

# Nuclear physics impact on *r*-process and kilonovae

Meng-Ru Wu (Institute of Physics, Academia Sinica)

EMMI Rapid Reaction Task Force: The physics from neutron star  
mergers at GSI/FAIR

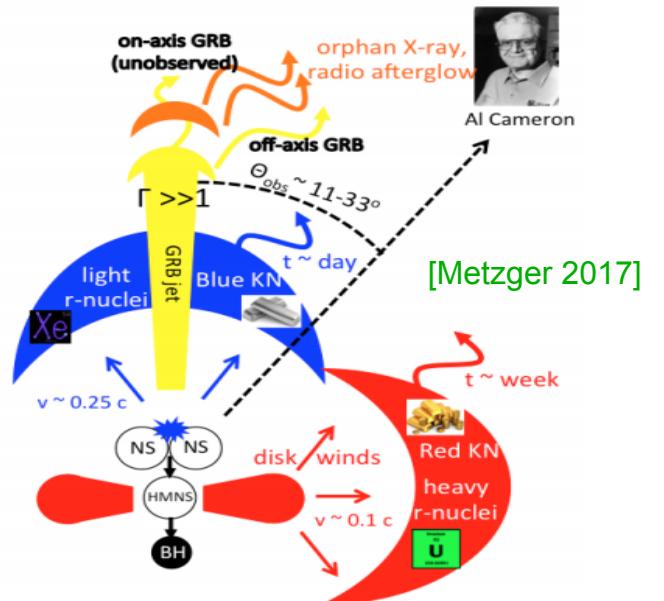
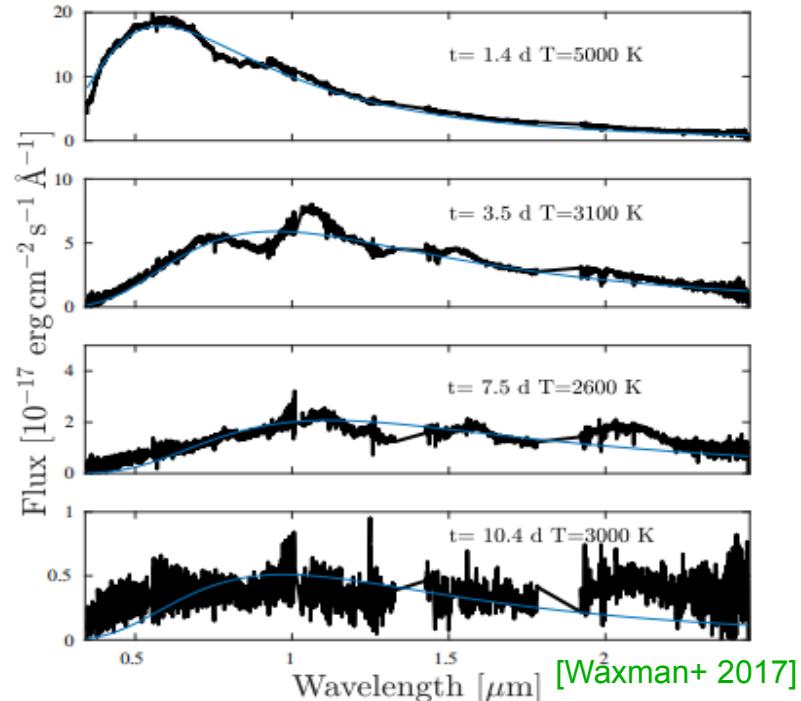
June 04 – June 15, 2018, GSI, Darmstadt, Germany

# Neutron star merger and kilonova

The GW170817 follow-up optical/infrared observations strongly indicate kilonova being powered by the decay of the *r*-process nuclei

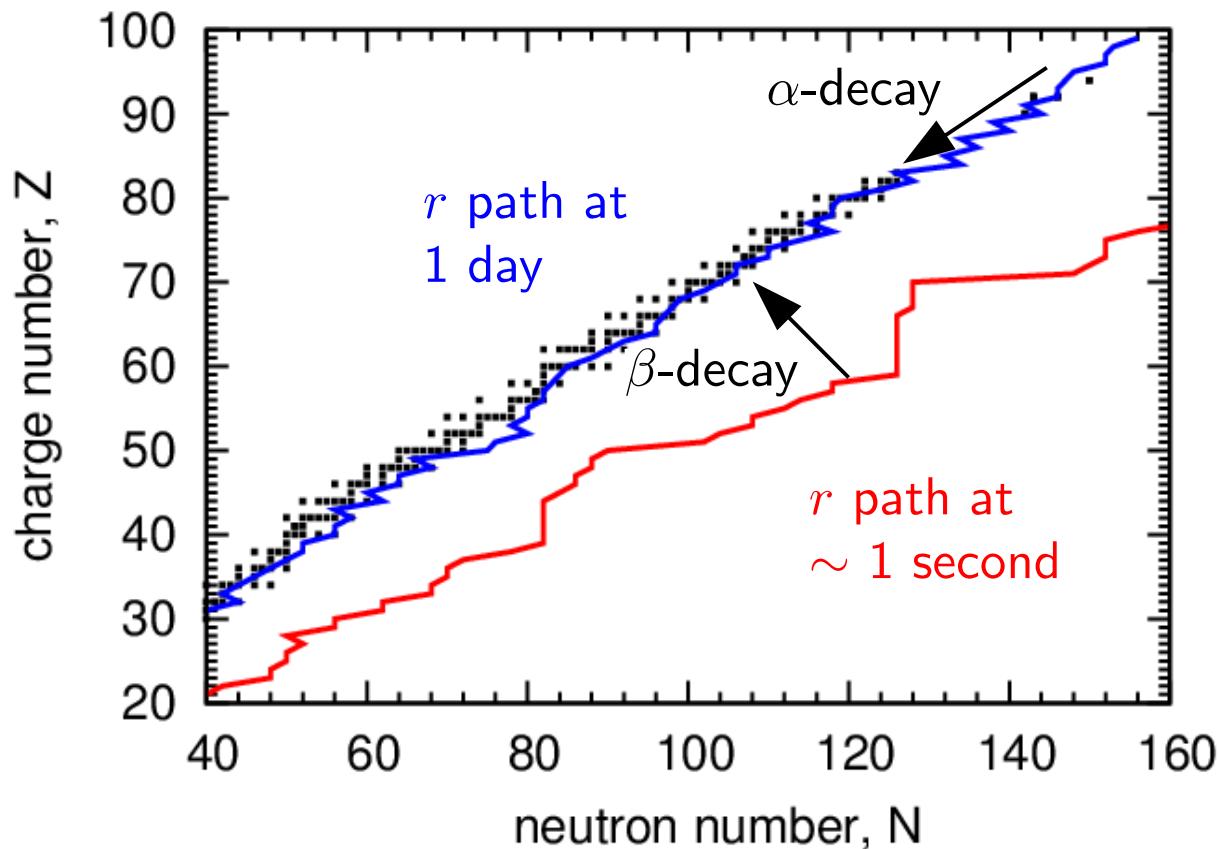
The kilonova lightcurve/spectra modeling depends on:

- ejecta mass/velocity
- opacity
- radioactive decay energy
- particle thermalization
- ...

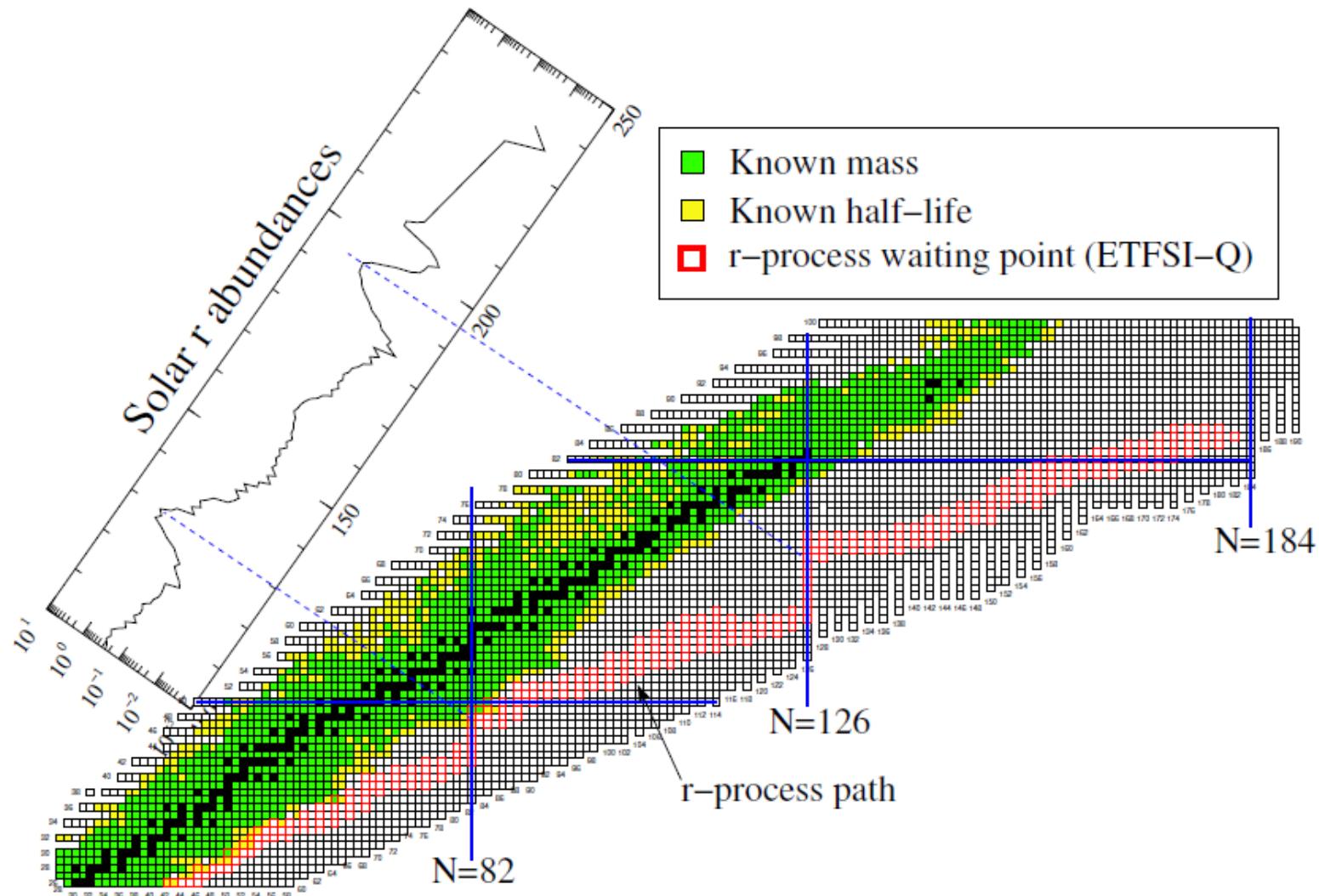


## Radioactive decay of the $r$ -process nuclei

The nuclear energy release from the radioactive decay of the  $r$ -process nuclei is the source powering the kilonovae [e.g., Arnett's law:  $L(t_{\text{peak}}) = \dot{\varepsilon}(t_{\text{peak}})$ ]



At  $\sim$  a day, the nuclear properties, e.g., the half-lives, the  $Q$ -value, are known. However, their abundances are determined by the initial astrophysical conditions and the unknown properties of the neutron-rich nuclei.



largely rely on theoretical nuclear physics inputs...

## nuclear masses

$(n, \gamma) \leftrightarrow (\gamma, n)$  equilibrium:

$$\frac{Y(Z, A + 1)}{Y(Z, A)} = n_n \left( \frac{2\pi\hbar^2}{m_u kT} \right)^{3/2} \left( \frac{A + 1}{A} \right)^{3/2} \frac{G(Z, A + 1)}{2G(Z, A)} \exp \left[ \frac{S_n(Z, A + 1)}{kT} \right]$$

along an isotopic chain, the abundance peaks at nucleus with neutron separation energy  $S_n \gtrsim S_n^0$

$$S_n^0(\text{MeV}) \approx \frac{T_9}{5.04} \left( 34.075 - \log n_n + \frac{3}{2} \log T_9 \right)$$

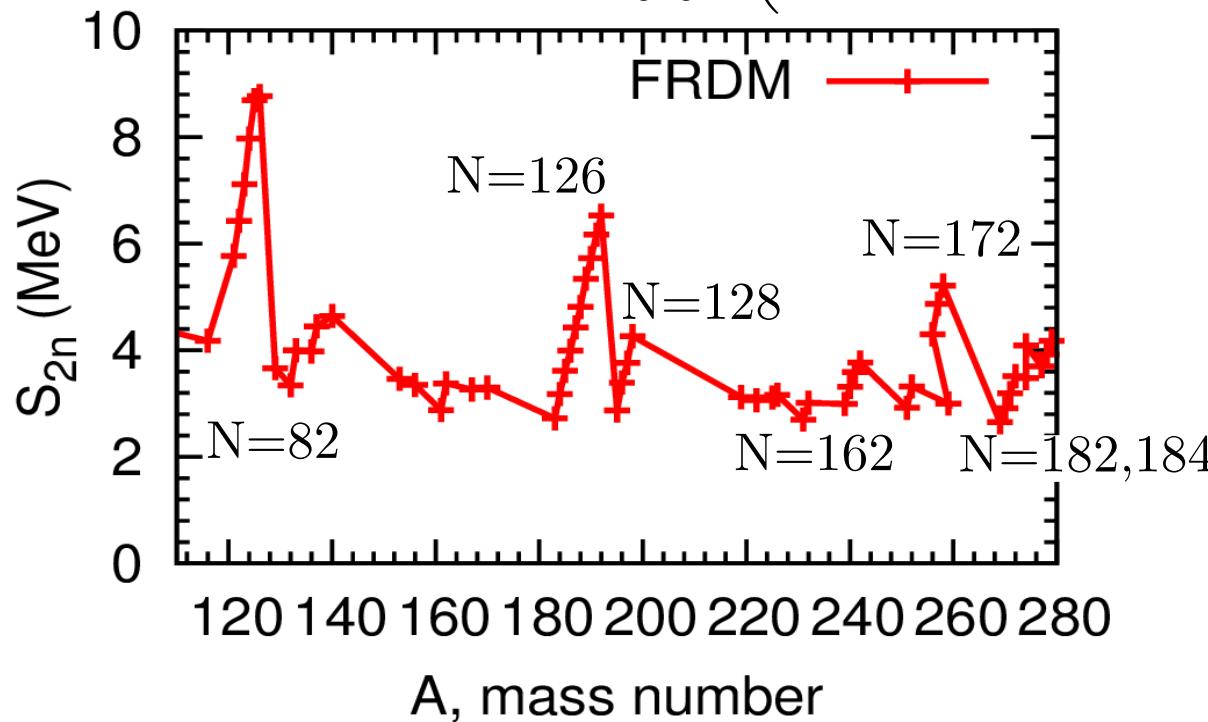
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$$R_{n/s} = 1$$

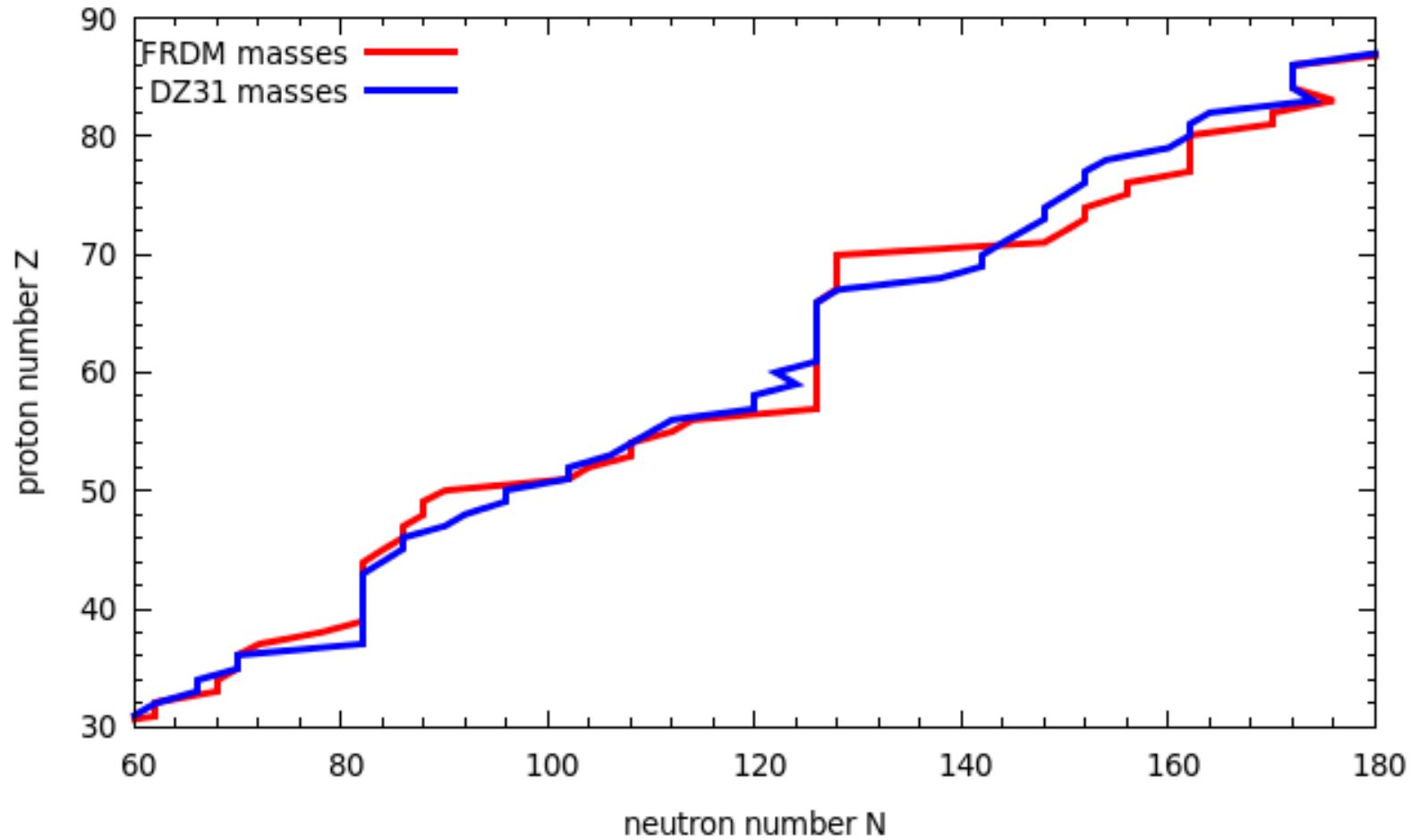
$$T \approx 0.75 \text{ GK}$$

$$n_n \approx 3 \times 10^{24} \text{ cm}^{-3}$$

$$S_n^0 \approx 1.4 \text{ MeV}$$

## nuclear masses

nuclear mass prediction determine the *r*-process path and therefore the abundances

