

Exotic atoms at extremely high magnetic fields: the case of Neutron Stars atmosphere

Wien, 12.09.2017

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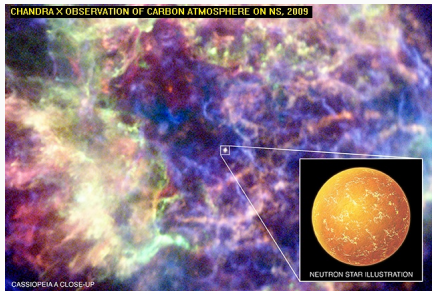
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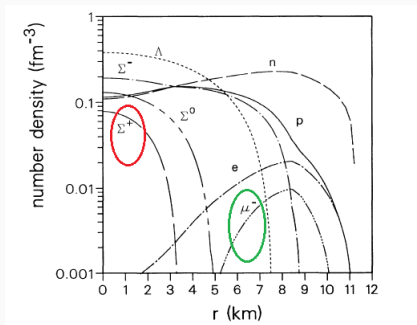
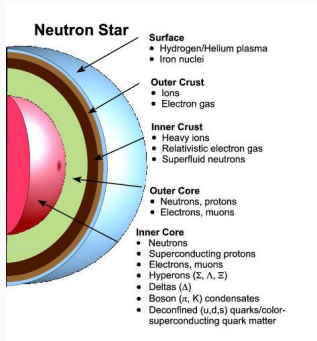
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- Key facts about Neutron Stars
 - Mass and radius
 - Star composition
 - Magnetic field
- Exotic atoms on NS?
 - Quark/Hybrid stars
 - NS/QS conversion
- Atoms in extreme magnetic fields
 - Cylindrical atoms
 - Center of mass motion
 - Hydrogen spectrum
 - Muonic hydrogen/Sigmium
- Outlook

NEUTRON STAR



Not only neutrons!

Main features of a Neutron Star (NS)^[1,2]:

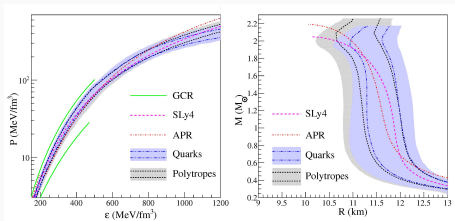
- very high density: nuclear saturation: $\rho_{sat} \approx 2.5 \times 10^{14} \frac{\text{g}}{\text{cm}^3}$ -
NS surface: $\approx 3 \times 10^{-3} \rho_{sat}$ - NS core: $\approx 7 \times \rho_{sat}$
- extremely intense magnetic field: ms pulsar: 10^7 G - magnetar: 10^{16} G
- ...

EQUATION OF STATE

Key goal: to determine the **equation of state** (EOS) for ultradense matter, i.e. the relation between density and pressure:

- At densities exceeding a few times the nuclear density, exotic states of matter may appear such as **hyperons** and Bose condensates
- At higher densities a phase transition to **strange quark matter** may occur

Ultradense matter EOS manifests itself as a **mass-radius** (M-R) relation.



GCR: quantum Monte Carlo calculations

SLy4: Skyrme density functional calculation

APR: variational calculations

Many theoretical EOS available in the literature, each predicting a different M-R relation for NS.

MASS AND RADIUS

Mass and **radius** are the **main observables** in the study of NS:

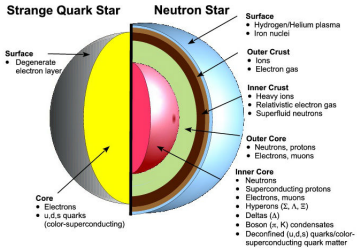
- Masses are measured with great precision from binary radio pulsars timing
- Radius measurements much more challenging, no reliable data
- M and R simultaneous methods not available

→ difficult to discriminate between EOS models.

Some **open classical problems**:

- Stiffness of the equation of state
- **Hyperon puzzle** (hyperons soften the EOS and reduce mass)
- Importance of three-body interactions and role of delta resonances
- The very **nature of star** uncertain: Neutron, Quark or Hybrid stars?

NEUTRON STAR/QUARK STAR

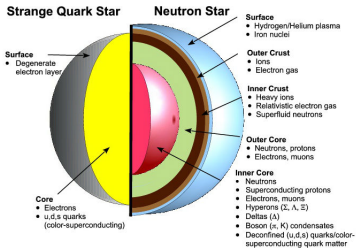


NEUTRON STAR/QUARK STAR

The **conversion process** of a NS into a QS was proposed by different authors [8,9] and is still under study.

