



# Exploring the low Z-shore of the Island of Deformation at N=60 using AGATA and VAMOS

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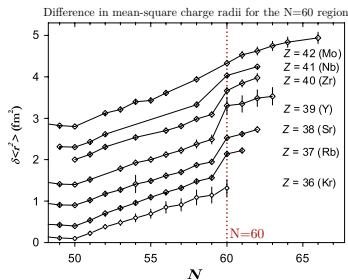
<sup>2</sup>GANIL, Caen

<sup>3</sup>Institut Pluridisciplinaire Hubert Curien, Strasbourg

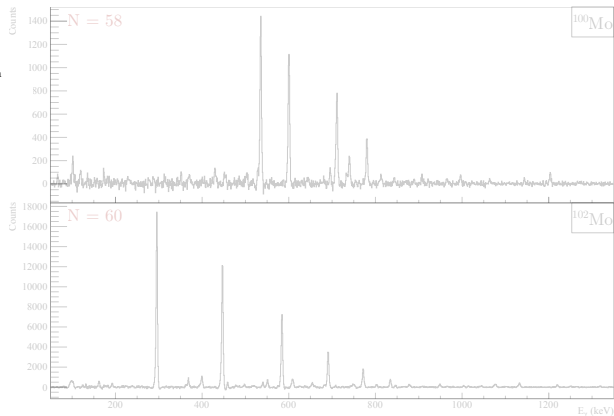
NUSPIN 2017: 26-29 June, GSI

# What are the limits of this N=60 island of deformation

- The Z=40 and N=60 region gives a remarkable example of sudden nuclear shape transition:
  - This effect seems to start at Z=42 (Mo) and  $\nearrow$  with  $\searrow$  Z
  - N=58 : quasi-spherical shape  $\Rightarrow$  N=60 : rigid rotors with large deformation ( $\beta_2 \sim 0.4$ )

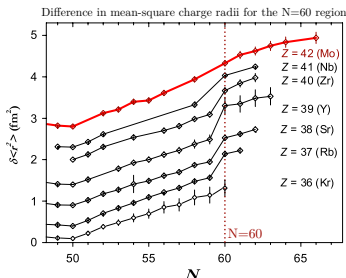


S. Naimi *et al.*, Phys. Rev. L **105**, 032502 (2010)

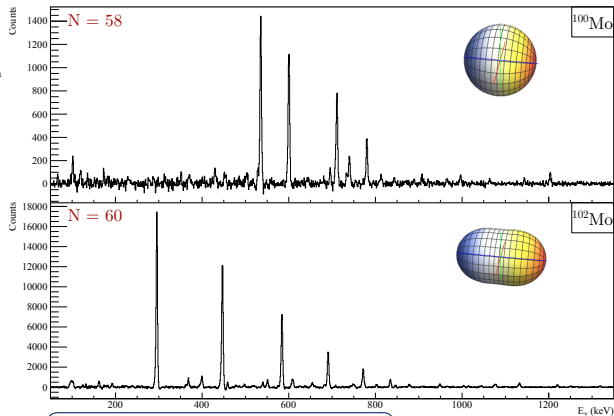


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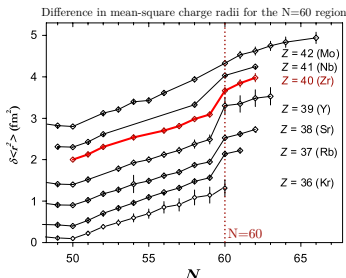
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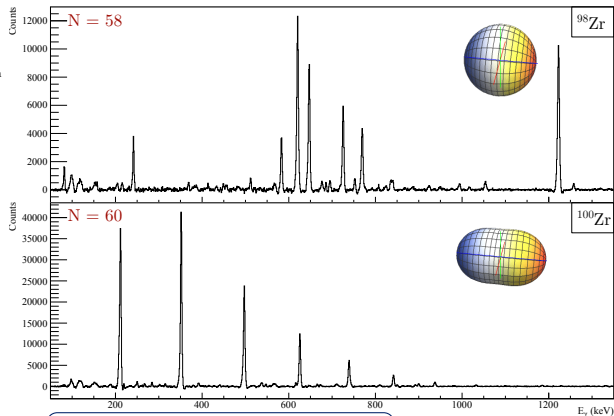
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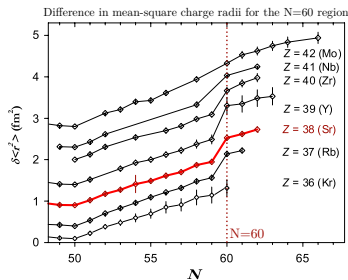
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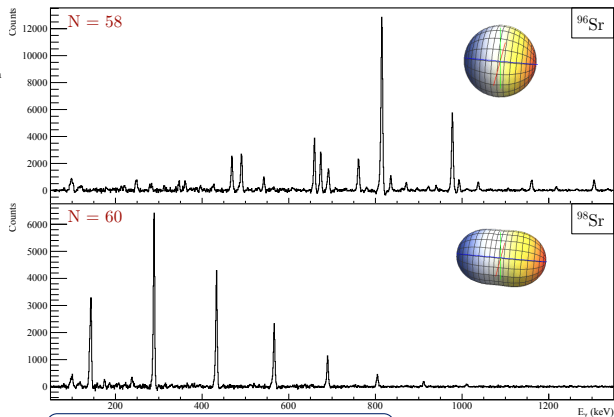
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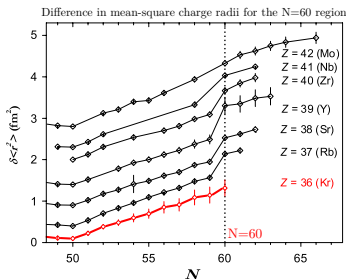


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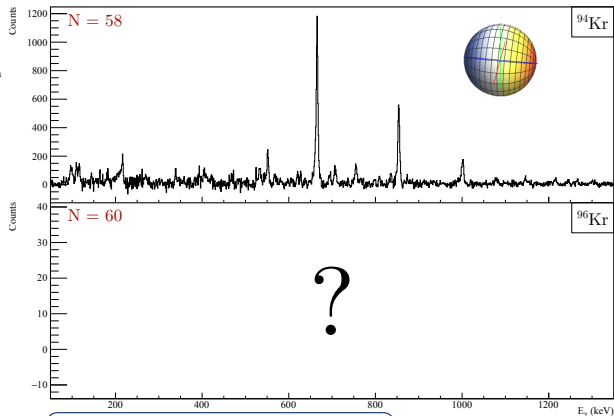


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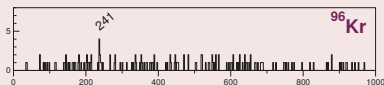
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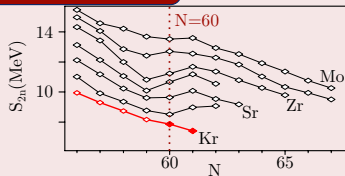
data from this experiment: <sup>238</sup>U@6.2 MeV/u on <sup>9</sup>Be

$^{96}_{36}\text{Kr}_{60}$  in the literatureN. Marginean *et al.*, Phys. Rev. C 80, 021301 (R) (2009)

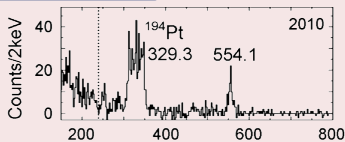
- Energy of the  $2^+_1$  excited state measured at 241 keV:
  - ⇒ Sudden drop of the  $E(2^+_1)$  from  $^{94}\text{Kr}$  to  $^{96}\text{Kr}$
  - ⇒ Possible rapid change in the ground state deformation as for Mo, Zr and Sr isotopic chains