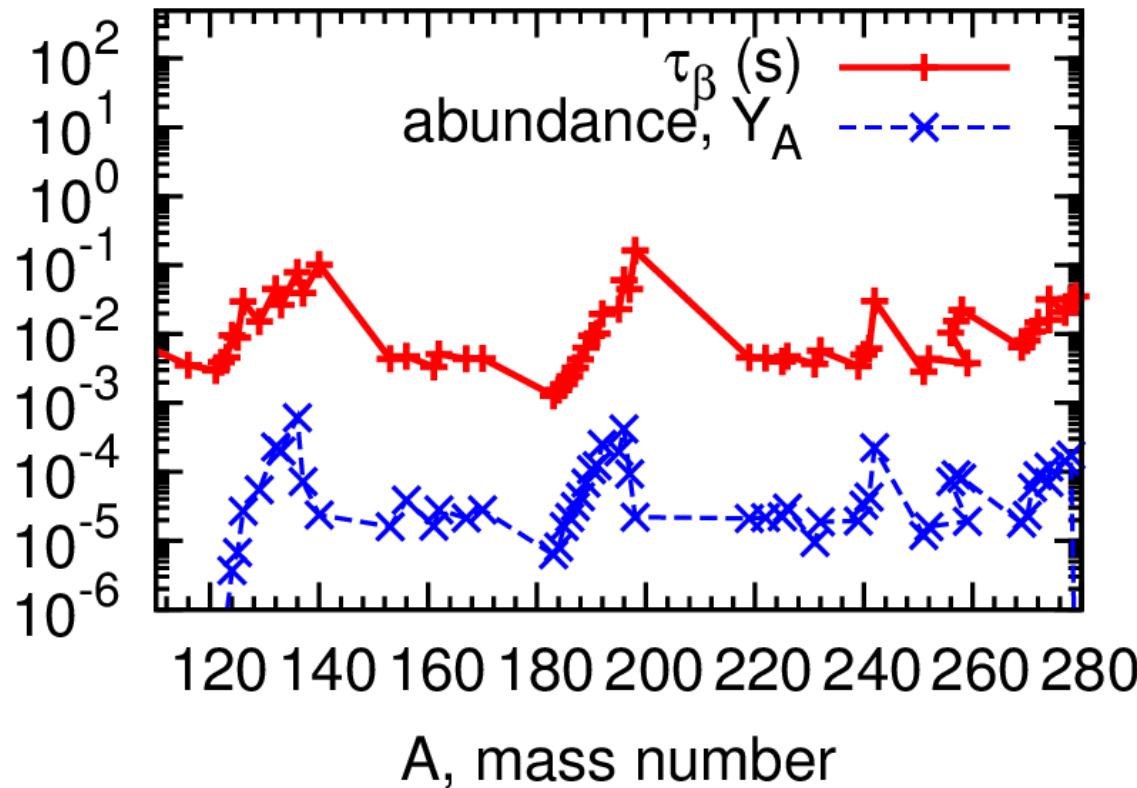


(See Martin+, Mendoza-Temis+, Mumpower+, Goriely+ and many many others)

## beta decay rates

steady  $\beta$  flow:  $Y(Z)\langle\lambda_\beta(Z)\rangle = Y(Z+1)\langle\lambda_\beta(Z+1)\rangle$

→ nuclei with longer  $\beta$ -decay halflives are more abundant



$$R_{n/s} = 1$$

$$T \approx 0.75 \text{ GK}$$

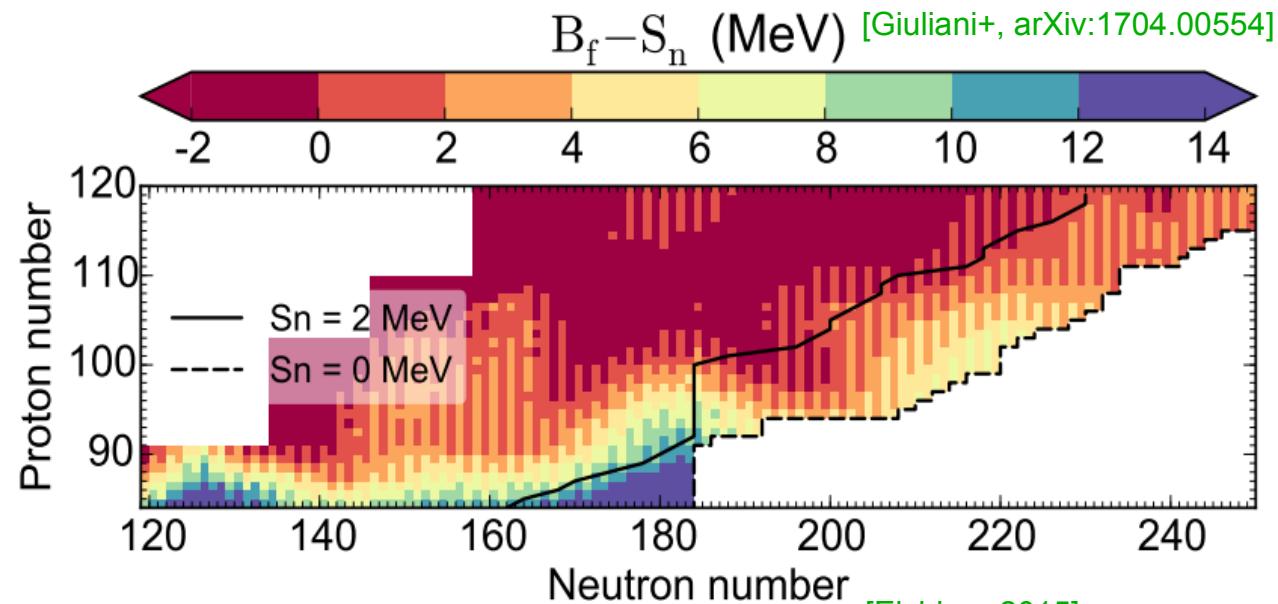
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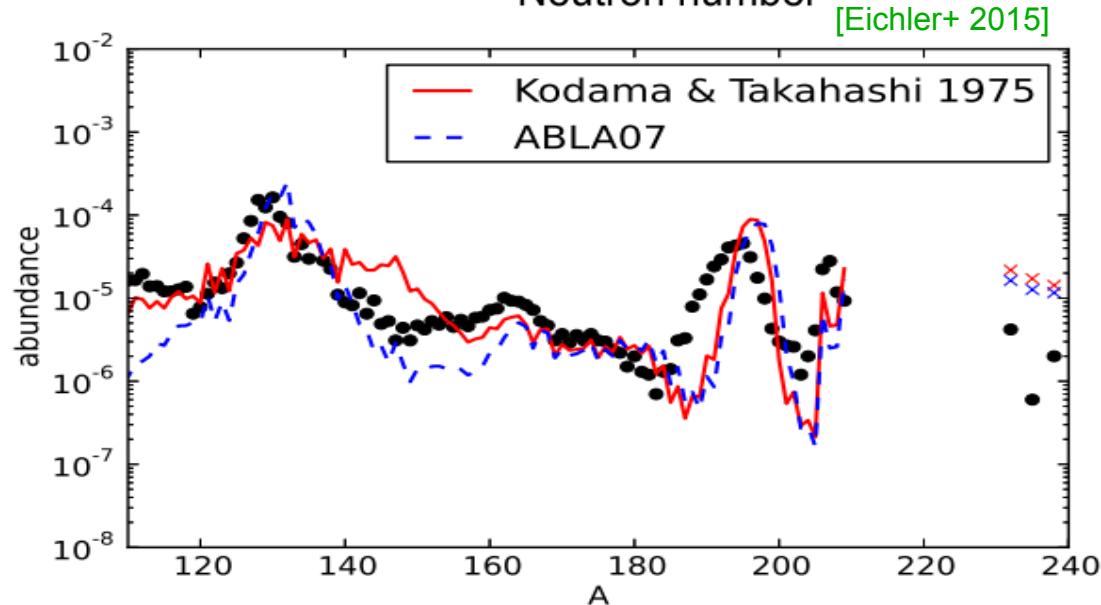
( $\beta$ -decay rates also shapes the final abundance pattern and peak locations during the  $r$ -process freeze-out. E.g., Eichler+ 2015, Friedel and Tomislav's talks in the workshop and other works...)

## fission rates and fragment distributions

fission barrier height  
prediction determines  
where the *r*-process ends



fragment distributions can  
shape the patterns around  
and above the 2nd peak



(See also Goriely+, Mumpower+,...)

Impact of nuclear physics input on low  $Y_e$  ejecta

## Nuclear mass models

[Mendoza-Temis, PhD Thesis]

**Table 2.2:** RMSD in MeV, for the fits and predictions for different mass models.

MODEL	fit	prediction	full set	
FRDM	0.655	0.765	0.666	[Moeller+ 1995]
HFB21	0.576	0.646	0.584	[Goriely+ 2010]
WS3	0.336	0.424	0.345	[Liu+ 2011]
DZ10	0.551	0.880	0.588	[Duflo+ 1995]
DZ31	0.363	0.665	0.400	

fit: 2149 nuclei from AME03 or 1845 nuclei from AME95

prediction: 219 nuclei from AME12

FRDM: Finite Range Droplet Model, macroscopic+microscopic

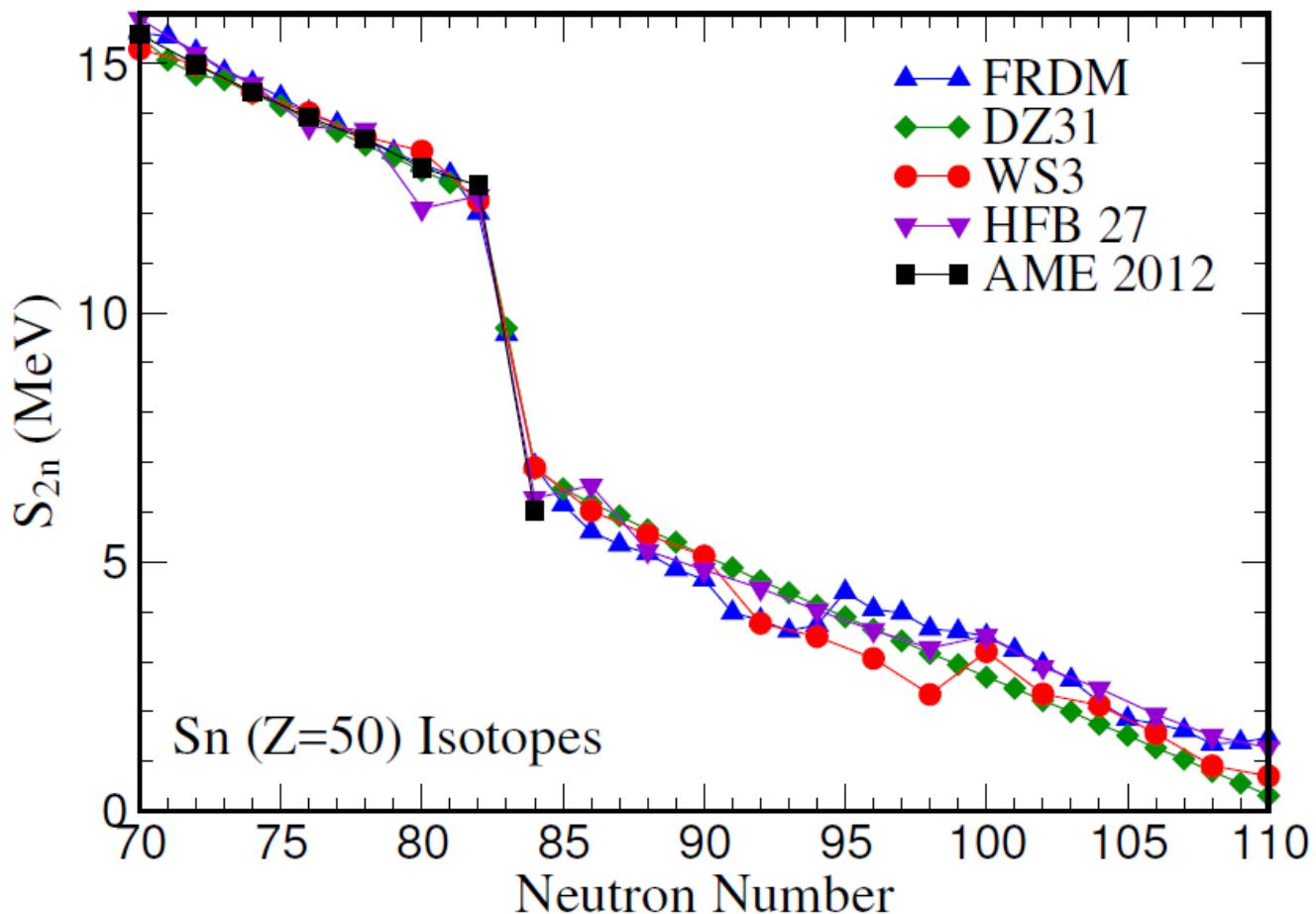
WS3: Weizsäcker-Skyrme mass model, macroscopic+microscopic

DZ10/31: Duflo-Zuker mass formula, shell model inspired, macroscopic+microscopic

HFB21: mean-field model with Hartree-Fock-Bogoliubov approximation, microscopic

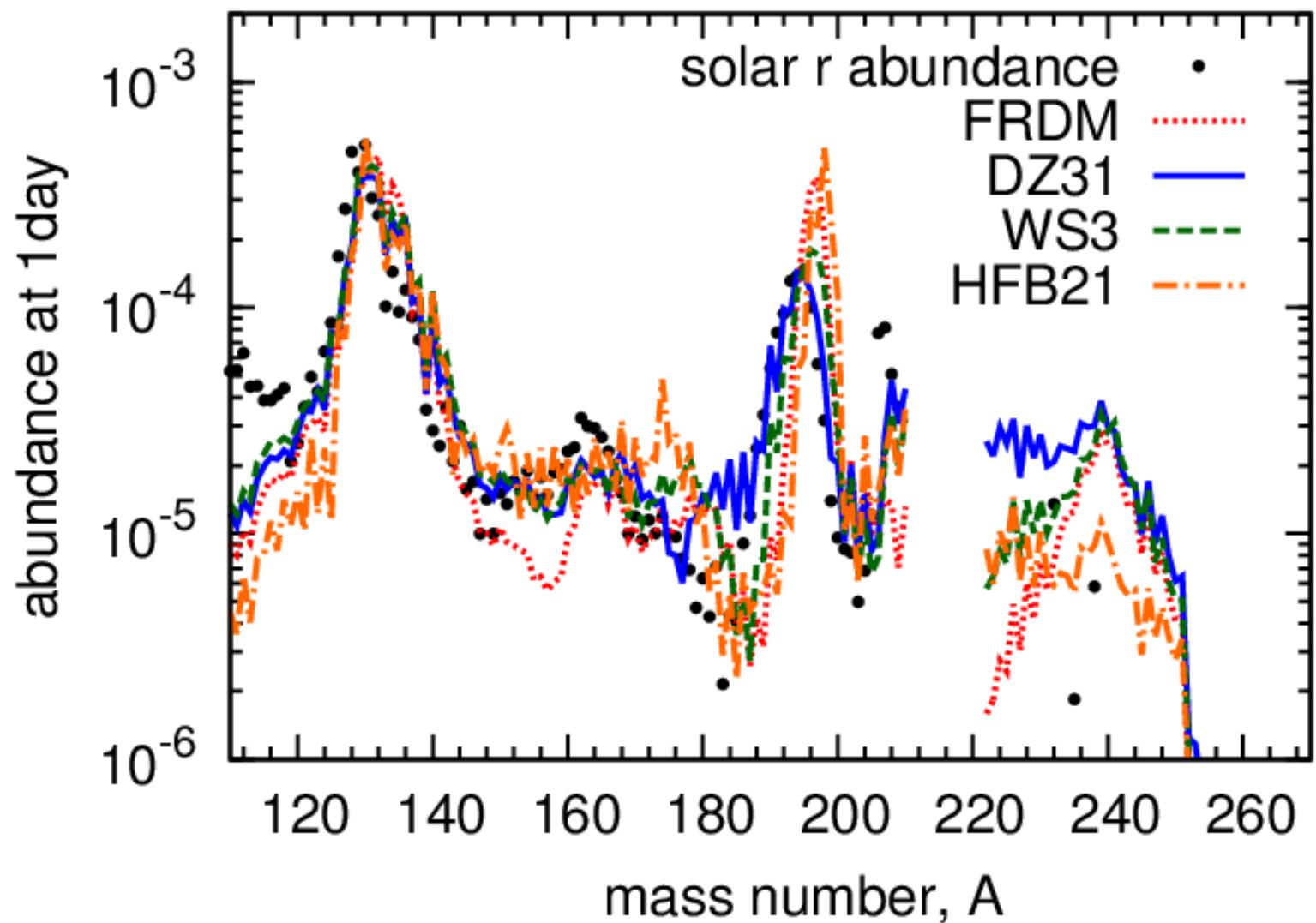
# Comparison $S_{2n}$

Very similar predictions for  $Q$ -values (relevant quantity). slide from Gabriel



Variations in localized regions responsible for different abundances predictions.

