



Non-equilibrium photons from thermalizing matter

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- 1 Motivation
- 2 *Bottom-up* thermalization
- 3 Turbulent thermalization
(and all that Jazz)
- 4 Photons from thermalizing matter
- 5 Summary and Outlook

Global Goal

Understand (nuclear) matter under extreme conditions



Local Goal

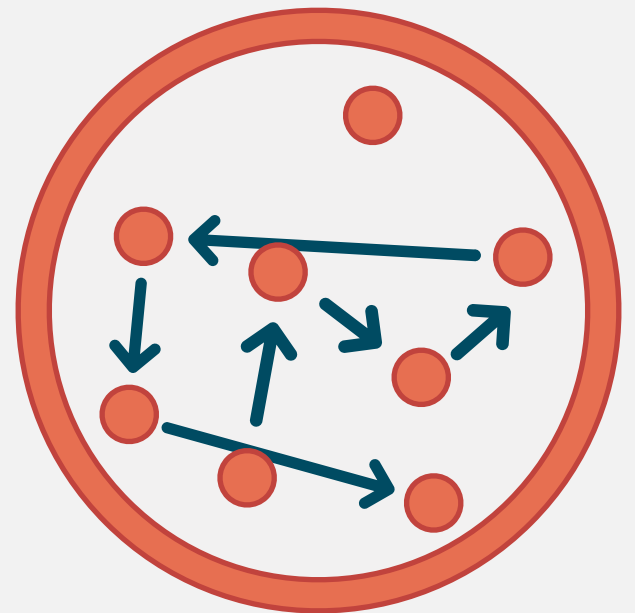
Use photons as probes of
thermalizing nuclear matter

Local Goal

Use photons as probes of
thermalizing nuclear matter

Why photons?

No strong interactions



Local Goal

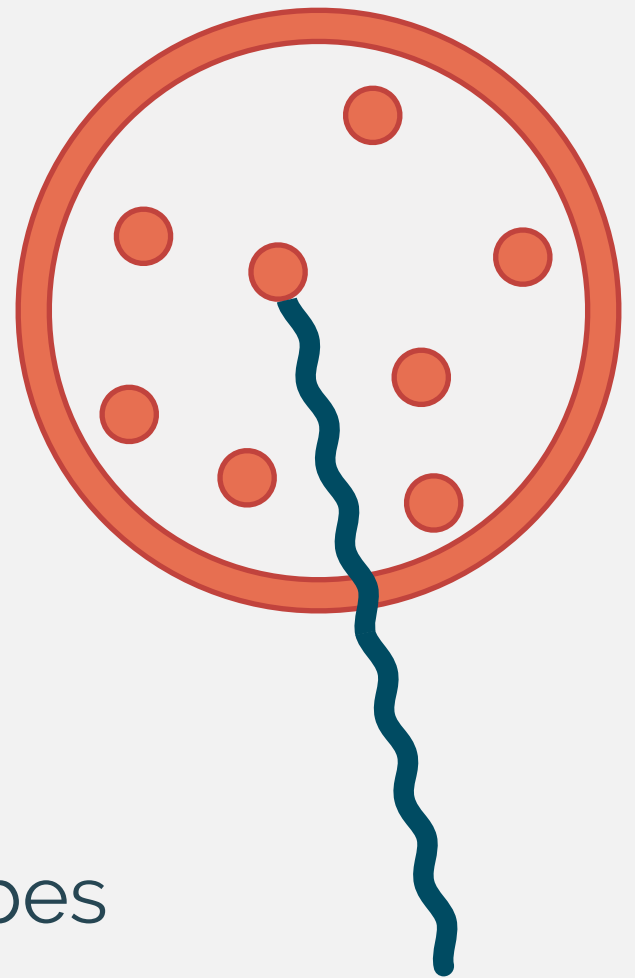
Use photons as probes of
thermalizing nuclear matter

Why photons?

No strong interactions



Clean probes



Local Goal

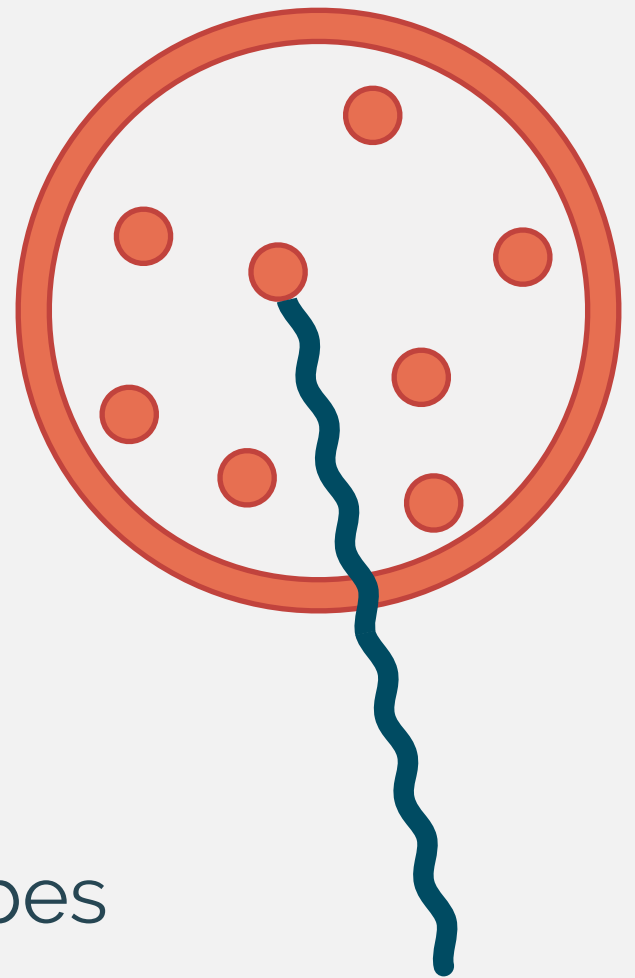
Use photons as probes of
thermalizing nuclear matter

Why photons?

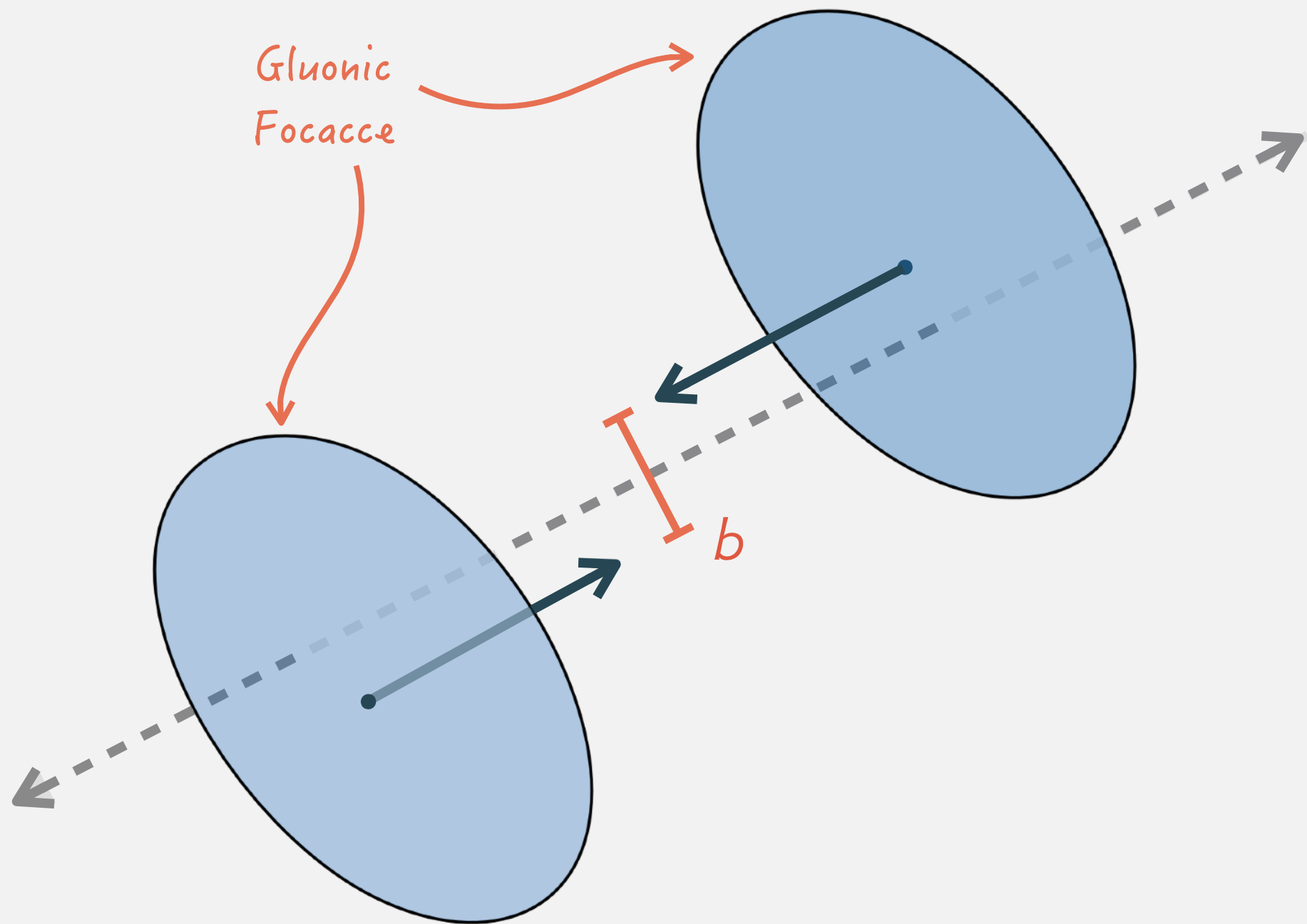
No strong interactions → Clean probes

Which system?

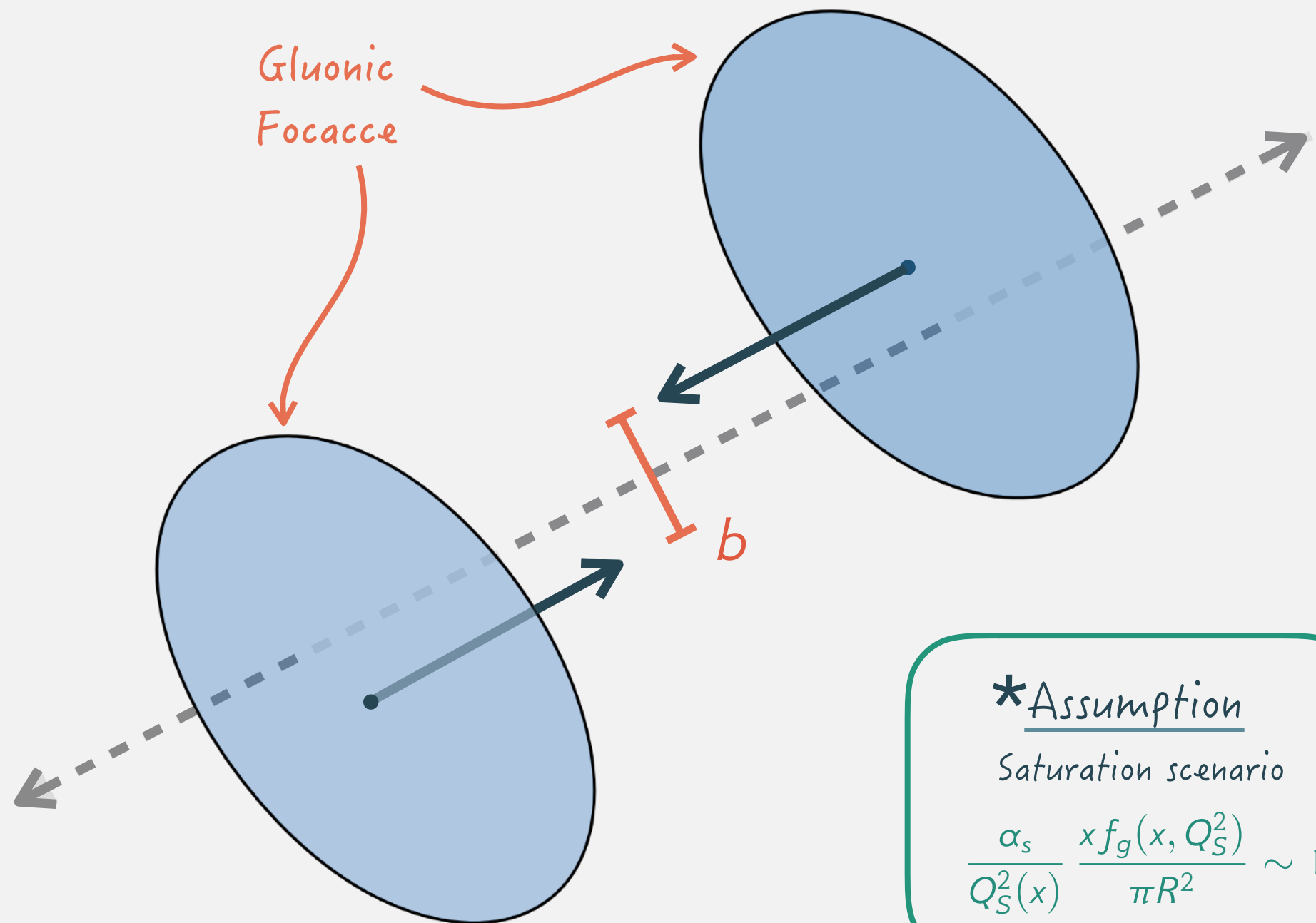
Ultrarelativistic Nucleus-Nucleus (A+A) Collisions



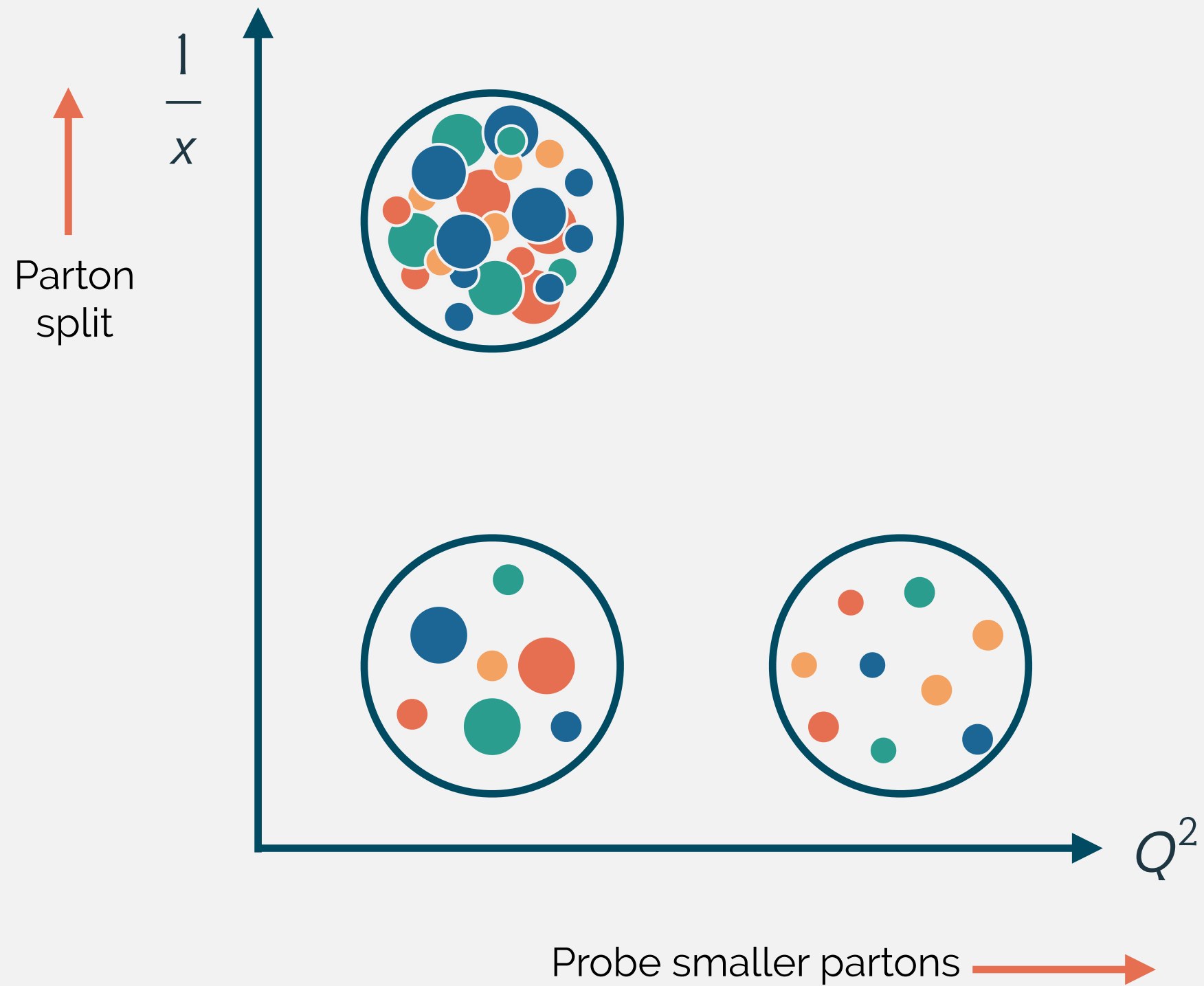
Ultrarelativistic Nucleus-Nucleus ($A+A$) Collisions



