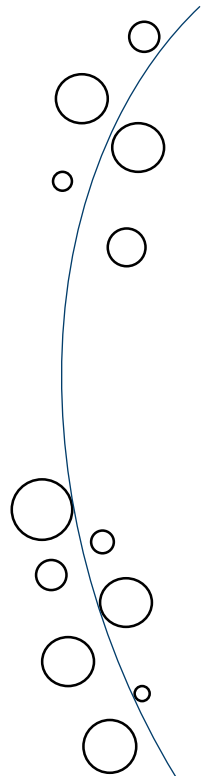


# A PANDA TRACK FINDING ALGORITHM BASED ON THE APOLLONIUS PROBLEM

25.06.2019 | ANNA SCHOLL

# INTRODUCTION

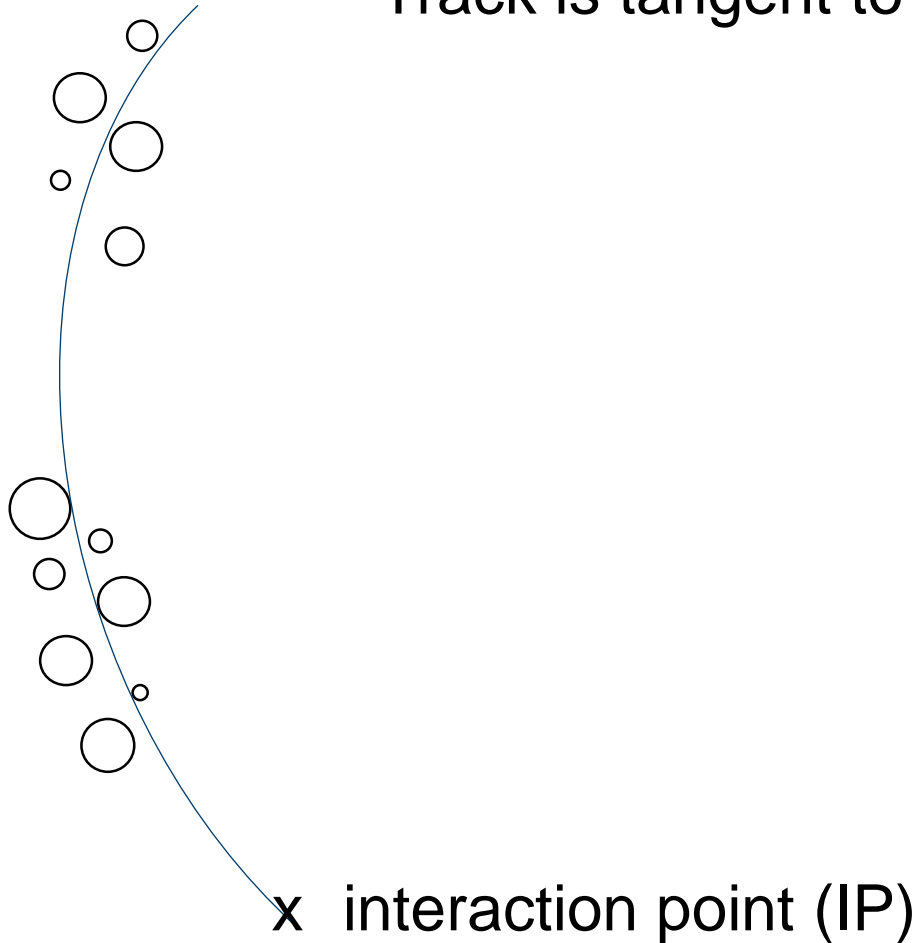


- Focussing on barrel part of the detector
- Use hits from MVD, STT, GEM detector
- Track passes through MVD and GEM hit points
- Track is tangent to STT isochrones

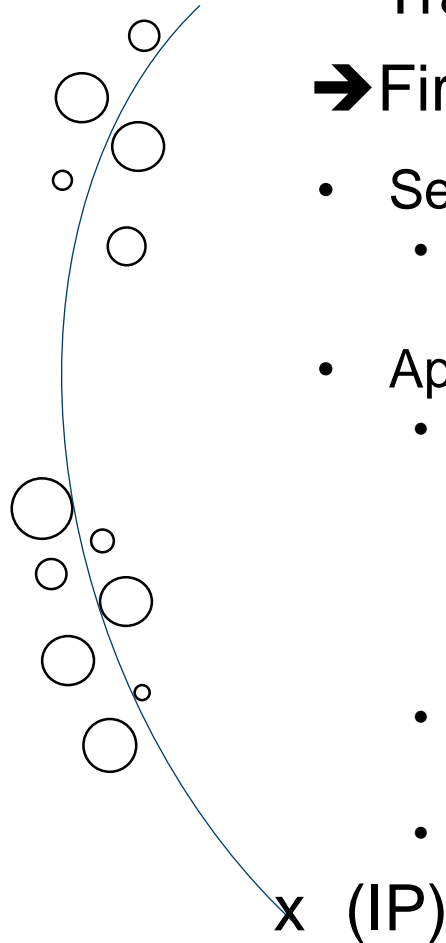
x interaction point (IP)

# HOW TO INCLUDE ISOCHRONE INFORMATION IN TRACKING ALGORITHMS?

- Track is tangent to the isochrone

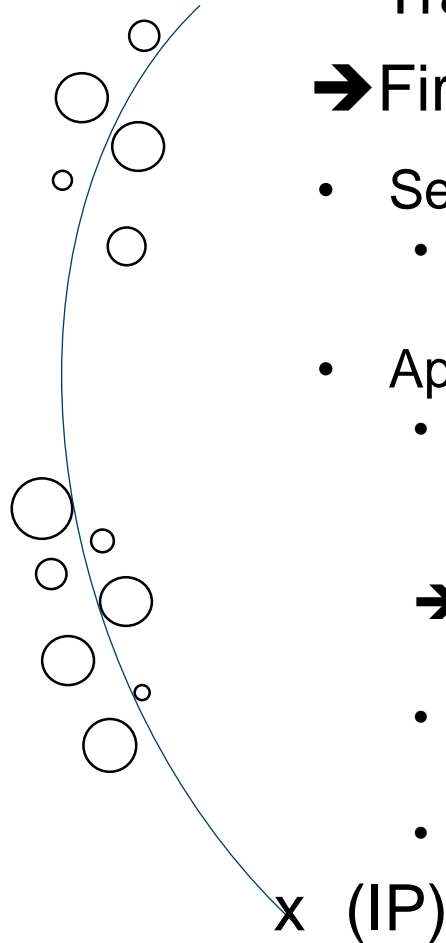


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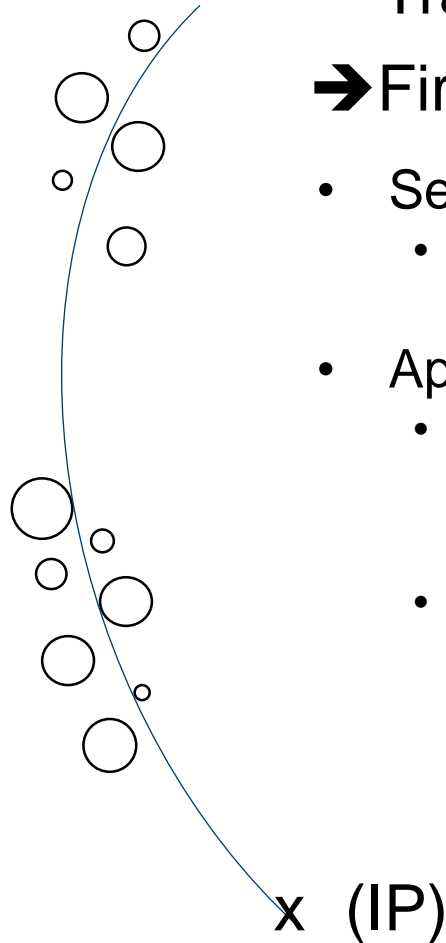
- Track is tangent to the isochrone
- ➔ First idea: **Hough transformation**
- Separate dimensions
  - 3D helix  $(R, \varphi, z) \rightarrow$  2D circle  $(R, \varphi) +$  line  $(z)$
- Apply Hough transform to detect tracks in a set of hits
  - For each hit, generate all possible tracks compatible with it (Circles in xy plane, passing through IP and are tangent to the isochrone)
- Collect generated track parameters for all hits (2D Hough Space)
- Count: most frequent values = parameters of actual tracks

