

Theoretical Aspects of Baryon Form Factors

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Theoretical aspects of baryon form factors – Ulf-G. Meißner – EMMI RRTF, GSI, Oct. 22nd, 2018 • O < < < < > > > > • •

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Introduction

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FACETS of the NUCLEON / of BARYONS

- Basic objects of QCD in the strong coupling regime
- Various probes (electromagnetic, weak) see different facets/scales





- \hookrightarrow use the nucleon to develop methods
- \hookrightarrow gain insight \rightarrow testbed for hyperons/cascades
- \hookrightarrow important role of final-state-interactions (FSI)
- \hookrightarrow beautiful link between electromagnetic and hadronic interactions

WHY DISPERSION RELATIONS for the NUCLEON FFs ?

- \bullet Model-independent approach \rightarrow important non-perturbative tool to analyze data
- Dispersion relations are based on fundamental principles: unitarity & analyticity
- Connect data from small to large momentum transfer

as well as time- and space-like data

- Allow for a **simultaneous analysis** of all four em form factors
- Spectral functions encode perturbative and non-perturbative physics e.g. vector meson couplings, multi-meson continua, pion cloud, ...
- Spectral functions also encode information on the strangeness vector current \rightarrow sea-quark dynamics, strange matrix elements
- Allow to extract nucleon electric and magnetic radii
- Can be matched to chiral perturbation theory [and not the other way around!]

Theoretical framework

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BASIC DEFINITIONS

• Nucleon matrix elements of the em vector current J^{I}_{μ}

$$\langle N(p')| oldsymbol{J}^{I}_{\mu}| N(p)
angle = ar{u}(p') \left[oldsymbol{F}^{I}_{1}(t) \, \gamma_{\mu} + i \, rac{F^{I}_{2}(t)}{2m} \, \sigma_{\mu
u} q^{
u} \,
ight] u(p)$$

* isospin I = S, V (isoScalar, isoVector) $[= (p \pm n)/2]$

 \star four-momentum transfer $t\equiv q^2=(p'-p)^2\equiv -Q^2$

 $\star F_1$ = Dirac form factor, F_2 = Pauli form factor

- * Normalizations: $F_1^V(0) = F_1^S(0) = 1/2, F_2^{S,V}(0) = (\kappa_p \pm \kappa_n)/2$
- \star Sachs form factors: $G_E = F_1 + rac{t}{4m^2}F_2 \;,\; G_M = F_1 + F_2$
- \star Nucleon radii: F(t)=F(0) $\left[1+t\langle r^2
 angle/6+\ldots
 ight]$ [except for the neutron charge ff]

DISPERSION RELATIONS

Federbush, Goldberger, Treiman, Drell, Zachariasen, Frazer, Fulco, Höhler, ...

- The form factors have cuts in the interval $[t_n, \infty[$ (n = 0, 1, 2, ...) and also poles
- \Rightarrow Dispersion relations for $F_i(t)$ (i = 1, 2):

$$F_i(t) = rac{1}{\pi} {\int_{t_0}^\infty} dt' \; rac{{
m Im}\; F_i(t')}{t'-t}$$

no subtractions

[only proven in perturbation theory]

- suppression of higher mass states
- central objects: spectral functions

 ${\sf Im}\ F_i(t)$

 $- \operatorname{cuts} \stackrel{\wedge}{=} \operatorname{multi-meson} \operatorname{continua}$ $- \operatorname{poles} \stackrel{\wedge}{=} \operatorname{vector} \operatorname{mesons}$



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<u>SPECTRAL FUNCTIONS – GENERALITIES</u>

• Spectral decomposition:

$$\operatorname{Im} \langle \bar{N}(p')N(p)|J^{I}_{\mu}|0
angle \sim \sum_{n} \langle \bar{N}(p')N(p)|n
angle \langle n|J^{I}_{\mu}|0
angle \Rightarrow \operatorname{Im} F$$

- ***** on-shell intermediate states
- * generates imaginary part
- \star accessible physical states



• *Isoscalar* intermediate states: $3\pi, 5\pi, \ldots, K\bar{K}, K\bar{K}\pi, \pi\rho, \ldots +$ poles

• *Isovector* intermediate states: $2\pi, 4\pi, \ldots +$ poles $\rightarrow t_0 = 9M_\pi^2$ $\rightarrow t_0 = 4M_\pi^2$

• Note that some poles are *generated* from the appropriate continua

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ISOVECTOR SPECTRAL FUNCTIONS

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Frazer, Fulco, Höhler, Pietarinen, ...

