

Survival factors in CEP; and the elusive Odderon

See the Review
KMR: 1710.11505

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EMMI Workshop on Central Exclusive
Production (CEP) at the LHC
Heidelberg, February 6th, 2019

The two topics seem disconnected, but not so

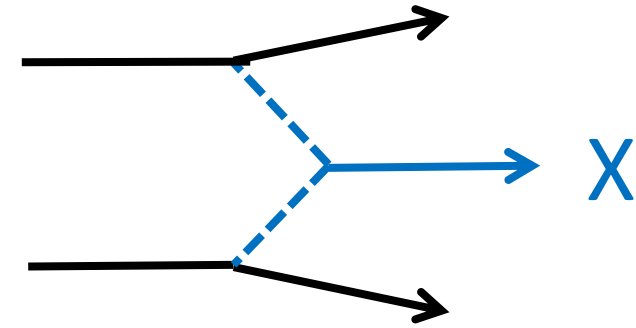
CEP must take care of gap survival factor S^2

Odderon searching must take care of absorptive corr^{ns}

$\Omega = \Omega_{\text{even}} + \Omega_{\text{odd}}$, and of background processes

Advantages of CEP

For example: $pp \rightarrow p + X + p$

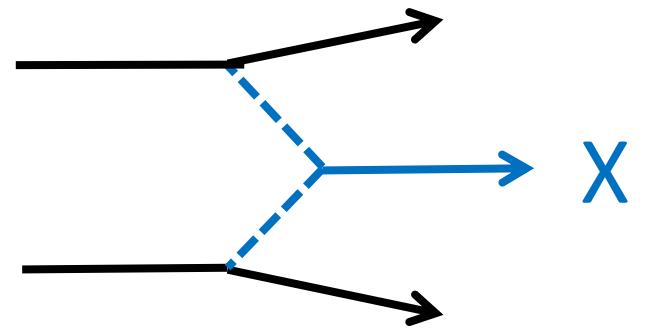


- Very clean experimental environment to explore the system X
- Mass of system X can be measured two ways
 1. From its decay products (using the central detector)
 2. From dedicated **forward proton detectors** about 200m either side of interaction point---measuring intact protons with fractional energy loss $0.015 < \xi < 0.15$ corresponding to $0.2 < M_X < 2 \text{ TeV}$

but there is a price to pay

CEP of X $pp \rightarrow p + X + p$

X may result from gg , $\gamma\gamma$ or (WW if p^*) fusion

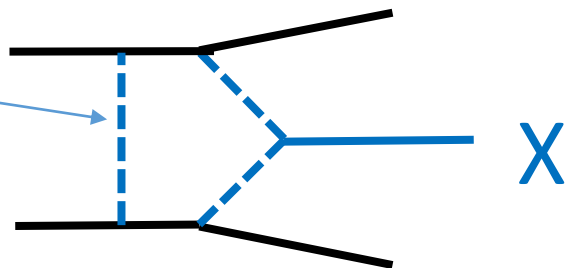


Survival of LRGs Gaps may be populated by:

Soft multiple inter^{ns} (MI) of spectator partons: mean no. $\langle n \rangle$
exclusive event---no MI---survival prob. $S^2 = P_0 \sim \exp(-\langle n \rangle)$
(eikonal suppression)

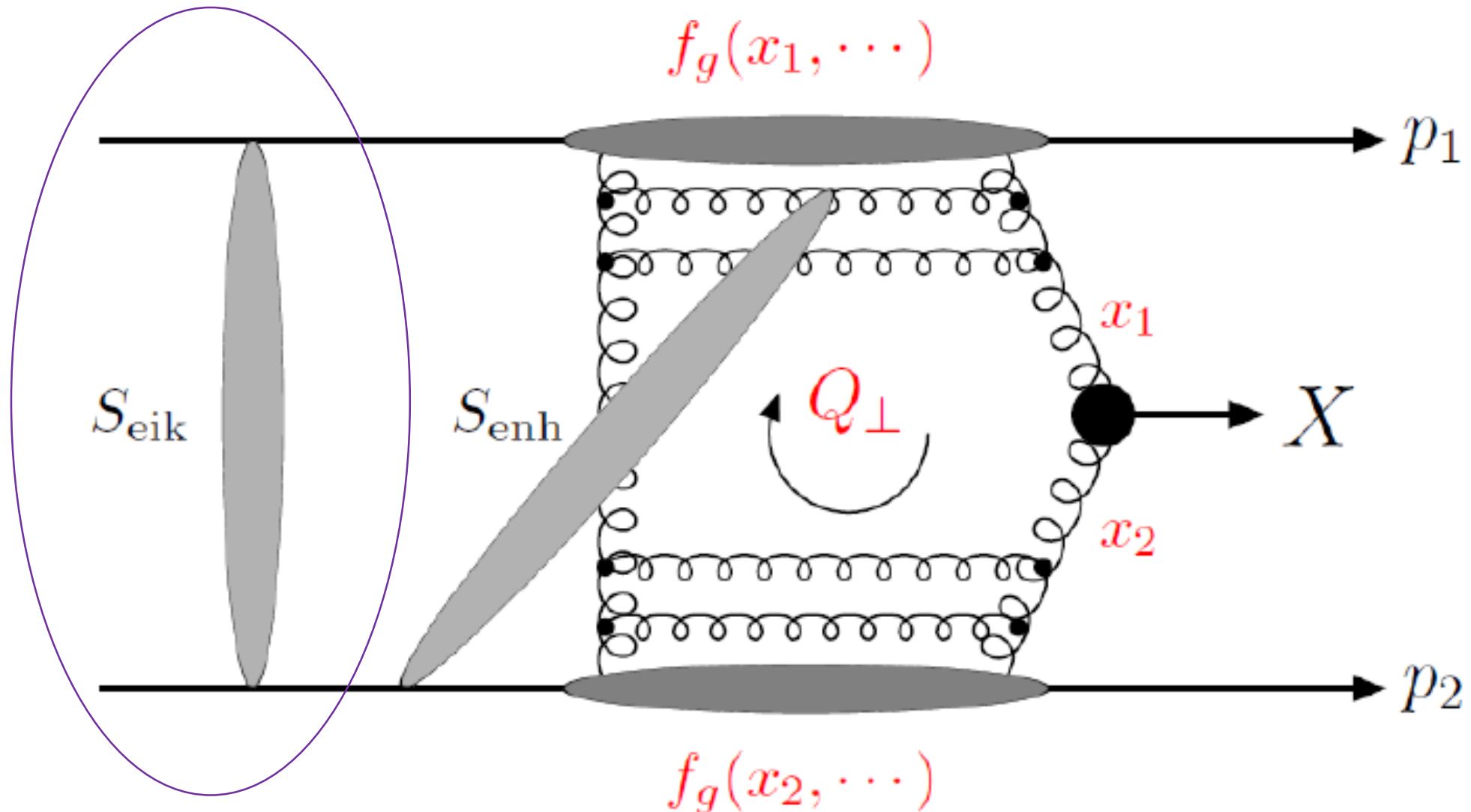
Hard QCD bremsstrahlung: X accompanied by QCD minijets
exclusive event---survival prob. $T^2 = P_0 \sim \exp(-\langle n_{\text{jets}} \rangle)$
(Sudakov suppression)

Gluon needed to
neutralize colour
for gg fusion



$$\text{Exclusive price} = S^2 T^2$$

Possibilities to populate the rapidity gaps in $pp \rightarrow p + X + p$

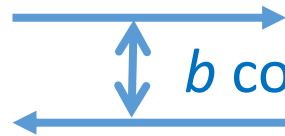


Survival factor S_{eik}^2 from eikonal parametrization

s-ch unitarity

$$SS^\dagger = I \quad (\text{let } S = I + iA) \quad \rightarrow \quad \underline{i(A^\dagger - A) = A^\dagger A}$$

Work in b space



b conserved at HE

$$\langle i | \dots | i \rangle$$

Unitarity equation

$$\underline{2 \operatorname{Im} A_{\text{el}}(b)} = \sum_n |A_{i \rightarrow n}(b)|^2 = \underline{|A_{\text{el}}(b)|^2 + G_{\text{inel}}(b)}$$

where $G_{\text{inel}}(b) = \sum_{n \neq i} |A_{i \rightarrow n}(b)|^2 < 1 =$ probability of inelastic scatt.

Solution of unitarity eq.

$$A(b) \equiv \underline{A_{\text{el}}(b)} = i(1 - e^{-\Omega(b)/2}) \quad \text{with } \operatorname{Re} \Omega(b) \geq 0$$

In terms of partial waves $l = b\sqrt{s}/2$: $\exp(2i\delta_l)$

Probability of no inelastic interⁿ at b

It is really $\exp(-\operatorname{Re} \Omega)$, but for Pom it is \sim real

$$\sigma_{\text{inel}}(b) = \sigma_{\text{tot}}(b) - \sigma_{\text{el}}(b) = \operatorname{Im} A(b) - |A(b)|^2 = 1 - e^{-\Omega}$$

At HE the inelastic contribution, G_{inel} , dominates; $\Omega(s, b) \gg 1$.
 In this so-called "black disk" limit $\text{Im}T_{\text{el}}(s, b) = 1$

Example: black disc of radius R

$$\left. \begin{array}{l} \text{for } b < R, \Omega = \infty \\ \quad (T_{\text{el}} = i) \end{array} \right\} \sigma_{\text{inel}} = 2\pi \int_0^R (1 - e^{-\Omega}) b db = \pi R^2 \quad \text{total absorption}$$

$$\left. \begin{array}{l} \text{for } b > R, \Omega = 0 \\ \quad (T_{\text{el}} = 0) \end{array} \right\} \sigma_{\text{el}} = \pi R^2 \quad \left\{ \begin{array}{l} \text{shadow due to absorption} \\ \text{leads to elastic scattering} \end{array} \right.$$

$$\sigma_{\text{tot}} = 2\pi R^2$$

Note

$$T_{\text{el}} = A_{\text{el}}$$

Since $\frac{d\sigma_{\text{el}}}{dt} = |\text{Im}T_{\text{el}}(s, t)|^2 (1 + \rho^2)$

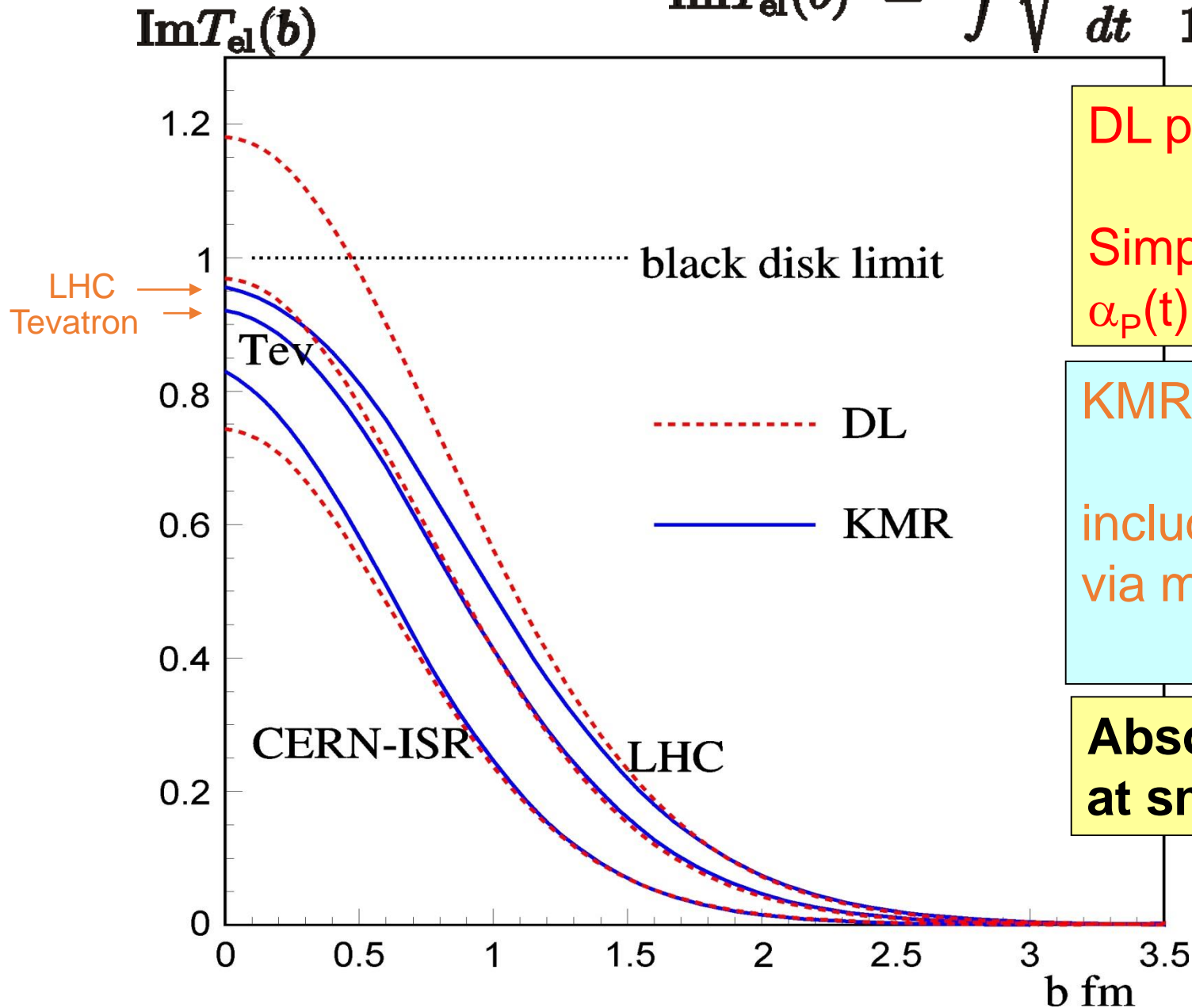
data \nearrow directly determines $\text{Im}T_{\text{el}}(s, b)$

