

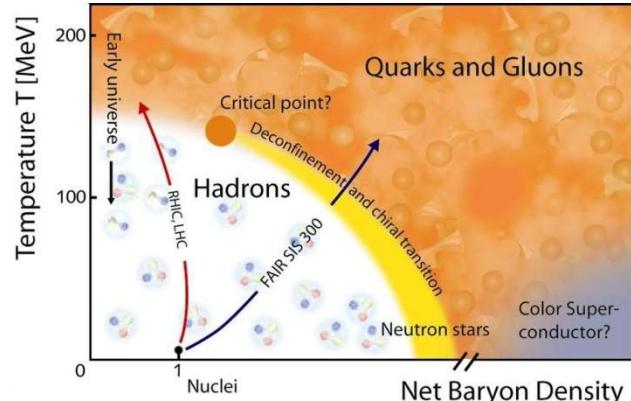
Constraining the EOS of strongly interacting matter in heavy ion collisions

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Darmstadt*

EMMI Rapid Reaction Task Force
The physics of neutron star mergers
Symposium
8.6.2018





or... Squeezing the symmetry energy out of heavy ion reactions

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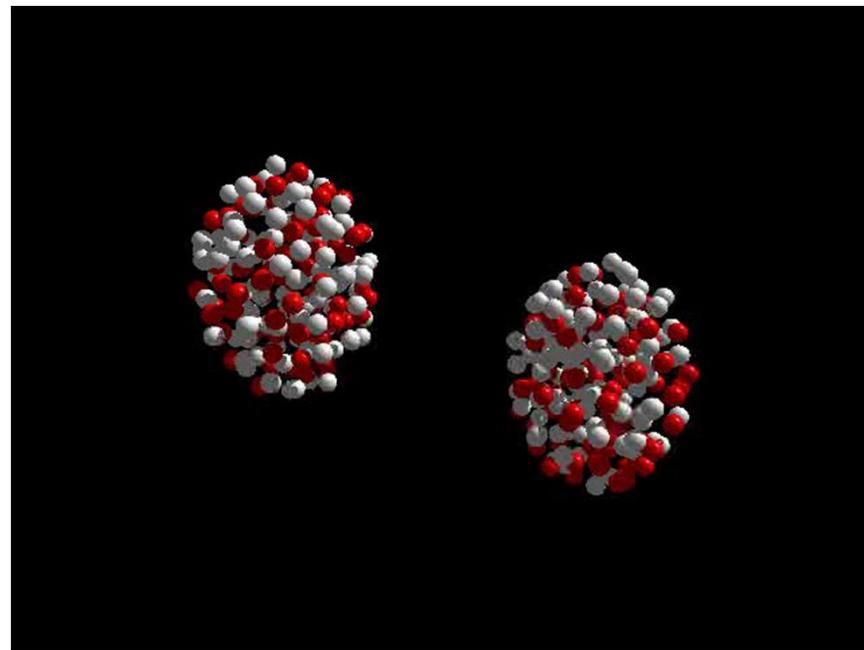
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Introduction



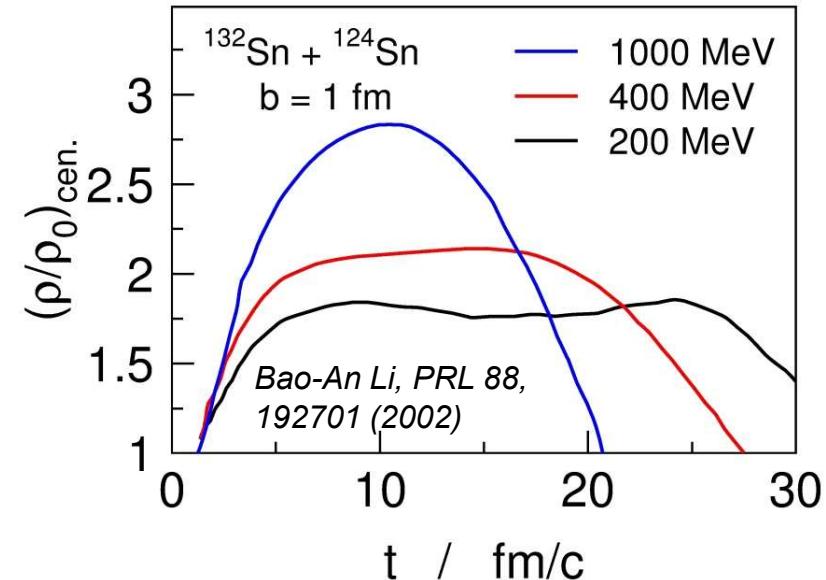
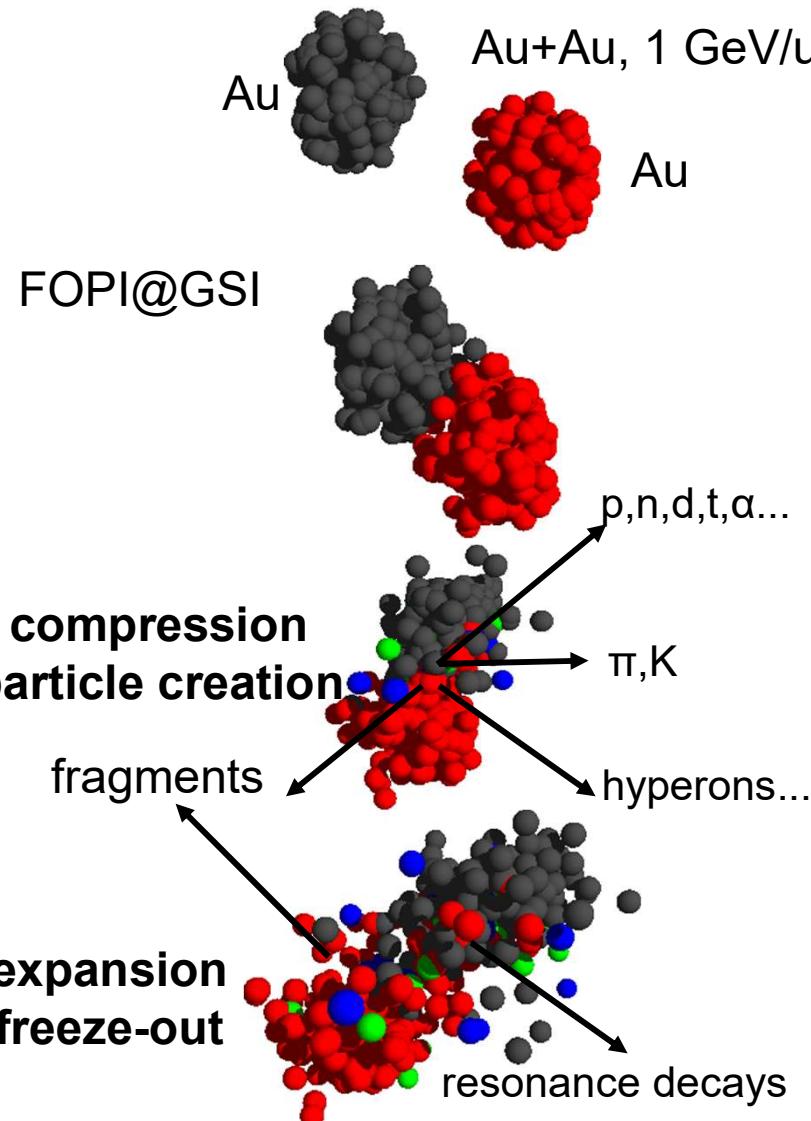
- neutron star mergers: $T = 0\text{--}100$ MeV, $\rho = 10^{-3} - 10\rho_0$
 - mass: $\sim 4 \cdot 10^{30}$ kg
 - size: $\sim 2 \cdot 10^4$ m
- neutron stars: $T = 0$, $\rho = 10^{-3} - 5\rho_0$
- supernovae simulations: $T = 1\text{--}50$ MeV, $\rho = 10^{-10} - 2\rho_0$



Au+Au 1.5 AGeV UrQMD

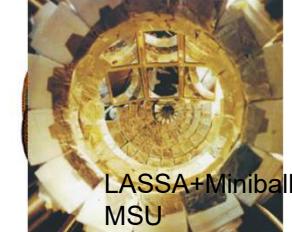
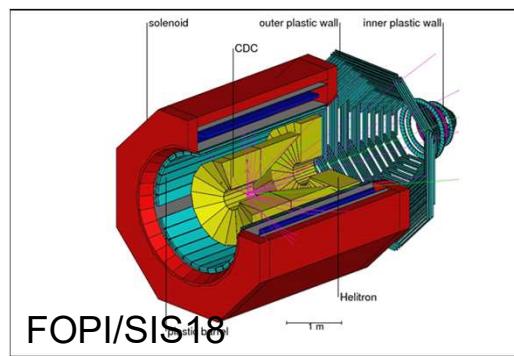
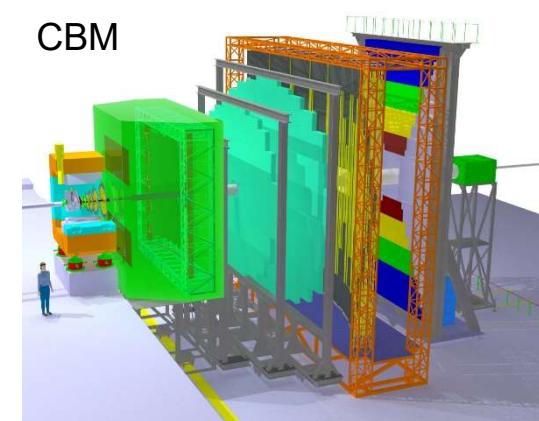
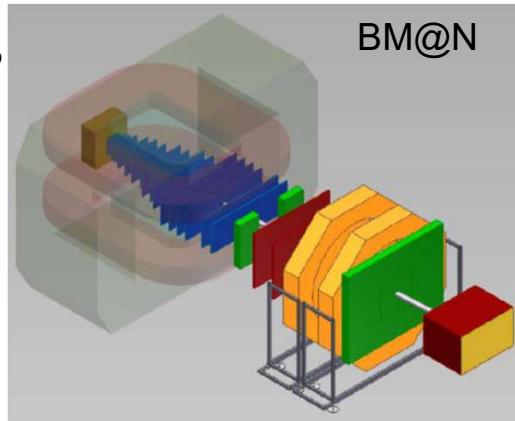
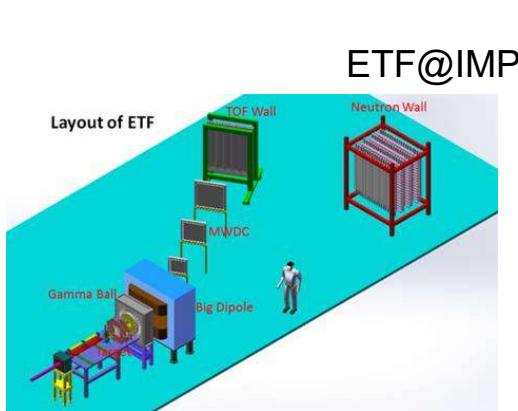
- heavy ion reactions: $T = 5$ MeV – >180 MeV, $\rho = 10^{-3} - 5\rho_0$
 - mass: $6.540 \cdot 10^{-24}$ kg
 - size: $2 \cdot 10^{-14}$ m
 - life time: $3 - 100 \cdot 10^{-24}$ s

