

# Characterisation of radiation-damaged SiPMs

S. Cerioli, E. Garutti, R. Klanner, D. Lomidze, S. Martens,  
J. Schwandt, M. Zvolsky



Hamburg University



## 1. Aims

## 2. SiPMs + measurements

## 3. Results

3.1 C-V: Electrical parameters and doping profile

3.2  $I_{\text{dark}}$ :  $V_{\text{bd}}$ , DCR

3.3  $PH_{\text{dark}}$ : DCR

3.4  $PH_{\text{light}}$ : photo-detection

## 4. Conclusions + next steps

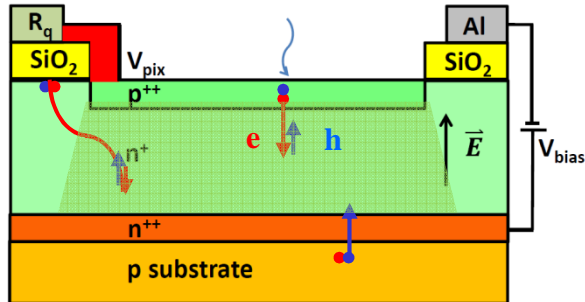
# Aims + SiPMs investigated

**Aim:** Develop and test **methods** to characterise hadron-damaged SiPMs

- Demonstrate them on a specific SiPM → which is the best method?
- Which parameters change with fluence? → physics of damage → Improvements?
- Quantify optimal operating conditions + pulse shaping for a given task

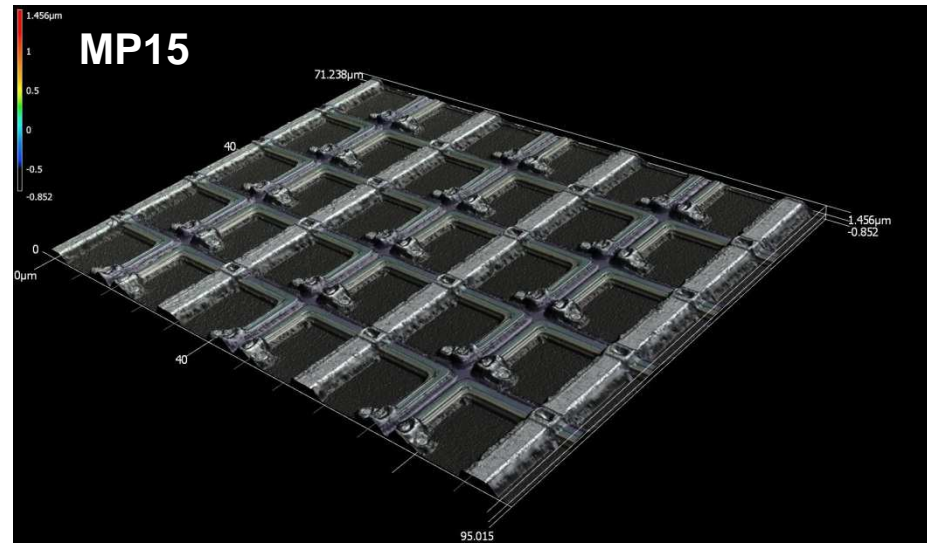
**SiPM:** KETEK MP15<sup>\*)</sup> with 4384 pixels  $15 \times 15 \mu\text{m}^2$

n-irradiated at JSI (reactor) to  $10^9$ ,  $10^{11}$ ,  $5 \cdot 10^{11}$ ,  $10^{12}$ ,  $5 \cdot 10^{12}$ ,  $10^{13}$ ,  $5 \cdot 10^{13}$ ,  $5 \cdot 10^{14} \text{ cm}^{-2}$



- Depth ampli-region  $\sim 1 \mu\text{m}$
- $V_{bd} \approx 27.5 \text{ V}$  at  $20^\circ\text{C}$
- $V_{off} \approx V_{bd} - 850 \text{ mV}$
- $R_q$  poly-Si

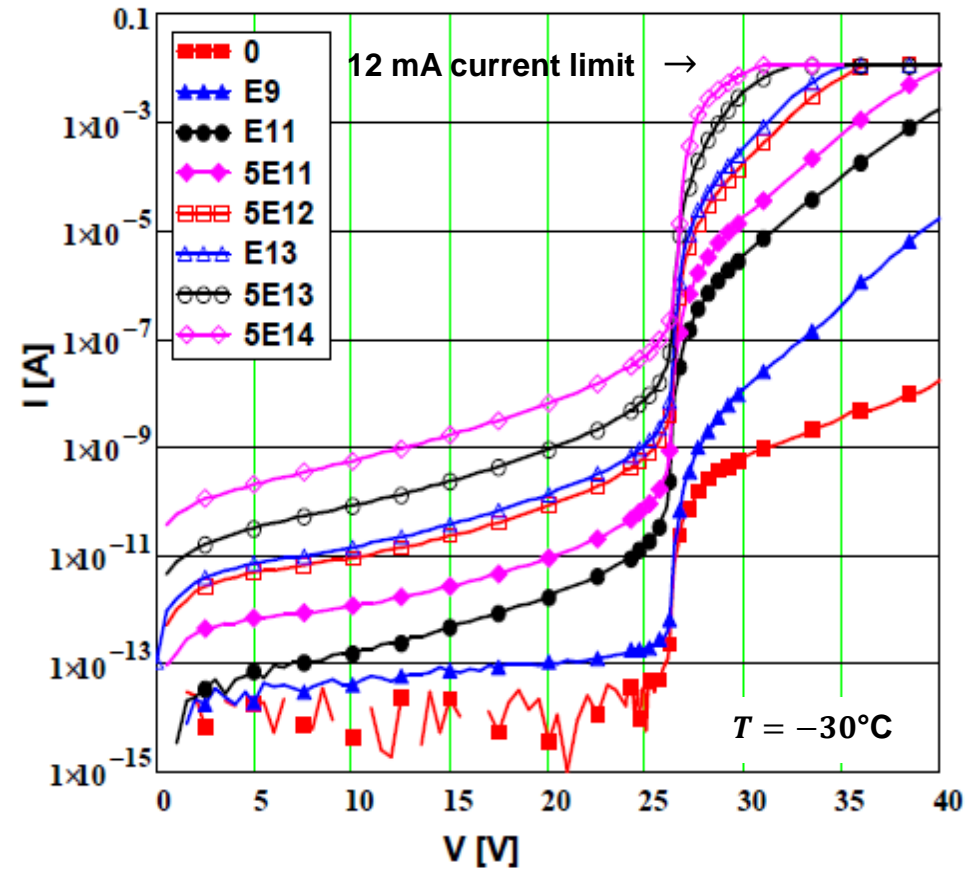
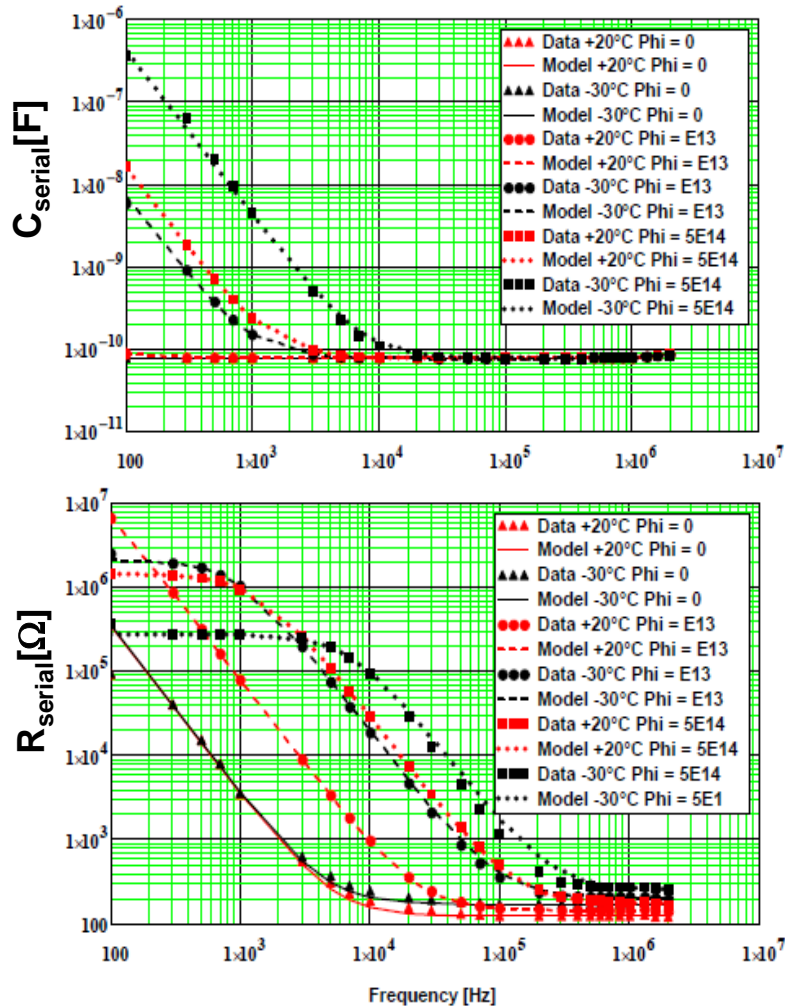
<sup>\*)</sup> SiPM well studied @ UHH  
(RK. et al., NIM-A 854 (2016) 70)