Fourier transform
to b-space:

$$\vec{b} \longleftrightarrow \vec{q}_T \quad (-t = q_T^2)$$

wide narrow

$$\text{Im}T_{\text{el}}(b) = \int \sqrt{\frac{d\sigma_{\text{el}}}{dt} \frac{16\pi}{1+\rho^2}} J_0(qb) \frac{q dq}{4\pi}$$



DL parametrization:

Simple Pom. pole
 $\alpha_P(t) = 1.08 + 0.25t$

KMR eikonal paramⁿ

includes absorption
 via multi-Pomeron
 effects

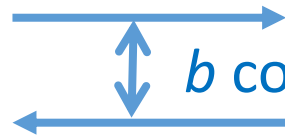
**Absorption crucial
 at small b**

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Probability of no inelastic interⁿ at b

It is really $\exp(-\operatorname{Re} \Omega)$, but for Pom it is \sim real

$$\sigma_{\text{inel}}(b) = \sigma_{\text{tot}}(b) - \sigma_{\text{el}}(b) = \operatorname{Im} A(b) - |A(b)|^2 = 1 - e^{-\Omega}$$

First Approx: one-channel eikonal; take average value of S_{eik}^2

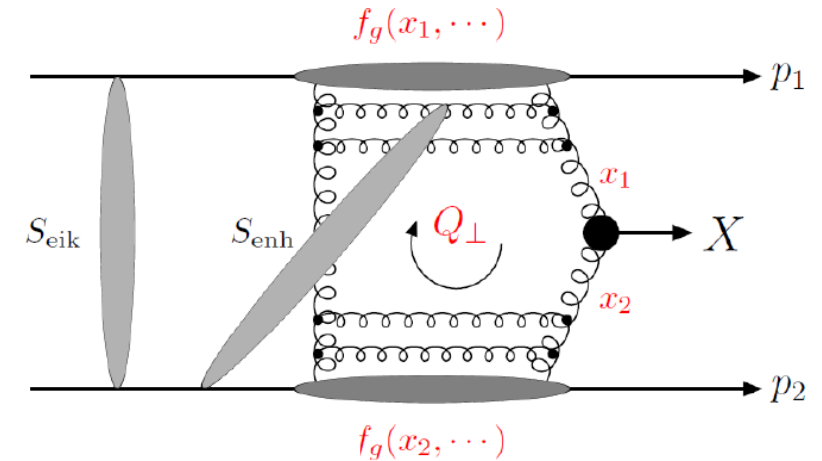
$$\langle S_{\text{eik}}^2 \rangle = \frac{\int d^2\mathbf{b}_1 d^2\mathbf{b}_2 |T(s, \mathbf{b}_1, \mathbf{b}_2)|^2 \exp(-\Omega(s, \mathbf{b}))}{\int d^2\mathbf{b}_1 d^2\mathbf{b}_2 |T(s, \mathbf{b}_1, \mathbf{b}_2)|^2}$$

where $\mathbf{b} = \mathbf{b}_1 + \mathbf{b}_2$

$$T(s, \mathbf{p}_{1\perp}, \mathbf{p}_{2\perp}) = \int d^2\mathbf{b}_1 d^2\mathbf{b}_2 e^{i\mathbf{p}_{1\perp} \cdot \mathbf{b}_1} e^{-i\mathbf{p}_{2\perp} \cdot \mathbf{b}_2} T(s, \mathbf{b}_1, \mathbf{b}_2)$$

is the CEP amplitude given by pQCD for high M_X

$\Omega(s, \mathbf{b})$ is the opacity determined from soft HE pp scattering data



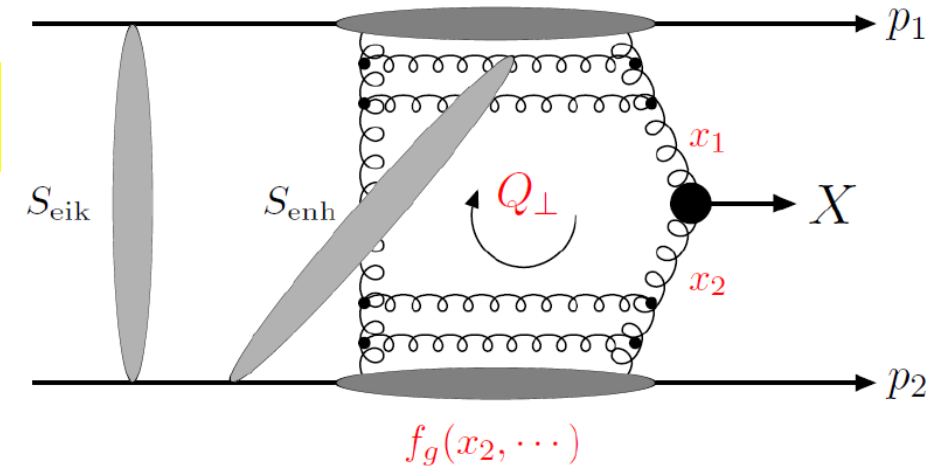
Need to allow for low-mass proton excitations N^* , that is $p \rightarrow N^* \rightarrow p$,
in determining $\Omega(s, \mathbf{b})$ from pp scattering data

Two-channel eikonal (p, N^*) determination of S_{eik}^2

GW formalism:

$$|p\rangle = \sum_i a_i |\phi_i\rangle, \quad |N^*\rangle = \sum_k c_k |\phi_k\rangle$$

states $|\phi_1\rangle, |\phi_2\rangle$ only undergo 'elastic scattering' $\langle \phi_i | A | \phi_k \rangle = 0$ for $i \neq k$



$$S_{\text{eik}}^2(\mathbf{b}) = \frac{\left| \sum_{i,k} |a_i|^2 |a_k|^2 \mathcal{M}_{ik}(\mathbf{b}) \exp(-\Omega_{ik}(s, \mathbf{b})/2) \right|^2}{\left| \sum_{i,k} |a_i|^2 |a_k|^2 \mathcal{M}_{ik}(\mathbf{b}) \right|^2}$$

Need hypothesis to distribute global PDFs between components of $|\phi_i\rangle$

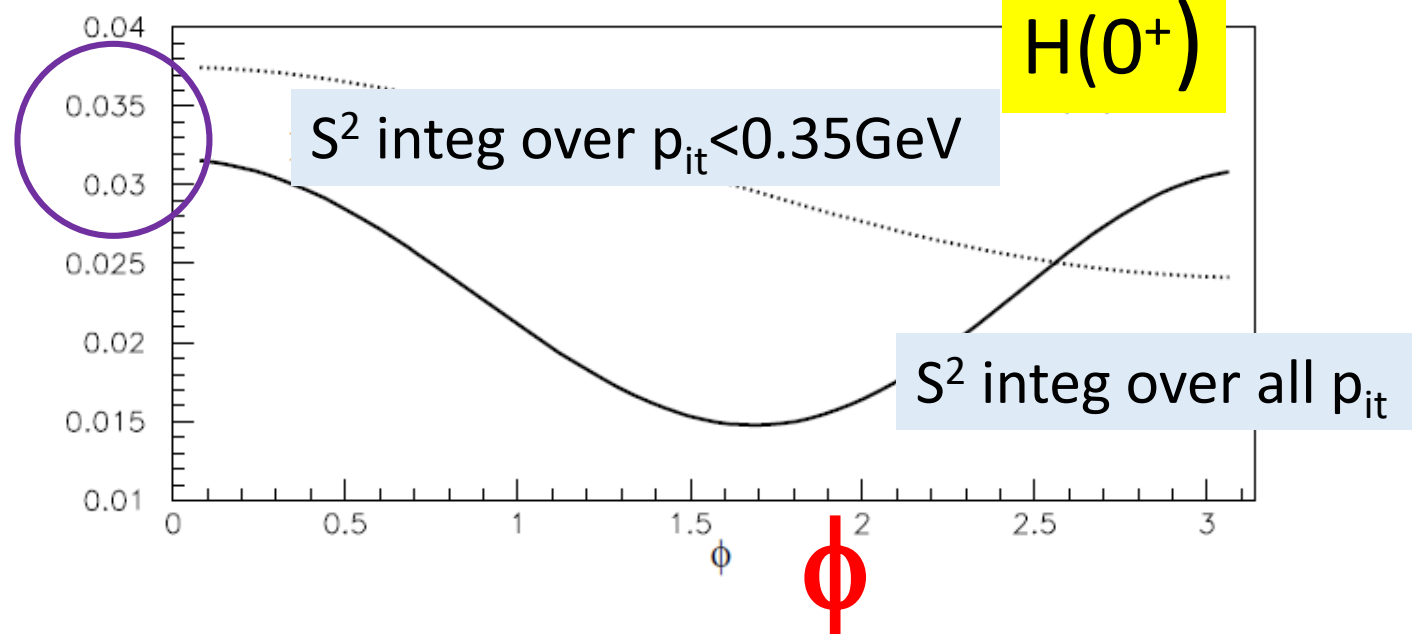
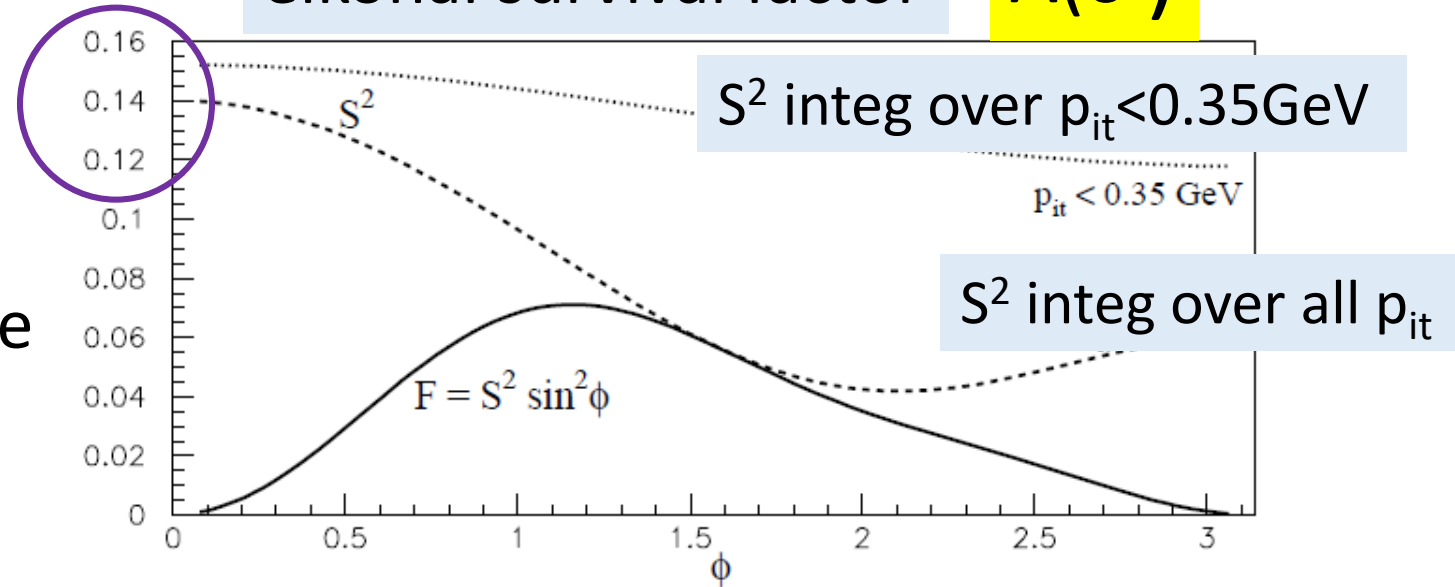
Need to do 2-ch eikonal fit to HE pp scatt. data for $d\sigma(\text{el})/dt$, $\sigma_{\text{lowM}}^{\text{diff}}$, $\sigma(\text{tot})$, ...

S_{eik}^2 suppression depends on matrix element of CEP hard process and on transverse momentum of the outgoing protons. Plots are for **azimuthal angle ϕ between proton transverse momenta**