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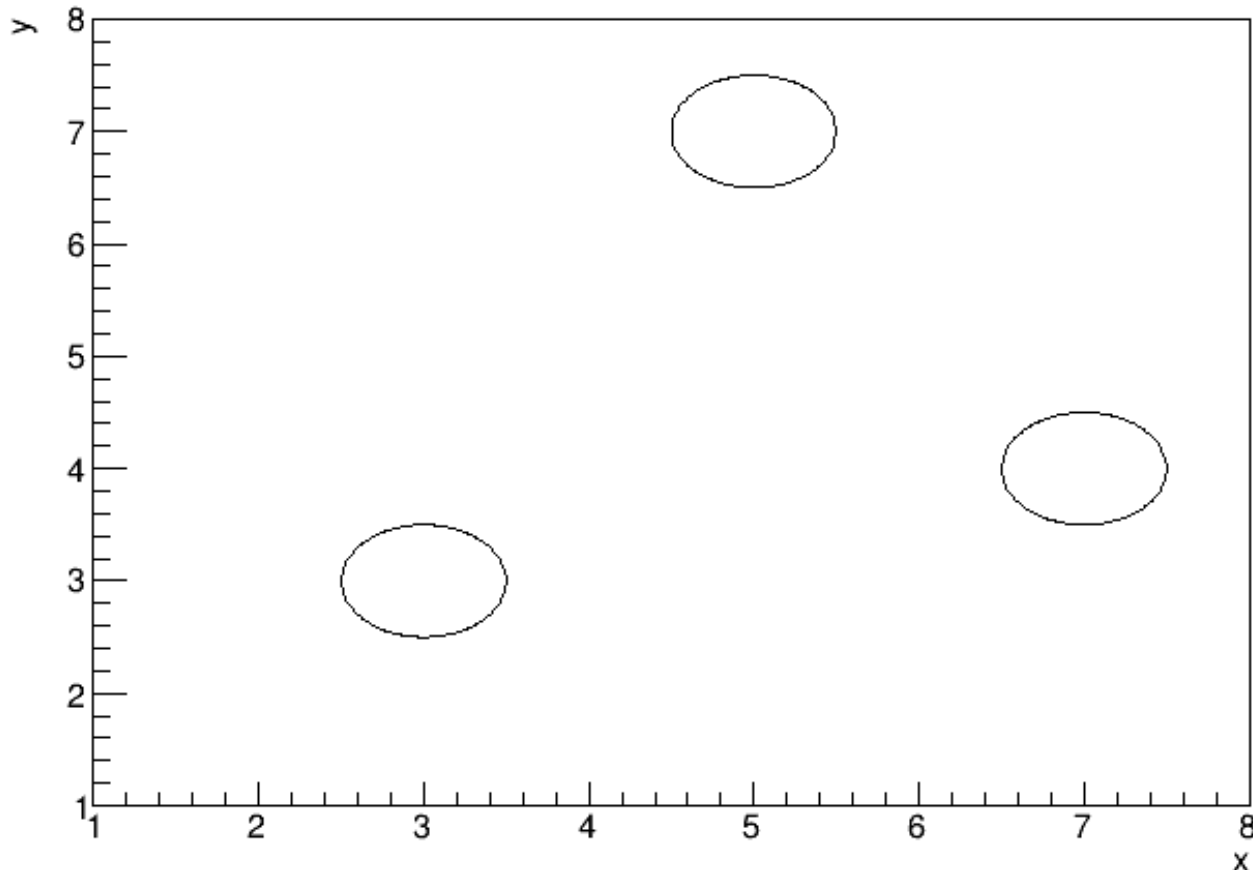


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- Apply Hough transform to detect tracks in a set of hits
  - **Problem:** a lot of false combinations for increasing number of tracks per event
  - **Idea:** reduce combinatorics by using 2 Isochrones and IP

➔ **problem of Apollonius**

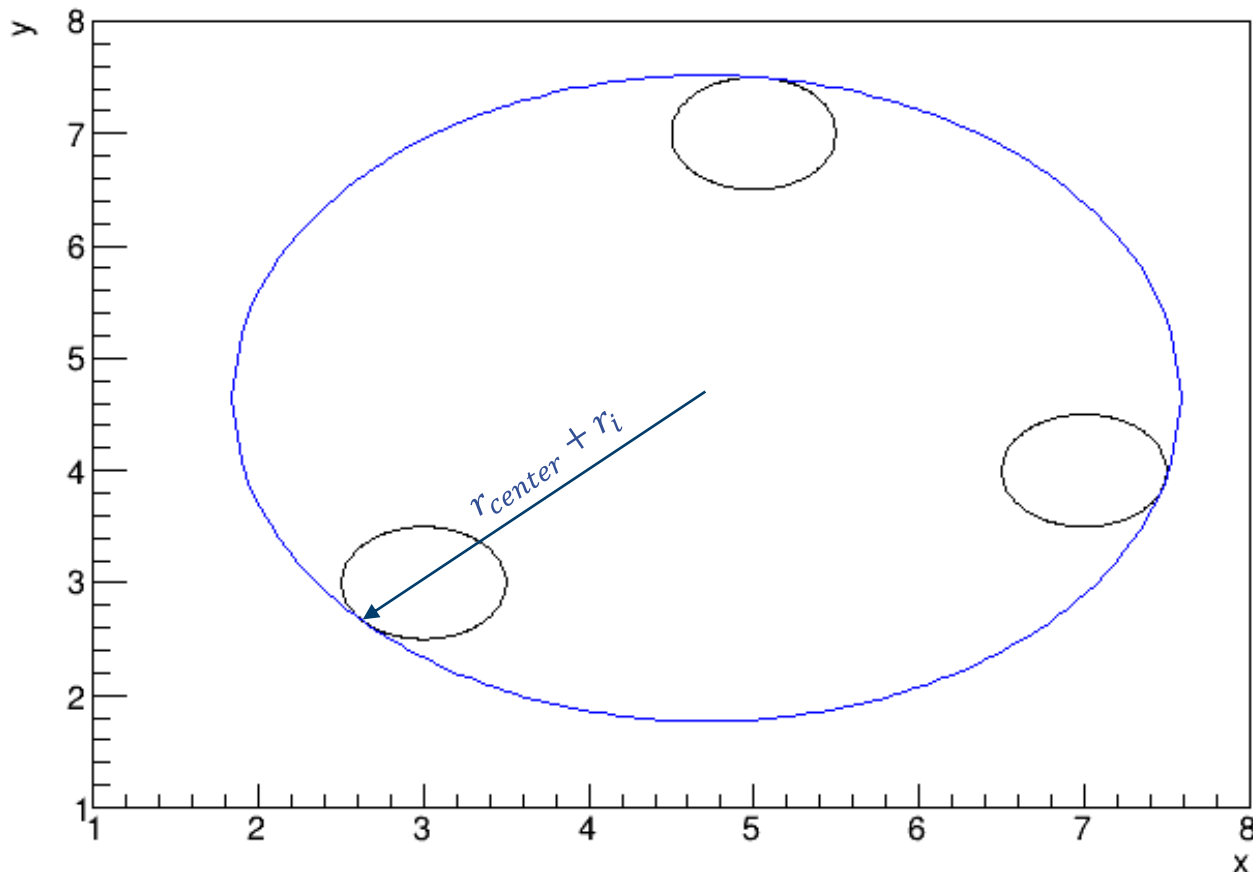
# APOLLONIUS PROBLEM

- General Apollonius problem for 3 circles:  
Find circles that are tangent to three given circles in a plane