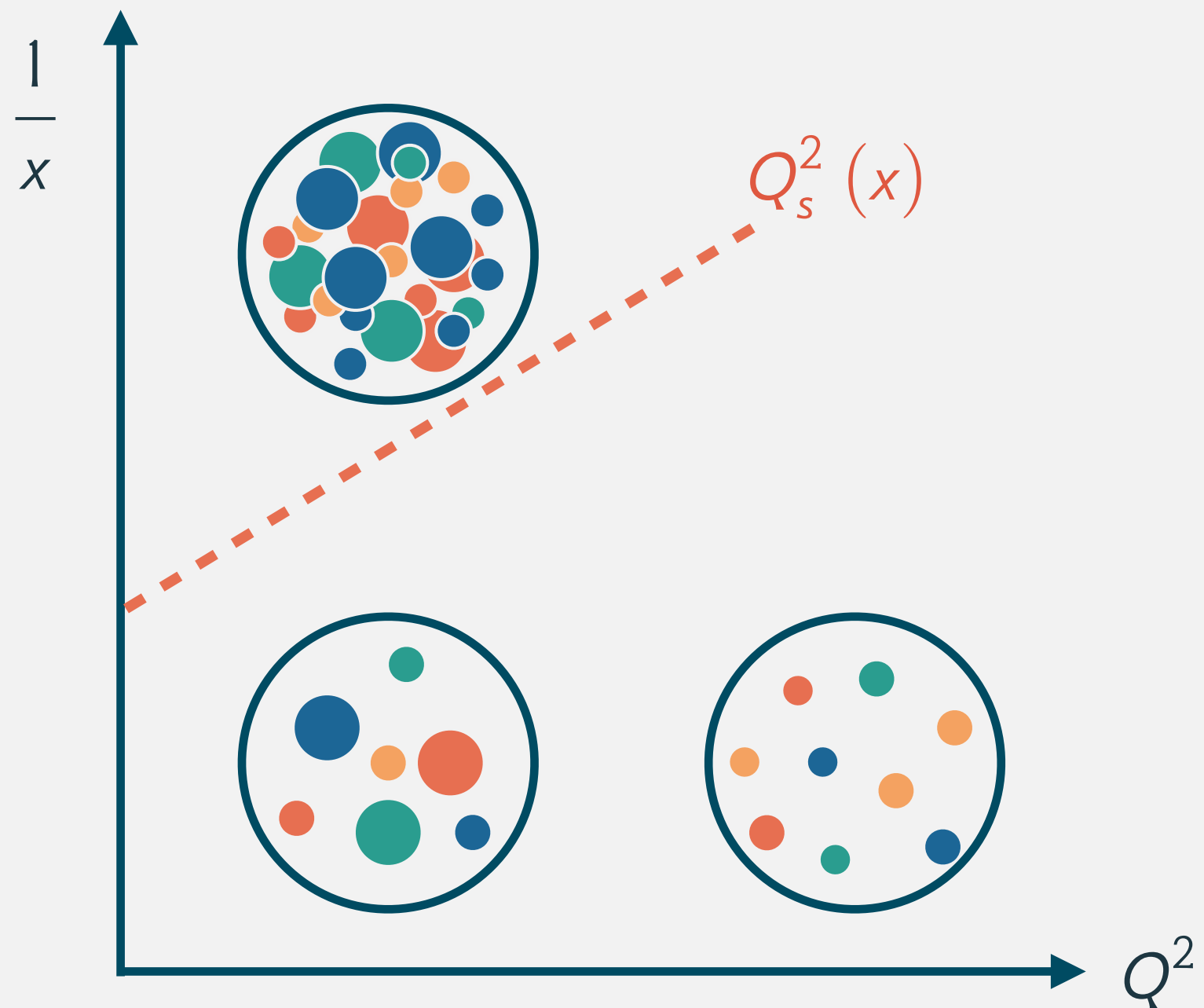
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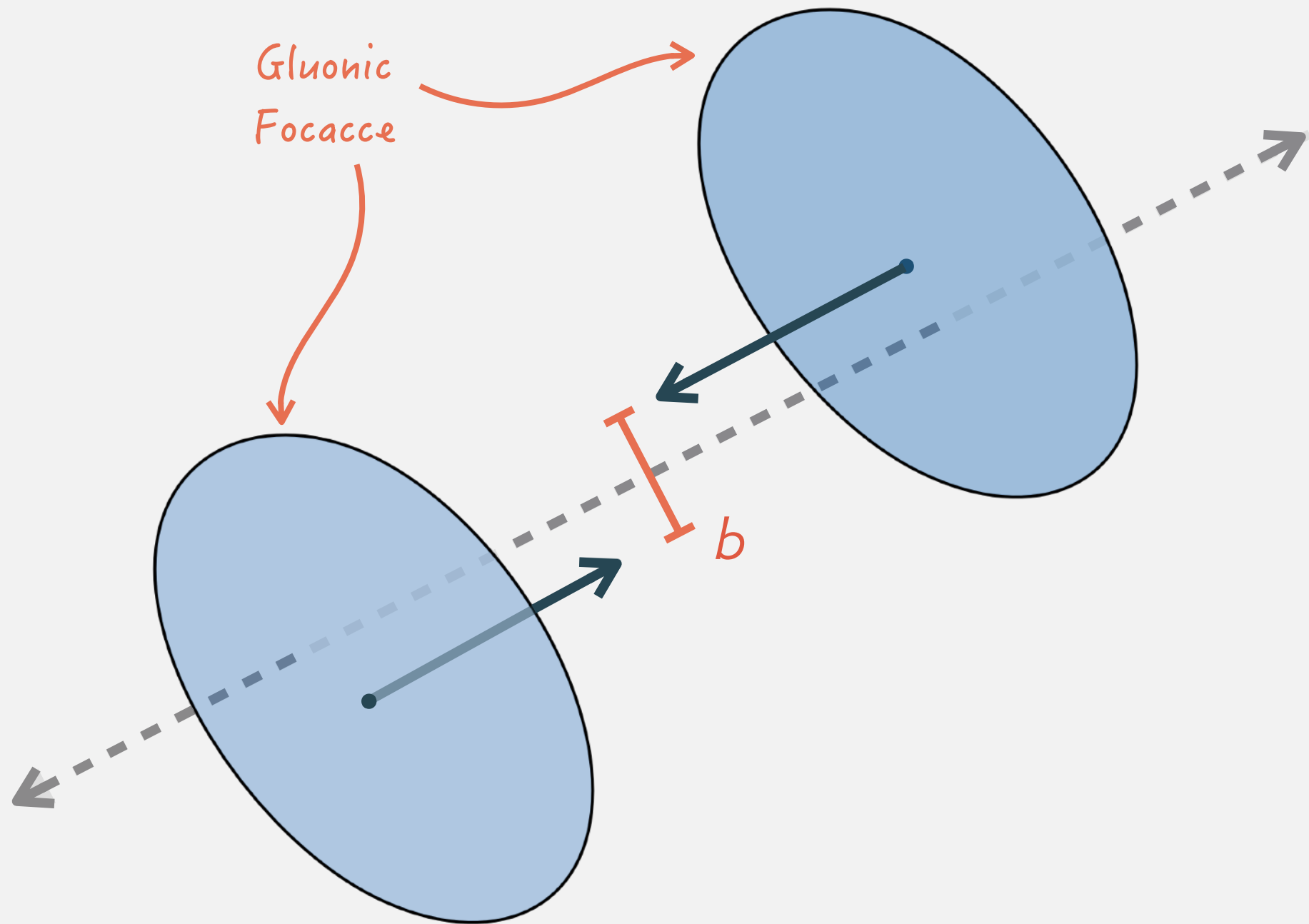
Saturation