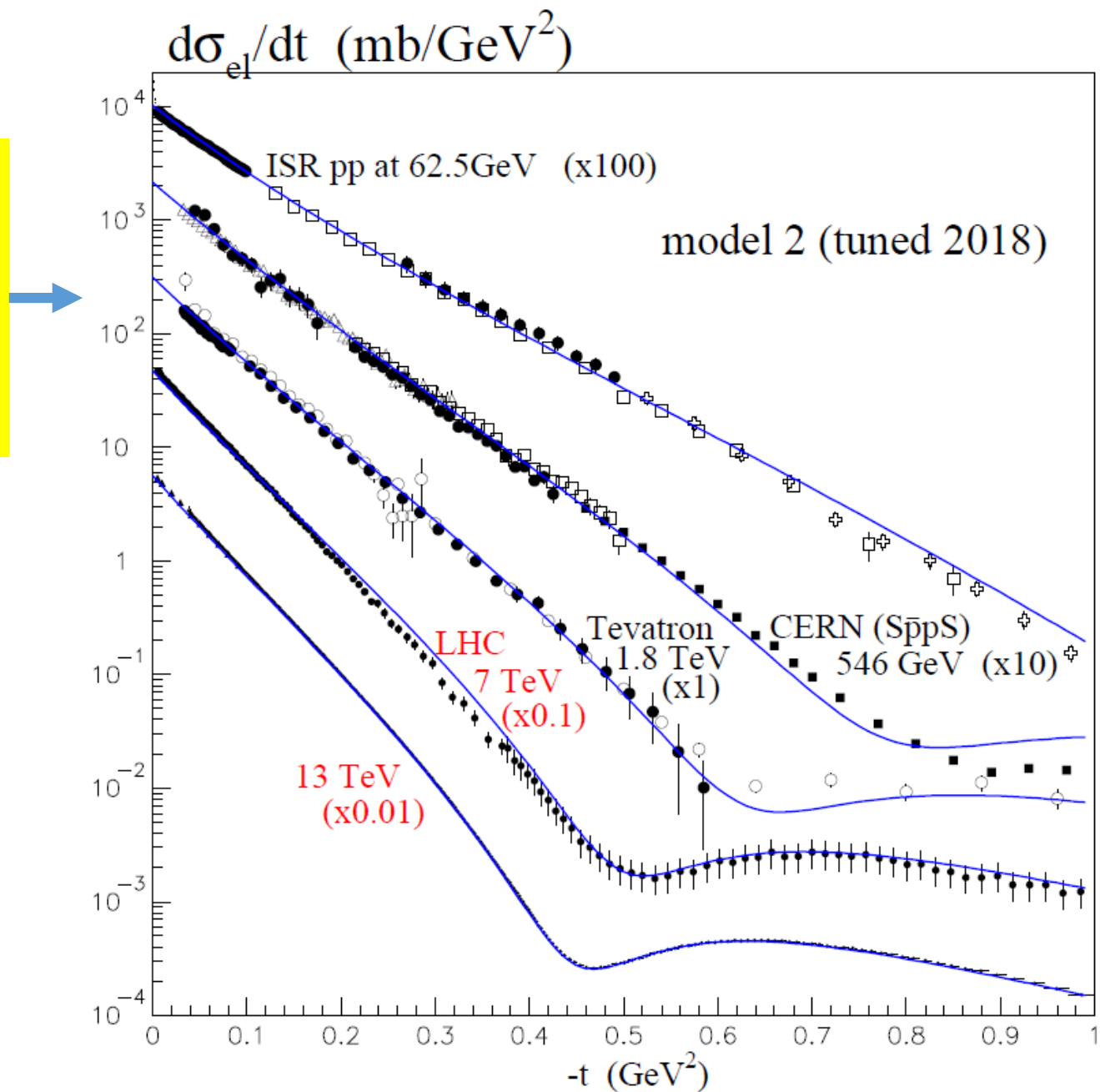
$$pp \rightarrow p + (A \text{ or } H) + p$$

eikonal survival factor

$A(0^-)$



Part of 2-ch eikonal fit
which determines $\Omega(b,s)$
--- which is needed to
calculate S_{eik}^2



HE behaviour dominated by leading (highest) Regge-exch. trajectory

$\sigma_{\text{tot}}(\text{hadron-hadron}) \rightarrow \text{const.}$ (actually slightly rising as $s \rightarrow \text{infinity}$)

that is $T(s, t=0) \sim s$ (actually $s^{1.08}$)

Implies Regge-pole exchange with $\alpha(0) = 1$ (1.08 ?)

called the **Pomeron**

We shall see later that the Pomeron is represented by gluon exchange – we need **two** gluons to form colourless exchange. But, for the moment, let us consider the Pomeron as a simple (effective) Regge pole

three?

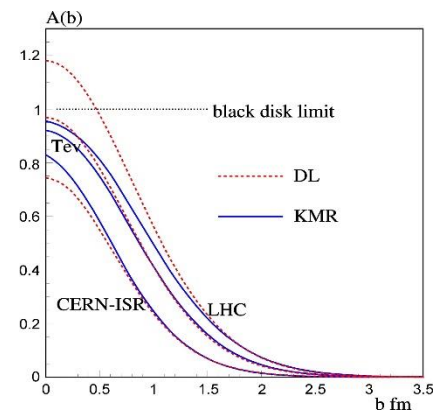
Optical theorem

$$\sigma_{\text{total}} = \sum_X \left| \begin{array}{c} \text{diagram: circle with two incoming arrows and one outgoing arrow labeled } X \end{array} \right|^2 = \text{Im} \begin{array}{c} \text{diagram: circle with two incoming arrows and two outgoing arrows, one solid and one dashed red} \end{array} = \begin{array}{c} \text{diagram: Y-shaped vertex with two outgoing arrows labeled } g_N \text{ and } \alpha_P(0) \end{array}$$

but screening/s-ch unitarity important so σ_{total} suppressed

at high energy use Regge

$$g_N^2 \left(\frac{s}{s_0} \right)^{\alpha_P(0)-1}$$



Elastic amp. $T_{\text{el}}(s, b)$

$$\text{Im } A_{\text{el}} = \begin{array}{c} \text{diagram: shaded oval} \end{array} = 1 - e^{-\Omega/2} = \sum_{n=1}^{\infty} \begin{array}{c} \text{diagram: rectangle with vertical lines} \end{array} \Omega/2$$

(s-ch unitarity)

bare amp. $\Omega/2 = \begin{array}{c} \text{diagram: rectangle with vertical lines} \end{array}$ (-20%)

Low-mass diffractive dissociation

introduce diff^{ve} estates ϕ_i, ϕ_k (comb^{ns} of p, p^*, \dots) which **only** undergo “elastic” scattering (Good-Walker)

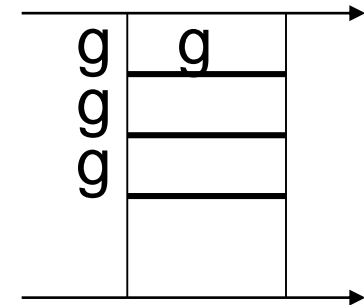
$$\text{Im } A_{ik} = \begin{array}{c} \text{diagram: shaded oval with superscript } i \text{ and subscript } k \end{array} = 1 - e^{-\Omega_{ik}/2} = \sum \begin{array}{c} \text{diagram: rectangle with vertical lines} \end{array} \Omega_{ik}/2$$

(-40%)

$p^* \rightarrow$ multichannel eikonal

Ladder structure of the Pomeron after QCD

Shortly after the discovery of QCD it was proposed that (colourless) two-gluon exch. had properties of Pomeron exch:
vacuum quantum no's, singularity close to $j=1$



- Later, using the BFKL formalism, in which the t-ch gluons (rather than hadrons) become Reggeized, it was found possible (for sufficiently large k_T) to describe HE (low x) interactions in pQCD.
- BFKL sum up the leading $(\alpha_s \log 1/x)^n$ contributions and build up the hard/pQCD/BFKL Pomeron.
- The Pomeron, is not a pole, but a branch cut in the complex angular momentum plane, plus more complicated cuts at HO

“Soft” and “Hard” Pomerons

A vacuum-exchange object drives soft HE interactions. Not a simple pole, but an enigmatic non-local object. Rising σ_{tot} means multi-Pom diags (with Regge cuts) are necessary to restore unitarity. σ_{tot} , $d\sigma_{\text{el}}/dt$, $\sigma_{\text{low}M}^{\text{diff}}$, described, by an effective pole
 $\alpha_P^{\text{eff}} = 1.13 + 0.05t$

Sum of ladders of Reggeized gluons with, in LLx BFKL, a singularity which is a cut and not a pole. When HO are included the intercept of the BFKL/hard Pomeron is
 $\alpha_P^{\text{bare}}(0) \sim 1.3$
 $\Delta = \alpha_P(0) - 1 \sim 0.3$

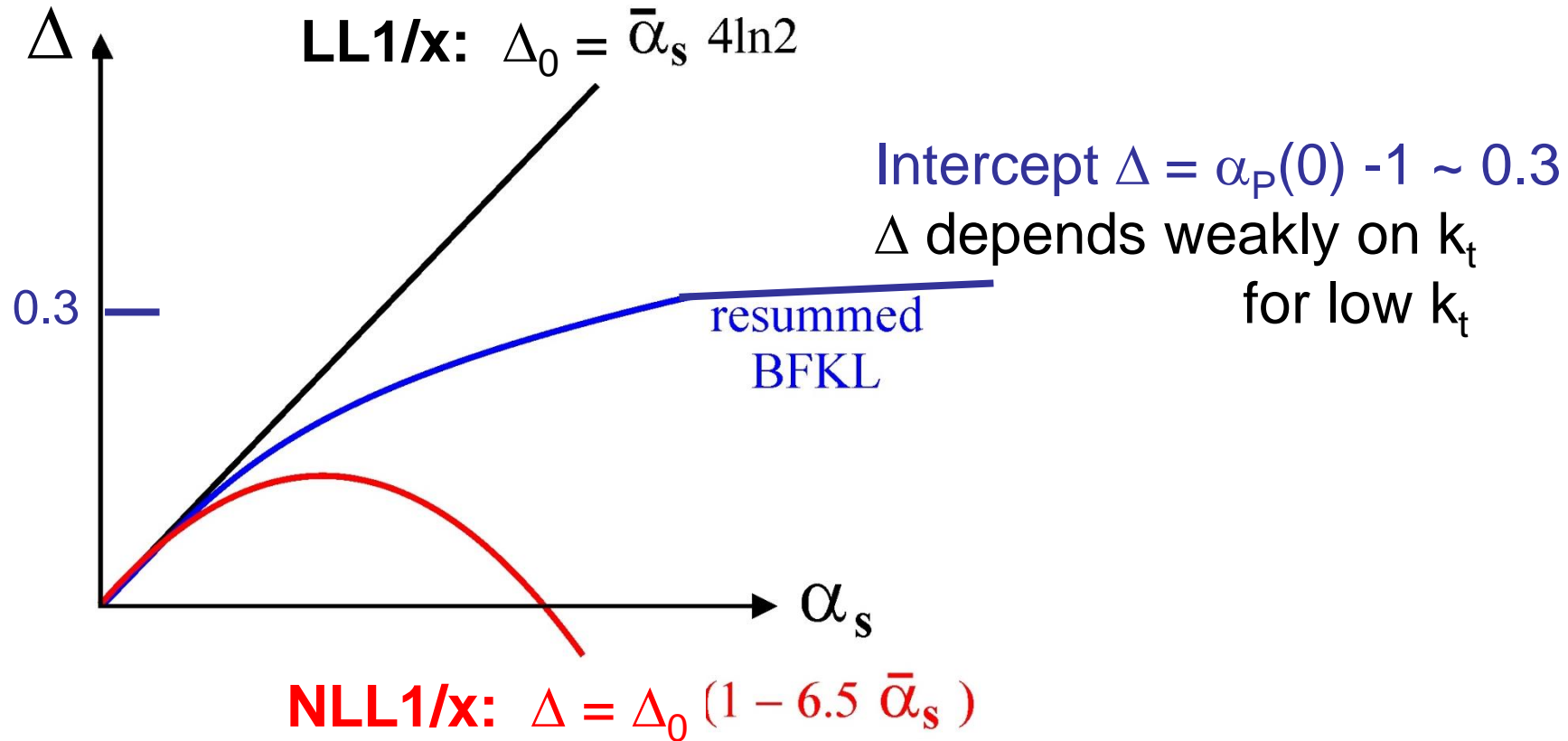
$$\alpha_P^{\text{eff}} \sim 1.13 + 0.05 t$$

Accounting for absorptive
(multi-Pomeron) effects

$$\alpha_P^{\text{bare}} \sim 1.3 + 0 t$$

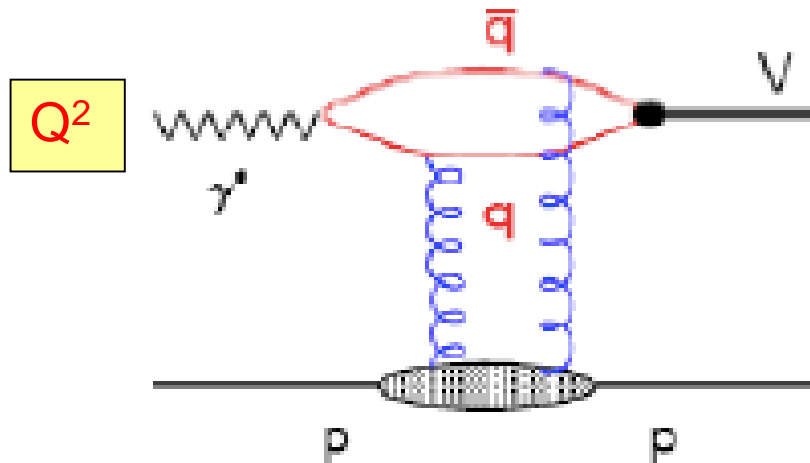
BFKL stabilized

$$\Delta = \alpha_p(0) - 1$$



Small-size “BFKL” Pomeron is natural object to continue from “hard” to “soft” domain