S. Naimi *et al.*, Phys. Rev. L 105, 032502 (2010)

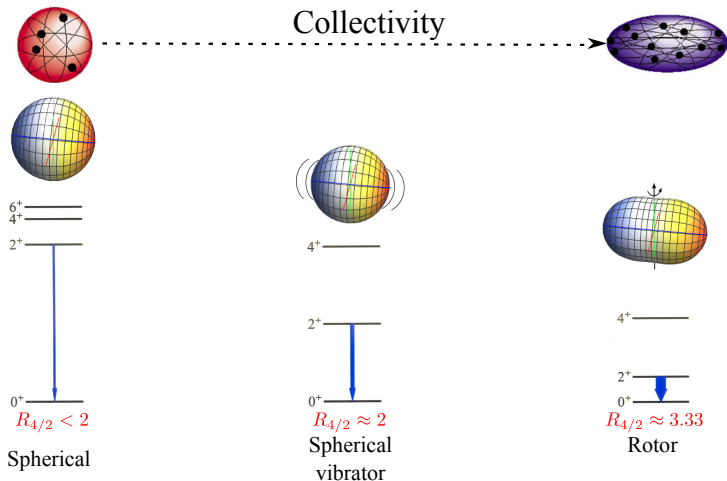
- Mass measurement of  $^{96,97}\text{Kr}$ :
  - ⇒ Contrary to the heavier isotopic chains,  $S_{2n}$  still decrease after N=58
  - ⇒ Result in contradiction with Marginean *et al.*

S. Albers *et al.*, Phys. Rev. L 108, 062701 (2012)

- Energy of the  $2^+_1$  excited state measured at 554.1 keV (no  $\gamma$  at 241 keV):
  - ⇒ This  $\gamma$  spectroscopic result imply a smooth onset of deformation in neutron-rich Kr isotopes around N=60
  - ⇒ Result in contradiction with Marginean *et al.* but validating Naimi *et al.* results



# $B(E2)$ , $R_{4/2}$ : main indicators of collectivity



$B(E2; 2_1^+ \rightarrow 0_1^+)$ : reduced electric quadrupole transition probability  
 $R_{4/2} = E(4^+)/E(2^+)$



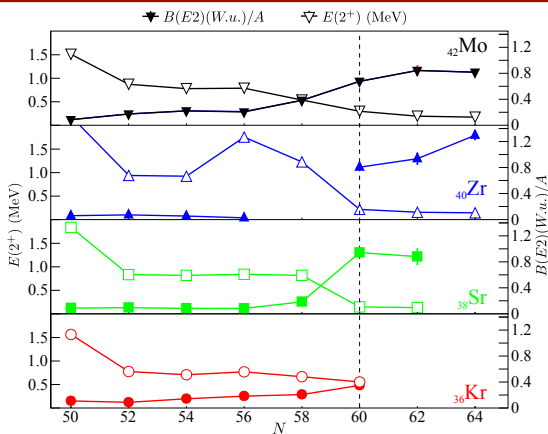
## Systematic in the region

## Standard increasing of collectivity

$\Rightarrow E(2_1^+) \text{ vs } B(E2 : 2^+ \rightarrow 0^+) : E(2_1^+) \searrow, B(E2) \nearrow$

$\Rightarrow R_{4/2} = E(4^+)/E(2^+) \text{ vs } B(E2 : 2^+ \rightarrow 0^+) : R_{4/2} \nearrow, B(E2) \nearrow$

$\hookrightarrow$  Kr follows a standard smooth increase of collectivity



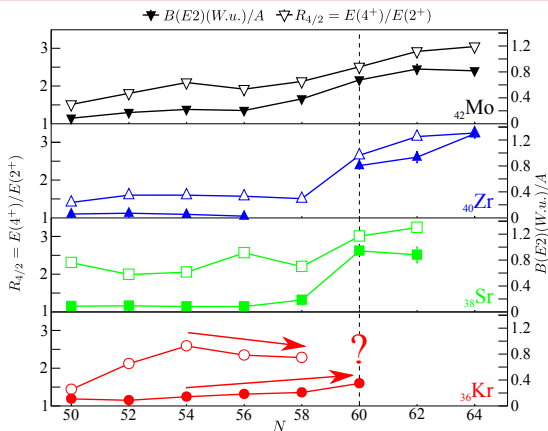
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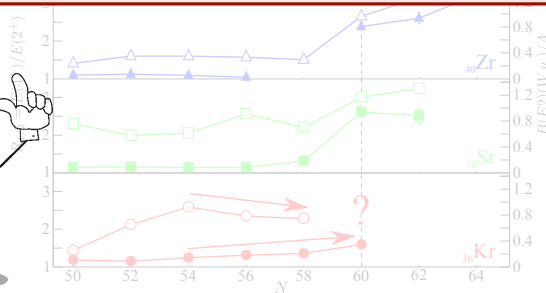
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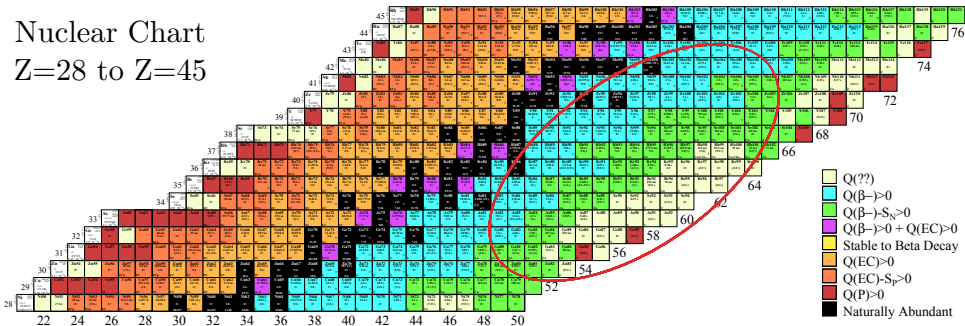
### Quid of $^{96}\text{Kr}$

- How can we resolve this contradiction on the  $2_1^+$  state energy ?  
 $\Rightarrow$  New high resolution  $\gamma$ -ray spectroscopy with isotopic identification
- Does this unexpected trend between  $R_{4/2}$  and  $B(E2)$  persists at N=60 ?
- What are the consequences on the nuclear  $^{96}\text{Kr}$  structure ?  
 $\Rightarrow$  Need spectroscopic measurements beyond the  $2_1^+$  state



# How to populate Z=40 and N=60 region ?

## Nuclear Chart Z=28 to Z=45

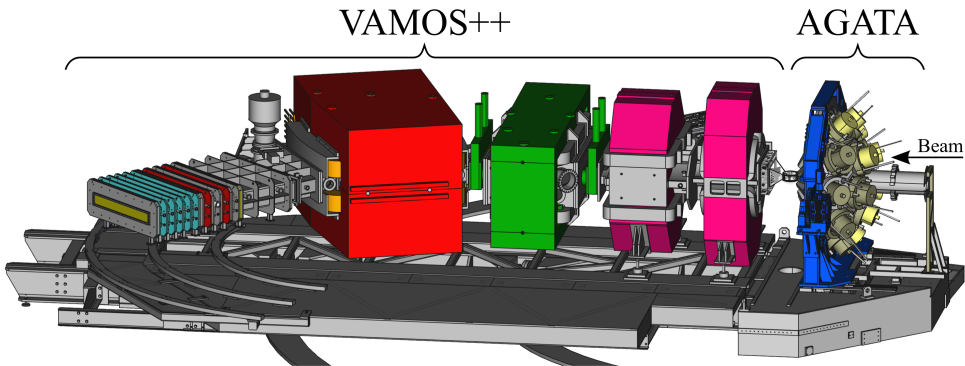


⇒ Transfer and fusion induced fission reactions in inverse kinematics:

# Experimental setup

## AGATA@GANIL: E680 experiment (May 2015)

- Spokesperson: Gilbert Duchêne (IPHC Strasbourg)
- Reaction : Transfer and fusion induced fission:  
 $\hookrightarrow {}^{238}\text{U}@6.2\text{ MeV/u} + {}^9\text{Be}$  ( $1.85\text{ mg/cm}^2$ ),  $I \sim 6 \times 10^9\text{ pps}$
- Setup : VAMOS++ and AGATA spectrometers