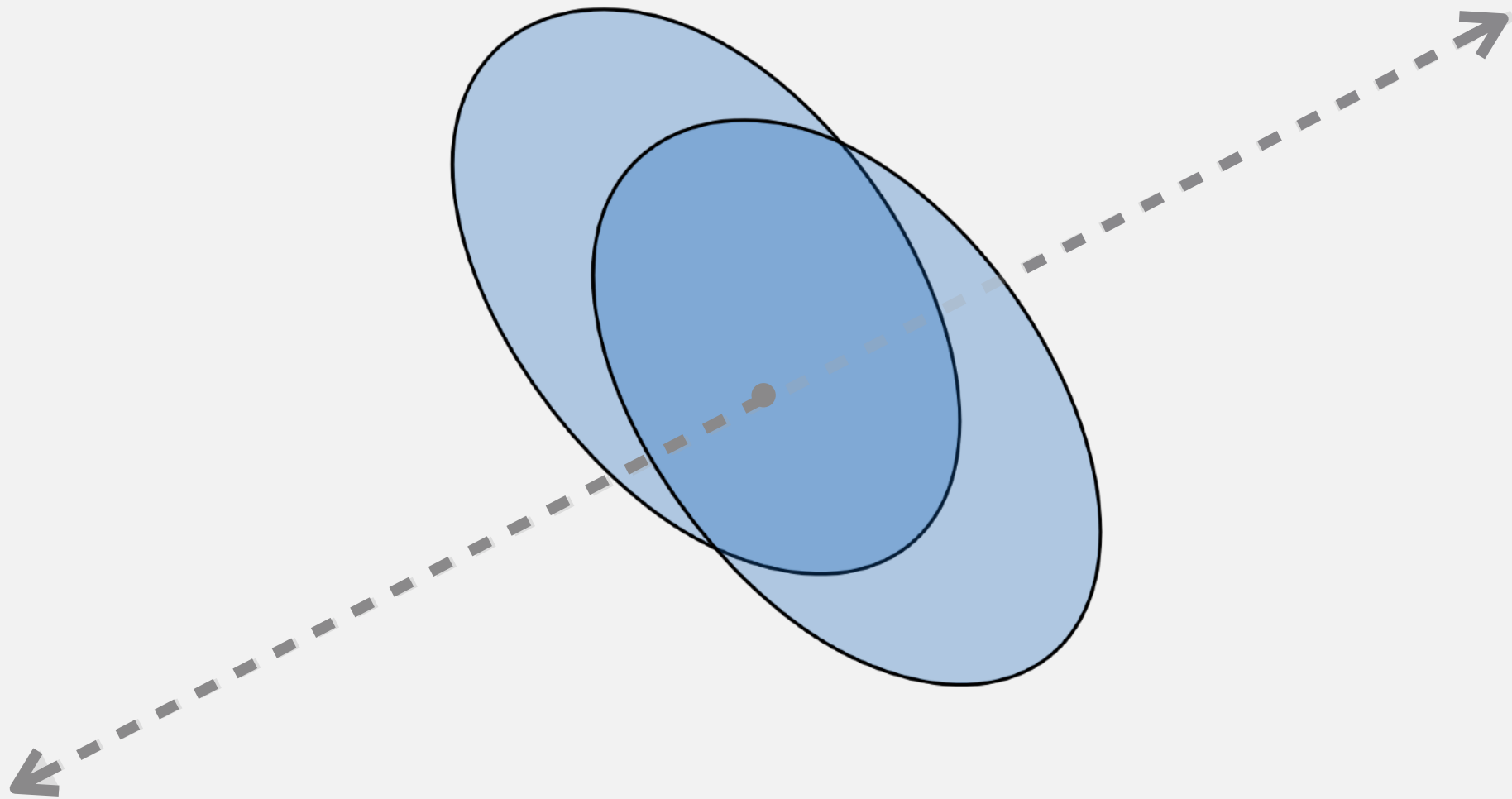
Saturation



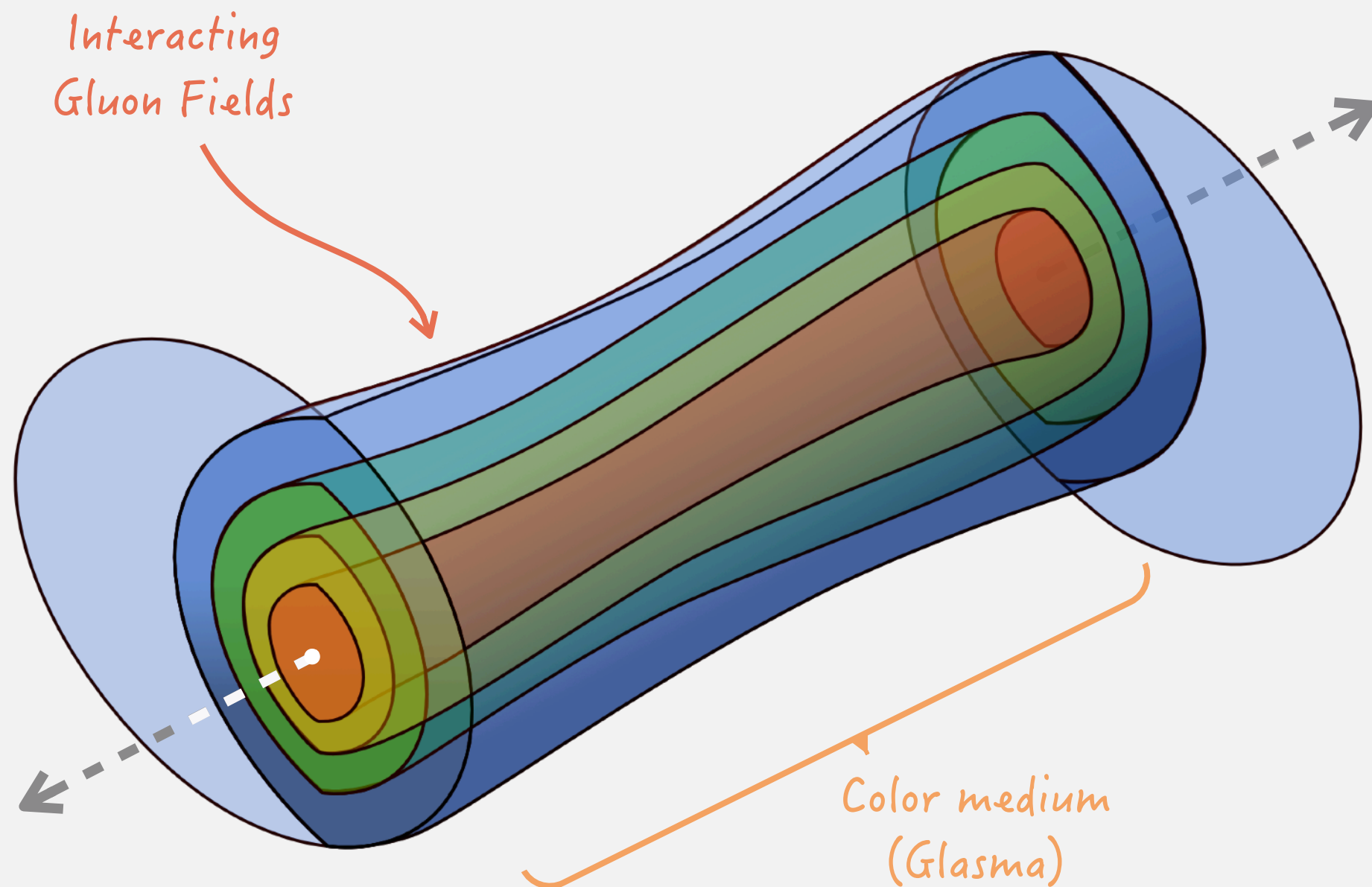
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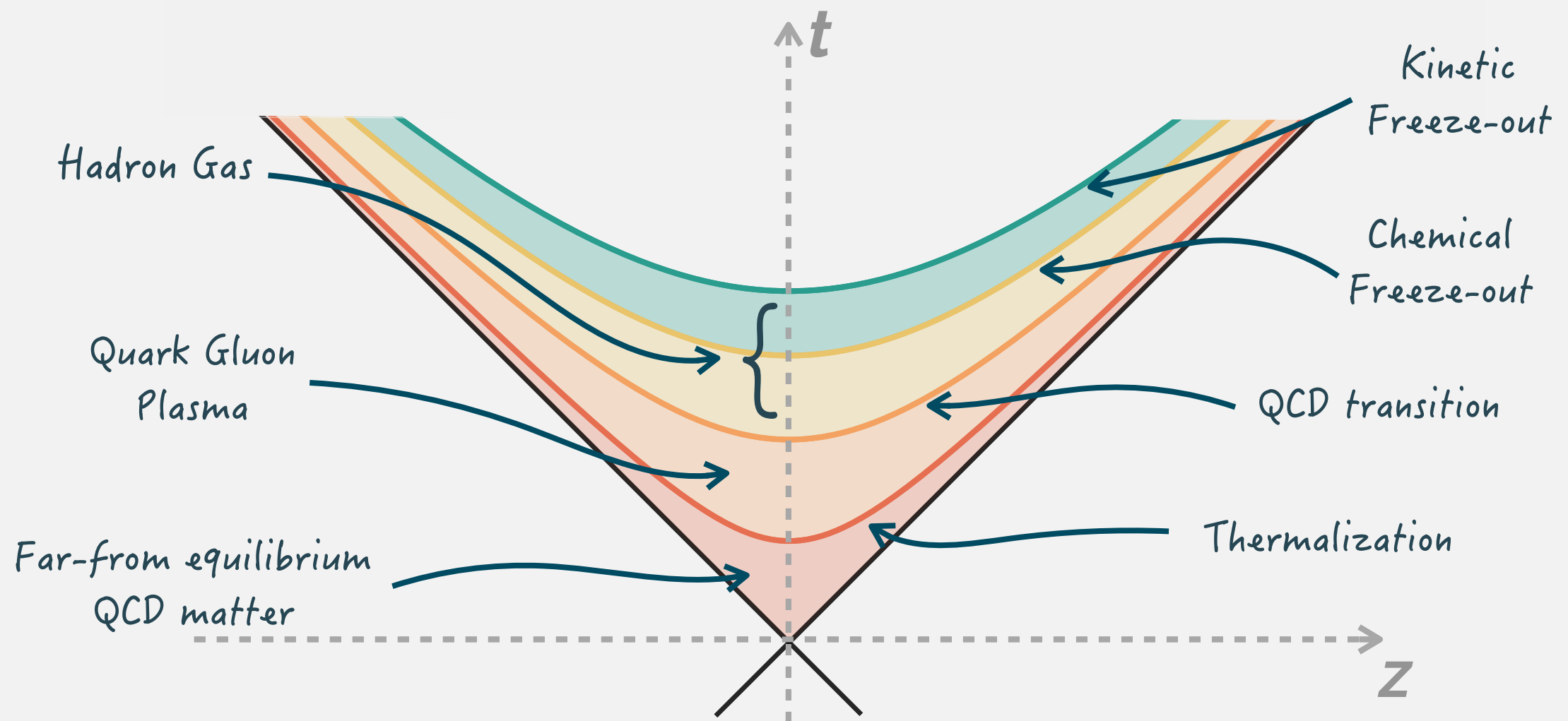
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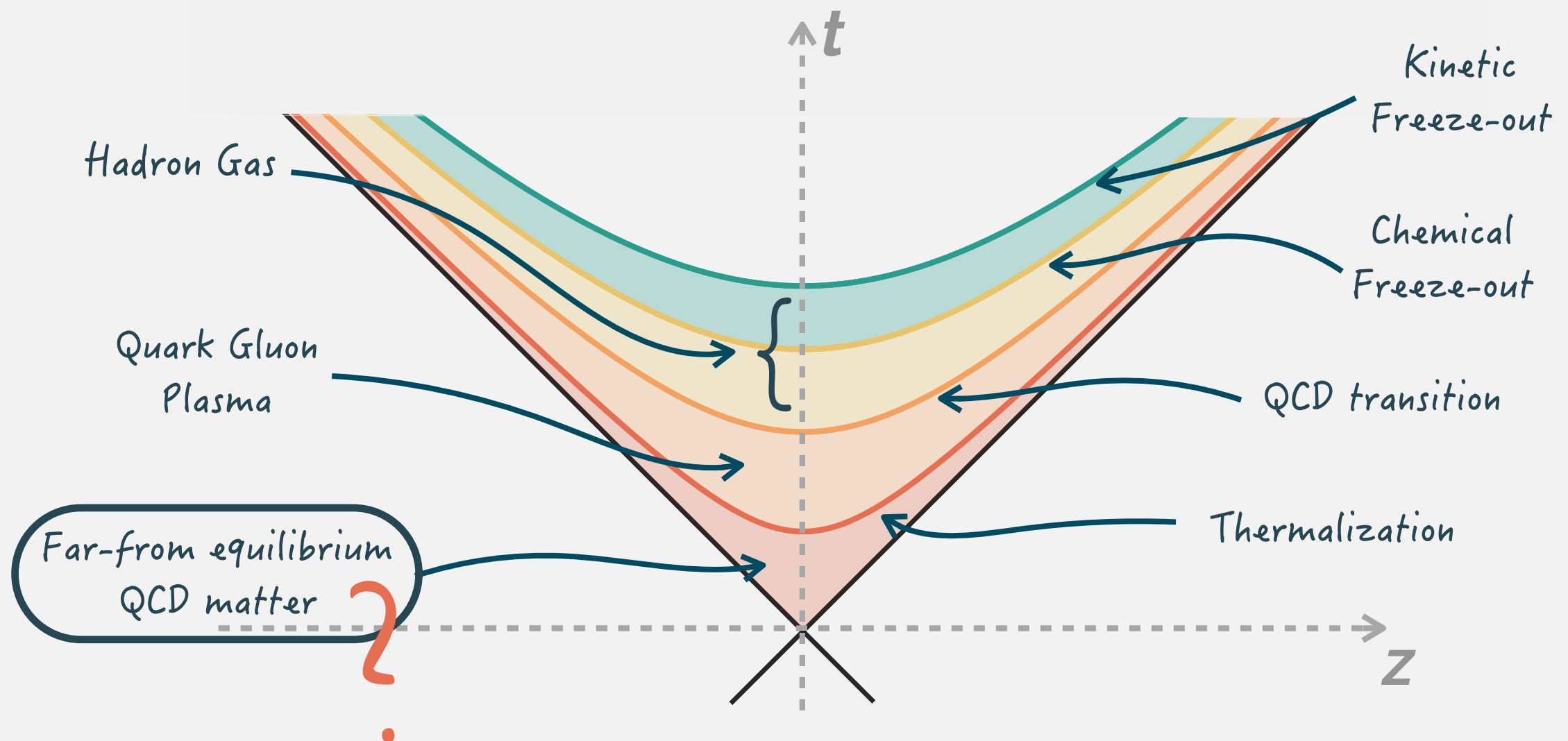
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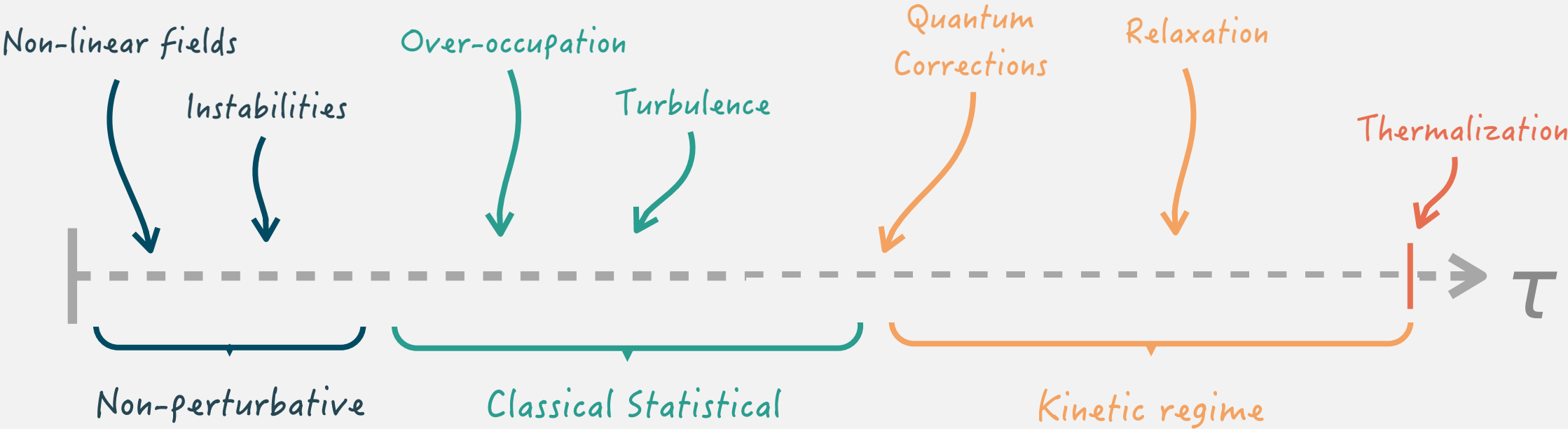
The Standard model of Heavy Ion Collisions

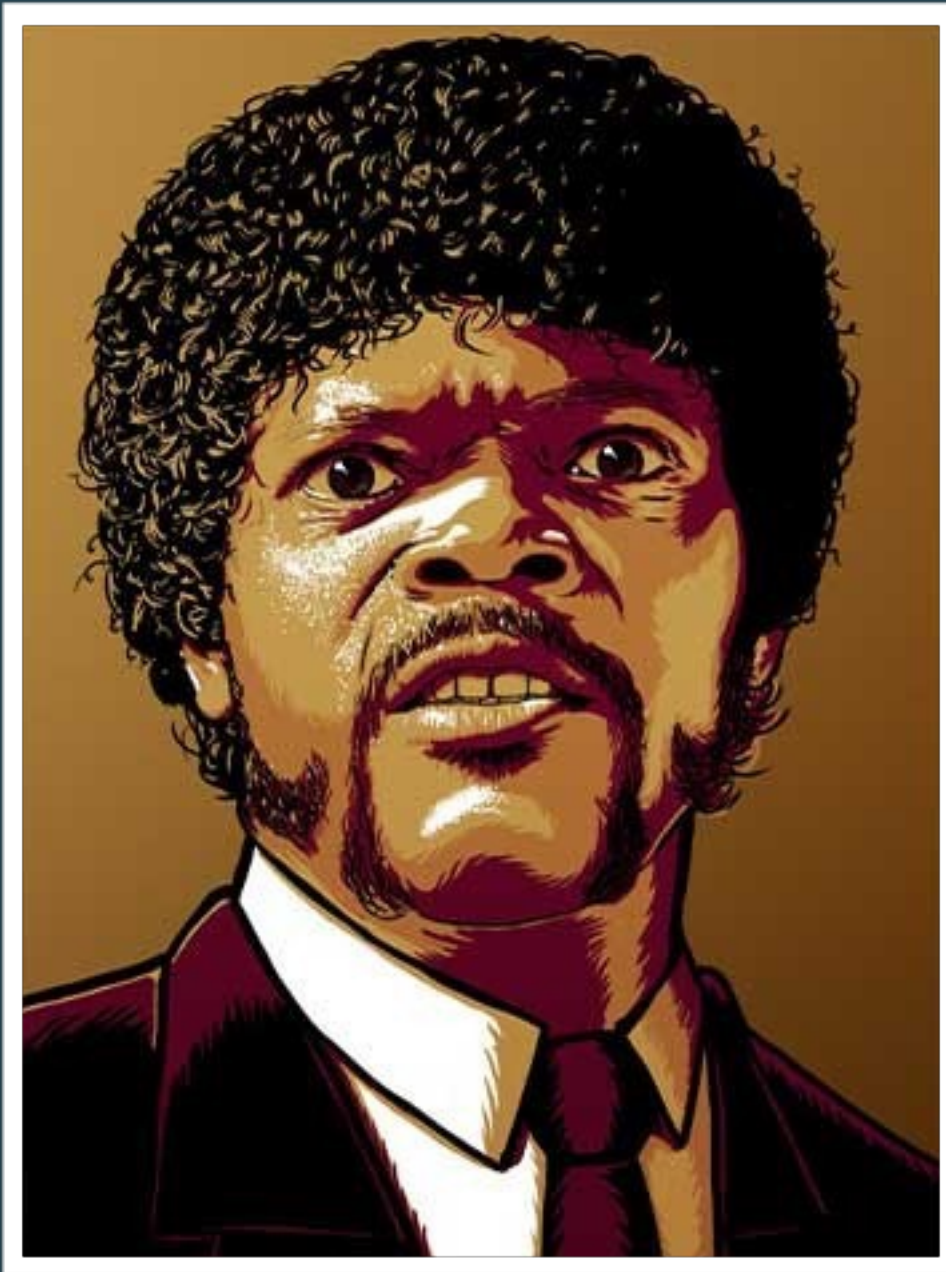


The Standard model of Heavy Ion Collisions



Pre-equilibrium stages





**DATA,
DO YOU
SPEAK IT?**

The Observables

$$\frac{dN}{d^2p_{\perp} dy}$$

The Observables

$$\frac{dN}{d^2p_{\perp}dy}$$

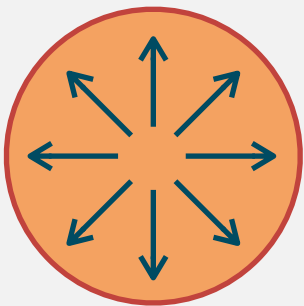
Invariant
Yield



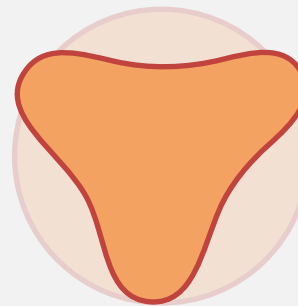
The Observables

$$\frac{dN}{d^2p_{\perp} dy} = \frac{1}{2\pi p_{\perp}} \frac{dN^{iso}}{dp_{\perp} dy} \left(1 + \sum_{n=1}^{\infty} v_n \cos(n\phi) \right)$$

v_2



v_3



v_4

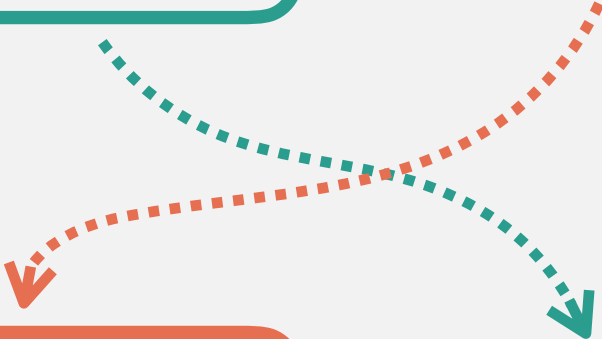


The Observables

$$\frac{dN}{d^2p_{\perp} dy} = \frac{1}{2\pi p_{\perp}} \frac{dN^{iso}}{dp_{\perp} dy} \left(1 + \sum_{n=1}^{\infty} v_n \cos(n\varphi) \right)$$

The Observables

$$\frac{dN}{d^2p_{\perp}dy} = \boxed{\frac{1}{2\pi p_{\perp}} \frac{dN^{iso}}{dp_{\perp}dy}} \left(1 + \sum_{n=1}^{\infty} \boxed{v_n} \cos(n\varphi) \right)$$



The diagram illustrates the interchange of the prefactor and the Fourier coefficient v_n between the two equations. A green dashed arrow points from the prefactor in the top equation to the prefactor in the bottom equation. A red dashed arrow points from the v_n term in the top equation to the v_n term in the bottom equation.

$$\frac{dN}{d^2p_{\perp}dy} = \boxed{\frac{1}{2\pi p_{\perp}} \frac{dN^{iso}}{dp_{\perp}dy}} \left(1 + \sum_{n=1}^{\infty} \boxed{v_n} \cos(n\varphi) \right)$$

The “Photon Puzzle”

$$\frac{dN}{d^2p_{\perp} dy} = \frac{1}{2\pi p_{\perp}} \frac{dN^{iso}}{dp_{\perp} dy} \left(1 + \sum_{n=1}^{\infty} v_n \cos(n\varphi) \right)$$

The inability to calculate both the direct photon's yield,
and its anisotropy coefficients with current models



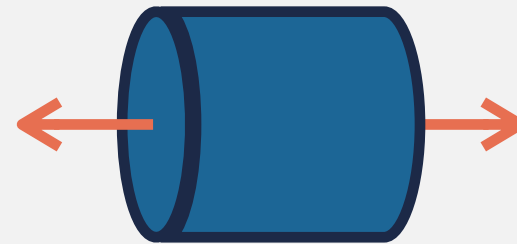
DISCLAIMER



DISCLAIMER

ASSUMPTIONS

Bjorken Expansion



$$u = (\cosh \eta, u_x, u_y, \sinh \eta)$$

Transverse Translation
Invariance

$$u = (\cosh \eta, 0, 0, \sinh \eta)$$



DISCLAIMER

OBJECTIVE

Solve the “Photon
Puzzle”?

NO



So?



Show that NEQ
photons are relevant



Change the
perspective



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Bottom-up thermalization

Three
Stages

I. Early Times

$$1 \ll Q\tau \ll \alpha_s^{-3/2}$$

II. Onset of thermalization

$$\alpha_s^{-3/2} \ll Q\tau \ll \alpha_s^{-5/2}$$

III. Thermalization of the soft sector

$$\alpha_s^{-5/2} \ll Q\tau \ll \alpha_s^{-13/5}$$

I. Early Times $1 \ll Q\tau \ll \alpha_s^{-3/2}$

$$\frac{dN_g}{d^2p_\perp dy} = \frac{1}{\alpha_s} f\left(\frac{p_\perp}{Q_s}\right)$$

Dominated by
hard gluons

$$\langle p_\perp \rangle \sim Q_s$$

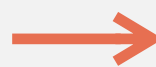
Instabilities freed hard Gluons

$$n_h \sim \frac{1}{\alpha_s} \frac{Q^3}{Q_s \tau}$$

Inelastic processes produce soft glue

$$n_s \sim \frac{1}{\alpha_s} \frac{Q^3}{(Q_s \tau)^{4/3}}$$

Screening mass



$$m_D^2 \sim \alpha_s \int \frac{d^3p}{p} f_g \sim \frac{Q_s^2}{Q_s \tau}$$

I. Early Times

$$\frac{dN_g}{d^2p_\perp dy} = \frac{1}{\alpha_s} f\left(\frac{p_\perp}{Q_s}\right)$$

Dominated by
hard gluons

$$\langle p_\perp \rangle \sim Q_s$$

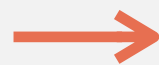
Instabilities freed hard Gluons

$$n_h \sim \frac{1}{\alpha_s} \frac{Q^3}{Q_s \tau}$$

Inelastic processes produce soft glue

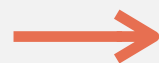
$$n_s \sim \frac{1}{\alpha_s} \frac{Q^3}{(Q_s \tau)^{4/3}}$$

Free streaming



$$\langle p_z \rangle \sim Q_s (Q_s \tau)^{-1}$$

Interactions



$$\langle p_z \rangle^3 \sim \alpha_s n_h$$

$$\langle p_z \rangle \sim Q_s (Q_s \tau)^{-1/3}$$

II. Onset of thermalization

$$\alpha_s^{-3/2} \ll Q\tau \ll \alpha_s^{-5/2}$$

Occupation of Hard Gluon
drops below unity

$$n_h \sim \frac{1}{\alpha_s} \frac{Q^3}{Q_s \tau}$$

**Dominated by
hard gluons**

$$\langle p_\perp \rangle \sim Q_s$$

Soft gluons dominate the
screening mass

$$n_s \sim \frac{\alpha_s^{1/4} Q_s^3}{(Q_s \tau)^{1/2}}$$

Soft avg. mom. $p_s^2 \sim \alpha_s Q_s^2$

Screening mass is dominated
by soft sector

$$m_D^2 \sim \frac{\alpha_s N_s}{p_s} \sim \frac{\alpha_s^{3/4} Q_s}{(Q_s \tau)^{1/2}}$$