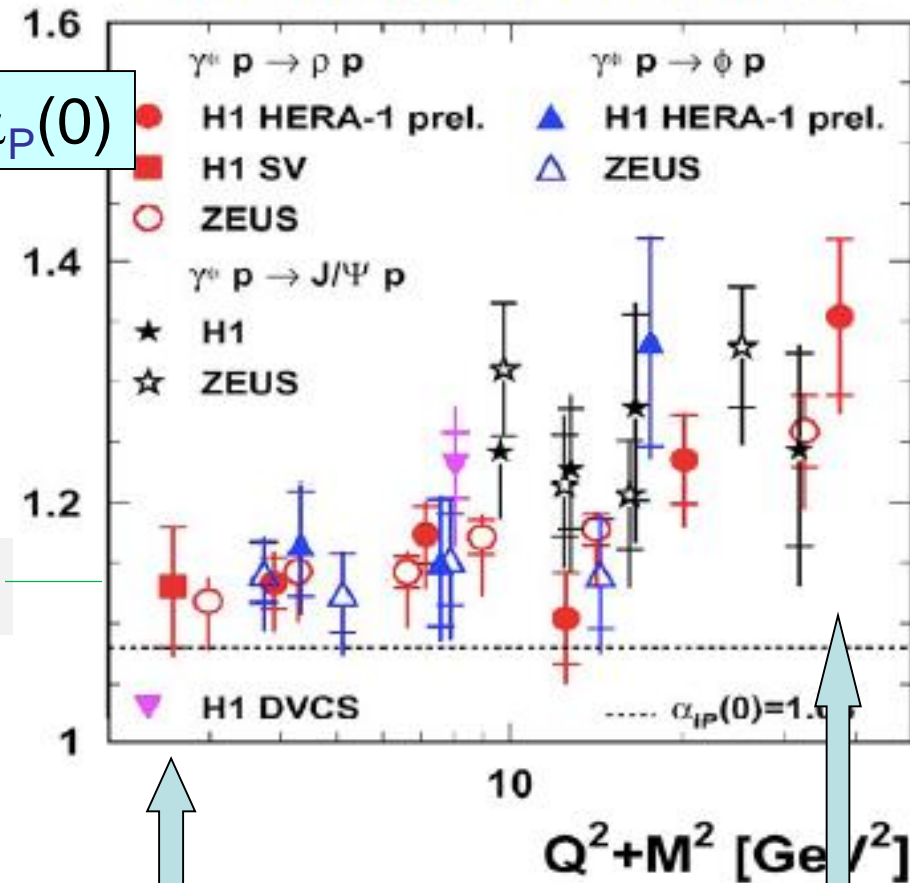
Vector meson prodⁿ at HERA
 ~ bare QCD Pom. at high Q^2
 ~ no absorption



hard energy dependences

$\alpha_P(0)$

1.13



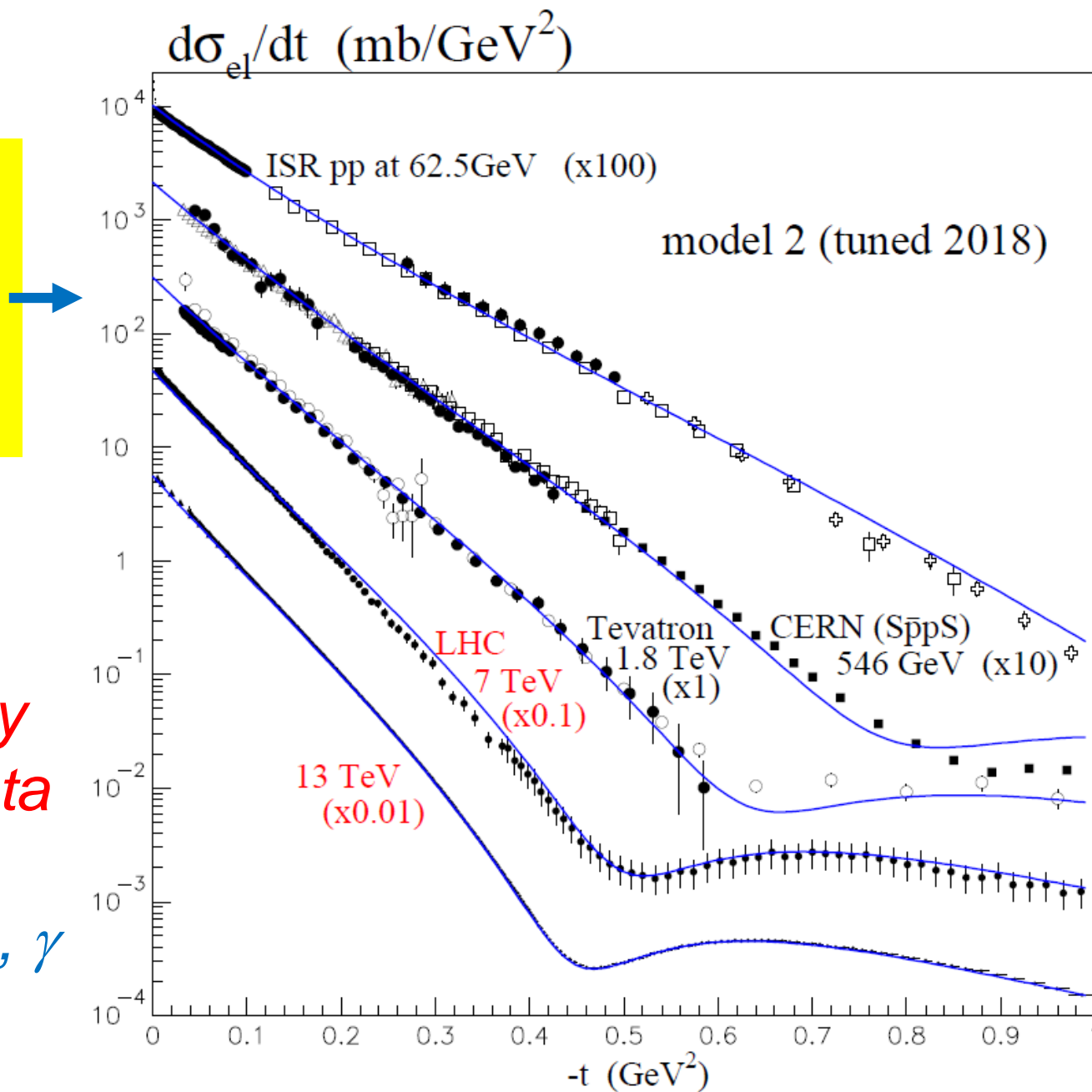
$\alpha_P(0) \sim 1.1$
 after absorption

$\alpha_P^{\text{bare}}(0) \sim 1.3$

Part of 2-ch eikonal fit
which determines $\Omega(b,s)$
--- which is needed to
calculate S_{eik}^2

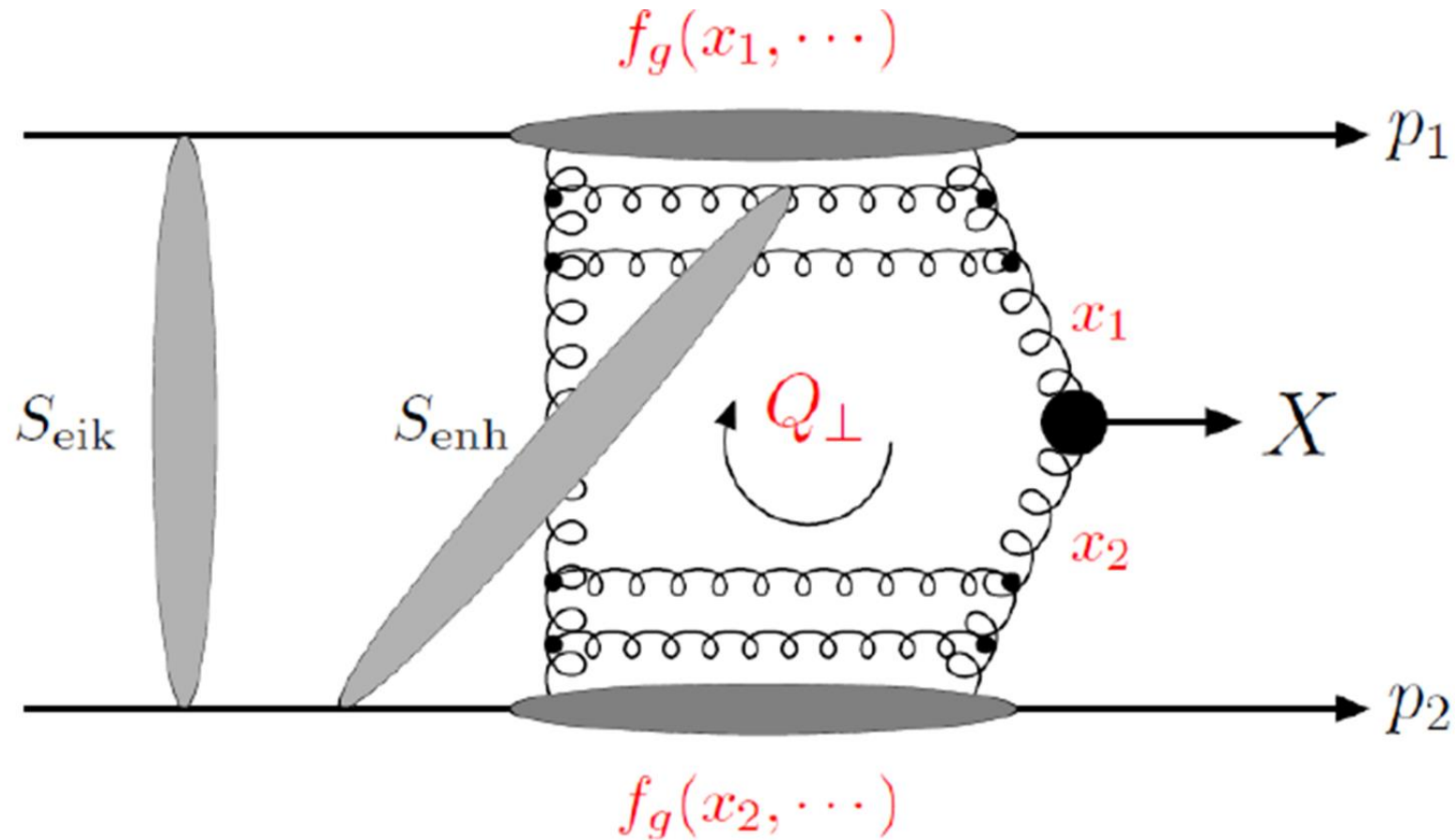
11 parameters in total
to describe all high-energy
 $d\sigma_{\text{el}}/dt$, σ_{tot} , $\sigma_{\text{lowM}}^{\text{diff}}$ pp data

4 for Pom: σ_0 , $\alpha_P(0)$, α'_P , γ
7 for two GW eigenstates
 $\alpha_P(0)=1.13$



Large number of intermediate partons

In general “enhanced” screening is small for large M_X due to strong k_t ordering of intermediate partons



QCD bremsstrahlung --- Sudakov suppression

$$pp \rightarrow p + H + p$$

Survival prob. of rap. gaps

$$W = S^2 T^2$$

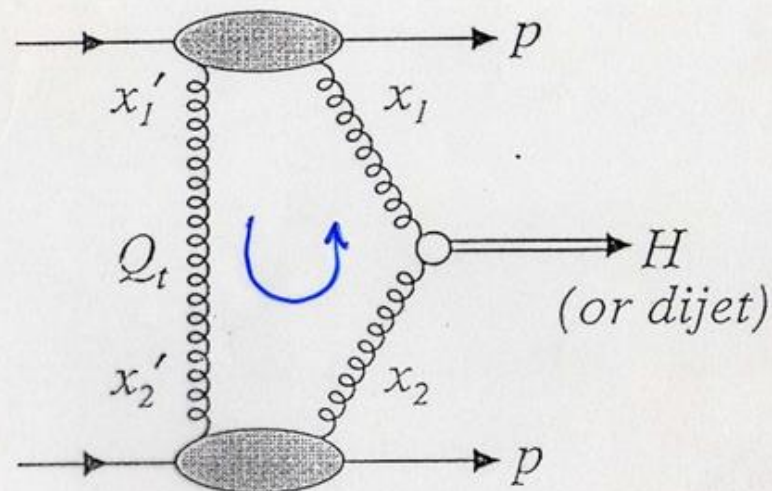
price for

no soft rescatt.

no g radⁿ
in $gg \rightarrow H$

Not a simple multiplication.
Need to embed the Sudakov factor in the pQCD integral over Q_t to ensure infrared convergence

$$f(x_1, x_1', Q_t, M_H)$$



$$\Lambda_{\text{QCD}}^2 \ll Q_t^2 \ll M_H^2 \rightarrow \text{pQCD}$$

$$\left(x' \sim \frac{Q_t}{\sqrt{s}}\right) \ll \left(x \sim \frac{M_H}{\sqrt{s}}\right) \ll 1$$

need uninteg. skewed gluons

$$f(x_i, x_i', \dots)$$

Sudakov factor $T(Q_t, \mu) \sim \exp(-\alpha_s \ln^2(Q_t^2/M_H^2))$ ensures **no** gluon emission from the fusing gluon as it evolves from Q_t to hard scale μ . It ensures infrared convergence of Q_t integral

$$\left(x' \sim \frac{Q_t}{\sqrt{s}}\right) \ll \left(x \sim \frac{M_H}{\sqrt{s}}\right) \ll 1$$

need uninteg. skewed gluons

$$\mathcal{M} = \frac{A}{M_H^2} \int \vec{Q}_{1t} \cdot \vec{Q}_{2t} \frac{d^2 Q_t}{Q_t^6} f(x_1, x'_1, Q_t^2, \frac{M_H^2}{4}) f(x_2, x'_2, Q_t^2, \frac{M_H^2}{4})$$

where $f(x, x', Q_t^2, \mu^2) \approx R \frac{\partial}{\partial \ln Q_t^2} \left[\sqrt{T(Q_t, \mu)} x g(x, Q_t^2) \right]$

