



Tracking

Juli 4, 2017

Motivation

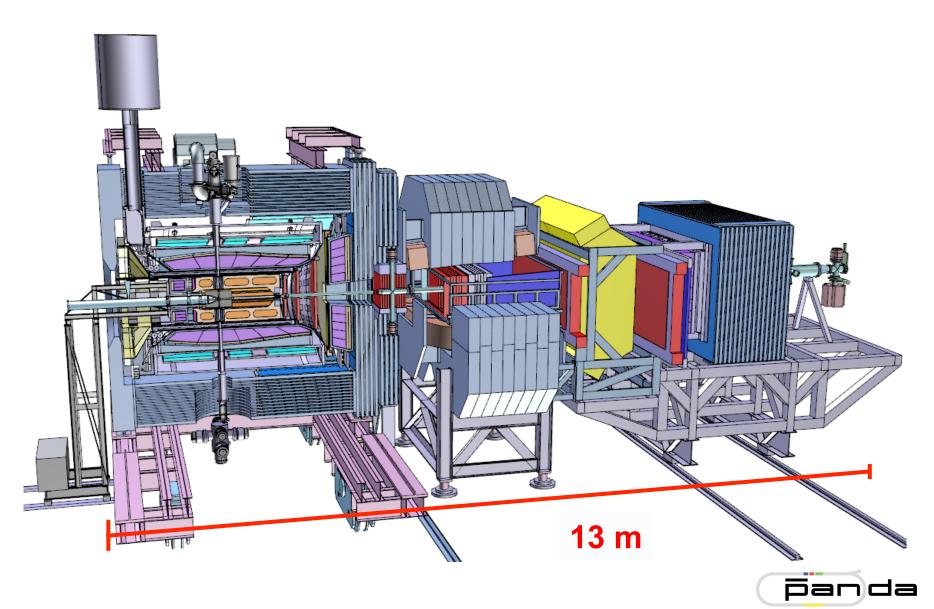


- Why tracking?
 - Distinguish charged from neutral particles
 - Determine the charge of a particle
 - Determine the absolute momentum
 - Determine the direction of momentum
 - Determine the production/decay point
 - See the full story



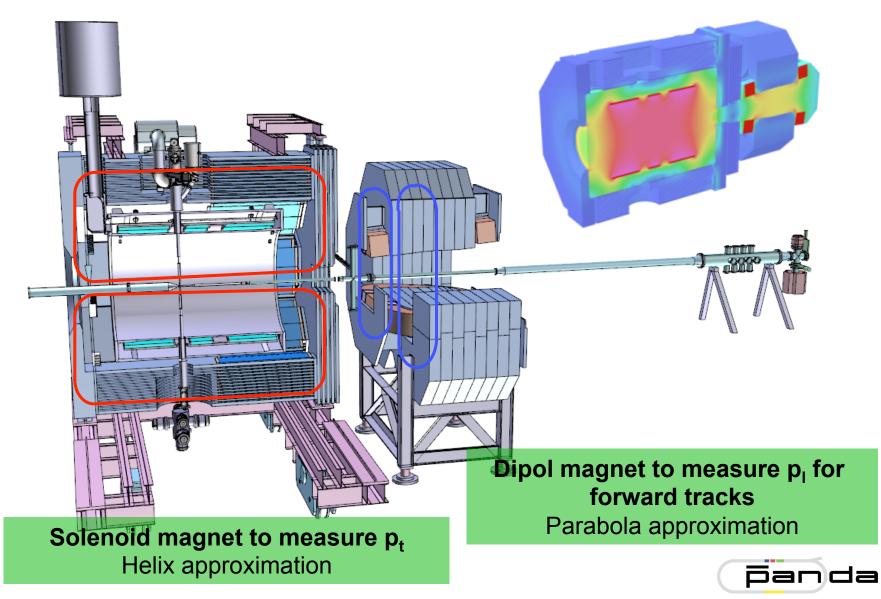
AntiProton Annihilation at Darmstadt





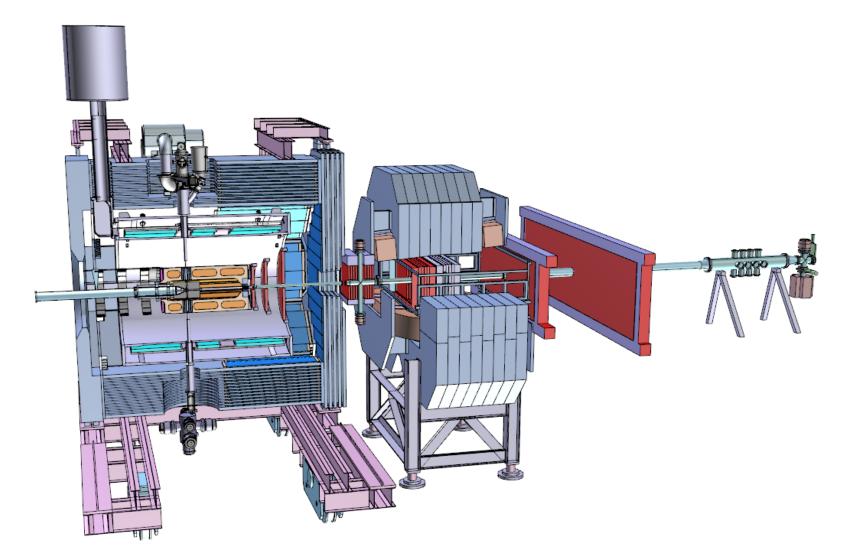
Magnet System





Spurdetektoren

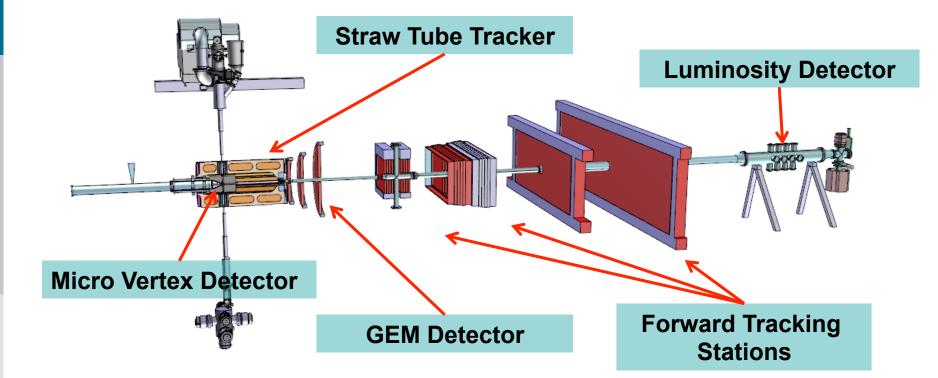






Tracking Detectors

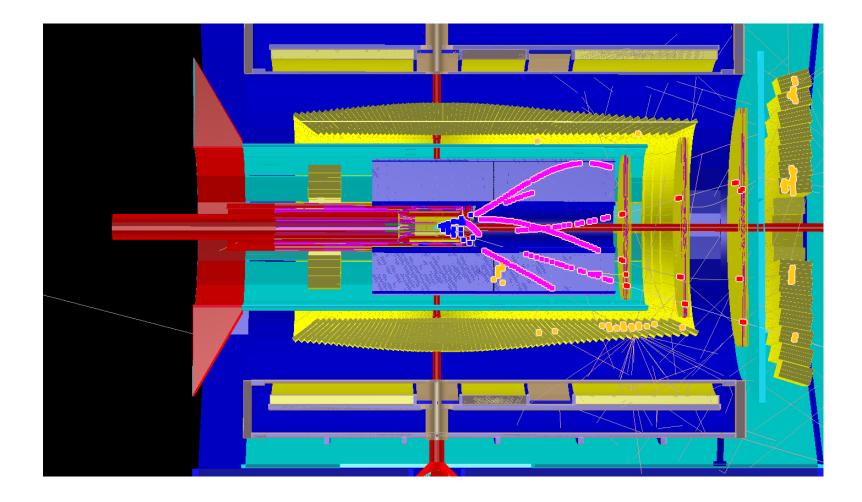






PANDA Event Simulation

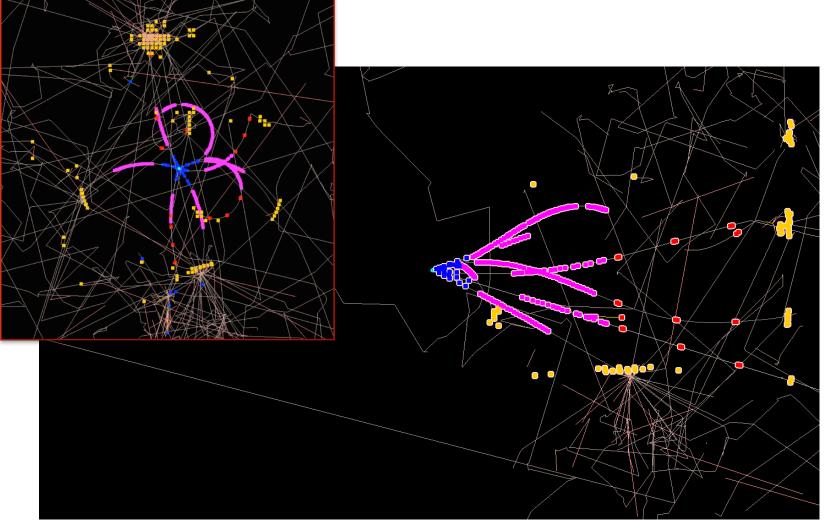






PANDA Event Simulation







Procedure

- Full track reconstruction happens in various steps:
 - Group the hits which belong to the same track
- pattern recognition / track finding

pre-fit

Kalman fit

- 2. Fast evaluation of the track parameters
- 3. Precise fitting of the track parameters
- 4. Propagate track parameters to the point propagation / where they are needed extrapolation



The Data



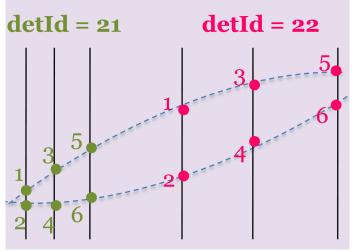
- The following objects contain the tracking information
- They "live" in pnddata/TrackData
 - PndTrackCand
 - Collection of hits inside a track
 - Output of track finder
 - PndTrack
 - Parameters of track
 - Output of prefit and Kalman fit



