

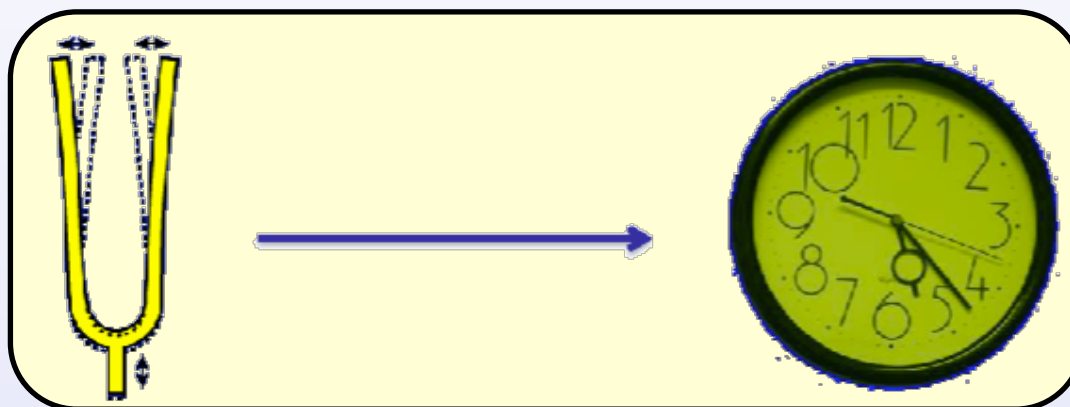
Direct Detection of the Elusive ^{229}Th Isomer: Milestone towards a Nuclear Clock

P.G. Thirolf, LMU München

- Clock basics
- $^{229\text{m}}\text{Th}$ properties and prospects
- Experimental approach & setup
- Isomer decay study results
- Verification studies
- Summary & Perspectives



Functional Principle of Clocks



**periodic event
(oscillation)**

counting device

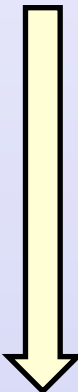
examples:

- rotation of earth, moon phases
- pendulum, spring
- quartz crystal
- atomic transitions
- **nuclear transitions ?**

examples:

- sun dial
- mechanical clocks
- 'digital' clocks
- microwave, laser

rising frequency





Mechanical clocks



accuracy: 1s / day
world record (NIST): 1s / year

Quartz clocks



accuracy: 1s / month
world record: 10^{-12}

Atomic clocks



accuracy: 10^{-14}
world record: 10^{-18}



nuclear clocks ??



$^{229\text{m}}\text{Th}$

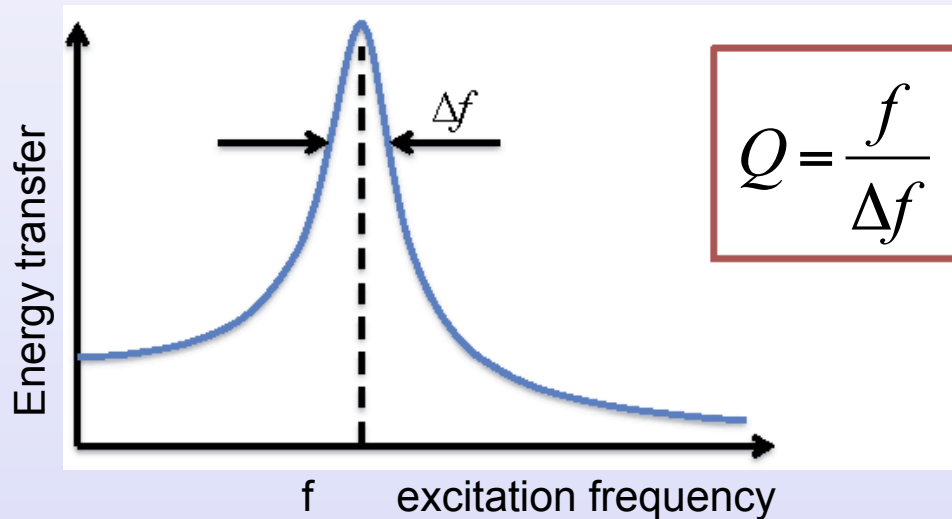




- continuous operation:

- feedback on resonance
- optimum energy transfer at specific excitation frequency f

- Quality factor Q :



best clock:

- highest oscillation frequency (f large)
- as precise as possible (Δf small)

microwave atomic clocks: $Q \sim 10^{10}$

'optical' atomic clocks: $Q \sim 10^{14}$

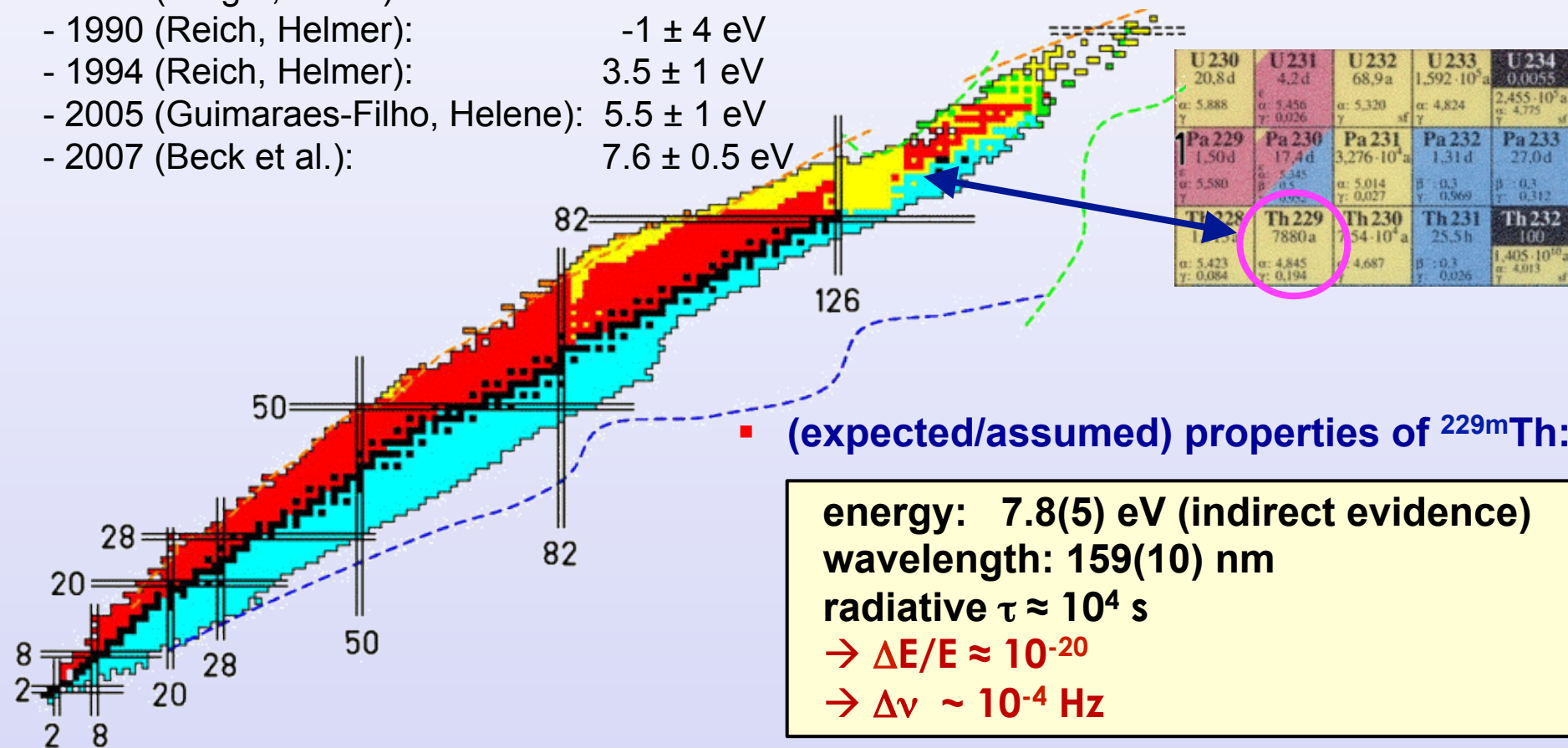
nuclear clock: $Q > 10^{15} ??$

What makes ^{229m}Th so unique ?

- since 40 years nuclear physicists seemed to chase a phantom:

presumed low-lying isomer in ^{229}Th :

- 1976 (Kroger, Reich): $< 100 \text{ eV}$
- 1990 (Reich, Helmer): $-1 \pm 4 \text{ eV}$
- 1994 (Reich, Helmer): $3.5 \pm 1 \text{ eV}$
- 2005 (Guimaraes-Filho, Helene): $5.5 \pm 1 \text{ eV}$
- 2007 (Beck et al.): $7.6 \pm 0.5 \text{ eV}$

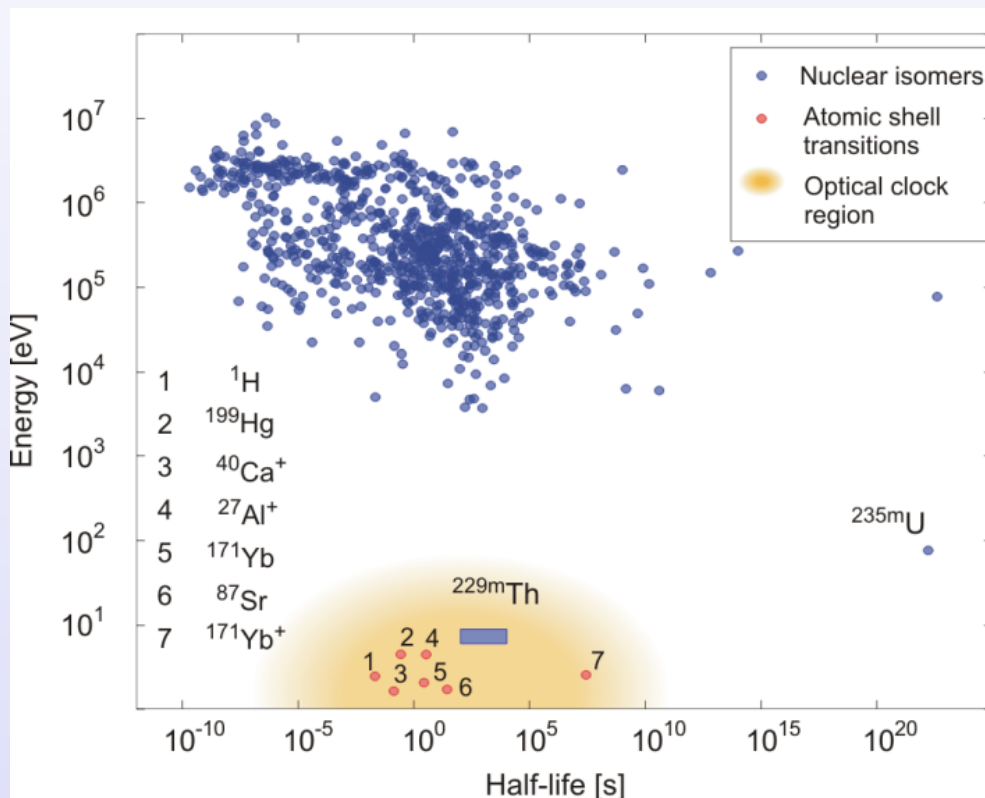


B.R. Beck et al., LLNL-PROC-415170 (2009)

^{229m}Th : Nuclear Clock ?



→ lowest excitation energy of all ca. 176000 presently known excited nuclear states



- insensitivity of ^{229m}Th nuclear transition frequency to external perturbations
 - small nuclear moments
 - largely immune to systematic frequency shifts:
 - ultra-precise nuclear frequency standard ?

$^{229\text{m}}\text{Th}$ and time dependence of fundamental constants



Theories unifying gravity with other interactions suggest temporal and spatial variations of the fundamental “constants” in an expanding universe

Uzan, Rev. Mod. Phys. 75, 403 (2003)

- near degeneracy of $^{229,229\text{m}}\text{Th}$ results from cancellation between large contributions from Coulomb energy ($\sim 10^9$ eV)
- dependencies on fundamental constants
→ any variation would be enhanced in the transition frequency

temporal variation in transition energy may provide enhanced sensitivity by $(10^2 - 10^5)$ for fine structure constant $\dot{\alpha}/\alpha$ and strong interaction parameter $(m_q/\Lambda_{\text{QCD}})$

- | | |
|--|--|
| - Flambaum, PRL 97 (2006) | - Hayes, Friar, PL B 650 (2007) |
| - He, Ren, NP A 806 (2008) | - Berengut, Flambaum et al., PRL 102 (2009) |
| - Litvinova, Feldmeier et al., PRC 79 (2009) | - Flambaum et al., Europhys. Lett. 85 (2009) |
| - Flambaum, Wirlinga, PRC 79 (2009) | - Flambaum, Porsev, PRA 80 (2010) |
| - Rellergert et al, PRL 104 (2010) | |

- current (theor.) limit of potential time variation:

$$\frac{\dot{\alpha}}{\alpha} = (-1.6 \pm 2.3) \cdot 10^{-17} \text{ yr}^{-1}$$

Fujii et al., NP B573, 377 (2000)



- sensitivity of $^{229\text{m}}\text{Th}$ transition frequency ω to temporal variation of $\alpha = e^2/\hbar c$:

$$\delta\omega = \Delta V_C \frac{\delta\alpha}{\alpha}, \quad \frac{\delta\omega}{\omega} = K \frac{\delta\alpha}{\alpha}$$

