

# High precision $g$ -factor measurements with stable and radioactive nuclei and perspectives for experiments @SPES and @ELI-NP

Aslı KUŞOĞLU<sup>1,2</sup>



<sup>1</sup>ELI-NP, Magurele, Romania

<sup>2</sup>Istanbul University, Istanbul, Turkey

*asli.kusoglu@eli-np.ro*

- g factor– how do we measure them and why do we need different methods and approaches?
- Alternative  $g$ -factor measurements need to be developed for RIB  
 $g$ -factor measurements of short-lived excited states:  
Time Differential Recoil In Vacuum (TDRIV) on radioactive geometry
  - $^{24}\text{Mg}$  – proof of principle on H-like ions @ ALTO
  - $^{56}\text{Fe}$  – proof of principle on Na-like ions @ ALTO
- Perspective experiments @SPES and @ELI-NP

# Magnetic dipole moments

- Nuclei with non-zero spin have magnetic dipole moment

$$\mu = gI[\mu_N]$$

- Source of nuclear magnetism:
  - ∞ orbital movement of charged particles
  - ∞ intrinsic spin of the nucleus

- Nuclei with non-zero spin have magnetic dipole moment

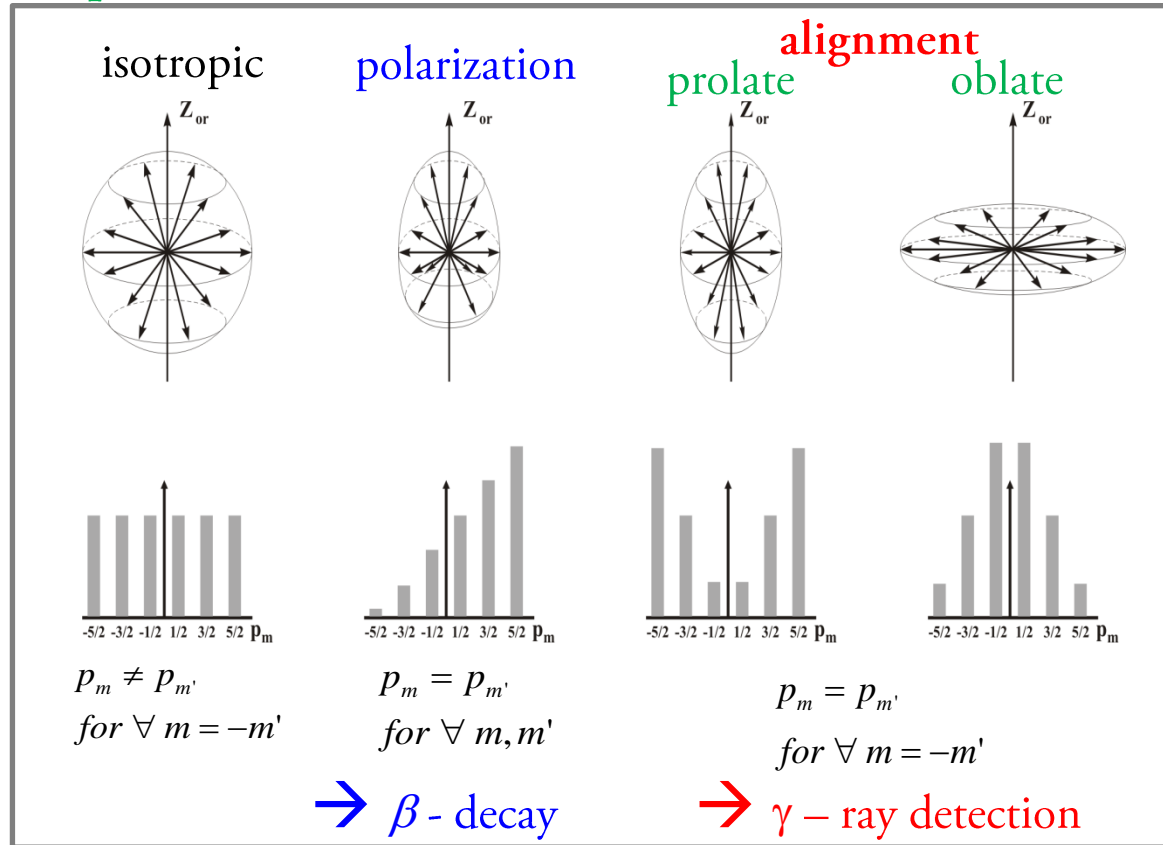
$$\vec{\mu} = \sum_{k=1}^A g_{\ell}^{(k)} \vec{\ell}^{(k)} + \sum_{k=1}^A g_s^{(k)} \vec{s}^{(k)} \quad \text{- the contribution of every nucleon}$$

- $\pi/\nu$  g factors:

	free-nucleon		effective	
$g_s^{\pi}$	$= 5.585$	$g_{\ell}^{\pi} = 1$	$g_s^{\pi} = 0.7 * g_s^{\pi}$	$g_{\ell}^{\pi} = 1$
$g_s^{\nu}$	$= -3.826$	$g_{\ell}^{\nu} = 0$	$g_s^{\nu} = 0.7 * g_s^{\nu}$	$g_{\ell}^{\nu} = 0$

# How to measure $g$ factor?

- Obtain **nuclear spin-oriented** ensemble



- Apply perturbing **magnetic field** (external or hyperfine field)  $\rightarrow$

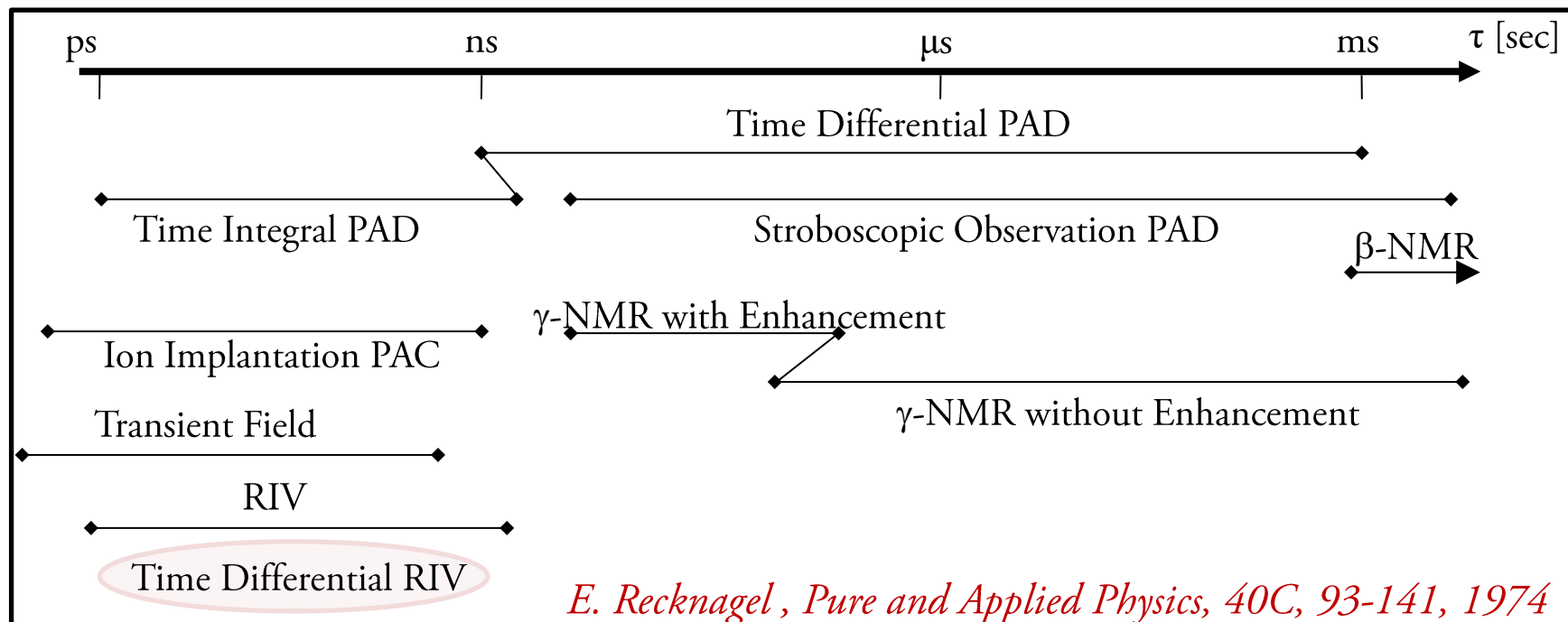
$$\omega = -g \frac{\mu_N}{\hbar} B$$

- Have **sufficient time** for interaction within the nuclear lifetime
- Know with a **sufficient precision** the **perturbing field**

- Observe **modification of the perturbation**

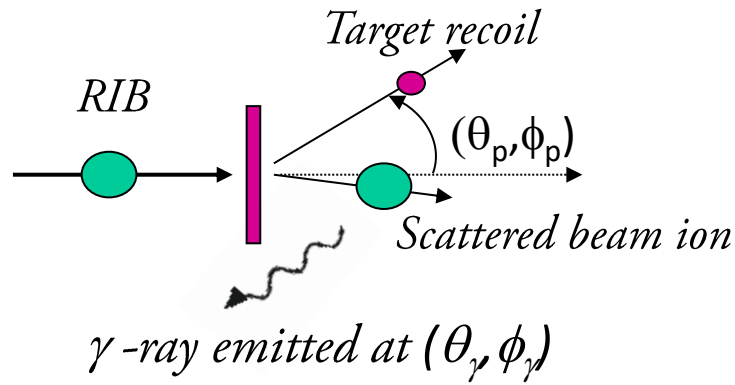
# Experimental nuclear moment measurement techniques

- Different measurement techniques depending on the **nuclear state properties** (lifetime, spin, production method etc.)



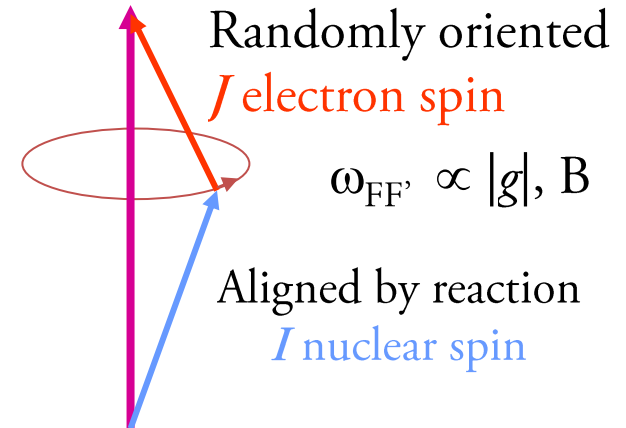
- Transient Field (TF) or Recoil In Vacuum (RIV) techniques need **calibration measurements** with known g factors

# RIV (Recoil In Vacuum)



$$B_{ns} = 16.7 \frac{Z^3}{n^3} \left[ 1 + \left( \frac{Z}{84} \right)^{2.5} \right] [T]$$

$$F = I + J$$



A.E. Stuchbery et al., *Hyperfine Interact* 220, 29-45, (2013)

