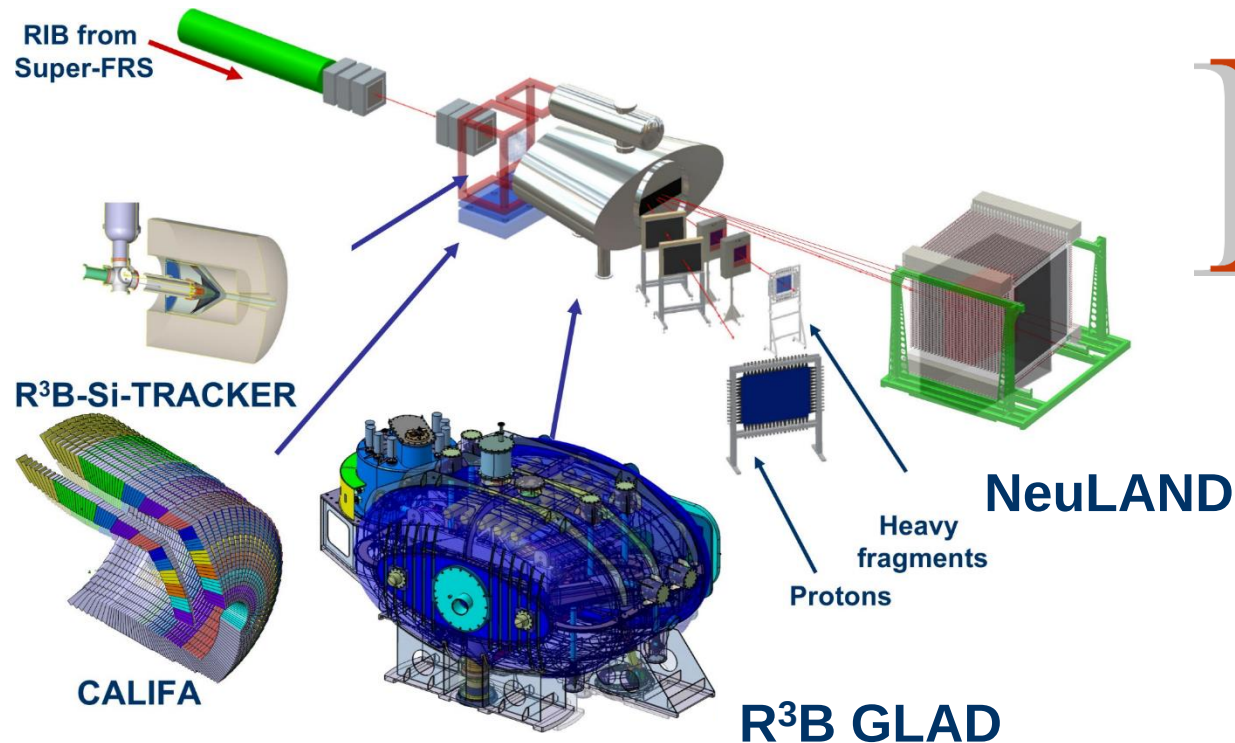


Dipole response and constraints on the nuclear equation of state



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Dominic Rossi



- Introduction
 - What is the Equation of State of nuclear matter?
 - Why measure low-lying E1 strength?
 - Why measure it in ^{68}Ni ?
- Experimental method:
 - Measuring E1 strength in unstable nuclei
 - R³B-LAND setup at GSI
- Results
 - E1 strength in ^{68}Ni
 - Dipole polarizability
 - Neutron-skin thickness of ^{68}Ni and ^{208}Pb
- Outlook
- Summary

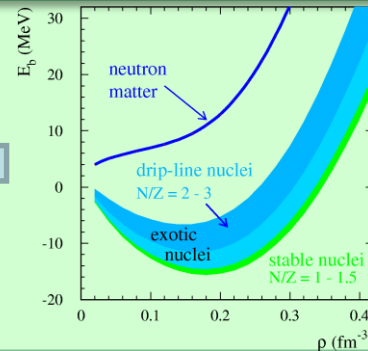
Why measure low-lying E1 strength?

Low-lying E1 strength

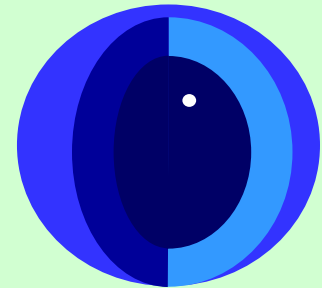
Dipole polarizability

$$\alpha_D = \frac{\hbar c}{2\pi^2} \int_0^\infty \omega^{-2} \sigma_\gamma(\omega) d\omega$$

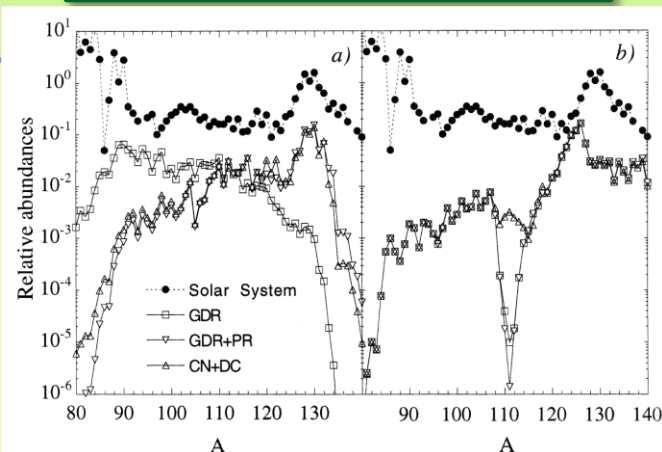
Equation of State



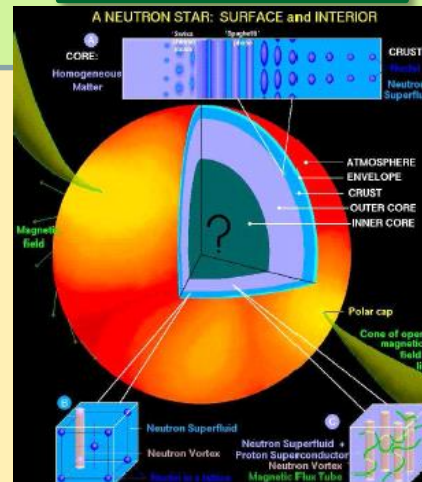
Neutron skin



Nucleosynthesis



Neutron star



S. Goriely, Phys. Lett. B **436**(1-2), 10-18 (1998)

Nuclear Equation of State: basics

- At the beginning: liquid-drop formula (Bethe and Weizsäcker)

$$B(Z, N) = a_V A - a_S A^{2/3} - a_C \frac{Z^2}{A^{1/3}} - a_A \frac{(N - Z)^2}{A} + \dots$$

- Then, one defines the binding energy per nucleon (in the thermodynamic limit)

$$\varepsilon(\alpha) = -\frac{B(Z, N)}{A} = -a_V + a_A \frac{(N - Z)^2}{A^2} = -a_V + J\alpha^2$$

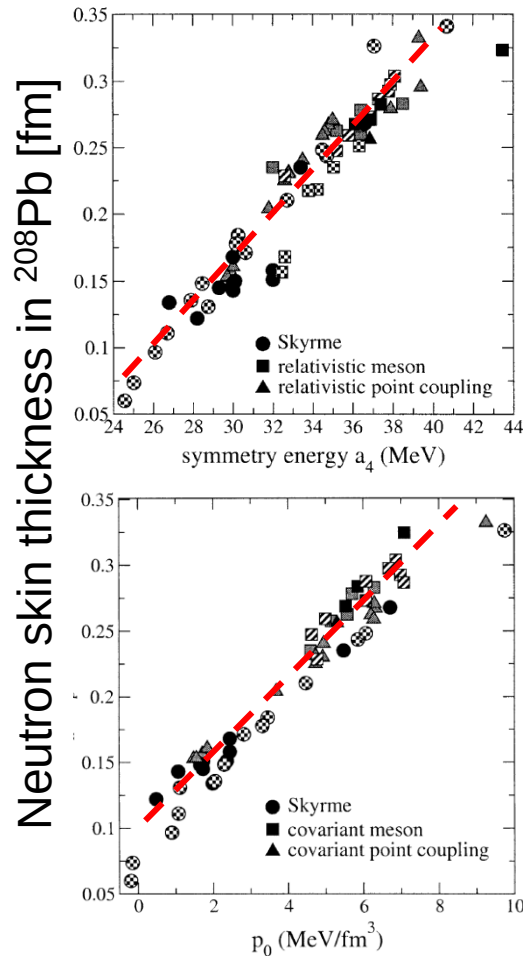
- Nuclear matter is not incompressible $\rightarrow$ density dependence $\rightarrow \varepsilon(\alpha) \rightarrow E(\rho, \alpha)$