PndTrackCand



- Is a collection of hits
- Each hit is represented by a PndTrackCandHit which is a FairLink(detId, hitId) plus a sorting parameter rho.
- detId is the branch ID of the detector who generated the hits
- hitld is the position in the TCIonesArray

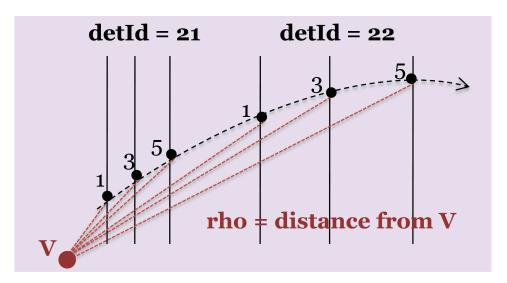


- Rho is an sorting parameter of a hit along the track
- No fixed rule how to calculate rho



PndTrackCand - Rho





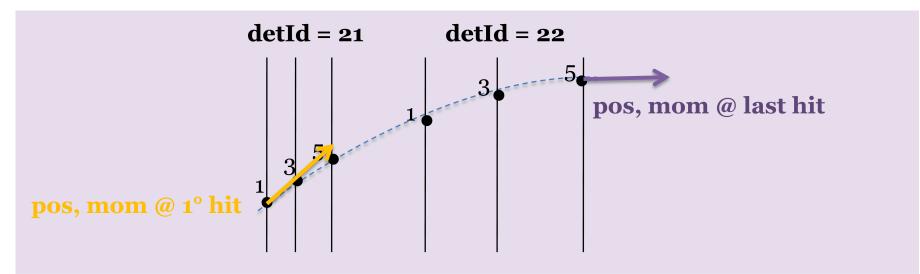
- Possible candidates for Rho
 - Distance from vertex (not a good one)
 - Time (but time resolution usually not sufficient)
 - Length along track (arc length for helix)
 - Secondaries: Where is the start of the track?



PndTrack



- This is the hypothesis of a track
 - Identified by the momentum, charge and position at the first and last hit
 - PndTrackCand accessible via PndTrack
 - Why two times the track information?





Data Summary



We have two objects to describe a track:

- PndTrackCand which contains the list of hits in the track
- PndTrack which contains the parameters of the track
- Why two objects instead of one?



Data Summary



We have two objects to describe a track:

- PndTrackCand which contains the list of hits in the track
- PndTrack which contains the parameters of the track
- Why two objects instead of one?
 - PndTrackCand can be used by different algorithms or different particle hypotheses





TRACK FINDING



Juli 4, 2017

Track Finding Strategies



- local
 - operates on the data of one sub-detector
 - finds all possible tracks in this sub-detector
 - tracks in different sub-detectors are combined via their track parameters
 - refit of complete track at the end
- global
 - operates on the data of more then one sub-detector at once
 - finds a complete track



Track Finding Strategies



- local vs. global
 - local
 - optimized algorithms for each sub-detector
 - no need to wait until data from all sub-detectors is available
 - several different algorithms needed (for each sub-detector and to combine the data)
 - how to handle tracks with insufficient hits in one subdetector?
 - global
 - all information at hand from the beginning
 - just one (but big) algorithm
 - treatment of different kind of data difficult (straws vs. pixel)

Track Finding Strategies



Additional considerations:

- All at once $\leftarrow \rightarrow$ Iterative
- Online $\leftarrow \rightarrow$ Offline
 - Performance vs. speed
- Primary $\leftarrow \rightarrow$ Secondary
 - Primary: coming from the interaction point
 - Secondary: all the rest
 - Primary tracks more easy to find
 - Secondaries important e.g. for hyperon physics



Track Finding



Considerations

Finite number of planes

A track goes through, leaving hits

All you really see are the hits, actually

- Often only one coordinate per plane
- Interactions with material (multiple scattering, energy loss, Bremsstrahlung for e-)
- Detector imperfections (inefficiency, limited spatial resolution, alignment)
- Extra hits from noise, pileup, low momentum particles...



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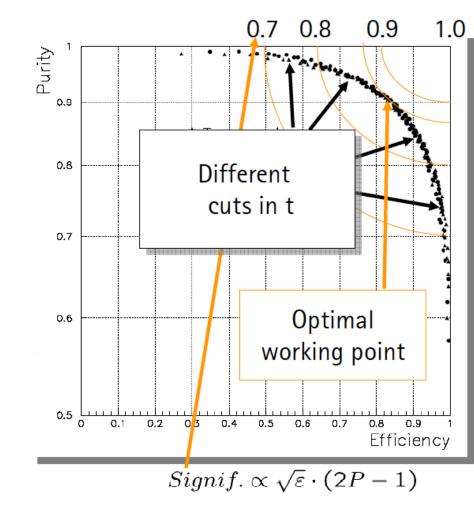
Track Finding



Conflicting Demands

- High efficiency find all true tracks relevant for the physics
- High purity

minimize incorrect assignment of hits to a track, that reduces the resolution



 Low ghost rate do not find fake tracks

Speed

often online tracking is needed as part of a trigger decision (limited time (latency) and resources).

Tobias Stockmanns

Track Finding with 1D Detectors



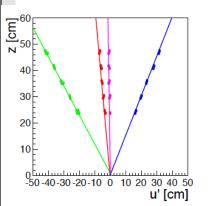
Tracking in space

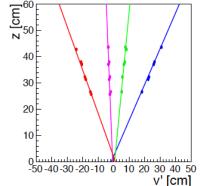
(generally needs many layers)

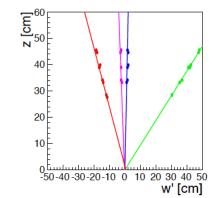
- Combine layers to get a 3D space point,
- do 3D tracking with these points

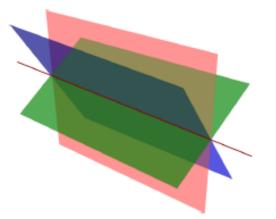
Tracking in projections (generally needs more CPU)

- find 2D track candidates, then
- combine projections (here each line in 2D is a plane in 3D)







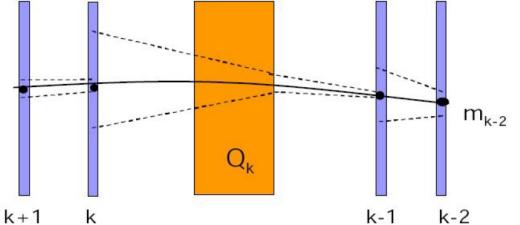


Local Method: Track Following



Follow track through layers

- Define initial track segment (track seed)
- Use track model to extrapolate to next detector layer



- Define search window around expected position, depends on resolution and amount of material
- If hit found, add it to the track candidate and iterate to next layer
 - Detector inefficiency: if no hit found go to next layer, allow several missing layers
 - Allow for combinations, if more than one hit in window follow all paths concurrently, decide later what is correct

Kalman-filter, will be discussed later



Global Method: Histogramming



For circular tracks (homogeneous B-field (usually solenoid)) Conformal mapping (transformation: circles to lines)

 $u = x/(x^2 + y^2), \quad v = -y/(x^2 + y^2)$

Compute angle Φ Make a histogram of Φ

$$\Phi = \arctan(v/u)$$

Find peaks in Φ histogram

Transforms a 2D problem to 1D

If tracks don't come from (x,y)=(0,0)

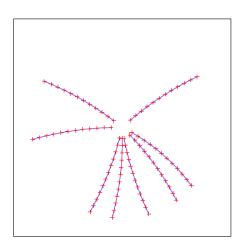
- Line is offset, and washed out peak in 1D histogram
- Solution: x'=x-x₀ and y'=y-y₀ where (x₀,y₀) is e.g. the innermost point on the track



Histogram Method



Coordinate space

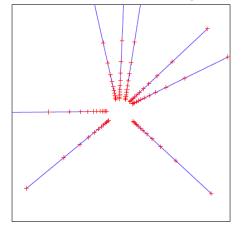


Original tracks and hits

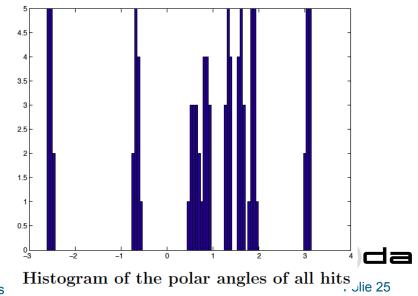
As you see, the histogram binning is not arbitrary, it is related to the resolution.

Too fine: then the hits don't make a peak Too coarse: then the peaks overlap, and the resolution gets worse.

Transformed space



Transformed tracks and hits



Hough Transformation



- Histogramming technique based on coordinate transformation
- Transform point (image space) to parameter space
- Hit in image space becomes a trajectory in parameter space
- Hits from the same track \rightarrow trajectories cross in param. space
- Binning of parameter space (histogram) (bin size: tradeoff between resolution, efficiency and speed)
- Find peaks in histogram \rightarrow track candidate
- Very fast for simple track models (straight line, circle)
- Well suited for parallel processing \rightarrow fast online trigger





OFFLINE PANDA EXAMPLES



Global pattern recognition



PndSttMvdTrackFinder / PndSttMvdGemTrackFinder

- default global PR
- Contains: MVD + STT + GEM
- Starts from MVD and STT stand alone track finders
- Extrapolates STT to MVD and vice versa
- New track candidate of MVD and STT is refitted
- Refitted track extrapolated to GEM stations
- Only primary tracks
- No refit with GEM stations because magnetic field in GEMs not homogeneous enough for helix assumption



Global pattern recognition 2



PndBarrelTrackFinder

- Alternative global PR
- Does not start at any specific detector
- Treats MVD, STT and GEM hits equal
- Looks for correlation in xy plane
- Tries to gather z information when possible
- Hit mixing to avoid unphysical correlations
- Only primary tracks





