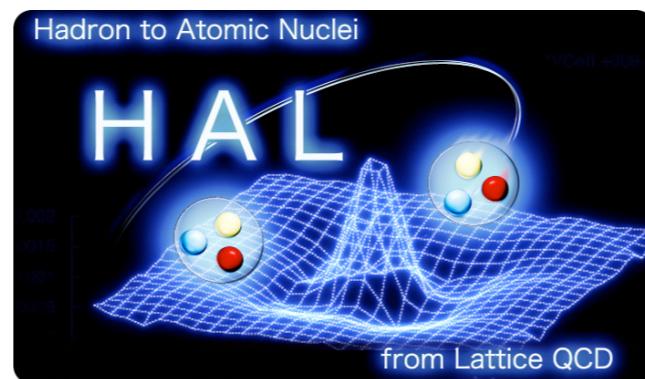


Lattice QCD studies of dibaryon candidates

Shinya Gongyo (RIKEN)
for HAL QCD collaboration



HAL(Hadrons to Atomic nuclei from Lattice) QCD Collaboration

K.Sasaki(YITP), S. Aoki (YITP), T. Doi (RIKEN), F. Etiminan (Birjand U.),
T. Hatsuda (RIKEN), Y. Ikeda (YITP), T. Inoue (Nihon Univ.),
T. Iritani (RIKEN), N. Ishii (RCNP) , D. Kawai (YITP),
T. Miyamoto (YITP), K. Murano (RCNP), H. Nemura (RCNP)

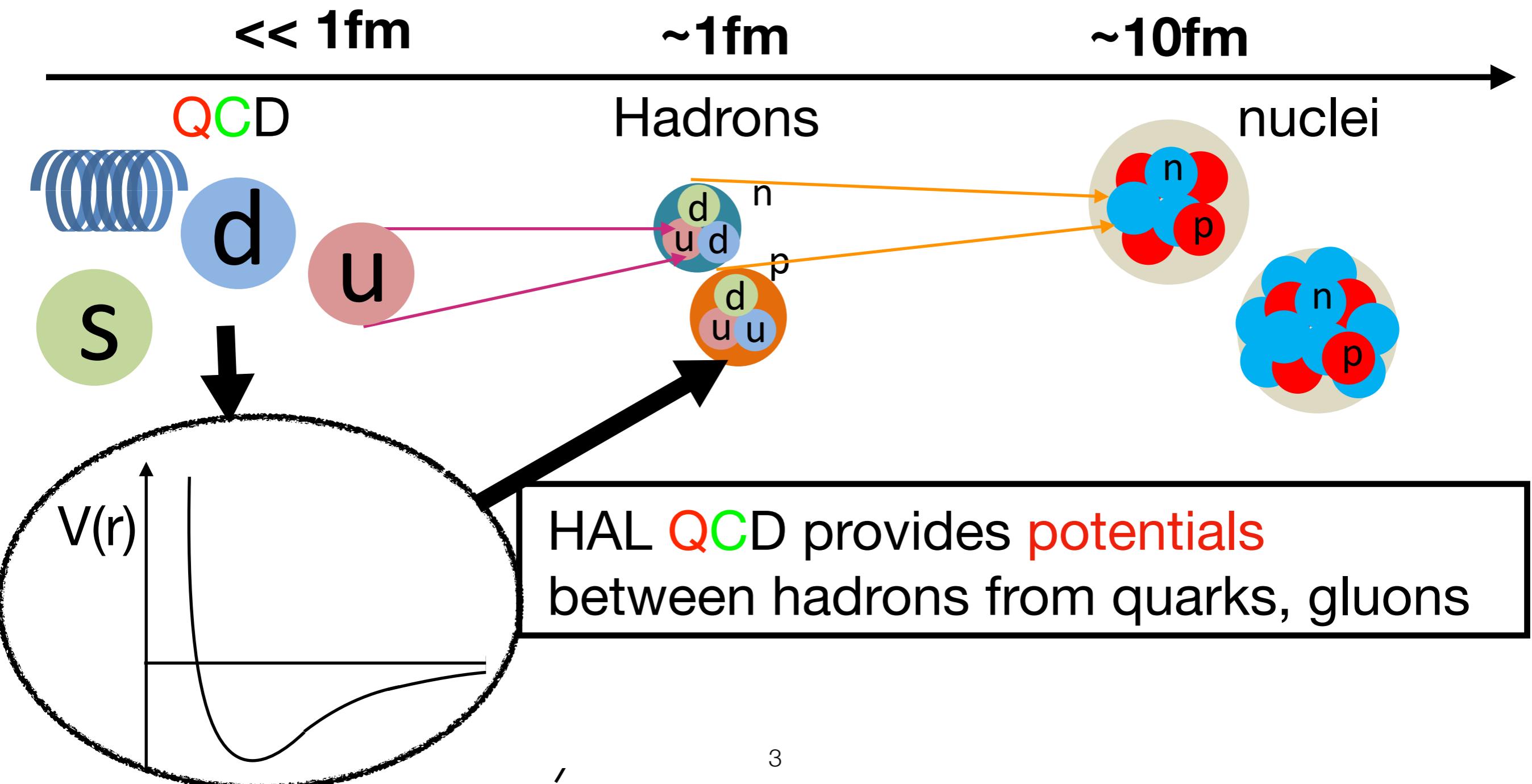
10-15.Sep.2017@EXA2017 (Vienna)

Outline

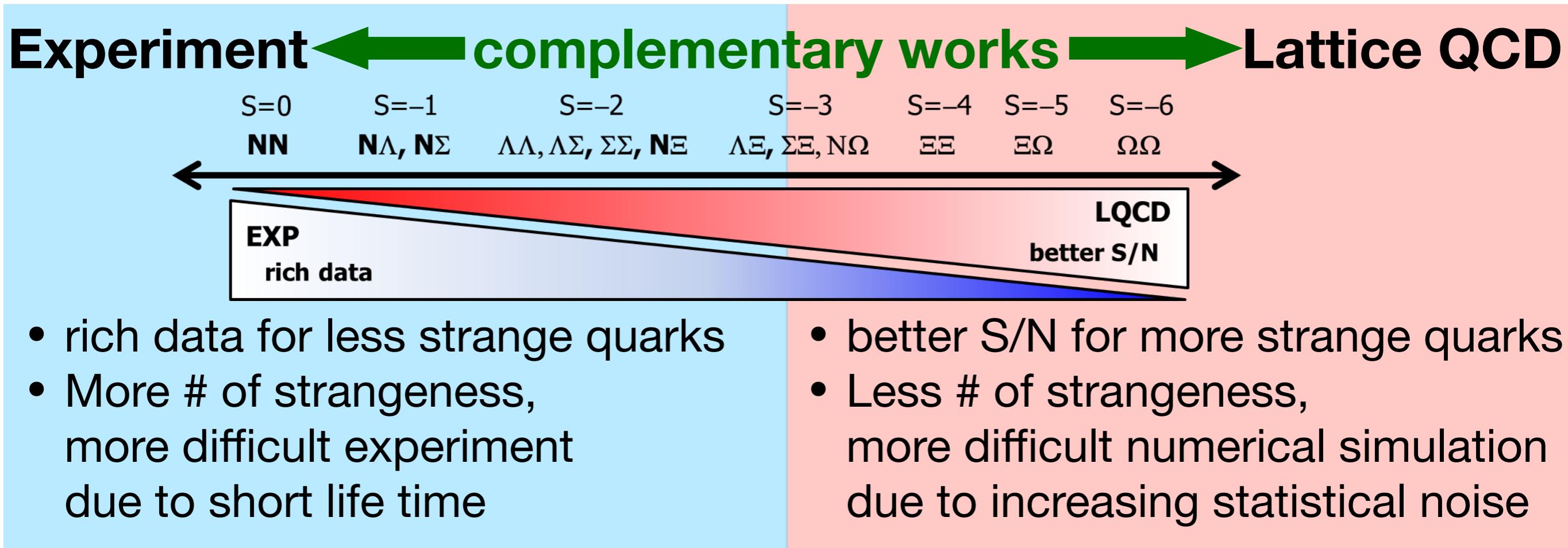
- Introduction
 - What's HAL QCD method and its role?
 - Dibaryon candidates from model works
- Theoretical framework for HAL QCD method
- results at heavy quark masses
- results **at physical quark masses**

Introduction

- HAL QCD method: we study hadron physics from QCD (quarks and gluons) —first-principles calculation—



role of our work



models & EFTs

Best to collaborate with three fields to understand hadron physics

Dibaryon candidates

model study gives the prediction of dibaryons

- H-dibaryon

R.L. Jaffe PRL38(1977)

- $N\Omega$ system

F.Wang et al. PRC51(1995)

Q.B.Li, P.N.Shen, EPJA8(2000)

- $\Delta\Delta$ system, $\Omega\Omega$ system

F.J.Dyson, N-H.Xuong, PRL13(1964)

M.Oka, K.Yazaki, PLB 90(1980)

found in experiment
(CELSIUS/WASA
PRL 102, 052301 (2009))

- B.E. largely depends on the model parameters
- Depending on models, the dibaryon does not exist
Lattice QCD avoids these problems.
- Some dibaryon candidates include decuplet baryons
- We focus on the channels where dibaryon candidates exit

Outline

- Introduction
 - What's HAL QCD method and its role?
 - Dibaryon candidates from model works
- **Theoretical framework for HAL QCD method**
- results of $N\Omega$, $\Delta\Delta$, $\Omega\Omega$ interactions at heavy quark masses
- results of $\Omega\Omega$ interactions at physical quark masses

How to get the potential from QCD

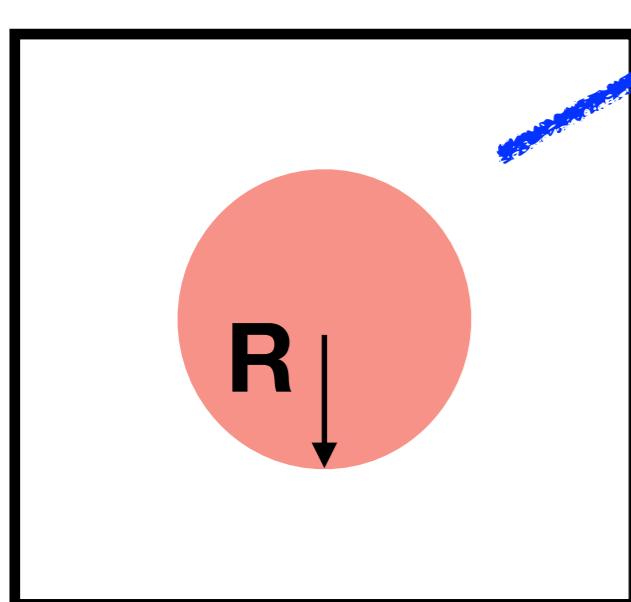
Key quantity: Nambu-Bethe-Salpeter (NBS) wave function

$$\Psi_n(\vec{r}) e^{-E_n t} = \sum_{\vec{x}} \langle 0 | B_1(t, \vec{r} + \vec{x}) B_2(t, \vec{x}) | E_n \rangle$$

Local operators $B_1 \& B_2$ for decuplet baryons

$$D_{\mu\alpha} = \epsilon_{abc} (q^{aT} C \gamma_\mu q^b) q_\alpha^c$$

Outside interactions (asymptotic region)
Helmholtz eq. is satisfied for $r \gg R$



$$(\vec{p}_n^2 + \nabla^2) \Psi_n(\vec{r}) = 0 \quad \Psi_n(\vec{r}) \sim A \frac{\sin(kr + \delta_l(k))}{kr}$$

$S(k) = e^{2i\delta(k)}$ NBS includes information
on the phase shifts & S matrix

How to get the potential from QCD

Key quantity: Nambu-Bethe-Salpeter (NBS) wave function

$$\Psi_n(\vec{r}) e^{-E_n t} = \sum_{\vec{x}} \langle 0 | B_1(t, \vec{r} + \vec{x}) B_2(t, \vec{x}) | E_n \rangle$$

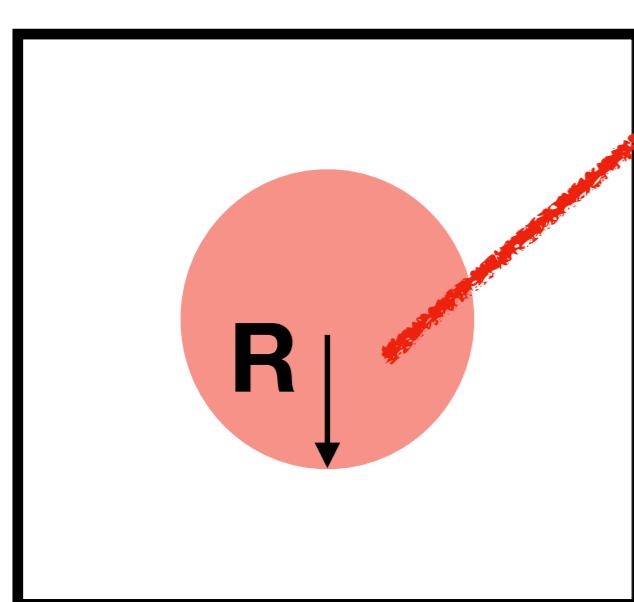
Local operators $B_1 \& B_2$ for decuplet baryons

$$D_{\mu\alpha} = \epsilon_{abc} (q^{aT} C \gamma_\mu q^b) q_\alpha^c$$

Inside interactions ($r < R$)

Schroedinger-type eq. is satisfied:

$$(\vec{p}_n^2 + \nabla^2) \Psi_n(\vec{r}) = 2\mu \int d\vec{r}' U(\vec{r}, \vec{r}') \Psi_n(\vec{r}')$$



HAL QCD method extracts the nonlocal potential $U(r, r')$ from NBS w.f.

Nonlocal potential $U(\mathbf{r}, \mathbf{r}')$

$$(\vec{p}_n^2 + \nabla^2) \Psi_n(\vec{r}) = 2\mu \int d\vec{r}' U(\vec{r}, \vec{r}') \Psi_n(\vec{r}')$$

Remarkable facts for the non-local potential $U(\mathbf{r}, \mathbf{r}')$

- The potential is given by energy-independent potential, but non-locality cannot be removed.
- The local potential can be obtained by its derivative expansion:

$$\begin{aligned} U(\vec{r}, \vec{r}') &= \frac{V_c(r) + V_\sigma(r)(\vec{S}_1 \cdot \vec{S}_2) + S_{12}V_{T_1}(r)}{+ O(\nabla^2)} \\ &= \underline{V_C^{eff}(r)} + O(\nabla^2) \end{aligned}$$

- The convergence of the expansion can be checked
- The potential includes the tensor parts

How to extract the NBS w.f. on lattice

4pt correlation function

$$\mathcal{G}(\vec{x}, \vec{y}, t - t_0; J^P) = \langle 0 | B_1(\vec{y}, t) B_2(\vec{x}, t) \bar{\mathcal{J}}(t_0; J^P) | 0 \rangle$$

$$1 = \sum_n |E_n\rangle \langle E_n|$$

$$\begin{aligned} &\Rightarrow = \sum_{n=0}^{\infty} A_n \Psi_n(\vec{r}) e^{-E_n(t-t_0)} \\ t \gg t_0 &\rightarrow A_0 \Psi_0(\vec{r}) e^{-E_0(t-t_0)} \end{aligned}$$

- NBS w.f. can be extracted from 4pt correlation function
- Elastic saturation & **ground state** saturation are required.

$$E_1 = \sqrt{E_0^2 + (2\pi/L)^2} \sim E_0 \quad (L \gg 1)$$

This becomes more serious as lattice size becomes larger
 In HAL method, this is avoided by time-dependent extension.
 [c.f. serious problem for Luscher's method, see Iritani 2016&2017]

Technical development: Time-dependent method

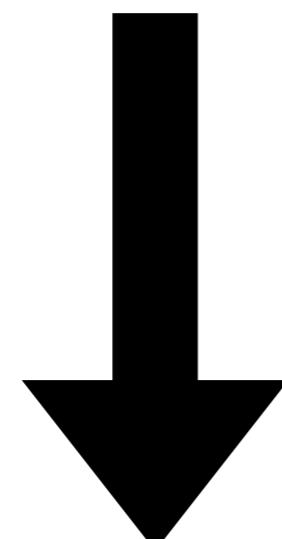
normalized 4pt correlation function:

$$m_{B_1} = m_{B_2}$$

$$\mathcal{R}(\vec{x}, \vec{y}, t - t_0; J^P) = e^{(m_{B_1} + m_{B_2})t} \langle 0 | B_1(\vec{y}, t) B_2(\vec{x}, t) \bar{\mathcal{J}}(t_0; J^P) | 0 \rangle$$

$$\xrightarrow{\quad} \simeq \sum_n A_n \Psi_n(\vec{r}) e^{-\Delta E_n t} \quad \Delta E_n = 2\sqrt{m_B^2 + k_n^2} - 2m_B$$

elastic saturation



$$1. \frac{\partial}{\partial t}$$

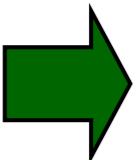
$$2. \Delta E_n = \frac{k_n^2}{m_B} - \frac{\Delta E_n^2}{4m_N}$$

$$\left(\frac{1}{4m_B} \frac{\partial^2}{\partial t^2} - \frac{\partial}{\partial t} + \frac{\nabla^2}{m_B} \right) \mathcal{R} = \int U(\vec{r}, \vec{r}') \mathcal{R} d^3 r'$$

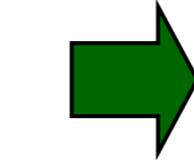
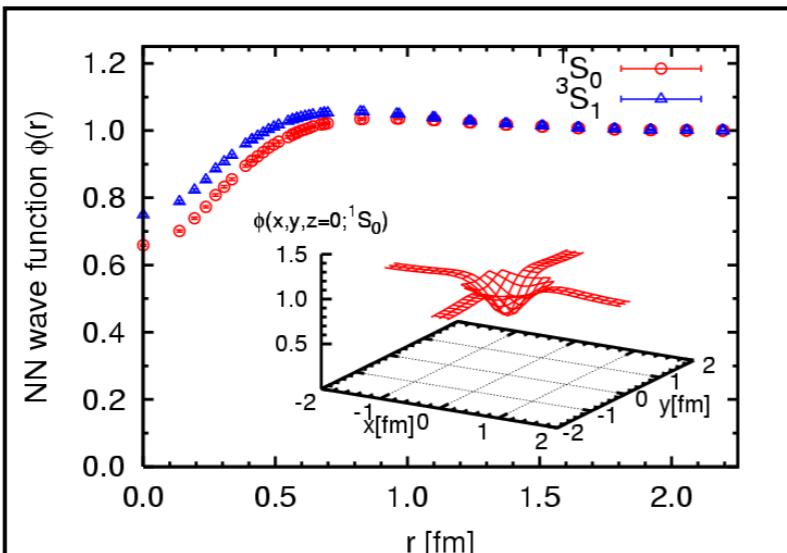
- Potential can be extracted directly from the correlator
- No need for ground state extraction

Strategy for HAL method

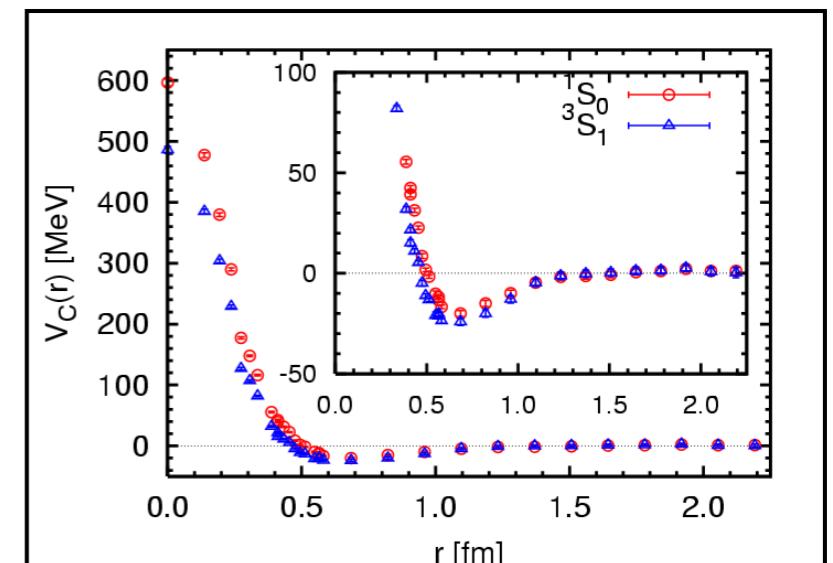
Lattice QCD



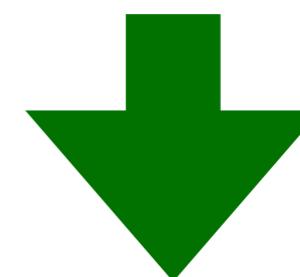
NBS wave func.