III. Thermalization of the soft sector

$$\alpha_s^{-5/2} \ll Q\tau \ll \alpha_s^{-13/5}$$

Soft sector thermalizes



Acts like a bath

Hard sector loses energy to soft bath



Temperature rises as $T = c_T \alpha_s^3 Q_s (Q_s \tau)$

Dominated by
soft gluons

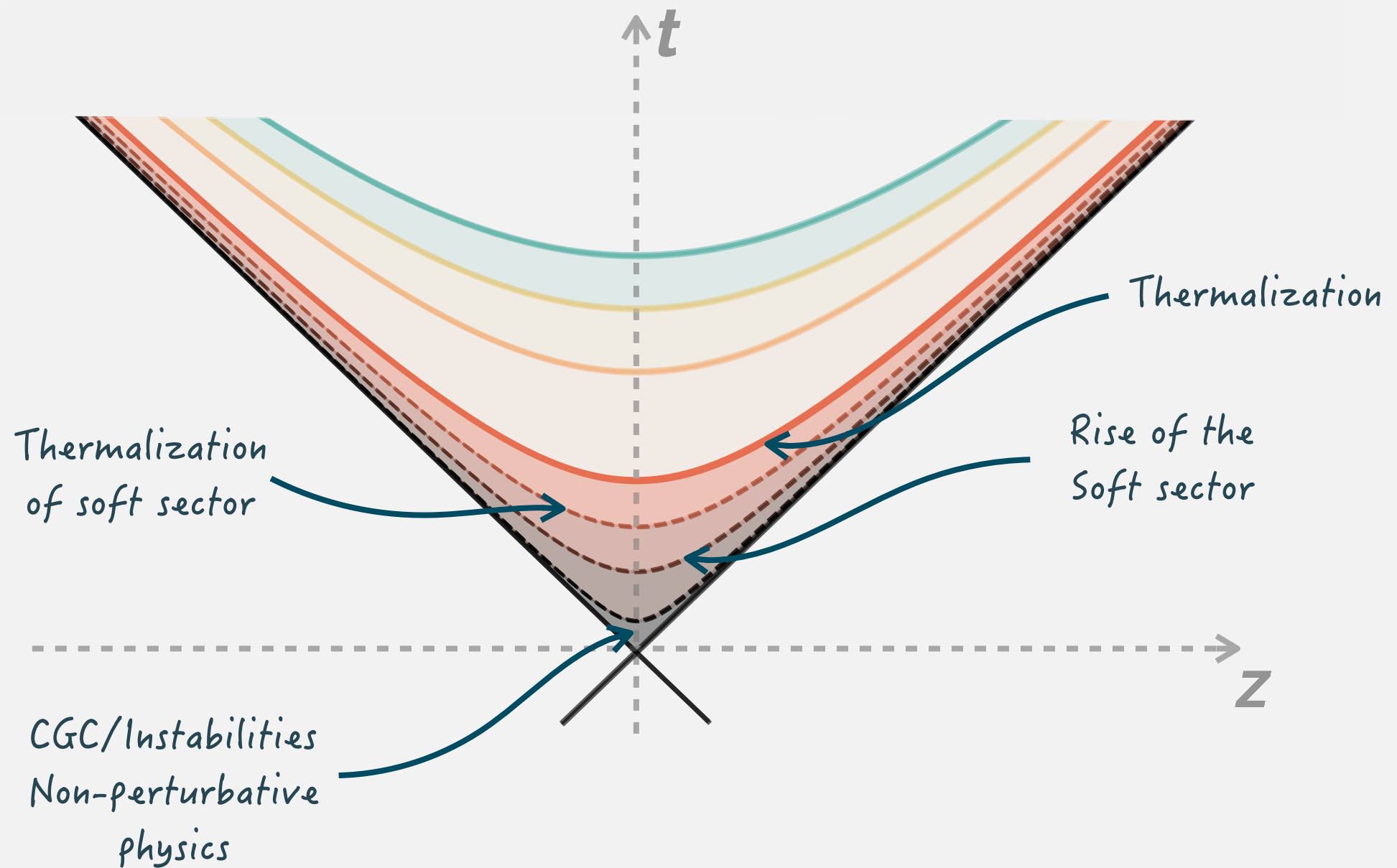
$$\langle p_\perp \rangle \sim m_D$$

$$\tau_{th} \sim c_{eq} \alpha^{-13/5} Q_s^{-1}$$

$$T_{th} \sim c_T c_{eq} \alpha^{2/5} Q_s$$

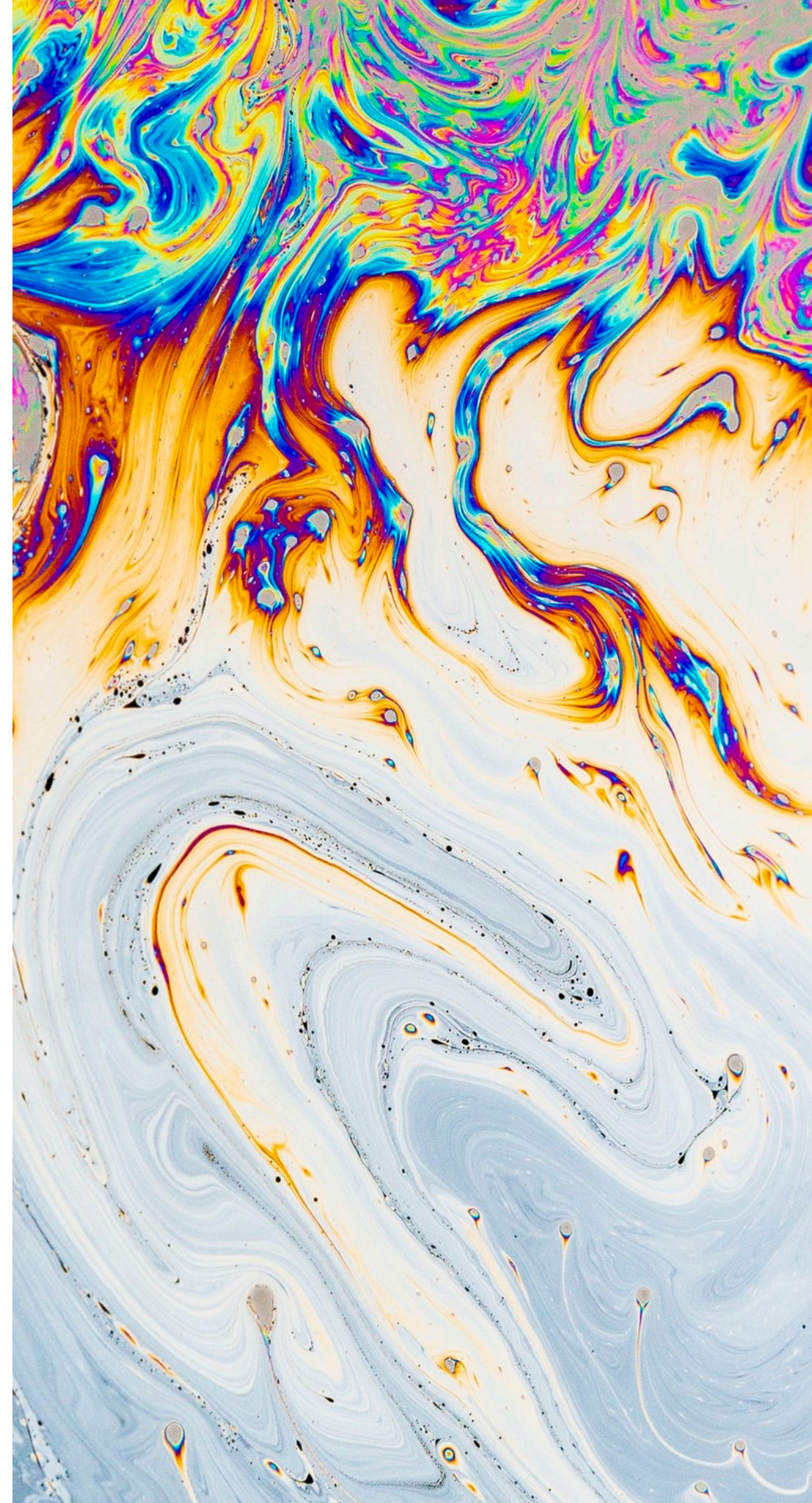
The Song of Heavy Ion Collisions

(revisited)



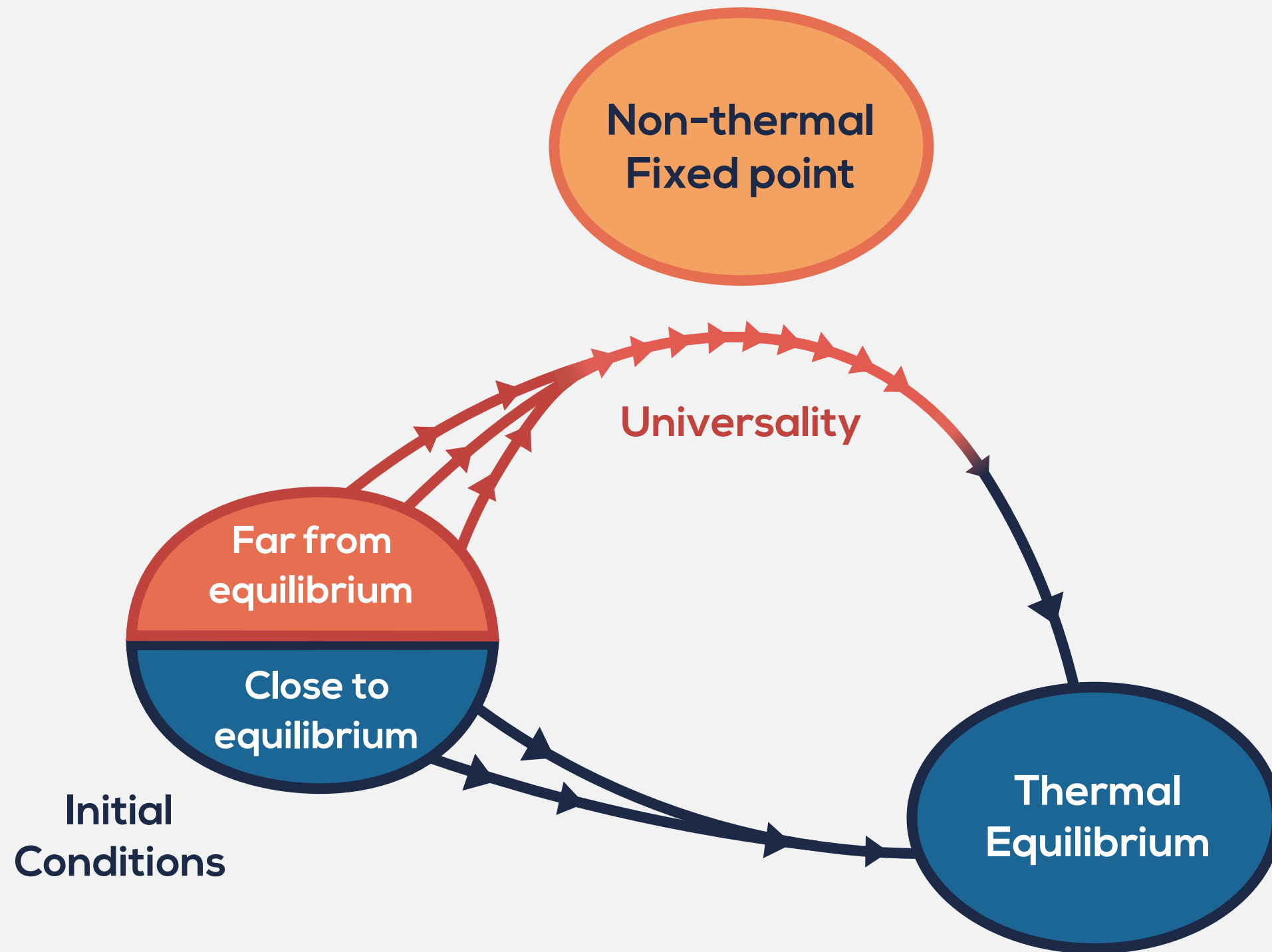
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Turbulent thermalization

Of **highly occupied**
non-abelian plasmas
very far from equilibrium



Non-thermal fixed point

def. Parametrically long self-similar regime quantum fields under go in their way to Thermal Equilibrium

Self - Similarity

def. distribution function depends on
a Universal, time-independent
function

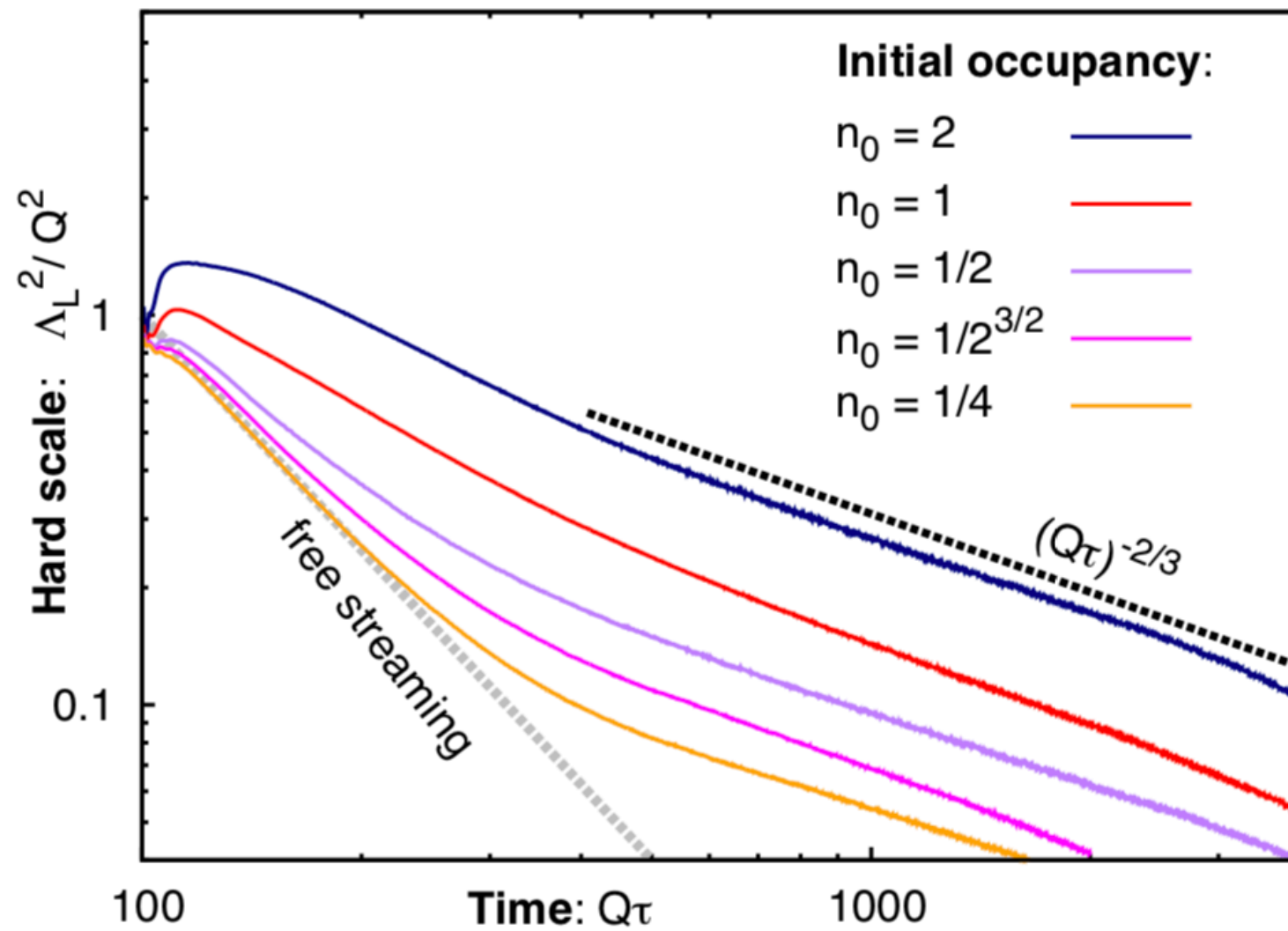
$$f(t, p) = t^\alpha f_S(p_\perp t^\beta, p_z t^\gamma)$$