# Measurements

**C/G-V:**  $V = 0 \dots 26.5 \text{ V}$ ,  $f = 100 \text{ Hz} \dots 2 \text{ MHz}$   
 $T = -30^\circ\text{C}$  and  $+20^\circ\text{C}$

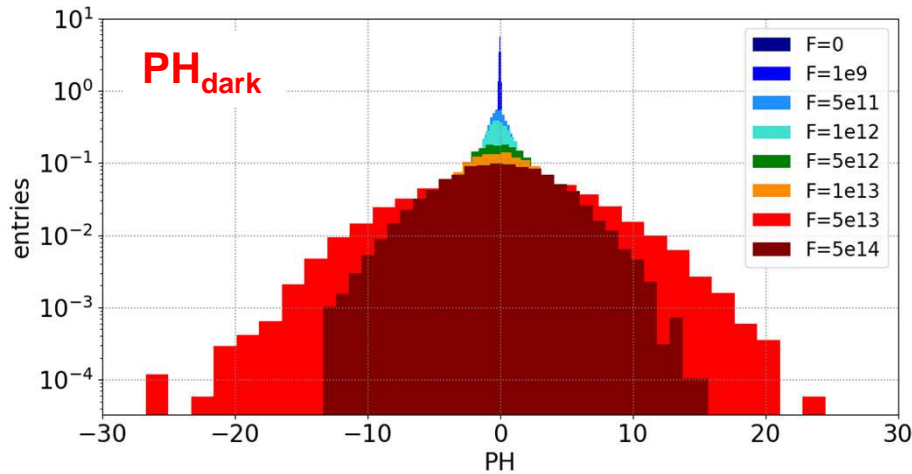
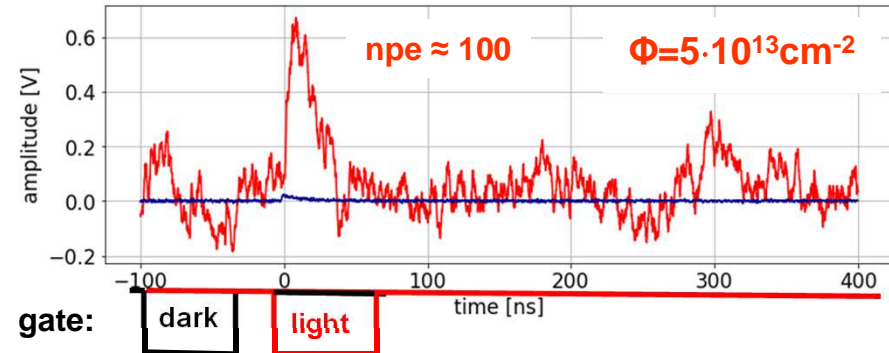
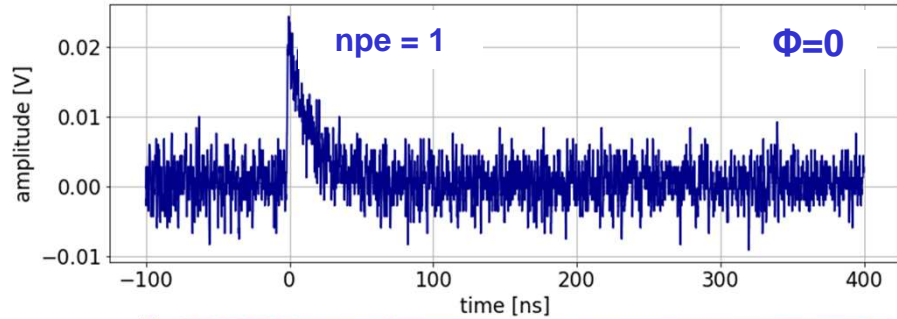
**$I_{\text{dark}}$ :**  $V = -2 \dots +35 (40) \text{ V}$ ,  
 $T = -30^\circ\text{C}$  and  $+20^\circ\text{C}$



**$I_{\text{dark}}$  used in analysis**

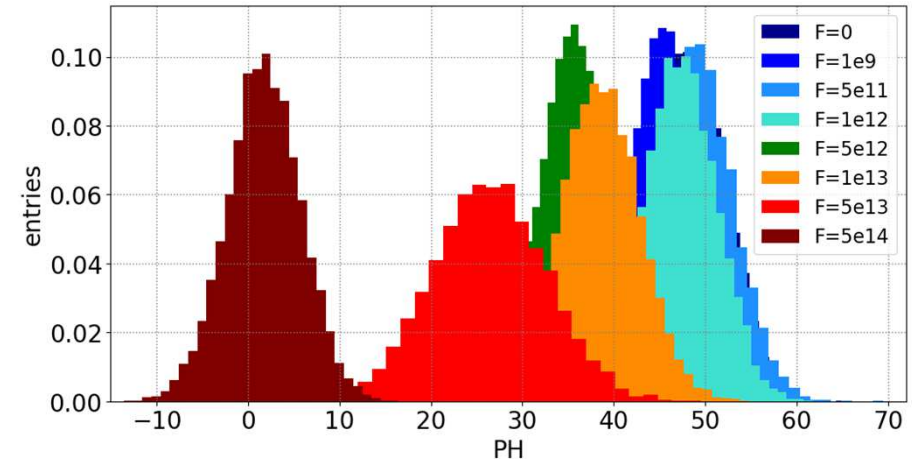
# Measurements

**Current transients:**  $V = 27.7 \dots 30.5V$ ,  $T = -30^\circ C \rightarrow PH_{\text{dark}}$  and  $PH_{\text{light}}$ -spectra  
for  $t_{\text{gate}} = 15 \dots 75 \text{ ns}$



**$Var_{\text{dark}}$  used in analysis**

$$Var_{\text{light}} = Var_{\text{light}}^{\text{meas}} - Var_{\text{dark}}$$



**$Mean_{\text{light}} + Var_{\text{light}}$  used in analysis**

# Parameters and formulae for analysis

$C_{pix}$  ... pixel capacitance  
 $R_q$  ... quenching resistance  
 $C_q$  ... quenching capacitance  
 $V_{bd}$  ... breakdown voltage  
 $V_{off}$  ... Geiger turnoff voltage  
 DCR ... dark count rate

pulse shape (slow comp.):  $\tau = C_{pix} \cdot R_q$

$$Gain \approx (C_{pix} + C_q) \cdot (V - V_{off}) \cdot f_{gate}$$

( $f_{gate}$  ... fraction of signal in gate)

$$I_{dark} = DCR \cdot EQF \cdot Gain (f_{gate} = 1)$$

EQF ... excess charge factor  $EQF = \frac{Mean}{Mean_{Poisson}}$

ENF ... excess noise factor  $ENF = \frac{Var/Mean^2}{Var_{Poisson}/Mean^2_{Poisson}}$

PDE ... photon detection efficiency

$\mu$  ... no. photons initiating Geiger discharge

$$\mu = Mean_{Poisson} = Var_{Poisson}$$

$$Mean = \mu \cdot Gain \cdot EQF$$

$$Var = \mu \cdot Gain^2 \cdot EQF^2 \cdot ENF$$

→ 3 ways to obtain  $\mu$  +

$$\rightarrow Gain = \frac{Var}{Mean \cdot EQF \cdot ENF}$$

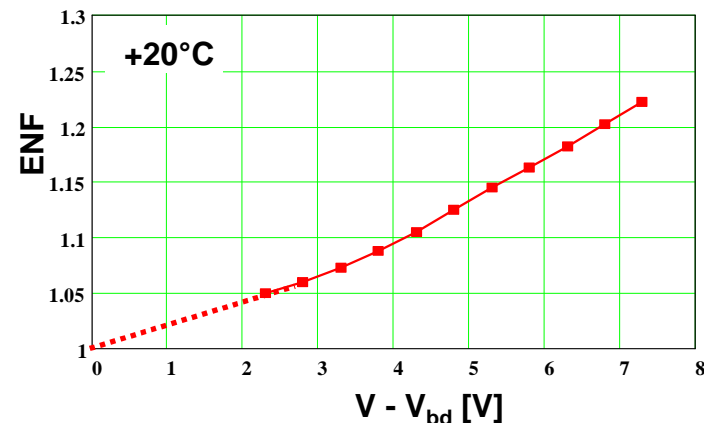
**N.B:** valid if **no saturation effects!**