Bernard, Kaiser, UGM, Nucl. Phys. A 611 (1996) 429

• exact 2π continuum is known from threshold $t_0 = 4 M_\pi^2$ to $t \simeq 40 \, M_\pi^2$

Im
$$G_{E/M}^V(t) = rac{q_t^3}{(m_N/\sqrt{2})\sqrt{t}} F_{\pi}(t)^{\star} f_{+/-}^1(t)$$

- $\star F_{\pi}(t)$ = pion vector form factor
- \star P-wave pion-nucleon partial waves in the t-channel [$\sim f^1_{\pm}(t)$]



ullet Spectral functions inherit singularity on the second Riemann sheet in $\pi N o \pi N$

 $t_c = 4 M_\pi^2 - M_\pi^4/m^2 \simeq 3.98\,M_\pi^2 \Big| o$ strong shoulder o isovector radii

- This singularity can also be analyzed in CHPT
- For a recent determination of the 2π continuum, see HKRHM, EPJA 52 (2016) 331
- Higher mass states represented by poles (not necessarily physical masses)

ISOSCALAR SPECTRAL FUNCTIONS

- $K\bar{K}$ continuum can be extracted from analytically cont. KN scattering amplitudes
 - \rightarrow analytic continuation must be stabilized
 - ightarrow generates most of the ϕ contribution

Hammer, Ramsey-Musolf, Phys. Rev. C 60 (1999) 045204, 045205

- Further strength in the ϕ -region generated by correlated $\pi \rho$ exchange
 - ightarrow strong cancellations ($Kar{K}, K^*K, \pi
 ho$)
 - ightarrow takes away sizeable strength from the ϕ

UGM, Mull, Speth, van Orden, Phys. Lett. B 408 (1997) 381

• Spectral functions exhibit anomalous threshold (analyzed in 2-loop CHPT)

$$t_c = M_\pi^2 \left(\sqrt{4 - M_\pi^2/m^2} + \sqrt{1 - M_\pi^2/m^2}
ight)^2 \simeq 8.9 \, M_\pi^2
ight|
ightarrow ext{effectively masked}$$

Bernard, Kaiser, M, Nucl. Phys. A 611 (1996) 429

• Higher mass states represented by poles (with a finite width)



CONSTRAINTS ON THE SPECTRAL FUNCTIONS

- Normalizations: electric charges, magnetic moments
- Radii not imposed [can be done using subtracted DR]
- Superconvergence relations \cong leading pQCD behaviour

$$F_1(t) \sim 1/t^2 , F_2(t) \sim 1/t^3 \text{ (helicity - flip)} \xrightarrow{} F_2(t) \xrightarrow{} F_2(t) \text{ Brodsky et al.}$$

$$\Rightarrow \int_{t_0}^{\infty} \operatorname{Im} F_1(t) \, dt = 0 , \quad \int_{t_0}^{\infty} \operatorname{Im} F_2(t) \, dt = \int_{t_0}^{\infty} \operatorname{Im} F_2(t) \, t \, dt = 0$$

• Various ways of implementing the asymptotic QCD behaviour

 \Rightarrow severely restricts the number of fit parameters

SUMMARY: SPECTRAL & FIT FUNCTIONS

• Representation of the pole contributions: vector mesons [NB: can be extended for finite width]

$$\operatorname{Im} F_i^V(t) = \sum_v \pi a_i^v \,\delta(t - M_v^2) \,, \quad a_i^v = \frac{M_v^2}{f_V} g_{vNN} \,\Rightarrow\, F_i(t) = \sum_v \frac{a_i^v}{M_v^2 - t}$$

• Isovector spectral functions:

$$\operatorname{Im} F_{i}^{V}(t) = \operatorname{Im} F_{i}^{(2\pi)}(t) + \sum_{v=v_{1},v_{2},\dots} \pi a_{i}^{v} \delta(t - M_{v}^{2}), \quad (i = 1, 2)$$

• Isoscalar spectral functions:

$$\mathrm{Im}F_{i}^{S}(t) = \mathrm{Im}F_{i}^{(K\bar{K})}(t) + \mathrm{Im}F_{i}^{(\pi\rho)}(t) + \sum_{v=\omega,\phi,s_{1},s_{2},...} \pi a_{i}^{v}\delta(t - M_{v}^{2})$$