Lat Hadron Force



Time-dependent HAL method



observables
phase shift, binding energy,

Outline

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interaction of decuplet baryons

Irreducible representation involving with decuplet baryons

I. decuplet-octet system

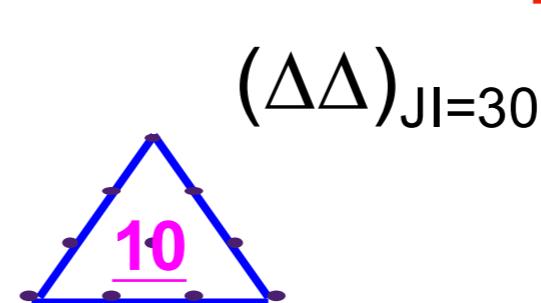
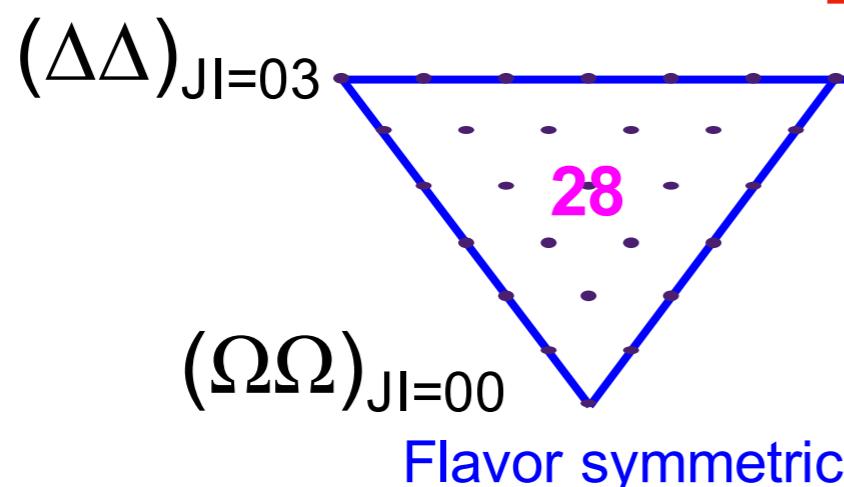
$$10 \otimes 8 = 35 \oplus \boxed{8} \oplus 10 \oplus 27$$

M. Oka PRD38 -298

strong attractive CMI is expected
dibaryon (ΩN in $J^P(I) = 2^+(1/2)$) is expected

II. decuplet-decuplet system

$$10 \otimes 10 = \boxed{28} \oplus 27 \oplus 35 \oplus \boxed{\bar{10}}$$

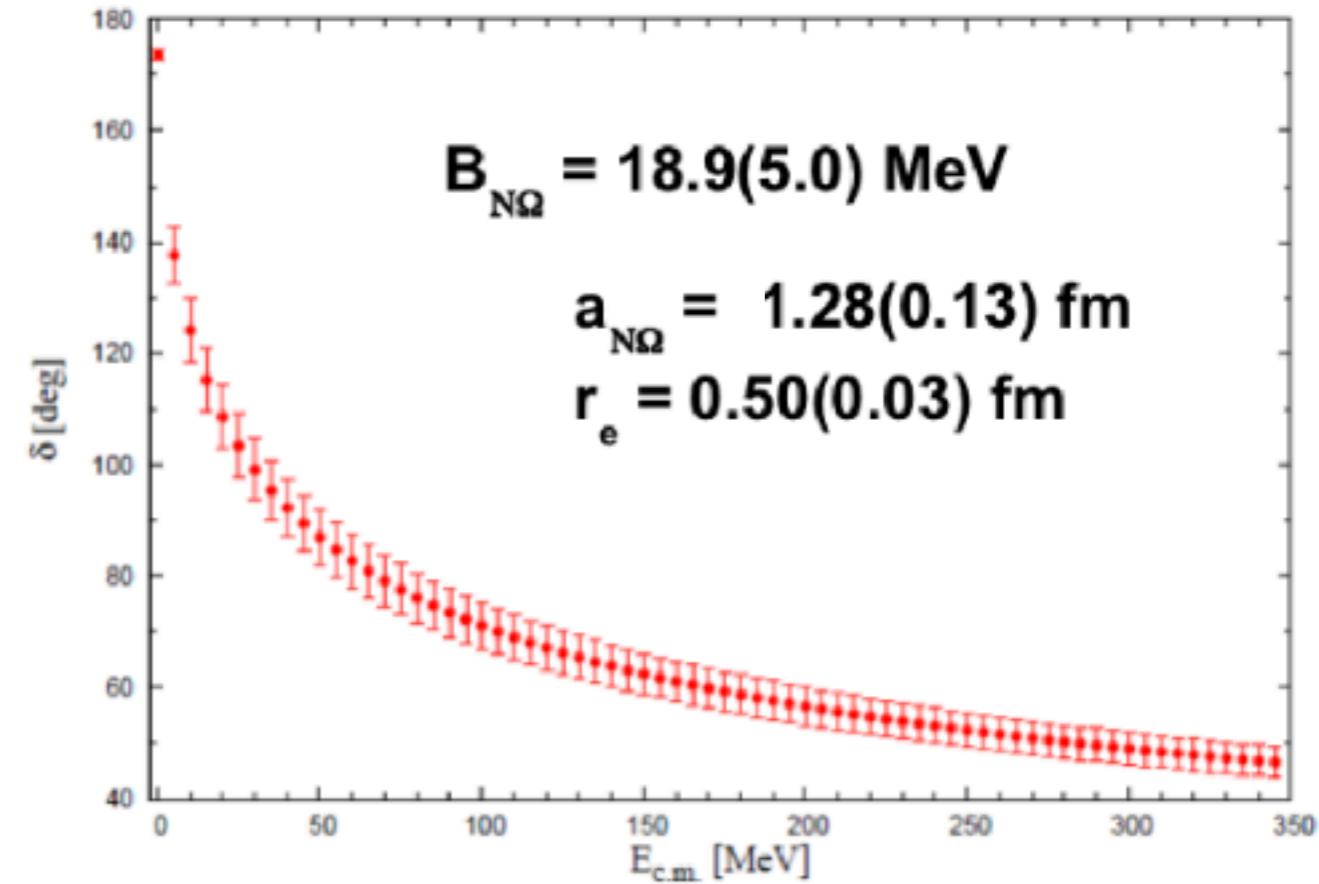
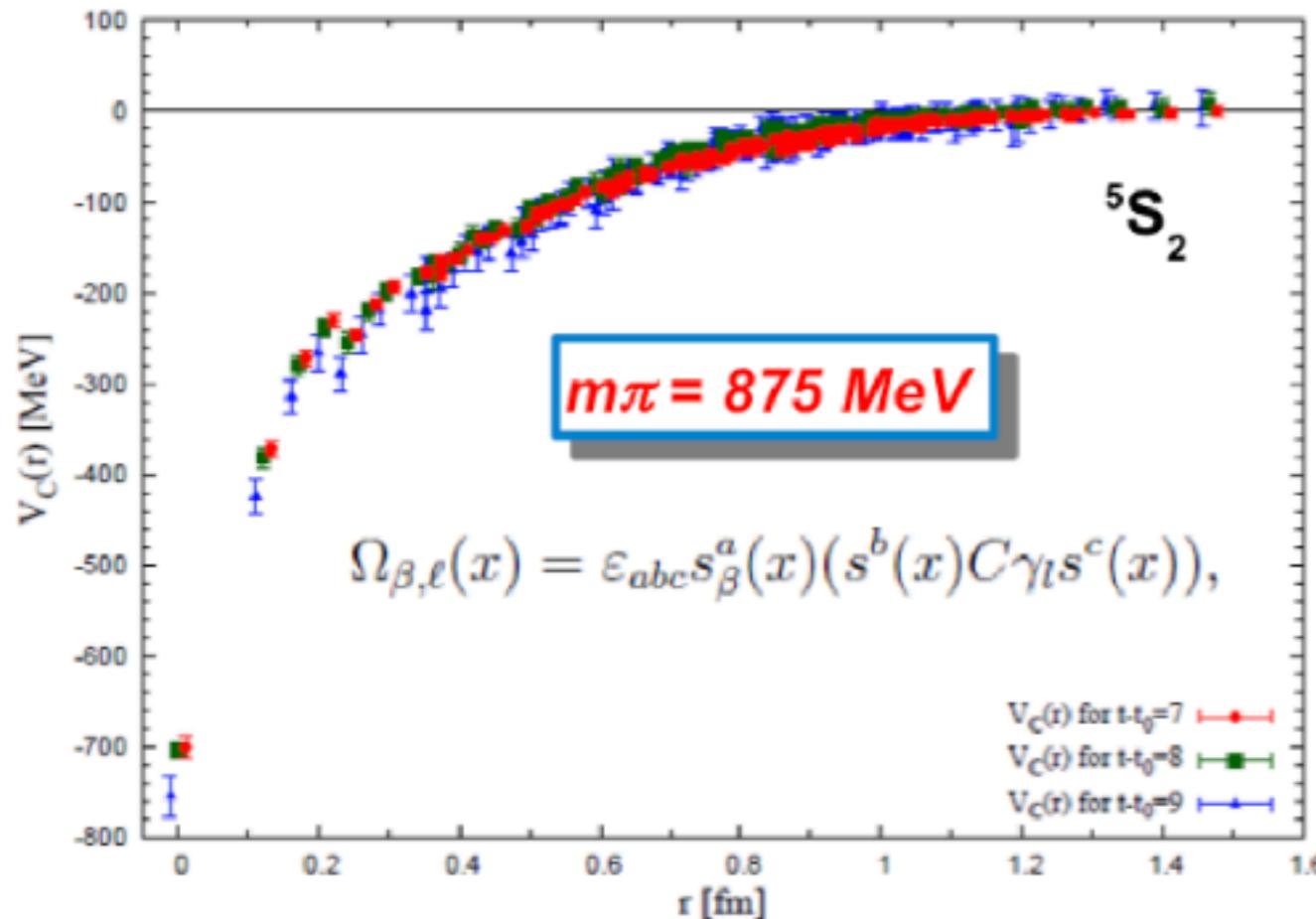


I. decuplet-octet system $N\Omega$ system

N Ω system $J^P(l) = 2^+(1/2)$

Nf = 2+1 full QCD with L= 1.9fm, m π =875MeV

F. Etminan et.al (HAL QCD), NPA928(2014)89

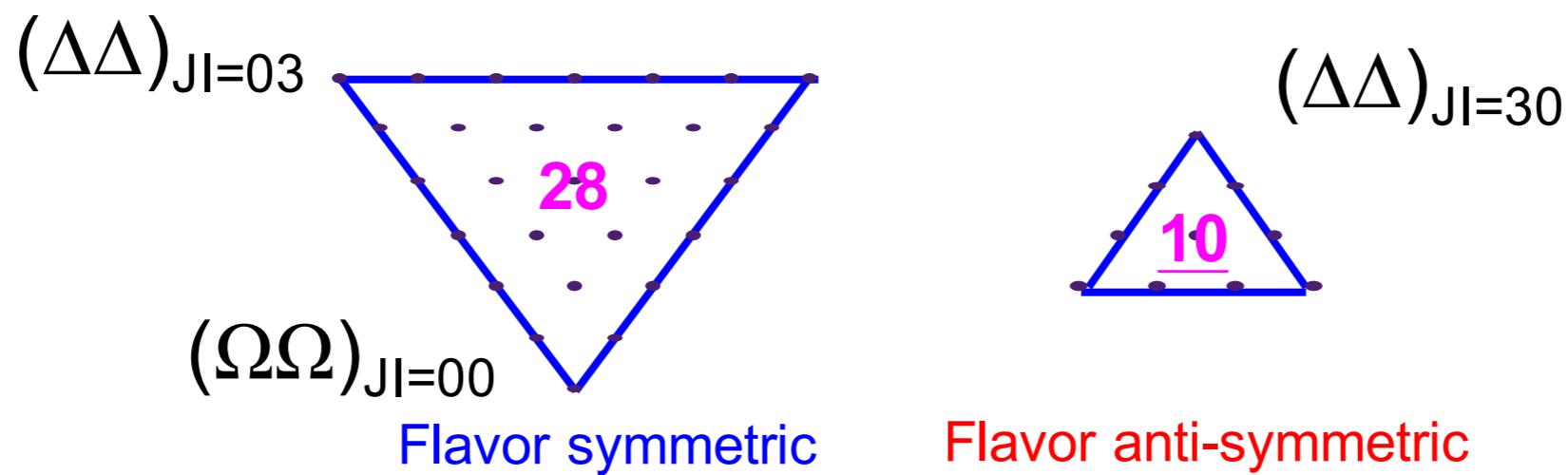


- In short range, there is no repulsive core
- strong attraction leads to deep bound state
<= the signal is expected to be found in HIC

Physical point result will be open. (Iritani et al.)

II. decuplet-decuplet system

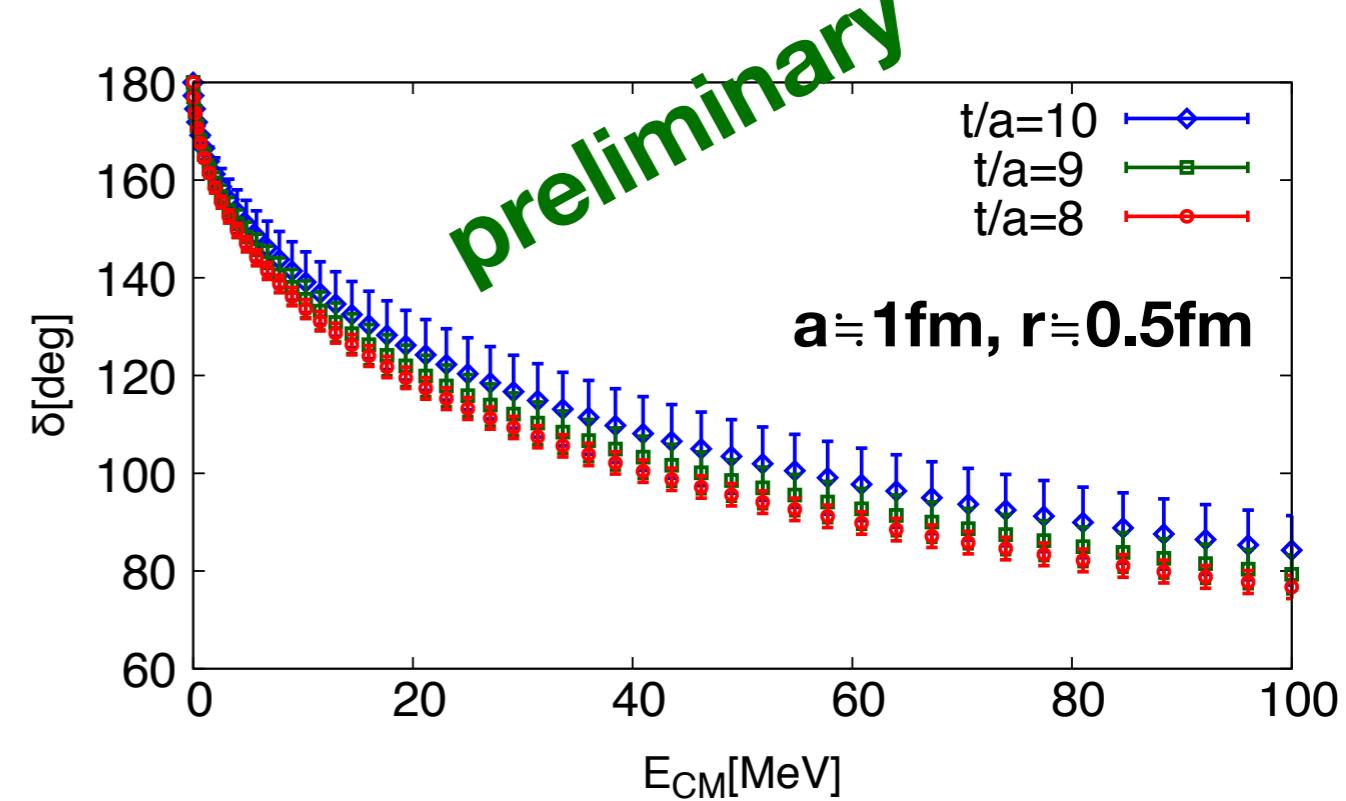
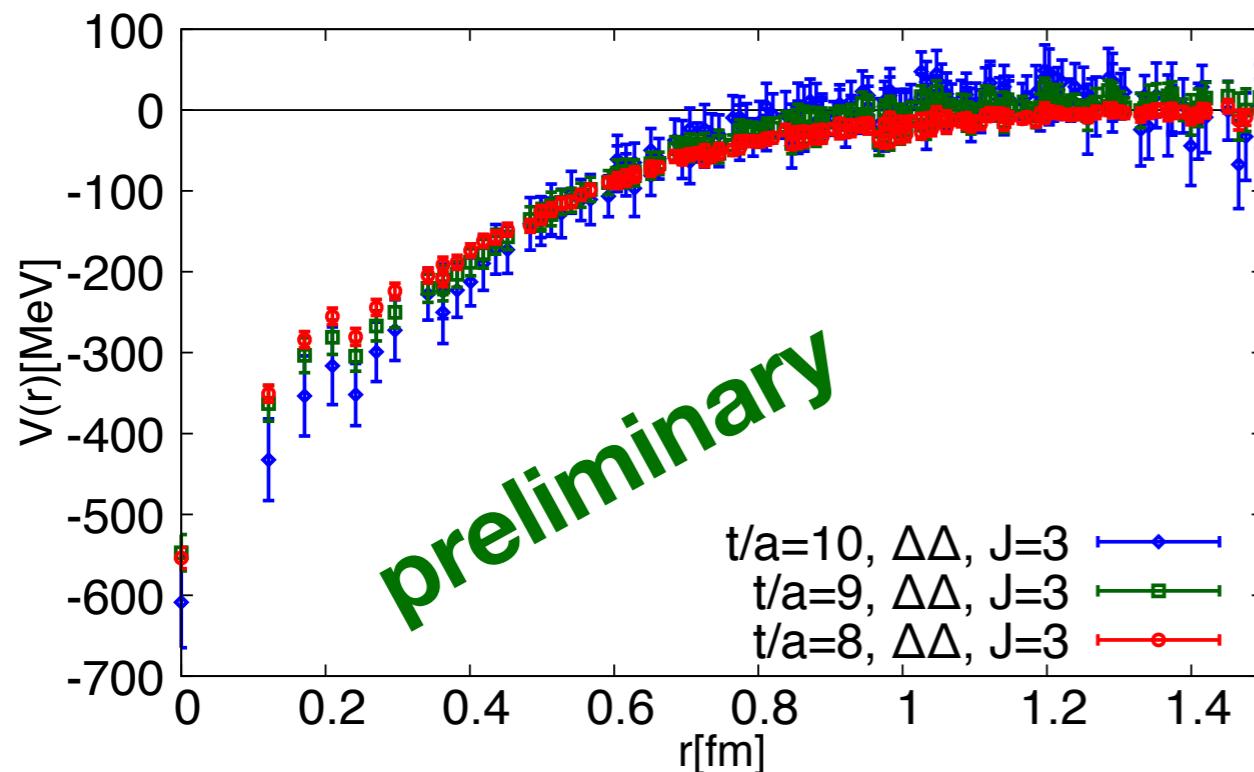
$$10 \otimes 10 = \boxed{28} \oplus 27 \oplus 35 \oplus \boxed{\bar{10}}$$