$V_{bd} - V_{off} \approx 850$  mV from high statistics  $\Phi=0$  data at +20°C

→ assume  $V_{bd} - V_{off}$  does not depend on  $\Phi, T$

EQF and ENF determined from high statistics  $\Phi=0$  data at +20°C → for most cases a small correction

find:  $EQF \approx ENF$



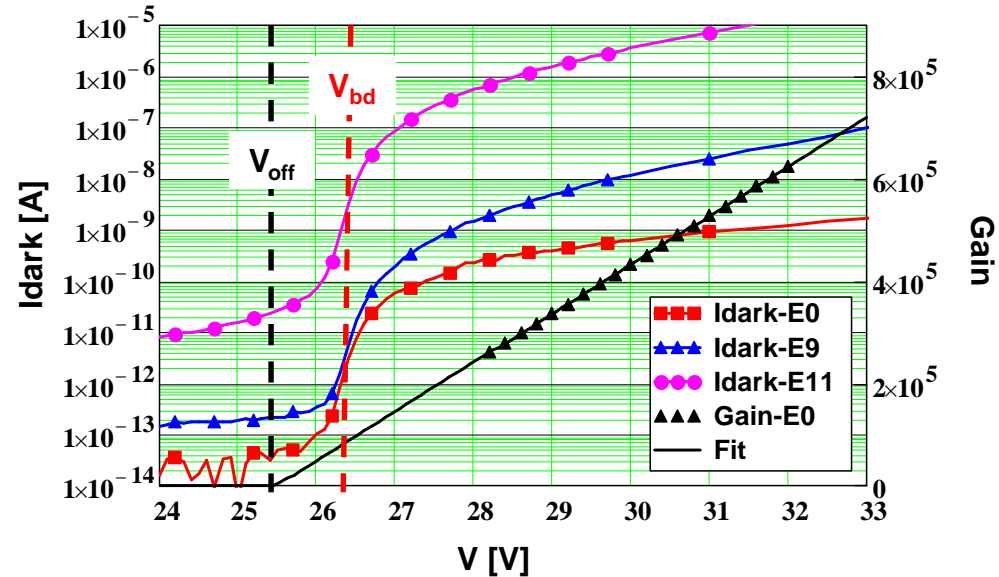
## $V_{bd}$ versus $V_{off}$

From PH-fits:  $Gain(V) \rightarrow$  find  $Gain(V) = dGain/dV \cdot (V - V_{off}) \rightarrow$  with  $dGain/dV = \text{const}$   
 $\rightarrow$  straight line describes  $Gain(V) \rightarrow V_{off}$  from extrapolation to  $Gain = 1$  ( $f_{gate} = 1$ )

$\rightarrow$  for  $t_{gate} = 75$  ns (compatible results for other  $t_{gate}$  values):

$dGain/dV = 9.75 \cdot 10^4 \text{ V}^{-1}$  (compare to:  $C_{pix}/q_0 = 17.8 \text{ fF}/1.6 \cdot 10^{-19} \text{ C} = 11.1 \cdot 10^4 \text{ V}^{-1} \approx \text{ok}$ )

$V_{off} = V_{bd} - 850 \text{ mV}$



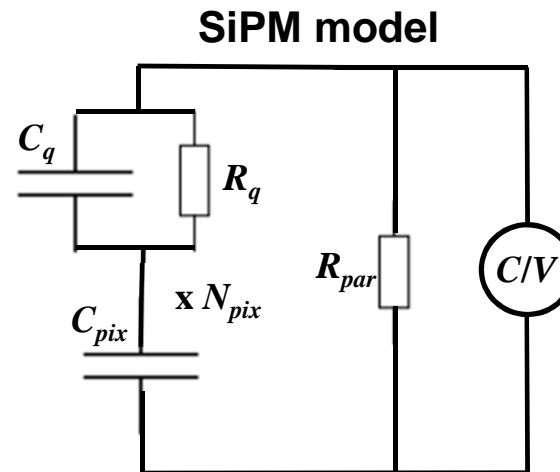
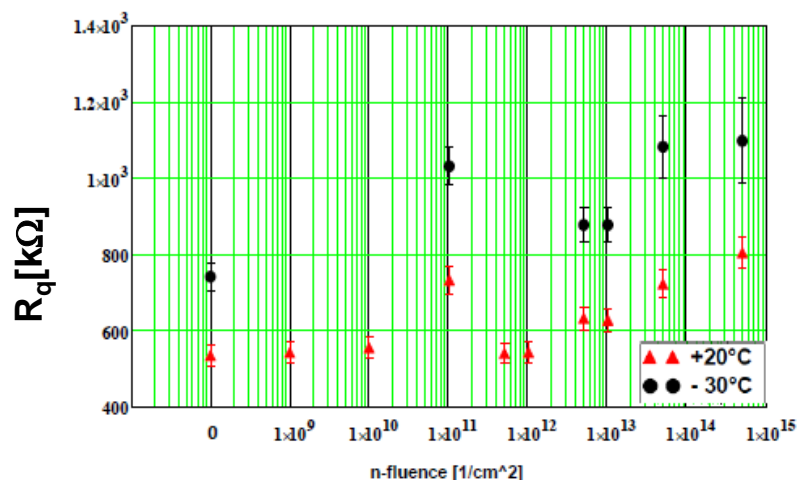
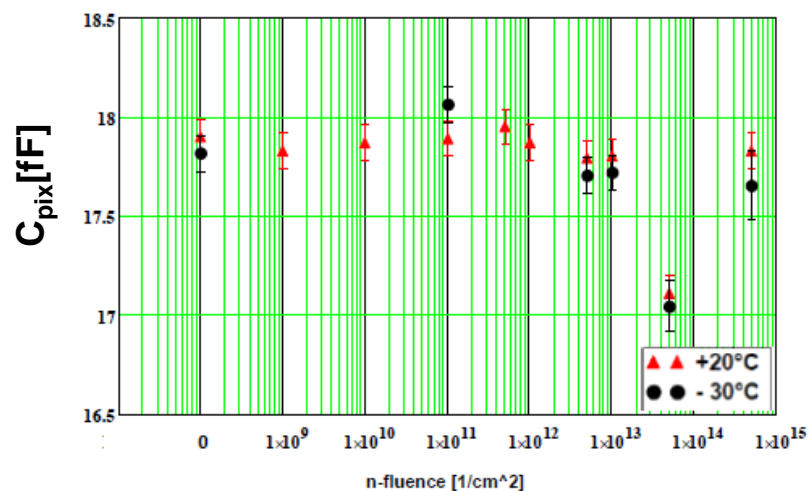
**Difference:  $V_{bd} - V_{off} \approx 850$  mV to be taken into account for analysis**

**for further analysis assume no dependence of  $V_{bd} - V_{off}$  on  $\Phi$**

**$dGain/dV \approx$  compatible with  $C_{pix}/q_0$**

# C-V measurements and $C_{pix}$ , $R_q$ , $C_q$

Dependence of  $C_{pix}$  and  $R_q$  on  $T$  and  $\Phi$  (neutron fluence):



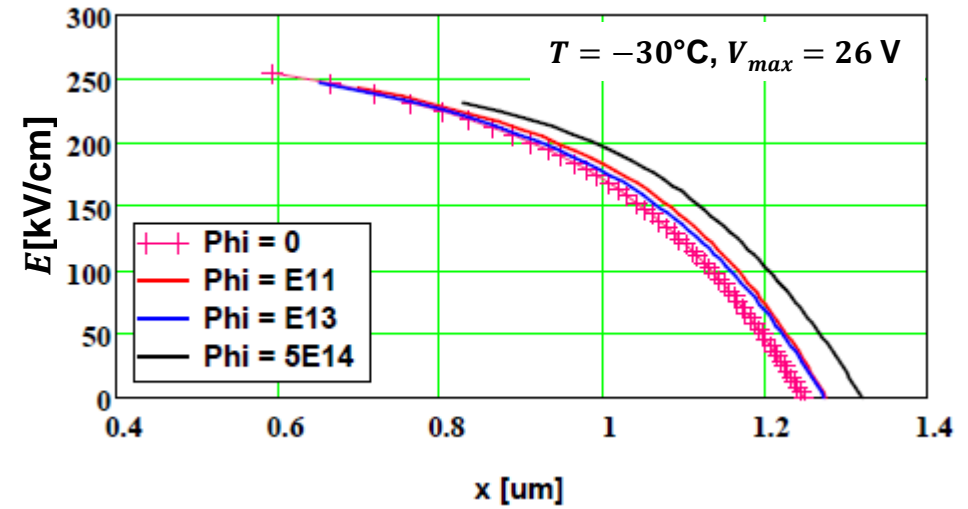
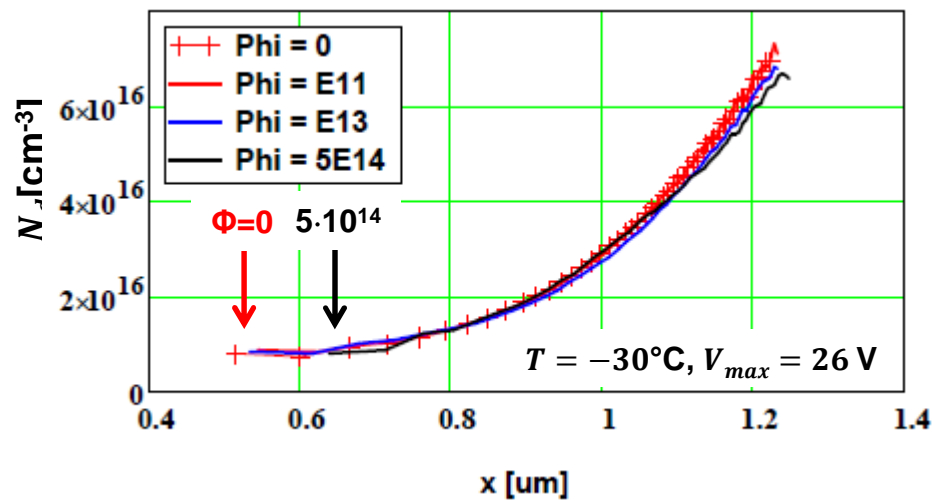
- Upper limit  $C_q < 5$  fF ( $\sim 1$  fF-pulse shape)
- Significant differences for SiPM samples