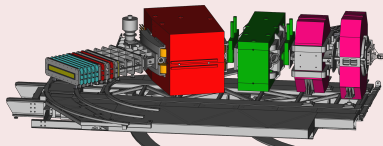


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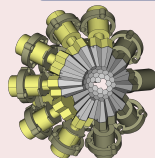
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### VAMOS++ setup



- VAMOS angle :  $28^\circ$
- A, Z identified nuclei:  $5 \times 10^8$
- Recoil velocity :  $\beta \sim 0.11$
- Validation rate :  $\sim 1.5 \text{ kHz}$

### AGATA setup



- Detectors : 24 crystals
- Geometry : compact ( $\sim 14 \text{ cm}$ )
- Tracked eff.:  $\sim 10\%@1 \text{ MeV}$
- Trigger : VAMOS++ & AGATA

# Multi-parametric analysis of the VAMOS++ spectrometer

## VAMOS++ spectrometer

### ● Mass identification

↪ Nucleus trajectory reconstruction

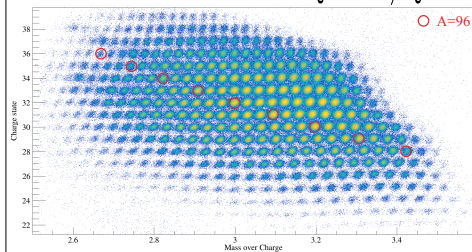
↪ Velocity measurement

↪ Total energy measurement

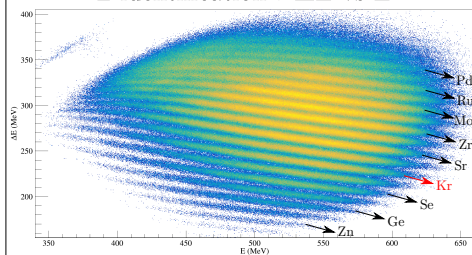
### ● Z identification

↪ Energy measurement ( $\Delta E$ -E method)

### Mass identification : Q vs M/Q



### Z identification : $\Delta E$ vs E



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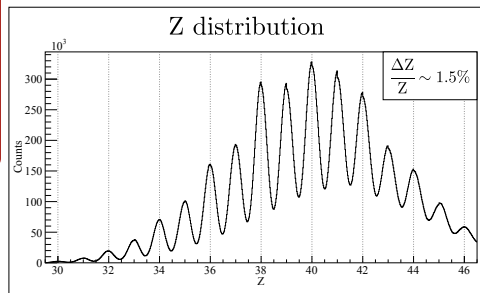
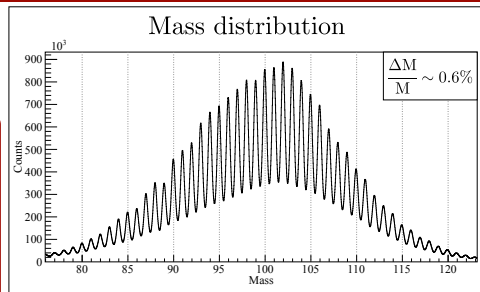
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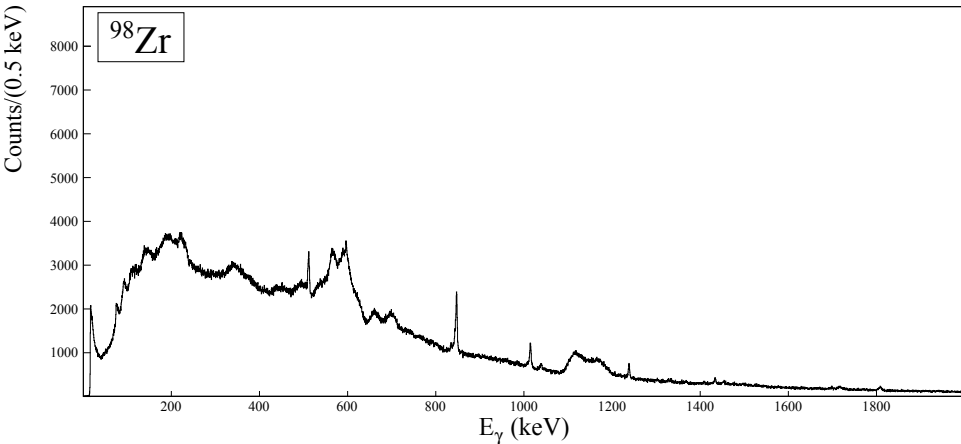




