A large, detailed wireframe model of a particle accelerator is the central background image. It shows a large, roughly circular main ring with several smaller, more complex structures branching off from it, representing different stages or components of the facility. The model is rendered in a light gray wireframe style, showing the internal structure and curvature of the rings.

Injection schemes for intense beams

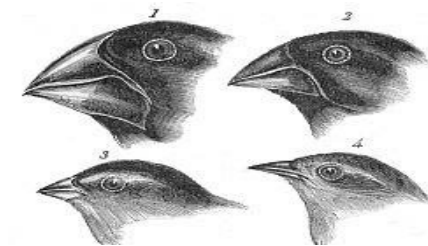
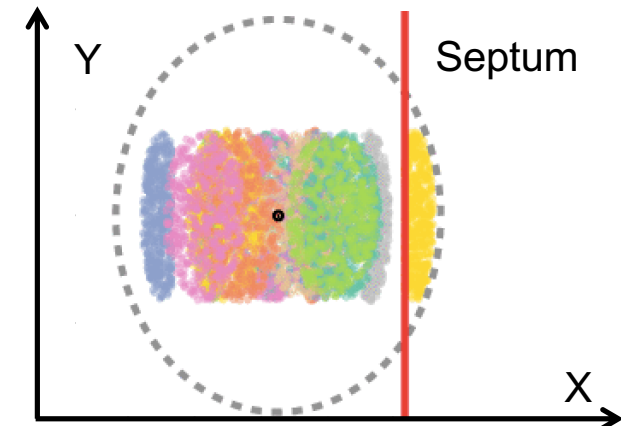
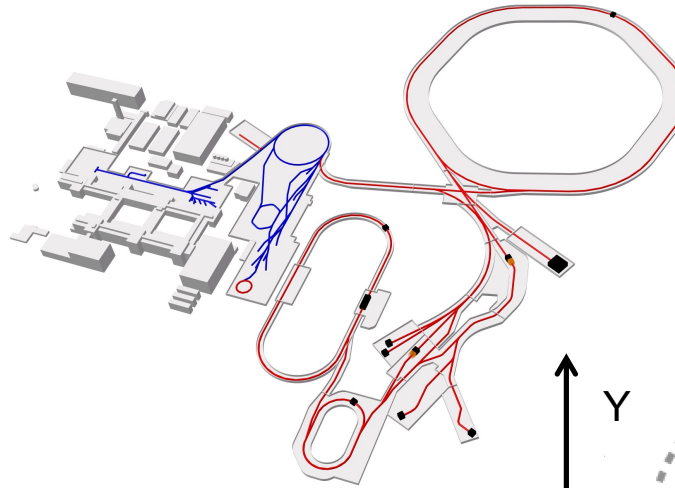
Dr. Sabrina Appel, Accelerator Physics Department, GSI, Darmstadt

- **Multi-Turn Injection**

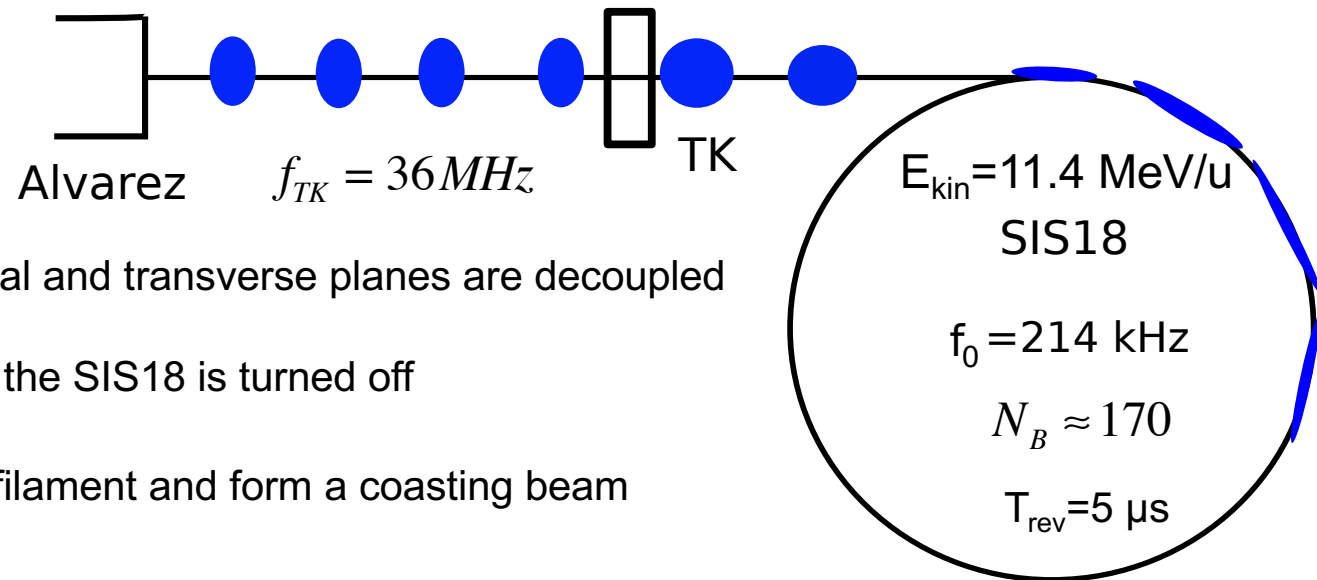
- SIS18
- Intensity limitation

- **Optimization**

- Algorithms
 - Genetic Algorithms
 - Particle swarm algorithms
- Technical solution
 - EMTEX
 - Skew quadrupoles



Overview injection into SIS18



We assume that the longitudinal and transverse planes are decoupled

During MTI injection the RF in the SIS18 is turned off

The micro-bunches debunch, filament and form a coasting beam within a few turns

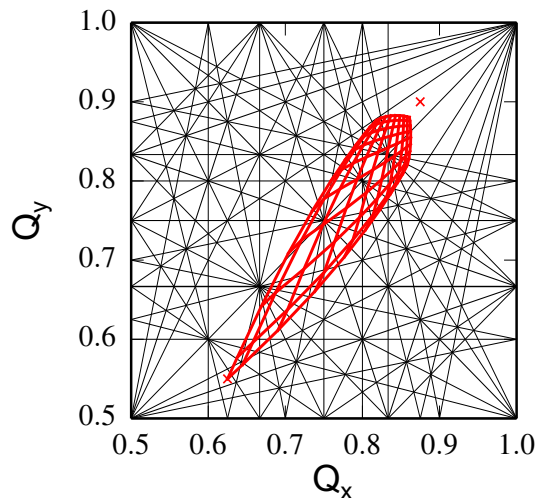
Final full momentum spread after injection should be within the rf bucket area

$$\Delta p / p \leq 10^{-3} \quad (\text{equivalent parabolic distribution})$$

Transverse beam size (4 rms physical emittance) should be within the machine acceptance

$$\epsilon_x = 150 \text{ mm mrad} \quad \epsilon_y = 50 \text{ mm mrad} \quad (\text{equivalent K-V distribution})$$