$\overline{10}$ plet in decuplet-decuplet system

$N_f = 2+1$ full QCD with $L = 1.93\text{fm}$, $m_\pi=1015\text{MeV}$, **SU(3) limit**

$\Delta\Delta$ in $J^p(l) = 3^+(0)$

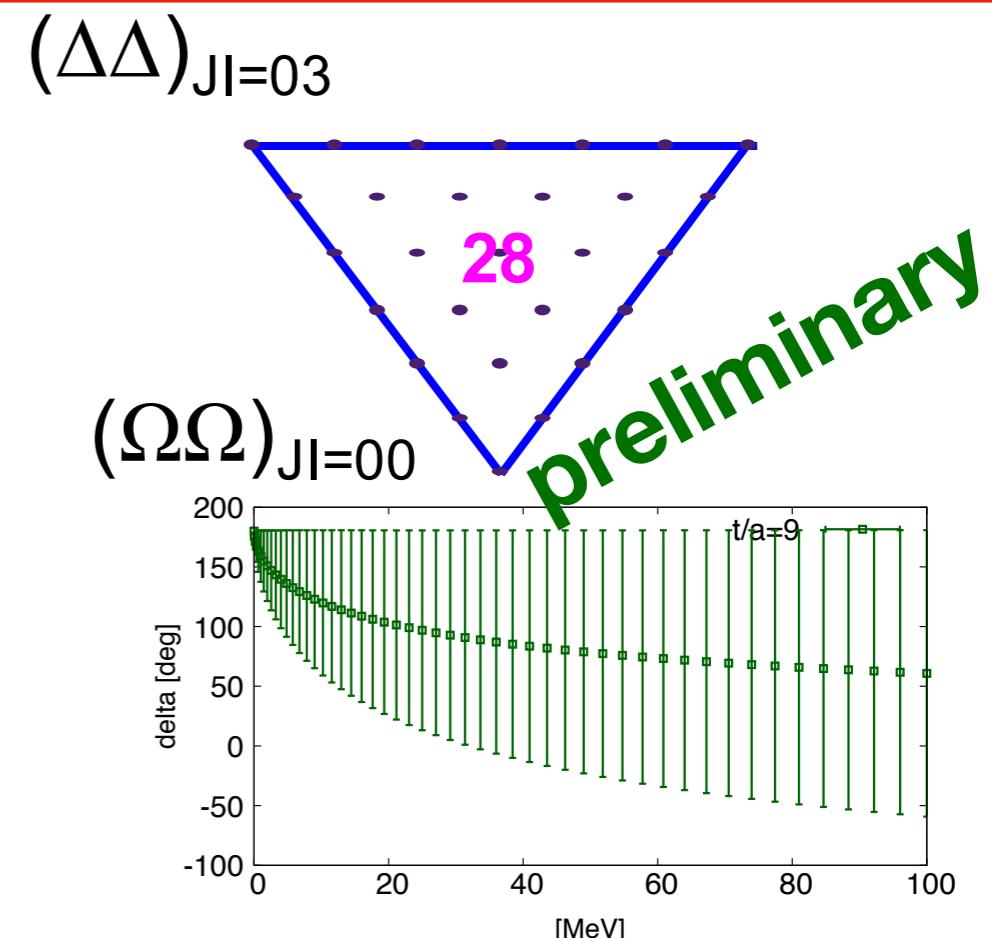
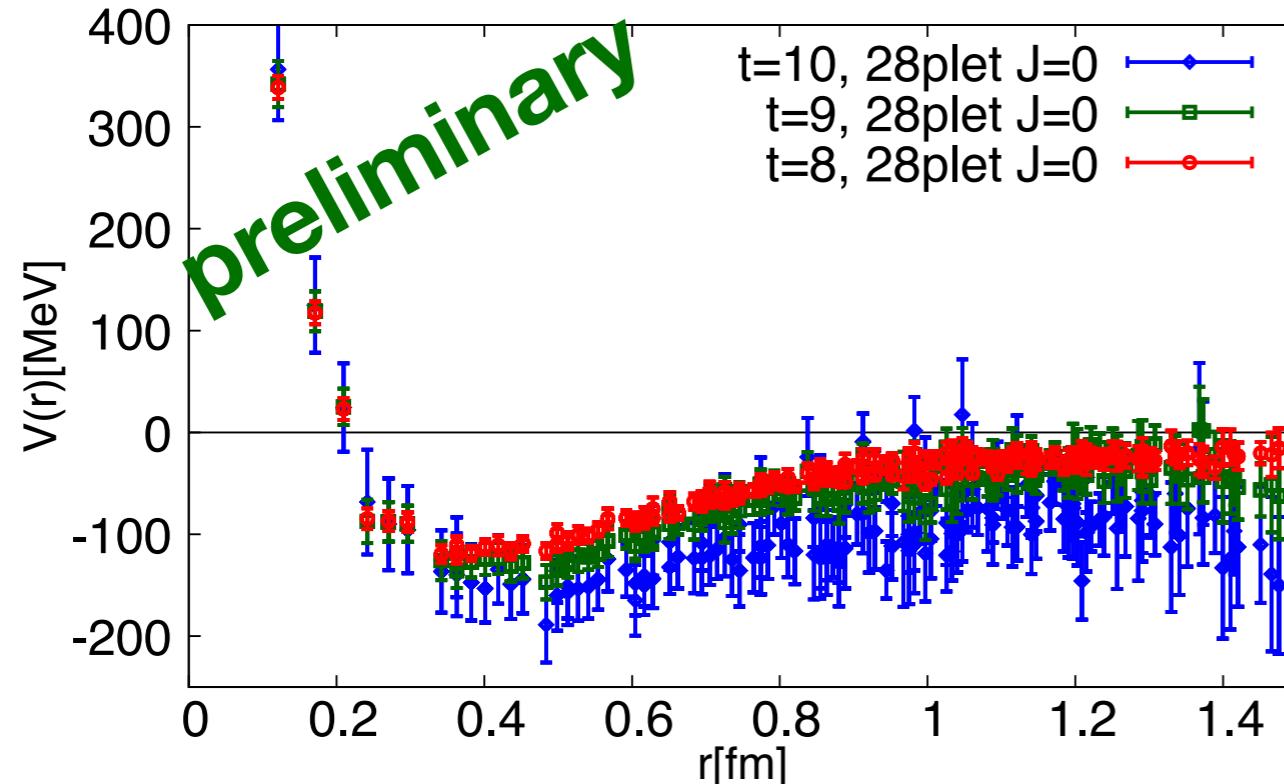


- In short range, there is no repulsive core
- strong attraction leads to deep bound state (ABC effect)

28 plet in decuplet-decuplet system

Nf=2+1 full QCD with L = 1.93fm, $m_\pi = 1015\text{MeV}$, SU(3) limit

$\Omega\Omega$ in $J=0$ is identical with $\Delta\Delta$ in $J=0$ due to SU(3) symmetry



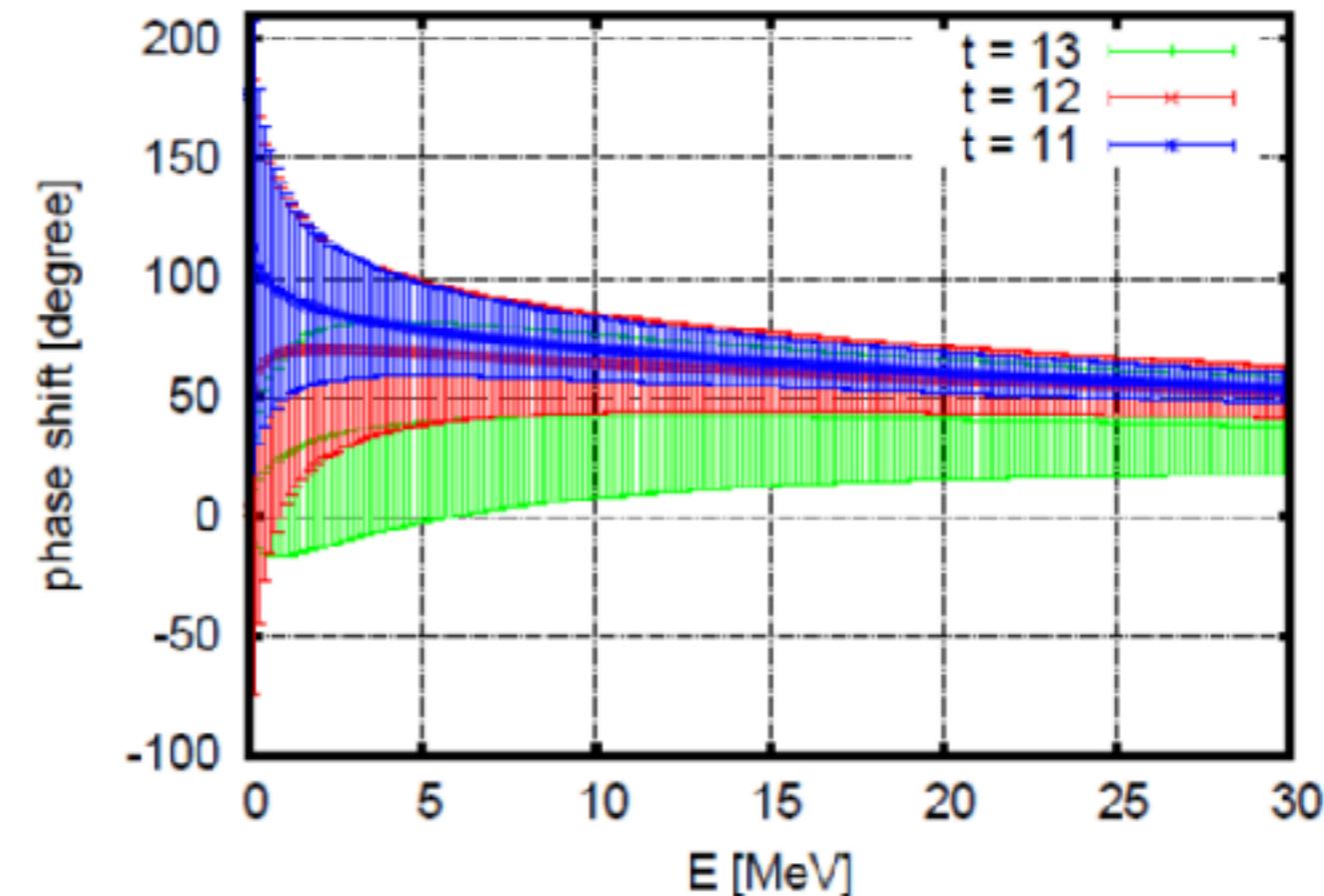
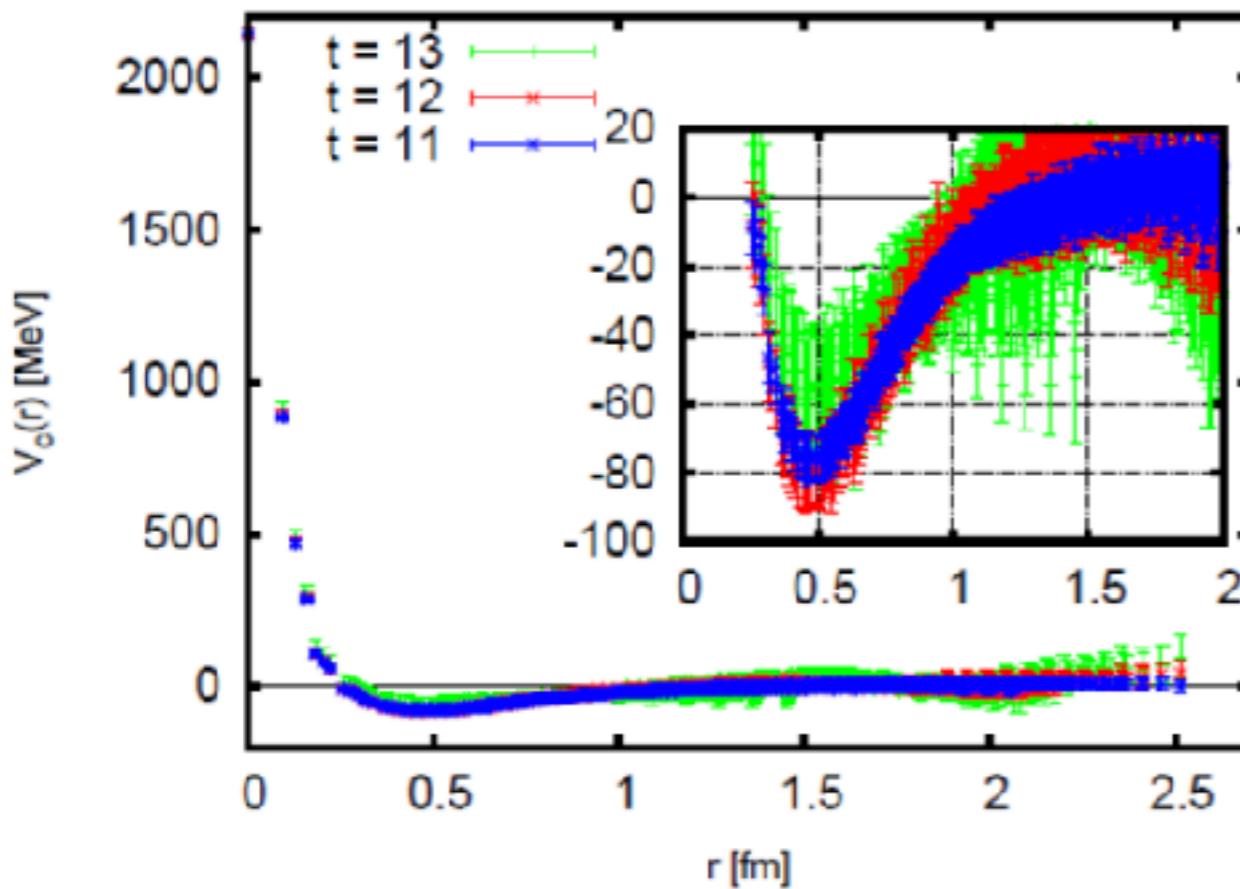
- Short range repulsive core and attractive pocket are found
- Phase shift shows the system is in the unitary limit
- *Is it the same situation in other conditions?
(lighter pion mass & SU(3) breaking case)?*

28 plet in decuplet-decuplet system

$N_f=2+1$ full QCD with $L = 3\text{fm}$, $m_\pi = 700\text{MeV}$

$\Omega\Omega$ in $J=0$

$m_\Omega = 1970\text{MeV}$



- Short range repulsive core and attractive pocket are found
- Phase shift shows the system is in the unitary limit
- *Is it the same situation even in physical pion mass?*

Decuplet-Decuplet interaction **at physical point**

Difficulties of Dec-Dec interaction at physical point

- decuplet baryons except for Ω -baryon decays into other hadrons via the strong interaction at physical point
- There are many coupled channels except for Omega-Omega interaction at physical point

We focus on Omg-Omg at physical point
in decuplet-decuplet interactions

Numerical Setup at (almost) physical mass

2+1 flavor gauge configurations

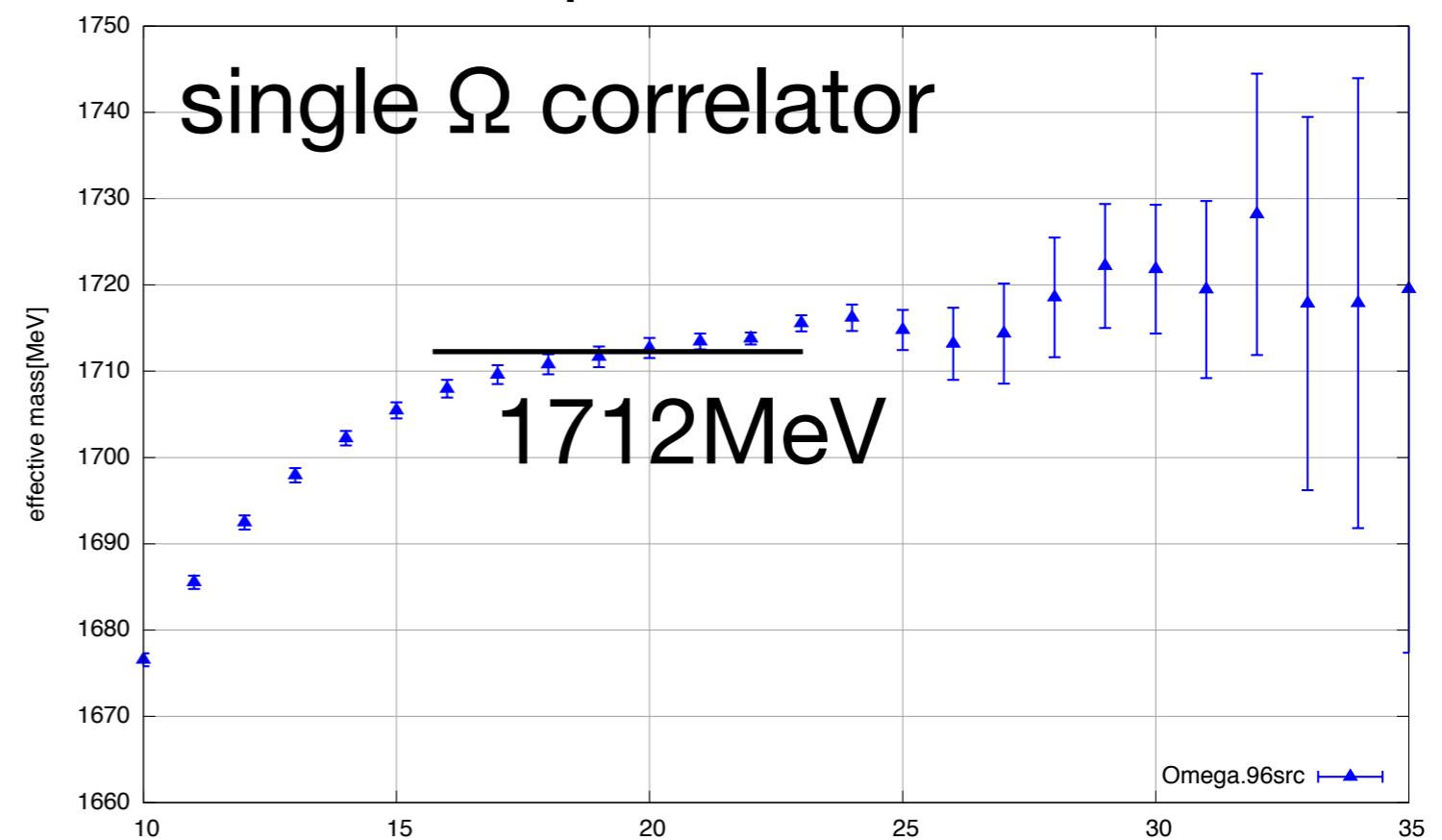
- Iwasaki gauge action & O(a) improved Wilson quark action
- $a = 0.0846$ [fm], $a^{-1} = 2333$ [MeV]
- $96^3 \times 96$ lattice, $L = 8.1$ [fm]
- 400 confs \times 48 source positions \times 4 rotations