# VAMOS++: Conclusions on VAMOS analysis

## Results

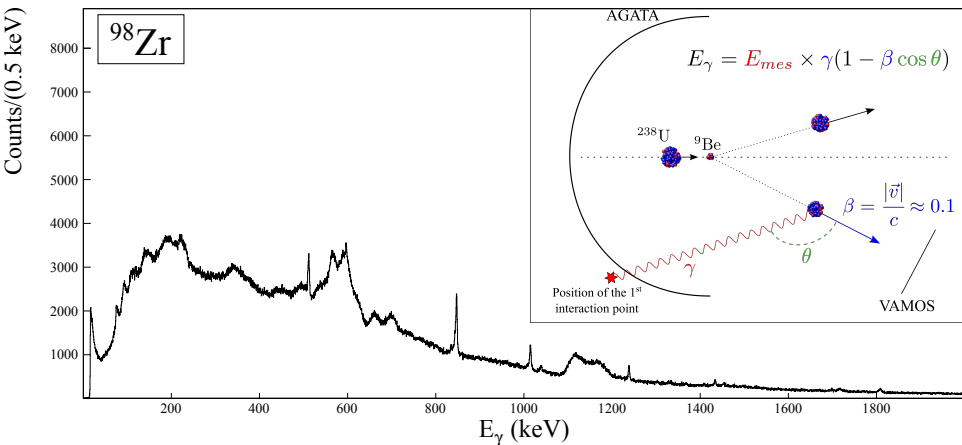
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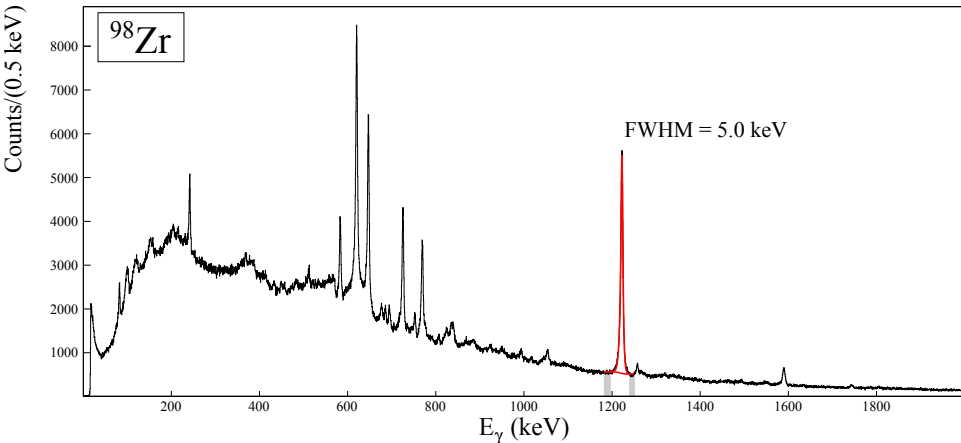
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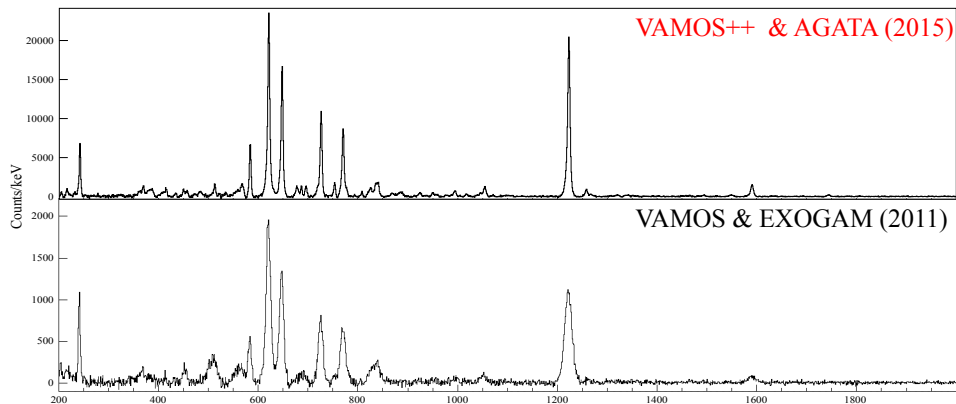
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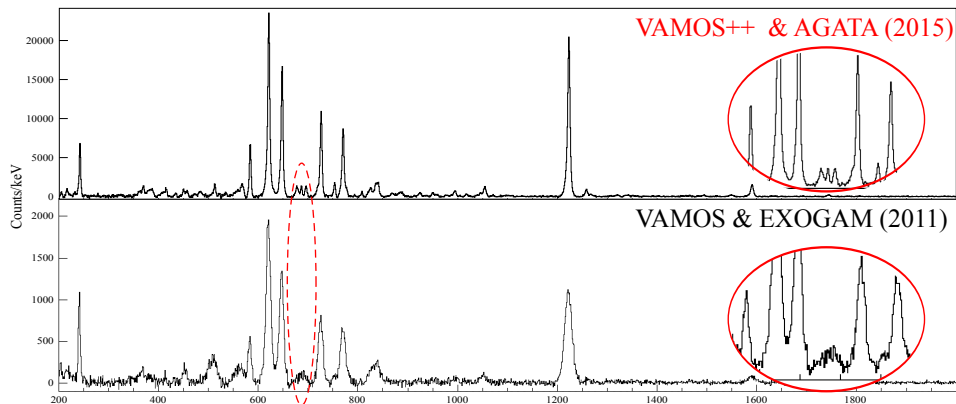
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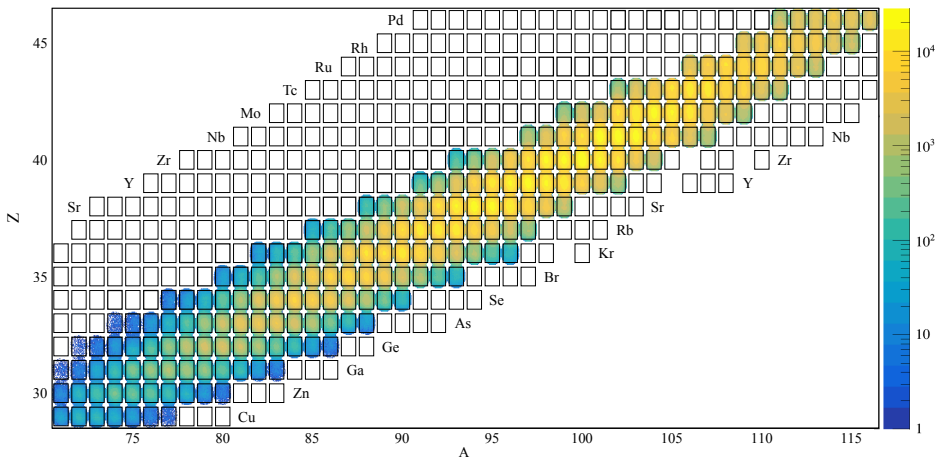
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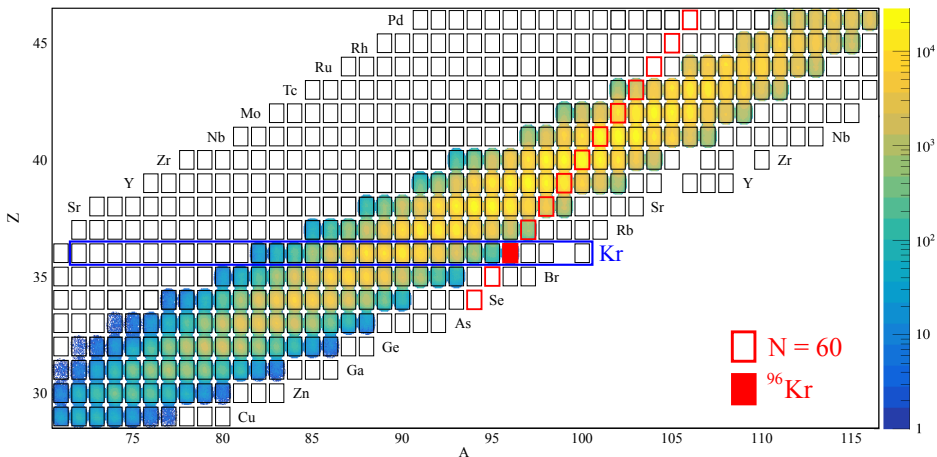
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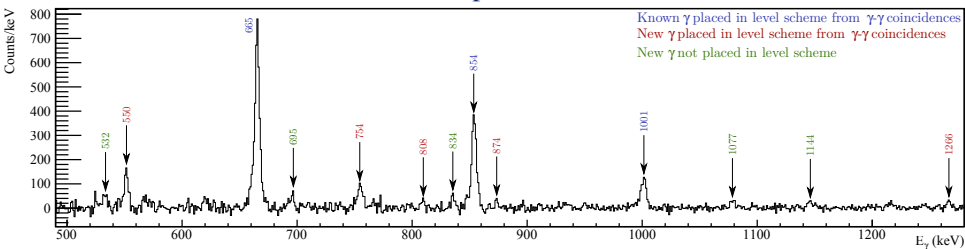
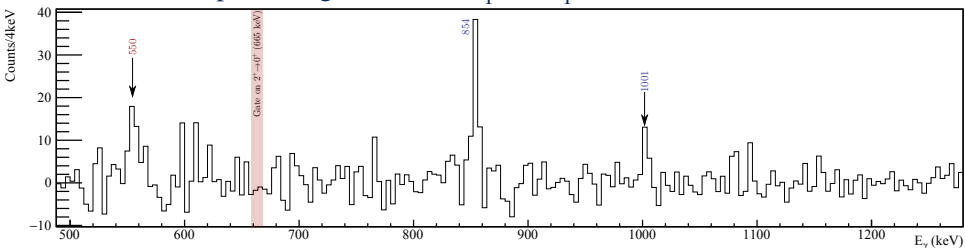


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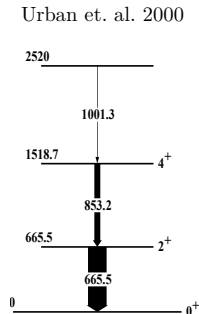
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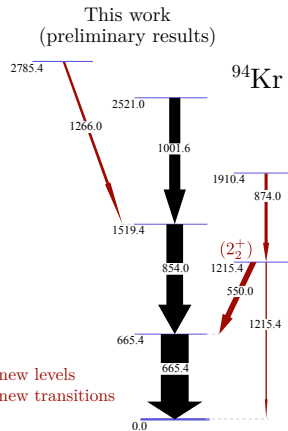


Spectroscopic results for Kr isotopes:  $^{94}\text{Kr}$  $^{94}\text{Kr}$  spectrum $^{94}\text{Kr}$  spectrum gated on the  $2_1^+ \rightarrow 0_1^+$  transition (665 keV)

