Single-particle spectral function of the Λ-hyperon in finite nuclei

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Motivation

Most of the theoretical descriptions of single Λ-hypernuclei rely on the validity of the mean field picture



- Correlations induced by the YN interaction can, however, substantially change this picture and, therefore, should not be ignored
- The knowledge of the single-particle spectral function of the Λ in finite nuclei is fundamental to determine:
 - \checkmark To which extent the mean field description of hypernuclei is valid
 - ✓ To describe properly the cross section of different production mechanisms of hypernuclei
- Information on the Λ spectral function can be obtained from a combined analysis of data provided by e.g., (e,e'K⁺) reactions or other experiments with theoretical calculations

Scheme of the Calculation



Finite nuclei hyperon-nucleon G-matrix

- Finite nuclei G-matrix
- Nuclear matter G-matrix

$$G_{FN} = V + V \left(\frac{Q}{E}\right)_{FN} G_{FN}$$

$$G_{NM} = V + V \left(\frac{Q}{E}\right)_{NM} G_{NM}$$

Eliminating V:

$$G_{FN} = G_{NM} + G_{NM} \left[\left(\frac{Q}{E} \right)_{FN} - \left(\frac{Q}{E} \right)_{NM} \right] G_{FN}$$

Truncating the expansion up <u>second order</u>:

$$G_{FN} \approx G_{NM} + G_{NM} \left[\left(\frac{Q}{E} \right)_{FN} - \left(\frac{Q}{E} \right)_{NM} \right] G_{NM}$$

Finite nucleus Λ self-energy in the BHF approximation

Using G_{FN} as an effective YN interaction, the finite nucleus Λ self-energy is given as sum of a 1st order term & a 2p1h correction



 \diamond 1st order term

Λ

Λ



This contribution is real & energy-independent

\diamond <u>2p1h correction</u>

This contribution is the sum of two terms:

• The first, due to the piece $G_{NM}(Q/E)_{FN}G_{NM}$, gives rise to an imaginary energy- dependent part in the Λ self-energy

$$\begin{aligned} \mathcal{W}_{2p1h}(k_{\Lambda},k_{\Lambda}',l_{\Lambda},j_{\Lambda},\omega) \\ &= -\frac{\pi}{2j_{\Lambda}+1} \sum_{n_{h}l_{h}j_{h}t_{z_{h}}} \sum_{\mathcal{L}LSJ} \sum_{Y'=\Lambda\Sigma} \int dq q^{2} \int dKK^{2}(2\mathcal{J}+1) \\ &\times \langle (k_{\Lambda}'l_{\Lambda}j_{\Lambda})(n_{h}l_{h}j_{h}t_{z_{h}})\mathcal{J}|G|K\mathcal{L}qLSJ\mathcal{J}TM_{T} \rangle \\ &\times \langle K\mathcal{L}qLSJ\mathcal{J}TM_{T}|G|(k_{\Lambda}l_{\Lambda}j_{\Lambda})(n_{h}l_{h}j_{h}t_{z_{h}})\mathcal{J} \rangle \\ &\times \delta \left(\omega + \varepsilon_{h} - \frac{\hbar^{2}K^{2}}{2(m_{N}+m_{Y'})} - \frac{\hbar^{2}q^{2}(m_{N}+m_{Y'})}{2m_{N}m_{Y'}} - m_{Y'} + m_{\Lambda} \right) \end{aligned}$$

From which can be obtained the contribution to the real part of the selfenergy through a dispersion relation

$$\mathcal{V}_{2p1h}^{(1)}(k_{\Lambda},k_{\Lambda}',l_{\Lambda},j_{\Lambda},\omega) = \frac{1}{\pi} \mathcal{P} \int_{-\infty}^{\infty} d\omega' \frac{\mathcal{W}_{2p1h}(k_{\Lambda},k_{\Lambda}',l_{\Lambda},j_{\Lambda},\omega')}{\omega'-\omega}$$