HICs: Characteristics at 0.1 – 10 GeV/u

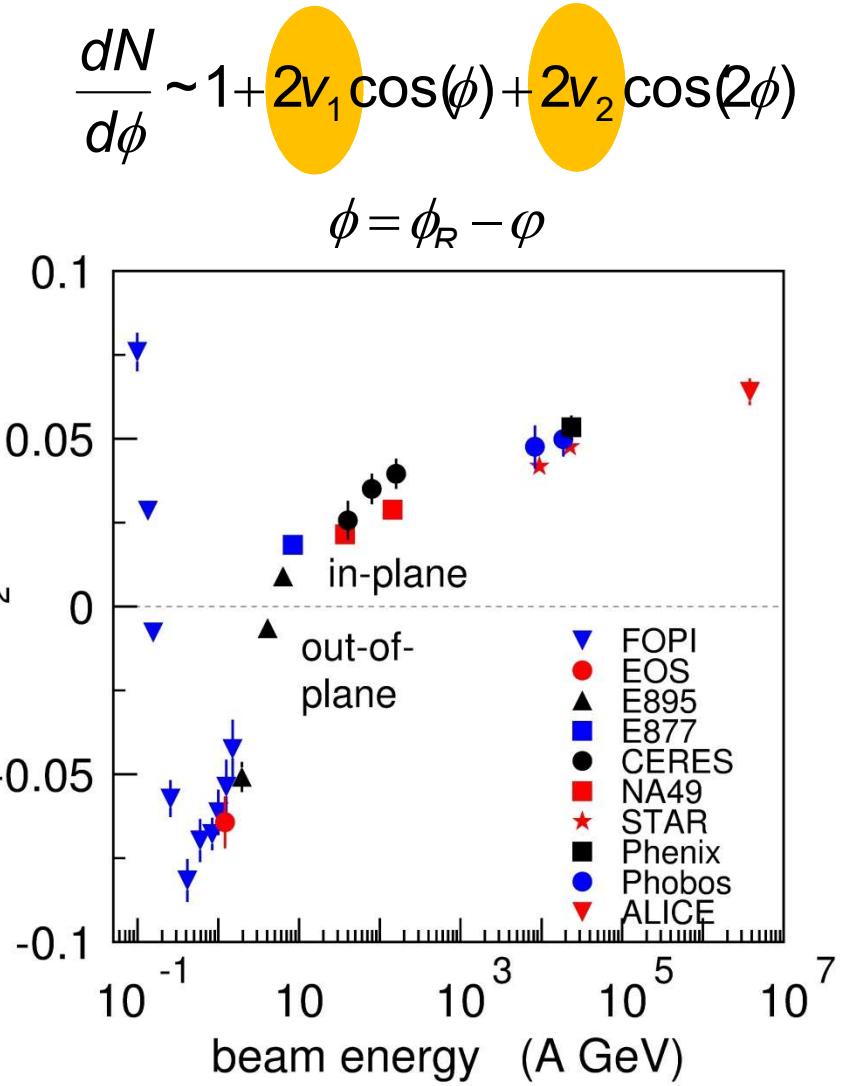
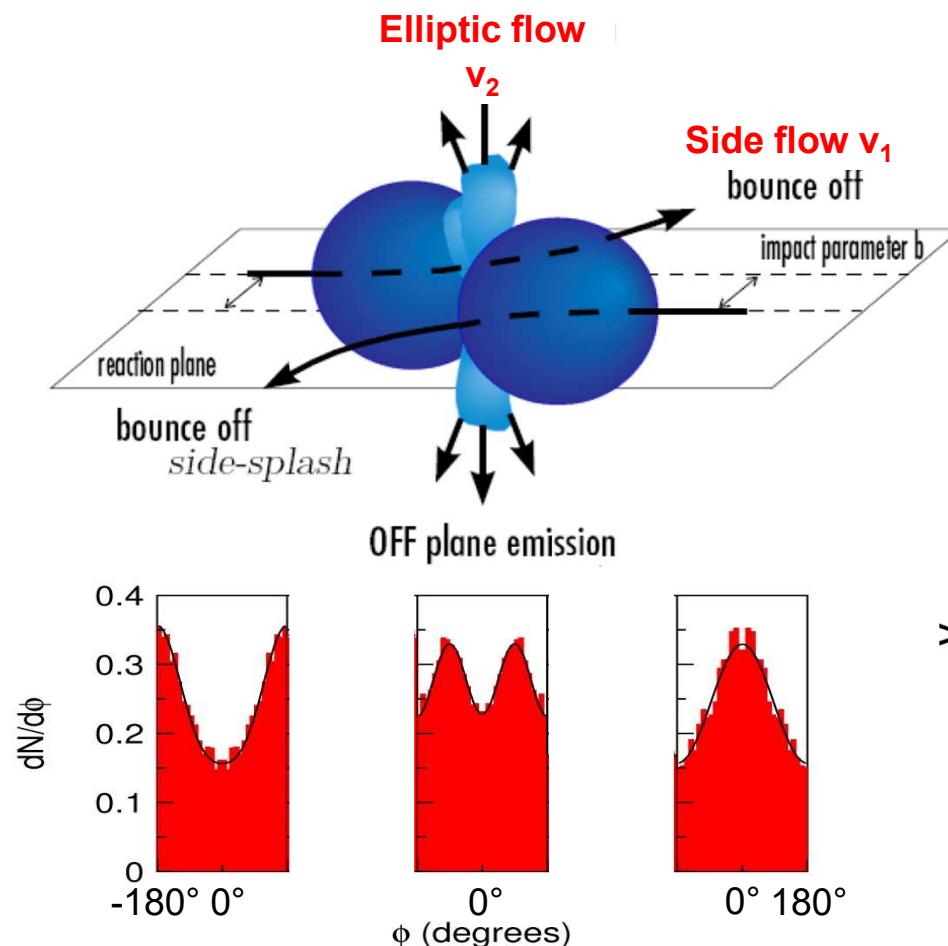


- reaching high densities, several ρ_0
 - creating (thermal) pressure
 - controlling density and pressure by varying system size and/or energy

Experiments



1. Flow



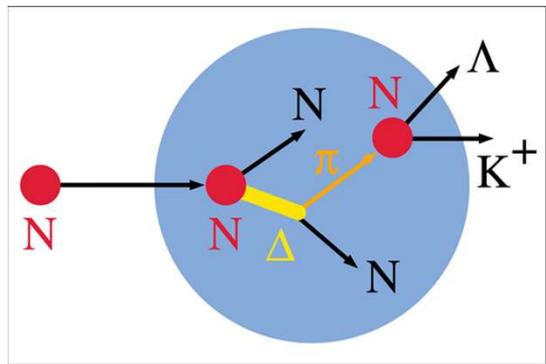
Discovery at Bevalac

H.A. Gustafsson, et al., Phys. Rev. Lett. 52 (1984) 1590.

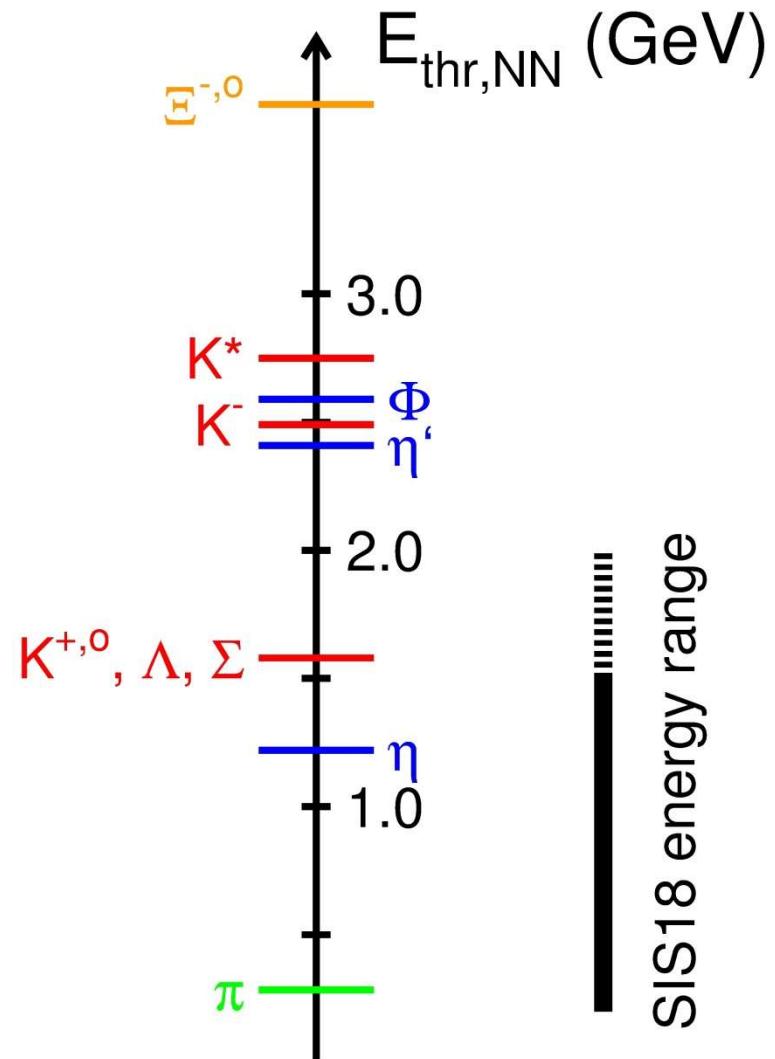
R.E. Renfordt, et al., Phys. Rev. Lett. 53 (1984) 763.

2. Particle production

Possible at energies below to the threshold in NN system

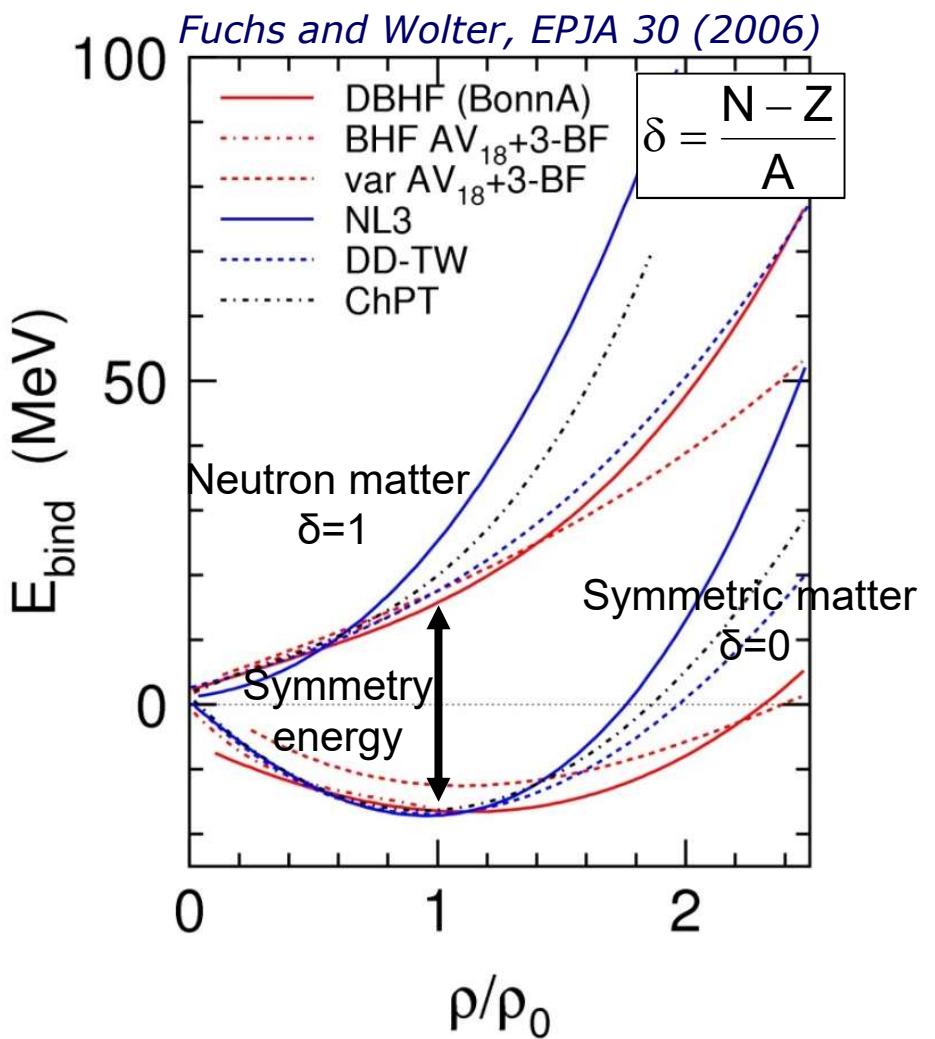


- multi-step processes can cumulate the energy needed
- intermediate resonances used as an energy reservoir
- production at high densities due to short life time of resonances
- probing density (number of binary collisions)



Interpretation of results

- heavy ion reactions rapidly evolving, transient state
- influenced by
 - **nuclear matter equation of state**
 - *momentum dependence*
 - in-medium cross sections
 - *Pauli blocking*
 - in-medium characteristics of particles
 - *effective masses/potentials, spectral functions*
 - *decay widths*
- microscopic transport models needed
- convincing conclusions on basic nuclear properties imply a successful simulation:
 - of the full set of experimental observables
 - with the same code
 - using the same physical and technical parameters.