ΔV_C : difference in Coulomb energy between ^{229}Th , $^{229\text{m}}\text{Th}$
(proton polarization by modified neutron distribution)

enhancement factor:

$$K = \frac{\Delta V_C}{\omega}$$

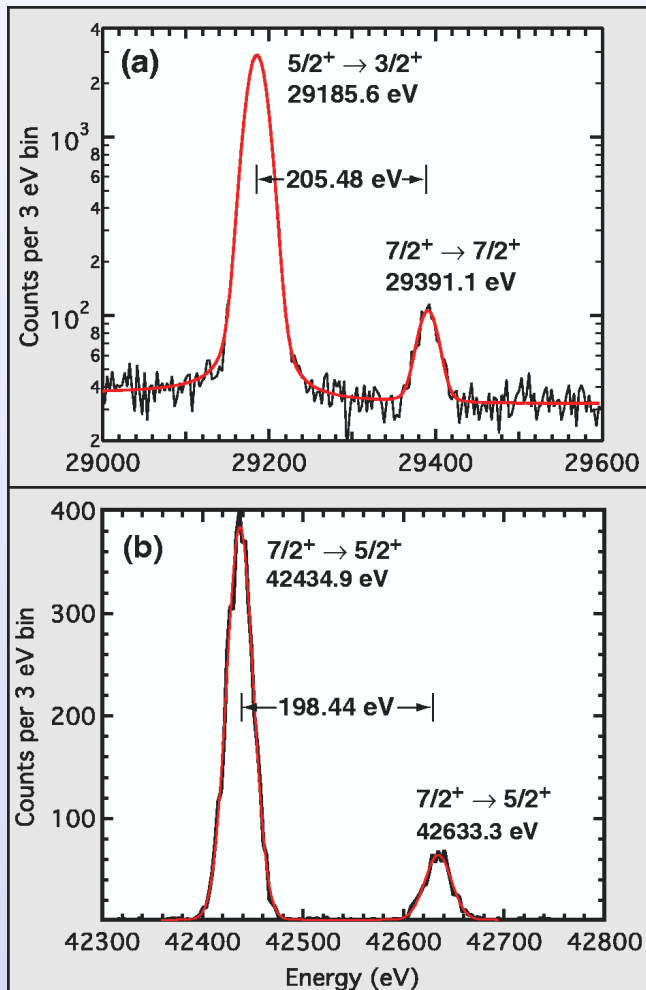
- example:** for $\Delta V_C = 100 \text{ keV}$, $\delta\alpha/\alpha = 10^{-16}$
 $\rightarrow \delta\omega = 10^{-11} \text{ eV} (= 2.4 \cdot 10^3 \text{ Hz})$
 $\rightarrow 10^4$ larger than limits on shifts in atomic transitions
- problem:** - Coulomb energy cannot be directly measured
 - V_C needs to be calculated in nuclear models
 - insufficient accuracy in present nuclear models
 (e.g. Hartree-Fock, Hartree-Fock-Bogoliubov:
 $-300 \text{ keV} < \Delta V_C (^{229}\text{Th}) < 400 \text{ keV} \rightarrow -4 \cdot 10^4 < K < +4 \cdot 10^4$)

system	K	λ [nm]
Sr	0.06	699
Yb ⁺ E2	0.91	436
Yb ⁺ E3	-6	467
Hg ⁺	-2.9	281.5
Al ⁺	0.01	267
Ir ¹⁷⁺ T1	-20.6	ca. 267
Ir ¹⁷⁺ T2	32.2	ca. 470
Cf ^{16+*} T1	75	ca. 520
Cf ^{16+*} T2	-46	ca. 653
Th [*] (nuclear)	8000	ca. 160

Schmidt & Crespo,
Phys. Jour. Oct. 2016

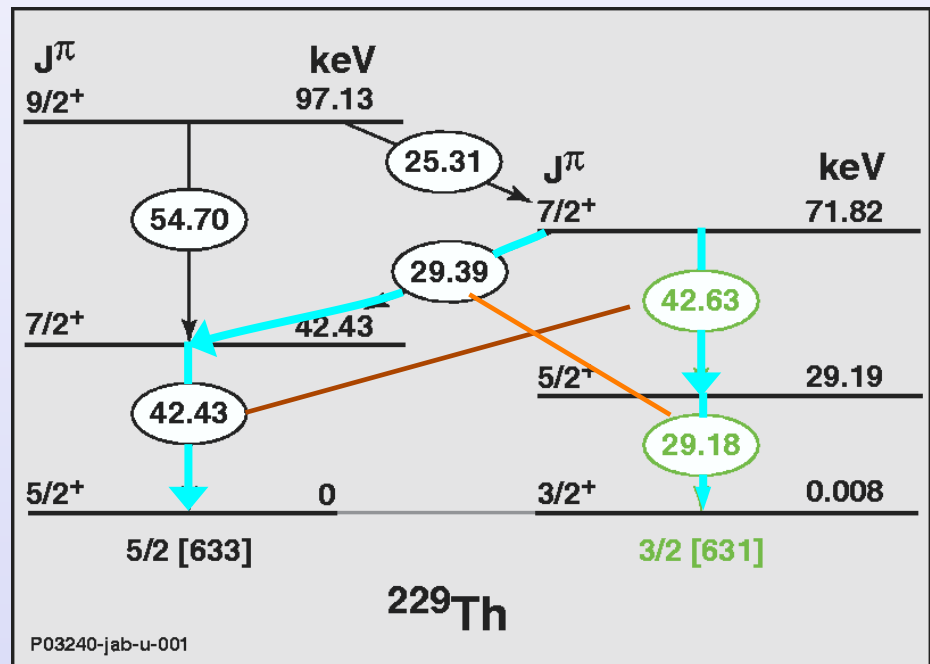
Indirect Evidence for ^{229m}Th

- data from X-ray micro-calorimeter



$$E^* (^{229m}\text{Th}) = \Delta E_{29} - \Delta E_{42}$$

$$E^* (^{229m}\text{Th}) = (7.8 \pm 0.5) \text{ eV}$$



B.R. Beck et al., PRL **98** (2007) 142501
LLNL-PROC-415170 (2009)

from energy difference of high-energy transitions $\rightarrow$ low isomer excitation energy

- concept:**
- populate the isomeric state via 2% decay branch in the α decay of ^{233}U
 - spatially decouple $^{229(\text{m})}\text{Th}$ recoils from the ^{233}U source
 - detect the subsequently occurring isomeric decay

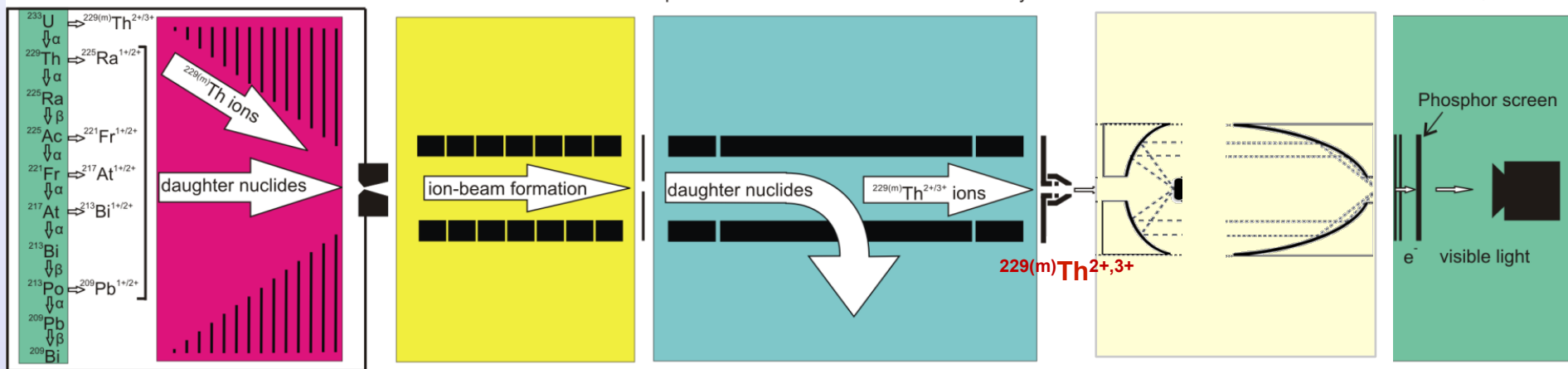
Buffer gas
stopping cell

Laval
nozzle

aperture
electrode

triodic
extraction
electrode

detection
system



^{233}U source RF + DC funnel RF quadrupole ion guide Quadrupole mass separator UV detection MCP CCD

40 mbar (He)

10^{-2} mbar

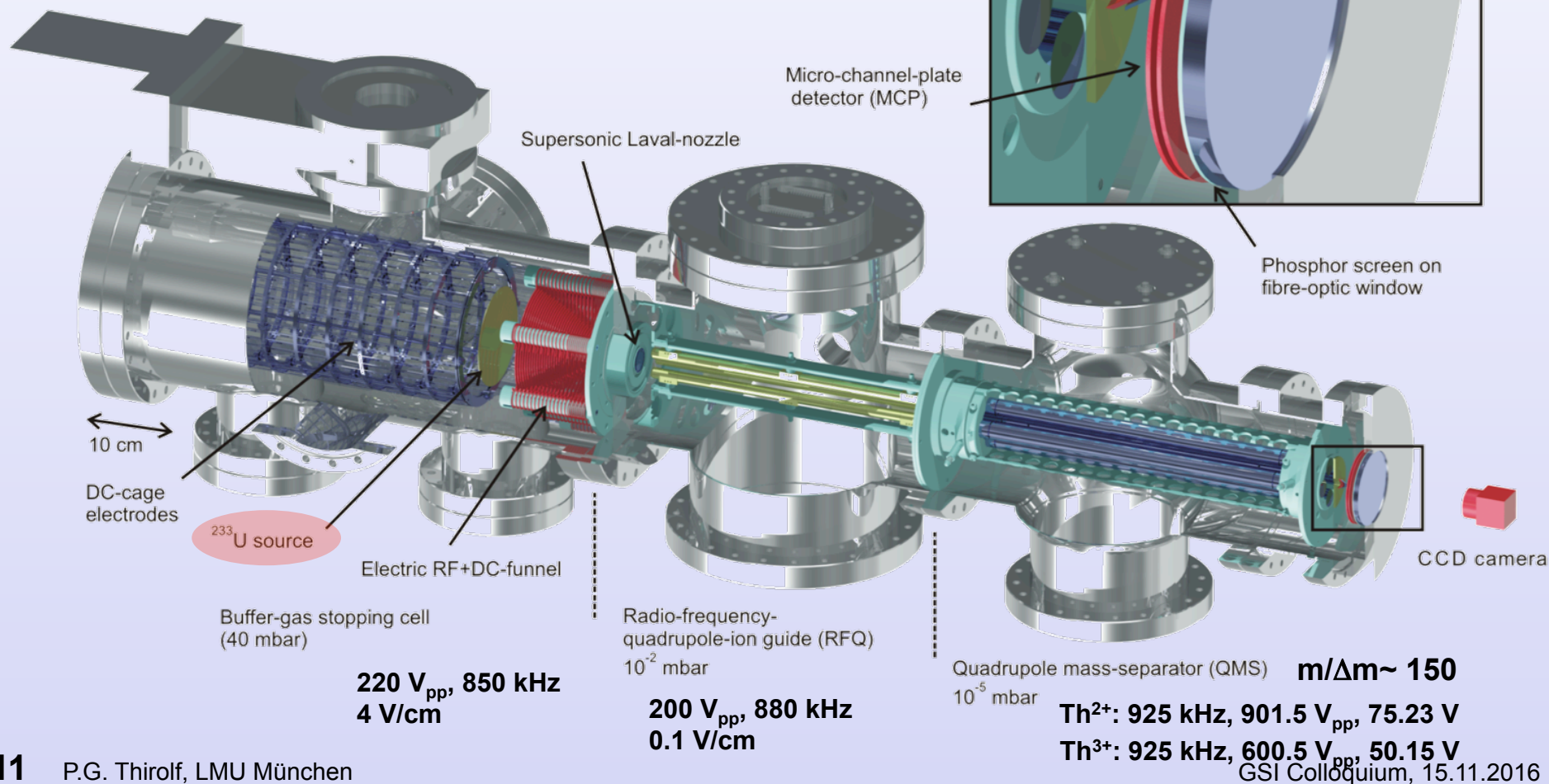
10^{-6} mbar

→ 4 vacuum chambers, 3 differential pump sections, overall length ~ 2 m

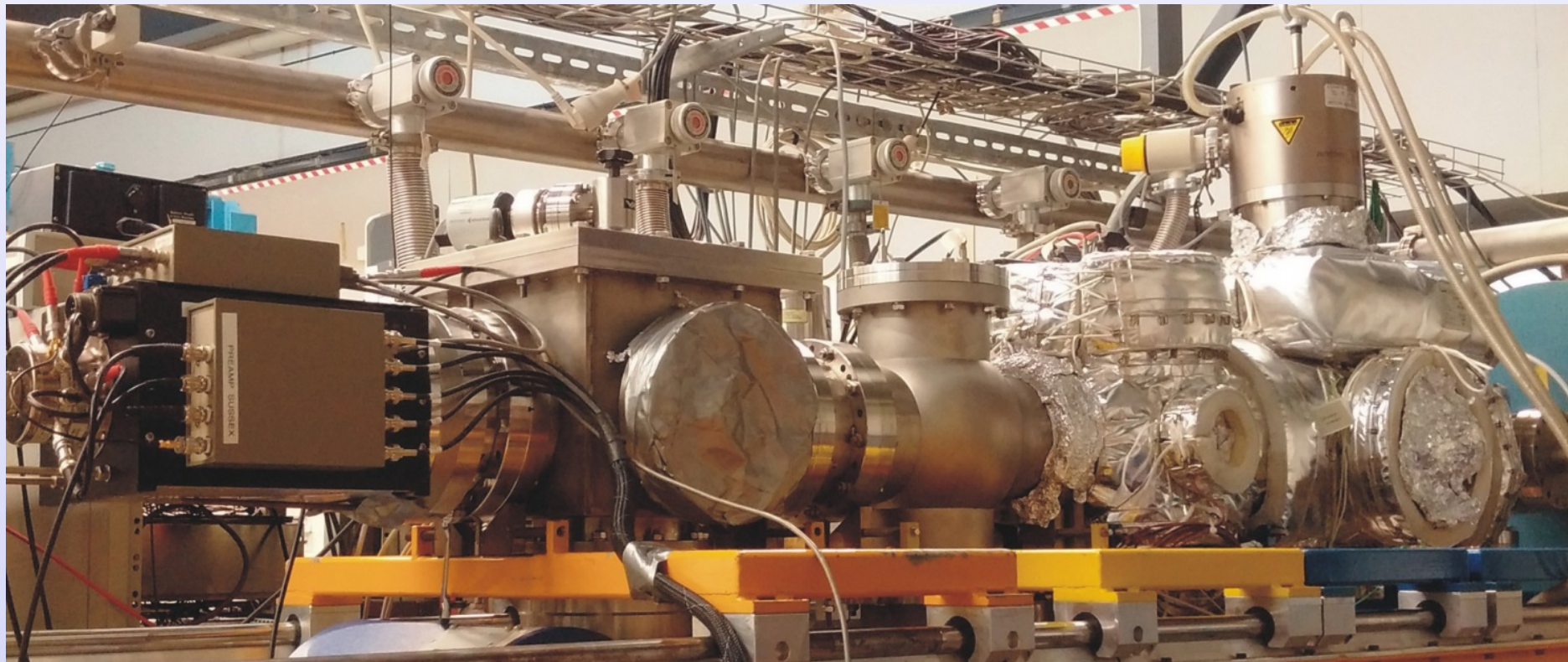
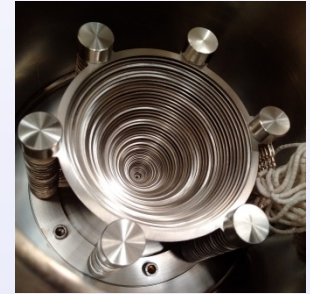
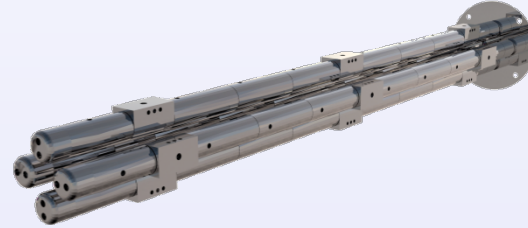
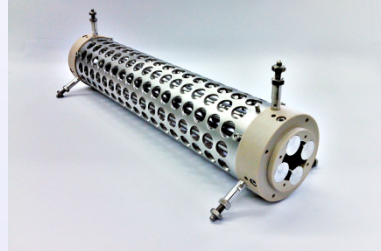
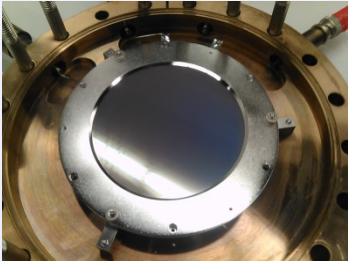
Experimental Setup