K-computer [10PFlops]

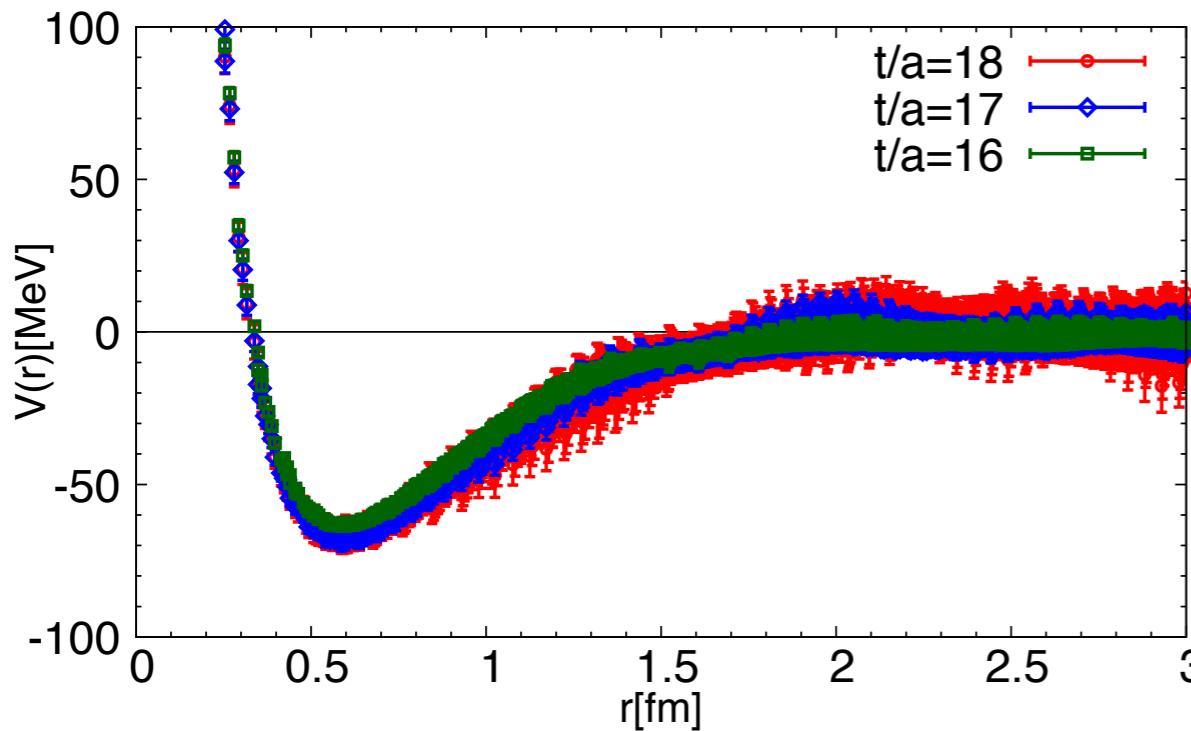
Wall source is employed. only Swave state is produced.

	[MeV]	phys.
π	146	8%
K	525	6%
N	964	3%
Ω	1712	2%



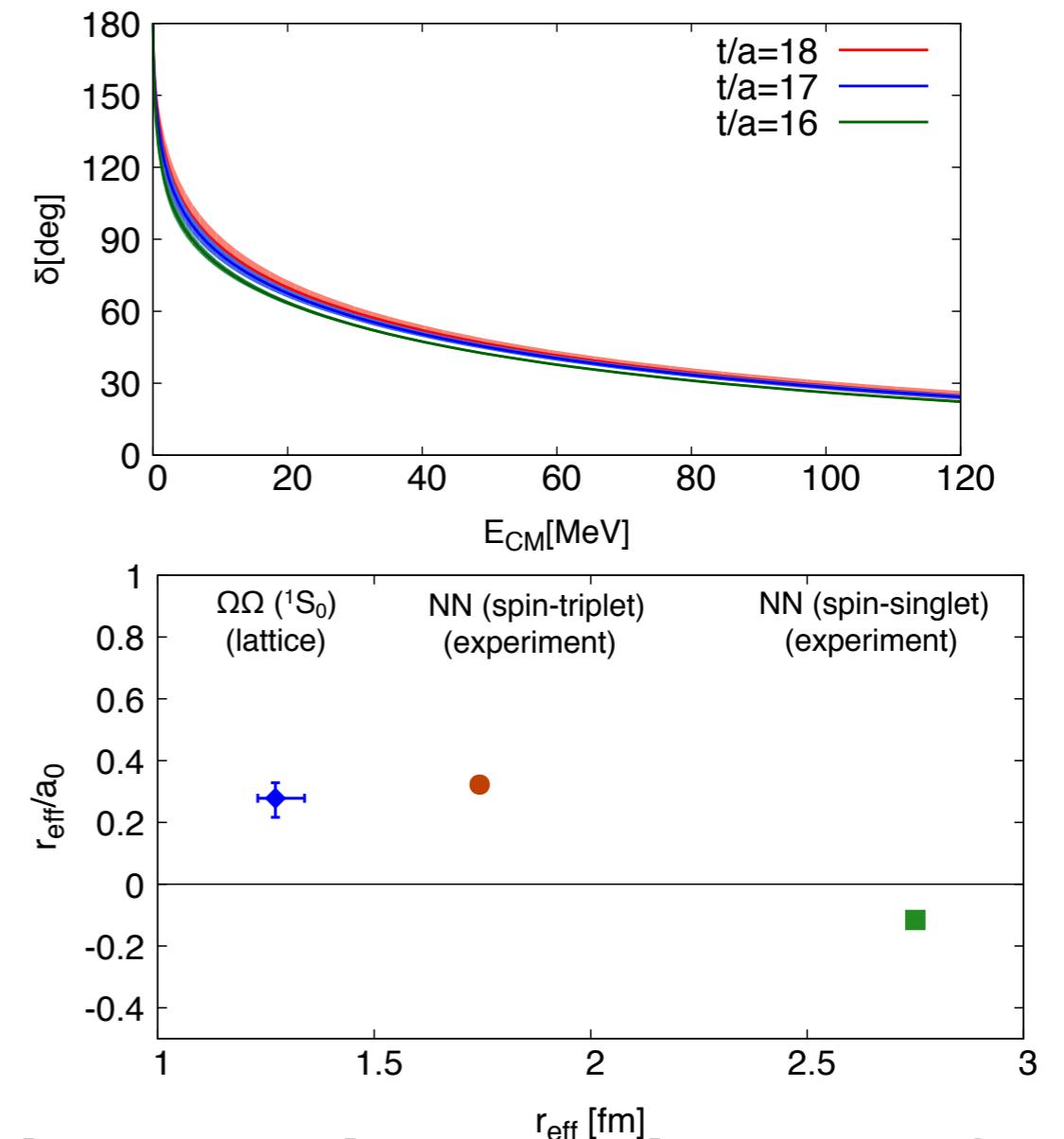
$\Omega\Omega$ in $J=0$

Nf=2+1 full QCD with $L = 8.1\text{fm}$, $m_\pi = 146\text{MeV}$



$$a_0^{(\Omega\Omega)} = 4.6(6)(^{+1.2}_{-0.5}) \text{ fm},$$

$$r_{\text{eff}}^{(\Omega\Omega)} = 1.27(3)(^{+0.06}_{-0.03}) \text{ fm}.$$

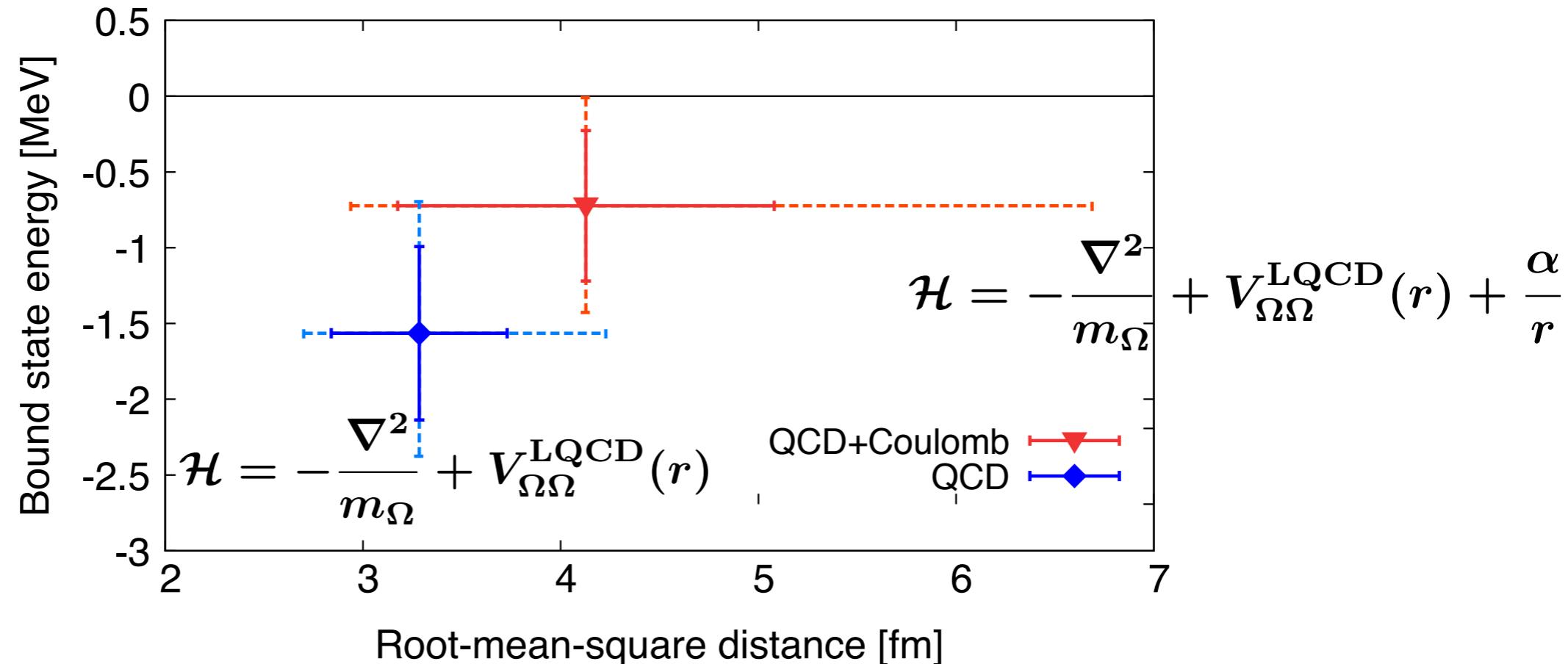


- Short range repulsive core and attractive pocket are found
- Phase shift shows the presence of a bound state
- It is very close to the unitary region ($r/a < 1$)

$\Omega\Omega$ in $J=0$

Binding energy and the Coulomb effect

“most strange dibaryon”

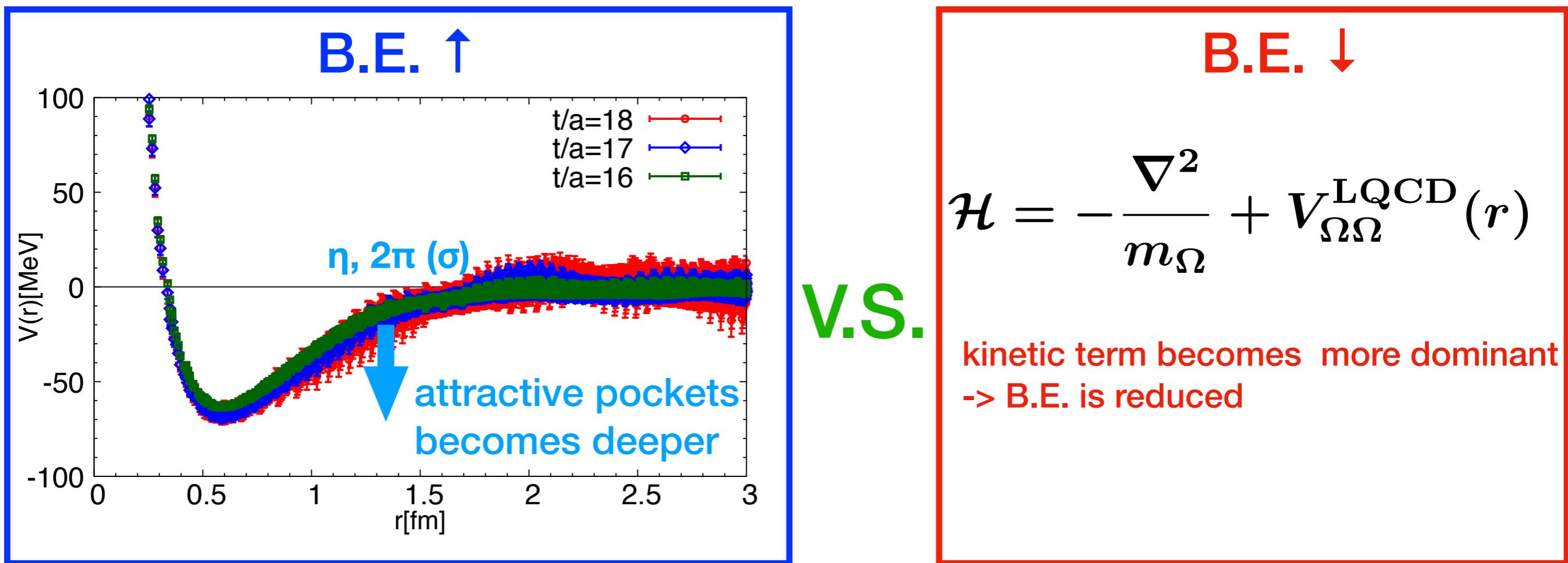


- Most strange dibaryon appears (within 1σ) even if Coulomb effect is considered.

$$(B_{\Omega\Omega}^{(\text{QCD})}, B_{\Omega\Omega}^{(\text{QCD+Coulomb})}) = (1.6(6)\text{MeV}, 0.7(5)\text{MeV})$$

Conservative estimate at exact phys. pt.

$m_\pi = 146 \text{ MeV} \rightarrow 135 \text{ MeV}$, $m_\Omega = 1712 \text{ MeV} \rightarrow 1672 \text{ MeV}$



conservative estimate:
only change the mass of schroedinger eq.

$$(B_{\Omega\Omega}^{(\text{QCD})}, B_{\Omega\Omega}^{(\text{QCD+Coulomb})}) = (1.6(6)\text{MeV}, 0.7(5)\text{MeV})$$
$$\rightarrow (1.3(5)\text{MeV}, 0.5(5)\text{MeV})$$

These changes are well within errors

Conclusion and future work

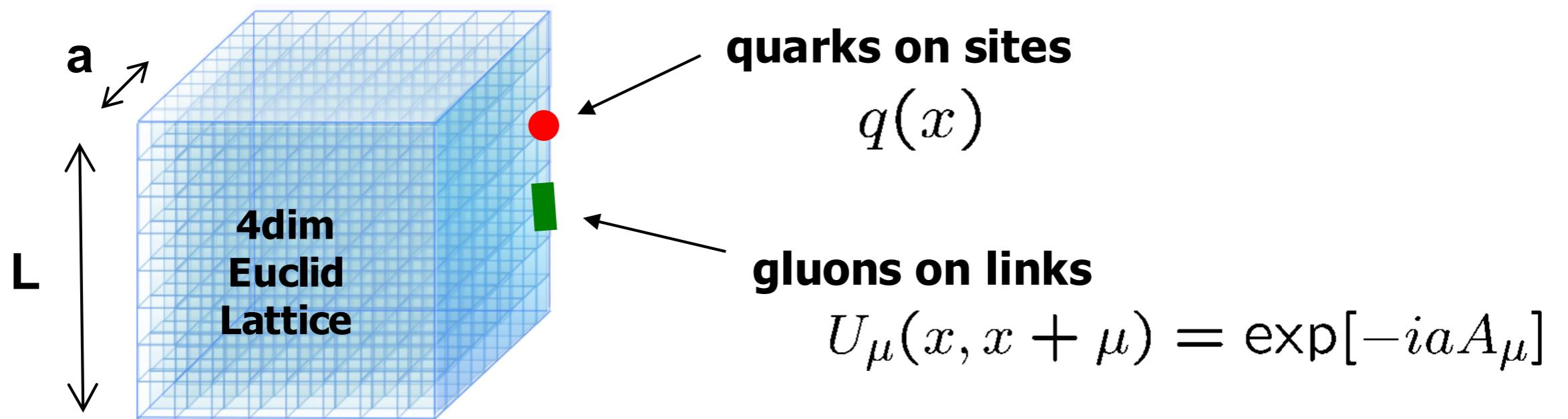
- We have investigated dibaryon candidates involving with decuplet baryon from lattice QCD
- heavy pion masses:
 - (i) ΩN interaction in (5S_2)
 - no repulsion core and only attractive region
 - a bound state (is expected to be found in HIC)
 - (ii) $\Delta\Delta$ interaction in (5S_2)
 - bound state in $\Delta\Delta$ interaction (7S_0)
 - a bound state (ABC effect)
- physical pion masses:
 - $\Omega\Omega$ interaction in (1S_0)
 - short range repulsive and attractive pocket
 - a very shallow bound state [Most strange dibaryon]
(or unitary region?)