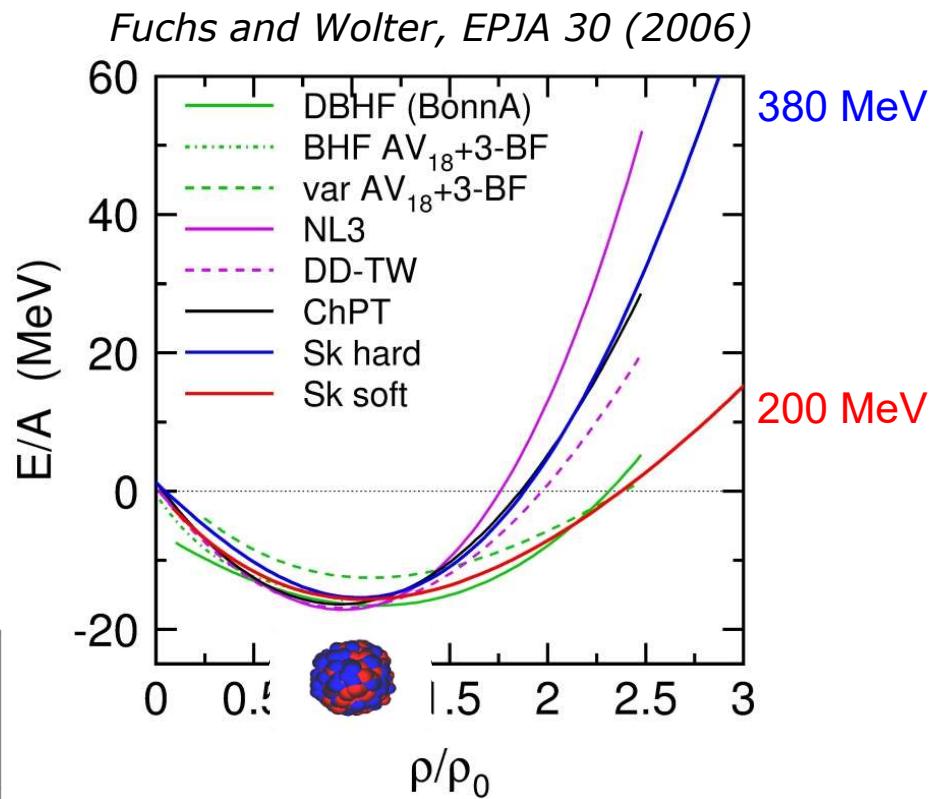
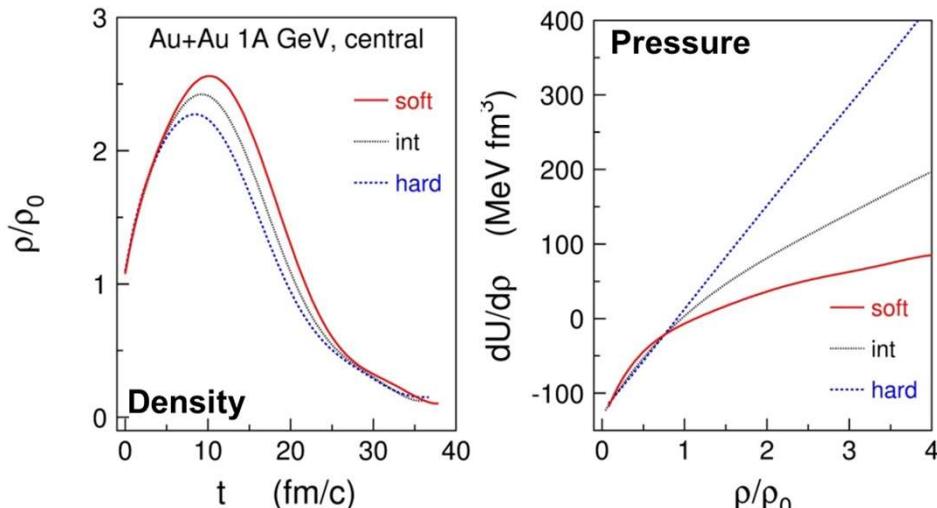


EQUATION OF STATE OF SYMMETRIC MATTER

Equation of state for symmetric nuclear matter

- infinite symmetric nuclear matter $N=Z$
- ground state properties: $\rho_0 = 0.16 \text{ N/fm}^3$ and $E(\rho_0) = -16 \text{ MeV}$
- expansion in density:

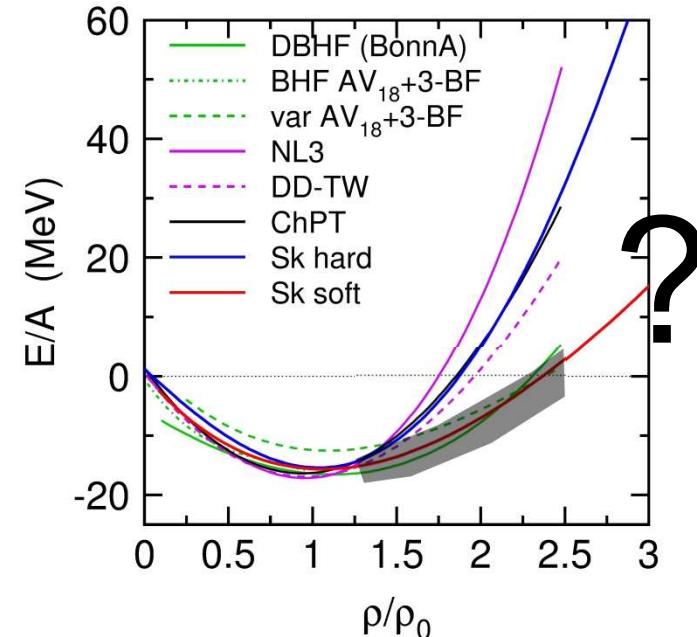
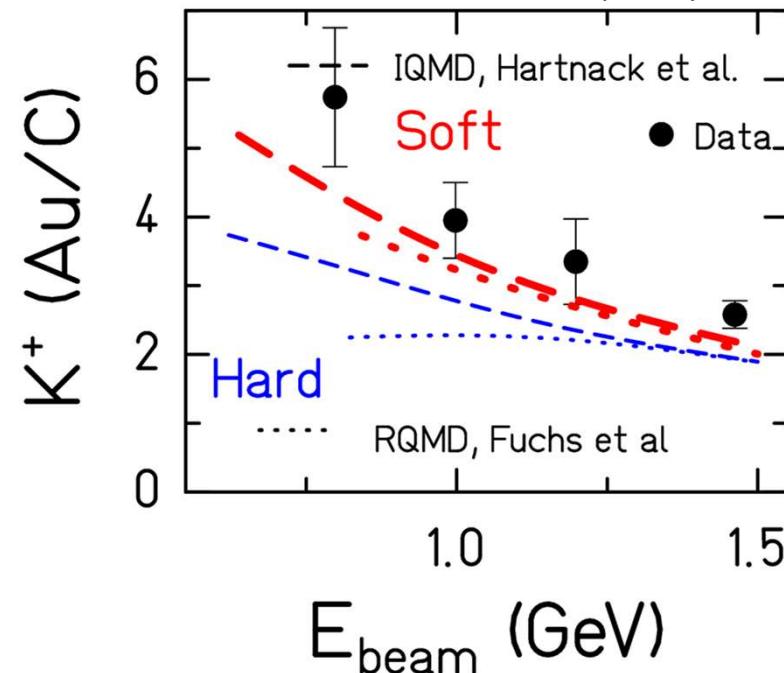
$$E(\rho, T = 0, \delta = 0) = E_0 + \frac{K}{18\rho^2} (\rho - \rho_0)^2 + \dots$$



J. Piekarewicz, PRC 69 (04) 041301,
RMF: $K=248 \text{ MeV}$
G. Colò et al., PRC 70 (04) 024307
Skyrme HF: $K=230 \text{ MeV}$
S. Shlomo et al. Eur. Phys. J. A 30, 23 (06)
 $K=240\pm 20 \text{ MeV}$
D.H. Youngblood et al., PRC 80, 064318 (09):
 $K=231\pm 5 \text{ MeV}$

Compressibility of symmetric nuclear matter: Kaon production

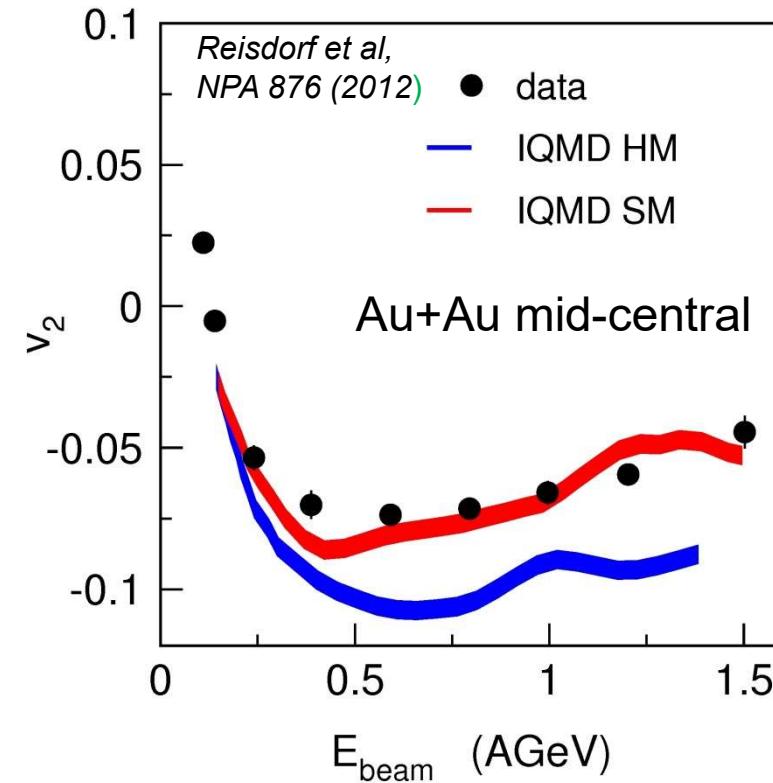
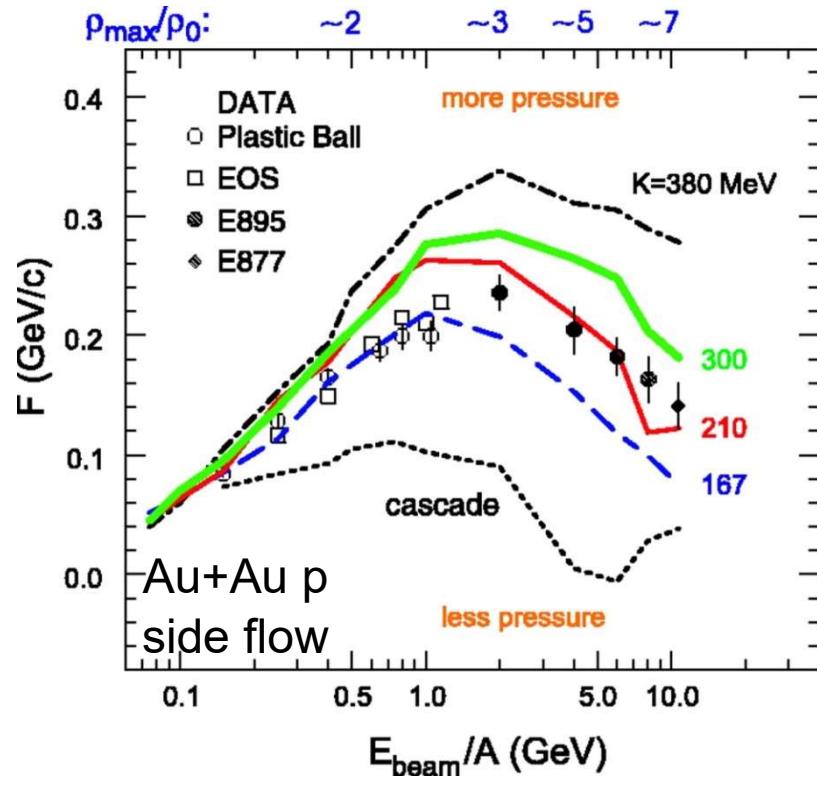
C. Sturm et al., PRL 86 (01) 39
Ch. Hartnack et al., PRL 96 (2006) 012302



- Kaon yield
 - ~ density reached
 - ~ compressibility
- robust observable
 - independent on model ingredients

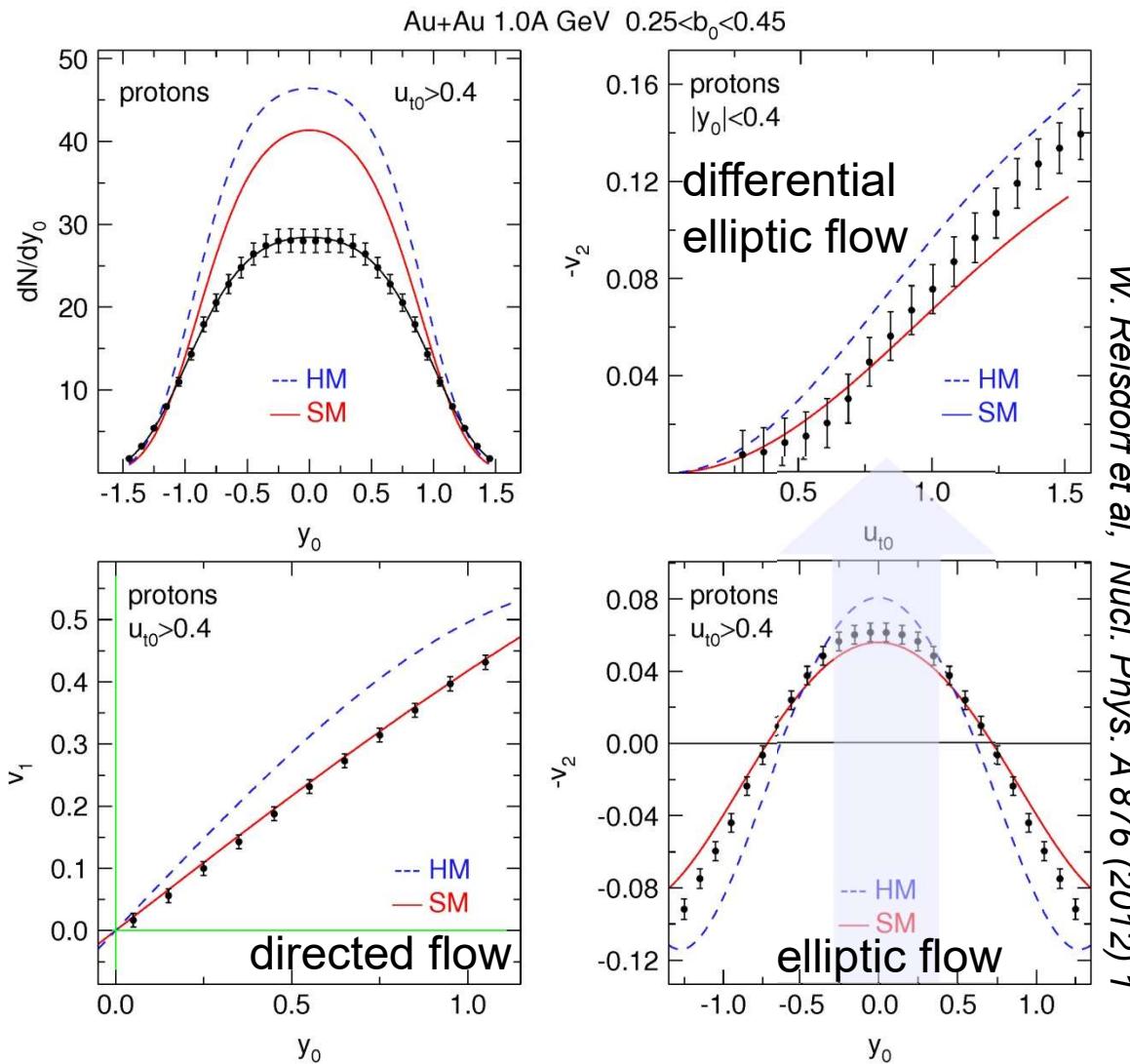
- sensitivity to compressibility
- largest below threshold
- relevant density $\sim 2\rho_0$