The second, due to the piece G_{NM}(Q/E)_{NM}G_{NM}, gives also a real & energy-independent contribution to the Λ self-energy and avoids double counting of Y'N states

$$\begin{aligned} \mathcal{V}_{2p1h}^{(2)}(k_{\Lambda},k_{\Lambda}',l_{\Lambda},j_{\Lambda}) \\ &= \frac{1}{2j_{\Lambda}+1} \sum_{n_{h}l_{h}j_{h}t_{z_{h}}} \sum_{\mathcal{L}LSJ} \sum_{\mathcal{Y}'=\Lambda\Sigma} \int dq q^{2} \int dKK^{2}(2\mathcal{J}+1) \\ &\times \langle (k_{\Lambda}'l_{\Lambda}j_{\Lambda})(n_{h}l_{h}j_{h}t_{z_{h}})\mathcal{J}|G|K\mathcal{L}qLSJ\mathcal{J}TM_{T} \rangle \\ &\times \langle K\mathcal{L}qLSJ\mathcal{J}TM_{T}|G|(k_{\Lambda}l_{\Lambda}j_{\Lambda})(n_{h}l_{h}j_{h}t_{z_{h}})\mathcal{J} \rangle \\ &\times \mathcal{Q}_{Y'N} \left(\Omega - \frac{\hbar^{2}K^{2}}{2(m_{N}+m_{Y'})} - \frac{\hbar^{2}q^{2}(m_{N}+m_{Y'})}{2m_{N}m_{Y'}} - m_{Y'} + m_{\Lambda} \right)^{-1} \end{aligned}$$

Summarizing, in the BHF approximation the finite nucleus Λ selfenergy is given by:

$$\Sigma_{l_{\Lambda}j_{\Lambda}}(k_{\Lambda},k_{\Lambda}',\omega)=\mathcal{V}_{l_{\Lambda}j_{\Lambda}}(k_{\Lambda},k_{\Lambda}',\omega)+i\mathcal{W}_{l_{\Lambda}j_{\Lambda}}(k_{\Lambda},k_{\Lambda}',\omega)$$

with

$$\mathcal{V}_{l_{\Lambda}j_{\Lambda}}(k_{\Lambda},k_{\Lambda}',\omega) = \mathcal{V}_{1}(k_{\Lambda},k_{\Lambda}',l_{\Lambda},j_{\Lambda}) + \mathcal{V}_{2p1h}^{(1)}(k_{\Lambda},k_{\Lambda}',l_{\Lambda},j_{\Lambda},\omega) - \mathcal{V}_{2p1h}^{(2)}(k_{\Lambda},k_{\Lambda}',l_{\Lambda},j_{\Lambda})$$

$$\mathcal{W}_{l_{\Lambda}j_{\Lambda}}(k_{\Lambda},k'_{\Lambda},\omega) = \mathcal{W}_{2p1h}(k_{\Lambda},k'_{\Lambda},l_{\Lambda},j_{\Lambda},\omega)$$

Λ self-energy in finite nuclei



- ♦ $|\text{Im} < \Psi |\Sigma| \Psi > |$ larger in Nijmegen models → strong ω dependence of Re $< \Psi |\Sigma| \Psi >$
- ♦ Im $\langle \Psi | \Sigma | \Psi \rangle \neq 0$ only for $\omega > 0$ & always negative
- ♦ Im $\langle \Psi | \Sigma | \Psi \rangle$ behaves almost quadratically for energies close to $\omega = 0$
- ♦ Re $\langle \Psi | \Sigma | \Psi \rangle$ attractive for $\omega < 0$ up to a given value of ω turning repulsive at high ω
- ♦ Up to 500-600 MeV Re < Ψ |Σ|Ψ> more attractive for heavier hypernuclei. At higher ω more repulsive than that of lighter ones