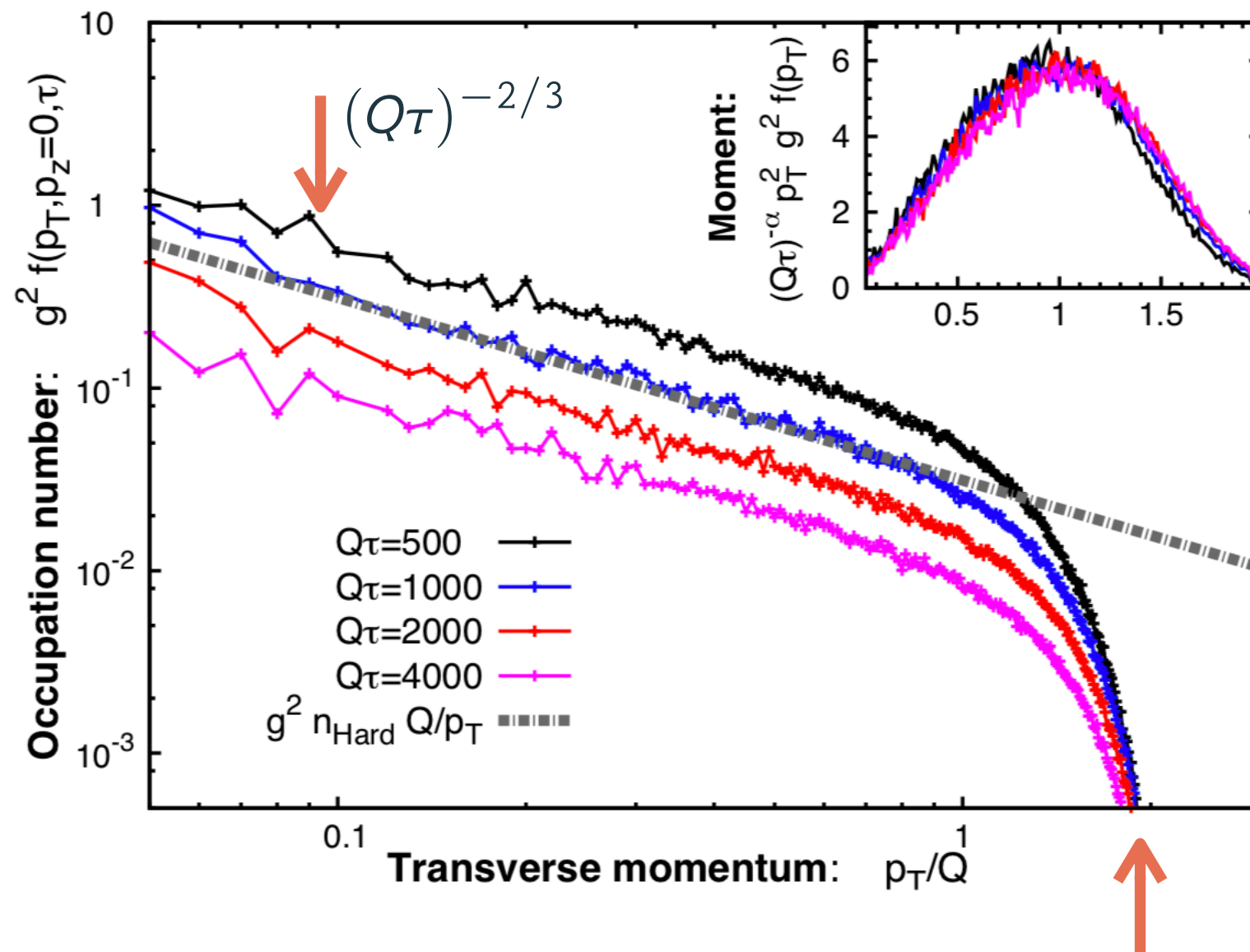
Transport and Turbulence

def. Local flow of conserved
charges to accommodate better
the total corresponding charge.
The flow is turbulent when is self-
similar

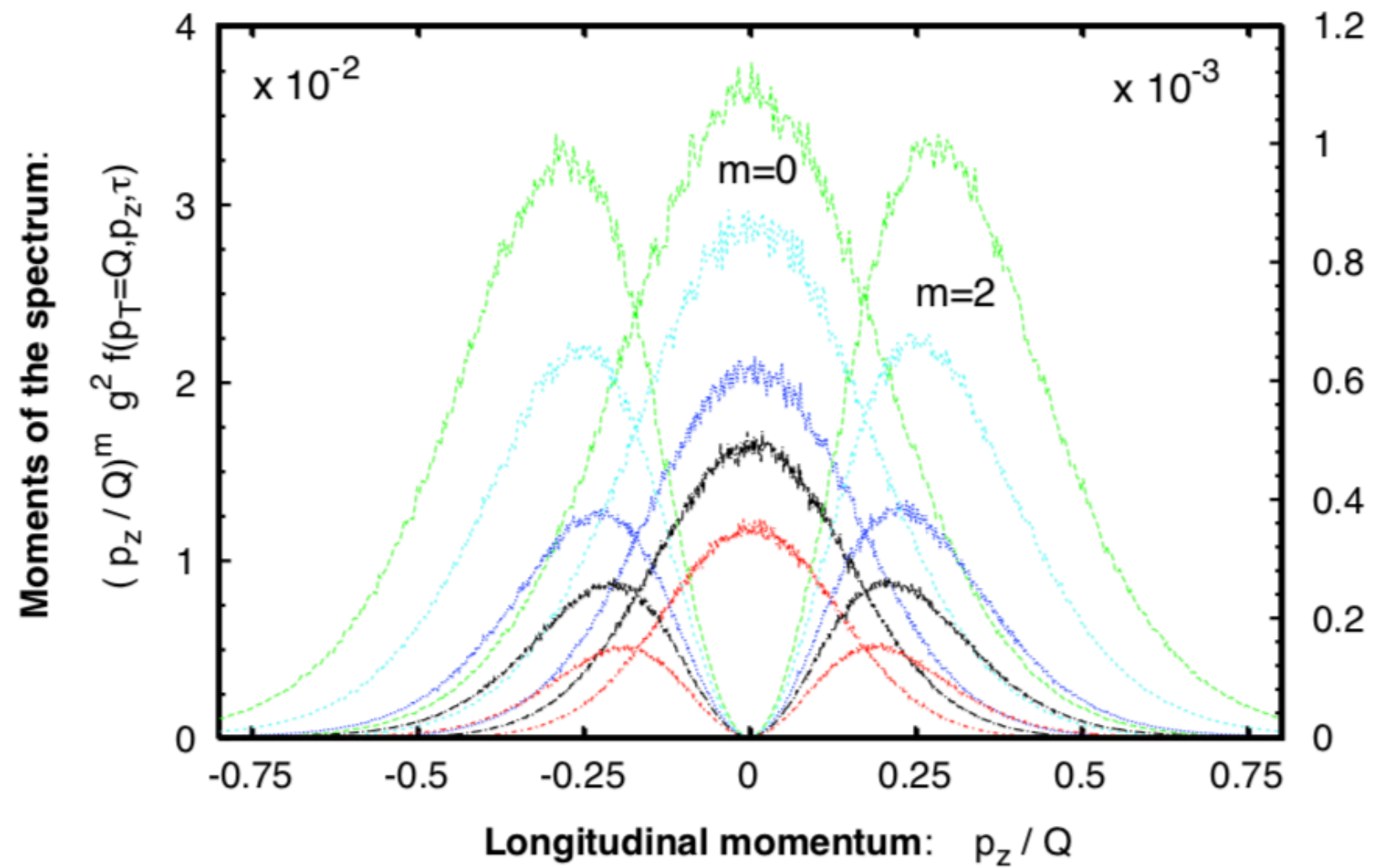
Hard Scale: $\Lambda_L^2 \sim \langle p_z \rangle^2$



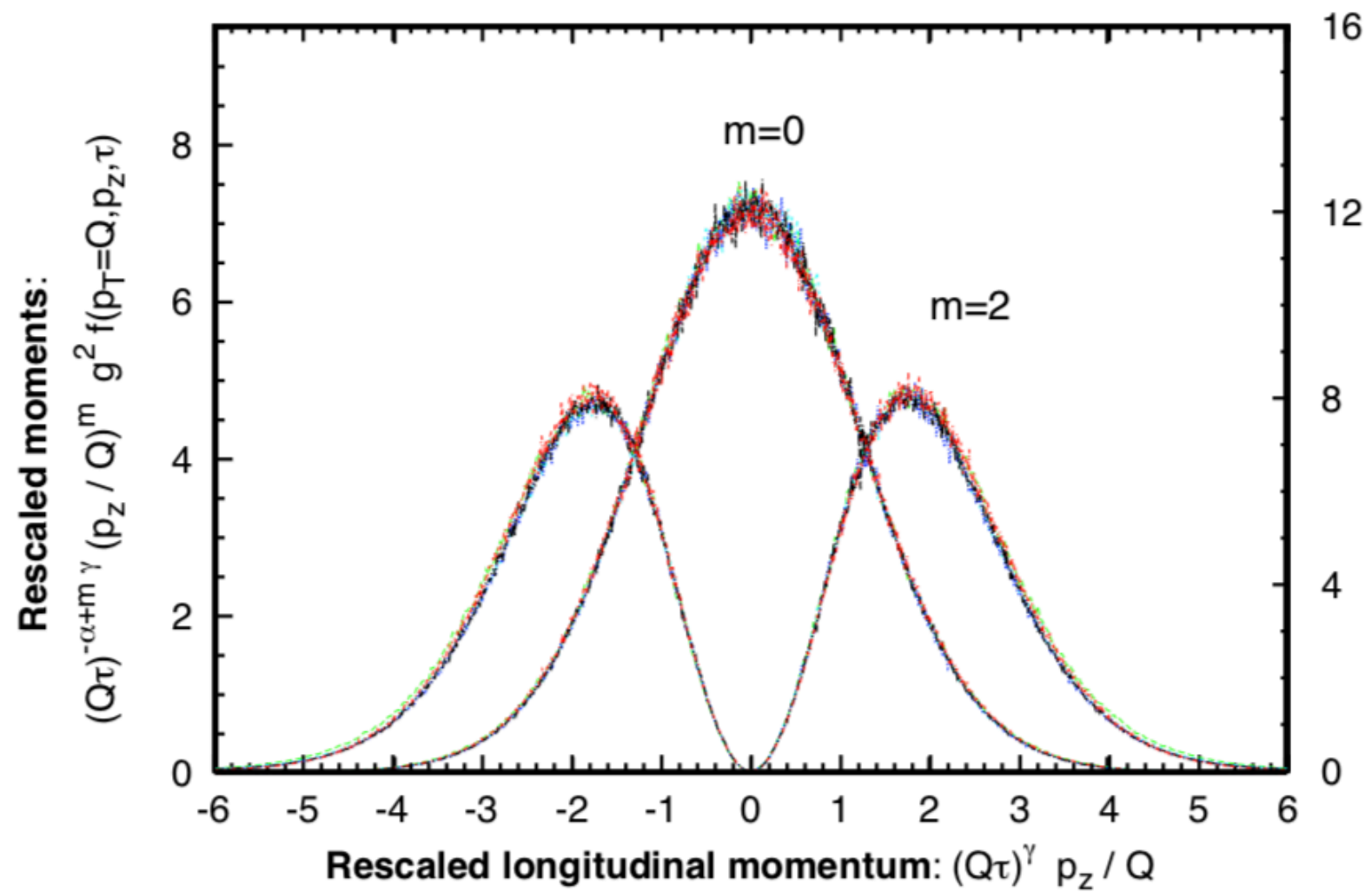
Occupancy: $p_{\perp}$



Occupancy: p_z

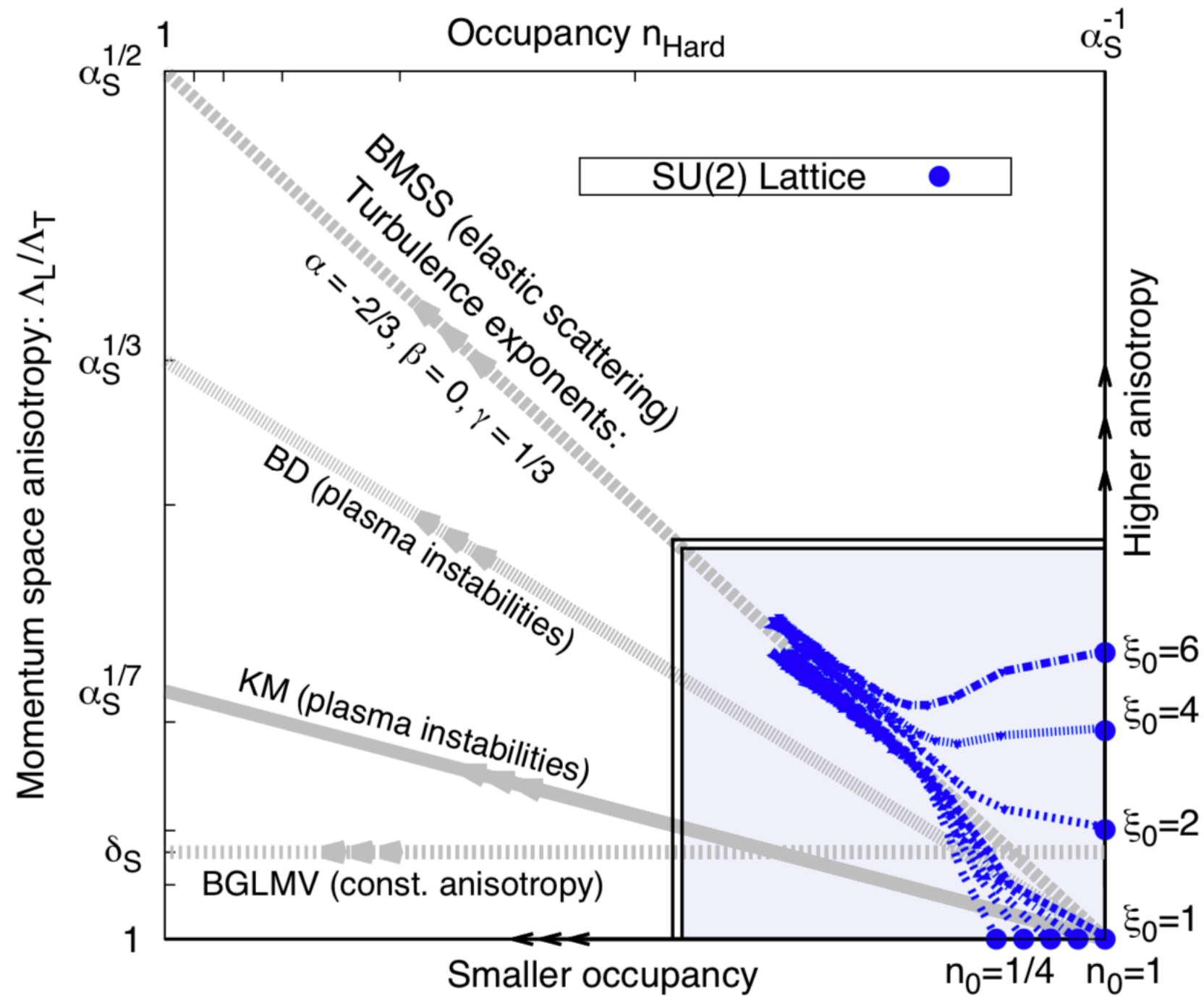


Occupancy: p_z



$$\gamma = 1/3$$

Finding the right scenario



Fit the lattice results

Gluon Distribution $\rightarrow f_g(\tau, p_\perp, p_z) = \frac{1}{\alpha_s} (Q_s \tau)^\alpha f_S(p_\perp, (Q_s \tau)^\gamma p_z)$

with
$$f_S(p_\perp, p_z) = \frac{Q_s}{p_\perp} e^{-\frac{1}{2} \left(\frac{p_z}{\sigma_0} \right)^2} W_r(p_\perp - Q_s, r)$$

and
$$W_r(p_\perp - Q_s, r) = \theta(Q_s - p_\perp) + \theta(p_\perp - Q_s) e^{-\frac{1}{2} \left(\frac{p_\perp - Q_s}{r Q_s} \right)^2}$$

Extension

Quark Distribution

Hard dipole approximation $\rightarrow f_q(\tau, p_\perp, p_z) = \alpha_s f_g(\tau, p_\perp, p_z)$

* Q.Stat. kick in lower than region of interest.