- Parameters: 2 for the ω , ϕ , 3 (4) for each other V-mesons minus # of constraints
- Ill-posed problem \rightarrow extra constraint: minimal # of poles to describe the data

Results

Belushkin, Hammer, UGM, Phys. Rev. C 75 (2007) 035202 [hep-ph/0608337]

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GENERAL COMMENTS ON THE FITS

- large MC sampling for initial values, successive improvement by pole reduction, new MCs, ...
- theoretical uncertainty (error bands) from $\chi^2_{\rm min} + 1.04$ [1- σ devs.]

 \rightarrow first time: dispersive analysis w/ error bars !

	this work	HM 04	recent determ.		
r_E^p [fm]	0.844 (0.8400.852)	0.848	0.880(15) [1,2,3]		
r^p_M [fm]	0.854 (0.8490.859)	0.857	0.855(35) [4]		
$(r_E^{m{n}})^{m{2}}$ [fm 2]	-0.117 (-0.110.128)	-0.12	-0.115(4) [5]		
$\stackrel{-}{r_M^n}$ [fm]	0.862 (0.8540.871)	0.879	0.873(11) [6]		

[1] Rosenfelder, Phys. Lett. B 479 (2000) 381

[2] Sick, private communication

[3] Melnikov, van Ritbergen, Phys. Rev. Lett. 84 (2000) 1673

[4] Sick, Phys. Lett. B 576 (2003) 62

[5] Kopecky et al., Phys. Rev. C 56 (1997) 2229

[6] Kubon et al., Phys. Lett. B **524** (2002) 26

* Magnetic radii in good agreement with recent determinations

 \star Proton electric radius comes out \lesssim 0.855 fm

SPACE-LIKE FORM FACTORS

- present best fit incl. time-like data
- ω, ϕ + 2 eff. IS poles
- 5 effective IV poles
- weighted χ^2 /dof = 1.8 error bands: $\chi^2_{min} + 1.04$

Improved description

- * JLab data described
- higher mass poles
 not at physical values

MMD 96, HMD 96, HM 04

$$G_D(Q^2) = \left(1 + \frac{Q^2}{0.71 \, {\rm GeV}^2}\right)^{-2}$$



TIME-LIKE FORM FACTORS



- Only proton data participate in the fits
- All data within one sigma first time consistent fit w/ space-like ffs

 \Rightarrow Need more data on time-like G_M^n & E/M separation

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The proton radius

Lorenz, Hammer, UGM, Eur. Phys. J. **A 48** (2012) 151 [arXiv:1205.6628 [hep-ph]] Lorenz, UGM, Phys. Lett. **B 737** (2014) 57 [arXiv:1406.2962 [hep-ph]] Lorenz, UGM, Hammer, Dong, Phys. Rev. **D 91** (2015) 014023 [arXiv:1411.1704 [hep-ph]]

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<u>A SHORT HISTORY</u>

• Dispersion relations always found a "small" radius

 $r_E^p = 0.847 \, {
m fm}$ Mergell, UGM, Drechsel 1995 $r_E^p = 0.848 \, {
m fm}$ Hammer, UGM 2004 $r_E^p = 0.844 \, (0.840...0.852) \, {
m fm}$ Belushkin, Hammer, UGM 2007

• CODATA 2008: $r_E^p = 0.8768(69)$ fm

- Muonic hydrogen at PSI: $r_E^p = 0.84184(67)$ fm Pohl et al. 2010 $r_E^p = 0.84087(39)$ fm Antognini et al. 2013
- Electron-proton scattering at MAMI: $r_E^p = 0.876(8)$ fm

Bernauer et al. 2010

- \Rightarrow zillions of papers, different levels of sophistication, ...
- \Rightarrow reanalyze Mainz data including constraints from analyticity and unitarity
- \Rightarrow study various sources of uncertainties (2π continuum, radiative corrections, etc.)

DIRECT CROSS SECTION FITS

- is the small radius in the DR approach consistent with the Mainz data?
- Fit directly to ep Xsections (and other world data & also the neutron FF data)
 - \star use the recent MAMI data \rightarrow slide
 - floating normalizations for individual data sets w/ different kinematical conditions [as done by the Mainz group, see PhD thesis J. Bernauer]
 - ***** include new and improved TPE corrections
 - * include error correlations and use bootstrap methods to estimate fit errors
 - \Rightarrow improves the earlier methods based on χ^2 only
 - perform also purely statistical fits based on a conformal mapping (not including all physics constraints, not discussed here)

Will we still obtain a small radius?

