

Any kind of  $1/2^+$  octet hyperon EM form factor  
timelike behaviors by a measurement of the  
hyperon polarizations in  $e^+e^- \rightarrow Y\bar{Y}$  processes

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# INTRODUCTION

An application of the SU(3) symmetry to a **classification of mesons and baryons** revealed theoretically an existence of **"quarks"**, and induced the idea

- **"mesons"** are bound states of quarks and antiquarks,
- **"baryons"** are compound of 3 quarks,

therefore it was natural to expect that **they have some EM structure** to be described by some EM form factors (FFs).

The  $1/2^+$  octet hyperons  $Y = \Lambda^0, \Sigma^+, \Sigma^0, \Sigma^-, \Xi^0, \Xi^-$  **contain always at least one strange quark**

$\Lambda^0 = uds$ ,  $\Sigma^+ = uus$ ,  $\Sigma^0 = uds$ ,  $\Sigma^- = dds$ ,  $\Xi^0 = uss$ ,  $\Xi^- = dss$   
therefore they are also called to be **"strange baryons"**.

# INTRODUCTION

Since  $1/2^+$  octet hyperons  $Y = \Lambda^0, \Sigma^+, \Sigma^0, \Sigma^-, \Xi^0, \Xi^-$  are **particles with the spin  $S = 1/2$**

$\implies$  their EM structure is **completely described by 2 independent functions** of one variable

(in timelike region it is the total energy squared  $s = W^2$ )

the "**Sachs electric FF**"  $G_E^Y(s)$

the "**Sachs magnetic FF**"  $G_M^Y(s)$ .

They can be expressed through the **Dirac  $F_1^Y(s)$**  and the **Pauli  $F_2^Y(s)$**  FFs of hyperons

$$G_E^Y(s) = F_1^Y(s) + \frac{s}{4m_Y^2} F_2^Y(s)$$

$$G_M^Y(s) = F_1^Y(s) + F_2^Y(s) \quad (1)$$

where  $m_Y$  is the hyperon mass.

# INTRODUCTION

From (1) ( $\sigma_{tot}^{c.m.}(e^+e^- \rightarrow Y\bar{Y})$ ) the **equality**

$$G_E^Y(4m_Y^2) \equiv G_M^Y(4m_Y^2) \quad (2)$$

automatically follows **at the production threshold of hyperon-antihyperon pair** in electron-positron annihilation.

$F_1^Y(s)$ ,  $F_2^Y(s)$  FFs are obtained as **coefficients in a decomposition of the hyperon matrix element of the EM current  $J_\mu^{EM}$  into maximum number of linearly independent covariants** constructed from the four momenta  $p_1, p_2$ , Dirac  $\gamma$ -matrices and Dirac bispinors of the hyperons

$$\langle Y | J_\mu^{EM} | Y \rangle = e\bar{u}(p_2)\{\gamma_\mu F_1^Y(s) + \frac{i}{2m_Y}\sigma_{\mu\nu}(p_2 - p_1)_\nu F_2^Y(s)\}u(p_1). \quad (3)$$

# CURRENT DETERMINATION OF $|G_E^Y(s)|$ and $|G_M^Y(s)|$ BEHAVIORS

The electric  $G_E^Y(s)$  and magnetic  $G_M^Y(s)$  FFs are very **suitable in extracting experimental information** on the hyperon EM structure from measured e.g.

the **total cross section**

$$\sigma_{tot}^{c.m.}(e^+e^- \rightarrow Y\bar{Y}) = \frac{4\pi\alpha^2\beta_Y(s)}{3s} \{ |G_M^Y(s)|^2 + \frac{2m_Y^2}{s} |G_E^Y(s)|^2 \} \quad (4)$$

or the **differential cross section**

$$\frac{d\sigma(e^+e^- \rightarrow Y\bar{Y})}{d\Omega} = \frac{\alpha^2\beta_Y(s)}{4s} \{ |G_M^Y(s)|^2 (1 + \cos^2\theta) + \frac{4m_Y^2}{s} |G_E^Y(s)|^2 \sin^2\theta \} \quad (5)$$

where  $\beta_Y(s) = \sqrt{1 - \frac{4m_Y^2}{s}}$  is the **velocity of produced hyperon** and  $\theta$  **scattering angle**.

