

MEASUREMENT OF THE HYDROGEN

HYPERFINE SPLITTING :

TOWARDS ANTIHYDROGEN SPECTROSCOPY



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MOTIVATIONS

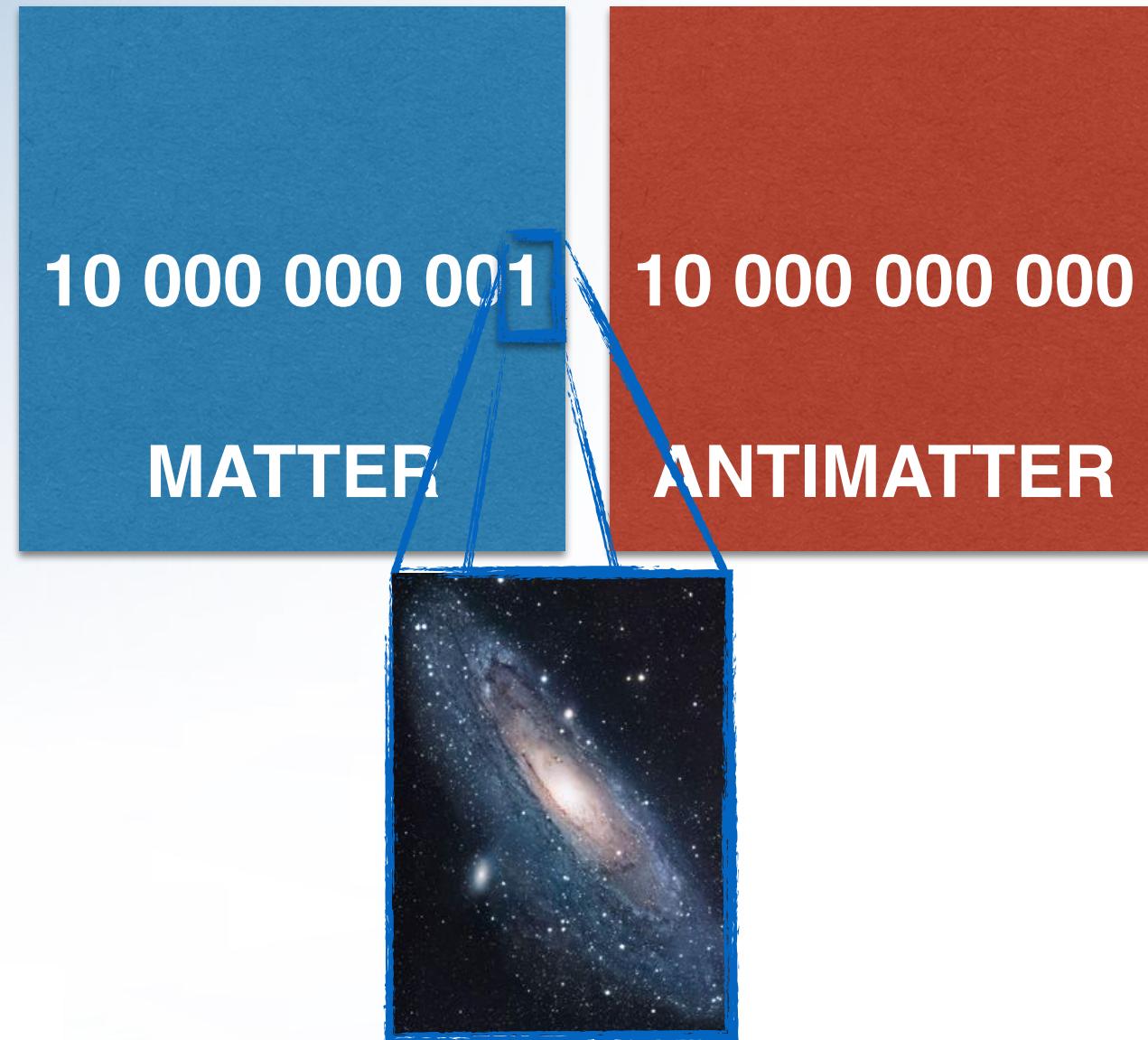
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MATTER

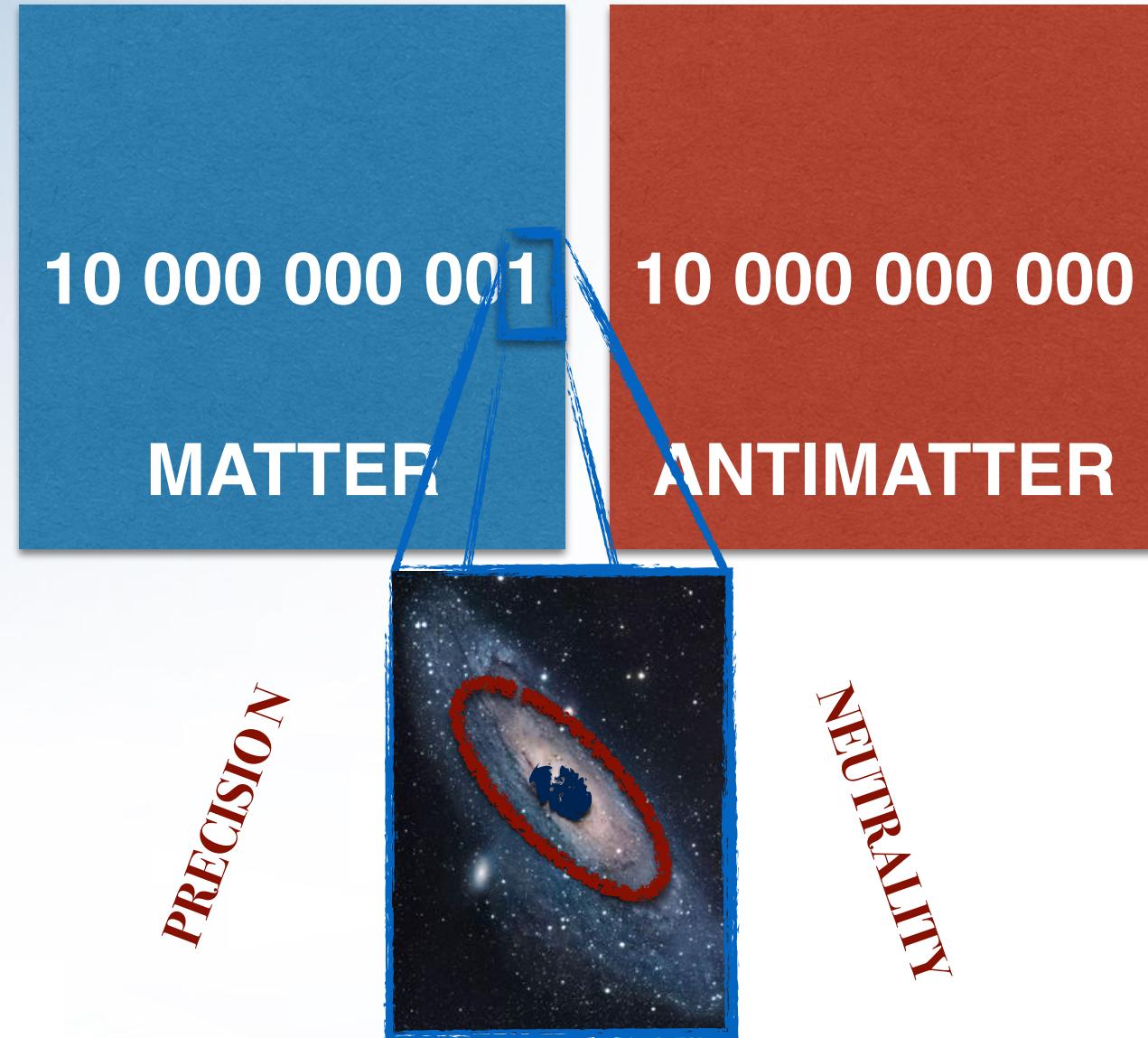
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ANTIMATTER

MOTIVATIONS



MOTIVATIONS





MOTIVATIONS

CPT Theorem
Quantum Field Theory
Lorentz invariance
Locality
Unitarity



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Implies : properties of matter & antimatter particles have to be exactly equal (mass) or opposite (charge, magnetic moment)



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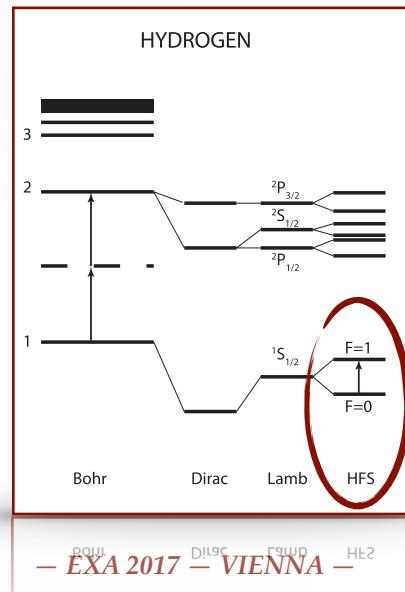
Atomic structures identical