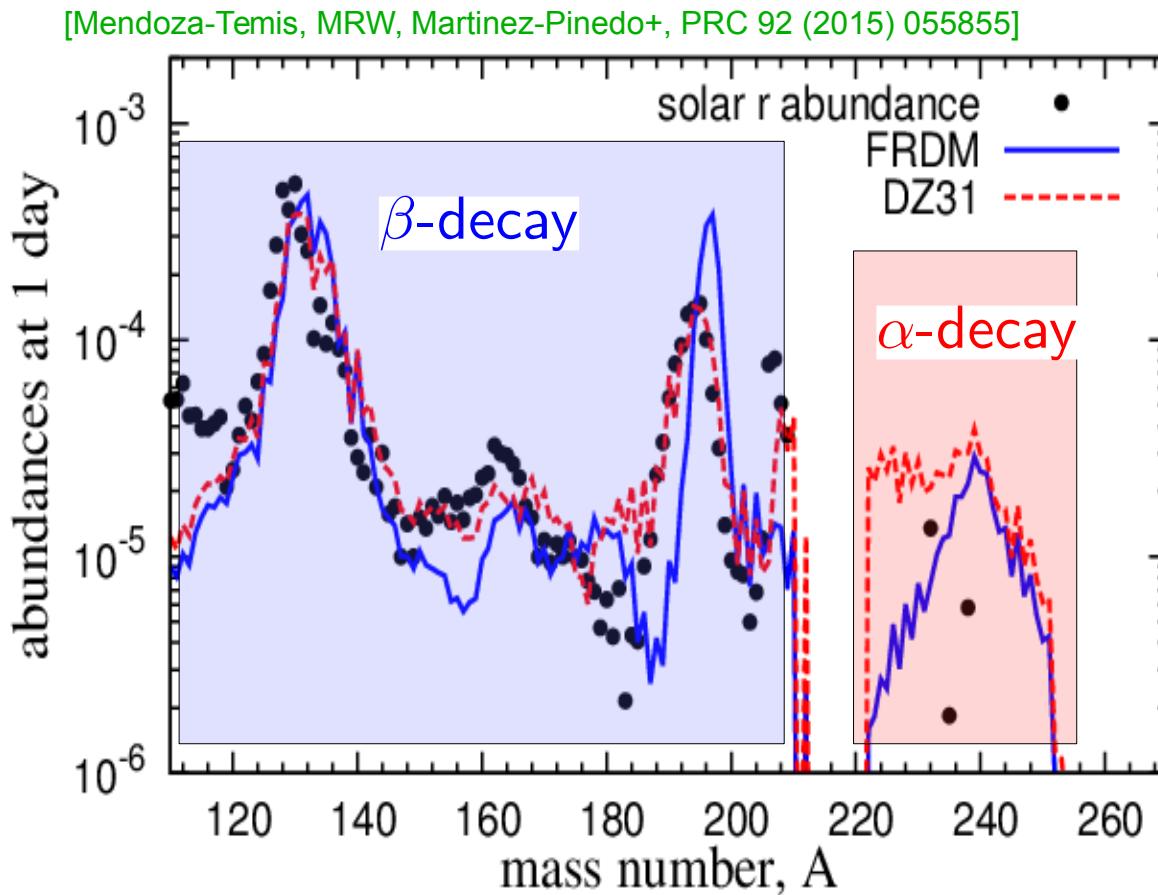
## Impact of masses on abundances



\*\*only the  $(n, \gamma)$  and  $(\gamma, n)$  for nuclei with  $Z \leq 83$  are changed\*\*

## Impact of masses on abundances

the prediction of the trans-lead abundances can depend greatly on the adopted nuclear mass models

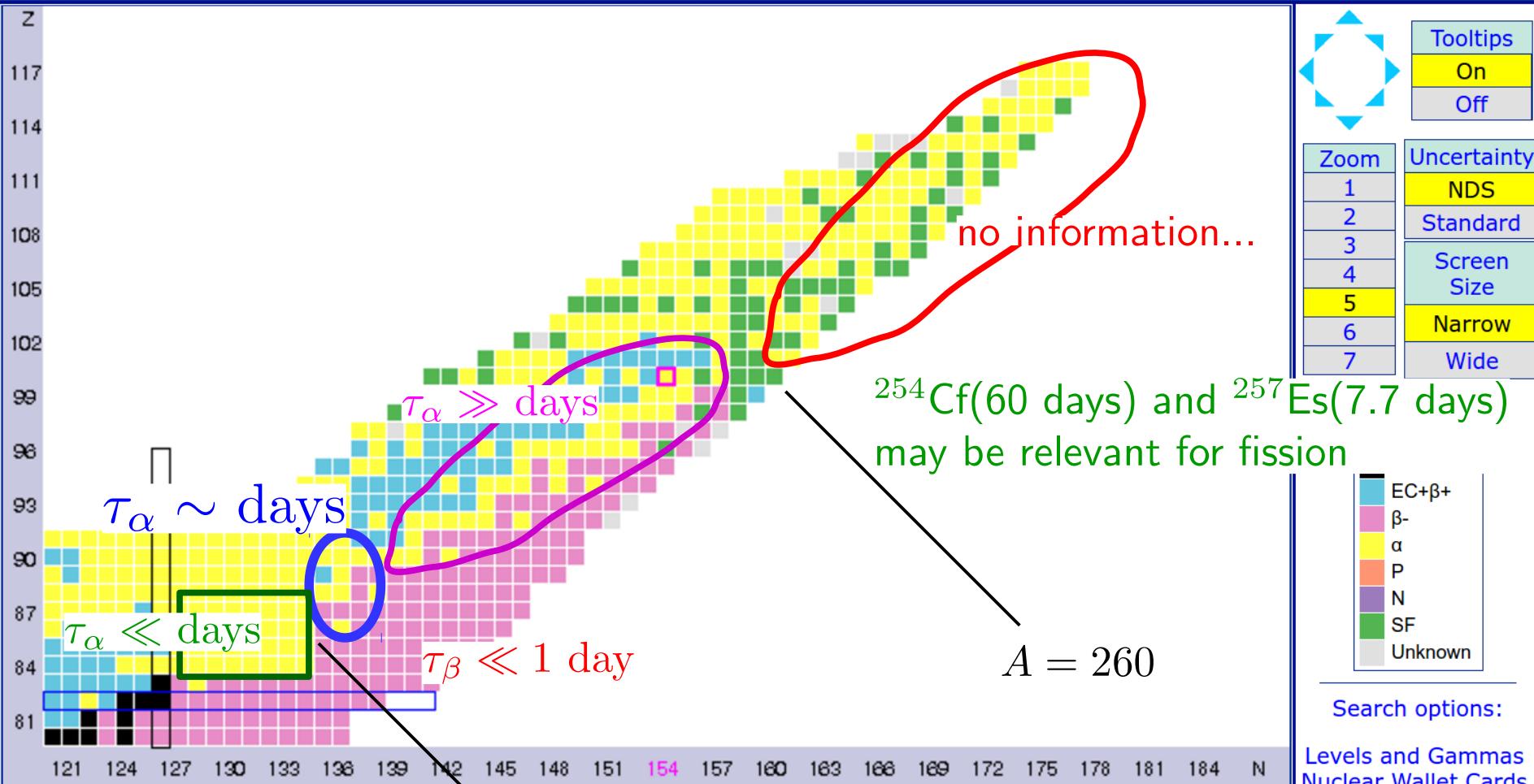




# Chart of Nuclides

Click on a nucleus for information

Color code	Half-life	Decay Mode	$Q_{\beta^-}$	$Q_{EC}$	$Q_{\beta^+}$	$S_n$	$S_p$	$Q_a$	$S_{2n}$	$S_{2p}$	$Q_{2\beta^-}$	$Q_{2EC}$	$Q_{ECp}$
$Q_{\beta^-n}$	BE/A	(BE-LDM Fit)/A	$E_{1st \ ex. \ st.}$	$E_{2+}$	$E_{3-}$	$E_{4+}$	$E_{4+}/E_{2+}$	$\beta_2$	$B(E2)_{42}/B(E2)_{20}$	$\sigma(n,\gamma)$	$\sigma(n,F)$	235U FY	239Pu FY

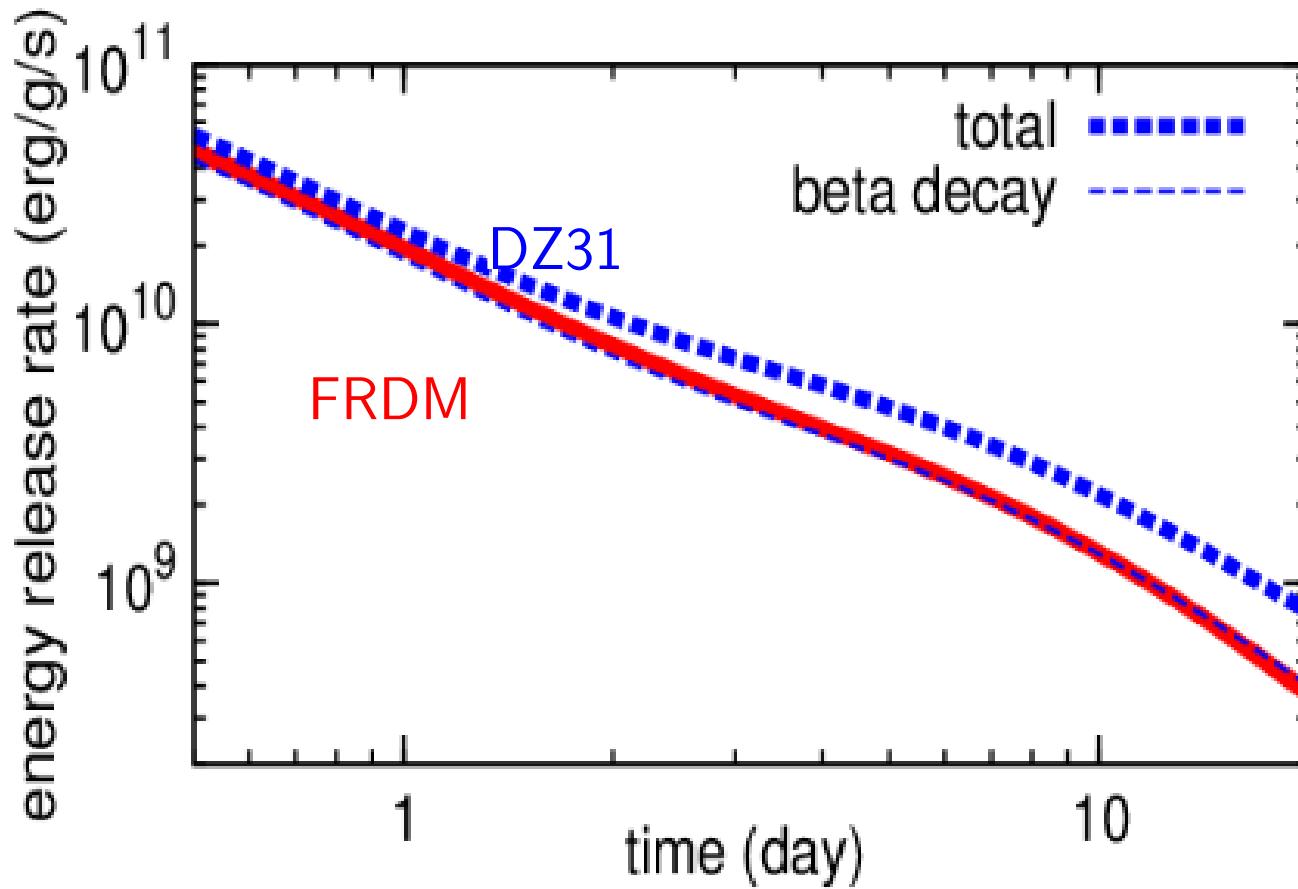


$A = 220$

## Relevant $\alpha$ -decays

## Nuclear physics inputs and the kilonova heating rate

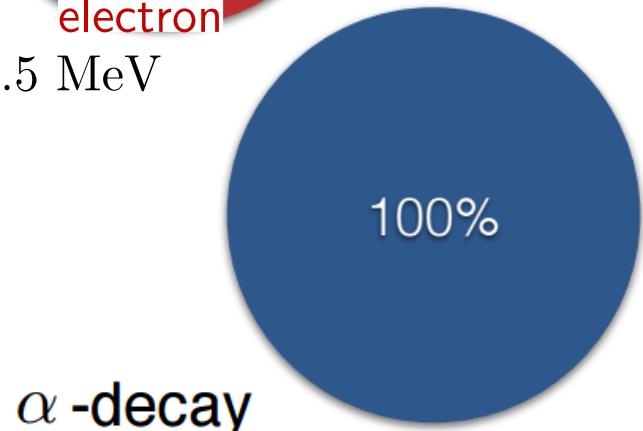
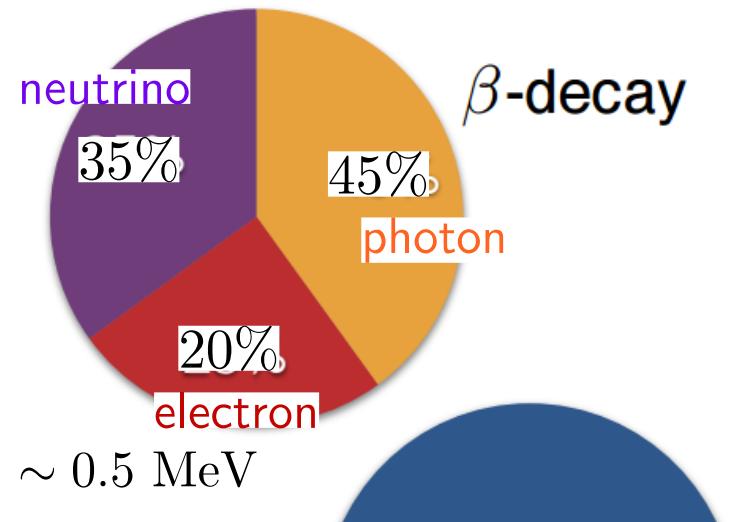
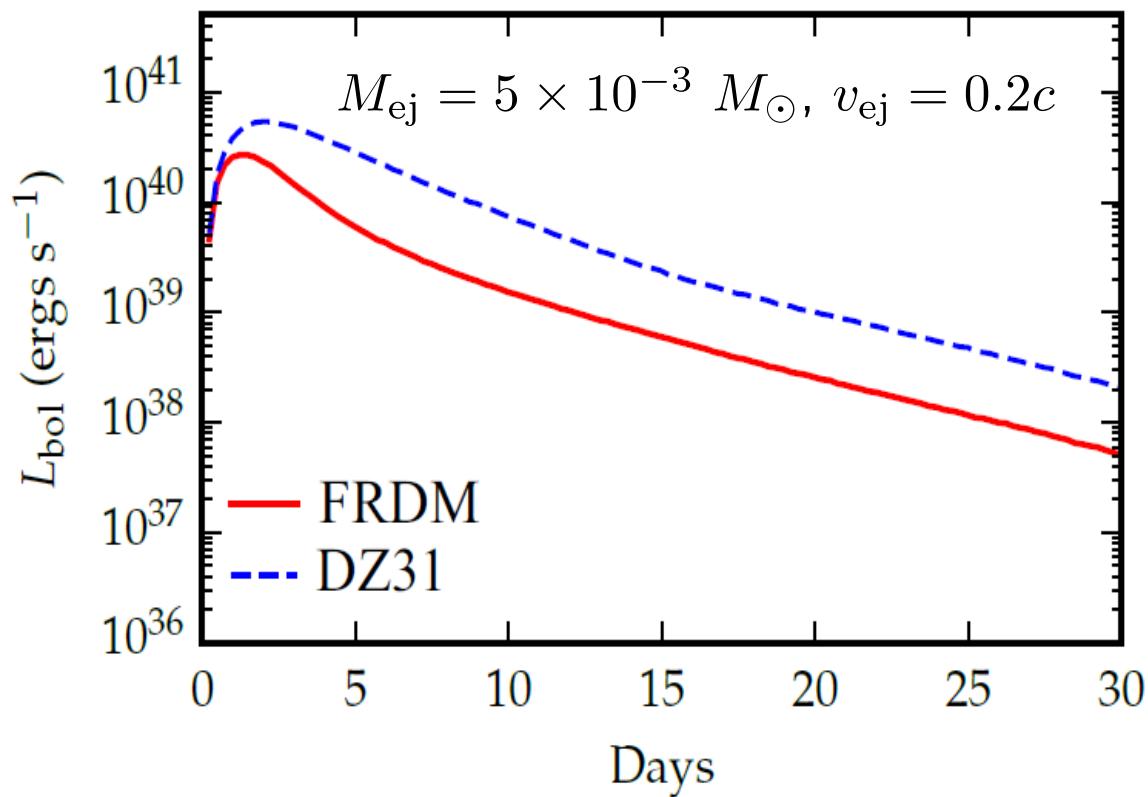
$\alpha$ -decays goes in “chains” at  $t \gtrsim 3$  days and releases  $Q_\alpha \sim 6$  MeV in each decay, compared to typical  $Q_\beta \sim 1$  MeV. Therefore, it can dominate the radioactive energy release