Two Families scenario [10,11]:

droplet becomes a macroscopic expanding bubble of QM. **Hydrodynamical** description in two steps: rapid burning (few ms), favoured by instabilities, followed by slow burning (~ 10 s), with strangeness diffusion.



In this model NS co-exist with **quark stars** (QS):

- NS can be very compact and have a maximum mass of $\sim 1.5 - 1.6M_{\odot}$
- QS can have large radii and be even more massive, up to $2.75M_{\odot}$.

NS/QS CONVERSION AND TWO FAMILIES SCENARIO

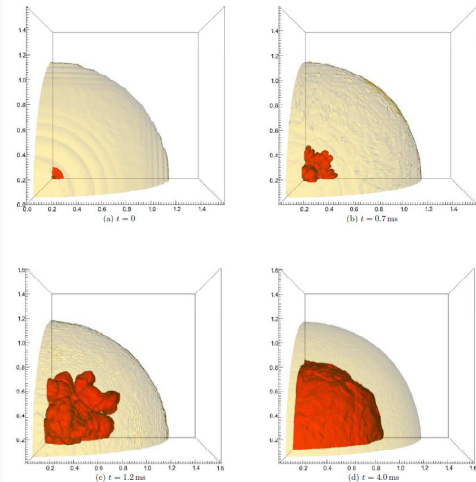
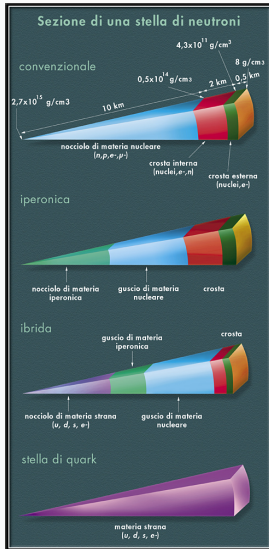


FIG. 1: (color online) Model: Set 1, $M = 1.4M_{\odot}$. Conversion front (red) and surface of the neutron star (yellow) at different times t . Spatial units 10^6 cm.

- Three-dimensional **hydrodynamic simulations** of the combustion process: temperature profiles and expected neutrino signal.
- The process is a powerful source of neutrinos: initial luminosity $3 \times 10^{52} \text{ erg/s}$.
- Neutrino ablation can lead to a **significant mass ejection** of the nuclear envelope.

MODELS FOR NS/QS CONVERSION



Other models:

- **Quark Droplet Nucleation:** [12]
quark deconfinement as first order phase transition, with formation of a critical size drop (as dew formation in supersaturated vapor).
- **Quark-Novae** model [13]
quark deconfinement as detonation/deflagration, with significant amount of matter ejection by a mechanical shock at the end of the process.

In all cases, **exotic matter** could be **ablated by neutrinos** towards the surface of the star.

ATMOSPHERE OF NS

We focus our attention on the **atmosphere**:

- theoretical models from H, He, C atmospheres and for Fe crust
- difference between isolated and binary NS (accretion process)
- good fits to data by recent C atmosphere models

Given the uncertainties on the EOS for these stars, it is worth to look for **new observables**:

1. looking first at the H case...
2. ...and trying to extend what we find to exotic atoms.

The **atmosphere of a QS** could be radically **different** from the **atmosphere of a NS**. Is there a chance to distinguish between these two types of compact stars?

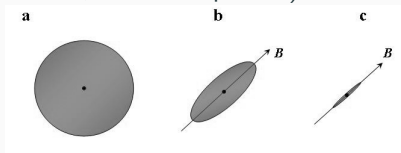
ATOMS IN STRONG MAGNETIC FIELDS

Effects of a **strong magnetic field** on H atoms (grey areas: ellipsoids with probability to find an electron $> e^{-1}$; solid dots: protons)

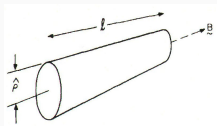
a) $B \ll 10^9 \text{ G}$

b) $B = 10^9 \text{ G}$

c) $B = 10^{12} \text{ G}$



E field as perturbation: "spherical" atomic levels \rightarrow "**cylindrical**" atomic levels ^[3,4]



$$\hat{\rho} = \rho_0 \ll a_0$$

ρ_0 : radius of ground state

Reference field for NS: $B_0 = \frac{m_e^2 e^3 c}{\hbar^3} = 2.3505 \times 10^9 \text{ G}$,
corresponding to cyclotron radius \equiv Bohr radius.

