

Describing Gluons at zero and finite temperature

Axel Maas

31st of August 2009

Quarks, Hadrons, and the QCD Phase Diagram

St. Goar

Germany

Overview

- Describing **gluons** at **zero temperature**

Supported by the FWF

See: 0907.5185, 0810.1987, hep-lat/0702022,
hep-ph/0408074

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- Describing **gluons** at **zero temperature**
 - Fixing an **unambiguous gauge**
- **Gluons** at **finite temperature**
 - Resolving the Linde problem
 - Properties of gluons for $SU(2)$ and $SU(3)$

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Part I

Zero Temperature

Gauge freedom

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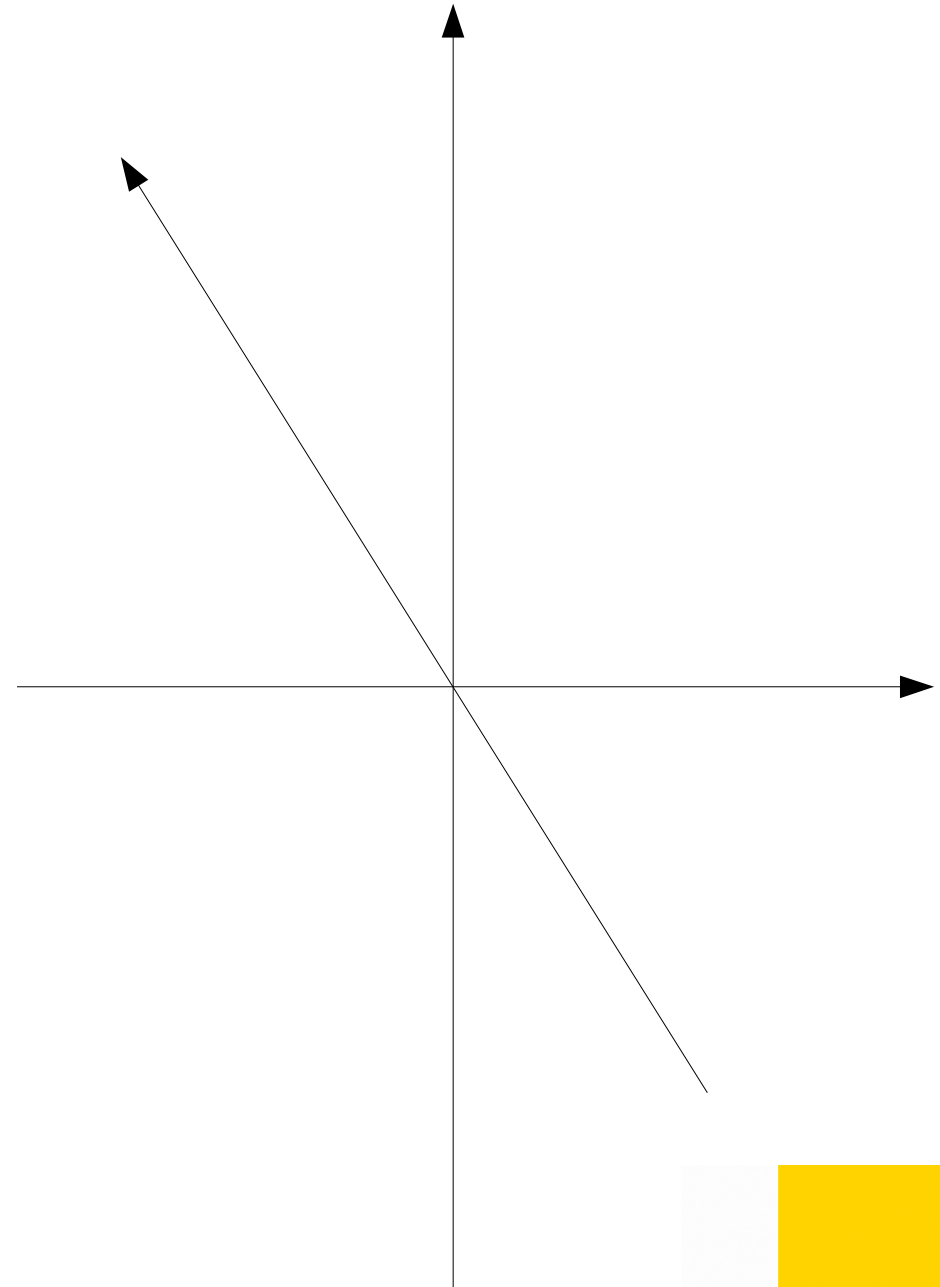
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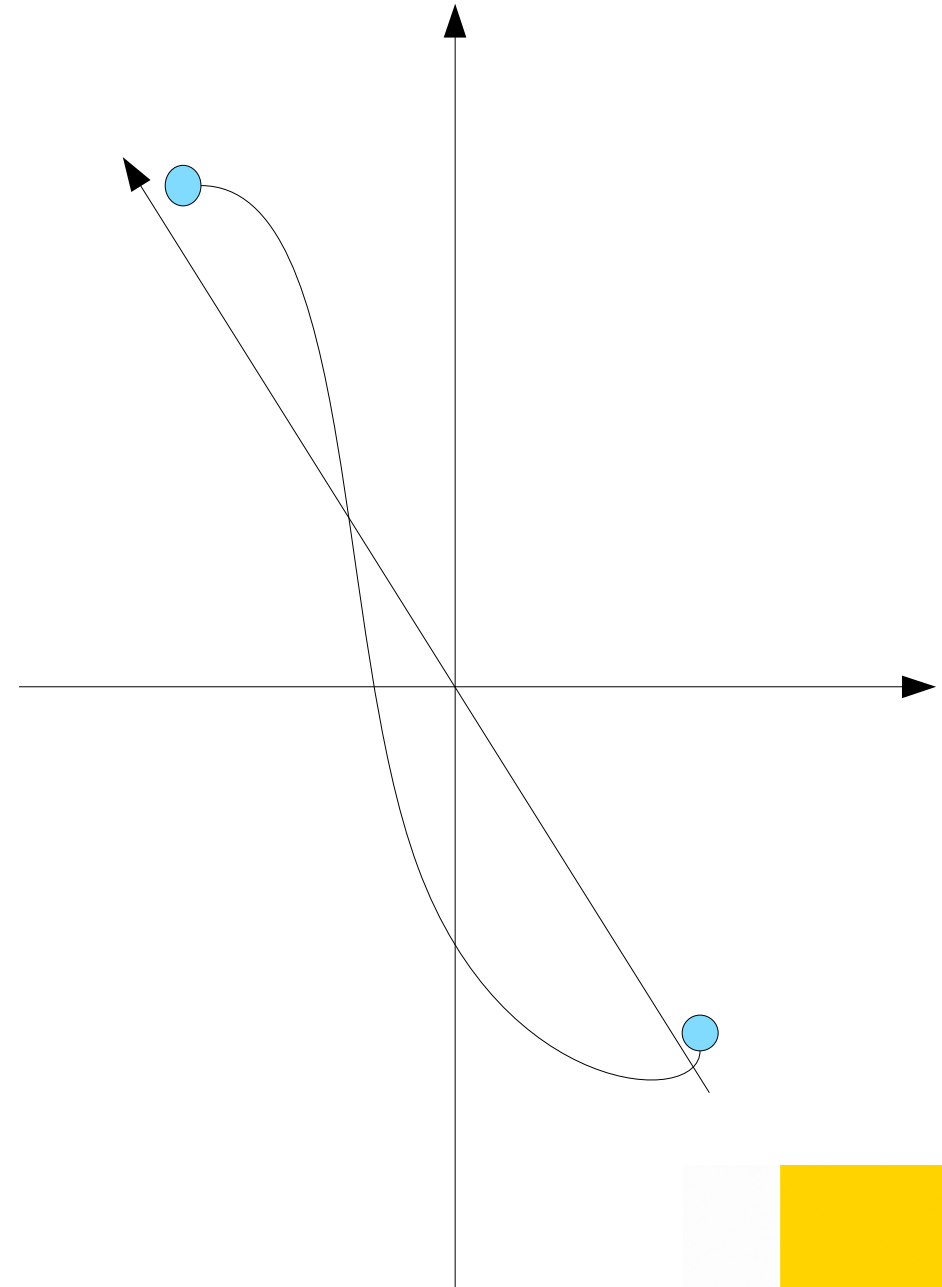
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- Describing **gluons requires gauge-fixing**
 - Comparison of different methods requires the same gauge fixing in all methods

Configuration space (artist's view)

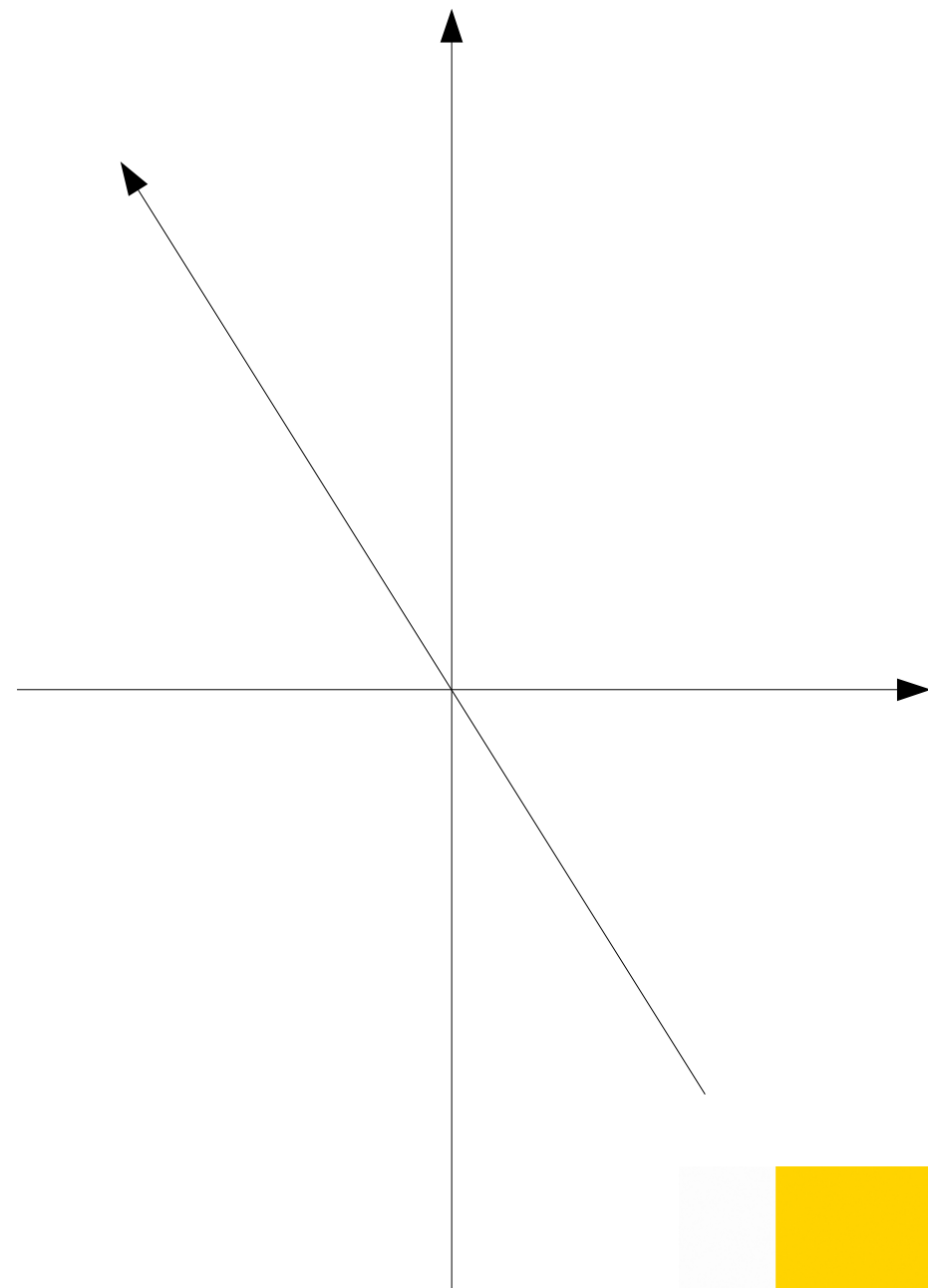


Configuration space (artist's view)