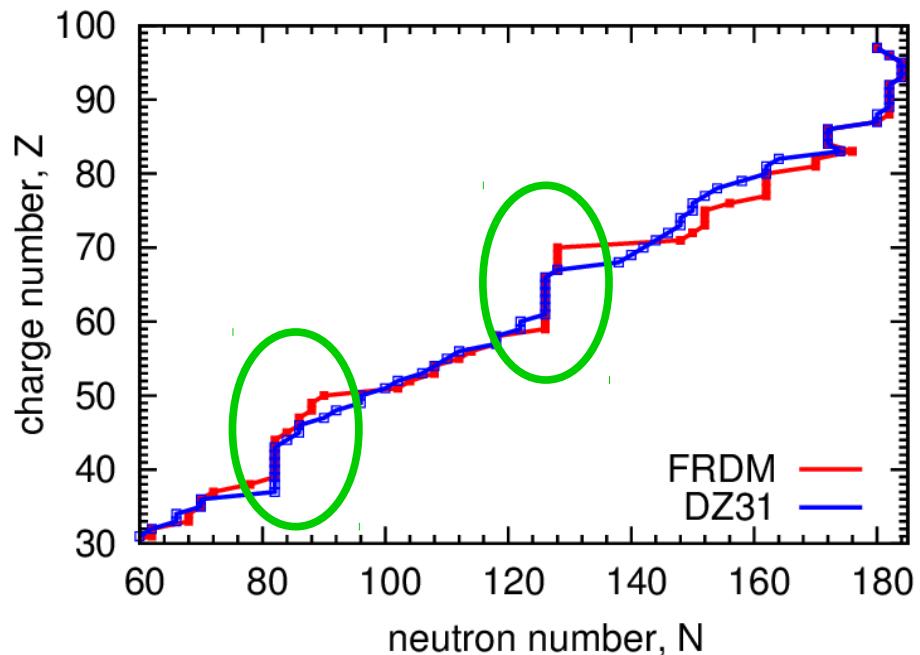
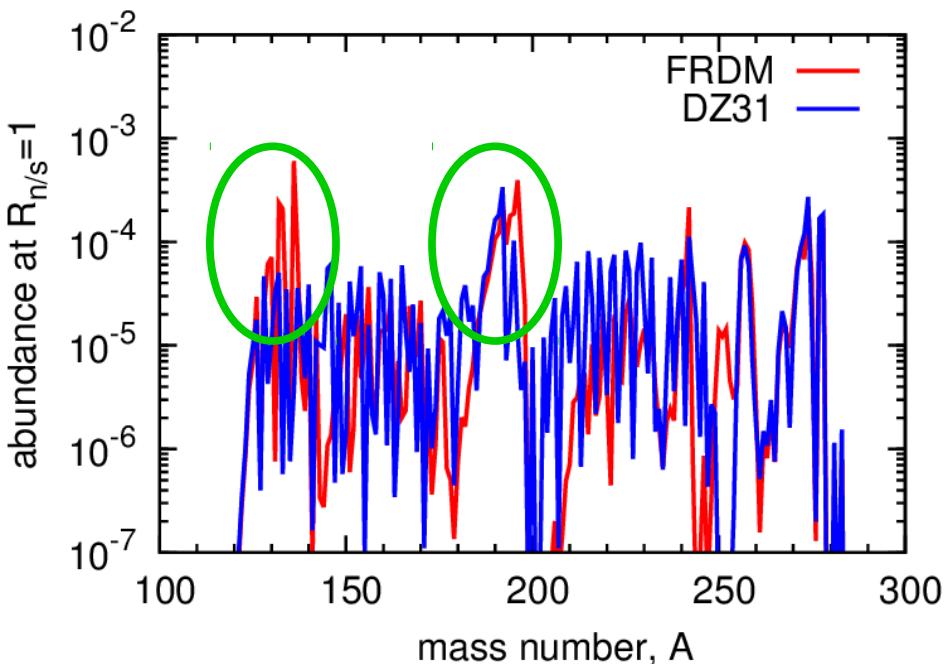
# Nuclear physics inputs and the kilonova heating rate

- $\alpha$  &  $\beta$  particles thermalize in a similar way while  $\gamma$ -ray thermalization quickly become inefficient

[Barnes, Kasen, MRW, Martinez-Pinedo, ApJ 829 (2016) 110]



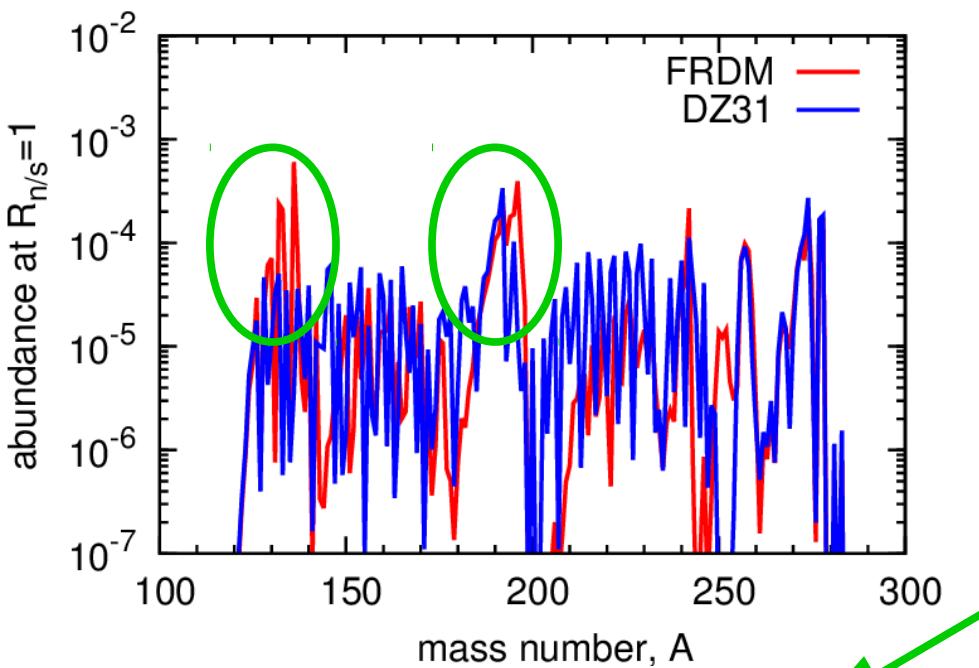
## Link to nuclear mass predictions



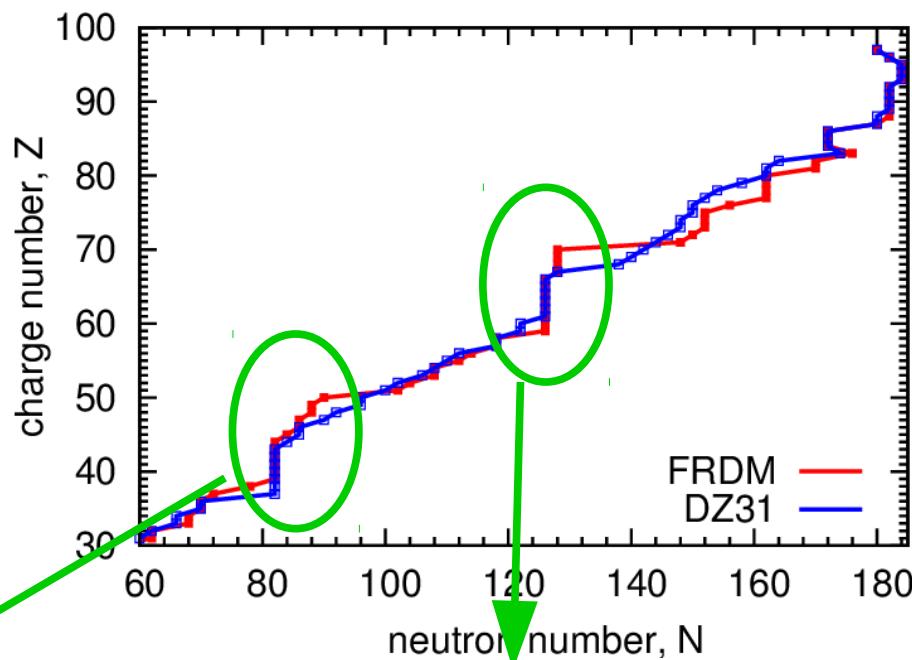
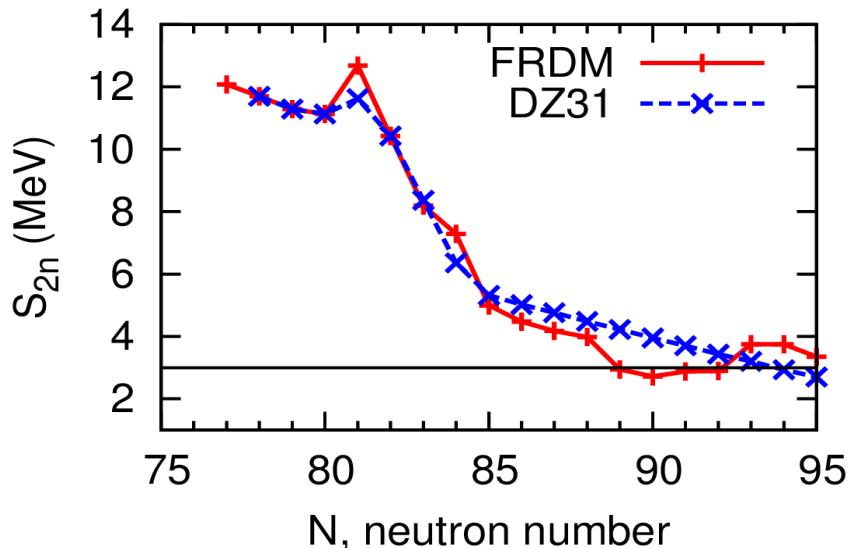
the  $r$ -process path with FRDM mass model extends to larger  $Z$  for regions slightly above the shell closure

- longer  $\beta$ -decay half-lives
- larger abundances at peaks and smaller abundances in-between the peaks

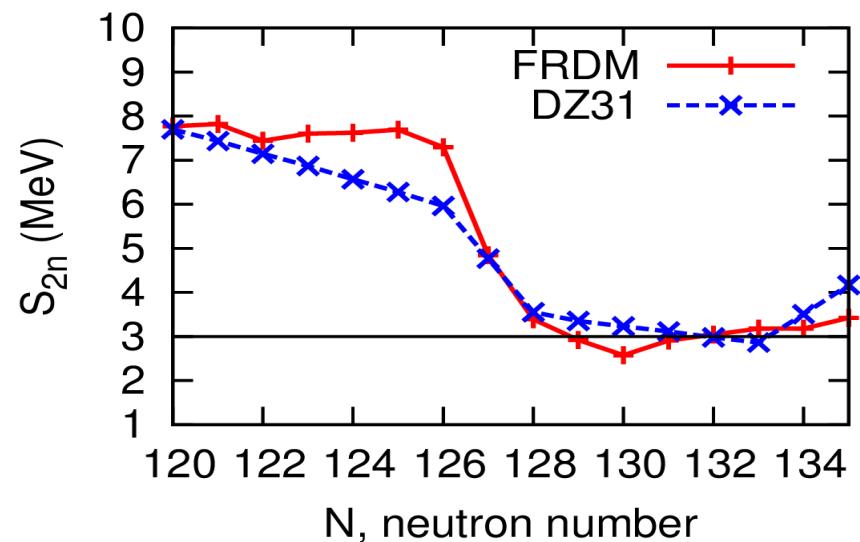
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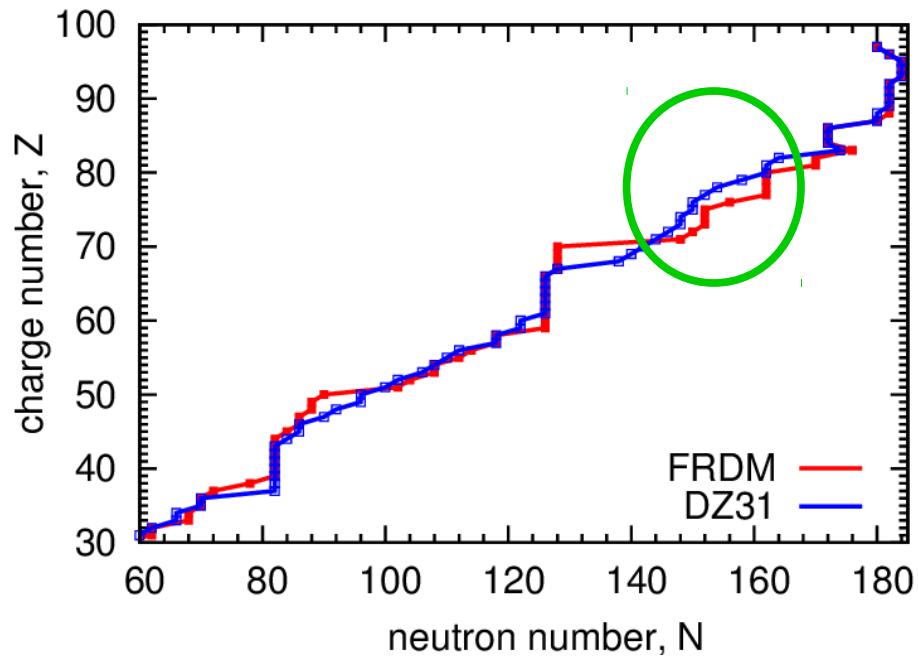
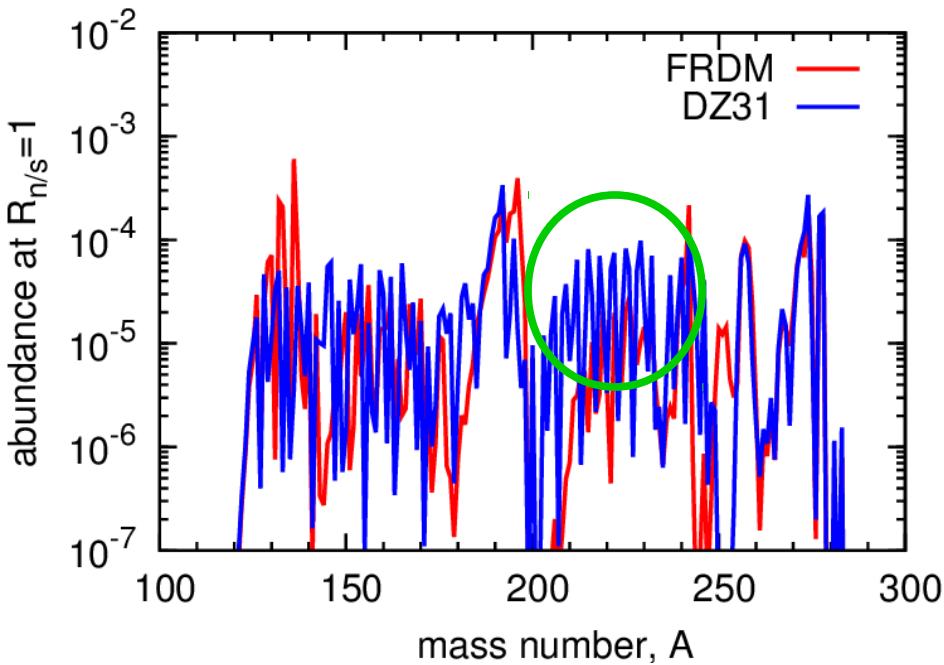
$Cd(Z = 48)$  isotopic chain



$Er(Z = 68)$  isotopic chain



## Link to nuclear mass predictions

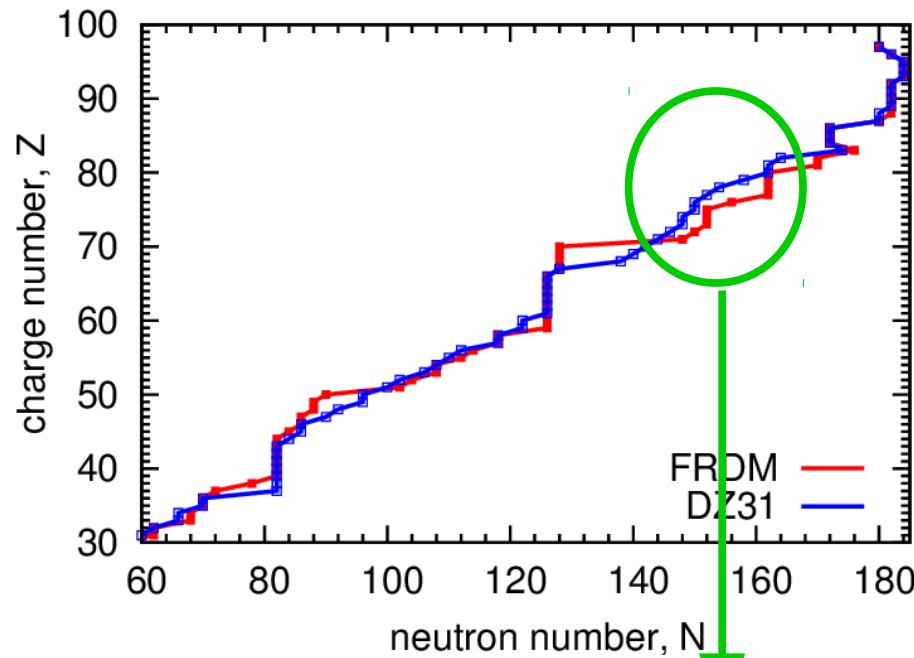
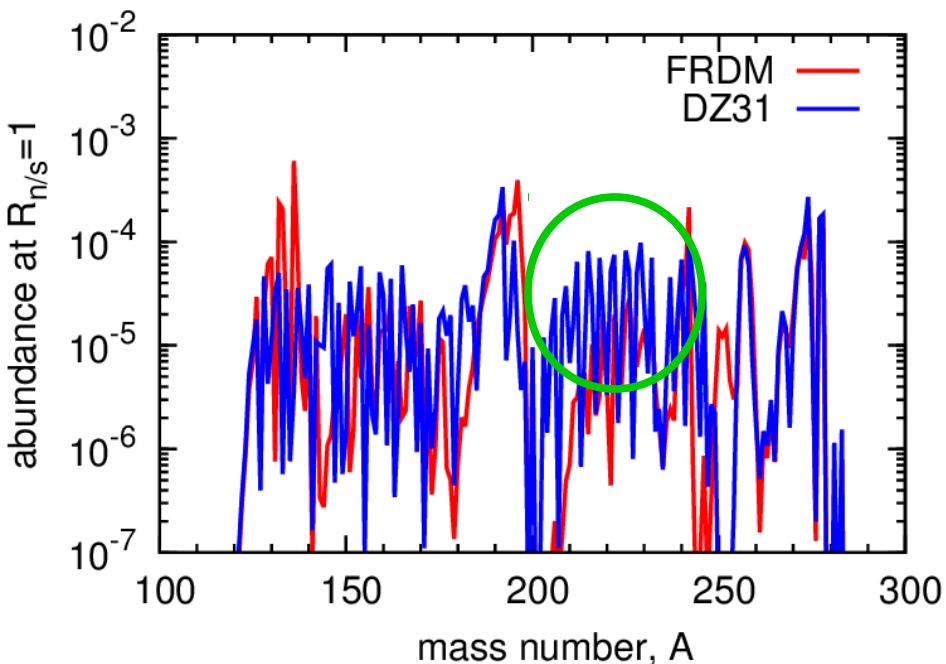


on the other hand, at the region around  $A \sim 230$ , the path of FRDM extends to larger  $N$