QUANTUM MECHANICAL TREATMENT

- Numerical **solutions** exist **only for H** atom
- Landau energy levels: principal quantum number n
- 1D Schrödinger equation with solution $f_{m\nu}(z)$:

$$-\frac{\hbar^2}{2m_e\rho_0^2}f''_{m\nu} - \frac{e}{\rho_0}V_m(z)f_{m\nu} = E_{m\nu}f_{m\nu} \quad m, \nu = 0, 1, 2, \dots$$

- **Two quantum numbers** m and ν : m for radial excitations

$$\rho_m = (2m + 1)^{1/2}\rho_0 \quad m = 0, 1, 2, \dots$$

and ν to account for longitudinal nodes

- **Two types of states**^[5]:

DEEPLY BOUND

$$m \geq 0 \quad \nu = 0$$

WEAKLY BOUND

$$m \geq 0 \quad \nu > 0$$

Classification of states with the parameter $b \equiv \frac{B}{B_0}$

ENERGY LEVELS

INFINITE PROTON MASS

$$E_{m0} \approx -0.16 I_m^2 \text{ a.u.} \quad (\text{for } 2m + 1 \ll b) \quad I_m = \ln\left(\frac{b}{2m + 1}\right)$$

$$E_{m\nu} = -\frac{1}{(2\nu_1 + \delta)^2} \text{ a.u.} \quad (\nu_1 = 1, 2, 3, \dots)$$

$$\delta = \begin{cases} 2\rho_m/a_0 & \nu = 2\nu_1 - 1 \\ [\ln(a_0/\rho_m)]^{-1} & \nu = 2\nu_1 \end{cases}$$

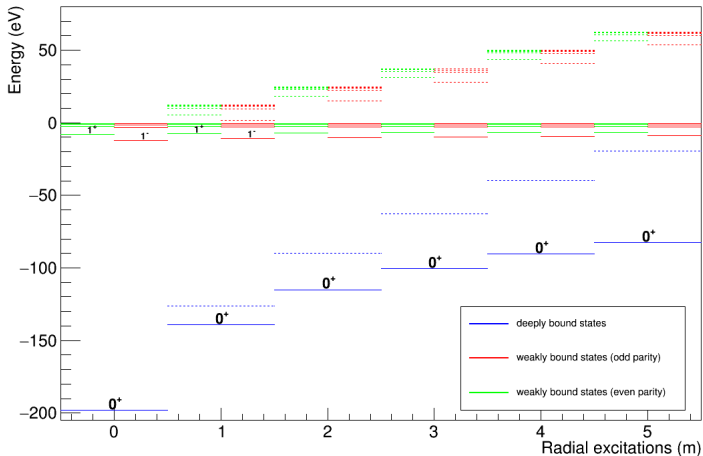
FINITE PROTON MASS

$$m_e \rightarrow \mu = \frac{m_e \times m_p}{m_e + m_p}$$

$$\Delta E = 29.6 m \frac{B}{4.7 \times 10^{12} \text{ G}} \text{ eV}$$

ENERGY LEVELS

Spectrum of H atom in a field 2×10^{12} G



Continuous lines: infinite proton mass

Dashed lines: finite proton mass

CENTER OF MASS MOTION

Atoms motion described by a **pseudo-momentum** \mathbf{K} , derived from canonical momentum $\mathbf{\Pi}$ [6]:

$$\mathbf{K} \equiv \mathbf{\Pi} - \frac{e}{c} \mathbf{B} \times \mathbf{r}$$

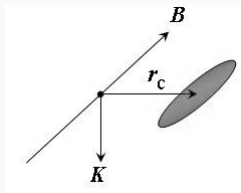
$$\mathbf{K} = \mathbf{K}_e + \mathbf{K}_p,$$

$$r_c = \frac{c \mathbf{B} \times \mathbf{K}_\perp}{eB^2}, \quad r_c = \frac{K_\perp}{b} \text{ a.u.}$$

K_\perp : \mathbf{K} component orthogonal to \mathbf{B} .

Motion unit scale:

$$1 K_\perp (\text{a.u.}) = 3.73 \text{ keV}/c$$



Two different solutions:

- centered states
- **decentered** states

Atoms moving across \mathbf{B} may become decentered: **proton external to electron cloud!**

The guiding center r_c is perpendicular to \mathbf{B} and to \mathbf{K} .