Λ single-particle bound states

 Λ s.p. bound states can be obtained using the real part of the Λ self-energy as an effective hyperon-nucleous potential in the Schoedinger equation

$$\sum_{i=1}^{N_{max}} \left[\frac{\hbar^2 k_i^2}{2m_{\Lambda}} + \mathcal{V}_{l_{\Lambda} j_{\Lambda}}(k_n, k_i, \omega = \varepsilon_{l_{\Lambda} j_{\Lambda}}) \right] \Psi_{i l_{\Lambda} j_{\Lambda} m_{j_{\Lambda}}} = \varepsilon_{l_{\Lambda} j_{\Lambda}} \Psi_{n l_{\Lambda} j_{\Lambda} m_{j_{\Lambda}}}$$

solved by diagonalizing the Hamiltonian in a complete & orthonormal set of regular basis functions within a spherical box of radius R_{box}

$$\Phi_{nl_{\Lambda}j_{\Lambda}m_{j_{\Lambda}}}(\vec{r}) = \langle \vec{r} | k_n l_{\Lambda}j_{\Lambda}m_{j_{\Lambda}} \rangle = N_{nl_{\Lambda}} j_{l_{\Lambda}}(k_n r) \psi_{l_{\Lambda}j_{\Lambda}m_{j_{\Lambda}}}(\theta, \phi)$$

- $N_{nl\Lambda} \longrightarrow$ normalization constant
- $N_{max} \longrightarrow maximum$ number of basis states in the box
- $j_{j\Lambda}(k_n r) \longrightarrow$ Bessel functions for discrete momenta $(j_{j\Lambda}(k_n R_{box})=0)$
- $\psi_{1\Lambda j\Lambda m j\Lambda}(\theta,\phi) \longrightarrow$ spherical harmonics the including spin d.o.f.
- $\Psi_{nl\Lambda j\Lambda m j\Lambda} = \langle k_n l_\Lambda j_\Lambda m_{j\Lambda} | \Psi \rangle \longrightarrow$ projection of the state $|\Psi\rangle$ on the basis $|k_n l_\Lambda j_\Lambda m_{j\Lambda}\rangle$

N.B. a self-consistent procedure is required for each eigenvalue

Λ single-particle bound states: Energy

Nuclei	$l_{\Lambda} j_{\Lambda}$	JB	J04	NSC89	NSC97a	NSC97b	NSC97c	NSC97d	NSC97e	NSC97f	Exp.
⁵ He											(⁵ He)
Λ	\$1/2	-2.28	-5.89	-0.58	-3.16	-3.38	-3.94	-4.24	-4.20	-3.59	-3.12
12 -	.,2										.12
¹³ C											$(^{13}_{\Lambda}C)$
	\$1/2	-9.48	-18.94	-5.69	-11.46	-11.79	-12.76	-13.08	-12.82	-11.37	-11.69
	P3/2		-3.66	-	-0.24	-0.32	-0.63	-0.68	-0.54	-0.01	-0.7 (p)
	<i>p</i> _{1/2}	· -	-4.07	-	-0.12	-0.14	-0.37	-0.35	-0.19	-	
17 AO											(¹⁶ _A O)
	\$1/2	-11.83	-23.40	-7.39	-14.31	-14.65	-15.70	-15.99	-15.68	-14.02	-12.5
	P3/2	-0.87	-8.16	-	-2.57	-2.72	-3.24	-3.33	-3.10	-2.17	-2.5 (p)
	P1/2	-1.06	-8.03	-	-2.16	-2.22	-2.61	-2.57	-2.30	-1.41	
⁴¹ Ca	1.1										(⁴⁰ Ca)
Λ	\$1/2	-19.60	-36.16	-15.04	-23.09	-23.42	-24.60	-24.74	-24.20	-21.96	-20.0
	P3/2	-9.64	-23.81	-6.92	-12.37	-12.57	-13.40	-13.35	-12.84	-11.09	-12.0 (p)
	P1/2	-9.92	-23.78	-6.29	-12.10	-12.23	-12.95	-12.78	-12.22	-10.45	i i i i i i i i i i i i i i i i i i i
	d5/2	-0.70	-11.72	-	-2.80	-2.93	-3.47	-3.38	-3.00	-1.83	-1.0 (d)
	d3/2	-1.01	-11.65	-	-2.43	-2.46	-2.85	-2.61	-2.18	-1.04	
91Zr											(89Y)
Λ	\$1/2	-25.80	-46.30	-22.77	-31.38	-31.73	-33.05	-33.06	-32.33	-29.56	-23.0
	D3/2	-18.19	-37.73	-17.08	-23.92	-24.20	-25.28	-25.22	-24.58	-22.25	-16.0 (p)
	P1/2	-18.30	-38.01	-16.68	-23.82	-24.06	-25.07	-24.92	-24.23	-21.88	
	d5/2	-11.16	-28.35	-9.05	-14.41	-14.58	-15.36	-15.09	-14.42	-12.41	-9.0 (d)
	d3/2	-11.17	-28.44	-8.49	-14.30	-14.40	-15.12	-14.77	-14.06	-11.99	
	f7/2	-3.05	-18.45	-1.56	-5.46	-5.52	-6.03	-5.59	-4.93	-3.27	-2.0 (f)
	f5/2	-2.99	-18.76	-1.00	-5.28	-5.26	-5.69	-5.20	-4.52	-2.86	
209 pb											(208pb)
Λ	\$1/2	-31.36	-59.95	-29.52	-38.85	-39.23	-40.63	-40.44	-39.50	-39.30	-27.0
	D2/2	-27.13	-55.21	-26.01	-33.49	-33.91	-35.13	-34.80	-33.86	-31.03	-22.0 (p)
	P 5/2 D1/2	-27.18	-55.40	-25.72	-33.38	-33.78	-34.94	-34.54	-33.56	-30.72	
	d5/2	-21.70	-45.08	-17.85	-23.23	-23.54	-24.38	-23.79	-22.86	-20.60	-17.0 (d)
	d3/2	-21.77	-45.07	-17.65	-23.17	-23.45	-24.27	-23.68	-22.75	-20.51	
	f7/2	-13.00	-37.15	-9.67	-15.38	-15.43	-16.04	-15.05	-13.81	-10.98	-12.0 (f)
	f5/2	-13.13	-37.16	-9.31	-15.35	-15.33	-15.90	-14.87	-13.61	-10.76	
	89/2	-8.14	-29.91	-5.27	-10.07	-10.14	-10.68	-9.80	-8.71	-6.28	-7.0 (g)
	87/2	-8.26	-30.16	-4.80	-10.01	-10.00	-10.46	-9.49	-8.37	-5.91	6
	0.74										1