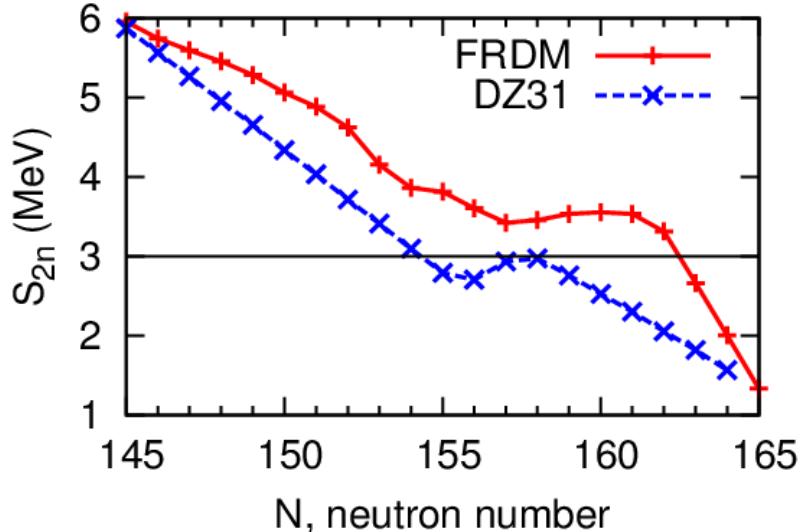
→ shorter  $\beta$ -decay half-lives

→ smaller abundances

## Link to nuclear mass predictions



Pt( $Z = 78$ ) isotopic chain

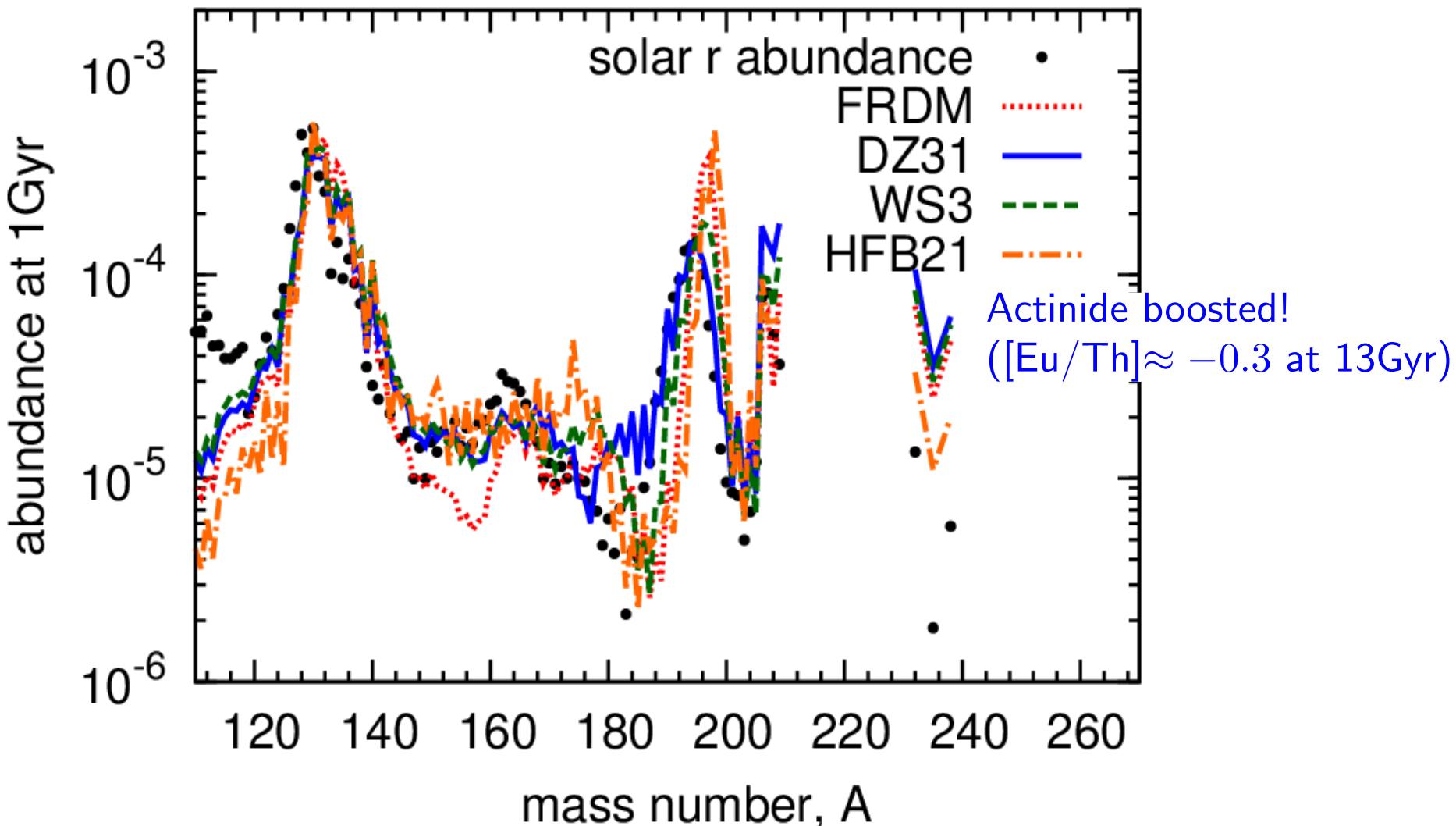


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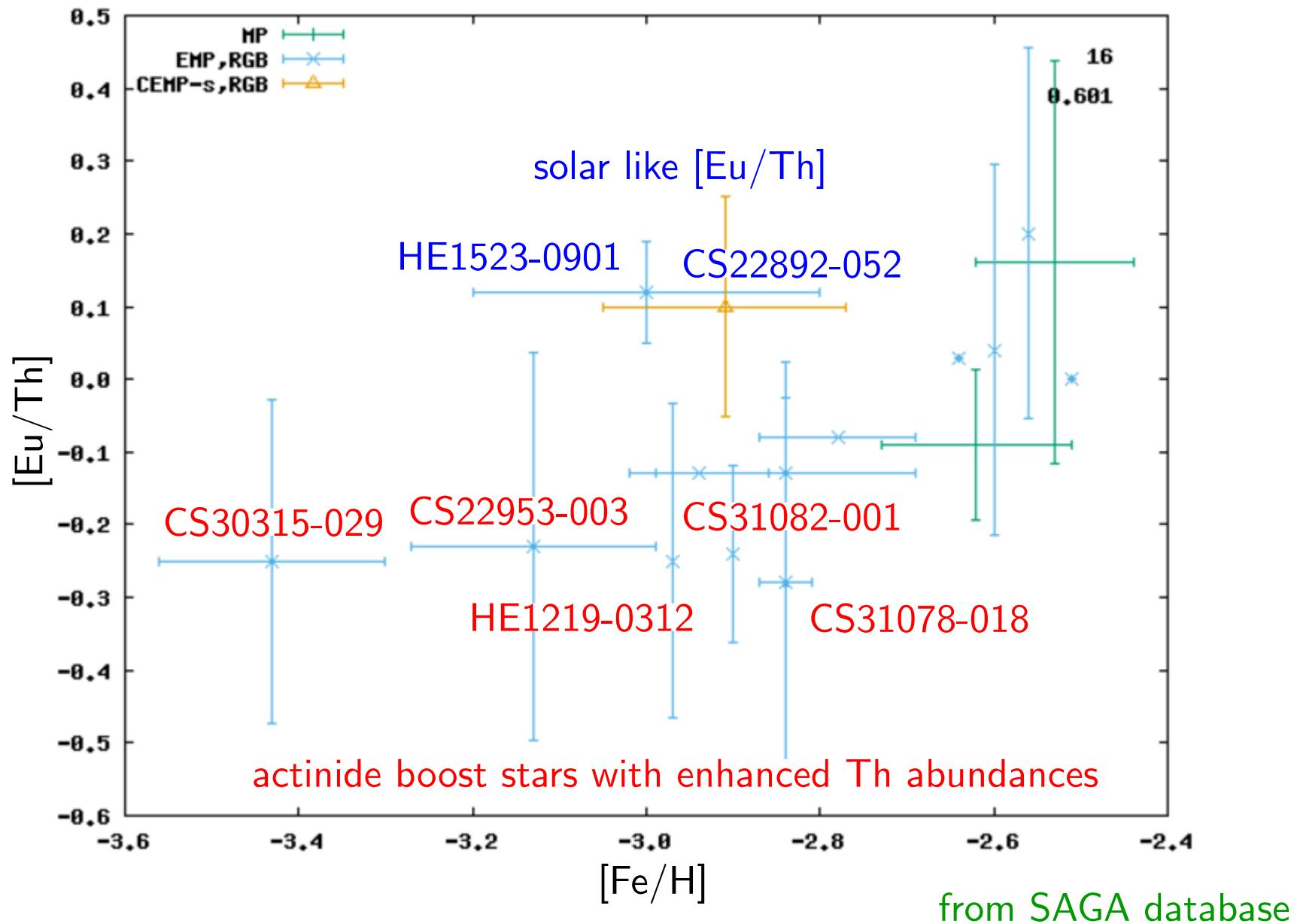
→ shorter  $\beta$ -decay half-lives

→ smaller abundances

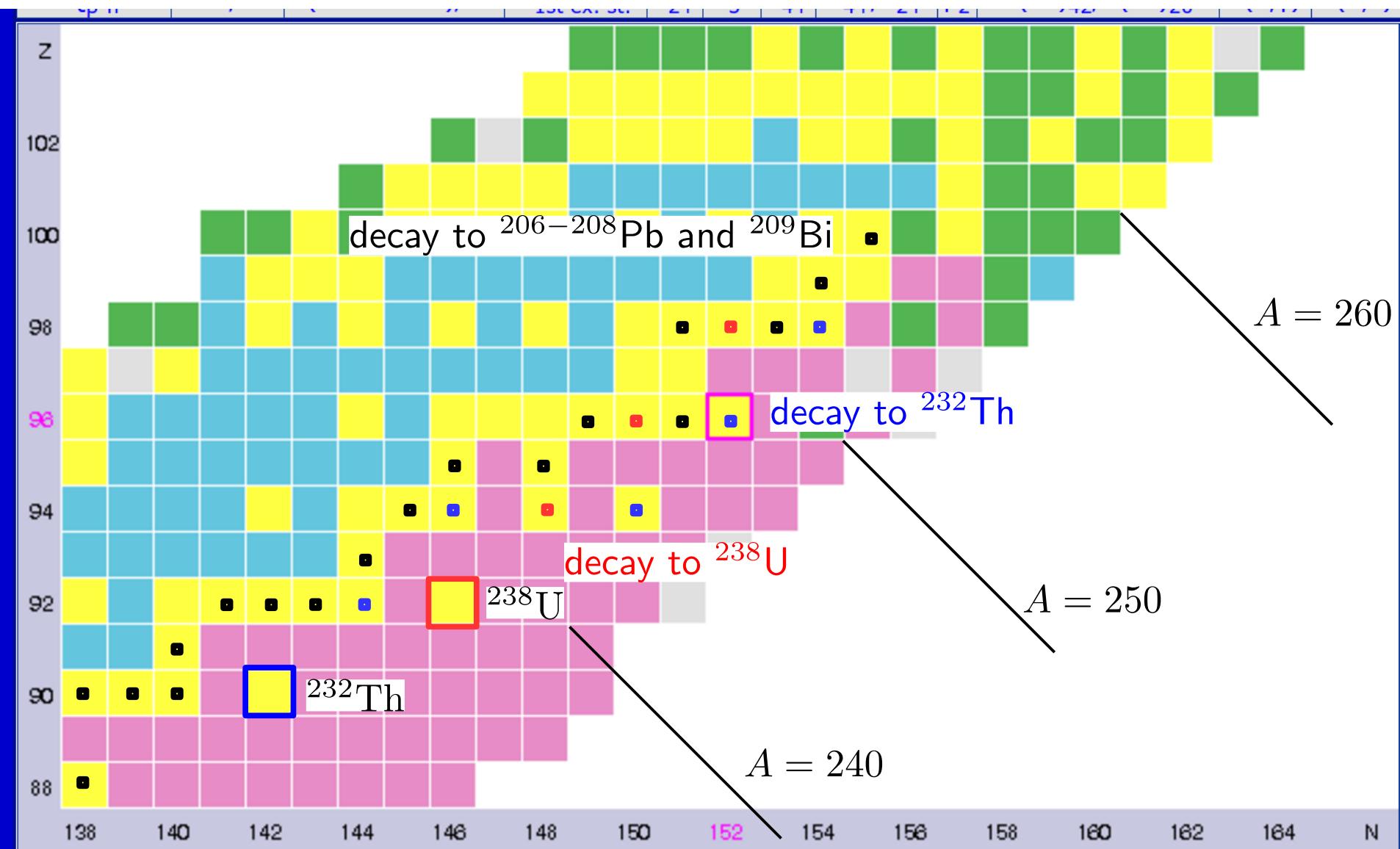
## “Final” abundances and metal-poor stars