$$E(\rho, \alpha) = E(\rho, 0) + S_2(\rho)\alpha^2 + \dots$$

- This is a possible expression of the Equation of State of nuclear matter

C. Horowitz, *et al.*, JPG 41, 093001 (2014)

Nuclear Equation of State: symmetry energy



$$E(\rho, \alpha) = E(\rho, 0) + S_2(\rho)\alpha^2 + O(\alpha^4), \quad \alpha = \frac{N-Z}{A}$$

$$E(\rho, 0) = -a_v + \frac{K_0}{18\rho_0^2}(\rho - \rho_0)^2 + \dots$$

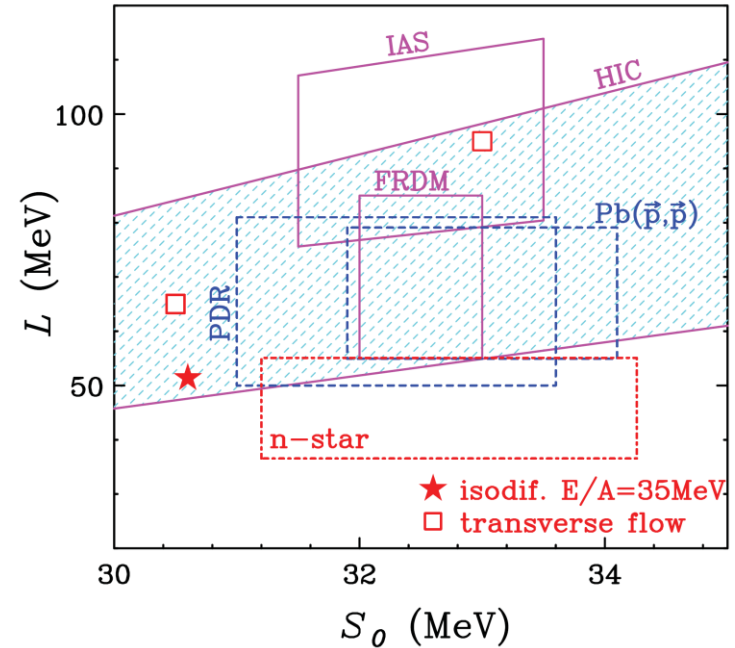
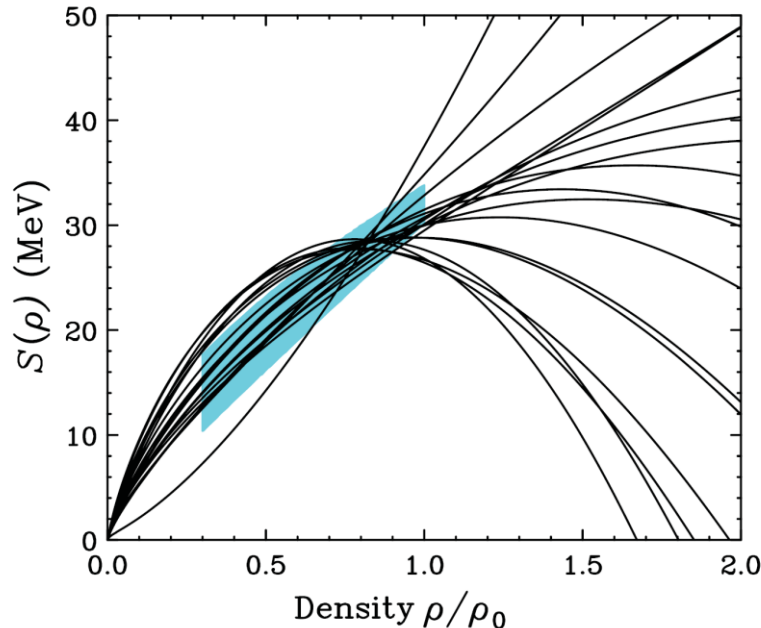
$$S_2(\rho) = \frac{1}{2} \frac{\partial^2 E(\rho, \alpha)}{\partial \alpha^2} \Big|_{\alpha=0} = a_4 + \frac{p_0}{\rho_0^2}(\rho - \rho_0) + \frac{\Delta K_0}{18\rho_0^2}(\rho - \rho_0)^2 + \dots$$

$$a_4 \rightarrow J$$

$$p_0 \rightarrow S'(\rho)|_{\rho=\rho_0} = \frac{L}{3\rho_0}$$

- a_4 : symmetry energy
- p_0 : symmetry energy pressure $\rightarrow$ density dependence
- Linear correlation between neutron skin thickness and a_4 and p_0 parameters of nuclear Equation of State for various mean-field models for ^{208}Pb case

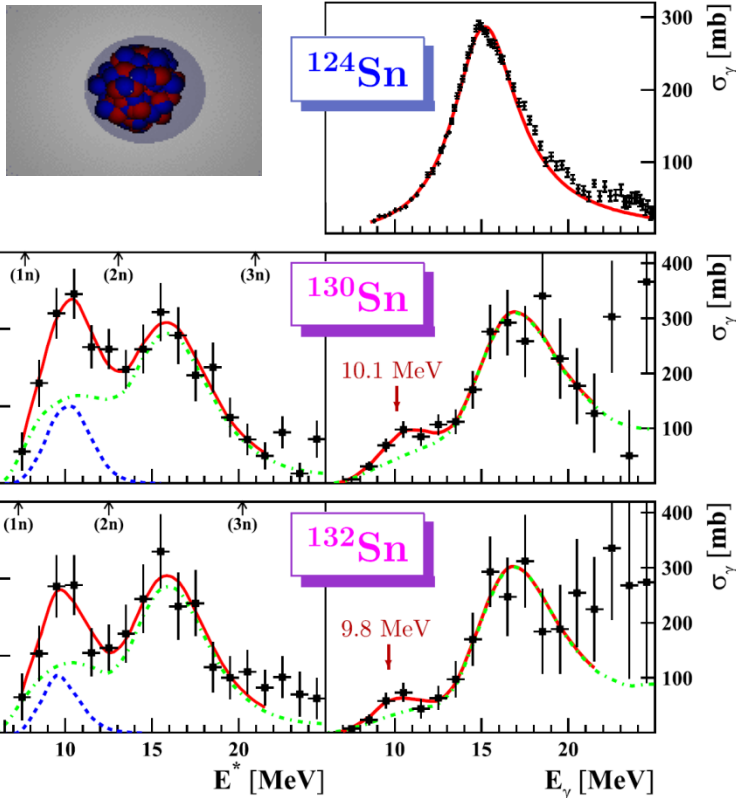
Nuclear Equation of State: symmetry energy



- Density dependence of the symmetry energy is not well constrained
- Experimental data is necessary to provide constraints as tight as possible
- Results from various types of probing of nuclear matter are combined to provide best possible set of constraints

M.B. Tsang, *et al.*, PRC 86, 015803 (2012)

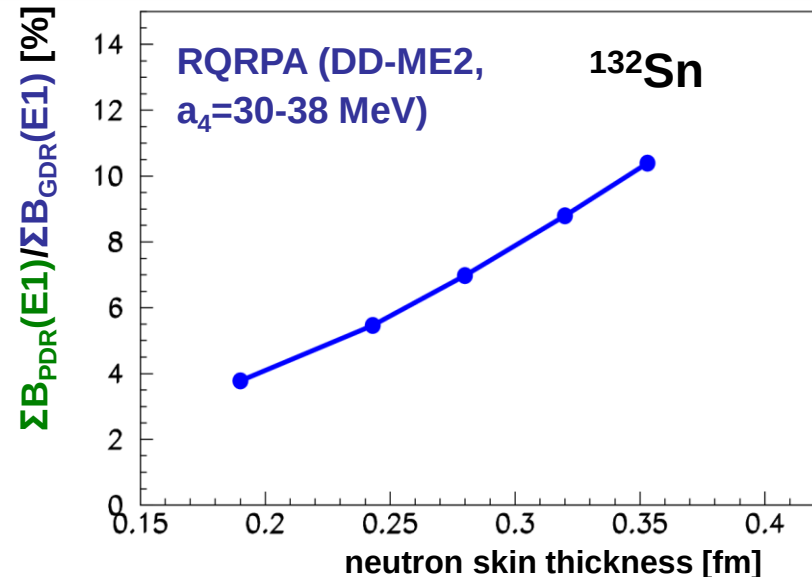
Measuring $\Delta R_{n,p}$ using low-lying E1 strength



P. Adrich *et al.*, PRL **95**, 132501 (2005)

GDR $\rightarrow$ Breit-Wigner
PDR $\rightarrow$ Gaussian

- RQRPA calculations provide correlation between the measured PDR strength and the neutron skin thickness