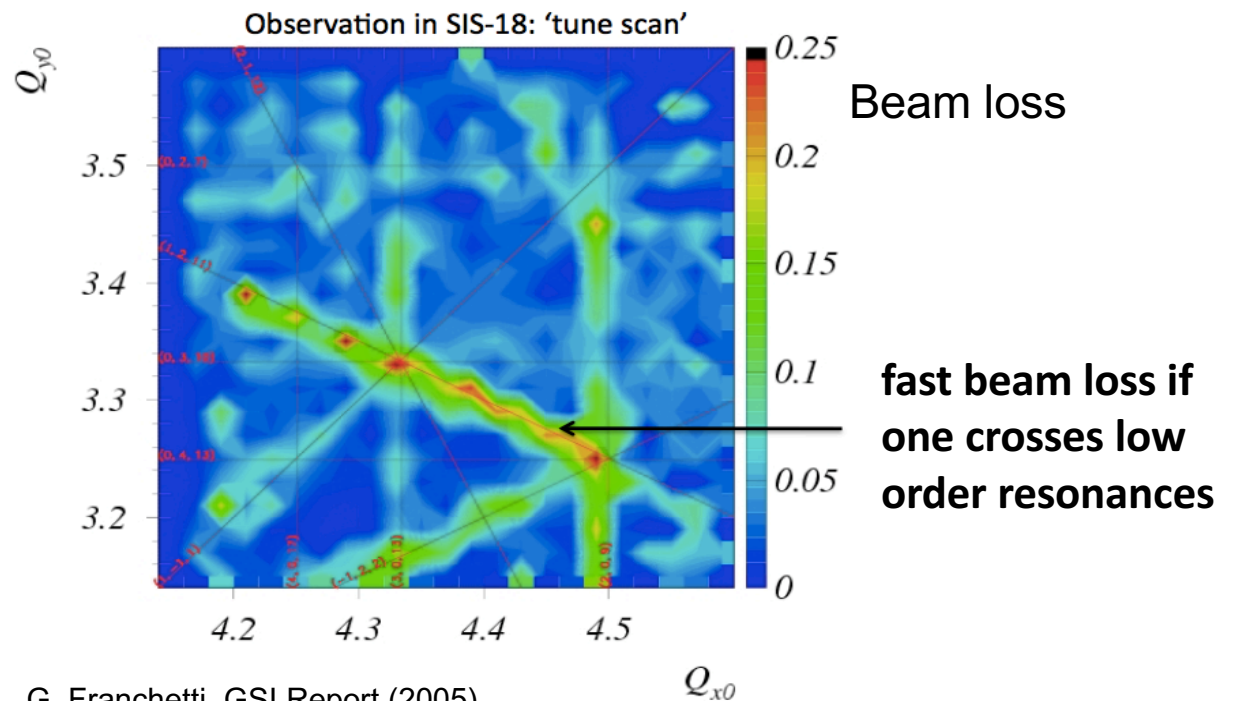
Intensity limit: Space charge



The (incoherent) transverse space charge force is the main intensity limiting effect in the FAIR synchrotrons

Tune shift:
$$\Delta Q_y^{sc} \propto -\frac{q^2}{m} \frac{N}{B_f} \frac{4}{\epsilon \beta_0^2 \gamma_0^3}$$

Intensity limit:
$$|\Delta Q^{sc}| \lesssim 0.1 - 0.5$$



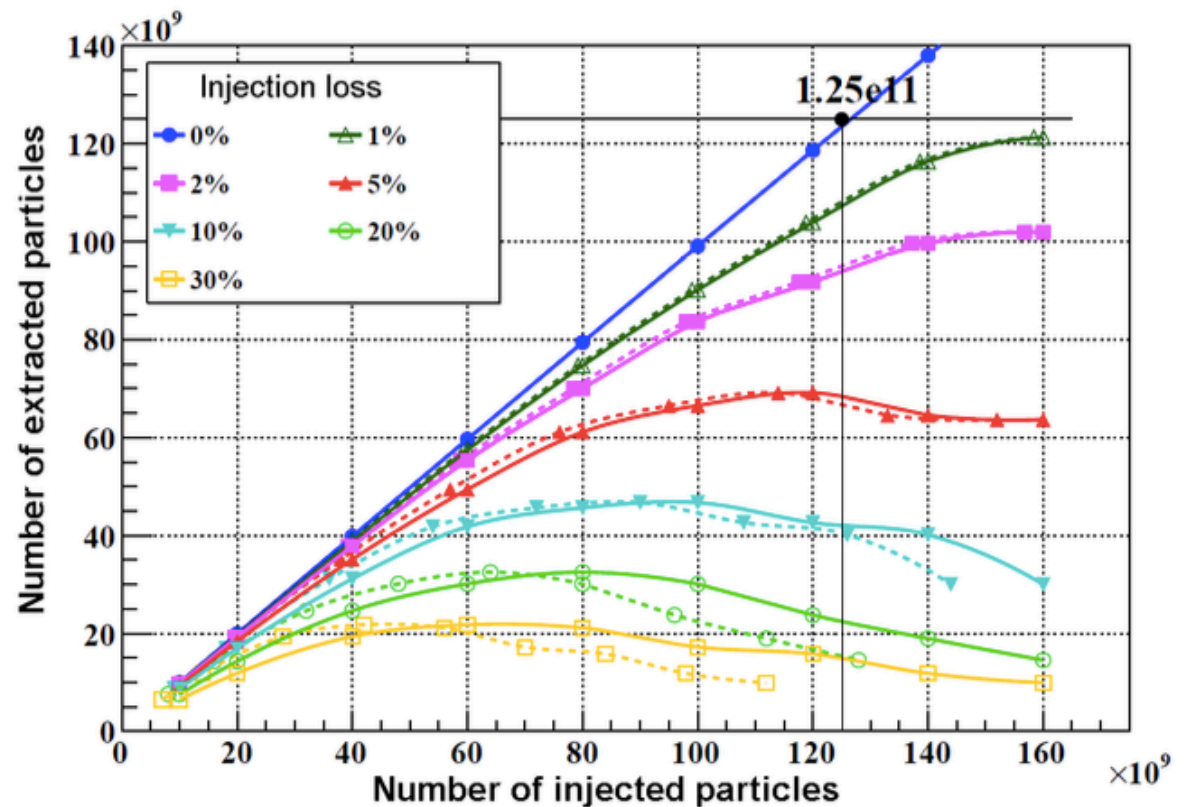
G. Franchetti, GSI Report (2005)

Intensity limit: Dynamic vacuum

For intermediate charge state ions, the loss-induced vacuum degradation is another important key intensity-limiting factor.

Results of STRAHLSIM simulations for the desired SIS18 booster operation with different (uncontrolled) initial beam loss.