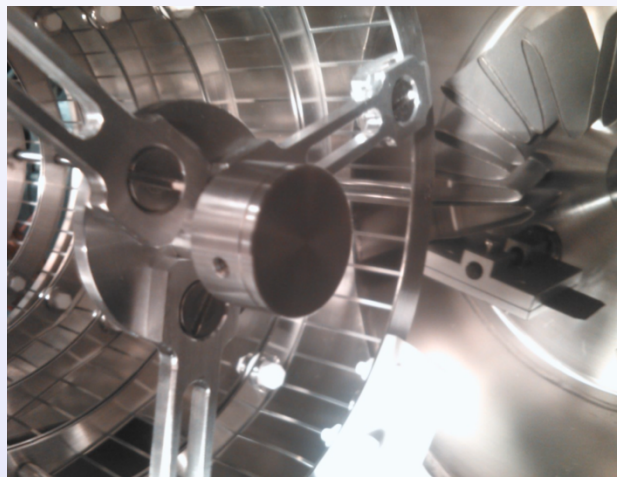
- strictly UHV compatible, bakeable (180°)
- typical: $2.8 \cdot 10^{-10}$ mbar
- operated at 40 mbar He 6.0
- catalytically purified ($< \text{ppb}$)



located at Maier-Leibnitz Laboratory, Garching:



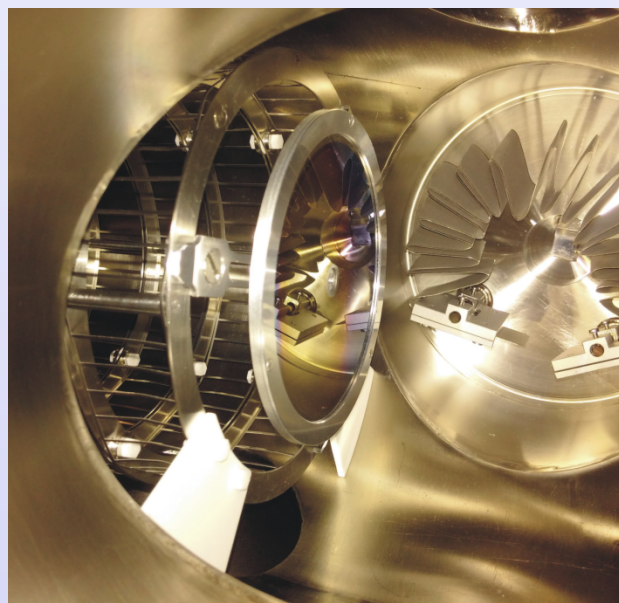
population of $^{229\text{m}}\text{Th}$ via 2% α decay branch of ^{233}U



2 different ^{233}U sources were used:

source 1:

- 200 kBq $^{233}\text{UF}_4$ evaporated onto 20 mm $\varnothing$ steel plate
- no radio-chemical purification before evaporation
- ^{232}U contamination $\leq 10^{-6}$
- eff. $^{229(\text{m})}\text{Th}$ recoil activity: ca. 4000/s



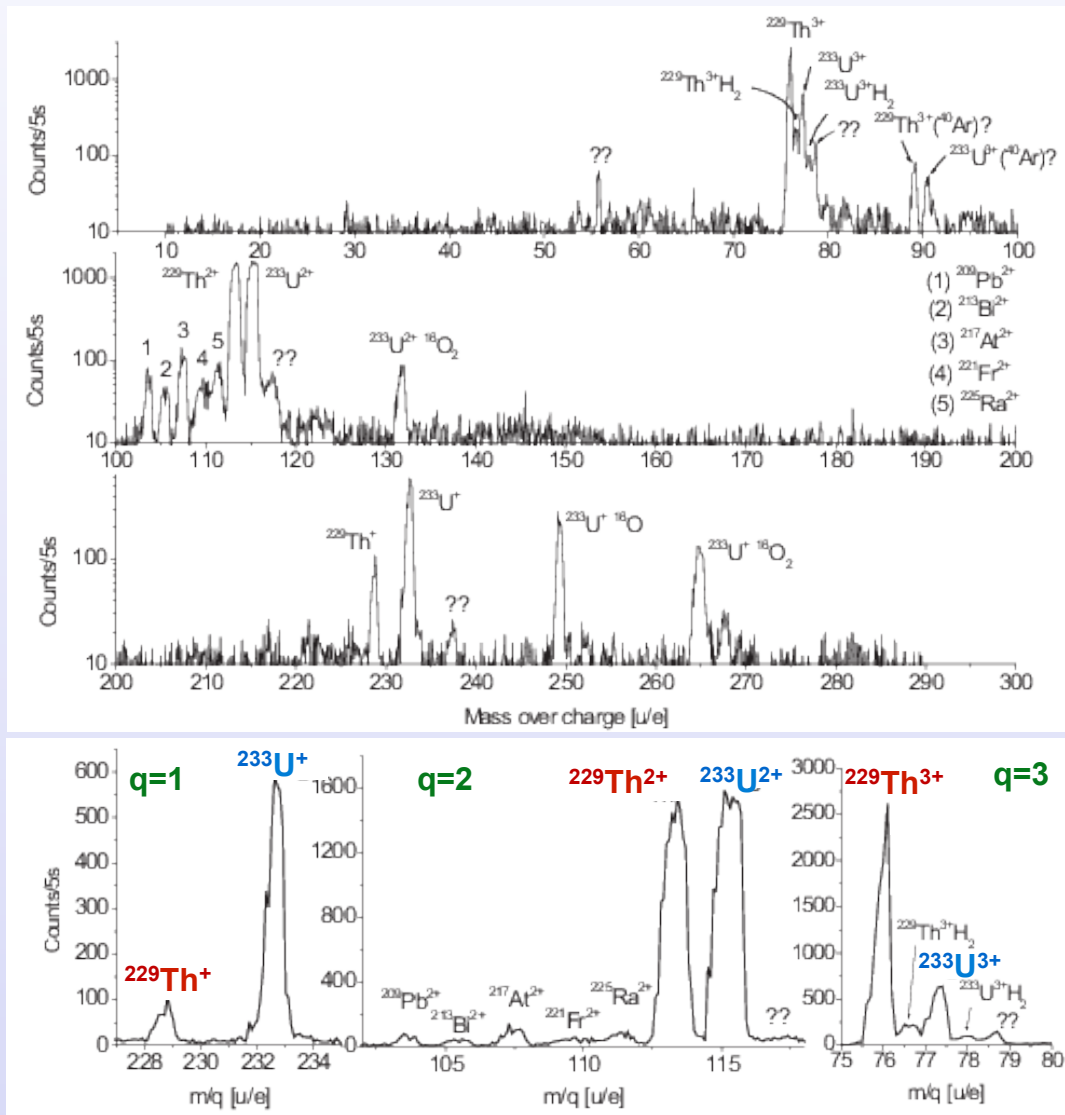
source 2: (IRC Uni Mainz)

- 290 kBq electro-deposited onto 90 mm $\varnothing$ wafer
- radio-chemical purification before evaporation
- ^{232}U contamination $\leq 10^{-6}$
- eff. $^{229(\text{m})}\text{Th}$ recoil activity: ca. 55000/s

Ion Extraction from Buffer Gas Cell



mass scan of extracted ion species: efficient $^{229(m)}\text{Th}^{3+}$ extraction



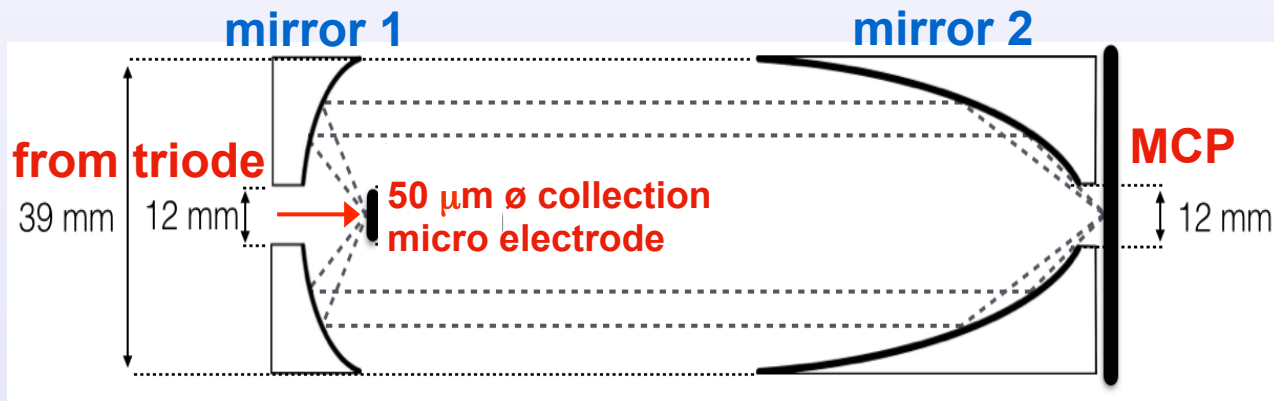
element	1+ [%]	2+ [%]	3+ [%]
Th	0.37(7)	5.5(11)	10(2)
Fr	21.0(42)	16.0(32)	$\leq 1.5 \cdot 10^{-3}$
Rn	5.8(12)	9.3(19)	0.053(11)
At	8.6(17)	13.0(26)	0.033(7)
Po	7.3(15)	8.1(16)	≤ 0.0021
Bi	4.3(9)	21.0(42)	0.083(16)
Pb	2.2(4)	11.0(22)	≤ 0.012

element	1+ [eV]	2+ [eV]	3+ [eV]
U	6.1	11.6	19.8
Th	6.3	11.9	18.3
Ra	5.3	10.1	31.0
Fr	4.1	22.4	33.5
Rn	10.7	21.4	29.4
At	9.3	17.9	26.6
Po	8.4	19.3	27.3
Bi	7.3	16.7	25.6

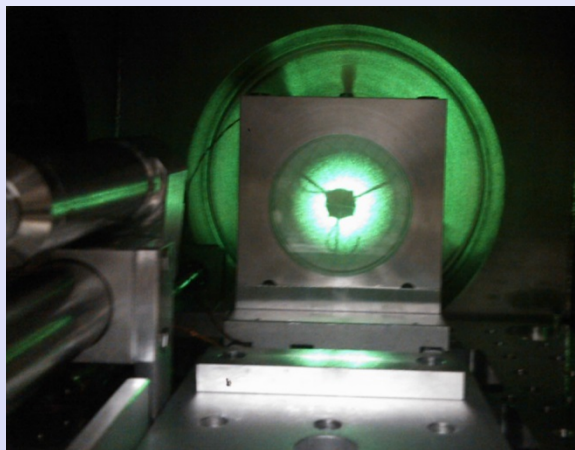
Isomer Decay: Search for VUV Fluorescence

UV optical setup designed, built and commissioned (aligned):

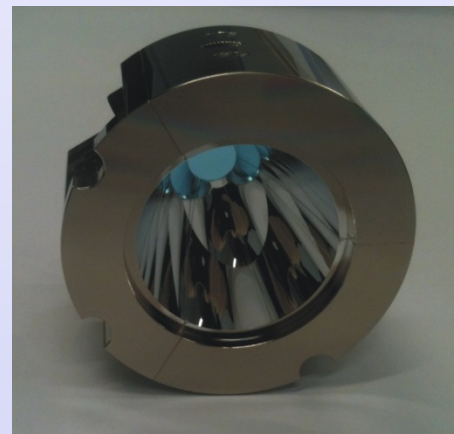
→ 2 annular, parabolic mirrors (MgF₂ coated, from Fraunhofer IOF, Jena)



mirror 1:



mirror 2:



B. Seiferle, L. v.d. Wense, M. Laatiaoui, PT, EPJ D70, 58 (2016)

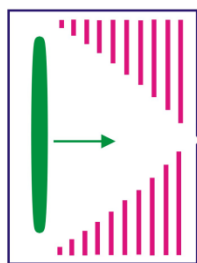
Step 1:
Stopping & Extraction

Step 2:
Mass Filtering

Step 3:
Collection

Step 4:
VUV Optics &

Step 5:
Detection



efficiency:

Isomer: Extraction: Charge: Mass Filter: Collection: Mirror acceptance: Mirror reflectivity: Focusing: Detection:

2% 16% 65% 80% 40% 42% 49% 76% 10%

Total efficiency:
 $1.3 \cdot 10^{-5}$

L. v.d. Wense, PT, D. Kalb, M. Laatiaoui, Journal of Instrumentation 8, P03005 (2013)

▪ signal-to-noise ratio:

▪ VUV fluorescence ?

ion collection on micro-electrode:
no fluorescence signal was observed

→ radiative decay branch too weak ?