# CURRENT DETERMINATION OF $|G_E^Y(s)|$ and $|G_M^Y(s)|$ BEHAVIORS

In the case of the total cross section **from one measured value of  $\sigma_{tot}^{c.m.}(e^+e^- \rightarrow Y\bar{Y})$  at some energy one has to specify two independent numbers  $|G_E^Y(s)|$  and  $|G_M^Y(s)|$ .**

As we have an experience from the protons

a) **either equality of both EM FFs is applied** in (4), - it can be used only at the neighborhood of the production threshold  $s = 4m_Y^2$  in  $e^+e^-$  annihilation,

b) **or at higher energies, due to the factor  $\frac{2m_Y^2}{s}$ , a negligible contribution, i.e.  $G_E^Y(s) \approx 0$ , is assumed.**

**Both assumptions are model ingredients leading to hyperon magnetic FF  $|G_M^Y(s)|$  behavior not to be very reliable.**

# CURRENT DETERMINATION OF $|G_E^Y(s)|$ and $|G_M^Y(s)|$ BEHAVIORS

**More powerful** in determination of  $|G_E^Y(s)|$  and  $|G_M^Y(s)|$  **is a measurement of the differential cross section** (5), under an assumption that there are colliders **with enough large integrated luminosity  $L$** .

Such accelerating facilities now exist, mainly the **SLAC PEP-II asymmetric-energy  $e^+e^-$  collider** and also the **BEPC II double-ring  $e^+e^-$  collider in Beijing**, at which at some discrete values of energies for protons differential cross section  $\frac{d\sigma(e^+e^- \rightarrow p\bar{p})}{d\Omega}$  has been measured, giving a **new model independent information on the EM structure of the proton in timelike region** for the first time.



# CURRENT DETERMINATION OF $|G_E^Y(s)|$ and $|G_M^Y(s)|$ BEHAVIORS

The **method is transparent** if differential cross section (5) is rewritten into the form

$$\frac{d\sigma(e^+e^- \rightarrow Y\bar{Y})}{d\Omega} = a(s) + b(s) \cos^2 \theta \quad (6)$$

where

$$a(s) = \frac{\alpha^2 \beta_Y(s)}{s} \left\{ \frac{1}{4} |G_M^Y(s)|^2 + \frac{m_Y^2}{s} |G_E^Y(s)|^2 \right\} \quad (7)$$

$$b(s) = \frac{\alpha^2 \beta_Y(s)}{s} \left\{ \frac{1}{4} |G_M^Y(s)|^2 - \frac{m_Y^2}{s} |G_E^Y(s)|^2 \right\}. \quad (8)$$

# CURRENT DETERMINATION OF $|G_E^Y(s)|$ and $|G_M^Y(s)|$ BEHAVIORS

The latter method is **very effective for stable protons**, but **all  $1/2^+$  octet hyperons are weakly decaying particles** with the mean life  $\sim 10^{-10}$ s, besides  $\Sigma^0$ -hyperon - the mean life of which is  $\sim 10^{-20}$ s.

As a result the **angular distribution of created hyperon-antihyperon pairs has to be reconstructed from the secondary particles appearing in the electron-positron annihilation processes.**

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

Till now an **experimental determination of absolute values of hyperon complex EM FFs** in timelike region has been discussed.

However, for the complete determination of the hyperon EM FFs in timelike region it is **necessary to know the following four combinations** of FFs

$$|G_E^Y(s)|^2, |G_M^Y(s)|^2, \text{Re}[G_E^Y(s)G_M^{Y*}(s)], \text{Im}[G_E^Y(s)G_M^{Y*}(s)], \quad (9)$$

and they **can not be specified without measurements of polarizations** in the  $e^+e^- \rightarrow Y\bar{Y}$  processes.

Further, explicit forms of **vector and tensor polarizations of final particles** in the  $e^+e^- \rightarrow Y\bar{Y}$  processes in the framework of the one photon exchange approximation **are calculated**.

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

In order to calculate the **single and double spin polarization observables** one is in need of the matrix element of  $e^+e^- \rightarrow Y\bar{Y}$  in the framework of the one-photon exchange approximation, which is defined by the formulae

$$\begin{aligned}
 \mathcal{M} &= \frac{e^2}{k^2} j_\mu J_\mu, \\
 j_\mu &= \bar{u}(k_2) \gamma_\mu u(k_1), \\
 J_\mu &= \bar{u}(p_2) \left[ F_1^Y(s) \gamma_\mu + F_2^Y(s) \frac{i\sigma_{\mu\nu} k_\nu}{2m_Y} \right] u(p_1),
 \end{aligned} \tag{10}$$

where  $s = k^2 \geq 4m_Y^2$ .