$C_{pix}$  not influenced by  $T$  and  $\Phi$   
 $R_q$  increases with decreasing  $T$  (poly-Si)  
 $R_q$  appears to increase for  $\Phi > 10^{13}$  cm<sup>-2</sup>

# C-V measurements: Doping and E-field

Doping profile  $N_d(x)$  and E-field  $E(x)$  assuming 1-D abrupt p+n-junction:

$$x(V) = \frac{\epsilon_0 \epsilon_{Si} A}{C(V)} \quad N_d(x) = \frac{2}{q_0 \epsilon_0 \epsilon_{Si} A^2} \cdot \frac{1}{d(1/C^2)/dV} \quad E(x) = \int_{x_{max}}^x \frac{q_0 N_d(x)}{\epsilon_0 \epsilon_{Si}} dx \quad A = N_{pix} \cdot pitch^2$$

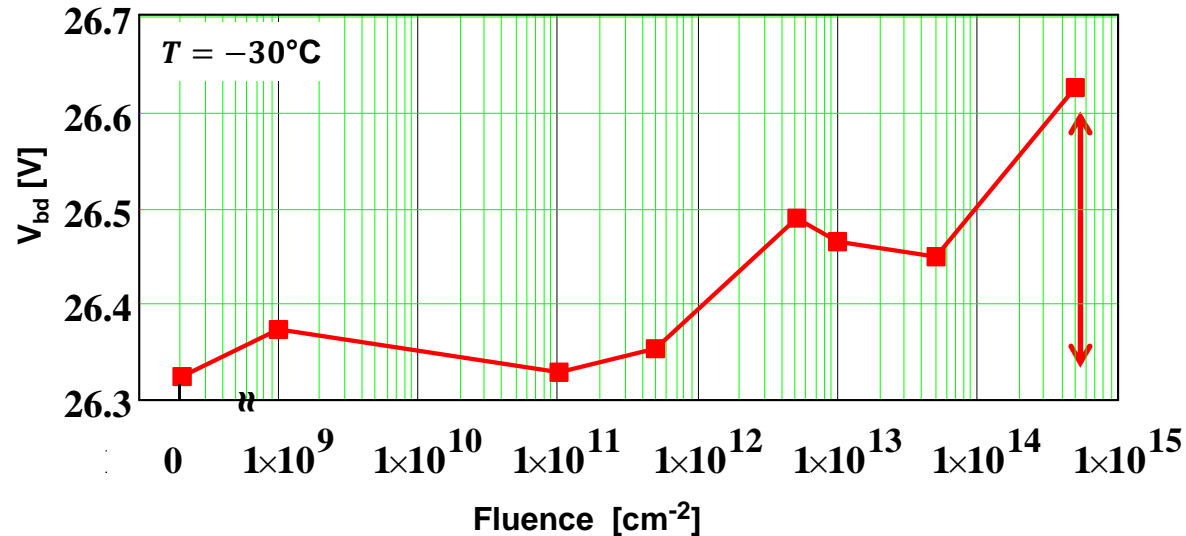


**Minor decrease of  $N_d$  for  $\Phi = 5 \cdot 10^{14} \text{ cm}^{-2}$   
(expected from radiation-induced donor removal)**



# Breakdown voltage $V_{bd}$

$V_{bd}$  using max(ILD) with  $ILD = (d \ln |I| / dV)^{-1}$



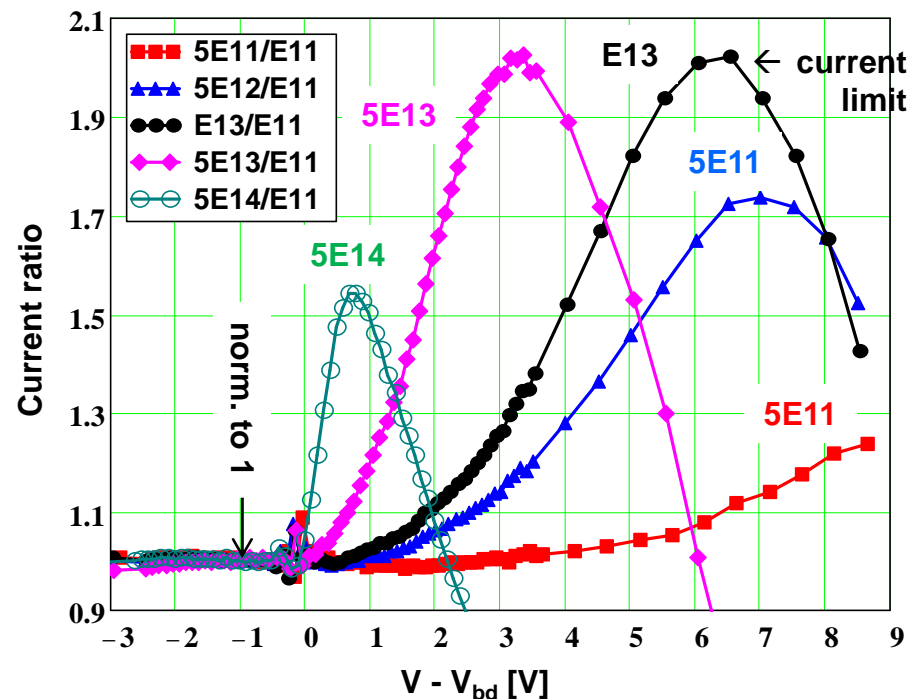
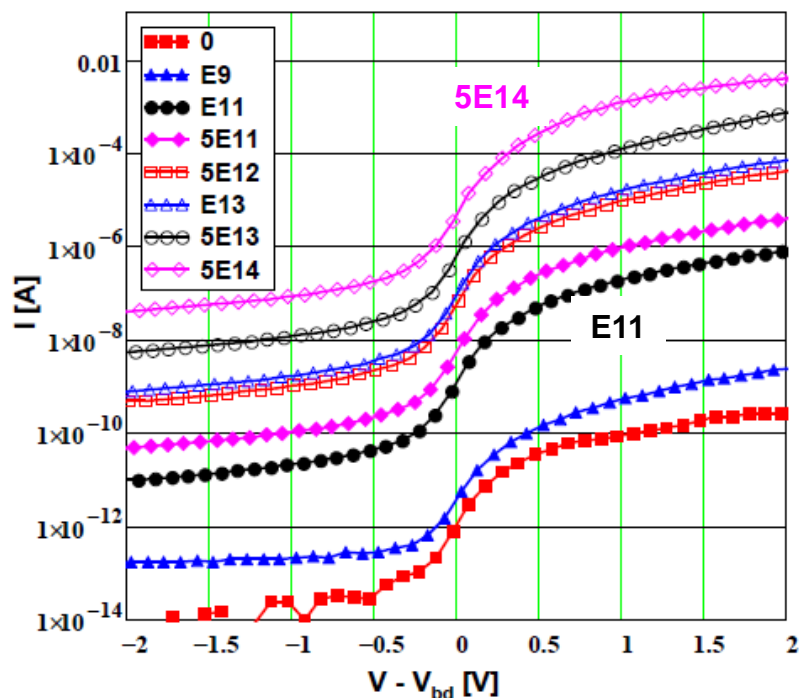
Only at +20°C  $I_{dark}$  measured for all SiPMs for  $\Phi = 0 \rightarrow$  variations observed

$\rightarrow$  difference  $V_{bd}(\Phi) - V_{bd}(\Phi = 0)$  significant only at  $5 \cdot 10^{14} \text{ cm}^{-2}$

**$V_{bd} \approx \text{const. up to } \approx 5 \cdot 10^{13} \text{ cm}^{-2}$**   
**Increase by  $\approx 300 \text{ mV}$  at  $5 \cdot 10^{14} \text{ cm}^{-2}$**