- Gauge fields not unique
 - Gauge transformation does not change physics

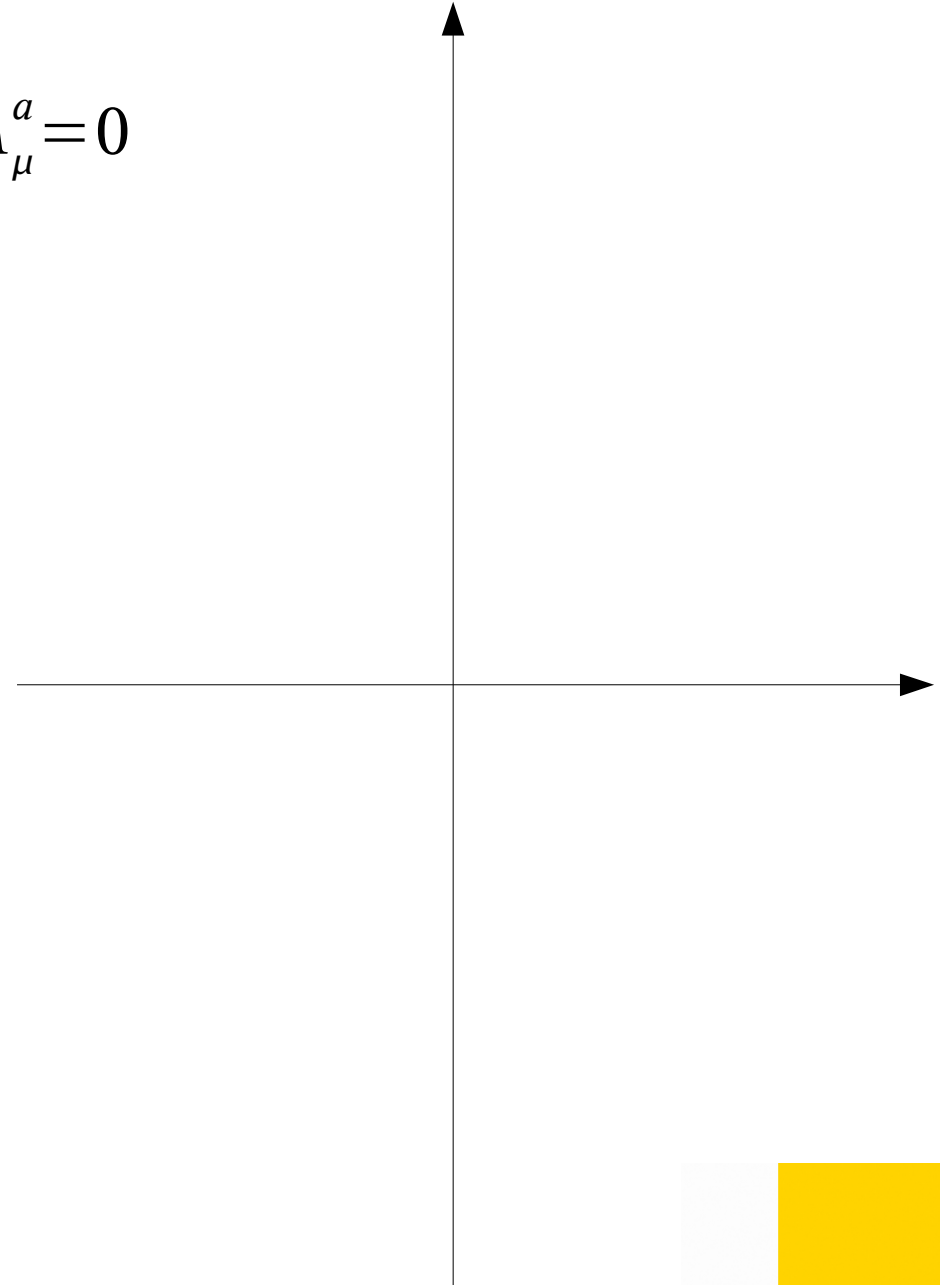


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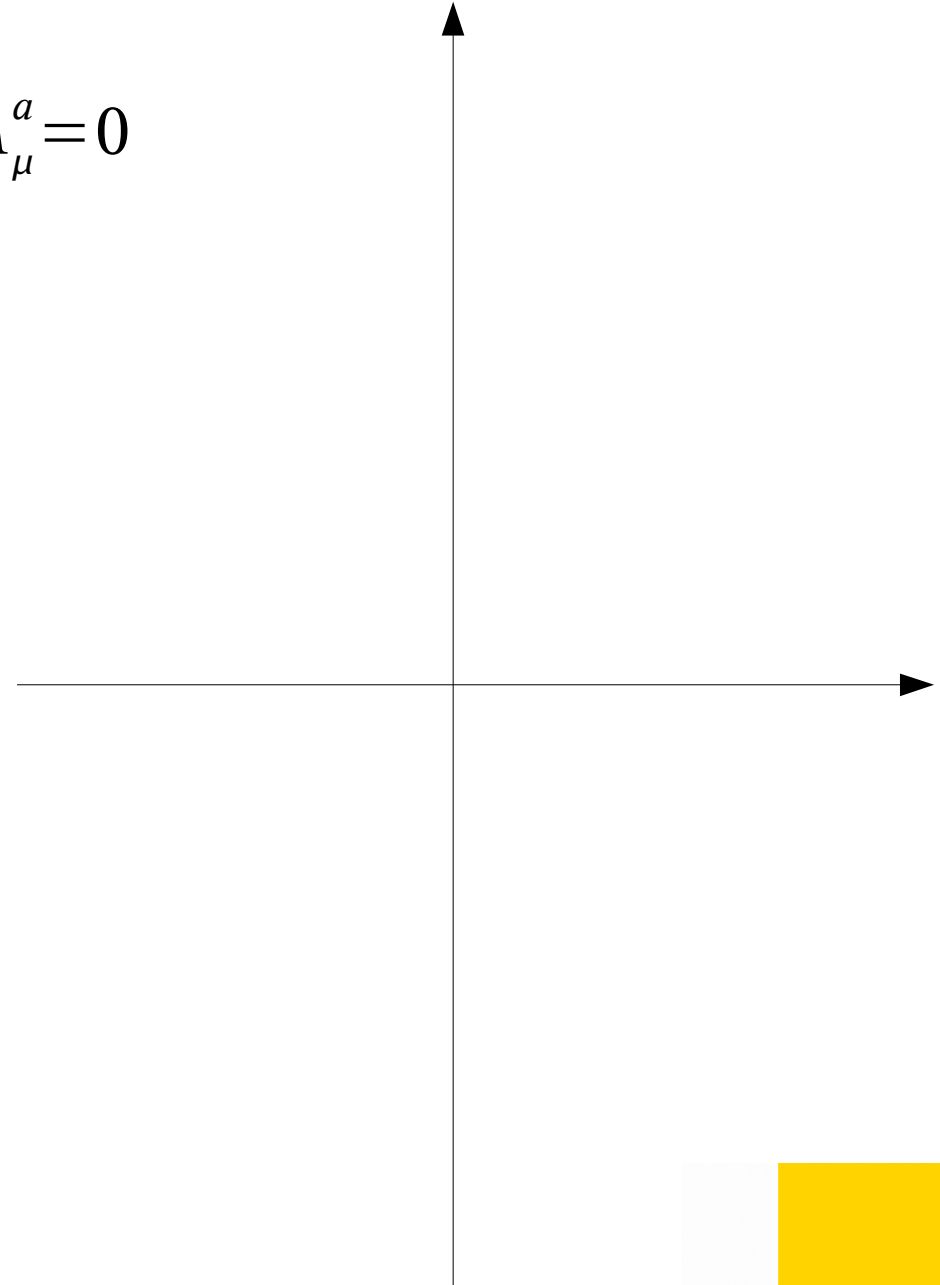
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(Perturbative) Landau gauge

- Lagrangian:

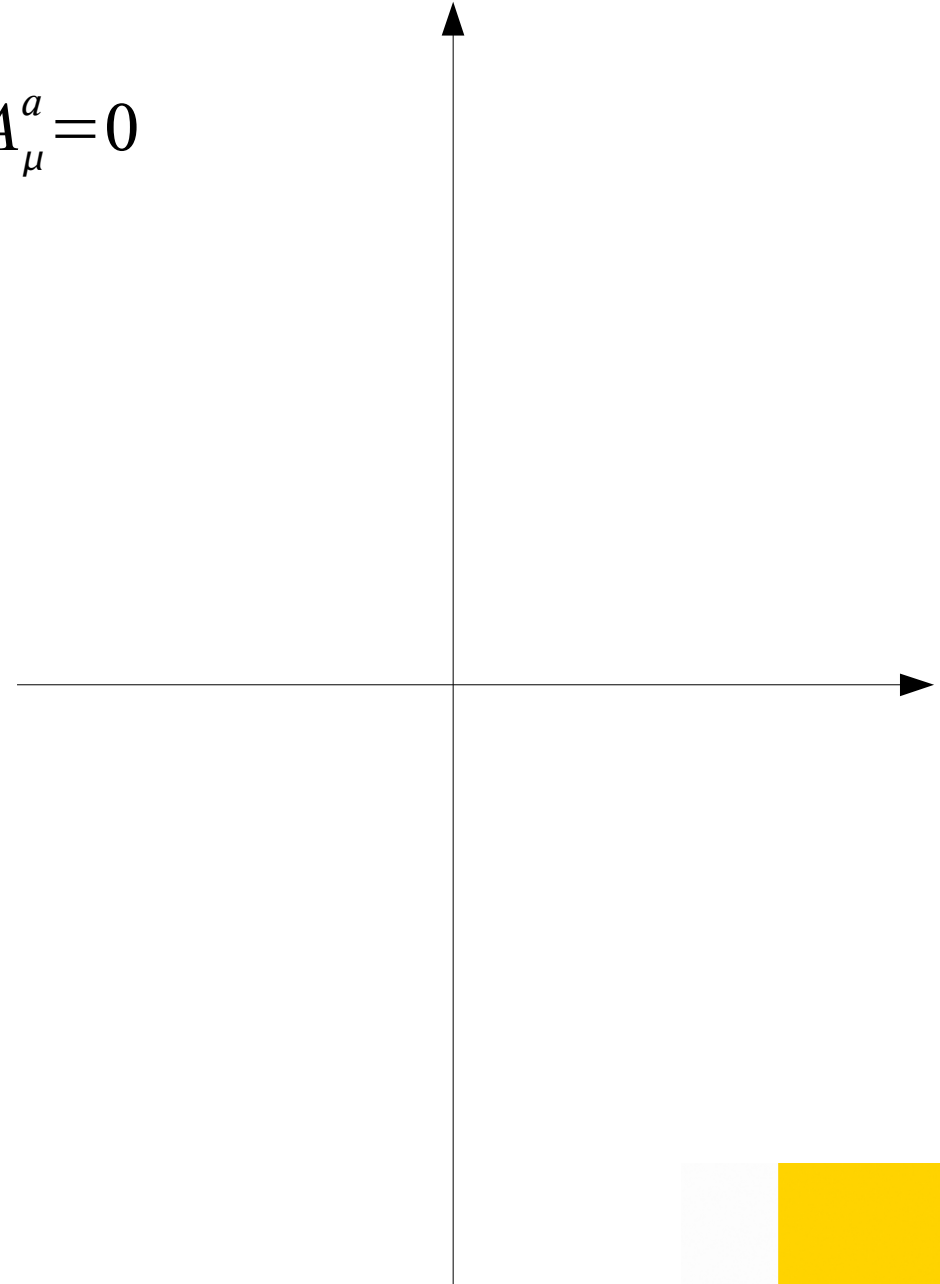
$$L = -\frac{1}{4} F_{\mu\nu}^a F_{\mu\nu}^a - \bar{c}^a \partial_\mu D_\mu^{ab} c^b$$

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - gf^{abc} A_\mu^b A_\nu^c$$

$$D_\mu^{ab} = \delta^{ab} \partial_\mu - gf^{abc} A_\mu^c$$
- Degrees of freedom:
 - Gluons: A_μ^a
 - Ghosts: \bar{c}^a, c^a
- Ghosts interact with gluons: They have to be included

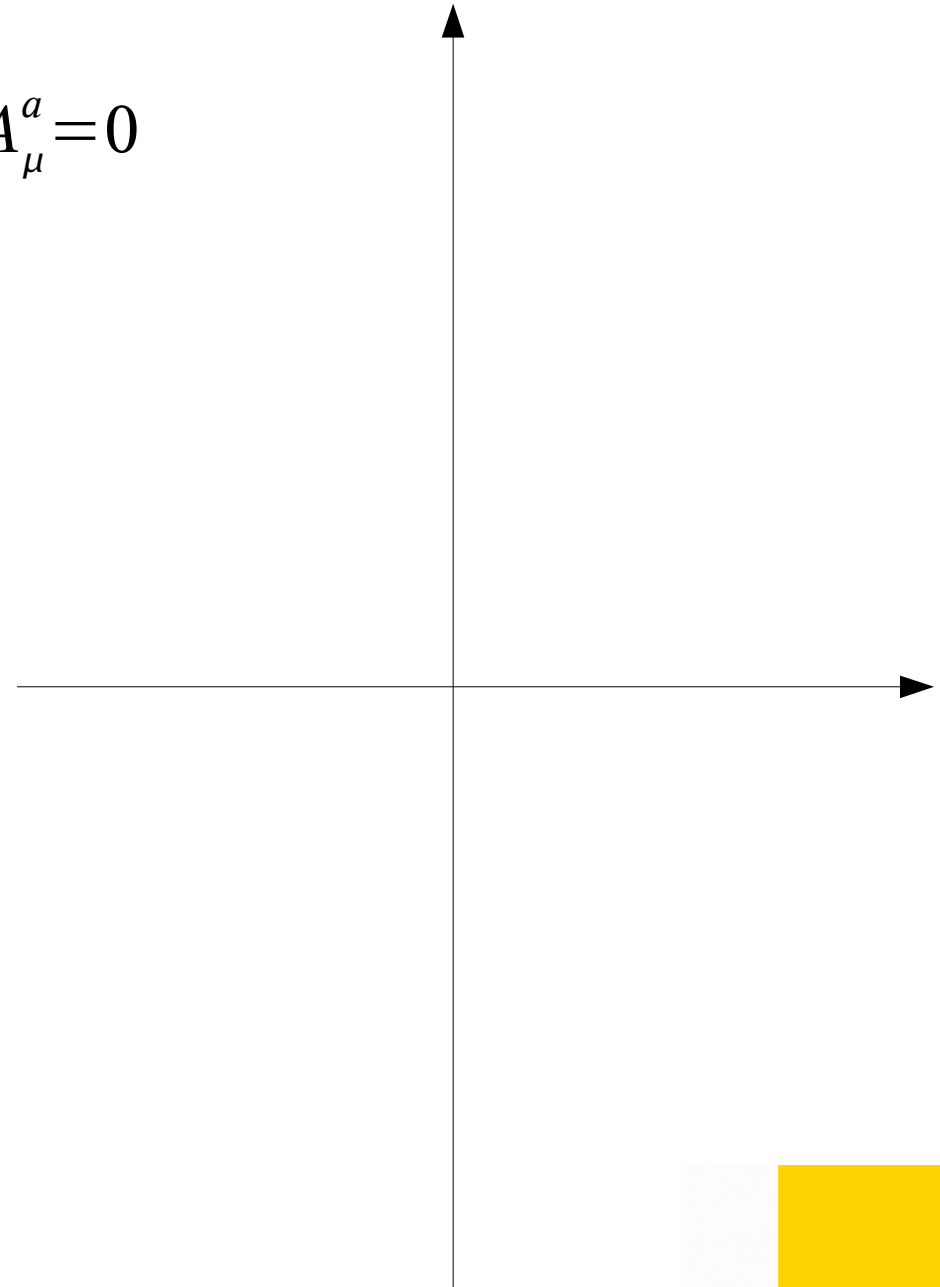
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 - Well-defined and unique prescription in perturbation theory
 - Permits to describe **gluons using correlation functions**



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- Simplest non-zero Green's functions: 2-point functions or propagators
 - Expectation values of products of two field operators
 - 1-point functions vanish

Propagators

- In Landau gauge: **Gluon** and one auxiliary field: **Ghost**
- **Gluon:**

$$D_{\mu\nu}^{ab}(x-y) = \langle A_{\mu}^a(x) A_{\nu}^b(y) \rangle$$

$$D_{\mu\nu}(p) = \left(\delta_{\mu\nu} - \frac{p_{\mu} p_{\nu}}{p^2} \right) \frac{Z(p)}{p^2}$$

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- G and Z are the dressing functions

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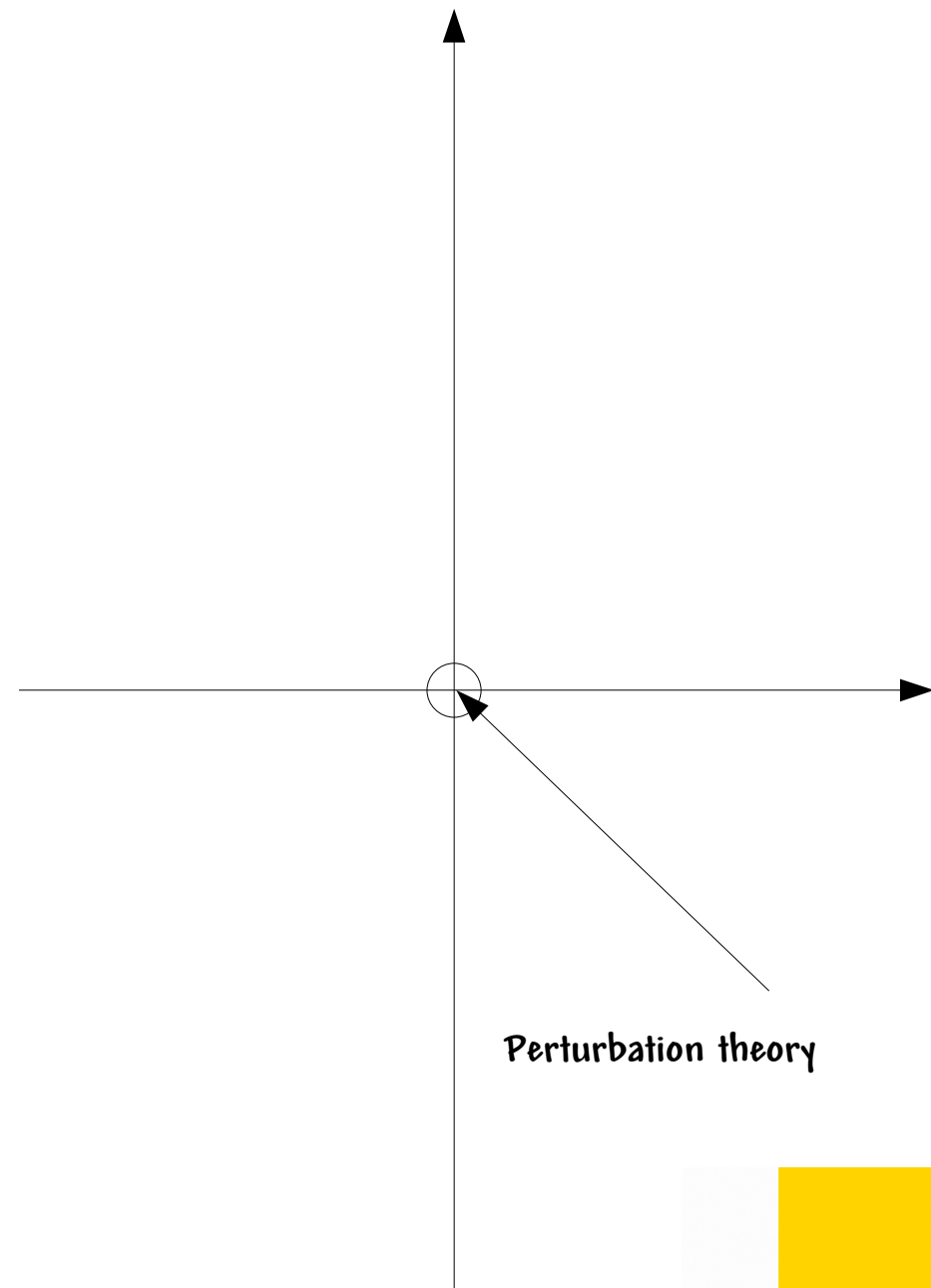
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- Also for the non-perturbative physics?