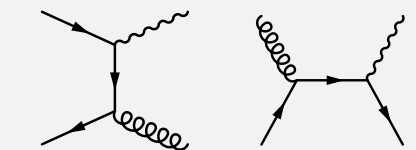
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Kinetic Rates

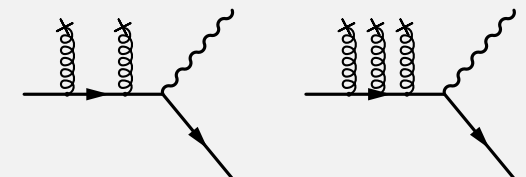
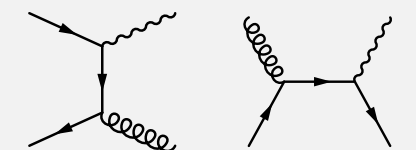
$$E \frac{dN_\gamma}{d^4X d^3p} = |\mathcal{M}|^2 \otimes F[f_i] \otimes \delta(p_{in} - p_{out})$$

Leading Log — $\left\{ \begin{array}{l} 2 \leftrightarrow 2 \text{ scatterings} \\ \text{Momentum transfer:} \end{array} \right.$



$gT \leftrightarrow T$
 $gQ_s \leftrightarrow Q_s$

Complete LO — $\left\{ \begin{array}{l} 2 \leftrightarrow 2 \text{ scatterings} \\ 1 \leftrightarrow 2 \text{ scatterings} \end{array} \right.$



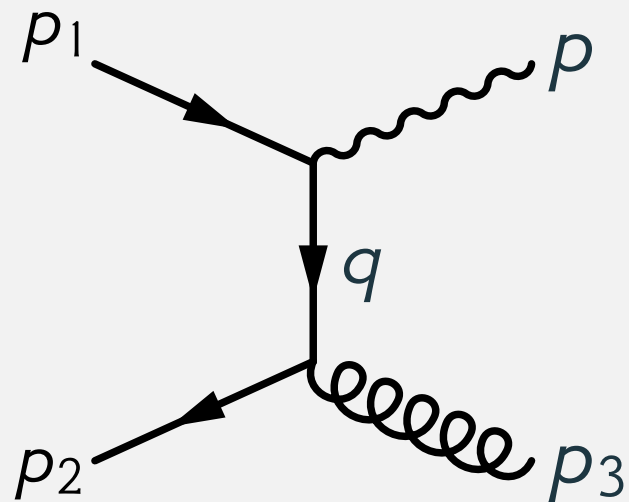
Colinearly enhanced,
inelastic processes

LPM

Kinetic Rates

$$E \frac{dN_\gamma}{d^4X d^3p} = \frac{1}{2 (2\pi)^{12}} \int \frac{d^3p_3}{2E_3} \frac{d^3p_2}{2E_2} \frac{d^3p_1}{2E_1} |\mathcal{M}|^2 \\ \times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P) \\ \times f_1(p_1) f_2(p_2) [1 \pm f_3(p_3)]$$

Small angle approximation $\longrightarrow$ Expansion on momentum exchange



$$|\mathbf{p}| = \sqrt{(\mathbf{p}_1 + \mathbf{q})^2} \sim |\mathbf{p}_1| + \mathbf{q} \cdot \mathbf{p}_1 / |\mathbf{p}_1|$$

$$|\mathbf{p}_3| = \sqrt{(\mathbf{p}_2 - \mathbf{q})^2} \sim |\mathbf{p}_2| - \mathbf{q} \cdot \mathbf{p}_2 / |\mathbf{p}_2|$$

Kinetic Rates

$$E \frac{dN_\gamma}{d^4 X d^3 p} = \frac{1}{2 (2\pi)^{12}} \int \frac{d^3 p_3}{2E_3} \frac{d^3 p_2}{2E_2} \frac{d^3 p_1}{2E_1} |\mathcal{M}|^2$$

$$\times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P)$$

$$\times f_1(p_1) f_2(p_2) [1 \pm f_3(p_3)]$$

Small angle approximation

$$E \frac{dN}{d^4 X d^3 p} = \frac{40}{9\pi^2} \alpha \alpha_s \mathcal{L} f_q(\mathbf{p}) (I_g + I_q)$$

Amplitude

Kinetic Rates

$$E \frac{dN_\gamma}{d^4 X d^3 p} = \frac{1}{2 (2\pi)^{12}} \int \frac{d^3 p_3}{2E_3} \frac{d^3 p_2}{2E_2} \frac{d^3 p_1}{2E_1} |\mathcal{M}|^2 \\ \times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P) \\ \times f_1(p_1) f_2(p_2) [1 \pm f_3(p_3)]$$

Small angle approximation

$$E \frac{dN}{d^4 X d^3 p} = \frac{40}{9\pi^2} \alpha \alpha_s \mathcal{L} j_q(\mathbf{p}) (I_g + I_q)$$

Regulator

Kinetic Rates

$$E \frac{dN_\gamma}{d^4 X d^3 p} = \frac{1}{2 (2\pi)^{12}} \int \frac{d^3 p_3}{2E_3} \frac{d^3 p_2}{2E_2} \frac{d^3 p_1}{2E_1} |\mathcal{M}|^2 \\ \times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P) \\ \times f_1(p_1) f_2(p_2) [1 \pm f_3(p_3)]$$

Small angle approximation

$$E \frac{dN}{d^4 X d^3 p} = \frac{40}{9\pi^2} \alpha \alpha_s \mathcal{L} f_q(\mathbf{p}) (I_g + I_q)$$

Screening Masses

$$I_{q,g}(\tau) = \int \frac{d^3 p}{(2\pi)^3} \frac{1}{p} f_{q,g}(\tau, p)$$

Thermal Stage

Rate

$$E \frac{dN^{th}}{d^4X d^3p} = \frac{5}{9} \frac{\alpha \alpha_s}{2\pi^2} \mathcal{L} T^2 e^{-E/T}.$$

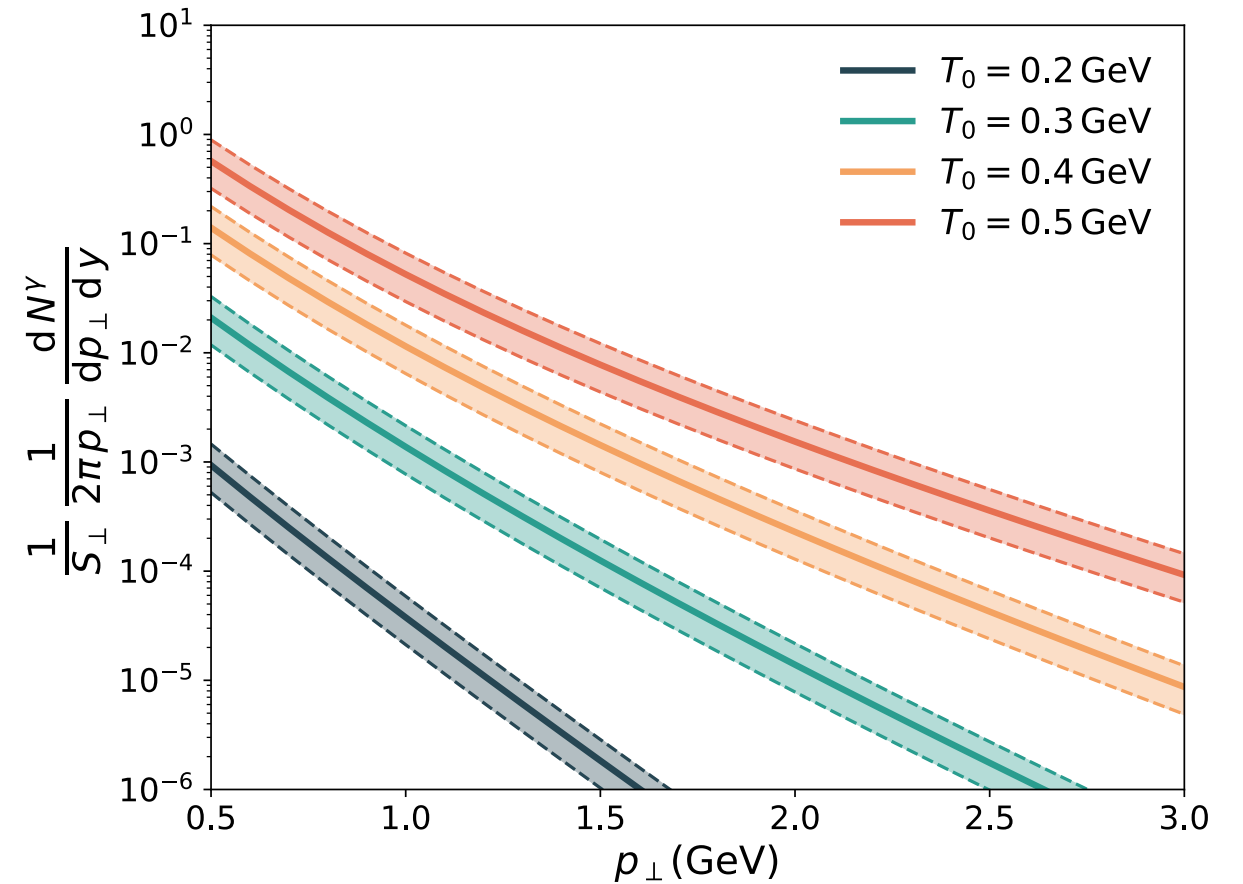
$$T = T_{th} (\tau_{th}/\tau)^{1/3}$$

Inv. Yield

$$\frac{1}{S_{\perp}} \frac{dN_{\gamma}}{d^2p_{\perp} dy} = \frac{5}{3} \frac{\alpha \alpha_s}{\pi^2} \tau_{th}^2 T_{th}^6 B_{th}(p_{\perp}).$$

$$B_{th}(p_{\perp}) = \left\{ \beta_{th}^4 \left[\frac{K_1(\beta_{th} p_{\perp})}{\beta_{th} p_{\perp}} + 2 \frac{K_2(\beta_{th} p_{\perp})}{(\beta_{th} p_{\perp})^2} \right] - \beta_c^4 \left[\frac{K_1(\beta_c p_{\perp})}{\beta_c p_{\perp}} + 2 \frac{K_2(\beta_c p_{\perp})}{(\beta_c p_{\perp})^2} \right] \right\},$$

$$\beta = T^{-1}$$



Total Yield

$$\frac{1}{S_{\perp}} \frac{dN_{\gamma}}{dy} = \frac{5}{3} \frac{\alpha \alpha_s}{\pi} \tau_{th}^2 T_{th}^4 \left(\frac{T_{th}^2}{T_c^2} - 1 \right).$$

Glasma. Stage I

Rate

$$E \frac{dN}{d^4 X d^3 p} = \frac{40}{9\pi^2} \alpha \alpha_S \mathcal{L} f_q(\tau, \mathbf{p}) I_g(\tau)$$

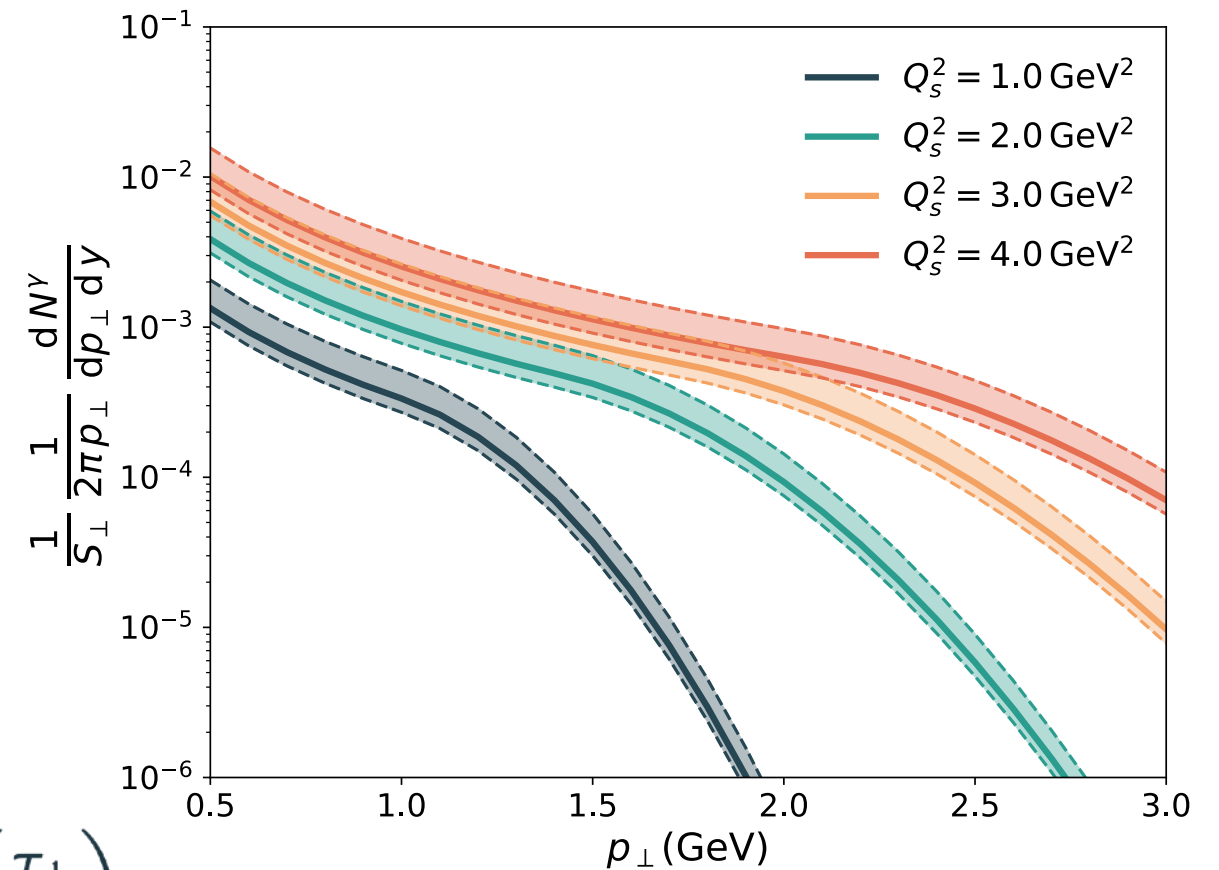
$$\rightarrow I_g(\tau) = \frac{Q_S^2}{4 \pi^2 \alpha_s} \frac{\kappa_g}{(Q_S \tau)}$$

Inv. Yield

$$\begin{aligned} \frac{1}{S_\perp} \frac{dN_\gamma}{d^2 p_\perp dy} &= \sqrt{\frac{\pi}{2}} \frac{20}{9\pi^4} \alpha_e \kappa_g f_0 \frac{\sigma_0}{Q_S} \log \left(\frac{\tau_1}{\tau_0} \right) \\ &\times \frac{Q_S^2}{p_\perp^2} W_r[p_\perp - Q_S] \end{aligned}$$

Total Yield

$$\frac{1}{S_\perp} \frac{dN_\gamma}{dy} = \sqrt{\frac{\pi}{2}} \frac{20}{3\pi^3} \alpha_e \kappa_g f_0 \sigma_0 Q_S \frac{2}{3} \log \left(\frac{\tau_1}{\tau_0} \right) \chi_r \quad \leftrightarrow \quad f_0 \frac{\sigma_0}{Q_S} = \sqrt{\frac{2}{\pi}} \kappa_q \left[\log \left(\frac{Q_S^2}{\sigma_0^2} \right) \right]^{-1}$$



Glasma. Stage II

Rate

$$E \frac{dN}{d^4 X d^3 p} = \frac{40}{9\pi^2} \alpha \alpha_S \mathcal{L} f_q(\tau, \mathbf{p}) I_g(\tau)$$

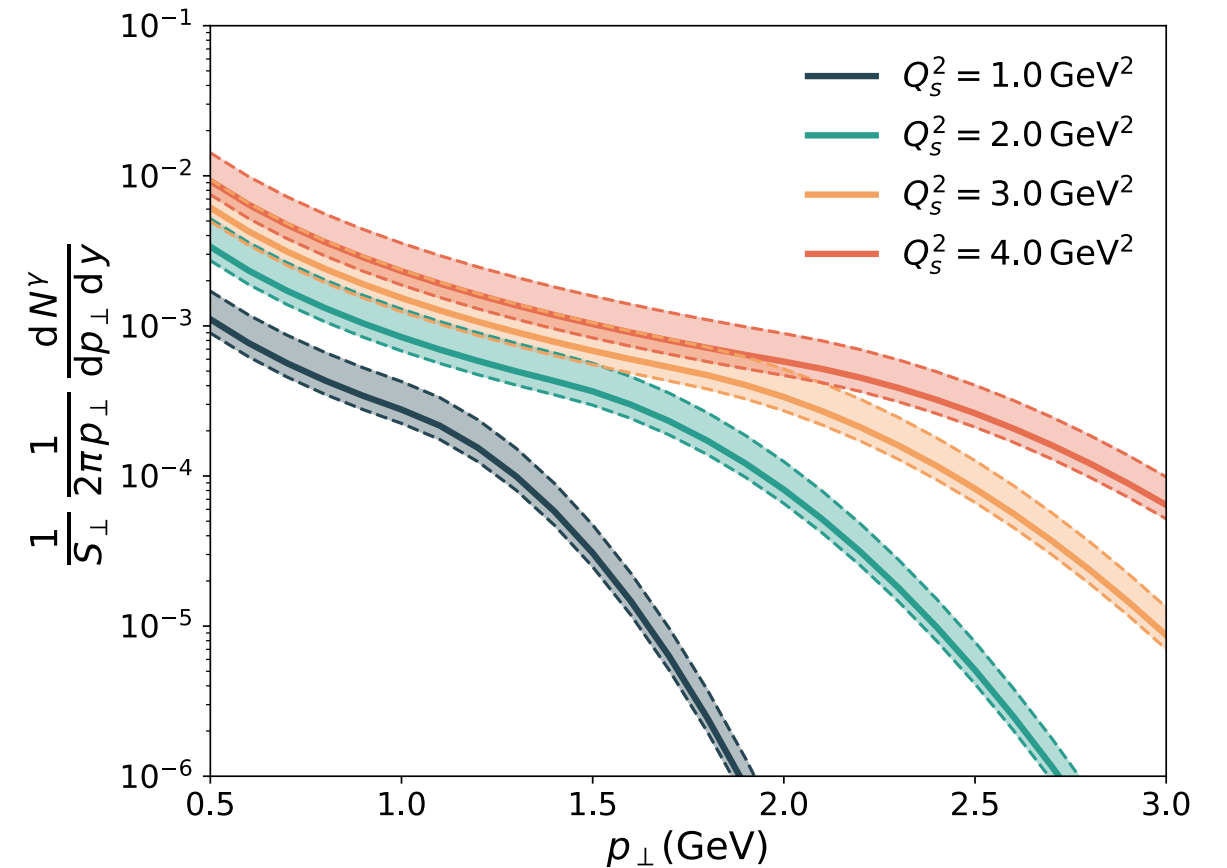
$$\rightarrow I_g(\tau) = \frac{\kappa_g \alpha_s^{-1/4}}{4 \pi^2} \frac{Q_S^2}{(Q_S \tau)^{1/2}}$$

Inv. Yield

$$\frac{1}{S_\perp} \frac{dN_\gamma}{d^2 p_\perp dy} = \sqrt{2\pi} \frac{20}{9\pi^4} \alpha_e \kappa_g f_0 \frac{\sigma_0}{Q_S} \frac{Q_S^2}{p_\perp^2} \times W_r[p_\perp - Q_S] \left(\alpha_s^{-1/2} - 1 \right)$$

Total Yield

$$\frac{1}{S_\perp Q_S^2} \frac{dN_\gamma}{dy} = \sqrt{\frac{\pi}{2}} \frac{80}{9\pi^3} \alpha_e \mathcal{L} \kappa_g f_0 \left(\alpha_s^{-1/2} - 1 \right) \quad \leftrightarrow \quad f_0 \frac{\sigma_0}{Q_S} = \sqrt{\frac{2}{\pi}} \kappa_q \left[\log \left(\frac{Q_S^2}{\sigma_0^2} \right) \right]^{-1}$$