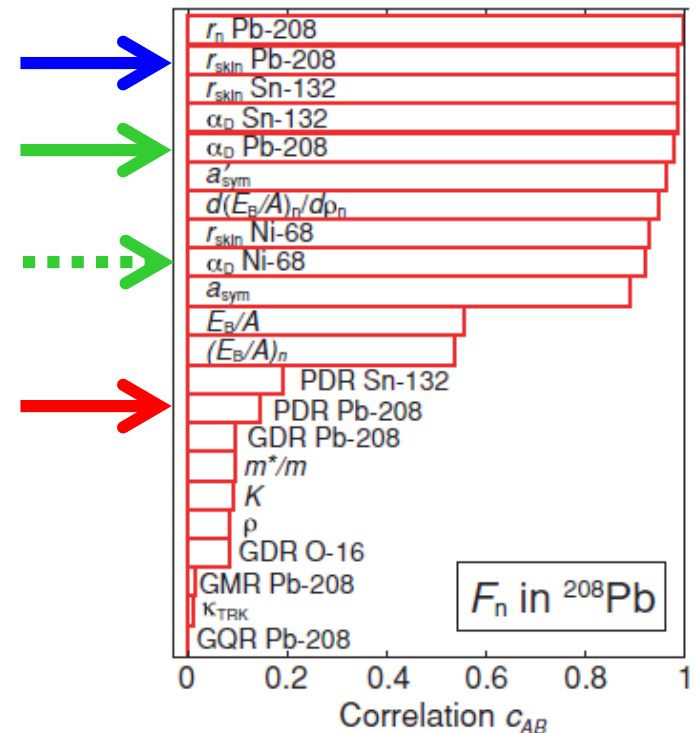
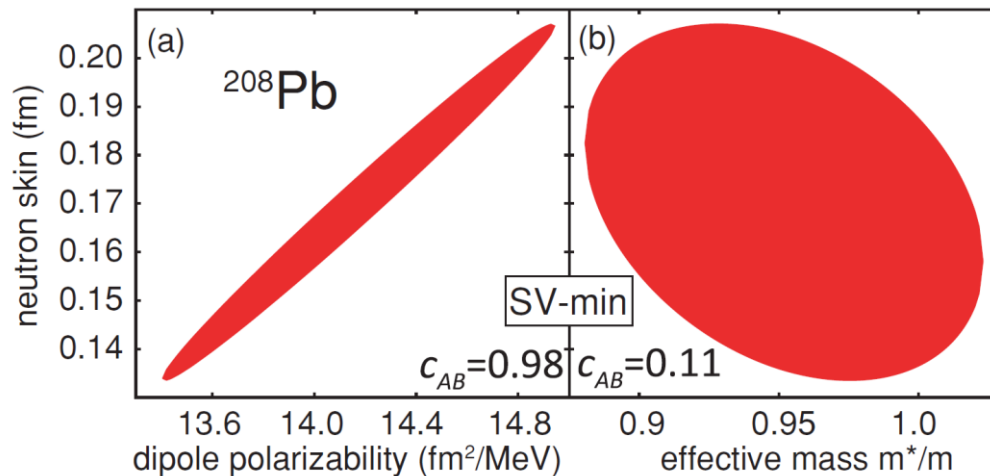
- Requires assumption of a specific line-shape of PDR and GDR
- Photoabsorption c.s. not very sensitive to low-lying E1 strength

Selecting a better observable for $\Delta R_{n,p}$

PHYSICAL REVIEW C 81, 051303(R) (2010)

Information content of a new observable: The case of the nuclear neutron skin

P.-G. Reinhard¹ and W. Nazarewicz^{2,3,4,5}



Dipole polarizability of ^{208}Pb

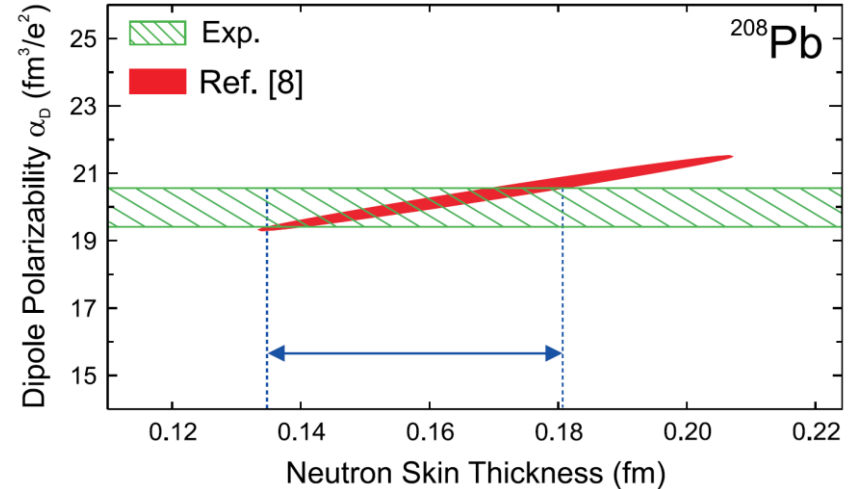
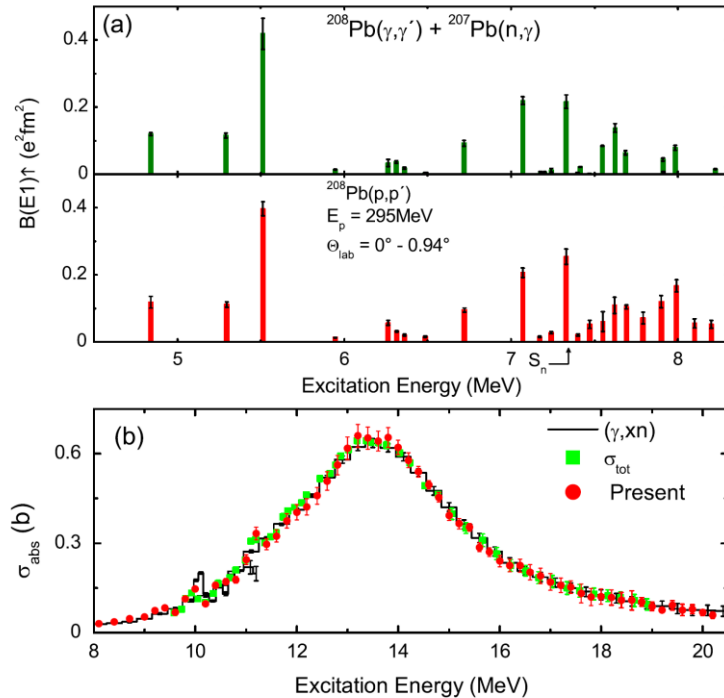
PRL **107**, 062502 (2011)

PHYSICAL REVIEW LETTERS

week ending
5 AUGUST 2011

Complete Electric Dipole Response and the Neutron Skin in ^{208}Pb

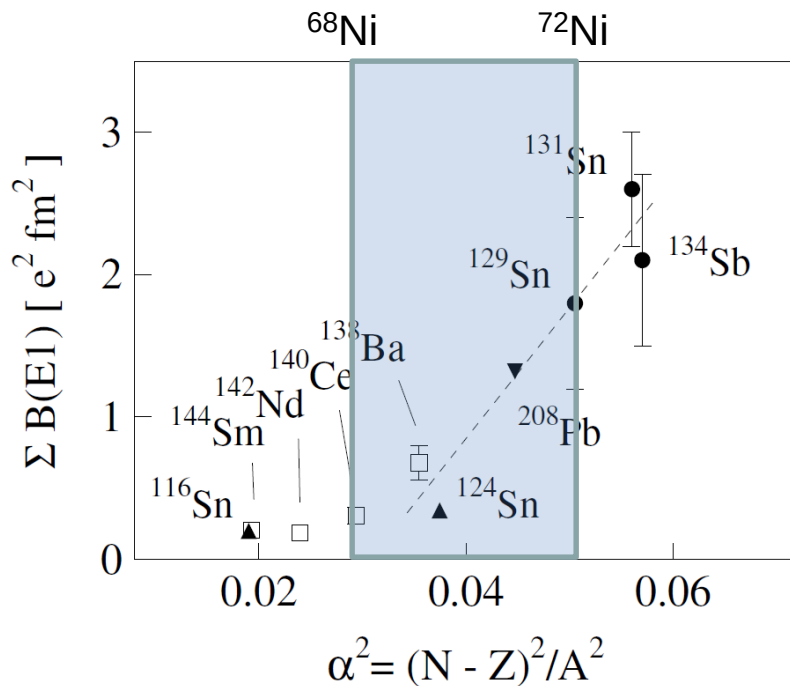
A. Tamii,¹ I. Poltoratska,^{2,*} P. von Neumann-Cosel,^{2,*} Y. Fujita,³ T. Adachi,^{3,4} C. A. Bertulani,⁵ J. Carter,⁶ M. Dozono,⁷ H. Fujita,¹ K. Fujita,⁷ K. Hatanaka,¹ D. Ishikawa,¹ M. Itoh,⁸ T. Kawabata,⁹ Y. Kalmykov,² A. M. Krumbholz,² E. Litvinova,^{10,11} H. Matsubara,¹² K. Nakanishi,¹² R. Neveling,¹³ H. Okamura,¹ H. J. Ong,¹ B. Özel-Tashenov,¹⁰ V. Yu. Ponomarev,² A. Richter,^{2,14} B. Rubio,¹⁵ H. Sakaguchi,¹ Y. Sakemi,⁸ Y. Sasamoto,¹² Y. Shimbara,^{3,16} Y. Shimizu,¹⁷ F. D. Smit,¹³ T. Suzuki,¹ Y. Tameshige,¹⁸ J. Wambach,² R. Yamada,¹⁶ M. Yosoi,¹ and J. Zenihiro¹



