

Relevance of cluster formation in heavy ion collisions and the fragmentation code FRIGA *Cold nuclei and hot matter*

Y. Leifels, A. Le Fevre GSI Helmholtzzentrum für Schwerionenforschung, Darmstadt J. Aichelin, C. Hartnack SUBATECH, CNRS, University of Nantes

CBM Symposium 3.10.2018





Outline

- Heavy ion reactions between 0.1 10AGev
- Introduction to transport models
- Characteristic observables
- Relevant quantities and comparison to experimental data
 - Equation of state of nuclear matter
 - Dependencies to other input parameters
 - Importance of cluster formation
- FRIGA
 - Introduction
 - Benchmarking BQMD + FRIGA
 - Benchmarking IQMD + FRIGA
 - Hyper nuclei
- Summary and Outlook

Phase diagram of QCD matter

How to explore nuclear matter under extreme conditions?



- heavy ion collisions tool to explore characteristics of compressed nuclear matter in the laboratory
- need microscopic transport models to interpret the data

Microscopic models – two approaches

Boltzmann-Vlasov-like (BUU/HSD)

$$\begin{pmatrix} \frac{\partial}{\partial t} + \frac{\vec{p}}{m} \vec{\nabla}^r - \vec{\nabla} U(r) \vec{\nabla}^p \end{pmatrix} f(\vec{r}, \vec{p}; t) = \\ I_{coll} (\sigma^{in-med}) + \frac{\delta I_{fluct}}{\delta I_{fluct}}$$

Dynamics of 1-body phase space distribution function f with 2-body dissipation

Molecular dynamics like (QMD/AMD)

$$\begin{split} |\Phi > &= A \prod_{i=1}^{n} \varphi(r; r_{i}, p_{i}) |0 > \\ \dot{r}_{i} &= \{r_{i}, H\}; \ \dot{p}_{i} = \{p_{i}, H\} \\ H &= \sum_{i} t_{i} + \sum_{i,j} V(r_{i} - r_{j}) \end{split}$$

Time-dependent Hartree Fock plus stochastic NN collisions

physical input:
mean field (potential),
$$\longrightarrow$$
 transport
 σ_{inmed} , spectral functions code

"technical input": discretization, averaging (coarse graining), Pauli blocking, etc. Code comparison project: H. Wolter, M. Colonna, J. Xu et al.

1. Stopping



Data: FOPI+Indra, A.Andronic et al. Eur.Phys. J.30 (2006) 31-46 IQMD, C. Hartnack et al. EPJ A1 (1997) 151 Stopping deduced from phase space distributions

$$var xz = \frac{\sigma_{y_x}^2}{\sigma_{y_z}^2}$$

- measured 0.12 1.5 (2.0)
 AGeV for Au+Au to Ca+Ca
- depending on energy (maximum at 0.5AGeV)
- sensitive to in-medium cross sections

2. Formation of clusters



- high degree of cluster formation in most central collisions
- yields cannot be described by coalescence
 - neutron capture of ³He enhances α yield at low energies
- cluster production influences phase space distribution of other particles

3. Particle production

Possible at energies below to the threshold in NN system



- multi-step processes can cumulate the energy needed
- intermediate resonances used as an energy reservoir
- production at high densities due to short life time of resonances
- probing density (number of binary collisisons)



4. Flow



H. Stoecker et al., PRC 285(1982) 349 Discovery at Bevalac

H.A. Gustafsson, et al., Phys. Rev. Lett. 52 (1984) 1590. R.E. Renfordt, et al., Phys. Rev. Lett. 53 (1984) 763.

Comparing experimental results to model predictions...

Yield information on

- nuclear matter equation of state
 - momentum dependence
 - symmetry energy

 $E(\rho,\delta,T)=E_{SN}(\rho,T)+\delta^2 E_{sym}(\rho,T)+\cdots$

- in-medium cross sections
 - scattering and production
- in-medium characteristics of particles
 - effective masses/potentials, spectral functions
 - decay widths



Equation of state for symmetric nuclear matter

Infinite symmetric nuclear matter N=Z

- ground state properties: $\rho_0 = 0.16$ N/fm³ and E(ρ_0) = -16 MeV
- expansion in density:

$$E(\rho, T = 0, \delta = 0) = E_0 + \frac{K}{18\rho^2}(\rho - \rho_0)^2 + \dots$$