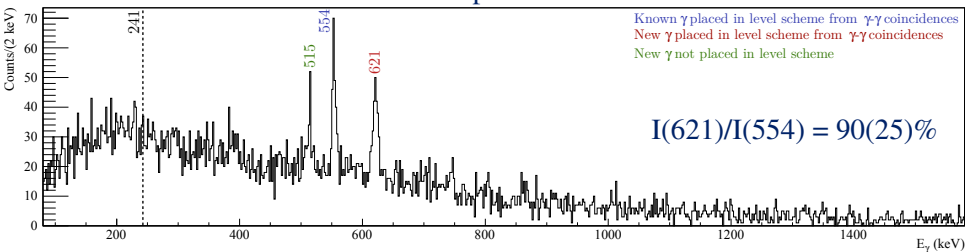
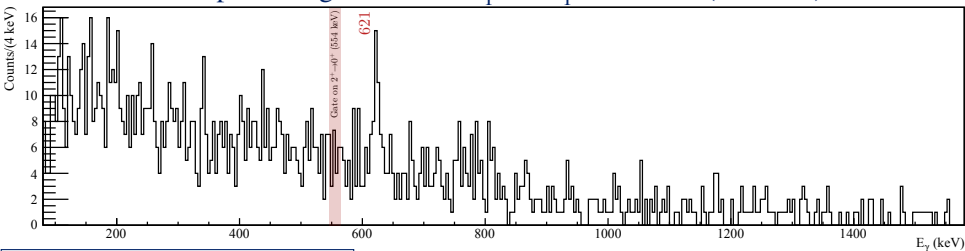


Spectroscopic results for Kr isotopes:  $^{94}\text{Kr}$  Level Scheme

- Spontaneous fission of  $^{248}\text{Cm}$ 
  - ⇒ EUROGAM 2 array
  - ⇒  $2.5 \times 10^9$   $\gamma$  coincidences of fold  $\geq 3$



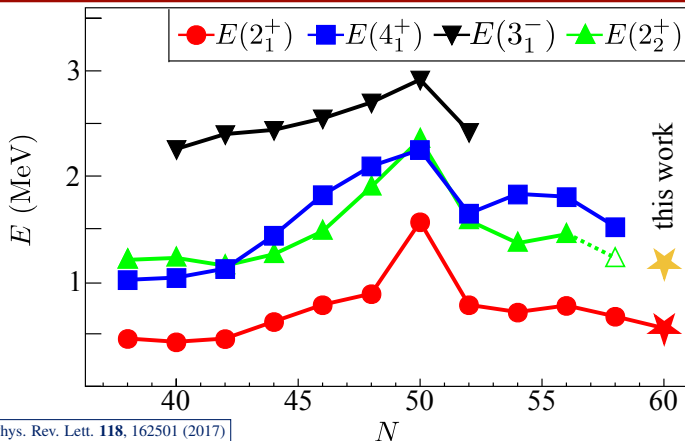
- $^{238}\text{U} + \text{Be}$  @ GANIL
  - ⇒ 24 AGATA crystals
  - ⇒  $5 \times 10^8$  A, Z identified fission fragments

Spectroscopic results for Kr isotopes:  $^{96}\text{Kr}_{60}$  $^{96}\text{Kr}$  spectrum $^{96}\text{Kr}$  spectrum gated on the  $2_1^+ \rightarrow 0_1^+$  transition (554 keV)J. Dudouet *et al.*, Phys. Rev. Lett **118**, 162501 (2017)

## Spectroscopic analysis

## Possible attributions: systematic on Kr isotopes

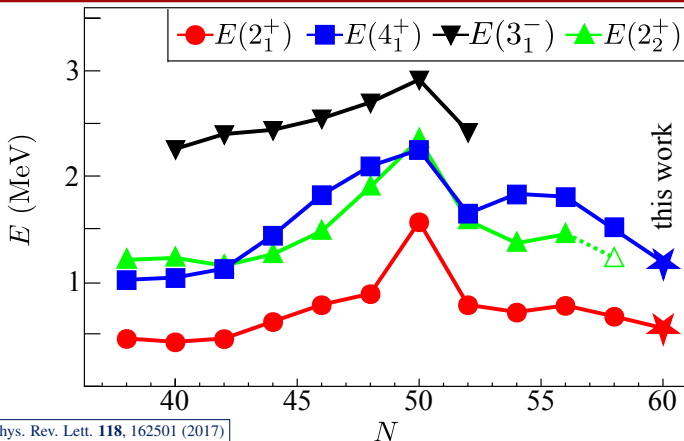
- $3_1^-$  : Energy ? – Intensity ( $\sim 0 \rightarrow 30\%$ ) ?  $I(621)/I(554) = 90(25)\%$
- $2_2^+$  : Energy ? – Intensity ( $\sim 0 \rightarrow 20\%$ ) ?
- $4_1^+$  : Energy ? – Intensity ( $\sim 50 \rightarrow 100\%$ ) ?



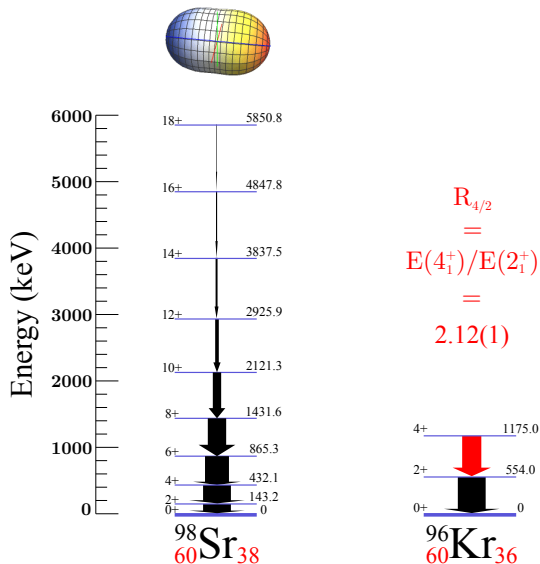
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- $I(621)/I(554) = 90(25)\%$
- 621 keV :  $4_1^+(1175 \text{ keV}) \rightarrow 2_1^+(554 \text{ keV})$



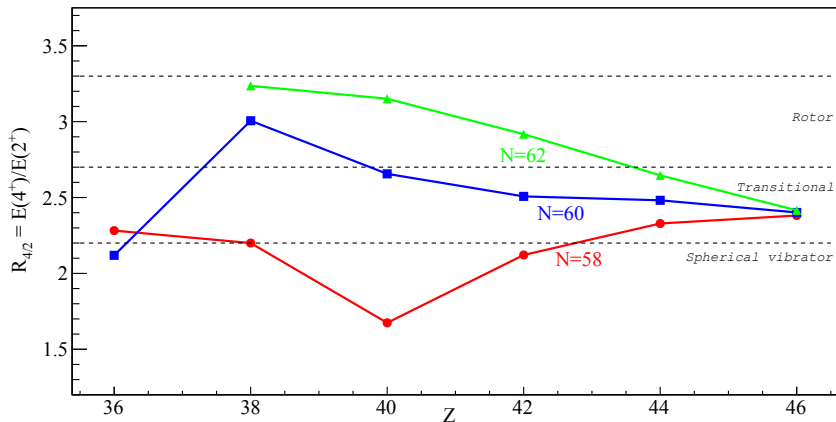
# Level scheme of the N=60 GS band



# The $^{96}\text{Kr}$ case : low Z boundary of the $A \sim 100$ island of deformation

Informations from the  $R_{4/2} = E(4^+)/E(2^+)$  ratio

- ⇒ Sharp transition at N=60 when moving from Sr to Kr
- ⇒  $R_{4/2}$  value confirms previous observations:  $^{96}\text{Kr}$  seems not highly deformed