Analyze particle- $\gamma$  angular correlations

$$W(\theta_p, \theta_\gamma, \Delta\phi) = \sum_{kq} B_{kq}(\theta_p) Q_k G_k F_k D_{q0}^{k*}(\Delta\phi, \theta_\gamma, 0)$$

$$G_k(t) = \sum_{F, F'} C_{FF'} \exp(-\omega_{FF'} t)$$

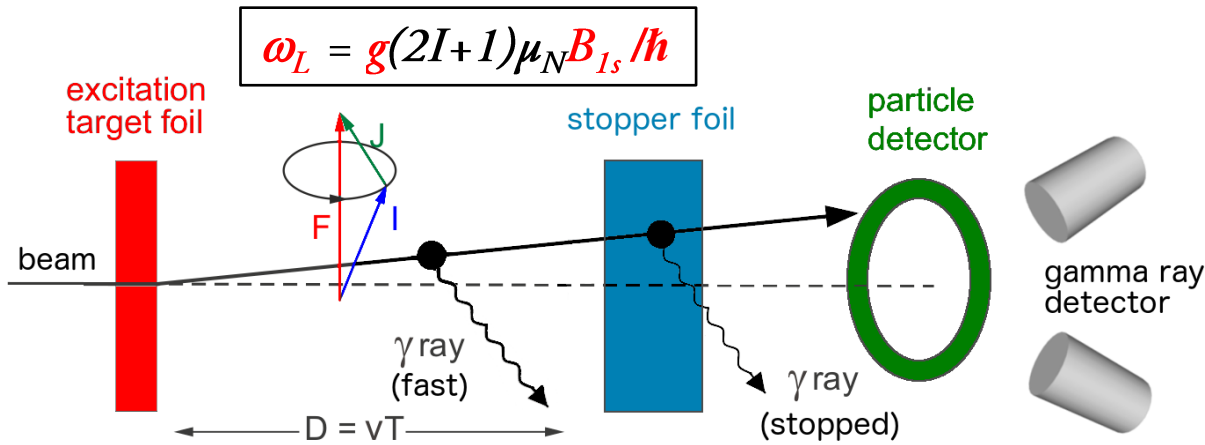
$(0 \leq |G_k| \leq 1)$

- attenuation coefficients  
contains information about  $g$  factor

$$\omega_{FF'} = \frac{\mu_N B}{2\hbar J} g (F(F+1) - F'(F'+1))$$

- interaction frequency

# TDRIV (Time-Differential Recoil In Vacuum) with stable beam



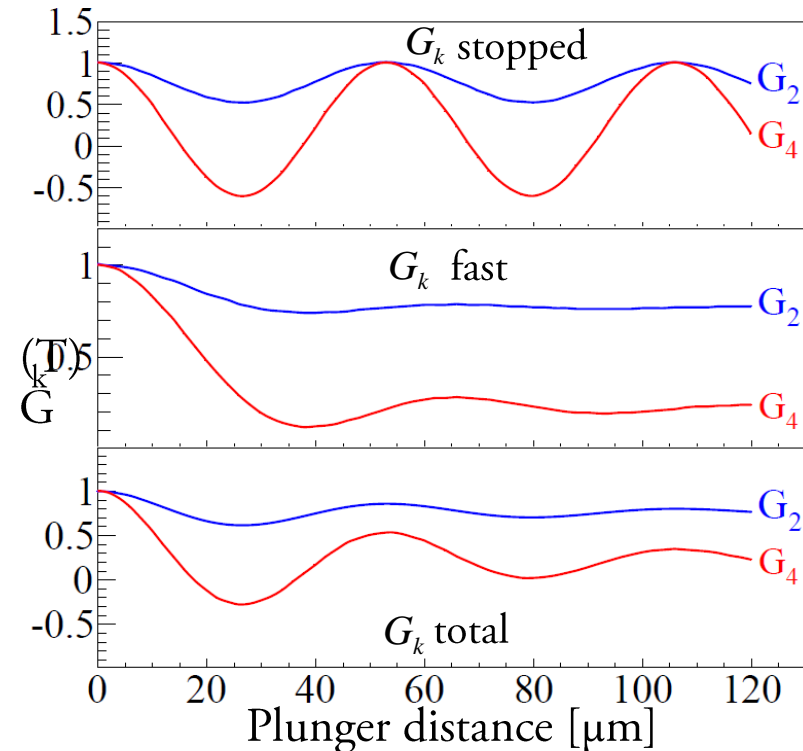
Stable beam geometry!

H-like ions  
attenuation factors

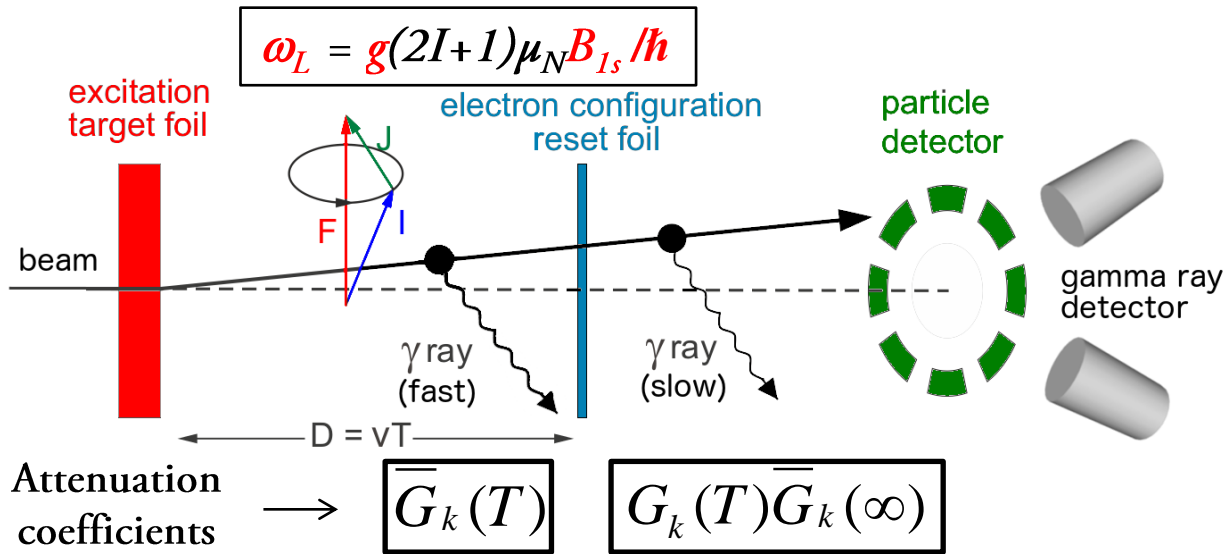
$^{12}\text{C}(^{16}\text{O}, \alpha\gamma)^{24}\text{Mg}$  @ 41.7 MeV  
 $\rightarrow \beta = 0.056$   
 $\rightarrow 15\%$  H-like charge state  
 $\rightarrow |g(2^+)| = 0.51(2)$

*R.E. Horstman et al., Nucl. Phys. A 248, 291 (1975)*

- The importance of the use of H-like ions comes from the simplicity of the electron configuration



# TDRIV (Time-Differential Recoil In Vacuum) with radioactive beam



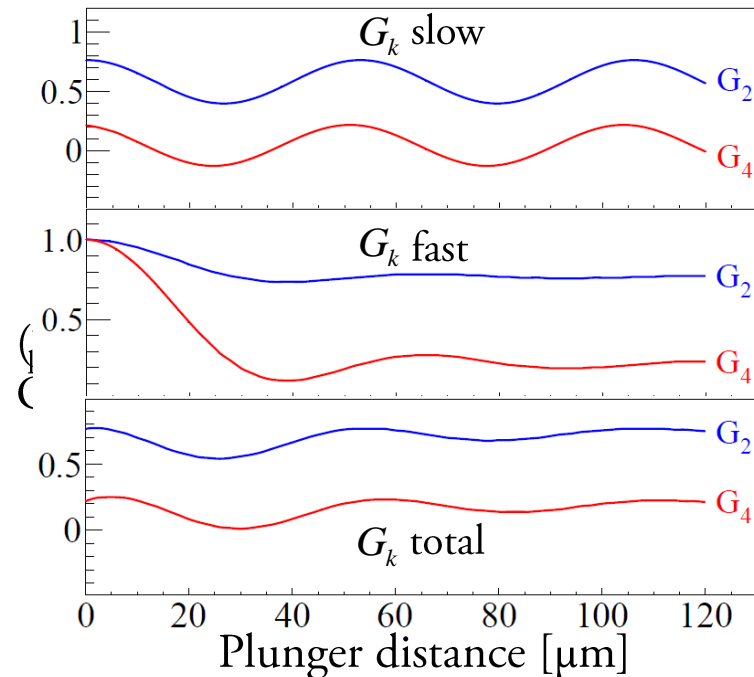
Radioactive beam geometry!

H-like ions  
attenuation factors

*A. E. Stuchbery et al., Phys. Rev. C 71, 047302 (2005)*

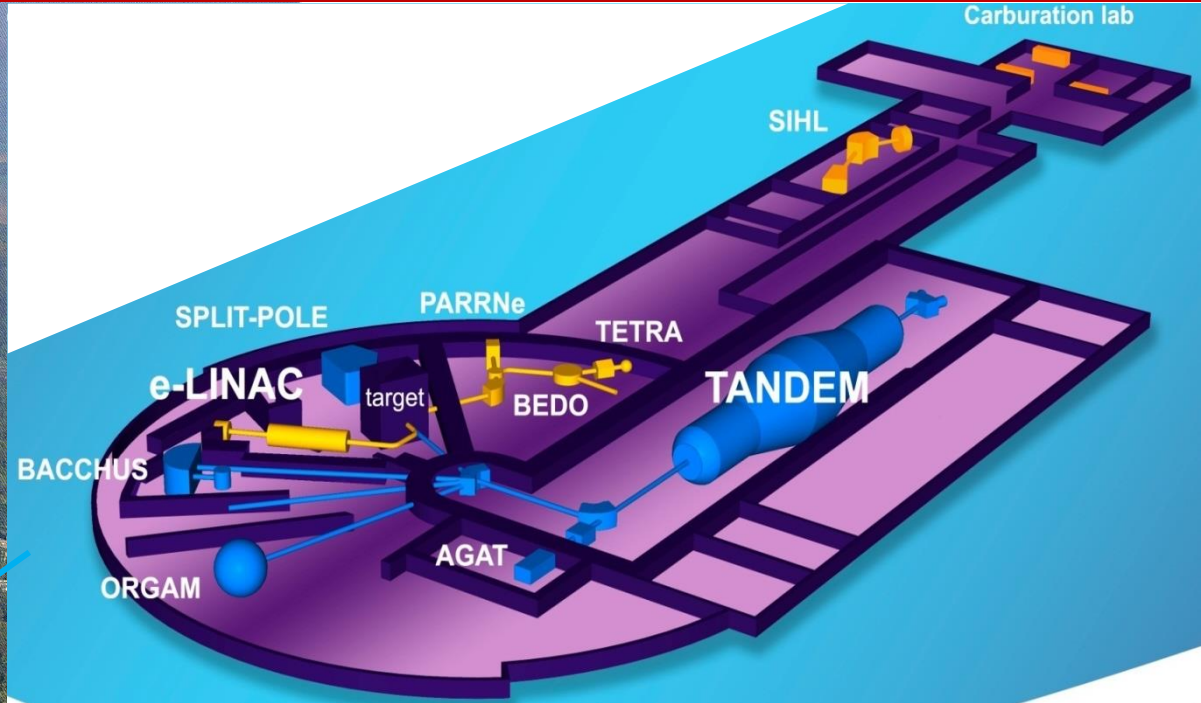
$$\overline{G}_k(T) = \int_0^T G_k(t) \lambda e^{-\lambda t} dt$$

$$G_k(\infty) = \int_0^{\infty} G_k(t) \lambda e^{-\lambda t} dt$$





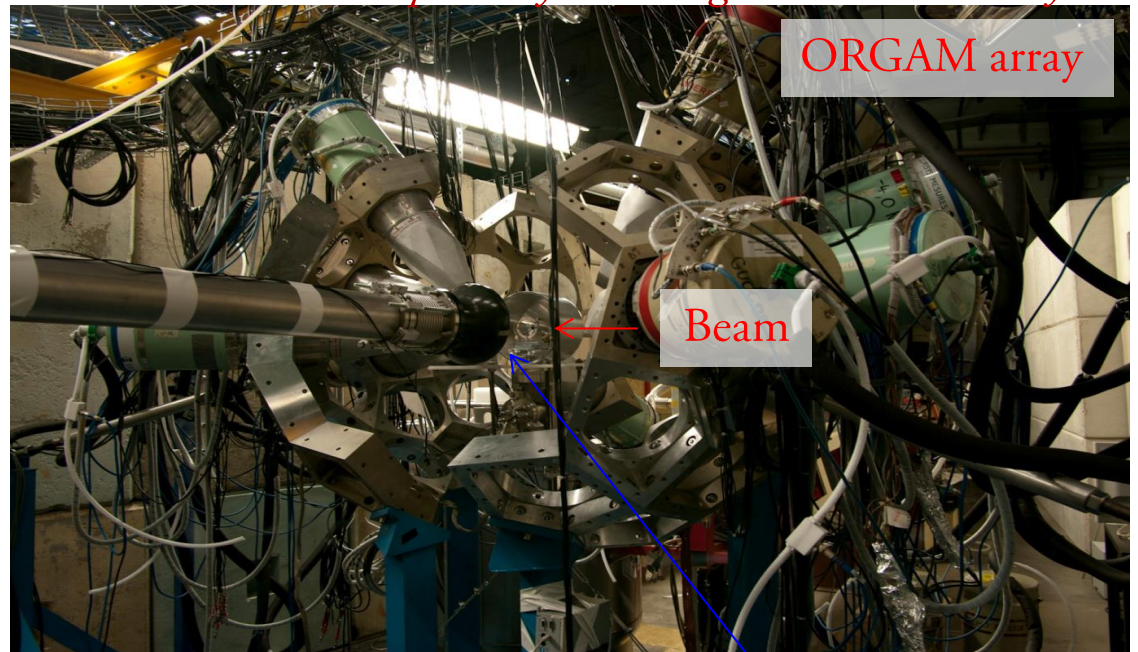
# ALTO facility @ IPN



Tandem building  
Institut de Physique Nucléaire  
Campus of the Paris Sud University  
Orsay (France)