K is the compression modulus

In the IQMD model

$$U(\rho) = \alpha \cdot \left(\frac{\rho_{\text{int}}}{\rho_0}\right) + \beta \cdot \left(\frac{\rho_{\text{int}}}{\rho_0}\right)^{\gamma}$$

- 3 parameters: 2 fixed by g. s. condition
- 3rd parameter: compression modulus
- artificial link between curvature and ground state behavior



J. Piekarewicz, PRC 69 (04) 041301, RMF: K=248 MeV G. Colò et al.,PRC 70 (04) 024307 Skyrme HF: K=230 MeV S. Shlomo et al. Eur. Phys. J. A 30, 23 (06) **K=240±20 MeV** D.H. Youngblood et al., PRC 80, 064318 (09): K=231±5 MeV

Symmetry energy

$$E_{sym}(\rho) = E_{sym,0} + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right)$$
$$+ \frac{K_{sym}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2 + \dots$$

Largely unconstrained at high densities \rightarrow related to uncertainty of three-body and tensor forces at high density

In IQMD

$$\mathsf{E}_{sym} = \mathsf{S}_0 \cdot (\rho/\rho_0)^{\gamma}$$



Compressibility of symmetric nuclear matter: Kaon production





- results are independent on production cross sections and mechanisms and on the in-medium properties of kaons
- sensitivity to compressibility largest below threshold
- relevant density ~2ρ₀

Compressibility of symmetric matter: Directed flow at Plastic Ball





- IQMD comparison to Plastic Ball data favors a soft EOS with mdi (C. Hartnack GSI-Report-93-05, Mod. Phys. Lett. A 09, 1994)
- ambiguities between Skyrme part and mdi contribution
- influence of cross sections

Momentum dependent interaction in IQMD

$$U(\rho) = \alpha \cdot \left(\frac{\rho_{\text{int}}}{\rho_0}\right) + \beta \cdot \left(\frac{\rho_{\text{int}}}{\rho_0}\right)^{\gamma} + \underbrace{\delta \cdot \ln^2(\epsilon \cdot (\Delta \vec{p})^2 + 1) \left(\frac{\rho_{\text{int}}}{\rho_0}\right)}_{U_{mdi}}$$

- optical potential linear in density
- parameters fitted to experimental pN data
- a soft EOS with mdi (SM) shows the same density dependence as a soft EOS without mdi (S)



IQMD, C. Hartnack et al. EPJ A1 (1997) 151

Directed flow depends on the EOS and...



Effect of mdi similar to the influence of EOS ... effects of other ingredients also strong

Luckily there is more than just one observable...



C. Hartnack GSI-Report 93-05

Directed flow data in comparison to IQMD



- all charged particles weighted with Z
- semi-central collisions
- no conclusions can be drawn

Compressibility of symmetric nuclear matter: Directed flow of protons



- quote of the authors: additional constraints needed on momentum dependence of NN potential and in-medium cross sections and symmetry potential
 - newer data on elliptic flow in agreement with a soft EOS (SM) → most available data and Kaon production is reasonably described by this model (input parameters constrained with experimental data)

Collective flows in Au+Au at 1.0A GeV



All flow results

- Au+Au 0.4 1.5AGeV
 Ru+Ru/Zr+Zr
- directed flow
- elliptic flow
- protons
- d, t, ³He, α

are reasonably well described by IQMD transport code employing **a SM EOS for symmetric matter**

Collective flow of light charged particles



- composite particles are less influenced by thermal noise, larger flows
- flow pattern of clusters described by IQMD SM despite mismatch in the overall yields
- mismatch in the region of target/projectile rapidity point to insufficient description of clusterization

 $V_{2}(Y^{(0)}) = V_{20} + V_{22} \cdot Y^{(0)2}$ $V_{2n} = |V_{20}| + |V_{22}|$

Elliptic flow of light charged clusters



- influence of clusterisation is partially removed by using this observable
- isotopically resolved elliptic
 flow is described by IQMD
 employing an SM EOS
- huge difference for the two types of EOS (SM and HM)
- much larger than the experimental error bars
- promising observable to constrain the EOS for symmetric matter

Constraining the symmetry energy

Sensitive observables that are or will be more extensively explored :