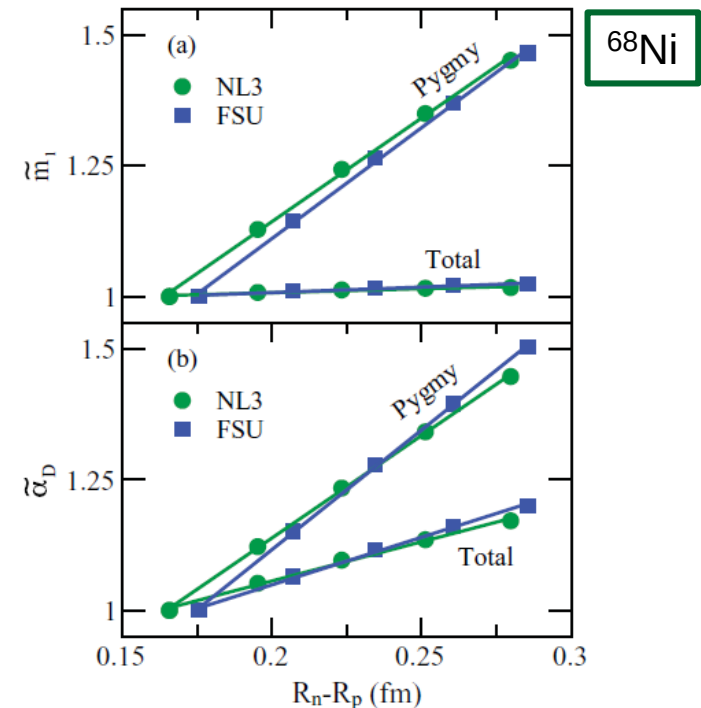
Measured α_D up to 20 MeV: $18.9(13) \text{ fm}^3/\text{e}^2$
 Extrapolated value up to 130 MeV: $20.1(6) \text{ fm}^3/\text{e}^2$
 $\Rightarrow r_{\text{skin}} = 0.156^{+0.025}_{-0.021} \text{ fm}$

Why measure dipole polarizability in ^{68}Ni ?

- Cover large asymmetry window within given mass range
- Larger sensitivity of $\Delta R_{n,p}$ on α_D than in ^{208}Pb
- Measurement of evolution of E1 strength within isotopic chain $\rightarrow$ isospin dependence

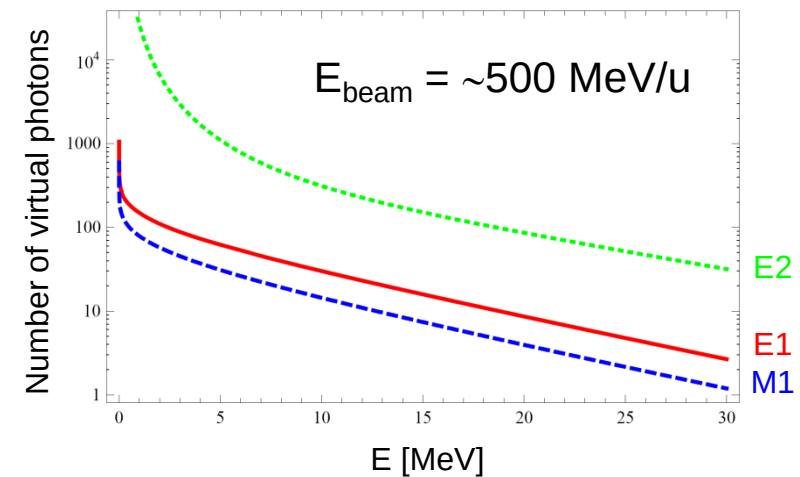
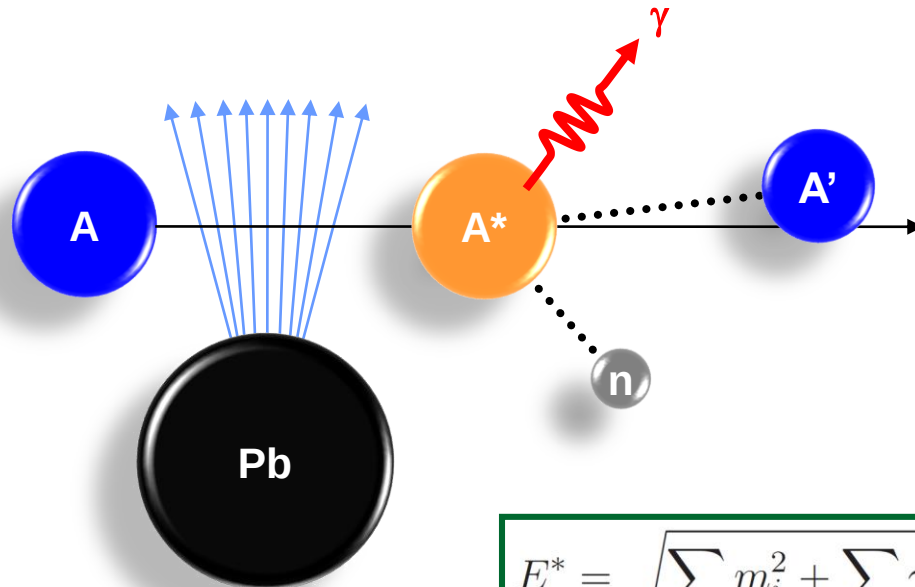


A. Klimkiewicz *et al.*, PRC **76**, 051603(R) (2007)



J. Piekarewicz, PRC **83**, 034319 (2011)

Measuring E1 strength in unstable nuclei

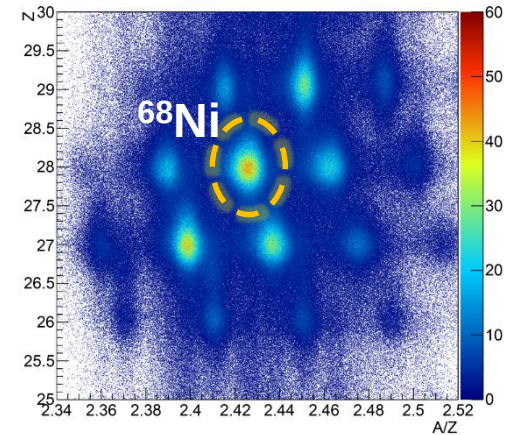
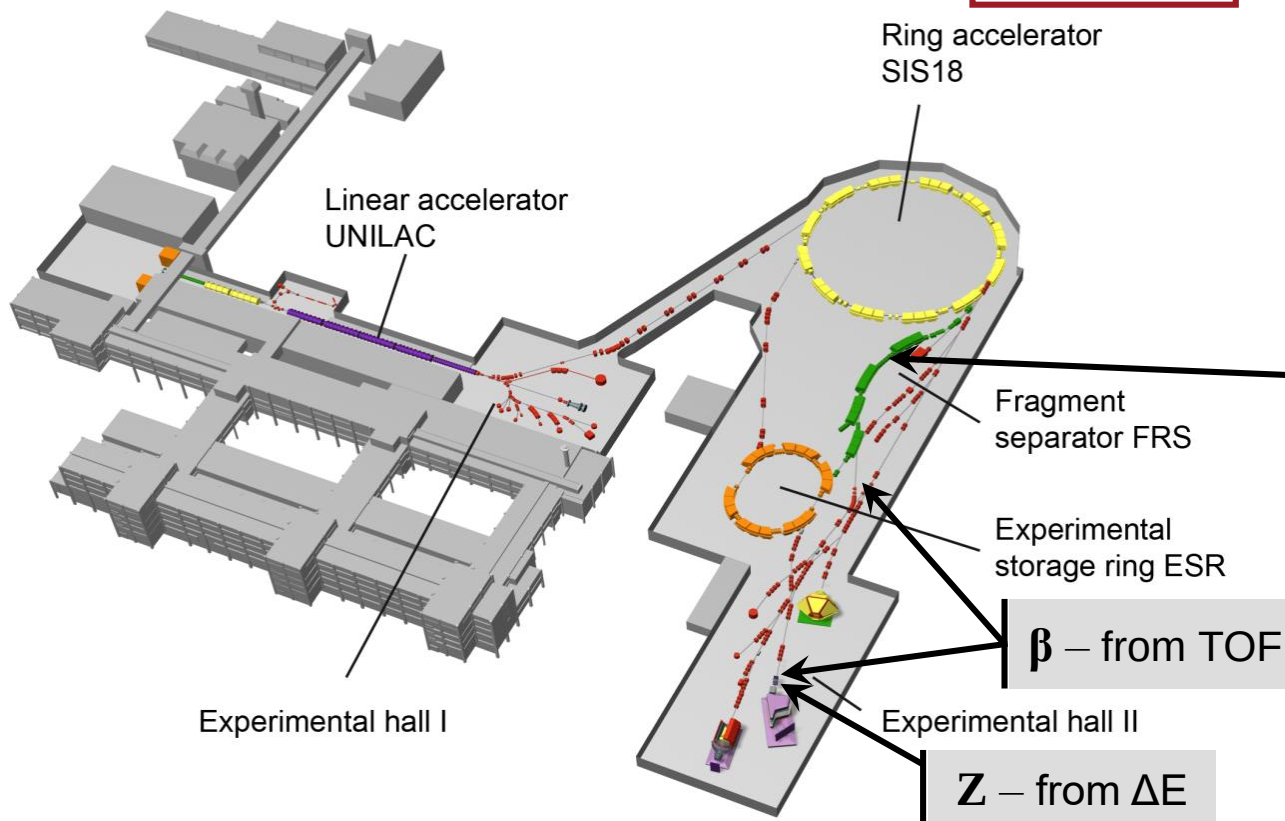


$$E^* = \sqrt{\sum_i m_i^2 + \sum_{i \neq j} \gamma_i \gamma_j m_i m_j (1 - \beta_i \beta_j \cos \vartheta_{ij})} + E_\gamma - m_{\text{proj}}$$