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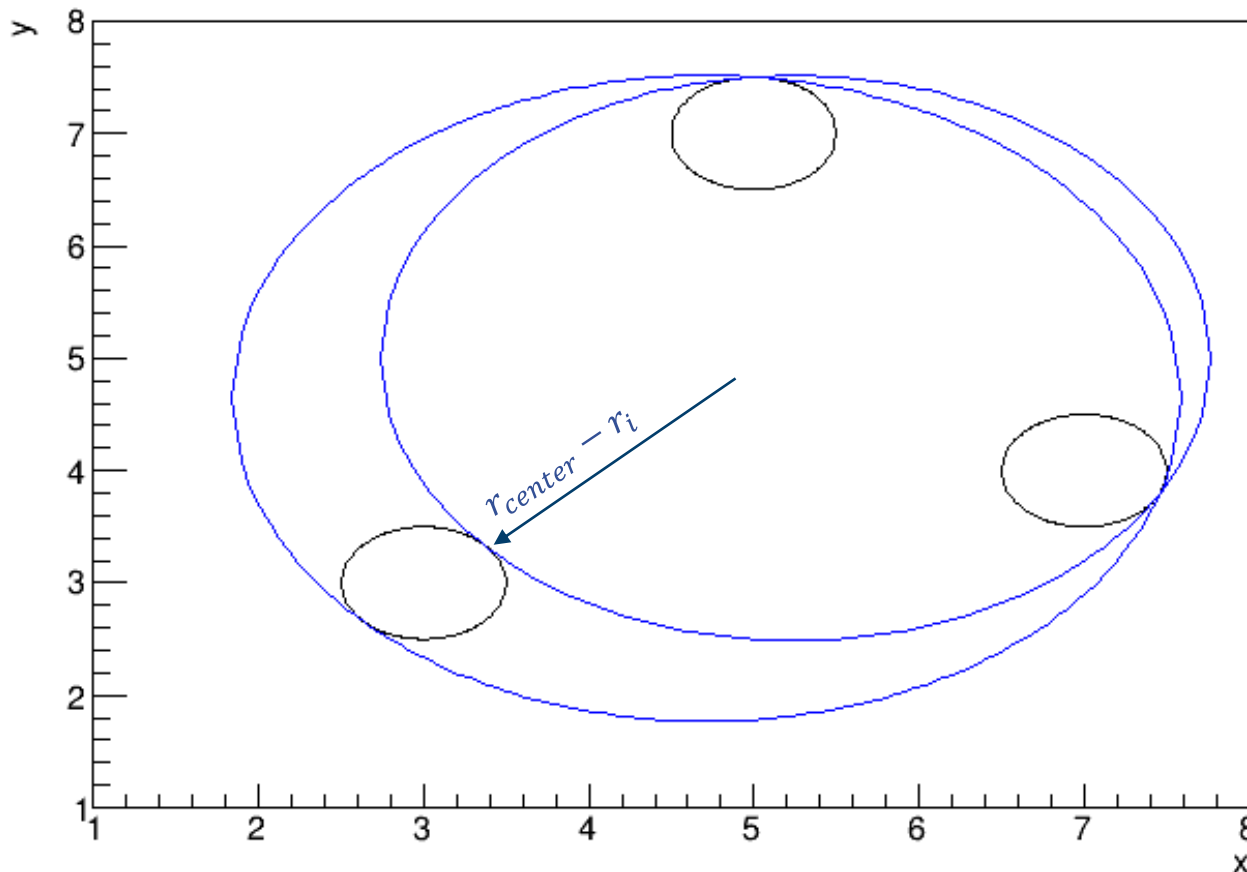
For each circle there are 2 possibilities for an Apollonius circle

1.  $r_{Apollonius} = r_{center} + r_i$



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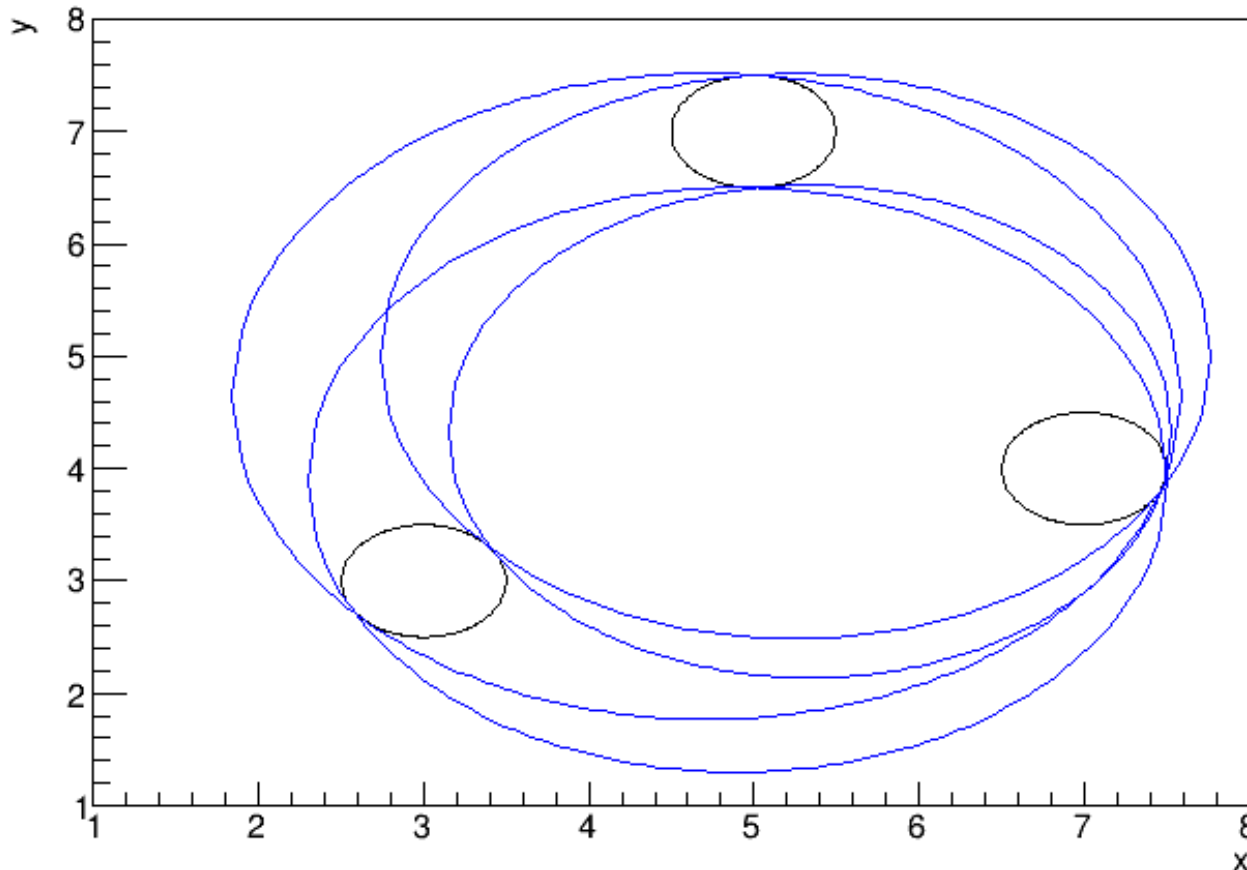


