Baryon electromagnetic transition form factors in the Covariant Spectator Theory

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Kandisky "Circles in a circle" (1923)



Baryon electromagnetic transition form factors in the Covariant Spectator Theory

Exciting near-future prospects of high-quality data. Expand our knowledge of the spectrum and structure properties of baryons.

Missing resonances? Diquark clusters?



Crossing the boundaries to explore baryon resonances



Crossing the boundaries to explore baryon resonances



CLAS/JLab electron scattering data constrain interpretation of HADES dilepton production data. Results have to match at the photon point.

Transition form factors



Baryon resonances transition form factors

CLAS: Aznauryan et al., Phys. Rev. C 80 (2009)

MAID: Drechsel, Kamalov, Tiator, EPJ A 34 (2009)

Spacelike form factors:

- Structure information: shape, qqq excitation vs. hybrid, ...
- Evolution of guark-photon coupling • with momentum transfer

Timelike form factors:

5

 $S_{1/2}$

3

 $Q^2 \, [\text{GeV}^2]$

2

4

- Particle production channels: vector mesons at small q²
- Test of vector meson dominance
- In-medium dilepton production

This talk:

Connect Timelike and SpacelikeTransition Form Factors (TFF) Baryon-photon coupling evolution with momentum transfer

Theoretical toolkits

Timelike baryon transition form factors not yet within reach in lattice QCD: explore alternative methods, estimate theory uncertainty!

Analyticity



 \rightarrow Dispersion theory

Dynamics

Quark-photon coupling dynamically generates VM poles!



- \rightarrow Dyson-Schwinger eqs.
- → Effective Lagrangian models
- \rightarrow Quark models
- \rightarrow Vector-meson dominance

Medium effects



→ In-medium description of resonances!





- Formulation in Minkowski space.
- Two-body CST equation effectively sums ladder and crossed-ladder exchange diagrams, due to cancelations.



- Provides wave functions from covariant vertex with simple transformation properties under Lorentz boosts, appropriate angular momentum structures and smooth non-relativistic limit.
- Manifestly covariant, but only three-dimensional loop integrations.

$$\int_{k} = \int \frac{d^3 \mathbf{k}}{2E_D (2\pi)^3}$$

• Allows to implement confinement and dynamical chiral symmetry breaking.

1 Evidence of separation of partonic and hadronic (pion cloud) effects?

2 Space-like e.m. transition FFs & extension to Timelike e.m. transition FFs Δ (1232) and N*(1520) cases.

3 Predictions for dilepton mass spectrum and decay widths.

4 Preliminary results for Timelike e.m. FFs of the baryon octet.

This talk: CST phenomenological ansatz for baryon wave functions.

Very recent: Significant progress in

the description of dynamical quark mass generation.

Recent: Good and economical description of

the masses of heavy and heavy-light mesons, including highly excited states.

Bare quark and pion cloud components



Model independent feature

$$\gamma N \rightarrow \Delta \qquad \qquad G_M^* = G_M^B + G_M^{\pi}$$

Separation seems to be supported by experiment. Missing strength of G_M at the origin is an universal feature, even in dynamical quark calculations.



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GR and MT Peña PRD 80, 013008 (2009)

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Bare quark core:

- dominates large
- Q^2 region.
- agrees with

EBAC analysis.



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E.M. matrix element



•Baryon wavefunction reduced to an effective quark-diquark structure due to the s integration.

•E.M. matrix element can be written in terms of an effective baryon composed by an off-mass-shell quark and an on-mass-shell quark pair (diquark) with an average mass.

Wave functions



Delta wave function

•A quark+ only axial vector-diquark term contributes

 $\Psi^{S}_{\Delta}(P,k) = -\psi^{S}_{\Delta}(P,k) \tilde{\phi}^{1}_{I} \varepsilon^{\beta*}_{\lambda P} w_{\beta}(P,\lambda_{\Delta})$

E.M. Current



quark-antiquark ⊕ gluon dressing Quark form factors f adjusted to quark charges and anomalous magnetic moments, such that experimental magnetic moments of the nucleons are reproduced.