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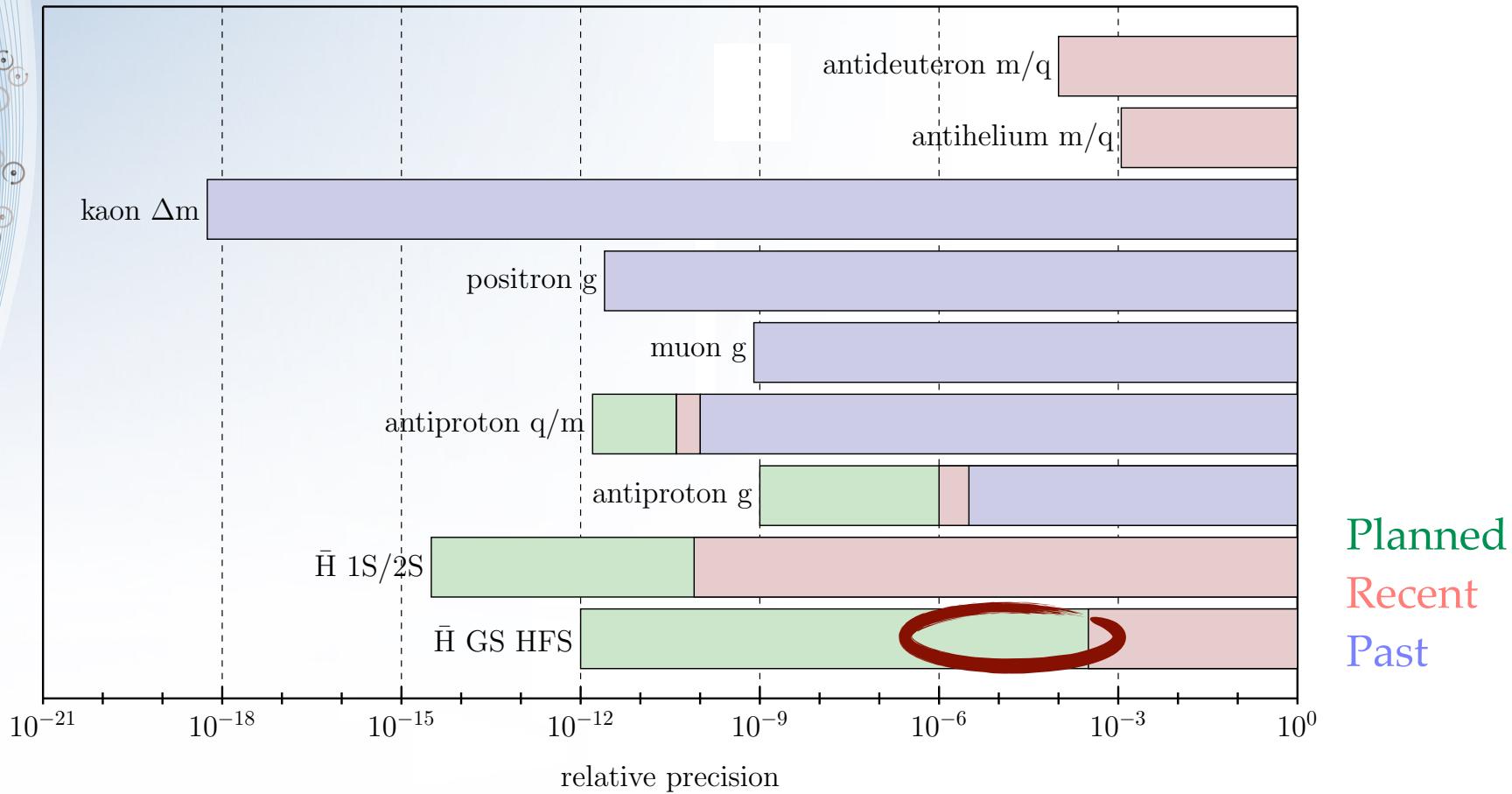
Implies : properties of matter & antimatter particles have to be exactly equal (mass) or opposite (charge, magnetic moment)

Atomic structures identical



MOTIVATIONS

Tests in different systems:



MOTIVATIONS

$$\nu = 1.420405751768(1) \text{ GHz}$$

S. G. Karshenboim, Precision Physics of Simple Atomic Systems, pages 142–162, Springer, Berlin, Heidelberg, 2003, hep-ph/0305205.

Leading term: Fermi contact term

$$\nu_F = \frac{16}{3} \left(\frac{M_p}{M_p + m_e} \right)^3 \frac{m_e}{M_p} \frac{\bar{\mu}_p}{\mu_N} \alpha^2 c R_y$$

has been measured to better than 1 ppm

Nagahama H et al. Nat Commun. (2017) doi: 10.1038/ncomms14084.

DiSciacca et al, Phys. Rev. Lett. 110, 13 (2013)

Finite electric and magnetic radius (Zemach corrections): ~41 ppm

access to the electric and magnetic form factors of the antiproton

$$\Delta\nu(\text{Zemach}) = \nu_F \frac{2Z\alpha m_e}{\pi^2} \int \frac{d^3 p}{p^4} \left[\frac{G_E(p^2)G_M(p^2)}{1+\kappa} - 1 \right]$$

e.g Friar et al. Phys.Lett. B579 (2004)

Polarizability of p(bar) = 1.88 ± 0.64 ppm

Carlson, Nazaryan, and Griffioen PRA 78, 022517 (2008)

Remaining deviation theory-experiment: 0.86 ± 0.78 ppm



MOTIVATIONS

Standard model extension (SME)

CPT Violation and the Standard Model, D. Colladay and A. Kostelecky,
Phys. Rev. D 55, 6760 (1997)

Lorentz and CPT Tests in Hydrogen,
Antihydrogen, and Related Systems,
A. Kostelecky and A. Vargas, Phys. Rev. D
92, 056002 (2015)

Dirac equation in mSME :

$$(i\gamma^\mu D_\mu - m_e - a_\mu^e \gamma^\mu - b_\mu^e \gamma_5 \gamma^\mu - \frac{1}{2} H_{\mu\nu}^e \sigma^{\mu\nu} + i c_{\mu\nu}^e \gamma^\mu D^\nu + i d_{\mu\nu}^e \gamma_5 \gamma^\mu D^\nu) \psi = 0$$

Different measurements (even of the same quantity) are sensitive (or not) to different SME coefficients

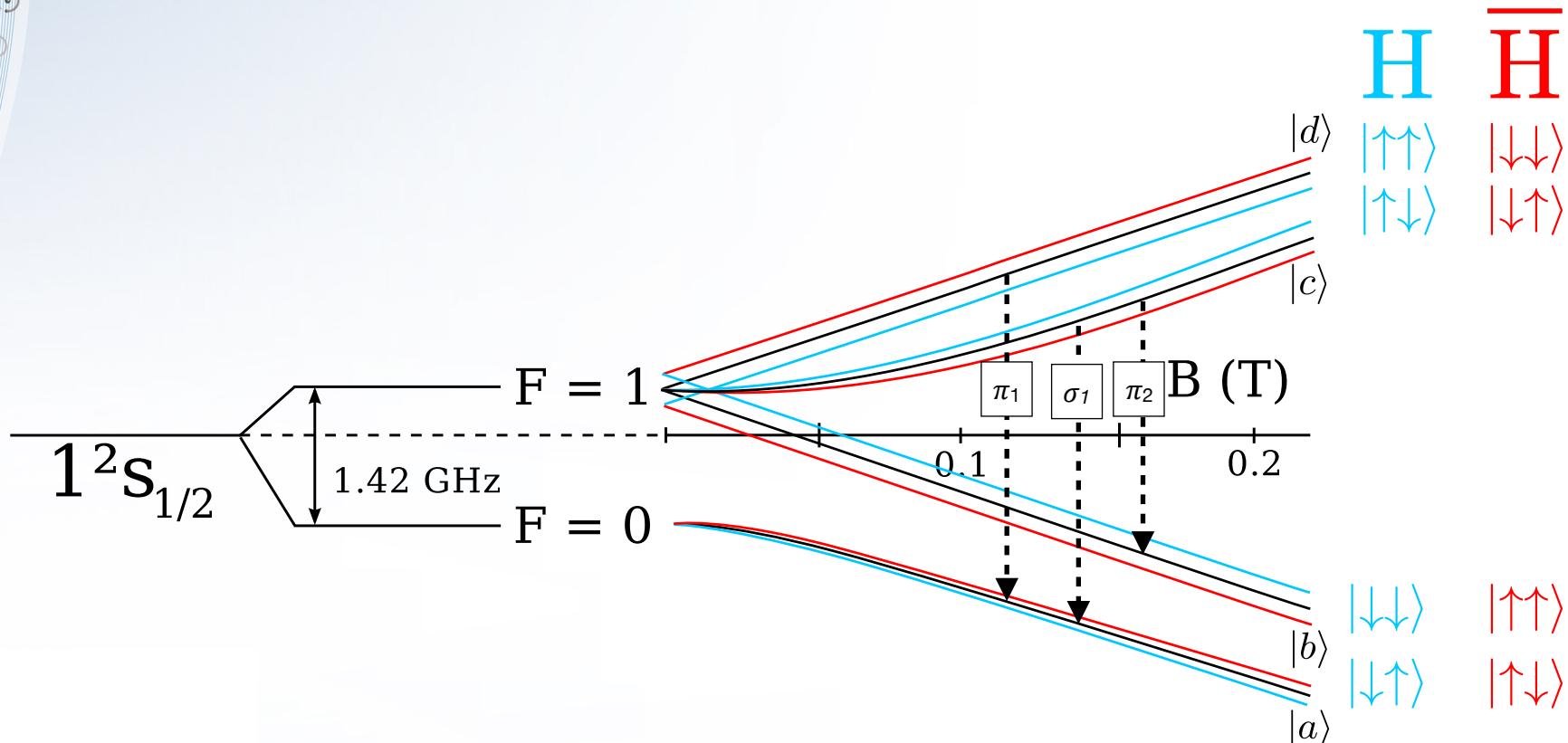
MOTIVATIONS

Measure ν_{HF} in antihydrogen :

$\pi_1 - \pi_2$
at a given field
 $\pi_1 \& \sigma_1$

$$\nu_0 = \frac{g_+ \sqrt{g_+^2 \nu_\sigma^2 - 4g_-^2 \nu_\pi^2 + 4g_-^2 \nu_\pi \nu_\sigma} + g_-^2 (2\nu_\pi - \nu_\sigma)}{g_+^2 + g_-^2}$$

where $g_\pm = g_I \pm g_J$.



MOTIVATIONS

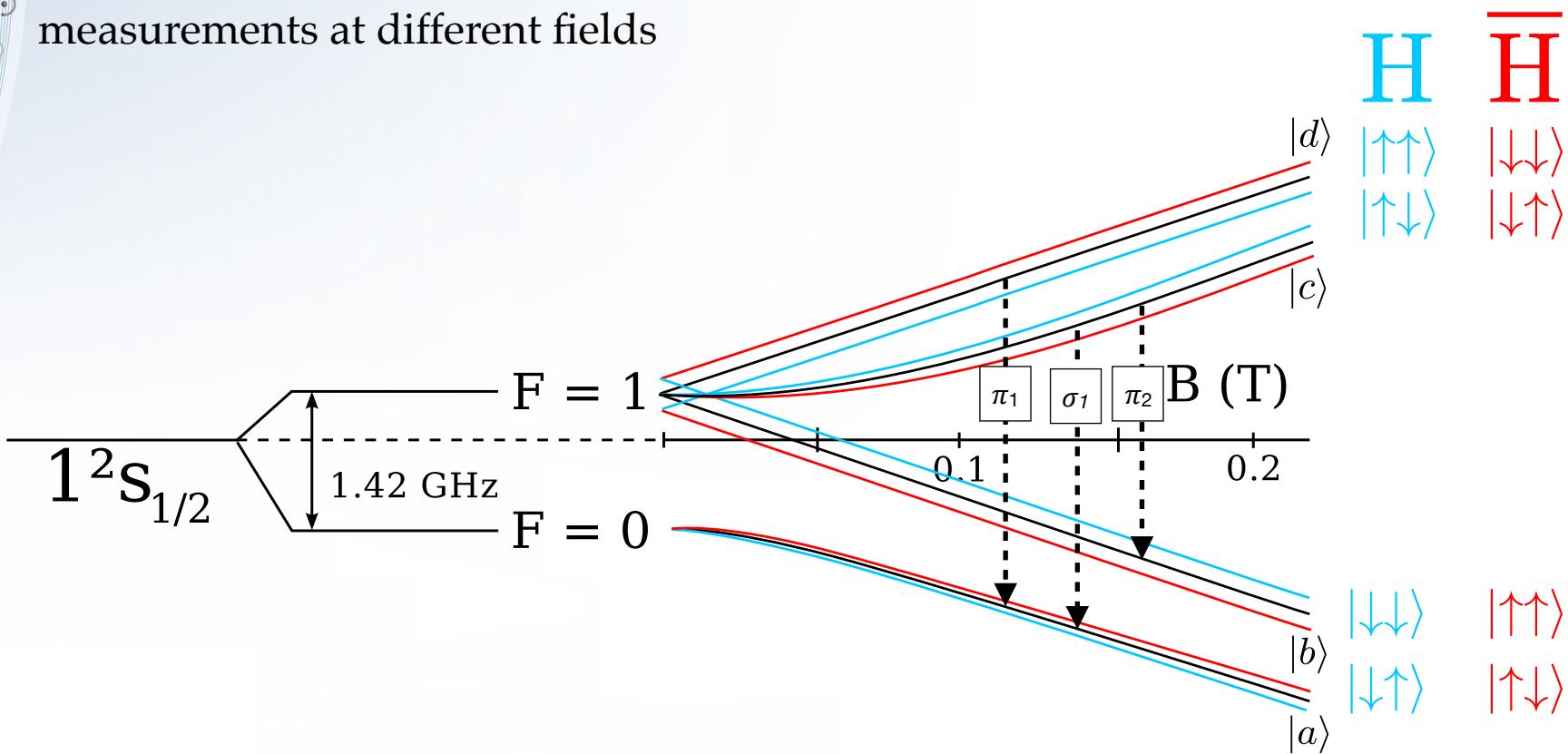
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Extrapolate either transition from several measurements at different fields