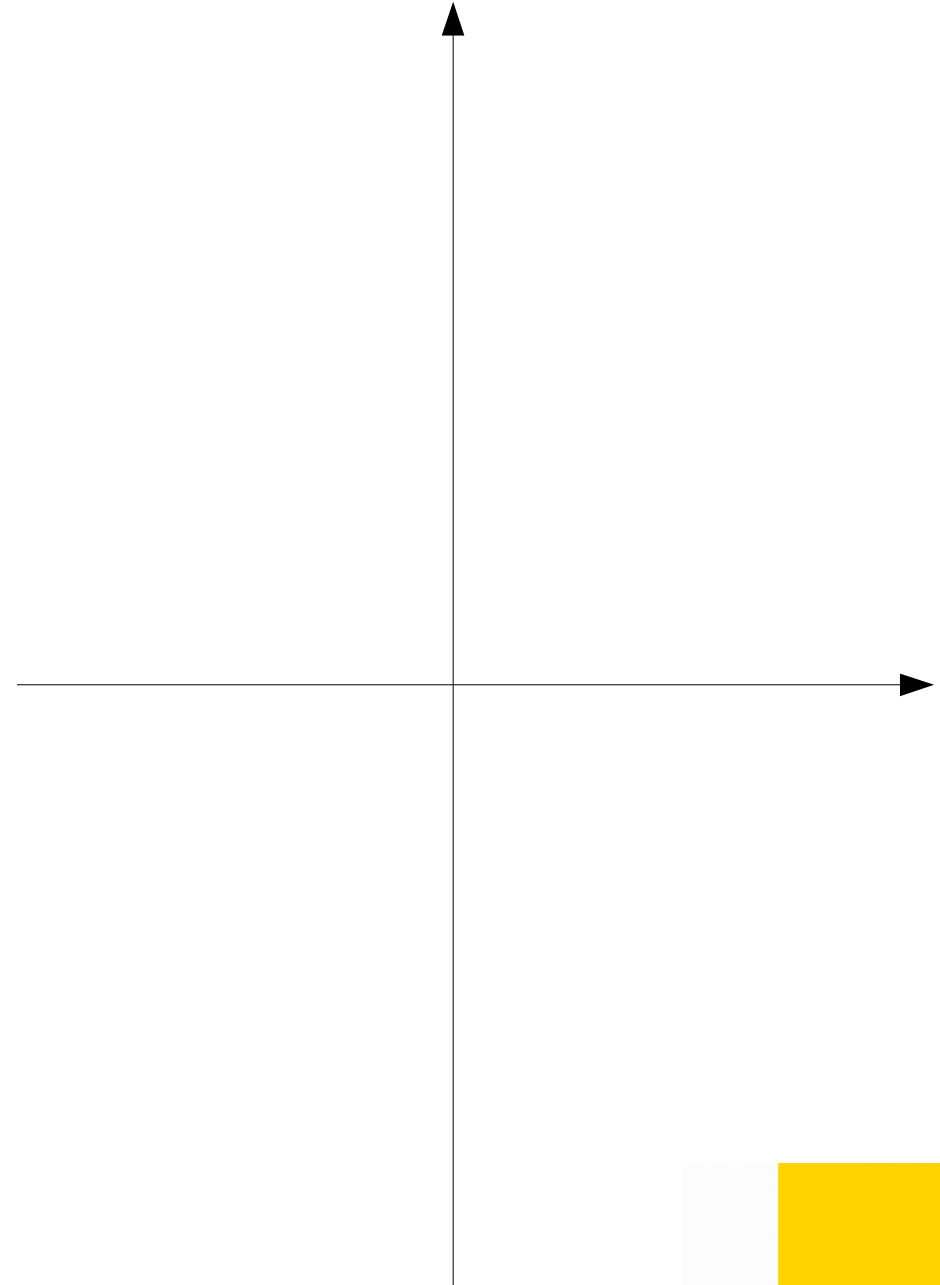
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- Perturbation theory is applicable close to the origin
- Non-perturbative physics probes the complete hypersurface



Unique gauge-fixing [For an introduction: Sobreiro & Sorella, 2005]

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- There are no local gauge conditions, which select a unique gauge field configuration [Singer 1978]
 - Gribov-Singer ambiguity

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- Resolves the Gribov-Singer ambiguity explicitly

Implementation

- Generates a **one-parameter family of Landau gauges**, parameterized by the ghost propagator at zero momentum: A second gauge parameter [Maas, 2009; Fischer, Maas, Pawłowski, 2008]

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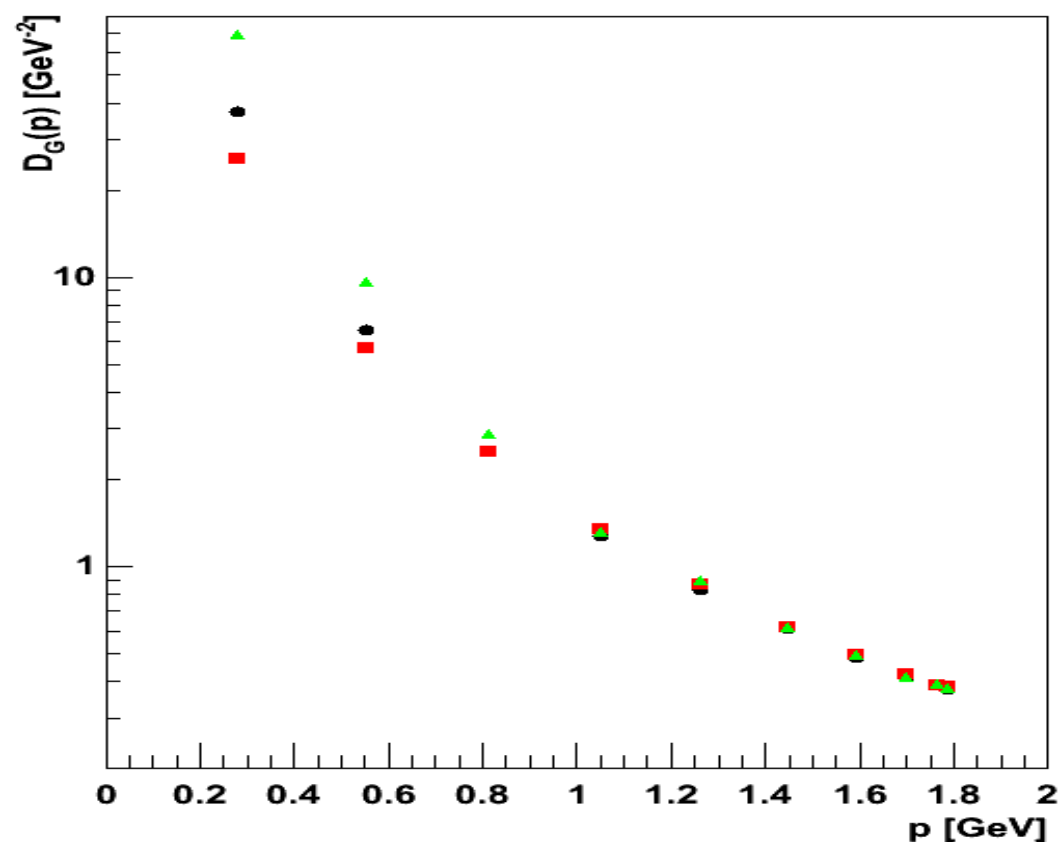
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- Differences only visible in the deep infrared

Ghost propagator from the lattice [3d, Maas, 2009]

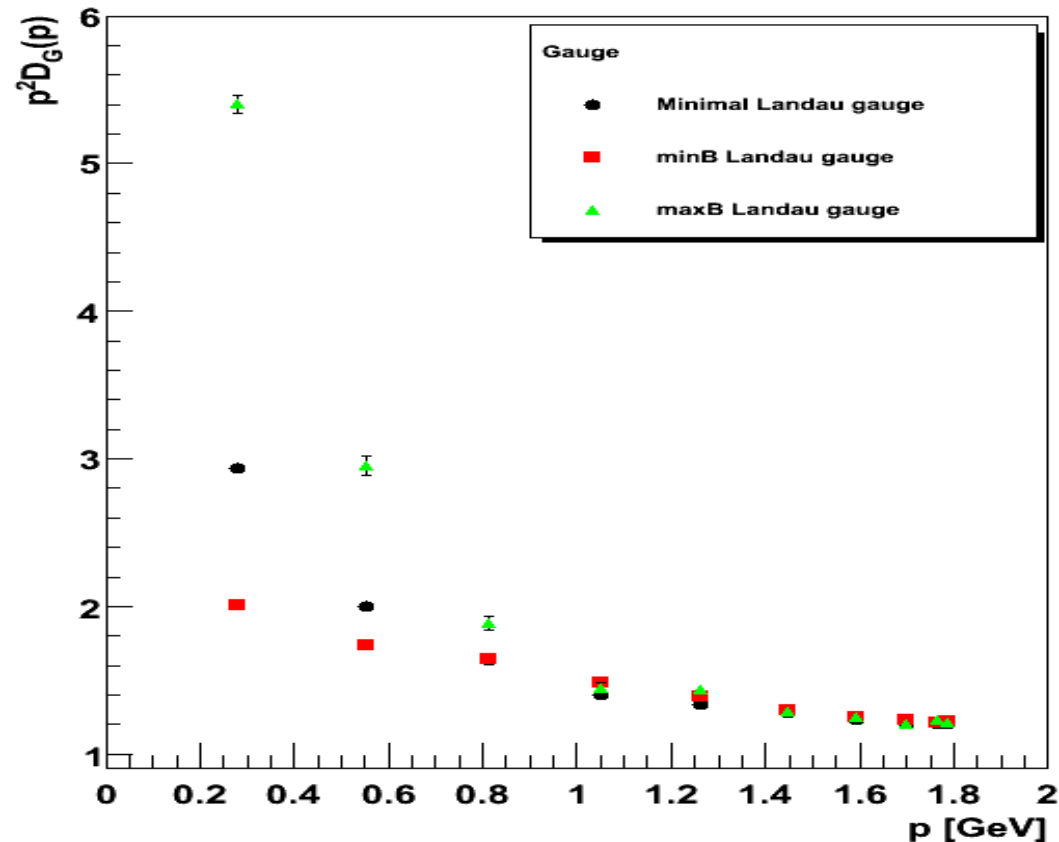
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Ghost propagator



Ghost dressing function

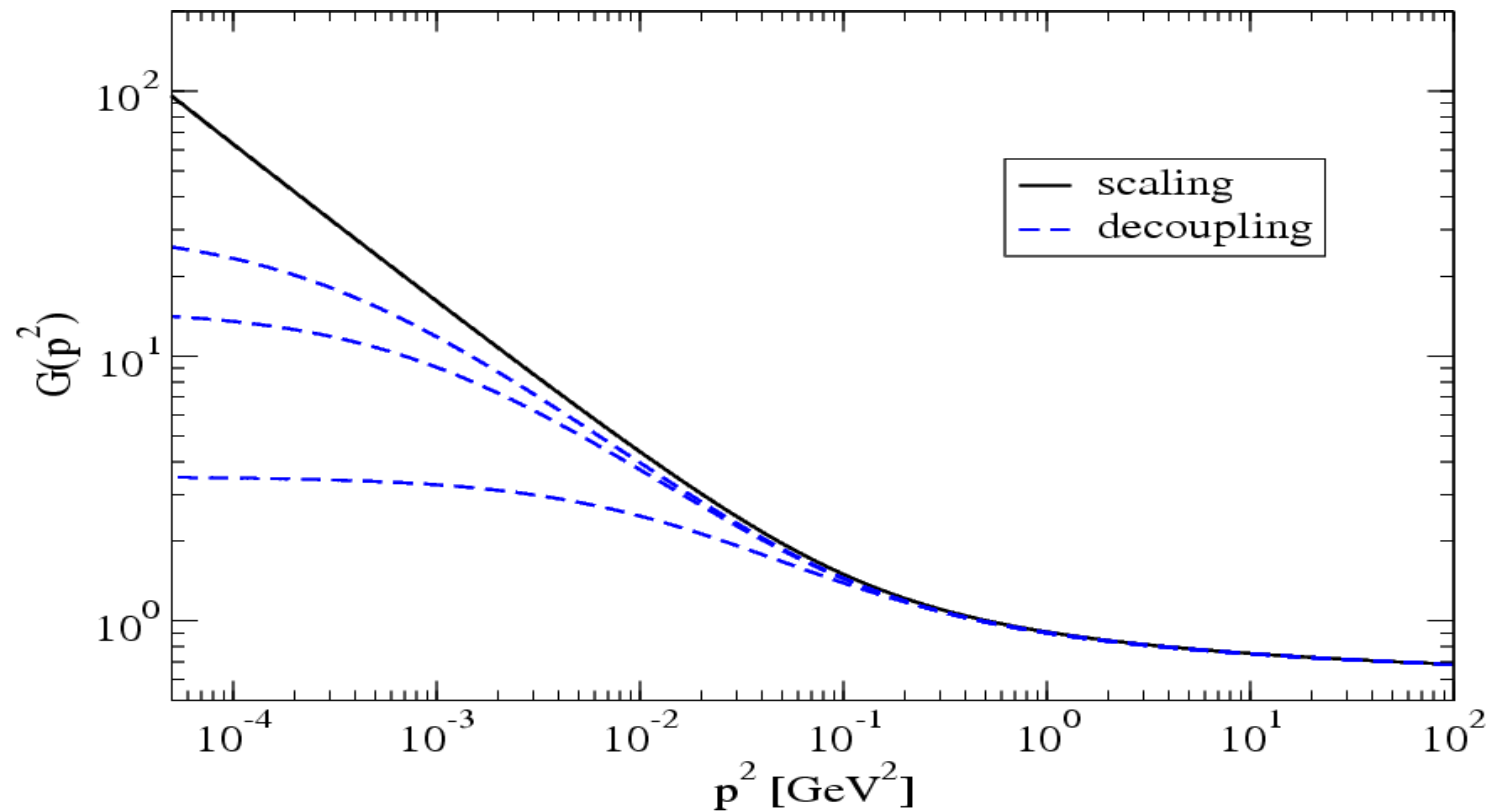


- Results from lattice calculations
- Different gauge choices yield different propagators
- Lattice artifacts still to be studied