# TDRIV Experimental Setup for H-like ions @ ALTO

Proposed by G.Georgiev, A.E. Stuchbery et. al



**Beam** :  $^{24}\text{Mg}$  @ 120 MeV (5MeV/u), 0.3 pA

**Target** : 2.4 mg/cm<sup>2</sup>  $^{93}\text{Nb}$ , Glancing collisions

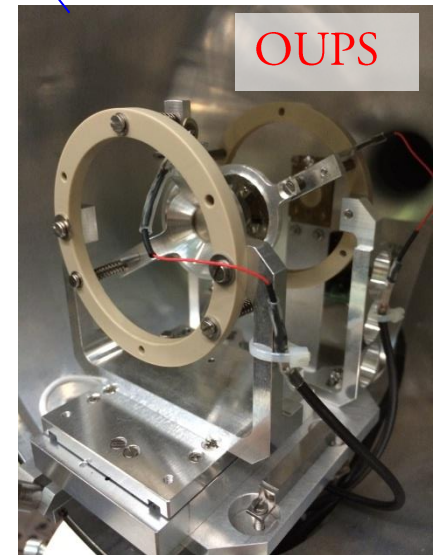
**Reset foil**: 1.7 mg/cm<sup>2</sup>  $^{197}\text{Au}$

□ 13 HPGe in ORGAM array

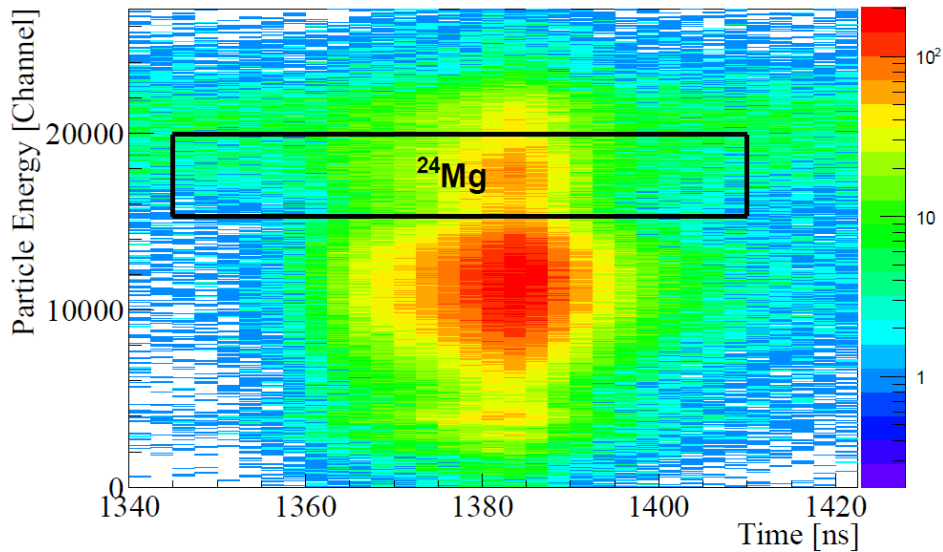
$\theta = 46.5^\circ, 72.1^\circ, 85.8^\circ, 94.2^\circ, 108.0^\circ, 133.6^\circ, 157.6^\circ$

□ 8-fold segmented plastic scintillation particle detector  
( $\Delta\phi_p = 30^\circ$ ,  $\theta_p = 33^\circ$  to  $38^\circ$ )

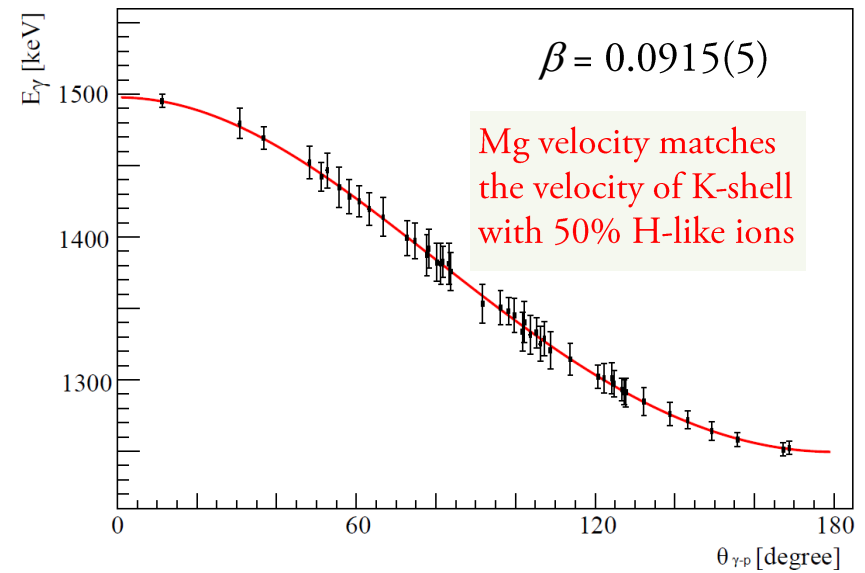
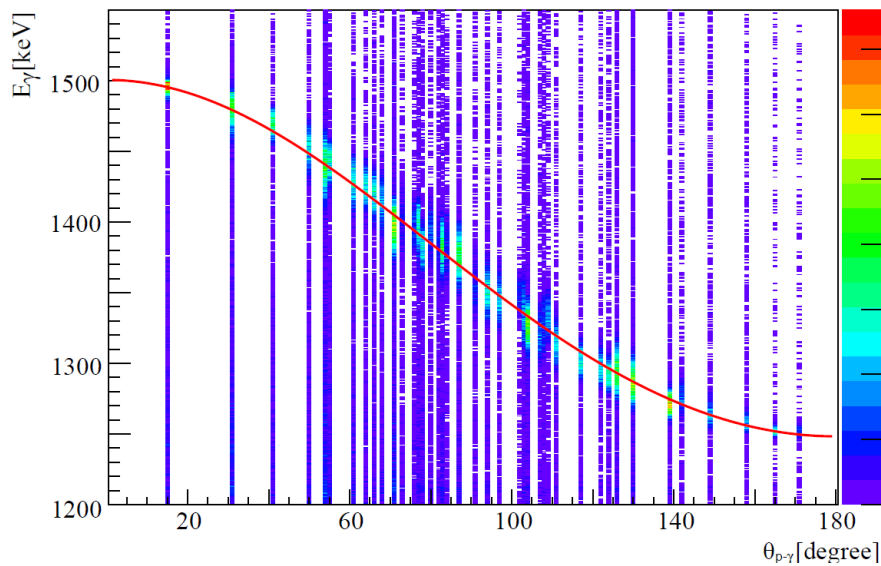
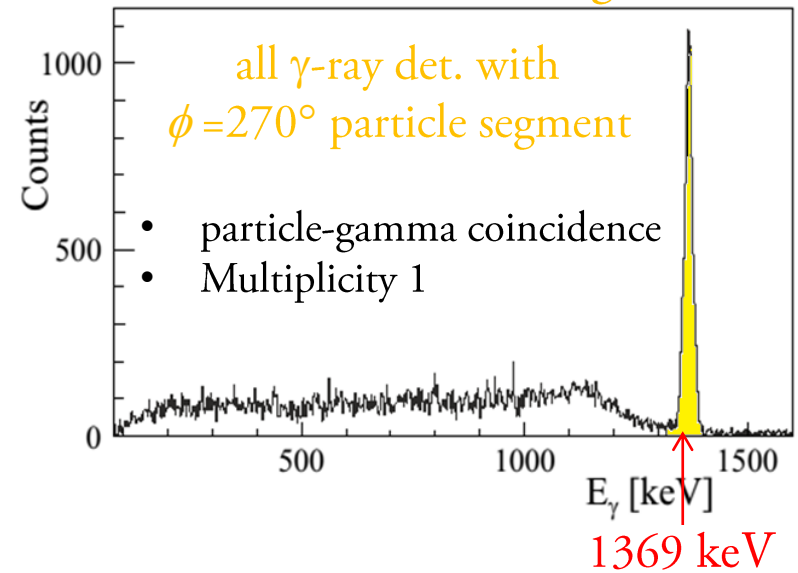
□ Plunger: OUPS (24 target-reset foil distance 100  $\mu\text{m}$ )



# Data Analysis

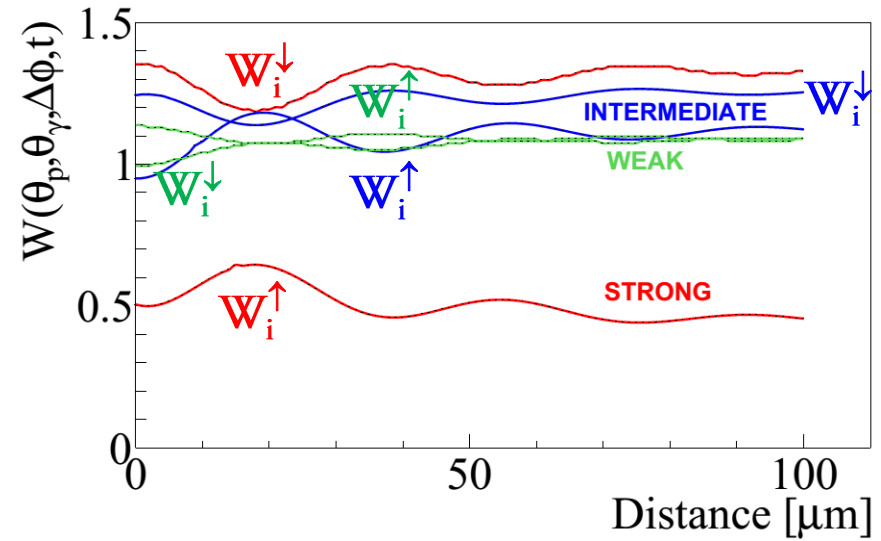
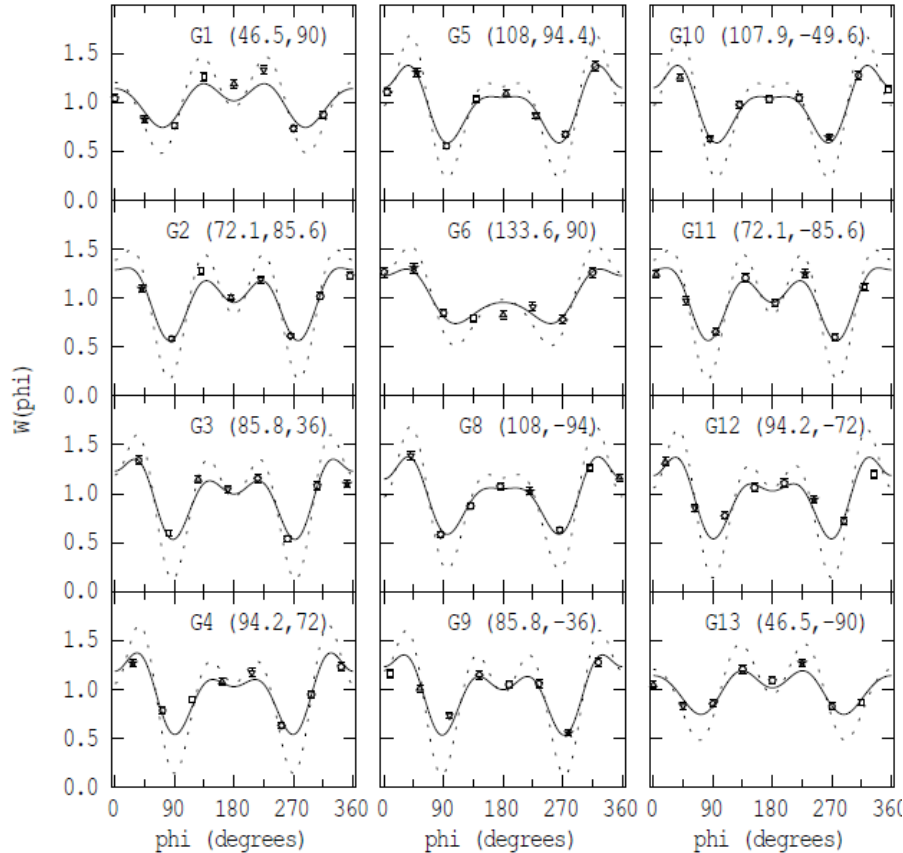