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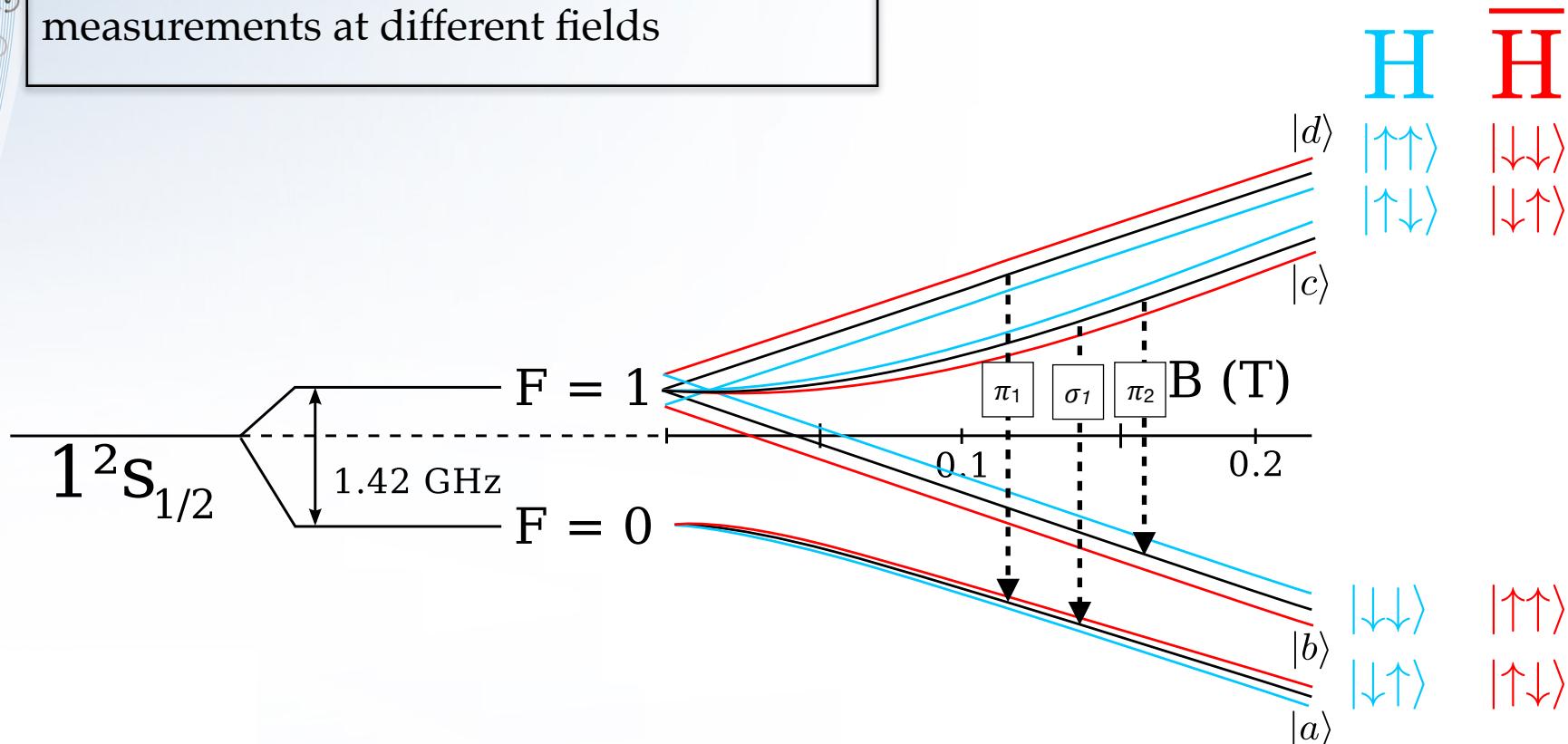
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But not all constrain SME parameters



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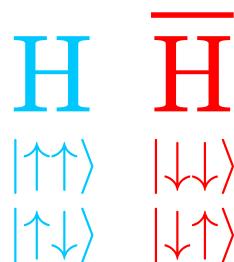
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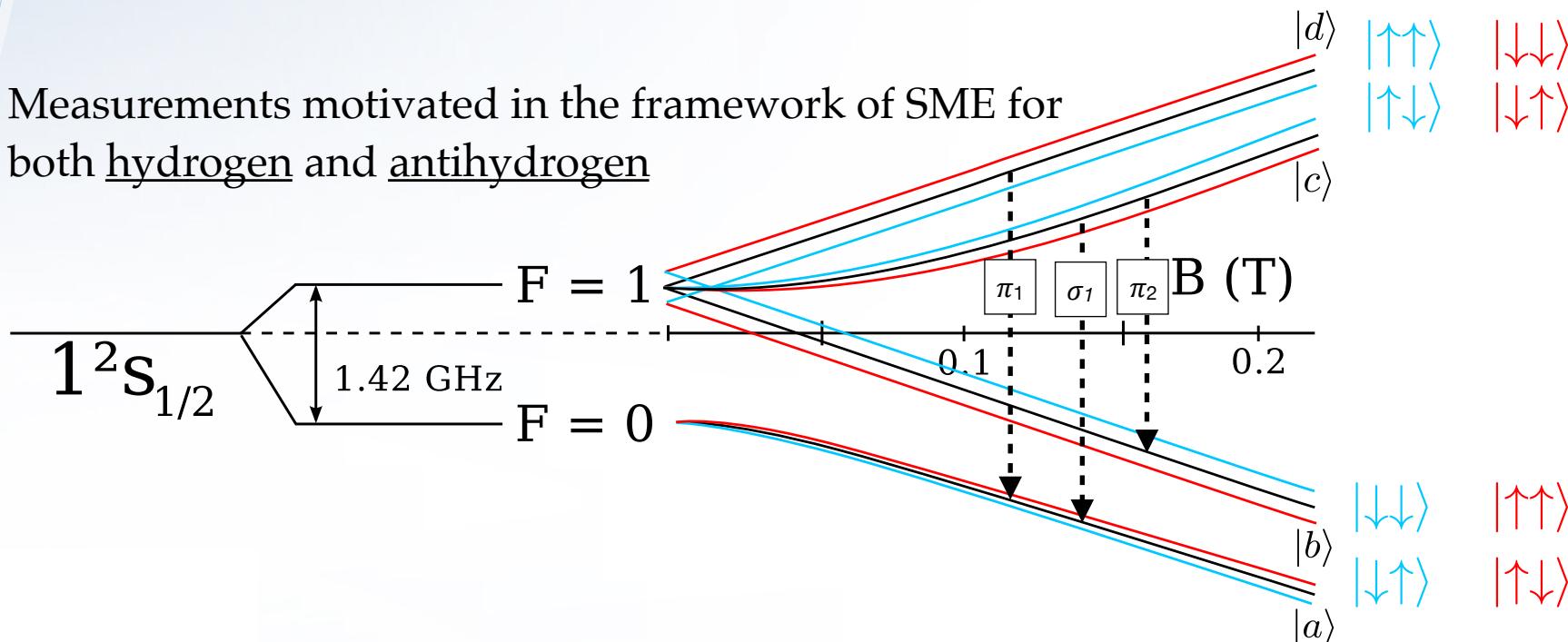
where $g_\pm = g_I \pm g_J$.

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Measurements motivated in the framework of SME for both hydrogen and antihydrogen



HYDROGEN & ANTIHYDROGEN EXPERIMENTS @ CERN



BEAM VS. TRAP

The diagram illustrates two experimental setups: ALPHA and ASACUSA. The ALPHA setup (left) shows a linear beamline for positrons (e^+) passing through a vacuum wall, cryostat wall, and mirror coils. It includes a 3-layer Si detector and a momentum transfer axis (\vec{p}). The ASACUSA setup (right) shows a trap configuration with three nested magnetic rings creating a hexagonal field, focusing particles onto a central detector.