# Dark current vs. fluence and voltage

Does  $I_{dark}(V - V_{bd})$  scale with  $\Phi$ ?  $\rightarrow R_{dark} = I_{dark}(\Phi)/I_{dark}(10^{11})$  vs.  $V - V_{bd}$



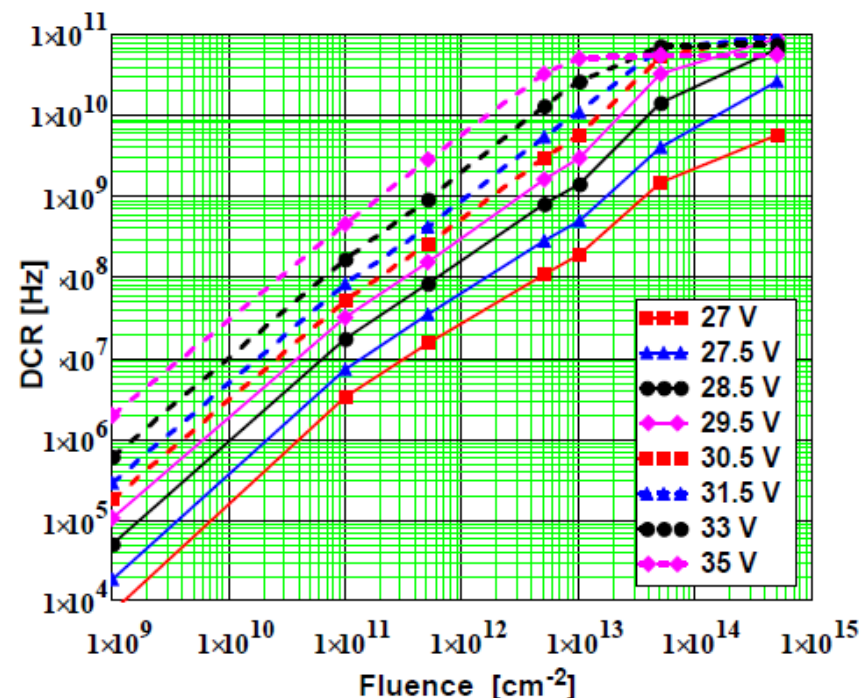
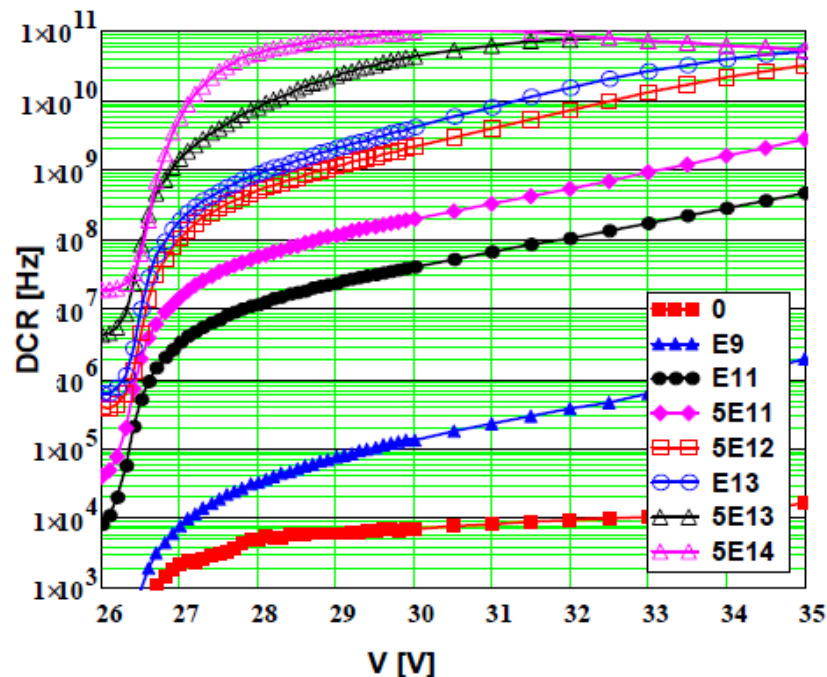
$\rightarrow V < V_{bd} \rightarrow R_{dark} \approx \text{const}$ ; for  $V > V_{bd}$  increase by factor up to 2 with  $V$

**Model:**  $I_{dark} = DCR \cdot (C_{pix} \cdot (V - V_{off})) \cdot EQF \rightarrow \times 2$  by  $EQF$  and gain implausible  $\rightarrow$  **assume change due to DCR  $\rightarrow$  "trap assisted high-field generation"?**

**$I_{dark}(\Phi)/I_{dark}(10^{11})$  increases with  $V - V_{bd}$ : higher  $\Phi \rightarrow$  faster increase**

# DCR vs. fluence and voltage

**Model:**  $I_{dark} = DCR \cdot (C_{pix} \cdot (V - V_{off})) \cdot EQF$  assume  $C_{pix} = 18$  fF  
 ( $V_{bd} - V_{off} = 850$  mV and  $ESF$  from  $\Phi = 0$  data)



**Comment:** Estimate fraction of busy pixels (occupancy)  $\approx (DCR \cdot \tau) / N_{pix} \approx 0.5$  for  $DCR = 10^{11} \text{ s}^{-1}$ ,  $\tau = 20 \text{ ns}$ ,  $N_{pix} = 4384$

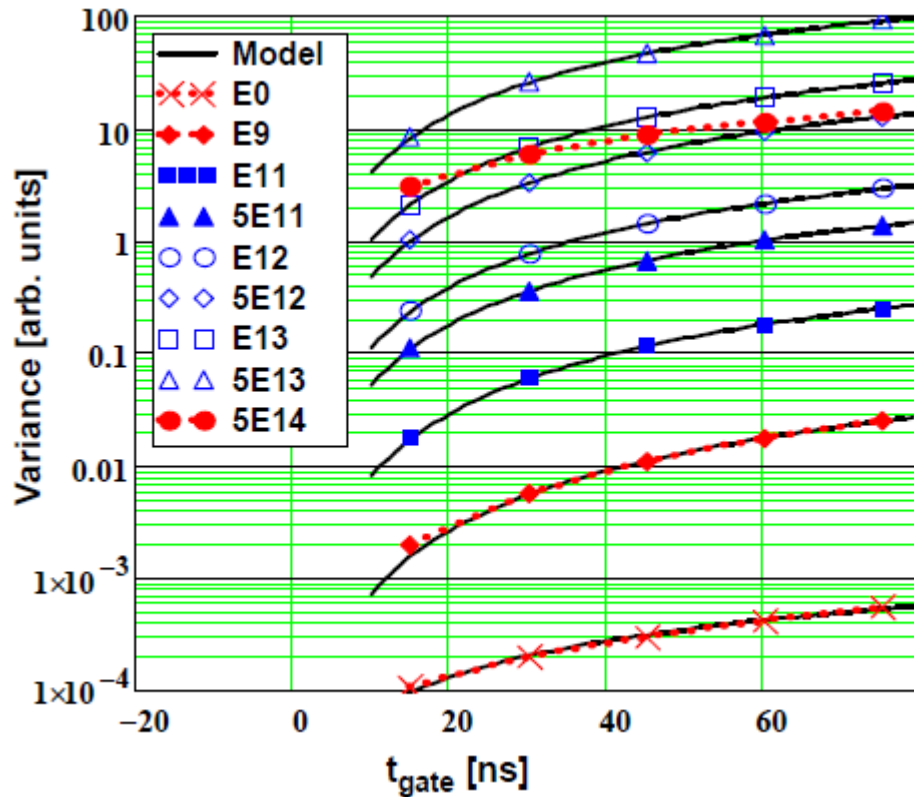
$I_{dark}(\Phi, V)$  allows estimation of  $DCR(\Phi, V)$

→  $V$ -dependence of  $DCR$  very different after irradiation!