Flow sensitive to pressure built up during reaction



- “additional constraints needed on momentum dependence of NN potential and in-medium cross sections”
- newer (FOPI) data on elliptic flow in agreement with a soft EOS (SM)
 - available heavy ion reaction (FOPI) data in this energy regime including Kaon production is reasonably described by this model (input parameters constrained with experimental data)

Collective flows in Au+Au at 1.0A GeV



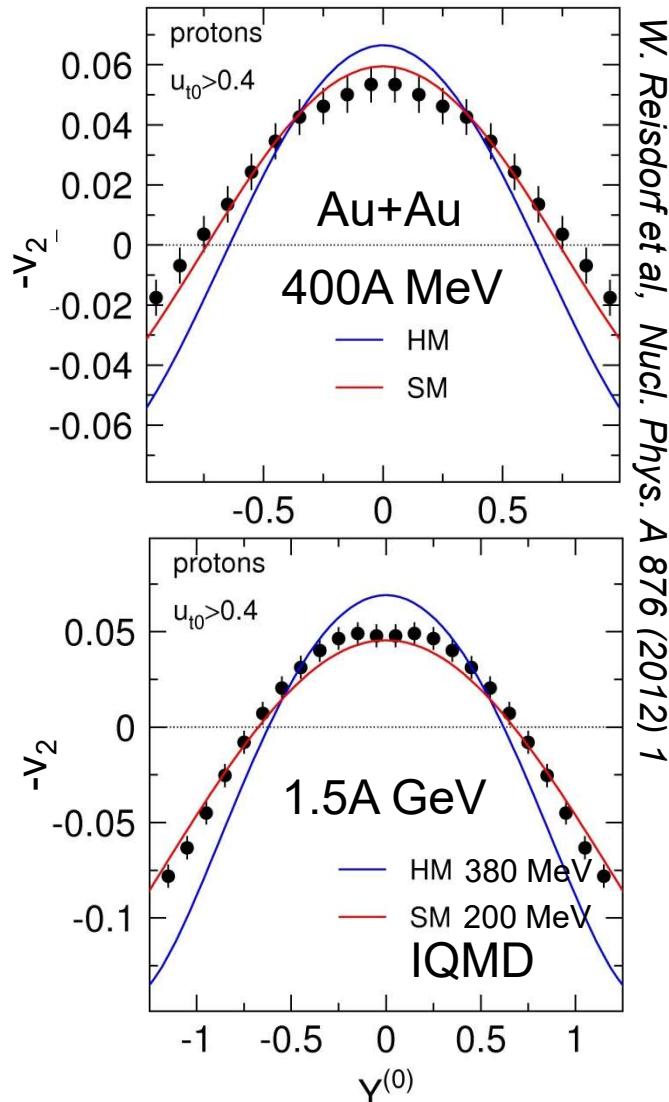
All flow results

- Au+Au 0.4 – 1.5AGeV
- Ru+Ru/Zr+Zr
- directed flow
- elliptic flow
- protons
- d, t, ^3He , α

reasonably well described
by IQMD transport code
employing a **soft EOS for symmetric matter**

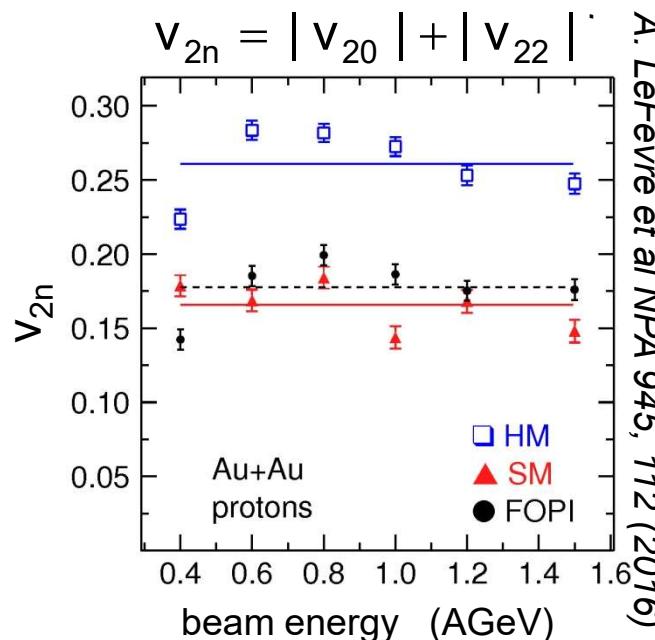
IQMD, C. Hartnack et al.
EPJA1 (1997) 151

Elliptic flow at energies 0.25-1.5 AGeV



Parametrization of shape:

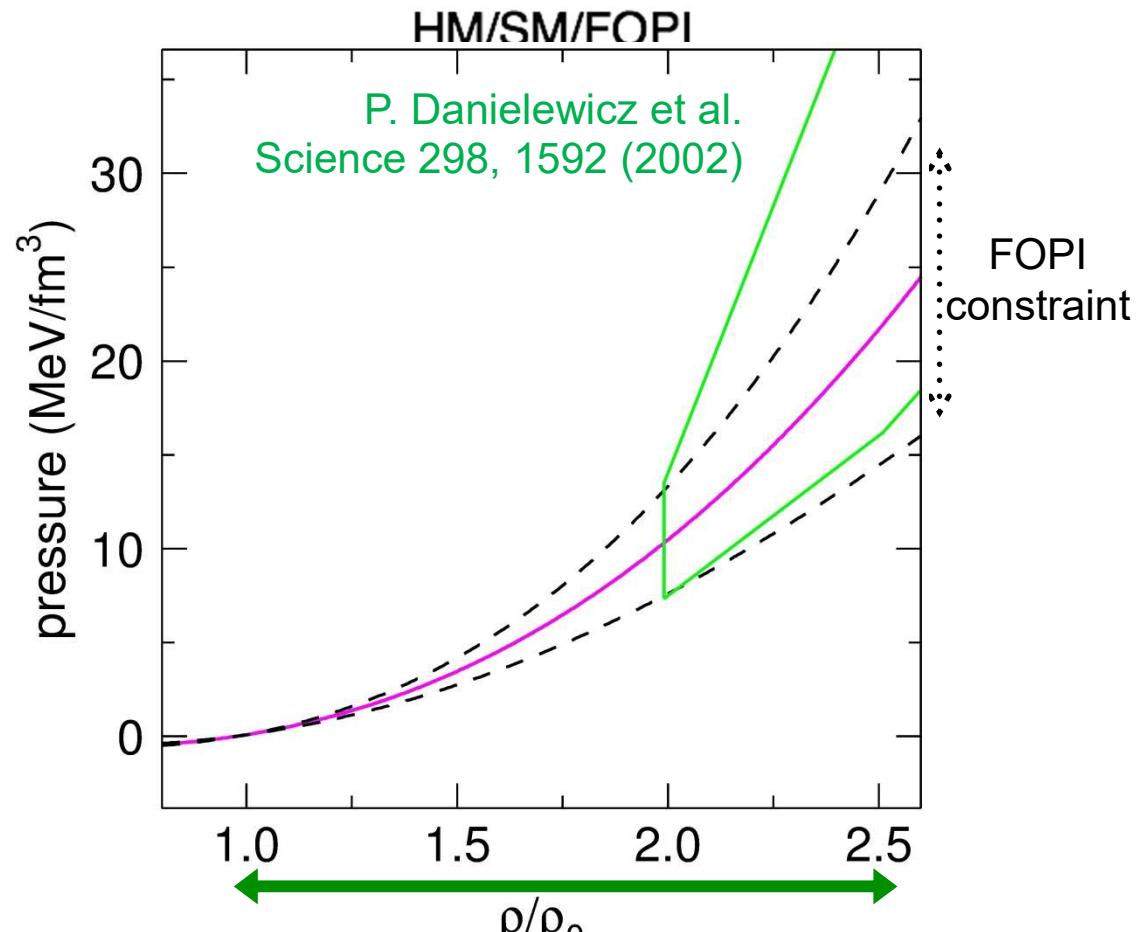
$$v_2(Y^{(0)}) = v_{20} + v_{22} \cdot Y^{(0)2}$$



- sensitive to EOS over a large energy range
- $v_{2n}(E_{\text{beam}})$ varies by a factor $\approx 1.6 >>$ measured uncertainty (≈ 1.1)
- relevant density range $\rho \simeq (1 - 3) \rho_0$
- extracted compressibility $K=190 \pm 30$ MeV

Resulting constraint

- phenomenological EOS
HM and SM include the saturation point at $\rho/\rho_0 = 1$,
 $E/A = -16$ MeV by construction,
fixes the absolute position of the curves:
- the heavy ion data are only sensitive to the shape, i.e. the pressure (derivative).
- a stiff EOS, characterized by $K_0 = 380$ MeV is not in agreement with flow data in the incident energy range 0.4 - 1.5 A.GeV.



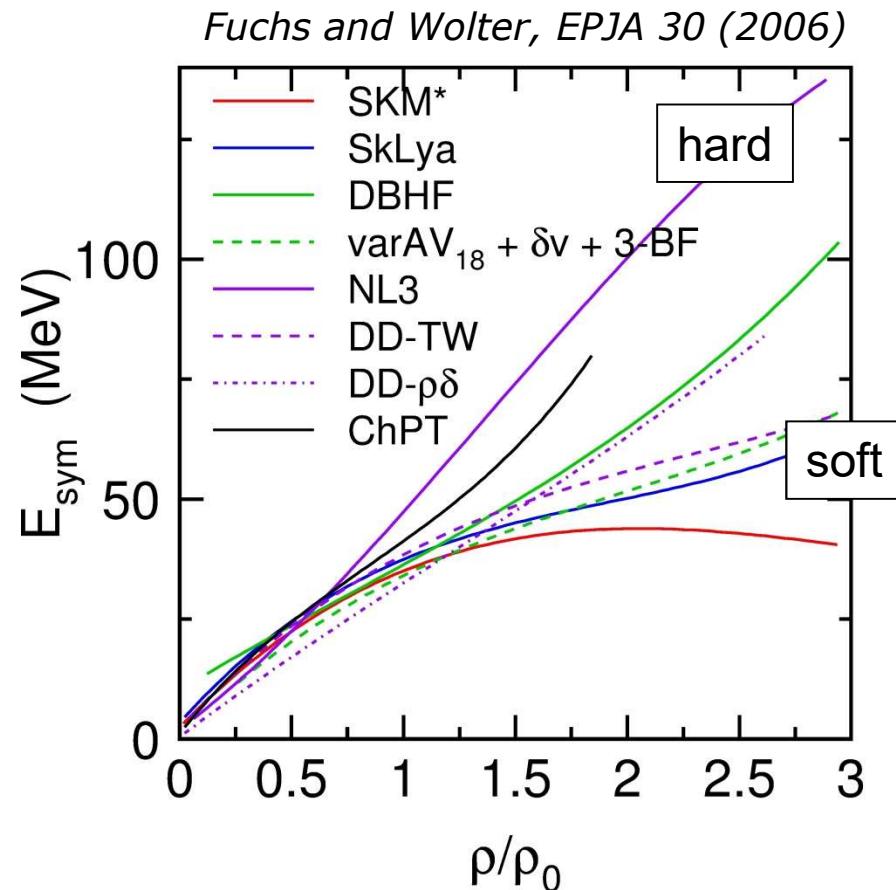
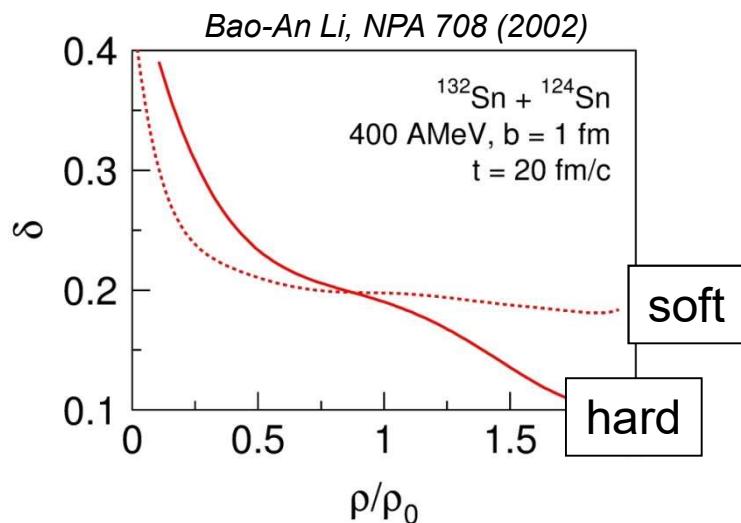
A. LeFevre et al NPA 945, 112 (2016)