We emphasize, that the **c.m. system of the reaction  $e^+e^- \rightarrow Y\bar{Y}$  is the most suitable for the analysis of polarization effects.**

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

The **EM currents  $j_\mu$  and  $J_\mu$  are conserved**, namely  $k \cdot j = k \cdot J = 0$ , therefore in the c.m. system of  $e^+e^- \rightarrow Y\bar{Y}$  reaction  $j_0 = J_0 = 0$ . Then the matrix element  $\mathcal{M}$  is determined only by product of spatial components of currents,

$$\begin{aligned} \mathcal{M} &= -\frac{e^2}{s} \vec{j} \cdot \vec{J} \\ |\mathcal{M}|^2 &= \frac{e^4}{s^2} j_{ik} W_{ik}, \end{aligned} \quad (11)$$

where

$$j_{ik} = j_i j_k^* \quad W_{ik} = J_i J_k^*.$$

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

The EM current  $\vec{J}$  can be expressed through two-component spinors  $\varphi_1$  and  $\varphi_2$

$$\vec{J} = \sqrt{s}\varphi_1^+ \left[ G_M^Y(s)(\vec{\sigma} - \vec{n}\vec{\sigma} \cdot \vec{n}) + \frac{2m_Y}{\sqrt{s}} G_E^Y(s)\vec{n}\vec{\sigma} \cdot \vec{n} \right] \varphi_2 \quad (12)$$

where we denote

$$\vec{F} = \sqrt{s} \left[ G_M^Y(s)(\vec{\sigma} - \vec{n}\vec{\sigma} \cdot \vec{n}) + \frac{2m_Y}{\sqrt{s}} G_E^Y(s)\vec{n}\vec{\sigma} \cdot \vec{n} \right], \quad (13)$$

$\vec{\sigma}$  are Pauli matrices and  $\vec{n}$  is the unit vector along the three momentum  $\vec{q}$  of the hyperon .

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

If **both initial leptons are unpolarized** lepton tensor takes the form

$$j_{ij} = (\delta_{ij} - m_i m_j) \quad (14)$$

and the vector polarization of the final hyperon or antihyperon is

$$\vec{P} = \frac{j_{ij} \text{Tr}[F_i F_j^\dagger \vec{\sigma}]}{j_{ij} \text{Tr}[F_i F_j^\dagger]}. \quad (15)$$

Calculating the traces in the numerator and denominator, respectively, **one finds the only  $P_y$  polarization component to be different from zero**

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

$$P_x = 0 \quad (16)$$

$$P_y = -\frac{\frac{1}{\sqrt{\tau}} \text{Im}(G_M^*(t)G_E(t)) \sin 2\vartheta}{\frac{1}{\tau} |G_E|^2 \sin^2 \vartheta + |G_M|^2 (1 + \cos^2 \vartheta)}; \quad (17)$$

$$P_z = 0. \quad (18)$$

In other words, **even annihilation of unpolarized electron and positron lead to a polarization of the created final hyperon** in direction of the y-axis, which is orthogonal to the scattering plane.



# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

Recently such measurement of the polarization of the  $\Lambda$ -hyperon in the process  $e^+e^- \rightarrow \Lambda\bar{\Lambda}$  has been carried out

*Patrik Adlarson(BESIII Collab.), Contribution in MESON'18 Conference, 7.-12.6.2018, Cracow (Poland)*

whereby **polarization is experimentally accessible in weak parity violating decays** of  $\Lambda$ -hyperons - daughter particles are emitted according to polarization of mother hyperon.

They have measured the asymmetry parameter  $\alpha_-$  for  $\Lambda \rightarrow p\pi^-$  to be overestimated by more than 15 percent in comparison with the PDG value.

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

Knowing the latter author are able from the measured angular distribution

$$I(\cos \theta_\Lambda) = \frac{1}{4\pi}(1 + \alpha_- P_y \cos \theta_\Lambda) \quad (19)$$

to determine  $P_y$  of the  $\Lambda$  polarisation.

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

If at least one of the initial leptons is longitudinally polarized the corresponding lepton tensor takes the form

$$j_{ij} = (\delta_{ij} - m_i m_j + \lambda i \varepsilon_{ijl} m_l). \quad (20)$$

and the vector polarization of the final hyperon or antihyperon is again in the form

$$\vec{P} = \frac{j_{ij} \text{Tr}[F_i F_j^\dagger \vec{\sigma}]}{j_{ij} \text{Tr}[F_i F_j^\dagger]}. \quad (21)$$