P. Spiller {SIS18} upgrade: Status, Present and Expected Performance Low Charge State Heavy Ion Beams. MAC, (2013)

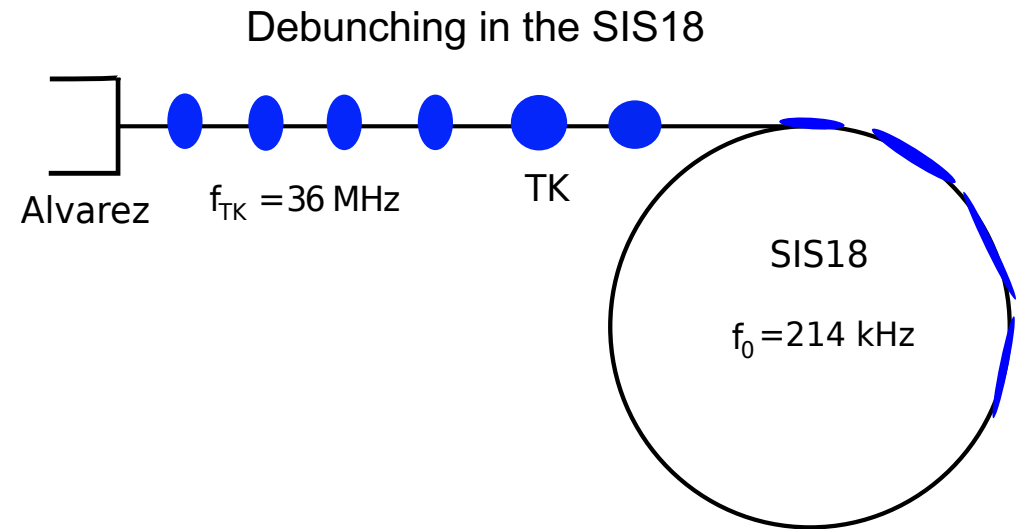
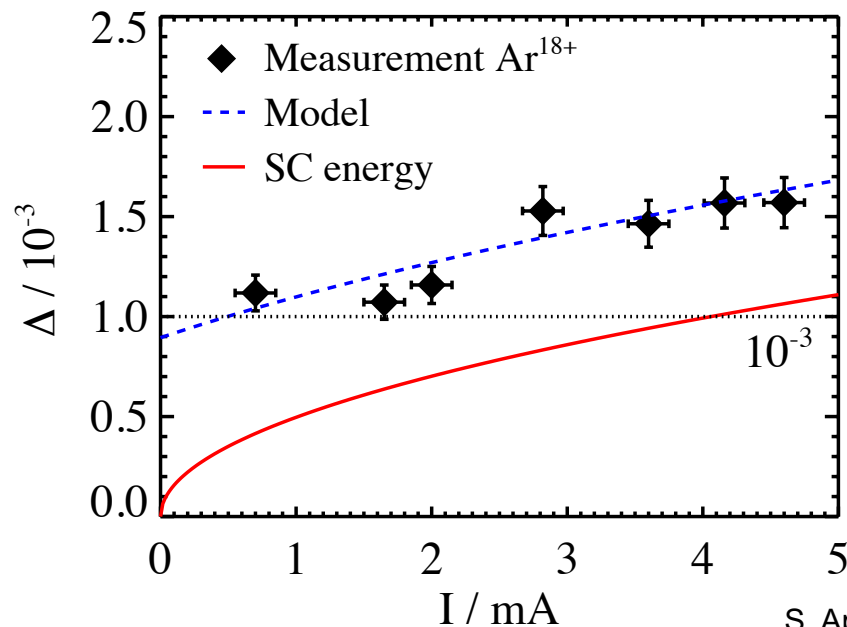


Momentum spread of SIS18 coasting beam

- SC and UNILAC momentum spread are the main sources of the SIS18 momentum spread

$$\Delta_f = \sqrt{\Delta_i^2 + \frac{2K_L}{\eta^2 z_{m,i}}}$$

Minimum momentum spread given by SC

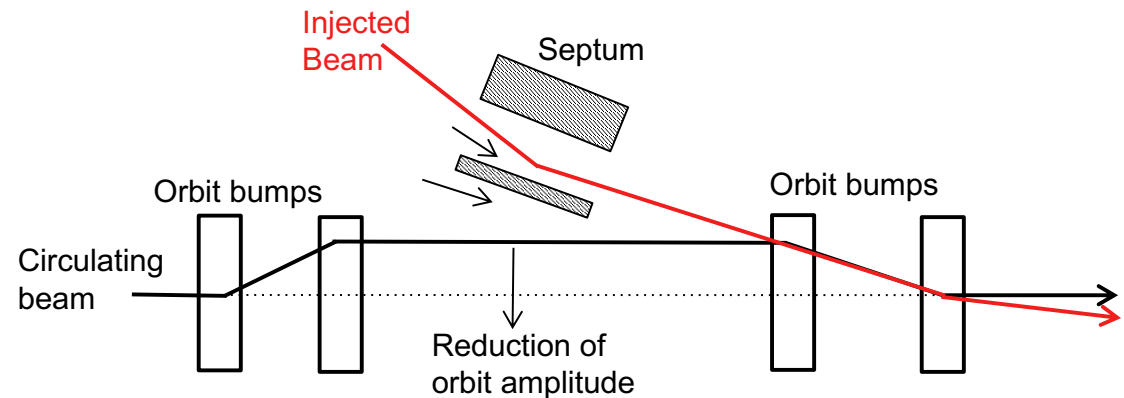
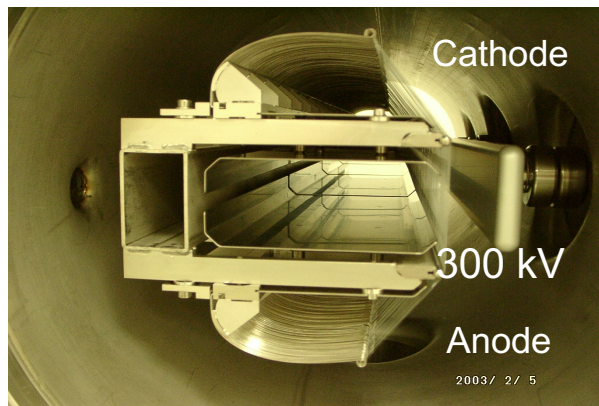


- SC energy of the micro-bunches is transformed into incoherent thermal momentum spread
- Since the SC effect depends on bunch length, the micro-bunches are stretched in TK
 - Further optimization might be possible

S. Appel, O. Boine-Frankenheim, Phys. Rev. ST Accel. Beams 15, 054201 (2012)

Multi-turn injection (MTI) into SIS18

SIS18 electrostatic injection septum

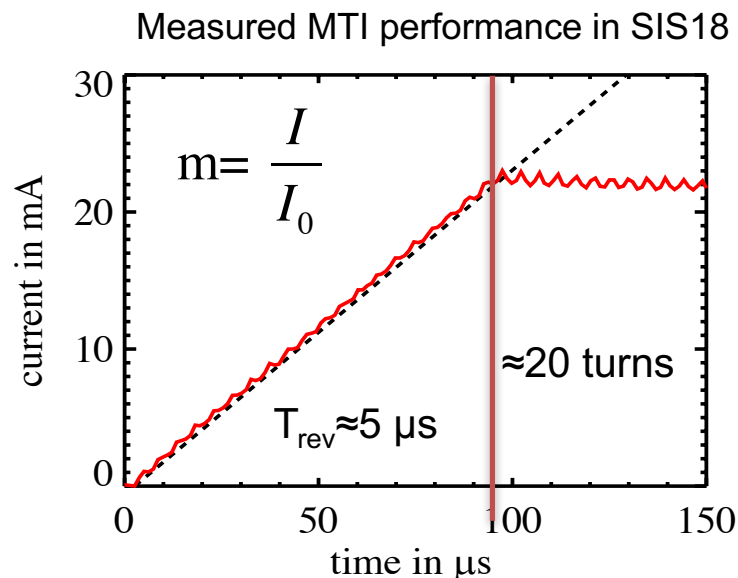


SIS18 **flexibility** in providing a broad range of ions allow only **Liouvillian injection** schemes