- neutron stars...
- nuclear masses
- neutron skins
- cluster formation at low densities
- fragmentation of nuclei
- isospin diffusion und isospin drift between nuclei of different N/Z in peripheral HIC
- neutron/proton, t/³He spectra and collective flows
- π-/π+ multiplicities and spectra



Symmetry energy at supra-normal densities



Model independence investigated in M.D. Cozma et al., arXiv:1305.5417 P. Russotto et al., PLB 267 (2010) Y. Wang et al., PRC 89, 044603 (2014)



Elliptic flow ratio of neutrons and charged particles



parametrization for SE used in UrQMD* model:

 $\mathsf{E}_{sym} = \mathsf{E}_{sym}^{\text{pot}} + \mathsf{E}_{sym}^{\text{kin}} = 22\mathsf{MeV} \cdot (\rho/\rho_0)^{\gamma} + 12\mathsf{MeV} \cdot (\rho/\rho_0)^{2/3}$

- systematic errors corrected: $\gamma = 0.72 \pm 0.19$
- slope parameter: L = 72 ± 13 MeV, $E_{svm}(\rho_0)$ = 34 MeV
- slope parameter: L = 63 ± 11 MeV, E_{sym}(ρ₀) = 31 MeV
- clusterization important

But... what about the clusters and fragments...?

- ambiguities due to different fragment species
- fragments much more sensitive to dynamical effect
- clusters formation is omnipresent in HIC, important for analysis (observables depend on degree of cluster formation)



FRIGA

Fragment Recognition In General Applications

- Simulated Annealing Procedure: PLB301:328,1993; later called SACA (Simulated Annealing Clusterisation Algorithm)
- So far applied with various transport models: BQMD, IQMD, pHSD.
- Prediction of (light and heavy) (hyper)isotope yields and full phase space distribution.

A. LeFevre, J. Aichelin, E. Bratkovskaya, C. Hartnack, V. Kireyeu, Y. Leifels



Germanic mythological goddess Frigg/Friga, spinning the clouds

Model used

Transport : IQMD (C. Hartnack et al., Eur. Phys. J. A 1 (1998) 151)

+ Clustering algorithm: FRIGA (A. Le Fèvre et al, 2016 J. Phys.: Conf. Ser. 668 012021)

simulated annealing with Minimum Spanning Tree coalescence as 1st step
 + overall cluster binding energy minimization

 $E_{bind} = E_{kin} + E_{Coul} + E_{m.f.} + E_{Yuk.}^{surf.} + E_{asy}^{pot} + E_{struct}$

- veto of unstable isotopes
- ³He+n; secondary decay of excited primary clusters (GEMINI);
- 1. Preselect fragments with MST
- 2. Take randomly 1 nucleon out of



3. Place it randomly in another fragment



FRIGA vs Minimum spanning tree

Unlike FRIGA, MST is not able to describe the early formation of fragments.

→ MSTs applied at later times (typically 200-400 fm/c

Advantage of FRIGA

Fragment partitions reflect the early dynamical conditions (Coulomb, density, flow details, strangeness...), which is particularly important for hyper nucleus formation.

* P.B. Gossiaux, R. Puri, Ch. Hartnack, J. Aichelin, Nuclear Physics A 619 (1997) 379-390



Yvonne Leifels - CBM Symposium 2018

Clustering with FRIGA

- MST at 200 fm/c
- FRIGA at 2-3 t_{pass} (time of nuclei to pass each other completely without deceleration)
- Less heavy fragments are produced with MST
- MST shows broader distribution
- Symmetry energy narrows distributions at around N=Z
- Structure effects small and underestimate binding energies for small clusters



Benchmarking BQMD+FRIGA with ALADIN data





- M_{imf} multiplicity of intermediate mass fragments (Z≥2) measured in forward direction
- Z_{bound} sum of charges detected at small polar angles (measures impact parameter)



Clustering with IQMD+FRIGA

- MST at 200 fm/c
- FRIGA at 2-3 t_{pass} (time of nuclei to pass each other completely without deceleration)
- Less heavy fragments are produced with MST but more light fragments
- Structure effects small and underestimate binding energies for small clusters