Constituent quarks (quark form factors)

$$j_{I}^{\mu} = \left[\frac{1}{6}f_{1+} + \frac{1}{2}f_{1-}\tau_{3}\right]\gamma^{\mu} + \left[\frac{1}{6}f_{2+} + \frac{1}{2}f_{2-}\tau_{3}\right]\frac{i\sigma^{\mu\nu}q_{\nu}}{2M_{N}}$$

E.M. Current



quark-antiquark ⊕ gluon dressing Processes where pions are created and absorbed by the same quark are included in the constituent quark internal structure, and thus included in the quark current.

Constituent quarks (quark form factors)

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E.M. Current



Vector meson dominance 2 poles

$$f(Q^{2}) = e + gB(Q^{2})e + gB(Q^{2})gB(Q^{2})e + \dots = e + \frac{gB(Q^{2})e}{1 - gB(Q^{2})}$$

$$\int \frac{d^4q}{\left(2\pi\right)^4} K(p,q,Q) S(q+\eta Q) \Gamma_{\mu}(q,Q) S(q-\eta Q)$$

n-energy sector could be a sector of the sector λ



• VMD enables link to LQCD:

in the current the vector meson mass is taken as a function of the running pion mass.

 Pion cloud contribution negligible for large pion masses, and bare quark model could be calibrated to the lattice data.

After that, in the limit of the physical pion mass value,

the experimental data is well described in the large Q² region.

Connection to Lattice QCD

To control model dependence: CST model and LQCD data are made **compatible.**



Model (no pion cloud) valid for lattice pion mass regime.

No refit of wave function scale parameters for the physical pion mass limit.

E.M. Current and TFF at the photon point

$$\gamma N \longrightarrow \Delta$$

$$\Gamma^{\beta\mu}(P,q) = \left[G_1 q^{\beta} \gamma^{\mu} + G_2 q^{\beta} P^{\mu} + G_3 q^{\beta} q^{\mu} - G_4 g^{\beta\mu}\right] \gamma_5$$

- Only 3 G_i are independent: $q^{\mu}\Gamma_{\beta\mu}=0$ E.M. Current has to be conserved

 G_M , G_E , G_C Scadron Jones popular choice.

• Only finite G_i are physically acceptable.

Orthogonality between initial and final states necessarily follows from both requirements, giving an important constraint to G_c at $Q^2=0$.

E.M. Current and TFF near the photon point

Pseudo Threshold PT
$$Q_0^2 = -(M_R - M_N)^2$$
; $|\vec{Q}| = 0$

An accident of the definition of the Jones and Scadron form factors:

$$G_E(PT) = \frac{M_R - M}{2M_R} G_C(PT)$$

A form of the "Siegert condition"! This is implied by orthogonality of states. If data analysis proceed through helicity Amplitudes this behavior may be missed.



 e^{-}

q

G.Ramalho Phys. Lett. B 759 (2016) 126

$\mathbf{G}_{\mathbf{E}}$ and $\mathbf{G}_{\mathbf{C}}$

$$\gamma N \rightarrow \Delta$$

Large N_C limit and SU(6) quark models:

- Suggest that pion cloud effects for $\rm G_E$ and $\rm G_C$ generate deviations from the Siegert condition of the order $~{\cal O}(1/N_c^2)$ and do not agree to data at low $\rm Q^2$



$\mathbf{G}_{\mathbf{E}}$ and $\mathbf{G}_{\mathbf{C}}$

$$\gamma N \rightarrow \Delta$$

Large N_C limit and SU(6) quark models:

- Suggest that pion cloud effects for $\rm G_E$ and $\rm G_C$ generate deviations from the Siegert condition of the order $\mathcal{O}(1/N_c^2)$ and do not agree to data at low Q².