Glasma. Stage III

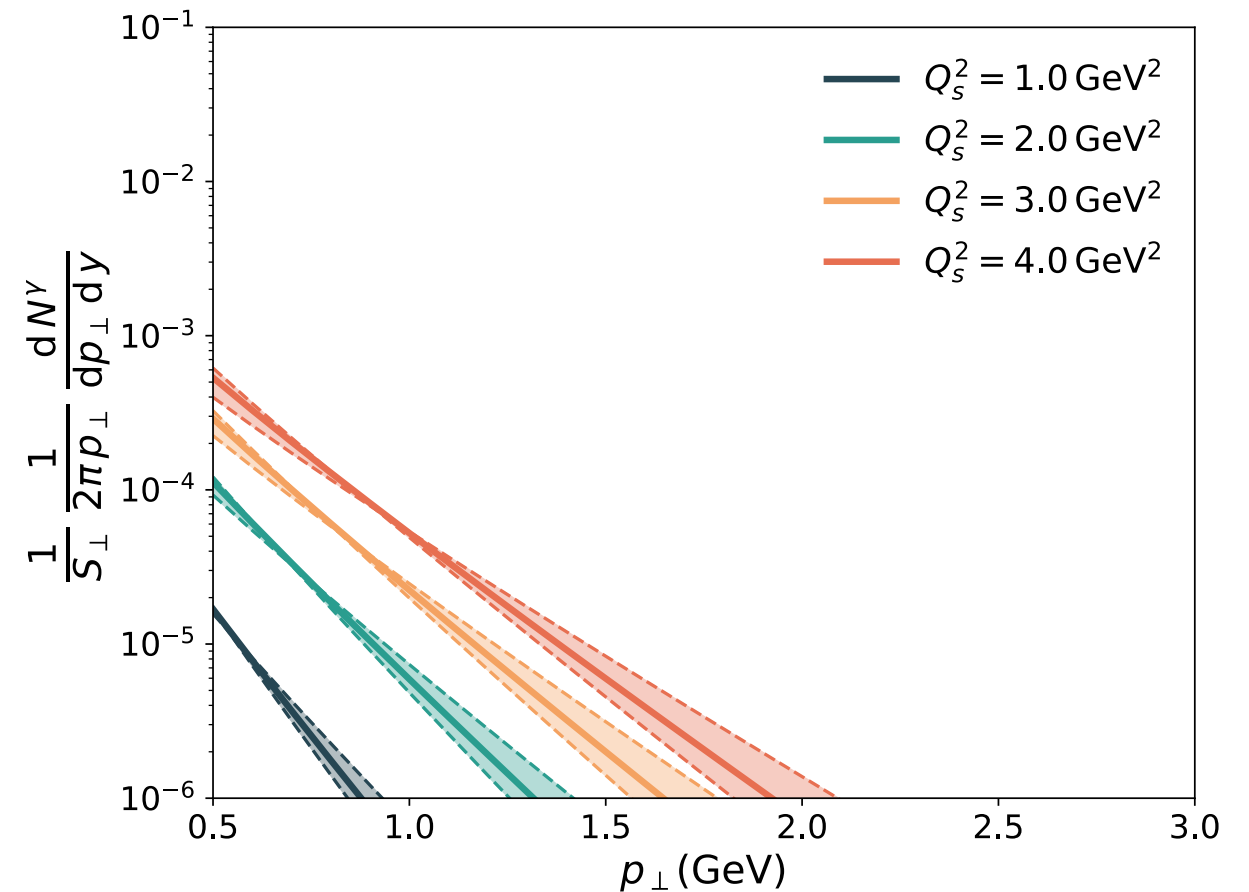
Rate

$$E \frac{dN^{\text{th}}}{d^4X d^3p} = \frac{5}{9} \frac{\alpha \alpha_s}{2\pi^2} \mathcal{L} T^2 e^{-E/T}.$$

$$T = c_T \alpha_s^3 Q_s(Q_s T)$$

Total Yield

$$\frac{1}{S_\perp Q_s^2} \frac{dN_\gamma}{dy} = \frac{5}{27} \frac{\alpha}{2\pi^2} c_{eq}^6 \mathcal{L} \alpha^{-13/5}$$



Inv. Yield

$$\begin{aligned} \frac{1}{S_\perp} \frac{dN_\gamma}{d^2p_\perp dy} = & \sqrt{\frac{\pi}{2}} \frac{5}{9} \frac{\alpha \alpha_s^{-5}}{\pi^2 c_T^2} \frac{p_\perp^4}{Q^4} \frac{32}{945} \mathcal{L} \left(\sqrt{\pi} \text{erf} \left(\sqrt{\frac{p_\perp}{T}} \right) \right. \\ & \left. + \sqrt{\frac{T}{p_\perp}} e^{-\frac{p_\perp}{T}} \left(1 - \frac{1}{2} \frac{T}{p_\perp} + \frac{3}{4} \frac{T^2}{p_\perp^2} - \frac{15}{8} \frac{T^3}{p_\perp^3} + \frac{105}{16} \frac{T^4}{p_\perp^4} \right) \right) \Bigg|_{T_2}^{T_{th}} \end{aligned}$$

Phenomenological Matching

$$\langle Q_s^2 \rangle = \frac{\int d^2 x_\perp Q_s^2(x_\perp)}{\langle S_\perp \rangle}$$

Glauber

IP-Glasma

$$\langle Q_s^2 \rangle = 2 \text{ GeV}$$



RHIC, 0-5% (Reference)

$$\langle Q_s^2 \rangle = 1.67 \text{ GeV}$$



RHIC, 0-20%

$$\langle Q_s^2 \rangle = 2.97 \text{ GeV}$$



ALICE, 0-20%

Phenomenological Matching

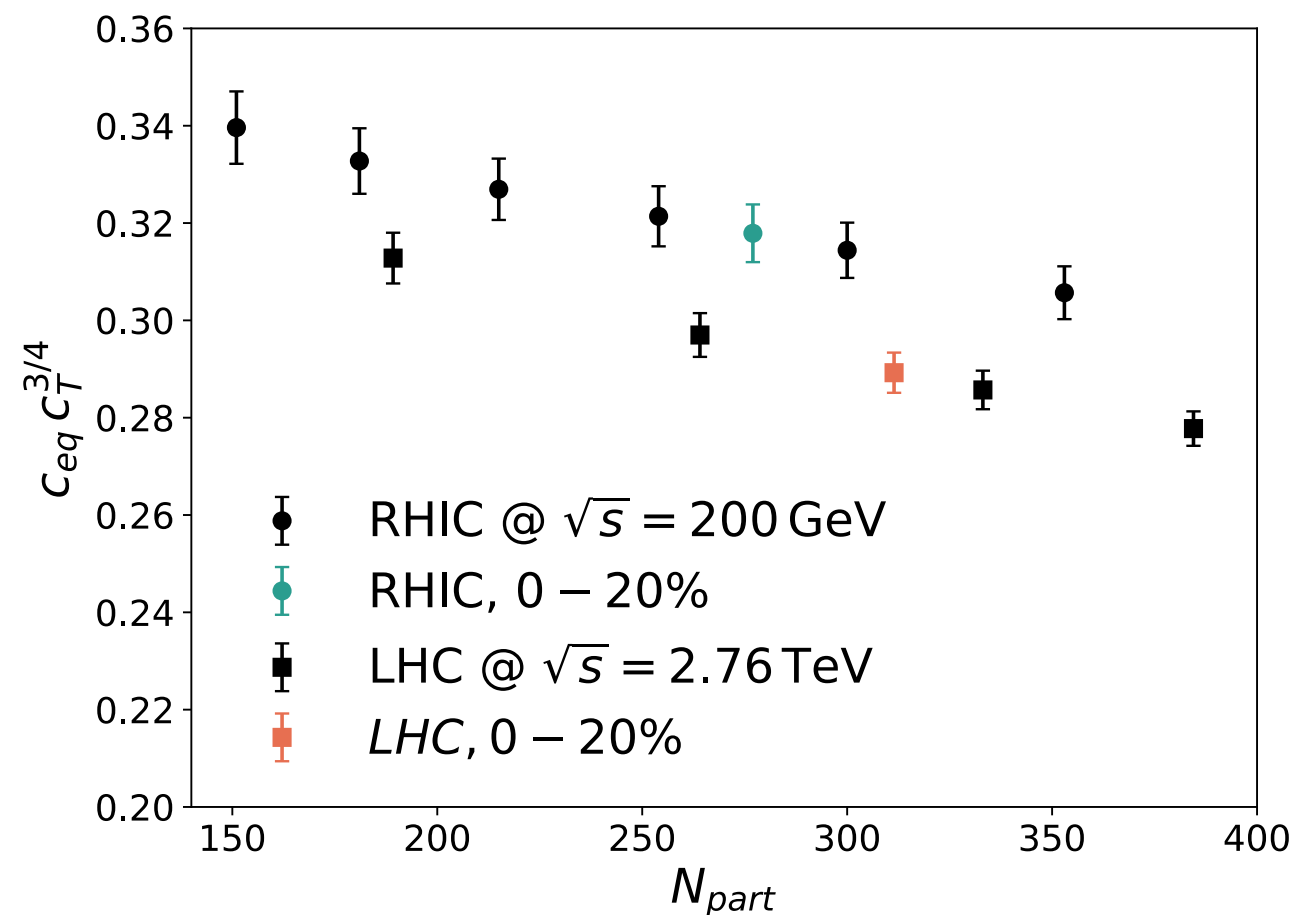
$$c_{eq} c_T^{3/4} = \left[\frac{45}{148\pi^2} k_{S/N} \alpha^{7/5} \frac{N_{part}}{Q_S^2 S_\perp} \frac{2}{N_{part}} \frac{dN_{ch}}{dy} \right]^{1/4}$$

Entropy is transported via

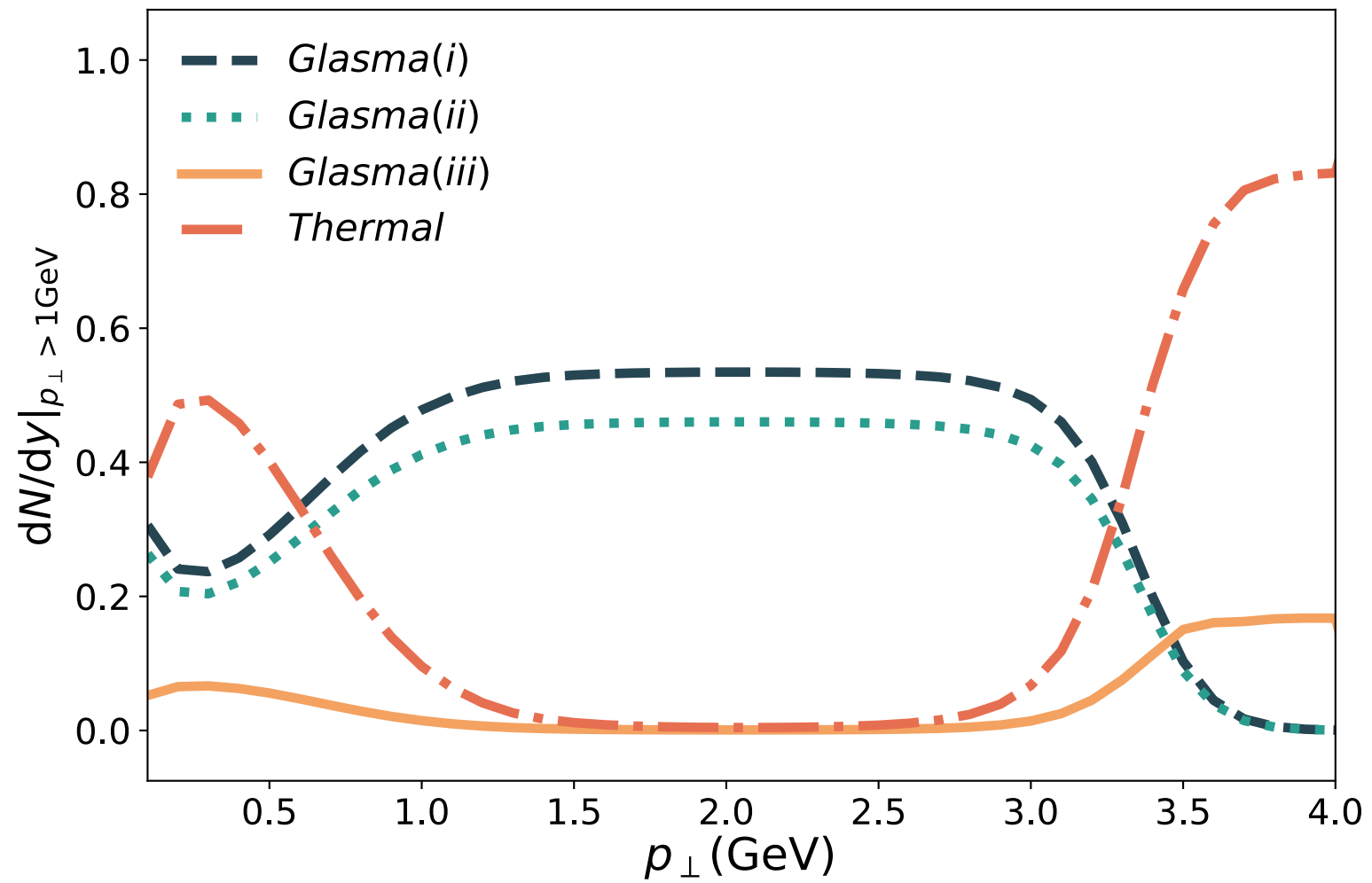
$$\frac{dS_{QGP}}{d\eta} = k_{S/N} \frac{dN_{ch}}{d\eta}$$