SOLUTION FOR HYDROGEN

Deeply bound states

- centered states:

$$E_{m0}(K_{\perp}) \simeq E_m + \frac{K_{\perp}^2}{2M_{\perp m}}$$

$M_{\perp m}$: effective transverse mass

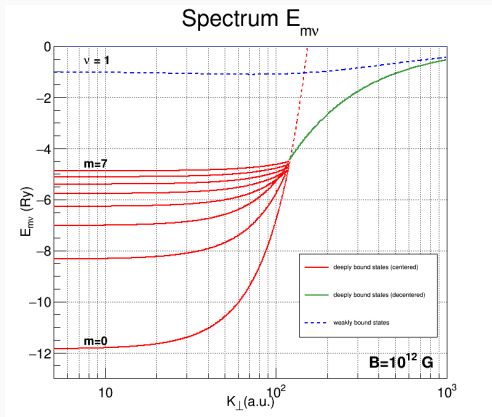
- decentered states:

$$E_{m0}(K_{\perp}) \sim -\frac{b}{K_{\perp}}$$

Weakly bound states:

analytical approximations^[7]

Validity limit of the model: $100 \leq b \leq 10^6$.



EXOTIC ATOMS?

VALIDITY LIMIT

$$100 \leq b \leq 10^6$$

DEFINITION

$$b = \frac{B}{B_0} = \frac{\hbar^3 B}{m_e^2 e^3 c}$$

EXOTIC ATOMS?

VALIDITY LIMIT

$$100 \leq b \leq 10^6$$

DEFINITION

$$b = \frac{B}{B_0} = \frac{\hbar^3 B}{m_e^2 e^3 c}$$

- **muonic hydrogen** (p- μ^-):

$$m_e \rightarrow m_\mu \quad \rightarrow \quad b = \frac{\hbar^3 B}{m_\mu^2 e^3 c}, \quad \frac{b}{b^H} \sim 10^{-2} \rightarrow B : 10^{12} \text{ G} \rightarrow 10^{16} \text{ G}$$

VALIDITY LIMIT

$$100 \leq b \leq 10^6$$

DEFINITION

$$b = \frac{B}{B_0} = \frac{\hbar^3 B}{m_e^2 e^3 c}$$

- **muonic hydrogen** ($p-\mu^-$):

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- **Sigmium** ($\Sigma^+ - e^-$):

$$m_e \rightarrow m_\Sigma \rightarrow b = \frac{\hbar^3 B}{m_\Sigma^2 e^3 c}, \frac{b}{b^H} \sim 1 \rightarrow B : 10^{12} \text{ G} \rightarrow 10^{12} \text{ G}$$

VALIDITY LIMIT

$$100 \leq b \leq 10^6$$

DEFINITION

$$b = \frac{B}{B_0} = \frac{\hbar^3 B}{m_e^2 e^3 c}$$

- **muonic hydrogen** ($p-\mu^-$):

$$m_e \rightarrow m_\mu \rightarrow b = \frac{\hbar^3 B}{m_\mu^2 e^3 c}, \frac{b}{b^H} \sim 10^{-2} \rightarrow B : 10^{12} \text{ G} \rightarrow 10^{16} \text{ G}$$

- **Sigmium** ($\Sigma^+ - e^-$):

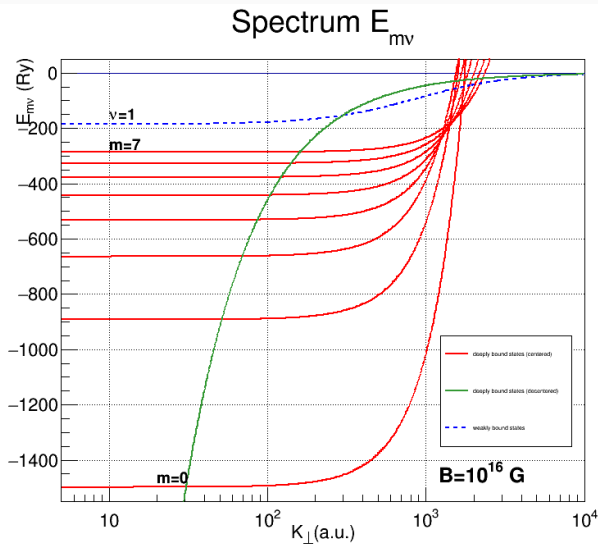
$$m_e \rightarrow m_\Sigma \rightarrow b = \frac{\hbar^3 B}{m_\Sigma^2 e^3 c}, \frac{b}{b^H} \sim 1 \rightarrow B : 10^{12} \text{ G} \rightarrow 10^{12} \text{ G}$$