→ Exponential increase for  $V - V_{bd} > 2 \text{ V}$  + saturation at high  $\Phi$

# PH<sub>dark</sub> – irradiated SiPM

$Var_{dark}(t_{gate})$  vs.  $\Phi$  at  $-30^\circ\text{C}$ :



1 pulse  $(e^{-t/\tau})/\tau$  per sec in random gate  $t_{gate}$ :

$$var_1 = t_{gate} - \tau(1 - e^{-t_{gate}/\tau})$$

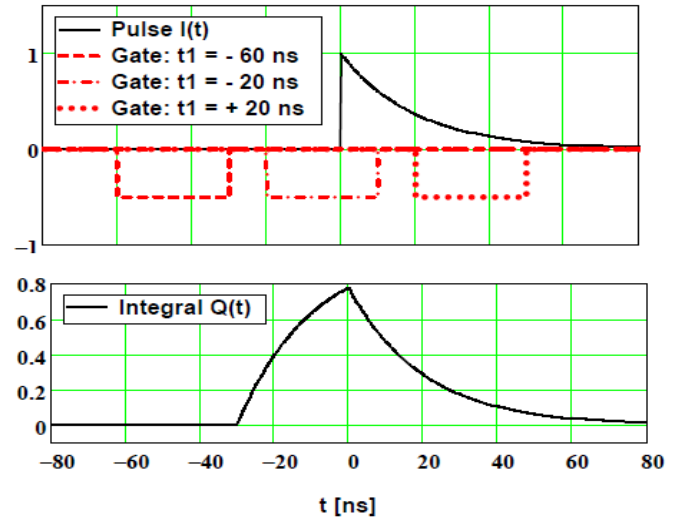
→ Solid curves, which describe data ( $\tau \approx 20$  ns)

$\Phi=5E14$

... poor fits

$\Phi=E9$

$\Phi=0$



Gain = 1 no CN (corr. noise):  $var_1 \cdot DCR$

Gain  $\neq$  1 no CN:  $Gain^2 \cdot var_1 \cdot DCR$

+ CN:  $Var = ENF \cdot EQF^2 \cdot Gain^2 \cdot var_1 \cdot DCR$

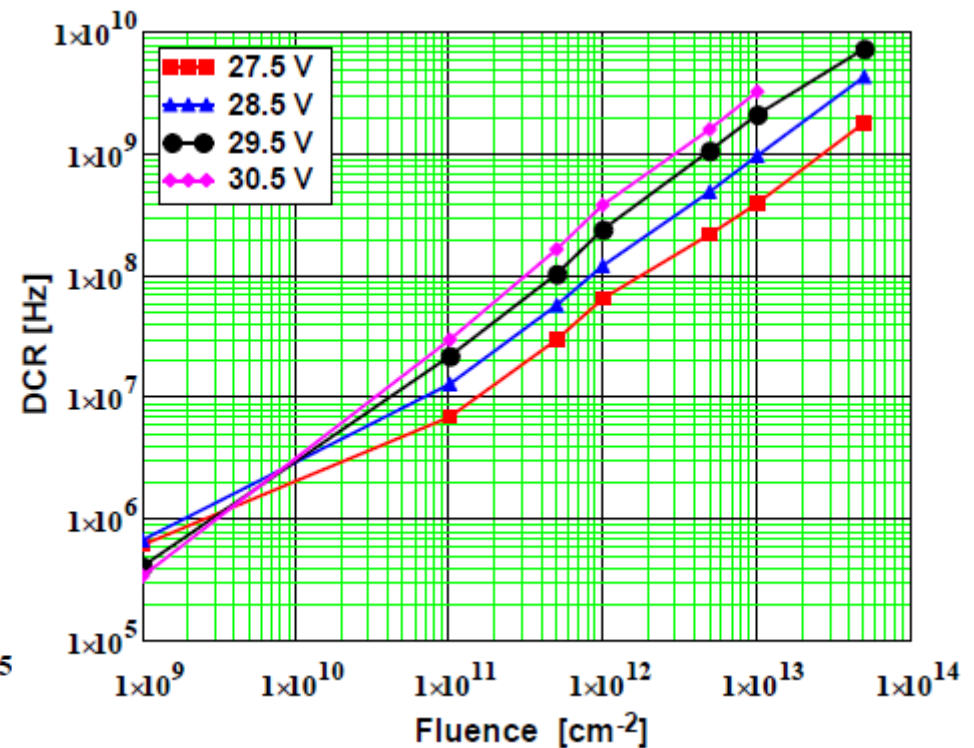
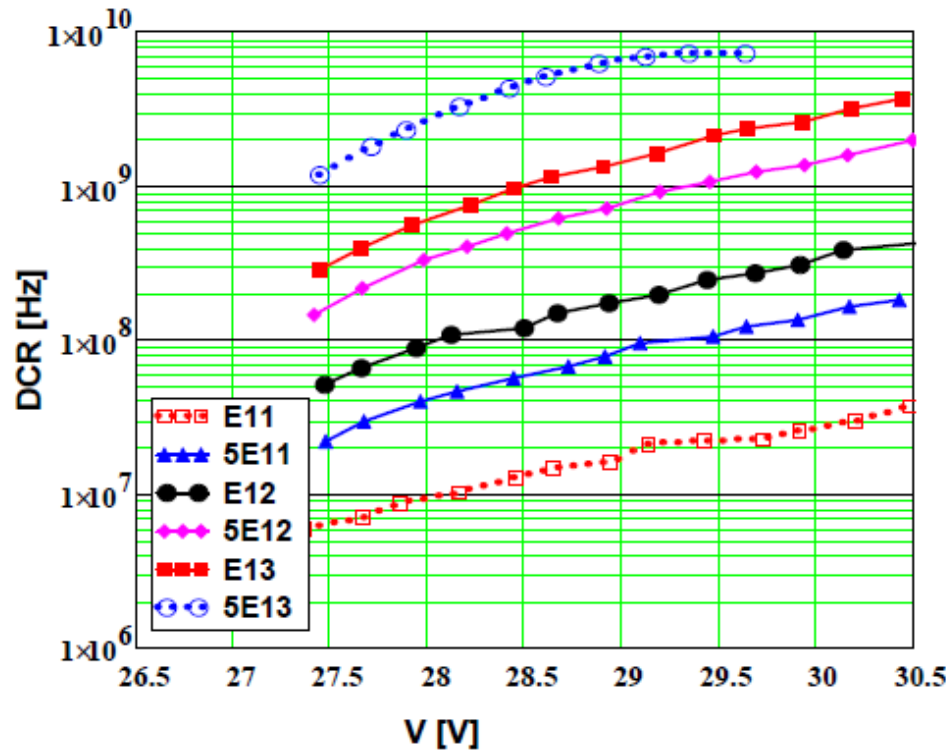
(N.B. only valid in absence of saturation)

$t_{gate}$  – dependence of  $Var$  → described by model for  $10^{11} < \Phi < 5 \cdot 10^{12} \text{ cm}^{-2}$

$Var$  allows to estimate  $\tau$  and  $DCR$  (if no strong saturation effects)

# PH<sub>dark</sub> – irradiated SiPM – DCR

$$Var = ENF \cdot EQF^2 \cdot Gain^2 \cdot var_1 \cdot DCR \rightarrow DCR = \frac{Var}{ENF \cdot EQF^2 \cdot Gain^2 \cdot (t_{gate} - \tau(1 - e^{-t_{gate}/\tau}))}$$



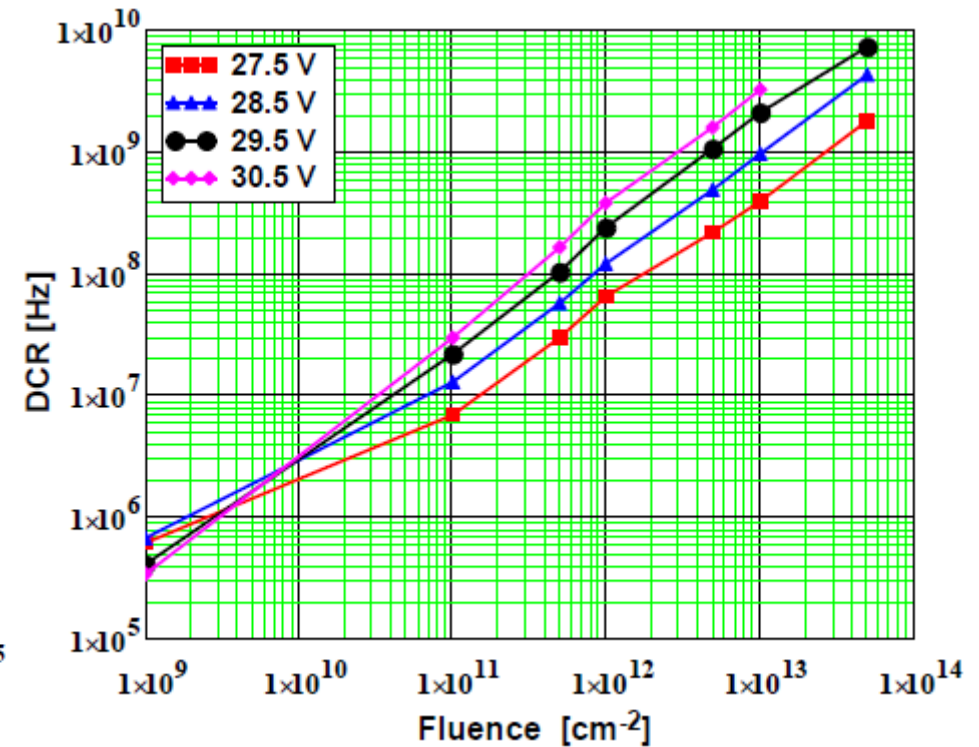
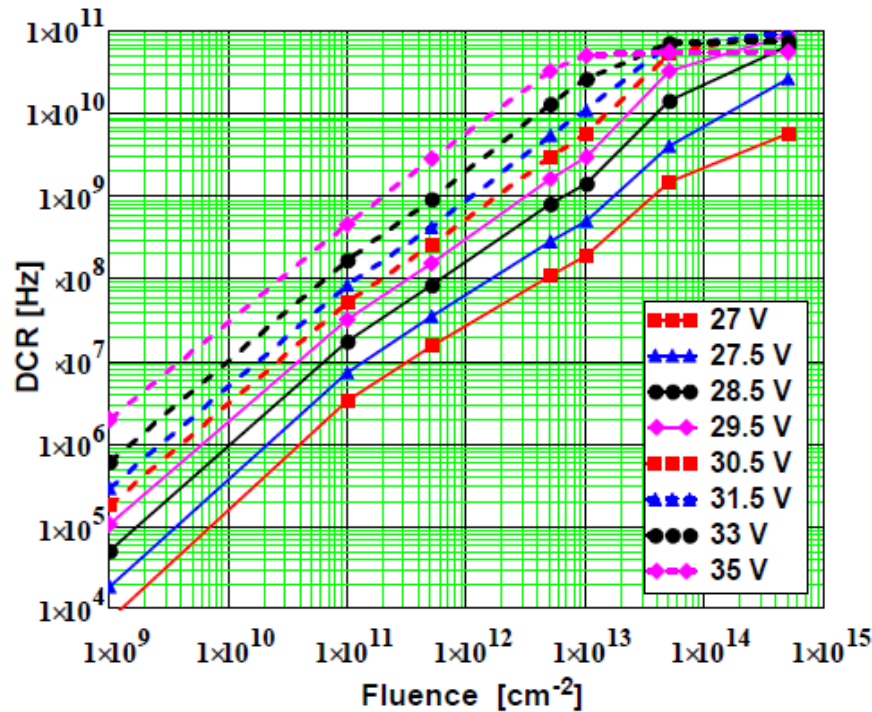
**DCR-results agree within  $\approx 30\%$  with results from  $I_{dark}$**