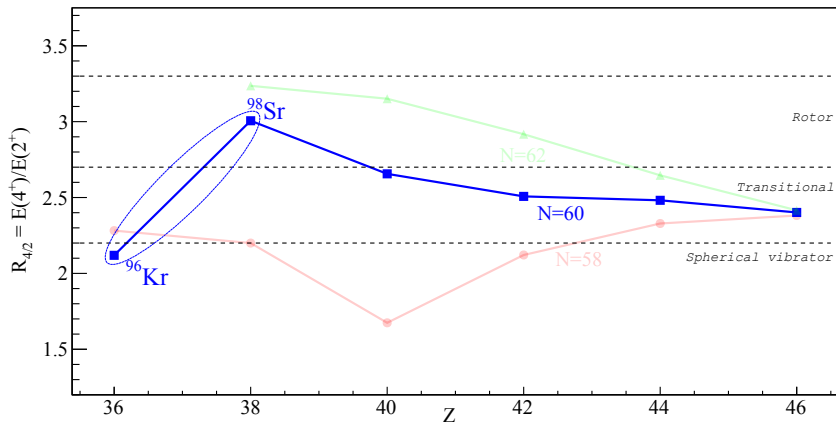


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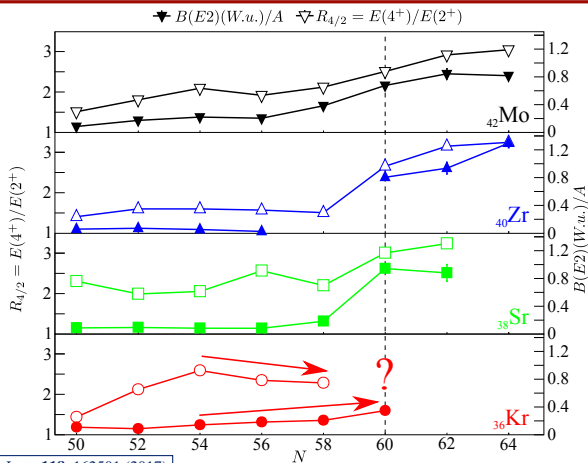
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# The strange behaviour of Kr nuclei

Usual increasing of collectivity

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$\hookrightarrow$  Kr follows an unexpected trend between  $R_{4/2}$  and  $B(E2)$  up to  $N = 58$



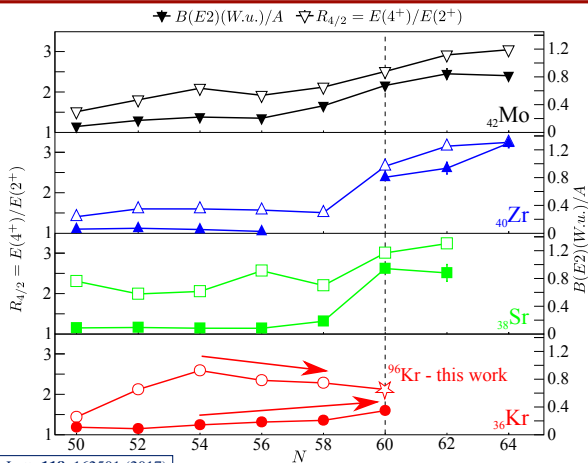


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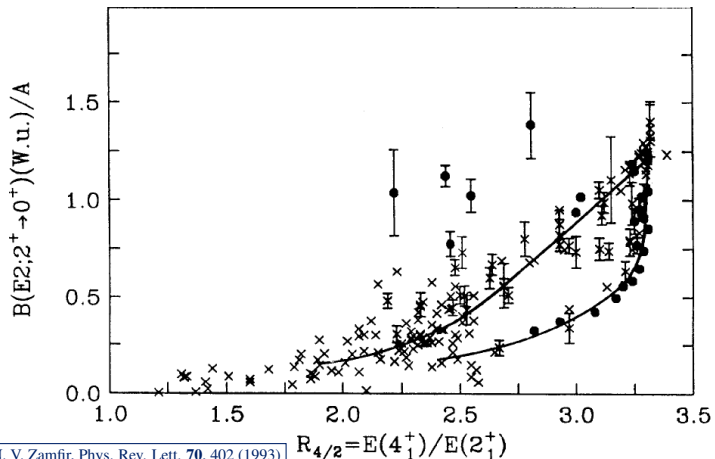


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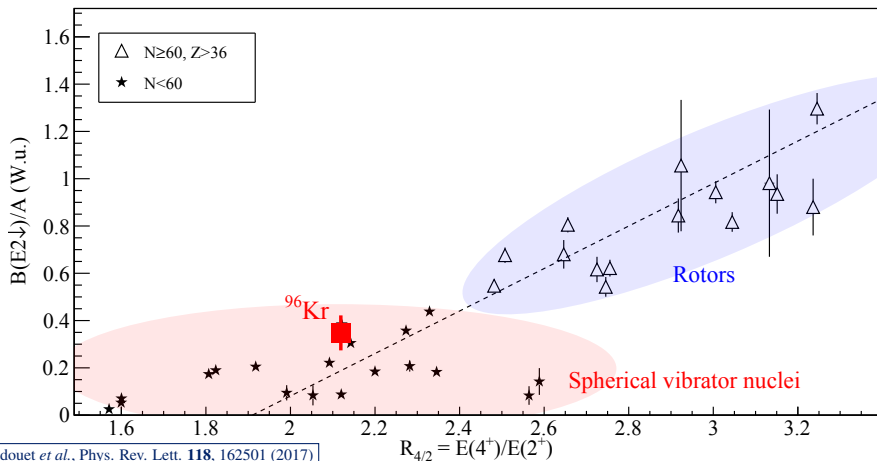
R. F. Casten and N. V. Zamfir, Phys. Rev. Lett. **70**, 402 (1993)

# The strange behaviour of Kr nuclei

Usual increasing of collectivity

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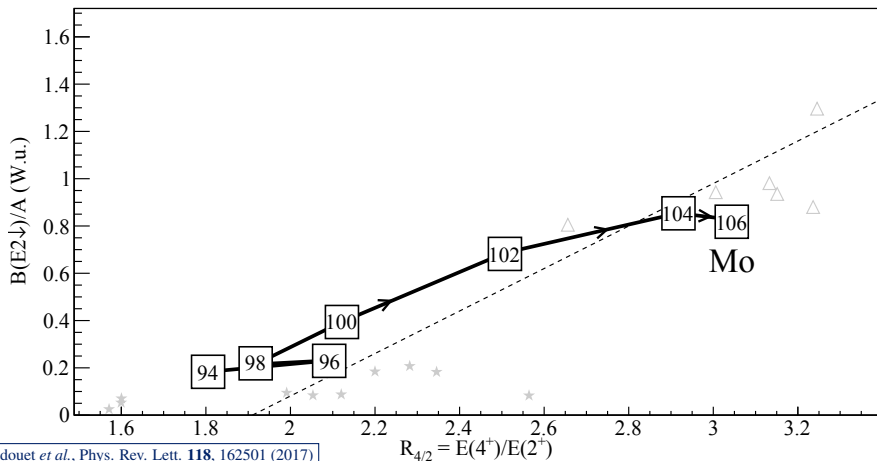
J. Dudouet *et al.*, Phys. Rev. Lett. **118**, 162501 (2017)

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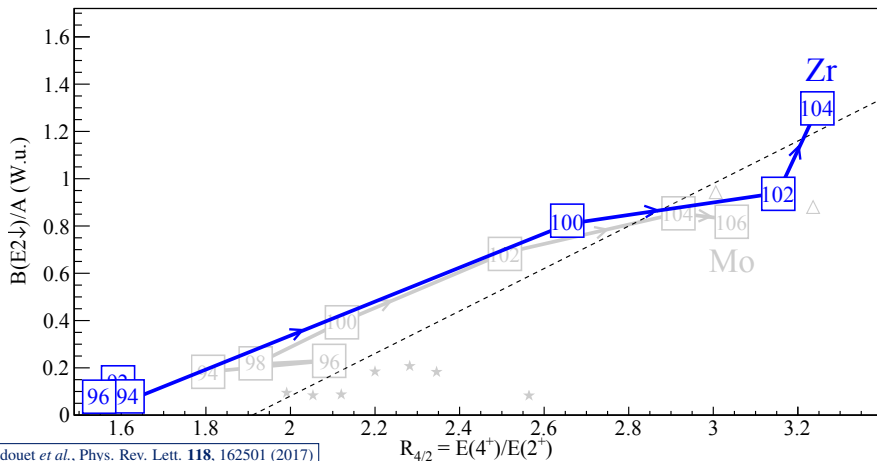