NEW MAINZ DATA

• Kinematical coverage of the new MAMI data (1422 data pts)



A1 collaboration, J. Bernauer et al., Phys. Rev. C 90 (2014) 015206

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NEW DEVELOPMENTS: TPE CORRECTIONS

Lorenz, UGM, Hammer, Dong, Phys. Rev. D 91 (2015) 014023 [arXiv:1411.1704v1]

- ullet improved calculation of two-photon exchange effects incl. the Δ
 - \rightarrow study dependence on nucleon ffs! [never done before]
- •TPE correction: $\delta_{2\gamma} = \delta_{2\gamma,N} + \delta_{2\gamma,\Delta}$
- $\delta_{2\gamma,\Delta}$ more sensitive to ffs than $\delta_{2\gamma,N}$





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 $\exists < \land \lor > \triangleright$

Ο

• Mainz uses the old Feshbach/Kinley approximation

 $\delta_F = Z lpha_{
m EM} \pi rac{\sin heta/2 - \sin^2 heta/2}{\cos^2 heta/2}$

incorrect for some kinematics Arrington 2011

- our TPE correction: $\delta_{2\gamma} = \delta_{2\gamma,N} + \delta_{2\gamma,\Delta}$
- $\delta_{2\gamma,\Delta}$ effects small for MAMI data \rightarrow important for world data at higher Q^2 Sick, priv. comm.
- $\delta_{2\gamma,N}$ quite different from Feshbach approx. \rightarrow important for the error budget!



 σ/σ_{dip}

NEW DISPERSIVE FITS to MAMI & WORLD DATA

- Fit to the Mainz data and also the world data on ep scattering at higher Q^2
- Float the normalizations similar what was done by the Mainz group
- Good fit requires 5 IS and 5 IV poles (28 + 31 + 23 parameters)

 \rightarrow show plots next slide

 \rightarrow achieve good χ^2 /ndf = 1.37 (1422 + 1922 data points)

ightarrow radii with 3σ uncertainties from bootstrap:

 $r_{E}^{p}=0.840~(0.828-0.855)\,{
m fm}$ $r_{M}^{p}=0.848~(0.843-0.854)\,{
m fm}$

- perfectly consistent with earlier DR determinations
- consistency check: predict the ff ratio G^p_E/G^p_M measured at JLAB \rightarrow slide

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PREDICTON of the JLAB DATA

• Polarisation measurements at low Q^2 give directly $\mu_p G_E^p/G_M^p$



Ron et al., Phys. Rev. C 84 (2011) 055204 Zhan et al., Phys. Lett. B 705 (2011) 59

The proton form factors in the timelike region

Haidenbauer, Kang, UGM, Nucl. Phys. A 929 (2014) 102 [arXiv:1405.1628 [nucl-th]]

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BASIC DEFINITIONS and FACTS

ullet differential Xsection for $e^+e^-\leftrightarrowar{p}p$ in the one-photon approximation

$$\frac{d\sigma}{d\Omega} = \frac{\alpha_{\rm EM}^2 \beta}{4s} C_p(s) \left[\left| G_M(s) \right|^2 \left(1 + \cos^2 \theta \right) + \frac{4M_p^2}{s} \left| G_E(s) \right|^2 \sin^2 \theta \right], \quad \beta = \frac{k_p}{k_e}$$

- $G_{E,M}(s)$ are complex for $s \geq 4M_p^2$
- threshold constraint: $G_E(4M_p^2) = G_M(4M_p^2)$
- Gamov-Sommerfeld factor:

$$C_p = rac{y}{1-e^{-y}}\,, \;\; y = rac{\pi lpha_{
m EM} M_p}{k_p}\,, \;\; \sqrt{s} = 2 \sqrt{M_p^2 + k_p^2}$$

ullet Data from $e^+e^-
ightarrow ar p p$ and $ar p p
ightarrow e^+e^-$

 \rightarrow extraction of ffs difficult, strong threshold enhancement





• effective FF ($\sigma \sim |G_{
m eff}|^2$)