# Actinide abundances in Metal-poor stars



measurement of lead abundance can be useful to infer the actinide production

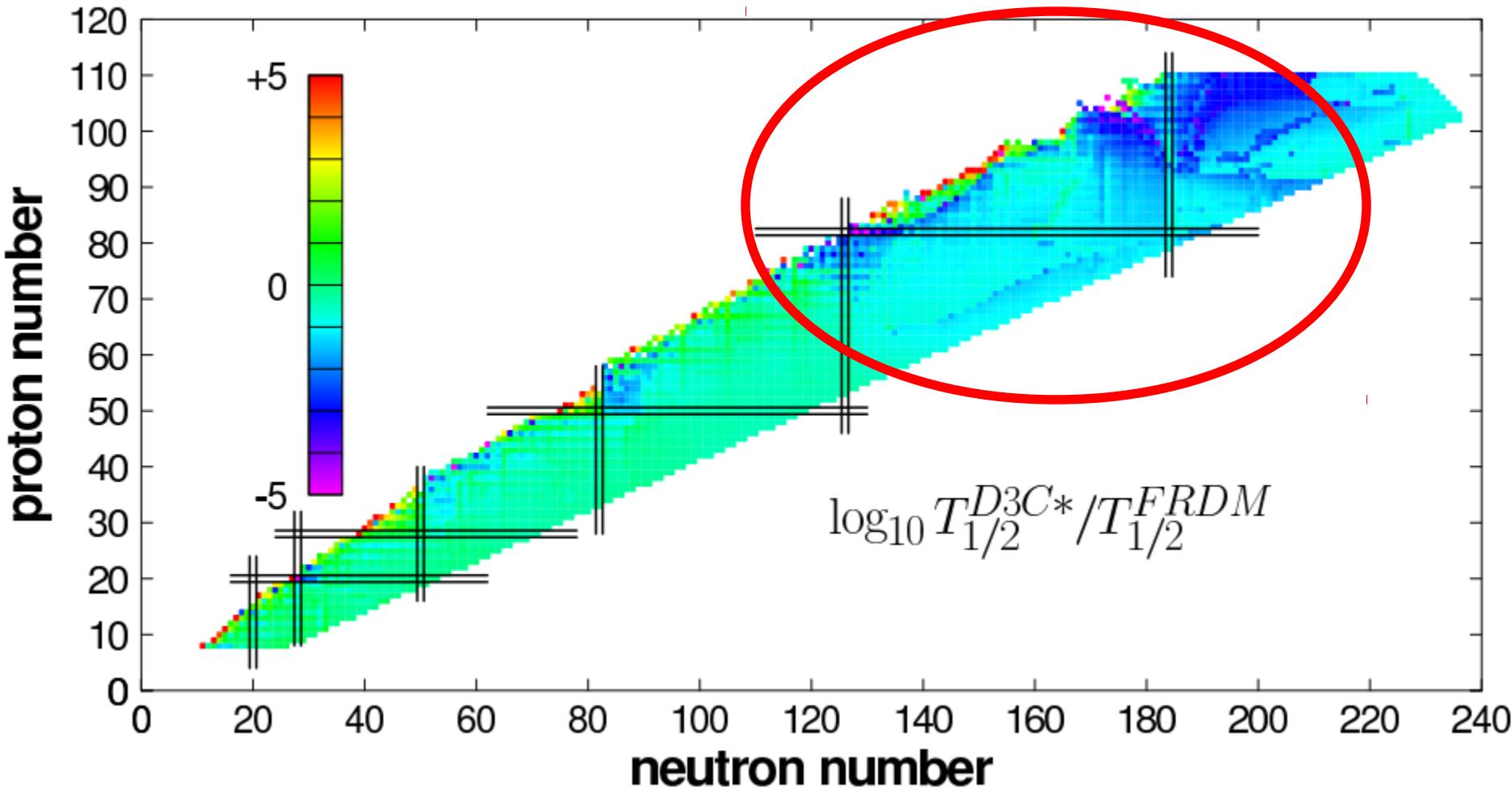


$$\tau(^{232}\text{Th}) \approx 14\text{Gyr}$$

$$\tau(^{238}\text{U}) \approx 4.5\text{Gyr}$$

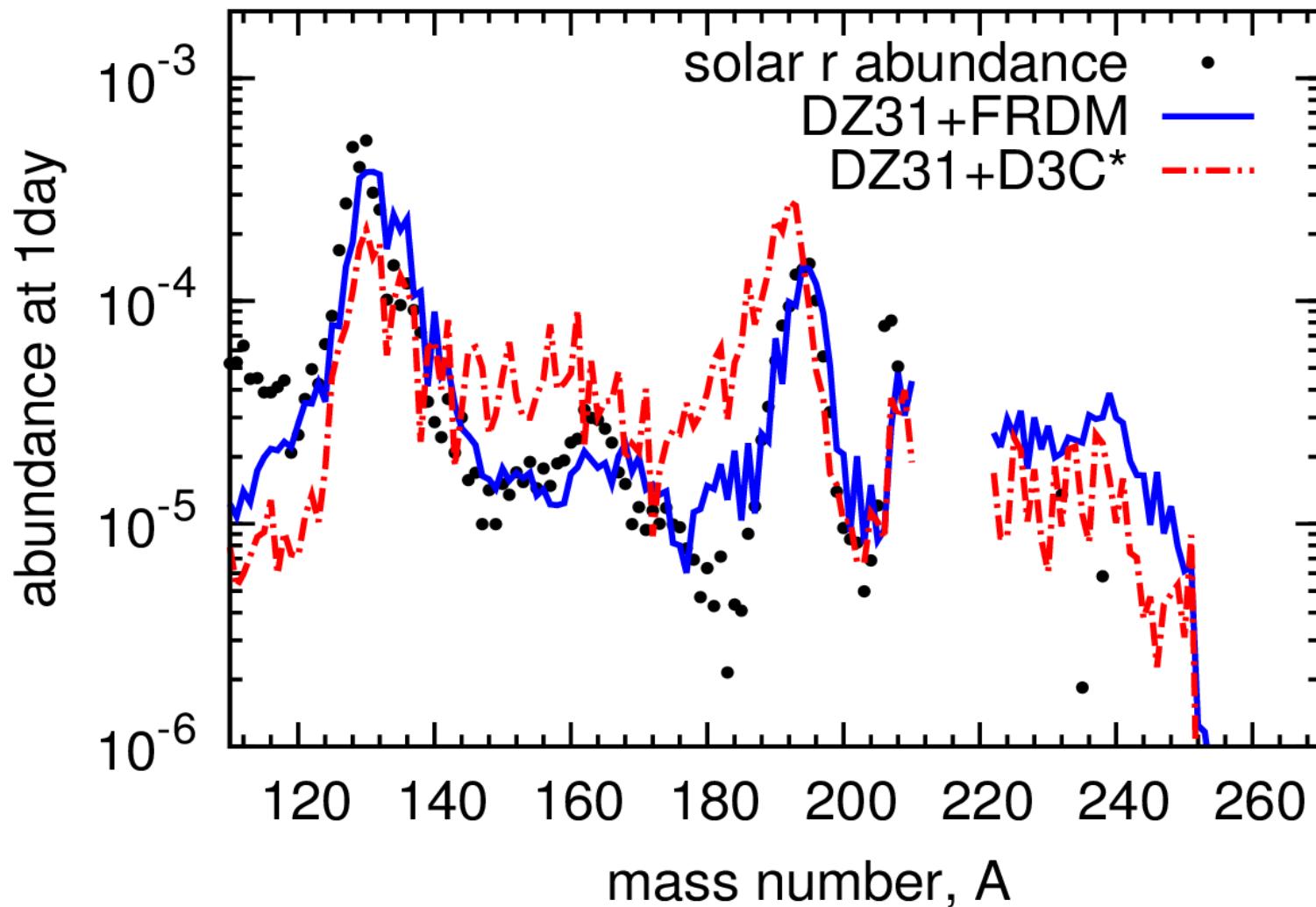
## Impact of $\beta$ -decay rates

[Markentin+ 2015]



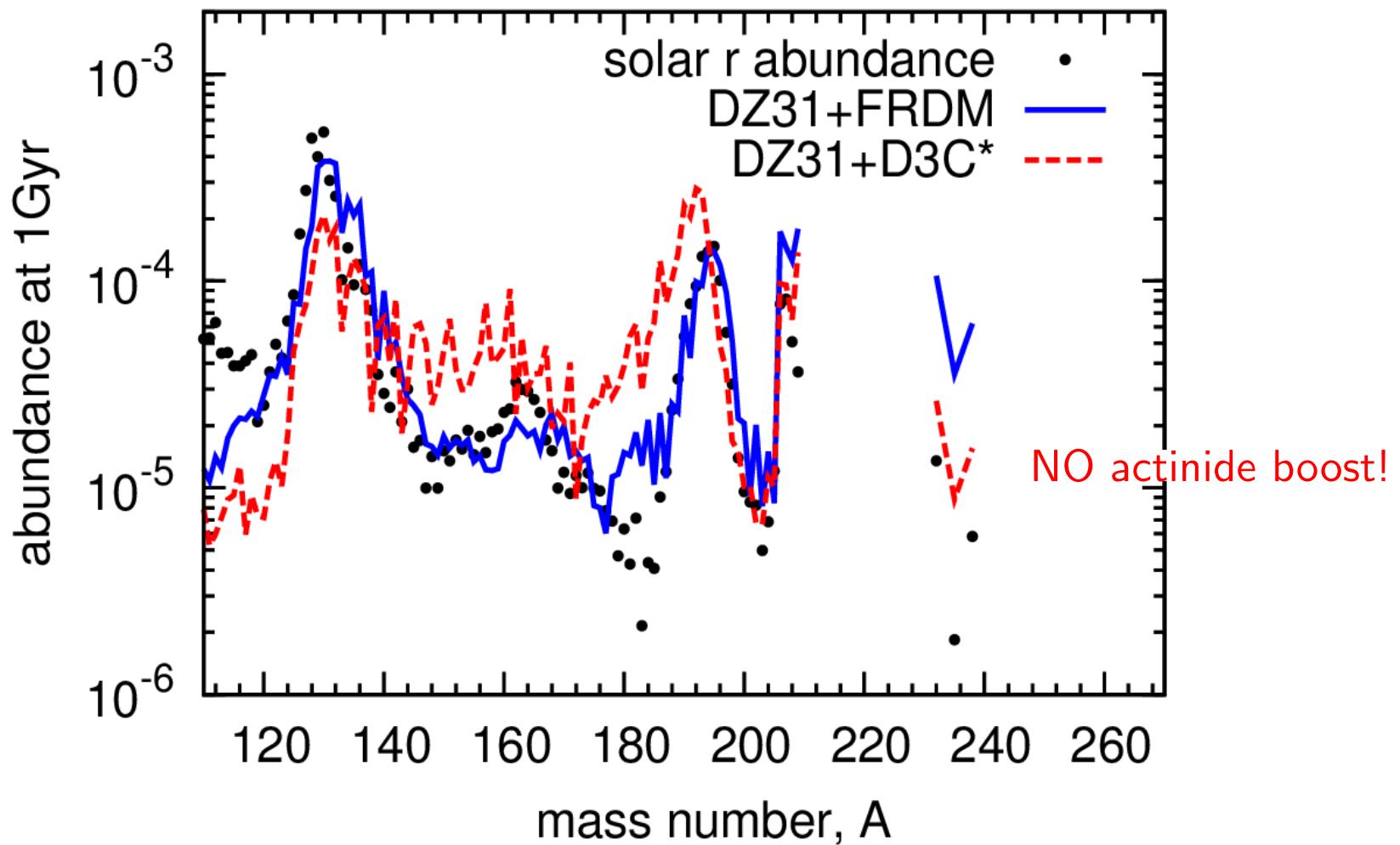
D3C\* model predicts shorter  $\tau_\beta$  for heavier nuclei

## Impact of $\beta$ -decay on abundances



impact on radioactive heating rates is on the level of  $\sim 30\%$ , due to the different relative height in peaks

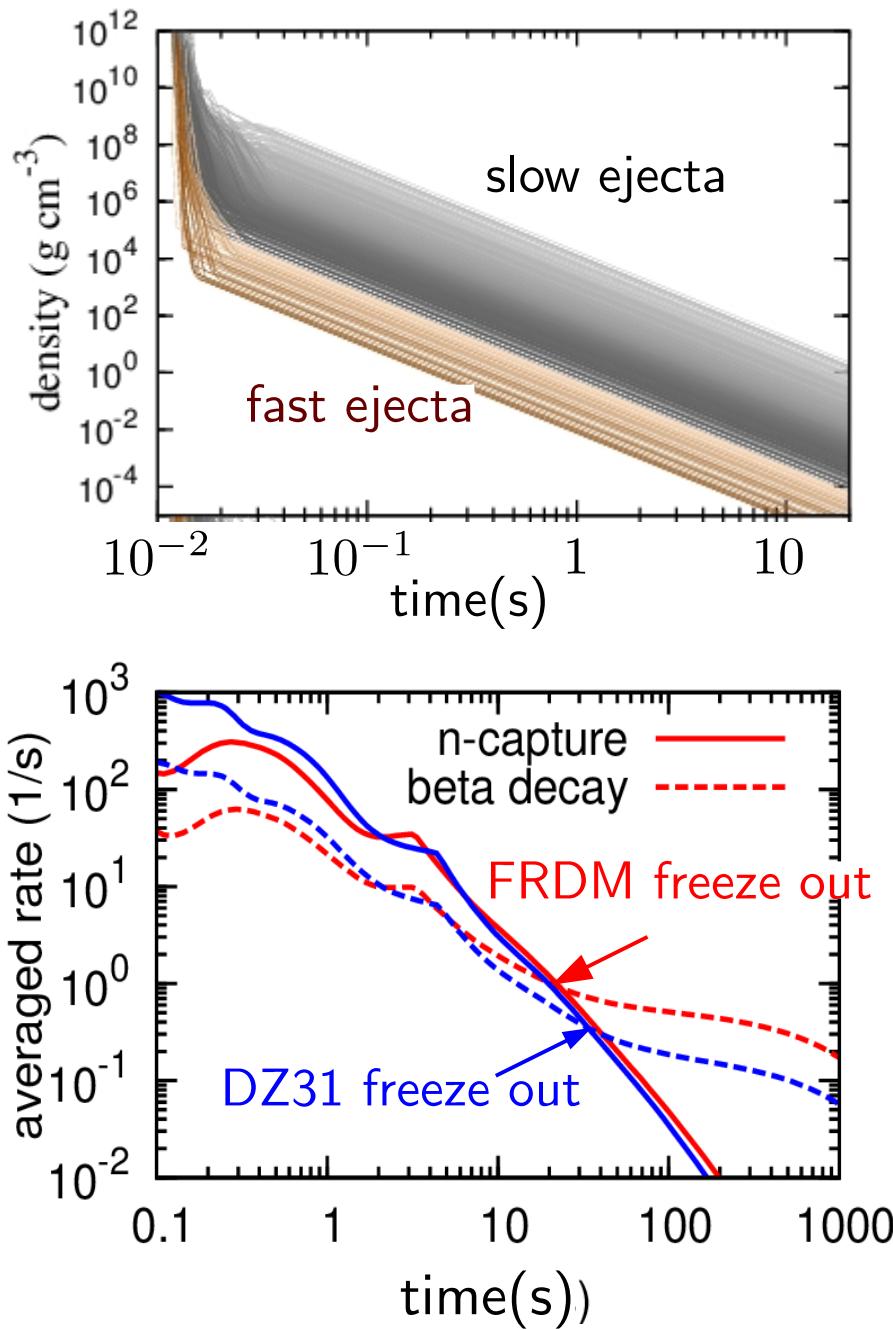
## Impact of $\beta$ -decay on abundances



\*if\* actinides-boost production is originated from low  $Y_e$  ejecta from mergers, one may be able to link the abundances to the half-lives for the translead neutron-rich nuclei?

# Neutron-decay powered pre-cursor?

- for  $\sim 90\%$  of the ejecta, neutrons are used out during the  $r$ -process time scale  $\sim 1$  second ( $\tau_{(n,\gamma)} \lesssim \tau_{\text{dyn}}$ )  
 $\rightarrow$  normal  $r$ -process
- $\sim 10\%$  of the ejecta expands very fast so that free neutrons left at the end of the  $r$ -process (“not-so-rapid”  $r$ -process)  
 $\rightarrow$  kilonova pre-cursor?  
[Metzger+2015, Goriely+ 2015]
- unused amount of neutrons depends on the mass model again:  
 $\sim 40\%$  with FRDM and  
 $\sim 20\%$  with DZ31 at  $t \approx 20$  s  
[Mendoza-Temis+, PRC 92, 055805 (2015)]



We know mergers should produce lots of high  $Y_e$  material...

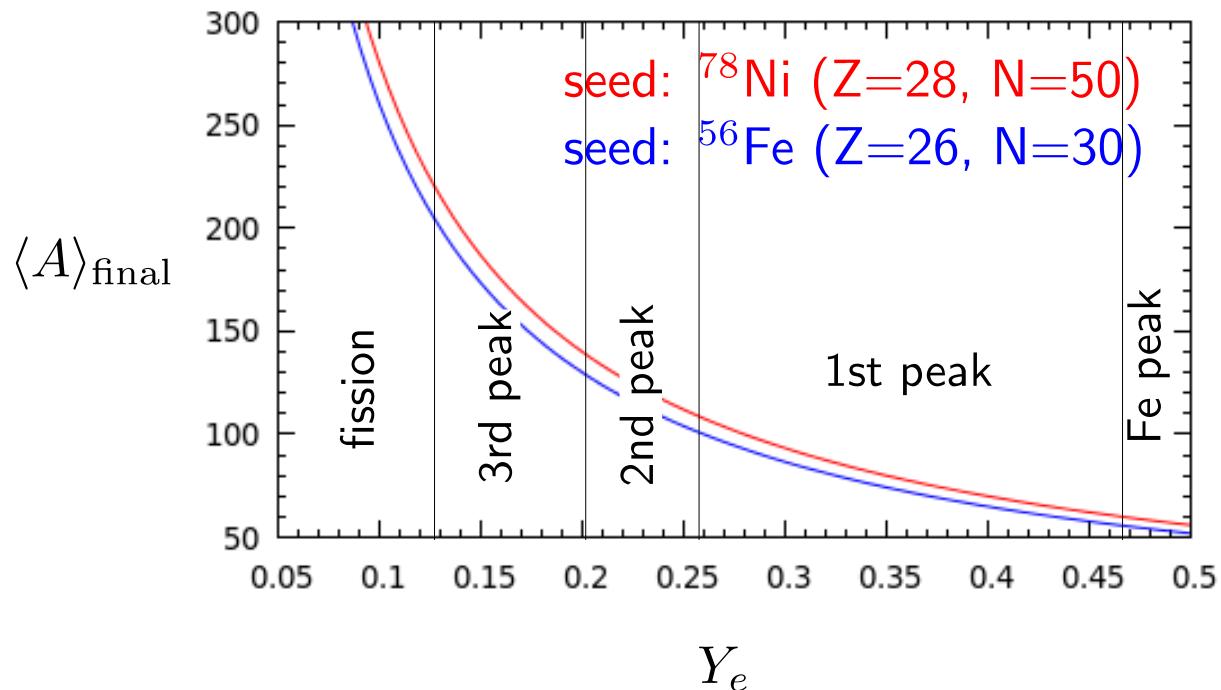
“Typical” condition of merger ejecta:

$$Y_e \sim [0.01, 0.5], s \sim [0 - 40] k_B/\text{nucleon}, \tau_{\text{dyn}} \sim [1, 100] \text{ ms}$$

The final nucleosynthesis outcome is mostly sensitive to the initial  $Y_e$  of the ejecta