¹²⁹Xe+¹²⁴Sn @ 100 MeV/u b<2.8fm



Clustering with FRIGA after secondary decays

- MST at 200 fm/c
- FRIGA at 2-3 t_{pass} (time of nuclei to pass each other completely without deceleration)
- after secondary decays

 IQMD SM does not produce enough (heavy) clusters ¹²⁹Xe+¹²⁴Sn @ 100 MeV/u b<2.8fm



Clustering with IQMD SM - revisited



Benchmarking IQMD+FRIGA results IQMD(H)+FRIGA (2-4t pass) Θ id. SM M_{IM}F IQMD(H)+MST (200 fm/c, prim.) ALADiN data 2 S254 measured by the ALADIN2000 collaboration **IQMD** modifications smaller Gaussian package width: 4.33 fm² reduction of Fermi momentum during initialization $\mathsf{Z}_{\mathsf{max}}$ Au+Au 600 MeV/u 80 cluster multiplicity stable upto 200 fm/c SM and H EOS yield similar results 60 40 20

80

 $\mathsf{Z}_{\mathsf{bound}}$

40

20

60

Reconstruction of hyper nuclei

FRIGA ingredients:

- Volume component: mean field (Skyrme, dominant), for NN, NΛ (hypernuclei). We consider the strange quark as inert as a first approach ⇒ U(NΛ) = 2/3·U(NN)
- 2 Surface effect correction: Yukawa term.
- And optionally:
- 3 Symmetry energy E_{asy}
 4 Extra « structure » energy (N,Z,p) = BMF(p).((Bexp-BBW)/(BBW-Bcour-Basy))(p0)
 3 He+n recombination.
 6 Secondary decay: GEMINI.
 7 Rejection of « non-existing » isotopes
- A rejection of « non-existing » isotope and hyper-clusters.

IQMD+FRIGA 1.9GeV/u Ni+Ni

Soft EOS

with m.d.i.

no Kaon pot.



Influence of Lambda re-scattering



- rescattering changes rapidity distribution of hyperons
- and consequently the overlapp region between hyperons and spectator nucleons
- huge influence on yields on hyper nuclei

Clusterisation time influence on rapidity distributions



Yvonne Leifels - CBM Symposium 2018









^{*:} Ch.Hartnack et al., Eur. Phys. J. A 1(1998) 151.

- formation of heavy hypernuclei predominantly in the spectator region
- crucially ingredient is the ΛN re-scattering cross section
- cluster multiplicity in the midrapidity region depends on the clusterization time
- in contrast to spectator region (relatively stable)
- multiplicity of the HYPHI data overpredicted
- different slopes of transverse momentum spectra of $.^{3}_{\Lambda}$ H and $.^{4}_{\Lambda}$ H reproduced

Summary

- Cluster formation is omnipresent in heavy ion collisions
 - Cluster have a larger sensitivity to dynamics
 - and influence all observables
- Understanding of production needed for more stringent constraints on equation of state and symmetry energy, important for reaction dynamics and formation mechanisms
- Dynamical creation of clusters during transport would be the most elegant approach
- Advantage of FRIGA
 - minimazation of cluster binding energies relatively fast
 - allows for clusterization at early times to preserve the dynamics at this stage
 - o the final state of FRIGA is a classical bound state (no Fermi motion)
- Experimental data
 - production of heavy clusters in the projectile/spectator region
 - light clusters in particular in the mid-rapidity region
- First results on cluster production with IQMD SM available, needs benchmarking
- Hyper nuclei production might be a very important tool to study the mechanisms of fragmentation and production of clusters
- more data (with larger phase space coverage) urgently needed

Outlook – Constraining the EOS with I/UrQMD



- Equation of state of symmetric nuclear matter from comparison of FOPI data with IQMD
- the symmetry energy as extracted from ASY-EOS results with UrQMD*