ONLINE PANDA EXAMPLES



Riemann Track Finder

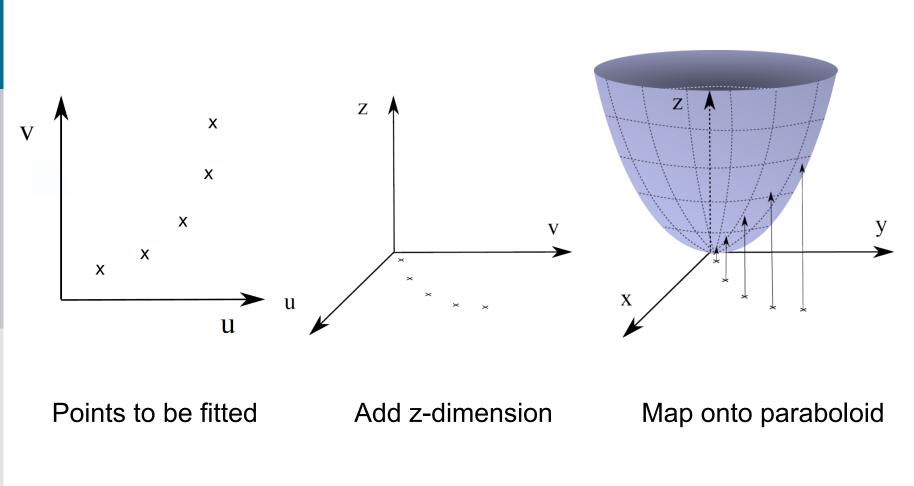


- The Riemann Track Finder is based on a fast circle fit using a Riemann surface:
 - The 2D points in xy-plane are projected on a paraboloid (w = x² + y²)
 - A fast fit of a plane through the new 3D points give you the plane parameters which can be bijectively mapped to the radius and the origin of the circle
 - In a second fit one plots the arc length of the hits on the circle versus their z-position which should be a straight line
- The method is very fast if you neglect energy loss and multiple scattering
- Both can be implemented which leads to very good accuracy but then it is slower than a standard Kalman fit
- Riemann fit was implemented by Sebastian in pandaRoot but without error treatment



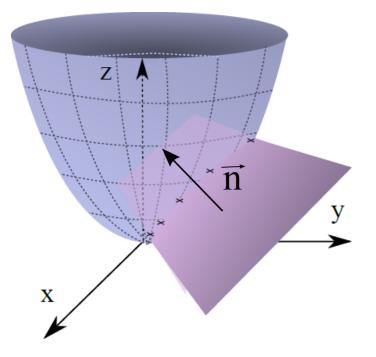
Riemann Track Finder











Calculation of plane through 3D points simple eigenvalue determination



Riemann Track Finder



- 1. Find all (reasonable) combinations of three points
- 2. Calculate Riemann plane
- 3. Calculate distance of all hits to plane
- 4. If below threshold add them to plane
- 5. Recalculate plane at the end (or in between?)
- 6. Take only those planes (circles) with more than 3 hits
- Linear fit or arc length vs. z-coordinates of hits for z-Dimension





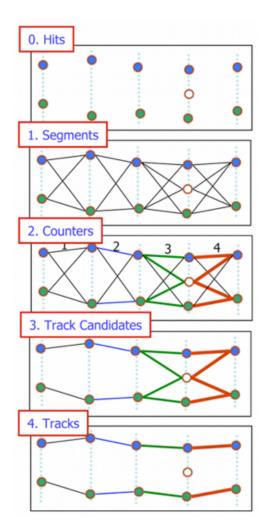
CA TRACK FINDER



Cellular Automaton as Track Finder



- 1. Build short track segments
- 2. Connect according to track model, estimate a possible position on a track
- 3. Tree structures appear, collect segments into track candidates
- 4. Select best track candidate







CELL TRACK FINDER



CellTrackFinder



1. Generation of tracklets in STT

- Primary tracklets: use of cellular automaton
- Combination of tracklets: use of Riemann Fit
- Faulty: Fit to center of the tubes
- Add remaining hits to best fitting Track

→ TrackletGenerator

2. Correction of STT-Hits based on event time

Correct points for Riemann Fit by calculating tangents to the isochrones





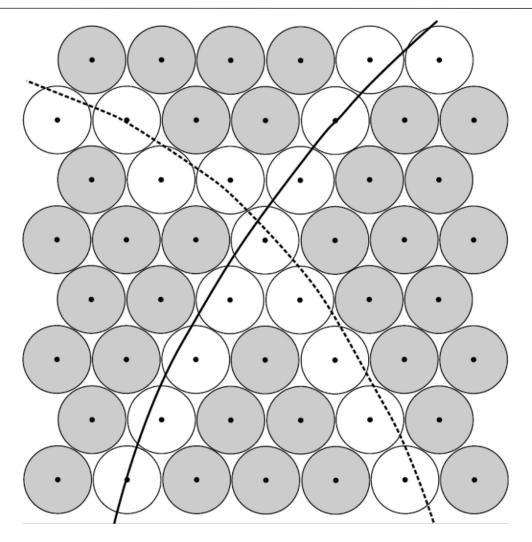


1. TrackletGenerator Cellular Automaton

- Abstract discrete model for dynamic systems
- Definition by:
 - Cell
 - Neighborhood relations
 - Discrete number of states
 - Transition rules for states
 - Simultaneous changes