→ search for dominant IC decay branch

→ measure conversion electrons

²³³U source 2

eff. ²²⁹ Th recoil activity	55000 / s
detectable VUV photons	0.72 / s
count rate/area	81.82 / mm ² s
dark count rate	0.01 / mm ² s
signal/noise ratio	8182:1

Isomer Detection Process



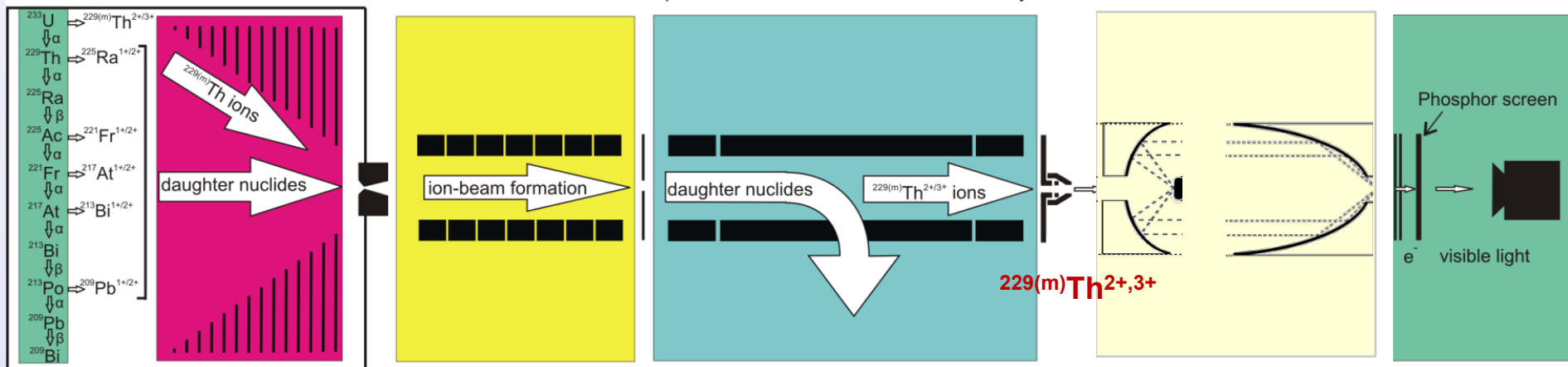
Buffer gas
stopping cell

Laval
nozzle

aperture
electrode

tridodic
extraction
electrode

detection
system



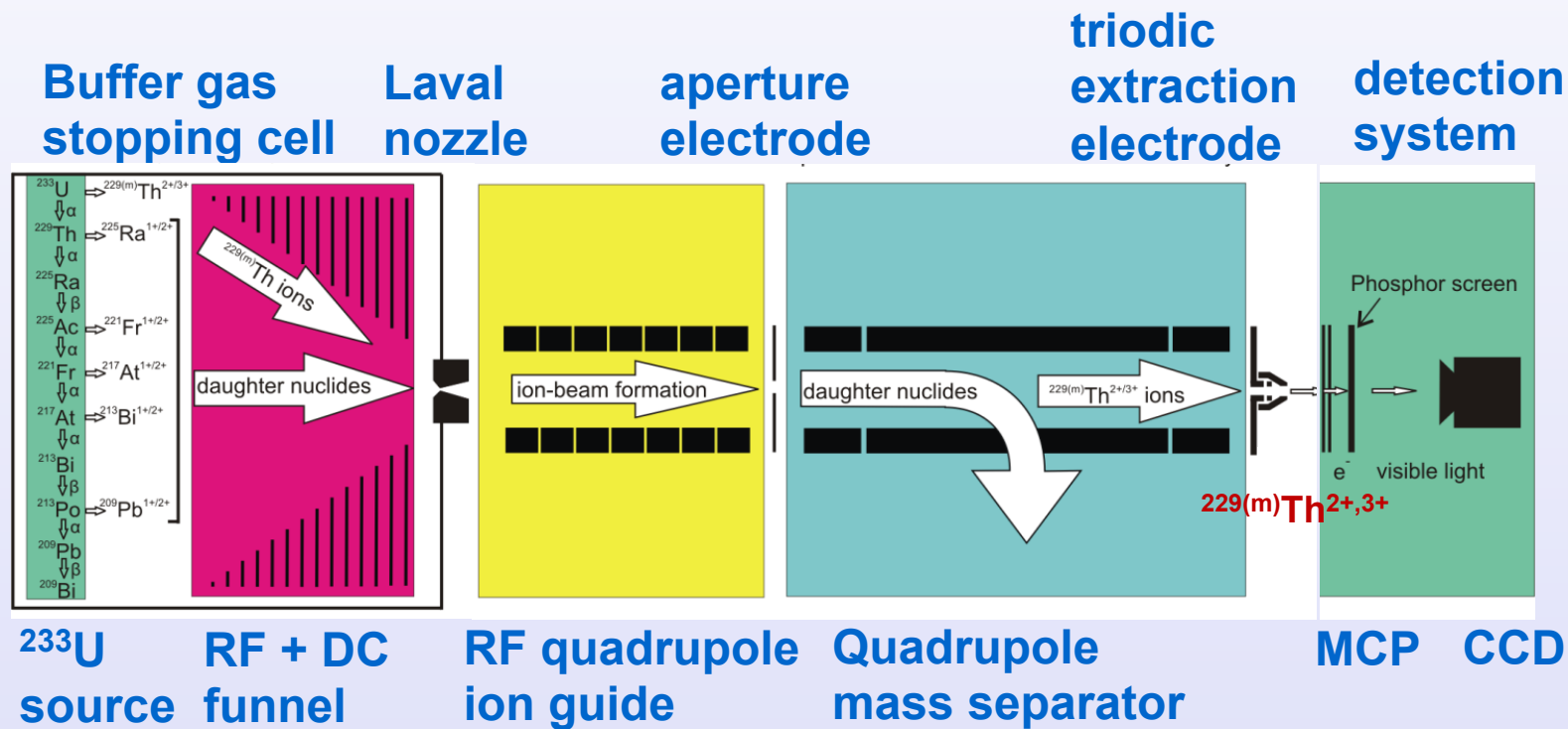
^{233}U
source
RF + DC
funnel

RF quadrupole
ion guide

Quadrupole
mass separator

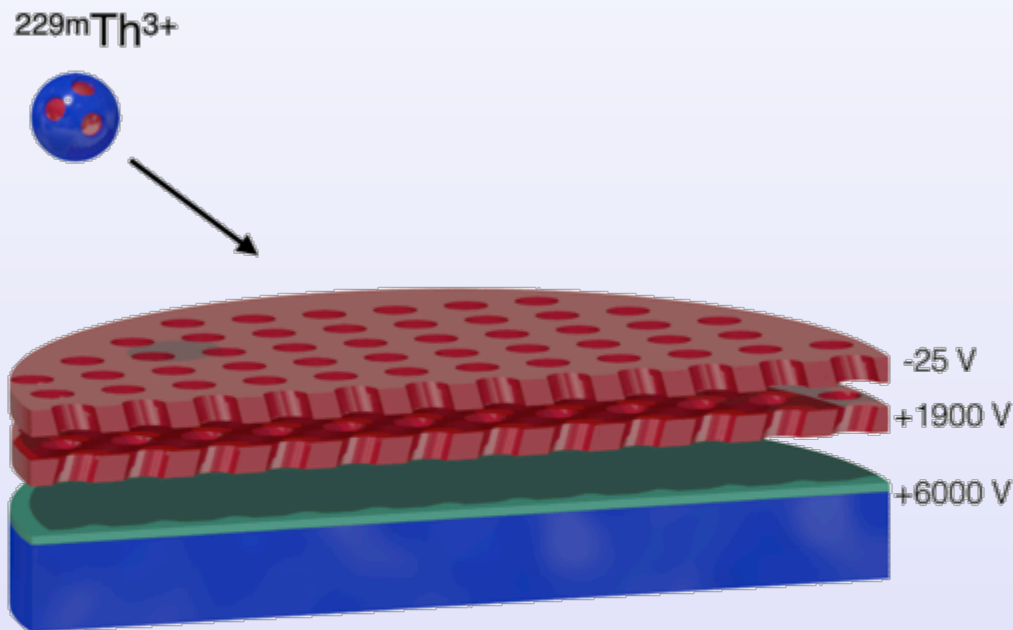
UV detection MCP CCD

Isomer Detection Process



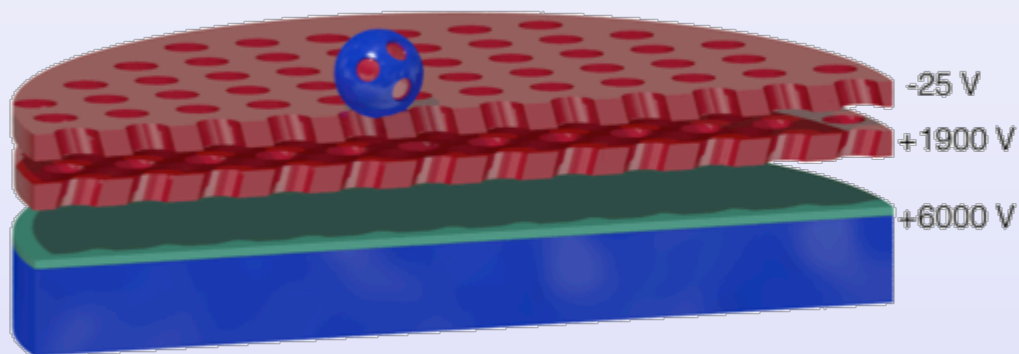
→ accumulate $^{229}\text{Th}^{2+,3+}$ ions directly onto MCP surface

extracted $^{229\text{m}}\text{Th}^{3+}$ ions: impinging directly onto MCP surface behind triode exit

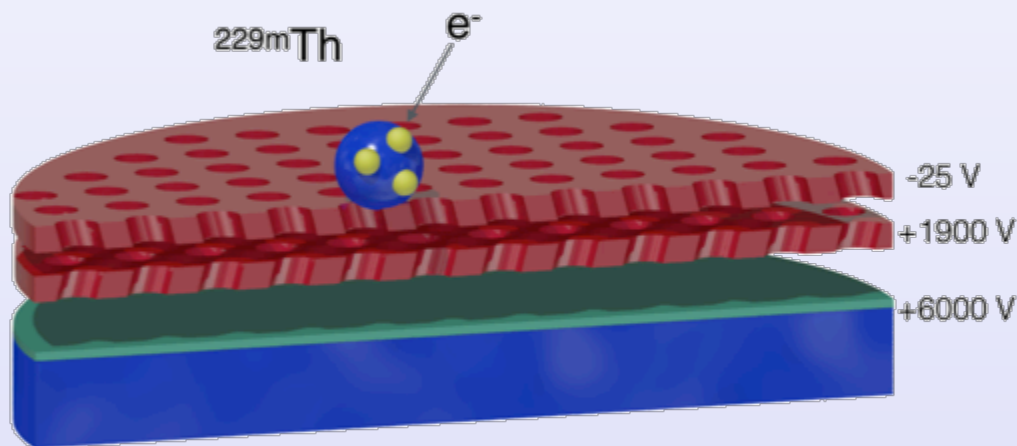


Isomer Detection Process

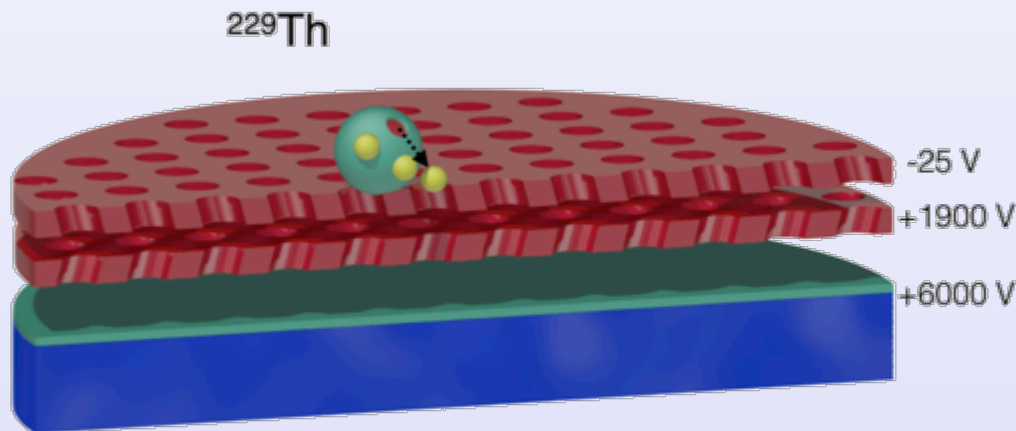
extracted $^{229\text{(m)}}\text{Th}^{3+}$ ions: 'soft landing' on MCP surface



electron capture on MCP surface: neutralization of Th ions



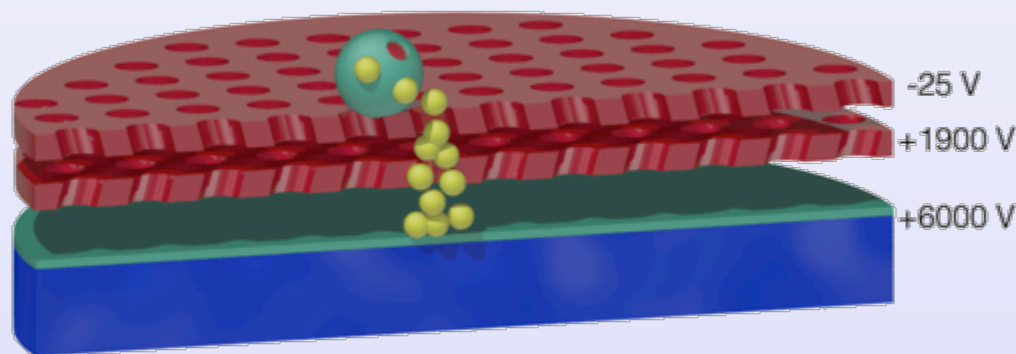
isomer decay by Internal Conversion: electron emission



- internal conversion (IC) energetically allowed for neutral thorium:

$$I(\text{Th}^+, 6.31 \text{ eV}) < E^*(^{229\text{m}}\text{Th}, 7.8 \text{ eV})$$
- isomer lifetime expected to be reduced by ca. 10^9 (from $\sim 10^4 \text{ s} \rightarrow \sim 10 \mu\text{s}$)
- Th ions: IC is energetically forbidden, radiative decay branch may dominate

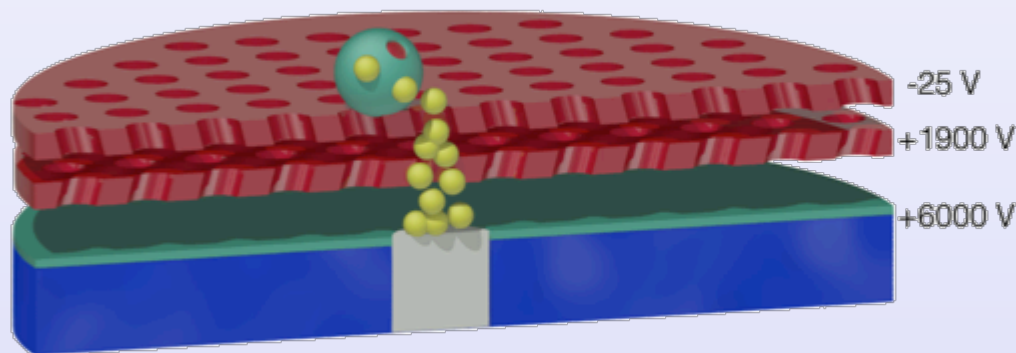
amplification of IC electron: electron cascade generated,
accelerated towards phosphor screen