Outlook



My thanks to the FOPI collaboration

A. Andronic, R. Averbeck, Z. Basrak, N. Bastid, M.L. Benabderramahne, M. Berger, P. Bühler, R. Caplar, M. Cargnelli, M. Ciobanu, P. Crochet, I. Deppner, P. Dupieux, M. Dzelalija, L. Fabbietti, J. Frühauf, F. Fu, P. Gasik, O. Hartmann, N. Herrmann, K.D. Hildenbrand, B. Hong, T.I. Kang, J. Keskemeti, Y.J. Kim, M. Kis, M. Kirejczyk, R. Münzer, P. Koczon, M. Korolija, R. Kotte, A. Lebedev, K.S. Lee, Y. Leifels, A. LeFevre, P. Loizeau, X. Lopez, M. Marquardt, J. Marton, M. Merschmeyer, M. Petrovici, K. Piasecki, F. Rami, V. Ramillien, A. Reischl, W. Reisdorf, M.S. Ryu, A. Schüttauf, Z. Seres, B. Sikora, K.S. Sim, V. Simion, K. Siwek-Wilczynska, K. Suzuki, Z. Tyminski, J. Weinert, K. Wisniewski, Z. Xiao, H.S. Xu, J.T. Yang, I. Yushmanov, V. Zimnyuk, A. Zhilin, Y. Zhang, J. Zmeskal

IPNE Bucharest, Romania, ITEP Moscow, Russia CRIP/KFKI Budapest, Hungary, Kurchatov Institute Moscow, Russia, LPC Clermont-Ferrand, France, Korea University, Seoul, Korea, GSI Darmstadt, Germany, IReS Strasbourg, France, FZ Rossendorf, Germany, Univ. of Heidelberg, Germany, Univ. of Warsaw, Poland, RBI Zagreb, Croatia, IMP Lanzhou, China, SMI Vienna, Austria, TUM, Munich, Germany, T.Yamazaki(RIKEN)



ls - CBM Symposium 2018

and to the ASYEOS collaboration

Co-Spokespersons: R.C. Lemmon¹ and P. Russotto²

List from the Proposal

F. Amorini², A. Anzalone¹⁷, T. Aumann³, V. Avdeichikov¹², V. Baran²³, Z. Basrak⁴, J. Benlliure¹³, I. Berceanu¹¹, A. Bickley¹⁴, E. Bonnet⁶, K. Boretzky³, R. Bougault³⁰, J. Brzychczyk⁸, B. Bubak²², G. Cardella⁷, S. Cavallaro², J. Cederkall¹², M. Chartier⁵, M.B. Chatterjee¹⁶, A. Chbihi⁶, M. Colonna¹⁷, D. Cozma¹¹, B. Czech¹⁰, E. De Filippo⁷, K. Fissum¹², D. Di Julio¹², M. Di Toro², M. Famiano²⁷, J.D. Frankland⁶, E. Galichet¹⁸, I. Gasparic⁴, E. Geraci¹⁵, V. Giordano², P. Golubev¹², L. Grassi¹⁵, A. Grzeszczuk²², P. Guazzoni²¹, M. Heil³, J. Helgesson³¹, L. Isaksson¹², B. Jacobsson¹², A. Kelic³, M. Kis⁴, S. Kowalski²², E. La Guidara²⁰, G. Lanzalone²⁹, N. Le Neindre³⁰, Y. Leifels³, Q. Li⁹, I. Lombardo², O. Lopez³⁰, J. Lukasik¹⁰, W. Lynch¹⁴, P. Napolitani³⁰, N.G. Nicolis²⁴, A. Pagano⁷, M. Papa⁷, M. Parlog³⁰, P. Pawlowski¹⁰, M. Petrovici¹¹, S. Pirrone⁷, G. Politi¹⁵, A. Pop¹¹, F. Porto², R. Reifarth³, W. Reisdorf³, E. Rosato¹⁹, M.V. Ricciardi³, F. Rizzo², W.U. Schroder²⁸, H. Simon³, K. Siwek-Wilczynska²⁶, I. Skwira-Chalot²⁶, I. Skwirczynska¹⁰, W. Trautmann³, M.B. Tsang¹⁴, G. Verde⁷, E. Vient³⁰, M. Vigilante¹⁹, J.P. Wieleczko⁶, J. Wilczynski²⁵, P.Z. Wu⁵, L.Zetta²¹, W. Zipper²²



Yvonne Leifels - CBM Symposium 2018

FAIR in 2025

THANK YOU FOR YOUR ATTENTION

Yvonne Leifels - CBM Symposium 2018

Confining the input parameters of IQMD



Choice in IQMD for

▶ σ_{NN},

momentum dependence of optical potentials,

prescription of Pauli blocking and detailed balance etc.

describes most of the data