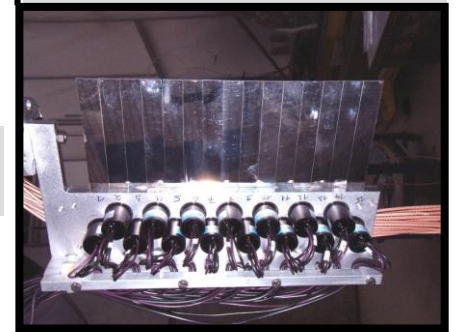
- Short lifetime of projectile → requires experiment in **inverse kinematics**
- Heavy-ion-induced **electromagnetic excitation**, via the virtual photon approach
- Reconstruction of excitation energy (using invariant mass) of each event requires detection of **ALL** participating species (identification and momentum):
 - Requires high-efficiency and high-resolution neutron and gamma detectors (for n-rich nuclei)

GSI experimental facility

$$\frac{A}{Z} = \frac{e}{m_u c} \frac{B\rho}{\beta\gamma}$$

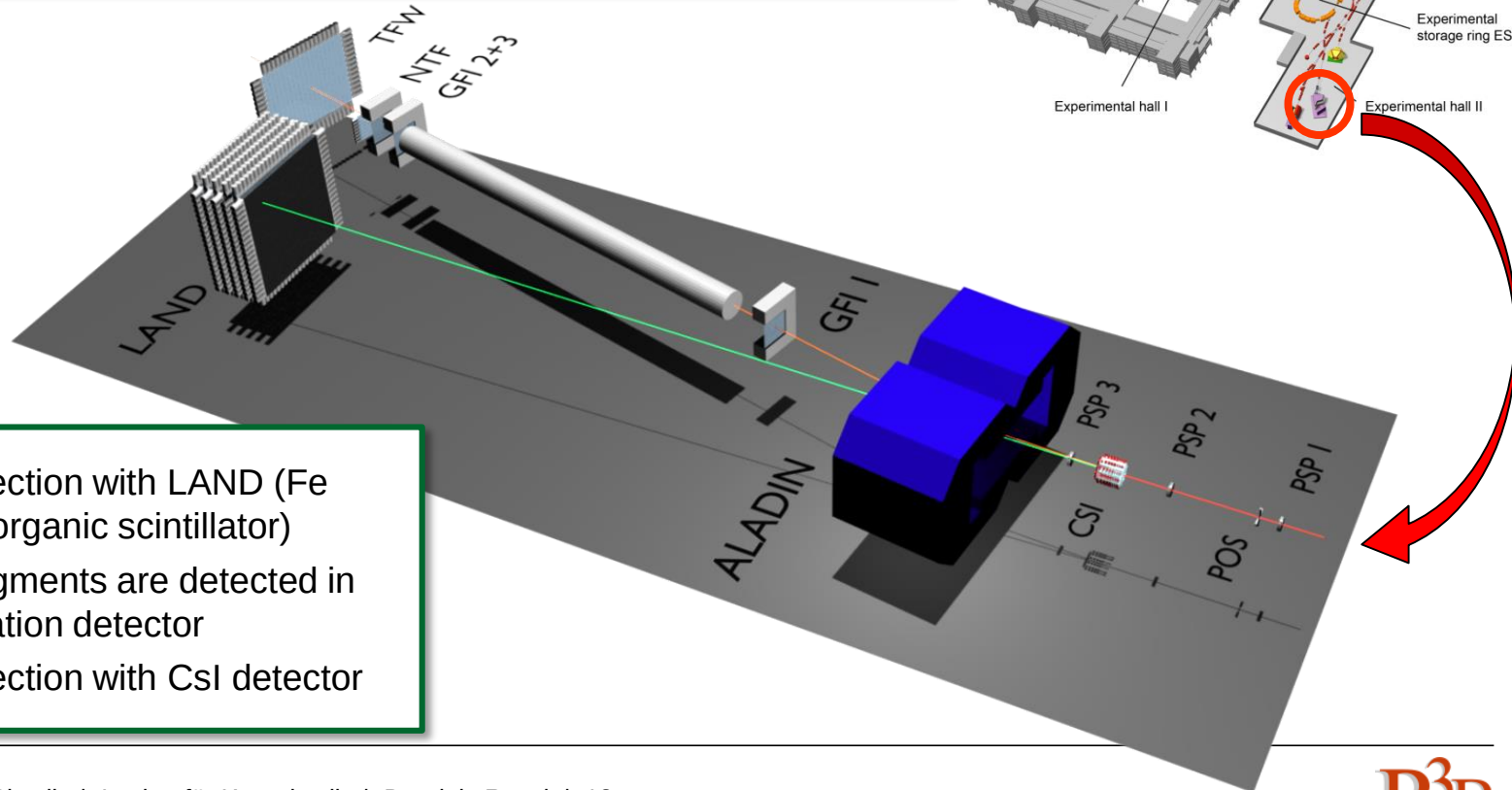
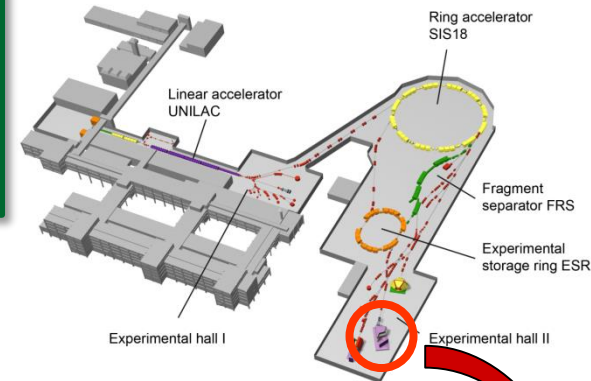


$B\rho$ – from position at
middle focal plane
of the FRS



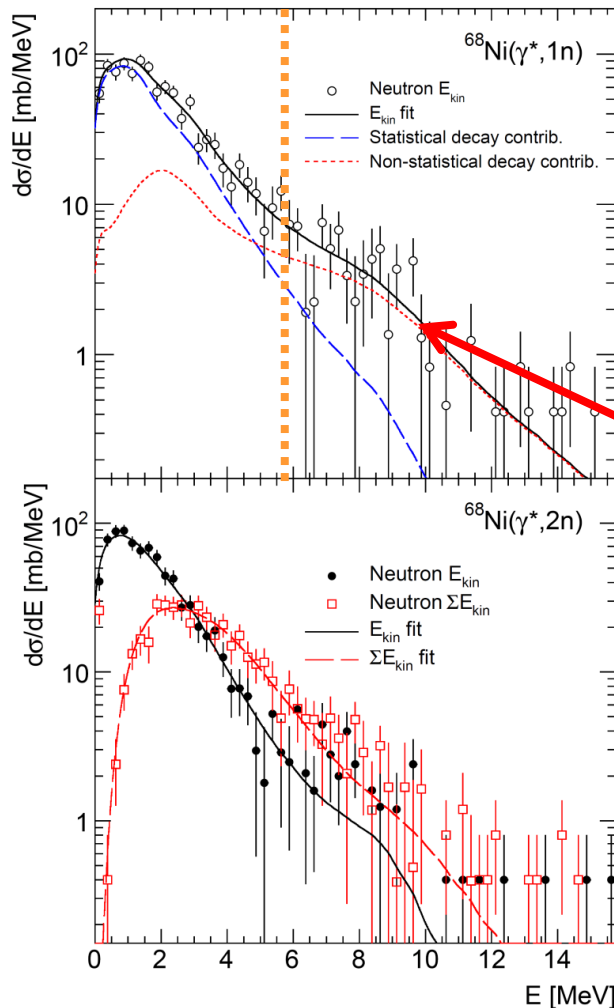
R³B-LAND setup

- Kinematic forward-focusing (relativistic beam energies)
→ high-acceptance measurement (almost full solid angle covered)
- Beam tracking in Cave C: Si detectors (PSP) and scintillation detectors (POS, GFI, TFW)