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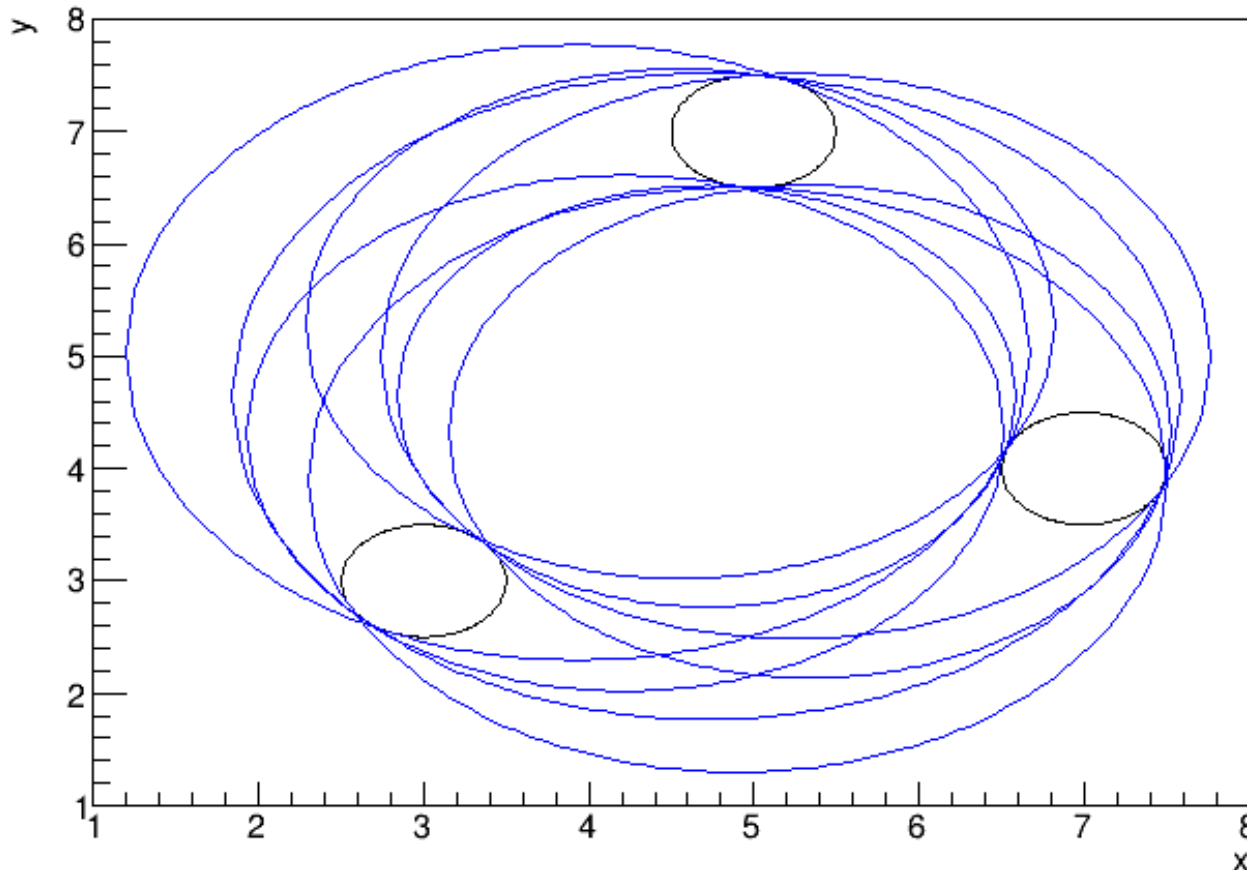


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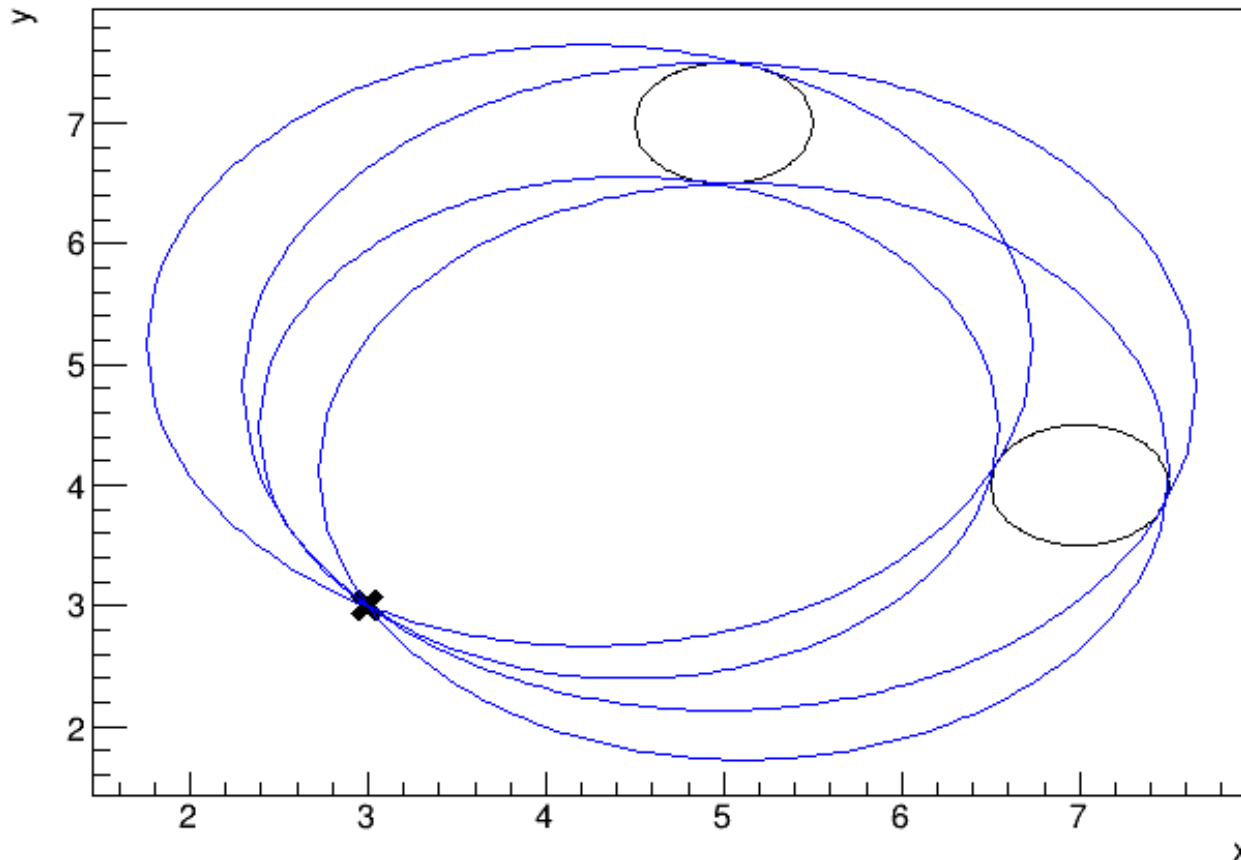
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1.  $r_{\text{Apollonius}} = r_{\text{center}} + r_i$
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In total  $2^3 = 8$   
Apollonius circles

# APOLLONIUS PROBLEM

- Special case: two circles and one point



For each circle there are 2 possibilities for an Apollonius circle

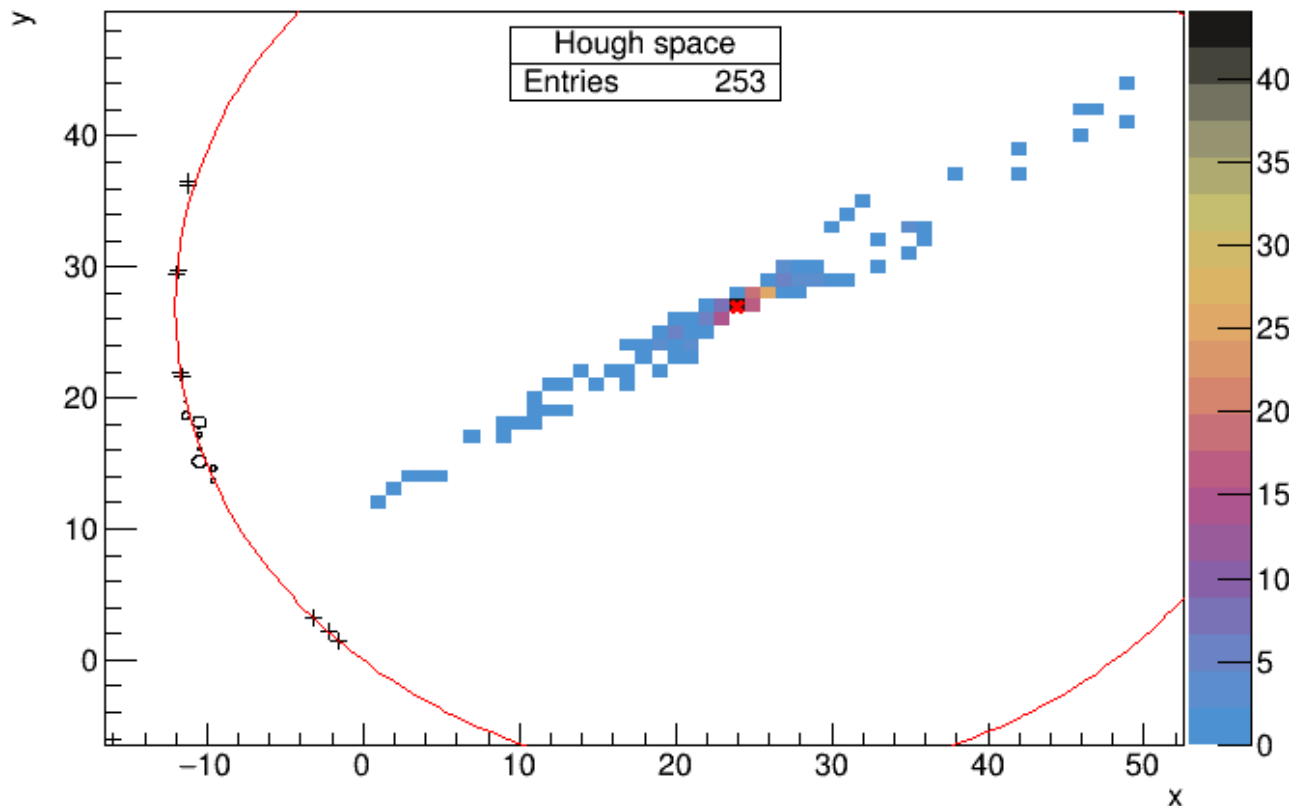
1.  $r_{\text{Apollonius}} = r_{\text{center}} + r_i$
2.  $r_{\text{Apollonius}} = r_{\text{center}} - r_i$