SYMMETRY ENERGY

Symmetry energy

$$E_{\text{sym}}(\rho) = E_{\text{sym},0} + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{\text{sym}}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2 + \dots$$

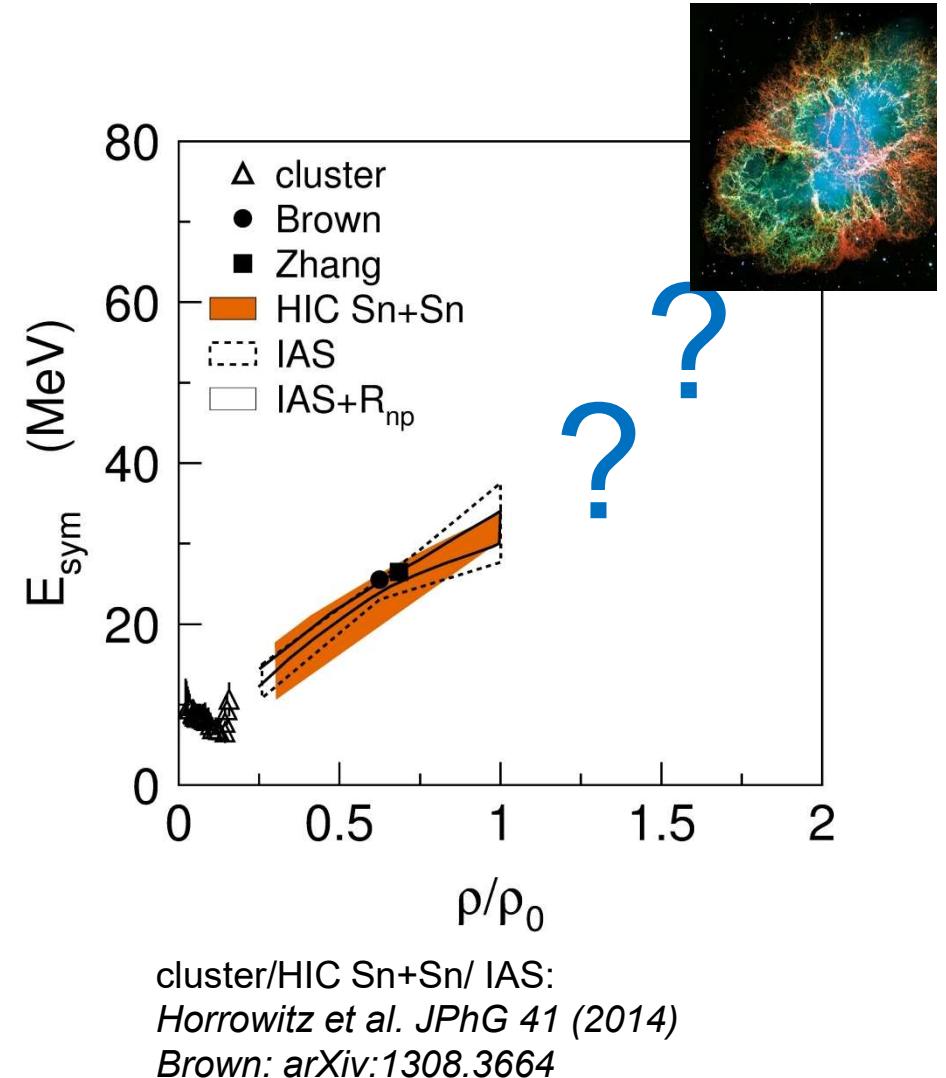
Largely unconstrained at high densities → related to uncertainty of three-body and tensor forces at high density



Symmetry energy

Sensitive observables that are or will be more extensively explored :

- neutron stars...
- masses
 - Isobaric Analog States (IAS)
- neutron skins
 - scattering with electrons, anti-protons
 - excitation of nuclei: Pygmy resonances, dipole polarizability...
 - neutron removal cross section
- cluster formation at low densities
- fragmentation of nuclei
- isospin diffusion und isospin drift between nuclei of different N/Z in peripheral HIC
- neutron/proton, $t/{}^3\text{He}$ spectra and collective flows
- π^-/π^+ multiplicities and spectra



Symmetry energy at supra-normal densities

Differential elliptic flow v_2 of n/p

UrQMD* (Q. Li et al.) predicts

"hard" E_{sym} protons unchanged
"soft" E_{sym} neutron and proton flow inverted

Towards model invariance:

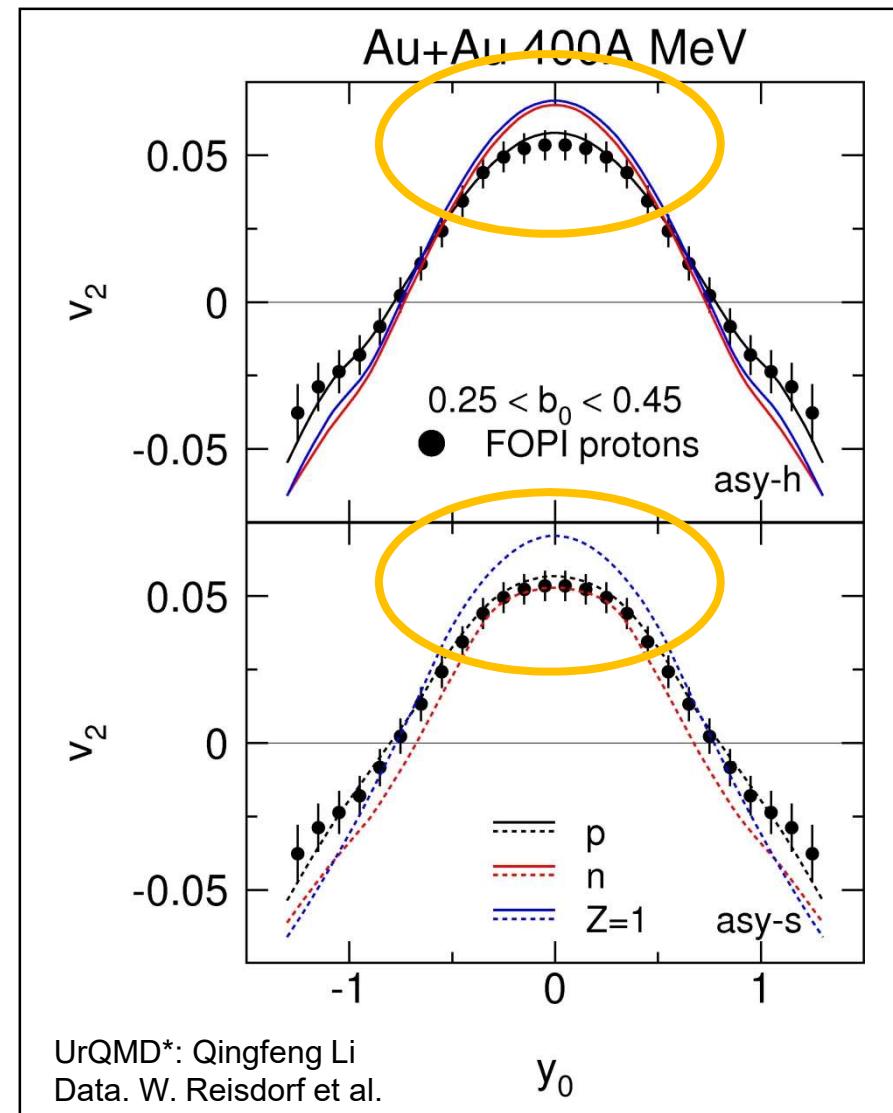
tested stability with different models:

- soft vs. hard EOS **190 < K < 280 MeV**
- density dependence of $\sigma_{\text{NN,elastic}}$
- asymmetry dependence of $\sigma_{\text{NN,elastic}}$
- optical potential
- momentum dependence of isovector potential

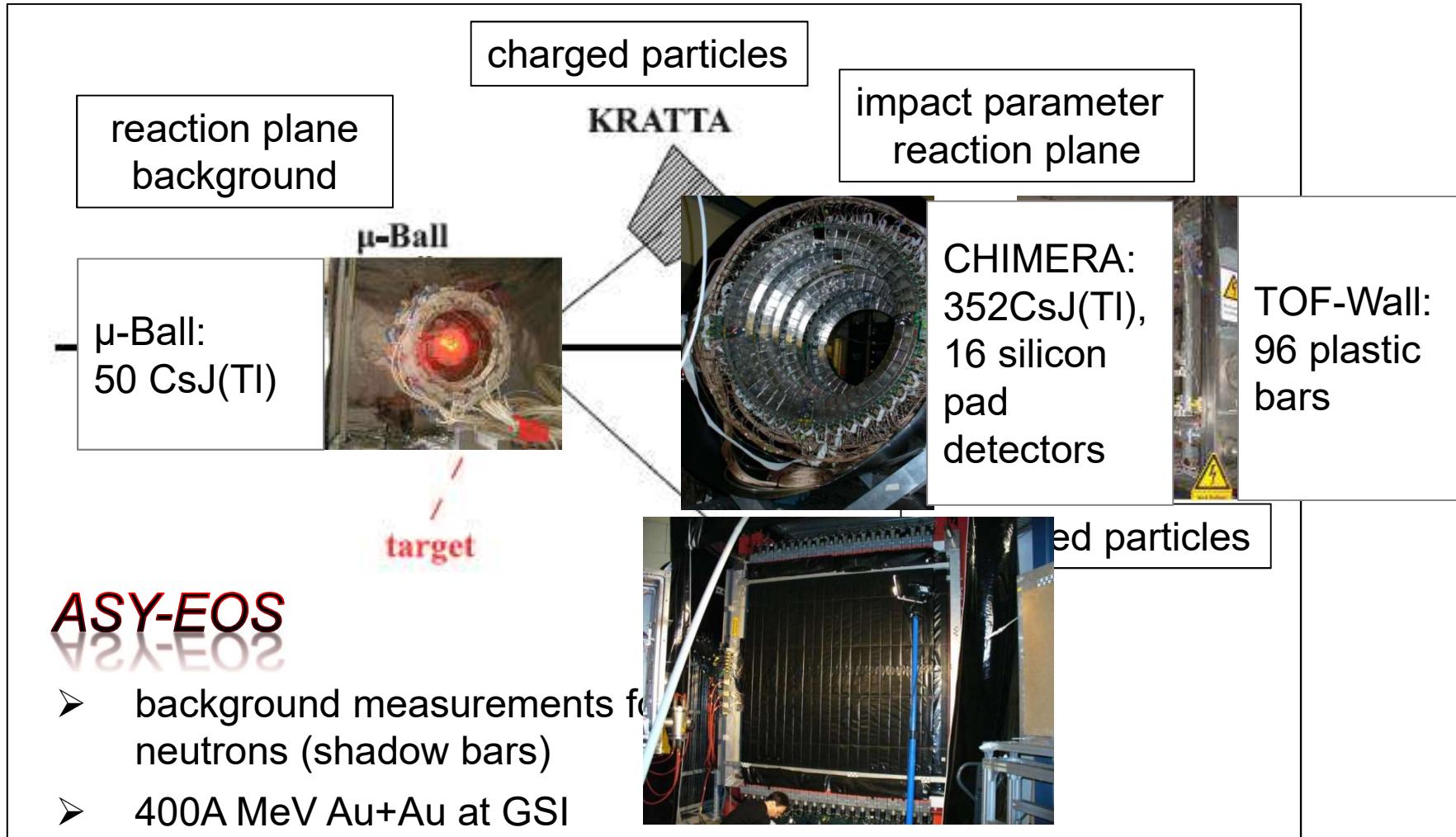
M.D. Cozma et al., arXiv:1305.5417

P. Russotto et al., PLB 267 (2010)

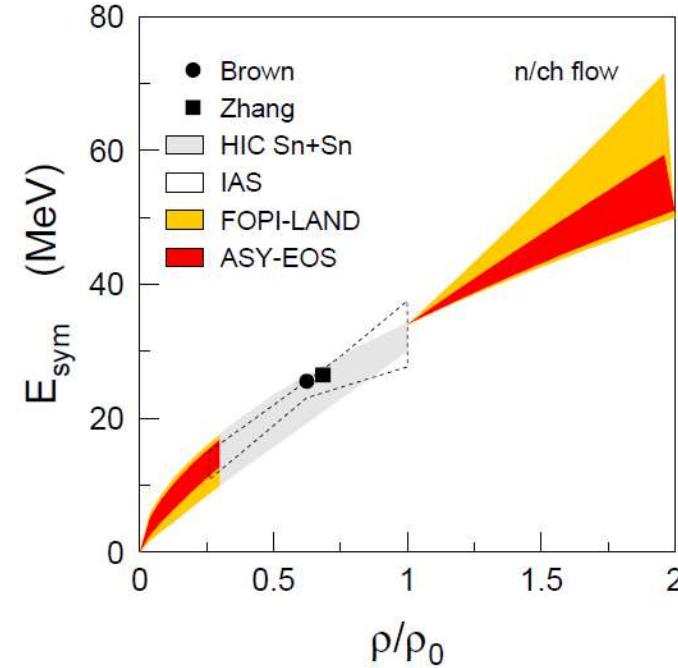
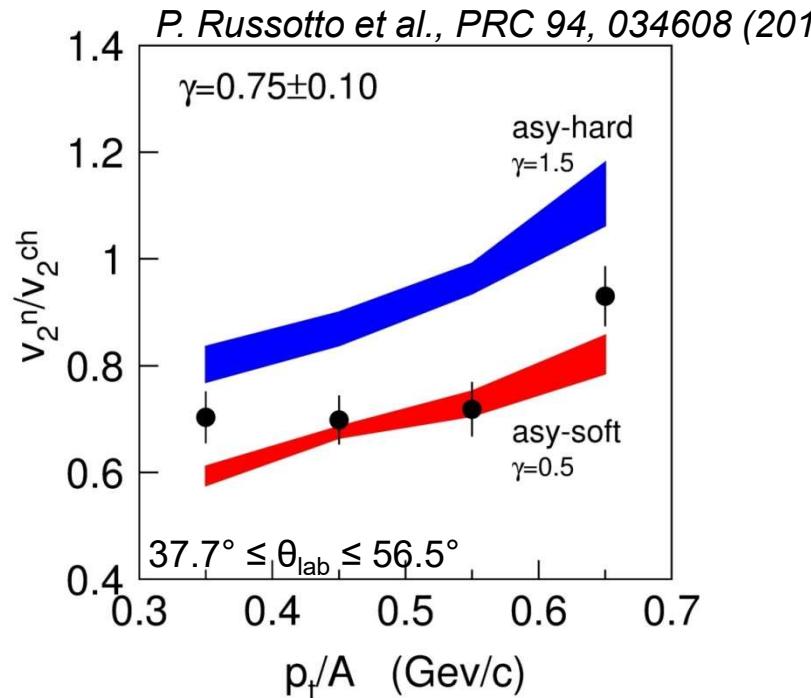
Y. Wang et al., PRC 89, 044603 (2014)