Ghost dressing function in the continuum [Fischer, Maas, Pawłowski, 2008]

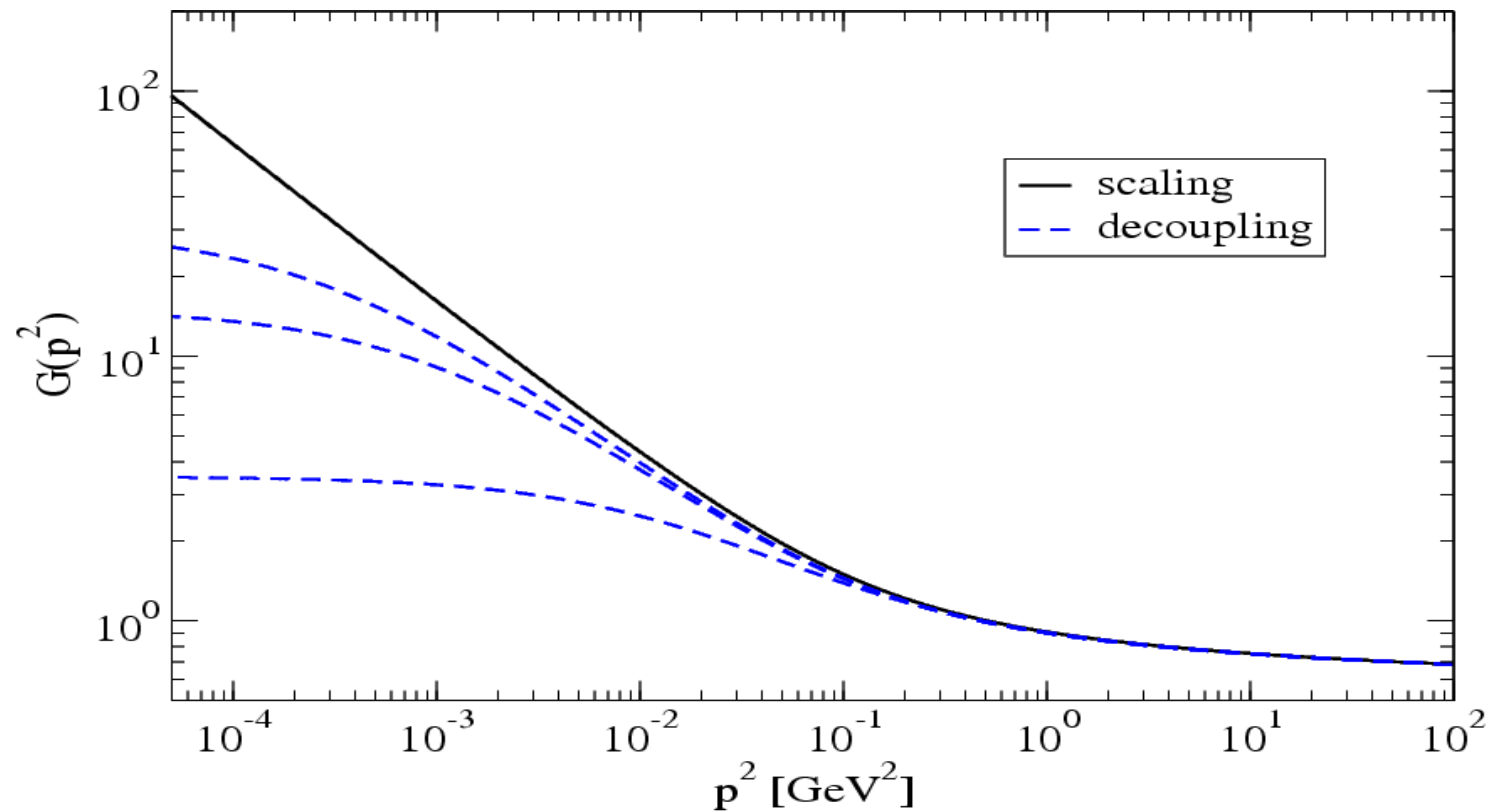
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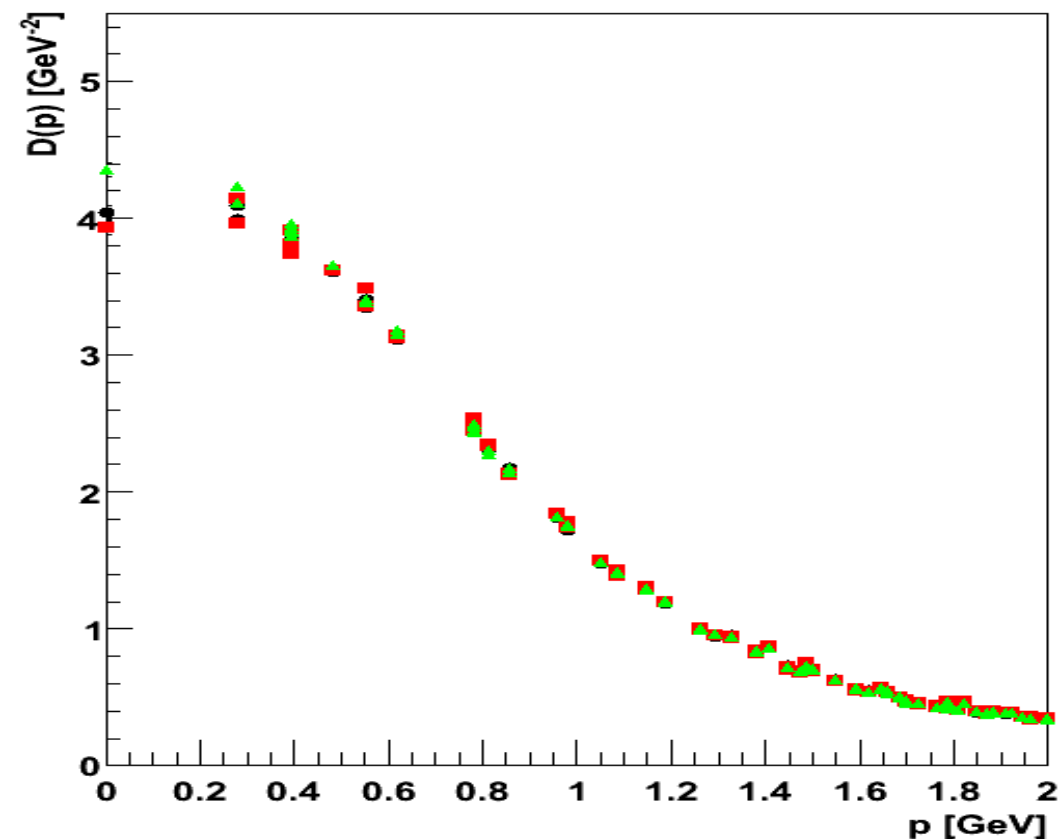
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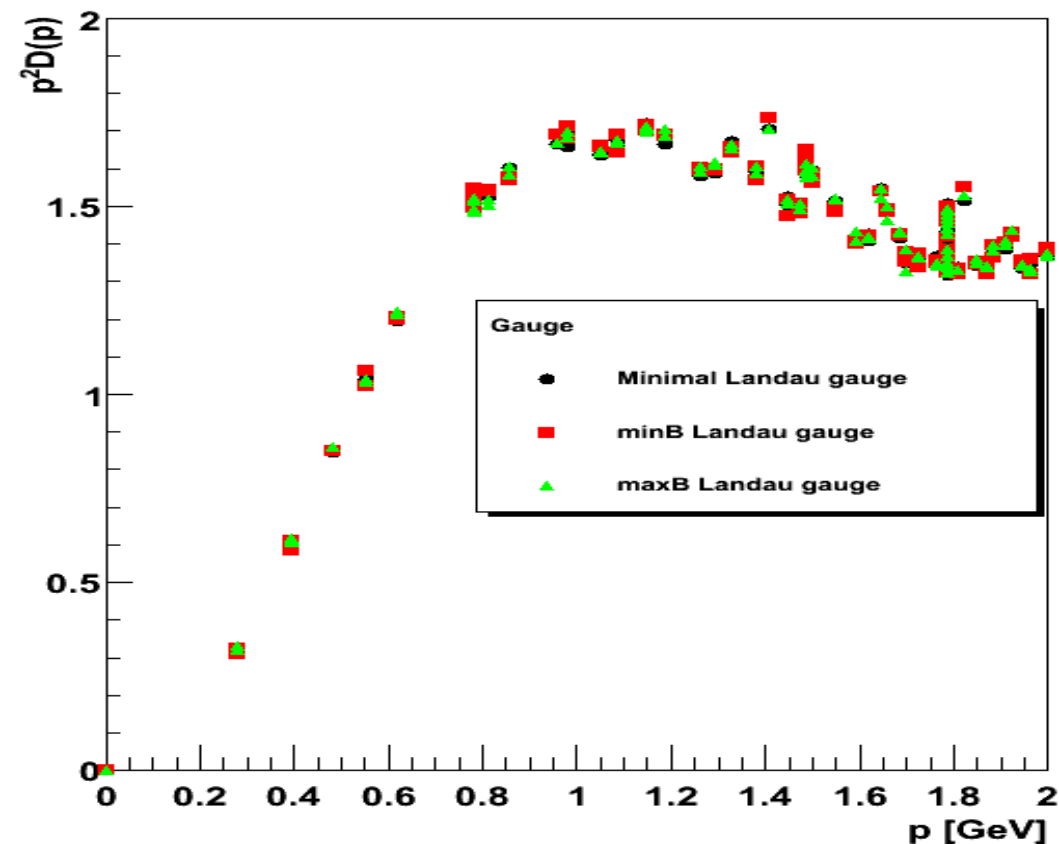
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- Scaling: Divergent, Decoupling: Finite dressing function

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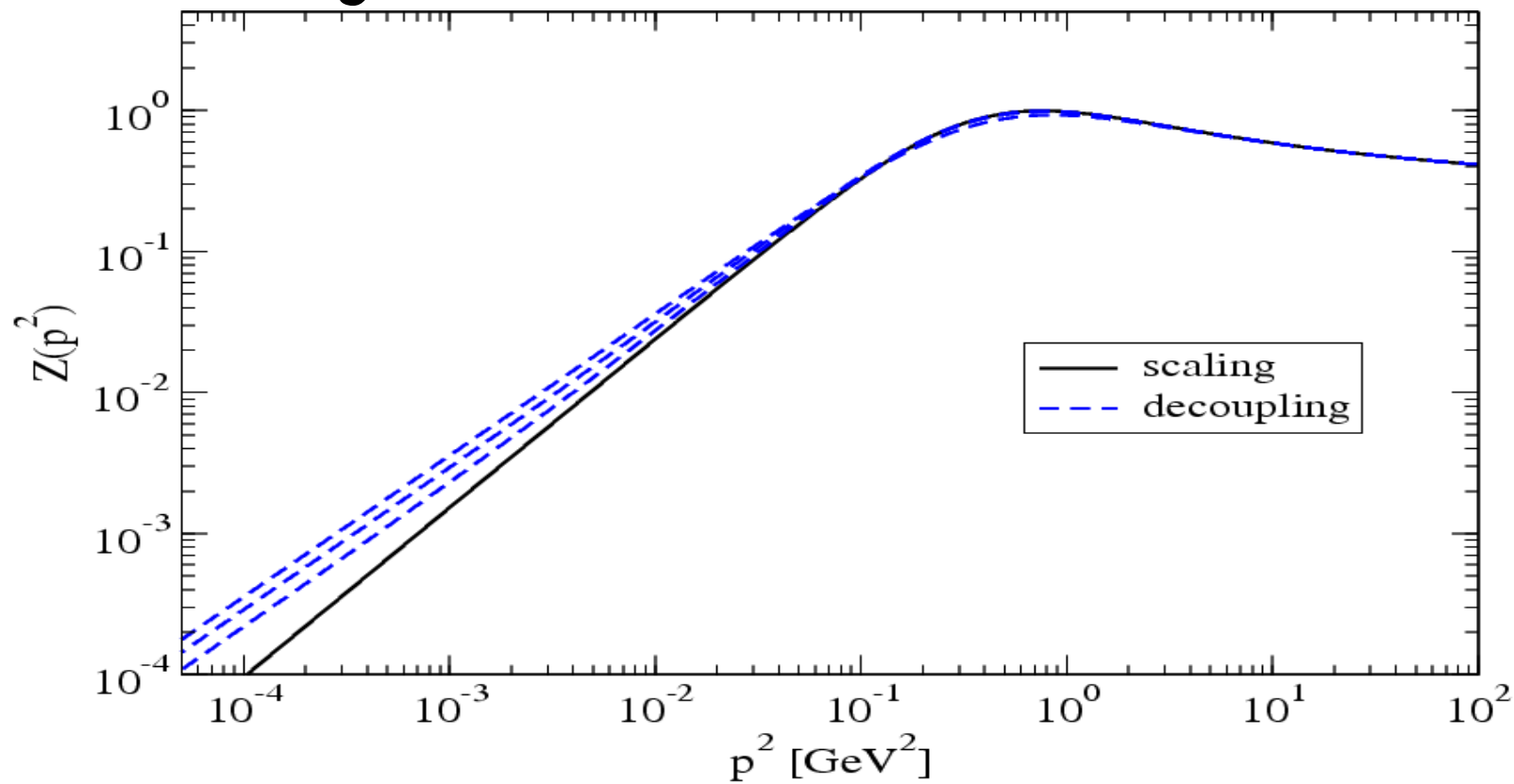


Gluon dressing function



- Almost unaffected of the **gauge choice** at presently accessible volumes
- Effects only expected below 200 MeV

Gluon dressing function in the continuum [Fischer, Maas, Pawłowski, 2008]



- **Scaling case: Vanishing gluon propagator**
 - No positive spectral function: Gluons confined [Zwanzgier, '90s]
- **Decoupling case: Screened gluon**
 - No positive spectral function [Fischer, Maas, Pawłowski, 2008; Cucchieri, Mihara, Mendes, 2004]

Part II

Finite Temperature

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Infinite-temperature case: See poster of Veronika Macher

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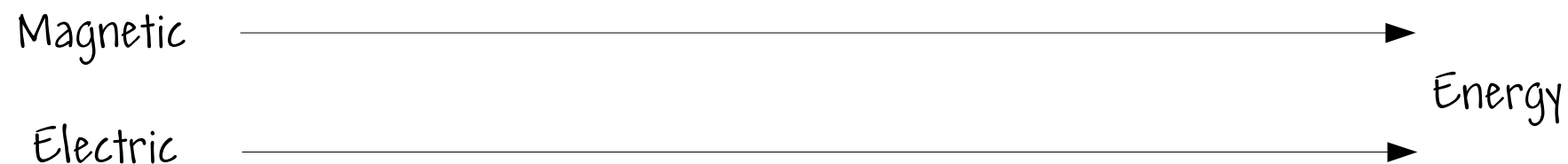
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Splitting of electric and magnetic sectors