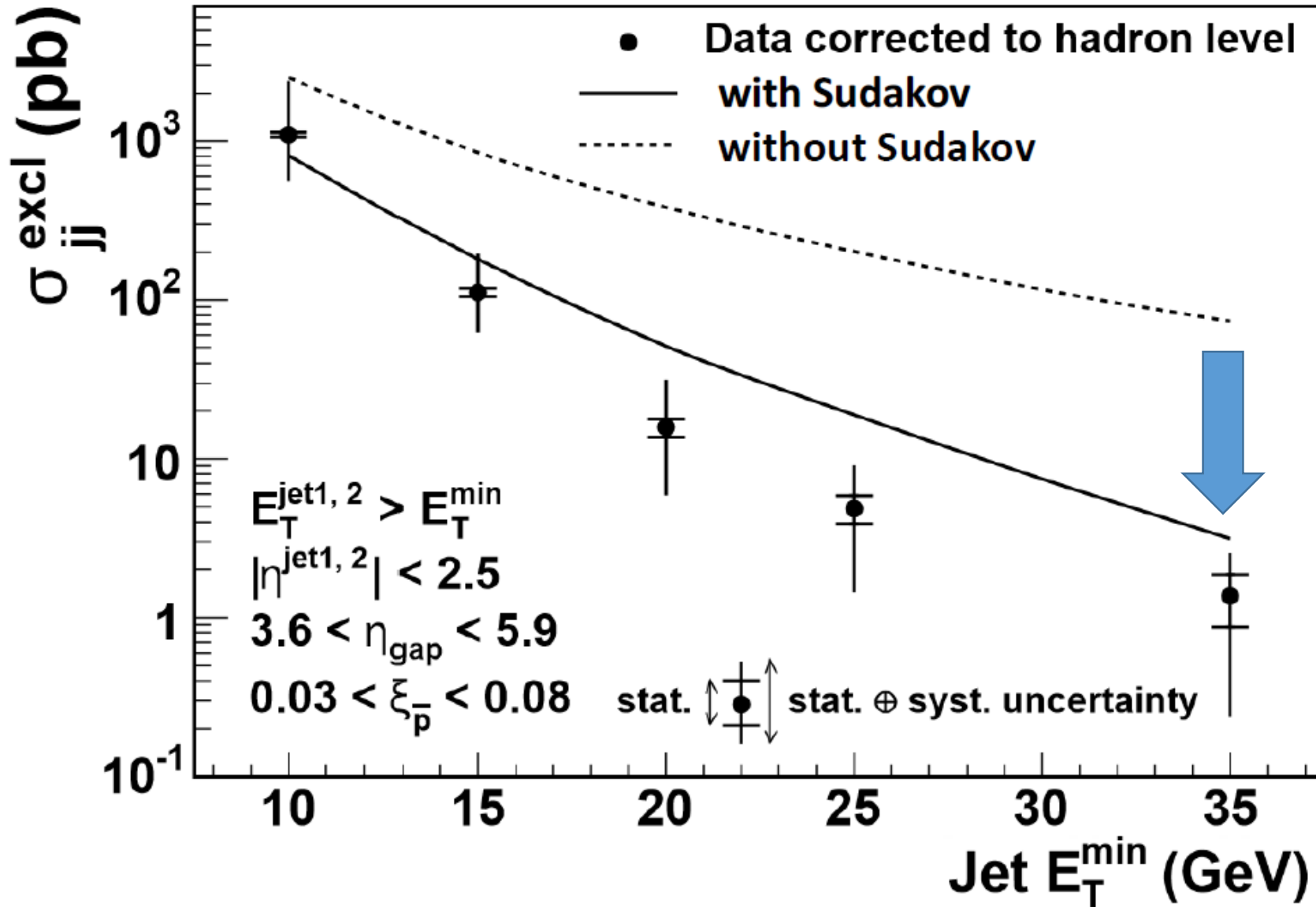
R is calculable
skewed effect
($R=1.2$ at LHC)

$$T(Q_t, \mu) = \exp \left(- \int_{Q_t^2}^{\mu^2} \frac{dk_t^2}{k_t^2} \frac{\alpha_s}{2\pi} \int_0^{1-k_t/\mu} dz z P_{gg} \dots \right)$$

strongly suppresses Q_t infrared region

no emission when $(\lambda \sim 1/k_t) > (d \sim 1/Q_t)$
i.e. only emission with $k_t > Q_t$

Exclusive dijet production



Odderon

Very nice review by Carlo Ewerz

The Odderon in QCD
hep-ph/0306137 (2003)

Properties of odd-signature high-energy amp studied in early 70's

Odderon first promoted in 1973 (Lukaszuk, Nicolescu) by Regge exchange for high-energy cross sections; for example **pp and p \bar{p}**

$$A_{\pm} = A(pp) \pm A(p\bar{p})$$

simple poles $\alpha_{P,O}(0) \sim 1$

$$A_{+}(pp) = A_{+}(p\bar{p}) \quad C = +1$$

Pomeron --- dominately imag

$$A_{-}(pp) = A_{-}(p\bar{p}) \quad C = -1$$

Odderon --- dominately real

Maximal Odderon (MO)

$$\begin{aligned} \text{Im}A_{+} &\leq c \ln^2 s \quad (\text{Froissart}) \\ \text{Re}A_{-} &\leq c' \ln^2 s \quad (\text{MO analogy}) \end{aligned}$$

allowed by asymptotic theorems

1. Pomeranchuk theorem $\Delta\sigma \equiv \sigma(\bar{p}p) - \sigma(pp) \sim \text{Im}A_{-} \rightarrow 0 \quad \text{as } s \rightarrow \infty$

2. Generalized Pomeranchuk th: $\frac{\sigma(\bar{p}p)}{\sigma(pp)} \rightarrow 1 \quad \text{as } s \rightarrow \infty$

1. Pommeranchuk theorem $\Delta\sigma \equiv \sigma(\bar{p}p) - \sigma(pp) \sim \text{Im}A_- \rightarrow 0$ as $s \rightarrow \infty$

2. Generalized Pommeranchuk th: $\frac{\sigma(\bar{p}p)}{\sigma(pp)} \rightarrow 1$ as $s \rightarrow \infty$

1 and 2 are not equivalent

$$\sigma(\bar{p}p) = A \ln^2 s + B \ln s + C$$

$$\sigma(pp) = A \ln^2 s + B' \ln s + C'$$

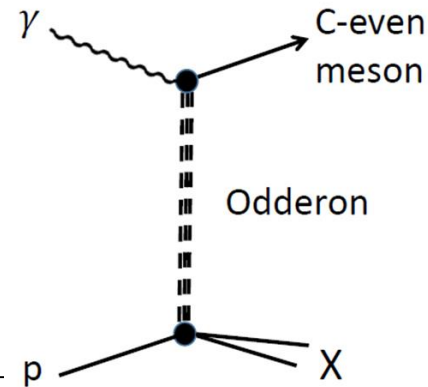
if $B \neq B'$ then satisfy 2, but not 1

In general $\Delta\sigma \leq c \ln s$

Little evidence of Odderon from $d\Delta\sigma/dt$ in dip region at 53 GeV

Then in 1980 the Odderon is found to be a firm prediction of QCD

But no evidence of Odderon exchange from HERA data for exclusive photoprod. of C-even mesons $\gamma p \rightarrow \pi^0 p, \eta p, f_2 p \dots$ (Nachtmann et al)
Discuss evidence from LHC later.



First, explain why Maximal Odderon violates unitarity →

Why the Maximal Odderon violates unitarity

Khoze, Martin, Ryskin
arXiv: 1801.07065

1. Unitarity

$$SS^\dagger = I \quad (\text{let } S = I + iA) \quad \rightarrow \quad \underline{i(A^\dagger - A) = A^\dagger A}$$

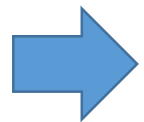
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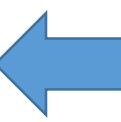
Solution of unitarity eq.

$$A(b) \equiv \underline{A_{\text{el}}(b)} = i(1 - e^{-\Omega(b)/2}) \quad \text{with } \operatorname{Re} \Omega(b) \geq 0$$



No solution of unitarity eq. if $G_{\text{inel}}(b) > 1$.

Let us calculate $G_{\text{inel}}(b)$



$\exp(2i\delta_l)$ in terms of
partial waves $l = b\sqrt{s}/2$

2. Finkelstein-Kajantie problem: $\sigma(\text{diff}^{\text{ve}}) > \sigma(\text{total})$ due to $\int_0^{\ln s} dy \dots \sim \ln s$

Simple example: Central Exclusive Prod. $pp \rightarrow p+X+p$

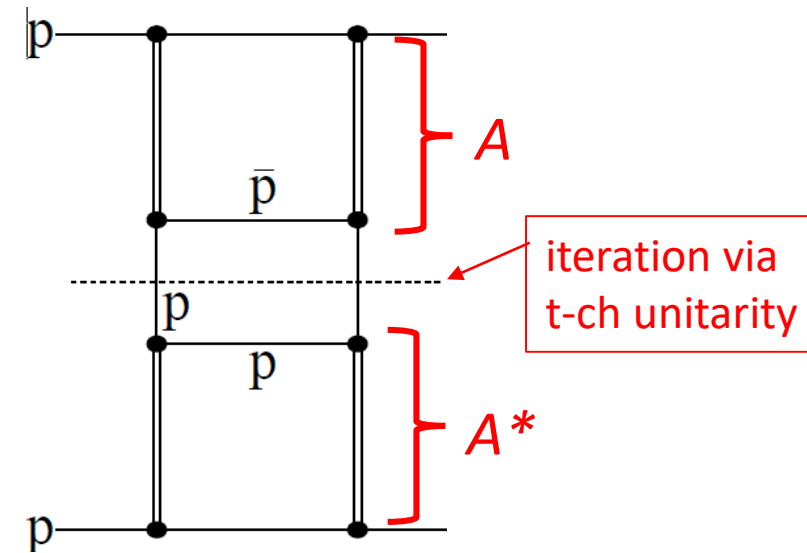
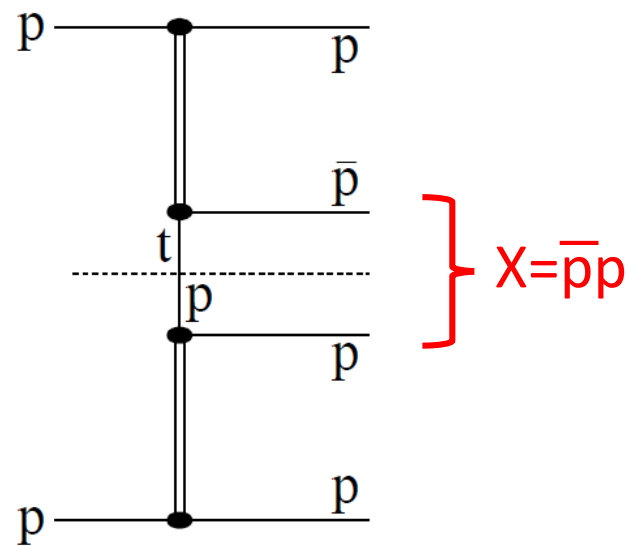
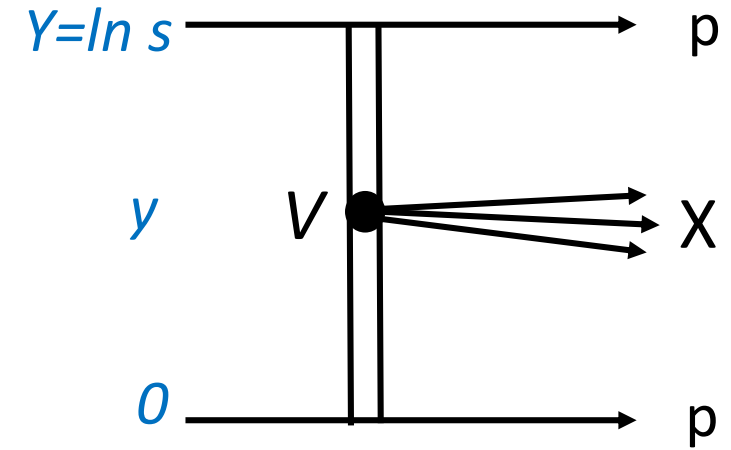
In the Froissart limit $\sigma_{\text{CEP}} \sim \ln^5 s$

so $\sigma_{\text{CEP}} > \sigma_{\text{tot}} \sim \ln^2 s$

Could the explanation be that vertex $V = 0$? **No**

Can show, for example, that the $p\bar{p}$ component of X generated by t-channel unitarity has $V \neq 0$, and cannot be compensated due to the singularity/pole at $t=m_p^2$.

So starting from A_{el} we see t-ch unitarity gives a component of $G_{\text{inel}}(b)$ increasing faster than $\int_0^{\ln s} dy \dots \sim \ln s$



Figs: amplitude (left) and cross section (right) of $\bar{p}p$ Central Exclusive Prod. generated by t-ch unitarity

3. Solution to the Finkelstein-Kajantie problem

Complete CEP **must include** rescattering S_{el} (that is the **survival probability** $S^2 = |S_{el}|^2$ of the rapidity gaps)

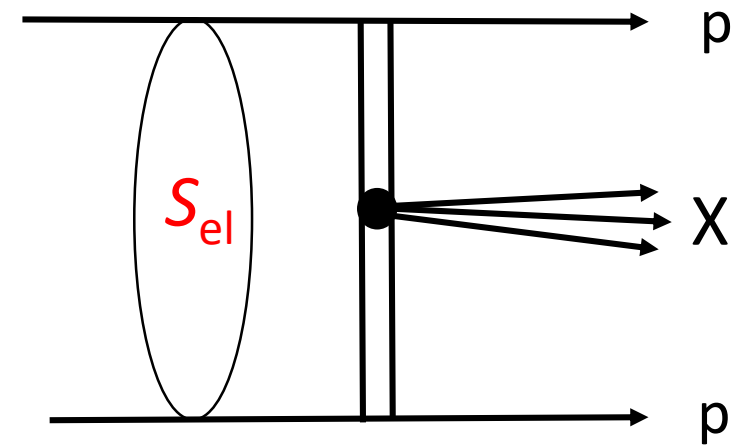
$$A_{CEP}(b) = S_{el}(b) A_{bare}(b)$$

$$\text{where } |S_{el}(b)|^2 = |1 + iA_{el}(b)|^2 = e^{-\text{Re}\Omega(b)}$$

Black disc asymptotics: $\text{Re}\Omega \rightarrow \infty$, $A_{el}(b) \rightarrow i$, $S^2(b) \rightarrow 0$ for $b < R$

If σ_{tot} increases, Black disc is the only known solution to the FK problem

To repeat, if at least one component of $G_{inel}(b)$ increases (due to $\int dy \sim \ln s$) then unitarity is violated as $s \rightarrow \infty$. The only way to restore unitarity is to have $S(b) \rightarrow 0$



4. Maximal Odderon contradicts unitarity as $s \rightarrow \infty$

Maximal Odderon

Asymptotically MO means $\text{Re}A/\text{Im}A \rightarrow \text{constant} \neq 0$

In this case $S^2(b) = |1 + iA(b)|^2 \geq |\text{Re}A(b)|^2 \neq 0$

so there is no possibility to compensate the growth of σ_{CEP} .