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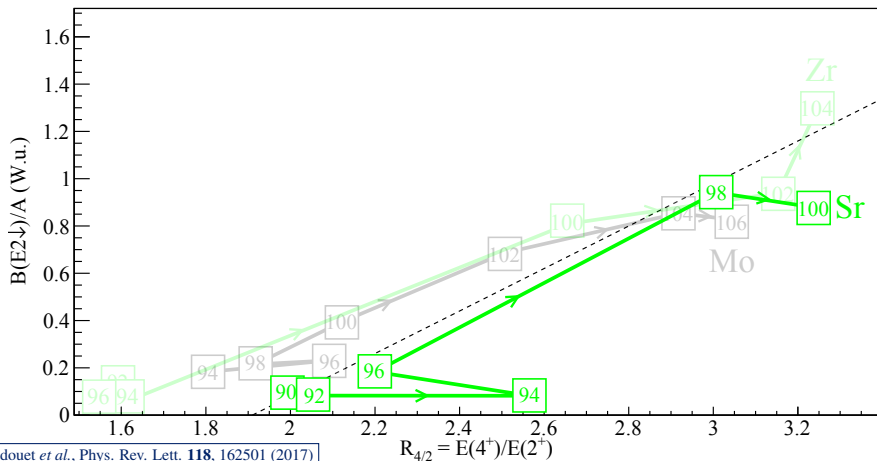
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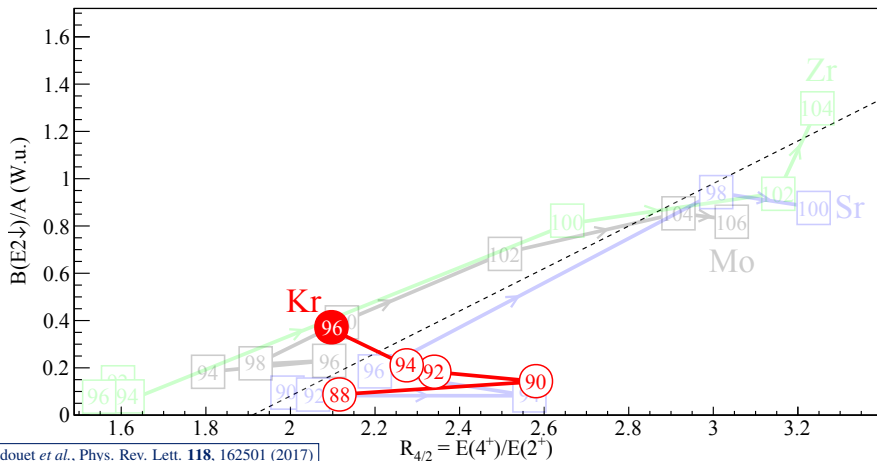


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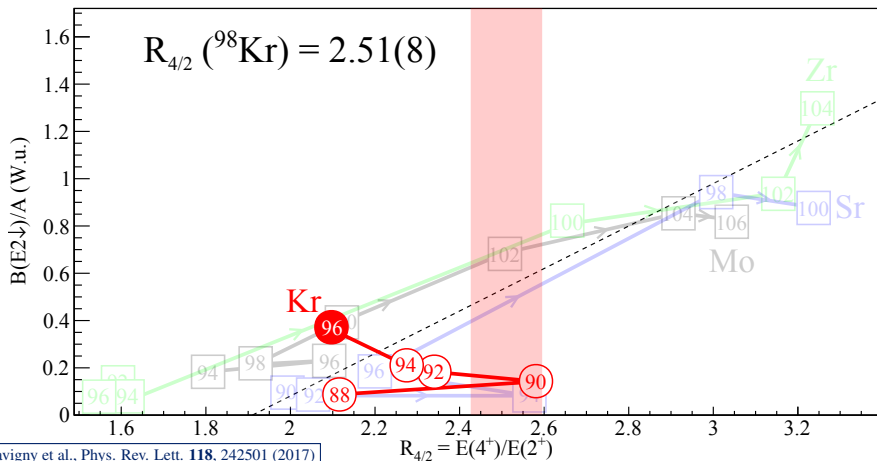
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# The strange behaviour of Kr nuclei

New measurements on very neutron rich  $^{98-100}\text{Kr}$

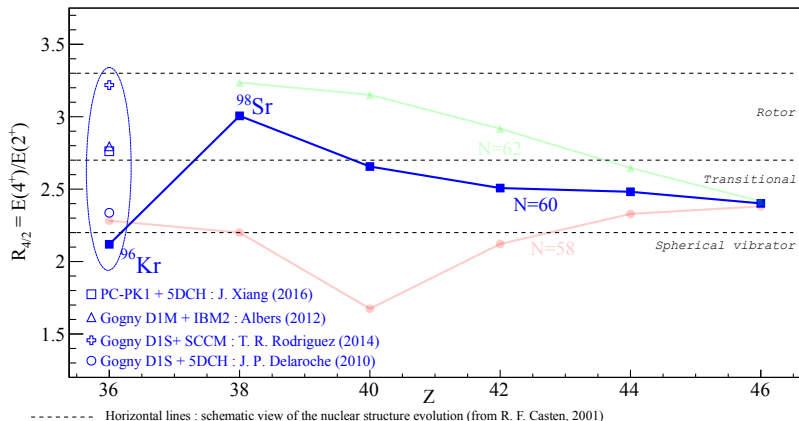
- ⇒ Recent results on  $^{98-100}\text{Kr}$  suggest a delayed onset of deformation at N=62
- ↔  $B(E2 : 2^+ \rightarrow 0^+)$  not measured





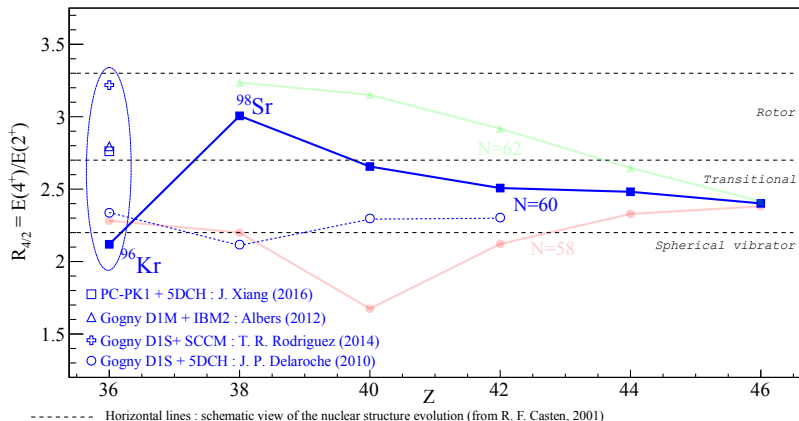
# Comparisons to theoretical calculations

- To understand these phenomena, theoretical calculations needs to reproduce:
  - ⇒ The sharp transition at N=60 for Z>36,
  - ⇒ the absence of transition at Z=36,
  - ⇒ the decreasing trend of the  $R_{4/2}$  ratio.