Scaling rule:

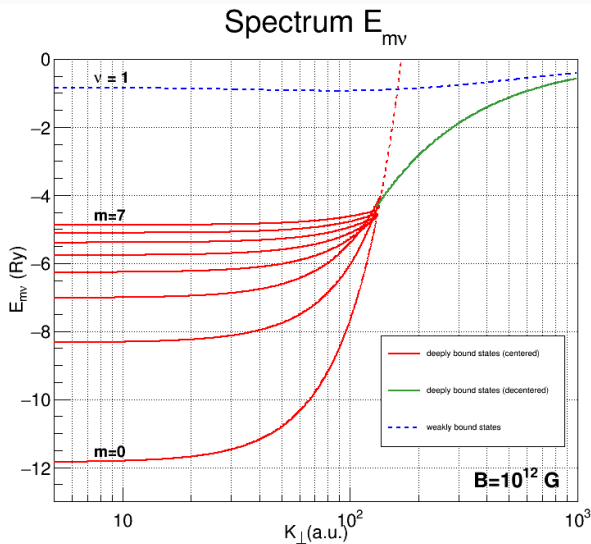
$$z = \frac{\mu}{m_e}, \quad a_0 = \frac{a_0^H}{z} \quad E = z \times E^H$$

MUONIC HYDROGEN

Muonic hydrogen



Sigmium



PRELIMINARY RESULTS FOR $1^- \rightarrow 0^+$

Atom	K_{\perp} (a.u.)	Energy (eV)	λ (nm)	Note
Hydrogen	0	147.5877	8.4	UV
"	10	146.6178	8.5	"
"	50	129.1634	9.6	"
"	100	77.6384	16	"
Muonic hydrogen	0	17848.5	0.06946	X-ray
"	10	17851.5	0.069453	"
"	50	17870.2	0.069381	"
"	100	17885.1	0.069323	"
Sigmium	0	149.832	8.27	UV
"	10	149.029	8.32	"
"	50	134.488	9.22	"
"	100	91.7076	13.52	"

Transitions with B intensities as indicated in the previous slides.

CONCLUSIONS

- Hydrogen-like atoms, involving μ^- , Σ^+ or other **exotic constituents** could be formed in the NS/QS conversion
- We have investigated the **energy levels structure** of hypothetical exotic atoms and made some predictions on transitions that could help to **discriminate among EOS**
- Hyperfine interaction for cylindrical atoms: calculation in progress. . .
- If the results are confirmed, the proposed calculations could give a **direct evidence** of the presence of **hyperons on NS**
- **Request** to the community: it would be interesting to
 1. Estimate **radial exotic fractions** during conversion process
 2. **Numerically solve** 1D Schrödinger equation for exotic atoms

ACKNOWLEDGMENTS

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Atoms in extreme magnetic fields

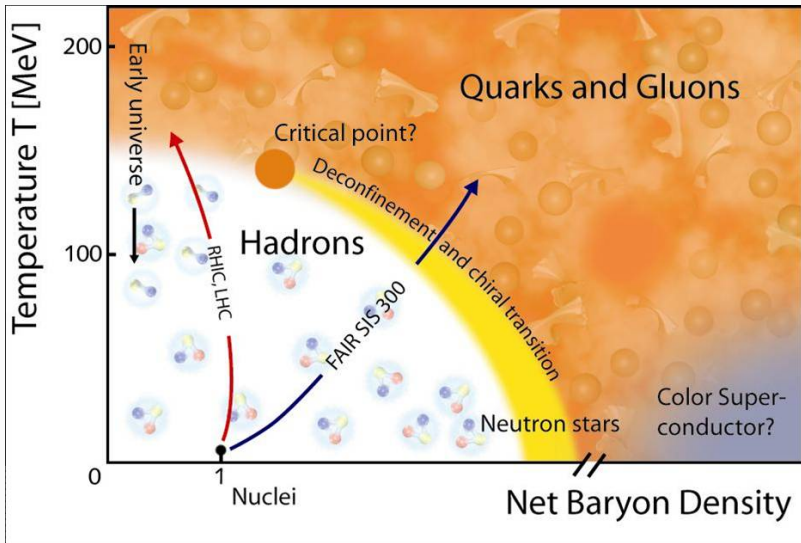
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NS/QS conversion

