

Low Mass Dileptons and Chiral Symmetry Restoration

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- ▶ Chiral symmetry of QCD; dynamical breaking
- ▶ restoration in the medium
- ▶ Dileptons and vector correlator
- ▶ in-medium spectral function of vector mesons
- ▶ theoretically convincing signatures of chiral symmetry restoration
- ▶ summary and outlook



Chiral symmetry of QCD

- ▶ In terms of chiral quark fields $(\gamma^5 q_{R,L} = \pm q_{R,L})$

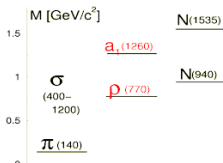
$$\mathcal{L}_{QCD} = i\bar{q}_R \not{D} q_R + i\bar{q}_L \not{D} q_L - \frac{1}{4} G_{\mu\nu} G^{\mu\nu} - m_q (\bar{q}_R q_L + \bar{q}_L q_R) \quad q_{L,R} = \begin{pmatrix} u_{L,R} \\ d_{L,R} \end{pmatrix}$$

- ▶ for **massless** quarks no mixing of L and R (chiralities)
 $m_q \ll 1$ GeV fairly good approximation
- ▶ invariant under **separate** isospin rotations of **left** and **right**
handed components $q_L \rightarrow U_L q_L$, $q_R \rightarrow U_R q_R$
- ▶ $\implies \mathcal{L}_{QCD}$ is $SU(2)_L \times SU(2)_R$ symmetric
- ▶ If the ground state of QCD is also chiral symmetric
so that $Q_V|0\rangle = 0$ and $Q_A|0\rangle = 0$
 \rightarrow we should expect **degenerate isospin multiplets of opposite parity** in hadron spectrum



What we actually observe

- ▶ we do see **isospin** multiplets (ρ^+ , ρ^0 , ρ^-), (p , n)
- ▶ but multiplets of **opposite parity** e.g (ρ , a_1) largely separated in mass ~ 500 MeV
 $m_q \neq 0$ unlikely reason
- ▶ QCD vacuum symmetric only under $SU(2)_V$
 $Q_V|0\rangle = 0$ but $Q_A|0\rangle \neq 0$
- ▶ \implies hypothesis: $SU(2)_L \times SU(2)_R$ dynamically broken to $SU(2)_V$
- ▶ with the pion multiplet (π^+ , π^0 , π^-) as the (approximately) massless **Goldstone bosons**
- ▶ existence of the **chiral condensate**: $\langle 0|\bar{q}q|0\rangle \sim -(250 \text{ MeV})^3$
 - ▶ QCD vacuum is a BE condensate of quark anti-quark pairs
 - ▶ induces $L \leftrightarrow R$ transitions
 - ▶ imparts dynamical (constituent) quark mass



Restoration of chiral symmetry

- ▶ heating/compression of hadronic matter leads to a non-trivial modification of the QCD vacuum leading to possible **restoration of chiral symmetry**

- ▶ ChPT calculations show a **decrease** of the chiral condensate with T

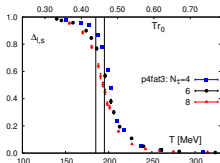
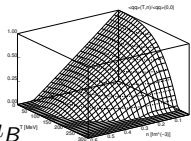
- ▶ linear density expansions show **decrease** with μ_B

$$\implies \text{to lowest order } \langle \bar{q}q \rangle \simeq \langle 0 | \bar{q}q | 0 \rangle \left(1 - \frac{T^2}{8F_\pi^2} - \frac{\rho N}{3\rho_0} \right)$$

- ▶ lattice show $\langle \bar{q}q \rangle \rightarrow 0$ around $T \sim 170$ MeV

- ▶ **an order parameter of χ SR**
(not measurable experimentally)

conjectured: $\frac{m_V^*}{m_V} \simeq \frac{\langle \bar{q}q \rangle}{\langle \bar{q}q \rangle_0}$ *Brown-Rho, Harada*



Bazavov (2009)