- ♦ Qualitatively good agreement with experiment, except for J04 (unrealistic overbinding)
- ♦ Zr & Pb overbound also for NSC97a-f models. These models predict $U_{\Lambda}(0) \sim -40$ MeV compared with -30 MeV extrapolated from data
- ♦ Splitting of p-, d-, fand g-waves of ~ few tenths of MeV due to the small spin-orbit strength of YN interaction

Λ single-particle bound states: Radial Wave Function



- ♦ $\Psi_{s1/2}$ state more and more spread when going from light to heavy hypernuclei \longrightarrow probability of finding the Λ at the center of the hypernuclei ($|\Psi_{s1/2}(r=0)|^2$) decreases.
- ♦ Only He falls out this pattern because the energy of the $s_{1/2}$ state is too low, therefore, resulting in a very extended wave function
- The small spin-orbit splitting of the p-, d-, f- and g-wave states cannot be resolved in the corresponding wave functions

General Remarks on the s.p. Spectral Function

Single-particle Green's function (Lehmann representation):

$$g_{\alpha\beta}(\omega) = \int_{E_0^{N+1}-E_0^N}^{\infty} d\omega' \frac{S_{\alpha\beta}^p(\omega')}{\omega-\omega'+i\eta} + \int_{-\infty}^{E_0^N-E_0^{N-1}} d\omega' \frac{S_{\alpha\beta}^h(\omega')}{\omega-\omega'-i\eta}$$

Describes propagation of a particle or a hole added to a N-particle system

being

$$S^{p}_{\alpha\beta}(\omega) = \sum_{m} \langle \Psi^{N}_{0} | \hat{c}_{\alpha} | \Psi^{N+1}_{m} \rangle \langle \Psi^{N+1}_{m} | \hat{c}^{\dagger}_{\beta} | \Psi^{N}_{0} \rangle \delta(\omega - (E^{N+1}_{m} - E^{N}_{0})), \ \omega > E^{N+1}_{0} - E^{N}_{0}$$