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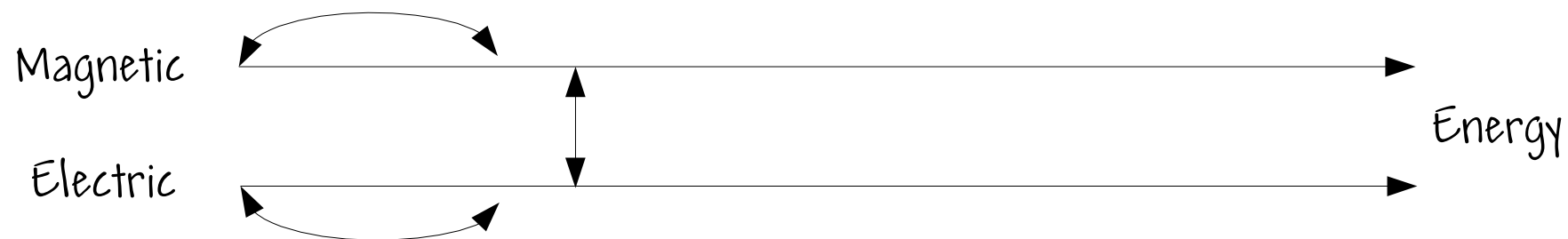
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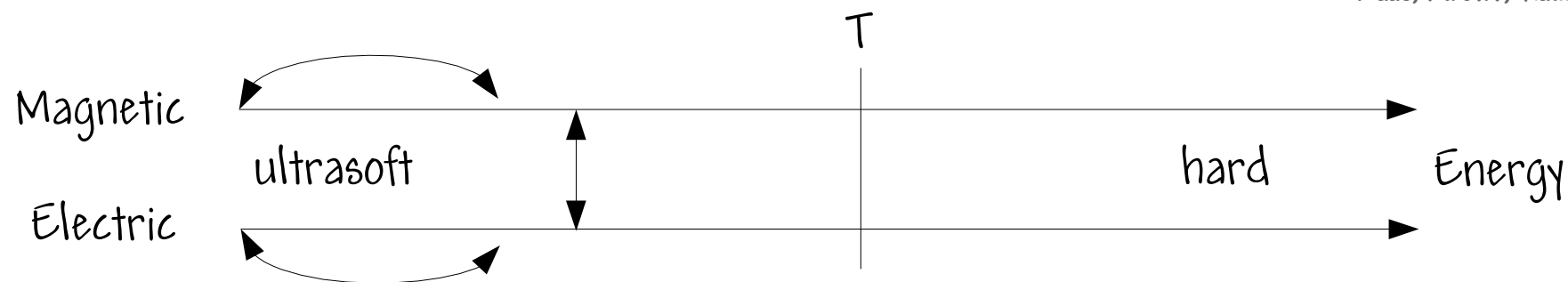
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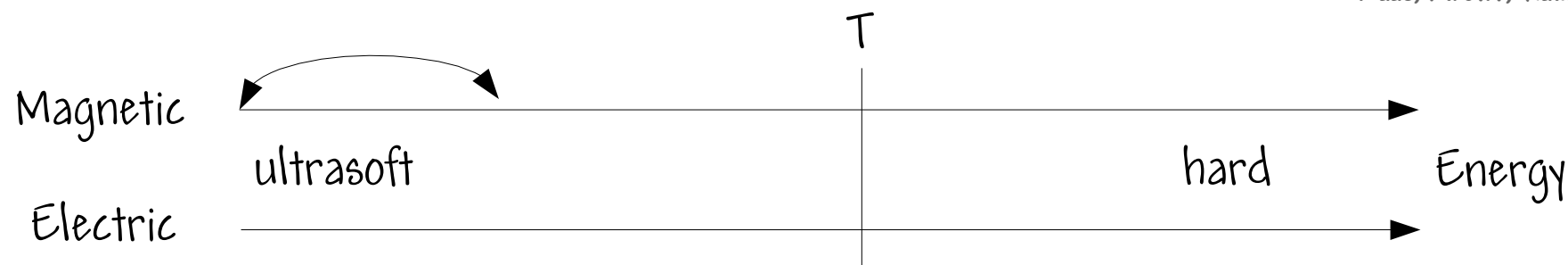


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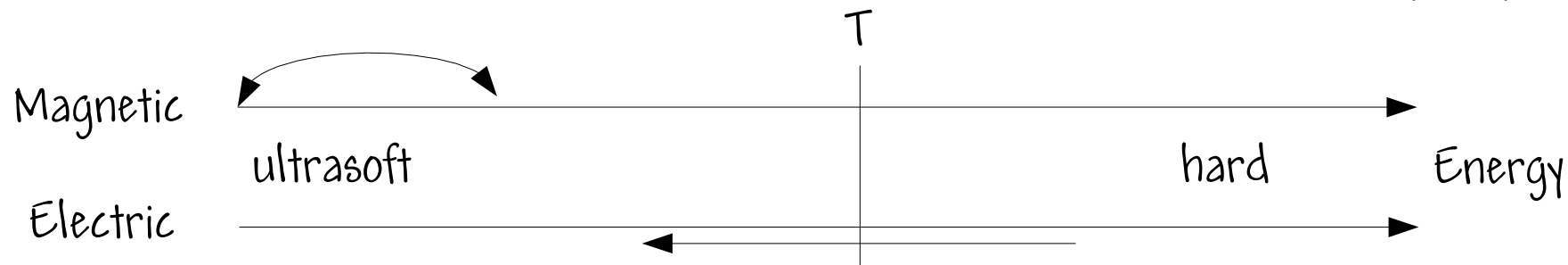


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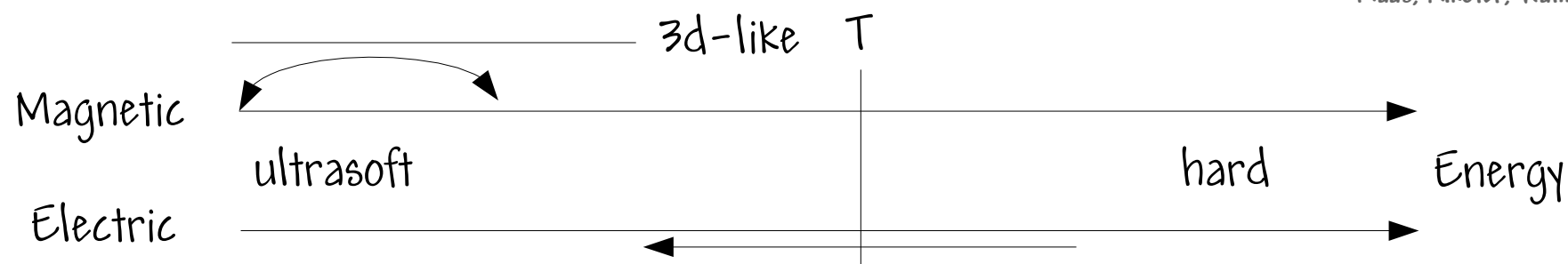


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- The ultrasoft magnetic sector behaves essentially as in a dimensionally reduced (3d) theory

Resolving the Linde problem

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- The deep infrared of the magnetic sector behaves as in a **pure zero-temperature 3d-Yang-Mills theory**

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- **No infrared divergencies left: No Linde problem**

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- Gluons are not deconfined!
- Gauge-invariant statement

Imprint of the phase transition [Cucchieri, Maas, Mendes, 2007]

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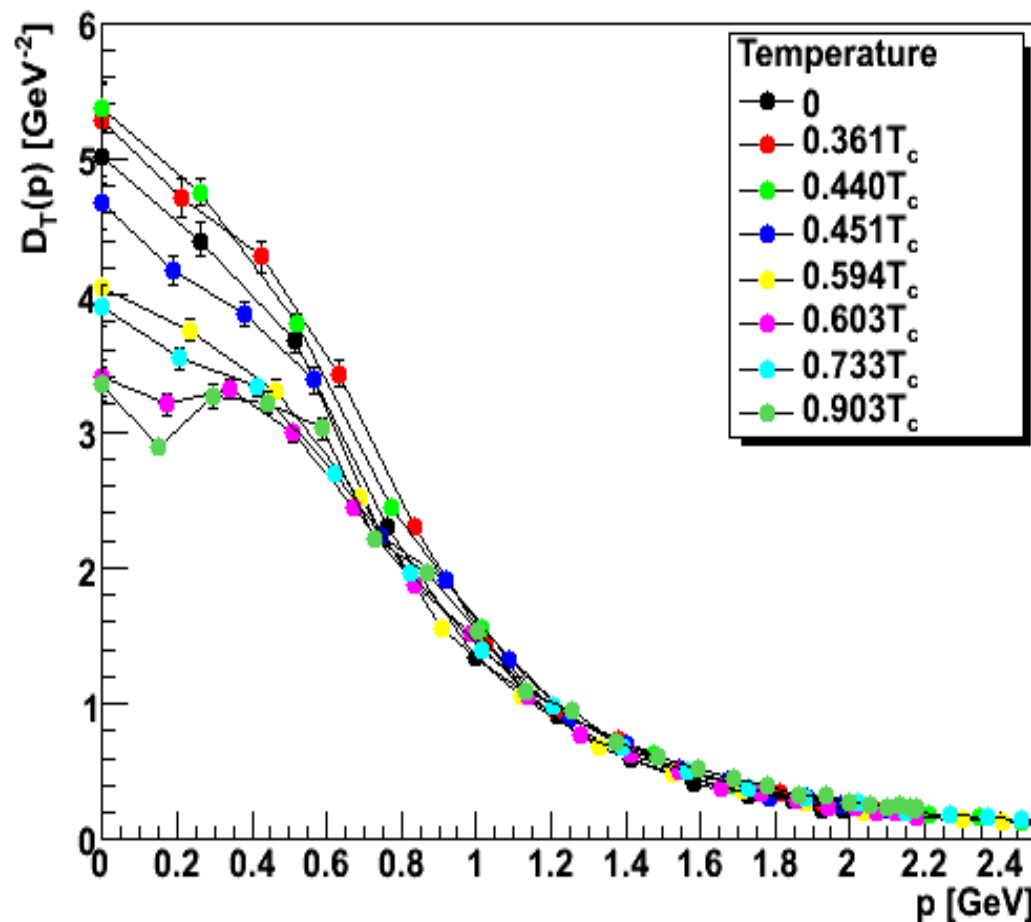
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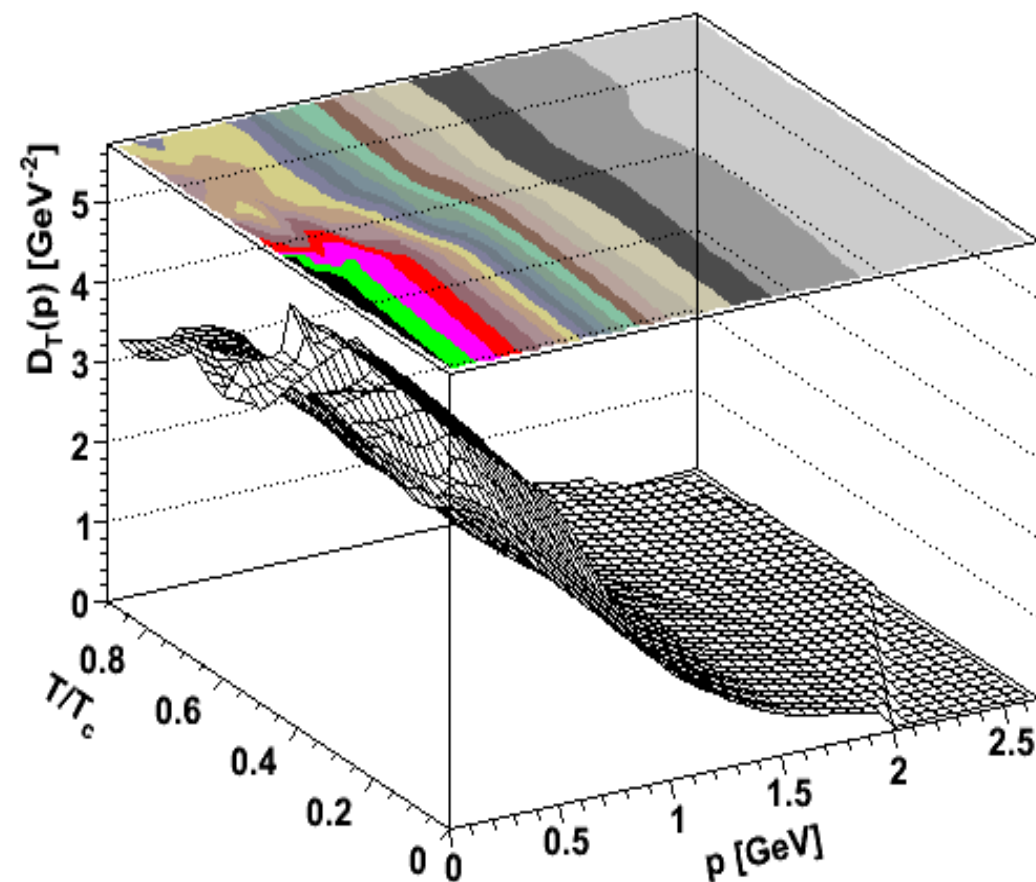
Magnetic gluon at low temperature

[SU(2), Maas, unpublished]

Magnetic gluon propagator



Temperature dependence

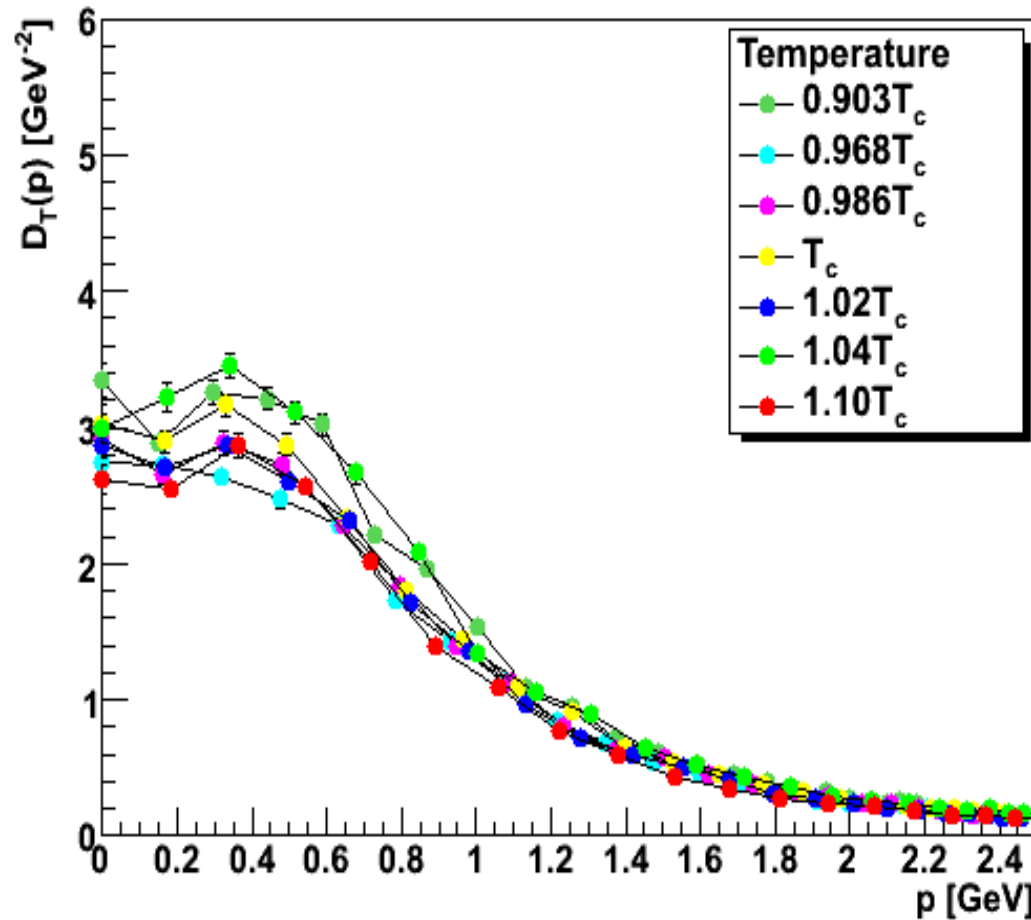


- Very small changes only
- Ultraviolet almost unchanged
- Somewhat stronger infrared suppressed with increasing temperature