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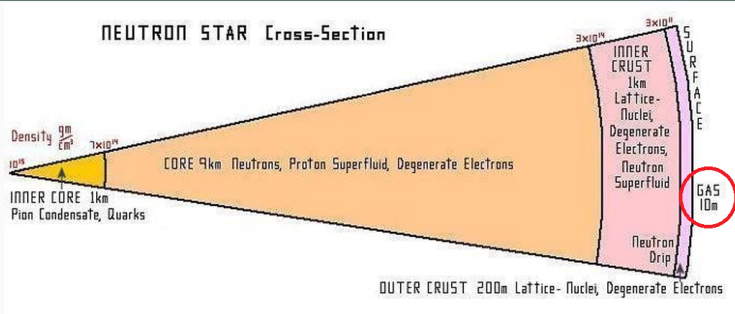
Backup slides

QUARK GLUON PLASMA



NEUTRON STARS

Original star mass (in M_{\odot})	Process	Final object
$1 < M < 8$	Planetary Nebula	White Dwarf
$\sim 8 - 10$	Supernova	Neutron Star
> 10	Supernova	Black Hole



- Degenerate Fermi gas $\rightarrow R \sim 10 \text{ km}$ e $M \sim 1.5M_{\odot}$
- **Giant nucleus** ($A_c \simeq 0.11 \times 10^{57}$ $A_{NS} \sim 1.6 \times 10^{57}$)

MASSES

Classification by the **maximum mass**

M_{max} that the EOS can sustain:

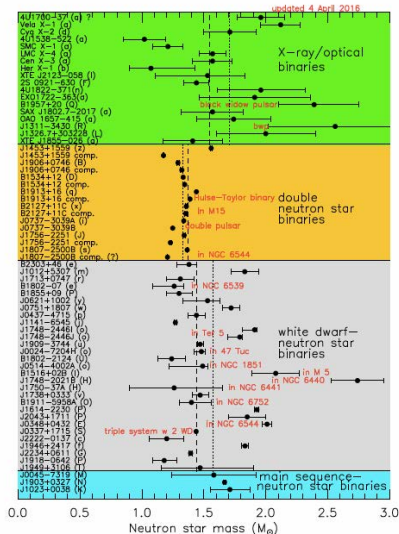
- **Soft EOS** (low central density) →
 $M_{max} \sim 1.5 - 1.7M_{\odot}$
- **Stiff EOS** (high central density) →
 $M_{max} \sim 2.4 - 2.5M_{\odot}$

Recent observations:

PSR J1614-2230: $M = 1.97 \pm 0.04M_{\odot}$

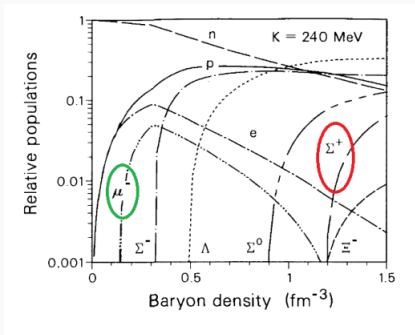
PSR J0348-0432: $M = 2.01 \pm 0.04M_{\odot}$

seem to **rule out** most **soft EOS** and to limit the presence of quark matter in the NS core.

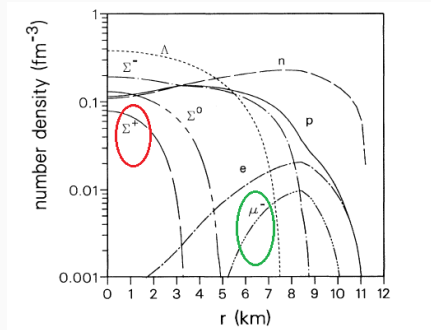


PARTICLES IN NEUTRON STARS

Not only neutrons!



Distribution of particles vs density of matter



Distribution of particles vs radius

Nuclear interactions (NN,YN,YY,NNN,NNY,NYY&YYY) are crucial and well studied in the core ^[1,2].

Any **EM interaction** among these particles?