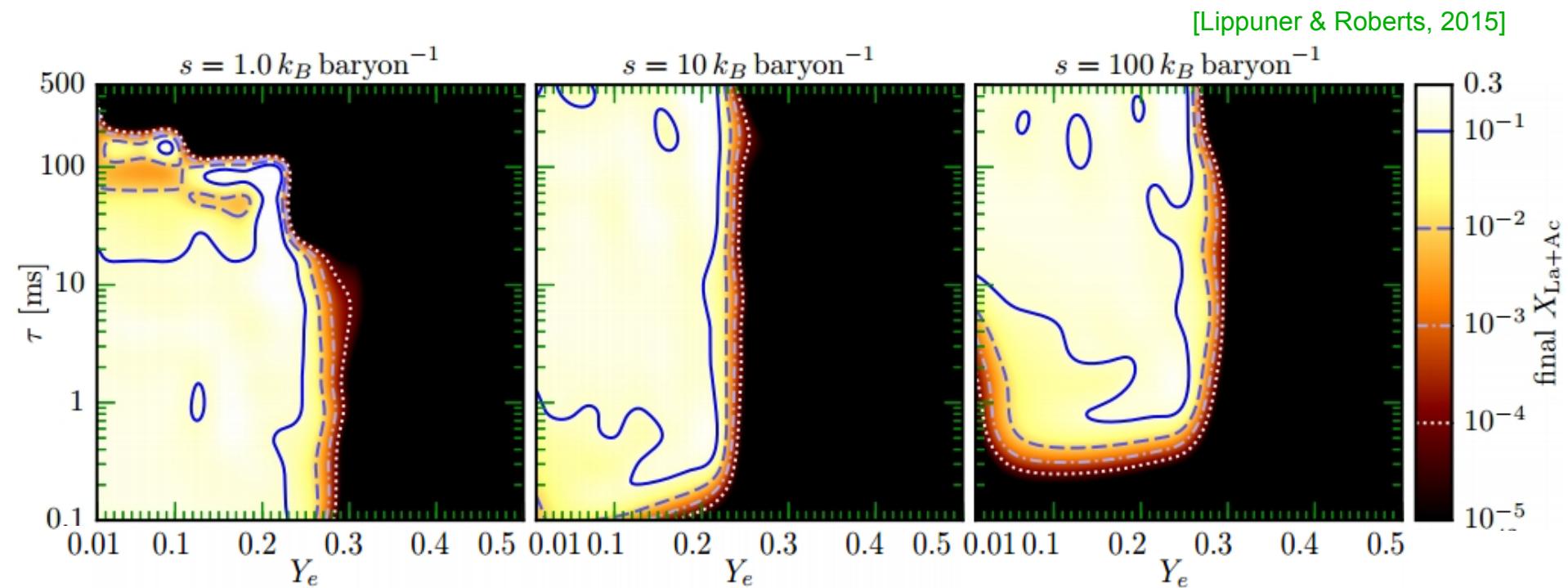
$$R_{n/s} = \frac{Y_n}{Y_{\text{seed}}} = \frac{(1 - Y_e) - N_{\text{seed}}(Y_e/Z_{\text{seed}})}{(Y_e/Z_{\text{seed}})}$$

$$\langle A \rangle_{\text{final}} \approx A_{\text{seed}} + R_{n/s}$$



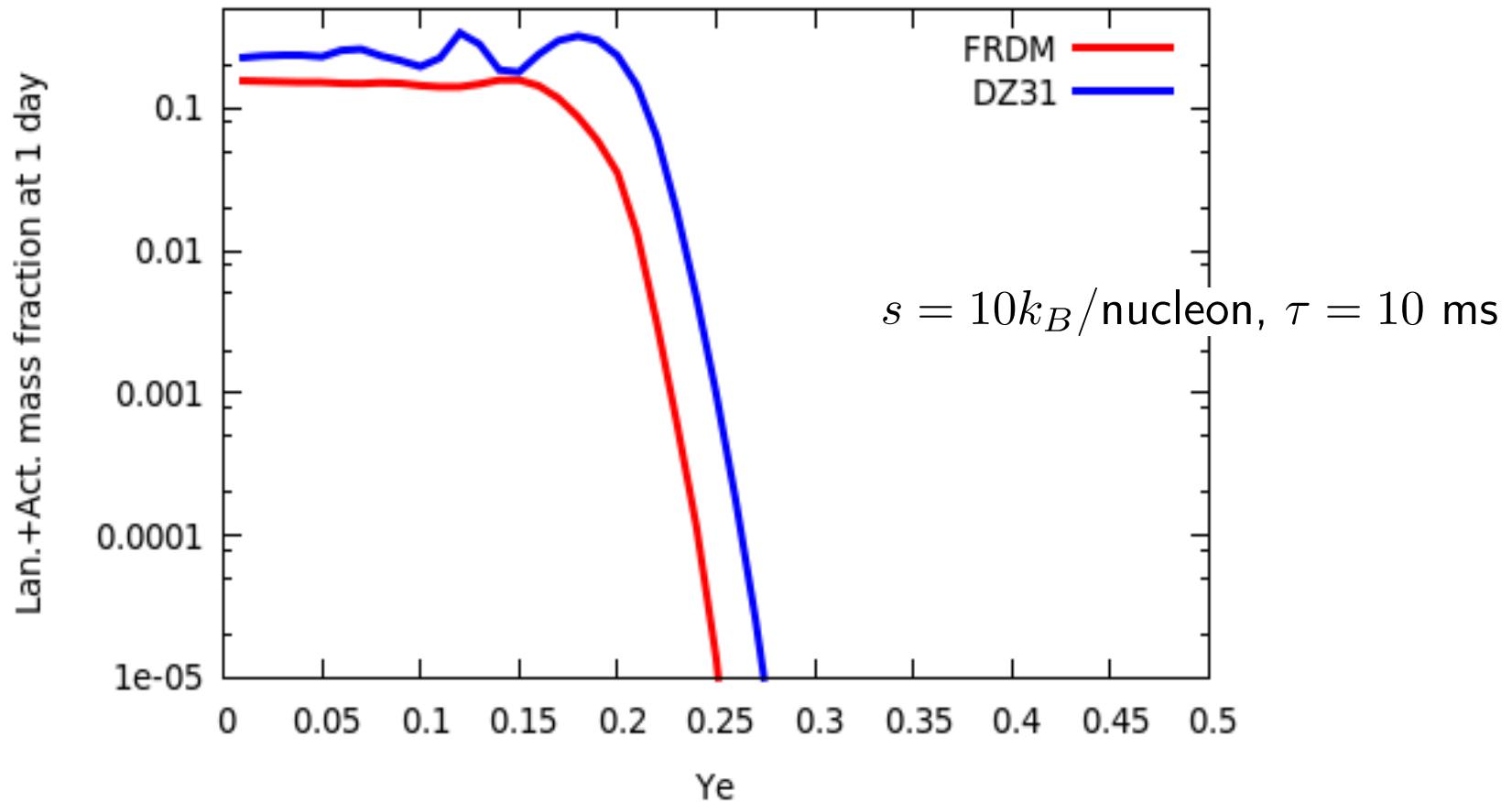
# Opacity source: lanthanides and actinides

The lanthanide turnover at  $Y_e \approx 0.25$



- not very sensitive to the initial entropy and the expansion timescale

## Opacity source: lanthanides and actinides

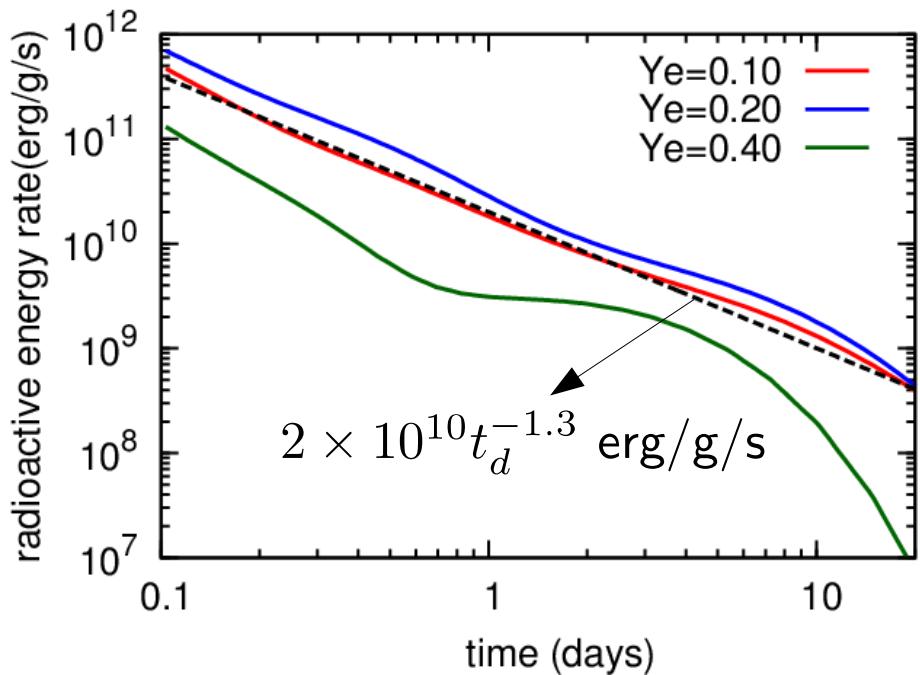
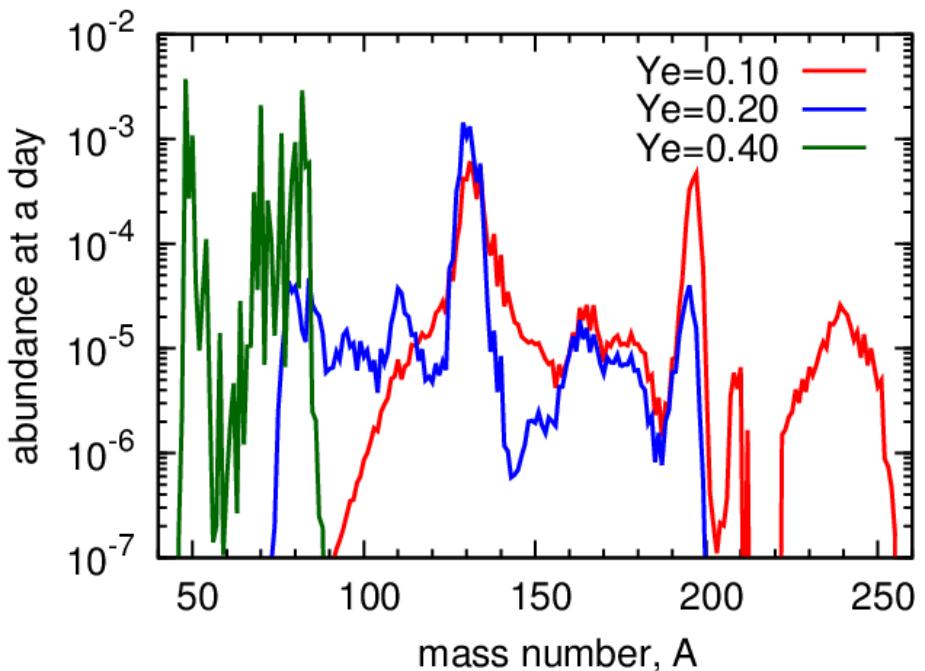


a relatively weak dependence of the lanthanide turnover on nuclear mass model inputs ( $\sim 0.02 - 0.03$ )

# Radioactive decay of the $r$ -process nuclei

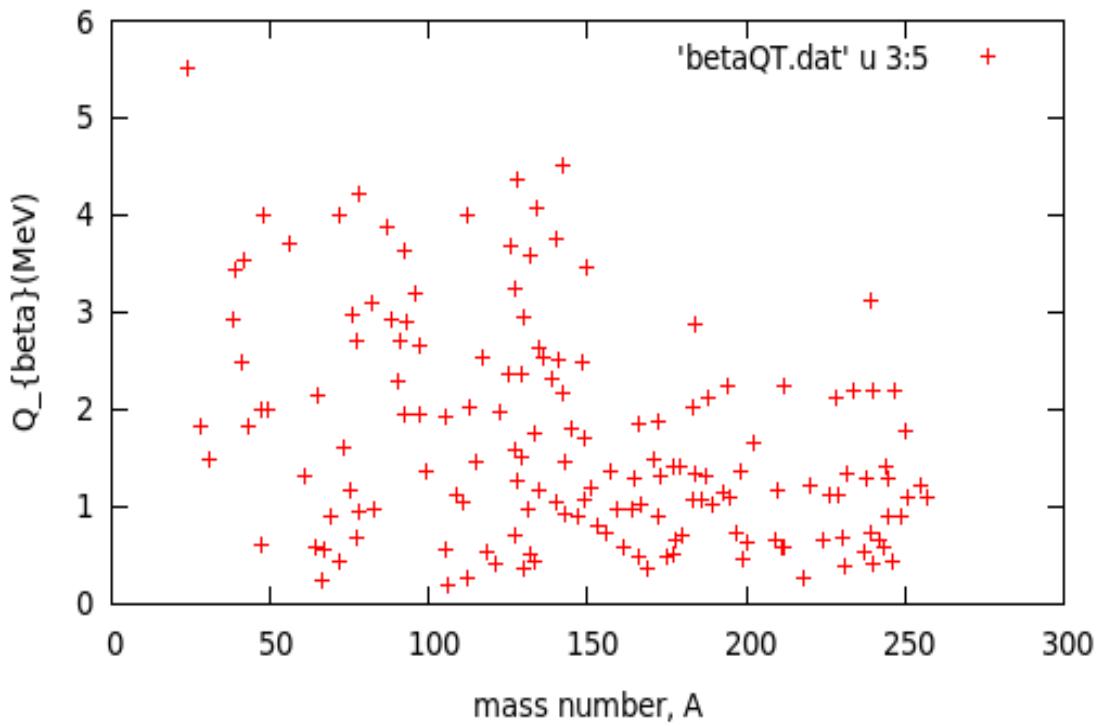
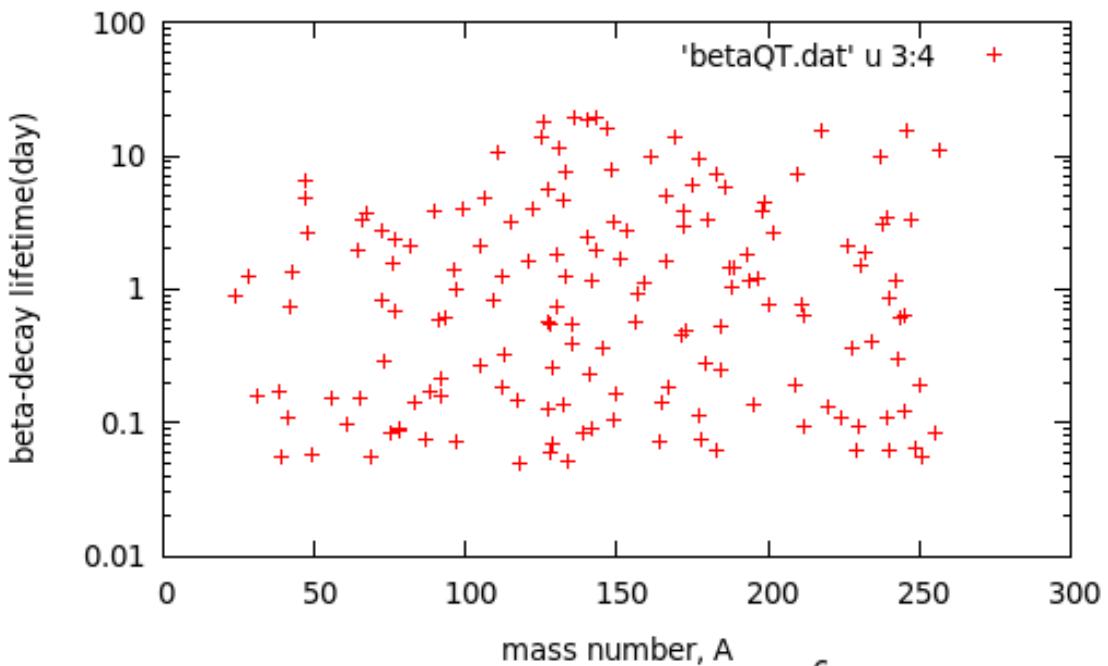
[Metzger+2010, Korobkin+ 2011, Hotokezaka+ 2016]

When the radioactive decay is governed by  $\beta$ -decay of a broad range of nuclei, the energy release rate can be approximated by a power law with an index  $\sim -1.3$

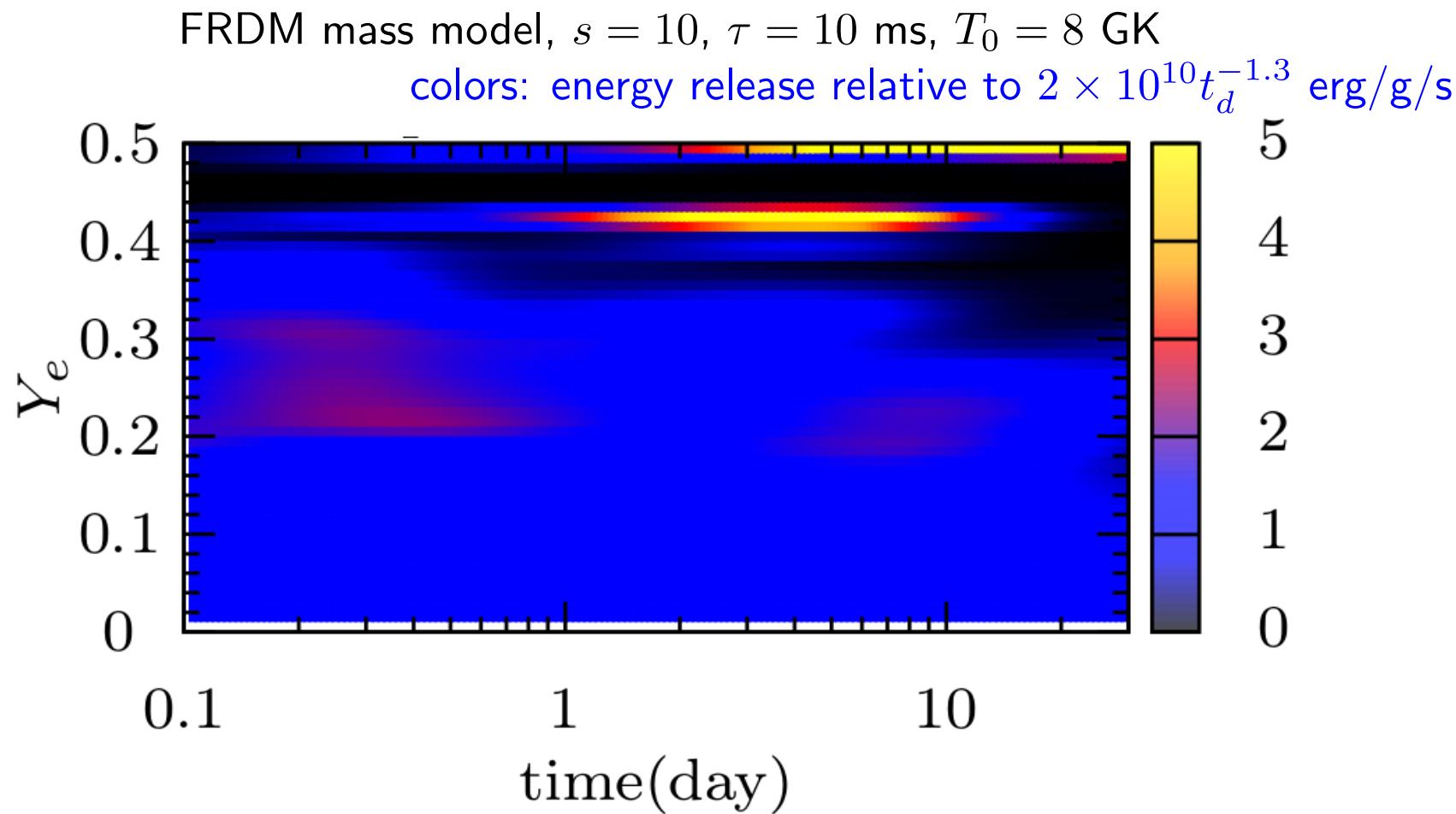


(see also Wanajo+2014, Tanaka+2017, ...)