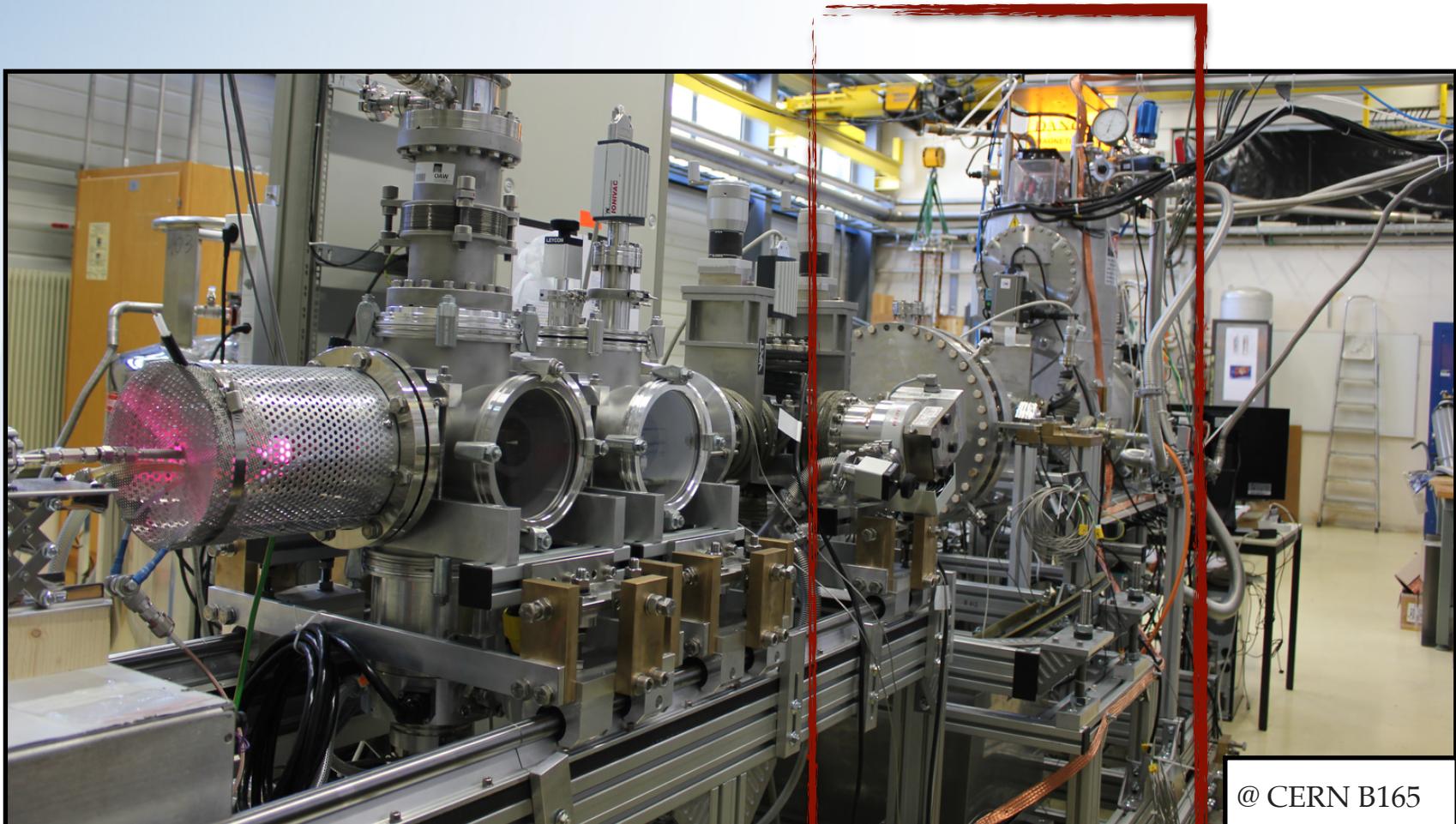
Advantage of beam:

- Absence of strong field gradient
- Lower requirement on the temperature of antihydrogen atoms

Inconvenient of beam:

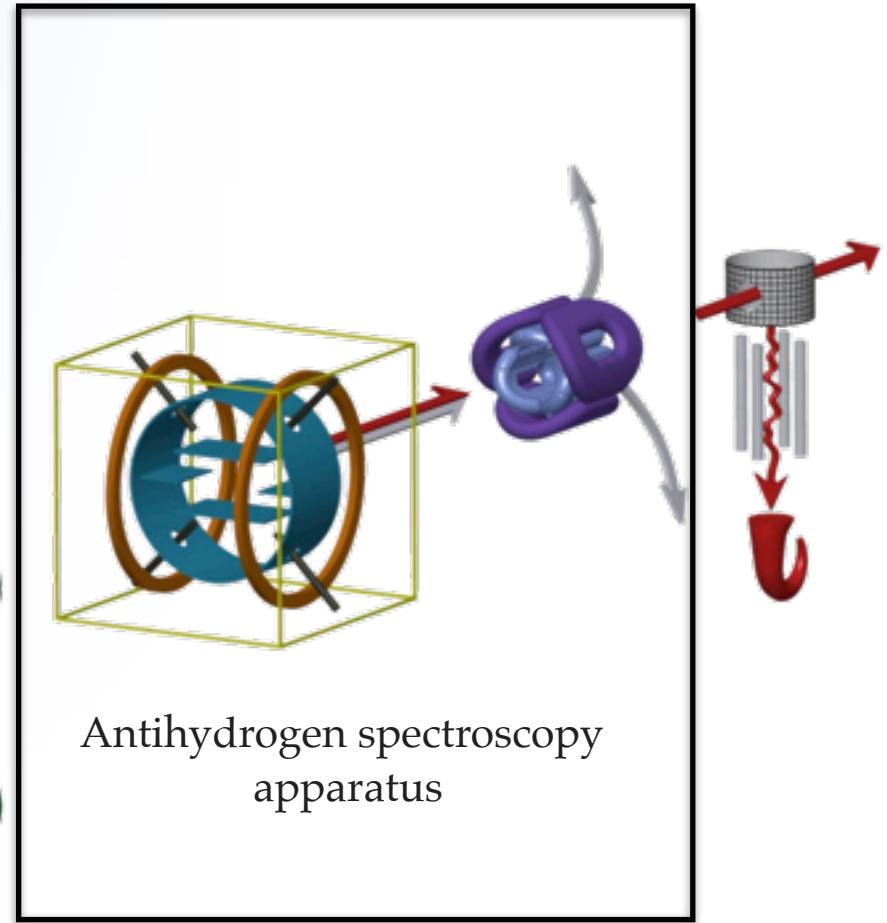
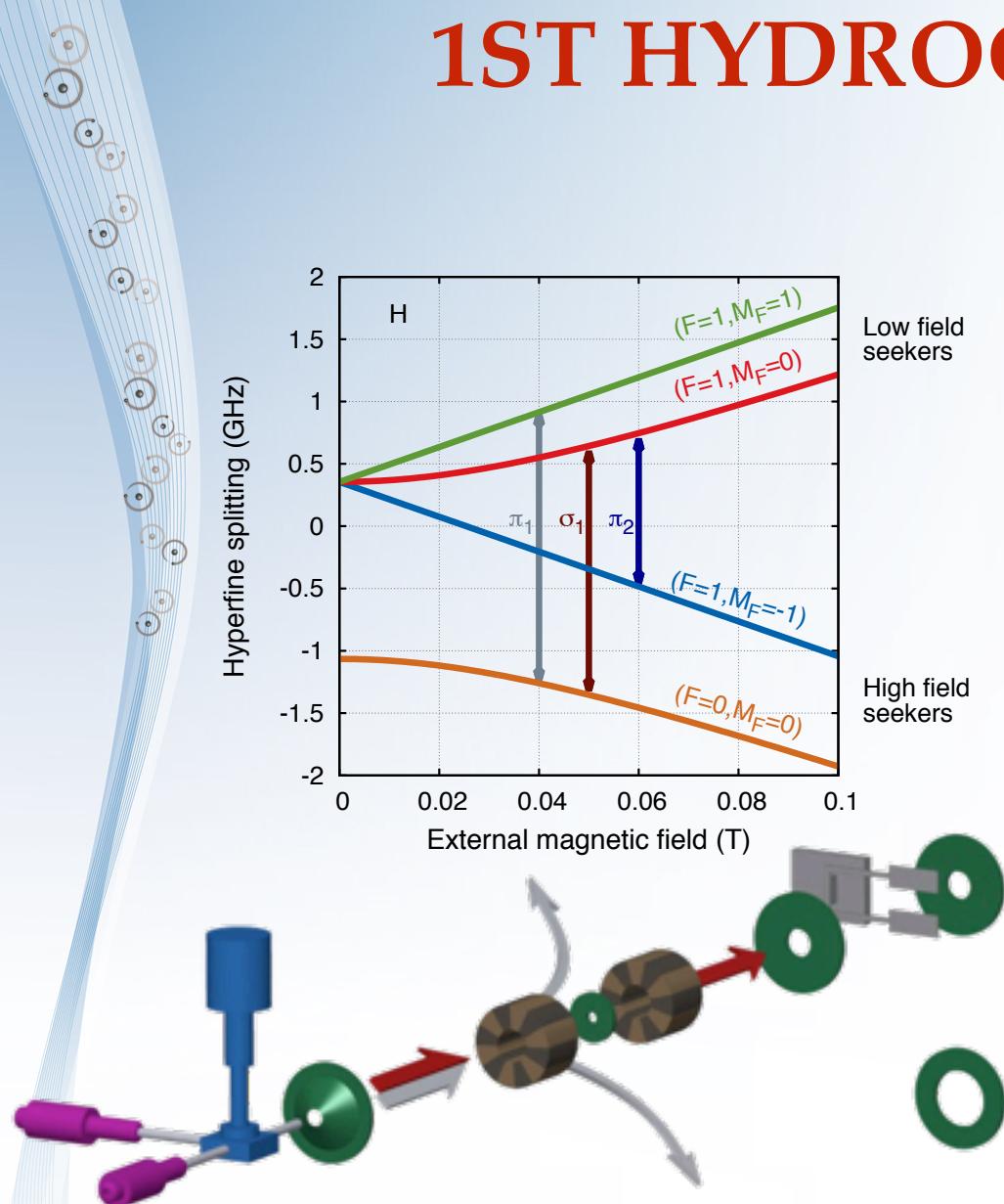
- Need “focussing” (loss of solid angle)
- Cannot easily control the quantum state at the detector
- More difficult to control the polarization