Corrected parametrization with deviations $\mathcal{O}(1/N_c^4)$ generated agreement with 2017 JLAB data









Dominance of iso-vector channel concurs to our model of the meson cloud: pion only

PDG data at the photon point:





The residue of the pion from factor ${\rm F}_{\rm \pi}({\rm q}^2)$ at the timelike ρ pole is proportional to the $\,\rho\to\pi\pi\,$ decay

(a) related with pion electromagnetic form factor $F_{\pi}(q^2)$



The residue of the pion from factor $F_{\pi}(q^2)$ at the timelike ρ pole is proportional to the $\rho \to \pi \pi$ decay

(a) related with pion electromagnetic form factor $F_{\pi}(q^2)$

Parametrization of pion Form Factor





Transition form factors in the timelike region are restricted to a given kinematic region that depends on the varying resonance mass W.





• Good description of the magnetic dipole physical data $(W = M_{\Delta})$

$$\begin{split} \Gamma_{\gamma^*N}(q;W) &= \frac{\alpha}{16} \frac{(W+M)^2}{M^2 W^3} \sqrt{y_+ y_-} y_- |G_T(q^2,W)|^2 \\ |G_T(q^2;M_\Delta)|^2 &= |G_M^*(q^2;W)|^2 + 3|G_E^*(q^2;W)|^2 + \frac{q^2}{2W^2}|G_C^*(q^2;W)|^2 \\ y_\pm &= (W\pm M)^2 - q^2 \end{split}$$

$$\Gamma_{\gamma N}(W) \equiv \Gamma_{\gamma^* N}(0; W)$$

$$\Gamma_{e^+e^- N}(W) = \frac{2\alpha}{3\pi} \int_{2m_e}^{W-M} \Gamma_{\gamma^* N}(q; W) \frac{dq}{q}$$

Δ (1232) Dalitz decay



Δ (1232) Dalitz decay



Crossing the boundaries N*(1520)

$$\Gamma_{\gamma^*N}(q,W) = \frac{3\alpha}{32} \frac{(W-M)^2}{M^2 W^3} \sqrt{y_+ y_-} y_+ |G_T(q^2,W)|^2$$
$$y_{\pm} = (W \pm M)^2 - q^2$$

$$|G_T(q^2, W)|^2 = 3|G_M(q^2, W)|^2 + |G_E(q^2, W)|^2$$

$$\begin{split} &+ \frac{q^2}{2W^2} |G_C(q^2, W)|^2.\\ &\Gamma_{e^+e^-N}'(q, W) \equiv \frac{d\Gamma}{dq}(q, W)\\ &= \frac{2\alpha}{3\pi q^3} (2\mu^2 + q^2) \sqrt{1 - \frac{4\mu^2}{q^2}} \Gamma_{\gamma^*N}(q, W) \end{split}$$

G. Ramalho, M. T. P., PHYSICAL REVIEW D 95 0104003 (2017)

N*(1520)



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N*(1520)



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N*(1520)







HADES Collaboration





PDG data:

	$ G_T(0, M_R) ^2$		$\Gamma_{\gamma N}$ (MeV)	
		Estimate	PDG limits	Model
p	$0.68 {\pm} 0.05$	$0.43 {\pm} 0.03$	0.31 - 0.62	0.34
n	$0.53 {\pm} 0.04$	$0.34{\pm}0.03$	0.30 - 0.64	0.34

 $G_T^{CST}(0, M_R) = 0.73$ Consistent with PDG value for γ N decay width.

N*(1520)

Update of 2017 results



- Similar Proton and neutron results due to iso-vector dominance of meson cloud.
- At higher energies evolution of $G_T(q^2, W)$ with q^2 becomes important.

Predictive power:



Summary 1

Covariant Spectator quark-diquark model enables description of different resonance states (spin/orbital motion).

Several applications: $\Delta(1232)$, N*(1440), N*(1535), N*(1520),..., dilepton mass spectrum.

Consistent with experimental data at high Q².

Consistent with LQCD in the large pion mass regime informing on "pion cloud" effects.

VMD and "pion cloud" sustained extension to the timelike region of the TFF of the $\Delta(1232)$ and N*(1520).

LQCD simulations below the N* threshold will help too refine interpretation provided by theoretical quark models.

New experimental data at large Q² and even more precise data in all ranges can improve interpretation of empirical results.

Dynamical calculations of diquark vertices within CST to be done, to support quark-diquark picture for baryons, seen within Dyson-Schwinger approach for dynamical quarks.