MTI has to respect Liouville's theorem:
Injected beams only in free space

The beam from linac is injected until machine acceptance is reached and maximize intensity

Loss at septum and acceptance should be as **low** as possible due to loss induced dynamic vacuum

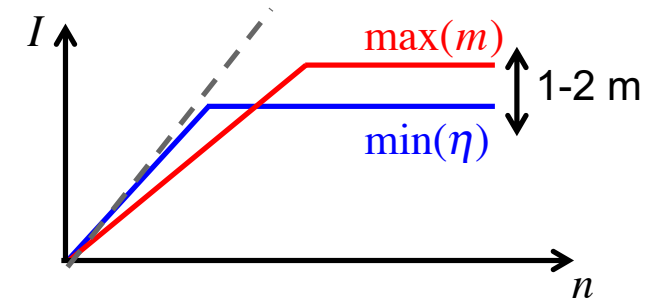


Multi-objectives:

- stacked current (maximize) $I = mI_0$
- beam loss (minimize) $\eta = \frac{I_{loss}}{nI_0}$
- emittance ϵ_x

output

$$m = (1 - \eta)n$$



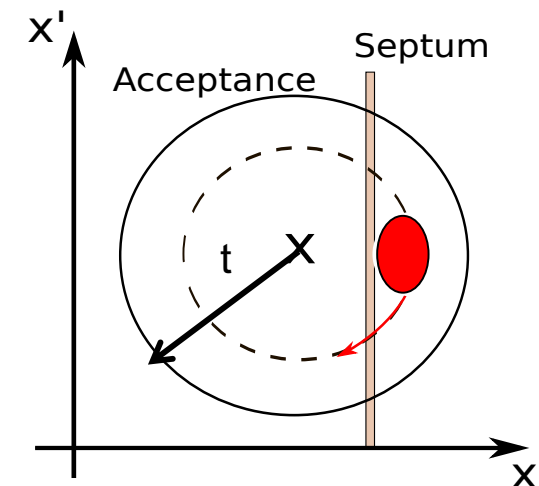
Constraints:

- Position of septum x_s
- Machine acceptance A
- Closed orbit (bumper kick) $\phi_i(Q_x)$

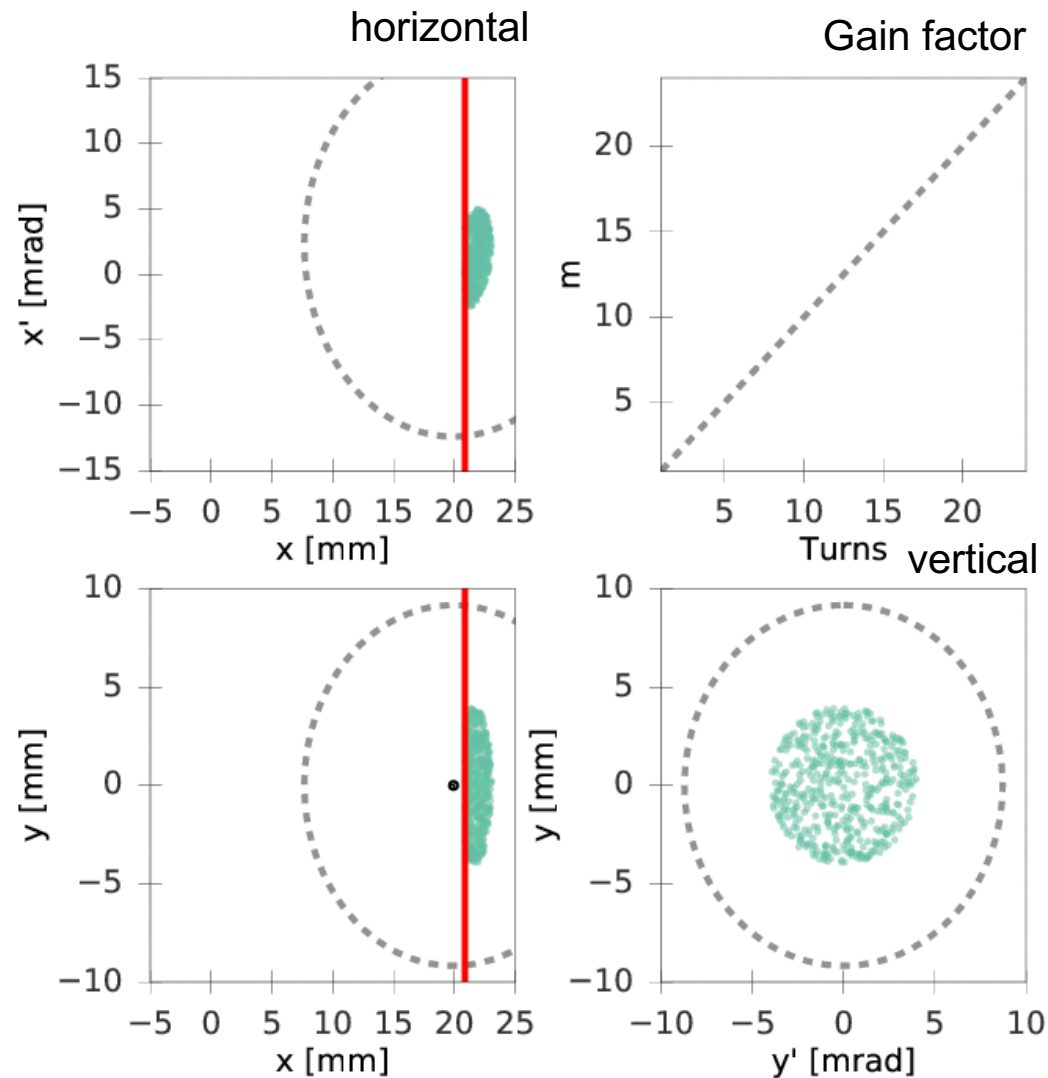
Model in
simulation code

Parameters:

- Position of incoming beam at septum x_c, x'_c, M
- Initial bump amplitude and its decreasing x_0, x'_0, τ
- Injected turns n
- Horizontal tune Q_x
- Horizontal emittance ϵ_x
- Coupling strengths k



Multi-turn injection into SIS: Movie



Multi-turn injection into SIS: Optimization problem

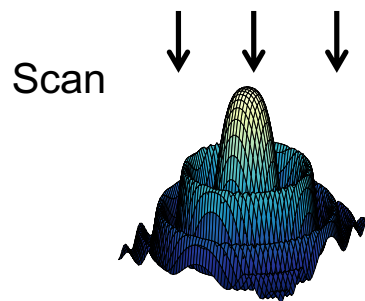
The analytical description characterizes:
Incoming beam position and this mismatch