ASY – EOS Experiment

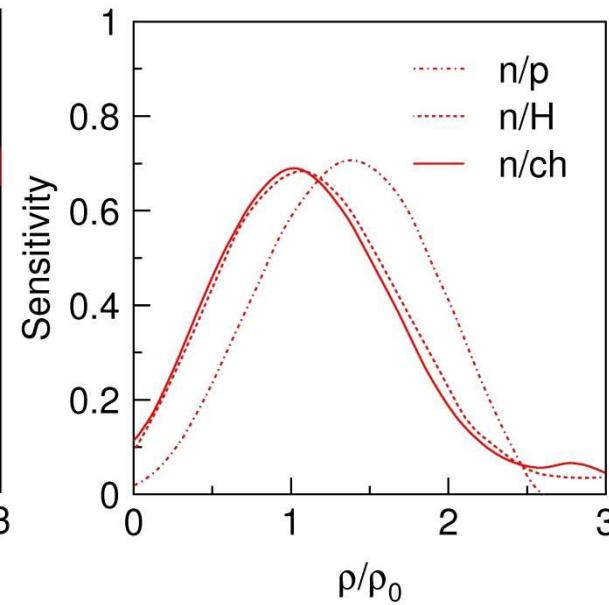
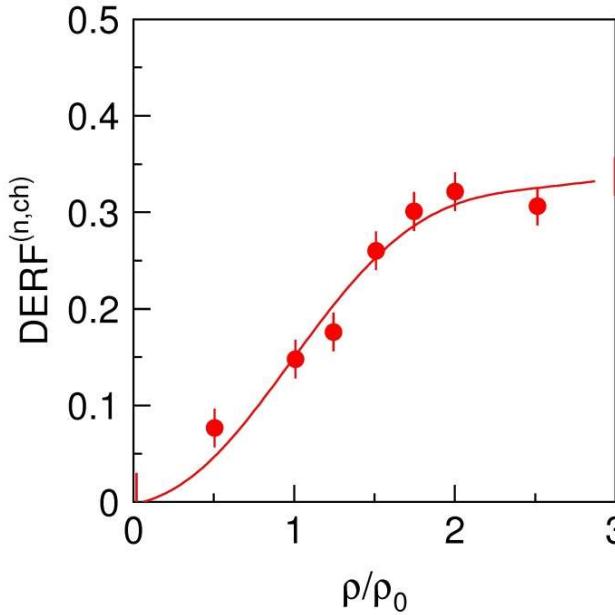
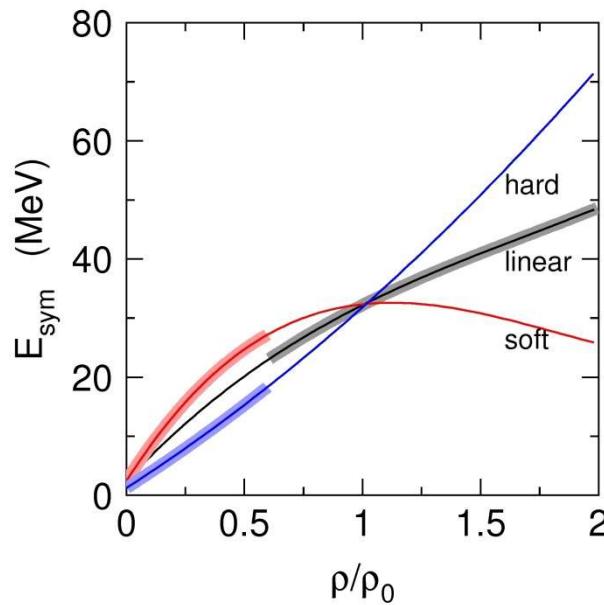


Elliptic flow ratio of neutrons and charged particles



- parametrization for SE used in UrQMD* model:
$$E_{\text{sym}} = E_{\text{sym}}^{\text{pot}} + E_{\text{sym}}^{\text{kin}} = 22 \text{ MeV} \cdot (\rho/\rho_0)^\gamma + 12 \text{ MeV} \cdot (\rho/\rho_0)^{2/3}$$
- systematic errors corrected: $\gamma = 0.72 \pm 0.19$
- slope parameter: $L = 72 \pm 13 \text{ MeV}$, $E_{\text{sym}}(\rho_0) = 34 \text{ MeV}$
- slope parameter: $L = 63 \pm 11 \text{ MeV}$, $E_{\text{sym}}(\rho_0) = 31 \text{ MeV}$

Extracting relevant density range



P. Russotto et al., PRC (2017)

- deducing density where the difference between neutron and charged particle flow is originating from by using transport models

$$\text{DERF}^{(n,Y)}(\rho) = \frac{v_2^n}{v_2^Y}(\text{hard}, \rho) - \frac{v_2^n}{v_2^Y}(\text{soft}, \rho)$$

- DERF: difference in elliptic flow ratios for two different $S(\rho)$
 - at large ρ full splitting
 - sensitivity is given by the derivative of DERF

Pion production as probe

- symmetry energy influences n/p ratio → nn, np, pp collisions

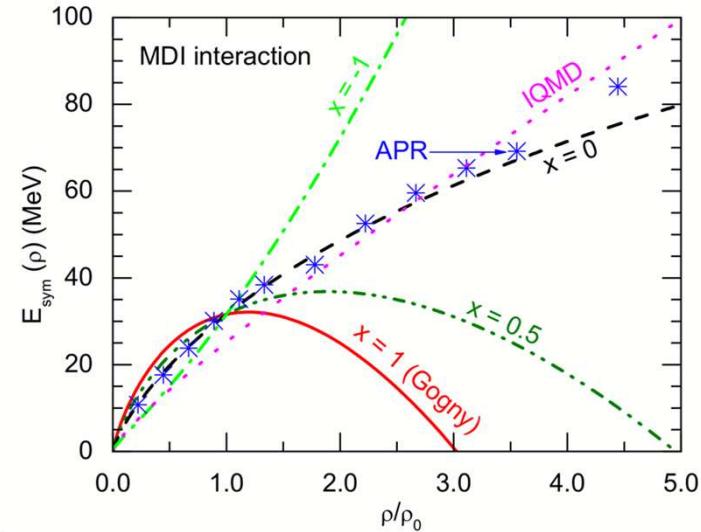
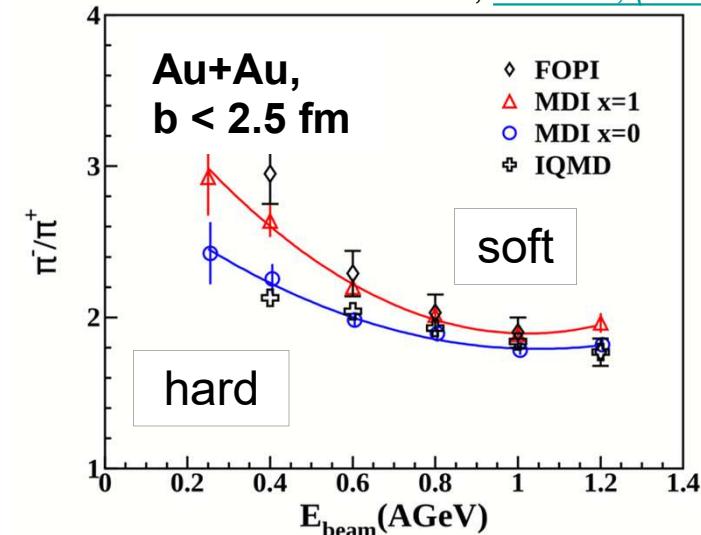
$$\text{hard SE} \quad \frac{n}{p} \downarrow \Rightarrow \frac{Y(\Delta^{0,-})}{Y(\Delta^{+,++})} \downarrow \Rightarrow \frac{\pi^-}{\pi^+} \downarrow$$

- But in the nuclear medium
 - pion optical potential, self energies, different for π^- and π^+
 - production via Δ resonances, potential
 - s- vs p-wave production
- π^-/π^+ ratio: interpretation model dependent

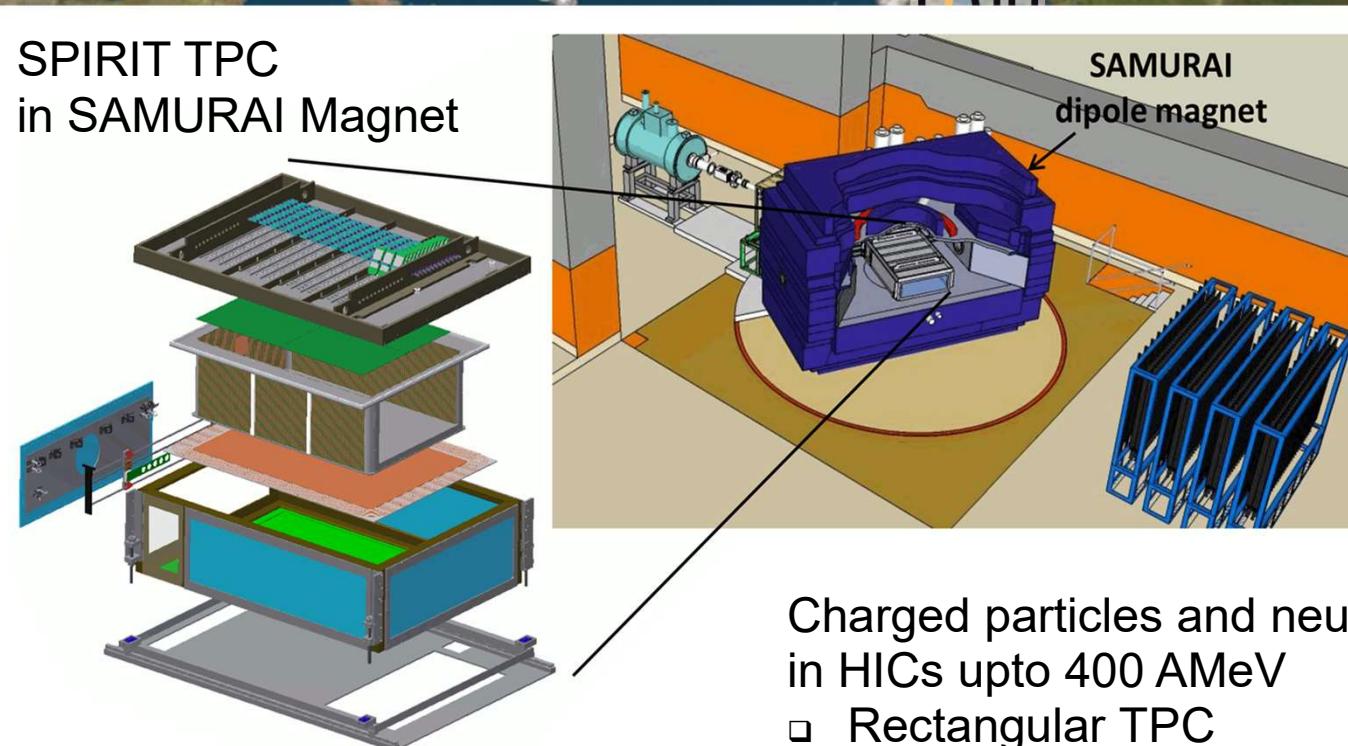
$$\text{hard SE} \quad \Rightarrow \frac{\pi^-}{\pi^+} ?$$

- measure double ratio $(\pi^-/\pi^+)^{\text{n-rich}} / (\pi^-/\pi^+)^{\text{p-rich}}$
 ${}^{132}\text{Sn} + {}^{124}\text{Sn} / {}^{108}\text{Sn} + {}^{112}\text{Sn}$