$^{24}\text{Mg}: 2^+ \rightarrow 0^+$



# Angular Correlation Analysis

$$W(\theta_p, \theta_\gamma, \Delta\phi, t) = \sum_{kq} B_{kq}(\theta_p) Q_k F_k G_k(t) D_{q0}^{k*}(\Delta\phi, \theta_\gamma, 0)$$

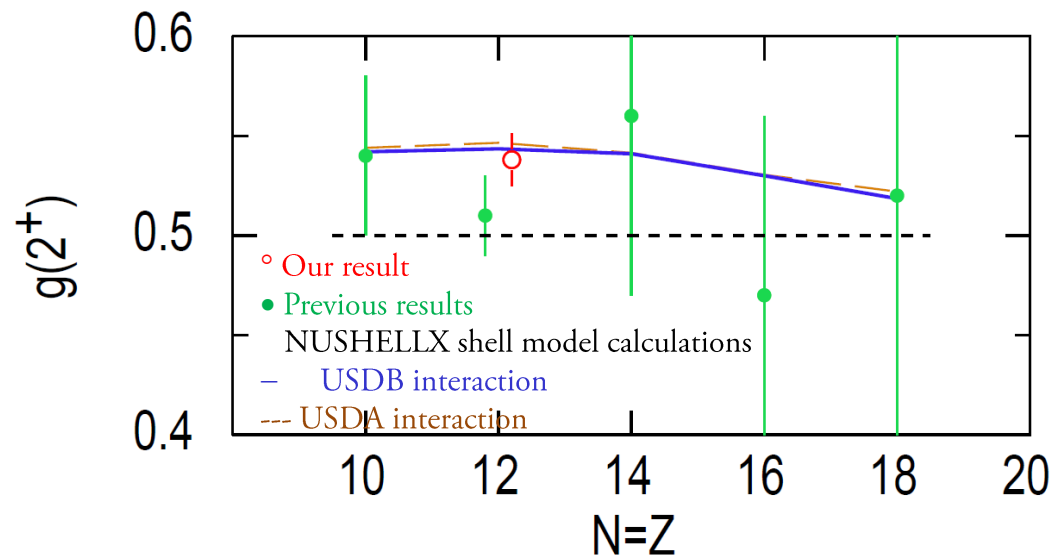
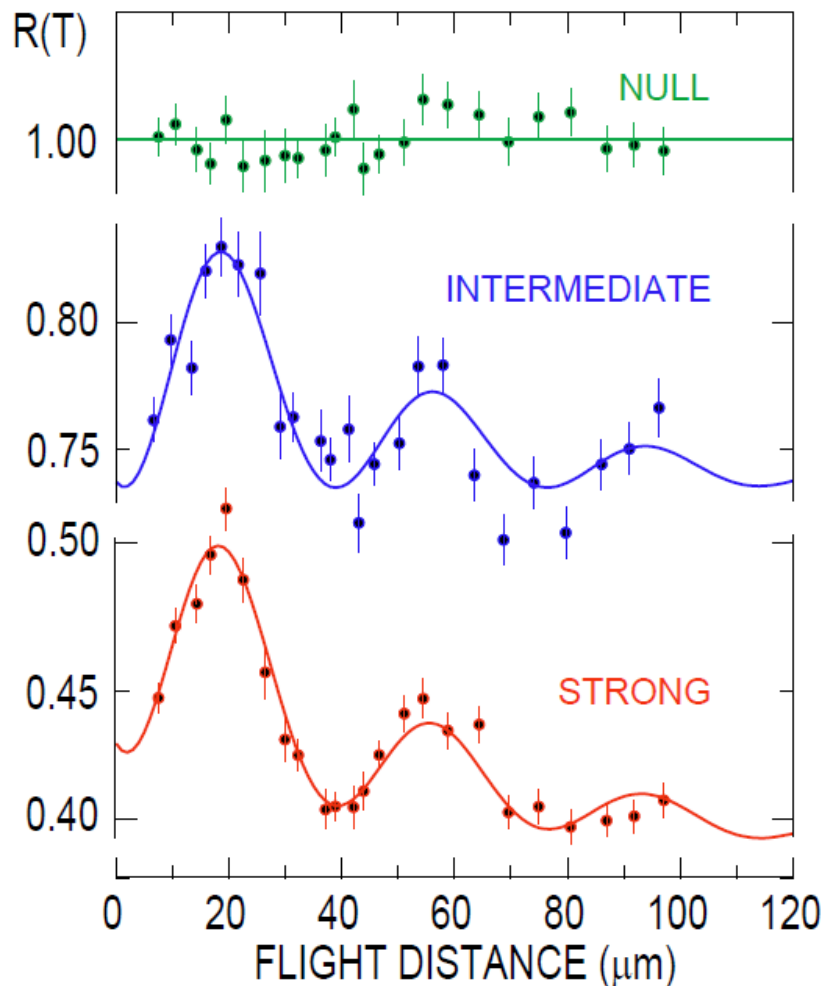


$$N(i, j) = N_0 \varepsilon_{pi} \varepsilon_{\gamma j} W(\theta_p, \theta_\gamma, \Delta\phi, t)$$

$$R(T) = \left( \frac{\prod_{i=1}^n W_i^{\uparrow}}{\prod_{i=1}^n W_i^{\downarrow}} \right)^{1/n}$$

*A. Kusoglu et al. JPCS, 590, 012041, 2015*

# Experimental Results



*R.E. Horstman et al., Nucl. Phys. A 248, 291 (1975)*

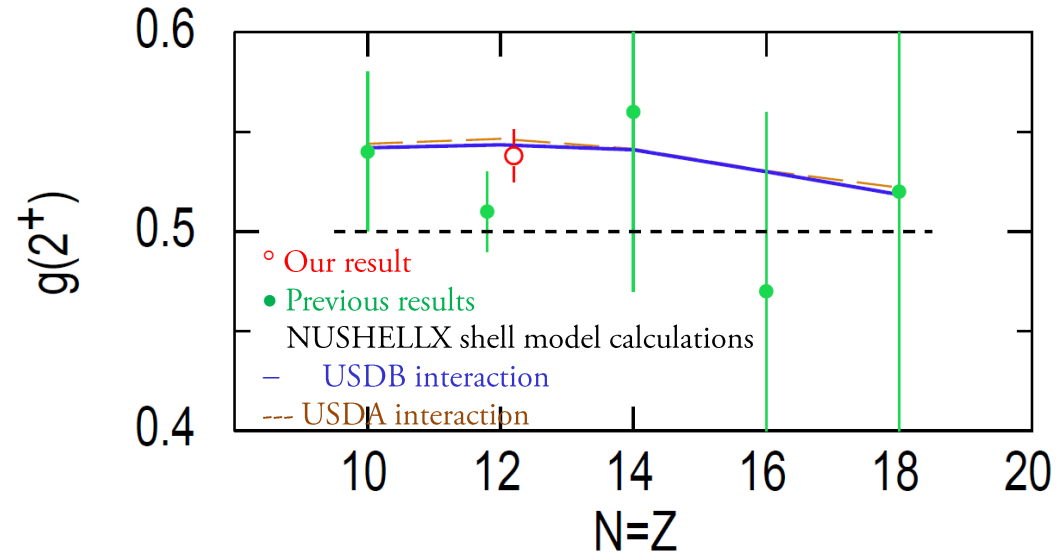
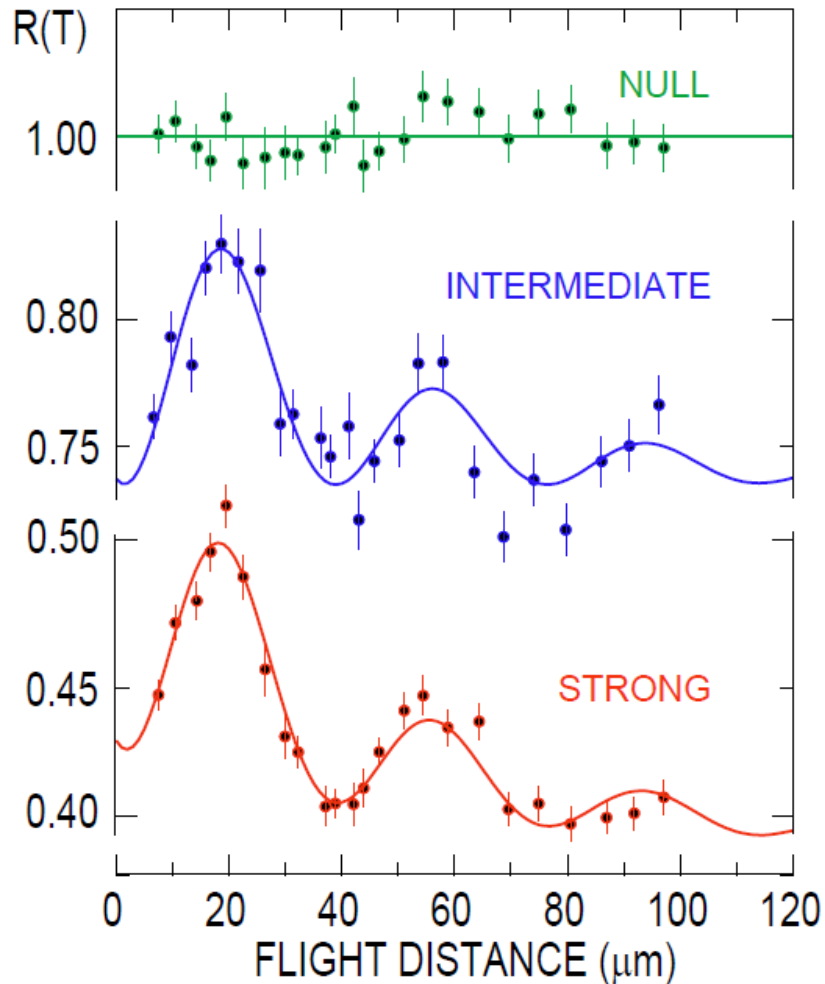
Previous measurement:  $|g(2^+)| = 0.51(2)$