***Var*-method more complicated and range of validity limited**

**Differences may help to better understand rad.damage effects on SiPMs ???**

# Comparison of $V_{ar}$ and $I_{dark}$ method

Comparison:

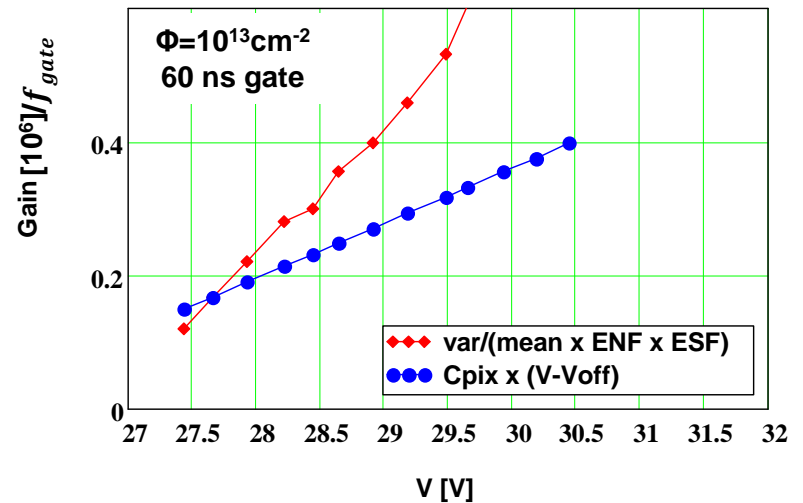
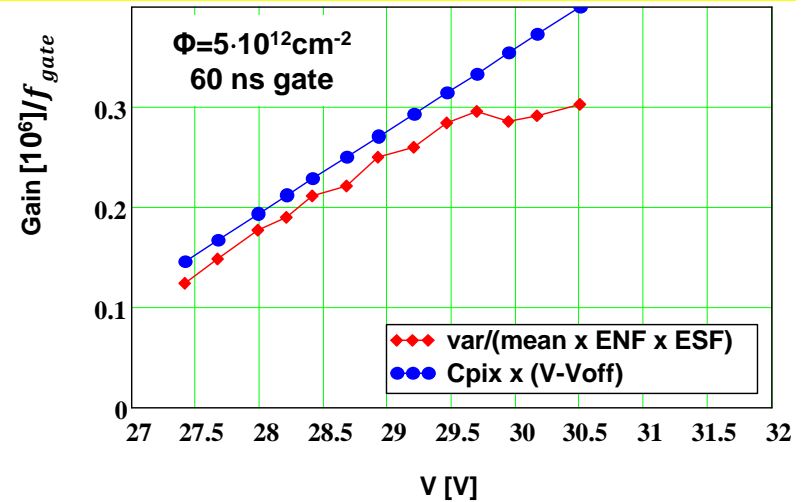
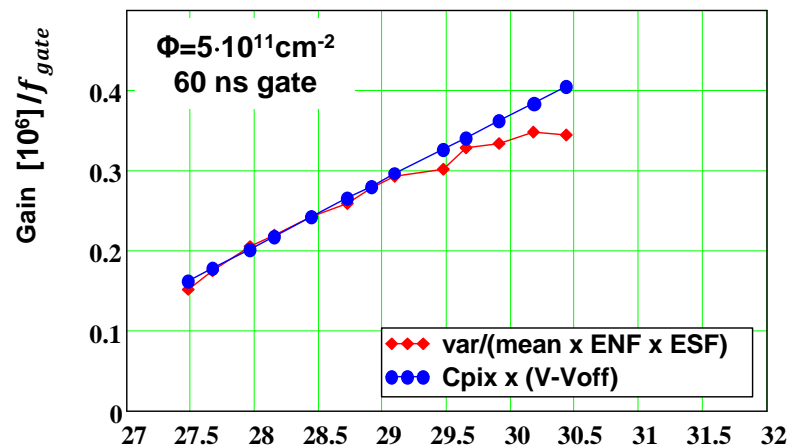
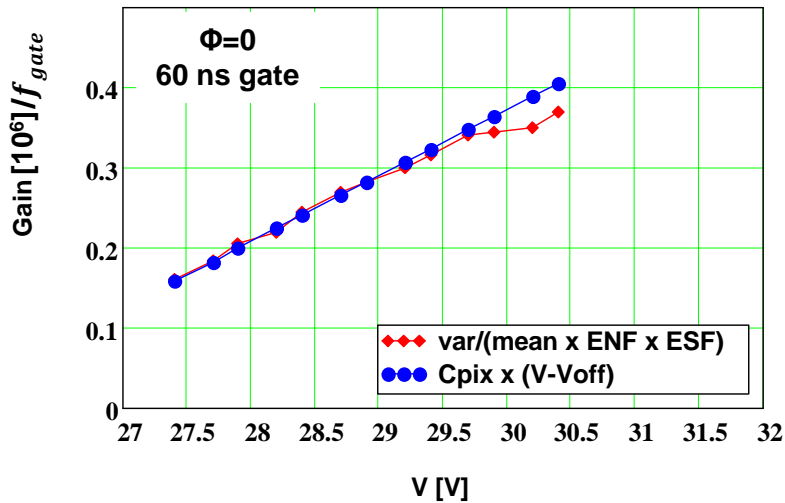


Typical agreement  $O(30\%)$ , however also larger differences  $\rightarrow$   
Detailed comparison + understanding of differences still to be done

# PH<sub>light</sub>: Gain determination

Can we determine *Gain* ?

$$Gain = \frac{Var}{Mean} \cdot \frac{1}{ENF \cdot EQF}$$



**Yes, up to  $\sim 10^{12} \text{cm}^{-2}$ ;**  
**No for higher fluences – saturation!**

# PH<sub>light</sub>: $\mu$ -determination

Can we determine  $\mu$  ?

( $\mu$  = no. of photons initiating a Geiger discharge)