*statistics will be increased
by two times!*

Back Slides

First-principles calculation (Lattice QCD)

$$Z = \int dU dq d\bar{q} e^{-S_E}$$



- Well-defined regularized system (finite a and L)
- Gauge-invariance manifest
- Fully-Nonperturbative
- DoF $\sim 10^9 \rightarrow$ Monte-Carlo w/ Euclid time

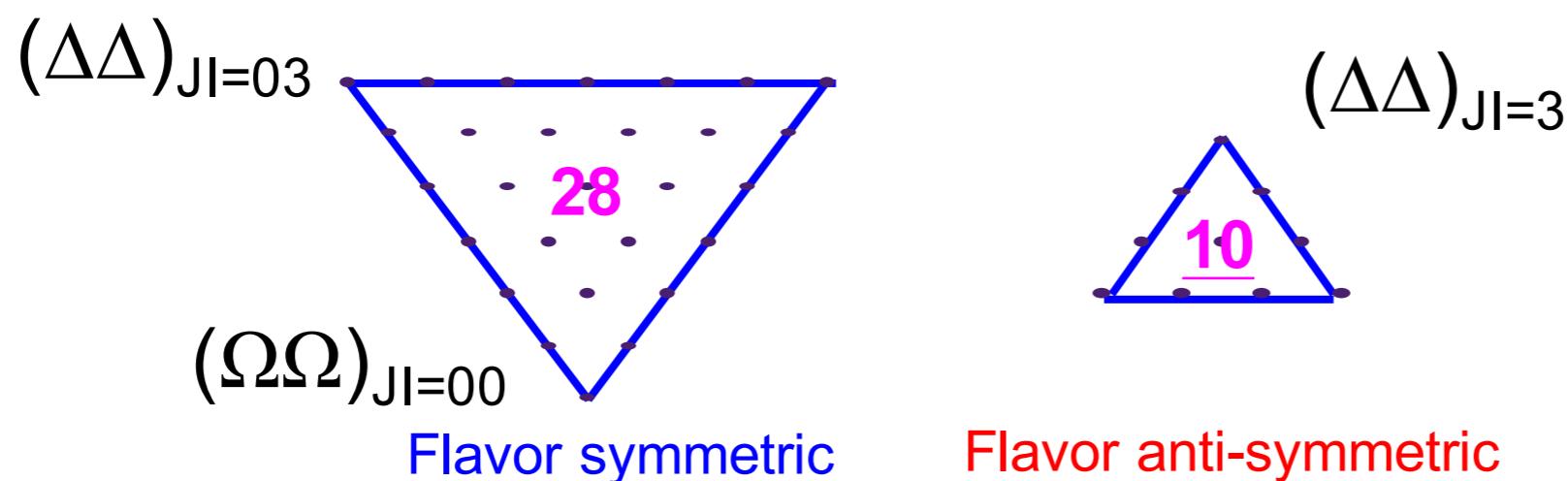
Significant theoretical and hardware advances

classification from CMI & quak pauli

Oka, Shimizu, and Yazaki NPA464 (1987)

- repulsive core is a result of Pauli principle and color-magnetic interaction for the quarks

$$10 \otimes 10 = \boxed{28} \oplus 27 \oplus 35 \oplus \boxed{\bar{10}}$$



	28plet (0+)	28plet(2+)	10*plet(1+)	10*plet (3+)
Pauli	allowed	forbidden	allowed	neutral
CMI	repulsive	-	Not attractive	-

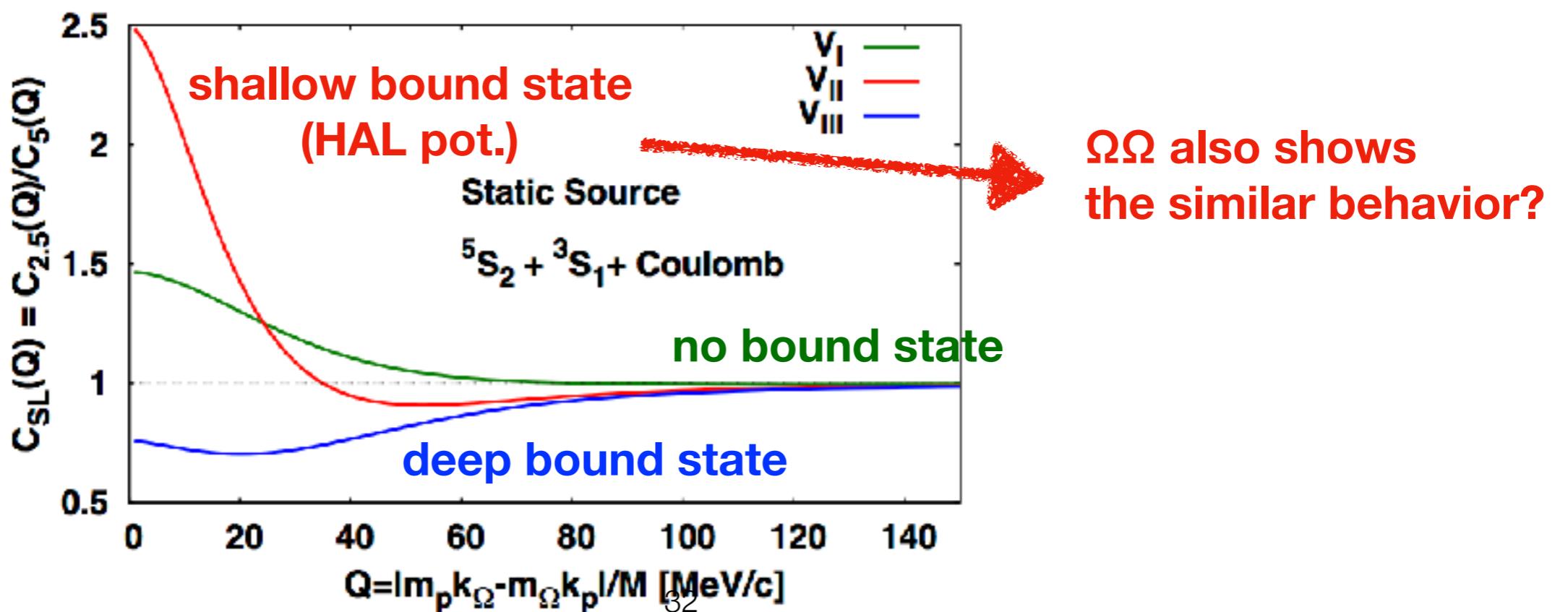
How to find a ΩN bound state in HIC

Morita, Ohnishi, Etminan, Hatsuda, 2016

$$C_{\text{SL}}(Q) \equiv \frac{C_{R_p, \Omega=2.5 \text{ fm}}(Q)}{C_{R_p, \Omega=5 \text{ fm}}(Q)},$$

$C_{R_p, \Omega}(Q)$: p Ω correlation function with effective size R

- (i) Comparison of the peripheral and central collisions for the same nuclear system
- (ii) Comparison of the central collisions with different system sizes
e.g. central Cu+Cu & central Au+Au collisions at RHIC.

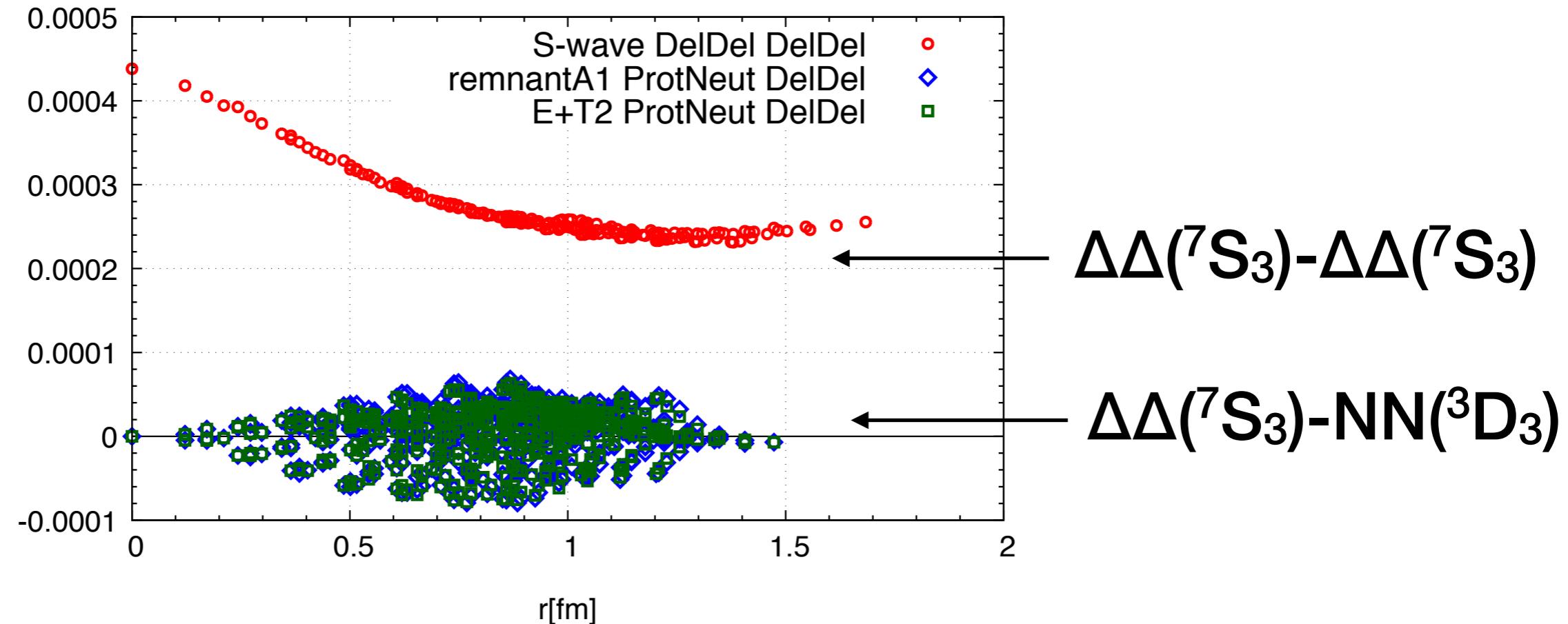


Coupled channel effects

$N_f = 2+1$ full QCD with $L = 1.93\text{fm}$, $m_\pi = 1015\text{MeV}$, SU(3) limit

Rcorrelators

$$m_\Delta \simeq 2230\text{MeV}$$
$$m_N \simeq 2030\text{MeV}$$



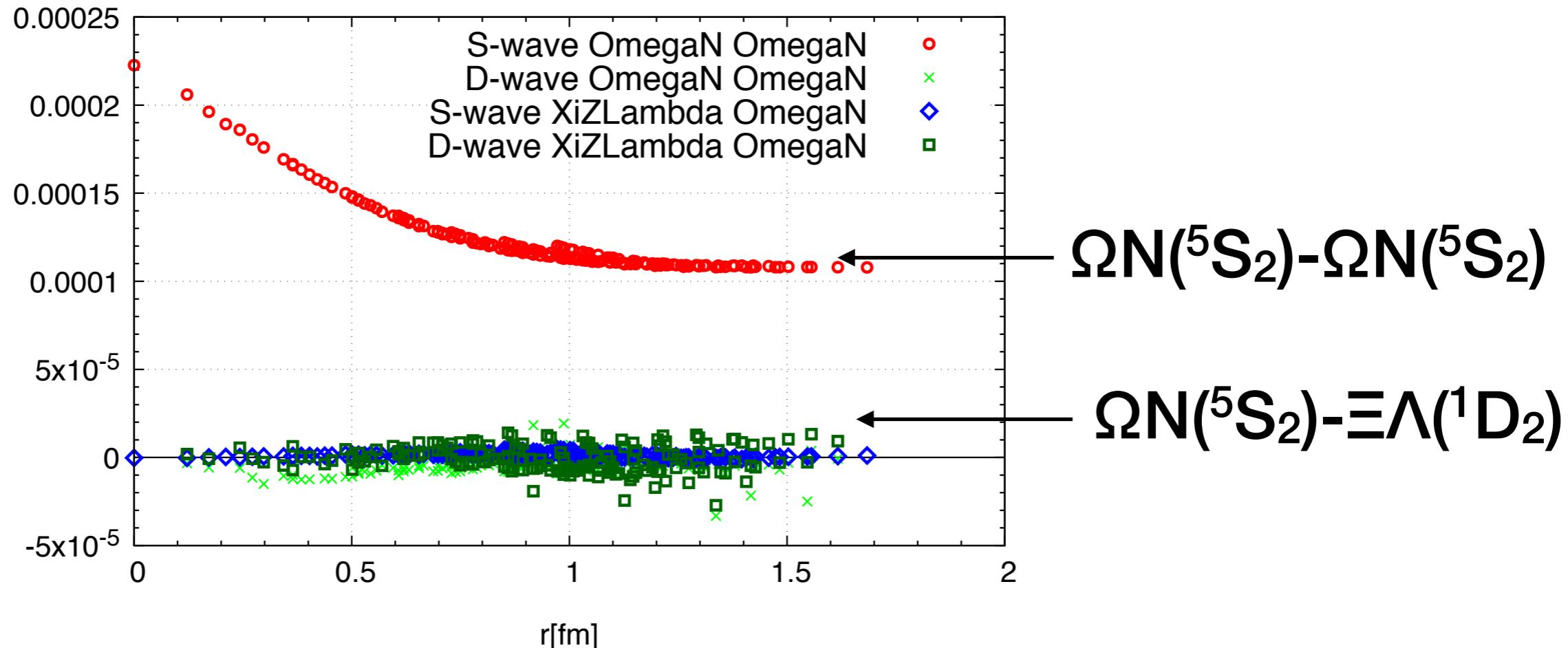
coupling between $\Delta\Delta(^7S_3)-NN(^3D_3)$ is small

Coupled channel effects

$N_f = 2+1$ full QCD with $L = 1.93\text{fm}$, $m_\pi = 1015\text{MeV}$, SU(3) limit

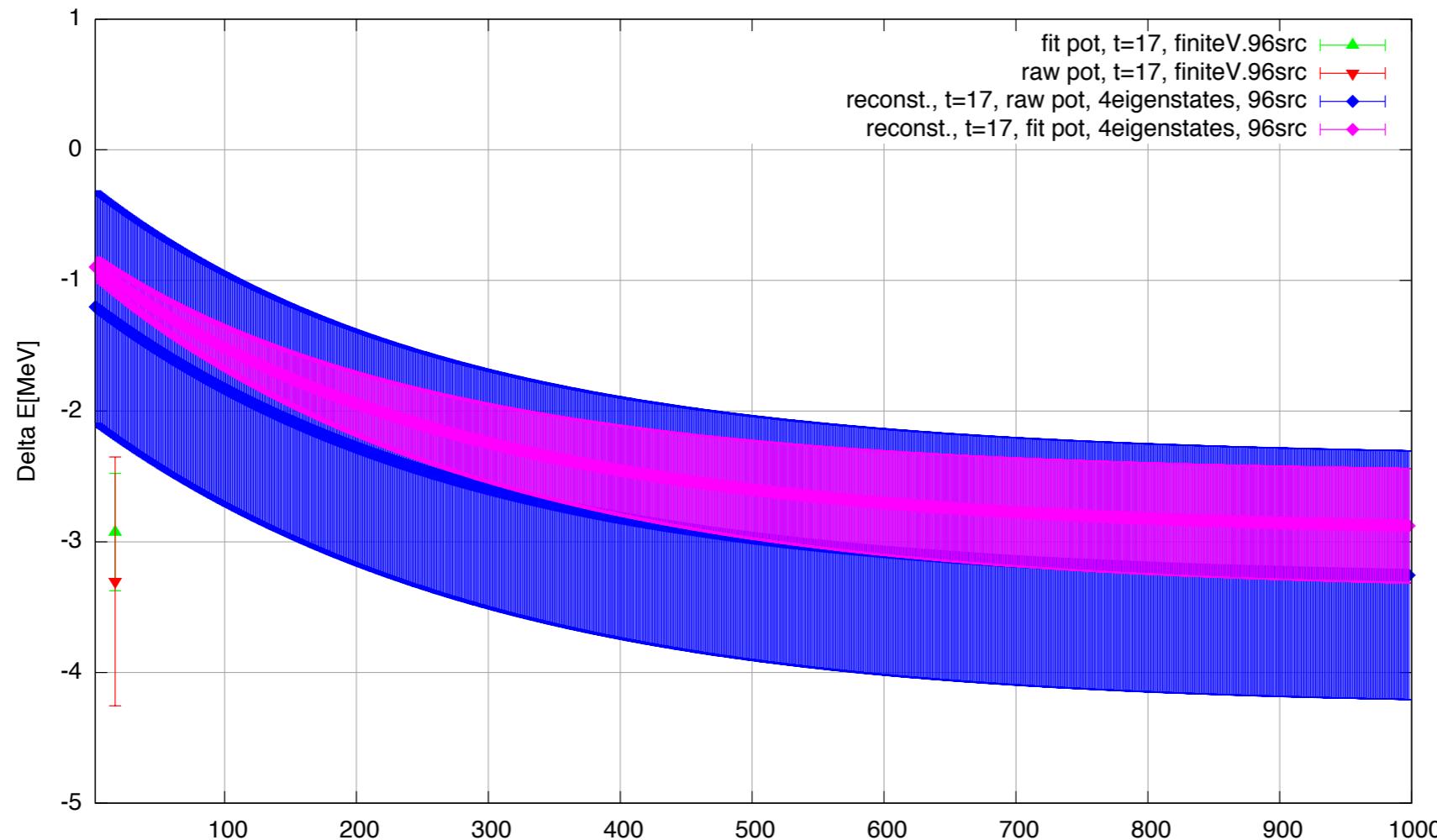
Rcorrelators

$$m_\Omega = m_\Delta \simeq 2230\text{MeV}$$
$$m_\Xi = m_\Lambda \simeq 2030\text{MeV}$$



coupling between $\Omega N(^5S_2) - \Xi \Lambda(^1D_2)$ is very small

platux region in Omg-Omg at phys. point



To extract the B.E. using Luscher's method,
t/a > 1000 is needed

Results w/ physical masses

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$\Xi\Xi(S=-4)$

1S_0 27plet \Leftrightarrow Flavor SU(3)-partner of NN(1S_0)

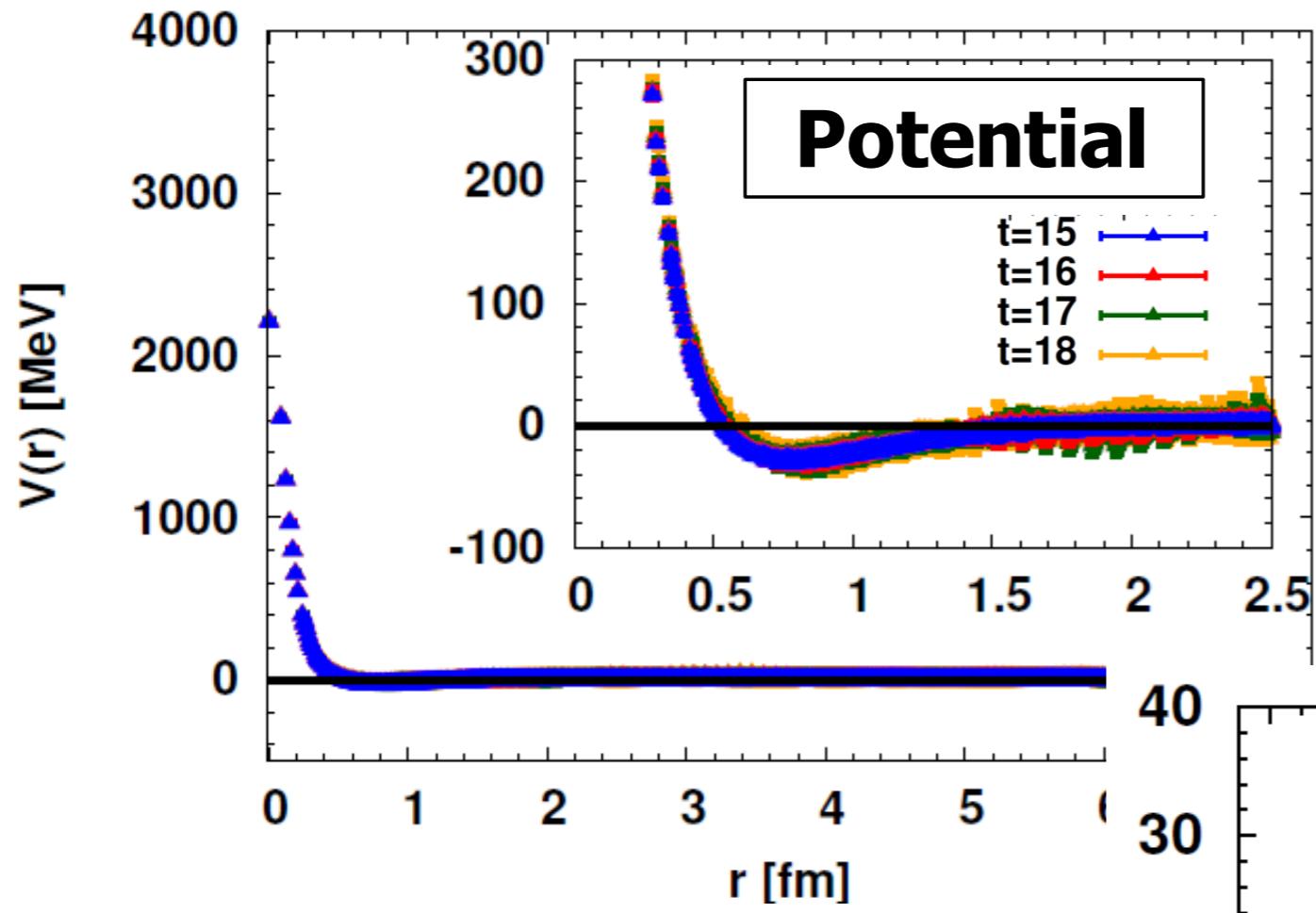
- \Rightarrow • Doorway to NN-forces
• Bound by SU(3) breaking ?