**Our result:  $|g(2^+)| = 0.538(13)$**

*A.Kusoglu et al. PRL, 114, 062501, 2015*

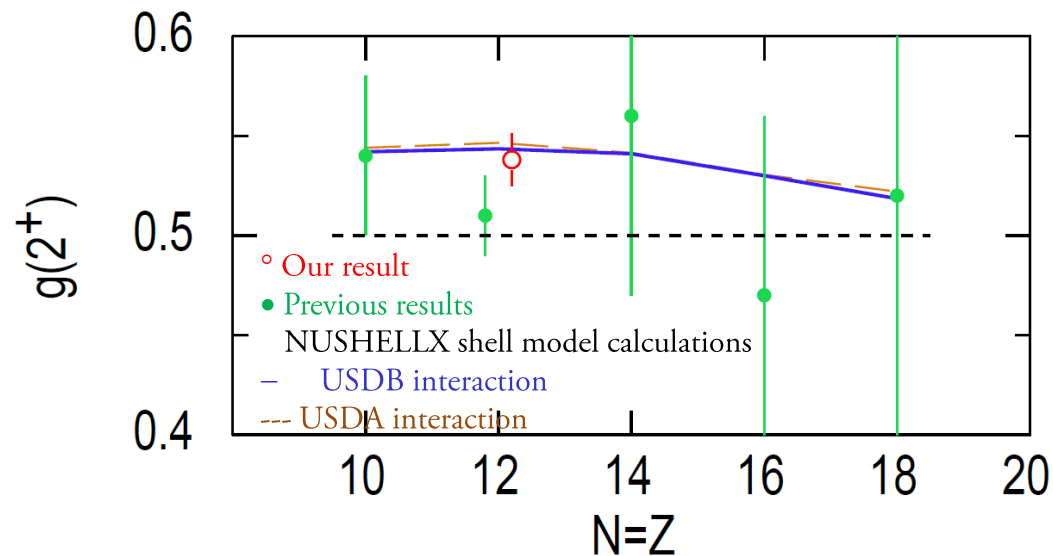
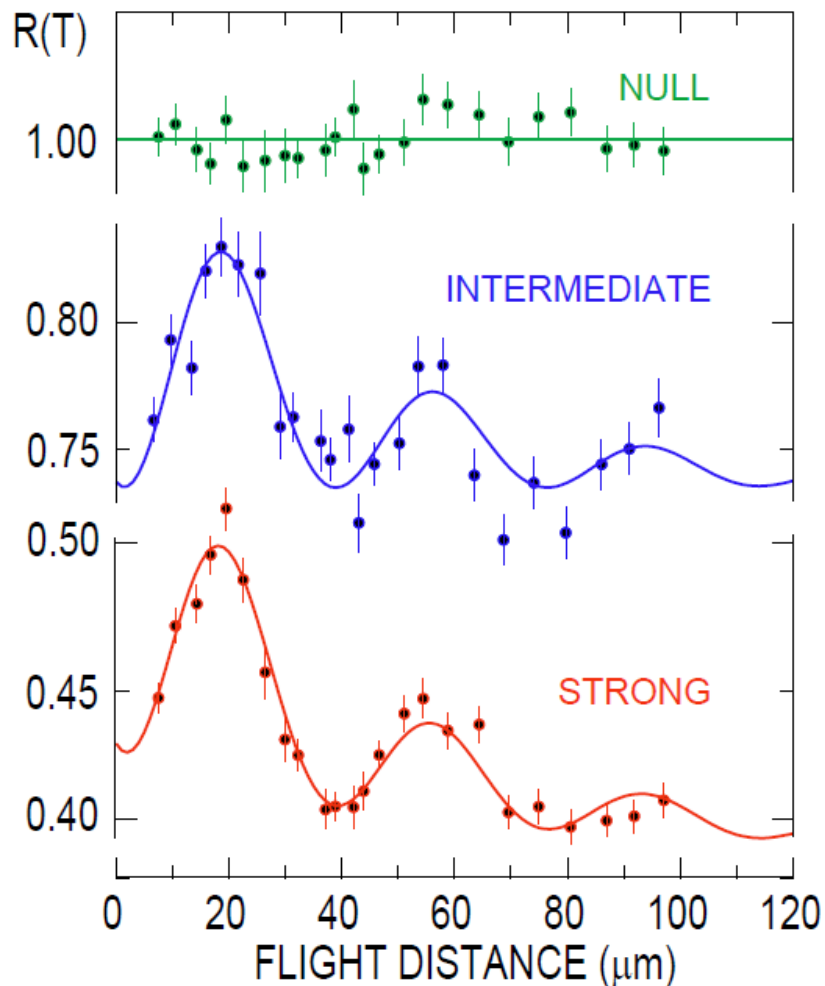
First high precision measurement of  $g(2^+)$  of  $^{24}\text{Mg}$

# Experimental Results



- Departure from  $g = 0.5$
- Configuration mixing
- Isospin mixing
- Meson exchange current

# Experimental Results



- Departure from  $g = 0.5$ 
  - Configuration mixing
  - Isospin mixing
  - Meson exchange current
- Open new perspectives:
  - High precision  $g$ -factor in stable nuclei
  - Validation of the technique for RIB
  - Extension to  $A \geq 20$  to determine **absolute  $g$  factors**

Method works for H-like ions



Does it work for ions with more than 1 electron?

$$B_{ns} = 16.7 \frac{Z^3}{n^3} \left[ 1 + \left( \frac{Z}{84} \right)^{2.5} \right] [T]$$

Proposed experiment with Na-like ions using  $^{56}\text{Fe}^{15+}$

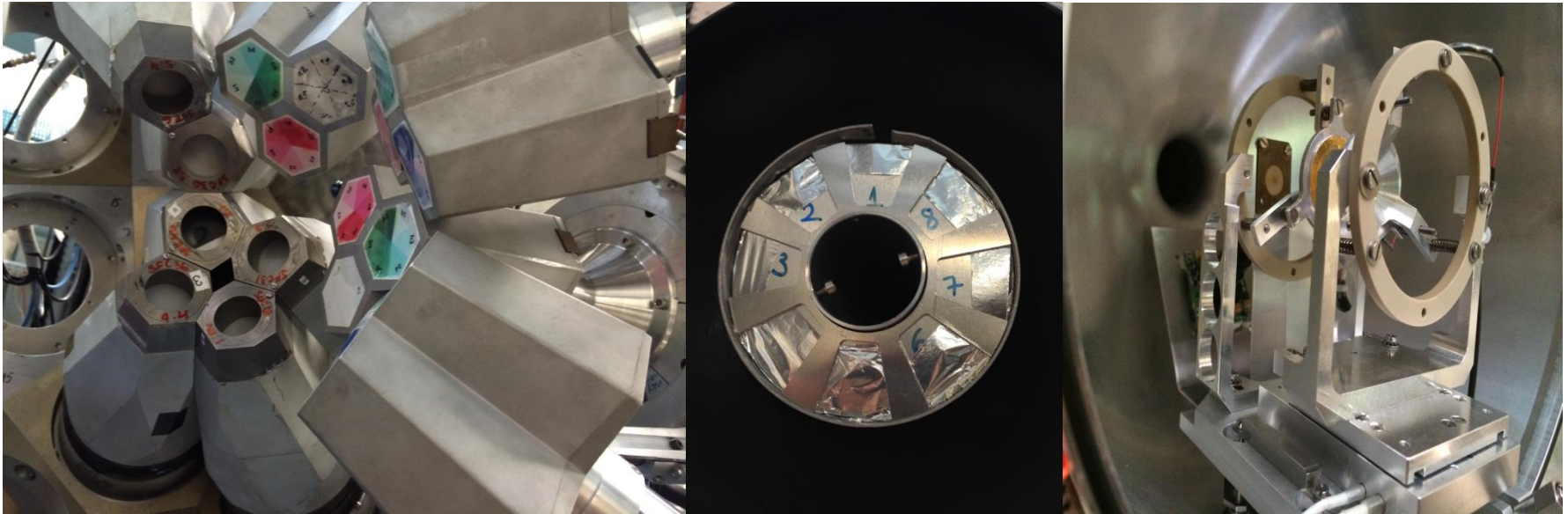
- ❑ Is it possible to observe oscillation?
- ❑ (if yes) Precise and independent  $g$ -factor measurement of  $^{56}\text{Fe}$ ,  $2^+$
- ❑ (if yes) Confront ab initio hyperfine field calculations



# TDRIV Experimental Setup for Na-like ions @ ALTO

*Proposed by A.E. Stuchbery et. al*

- ❑ 8 MINIBALL Cluster: 144 Segments
- ❑ 12 ORGAM detectors
- ❑ 8 fold segmented plastic detector
- ❑ OUPS plunger



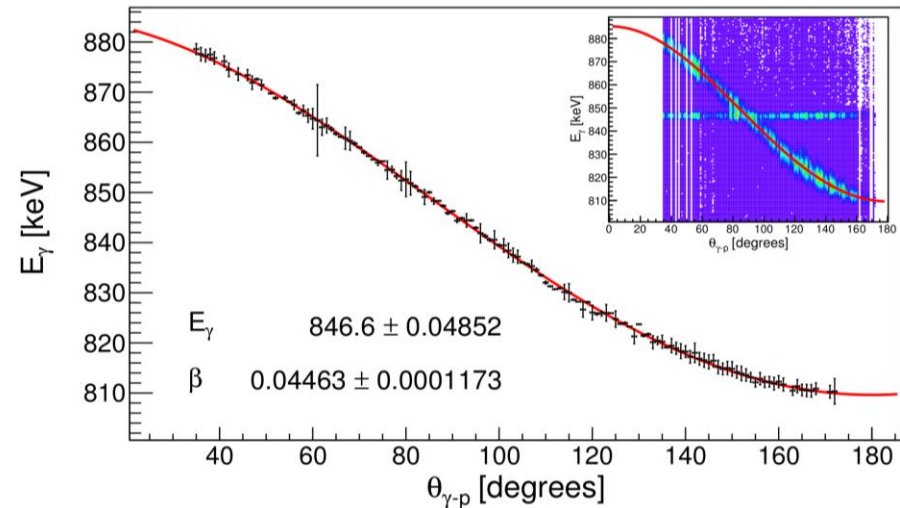
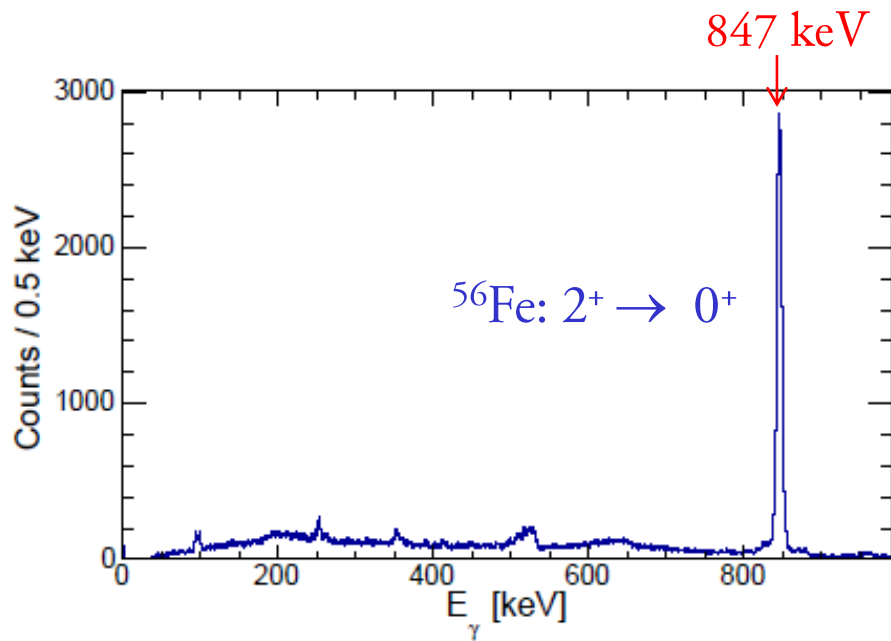
**Beam** :  $^{56}\text{Fe}^{15+}$  @ 130 MeV,

**Target** :  $230 \mu\text{m}/\text{cm}^2$  of  $^{12}\text{C}$  deposited on  $0.5 \mu\text{m}$   $^{\text{nat}}\text{Ni}$  foil

Coulomb excitation first  $2^+$  ( $E_x = 847 \text{ keV}$ ,  $\tau = 9.6 \text{ ps}$ )