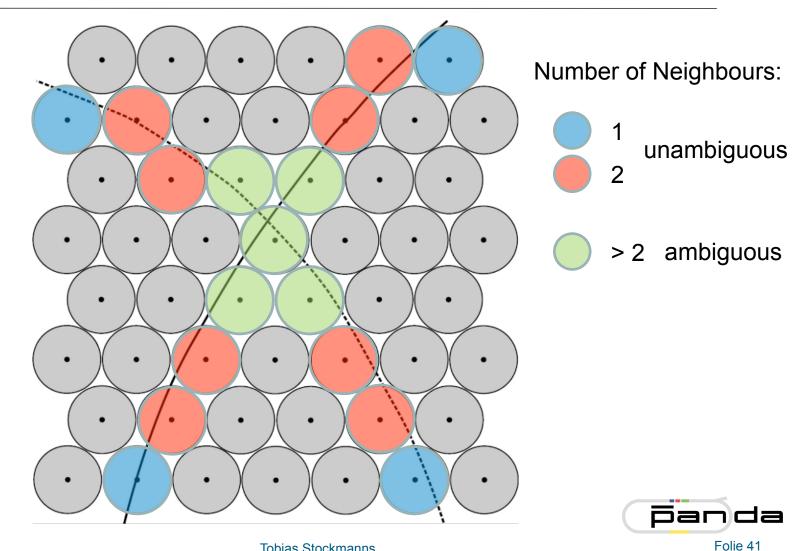




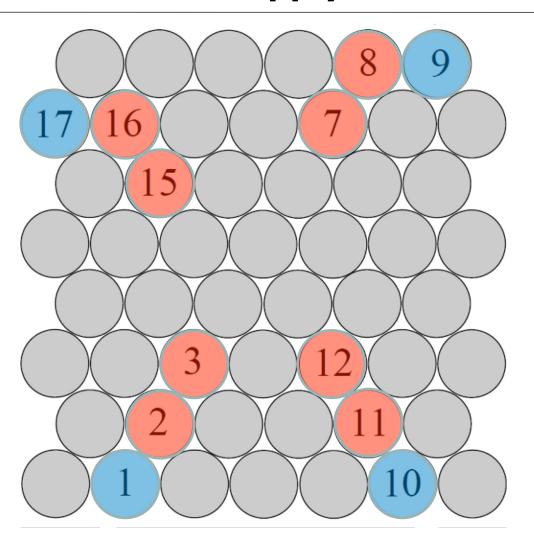








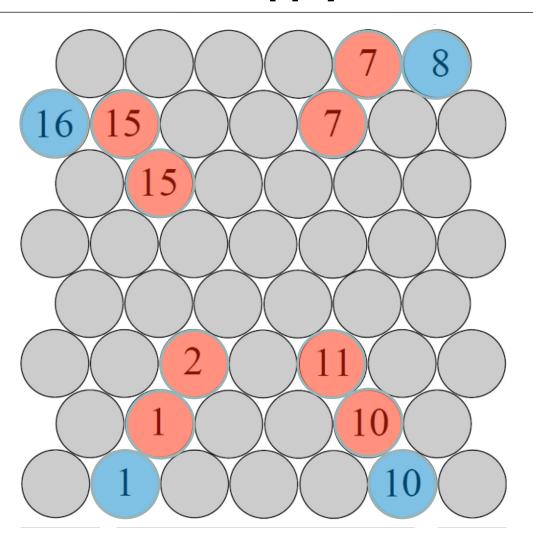




Cell: Straw with hit and one or two neighbours



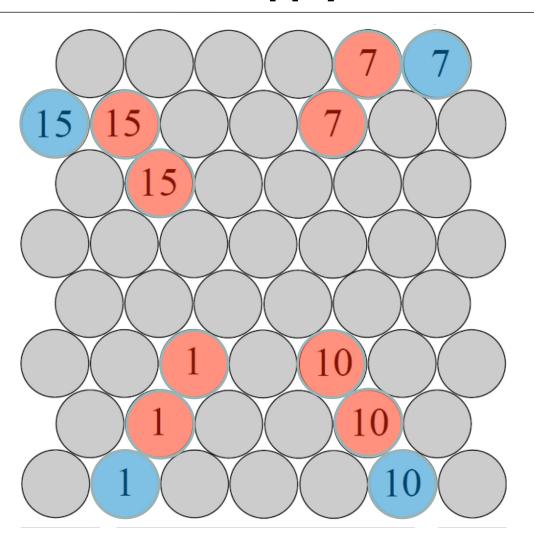




Cell: Straw with hit and one or two neighbours



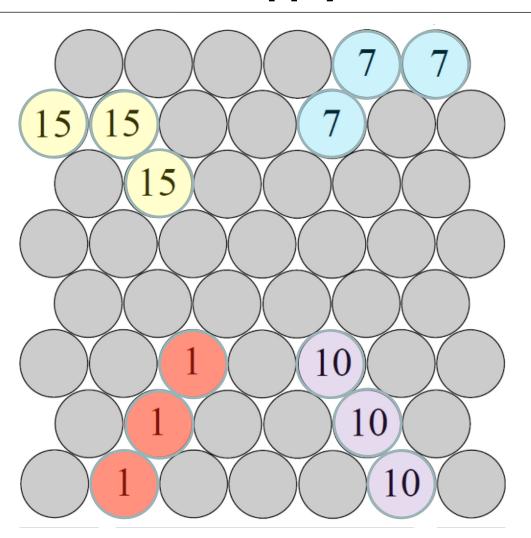




Cell: Straw with hit and one or two neighbours



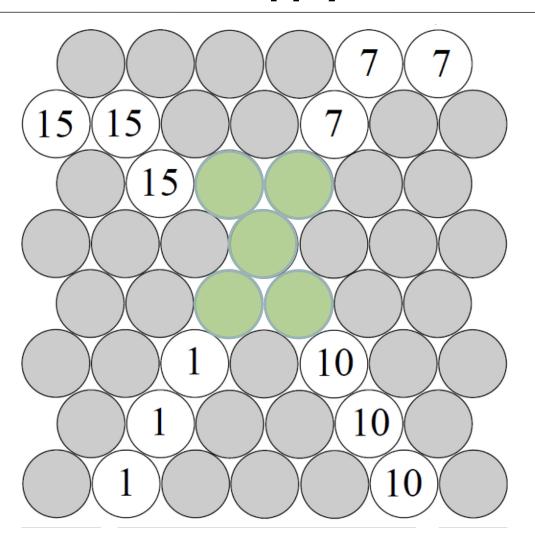




Cell: Straw with hit and one or two neighbours



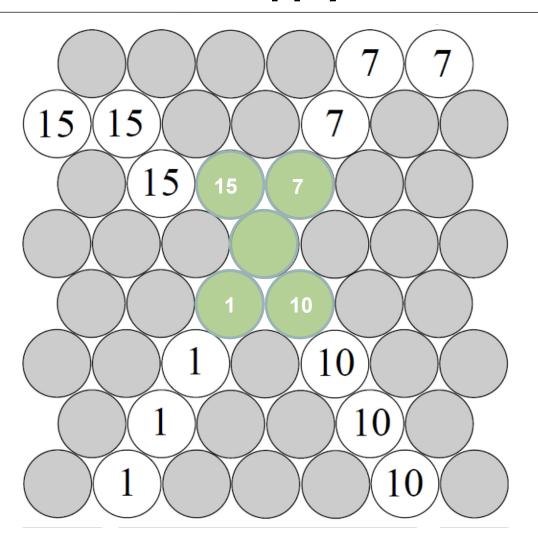




Cell: Straw with hit and more than two neighbours



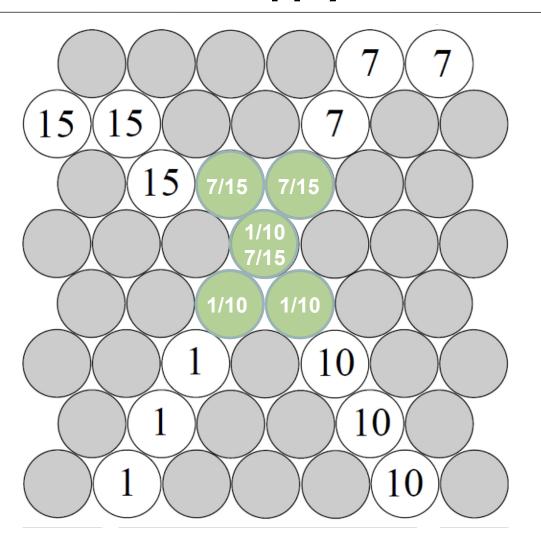




Cell: Straw with hit and more than two neighbours



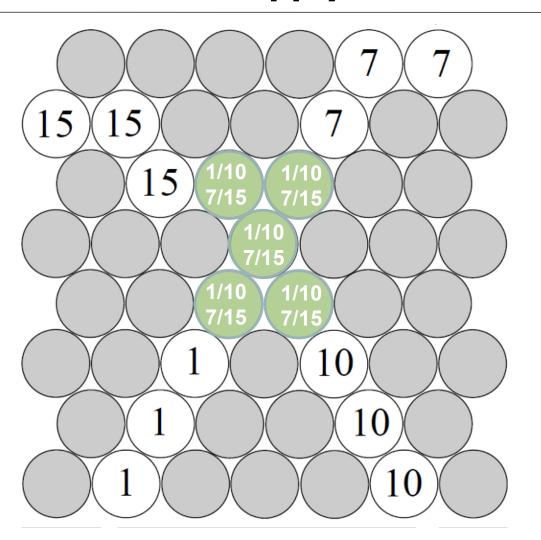




Cell: Straw with hit and more than two neighbours





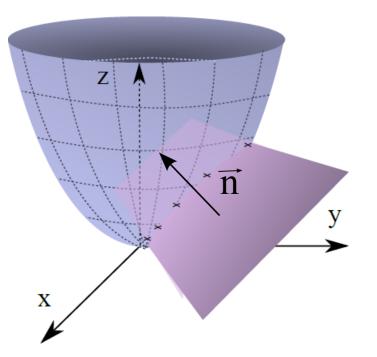


Cell: Straw with hit and more than two neighbours



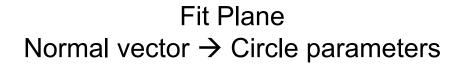


1. TrackletGenerator Riemann fit



Advantages

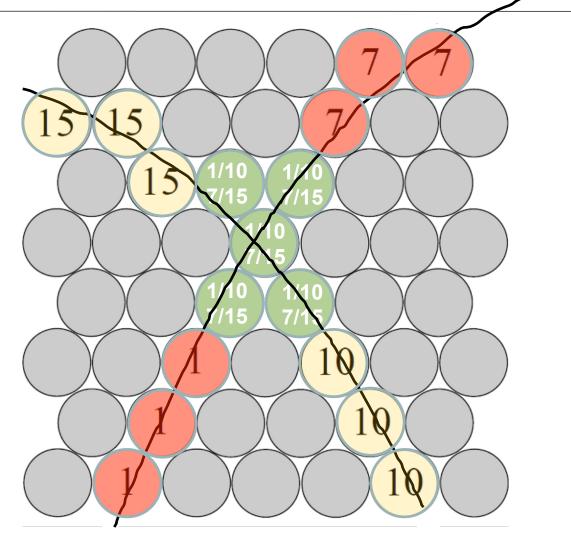
- quadratic \rightarrow linear
- explicit solution
- already implemented in PandaRoot