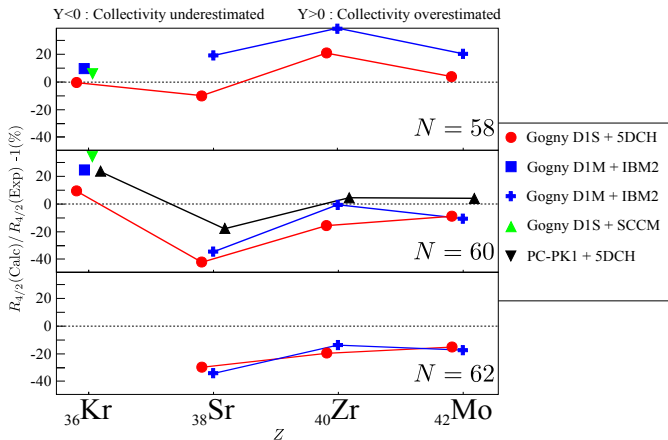
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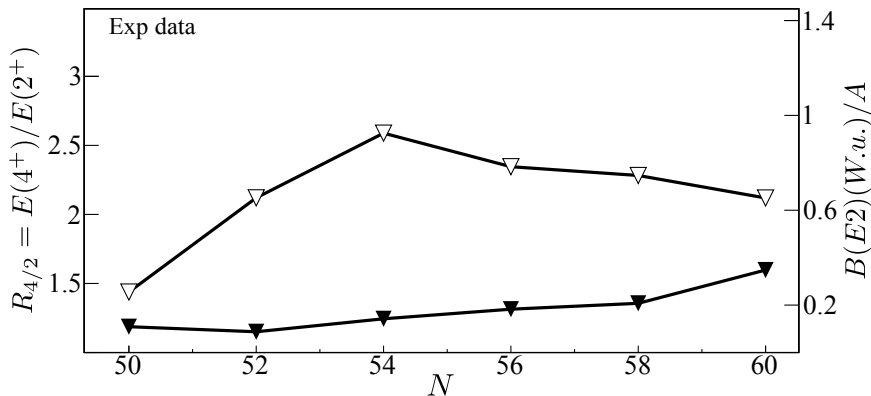


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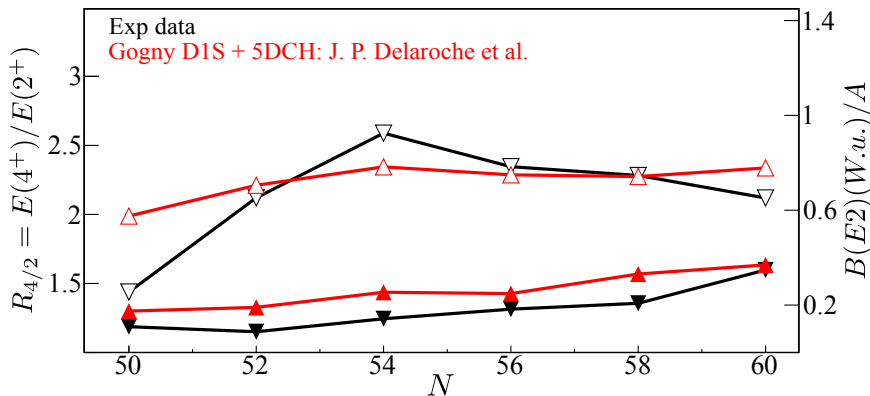


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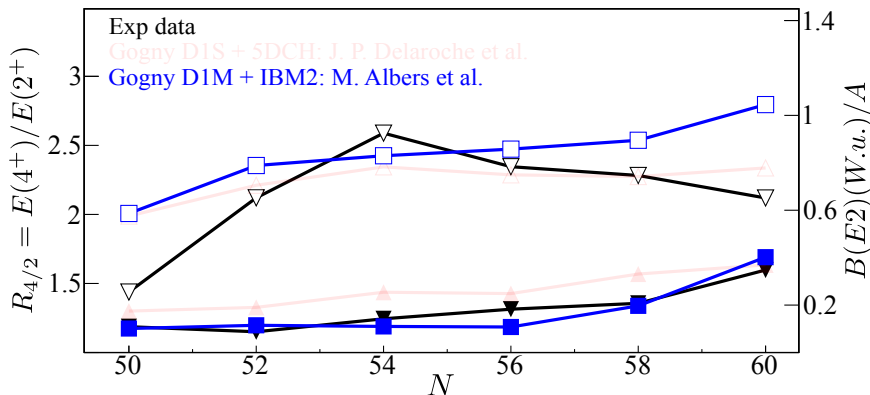


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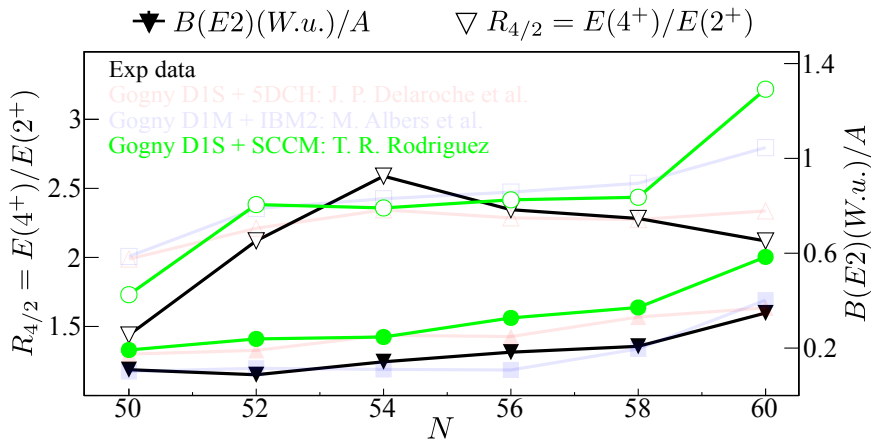
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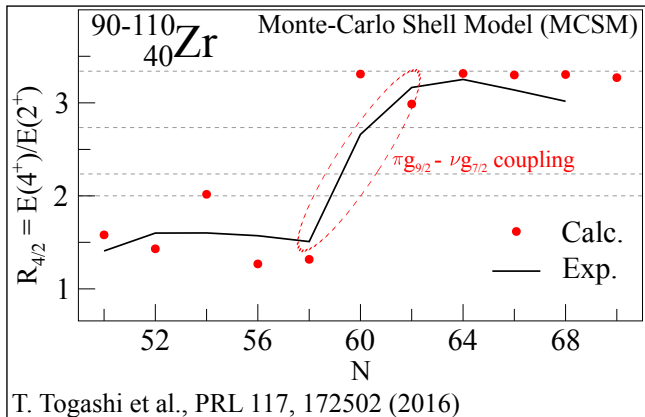
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## Comparisons to theoretical calculations

- Predictions from mean field calculations not able for the moment to reproduce this transition
- New Monte Carlo Shell-Model calculations performed along the Zr isotopic chain reproduce for the first time the N=60 transition along the Zr isotopic chain
- Could such a model help to understand this strange behavior in the Kr chain ?





# Conclusions

## Experimental results

- The powerful coupling between AGATA and VAMOS allowed to add new spectroscopic information to the Kr isotopic chain.
- $4_1^+$  level established for the first time in  $^{96}\text{Kr}$ .
  - ⇒  $R_{4/2}$  value confirms the non observation of sharp transition at N=60 in Kr
  - ⇒ contradicting trend between  $R_{4/2}$  and  $B(E2; 2^+ \rightarrow 0^+)$  evidenced

## Interpretation

- Mean-field approaches fail to reproduce the observed phenomena.
  - ⇒ Opposite  $R_{4/2}$  and  $B(E2; 2^+ \rightarrow 0^+)$  evolution still puzzling. Could be related to a shape coexistence phenomenon affecting the  $R_{4/2}$  ratio.
- MCSM calculations give the first microscopical reproduction of the N=60 transition in Zr nuclei.
  - ⇒ Z>36: transitions generated by a strong  $\pi g_{9/2} - \nu g_{7/2}$  coupling.



Thank you for your attention!

And thank you to all the person involved in this experiment:

A. Lemasson, G. Maquart, G. Duchêne, M. Rejmund, E. Clément, F. Didierjean, C. Lizarazo, C. Michelagnoli, F. Nowacki, R. Perez, K. Sieja, O. Stezowski, C. Andreoiu, G. de Angelis, A. Astier, C. Delafosse, I. Deloncle, Z. Dombradi, G. de France, A. Gadea, A. Gottardo, B. Jacquot, P. Jones, T. Konstantinopoulos, A. Korichi, I. Kuti, F. Le Blanc, S.M. Lenzi, G. Li, R. Lozeva, B. Million, D.R. Napoli, A. Navin, C.M. Petrache, N. Pietralla, D. Ralet, M. Ramdhane, C. Schmitt, D. Sohler, D. Verney.