- internal conversion (IC) energetically allowed for neutral thorium:

$$I(\text{Th}^+, 6.31 \text{ eV}) < E^*(^{229\text{m}}\text{Th}, 7.8 \text{ eV})$$
- isomer lifetime expected to be reduced by ca. 10^9 (from $\sim 10^4 \text{ s} \rightarrow \sim 10 \mu\text{s}$)
- Th ions: IC is energetically forbidden, radiative decay branch may dominate

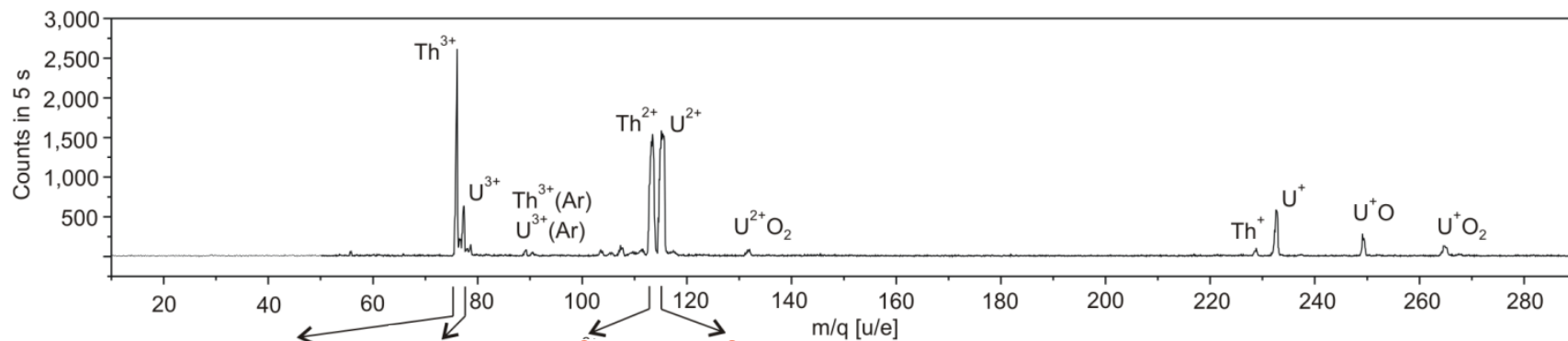
electrons hit phosphor screen: visible light imaged by CCD camera



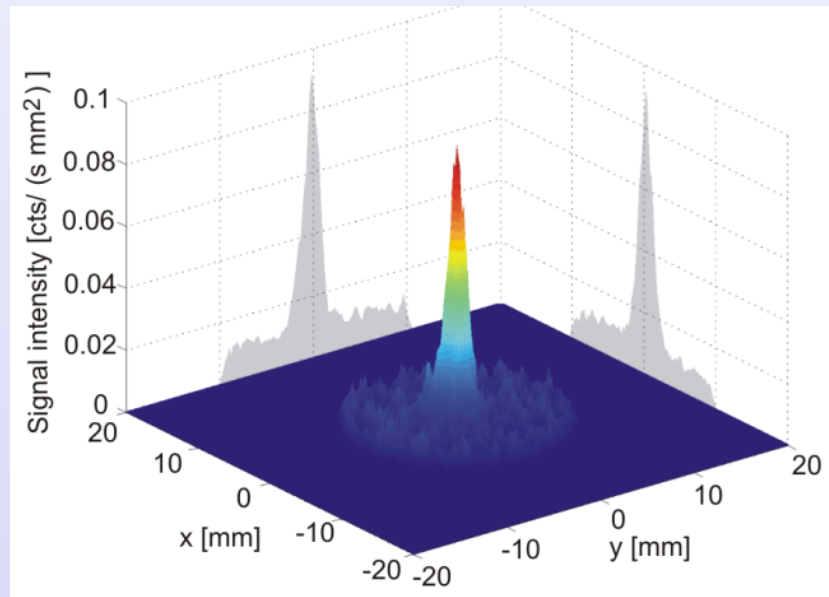
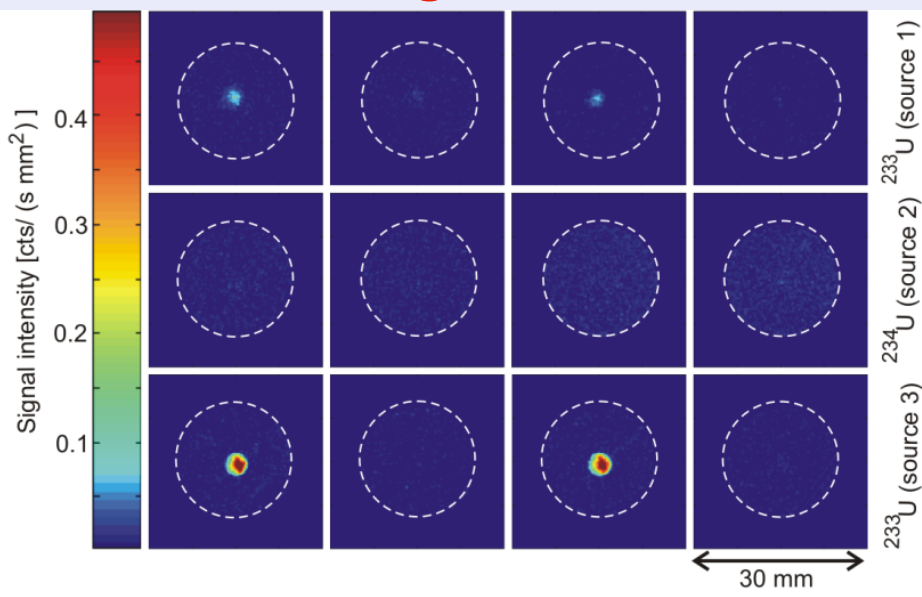
- internal conversion (IC) energetically allowed for neutral thorium:

$$I(\text{Th}^+, 6.31 \text{ eV}) < E^*(^{229\text{m}}\text{Th}, 7.8 \text{ eV})$$
- isomer lifetime expected to be reduced by ca. 10^9 (from $\sim 10^4 \text{ s} \rightarrow \sim 10 \mu\text{s}$)
- Th ions: IC is energetically forbidden, radiative decay branch may dominate

L. v.d. Wense, PT et al., Nature 533, 47-53 (2016)



Th³⁺ U³⁺ Th²⁺ U²⁺

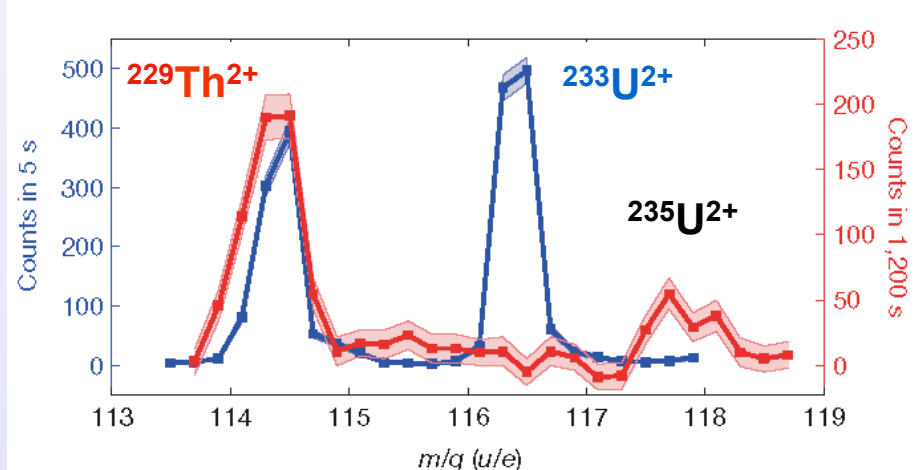
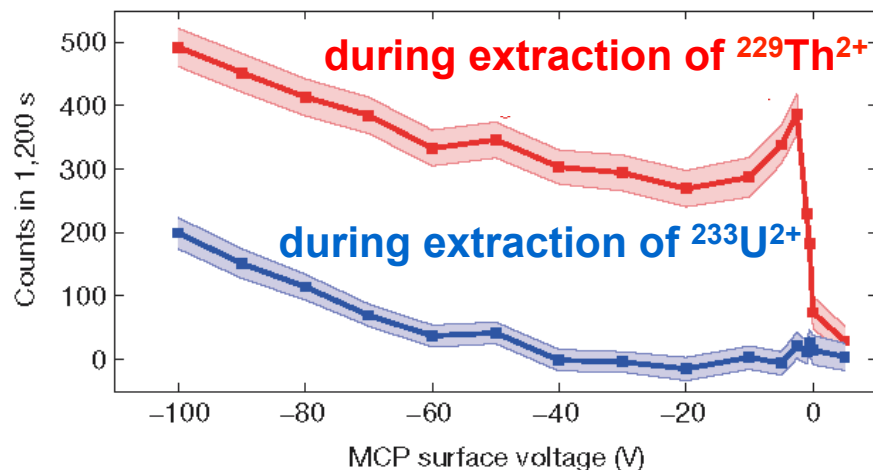


clear signal from Th^{3+} , Th^{2+}
no signal from U^{3+} , U^{2+}

Background-corrected isomeric decay signals:

$U_{MCP} = -25 \text{ V}$
→ isomeric decay

$U_{MCP} = -900 \text{ V}$
→ ionic impact



- ionic impact signal decreases with U_{MCP}
- $^{233}\text{U}^{2+}$ signal drops to zero
- $^{229}\text{Th}^{2+}$ signal remains, cutoff at $E_{kin}=0$
(rise: IC electrons back-attracted to MCP surface by repelling triode)

- comparable mass peak amplitudes for $^{229}\text{Th}^{2+}$, $^{233}\text{U}^{2+}$ ion impact signals
- for $U_{MCP} = -25 \text{ V}$ $^{233}\text{U}^{2+}$ signal vanishes
- $^{229}\text{Th}^{2+}$ signal remains



A) Background due to kinetic energy or charge state of impinging ions

B) Background signals from setup components

(source, gas stopping cell, extraction system, QMS , MCP system)

C) Signals from thorium atomic shell

(e.g. long-lived excited states, chemical reactions on MCP surface)

D) Signals from short-lived daughter nuclides or non- ^{229}Th isomers



could all be excluded,
mostly by several ways

No.	Way of background exclusion	Type of background			
		A	B	C	D
1	Signal comparison between $^{229}\text{Th}^{2+}$ and $^{233}\text{U}^{2+}$	x	x		
2	Comparative $^{229}\text{Th}^{2+}$ and $^{233}\text{U}^{2+}$ signal behaviour as a function of MCP surface voltage	x	x		
3	Signal comparison between ^{229}Th and ^{230}Th	x	x	x	
4	Signal comparison between $^{229}\text{Th}^{2+}$ and $^{229}\text{Th}^{3+}$				x
5	Signal comparison between ^{229}Th originating from chemically purified and unpurified ^{233}U sources				x
6	Exclusion based on signal appearance and the $^{229\text{m}}\text{Th}$ half-life limit				x
7	Search for α and β decays using Si and LN_2 cooled Si(Li) detectors				x



Nuclear clock breakthrough could revolutionize how we measure time

By Duncan Geere May 06, 2016 World of tech

Direct detection of nuclear transition in thorium-229 heralds new clock

May 5, 2016 by Bob Yirka report

News > Nuclear clock breakthrough could revolutionize how we measure time

Nuclear clock breakthrough could revolutionize how we measure time

By Duncan Geere May 06, 2016 World of tech

Tick tick boom



PHYSICS: FROM THE ATOMIC TO THE NUCLEAR CLOCK

BASIC SCIENCE / MAY 6, 2016 / BY SCIENCE NEWS STAFF

significantly improve precision beyond that of the current step toward this goal.

ld.com

Media In depth Events

nuclear-clock transition spotted in thorium-229

11 comment



... in the Element Thorium für eine

The Cosmos Gets a New Clock -- Beyond a Single Second in 20 Billion Years
May 09, 2016

Forbes Atomurets nøjagtighe
Energiovergange i kern

Why Do Physicists
It didn't
above W9

Sunday, 19 June, 2016
Updated 12:42 PM IST

SCIENCE

Шаг к ядерным часам

Открыто метастабильное состояние ядра тория-229, что открывает путь к созданию сверхточных ядерных часов.

История человеческой цивилизации связана с использованием точности часов. Без этого невозможно развитие науки и техники. Сейчас ученые пытаются создать атомные часы, поскольку они используют разность энергий между двумя метастабильными состояниями атомов.