NEUTRON STAR MAGNETIC FIELD

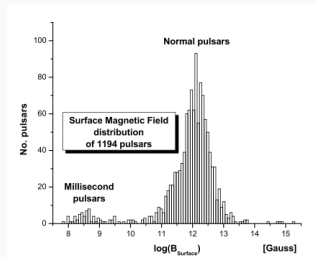
Typical fields on NS

Type of pulsar	Surface magnetic field
Millisecond	$10^7 - 10^9 G$
Normal	$10^{12} G$
Magnetar	$10^{14} - 10^{16} G$

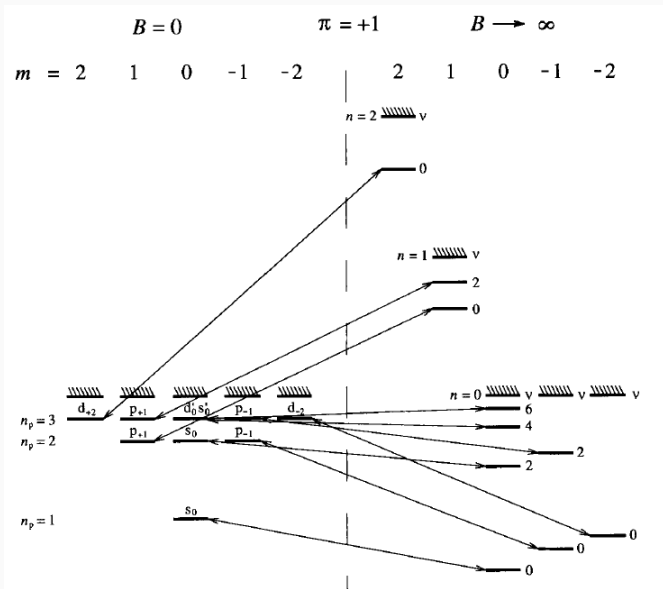
Origin:

- Conservation of magnetic flux during gravitational collapse of iron core
- Electric currents flowing in the highly conductive NS interior
- Spontaneous transition to a ferromagnetic state due to nuclear interactions

Extremely high compared to other natural or laboratory fields (pulsed max in lab $\sim 2.8 \times 10^7 G$).

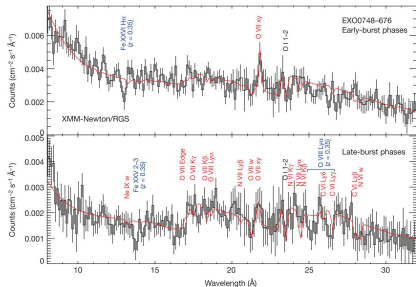


ENERGY LEVELS CORRESPONDENCE

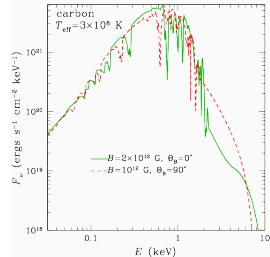


POSSIBLE FUTURE STUDIES

- **Search** of these lines in available datasets



EXO07482676 spectrum from XMM-Newton



CAS A C spectrum from Chandra X

- Estimate **radial exotic fractions** during conversion process (taking possibly into account also particles lifetimes)
- **Numerically solve** Schrödinger equation for exotic atoms
- Hyperfine interaction for cylindrical atoms
- Recent new missions as NICER, LOFT as source of new data

HYPERFINE SPLITTING

Evaluation of the **hyperfine constant** for cylindrical atoms:

$$a_J = 2 \mu_B \gamma_I \hbar \frac{l(l+1)}{j(j+1)} \langle r^{-3} \rangle_{l \neq 0}$$

Expectation value of $\langle r^{-3} \rangle$ on the 1D states.

- Traditional atoms:

$$\langle r^{-3} \rangle = \frac{1}{l(l+1)(l+\frac{1}{2})} \left(\frac{Z}{n a_0} \right)^3$$

- **Cylindrical atoms** (tightly bound states):

$$\langle r^{-3} \rangle = \left[\frac{\sqrt{\lambda_m^2} \gamma^m}{\Gamma(m+1)} l_1 l_2 \right] \frac{2}{\sqrt{\pi}} \left(\frac{b}{2} \right)^{3/2} \left(\frac{Z}{a_0} \right)^3$$

with λ_m obtained with variational methods, $\gamma = \frac{1}{2\rho_0^2}$, l_1 and l_2 integrals on the radial and longitudinal part of the wavefunction.

In principle, each level becomes a **doublet**.