1ST HYDROGEN SETUP



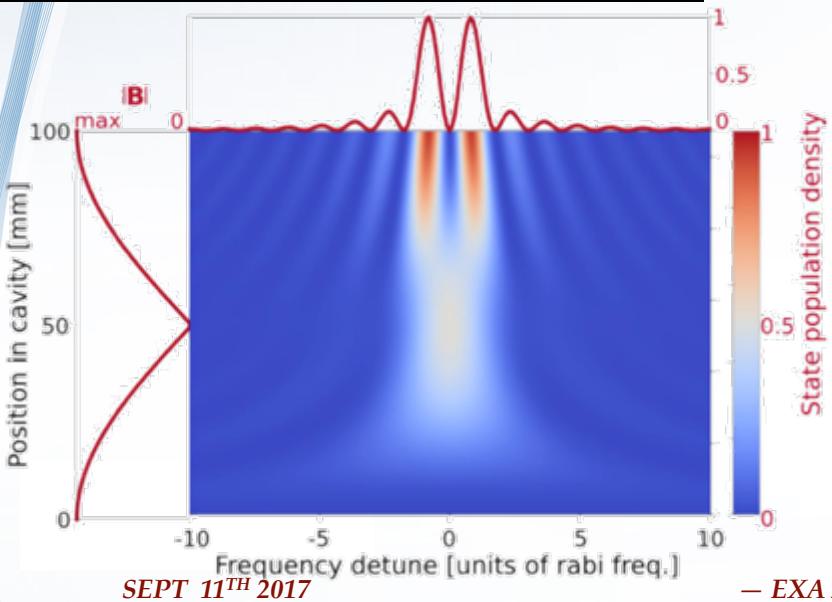
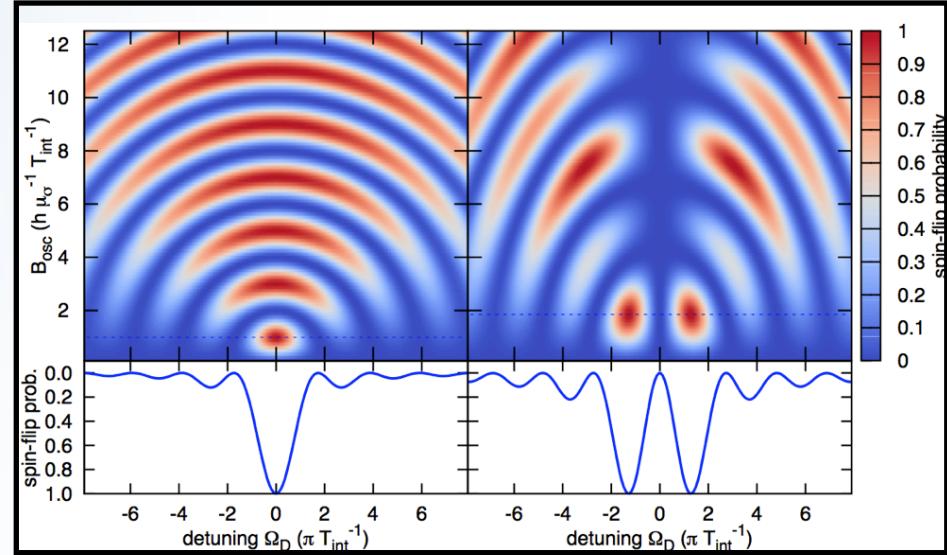
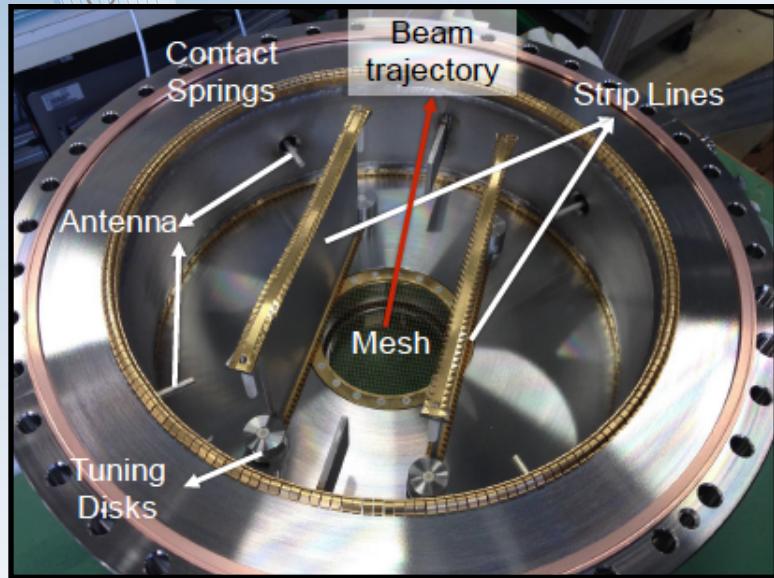
Antihydrogen
spectroscopy
apparatus

1ST HYDROGEN SETUP



1ST HYDROGEN SETUP

“strip-line” cavity design



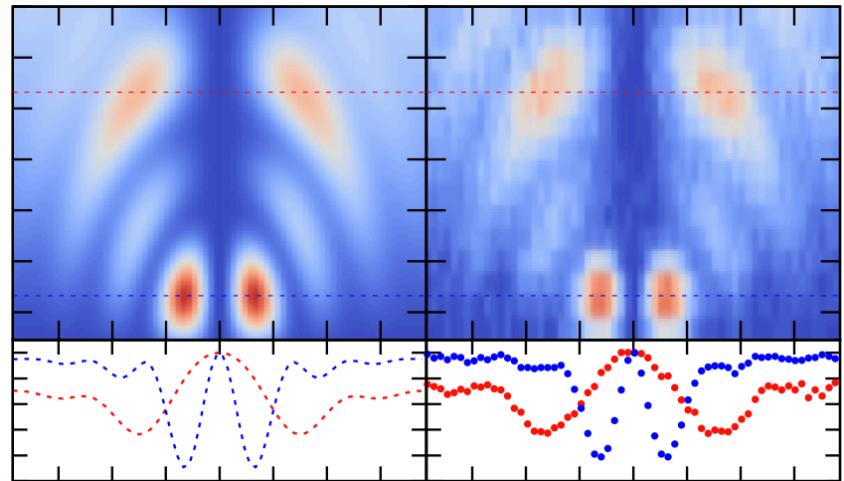
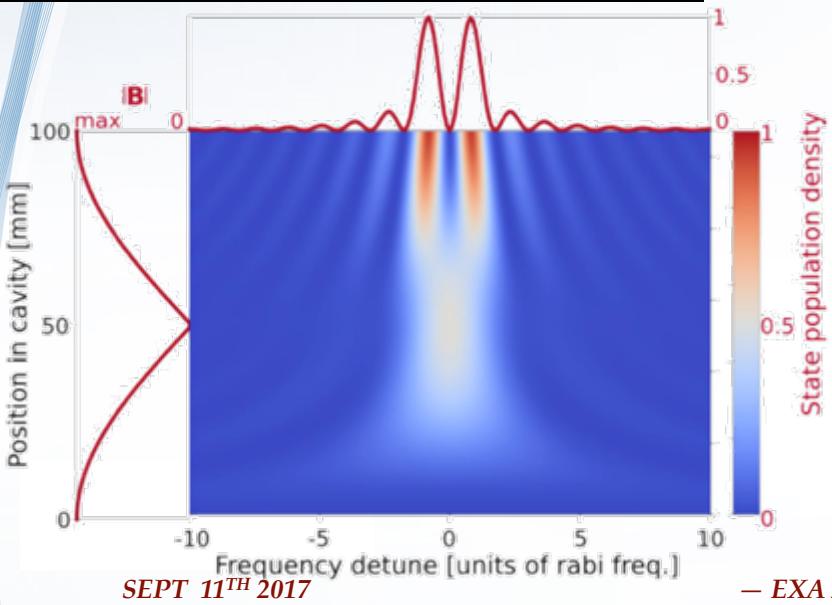
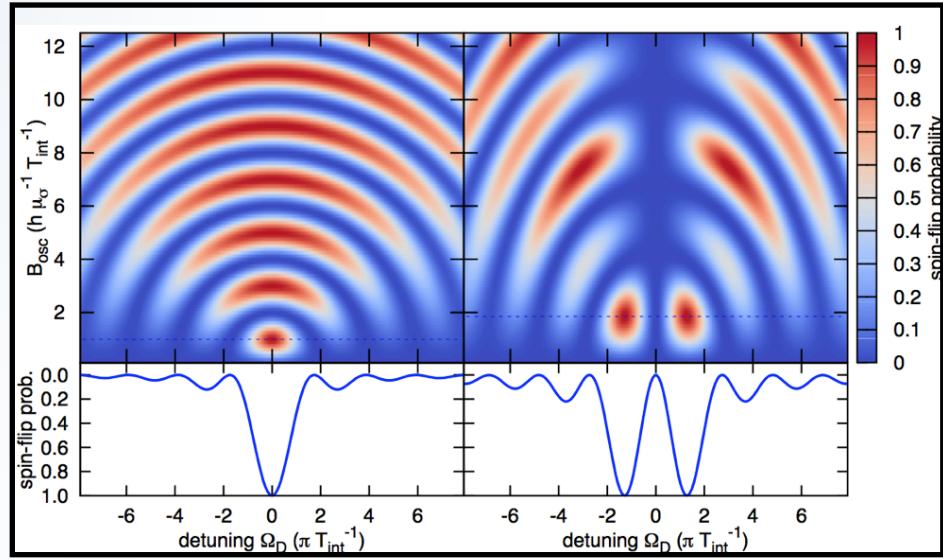
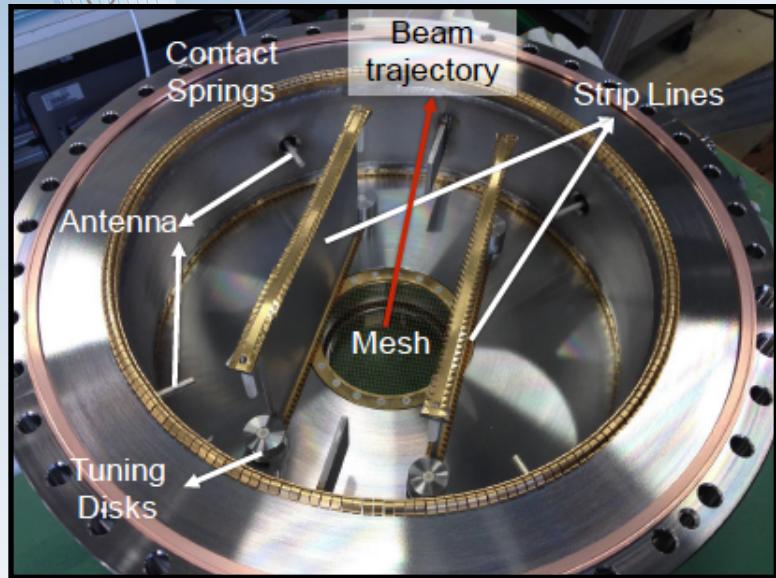
SEPT 11TH 2017

— EXA 2017 — VIENNA —

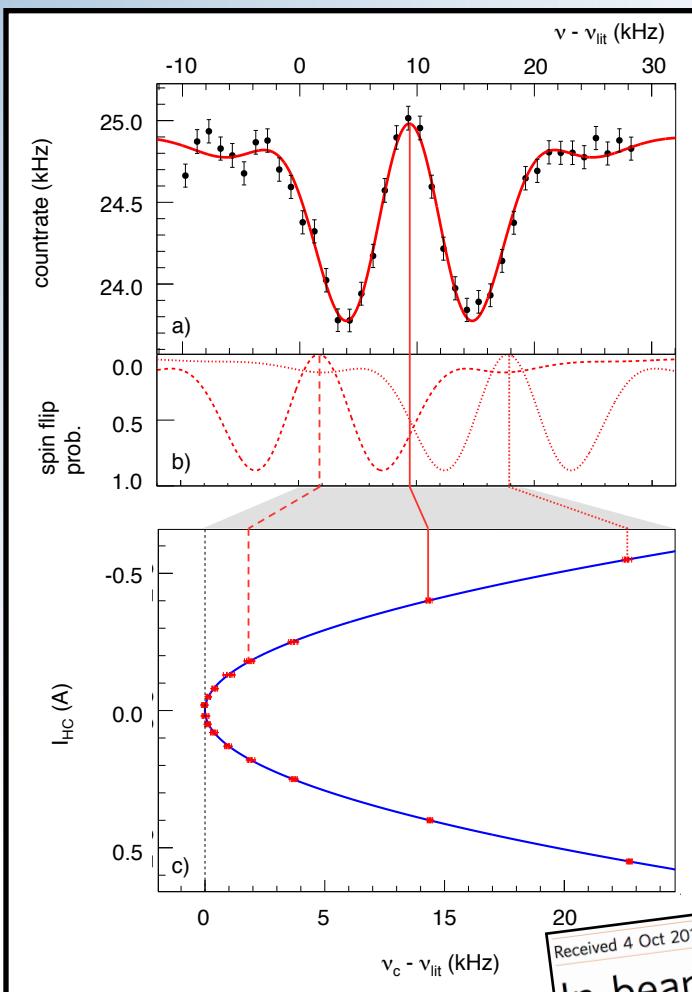
CHLOÉ MALBRUNOT

1ST HYDROGEN SETUP

“strip-line” cavity design



σ MEASUREMENT



$$\nu_{\text{HF}} = 1\ 420\ 405\ 748.4(3.4)(1.6)\ \text{Hz}$$

$$\Delta\nu/\nu = 2.7\ \text{ppb}$$

Table 2 | Error budget.