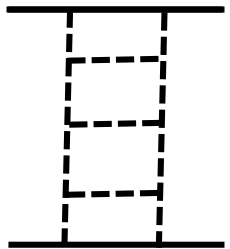
The Odderon exists in QCD

Need the existence of symmetric tensor d_{abc} of non-Abelian $SU(3)_{\text{col}}$ to form colourless ggg exchange with $C=-1$

Pomeron (gg)

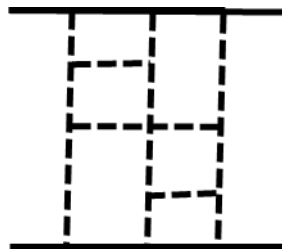
Odderon (ggg)

BFKL eq.



resum
 $\alpha_p(0) > 1$

BKP eq.



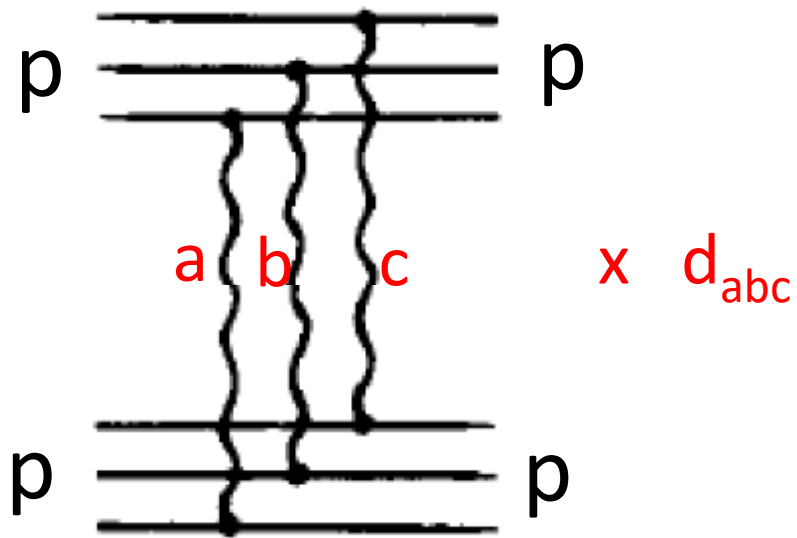
Bartels; Kwiecinski, Praszalowicz 1980

resum
 $\alpha_O(0) \approx 1$

Janik-Wosiek solution
Bartels-Lipatov-Vacca solution,
2000

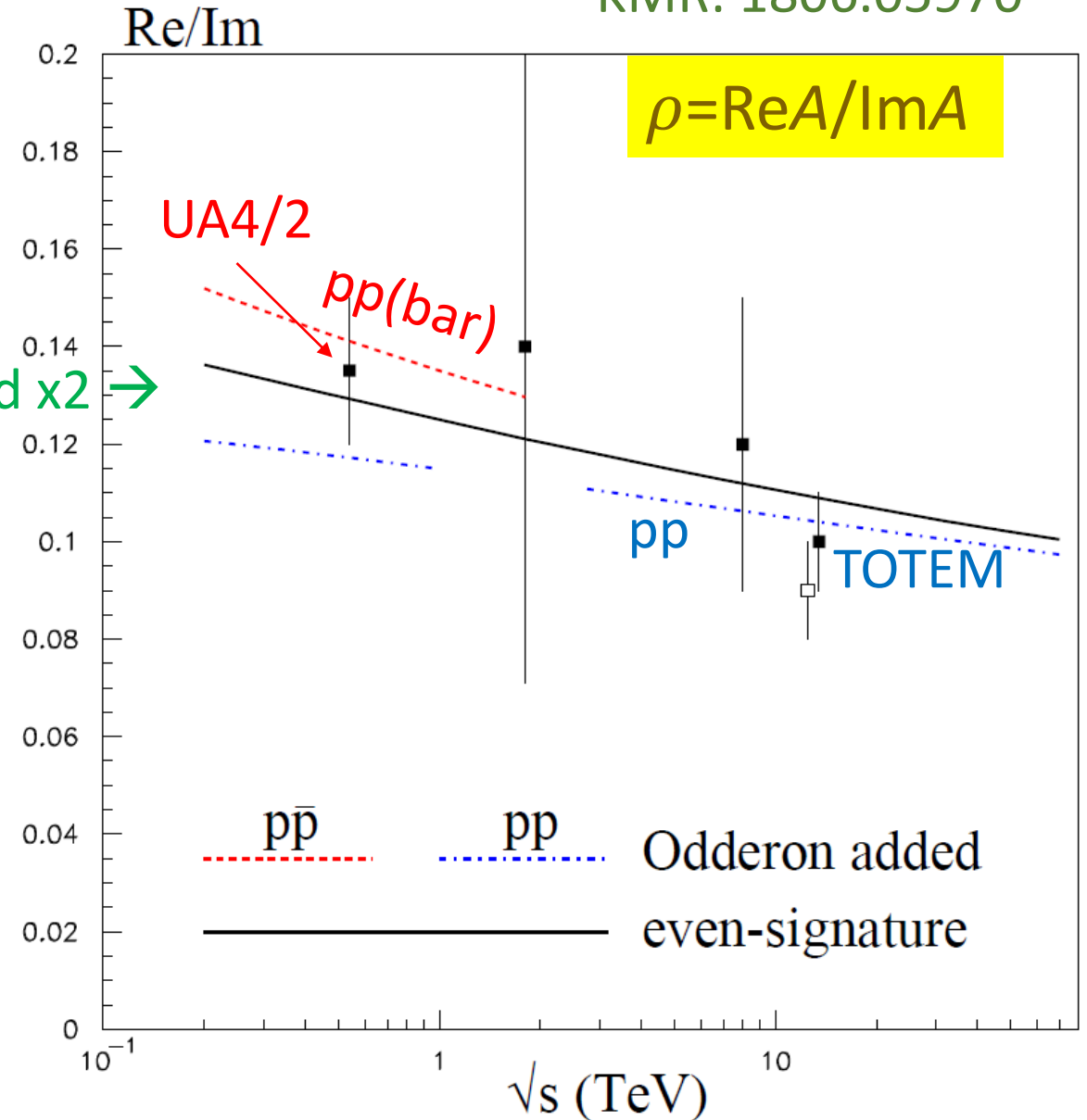
Estimate of Odderon contribⁿ

QCD lowest α_s order Ryskin '87
 (Fukugita, Kwiecinski '79;
 Kwiecinski, Motyka.. '96 (η_c at HERA))



enhanced x2 →

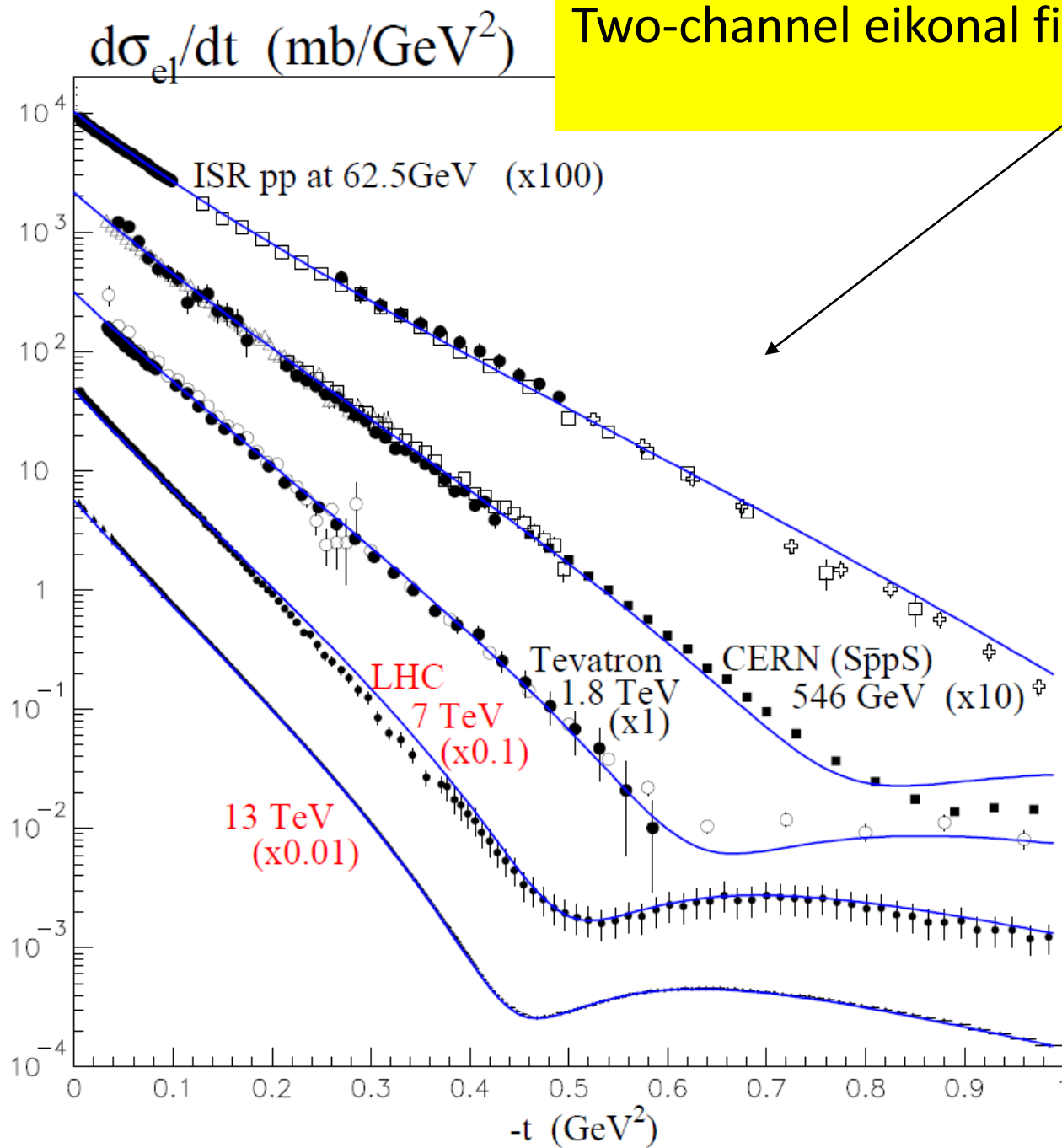
KMR: 1806.05970



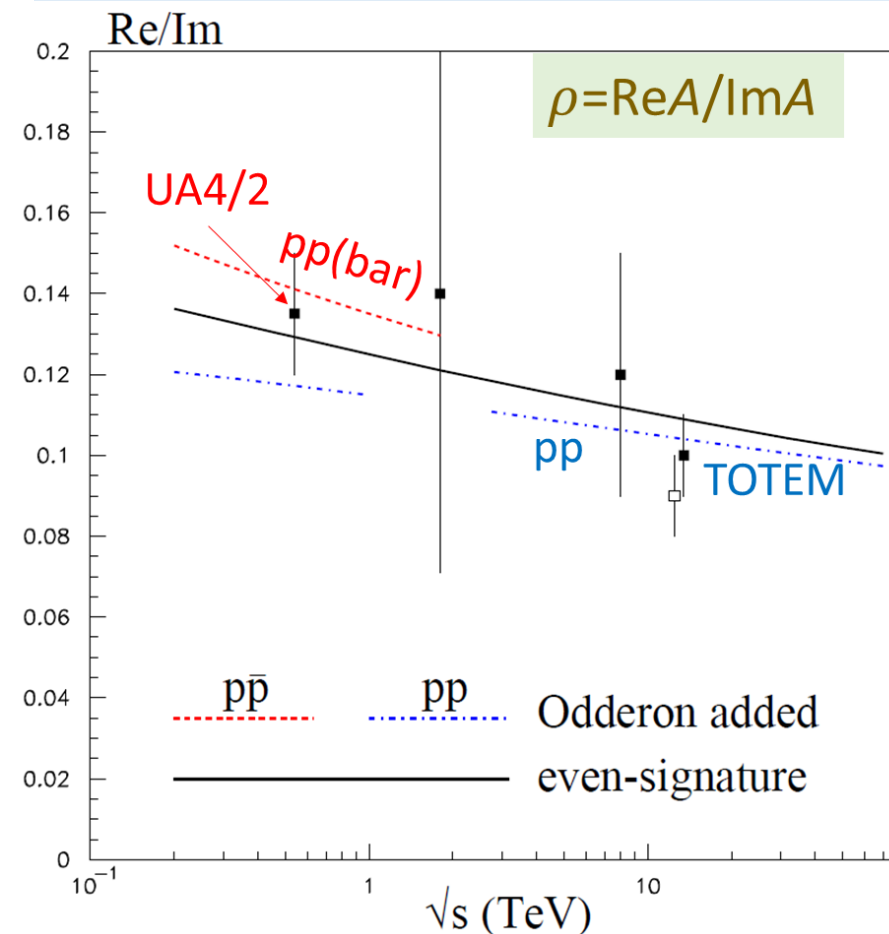
Two-channel eikonal fit to high-energy pp scatt. data