**Stopper** :  $5.8 \text{ mg}/\text{cm}^2$   $^{\text{nat}}\text{Ni}$

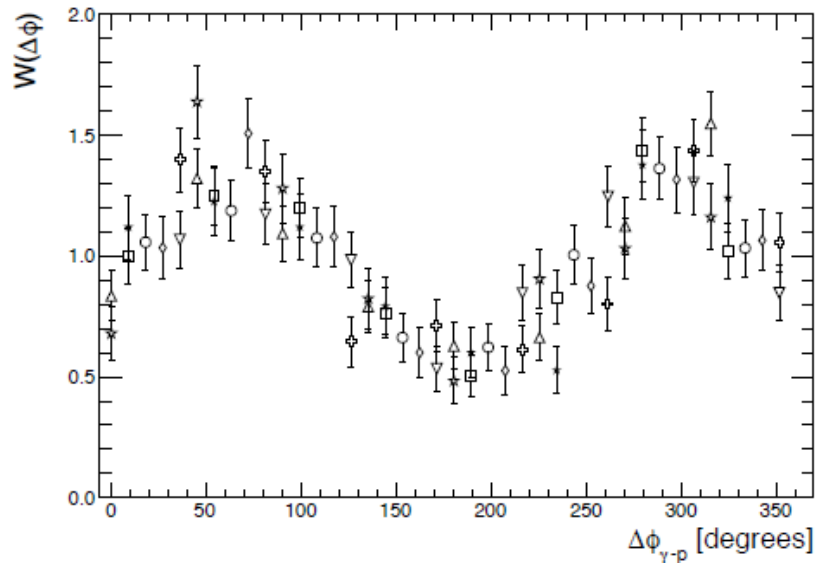
# Preliminary results



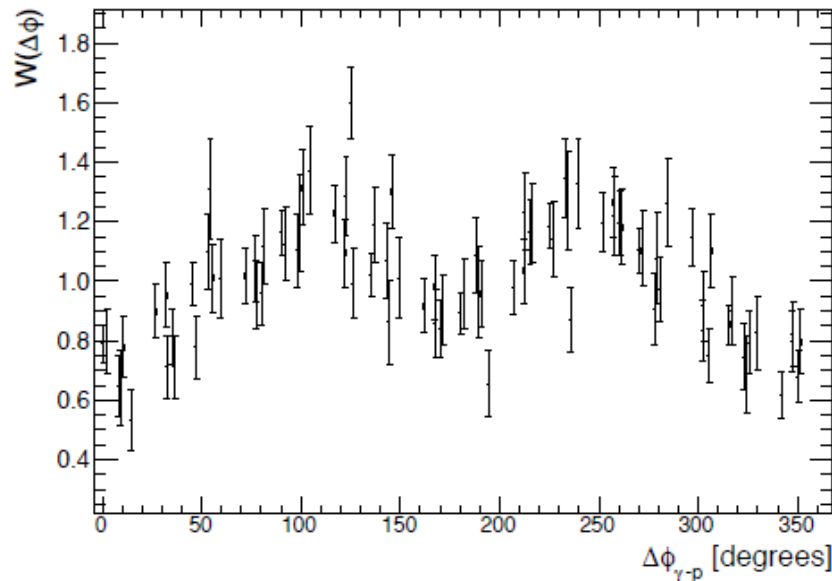
- ❑ Development of a  $^{12}\text{C}$  for plunger
- ❑ Beam energy tuned to optimize the charge state distribution
- ❑ Several conditions to clean the spectrum from:
  - ❑ Reactions with the C foil
  - ❑ Coulomb excitation in the Ni foil

*Analysis by A. Goasduff*

# Preliminary results

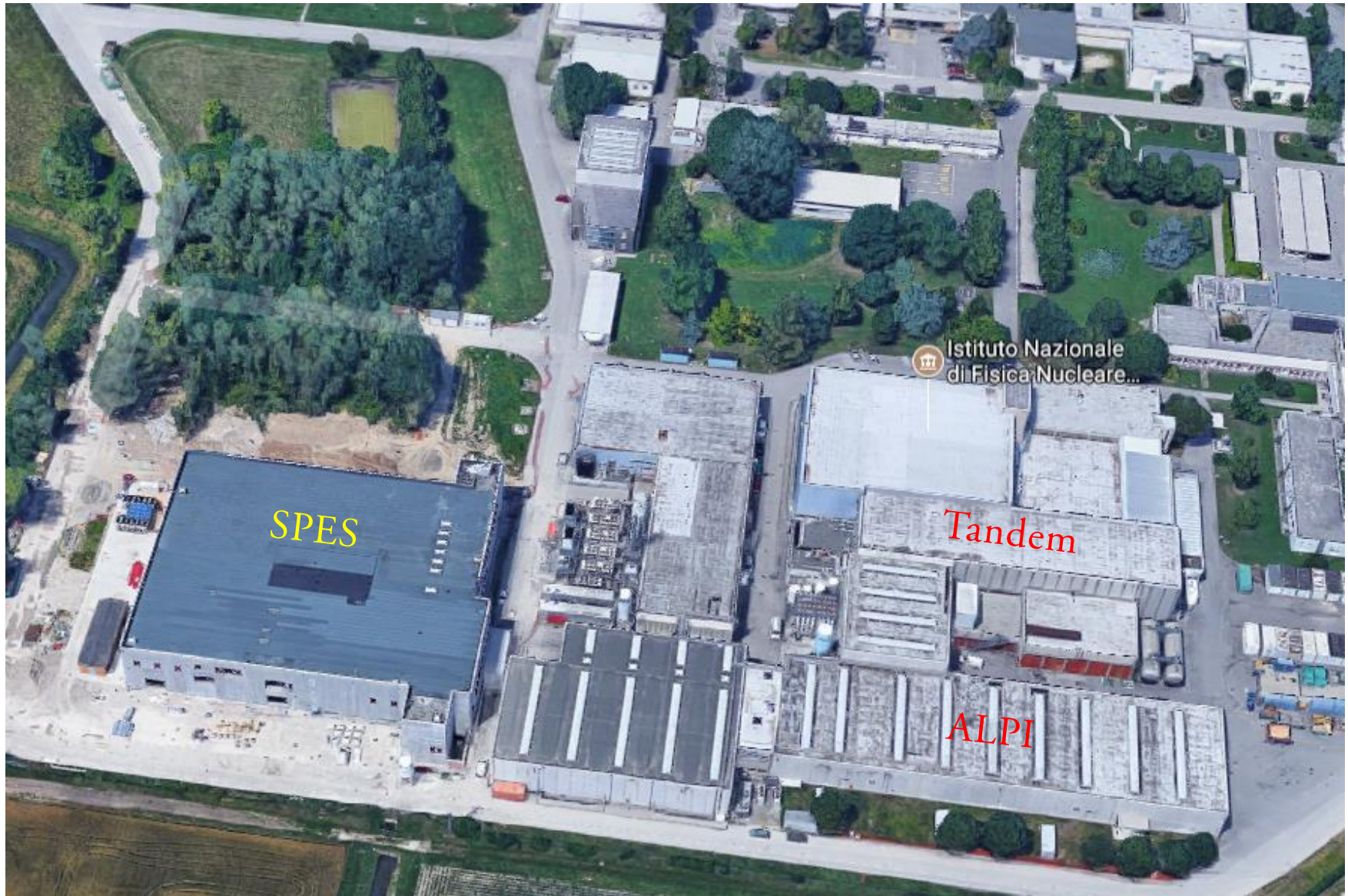


- Angular correlations for **ORGAM** detectors
  - For stopped and in-flight component
  - For all plunger distances



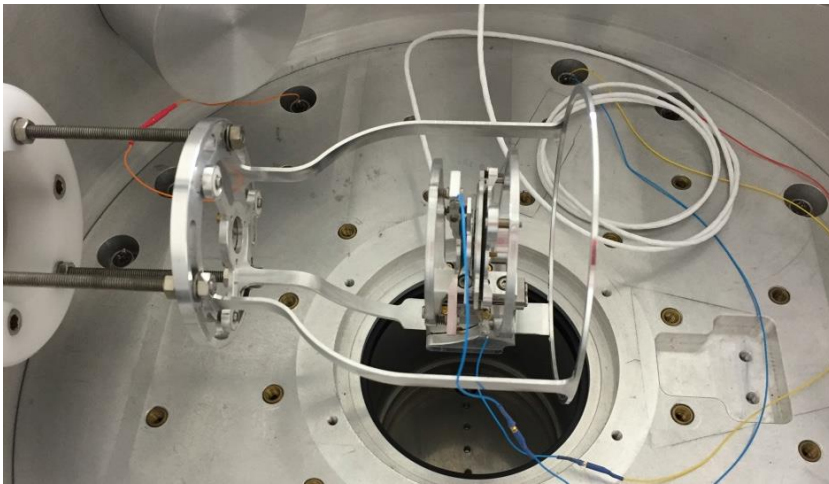
- Analysis of **MINIBALL** performed segment by segment

# LNL facilities



Essential ingredients:

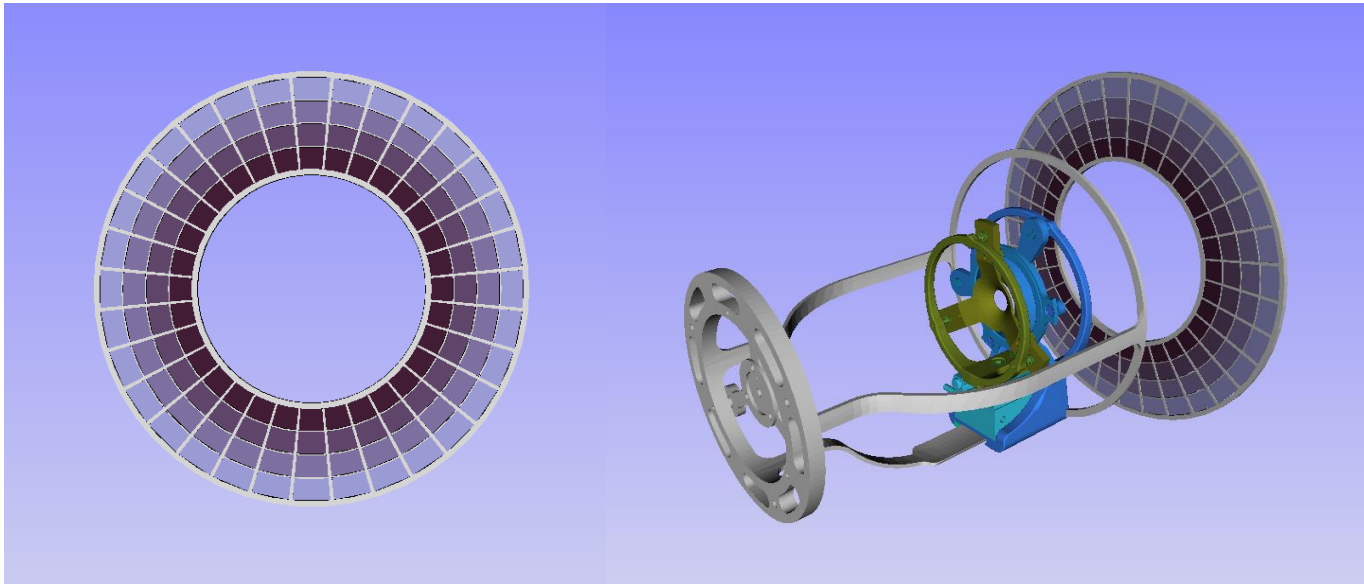
- ❑  $\gamma$ -ray transparency  
→ GALILEO array (phase1 2.4% at 1.3 MeV)
- ❑ Observe changes in the radiation pattern as a function of time  
→ IKP-LNL plunger
- ❑ Stable beam and post-accelerated SPES beam
- ❑ Segmentation in both  $\theta$ ,  $\phi$   
→ Particle detector (under development)



*Letter of Intent: High precision electromagnetic moment measurements with stable and radioactive nuclei with GALILEO and GALILEO plunger  
GALILEO + Plunger + Recoil detector  
A. Goasduff, A. Kusoglu et. al*

# LNL Particle detector

- ❑ Segmentation in both  $\theta$ ,  $\phi$   
→ Increased sensibility for g-factor and Doppler correction
- ❑ High counting rate capabilities and radiation hardness  
→ To be used with both stable and radioactive beams
- ❑ Coupling with the plunger and existing mechanics



Collaboration CSNSM (France), ANU (Australia), Istanbul University (Turkey) and INFN (Italy)

- ❑ Development of new recoil detector at forward angle:
  - ❑ high precision g-factor measurements taking advantage of:
    - ❑ Large efficiency of the GALILEO array at 90 degrees
    - ❑ PIAVE-ALPI beams ( $^{22}\text{Ne}, \dots$ )
    - ❑ High quality Mg beams
    - ❑ Exploration of the fp-shell nuclei to give calibration points to transient-field technique
  - ❑ Paving the way for the study of g-factor measurements in exotic nuclei with SPES RIBs beams
    - ❑ Post accelerated SPES beam  $\geq 10^5$  pps (neutron rich Zn, Ge and Se isotopes)
    - ❑ Study the evolution of the N=50 shell-closure towards  $^{78}\text{Ni}$

*Letter of Intent for SPES: Electromagnetic moment measurements with radioactive ion beams using GALILEO-ray array* A. Goasduff, A. Kusoglu et. al