In total  $2^2 = 4$   
Apollonius circles

# HOUGH TRANSFORMATION BASED ON APOLLONIUS PROBLEM

Implementation in PandaRoot and testing with simulated data

Example for one Track

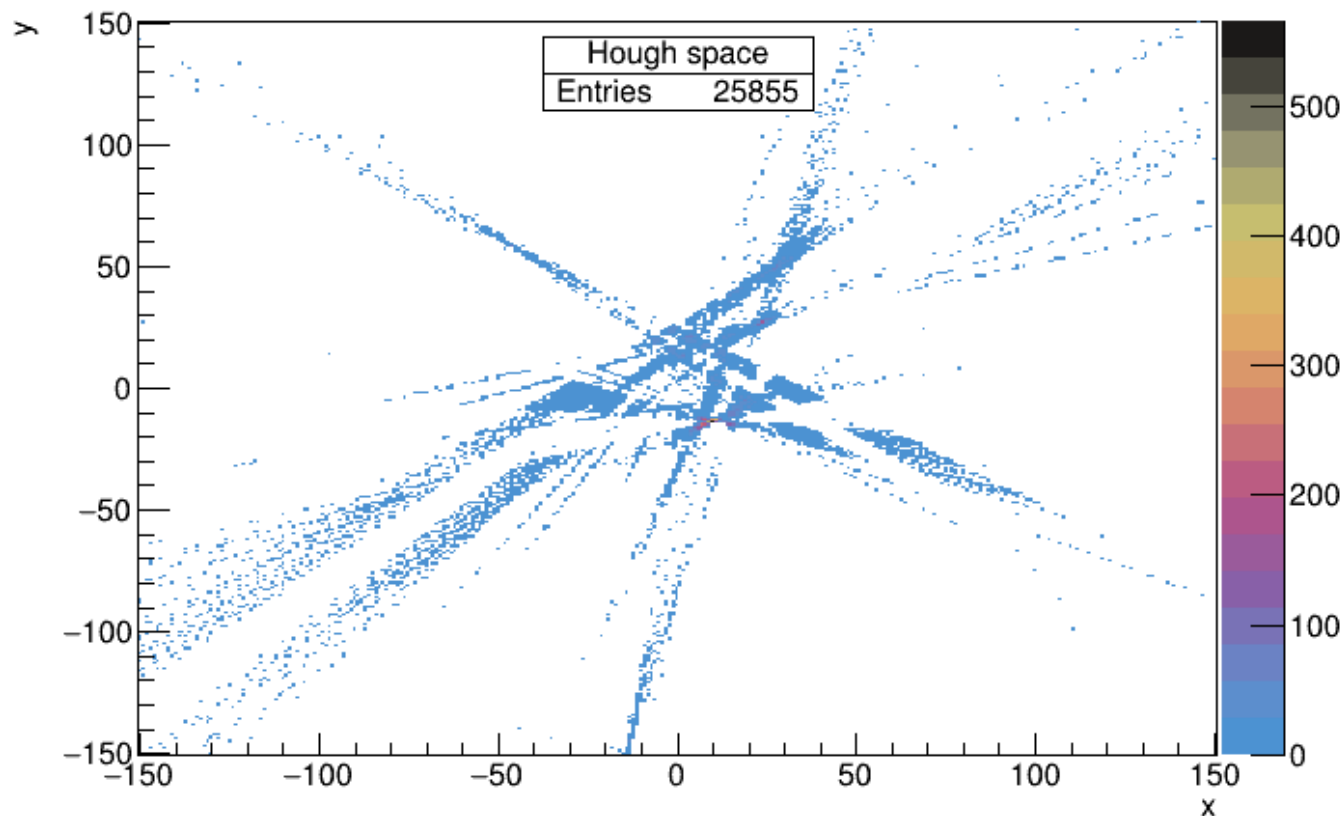


- Works quiet well if track candidate is known (IdealTrackFinder)

# HOUGH TRANSFORMATION BASED ON APOLLONIUS PROBLEM

Implementation in PandaRoot and testing with simulated data

Example for one Event

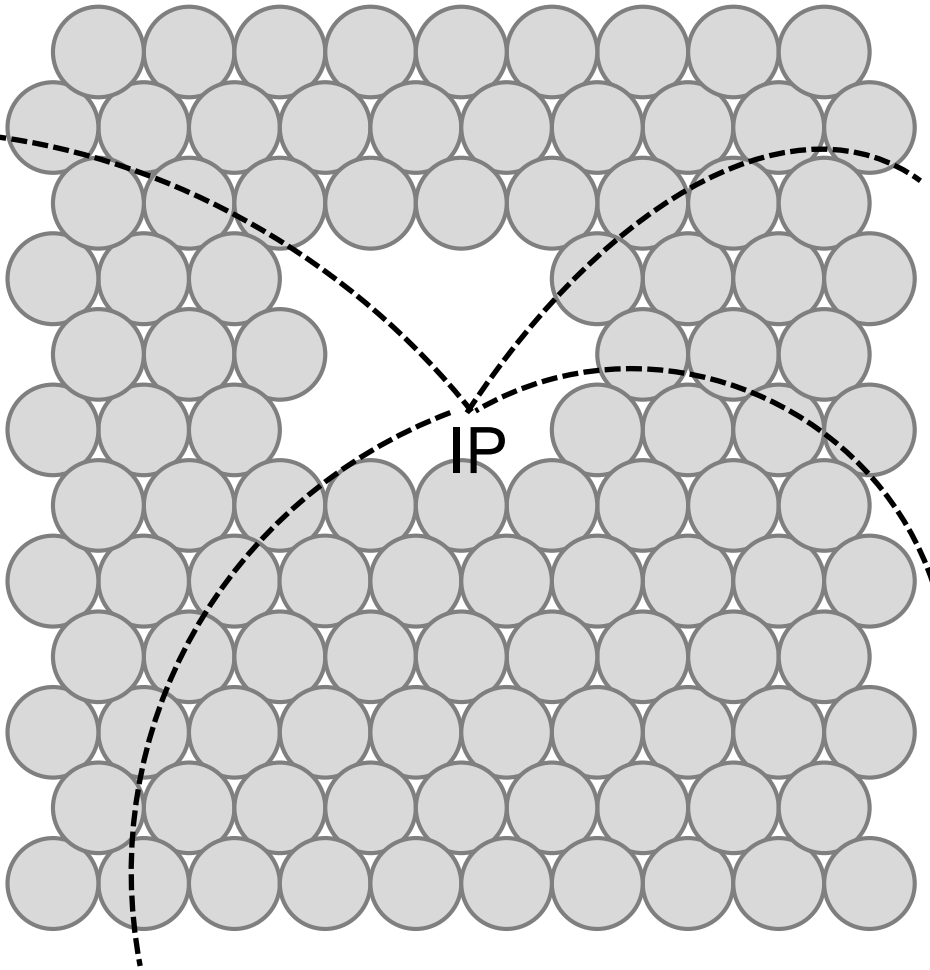


- Works quiet well if track candidate is known (IdealTrackFinder)
- For one event (many tracks): high combinatorics with (still) many false combinations