1. TrackletGenerator Result of the combination





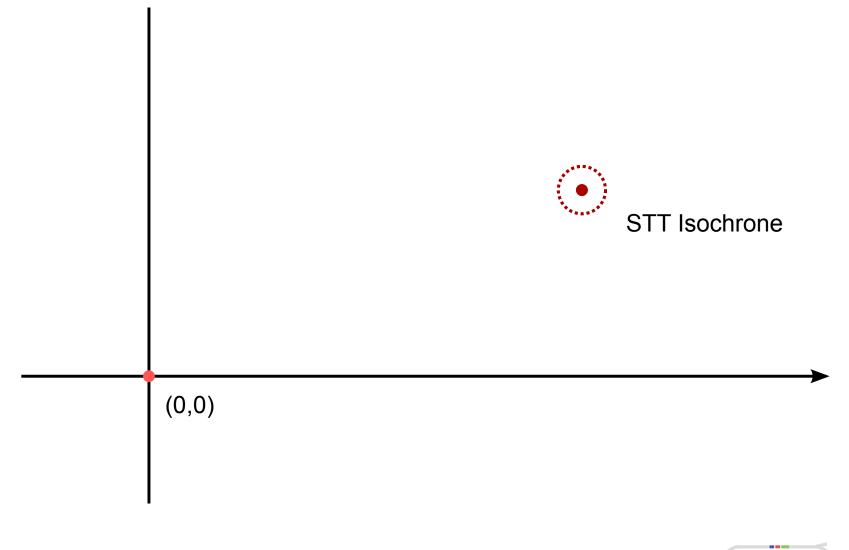


CIRCLE HOUGH



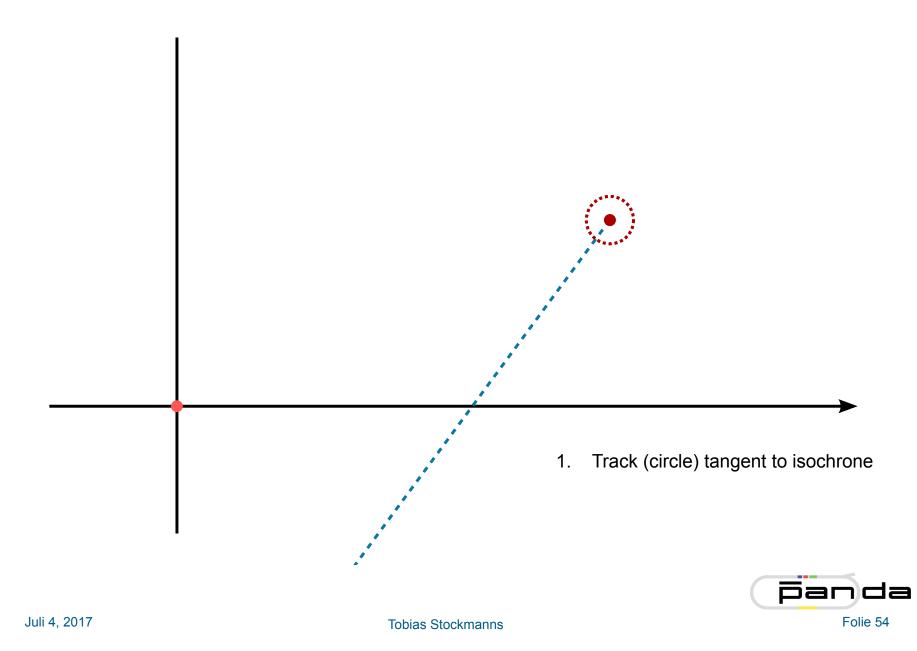




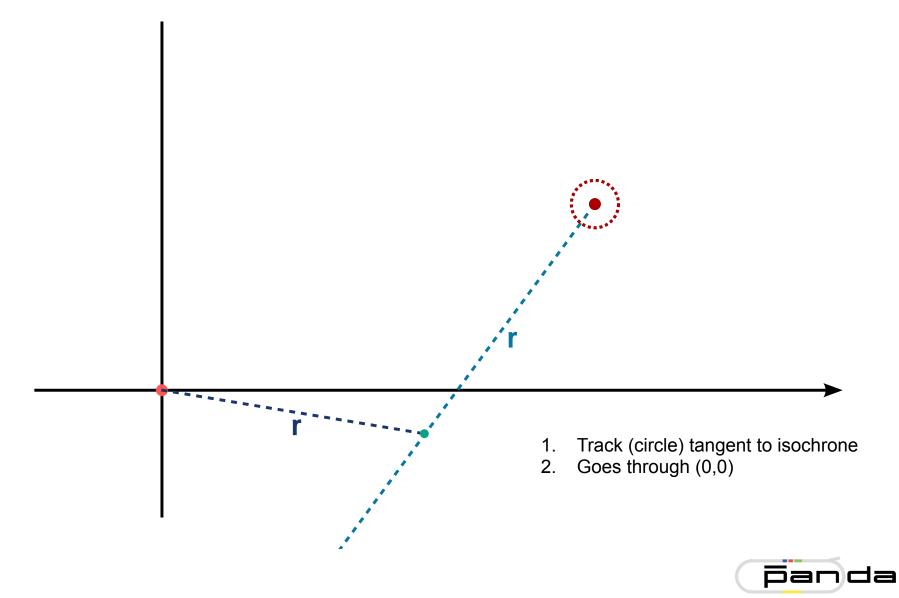






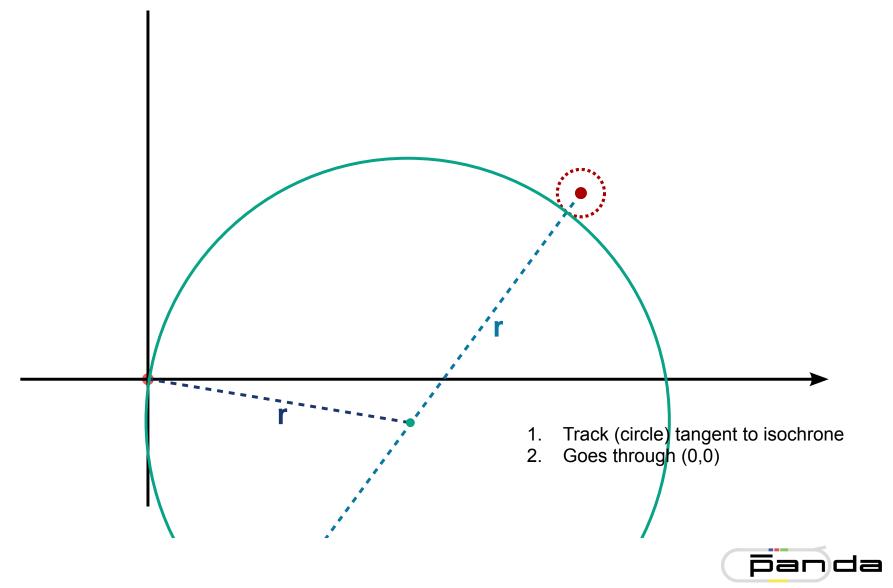






Folie 55

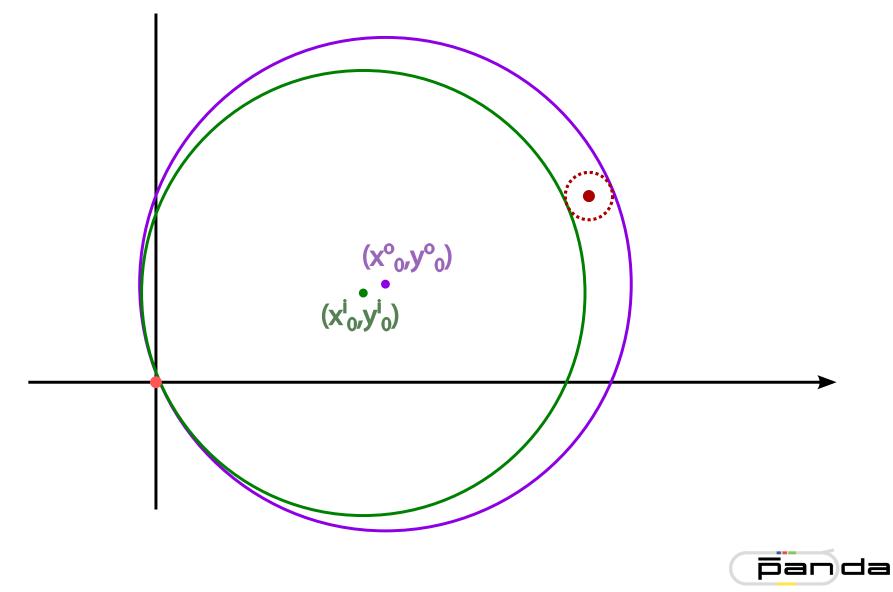




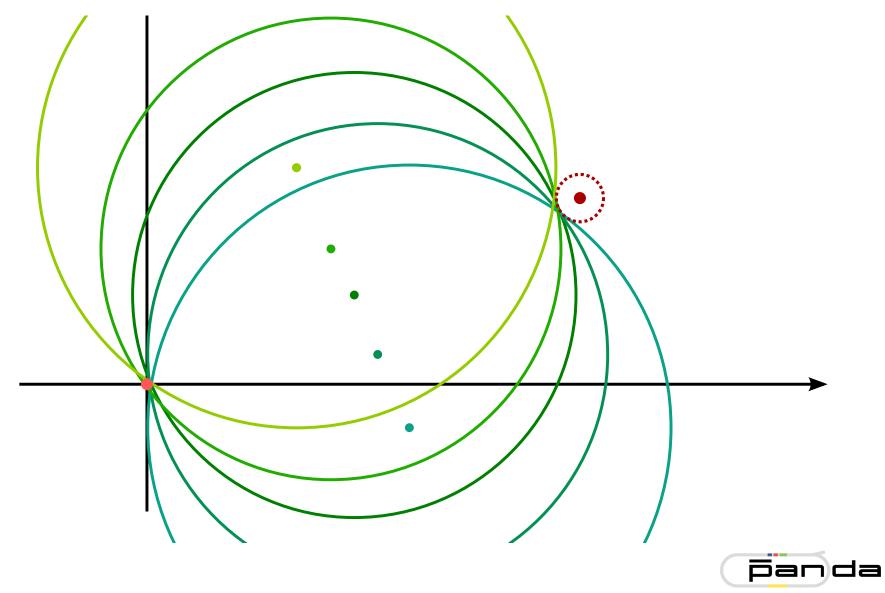
Folie 56



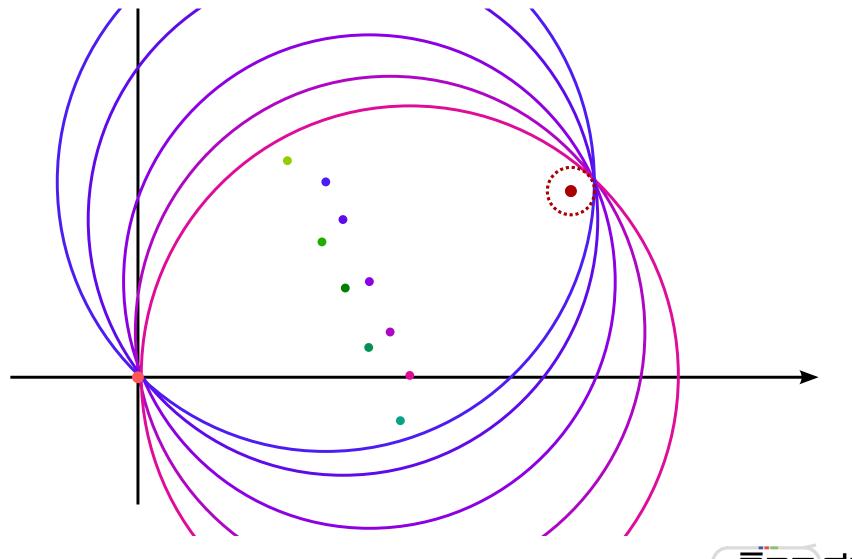






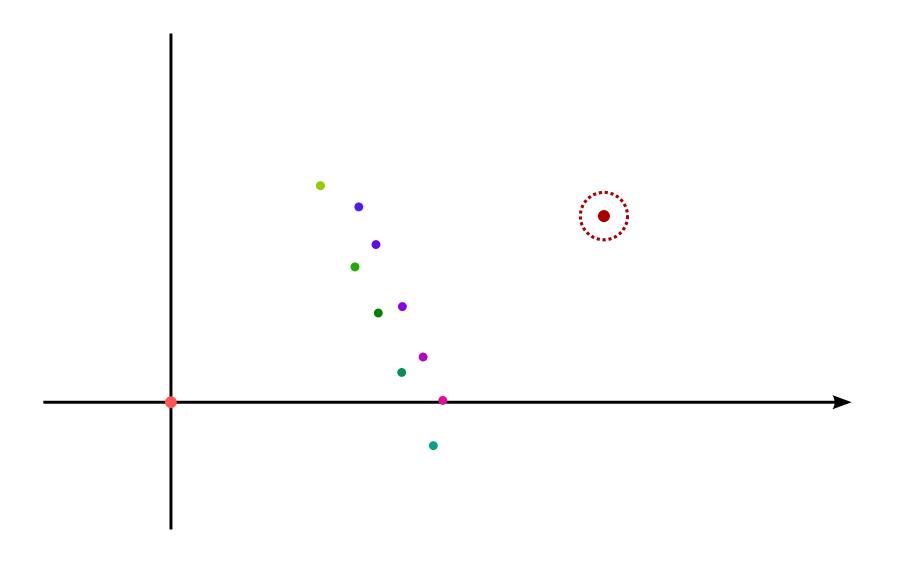






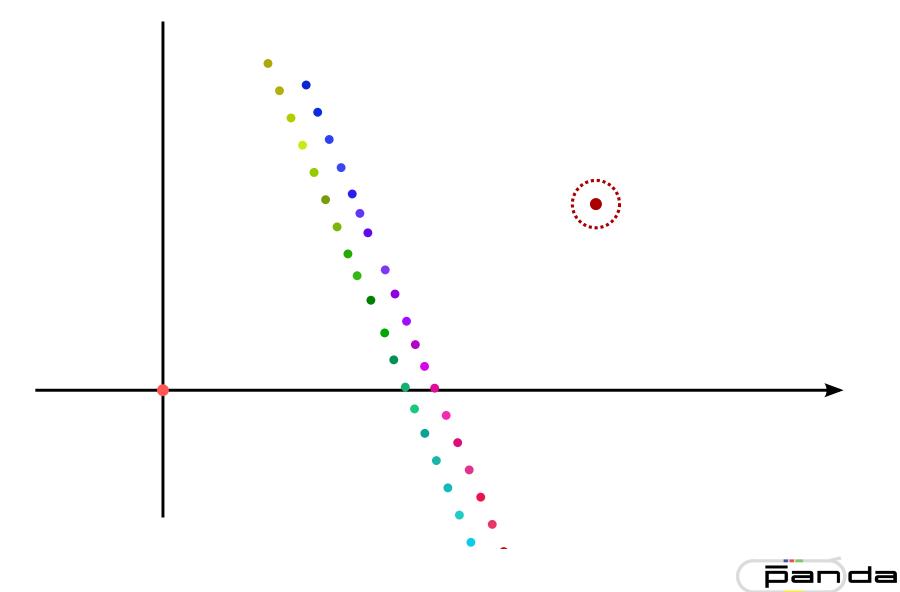






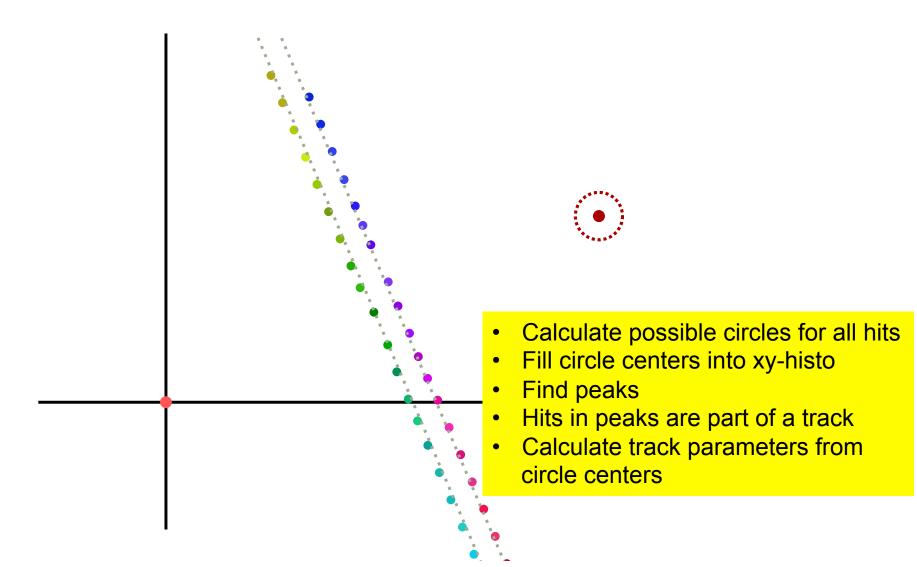






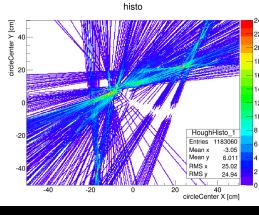


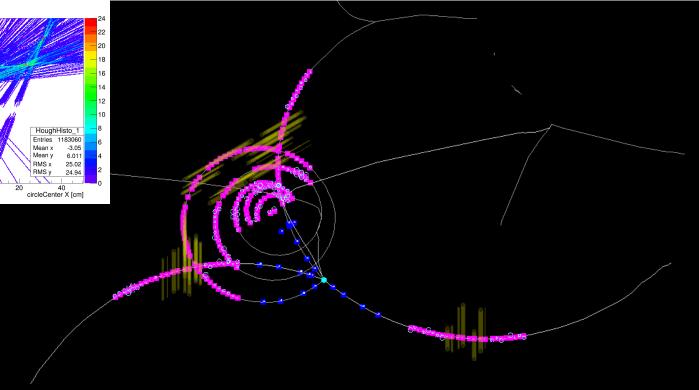






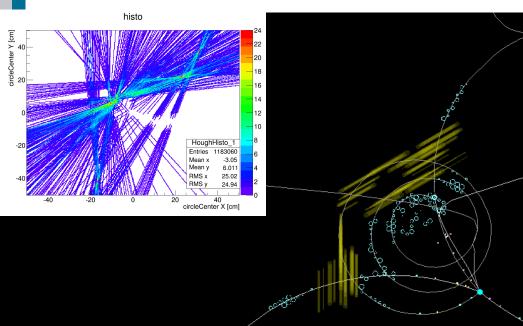






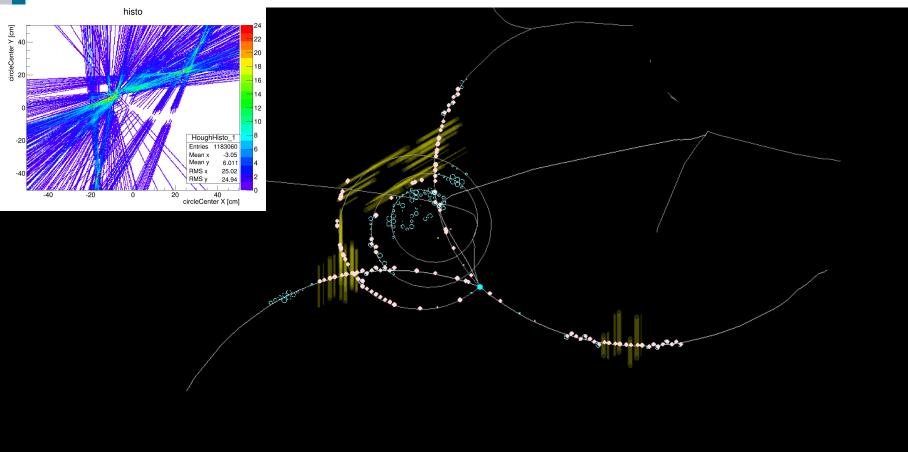






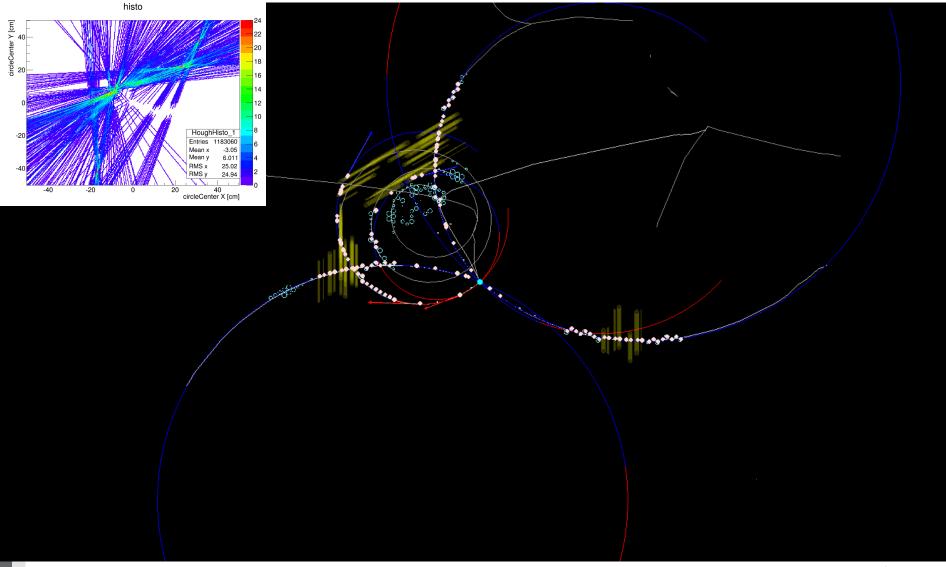
















KALMAN FILTER



Track Parametrization



- In vacuum the trajectory is defined by the initial parameters or state vector.
- 5 parameters are necessary and sufficient
- Each point along the trajectory, describe with a 5-component state-vector (and its 5x5 covariance vector)
- Should be continuous to small changes, approx. Gaussian errors, linear approximation to track propagation
- Best parameterization depends upon B-field and detector geometry: e.g.

detector surface normal to z-axis