Contribution	1σ s.d. (Hz)
Systematic error	
Frequency standard	1.62
Common fit parameters	
$\bar{\nu}_H$	0.05
σ_ν	0.03
B_{osc}	0.02
Systematic error total (σ_{sys})	1.62
Statistical error (σ_{stat})	3.43
Total error (σ_{tot})	3.79

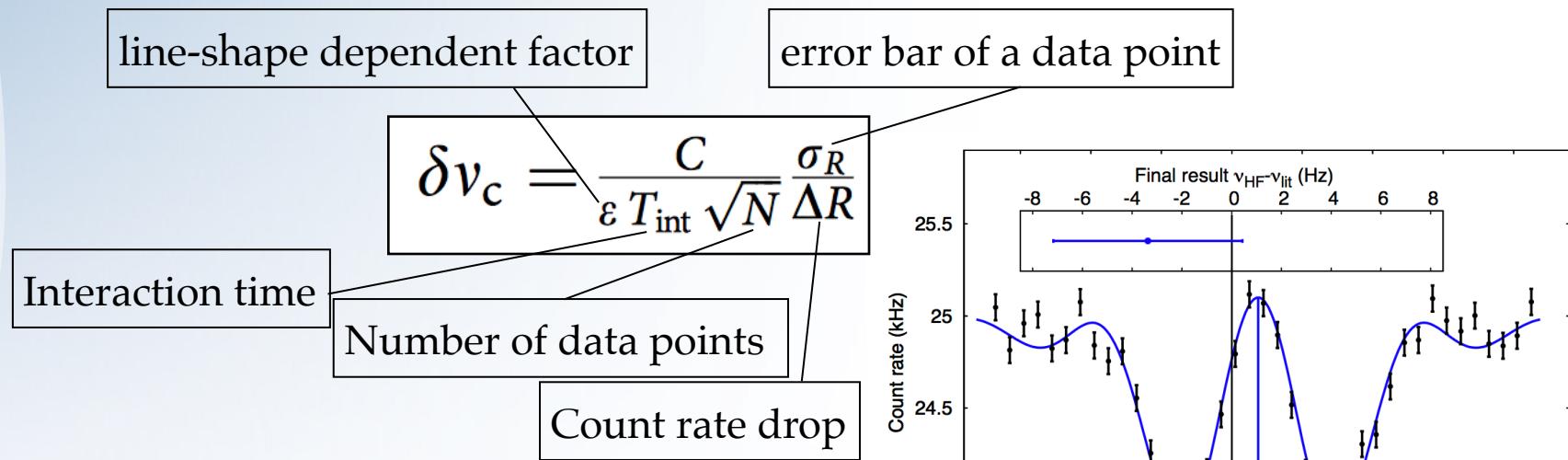
Robust lineshape fit
Extraction of amplitude of oscillatory field,
velocity and velocity spread

Spectroscopy apparatus if fully commissioned

In-beam measurement of the hydrogen hyperfine splitting and prospects for antihydrogen spectroscopy
Received 4 Oct 2016 | Accepted 24 Apr 2017 | Published 12 Jun 2017
DOI: 10.1038/ncomms15749 OPEN
M. Diermaier¹, C.B. Jepsen^{2,†}, B. Kolbinger¹, C. Malbrunot^{1,2}, O. Massicsek¹, C. Sauerzopf¹, M.C. Simon¹, J. Zmeskal¹ & E. Widmann¹

σ MEASUREMENT

ppm result with antihydrogen should be in reach if enough statistics can be gathered



Assuming background :

- 50% atoms are in excited states
- 50% of remaining are in wrong lfs state
- polarisation $P=1/3$

Assuming MB distribution @ 50K

$$P = \frac{f_{\text{LFS}} - f_{\text{HFS}}}{f_{\text{LFS}} + f_{\text{HFS}}}$$

For ppm measurement using 4 resonances we estimate ~ 8000 atoms should be recorded at the antihydrogen detector



π MEASUREMENT

Other possibility :

Measure π_1 & σ_1 at the same field (2 resonances needed, not sensitive to stray field
(from the earth or from CUSP in the antihydrogen experiment)

Advantage : π_1 is sensitive to SME coefficients

BUT π_1 more sensitive to magnetic field inhomogeneities

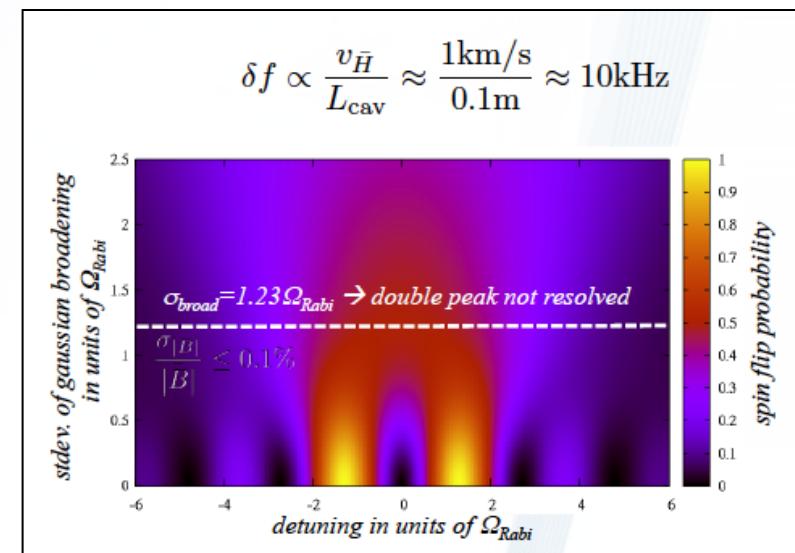
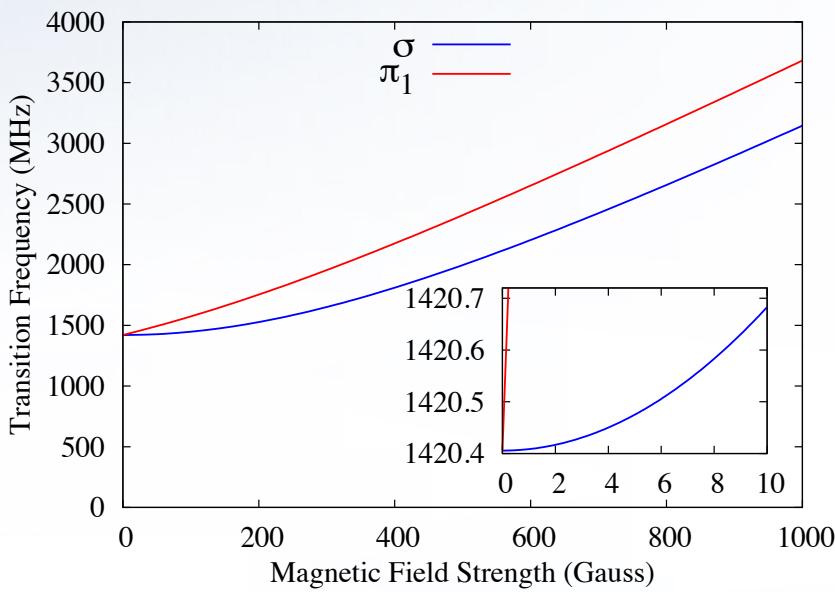
π MEASUREMENT

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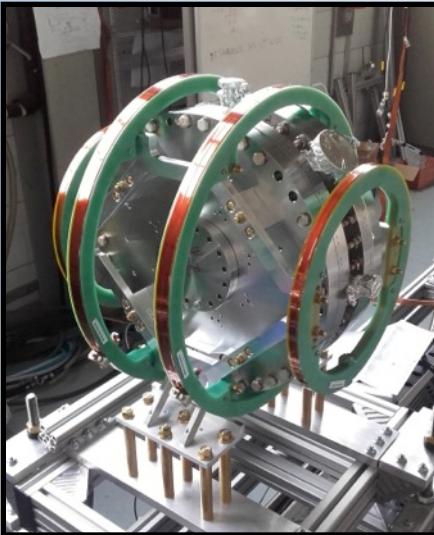
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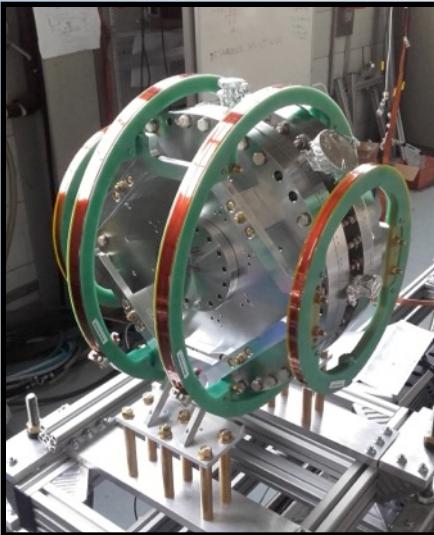