crucial data

$d\sigma_{el}/dt$, σ_{tot} , $\sigma_{low\ mass\ Diffraction}$



Gives acceptable fit to ReA/ImA without an Odderon



Including the Odderon gives only a marginal improvement

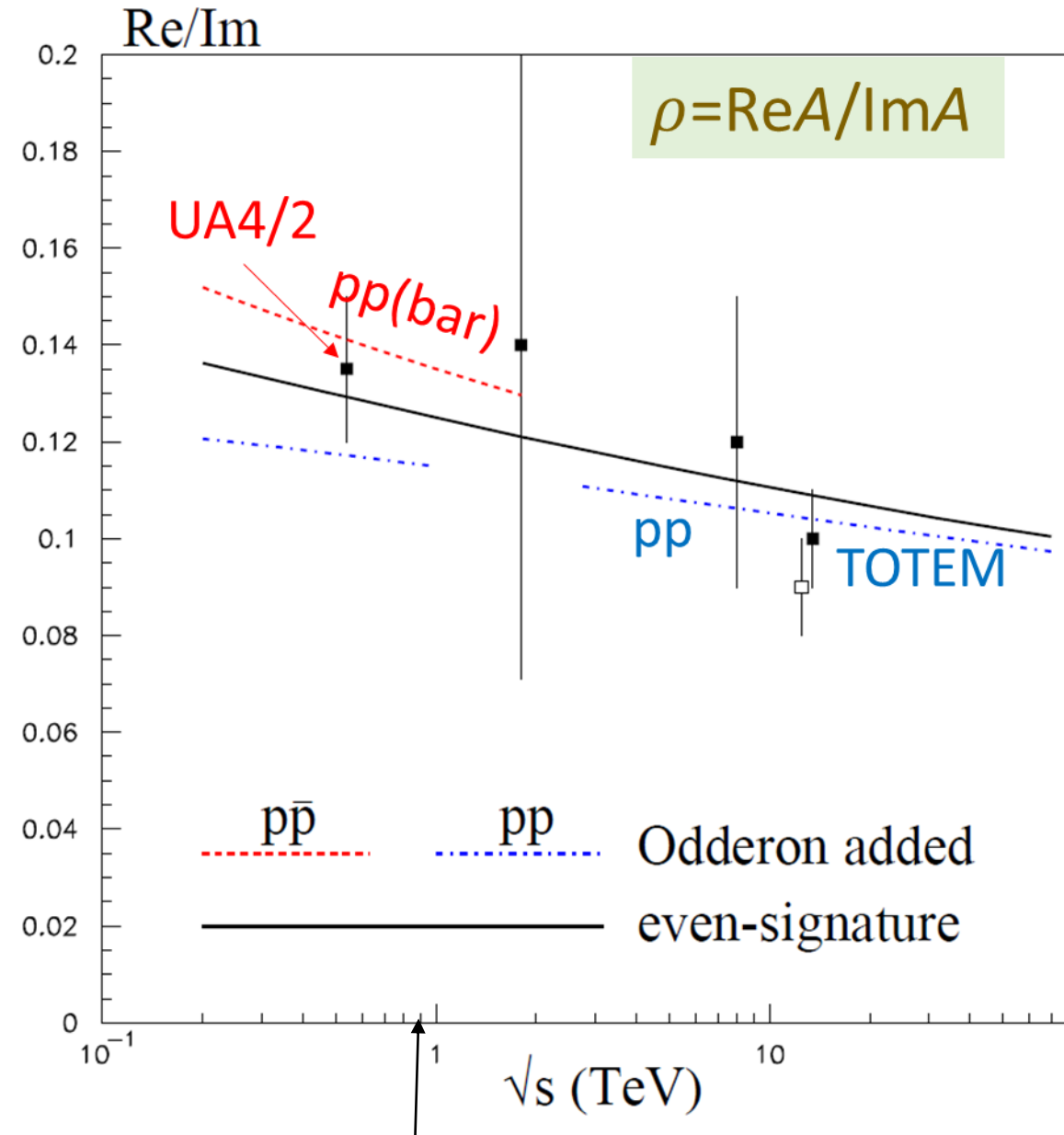
Must include full Ω in amplitude

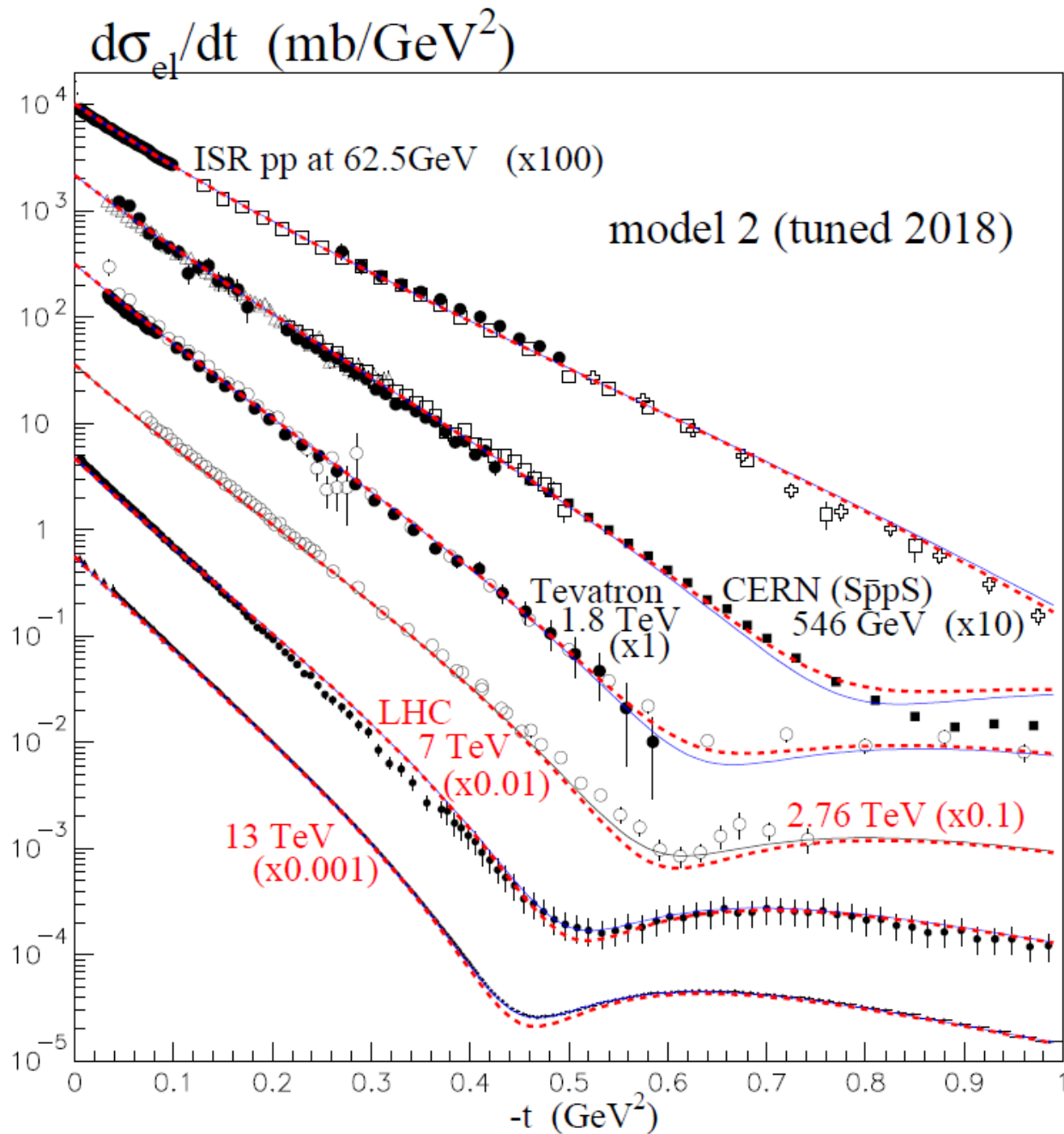
$$A(b) = i \left(1 - e^{-\Omega(b)/2} \right)$$

with $\Omega = \Omega_{\text{even}} + \Omega_{\text{odd}}$

Automatically accounts for absorptive effect caused by elastic rescattering

TOTEM measurement 0.9 TeV
could be informative?





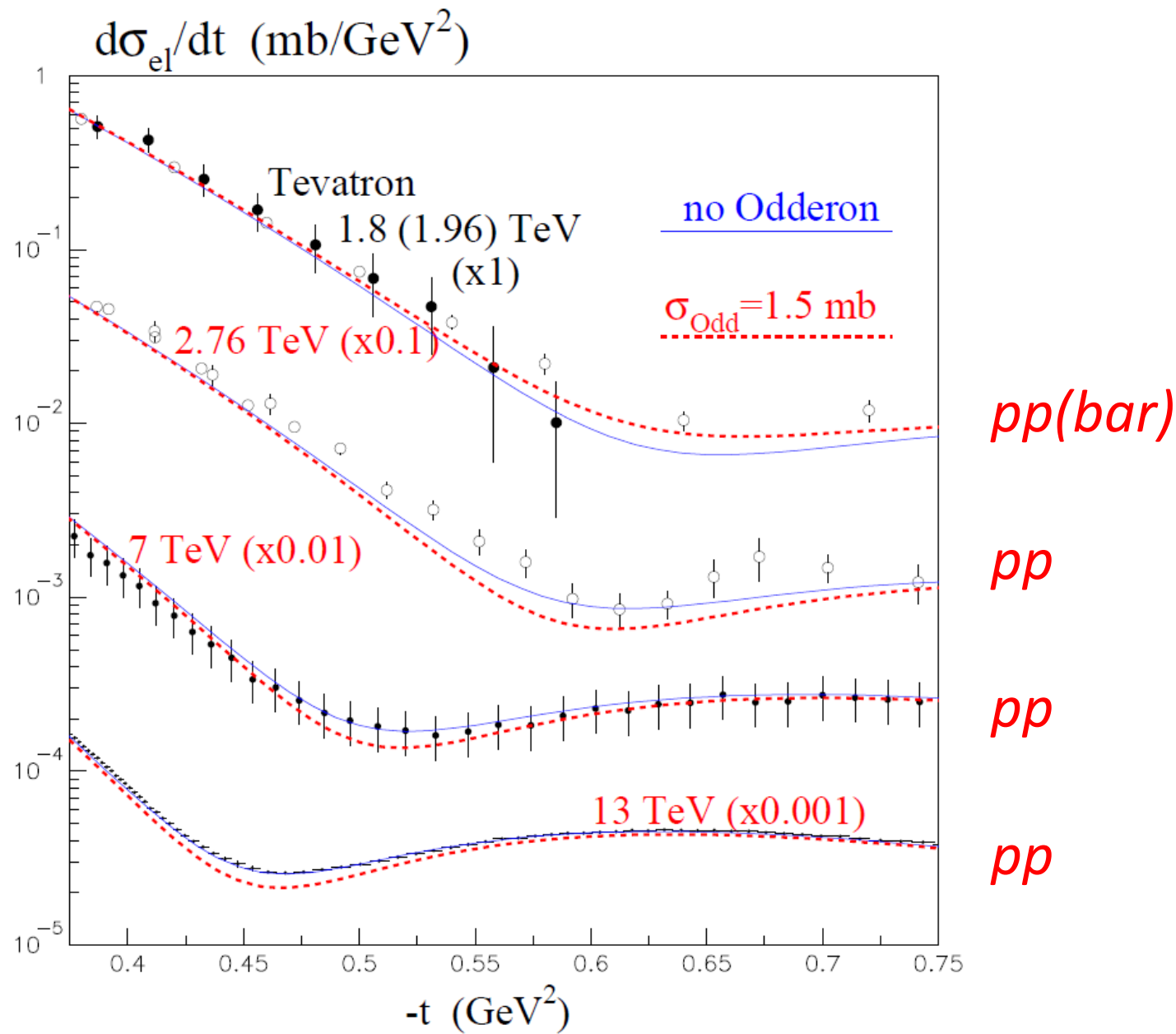
Previous fit, but now red-dotted curves show the effect of the Odderon fixed to agree with $\rho = \text{Re}A/\text{Im}A$

*Note Odderon increases $pp(\bar{p}p)$
decreases pp
Main effect in dip region*

← New TOTEM data at 2.76 TeV

Dip region

*No conclusive evidence for
a larger Odderon*



Odderon signals

- **pp scatt** Odderon exch. is a small correction to even-signature term $(g_{pO})^2$