News 1 Release

Een tikje dichterbij de nucleaire superklok

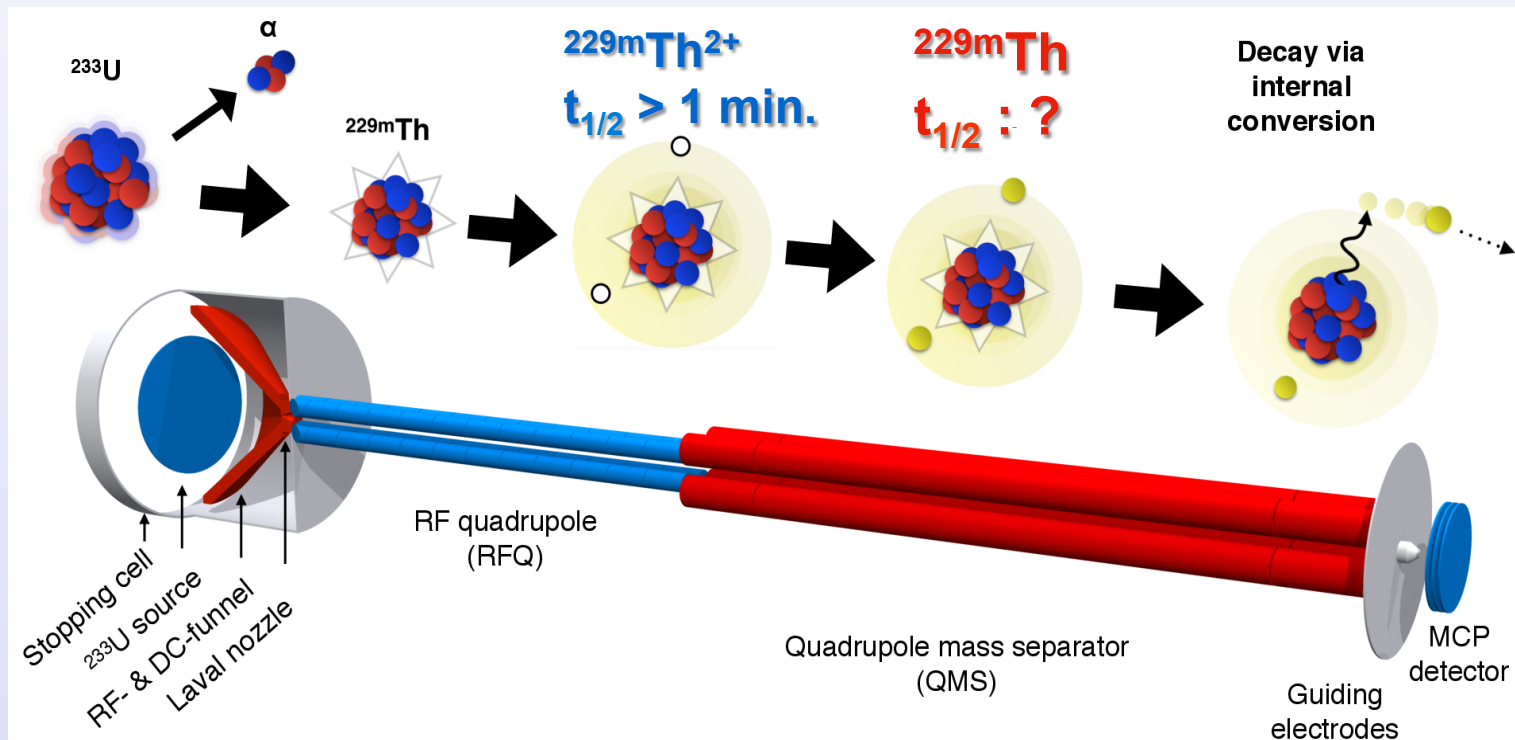
Wetenschappers vinden een meetbare 'pendule' in een atoomkern

herkömmlicher Atomuhren deutlich übertreffen
09.05.2016

... metastabilen Zuständen

Next steps: Halflife determination

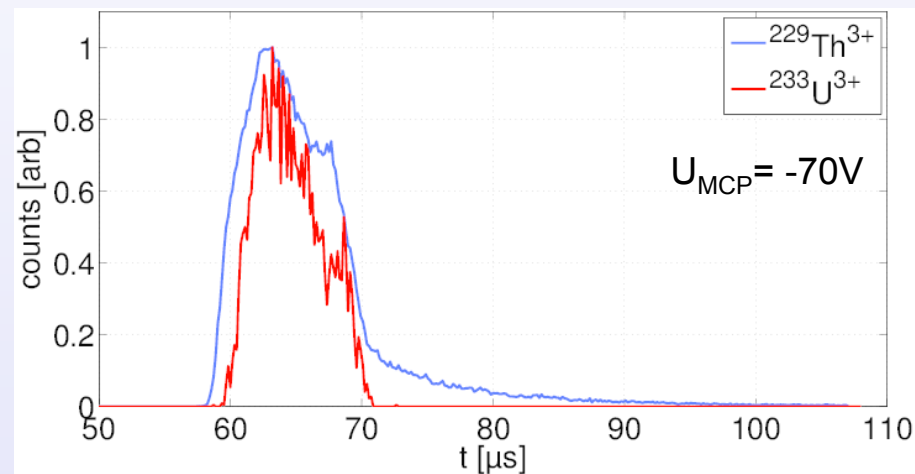
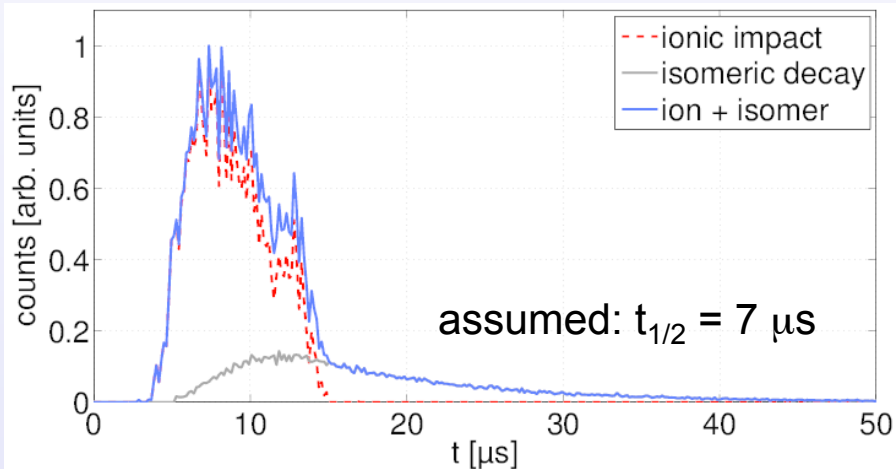
- charged $^{229m}\text{Th}^{2+}$: $t_{1/2} > 1$ min (limited by RFQ storage time)
- neutral ^{229m}Th : pulsed extraction from RFQ



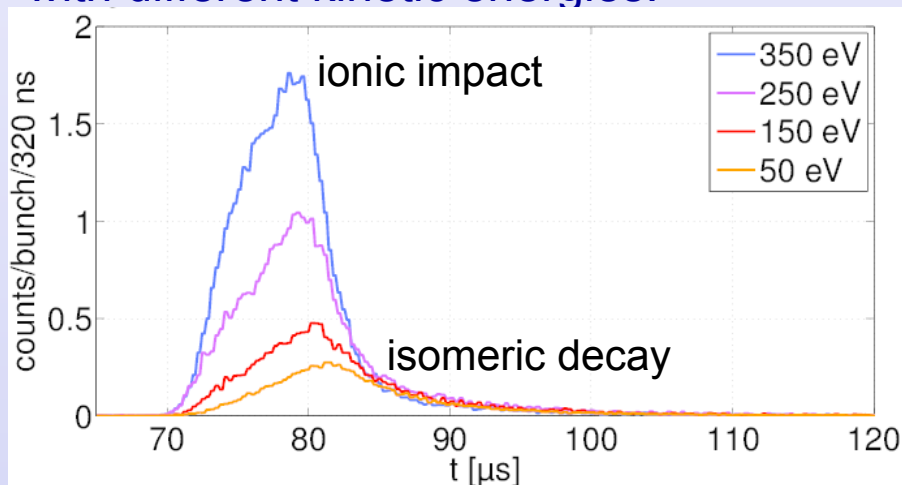
- expected conversion coefficient: ca. 10^9
- provides constraint for strength of photonic decay branch (if IC cannot be suppressed, e.g. by suitable lattice implantation)

simulation:

measurement:

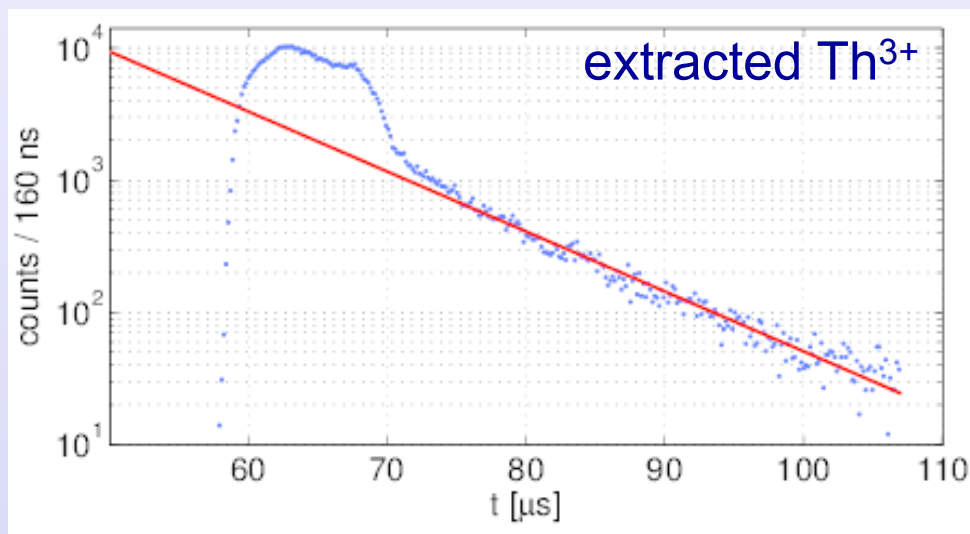
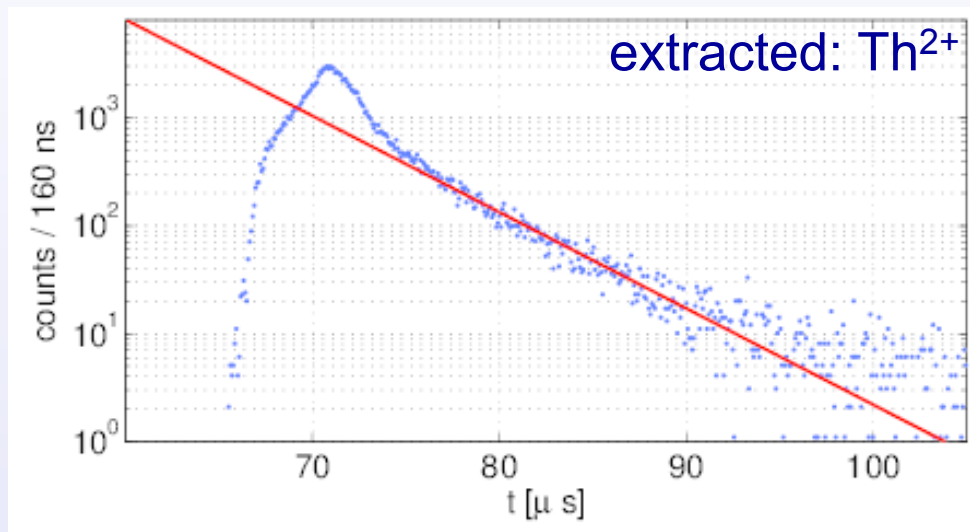


MCP signal of $^{229(m)}\text{Th}^{2+}$ ion bunches with different kinetic energies:



- bunch width: ca. $10 \mu\text{s}$
- 600- 800 $^{229(m)}\text{Th}^{2+,3+}$ ions/bunch

Halflife: Neutral ^{229m}Th

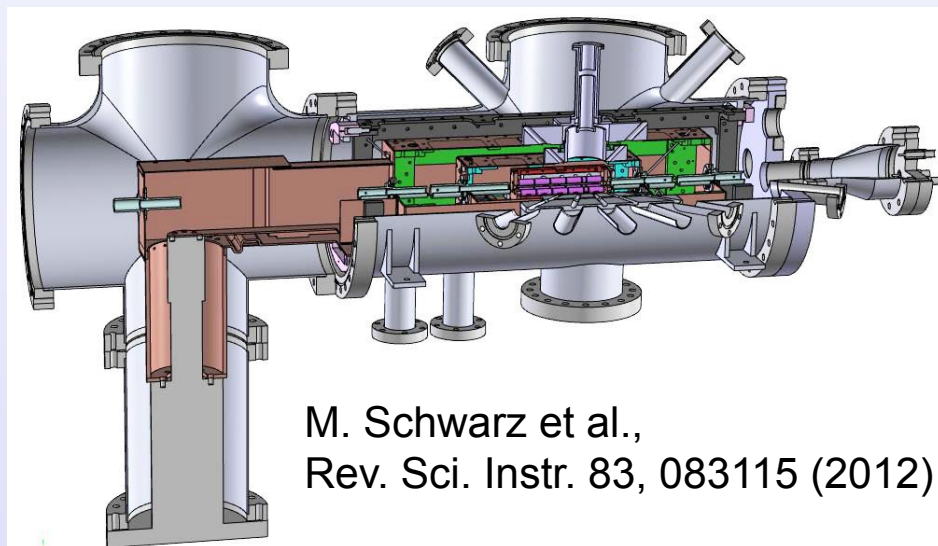


based on expected charged isomeric half-life of a few 10^3 s:
confirms expected conversion coefficient of ca. $10^9 \rightarrow$ photonic decay branch ??

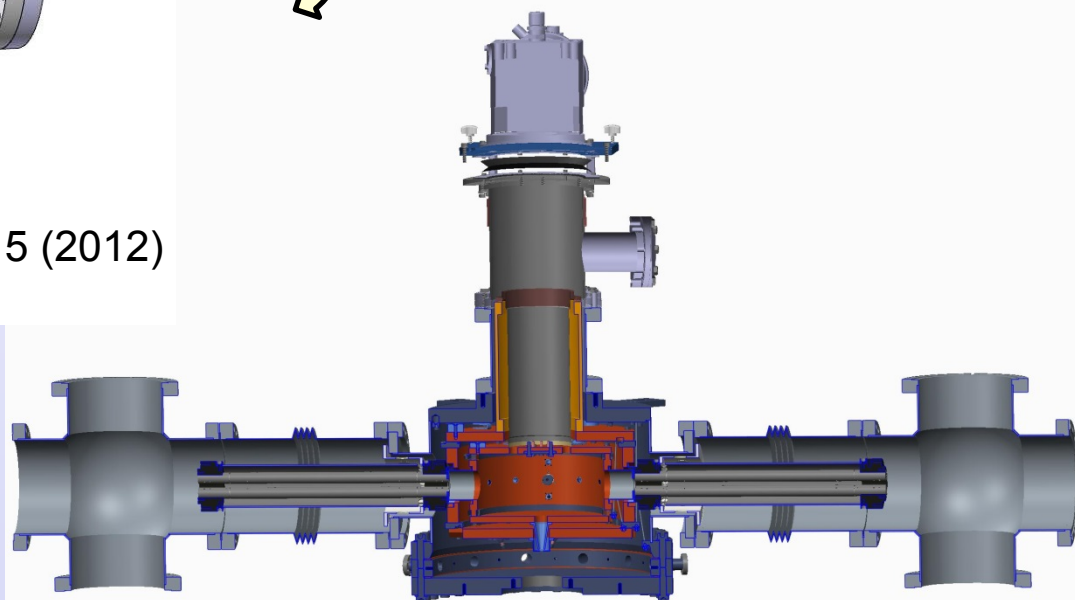
- $^{229m}\text{Th}^{q+}$: longer ion storage time needed ($\rightarrow$ UHV)
 $\rightarrow$ cryogenic linear Paul trap:

- in operation at MPI-K (HD): CryPTEx

- $\rightarrow$ operating at 4 K ($p(\text{H}_2) \sim 10^{-15}$ mbar)
- $\rightarrow$ ion storage time ≤ 30 h
- $\rightarrow$ laser access ports