Data: W. Reisdorf et al., NPA 781 (2007)
 Calculations: Z. Xiao et al, [PRL 102, \(2009\)](#)



Measuring pion production with radioactive beams



SPIRIT TPC
in SAMURAI Magnet

SAMURAI
dipole magnet

RAON

RIKEN
NISHINA
CENTER

Charged particles and neutrons
in HICs upto 400 AMeV

- Rectangular TPC
- With 12000 pads in x-z direction
- Active target option
- Inside a magnet (\rightarrow charged pions)
- Neutron detector

Yvonne Leifels - EMMI RRTF Symposium
2018

SYMMETRY ENERGY AT HIGHER DENSITIES

Symmetry energy at higher densities

Higher density → higher beam energy

Elliptic flow ratio of n and p

Sensitivity decreasing at higher beam energies but still existing

NEW ASY-EOS “proposal”:

Study of

**AuAu, $^{112}\text{Sn}+\text{Sn}$, $^{132}\text{Sn}+\text{Sn}$
400 and 900 AMeV**

measure Neutrons/protons:

NeuLAND@R³B

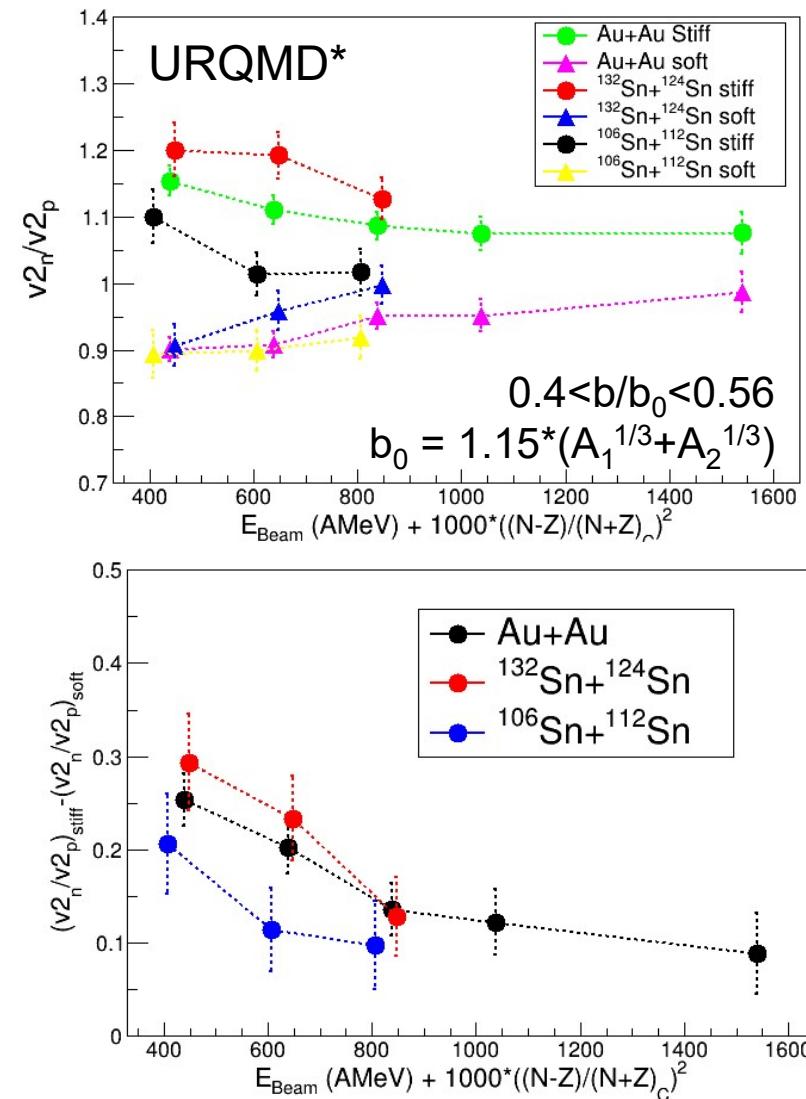
charged particles:

Kratta, Califa@R³B

impact parameter vector:

FOPI Plawa , Krakow Barrel

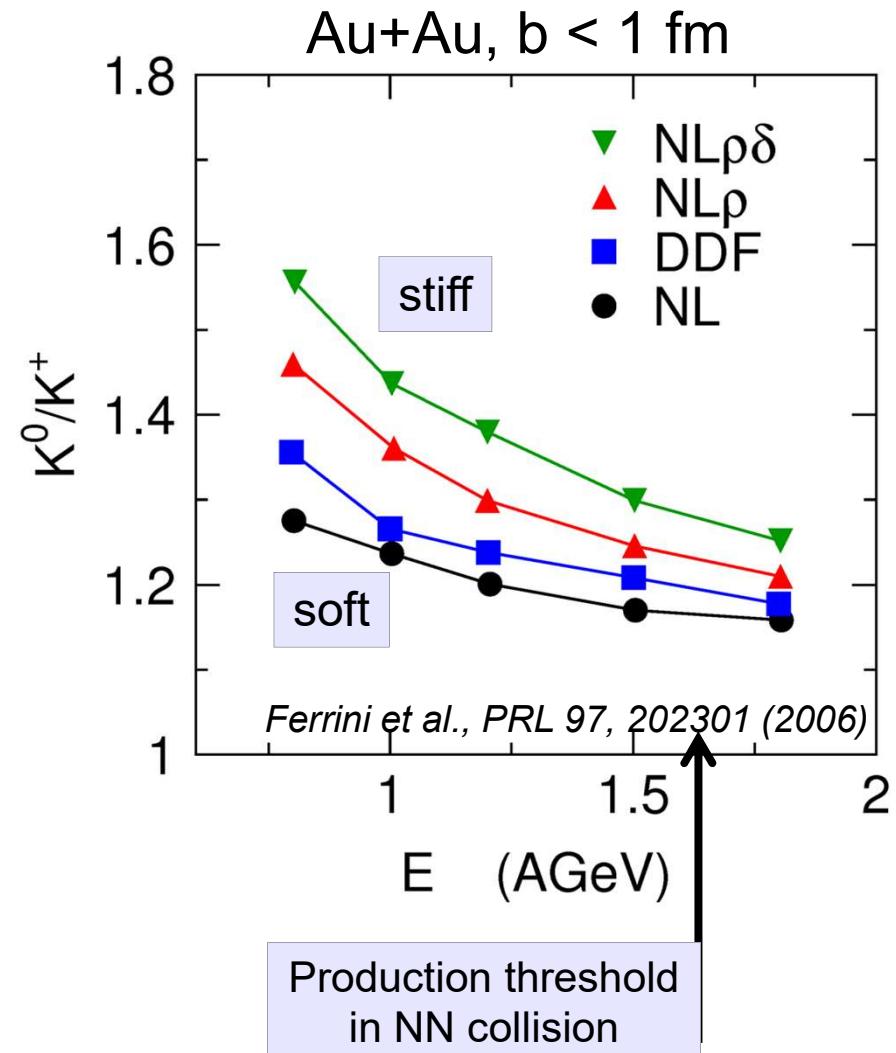
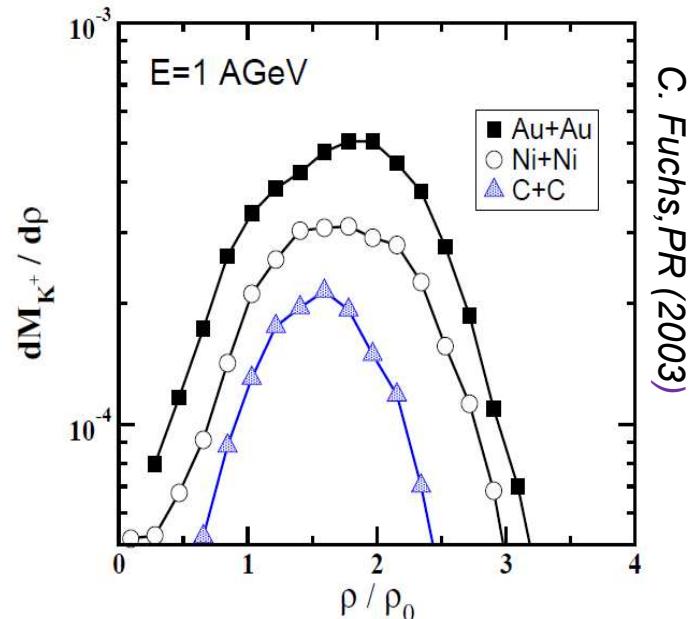
positive response from PAC



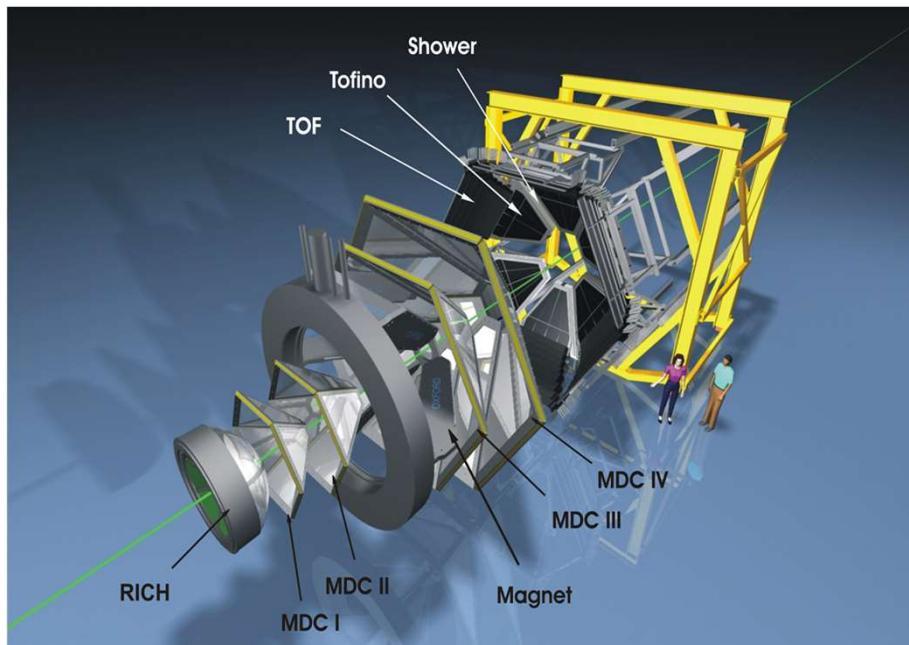
Kaon production

Kaons

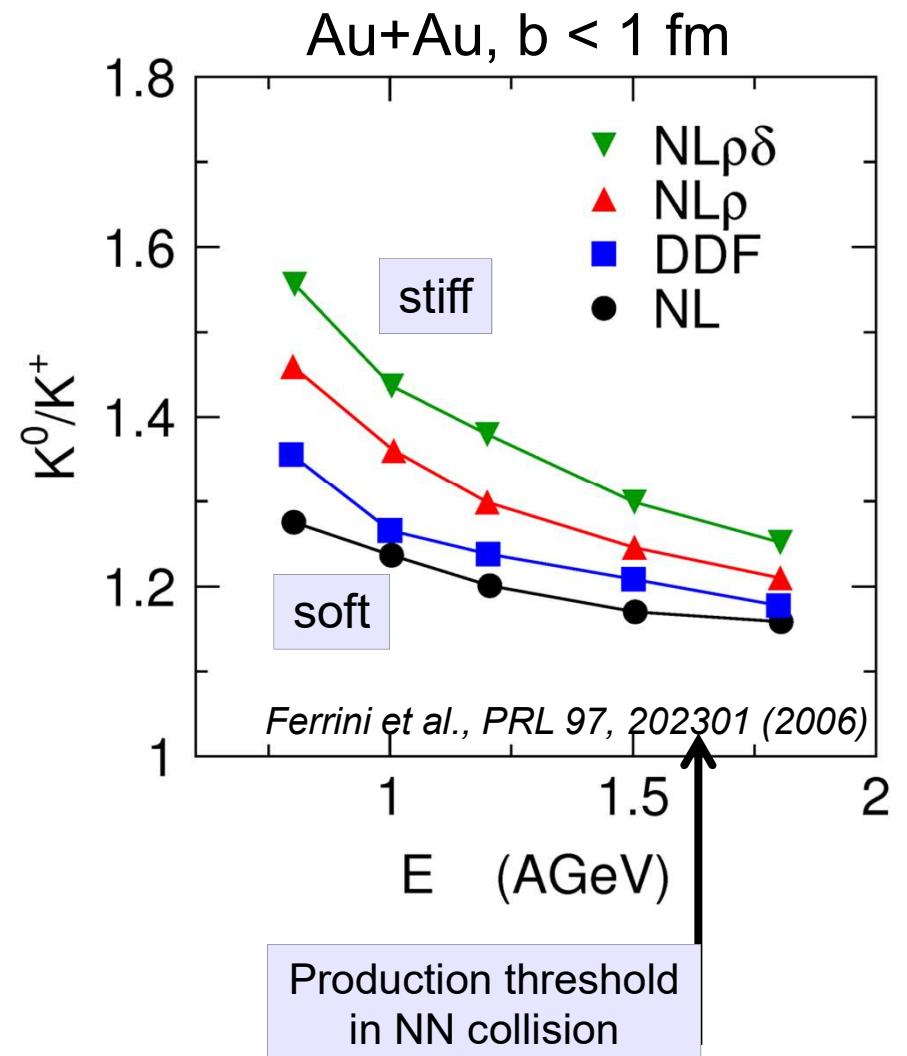
- subthreshold production is sensitive to density
- weakly interacting with medium, long mean free path
- early freeze-out
- but model dependence of pion ratio have to solved first