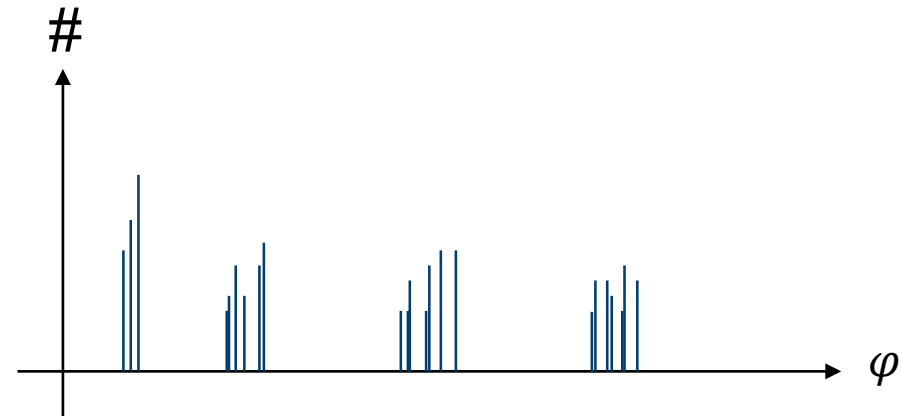
# PRESELECTION

- In reality track candidates are not known
  - Using Apollonius transform for all tracks in one event is very time consuming and leads to a lot of false combinations
- ➔ preselection for possible tracklets is needed
- Idea:
    - preselection by cutting on  $\varphi$ -plane: dividing x-y-plane dynamically in sectors

# CUT ON $\varphi$ -PLANE

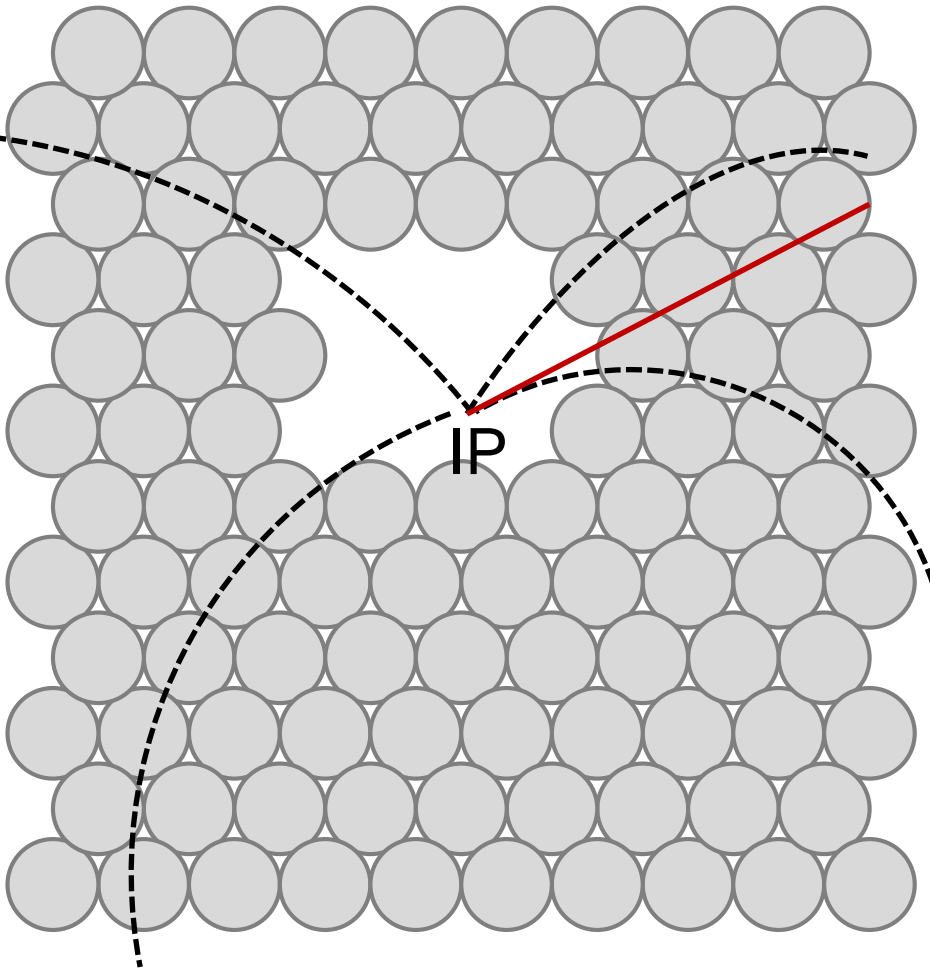


- Filling  $\varphi$ -values of all hits into histogram:

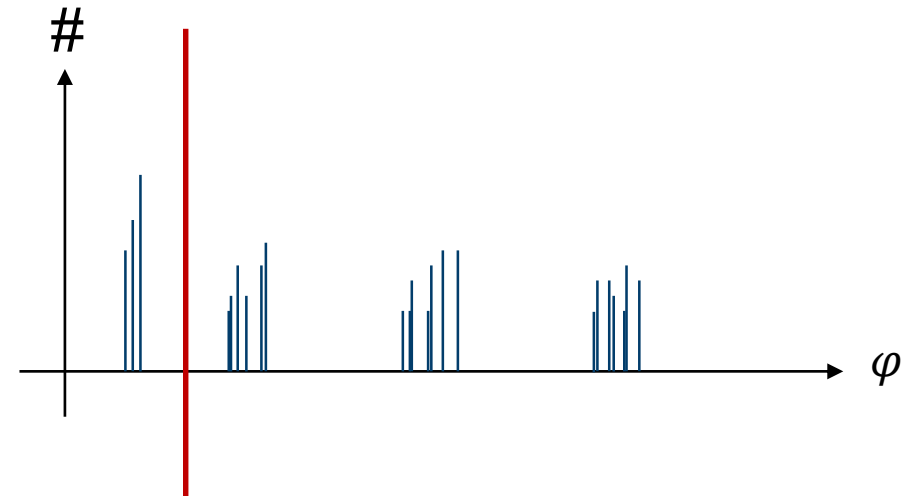




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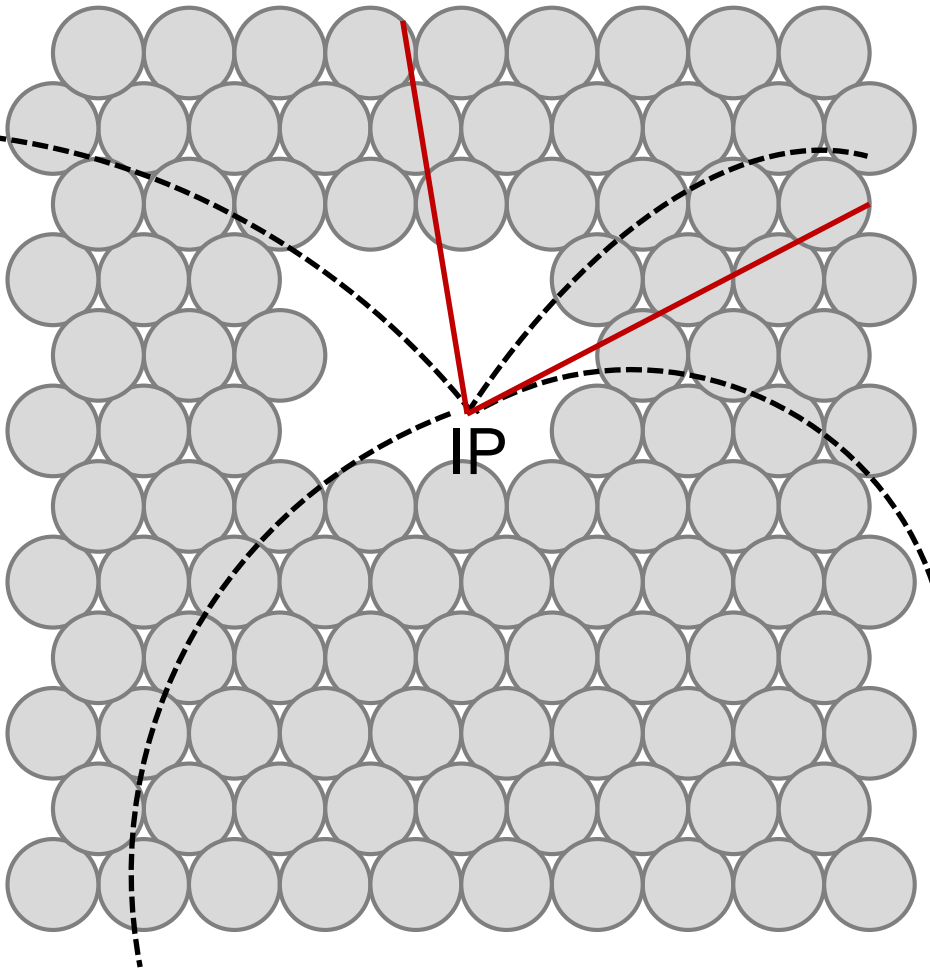


