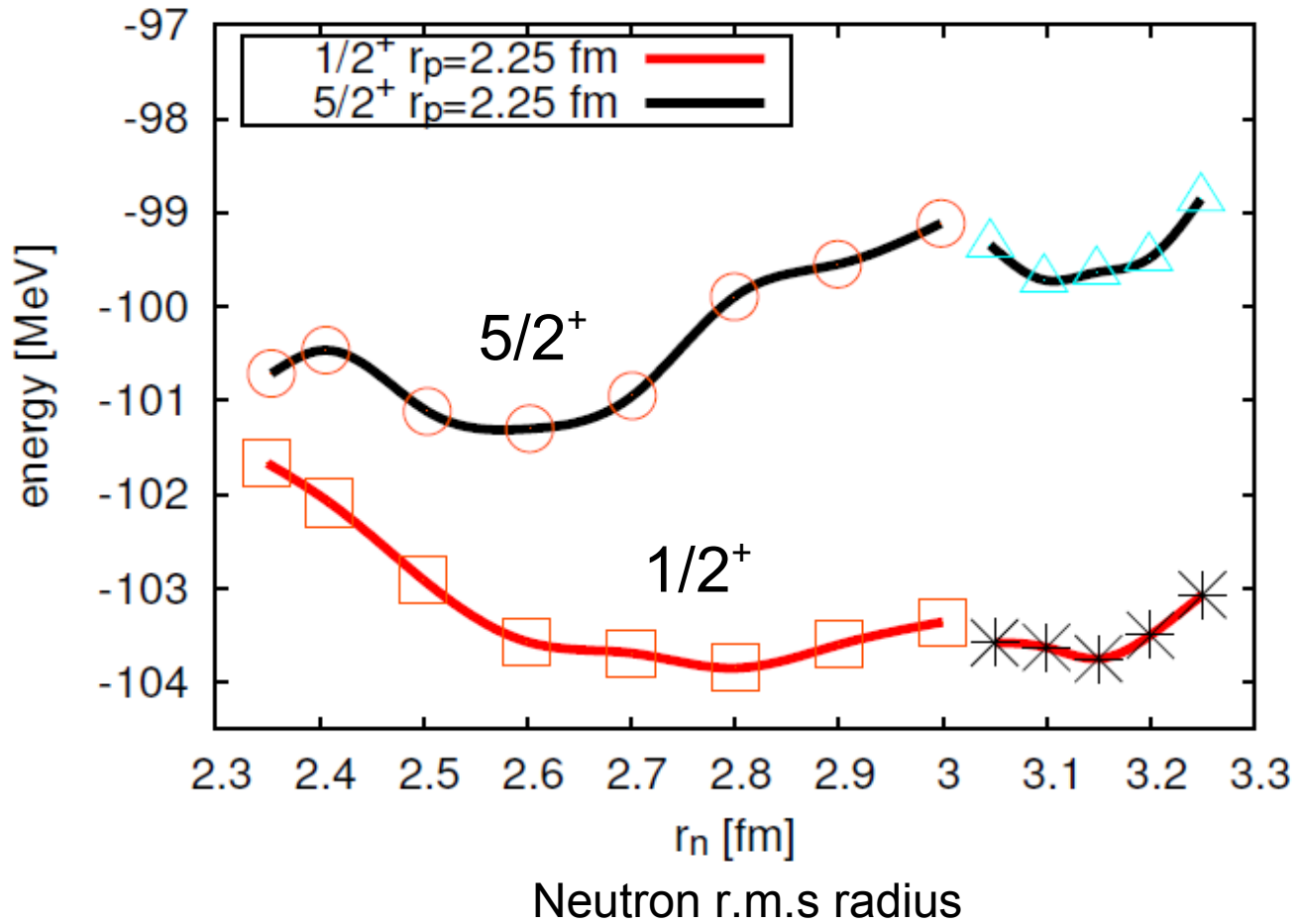
◆ Conf. (b): prolate deformation



◆ Different  $r_p$  dependence of Conf. (a) and (b)

- — Conf. (a): Similar  $r_p$  dependence with  $^{14}\text{C}$  → no core excitation
- — Conf. (b): Different  $r_p$  dependence from  $^{14}\text{C}$  → core excitation  
 → Increase of  $r_p$  is due to development of  $3\alpha$  cluster structure

# Energy surface of $5/2^+$ state



# Summary

- Structure of  $^{15}\text{C}$  has been investigated focusing on halo structure and core excitation  
—Extended framework of AMD was used.
  - Ground state binding energies of  $^{14}\text{C}$  and  $^{15}\text{C}$ , and ground state spin-parity of  $^{15}\text{C}$  ( $1/2^+$ ) are reproduced.
  - Large neutron radius and spatial extension of neutron density distribution  
→development of one neutron halo structure  
 $1/2^+$  state has larger proton radius than  $^{14}\text{C}$ .  
→Implication of core excitation
  - Two configurations are important for ground  $1/2^+$  state.
    - (a) Inert  $^{14}\text{C}$  core with valence neutron which occupy  $1s_{1/2}$  orbit
    - (b) Excited  $^{14}\text{C}$  core with development of  $3\alpha$  cluster structure  
—Energy surface as function of  $r_p$  is similar to that of ground state of  $^{12}\text{C}$ .
- Future plan:  $^{22}\text{C}$ 
  - ◆  $^{22}\text{C}$  is a two neutron halo nucleus?
  - ◆ Core excitation?