- **photoproduction of C even mesons**

$\pi^0, f_2, \eta \dots$

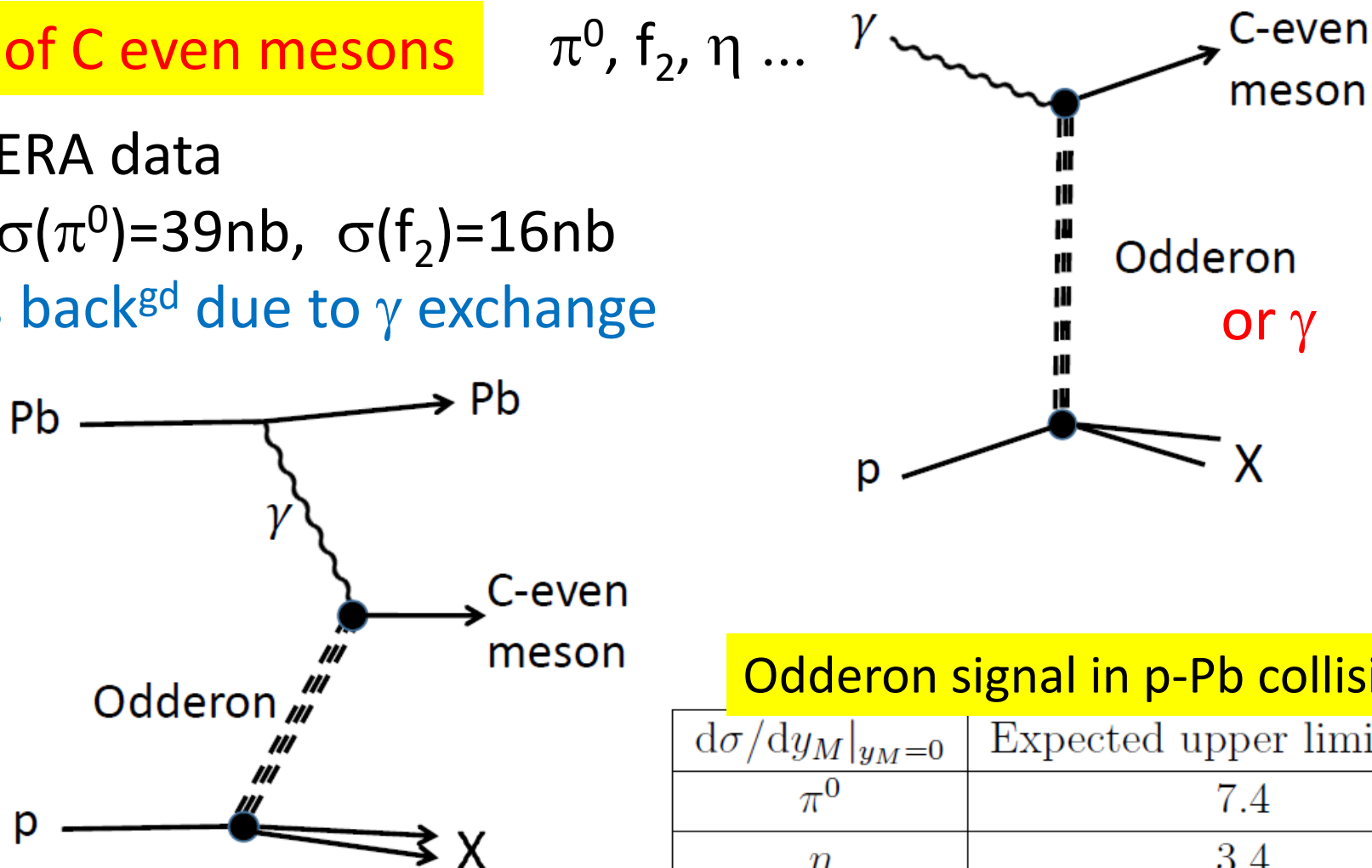
No evidence in HERA data

upper limits $\sigma(\pi^0)=39\text{nb}$, $\sigma(f_2)=16\text{nb}$

Need to suppress back^{gd} due to γ exchange

- **ultraperipheral production in p-Pb collisions**

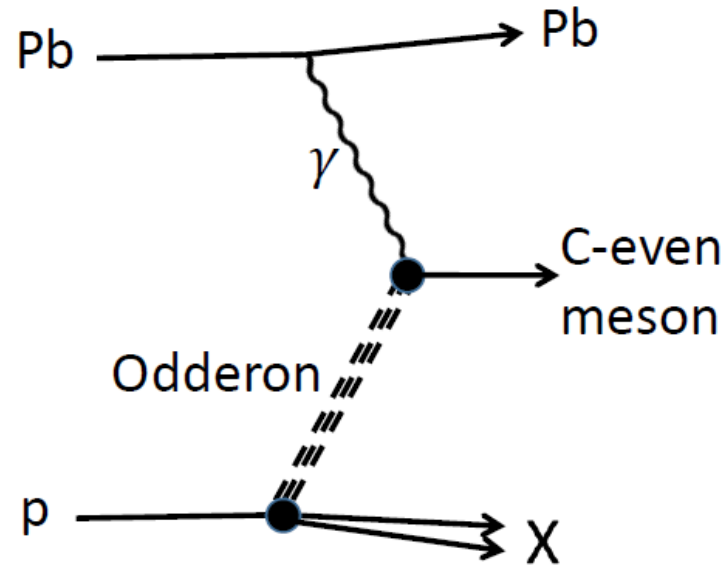
Z^2 in photon flux



Odderon signal in p-Pb collisions?

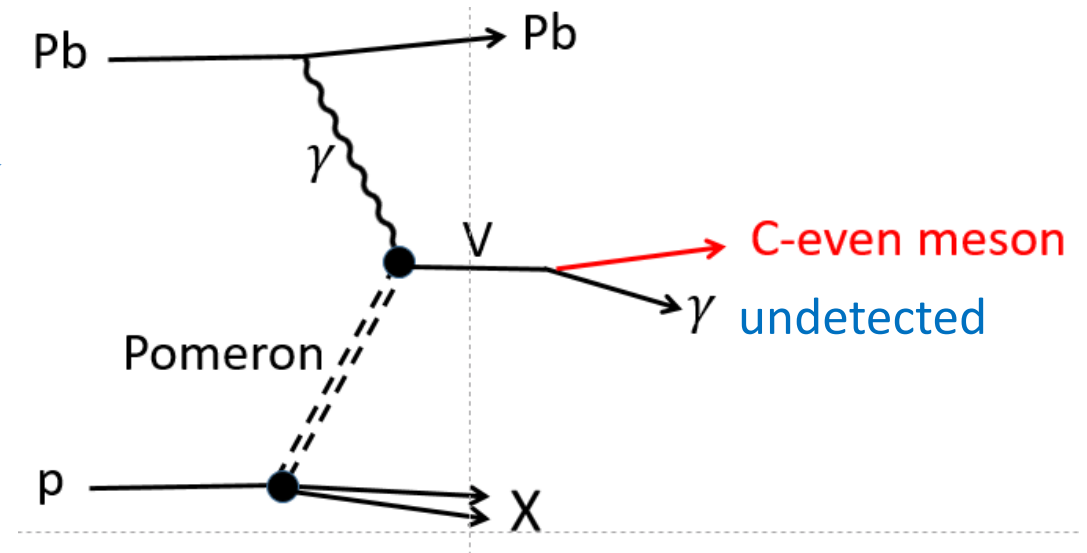
$d\sigma/dy_M _{y_M=0}$	Expected upper limits [μb]
π^0	7.4
η	3.4
$f_2(1270)$	3.0

Healthy signal,
but backgrounds
are due to



production of C-even meson by

1. $\gamma\gamma$ fusion
2. Pomeron-Pomeron fusion
3. Via vector meson
 $V \rightarrow \text{C-even meson} + \text{undetected } \gamma$



π^0

$\sigma(\pi^0)$ from $\gamma\gamma$ fusion is well known.
Estimating the cross section due to
Odderon exchange, allowing for
the colour factors etc. and integrating
over $0.04 < |t| < 1 \text{ GeV}^2$ we find

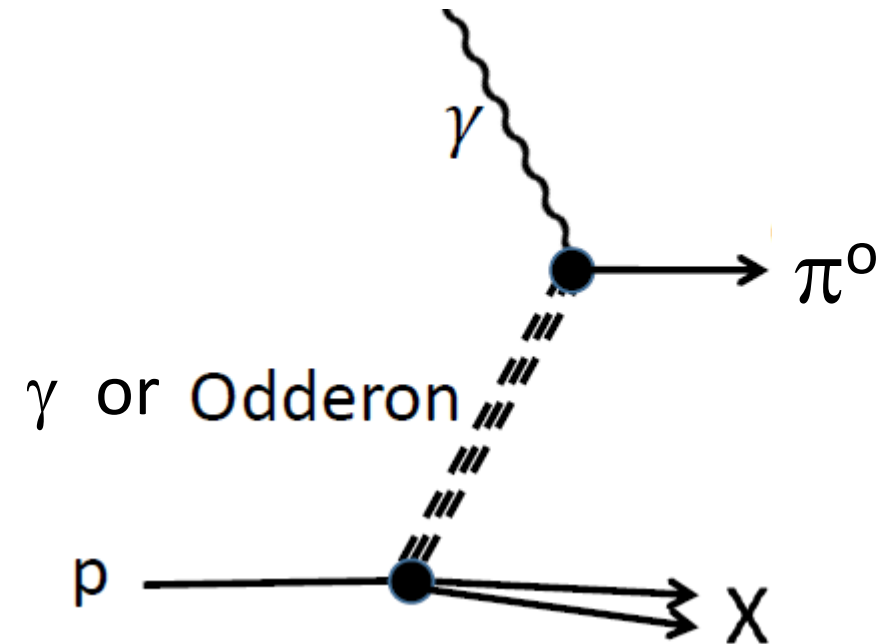
$$\sigma_{\text{Odd}}(\gamma p \rightarrow \pi^0 + X) \sim 5(1) \text{ nb}$$

for the cutoff $\mu = 0.3(0.5) \text{ GeV}$.
The t cut adequately suppresses
the $\gamma\gamma$ fusion background.

Pomeron-Pomeron background entirely absent by SU(3) flavour

However the reducible background from radiative ω decay is very large

$$\omega \rightarrow \pi^0 + \gamma \text{ (undetected)}$$

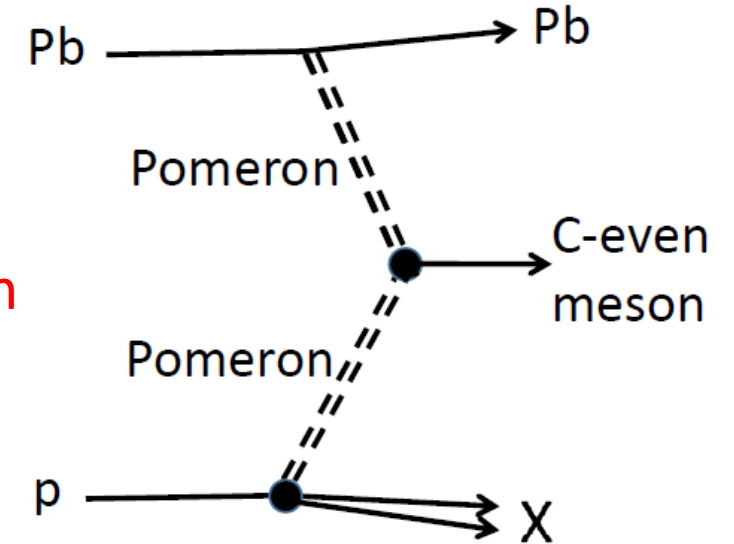


f_2

There is a very low background due to radiative V decay. However the problem here is the **v.large Pomeron-Pomeron** background. The signal-to-bkgd may be suppressed by observing central (semi)exclusive production (CEP*) of C-even mesons in which the proton may break up but the **Pb-ion remains intact**. For such events we expect a larger possibility of break-up for Odderon exchange --- exptally challenging.

In any nucleon-proton interaction creating the C-even meson there is a large probability of inelastic nucleon-proton interactions which will populate the rapidity gaps. Only in very **peripheral** ion-proton collisions is there a chance to observe a CEP* event.

Can show the A dependence of CEP* events scales as $A^{1/3}$. Recall the photoprodⁿ cross section (the signal) scales as Z^2 , so the expected $A^{1/3}$ back^{gd} scaling is much milder.



η

Pom-Pom background is small as η has small SU(3) singlet compt. However again the reducible backgrounds coming from $\phi \rightarrow \eta\gamma$ and $\eta' \rightarrow \eta\pi^0\pi^0$ are rather large

 η_c

In principle, viable channel but has a much smaller production rate.

C-even meson (M)	Odderon Signal		Backgrounds		
	Upper Limit	QCD Prediction	$\gamma\gamma$	Pomeron-Pomeron	$V \rightarrow M + \gamma$
π^0	7.4	0.1 - 1	0.044	—	<u>30</u>
$f_2(1270)$	3	0.05 - 0.5	0.020	<u>3 - 4.5</u>	0.02
$\eta(548)$	3.4	0.05 - 0.5	0.042	negligible	<u>3</u>
η_c	—	$(0.1 - 0.5) \cdot 10^{-3}$	0.0025	$\sim 10^{-5}$	0.012

 $\phi \rightarrow \eta\gamma$

0.05 included

signal and background for $d\sigma(\text{Pb p} \rightarrow \text{Pb} + M + X)/dY$ at $Y=0$

$d\sigma/dY_M$ at $Y_M = 0$ in μb

C-even meson (M)	Odderon Signal		Backgrounds		
	Upper Limit	QCD Prediction	$\gamma\gamma$	Pomeron-Pomeron	$V \rightarrow M + \gamma$
π^0	7.4	0.1 - 1	0.044	—	<u>30</u> ($\omega \rightarrow \pi^0\gamma$)
$f_2(1270)$	3	0.05 - 0.5	0.020	<u>3 - 4.5</u>	0.02 ($J/\psi \rightarrow f_2\gamma$)
$\eta(548)$	3.4	0.05 - 0.5	0.042	negligible	<u>3</u> ($\phi \rightarrow \eta\gamma$)
η_c	—	$(0.1 - 0.5) \cdot 10^{-3}$	0.0025	$\sim 10^{-5}$	0.012 ($J/\psi \rightarrow \eta_c\gamma$)

$\eta_c \times 0.05$ for observable BR included

$p p \rightarrow p + M + X$ Pom – Pom background overwhelming
 $\text{Pb Pb} \rightarrow \text{Pb} + M + \text{Pb}$ $\gamma\gamma$ background overwhelming

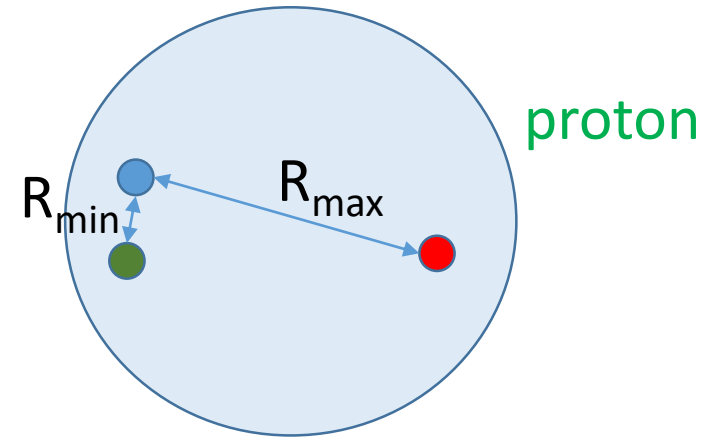
Ronan McNulty: Pb-Pb data could check model for Pom-Pom bk^{gd} for f_2 ; $\text{BR}(f_2 \rightarrow \gamma\gamma) \sim 10^{-5}$

Conclusions

CEP survival factors calculable but depend on kinematics

Theoretically the **Odderon** exists (pQCD), but the amplitude is small in comparison with the **Pomeron**

$$A_{\text{Odd}} \sim \alpha_s^3 R_{\text{min}}^2$$
$$A_{\text{Pom}} \sim \alpha_s^2 R_{\text{max}}^2$$



Experimentally the Odderon is elusive, but with experimental ingenuity and precision it stands a good chance of being cornered

Use HERA data to predict diffractive dijet production at Tevatron

$$\sigma = \text{PDF}_{\text{proton}}(x_1) \otimes |M|^2 \otimes \text{PDF}_{\text{pomeron}}(x_2)$$

factor ~ 10 too big