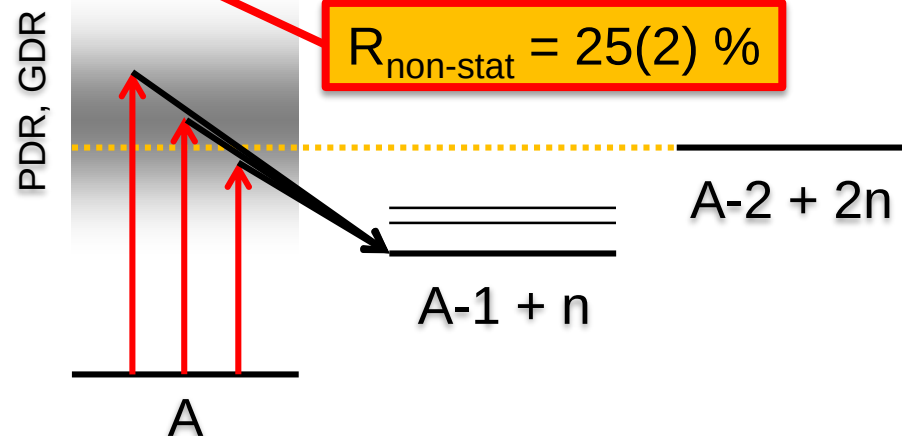


- Neutron detection with LAND (Fe converter + organic scintillator)
- Charged fragments are detected in TFW scintillation detector
- Gamma detection with CsI detector

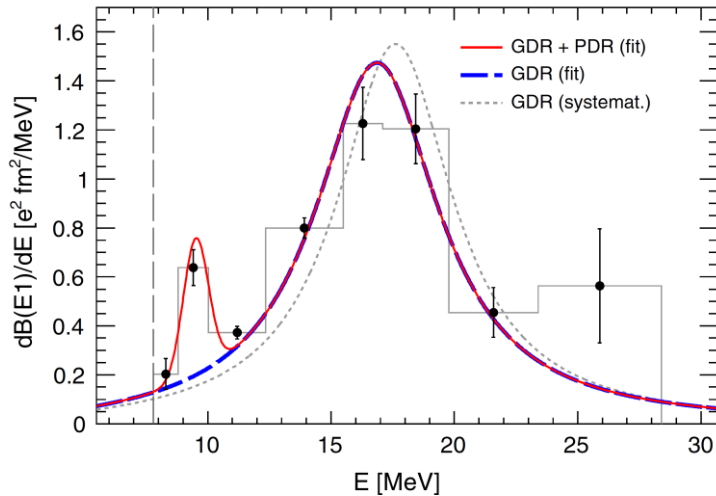
Reconstructing E^* : neutrons



- Neutron kinetic energies reach well beyond the 2n threshold (dotted orange line)
→ Not expected with statistical decay
- Only decay to the vicinity of the A-1 ground state was considered
- Non-statistical decay branching ratio obtained from fit to neutron energies



Low-lying E1 strength in ^{68}Ni



PRL **111**, 242503 (2013)

PHYSICAL REVIEW LETTERS

week ending
13 DECEMBER 2013

Measurement of the Dipole Polarizability of the Unstable Neutron-Rich Nucleus ^{68}Ni

D.M. Rossi, *et al.*

- One-step GDR+PDR fit to „deconvoluted“ data
- Comparison of fit result with RISING data

PDR in ^{68}Ni	(γ^*, xn)	(γ^*, γ')
E_m [MeV]	9.55(17)	11.0(5)
σ [MeV]	0.51(13)	< 1
S_{TRK} [%]	2.8(5)	-

$$\frac{d\sigma_{E1}}{dE_\gamma} = \sigma^{\text{exc}} * R_\gamma = \left(\frac{1}{E_\gamma} N \sigma^{\text{abs}} \right) * R_\gamma$$

$$R_\gamma (\text{PDR}) \approx 4 \% \rightarrow S_{\text{TRK}} \approx 5 \%$$

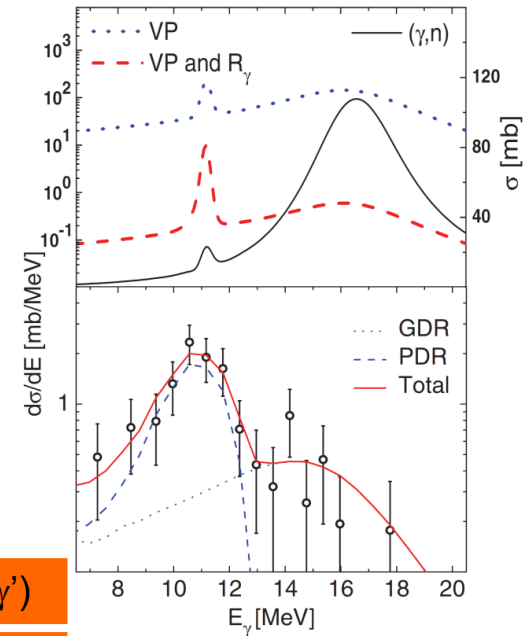
PRL **102**, 092502 (2009)

PHYSICAL REVIEW LETTERS

week ending
6 MARCH 2009

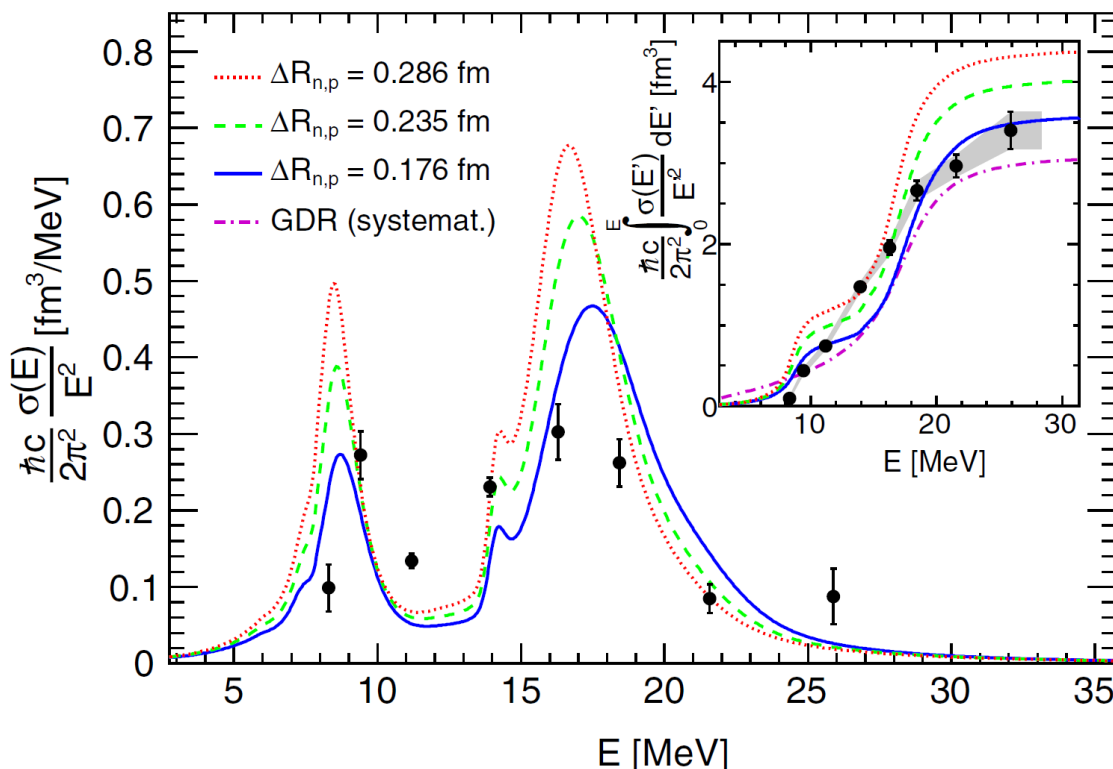
Search for the Pygmy Dipole Resonance in ^{68}Ni at 600 MeV/nucleon

O. Wieland, *et al.*



^{68}Ni
 (γ^*, γ')