$^3S_1 - ^3D_1$ 10plet \Leftrightarrow unique w/ hyperon DoF

Flavor SU(3)-partner of $\Sigma^- n$

- \Rightarrow • Σ^- in neutron star ?

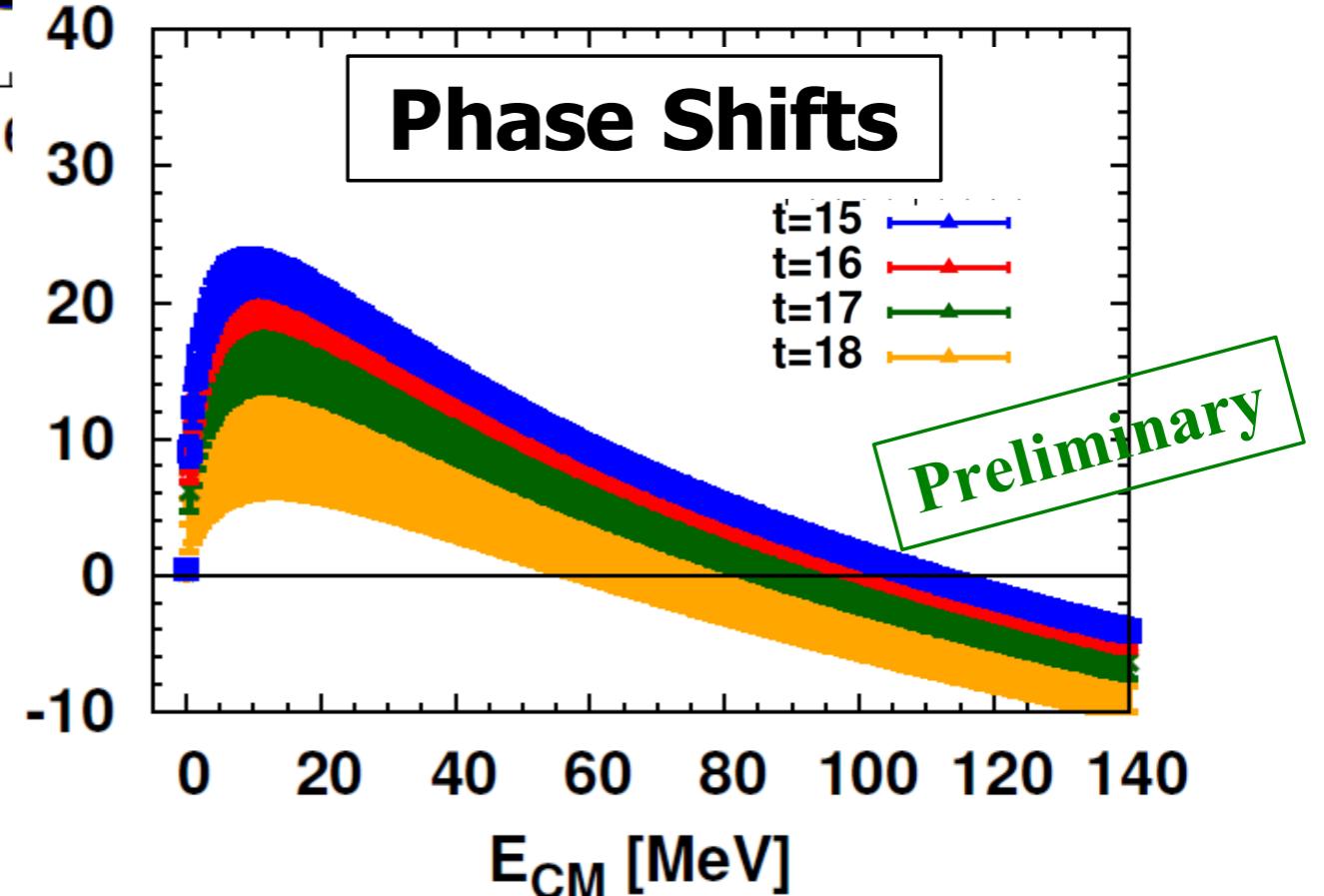
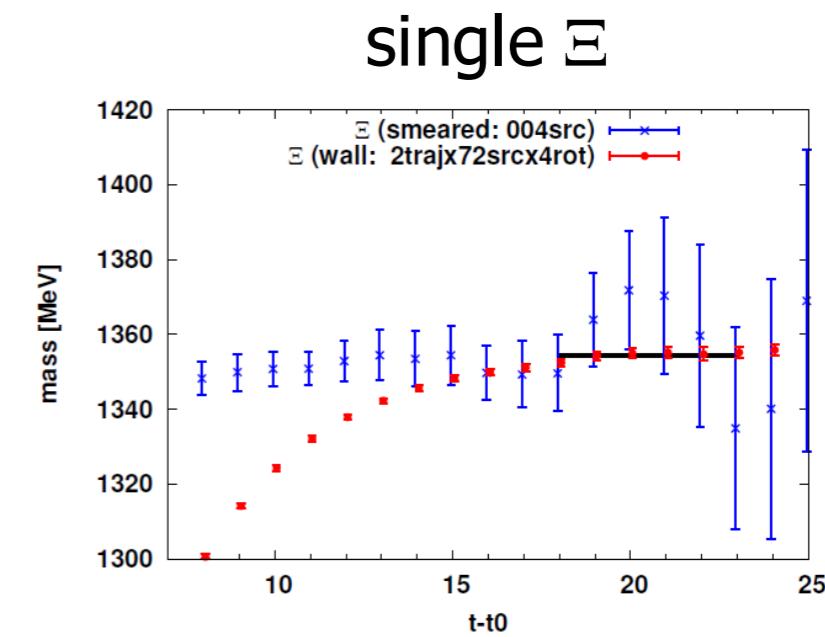
EE system (1S_0)



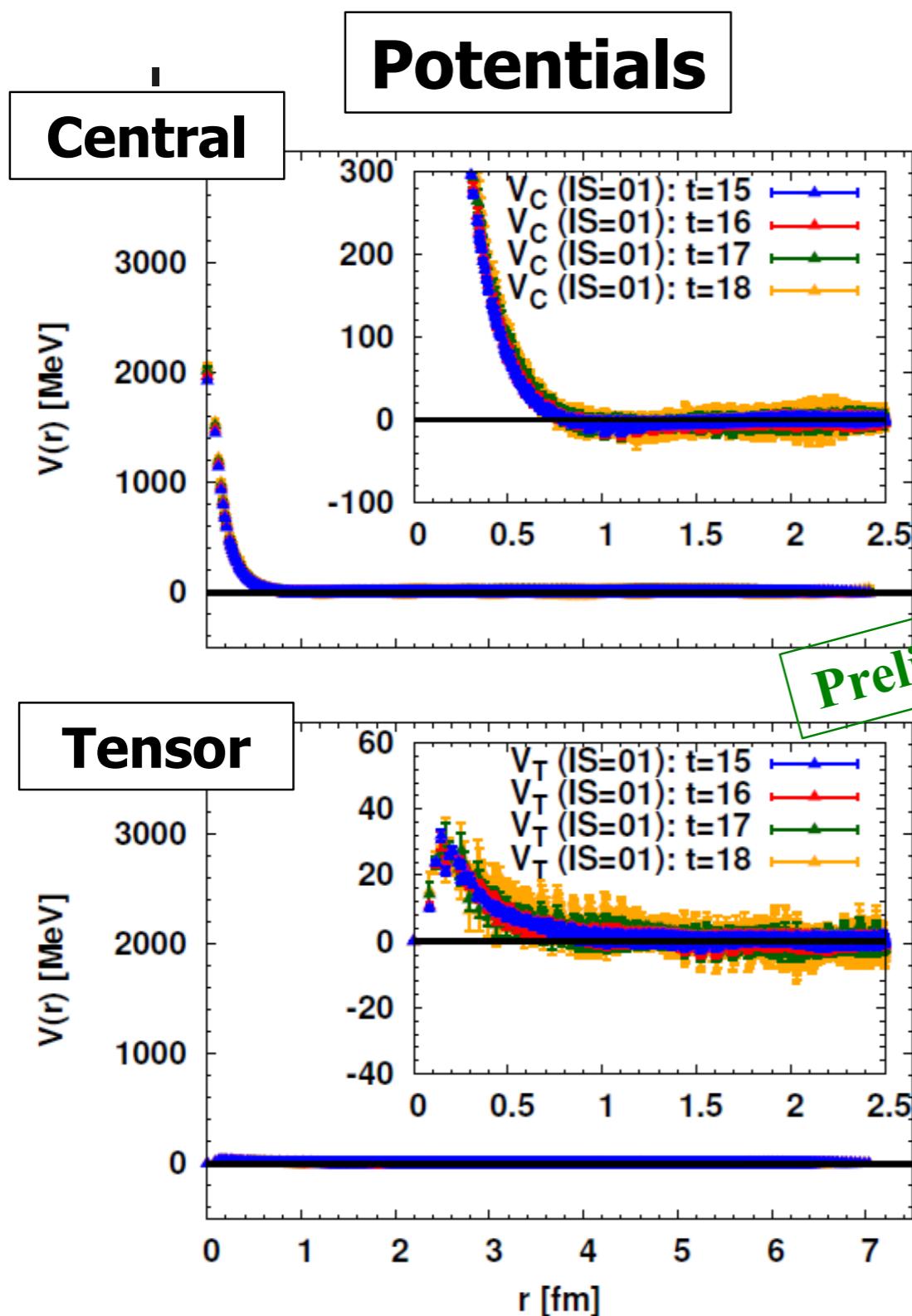
**Strong Attraction
yet Unbound**

↔ EE correlation in HIC

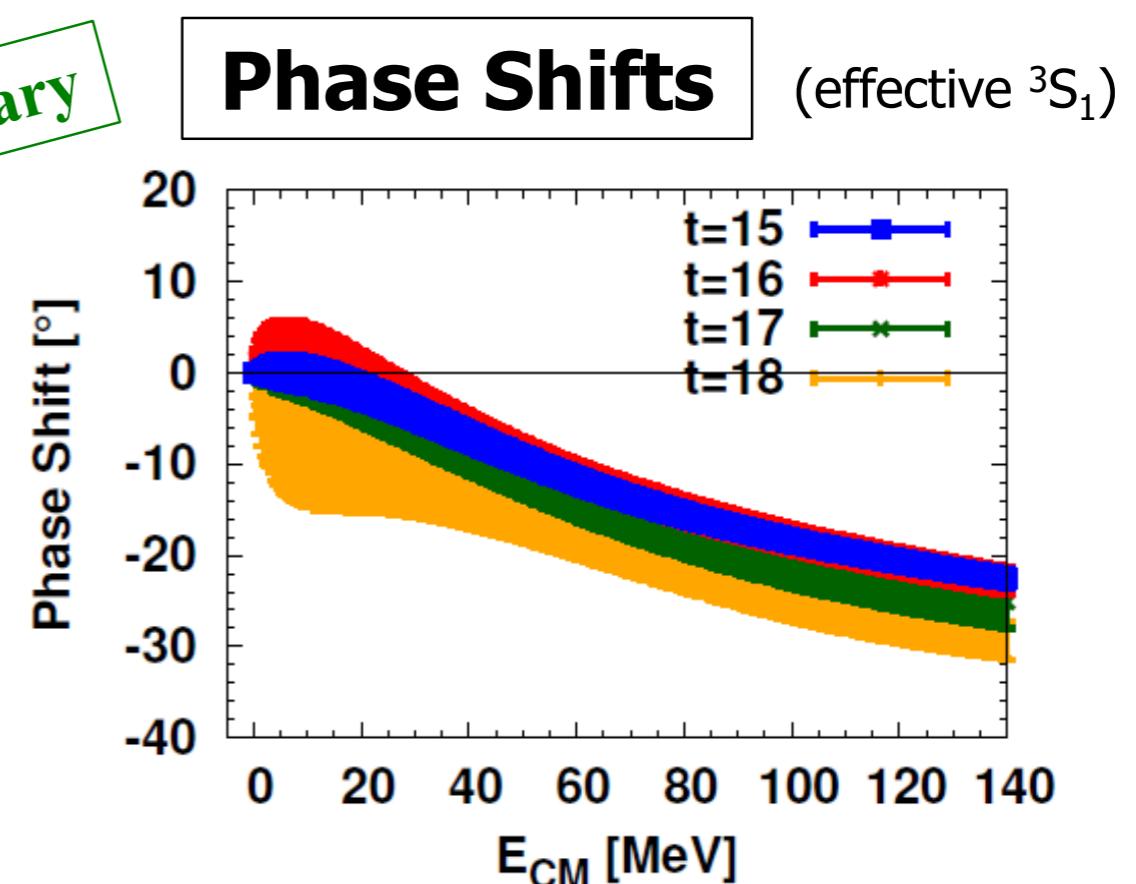
(2-gauss + 2-OBEP)



EE system (3S_1 - 3D_1)



Central: Strong Repulsion
Tensor: Weak

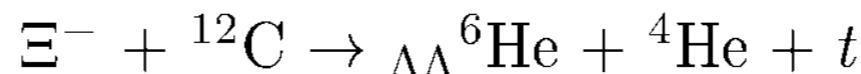


H-dibaryon channel ($S = -2$)

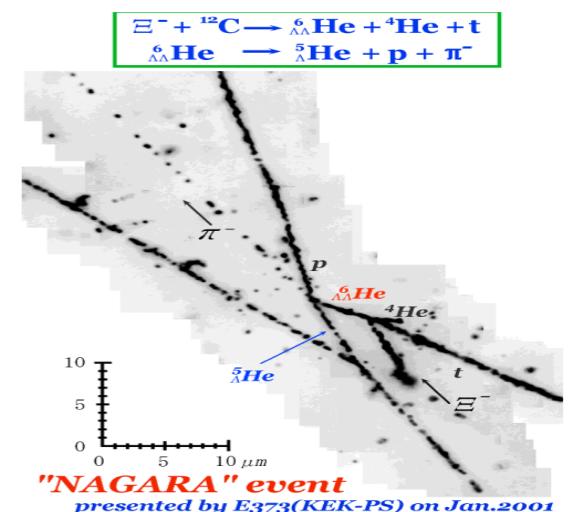
(1S_0 , $\Lambda\Lambda$ - $N\Xi$ - $\Sigma\Sigma$, Coupled Channel)

R. Jaffe (1977), “Perhaps a Stable Dihyperon”

NAGARA-event (2001)

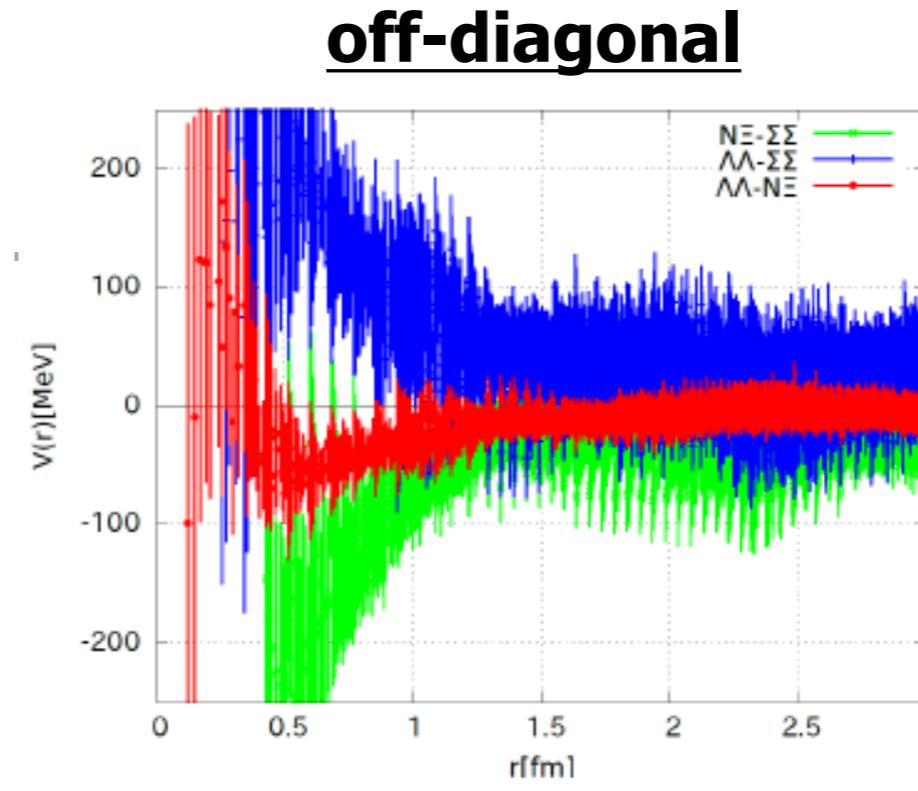
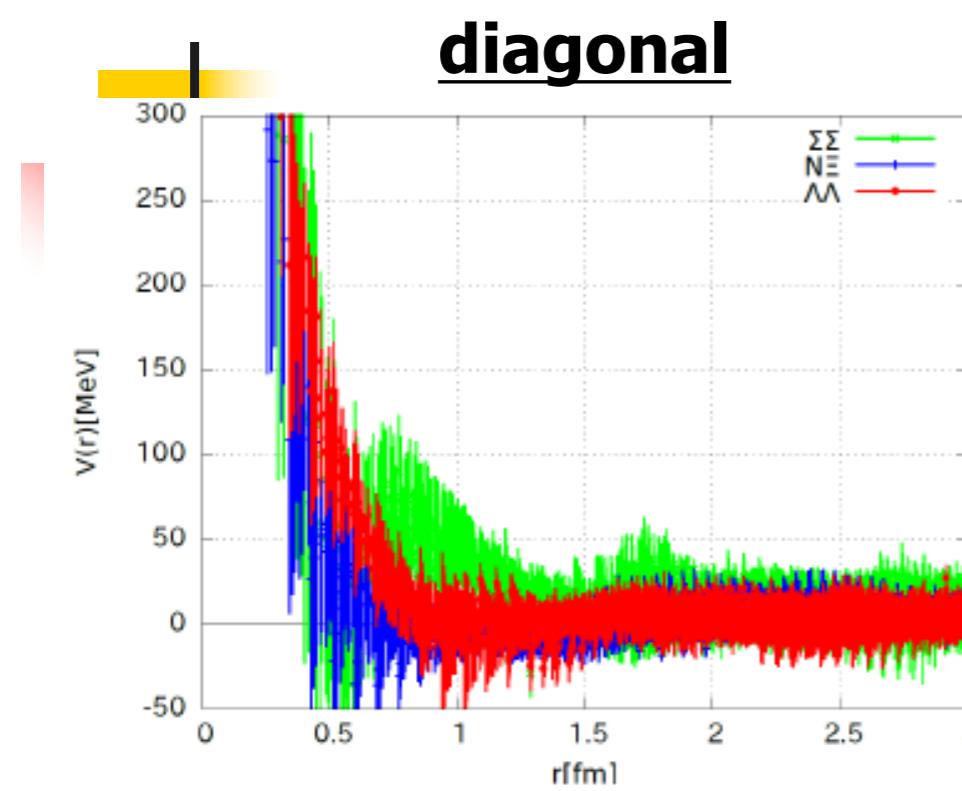