Loss minimization at septum: tune
Linear orbit bump reduction: tune + size

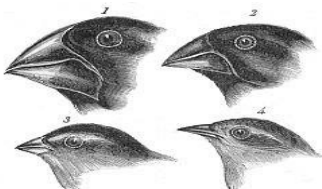


Unfortunately the MTI model is underrepresented:
A few variables can be chosen freely from a value range

Discover by trial and error optimum
settings or perform parameter scans

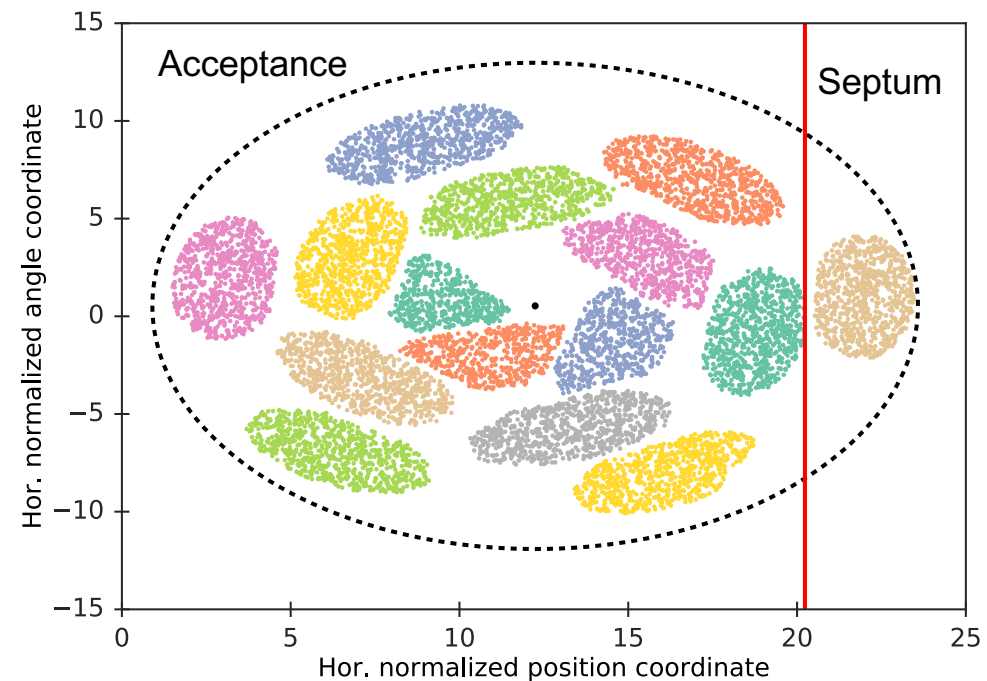


New approach is the use of genetic
algorithms (GA) and particle swarm (PA)



Darwin Finches
J. Gould,
Voyage of the
Beagle

GA optimized MTI

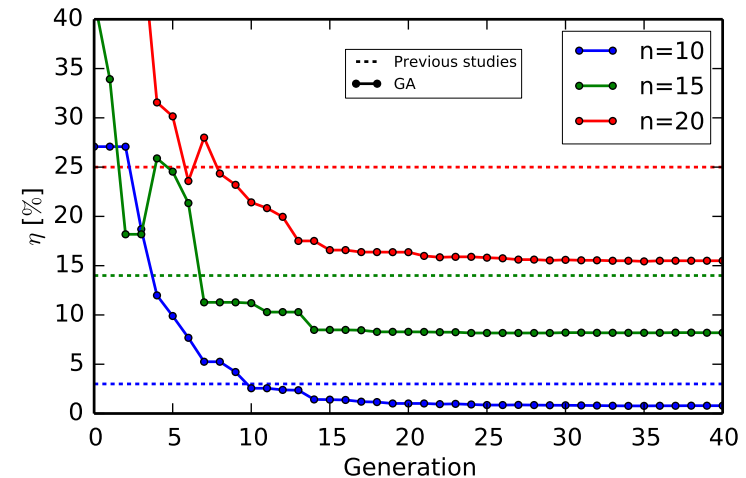


Multi-turn injection into SIS18

Optimization of loss

Genetic algorithms can improve MTI

Especially for **longer** injection GA discovers a much **better** solution

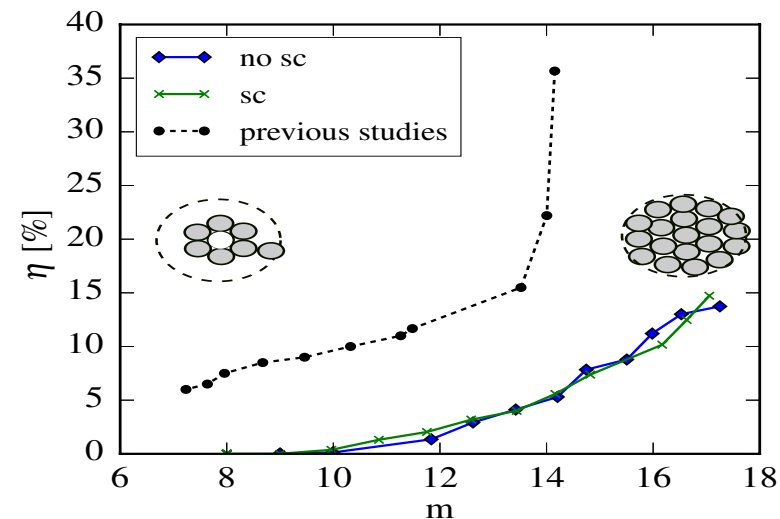


Optimization of loss and gain factor

Dependence of gain factor on loss

Loss-free injection could be found

Space charge results in a **similar PA front**, but with different injection settings

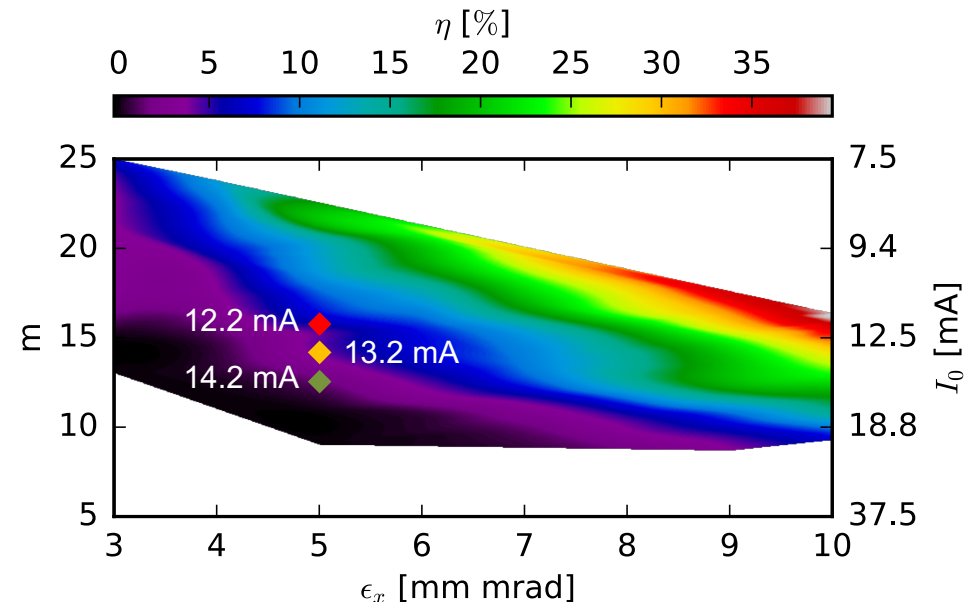


Optimization of loss, gain factor and beam emittance (injector)

Dependence of interface parameter

$$B = \frac{I}{\varepsilon} \quad m(\eta) = \frac{N}{I} q f_0$$

allows to define a frame, in which the required beam parameter can be
matched at best for a high performance



This crucial information gives more flexibility for the injector upgrade layout.