M. Schwarz et al.,
Rev. Sci. Instr. 83, 083115 (2012)



- $\rightarrow$ prerequisite for laser manipulation
of $^{229m}\text{Th}^{3+}$

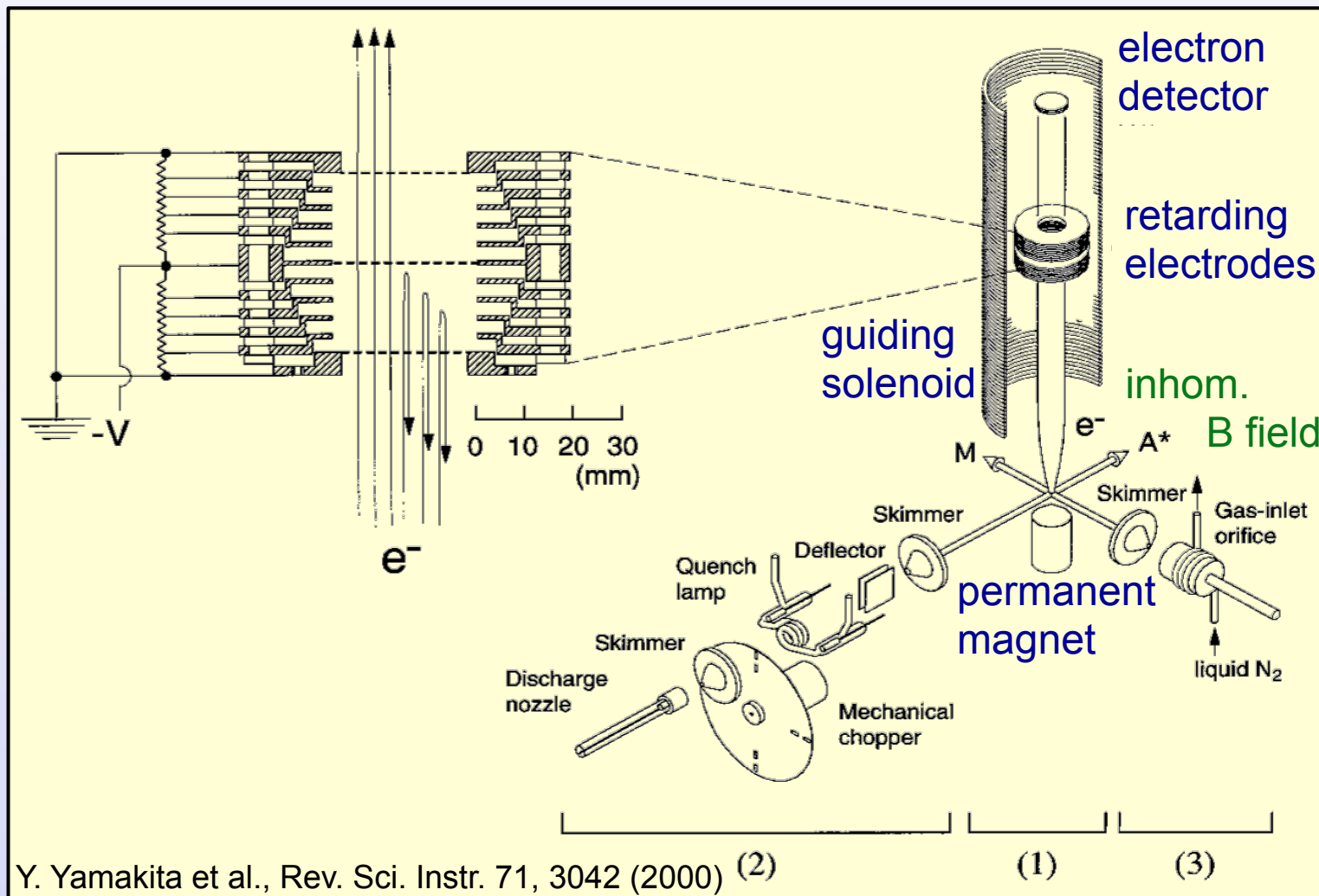
thanks to: MPIK (J. Crespo et al.), PTB (P. Schmidt)

"Holy Grail": Excitation Energy



our present constraint: $6.31 \text{ eV} < E(^{229\text{m}}\text{Th}) < 18.3 \text{ eV}$

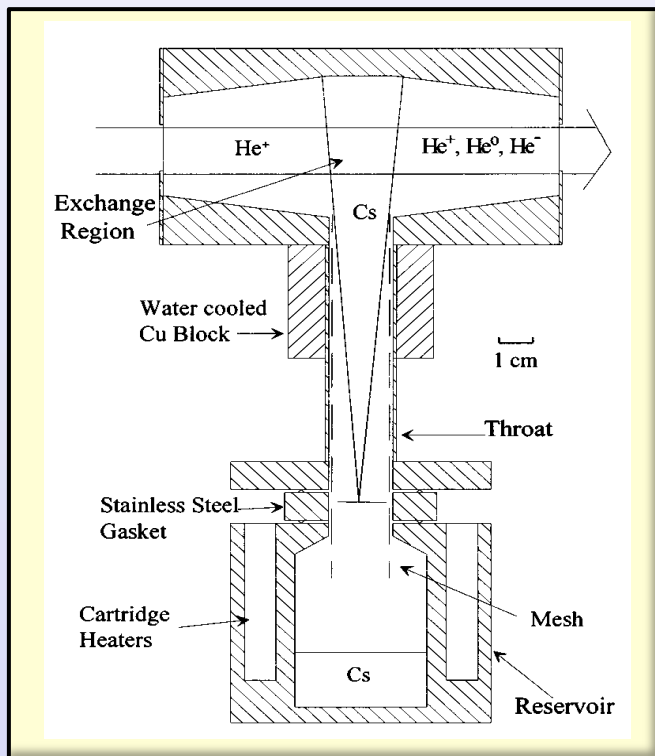
- Magnetic bottle spectrometer: large acceptance needed ($\sim 4\pi$)
10000 ^{229}Th ions extracted/sec. $\rightarrow$ 200 e/s



■ $^{229m}\text{Th}^{2+,3+}$ neutralization with subsequent IC:

- metallic catcher electrode
- but: how to control/avoid surface effects (work function) ?

→ contact-free neutralization: charge-transfer cell

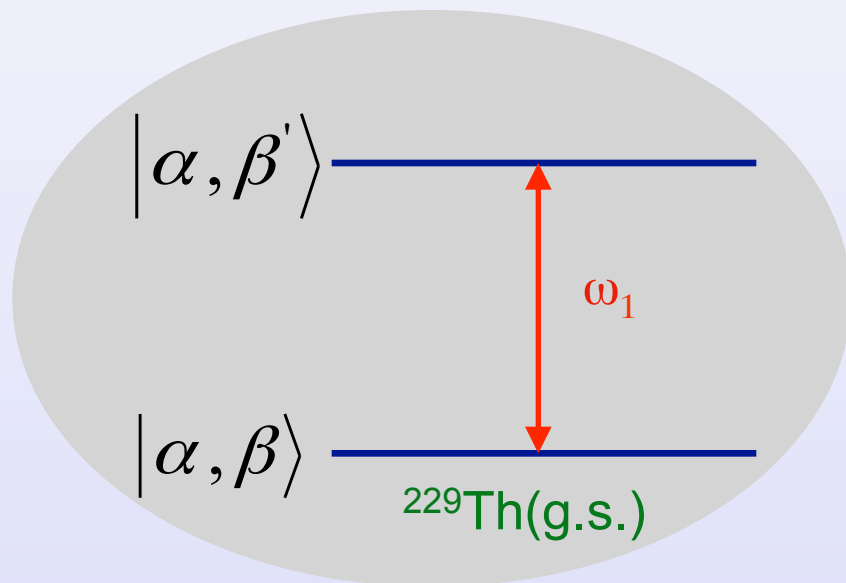


finally expected:
 $\Delta E < 50 \text{ meV}$

M.G. Helander et al., Applied Surface Science 256, 2602 (2010)

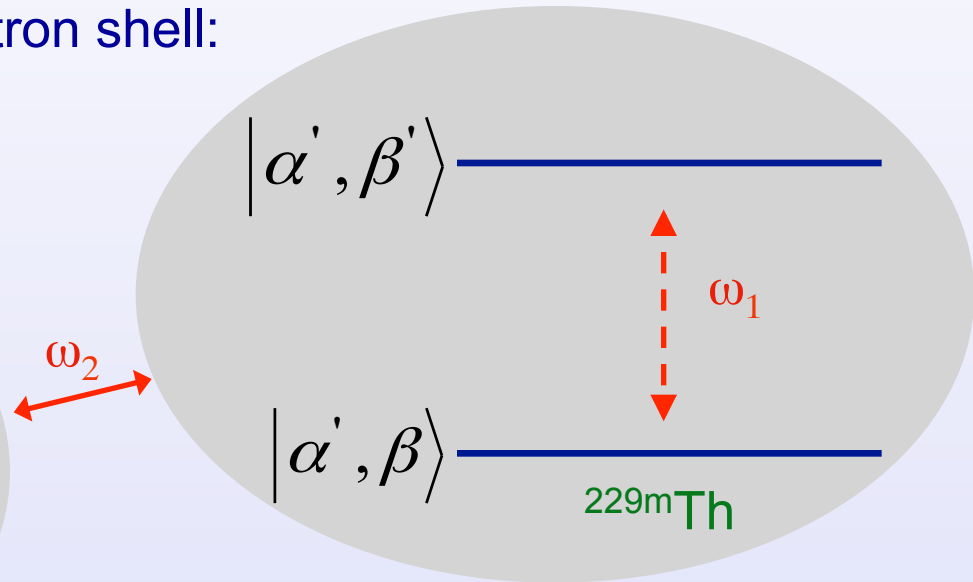
Laser diagnostics of isomer excitation

- use closed 2-level system in electron shell:



α : nuclear, β : electronic

→ double resonance method
Dehmelt's 'electron shelving'

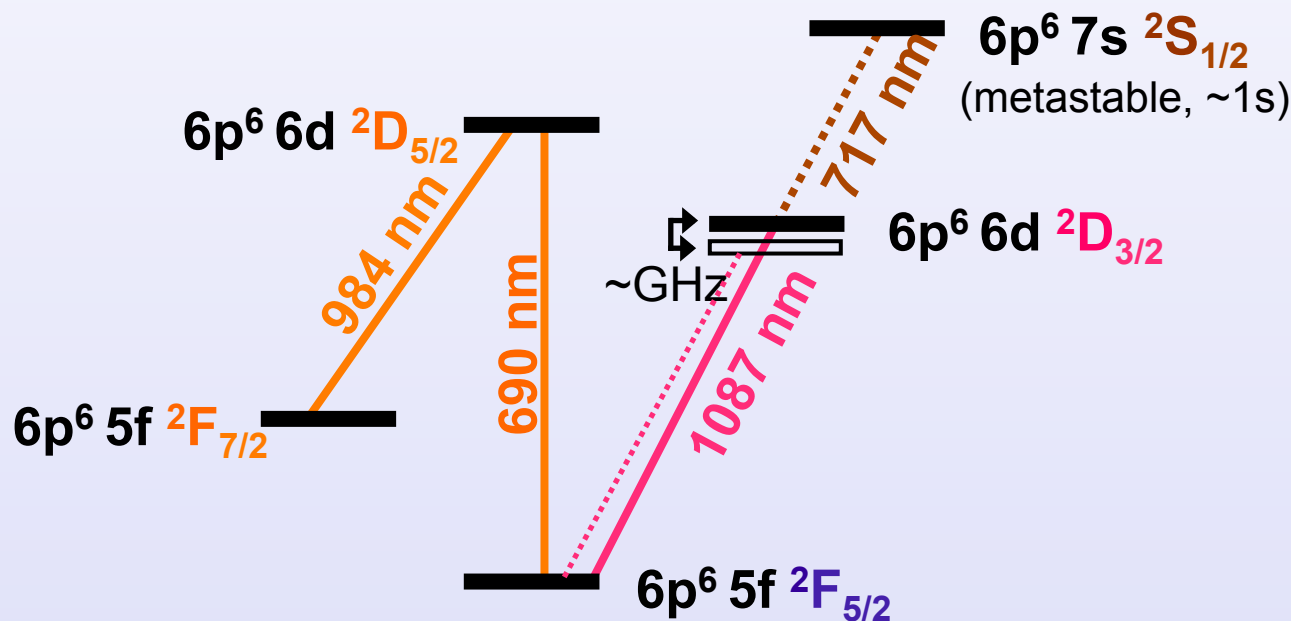


after nuclear transition (via ω_2):

- change of nuclear moments, spin
- change of hyperfine splitting, total angular momenta
- ω_1 out of resonance ($\sim\text{GHz}$)
- drop in resonance fluorescence

Peik, Tamm, Eur. Phys. Lett. 61 (2003) 181

- simple structure: alkali-like (Rn core + single valence electron)



→ closed 3-level Δ system and closed 2-level system available for laser cooling and fluorescence detection

- constant resonance fluorescence scattering with closed optical transition
- after nuclear excitation: out of resonance

→ spectroscopy of laser-cooled $^{229}\text{Th}^{3+}$ (e.g. in linear Paul trap)

Why better clocks at all ?

every time that clock precision has improved, new and frequently unexpected applications have emerged

- example: **GPS navigation**

- present technology:

- 'thermal' microwave atomic clocks (Rb, Cs)
- GPS, GLONASS: active
- Galileo, Beidou, IRNSS: under construction

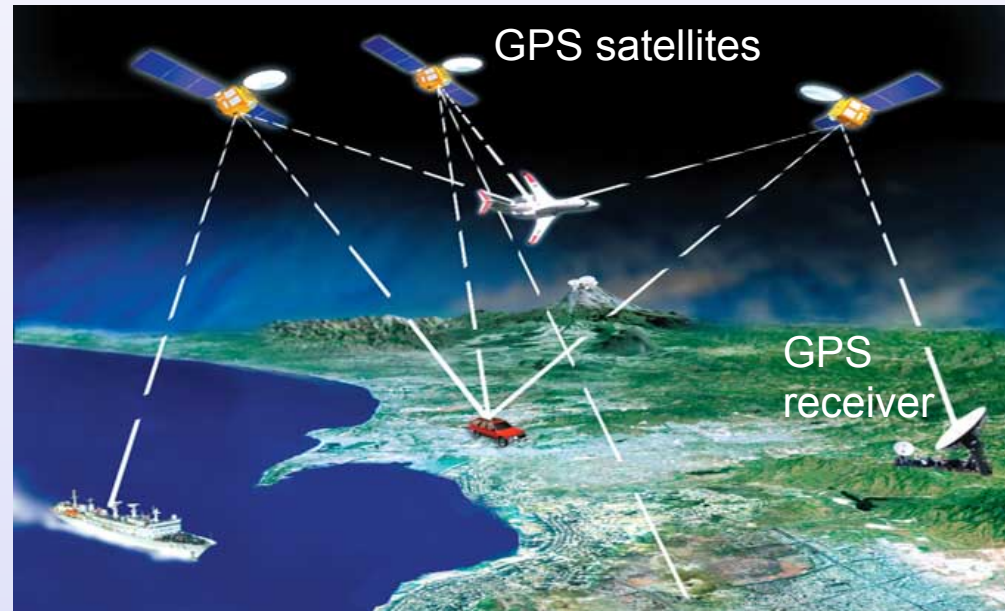
→ positioning precision: 1-10 m

- goal: positioning to cm – mm

- autonomous driving
- freight-/ component tracking
-

- requirements:

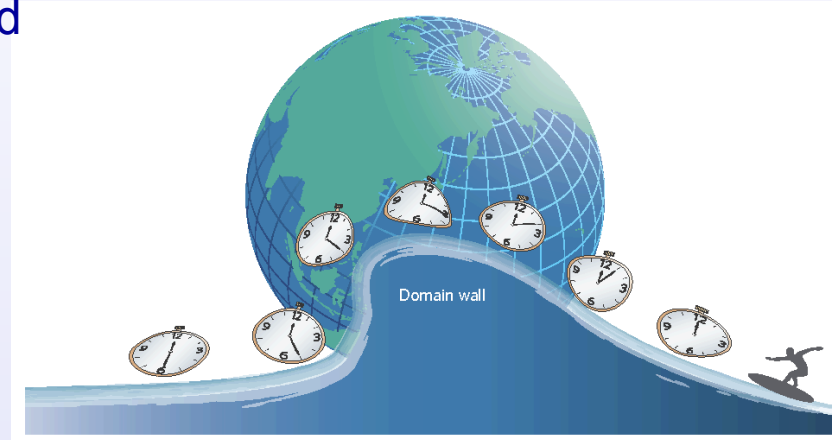
- better clocks (10^{-16} – 10^{-18})
- robust, small, low power consumption ...