- $\Lambda\Lambda$ weak attraction
- No deeply bound H-dibaryon



H-dibaryon @ Nf=2+1, $m_\pi = 146$ MeV

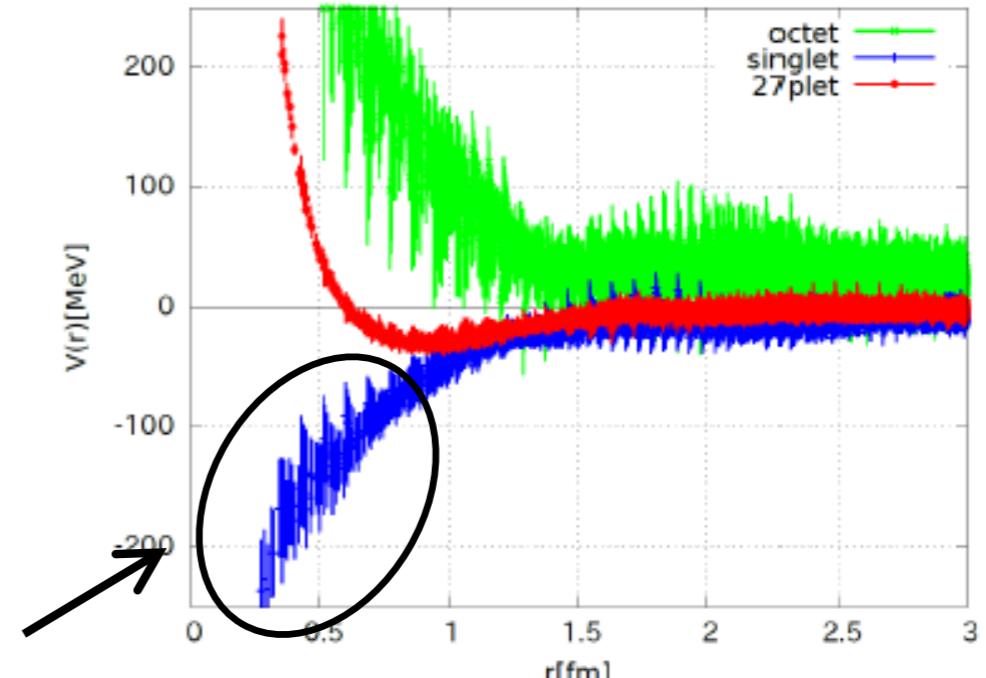
[K. Sasaki]



$m_{\Sigma\Sigma} = 2380$ MeV
120 MeV
$m_{N\Xi} = 2260$ MeV
30 MeV
$m_{\Lambda\Lambda} = 2230$ MeV

**diagonal in
SU(3)-irrep base**

**Strong Attraction in
flavor-singlet channel**

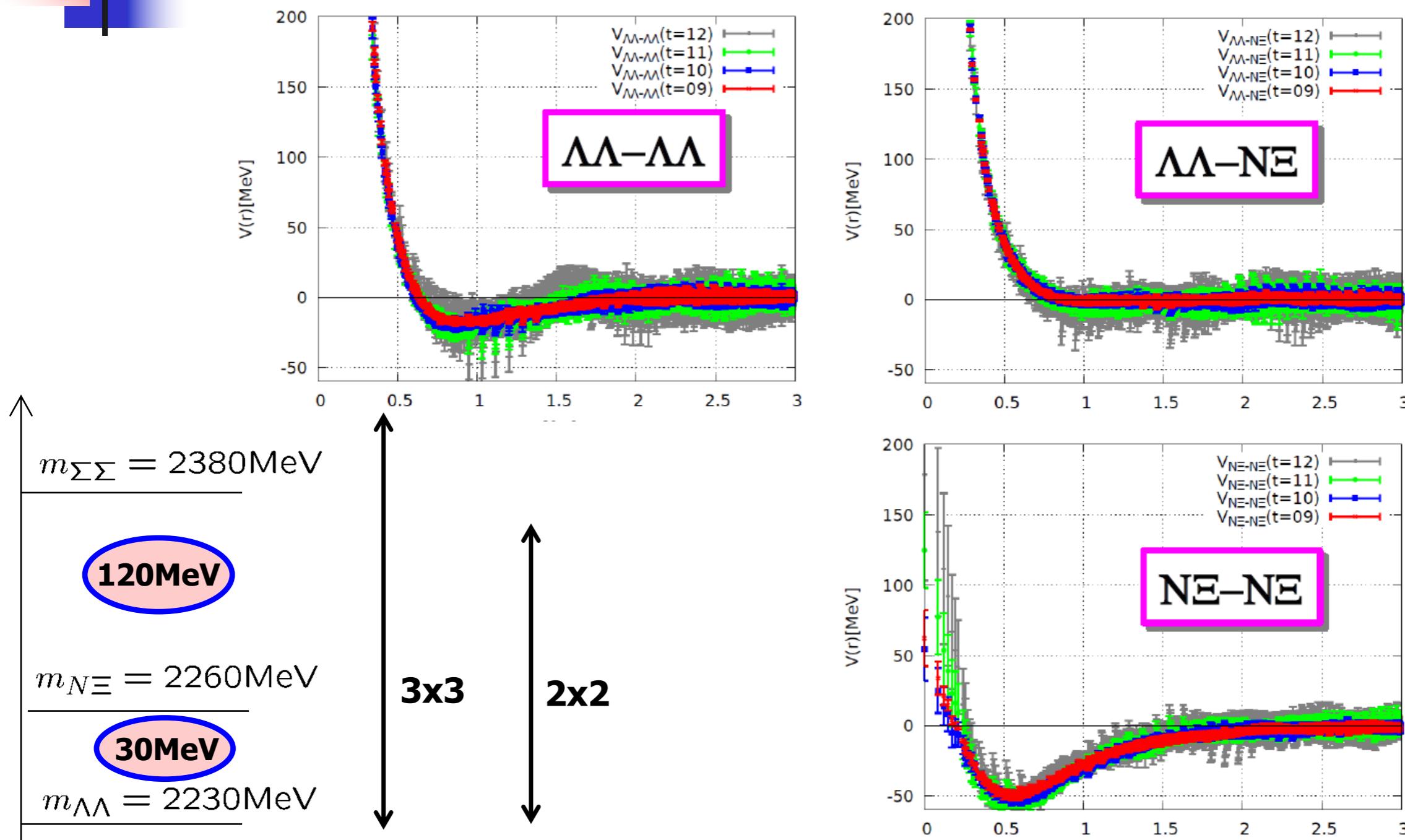


(400conf x 4rot x 28src, t=11)

$\Lambda\Lambda$, $N\Xi$ (effective) 2x2 coupled channel analysis

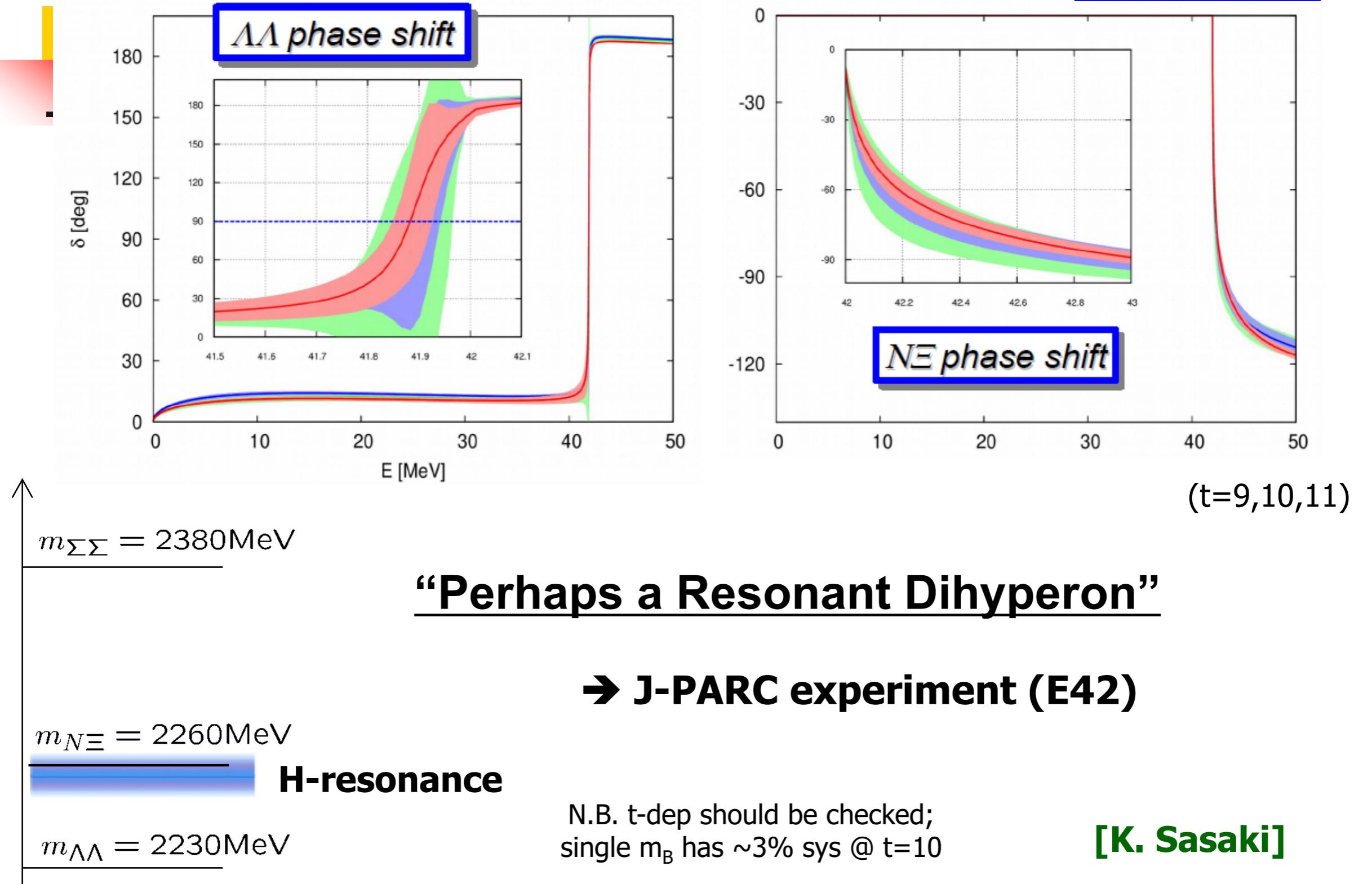
$\Sigma\Sigma$ channel \leftrightarrow couples strongly to flavor octet channel
 \leftrightarrow noisy because they are quark-Pauli forbidden

→ Improve the S/N by considering only $\Lambda\Lambda$, $N\Xi$ dof at low energies



$\Lambda\Lambda$, $N\Xi$ (effective) 2x2 coupled channel analysis

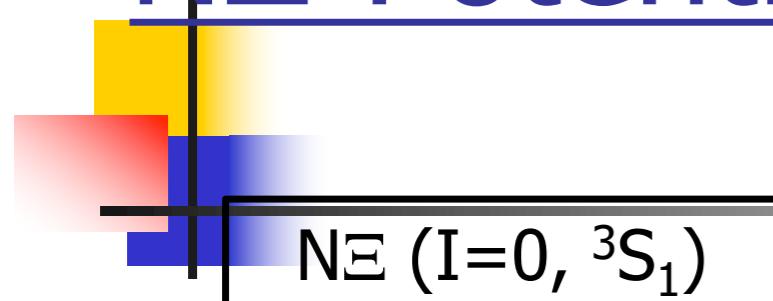
Preliminary



NΞ-Potentials

[K. Sasaki]

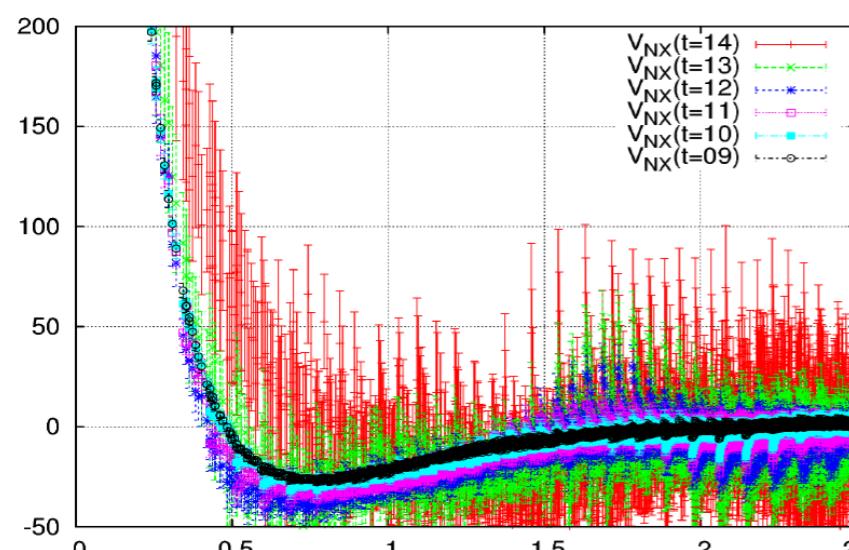
(200conf x 4rot x 20src, t=10)



$N\Sigma (I=0, {}^3S_1)$

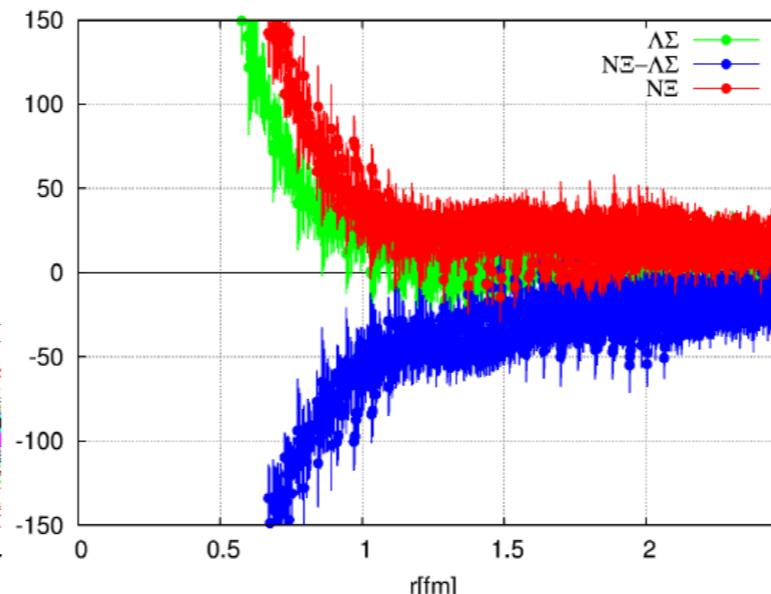
$N\Sigma-\Lambda\Sigma (I=1, {}^1S_0)$

$N\Sigma-\Lambda\Sigma-\Sigma\Sigma (I=1, {}^3S_1)$



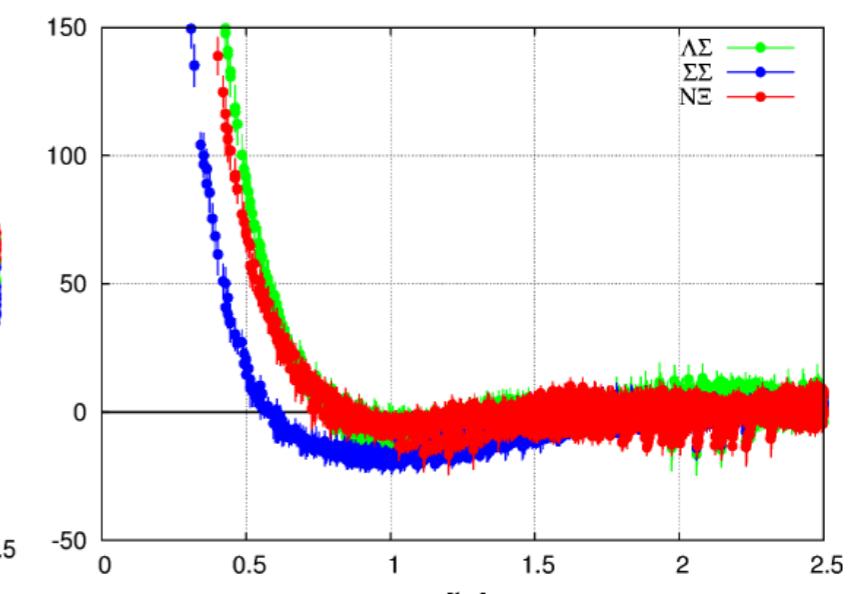
(8a)

Attractive



(8s, 27)

Repulsive



(8a, 10, 10bar)

Attractive

$(\Lambda\Lambda-N\Sigma-\Sigma\Sigma (I=0, {}^1S_0))$

Is interaction net attractive ? Stay tuned !

c.f. Net attractive @ $m(\pi)=0.66-88\text{GeV}$ (K. Sasaki et al., PTEP2015, 113B01)

S= -1 systems

↔ strangeness nuclear physics (Λ -hypernuclei @ J-PARC)

Λ should (?) appear in the core of Neutron Star

↔ Huge impact on EoS of high dense matter

- $\Lambda N - \Sigma N$ ($I=1/2$) : coupled channel
 - $^1S_0 \sim 27\text{-plet} \& 8s\text{-plet}$
 - $^3S_1 - ^3D_1 \sim 10^*\text{-plet} \& 8a\text{-plet}$
- ΣN ($I=3/2$)
 - $^1S_0 \sim 27\text{-plet}$
 $\Leftrightarrow NN(^1S_0) + SU(3)$ breaking
 - $^3S_1 - ^3D_1 \sim 10\text{-plet}$