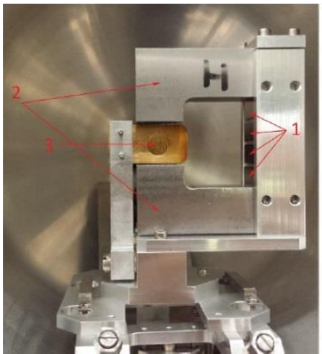




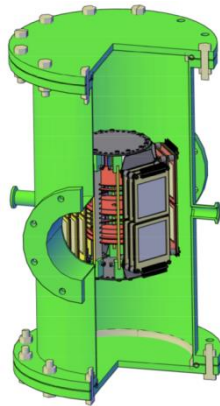
# Perspective Experiments @ELI-NP

- ❑ ELIADE array covers the backward angles
  - ❑ Triple and higher fold  $\gamma\gamma$ -coincidence
- ❑ ELI-BIC can be mounted at forward angles
- ❑ Fast-timing  $\text{LaBr}_3$  detectors
- ❑  $g$ -factor magnets
- ❑ Fission plunger

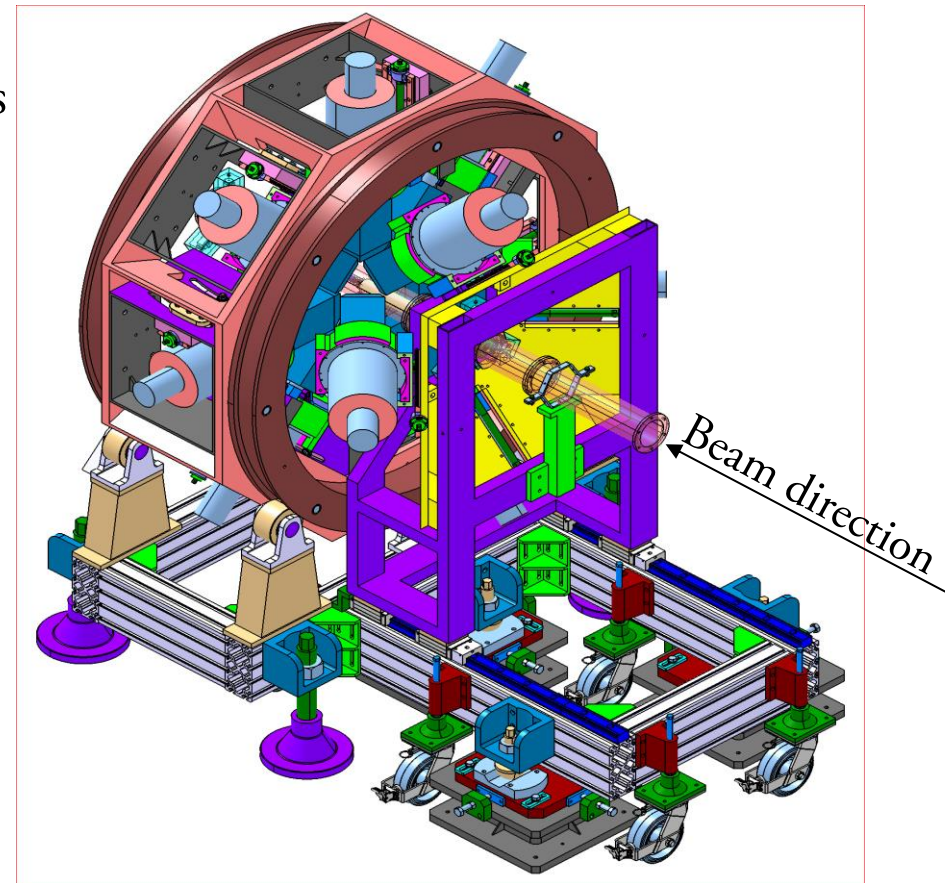
Permanent magnet



ELI-BIC



ELIADE Array



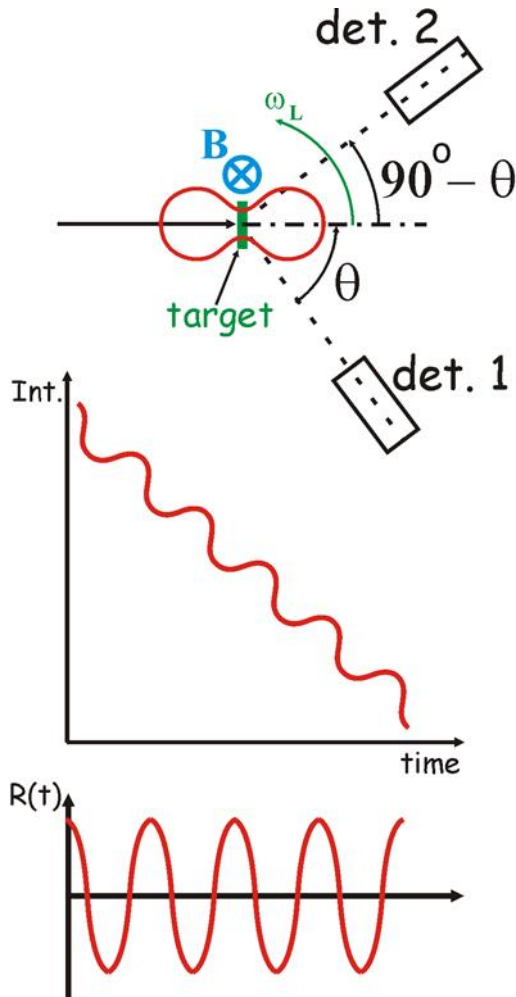
courtesy of C. Petku ELI-NP

- ❑  $g$ -factors of **short-lived nanosecond isomers** can be studied via in-beam  $\gamma$ -ray spectroscopy of fission fragments, using **ELIADE array**

Remember talk of G. Suliman

*D.L. Balabanski et al., Romanian Rep. in Phys. Vol 68, S621-S698 (2016)*

- Suitable Technique for isomeric lifetimes Time Differential Perturbed Angular Distribution (TDPAD)



$$I(t, \theta, B) = I_0 e^{-t/\tau} W(t, \theta, B)$$

$$W(t, \theta, B) = \sum_{k=\text{even}} A_k B_k P_k \cos(\theta - \omega_L t)$$

$$R(t) = \frac{I(\theta, t) - \varepsilon I(\theta + \pi/2, t)}{I(\theta, t) + \varepsilon I(\theta + \pi/2, t)} = \frac{3A_2 B_2}{4 + A_2 B_2} \cos\{2(\theta - \omega_L t - \alpha)\}$$

$A_2$  – angular distribution coefficient;  
 $B_2$  – nuclear orientation coefficient

- $\gamma$ -decay of excited states using photo fission of  $^{232}\text{Th}$  or  $^{238}\text{U}$
- understanding of the deformed  $A \sim 100$  and  $A \sim 150$  mass regions
  - $^{93,94,95}\text{Rb}$ ,  $^{95,97}\text{Sr}$ ,  $^{99}\text{Zr}$
  - Vicinity of doubly-magic  $^{132}\text{Sn}$  ( $^{130,131,132}\text{Sn}$ ,  $^{131}\text{Sb}$ ,  $^{133}\text{Te}$ ,  $^{132,134,135}\text{Te}$ )

# Collaboration

## ALTO TDRIV in $^{24}\text{Mg}$

- **A.E. Stuchbery** – *Department of Physics, RSPE, Australian National University, Canberra ACT 0200, Australia*
- **G.Georgiev, A. Goasduff**, J. Ljungvall, C. Sotty - *CSNSM, CNRS/IN2P3; Université Paris-Sud 11, UMR8609, F-91405 ORSAY-Campus*
- B.A. Brown - *National Superconducting Cyclotron Laboratory, Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA*
- D. L. Balabanski - *Extreme Light Infrastructure-Nuclear Physics Facility, MG-G Bucharest Magurele, Romania*
- M. Bostan - *Istanbul University, Vezneciler/Fatih, 34134, Istanbul, Turkey*
- L. Atanasova, P. Detistov - *Institute for Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, BG-1784, Sofia, Bulgaria*
- M. Danchev, K. Gladnishki - *Faculty of Physics, University of Sofia, Bulgaria*
- I. Matea, I. Stefan, D. Verney - *IPN, Orsay, France*
- D. Radeck - *IKP, University of Cologne, D-50937 Cologne, Germany*
- D.T. Yordanov - *ISOLDE, CERN, Switzerland*

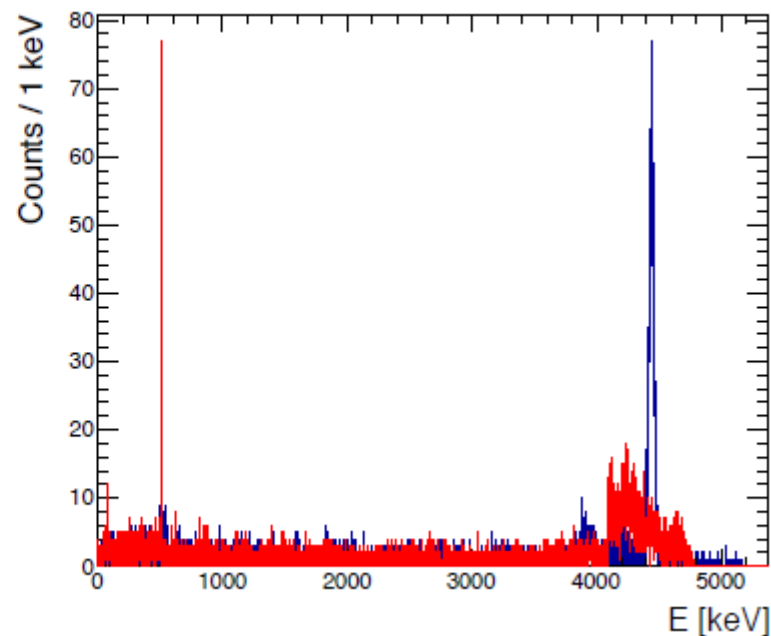
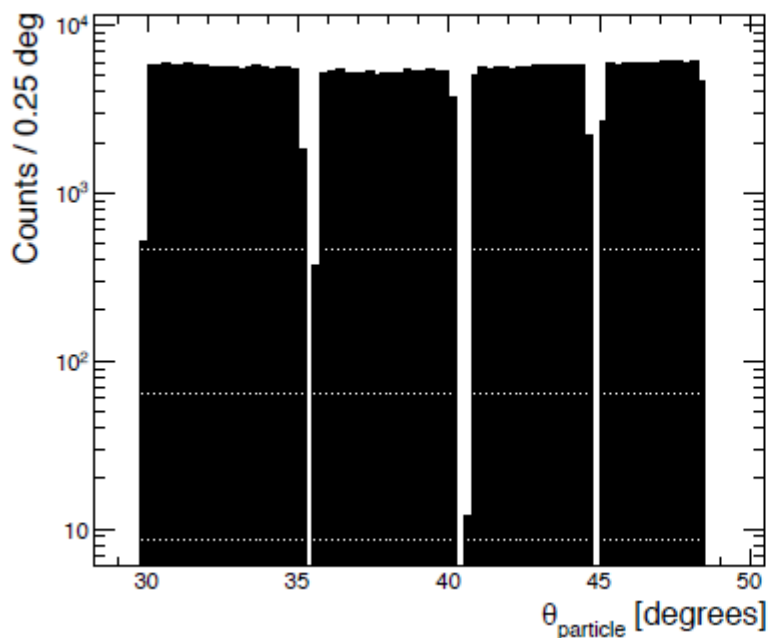
## ALTO TDRIV in $^{56}\text{Fe}$

- **A.E. Stuchbery** – *Department of Physics, RSPE, Australian National University, Canberra ACT 0200, Australia*
- **G.Georgiev, A. Goasduff**, J. Ljungvall, T. Konstantinopoulos - *CSNSM, CNRS/IN2P3; Université Paris-Sud 11, UMR8609, F-91405 ORSAY-Campus*
- I. Matea, A. Gottardo, D. T. Yordanov - *IPN, Orsay, France*
- K. Gladnishki - *Faculty of Physics, University of Sofia, Bulgaria*
- N. Warr - *Institut für Kernphysik, Universitat zu Köln, D-50937 Köln, Germany*