(parametrized trajectory with entropy  $s = 10$  per nucleon and dynamical time scale  $\tau = 10$  ms, c.f. Lippuner & Roberts 2016)



- parametrized trajectories to broadly examine the impact of both the composition and nuclear physics on the radioactive heating (c.f. Lippuner Roberts 2016)

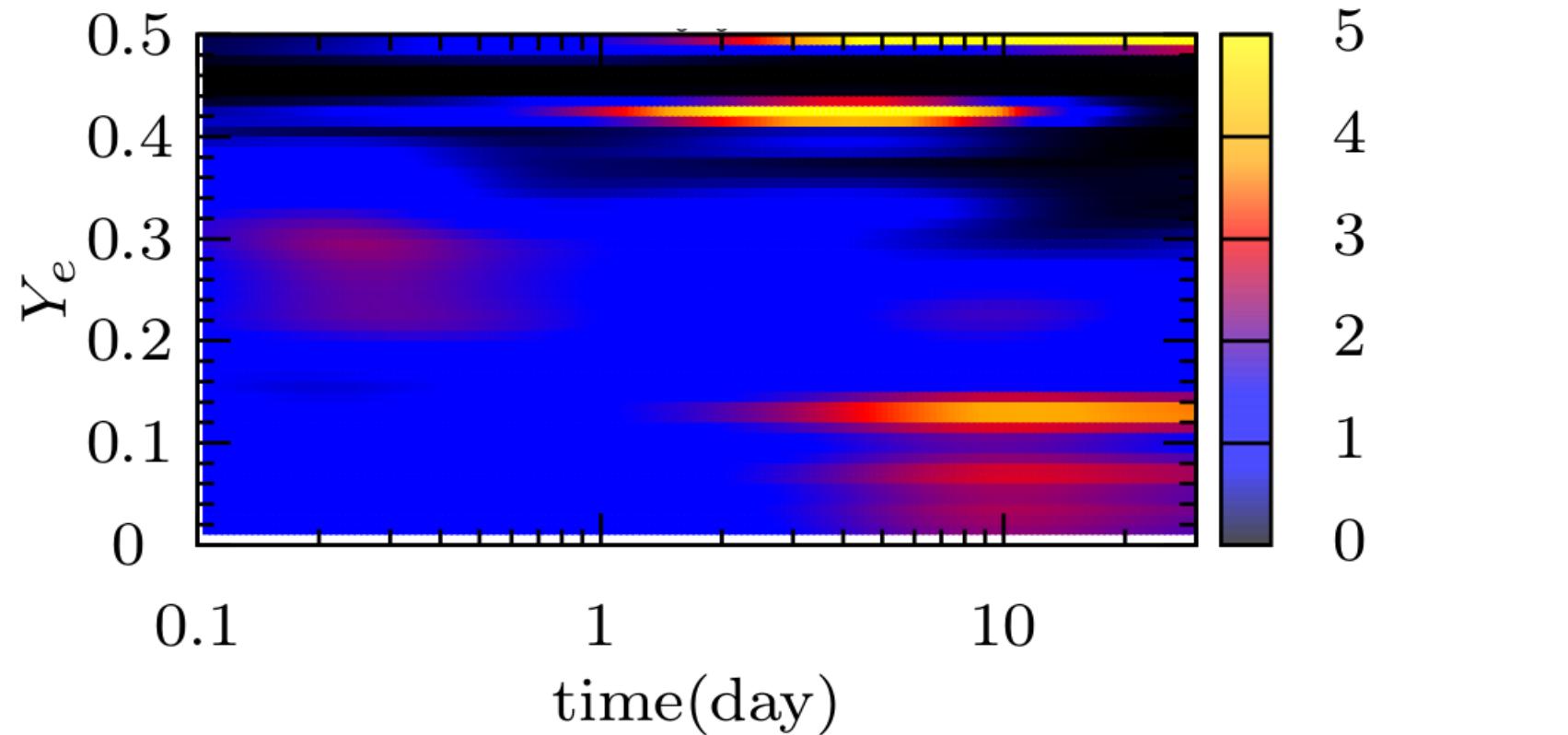


- the radioactive heating for  $Y_e \gtrsim 0.35$  is suppressed, except for i)  $Y_e \approx 0.42$  (Ni66 production) ii)  $Y_e \approx 0.5$  (Ni56 production)

- parametrized trajectories to broadly examine the impact of both the composition and nuclear physics on the radioactive heating (c.f. Lippuner Roberts 2016)

DZ31 mass model,  $s = 10$ ,  $\tau = 10$  ms,  $T_0 = 8$  GK

colors: energy release relative to  $2 \times 10^{10} t_d^{-1.3}$  erg/g/s



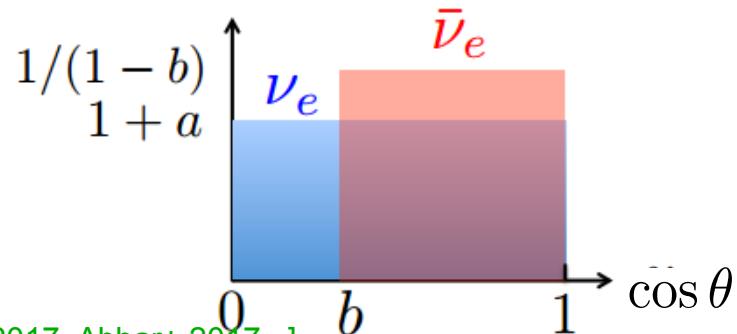
- $\alpha$ -heating may become dominant for ejecta with  $Y_e \lesssim 0.15$

Neutrino flavor conversion in merger remnant

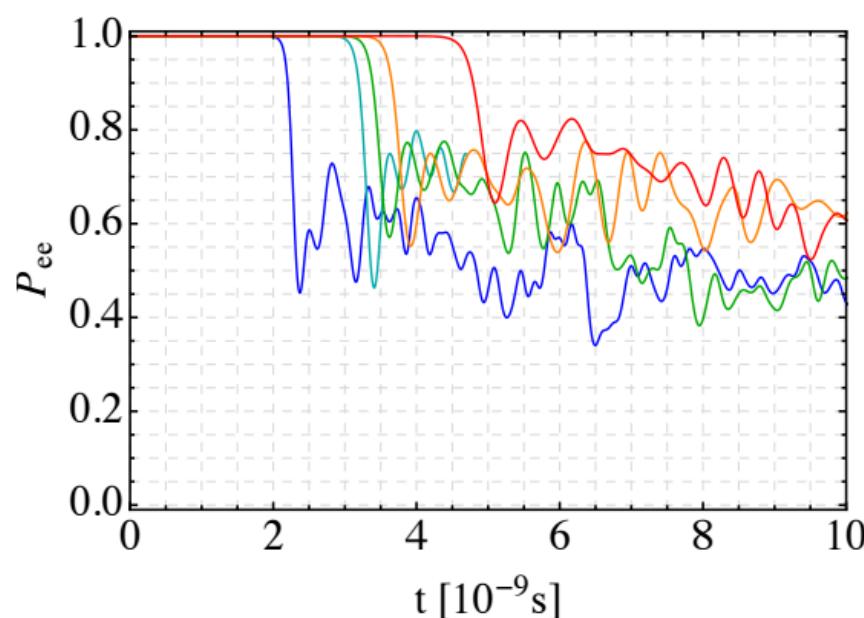
## Neutrino oscillations in neutrino-dense environment

“fast” conversion can happen extremely close to the  $\nu$  surfaces, provided that local angular distribution of neutrino lepton number has a “crossing” (more  $\bar{\nu}_e$  than  $\nu_e$  in some solid angle range, while more  $\nu_e$  than  $\bar{\nu}_e$  otherwise)

[Sawyer+ 2005, 2009, 2016, Izaguirre+ 2016-17, Dasgupta+ 2016, MRW+ 2017, Abbar+ 2017...]



→ flavor instability of time scale  $\tau \lesssim \mu^{-1} = (\sqrt{2}G_F n_\nu)^{-1}$ , which implies an oscillation length scale of  $\sim$  centimeters



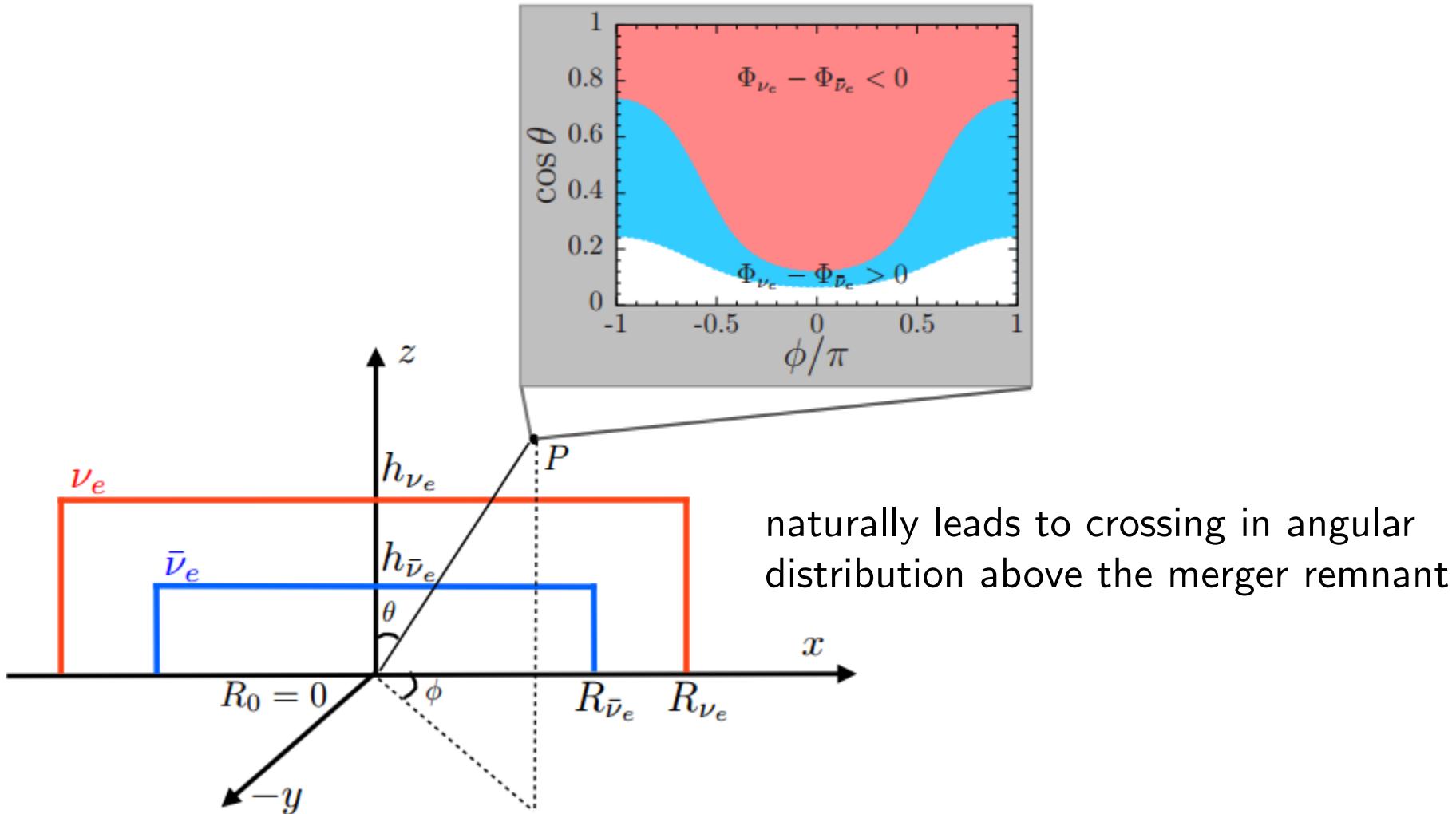
$$\begin{aligned}\mu &= 4 \times 10^5 \text{ km}^{-1} \\ a &= 0.1, b = 0.6 \\ a &= 0.2, b = 0.6 \\ a &= 0.1, b = 0.4 \\ a &= 0.1, b = 0.35 \\ a &= 0.1, b = 0.3\end{aligned}$$

[Dasgupta+ JCAP 1702, 019 (2017)]

# Fast $\nu$ oscillations in merger remnants – parametrized model

Why is this particularly relevant for merger remnants?

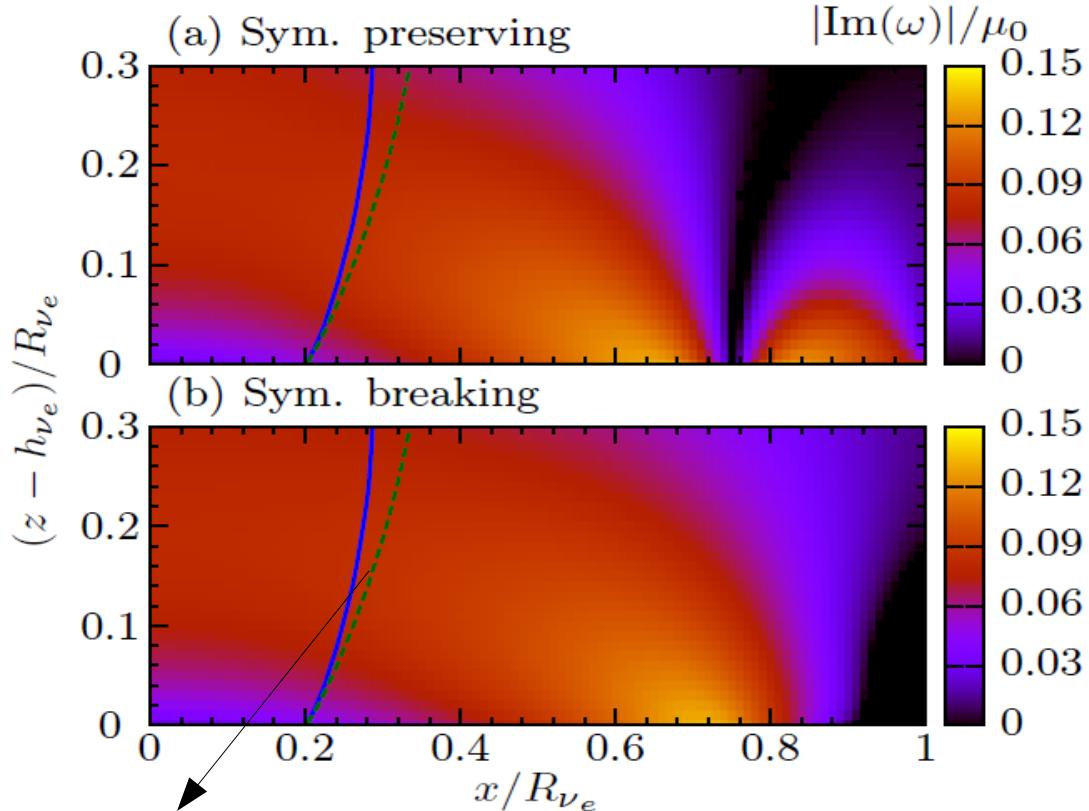
Because they **protonize**, i.e., more  $\bar{\nu}_e$  emission than  $\nu_e$  [Foucart+, Perego+, Janka+...]



# Fast $\nu$ oscillations in merger remnants – parametrized model

$$L_{n,\bar{\nu}_e}/L_{n,\nu_e} = 1.35, R_{\bar{\nu}_e} = 0.75R_{\nu_e}, h_{\nu_e}/R_{\nu_e} = h_{\bar{\nu}_e}/R_{\bar{\nu}_e} = 0.25, \vec{k} = 0.$$

[MRW & Tamborra, PRD 95, 103007, 2017]



$Im(\omega)$ : growth rate of flavor mixing in the linear regime

$$\mu_0 \approx 4.25 \text{ cm}^{-1} \times \left( \frac{L_{\nu_e}}{10^{53} \text{ erg/s}} \right) \left( \frac{10 \text{ MeV}}{\langle E_{\nu_e} \rangle} \right) \left( \frac{100 \text{ km}}{R_{\nu_e}} \right)^2$$

fast flavor conversion condition exists everywhere above the remnant, with any reasonable parameters

Matter-neutrino resonances [Malkus+, Zhu+, Frenzel+, MRW+,...]

- Flavor equipartition can affect dramatically the nucleosynthesis outcome in  $\nu$ -driven wind from a BH-disk system [MRW, Tamborra, Just, Janka, 2017]

angular distribution above the merger remnant from MC neutrino transport simulation