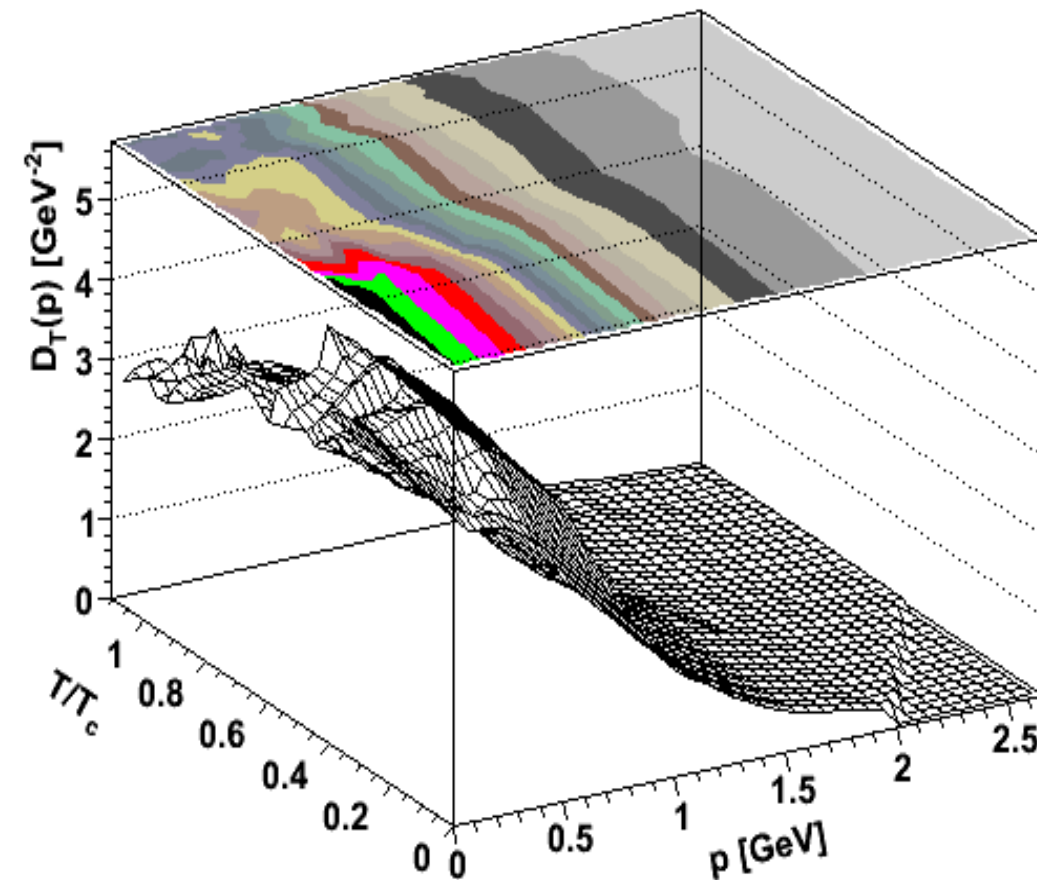
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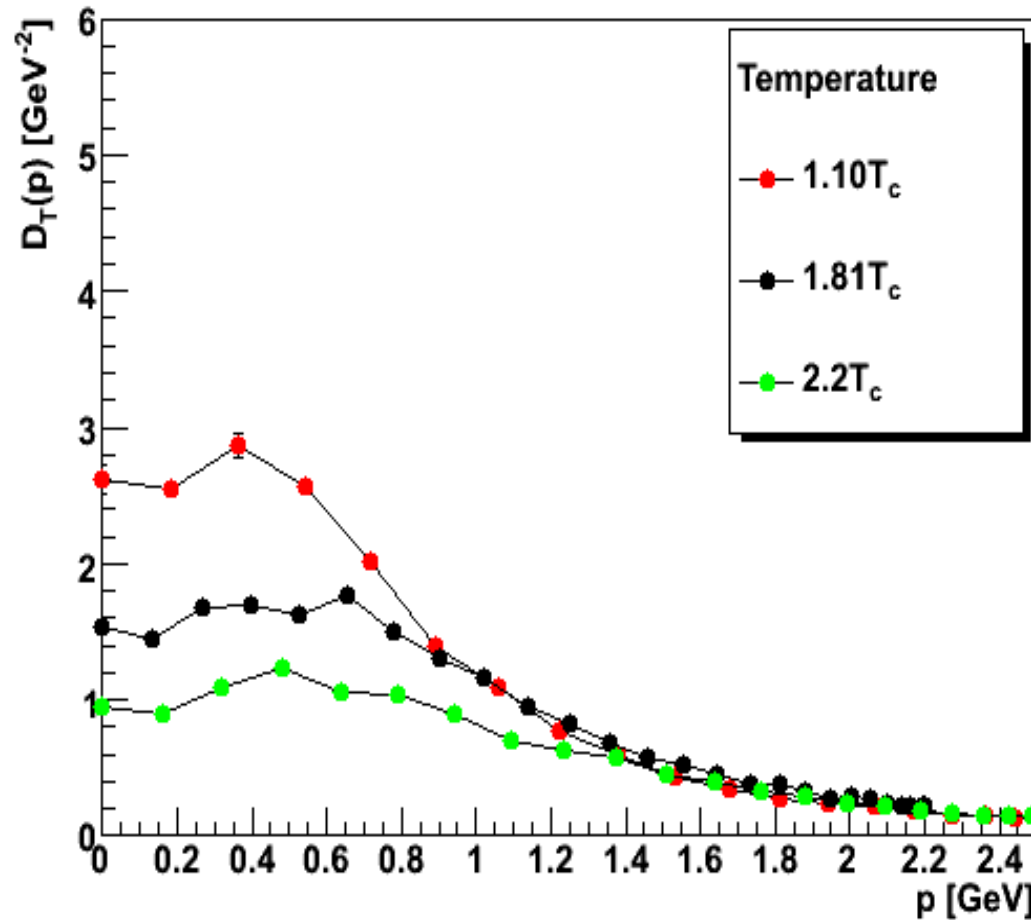


- No response to the phase transition visible

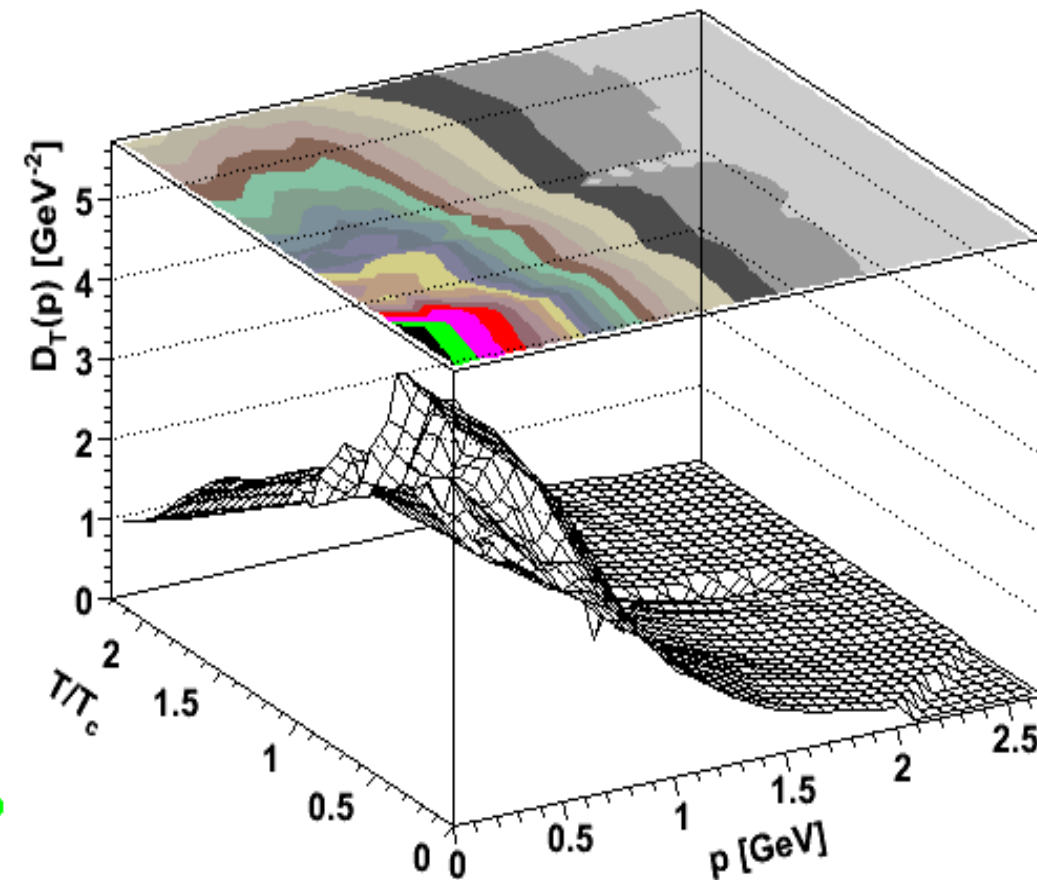
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Temperature dependence



- Continued infrared suppression
- Possibly emergence of a maximum structure around 0.5 GeV

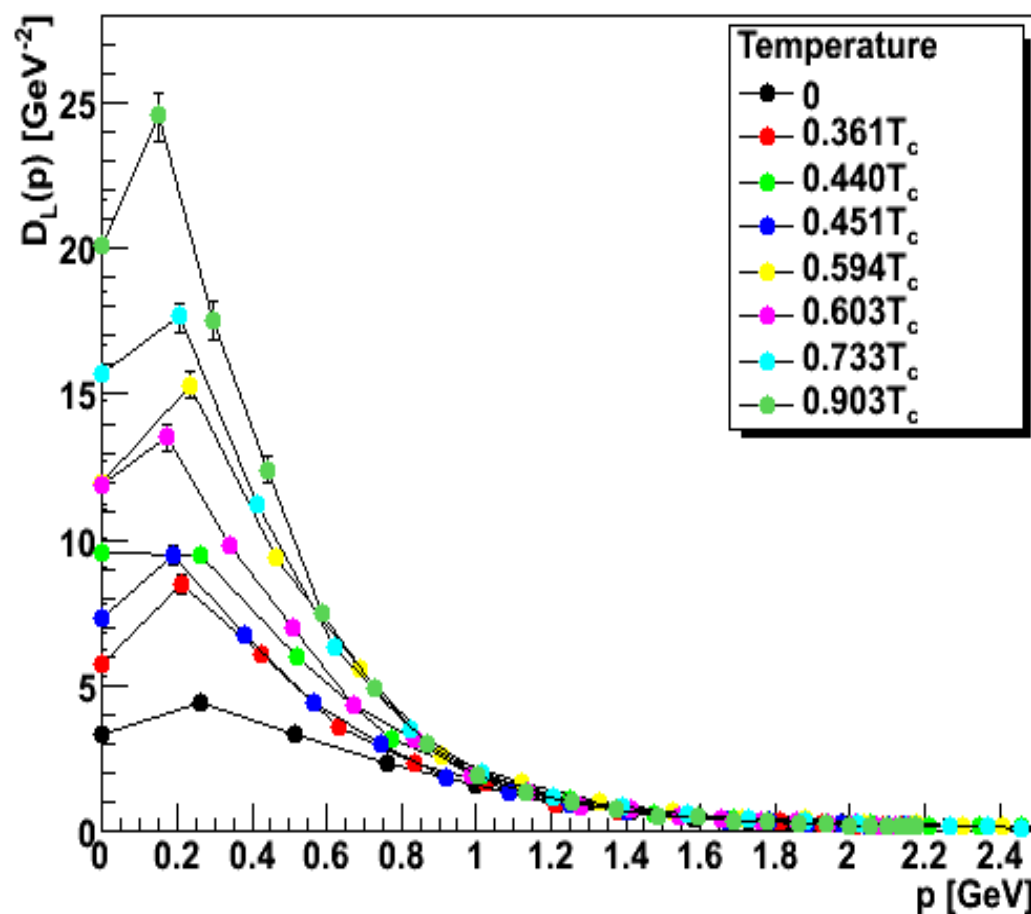
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- Electric sector sensitive to hard interactions: Impact expected