- ullet strong enhancement in the threshold region $q\sim 2M_p$
- effective form factor consistent with data from $\bar{p}p \rightarrow e^+e^-$ (mod. norm.)
- threshold enhancement also seen in $J/\psi o ar p p \gamma, \psi(3686) o ar p p \gamma, J/\psi o ar p p \omega, B^+ o ar p p K^+$

FINAL-STATE INTERACTIONS

- threshold enhancement appears to be an universal phenomenon
- hypothesis: it is generated by the strong $ar{p}p$ FSI
- bare ffs dressed by FSI, and these generated all the Q^2 dependence \rightarrow one number to be fitted
- FSI from chiral EFT
 - ightarrow only 3S_1 and 3D_1 partial waves







Kang, Haidenbauer, UGM, JHEP **1402** (2014) 113 Dai, Haidenbauer, UGM, JHEP **1707** (2017) 078

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CHIRAL NUCLEON-ANTINUCLEON POTENTIAL

Kang, Haidenbauer, UGM, JHEP 1402 (2014) 113; Dai, Haidenbauer, UGM, JHEP 1707 (2017) 078

• **N**N potential has two parts:

 $V^{\bar{\mathbf{N}}\mathbf{N}} = V^{\bar{\mathbf{N}}\mathbf{N}}_{\text{elast.}} + V^{\bar{\mathbf{N}}\mathbf{N}}_{\text{ann.}}$

• Elastic part from G-parity transformation:

 $V^{\rm NN} = +V_{1\pi} + V_{2\pi} + V_{3\pi} + \ldots + V_{\rm cont}$

- $ightarrow V_{ ext{elast.}}^{ ilde{ ext{NN}}} = -V_{1\pi} + V_{3\pi} V_{3\pi} + \ldots + V_{ ext{cont}}$
- \hookrightarrow can be taken over from the chiral EFT NN potential
- Annihilation potential accounts for the open annihilation channels

$$V_{
m ann.}^{ar{f N}f N} = \sum_{f X} V^{ar{f N}f N o f X}$$
 , $f X = \pi, 2\pi, 3\pi, 4\pi, \dots$

 \hookrightarrow describe annihilation by a few effective two-body channels (with 3/2/1/1 LECs for S/P/D/F) \hookrightarrow preserves unitarity!



ann.

elast

PROTON-ANTIPROTON ANNIHILATION

Dai, Haidenbauer, UGM, JHEP 1707 (2017) 078

- Results from chiral EFT at NNNLO
- Uncertainties as developed for the NN system







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FIT and PREDICTIONS

 one parameter fitted for excess energies smaller than 60 MeV



• Predictions:

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PREDICTIONS: DIFFERENTIAL XS

• differential X sections from BaBar and PS170 $[Q = \sqrt{s} - 2M_p]$





PS170: Bardin et al., Nucl. Phys. B 411 (1994) 3
BaBar: Aubert et al., Phys. Rev. D 73 (2006) 012005
BaBar: Lees et al., Phys. Rev. D 87 (2013) 092005

FURTHER PREDICTIONS

• complex form factor ratio



- ratio and phase are to be determined w/ PANDA at FAIR
- also predictions for the analyzing power and spin correlation coefficients
 → see Haidenbauer, Kang, UGM, Nucl. Phys. A 929 (2014) 102

 \hookrightarrow spares

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UNIVERSALITY of the FSI MECHANISM

• explains a large number of threshold enhancements



Kang, Haidenbauer, UGM, Phys. Rev. D 91 (2015) 074003

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UNIVERSALITY of the FSI MECHANISM cont'd

Dai, Haidenbauer, UGM, Phys. Rev. D 98 (2018) 014005

• and even the structure observed by BESIII in $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^$ at the $\bar{p}p$ threshold (coupled channel calculation)

M. Ablikim et al. (BESIII Coll.), Phys. Rev. Lett. 117 (2016) 042002 (2016)



The Λ form factors in the timelike region

Haidenbauer, UGM, Phys. Lett. B 761 (2016) 456 [arXiv:1608.02766 [nucl-th]]

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BASIC DEFINITIONS and FACTS

- ullet Consider the reaction $e^+e^-
 ightarrow ar{\Lambda} \Lambda$
- Formalism identical to the proton case, just change labels $[C_p(s) = 1]$

$$rac{d\sigma}{d\Omega} = rac{lpha_{
m EM}^2eta}{4s}\,\left[\left|G_M(s)
ight|^2 \left(1+\cos^2 heta
ight) + rac{4M_\Lambda^2}{s}\left|G_E(s)
ight|^2 \sin^2 heta
ight]$$