New Helmholtz coils with corrections coils

Cavity tilted at 45° to allow both transitions at the same time

Rotation and up / down movements possible for systematic studies

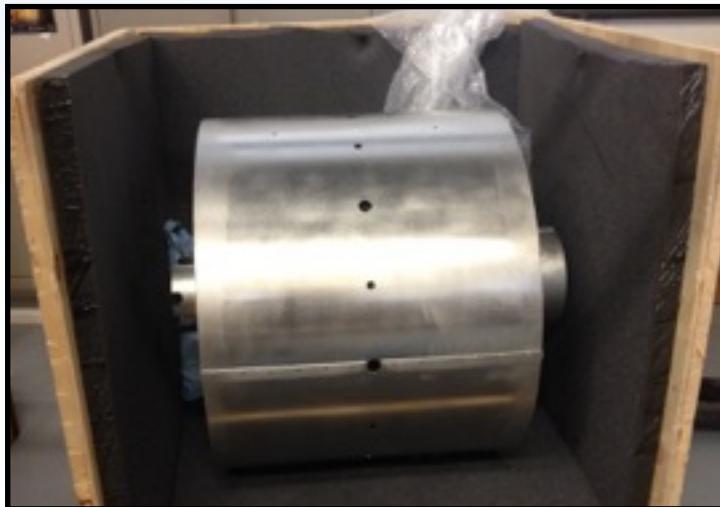
π MEASUREMENT



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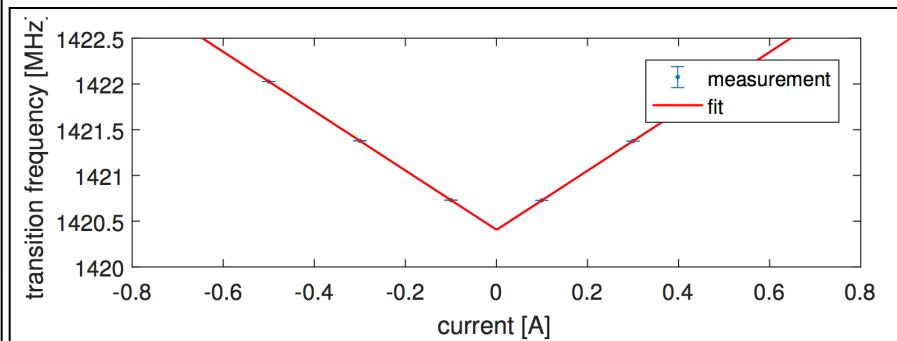
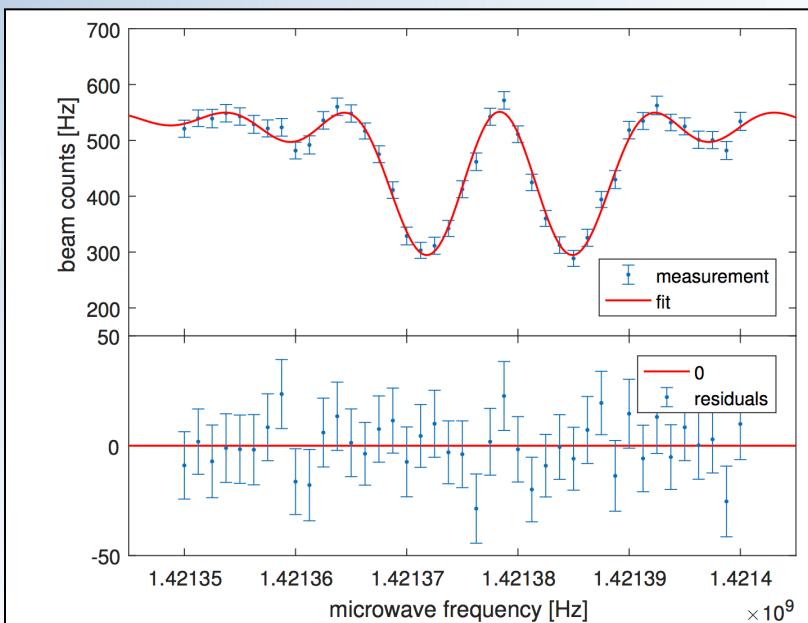
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New 3-layers cylindrical shielding

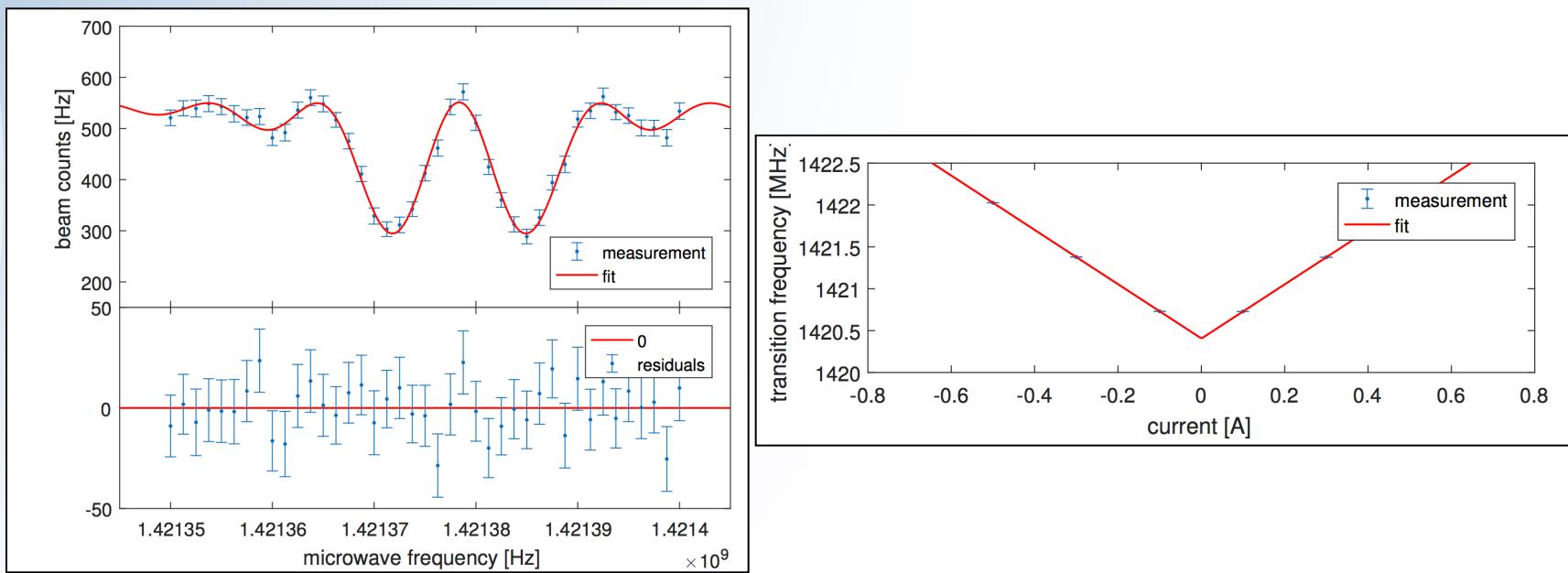
π MEASUREMENT

First π_1 resonance observed



π MEASUREMENT

First π_1 resonance observed



π_1 & σ_1 measured at the same time and same field

ppb measurement in reach

Systematic studies for antihydrogen experiment

2ND HYDROGEN SETUP



Siderial variations constrained by Harvard-Smithsonian maser at mHz level

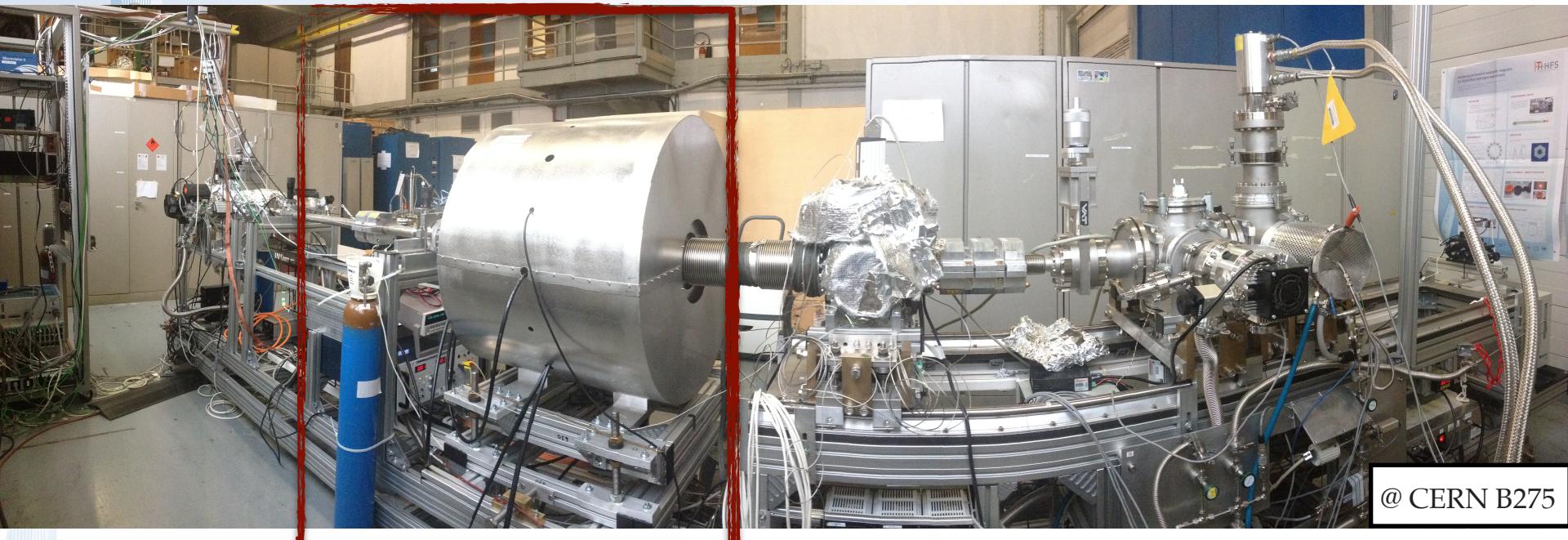
PHYSICAL REVIEW A **68**, 063807 (2003)

Testing *CPT* and Lorentz symmetry with hydrogen masers

M. A. Humphrey, D. F. Phillips, E. M. Mattison, R. F. C. Vessot, R. E. Stoner, and R. L. Walsworth
Harvard-Smithsonian Center for Astrophysics, Cambridge, Massachusetts 02138, USA