New Alvarez DTL provide requirement beam brilliance (including errors)

S. Appel et al: Nucl. Instrum. Methods A 852 (2017), pp. 73-79

A. Rubin, Beam dynamics design of the new FAIR post-stripper linac,
GSI Accelerator Seminar, 14.05.17

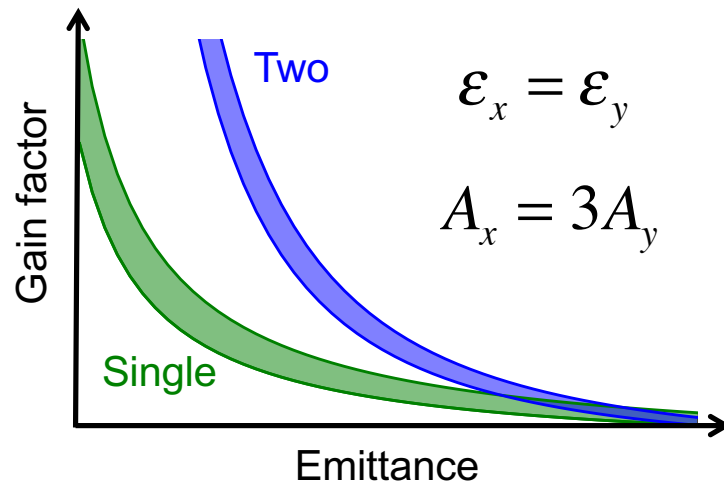
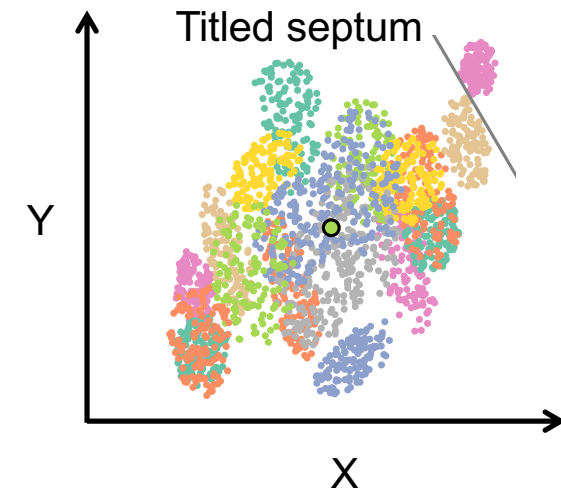
Multi-turn injection

Smaller beam emittance increase MTI performance

Available acceptance limited MTI performance

Besides the horizontal phase space, the vertical one can also be exploited, which can lead to higher gain factors

➤ Titled septum or skew quadrupoles



Single plane: $m = \frac{A}{d\epsilon} \quad d \approx 1.5 - 2$

Two plane: $m = \frac{A_x A_y}{d\epsilon_x \epsilon_y} \quad d \approx 8 - 10$

G.H. Rees in Handbook of accelerator physics and engineering

Multi-turn injection (Two plane)

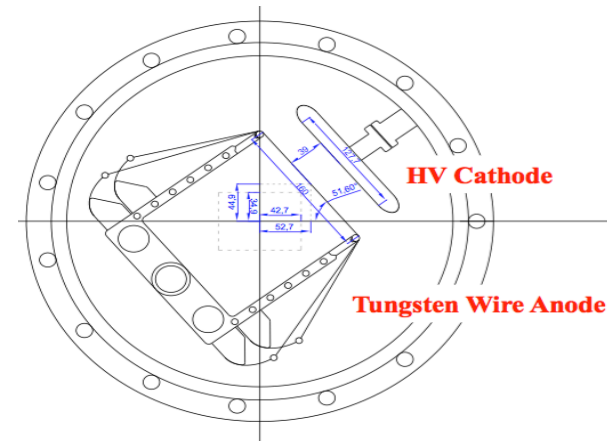
Titled septum

Need **new technical development**

Titled septum and magnets in transfer line

Coordinate rotation system

Four additional bumpers (vertical)



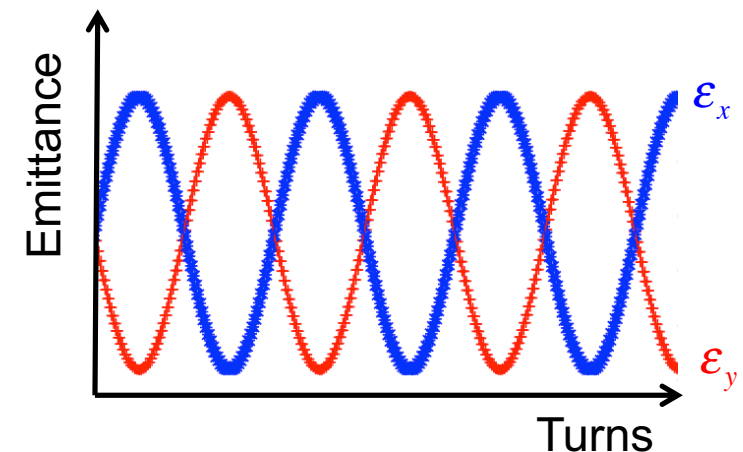
BRing of
HIARF
project

Skew quadrupoles

Using **installed** skew quadrupoles

Linear coupling of hor. and ver. phase space

Skew strength should be swift off after injection

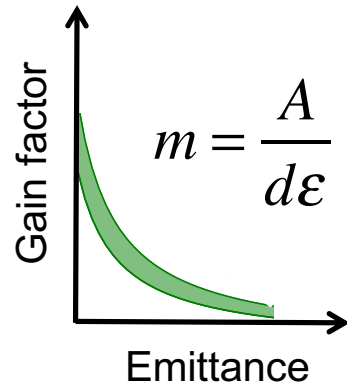


Which gain factors can be reached for a given beam emittance and loss for SIS18?

For conventional, skew and titled septum injection?

Injector brilliance depending

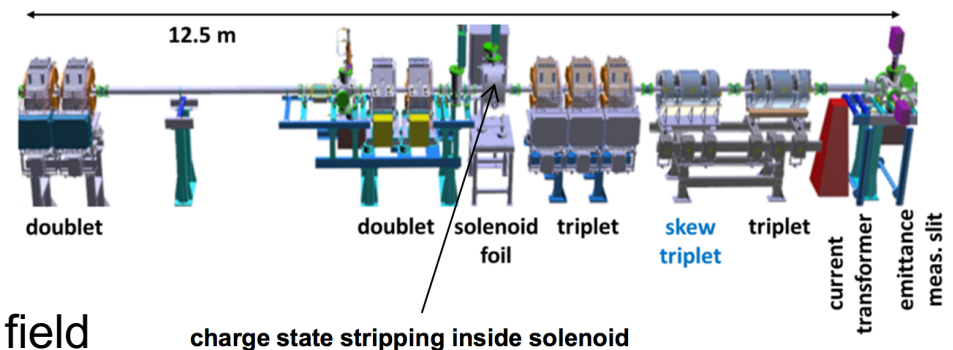
EMittance Transfer EXperiment (EMTEX)



One consequence of single-plane MTI is that the **required** horizontal injection **emittance** is very **demanding**; to the **other plane not**.