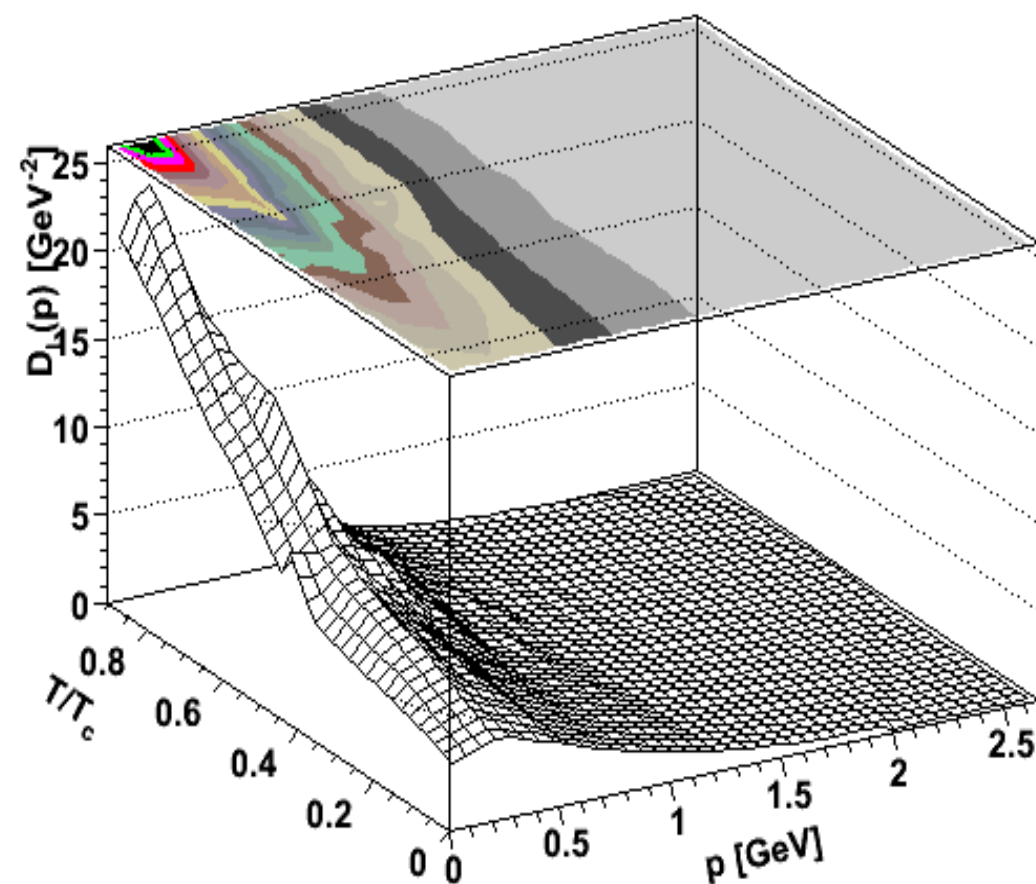
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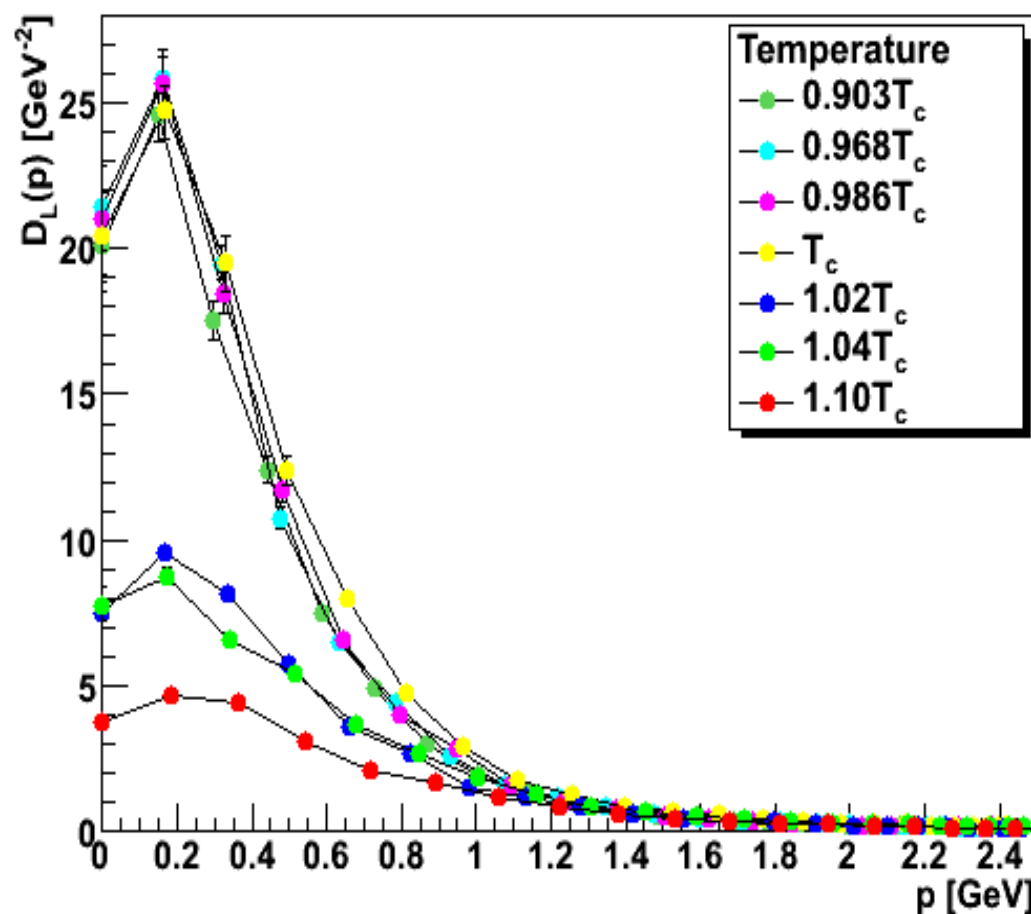


- Becomes infrared enhanced with temperature
- Already significant effects at low temperature

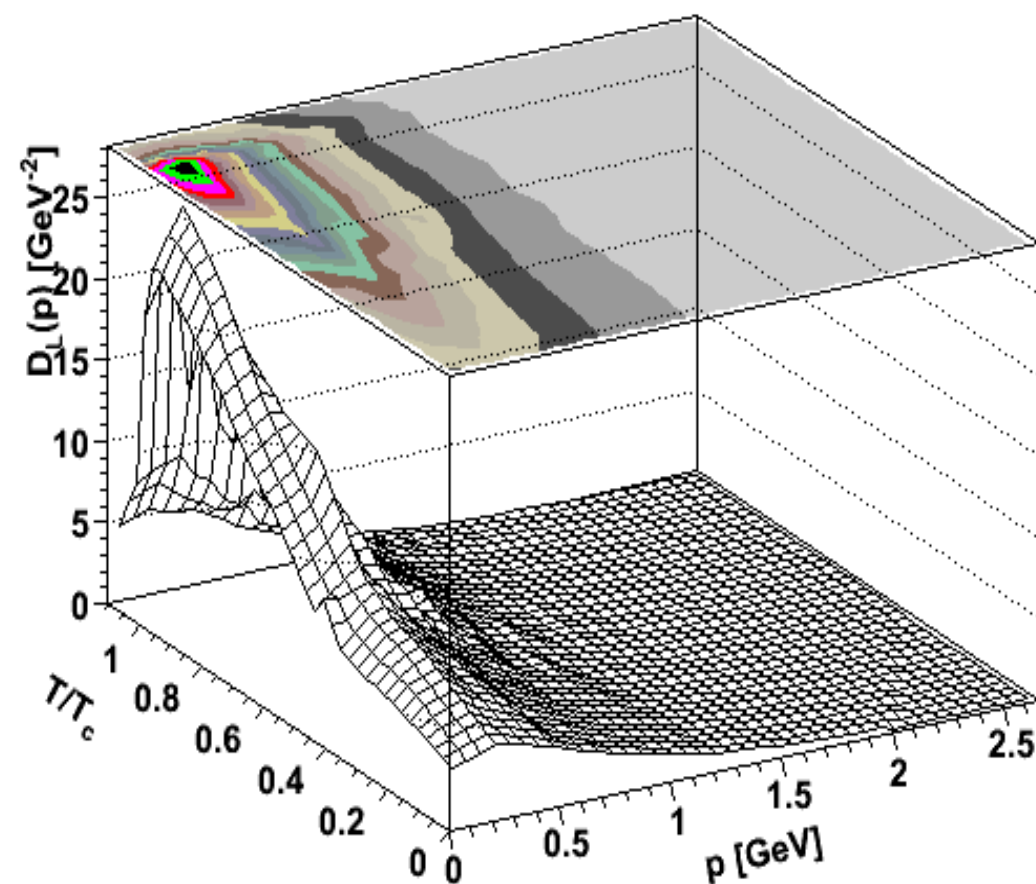
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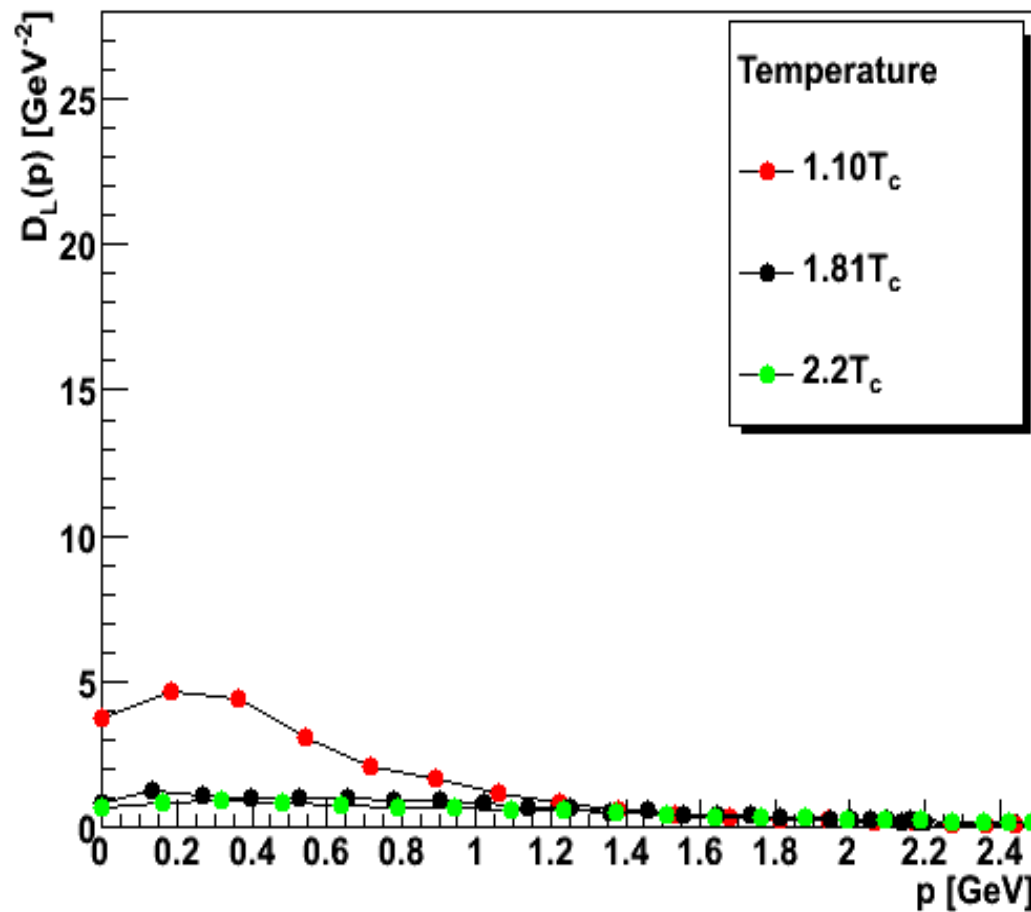


- Maximum at the phase transition temperature
- Sharp drop afterwards
- Very sensitive to the phase transition

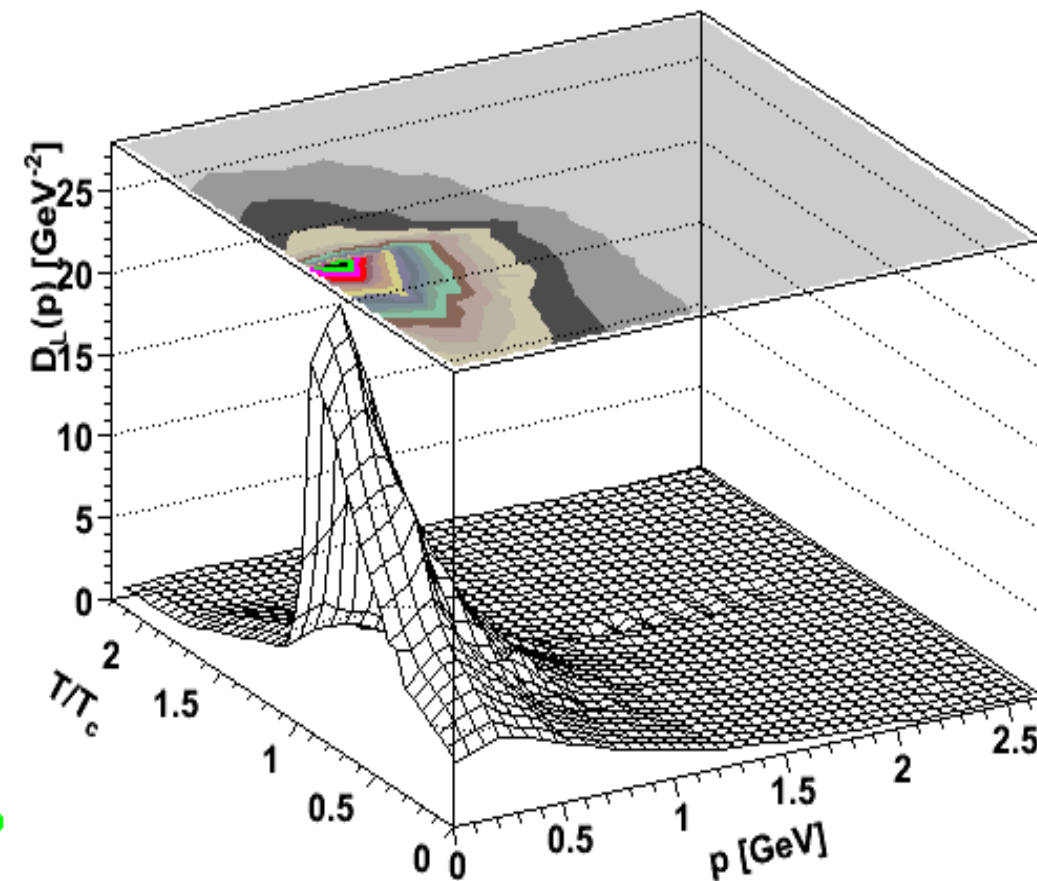
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Electric gluon propagator



Temperature dependence



- Further drop
- Less dramatic
- Becomes compatible with a massive particle

Electric screening mass

[Cucchieri, Maas, Mendes, 2007; Maas, unpublished]