Particle & hole part of the s.p. spectral function

$$S^{h}_{\alpha\beta}(\omega) = \mp \sum_{n} \langle \Psi^{N}_{0} | \hat{c}^{\dagger}_{\beta} | \Psi^{N-1}_{n} \rangle \langle \Psi^{N-1}_{n} | \hat{c}_{\alpha} | \Psi^{N}_{0} \rangle \delta(\omega - (E^{N}_{0} - E^{N-1}_{n})), \ \omega < E^{N}_{0} - E^{N-1}_{0}$$

Diagonal parts of $S^{p}_{\alpha\beta}$ & $S^{h}_{\alpha\beta}$ = probability density of adding or removing a particle to the ground state of the N-particle system & finding the resulting N+1 (N-1) one with energy ω -(E^{N+1}₀-E^N₀) or (E^N₀-E^{N-1}₀)- ω

The case of the single-particle Λ spectral function

In the case of a Λ hyperon that is added to a pure nucleonic system (e.g., infinite nuclear matter or an ordinary nuclei), it is clear, that since there are no other Λ 's in the N-particle pure nucleonic system, the Λ can only be added to it and, therefore, **the hole part of its spectral function is zero**

The Lehmann representation of he single- Λ propagator is simply:

$$g^{\Lambda}_{\alpha\beta}(\omega) = \int_{E_0^{N+\Lambda}-E_0^N}^{\infty} d\omega' \frac{S^{\Lambda p}_{\alpha\beta}(\omega')}{\omega - \omega' + i\eta}$$

Λ Spectral Strength

In any production mechanism of single- Λ hypernuclei a Λ can be formed in a bound or in a scattering state \longrightarrow the Λ particle spectral function is sum of a discrete & a continuum contribution

♦ <u>Discrete contribution</u>

$$S_{l_{\Lambda}j_{\Lambda}}^{p(d)}(k_{n},\omega) = Z_{l_{\Lambda}j_{\Lambda}} |\langle k_{n}l_{\Lambda}j_{\Lambda}m_{j_{\Lambda}}|\Psi\rangle|^{2}\delta(\omega - \varepsilon_{l_{\Lambda}j_{\Lambda}})$$

is a delta function located at the energy of the s.p. bound state with strength given by the Z-factor

$$Z_{l_{\Lambda}j_{\Lambda}} = \left(1 - \frac{\partial \langle \Psi | \Sigma_{l_{\Lambda}j_{\Lambda}}(\omega) | \Psi \rangle}{\partial \omega} \Big|_{\omega = \varepsilon_{l_{\Lambda}j_{\Lambda}}}\right)^{-1}$$

The discrete contribution to the total Λ spectral strength is obtained by summing over all discrete momenta k_n

$$S_{l_{\Lambda}j_{\Lambda}}^{p(d)}(\omega) = Z_{l_{\Lambda}j_{\Lambda}}\delta(\omega - \varepsilon_{l_{\Lambda}j_{\Lambda}})$$

Λ Spectral Strength

♦ Continuum contribution

$$S_{l_{\Lambda}j_{\Lambda}}^{p(c)}(k_{\Lambda},k'_{\Lambda},\omega) = -\frac{1}{\pi} \operatorname{Im} g_{l_{\Lambda}j_{\Lambda}}^{\Lambda}(k_{\Lambda},k'_{\Lambda},\omega)$$

where the single- Λ propagator can be derived from the following form of the Dyson equation



Λ Spectral Strength

Due to the delta function in the Dyson equation is numerically more convenient to obtain the continuum contribution of the Λ spectral function in coordinate space

$$S_{l_{\Lambda}j_{\Lambda}}^{p(c)}(r_{\Lambda},r_{\Lambda}',\omega) = \frac{2}{\pi} \int_{0}^{\infty} dk_{\Lambda} k_{\Lambda}^{2} \int_{0}^{\infty} dk_{\Lambda}' k_{\Lambda}'^{2} j_{l_{\Lambda}}(k_{\Lambda}r_{\Lambda}) S_{l_{\Lambda}j_{\Lambda}}^{p(c)}(k_{\Lambda},k_{\Lambda}',\omega) j_{l_{\Lambda}}(k_{\Lambda}'r_{\Lambda}')$$