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surface=beam pipe (collider)
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$$\left(\mathbf{r}, \mathbf{y}, \frac{d\mathbf{x}}{d\mathbf{z}}, \frac{d\mathbf{y}}{d\mathbf{z}}, \frac{\mathbf{q}}{\mathbf{p}}\right)$$
$$\left(\mathbf{r}, \mathbf{z}, \theta, \phi, \frac{\mathbf{q}}{\mathbf{p}}\right)$$

- \Rightarrow DELPHI barrel: x = (Φ, z, θ, β = φ Φ, 1/R)
- \Rightarrow DELPHI forward: x = (x, y, θ, φ, 1/R)
- ♦ CMS global: position, momentum, charge
- \Rightarrow CMS local: x = (q/p, dx/dz, dy/dz, x, y)

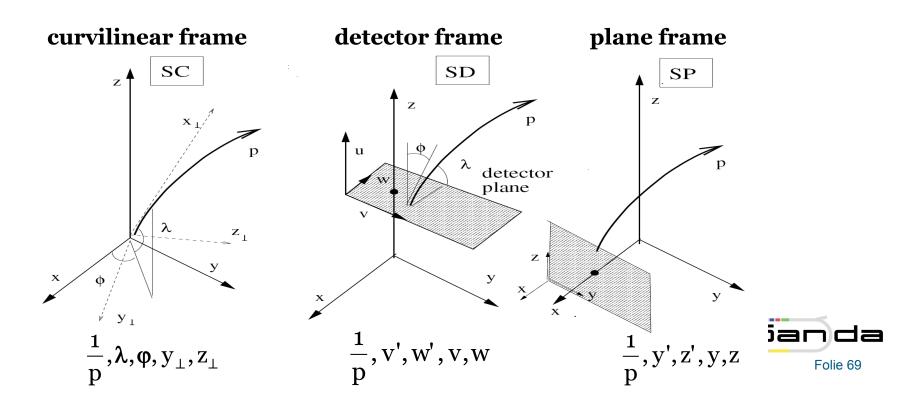


Panda Track Parametrization



FairTrackPar/FairTrackParP/FairTrackParH

- The physical path of a particle of assigned mass m and momentum p is a six-fold entity of parameters: x, y, z, p_x, p_y, p_z (+ q)
- Track is defined as set of points in detectors, corresponding to the intersection of the physical path of a particle with the detector planes
 → among six parameters one is fixed by the measurement plane



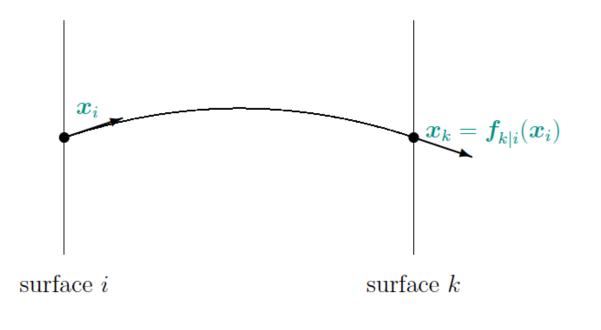
Track Model



 Track Model describes how the state vector at one surface depends on the state vector at a different surface. (describes particle trajectory)

$$\mathbf{x}_{k} = \mathbf{f}_{k|i}(\mathbf{x}_{i})$$

• f_{kli} is the track propagator from surface i to surface k.