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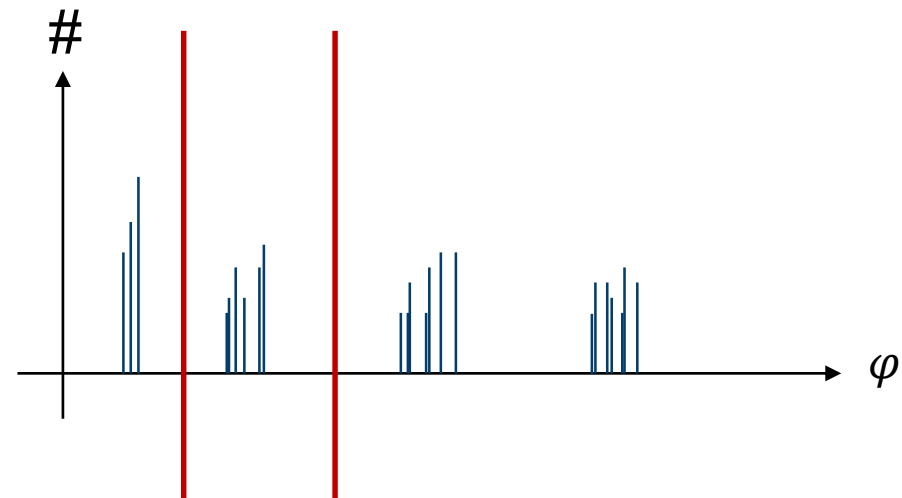


- Divide in  $\varphi$  - sectors

# CUT ON $\varphi$ -PLANE

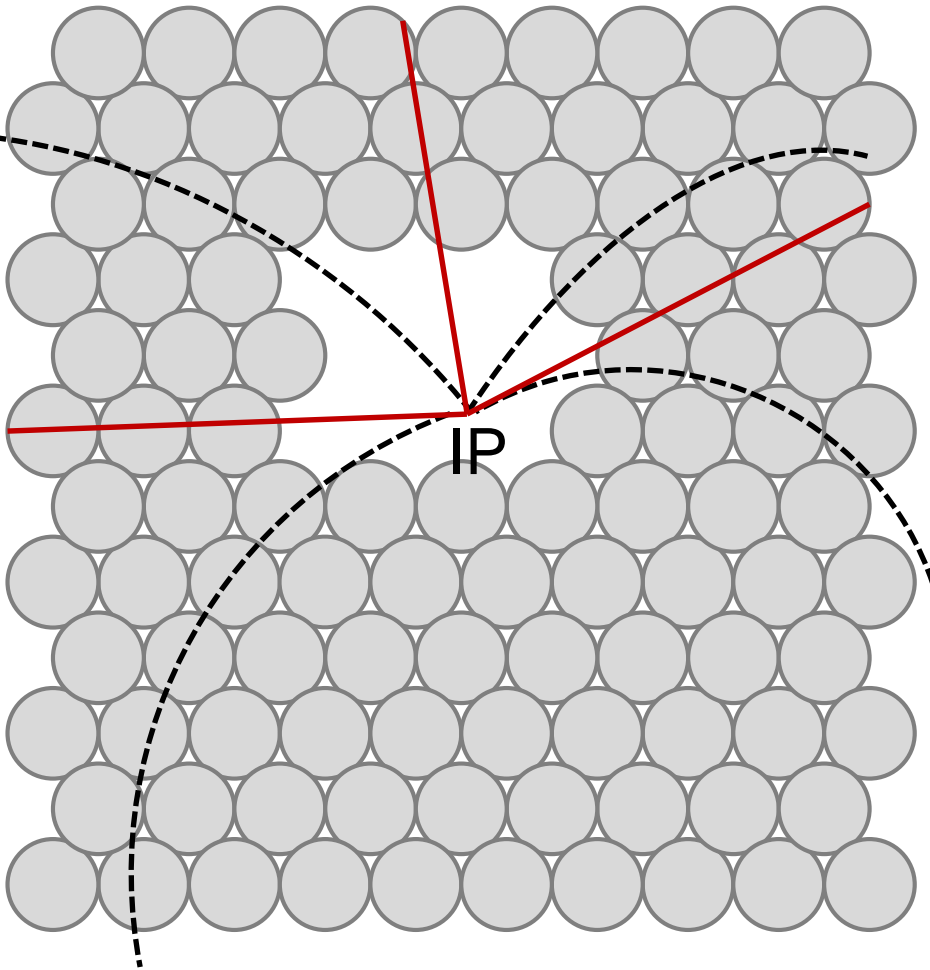


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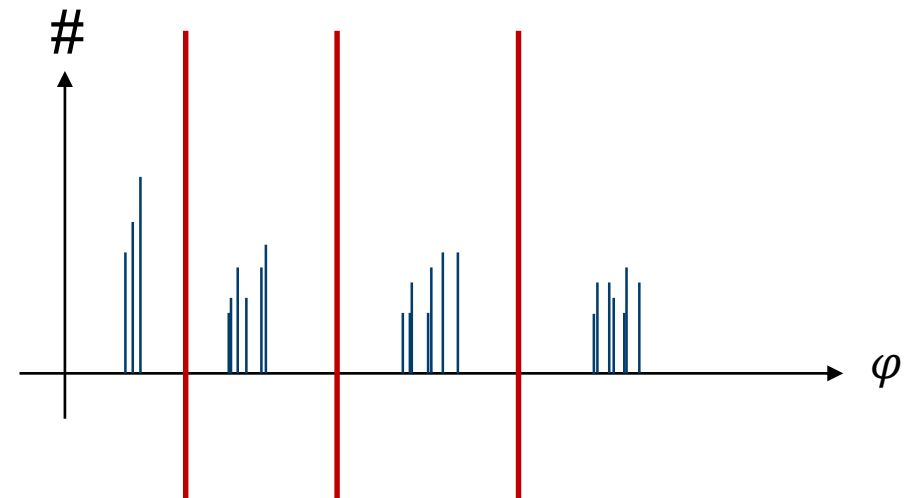