Dipole polarizability in ^{68}Ni



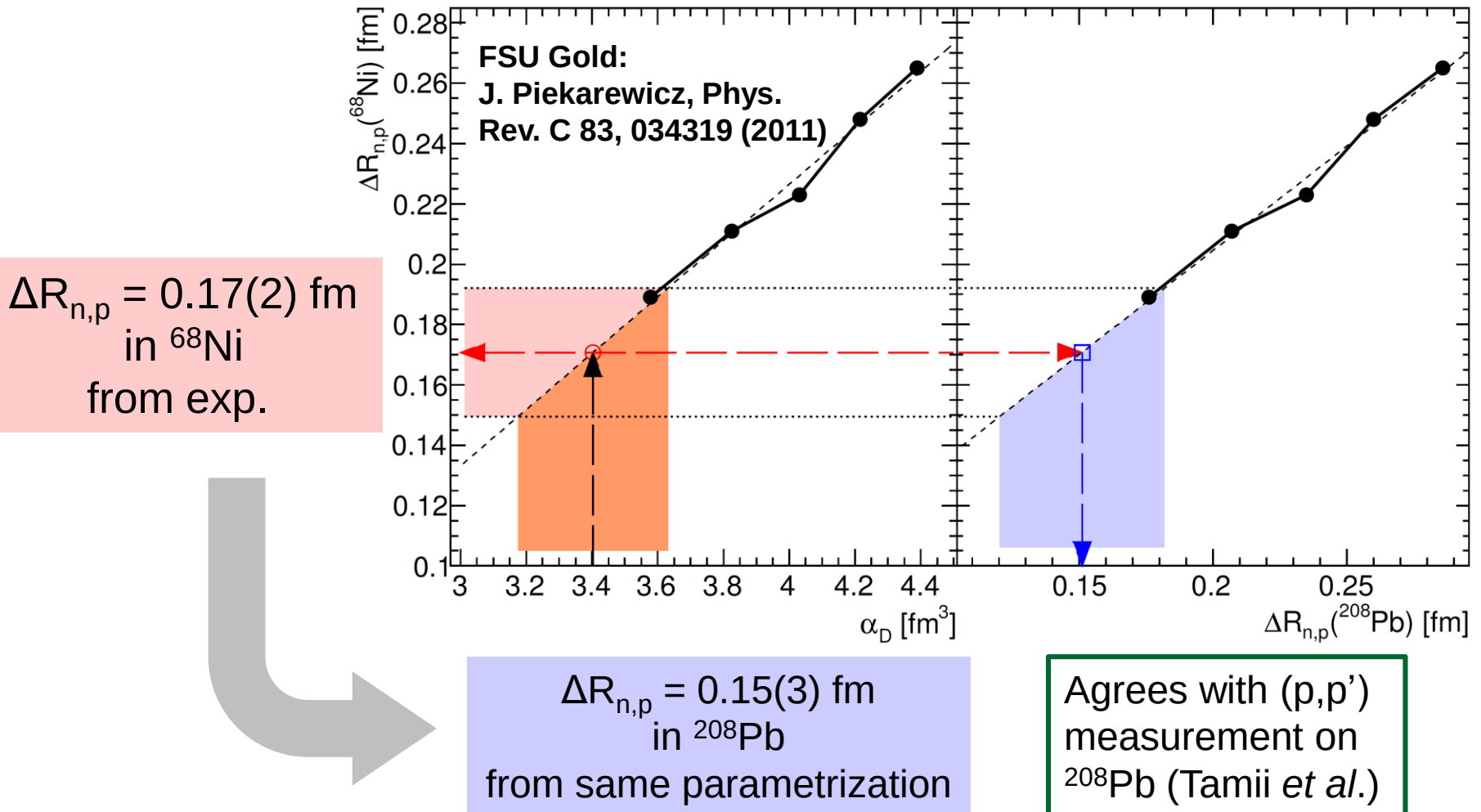
D.M. Rossi, *et al.*, PRL 111, 242503 (2013)

- Extraction of dipole polarizability from inverse energy-weighted dipole response
- Experimental data compared to FSUGold RMF calculations (Piekarewicz, PRC 83, 034319 (2011)), as well as GDR alone
- ➔ Significant enhancement when compared to GDR
- Theory “adjusted” to account for experimental integration limits (7.792 to 28.4 MeV) and resolution (→ Gaussian smearing)

Neutron-skin thickness of ^{68}Ni



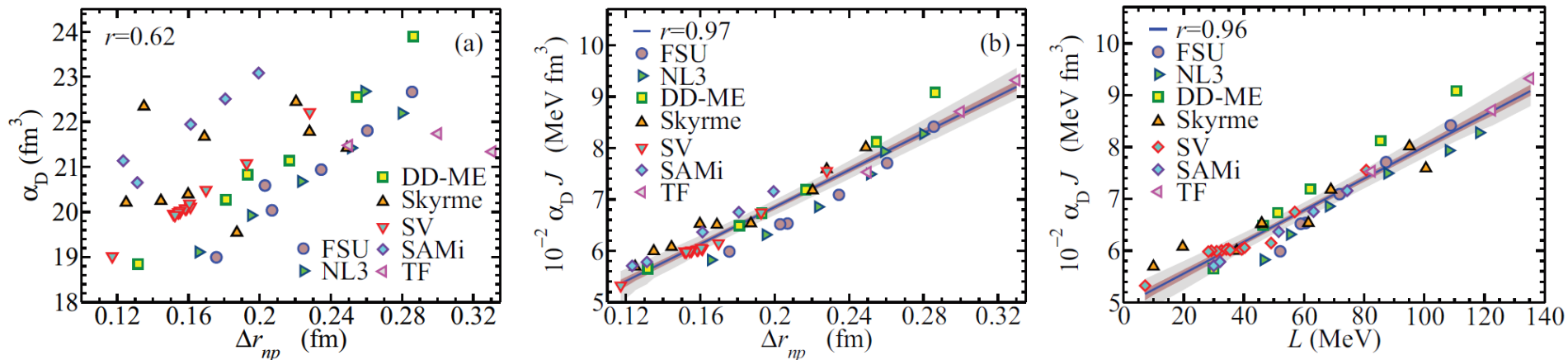
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Strategy to extract EOS parameters

^{208}Pb

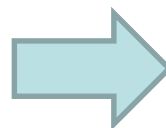
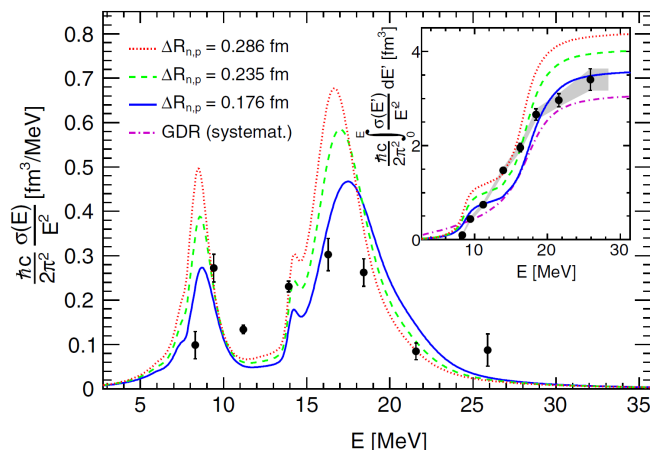
$$\alpha_D^{\text{DM}} \approx \frac{\pi e^2}{54} \frac{A \langle r^2 \rangle}{J} \left[1 + \frac{5}{2} \frac{\Delta r_{np}^{\text{DM}}}{I \langle r^2 \rangle^{1/2}} \right]$$