Re-partitioning of the injected beam emittances: round-to-flat transformation would **increase** the injection efficiency

EMTEX Beam line



Repartition with constant emittance product:
Effective solenoid exit fringe field + skewed quadrupole triplet

Twiss-parameters are preserved

Beam flatness amount is controlled by solenoid field

The effective solenoid exit fringe field is created by changing the ion charge state

L. Groening: Phys. Rev. ST Accel. Beams 14 064201 (2011)

C. Xiao et al: Phys. Rev. ST Accel. Beams 16 044201 (2013)

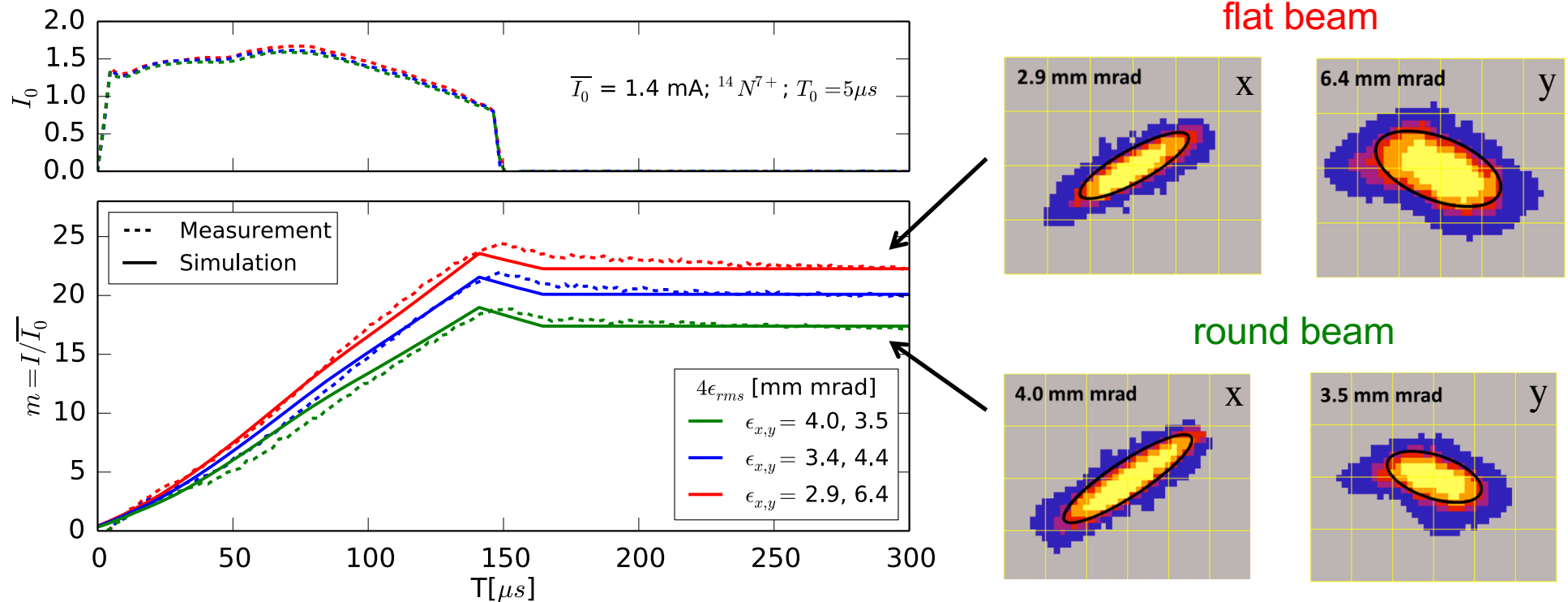
L. Groening et al: Phys. Rev. Lett. 113 264802 (2014)

S. Appel et al: Nucl. Instrum. Methods A 866 (2017), pp. 36-39

Injector brilliance depending

EMittance Transfer EXperiment (EMTEX)

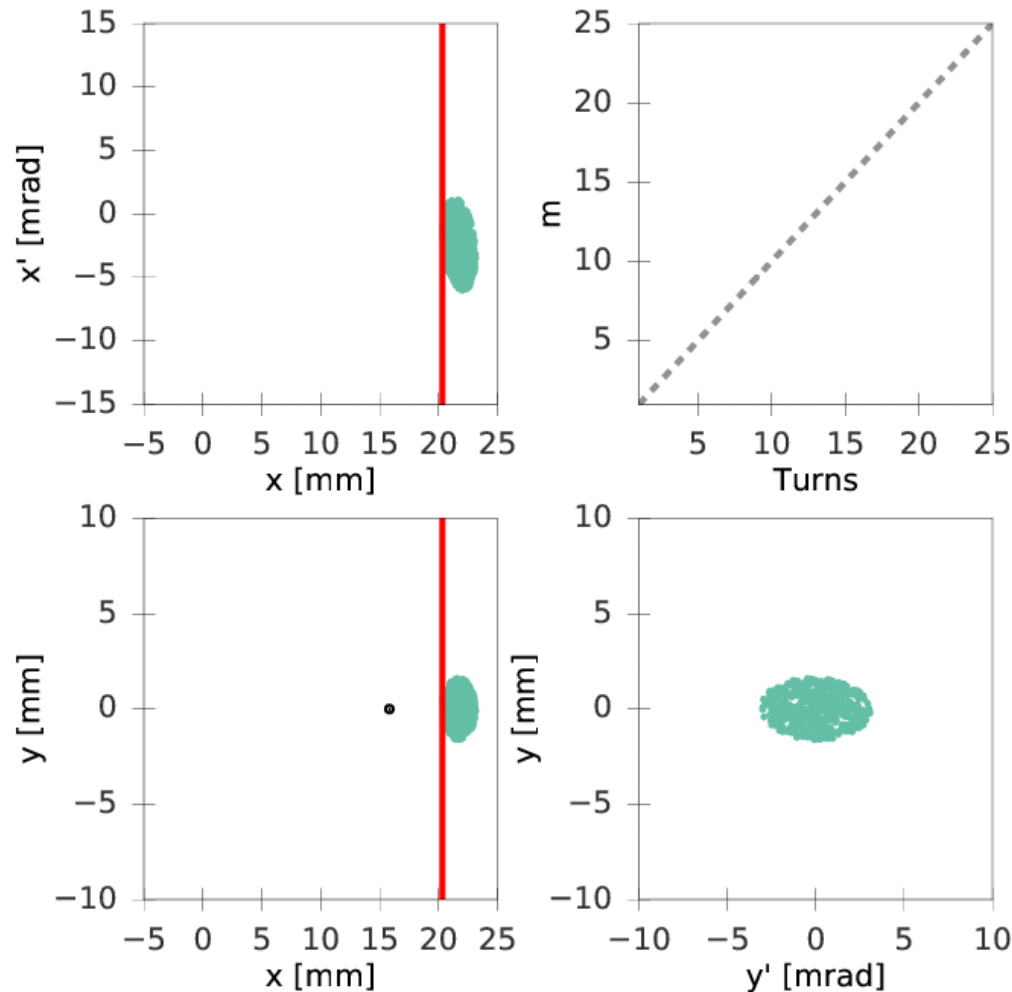
MTI performance has been measured as a function of the amount of beam flatness



Excellent agreement between simulation and measured injection performance was achieved thanks to fast adjustment of the beam flatness without changing other beam parameters.