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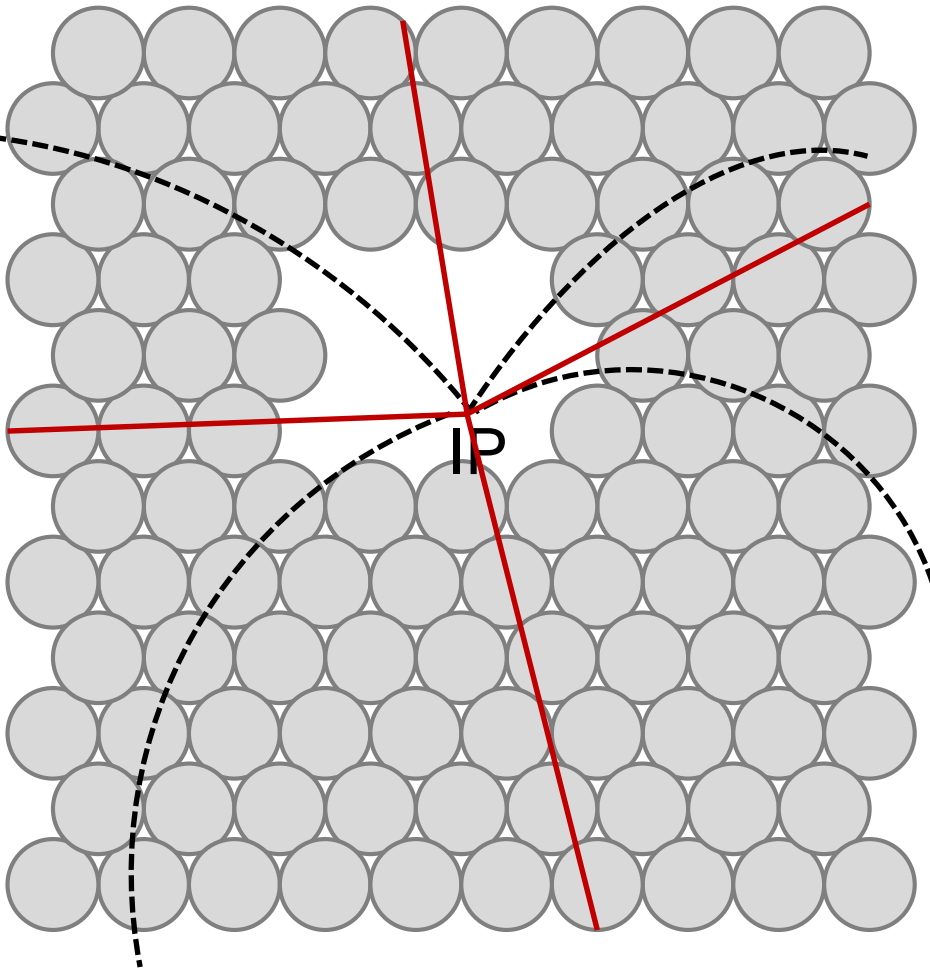


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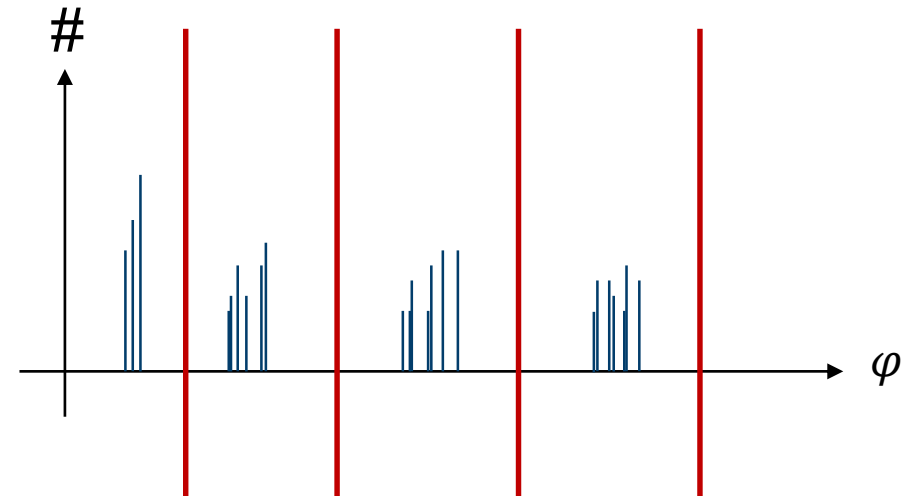


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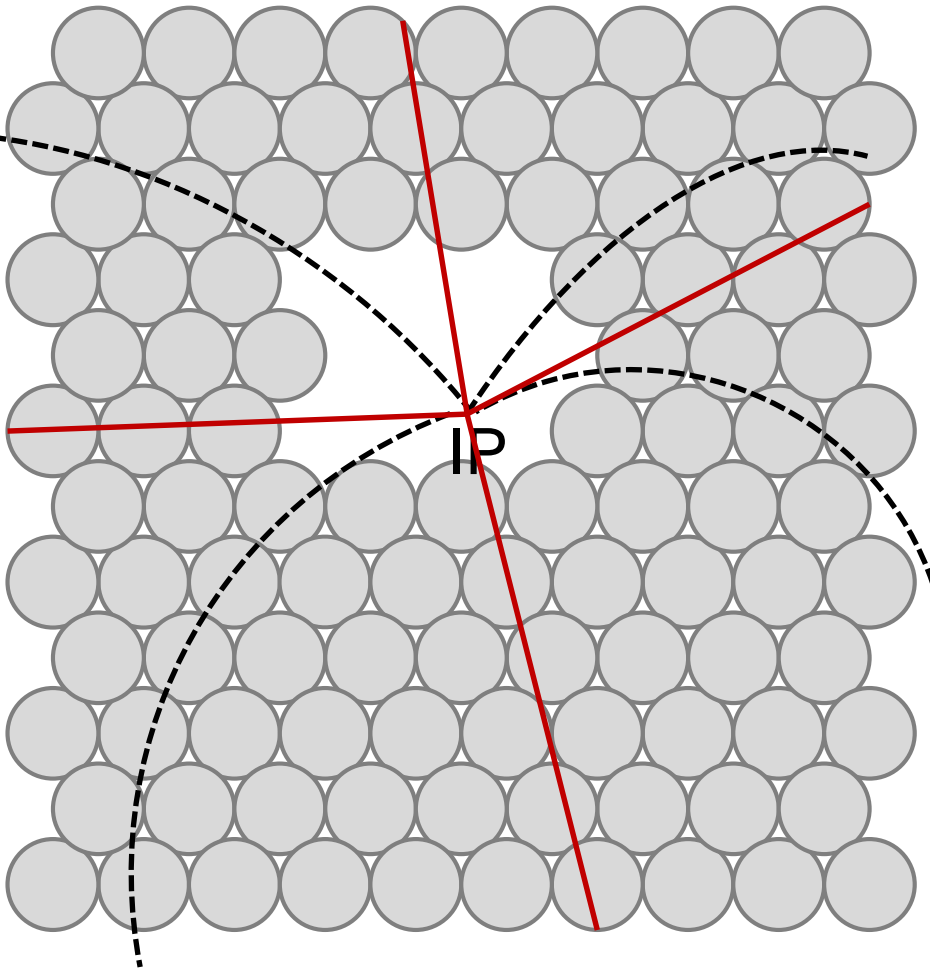


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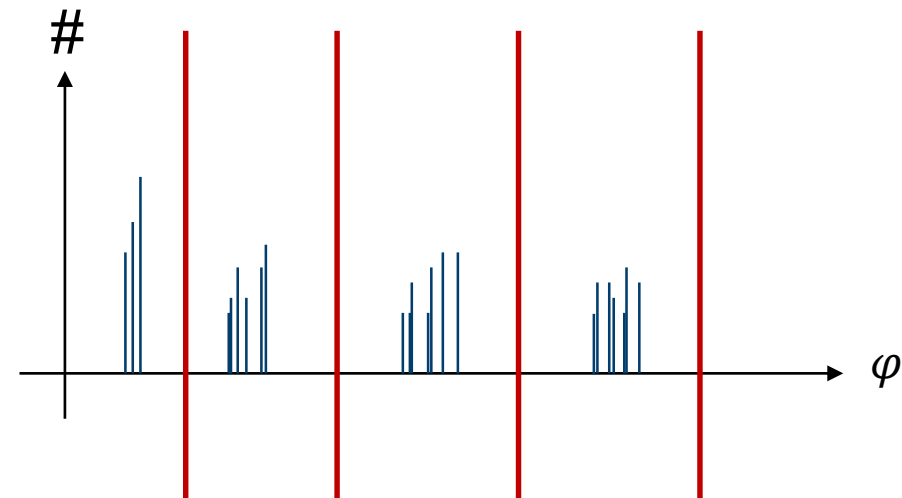


- Divide in  $\varphi$  - sectors
- Hough transformation for all hits in one sector

# CUT ON $\varphi$ -PLANE



- Filling  $\varphi$ -values of all hits into a histogram:



- Divide in  $\varphi$  - sectors
- Hough transformation for all hits in one sector
- Could be problematic for low  $p_T$  -Tracks

# CONCLUSION

- Implementation of Hough transformation based on the Apollonius problem in PandaRoot
- Testing with single tracks found by the Ideal Track Finder
- High combinatorics for many tracks per events
- Idea for preselection of track candidates:
  - Cut on  $\varphi$  - plane