• As usual, define an effective ff:

$$|G_{\text{eff}}(s)| = \sqrt{\frac{\sigma_{e^+e^- \to \bar{\Lambda}\Lambda}(s)}{\frac{4\pi\alpha_{\text{EM}}^2\beta}{3s} \left[1 + \frac{2M_{\Lambda}^2}{s}\right]}}$$

• The $\bar{\Lambda}\Lambda$ interaction must be modelled
 \rightarrow describe all PS185 data on $\bar{p}p \to \bar{\Lambda}\Lambda$
Haidenbauer et al., Phys. Rev. C **45** (1992) 931
Haidenbauer et al., Phys. Rev. C **46** (1992) 2158
P \bar{p}

SOME OLD RESULTS

total XS

diff. XS

Polarizations



Haidenbauer, Holinde, Mull. Speth, Phys. Rev. C 46 (1992) 2158

FIT and PREDICTIONS

• Fit: one parameter fitted to the value at the maximum

DM2: Bisello et al., Z. Phys. C 48 (1990) 23BaBar: Aubert et al., Phys. Rev. D 76 (2007) 092006

BESIII: P. Larin et al., PoS Hadron2017 (2018) 158



• Effective form factor:

- \hookrightarrow good description of the data \checkmark



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FURTHER PREDICTIONS

• complex form factor ratio



- stronger model predictions, PANDA at FAIR? or BESIII? or ...
- also predictions for differential XS and spin correlation parameters

 \hookrightarrow see Haidenbauer, UGM, Phys. Lett. B **761** (2016) 456

 \hookrightarrow spares

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Once more on the isovector spectral functions

Hoferichter, Kubis, Ruiz de Elvira, Hammer, UGM, Eur. Phys. J. A 52 (2016)331 [arXiv:1609.06722 [nucl-th]]

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ROY-STEINER EQUATION ANALYSIS

- improve the isovector spectral functions by
 - \hookrightarrow updated πN amplitudes from Roy-Steiner equations
 - → include modern data (esp. pionic hydrogen & deuterium)
 - \hookrightarrow better treatment of isospin-violating effects
 - \hookrightarrow construct the pion FF from precise knowledge of $\delta_1^1(s)$
 - \hookrightarrow perform systematic error analysis



Hoferichter, Ruiz de Elvira, Kubis, UGM, Phys. Rev. Lett. 115 (2015) 092301; Phys. Rev. Lett. 115 (2015) 192301; Phys. Rept. 625 (2016) 1; J.Phys. G45 (2018) 024001



NEW ISOVECTOR SPECTRAL FUNCTIONS

• Precise determinations of the isovector spectral functions



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MODELLING ISOVECTOR TRANSITIONS

- For hyperons, combine CHPT with dispersion relations
- ullet consider e.g. $\Sigma^0
 ightarrow \Lambda \gamma^{\star}$
- include only the 2π intermediate state
- \hookrightarrow dispersive representation for the form factor(s)
- \hookrightarrow best use MO scheme for pion rescattering
- \hookrightarrow induces some cutoff dependence (1 $\leq \Lambda \leq 2 \text{ GeV})$
- use baryon CHPT to describe pion-baryon scattering
- \hookrightarrow must include the decuplet
- → known from connecting the threshold with the subthreshold region
 Siemens et al., Phys. Lett. B 770 (2017) 27
- only applicable for isovector transitions
- \hookrightarrow must gauge on the nucleon case!

Granados, Leupold, Perotti, EPJA **53** (2017) 117 Leupold, EPJA **54** (2017) 1

 $\xrightarrow{\Sigma} \qquad \xrightarrow{\Sigma} \qquad \xrightarrow{\Sigma} \qquad \xrightarrow{\pi} \qquad \xrightarrow{\pi} \qquad \xrightarrow{\pi} \qquad \xrightarrow{\Lambda} \qquad \xrightarrow{\Sigma} \qquad \xrightarrow{\pi} \qquad \xrightarrow{\Sigma} \qquad \xrightarrow{\pi} \qquad \xrightarrow{\Sigma} \qquad \xrightarrow{\pi} \qquad \xrightarrow{\Sigma} \qquad$