The continuum contribution to the total Λ spectral strength is obtained from the following double folding of the spectral function

$$S_{l_{\Lambda}j_{\Lambda}}^{p(c)}(\omega) = \int_{0}^{\infty} dr_{\Lambda} r_{\Lambda}^{2} \int_{0}^{\infty} dr'_{\Lambda} r'_{\Lambda}^{2} \Psi_{l_{\Lambda}j_{\Lambda}}(r_{\Lambda}) S_{l_{\Lambda}j_{\Lambda}}^{p(c)}(r_{\Lambda}, r'_{\Lambda}, \omega) \Psi_{l_{\Lambda}j_{\Lambda}}(r'_{\Lambda})$$

Total Λ spectral strength

$$S^p_{l_{\Lambda}j_{\Lambda}}(\omega) = S^{p(d)}_{l_{\Lambda}j_{\Lambda}}(\omega) + S^{p(c)}_{l_{\Lambda}j_{\Lambda}}(\omega)$$

Λ Spectral Strength: Results



- ♦ Discrete contribution: delta function located at the energy of the s.p. bound state with strength given by the Z-factor. Decreases when moving from light to heavy nuclei → AN correlations more important when density of nuclear core increases
- ♦ Continuum contribution: strength spread over all positive energies. Structure for ω < 100 MeV reflects the behavior of self-energy. Monotonically reduction for ω > 200

ΛN correlations: Z-factor

$$Z_{l_{\Lambda}j_{\Lambda}} = \left(1 - \frac{\partial \langle \Psi | \Sigma_{l_{\Lambda}j_{\Lambda}}(\omega) | \Psi \rangle}{\partial \omega} \Big|_{\omega = \varepsilon_{l_{\Lambda}j_{\Lambda}}}\right)^{-1}$$

Z measures the importance of correlations. The smaller the value of Z the more important are the correlations of the system

- ♦ Z is relatively large for all hypernuclei → Λ keeps its identity inside the nucleus & is less correlated than nucleons

Nuclei	$l_{\Lambda}j_{\Lambda}$	JB	NSC89	NSC97a	NSC97f
⁵ _A He	\$1/2	0.976	0.983	0.965	0.964
¹³ C	\$1/2	0.950	0.940	0.933	0.933
n	P3/2	-	-	0.975	0.979
	P1/2	-	-	0.976	
17O	\$1/2	0.942	0.930	0.923	0.924
	P3/2	0.973	-	NSC97a NSC97f 0.965 0.964 0.933 0.933 0.975 0.979 0.976 0.976 0.923 0.924 0.956 0.959 0.957 0.961 0.898 0.898 0.911 0.914 0.910 0.912 0.932 0.938 0.931 0.939 0.879 0.876 0.884 0.883 0.891 0.893 0.891 0.893 0.891 0.893 0.891 0.893 0.891 0.891 0.902 0.907 0.857 0.856 0.858 0.857 0.858 0.857 0.858 0.857 0.869 0.869 0.863 0.857 0.863 0.857 0.863 0.855	
	P1/2	0.971	-	0.957	0.961
⁴¹ Ca	\$1/2	0.920	0.896	0.898	0.898
"	P3/2	0.930	0.915	0.911	0.914
	P1/2	0.929	0.914	0.910	0.912
	d5/2	0.952	-	0.932	0.938
	d3/2	0.949	-	0.931	0.939
⁹¹ _A Zr	\$1/2	0.904	0.870	0.879	0.876
	P3/2	0.906	0.875	0.884	0.883
	P1/2	0.907	0.876	0.885	0.883
	d5/2	0.910	0.886	0.891	0.893
	d3/2	0.911	0.886	0.891	0.891
	f7/2	0.919	0.903	0.903	0.906
00000	f5/2	0.920	0.905	0.902	0.907
209 Pb	\$1/2	0.884	0.846	0.857	0.856
	P3/2	0.885	0.847	0.858	0.857
	P1/2	0.885	0.847	0.858	0.857
	d5/2	0.896	0.858	0.870	0.869
	d3/2	0.896	0.857	0.869	0.867
	f7/2	0.891	0.852	0.863	0.857
	f5/2	0.891	0.851	0.863	0.855
	89/2	0.892	0.855	0.869	0.862
	87/2	0.892	0.854	0.868	0.860