C_T known to logarithmic precision

$$C_T = 0.18$$

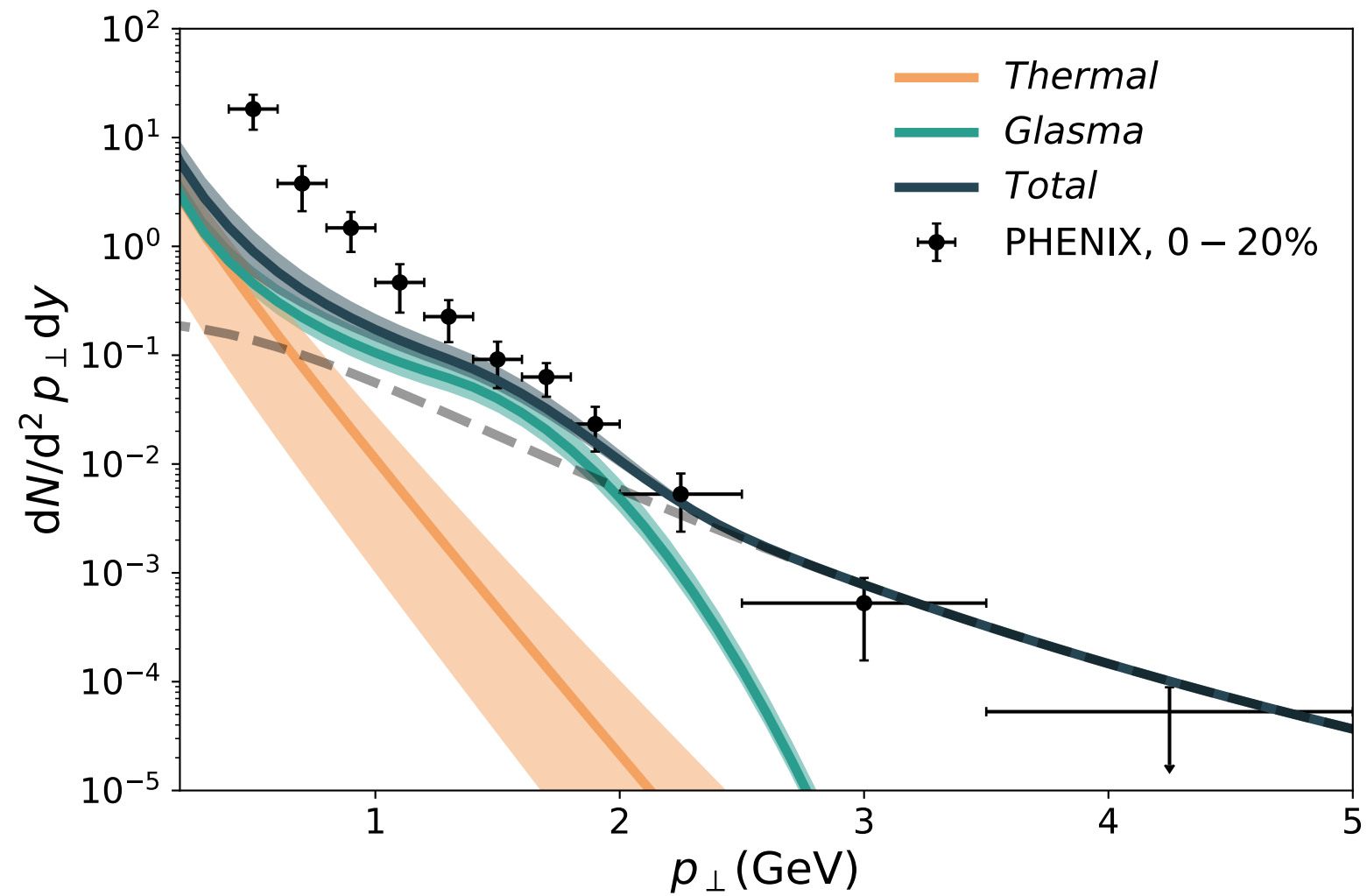


Contributions



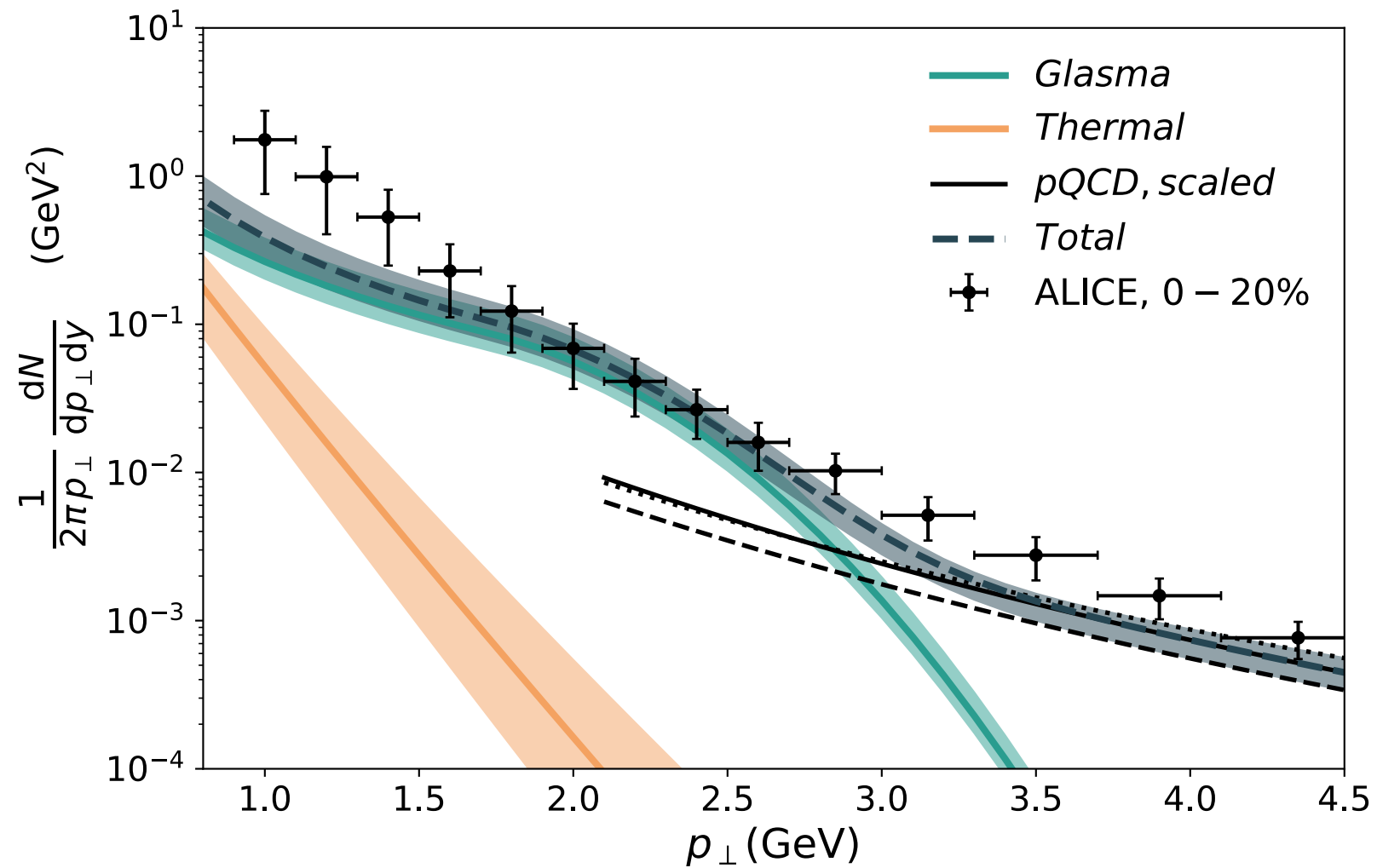
Comparison to data

PHENIX



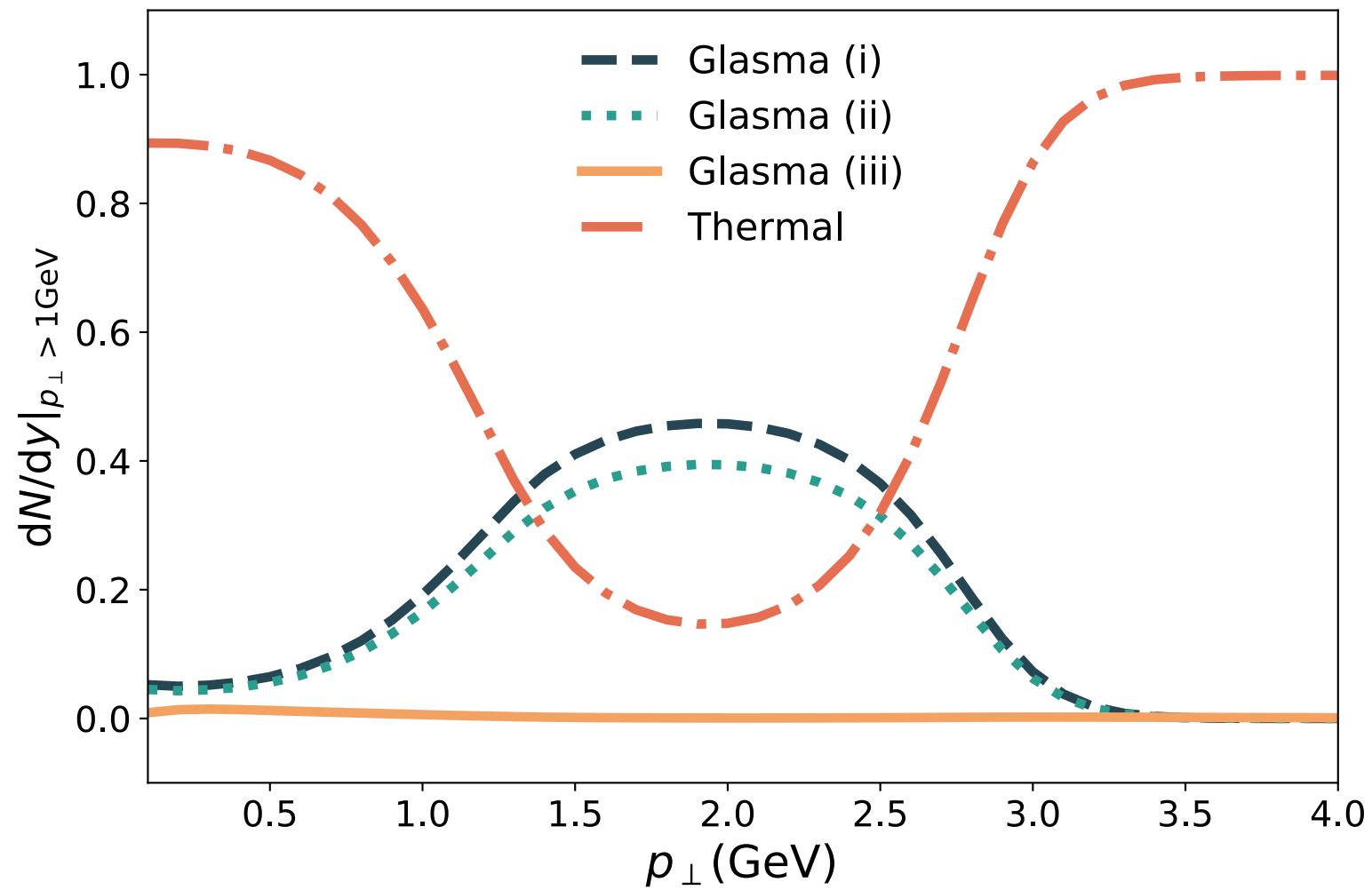
Comparison to data

ALICE



Contributions

(AMY revisited)



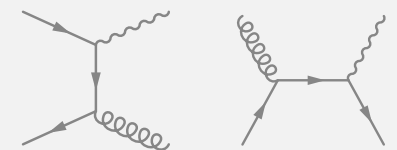
Kinetic Rates

$$E \frac{dN_\gamma}{d^4X d^3p} = |\mathcal{M}|^2 \otimes F[f_i] \otimes \delta(p_{in} - p_{out})$$

Leading Log

$2 \leftrightarrow 2$ scatterings

Momentum transfer:

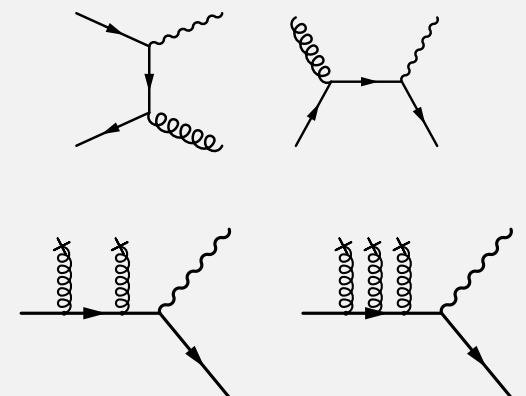


$gT \leftrightarrow T$
 $gQ_s \leftrightarrow Q_s$

Complete LO

$2 \leftrightarrow 2$ scatterings

$1 \leftrightarrow 2$ scatterings

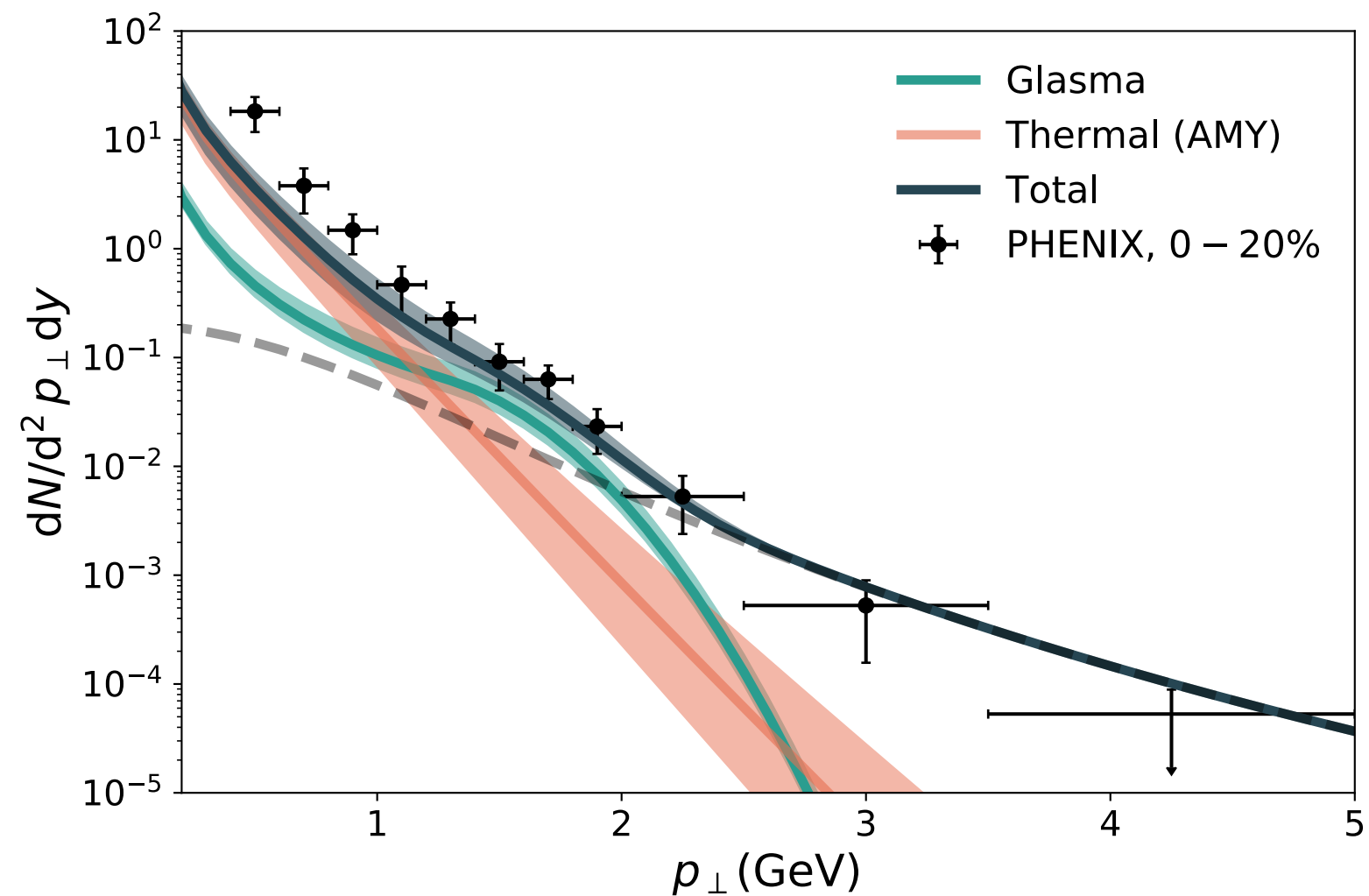


Colinearly enhanced,
inelastic processes

LPM

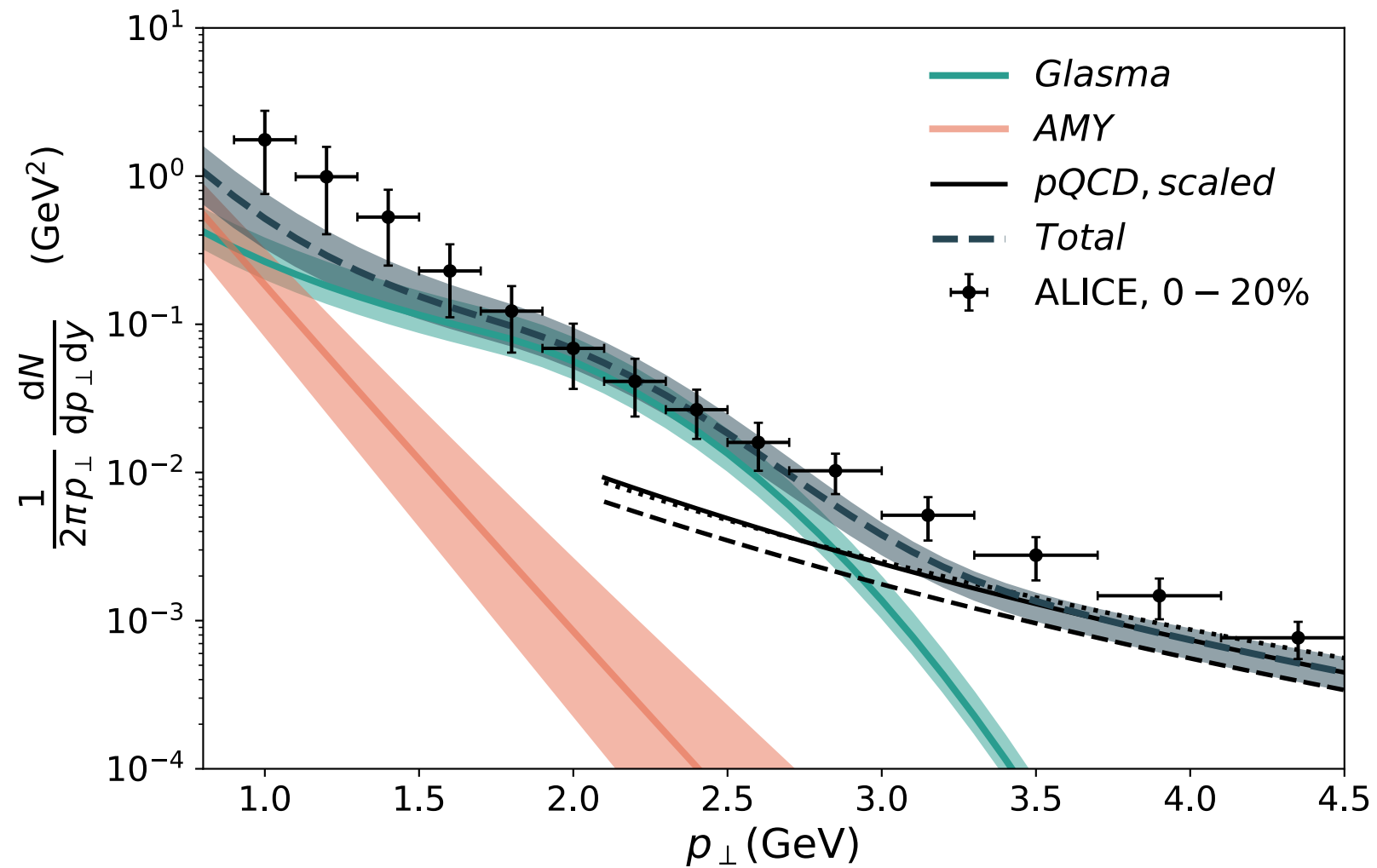
Comparison to data

PHENIX (AMY revisited)



Comparison to data

ALICE (AMY revisited)



Contents

- 1 Motivation
- 2 *Bottom-up* thermalization
- 3 Turbulent thermalization
(and all that Jazz)
- 4 Photons from thermalizing matter
- 5 Summary and Outlook



Caveats

- Simple model
- Pre-equilibrium doesn't account for anisotropies ... yet.
- Full kinetic approach will account for inelastic terms
 - ➔ IR enhancement?



Summary and Outlook

- Photons are our cleanest probes
- BMSS thermalisation is a consistent framework, confirmed by real-time lattice studies
- BMSS photons are relevant at scales relevant for saturation physics
- EKT studies are needed to discriminate, and to account for anisotropies
- Higher correlations (photon HBT) may be particularly sensitive to pre-equilibrium physics