Juli 4, 2017

Folie 71

(energy straggling, small angle scattering): iterative numerical extrapolation of track segments

Analytic calculation only for simple cases (like above)

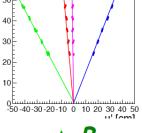
over short distances

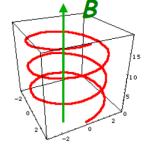
Inhomogeneous B-field, material

- Many tracks, many extrapolation steps, need high computing speed
- Simplest: Newton iteration, or describe each segment as a parabola
- Better: numerical integration like "Runge-Kutta"



- No magnetic field, no material: straight line
- Homogeneous magnetic field: helix (2D circle)







Measurement Model



 The measurement model describes the functional dependence of the measured quantities on the state vector at the detector surface:

$$oldsymbol{m}_k = oldsymbol{h}_k(oldsymbol{x}_k)$$

- The vector of measurements m_k usually collects the measured coordinates, but may contain also other quantities, e.g. measurements of direction or even momentum.
- Error on measurement assumed to be Gaussian which is not always true!



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Kalman Filter

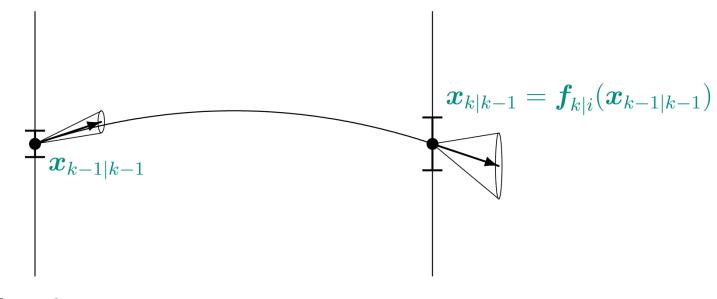


- Iterative LS estimation of the state vectors in all measurement layers (or even material layers).
- Two steps are repeated:
 - Prediction: extrapolate the state to the next layer, add up multiple scattering, subtract energy loss
 - Update: combine the predicted state with the current measurement
- A good initial state (seed) is important. Its weight should be small.



Prediction stage of Kalman Filter





surface k-1

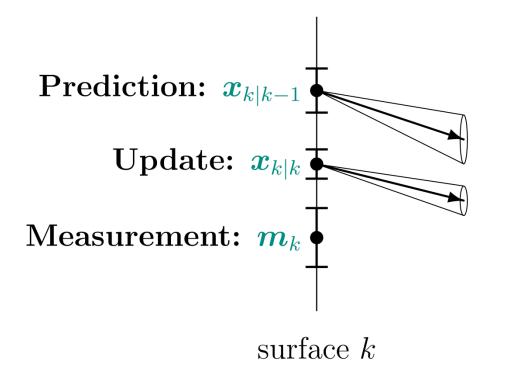
surface k

Prediction step of the Kalman filter



Update stage of Kalman Filter





Update step of the Kalman filter (weighted mean)



Smoother

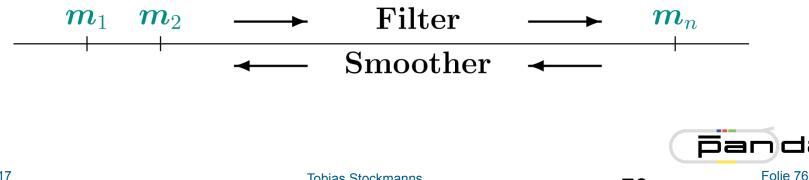


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The last estimate x_n of the filter contains the full information. The full information can be propagated back to all previous estimates.

This can be done by another iterative procedure, the smoother.

The smoother runs in the opposite direction to the filter.



Smoother



- The smoother can also be realized by combining two filters.
- One filter runs from m_1 to m_n : forward filter.
- One filter runs from m_n to m_1 : backward filter .
- The smoothed states are the weighted mean of the predicted states one filter and the updated states of the other filter.
- This is numerically more stable.
- The smoothed state x_{0|n} is the best linear estimate and therefore the same as the usual Least-Squares estimate x



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Kalman Filter



The Kalman filter can therefore be used for track finding. Generate a track seed.

Iterate the following sequence:

- Extrapolate and look for compatible measurements.
- If there is none, go on.
- If there is one, take the most compatible one and make an update.
- If no compatible measurements can be found in several layers, drop the track candidate.



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Kalman Filter in PandaRoot



Genfit

- Originally started as part of PandaRoot as a generic fitting package written by TU Munich
- Now independent external package
- Exists (at the moment) as two implementations: Genfit 1 and Genfit 2
- Genfit 1 is a very old version of Genfit using GEANE as track propagator
- Genfit 2 is a more up-to-date version using a Runge Kutta track propagator → change to recent Genfit 2 planned for next release
- Tests of performance are ongoing in PandaRoot



Genfit



Offers different track fitters:

Kalman Fitter

- standard track fitting algorithm
- sequential
- equivalent to least squares method

Deterministic Annealing Filter (DAF)

- sequence of Kalman filters
- annealing procedure for outlier rejection, ambiguity resolution

Generalized Broken Lines

- alternative to Kalman filter
- well-suited to Millipede II alignment
- treats track as a whole



Usage of Genfit in PandaRoot



PndRecoKalmanTask* recoKalman = new PndRecoKalmanTask(); recoKalman->SetTrackInBranchName("SttMvdGemTrack"); recoKalman->SetTrackOutBranchName("SttMvdGemGenTrack"); recoKalman->SetBusyCut(50); // CHECK to be tuned //recoKalman->SetIdealHyp(kTRUE); //recoKalman->SetIdealHyp(kTRUE); recoKalman->SetTrackRep(0); // 0 Geane (default), 1 RK //recoKalman->SetPropagateToIP(kFALSE); fRun->AddTask(recoKalman);



Usage of Genfit2 in PandaRoot



PndRecoKalmanTask2* recoKalman = new PndRecoKalmanTask2(); recoKalman->SetTrackInBranchName("SttMvdGemTrack"); recoKalman->SetTrackOutBranchName("SttMvdGemGenTrack"); recoKalman->SetBusyCut(50); // CHECK to be tuned //recoKalman->SetIdealHyp(kTRUE); //recoKalman->SetIdealHyp(kTRUE); //recoKalman->SetTrackRep(0); // 0 Geane (default), 1 RK //recoKalman->SetPropagateToIP(kFALSE); fRun->AddTask(recoKalman);





TRACK PROPAGATION -GEANE



GEANE



- Track follower / propagator
- Simplified geant3 tracking algorithm + error propagation
- Original Code is in Fortran
- Distributed with geant3 by CERN
- Part of FairRoot
- It extrapolates both the mean values of the parameters and their covariance matrices
- It uses the MC geometry
- It takes into account:
 - material effects
 - magnetic field
 - physical effects
- Different reference frames
- Different kinds of propagation



Geane Interface



In geane you will find:

- FairGeane: this is the task reading in the physics cuts and the physics effects to take into account
- This task has to be added to your macro otherwise GEANE will not work!
- FairGeanePro: contains the propagation stuff
- In trackbase you will find
- FairTrackPar/ParP/ParH: track representations of GEANE
- FairGeneUtil: frame transformations from to MARS, SC, SD, SP (C++ translation of FORTRAN methods)



How to use it



• First define the start plane:

Bool t PropagateFromPlane(TVector3& v1, TVector3& v2);

• Define the end position:

Bool_t PropagateToPlane(TVector3& v0, TVector3& v1, TVector3& v2); Bool_t PropagateToVolume(Tstring VolName, Int_t CopyNo,Int_t option); Bool_t PropagateToLength(Float_t length); Bool t PropagateToPCA(Int t pca, Int t dir);

• Do the propagation:

Bool_t Propagate(FairTrackParH* TStart, FairTrackParH* Tend, Int_t PDG) Bool_t Propagate(FairTrackParP* TStart, FairTrackParP* TEnd, Int_t PDG)

Back propagation:

Bool_t setBackProp()

How to use it



• First define the start plane:

Bool t PropagateFromPlane(TVector3& v1, TVector3& v2);

• Define the end position:

Bool_t PropagateToPlane(TVector3& v0, TVector3& v1, TVector3& v2); Bool_t PropagateToVolume(Tstring VolName, Int_t CopyNo,Int_t option);

Bool_t PropagateToLength(Float_t length);

Bool_t PropagateToPCA(Int_t pca, Int_t dir);

• Do the propagation:

Bool_t Propagate(FairTrackParH* TStart, FairTrackParH* Tend, Int_t PDG) Bool_t Propagate(FairTrackParP* TStart, FairTrackParP* TEnd, Int_t PDG)

Back propagation:

Bool_t setBackProp()

Track Propagator



- Additional track propagators:
 - FairRKPropagator
 - 4th order Runge-Kutta propagator
 - not used
 - PndHelixPropagator
 - much faster than GEANE
 - but no energy loss
 - no varying magnetic field





TRACKING QA



Juli 4, 2017

Introduction



- Various different tracking algorithms
- Common basis needed to compare and improve tracking algorithms
- Common development of Lia Lavezzi and me
- Idea:
 - Have a set of macros which work on any tracking algorithms which produces PndTrack and PndTrackCand
 - Set of identical simulation and digitization files for all tracking algorithms