- ♦ d^d_{lAjA}(k_A) gives the probability of adding a Λ of momentum k_Λ in the s.p. state l_Λj_Λ of the hypernucleus
- ♦ Intuitively one expects that if K_Λ is large the Λ can easily escape from the nucleus & the probability of binding it must be small. Both plots show in fact that d^d_{lΛjΛ}(k_Λ) decreases when increasing k_Λ and is almost negligible for very large values → In hypernuclear production reactions the Λ is formed in a quasi-free state

Total Disoccupation Number

The total spectral strength of the Λ hyperon fulfills the sum rule

$\int_{l_{\Lambda}}^{\infty} d\omega S_{l_{\Lambda}j_{\Lambda}}^{p}(\omega) = \int_{\mu_{\Lambda}}^{\infty} d\omega S_{l_{\Lambda}j_{\Lambda}}^{p(d)}(\omega) + \int_{\mu_{\Lambda}}^{\infty} d\omega S_{l_{\Lambda}j_{\Lambda}}^{p(c)}(\omega) = 1$ discrete continuum						The is 1 add sca ord	The total disoccupation number is $1 \rightarrow$ is always possible to add a Λ either in a bound or scattering state of a give ordinary nucleus					
Nuclei		\$1/2	P3/2	P1/2	d5/2	d3/2	f7/2	f5/2	89/2	87/2		
⁵ _A He	Discrete	0.964	-	_	-	-	-	_	-	_		
	Continuum	0.023	_	_	2	-	_	_	_	_		
	Total	0.987	-	-	2	-	_	S -	-	1		
13C	Discrete	0.933	0.979	-	-	-	-	2. 	-	-		
Λ	Continuum	0.040	0.017	-	-	_	-	-	-	-		
	Total	0.973	0.996	-	-	_	-	-	-	-		
170	Discrete	0.924	0.959	0.961	-	_	_	174	-	1 2		
Λ	Continuum	0.053	0.037	0.036	-	-	-	-	-	-		
	Total	0.977	0.996	0.997	-	-	-	-	-	-		
⁴¹ Ca	Discrete	0.898	0.914	0.912	0.938	0.939	-	-	-	_		
Λ	Continuum	0.071	0.063	0.064	0.048	0.047	-	_	-	2		
	Total	0.969	0.977	0.976	0.986	0.986	_	84	-			
⁹¹ _A Zr	Discrete	0.876	0.883	0.883	0.893	0.891	0.906	0.907	-	-		
	Continuum	0.120	0.113	0.113	0.103	0.105	0.089	0.090	-	-		
	Total	0.996	0.996	0.996	0.996	0.996	0.995	0.997	-	-		
²⁰⁹ _A Pb	Discrete	0.856	0.857	0.857	0.869	0.867	0.857	0.855	0.862	0.860		
	Continuum	0.138	0.142	0.142	0.129	0.130	0.140	0.141	0.137	0.139		
	Total	0.994	0.999	0.999	0.998	0.997	0.997	0.996	0.999	0.999		

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♦ Purpose:

- ✓ Calculation of finite nuclei Λ spectral function from its self-energy derived within a perturbative manybody approach with realistic YN interactions
- Results & Conclusions
 - ✓ Binding energies in good agreement with experiment
 - ✓ Z-factor relatively large \longrightarrow Λ less correlated than nucleons
 - ✓ Discrete cont. to disoc. numb decreases with $k_{\Lambda} \longrightarrow \Lambda$ is mostly formed in a quasi-free state in production reactions
 - Scattering reactions such as (e,e',K⁺) at MAMI-C & JLAB can provide valuable information on the disocuppation of Λ s.p. bound states

- \diamond You for your time & attention
- \diamond The organizers for their invitation