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

Calculating the traces in the numerator and denominator, respectively, one finds the vector polarization components

$$P_x = -\frac{2 \sin \theta \cdot \text{Re}[G_{Ep}(s)G_{Mp}^*(s)]\tau}{|G_{Ep}(s)|^2 \sin^2 \theta/\tau + |G_{Mp}(s)|^2(1 + \cos^2 \theta)} \quad (22)$$

$$P_y = -\frac{\frac{1}{\sqrt{\tau}} \text{Im}(G_M^*(t)G_E(t)) \sin 2\vartheta}{\frac{1}{\tau}|G_E|^2 \sin^2 \vartheta + |G_M|^2(1 + \cos^2 \vartheta)}; \quad (23)$$

$$P_z = \frac{2 \cos \theta |G_{Mp}(s)|^2}{|G_{Ep}(s)|^2 \sin^2 \theta/\tau + |G_{Mp}(s)|^2(1 + \cos^2 \theta)}, \quad (24)$$

assuming 100% i.e.  $\lambda = 1$  longitudinal polarization of the electron.

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

In a similar procedure one can find explicit forms of double spin polarization observables in the  $e^+e^- \rightarrow Y\bar{Y}$  process, where we are interested for components of the polarizations of created hyperons and antihyperons simultaneously. Then the corresponding tensor of polarization is

$$P_{kl} = \frac{j_{ij} \text{Tr}[F_i \sigma_k F_j^\dagger \sigma_l]}{j_{ij} \text{Tr}[F_i F_j^\dagger]} \quad (25)$$

where  $k, l = x, y, z$ .

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

Calculating the trace in the numerator and similarly the trace in the denominator, **considering unpolarized incoming leptons**, one finds

$$\begin{aligned}
 P_{xx} &= \frac{|G_M^Y(s)|^2 \cos^2 \vartheta - \frac{1}{\tau} |G_E^Y(s)|^2 \sin^2 \vartheta}{\frac{1}{\tau} |G_E^Y(s)|^2 \sin^2 \vartheta + |G_M^Y(s)|^2 (1 + \cos^2 \vartheta)}; \\
 P_{yy} &= \frac{|G_M^Y(s)|^2 (1 + \sin^2 \vartheta) - \frac{1}{\tau} |G_E^Y(s)|^2 \sin^2 \vartheta}{\frac{1}{\tau} |G_E^Y(s)|^2 \sin^2 \vartheta + |G_M^Y(s)|^2 (1 + \cos^2 \vartheta)}; \\
 P_{zz} &= \frac{|G_M^Y(s)|^2 \sin^2 \vartheta - \frac{1}{\tau} |G_E^Y(s)|^2 \cos^2 \vartheta}{\frac{1}{\tau} |G_E^Y(s)|^2 \sin^2 \vartheta + |G_M^Y(s)|^2 (1 + \cos^2 \vartheta)}; \\
 P_{xy} &= P_{yx} = 0; \\
 P_{xz} &= P_{zx} = \frac{\frac{1}{\sqrt{\tau}} \operatorname{Re}[G_M^{Y*}(s) G_E^Y(s)] \sin 2\vartheta}{\frac{1}{\tau} |G_E^Y(s)|^2 \sin^2 \vartheta + |G_M^Y(s)|^2 (1 + \cos^2 \vartheta)}; \\
 P_{yz} &= P_{zy} = 0
 \end{aligned} \tag{26}$$

# POLARIZATIONS IN $e^+e^- \rightarrow Y\bar{Y}$ PROCESSES

**Considering the longitudinally polarized electron or positron for components  $P_{xx}, P_{yy}, P_{zz}, P_{xy}, P_{yx}, P_{xz}, P_{zx}$  one finds identical expressions with (26), but the last two components are now nonzero as well**

$$P_{yz} = P_{zy} = -2 \frac{\frac{1}{\sqrt{\tau}} \text{Im}[G_M^{Y*}(s)G_E^Y(s)] \sin \vartheta}{\frac{1}{\tau} |G_E^Y(s)|^2 \sin^2 \vartheta + |G_M^Y(s)|^2 (1 + \cos^2 \vartheta)}. \quad (27)$$

Every of components  $P_{kl}$  characterize a polarization of the hyperon  $Y$  in the direction  $k$ , if antihyperon  $\bar{Y}$  is polarized at the direction  $l$  and they all are calculated for 100% polarization of one of the initial leptons.

## CONCLUSIONS

The single-spin and double spin polarizations of the created hyperons in the process  $e^+e^- \rightarrow Y\bar{Y}$ , dependent on the state of a polarization of the initial leptons, has been demonstrated.

It was shown, that **even annihilation of unpolarized electron and positron lead to a polarization of the created final hyperon** in direction of the y-axis, which is orthogonal to the scattering plane. This effect is already confirmed by BESIII Collaboration in Beijing recently by a measurement polarization in the process  $e^+e^- \rightarrow \Lambda\bar{\Lambda}$ .



# Thank you for your attention.