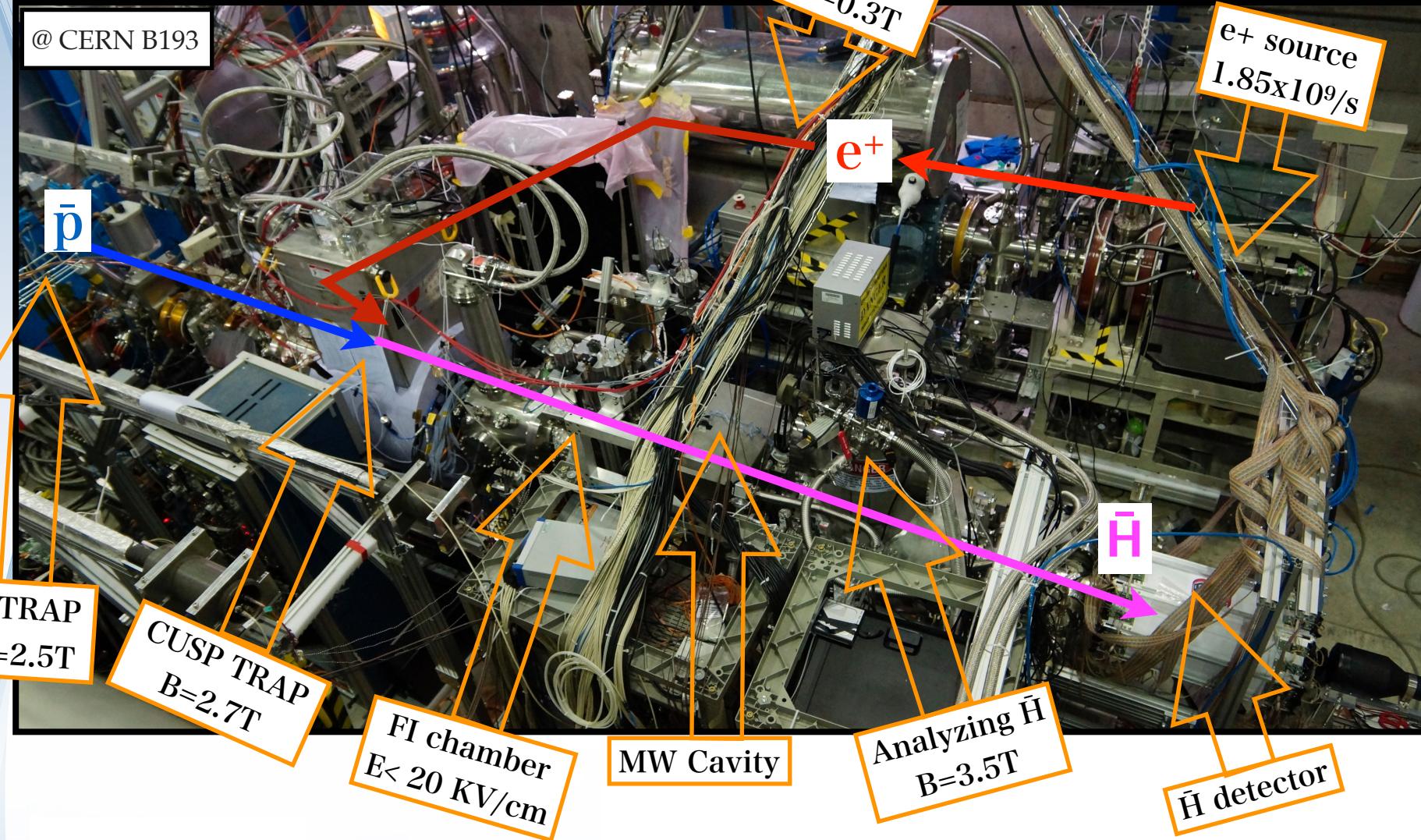
(Received 4 August 2003; published 9 December 2003)

72 SME coefficients involved. 48 constrained, 24 remaining and can be constrained using different orientation of the static B-field



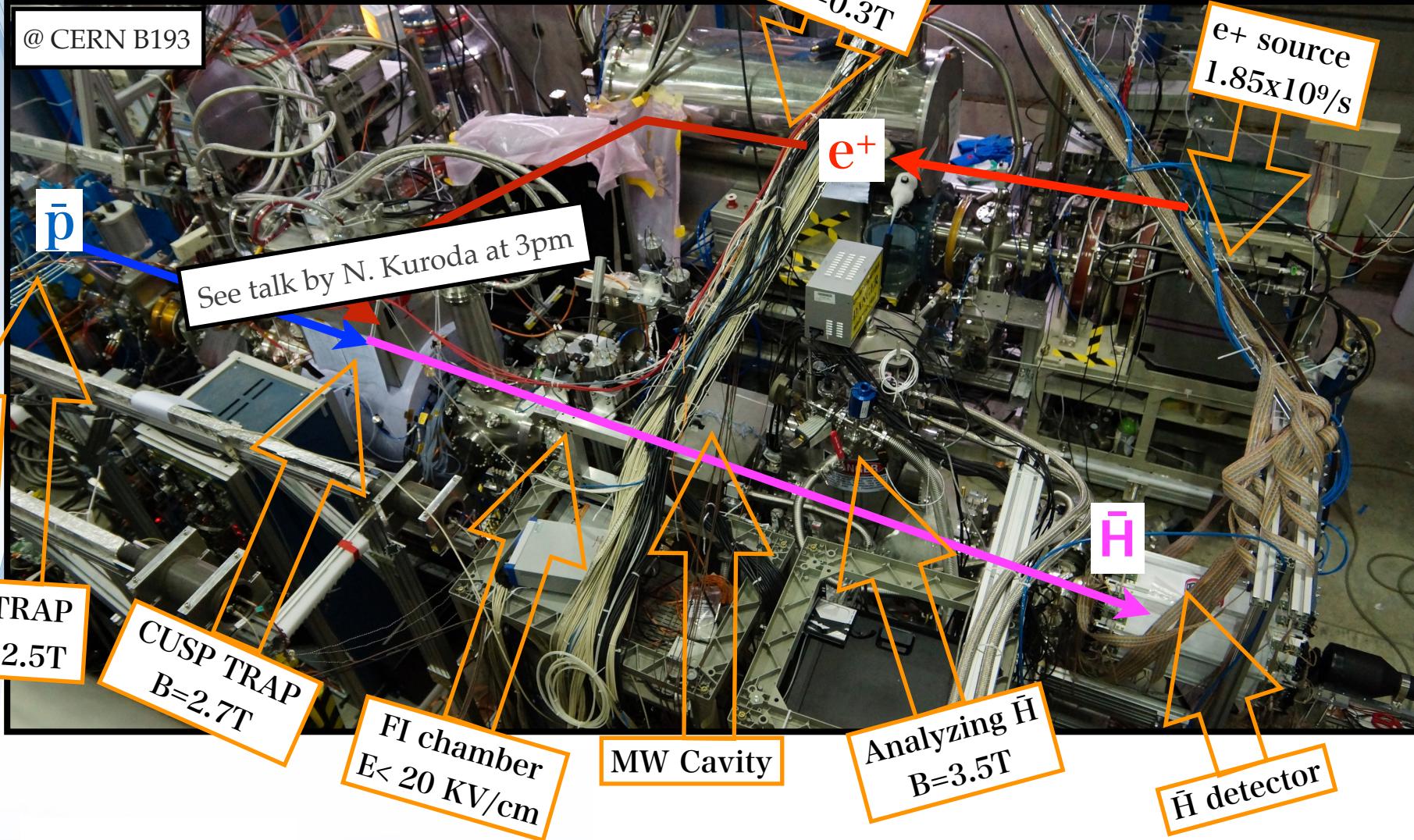
ANTIHYDROGEN SETUP

@ CERN B193



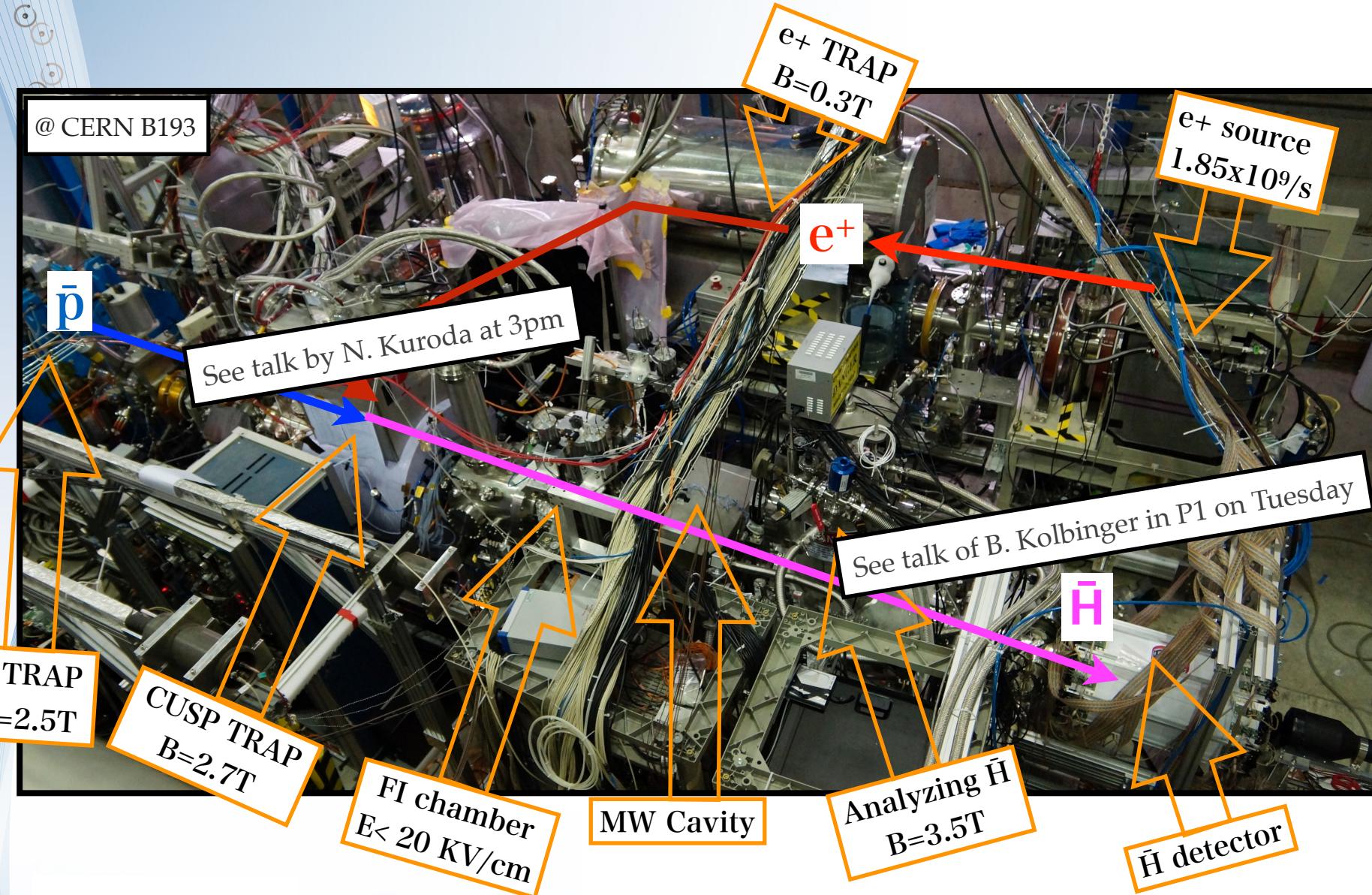
ANTIHYDROGEN SETUP

@ CERN B193



ANTIHYDROGEN SETUP

@ CERN B193



CONCLUSIONS

Two fronts:

- Hydrogen beam: ppb measurement achieved on σ transition.
- Characterization of \bar{H} beam —> towards spectroscopy

New program with Hydrogen :

- Measurement of σ and π
- Constraints on SME coefficients