X. Roca-Maza, et al., PRC 88, 024316 (2013)

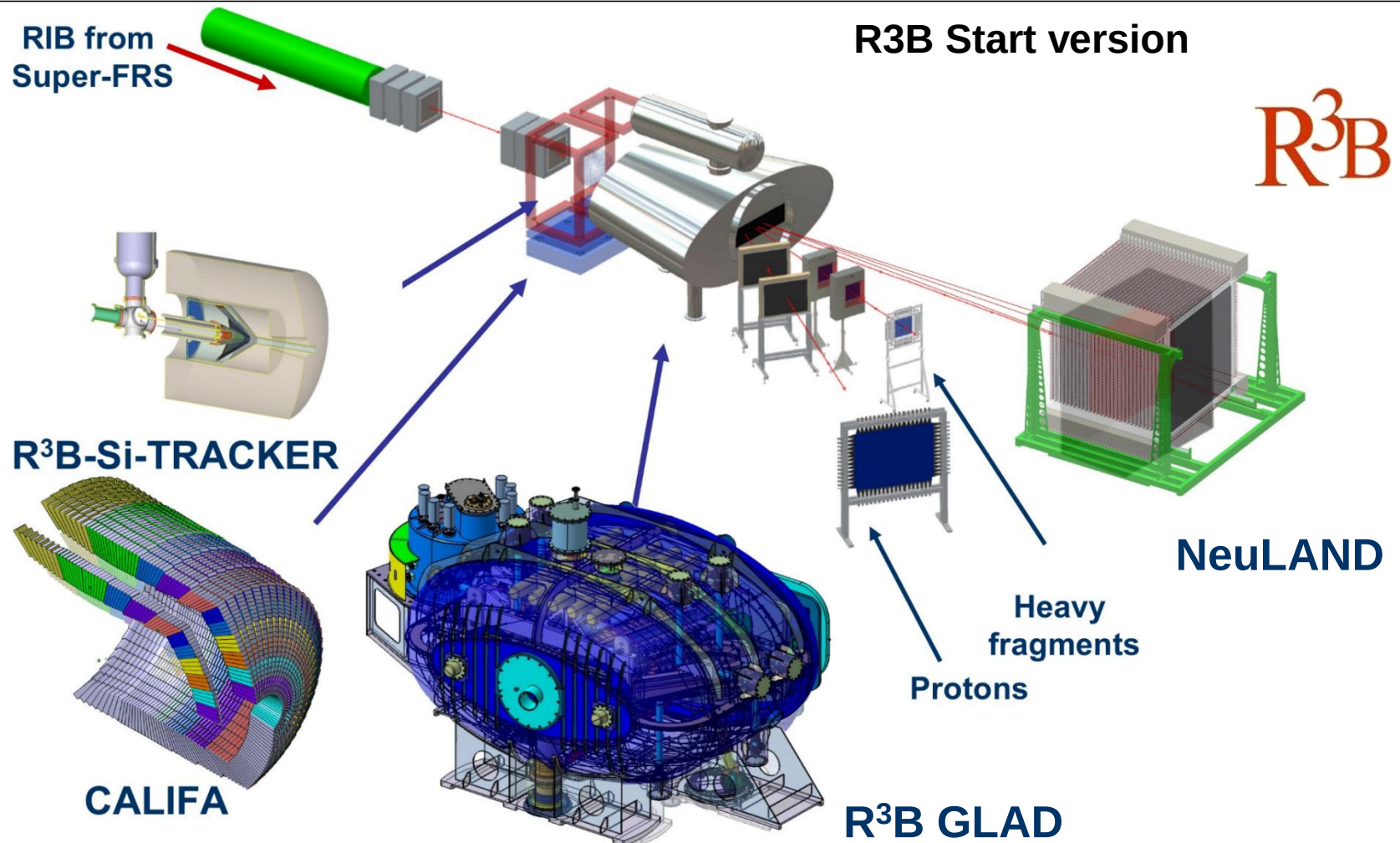
- Stronger linear correlation between models when $\alpha_D \cdot J$ is used instead of α_D
- Possibility to extract EOS parameters using various models

Outlook: determine full α_D for ^{68}Ni

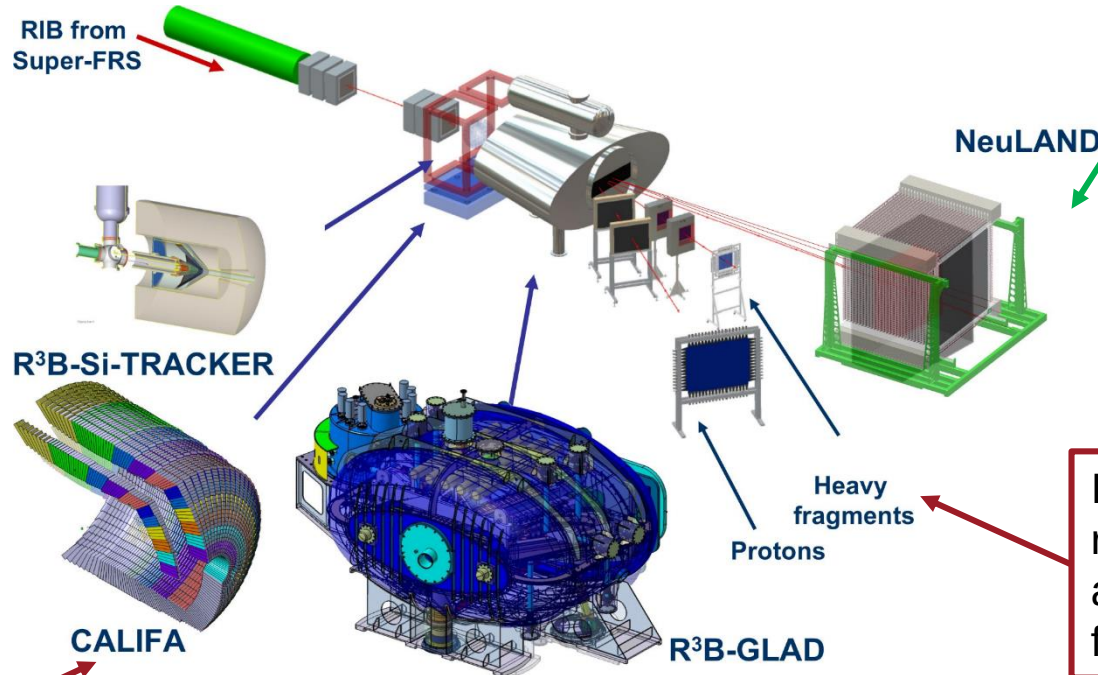


- Expand integration range from 7.792-28.4 MeV to 0-140 MeV
- Use Breit-Wigner tails from fit to data to extrapolate E1 strength beyond measurement range
- Reflect extrapolation in total error

Future setup: R³B



Future setup: R³B



Higher multi-neutron detection efficiency (63% for 4n at 1 GeV); better resolution ($\Delta p/p \approx 10^{-3}$)

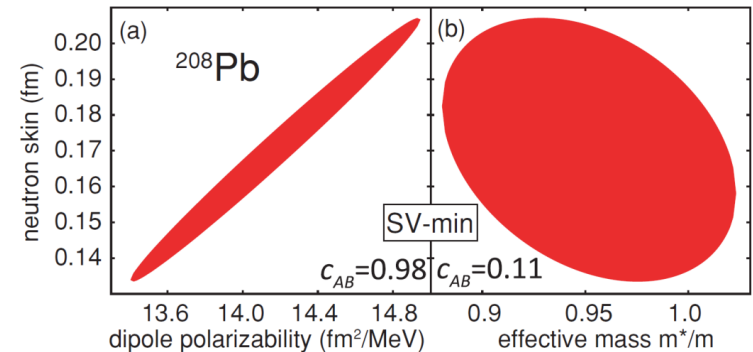
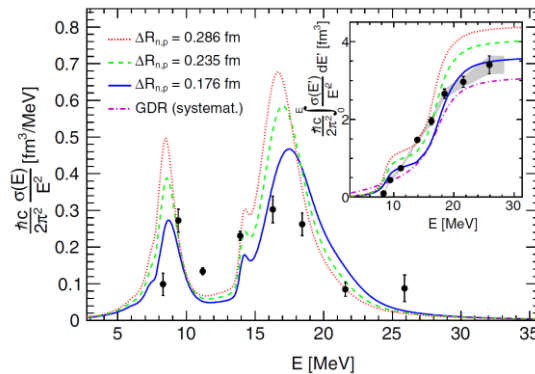
Improved $\sigma_{\Delta E}$ and σ_t , resulting in a better Z and A identification of fragments

Highest possible calorimetric efficiency required

Allows for beams up to 15 Tm (bending of 18°) already in Cave C (e.g., ~ 1.1 GeV/u ^{68}Ni !)

Summary

- Use of dipole polarizability instead of E1 strength to extract EOS parameters due to better parameter correlations



- Dipole polarizability of ⁶⁸Ni was measured successfully
- Neutron-skin thicknesses of ⁶⁸Ni and ²⁰⁸Pb in good agreement

- Ongoing work:
 - Full dipole polarizability of ⁶⁸Ni → extraction of EOS parameters
 - Dipole polarizabilities of ⁷⁰⁻⁷²Ni
 - Analysis of n-rich Sn isotopes (on both sides of neutron threshold)

Measurement of the Dipole Polarizability of the Unstable Neutron-Rich Nucleus ^{68}Ni

D. M. Rossi,^{1,2,*} P. Adrich,¹ F. Aksouh,^{1,†} H. Alvarez-Pol,³ T. Aumann,^{4,1,‡} J. Benlliure,³ M. Böhmer,⁵ K. Boretzky,¹
E. Casarejos,⁶ M. Chartier,⁷ A. Chatillon,¹ D. Cortina-Gil,³ U. Datta Pramanik,⁸ H. Emling,¹ O. Ershova,⁹
B. Fernandez-Dominguez,^{3,7} H. Geissel,¹ M. Gorska,¹ M. Heil,¹ H. T. Johansson,^{10,1} A. Junghans,¹¹ A. Kelic-Heil,¹
O. Kiselev,^{1,2} A. Klimkiewicz,^{1,12} J. V. Kratz,² R. Krücken,⁵ N. Kurz,¹ M. Labiche,^{13,14} T. Le Bleis,^{1,9,15} R. Lemmon,¹⁴
Yu. A. Litvinov,¹ K. Mahata,^{1,16} P. Maierbeck,⁵ A. Movsesyan,⁴ T. Nilsson,¹⁰ C. Nociforo,¹ R. Palit,¹⁷ S. Paschalis,^{4,7}
R. Plag,^{9,1} R. Reifarth,^{9,1} D. Savran,^{18,19} H. Scheit,⁴ H. Simon,¹ K. Sümmerer,¹ A. Wagner,¹¹ W. Waluś,¹²
H. Weick,¹ and M. Winkler¹