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Timelike transitions appear as a
unique opportunity to explore hyperon structure.
N. Cabibbo and R. Gatto,
Phys. Rev. Lett. 4, 313 (1960);
Phys. Rev. 124, 1577 (1961).
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They are new windows for the role of diquarks in baryons, deduced from how form factors vary with quark composition. S. Dobbs, A. Tomaradze, T. Xiao, K. K. Seth and G. Bonvicini, Phys. Lett. B 739, 90 (2014)

Extension to strangeness in the Spacelike region with a global fit to lattice data and physical magnetic moments

0.8

Extend the parametrization of the e.m. current to the valence quark d.o.f of the **whole** baryon octet.

$$j_{i} = \frac{1}{6}f_{i+}\lambda_{0} + \frac{1}{2}f_{i-}\lambda_{3} + \frac{1}{6}f_{i0}\lambda_{s}$$
$$\lambda_{0} = \begin{pmatrix} 1 & 0 & 0\\ 0 & 1 & 0\\ 0 & 0 & 0 \end{pmatrix}, \quad \lambda_{3} = \begin{pmatrix} 1 & 0 & 0\\ 0 & -1 & 0\\ 0 & 0 & 0 \end{pmatrix}$$
$$\lambda_{s} = \begin{pmatrix} 0 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & -2 \end{pmatrix}$$

Parameters for valence quark degrees of freedom and the pion cloud dressing determined by a global fit to octet baryon lattice data for the e.m. form factors and physical magnetic moments.

Lattice data: H.W. Lin and K. Orginos, Phys. Rev. D 79, 074507 (2009).



-0.5

Two examples:

G. Ramalho and K.Tsushima, PRD 84, 054014 (2011)

Red line: lattice

Blue line: physical regime

Extension to Strangeness in the timelike region

$$e^+e^- \to \gamma^* \to B\bar{B}$$

$$G(q^{2})|^{2} = \left(1 + \frac{1}{2\tau}\right)^{-1} \left[|G_{M}(q^{2})|^{2} + \frac{1}{2\tau}|G_{E}(q^{2})|^{2} + \frac{1}{2\tau}|G_{E}(q^{2})|^{2}\right]$$
$$= \frac{2\tau |G_{M}(q^{2})|^{2} + |G_{E}(q^{2})|^{2}}{2\tau + 1} \cdot \frac{\tau = \frac{q^{2}}{4M_{B}^{2}}}{\tau = \frac{q^{2}}{4M_{B}^{2}}}$$

Effective Form factor that gives the integrated cross section

Analiticity demands that for $\ q^2
ightarrow \infty$

 $G_M(q^2) \simeq G_M^{\rm SL}(-q^2),$ $G_E(q^2) \simeq G_E^{\rm SL}(-q^2).$



Extension to Strangeness in the timelike region



Extension to Strangeness in the timelike region



• Guide determination of onset of -scaling effects

-perturbative QCD falloffs : $G_M \propto 1/q^4$ and $G_E \propto 1/q^4$.

Summary 2

Covariant Spectator quark-diquark model enables description of different resonance states (spin/orbital motion).

Several applications: $\Delta(1232)$, N*(1440), N*(1535), N*(1520), baryon octet, octet to decuplet transitions, DIS, dilepton mass spectrum.

Consistent with experimental data at high Q².

Consistent with LQCD in the large pion mass regime informing on "pion cloud" effects, and **high q² behavior of time-like hyperon FFs**.

VMD and "pion cloud" sustained extension to the timelike region of the TFF of the $\Delta(1232)$ and N*(1520).

LQCD simulations below the N* threshold will help too refine interpretation provided by theoretical quark models.

LQCD data on the baryon octet e.m. FF's precious source of information, due to scarcity of experimental information.

New experimental data at large Q² and even more precise data in all ranges can improve interpretation of empirical results.

Dynamical calculations of diquark vertices within CST to be done, to support quark-diquark picture for baryons, seen within Dyson-Schwinger approach for dynamical quarks.

Thank you!

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Crossing the boundaries to explore baryon resonances