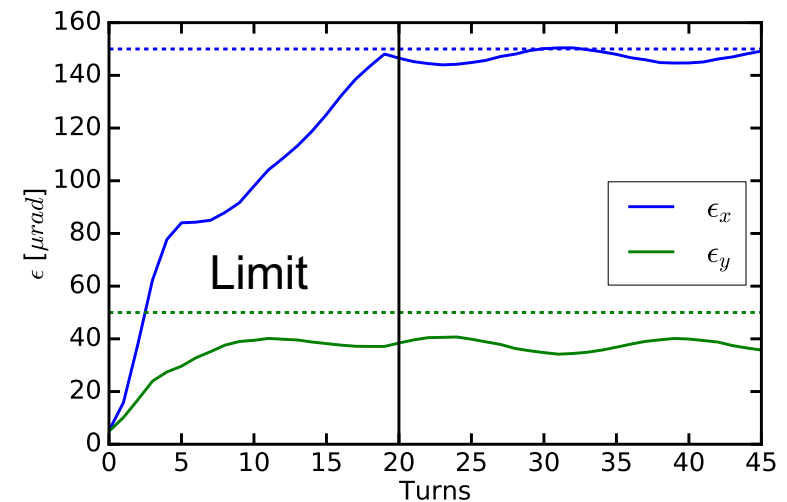
Multi-turn injection with skew quadrupoles

With linear coupling the injection loss could reduce from 15% to 1-5% for $n = 20$



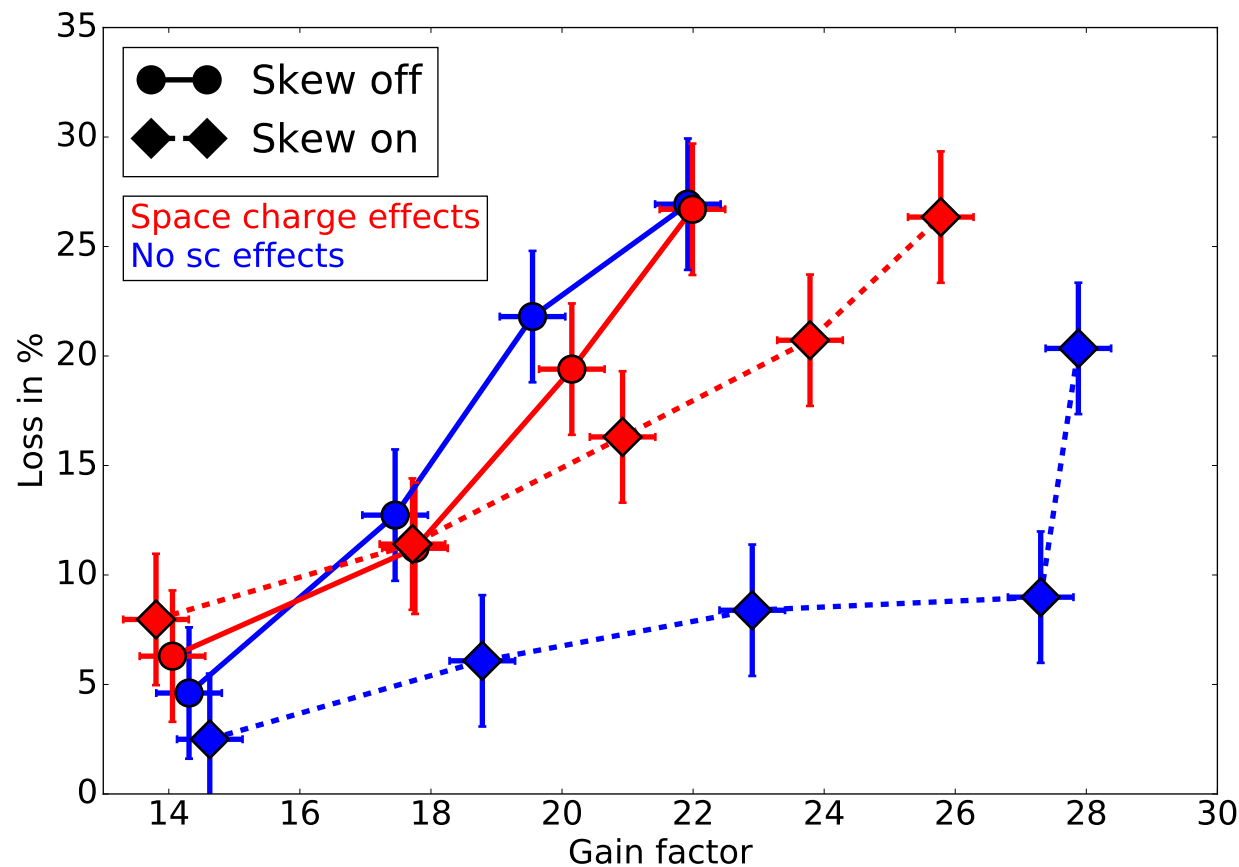
Coupling parameters: $Q_x : 4.17, Q_y : 3.22,$
 $k : 0.0141 / m, \delta : -0.05$

Emittance development



Multi-turn injection with skew quadrupoles

The injection performance can **increase** with linear coupling
Unfortunately, space charge effects **lower** the beneficial effect



Evolutionary Optimization

- ✓ MTI setting for a loss-free or low-loss injection were identified
- ✓ Range of optimum brilliances for all ions species can be defined (shown for U^{28+})
- Online optimization of MTI (GA, PSA or derivative-free algorithm)

EMTEX

- ✓ Injection optimization through generation of flat ion beams
- Application for intense beams (e.g. U^{28+})

Two plane MTI

- Skew
 - ✓ The injection performance can increase with linear coupling
 - Unfortunately, space charge effects lower the beneficial effect
- Corner septum

Thank you for your attention

MTI has to respect Liouville's theorem:
Injected beams only in free space

Loss of ions at the septum due to the betatron oscillation

Loss minimization at septum

$$Q_x \neq \text{integer}$$

Injected beam into upright ellipses

$$\frac{\alpha_0}{\beta_0} = -x'/x$$

Mismatch of lattice function to
adapt to ring curvature

$$\frac{\beta_0}{\beta_i} = \left(\frac{\epsilon}{\epsilon_i}\right)^{\frac{1}{3}}$$

Linear orbit bump reduction

$$\Delta x = \frac{1}{4}(2a + d_c)$$

Imagined best optimum injection
scheme has the smallest dilation and
the lowest loss at the septum.

→ Contradicting

Betatron oscillation and
orbit bump reduction
→ free phase space