- (networks of) ultra-precise clocks could be used to search for dark matter

→ Derevianko & Pospelov,
Nature Physics 10, 933–936 (2014)

- topological dark matter:
clumped to point-like monopoles,
1D strings, 2D ‘domain walls’



- networks of clocks can be used as 3D gravity sensors

→ Ludlow, Boyd, Ye, Peik, Schmidt, Rev. Mod. Phys. 87, 637–701 (2015)

$$\frac{\Delta f}{f} = -\frac{\Delta U}{c^2}$$

Δf : clock frequency difference
 ΔU : gravitational potential difference

- best present clocks: detect gravitational shifts of ± 2 cm
- “relativistic geodesy” or “chronometric leveling”:
→ allows long-distance potential difference measurements
- precise, fast measurements of nuclear clock network:
e.g. monitor volcanic magma chambers, tectonic plate movements

- FET-OPEN project within EU Horizon 2020:
→ experiment, theory, industrial R&D

TU Wien (T. Schumm et al., Coord.)
Univ. Jyväskylä (I. Moore et al.)
Univ. Heidelberg (C. Enss et al.)
MPI-K, HD (A. Pálffy et al.)
PTB Braunschweig (E. Peik et al.)
MPQ Garching (T. Udem et al.)
TOPTICA Photonics AG, Munich
LMU Munich (PT et al.)

associated:

- Okayama Univ., Japan (SPRING8)
- Metrology Light Source (MLS), Berlin-Adlershof
- U Mainz/ HIM (C. Düllmann et al.)

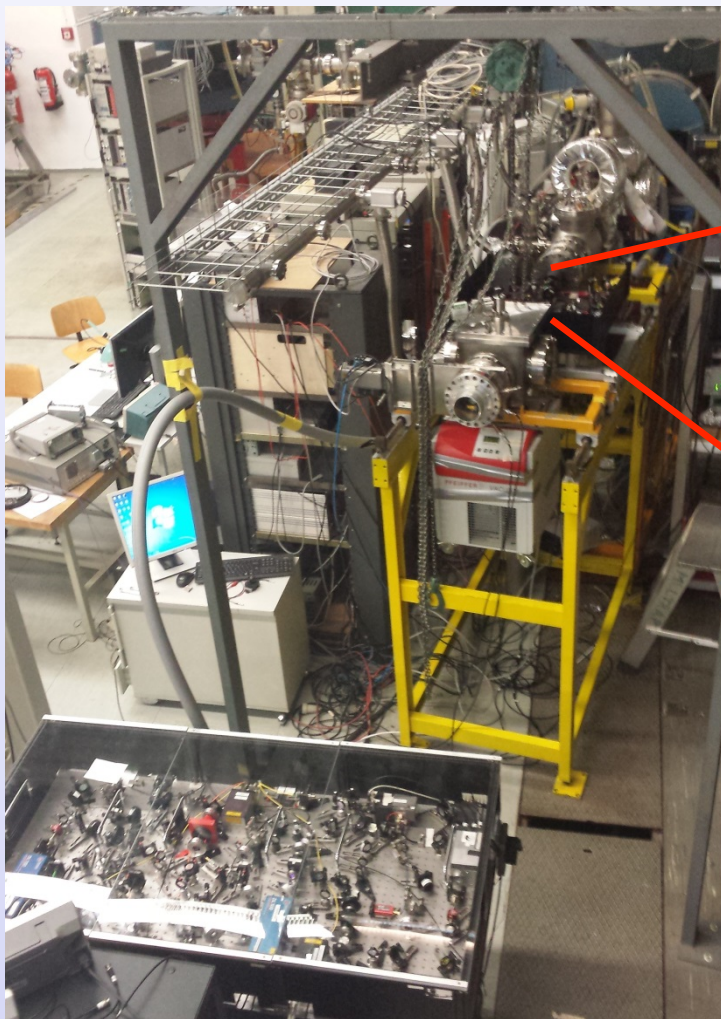
- Kerstin Ergenzinger (Berlin): artist, via FEAT (future emerging art and technology)



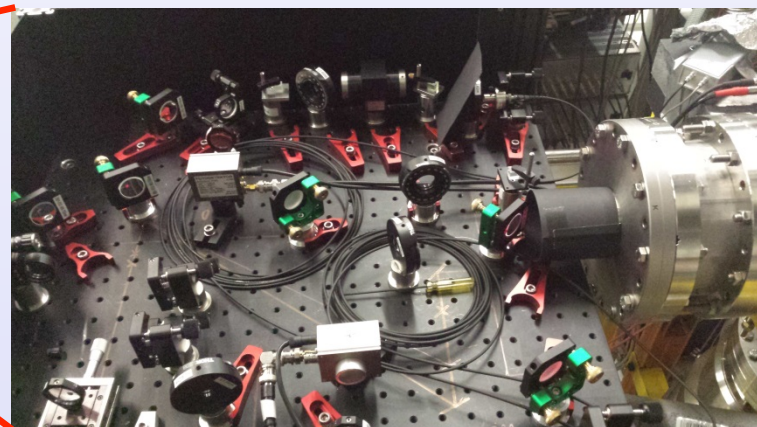
<http://www.nuclock.eu/>

Collaboration with PTB Braunschweig

- E. Peik, M. Okhapkin et al.: targeting hyperfine structure of $^{229\text{m}}\text{Th}^{1+,2+}$



collinear laser spectroscopy:

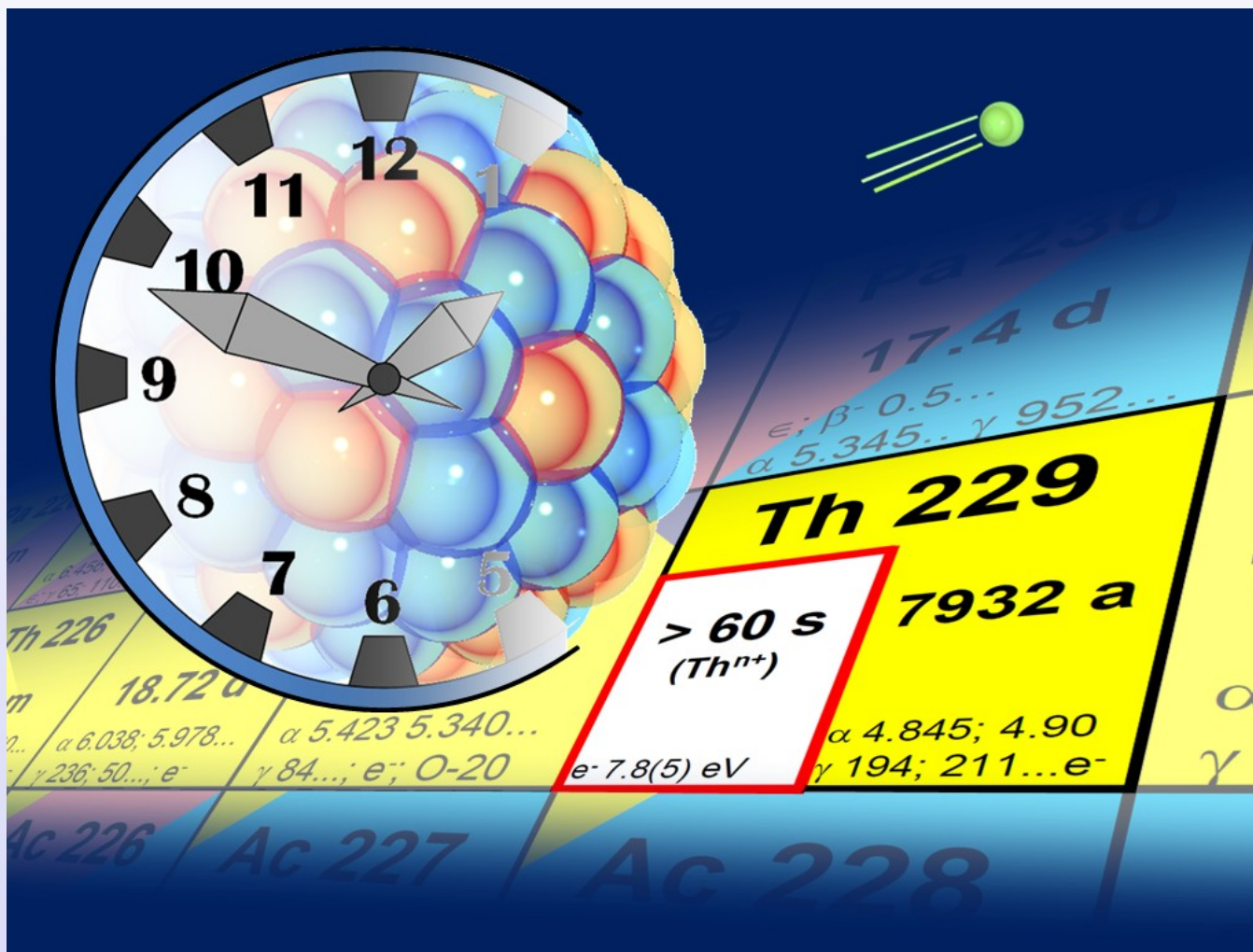


- laser interaction with ^{229}Th ions extracted from QMS
- measurement campaign started



- successful experimental approach based on spatial decoupling of population and deexcitation via buffer-gas stopping cell
- efficient extraction of pure $^{229\text{m}}\text{Th}^{2,3+}$ ions achieved
- VUV optical detection system was designed and commissioned
- radiative decay channel in neutral $^{229\text{m}}\text{Th}$ drastically reduced (in favor of IC)
- IC decay channel provided first direct (and unambiguous) identification of isomeric ground-state transition in $^{229\text{m}}\text{Th}$
- constraints of $^{229\text{m}}\text{Th}$ properties: $6.3 \text{ eV} \leq E^* \leq 18.3 \text{ eV}$
 $\tau > 60 \text{ s}$
- next steps: determination of half-life for neutral ^{229}Th
towards determination of isomeric excitation energy
(magnetic bottle spectrometer)
- started: setup of cryogenic Paul trap
 - to achieve longer storage times for half-life measurement in charged $^{229\text{m}}\text{Th}$
 - prerequisite also for laser manipulation of $^{229\text{m}}\text{Th}^{3+}$

we made a big step towards the ultimate goal of a Nuclear Clock



but many more are yet to come

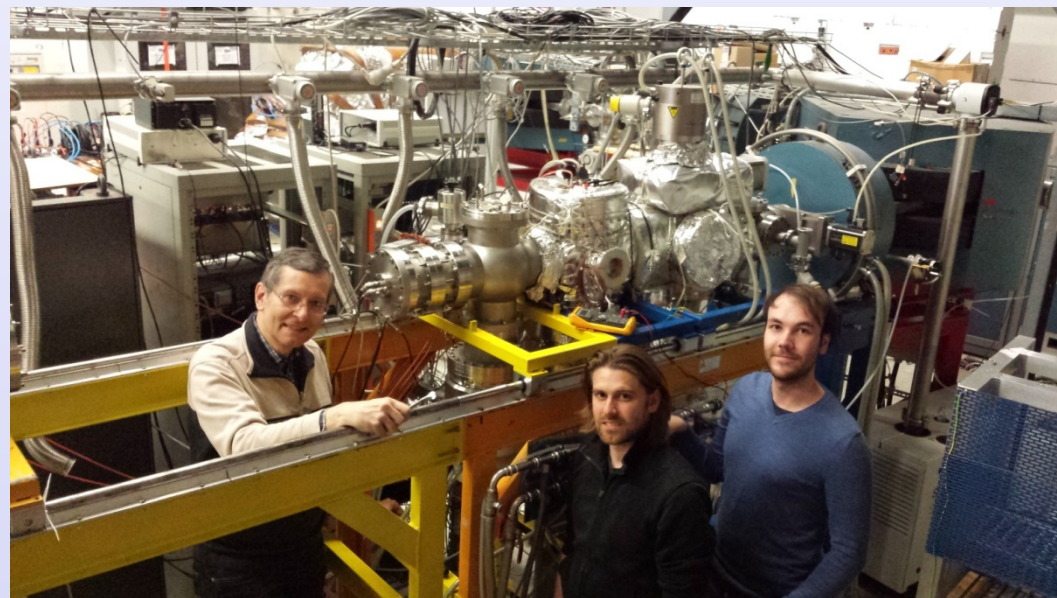
Thanks to



LMU Munich: L. v.d. Wense, B. Seiferle, J.B. Neumayr, H.-J. Maier, H.-F. Wirth,
D. Habs

GSI Helmholtzzentrum f. Schwerionenforschung, Darmstadt & Helmholtz-Institut Mainz:
M. Laatiaoui

Helmholtz-Institut Mainz & Johannes Gutenberg-Universität Mainz:
C. Mokry, J. Runke, K. Eberhardt, C.E. Düllmann, N.G. Trautmann



Thank you for your attention !