$\Lambda N - \Sigma N$ Vc potential in $^3S_1 - ^3D_1$

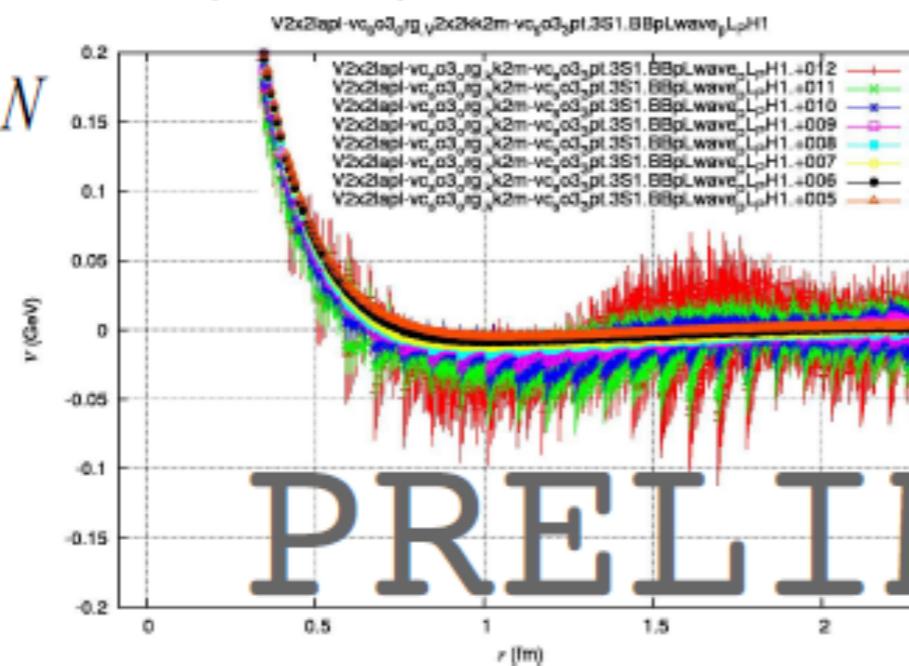
[H. Nemura]

Very preliminary result of LN potential at the physical point

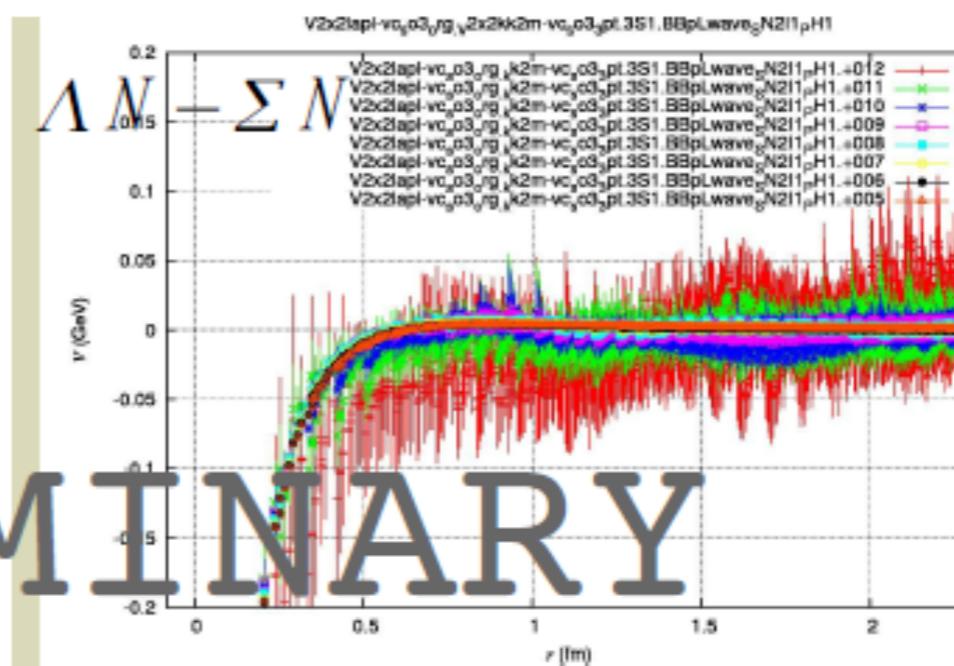
$$V_C(^3S_1 - ^3D_1)$$

$$\left(\frac{\nabla^2}{2\mu} - \frac{\partial}{\partial t} \right) R(\vec{r}, t) = \int d^3r' U(\vec{r}, \vec{r}') R(\vec{r}', t) + O(k^4) = V_{\text{LO}}(\vec{r}) R(\vec{r}, t) + \dots (8)$$

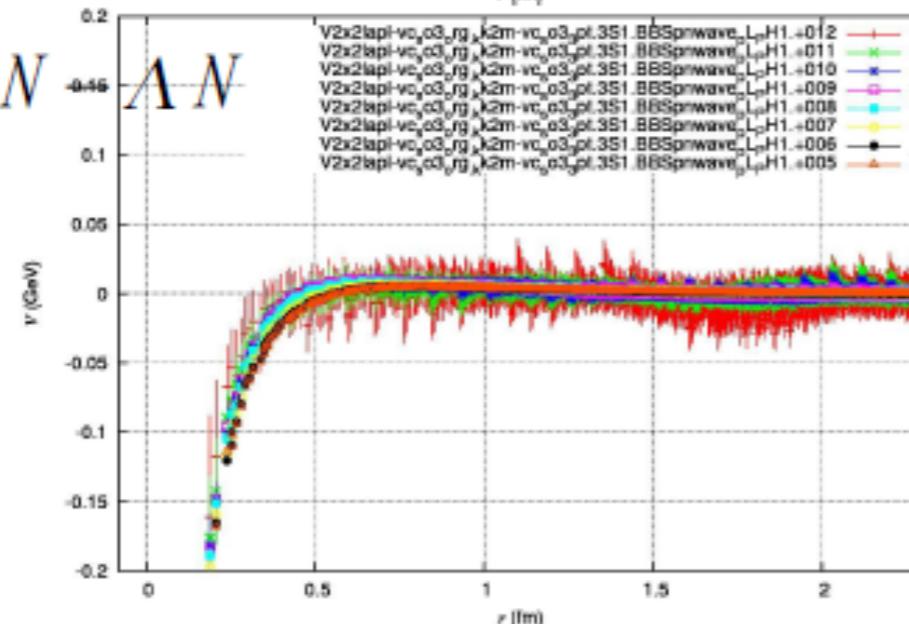
ΛN



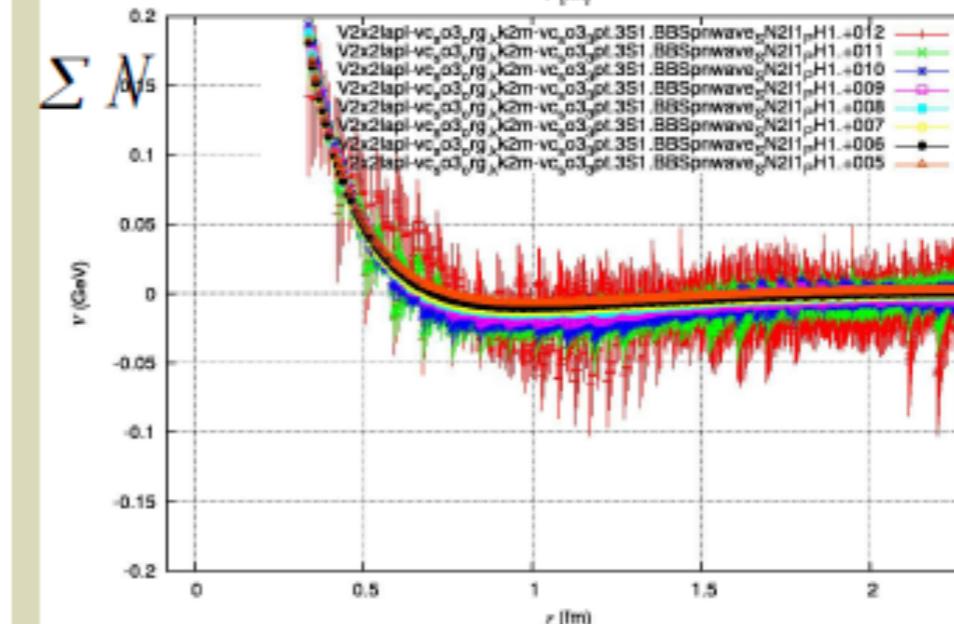
ΛN



ΣN



ΣN



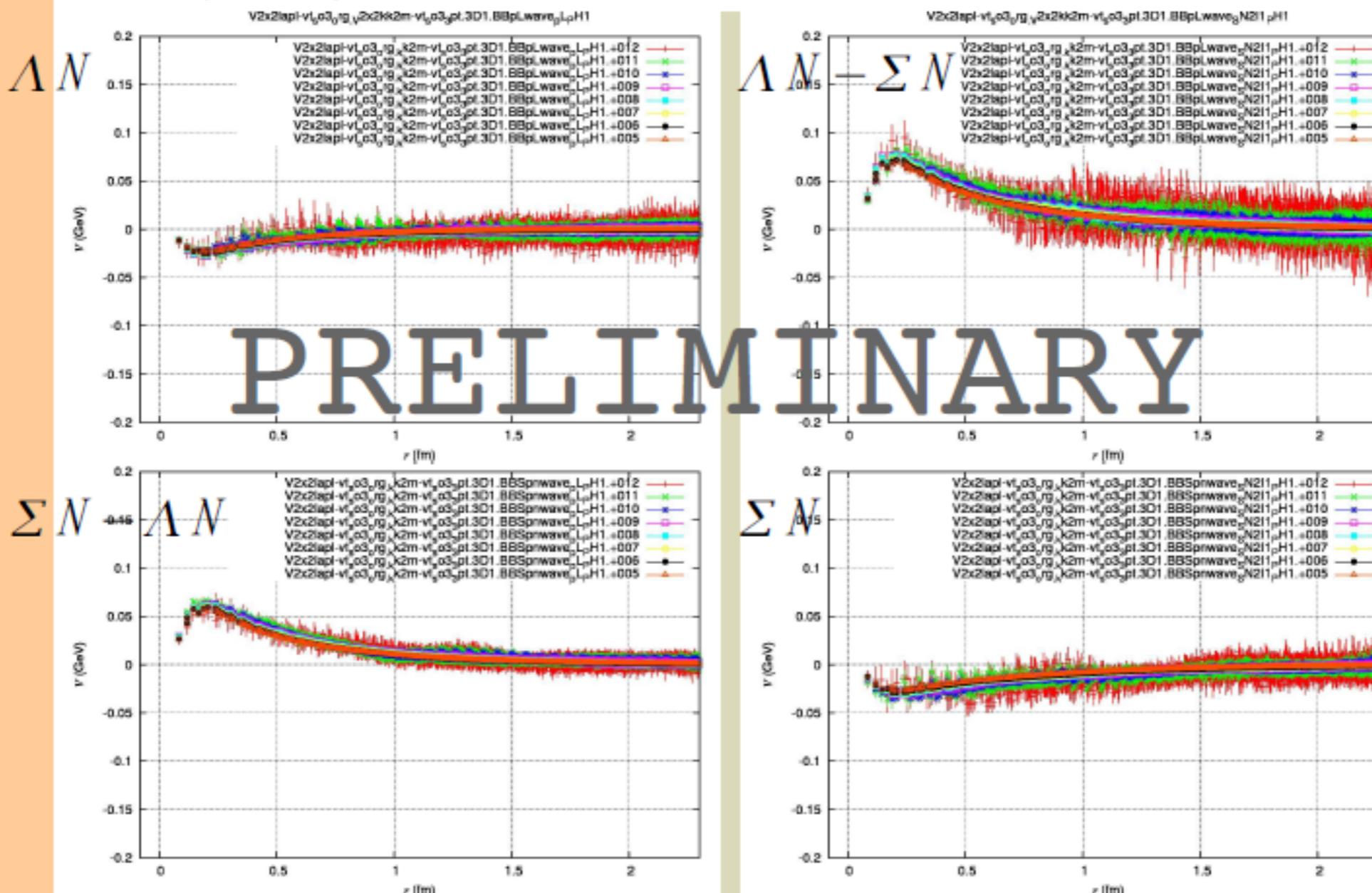
(200conf x 4rot x 52src)

$\Lambda N - \Sigma N$ Vt potential in $^3S_1 - ^3D_1$ [H. Nemura]

Very preliminary result of LN potential at the physical point

$$\left(\frac{\nabla^2}{2\mu} - \frac{\partial}{\partial t} \right) R(\vec{r}, t) = \int d^3 r' U(\vec{r}, \vec{r}') R(\vec{r}', t) + O(k^4) = V_{\text{LO}}(\vec{r}) R(\vec{r}, t) + \dots (8)$$

$$V_T(^3S_1 - ^3D_1)$$



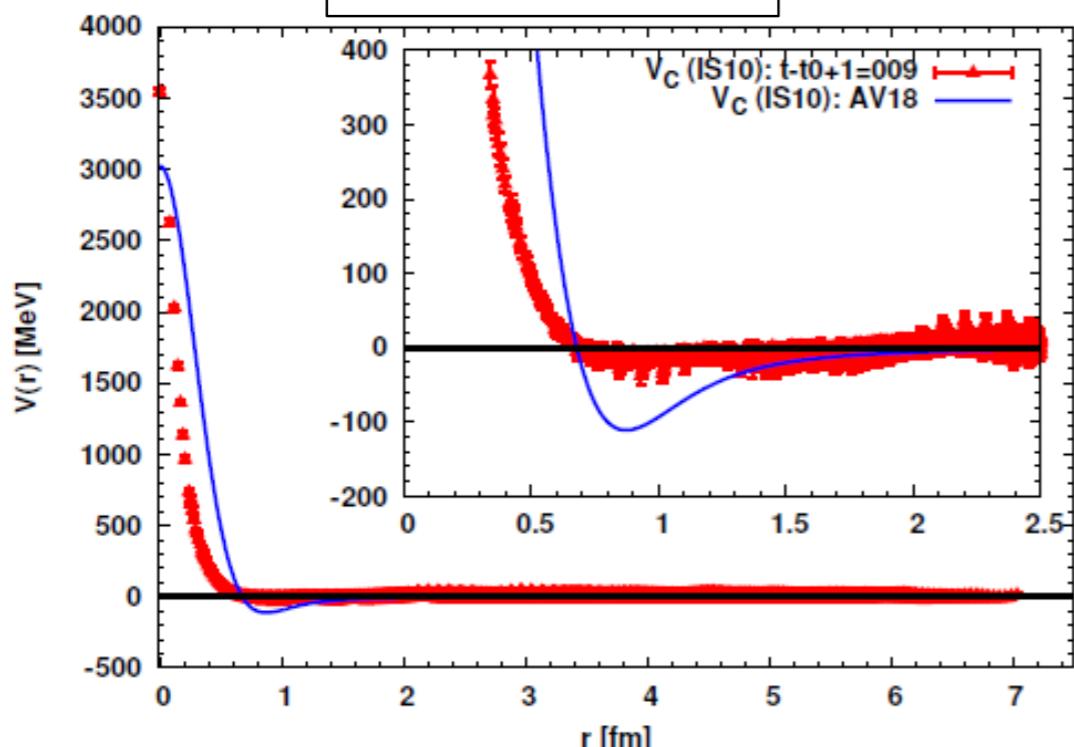
(200conf x 4rot x 52src)

NN system ($S=0$)

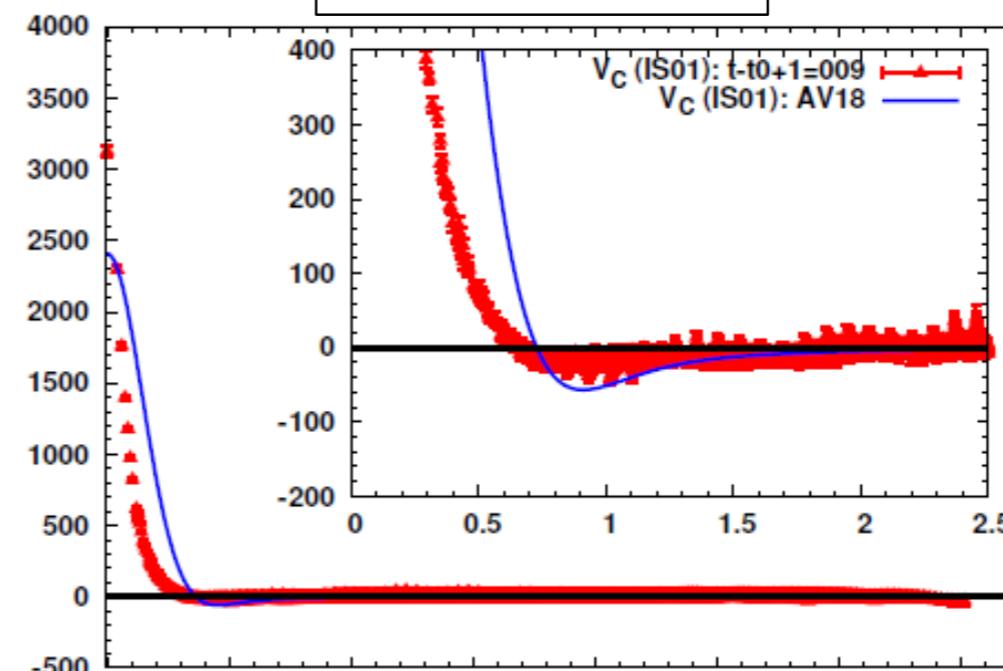
Naïve comparison w/ AV18

NN

1S0

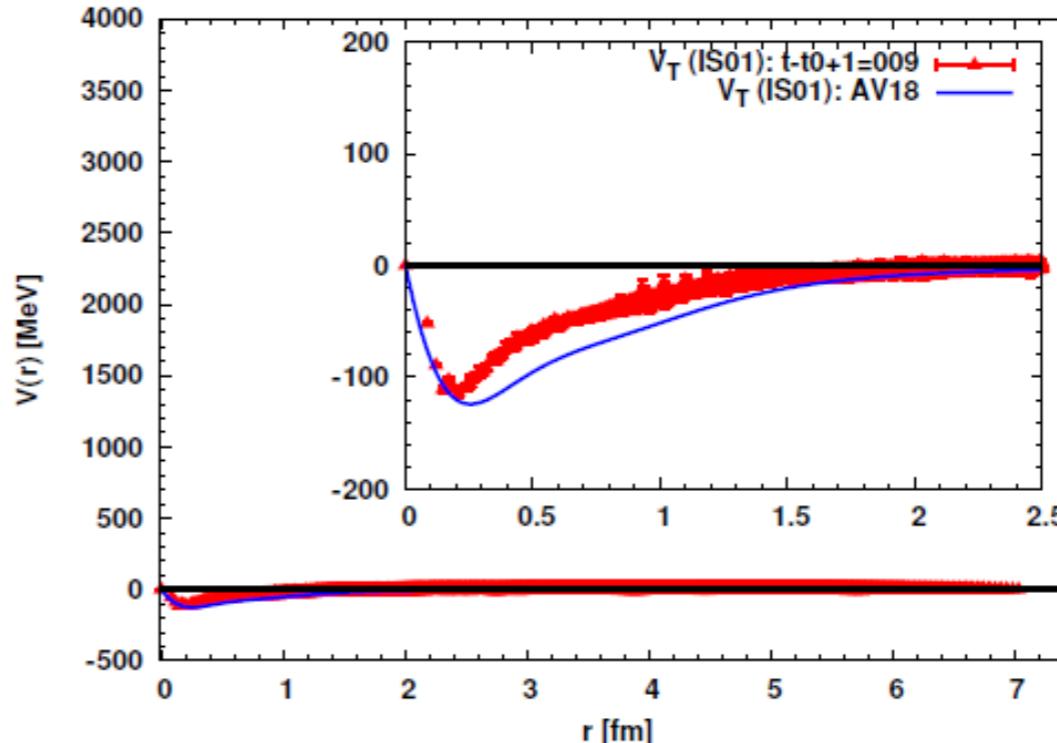


3S1-3D1



Central

$t-t_0=8$



Tensor

(400conf x 4rot x 48src)

Abashian-Booth-Crowe Effect in Basic Double-Pionic Fusion: A New Resonance?

$m = 2.37 \text{ GeV}$, $\Gamma \approx 70 \text{ MeV}$ and $I(J^P) = 0(3^+)$ in both pn and $\Delta\Delta$ systems.