Kaon production (HADES)

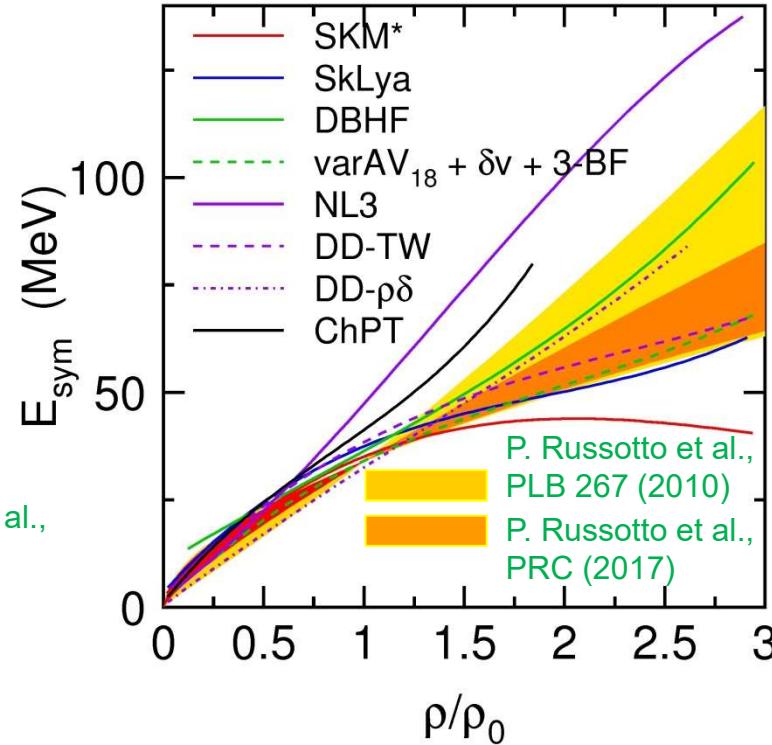
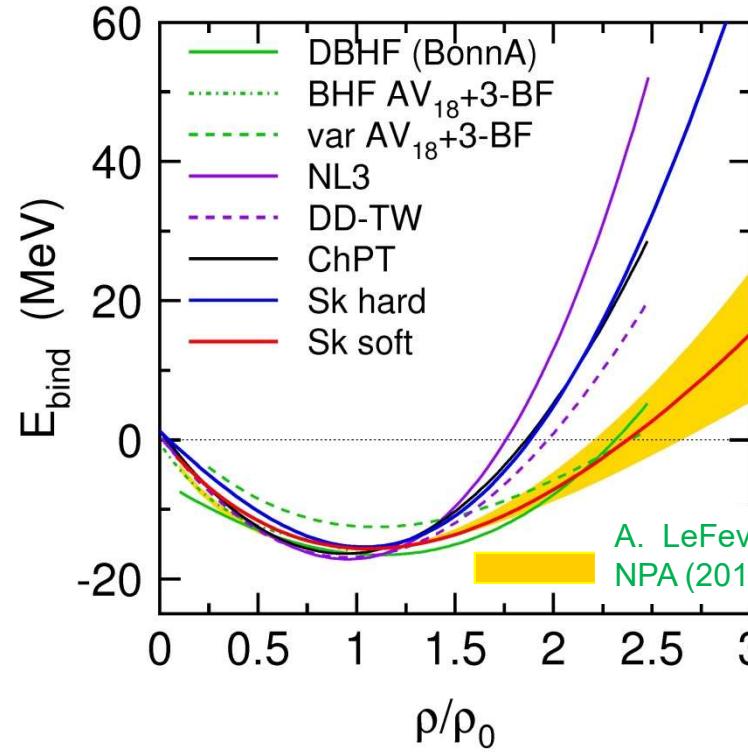


- Full azimuthal coverage, 18 to 85° in polar angle
- Hadron and lepton identification
- Event-plane reconstruction
- K^0/K^+ ratio at < 1 AGeV



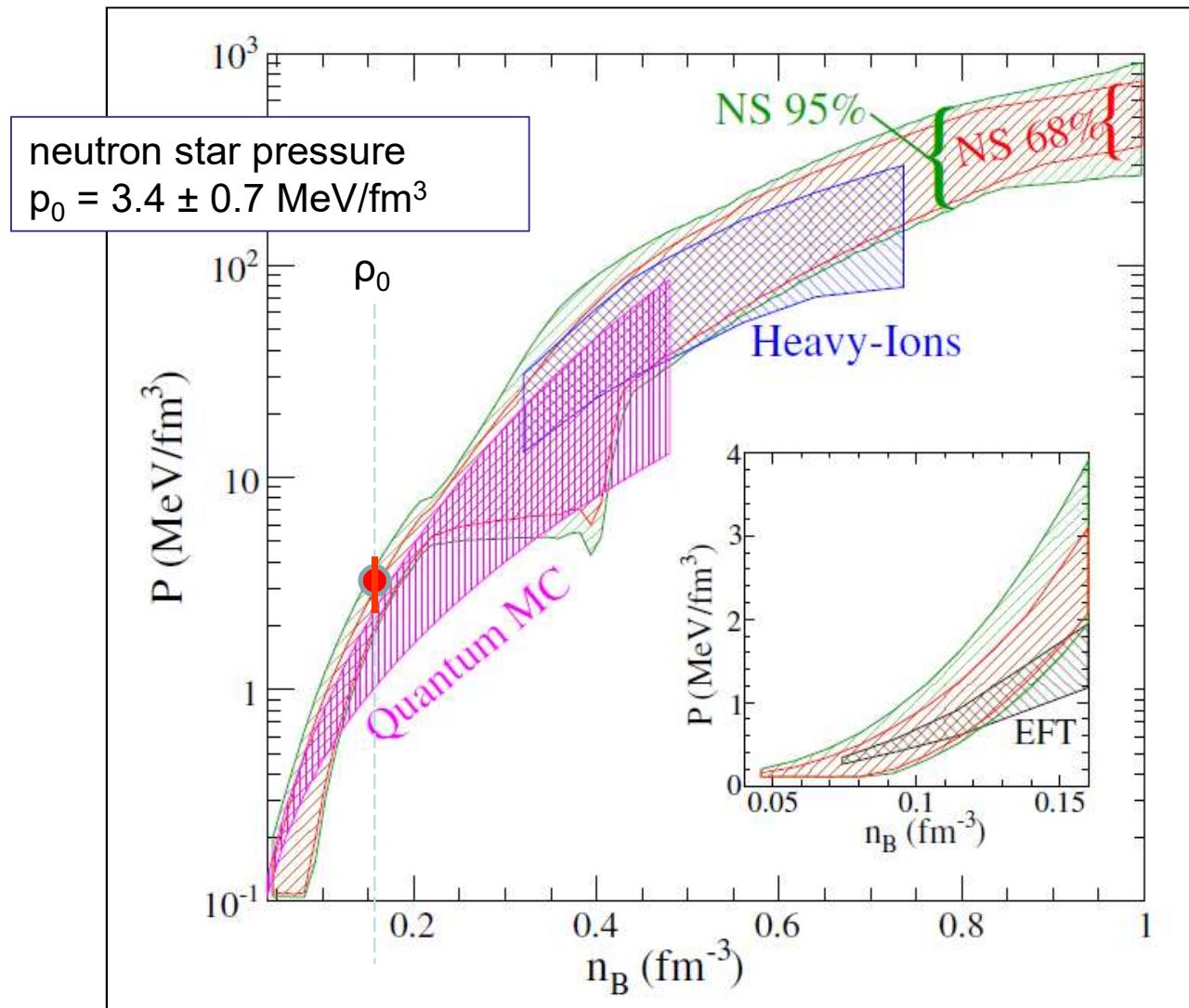
CONCLUSION AND OUTLOOK

Summary



- equation of state of symmetric nuclear matter from comparison of FOPI data with IQMD
- the symmetry energy as extracted from ASY-EOS results with UrQMD*

Symmetry pressure $p_0 = 3.8 \pm 0.7 \text{ MeV/fm}^3$



Steiner, Lattimer, and Brown, ApJ 765, L5 (2013)

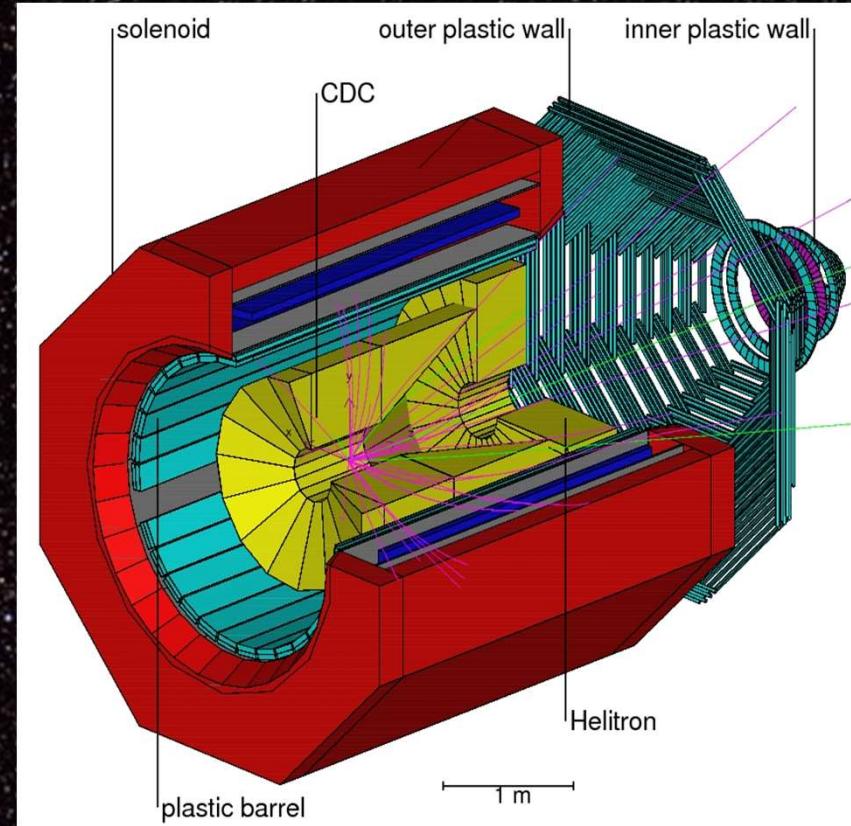
Conclusions

- Kaon production and charged particle flow give consistent constraints on the symmetric part of the EOS
 - soft $\kappa = \text{MeV}$
 - models „benchmarked“ with existing data
- Extension to higher densities (i.e. energies needed) to improve constraints, AGS data needs extension → BM@N, CBM
- symmetry energy at intermediate densities can be constrained
- very few measurements have been done
 - n/p/ or n/charged particle flow in Au+Au
 - pion production in Au+Au
- one needs robust observable
 - largely model invariant
 - ratios or double ratios
- n/proton studies at higher energies and radioactive beams
 - submitted letter-of-intent to GSI for beam in 2019/20
- **Close collaboration between experiments and theory important**

The FOPI collaboration

A. Andronic, R. Averbeck, Z. Basrak, N. Bastid,
M.L. Benabderramahne, M. Berger, P. Bühler,
R. Caplar, M. Cagnelli, M. Ciobanu, P. Crochet, I.
Deppner, P. Dupieux, M. Dzelalija, L. Fabbietti, J.
Frühauf, F. Fu, P. Gasik, O. Hartmann,
N. Herrmann, K.D. Hildenbrand, B. Hong,
T.I. Kang, J. Keskemeti, Y.J. Kim, M. Kis,
M. Kirejczyk, R. Münzer, P. Koczon, M. Korolija, R.
Kotte, A. Lebedev, K.S. Lee, Y. Leifels,
A. LeFevre, P. Loizeau, X. Lopez, M. Marquardt, J.
Marton, M. Merschmeyer, M. Petrovici,
K. Piasecki, F. Rami, V. Ramillien, A. Reischl, W.
Reisdorf, M.S. Ryu, A. Schüttauf, Z. Seres,
B. Sikora, K.S. Sim, V. Simion,
K. Siwek-Wilczynska, K. Suzuki, Z. Tyminski, J.
Weinert, K. Wisniewski, Z. Xiao, H.S. Xu,
J.T. Yang, I. Yushmanov, V. Zimnyuk, A. Zhilin, Y.
Zhang, J. Zmeskal

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Moscow, Russia, LPC Clermont-Ferrand, France,
Korea University, Seoul, Korea, GSI Darmstadt,
Germany, IReS Strasbourg, France, FZ Rossendorf,
Germany, Univ. of Heidelberg, Germany, Univ. of
Warsaw, Poland, RBI Zagreb, Croatia, IMP Lanzhou,
China, SMI Vienna, Austria, TUM, Munich, Germany,
T.Yamazaki(RIKEN)



and to the ASYEOS collaboration

authors of proposal 2009

Co-Spokespersons: R.C. Lemmon¹ and P. Russotto²

List from the Proposal

Collaboration

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