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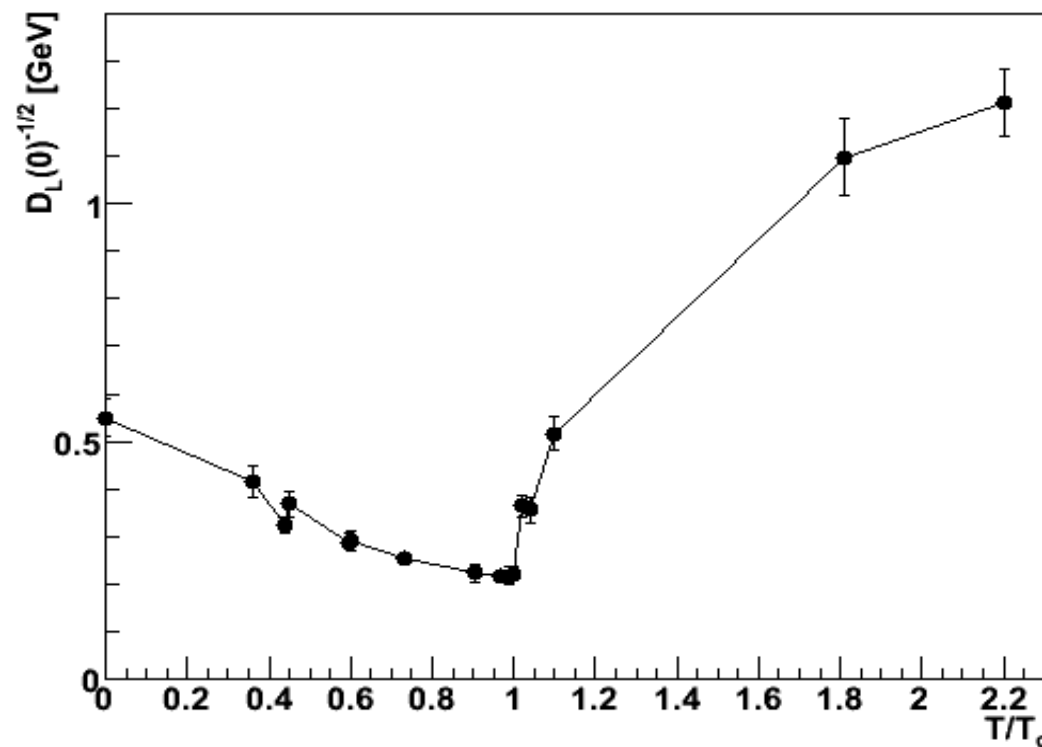
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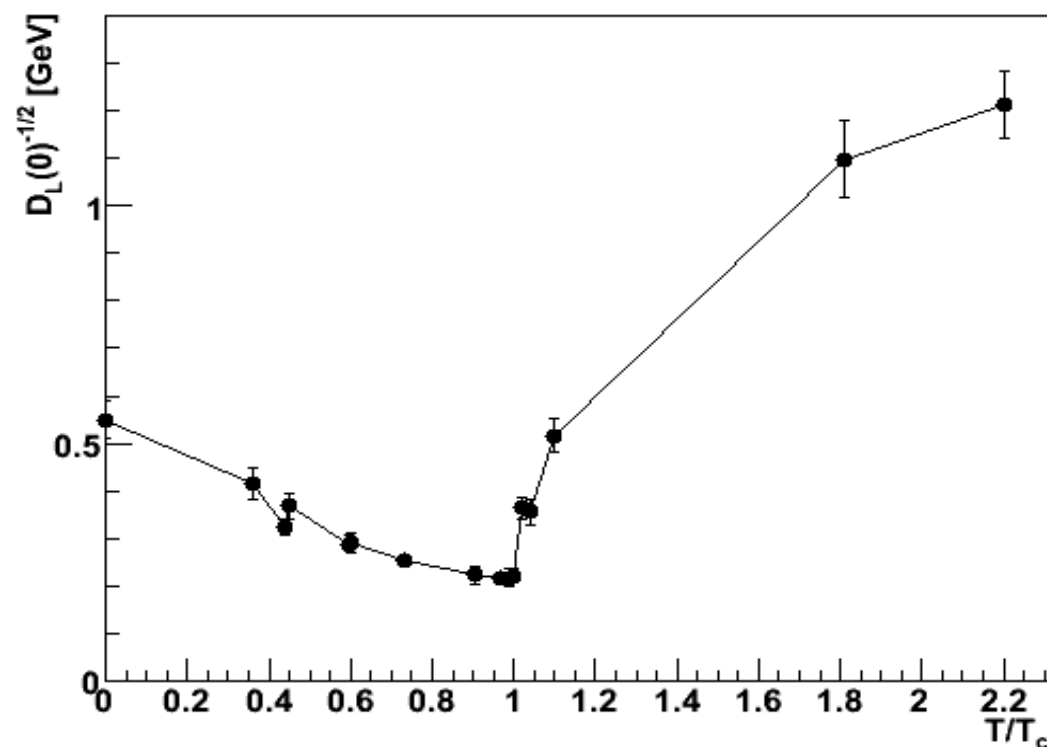


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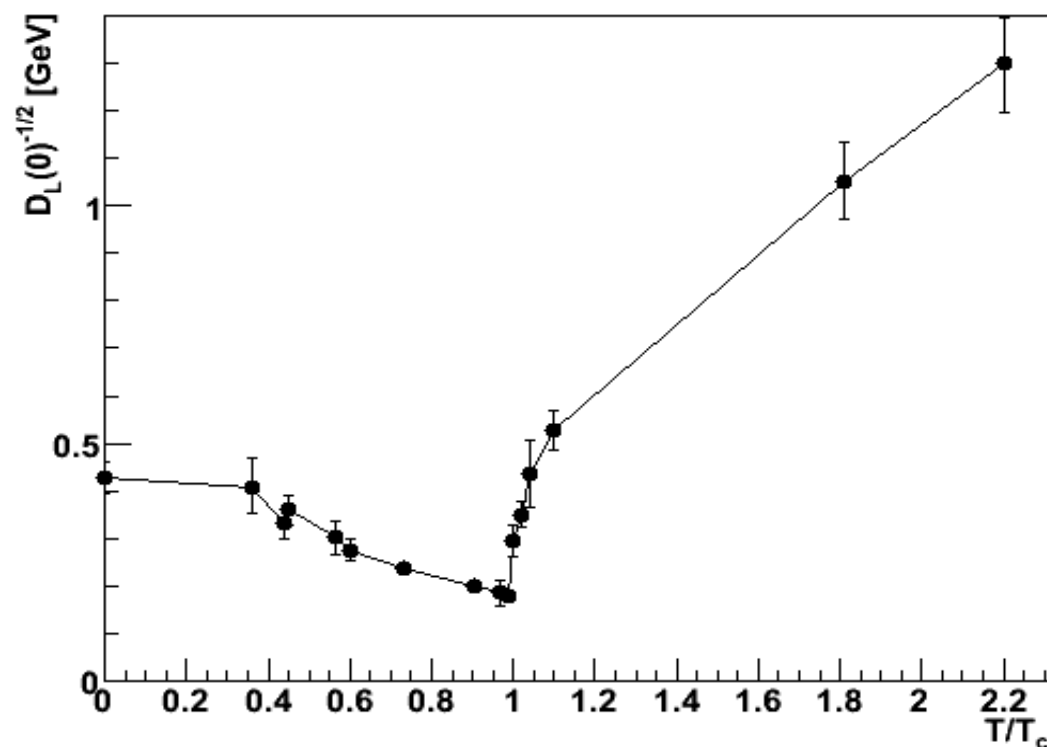
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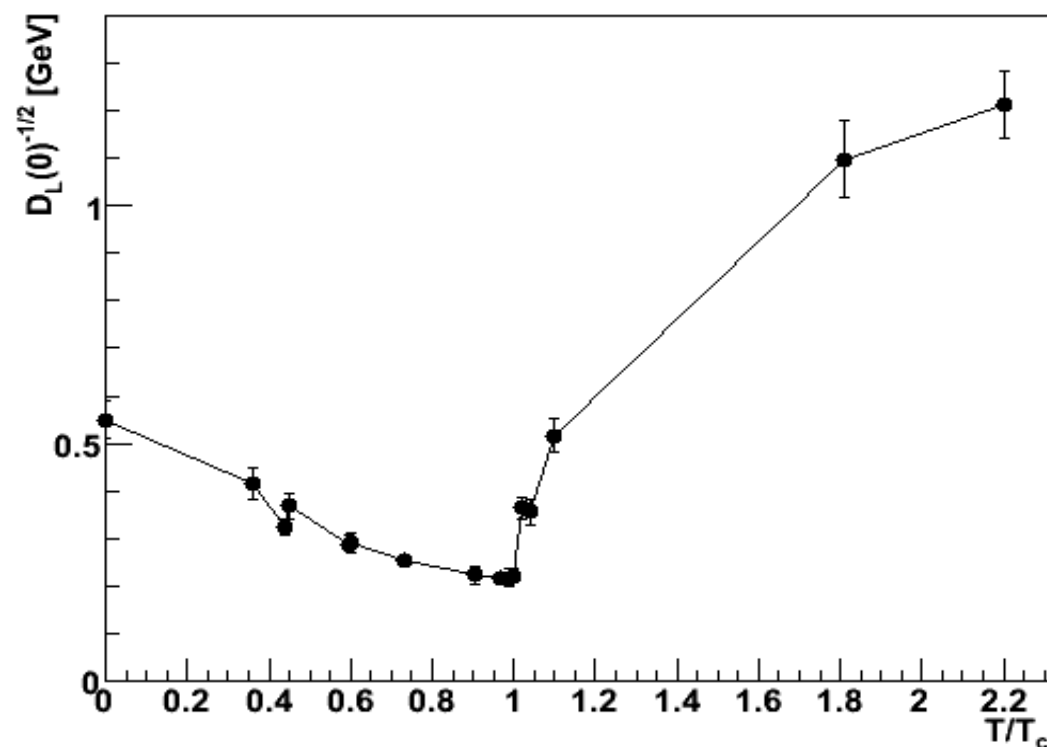


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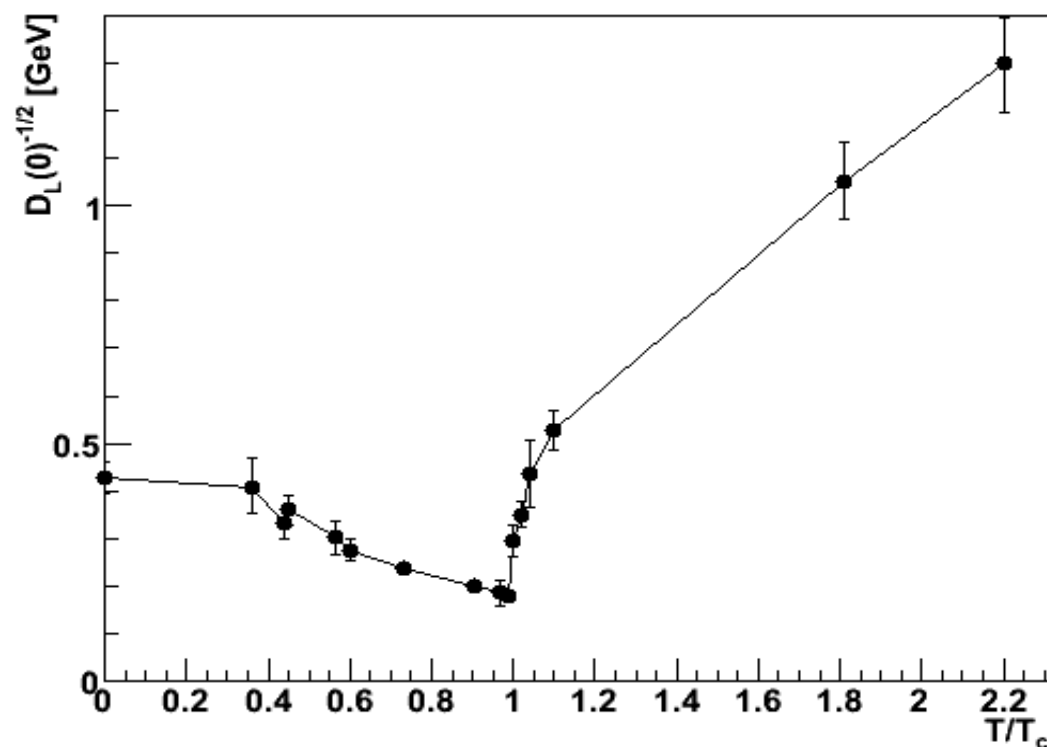
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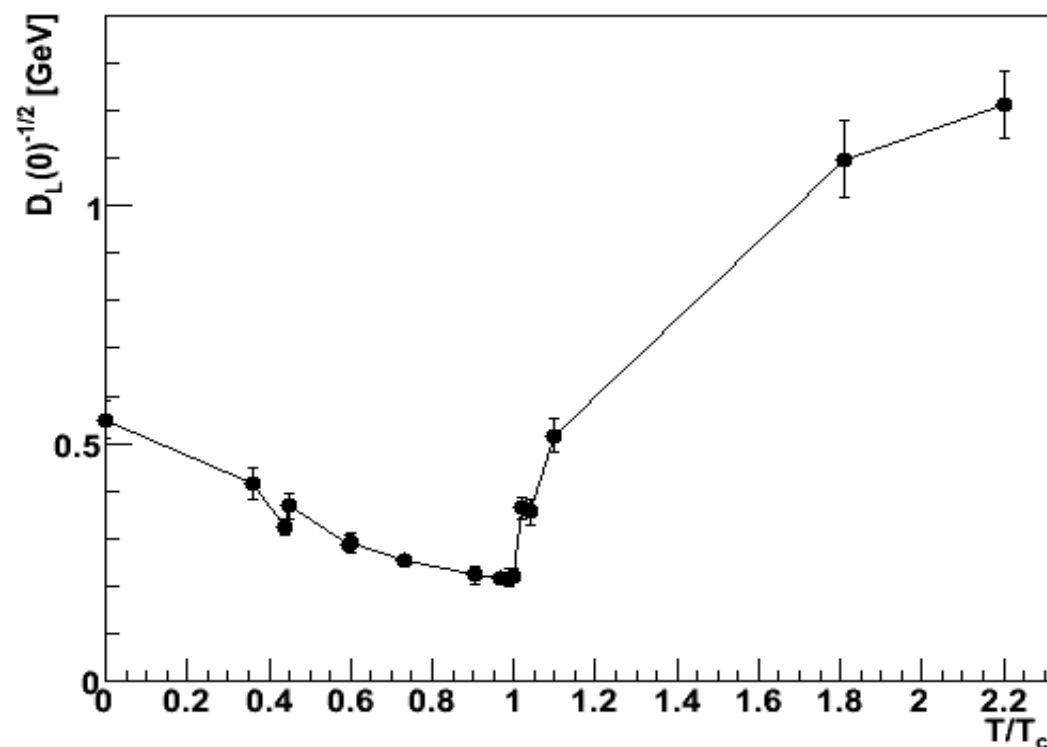


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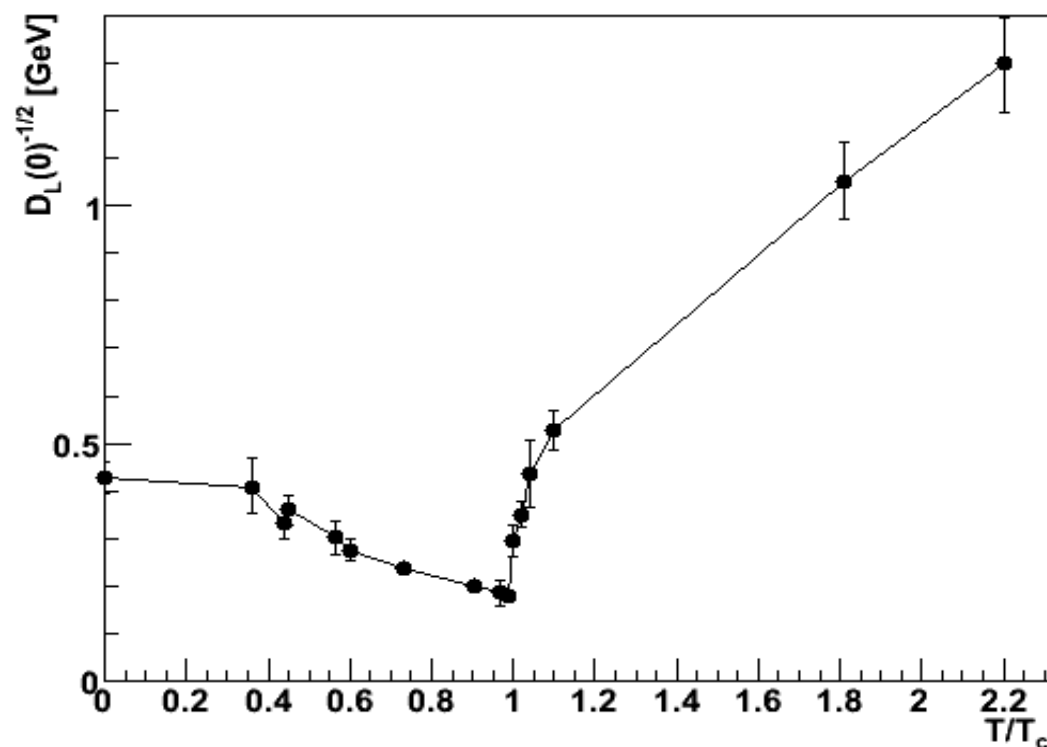
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 - Jump instead of rapid change? - Could distinguish the order

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- Application to quarks and mesons: See talks by J. Braun, C. S. Fischer, L. Haas, J. Müller, J. M. Pawłowski