Criteria



- Track efficiency
 - How many MC tracks have been found by track finder
- Hit efficiency
 - How many hits of a MC track have been found by the track finder
- Purity
 - Belong all hits of one found track belong to one MC track
- Clones
 - How often was a track found by the track finder
- Ghosts
 - How many hits not belonging to an MC track have been found



Criteria



- Partially found
 - Not all hits belonging to one track have been found but all hits belong to one MC track
- Spurious found
 - > 70% found hits belong to one MC track
- Fully found
 - 100 % of MC hits have been found and no other hits are part of the track
- Clone
 - A MC track was found more than once
- Ghost
 - A reconstructed track not matching to an MC track



Efficiency



- To determine the efficiency of a track finder a basis is needed:
 - All tracks? What about neutral particles or tracks without hits?
 - Only tracks with hits? How many hits?
 - A barrel track finder cannot find tracks in the forward region
- Different criteria defined:
 - At least three hits (minimum for circle determination)
 - Possible Track:
 - Definable by user via functor (who knows what a functor is?)
 - Some predefined in PndTrackers/PndIdealTrackFinder/ PndTrackFunctor.h



Efficiency



- Predefined functors:
 - StandardTrackFunctor:
 - *MVD* > 3 or *MVD*+Stt+GEM > 5
 - FtsTrackFunctor
 - *FTS* > 5
 - NoFtsTrackFunctor
 - FTS == 0 and StandardTrackFunctor
 - Some more specific for certain track finders
 - OnlySTTFunctor, RiemannMvdSttGemFunctor, ...



Implementation



- Macros in /macro/trackingQA
- sim, digi and par files provided in folder
- **reco_complete.C**(TString prefix)
 - Does the tracking. Your tracking code has to go here!
 - In addition runs an ideal track finder to compare with
 - Usage:
 - Add prefix to identify which data you want to run on
 - root reco_complete.C"(\"dpm_G4_7G0_1000\")"



Implementation



- trackingQA_complete.C(TString prefix, TString branch, Int_t nEvents=0):
 - Compares tracking algorithms with ideal tracking
 - Usage
 - Add the same prefix as in reco_complete.C
 - Add the branch name with the final results of your tacking code (has to be of type PndTrack)
 - Optional add the number of events you want to run on
 - root trackingQA_complete.C"(\"dpm_G4_7G0_1000\", \"SttMvdGemTrack\")"



Implementation

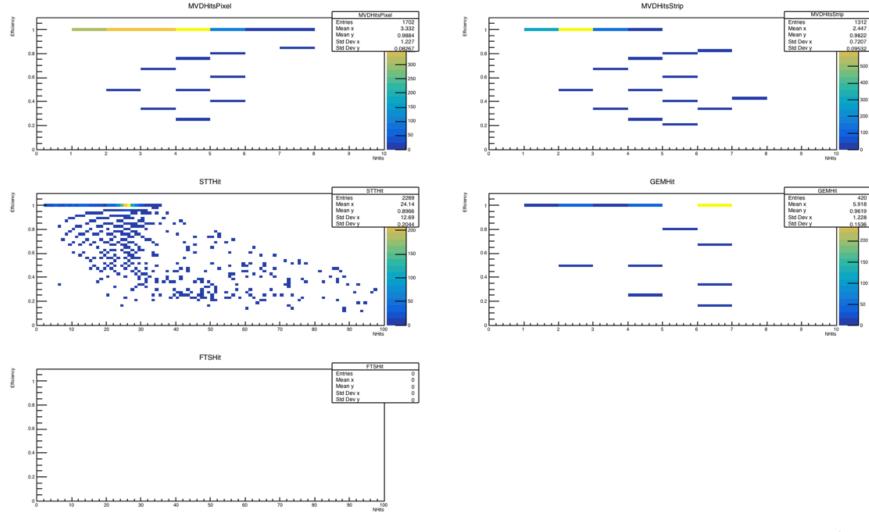


- plot_trackingQA(TString fileName)
 - Plots the generated histograms of trackingQA in a nice way
 - Usage:
 - Give the complete file name of the trackingQA.root file
- **QA_histos**(TString prefix, TString trackBranch)
 - Generates a large set of extracted histograms
 - Usage:
 - Give prefix and branchName
- **comp_recoqa**(TString , fn TString fn2, int picpercan, ...)
 - Combines the histograms of two different tracking algorithms
 - New feature pictures per canvas



Hit Efficiency

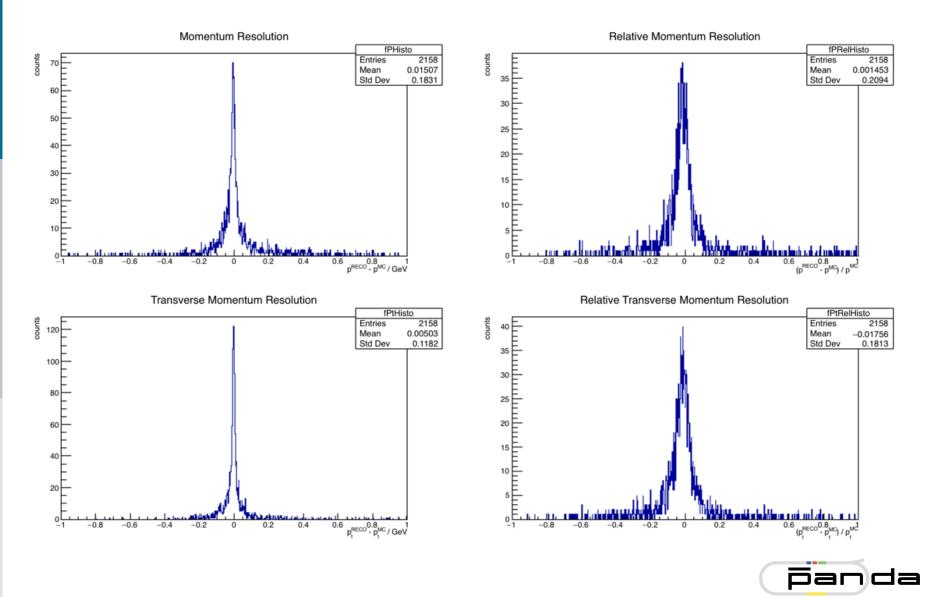






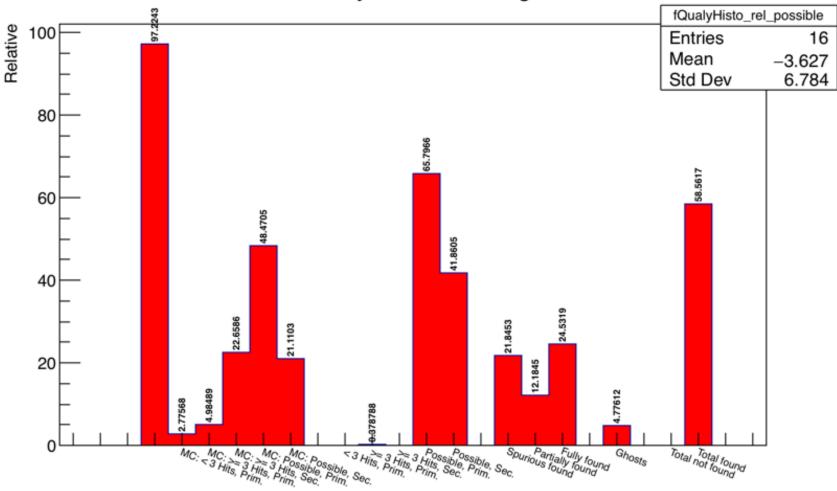
Momentum Resolution





Performance



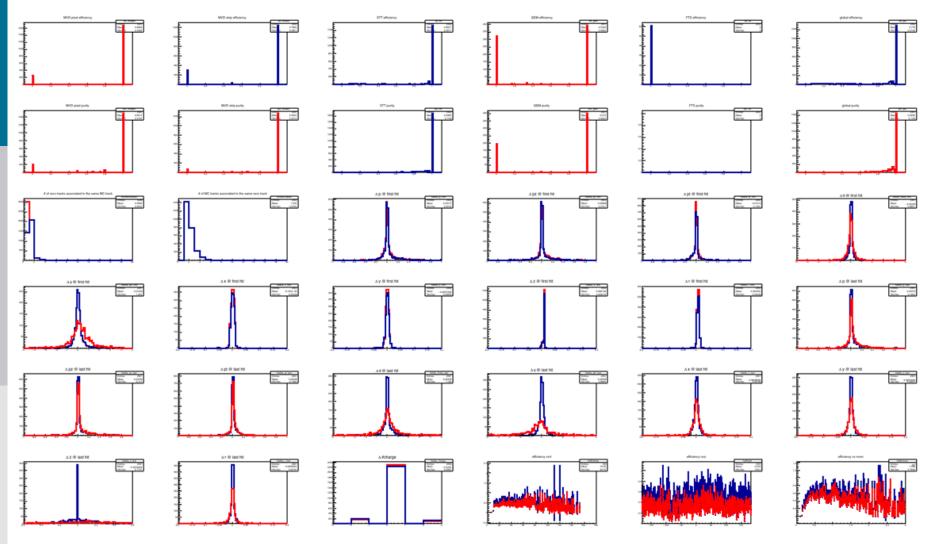


Quality of Trackfinding



Overview Performance







Overview of Track Finder



TRACKING

Algorithm name	Attached Person	Platform	In PandaRoot?	Output PndObjects?	SVN?	Online?	Secondaries?	Barrel/Fwd	Used Detectors	Notes	Links
PndTrkTracking2	Gianluigi	CPU	yes	PndTrack	yes	no	no	Barrel	MVD STT GEM	Main offline track finder	Gianluigimeet8sep15.pdf
BarrelTracker	Radoslaw Karabowicz	CPU	yes	PndTrack	yes	no	no	Barrel	MVD/STT/GEM		
Barrel Cellular Automaton	Ivan Kiesel	CPU	yes	PndTrack	yes			Barrel	MVD(Barrel) STT	Does not use the MVD disks	
Genfit1		CPU	yes	PndTrack	yes	no	yes	Barrel/Forward	all	old version of generic kalman track fitter	
Genfit2		CPU	yes	PndTrack	yes	no	yes	Barrel/Forward	all	current version of generic kalman	