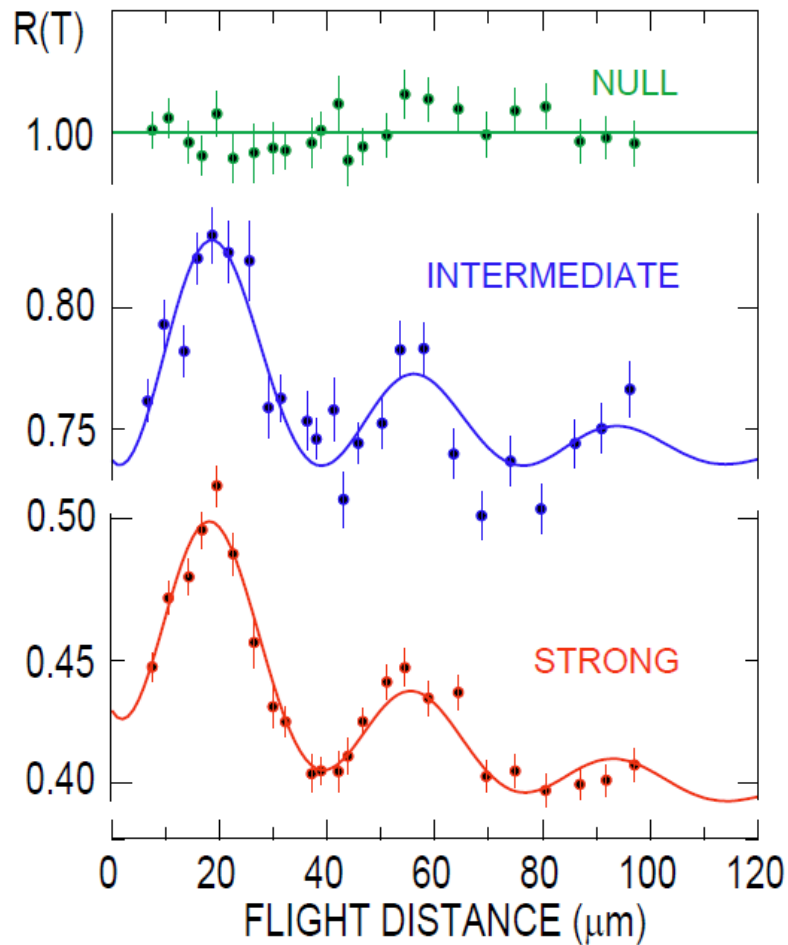
THANK YOU!

- $^{12}\text{C}$  Coulomb Excitation reaction on  $^{208}\text{Pb}$  target  $5\text{ mg/cm}^2$



- FWHM of 44 keV is achievable for the  $2^+ \rightarrow 0^+$  transition of  $^{12}\text{C}$  (4.4 MeV)

# Results



45% H-like, 43 % bare ions or He-like,  
12 % L-shell contribution  
 $B_{1s} = 29.09$  kTesla with GRASP2K

*A. Kusoglu et al. PRL, 114, 062501, 2015*

## Resulting $g$ -factor with statistical error

Ratio of particle- $\gamma$ combination	Label	Resulting $g$ - factor
n=14	strong	0.538(13)
n=17	intermediate	0.539(24)
n=18	weak	0.54(3)
Total weighted average:		<b>0.538(11)</b>

Source of systematic error	Value	Resulting $g$ factor
Target to particle distance	61.0(1.5) mm	$\pm 0.0045$
lifetime	1.97(5) ps	$\pm 0.0040$
$v/c$	0.0915(5)	$\pm 0.0035$
Distribution of hyperfine fields		$\pm 0.0010$
Total weighted average:		<b><math>\pm 0.0070</math></b>

$$|g(2^+)| = 0.538(13)$$

*Total uncertainty < 3%*

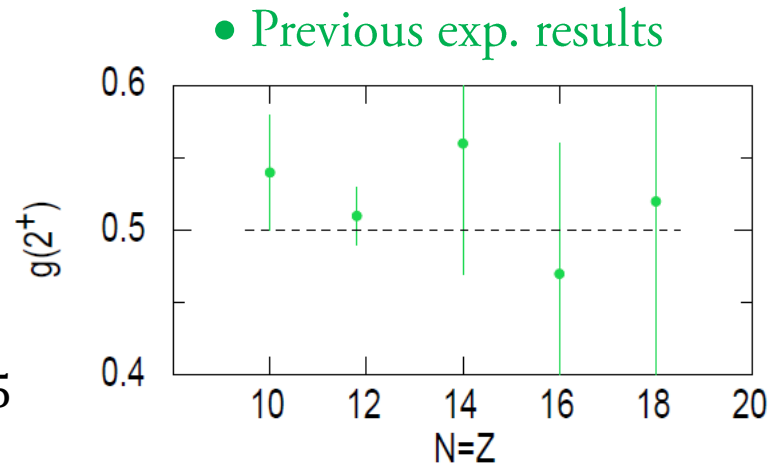
# TDRIV using H-like $^{24}\text{Mg}$ ions @ ALTO, Orsay

$$\mu = gI = g_{\ell_0} \langle \ell_0 \rangle + g_{s_0} \langle s_0 \rangle$$

$$I = \langle \ell_0 \rangle + \langle s_0 \rangle$$

$$\langle s_0 \rangle = 0$$

$$g_{\ell_p} = 1 \quad g_{\ell_n} = 0 \quad g_{\ell_0} = \frac{g_{\ell_p} + g_{\ell_n}}{2} = 0.5$$



☞ Experimentally **little departure from  $g = 0.5$**  for the  $g$  factors of the first-excited states of **even-even nuclei with  $N = Z$** .

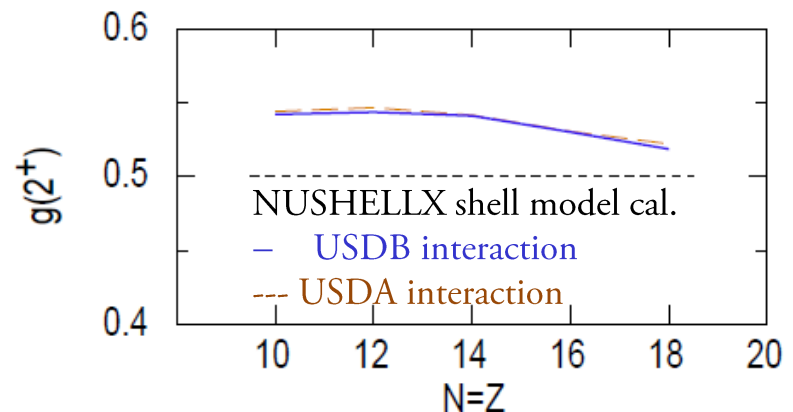
*Brown B. A. JPG 8(5), 679, 1982.*

☞ Recent shell-model calculations predict **departures from  $g = 0.5$**  by up to 10% for the first-excited  $2^+$  states in the  $N = Z$   $sd$ -shell nuclei **from  $^{20}\text{Ne}$  to  $^{36}\text{Ar}$** .

*Richter W.A., PRC, 78, 064302, 2008*

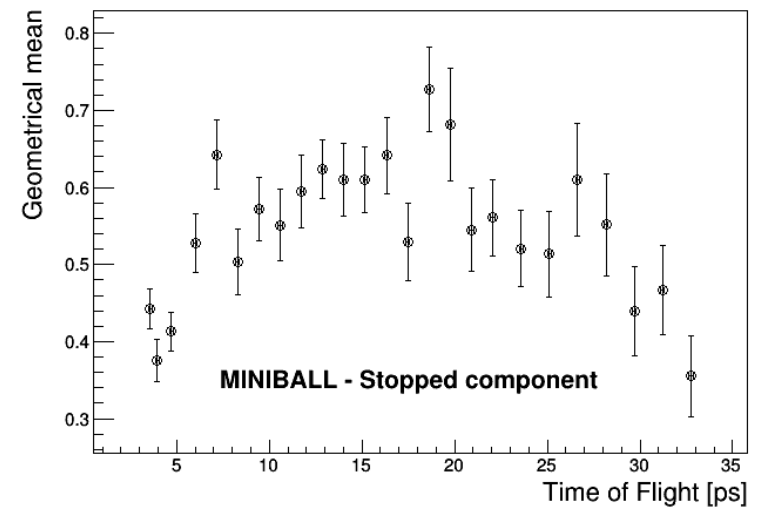
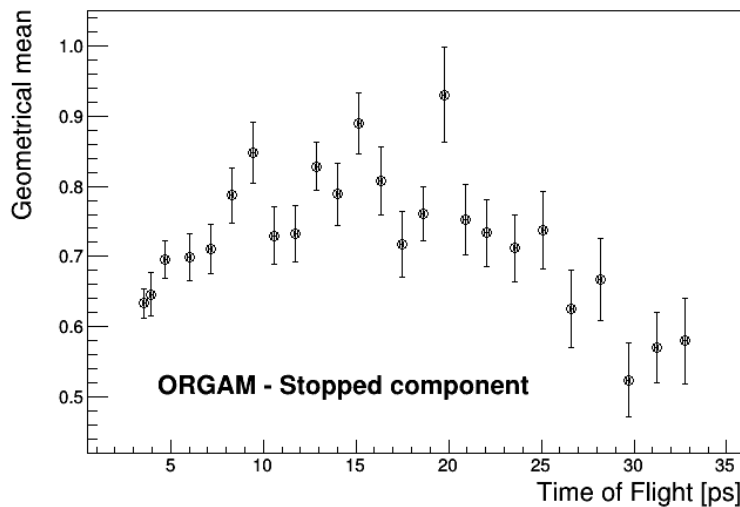
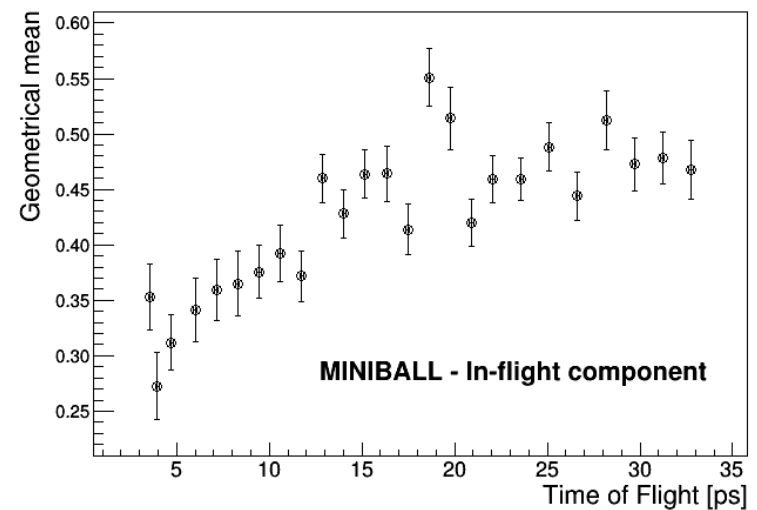
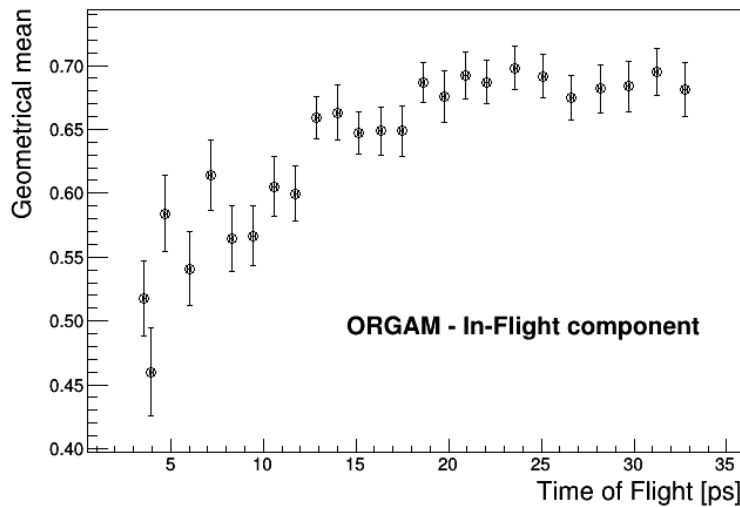
☞ These departures:

- configuration mixing
- isospin mixing
- meson exchange



# Preliminary results

□ Similar behavior for **ORGAM** and **MINIBALL** detectors



*Analysis by A. Goasduff*