**Yes,  $V < 29.5$  V + up to  $\sim 10^{12}$  cm<sup>-2</sup>;  
No for higher fluences – saturation!**

**Most reliable:  
 $\frac{Mean}{Gain \cdot EQF}$**

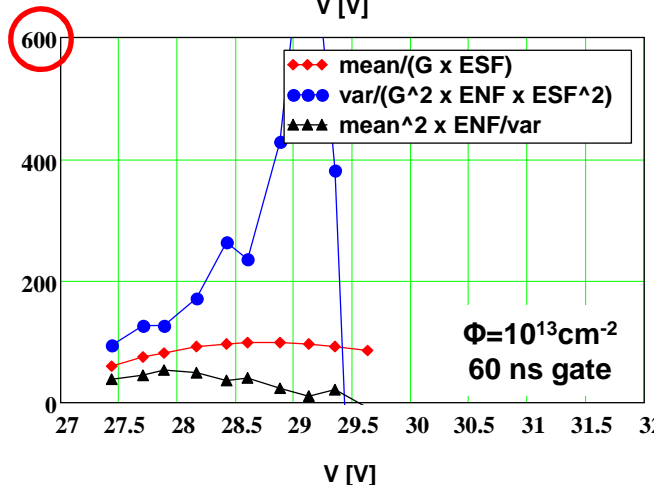
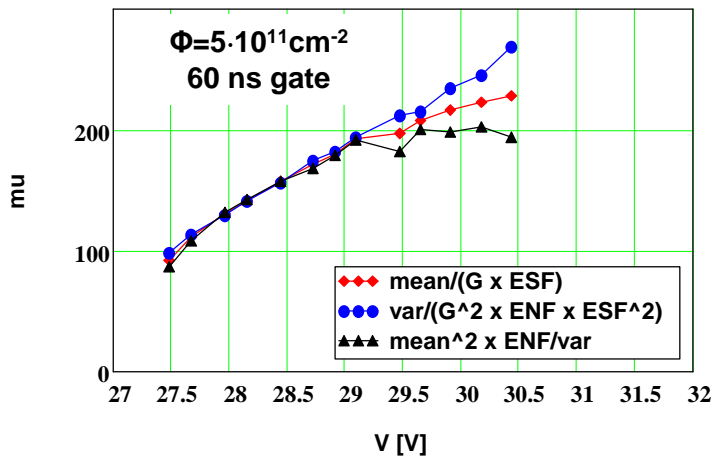
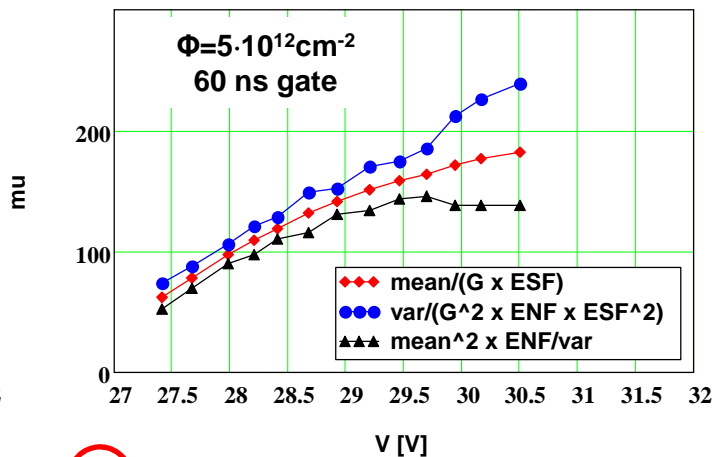
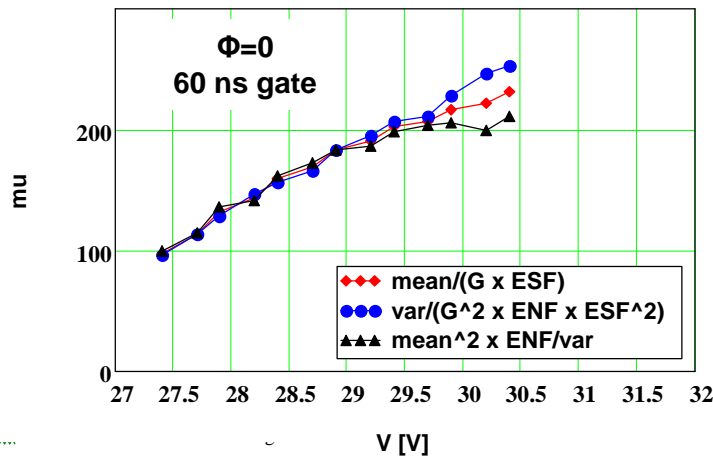
**3 ways to determine  $\mu$**

$$\mu = \frac{Mean}{Gain \cdot EQF}$$

$$\mu = \frac{Var}{Gain^2 \cdot ENF \cdot EQF^2}$$

$$\mu = \frac{Mean^2 \cdot ENF}{Var}$$

with  $Gain \approx C_{pix} \cdot (V - V_{off}) \cdot f_{gate}$



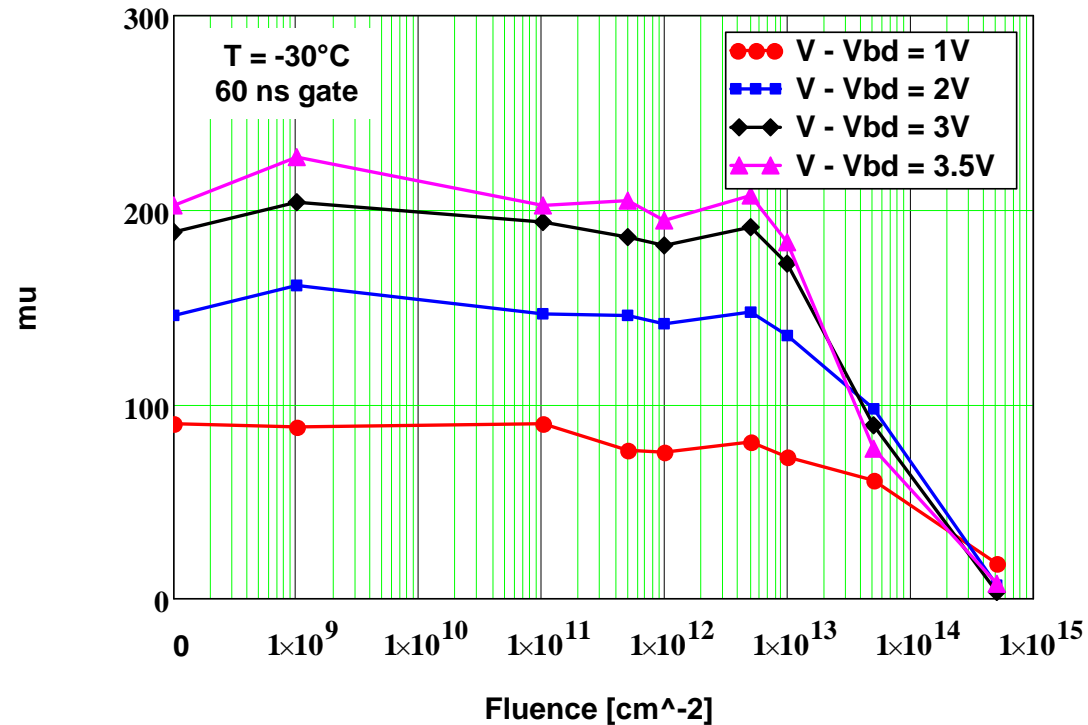


# PH<sub>light</sub>: $\mu$ ( $\propto$ PDE) photo-detection

$$\mu = \frac{\text{Mean}}{\text{Gain} \cdot \text{EQF}}$$

$$\mu = \frac{\text{Var}}{\text{Gain}^2 \cdot \text{ENF} \cdot \text{EQF}^2}$$

$$\mu = \frac{\text{Mean}^2 \cdot \text{ENF}}{\text{Var}}$$



$\Phi < 10^{13}$  : PDE essentially unaffected by irradiation  
 $\Phi = 10^{13} - 5 \cdot 10^{13}$  : irradiation affects PDE (low  $V - V_{bd}$  still ok)  
 $\Phi = 5 \cdot 10^{14}$  : SiPM not a useful photo-detector „all pixels occupied“  
 (→ „ $t_{gate}$ “ optimisation under way)

## Conclusions + next steps

1. C-V,  $I_{\text{dark}}$ ,  $\text{PH}_{\text{dark}}$ ,  $\text{PH}_{\text{light}}$  measured at  $-30^{\circ}\text{C}$  for  $\Phi = 0 \dots 5 \cdot 10^{14} \text{ n/cm}^2$
2. Formulae presented, which relate SiPM parameters to measured quantities
3.  $C_{\text{pix}}$  and  $R_q$  little affected by  $\Phi$
4.  $I_{\text{dark}} \rightarrow \text{DCR} \rightarrow$  increase with  $V$  and  $\Phi \rightarrow$  high DC pixel occupancy for  $\Phi > 10^{13}$   
 $\rightarrow$  expect a significant PDE reduction
5.  $\text{PH}_{\text{dark}} \rightarrow \text{DCR from variance} \rightarrow$  ~consistent with DCR from  $I_{\text{dark}}$
6.  $\text{PH}_{\text{light}} \rightarrow$  different methods indicate Gain not affected by  $\Phi$
7.  $\text{PH}_{\text{light}} \rightarrow$  approximate V- and  $\Phi$ -dependence of „relative“ PDE ( $\mu$ )  $\rightarrow$   
for  $\Phi=5 \cdot 10^{14} \text{ cm}^{-2}$  and  $-30^{\circ}\text{C}$  SiPM investigated not a useful photo-detector

### Next steps:

1. DCR-“PDE“ as a function of  $(\Phi, V, t_{\text{gate}})$  + noise vs. threshold as function of  $(\Phi, V, t_{\text{gate}})$
2. Optimisation of pulse-shaping  $\rightarrow$  how much can one gain?
3. Include fast component from  $C_q$  in analysis
4. Implement saturation effects due to dark counts + photons
5. Implement what we learn in Schwetzingen

**Most methods of SiPM characterisation fail after high  $\Phi$  irradiation  
??? Can we find + agree on the most suitable methods ???**