 π

 π

TESTING on the NUCLEON

- If the modelling should make sense, one must recover the isovector spectral functions based on the RS analysis!
- clearly the case for the MO approach to pion rescattering Leupold, Eur. Phys. J. A 54 (2017) 1
- Alternative: use the N/D approach to describe pion rescattering
 - \hookrightarrow clearly at odds with the exact description
 - \hookrightarrow overshoots the IV radius by far!
 - \hookrightarrow should be abandoned!
 - Alarcon, Weiss, Phys. Rev. C 97 (2018) 055203
- isoscalar case less well constrained (see earlier discussion)



SUMMARY & OUTLOOK

- Dispersion theory is the best tool to analyze the nucleon em FFs
 → always a small radius, status of electronic hydrogen unclear → slide
 → more data in the time-like region are needed
- Proton time-like FFs show a strong threshold enhancement $\rightarrow p\bar{p}$ FSI $\hookrightarrow p\bar{p}$ FSI can be described in chiral EFT \hookrightarrow appears to be a universal phenomenon
- A time-like FFs can be modelled in a similar way → no chiral EFT so far
 → works well, but puzzling datum just at the threshold from BESIII
- CHPT and dispersive approaches together allow for predictions of hyperon FFs
 → so far, only for the isovector transitions
 - \hookrightarrow must gauge on the well-determined nucleon IV spectral functions
- Nice interplay of electromagnetic & hadronic physics → interesting times ahead!

ELECTRONC LAMB SHIFT

• Recent results from PSI and ENS



PSI: Beyer et al., Science 358 (2017) 79 ENS: Fleurbaey et al., Phys. Rev. Lett. 120 (2018) 183001

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0.94



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ISOSCALAR SPECTRAL FUNCTION

• Two-loop CHPT calculation



• Electric/magnetic spectral fcts



* no shoulder on the left wing
* clean omega-pol dominance

RADIUS EXTRACTION

- We include the following **uncertainties** in the radius extraction:
 - variations in the 2π -continuum (F_{π}^{V} and f_{+}^{1})
 - variations of the isoscalar $(\pi
 ho, ar K K)$ continua
 - different #s of effective iso-scalar/vector poles
 - variations of the fit range (Q_{\max}^2)
 - inclusion of superconvergence relations
 - inclusion of data from polarization measurements
 - different available approximations for the radiative corrections

 \Rightarrow values for the extracted proton radii:

$$r_E^p = 0.84^{+0.01}_{-0.01}~{
m fm}~,~~r_M^p = 0.86^{+0.02}_{-0.03}~{
m fm}$$

 \rightarrow slide/spares

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PARAMETERS of the NEW DISPERSIVE FITS

• Vector meson parameters (5 IS, 5 IV needed)

$V_{\rm IS}$	m_V	a_1^V	a_2^V	V _{IV}	m_V	a_1^V	a_2^V
ω	0.783	0.500	-0.190	v_1	2.330	-1.911	0.314
ϕ	1.019	0.375	-0.861	v_2	2.192	0.644	2.265
s_1	3.052	-0.446	0.512	v_3	4.272	0.173	-0.322
s_2	1.571	0.095	-2.388	v_4	2.454	0.158	0.064
s_3	2.580	0.760	-0.538	v_5	2.492	0.142	-0.372

• Normalization parameters

n1	0.9982	n5	1.0059	n9	1.0056	n13	1.0052	n17	1.0008
n2	0.9928	n6	1.0017	n10	1.0025	n14	1.0044	n18	1.0076
n3	1.0051	n7	1.0003	n11	1.0000	n15	1.0023	n19	1.0055
n4	1.0078	n8	0.9975	n12	1.0031	n16	1.0006	n20	1.0035
n21	0.9995	n22	0.9975	n23	0.9996	n24	0.9984	n25	1.0056
n26	1.0080	n27	1.0004	n28	1.0011	n29	1.0078	n30	0.9985
n31	1.0060								

FURTHER PREDICTIONS for $par{p} ightarrow e^+e^-$

• Analyzing power at Q = 45 MeV • Spin correlation parameters at Q = 45 MeV



<u>FURTHER PREDICTIONS for $\Lambda \overline{\Lambda} \rightarrow e^+ e^-$ </u>

• Diff. XS & polarization [Q = 90 MeV] • Spin correlation parameters [Q = 90 MeV]



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