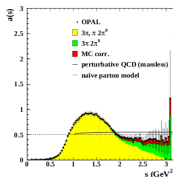
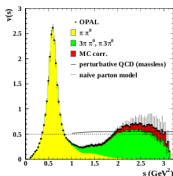
Current Correlators (in vacuum)

- modification of the vacuum is conveniently studied using **current correlators**

$$\Pi_V^{\mu\nu}(q) = i \int d^4x e^{iq \cdot x} \langle T V^\mu(x) V^\nu(0) \rangle$$

$$\Pi_A^{\mu\nu}(q) = i \int d^4x e^{iq \cdot x} \langle T A^\mu(x) A^\nu(0) \rangle$$

- $V^\mu = \bar{q} \gamma^\mu \tau_i q / 2$ and $A^\mu = \bar{q} \gamma^\mu \gamma^5 \tau_i q / 2$ are chiral currents of QCD
- at low energies, these are dominated by ρ and a_1 resonances: **very different spectral shapes** \rightarrow broken chiral symmetry
- $\Pi^{V,A}$ expanded in terms of quark and gluon condensates (QSR)
 \implies **behaviour of resonances reflects the vacuum structure of QCD**



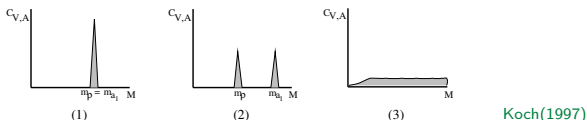
ALEPH and OPAL
 τ decays \rightarrow
 even(odd) no. of π 's
 $V (A)$

observing χSR through in-medium correlators

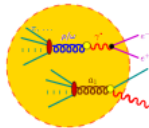
- ▶ at $T \geq T_\chi$ chiral symmetry demands that Π^V and Π^A are identical (not only mass and width but entire spectral shape)
- ▶ guidelines from Weinberg Sum Rules : relates difference of V and A correlators to vacuum parameters e.g.

$$\int \frac{ds}{s} \left[\text{Im}\Pi^V(s) - \text{Im}\Pi^A(s) \right] = F_\pi^2$$

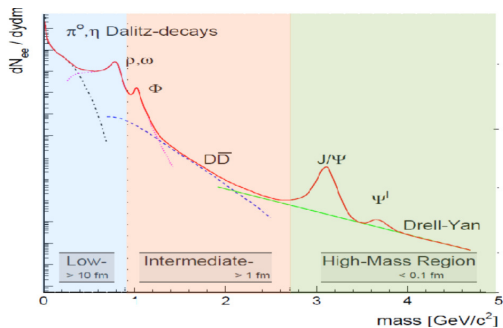
- ▶ three possibilities of observing χSR : Kapusta and Shuryak (1994)



- ▶ $\text{Im}\Pi^V$ is accessible from dilepton spectra
 $\text{Im}\Pi^A$ not so because of final state interactions
in $\pi\gamma$ invariant mass



$\text{Im}\Pi^V$ from Dileptons: HICs



We will look at thermal dilepton production in the **low mass** region

- ▶ **Low Mass Region:** Dalitz decays and thermal radiation from low mass hadrons
- ▶ **Intermediate Mass Region:** thermal radiation from QGP and hadronic matter, semi-leptonic decays of heavy quarks
- ▶ **High Mass Region:** Drell-Yan, decays of heavy quarkonia



Dilepton Emission Rate

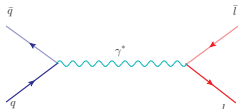
- ▶ Dilepton emission rate is given by the thermal expectation value of the **correlator of EM currents**

McLerran & Toimela

$$\frac{dN_{l+l-}}{d^4x d^4q} = -\frac{\alpha^2}{3\pi^3 q^2} \frac{L(m_l)}{e^{\beta q_0} + 1} g^{\mu\nu} W_{\mu\nu}(q_0, \vec{q})$$
$$W_{\mu\nu}(q_0, \vec{q}) = \text{Im} \int d^4x e^{iq \cdot x} \langle T J_\mu^{em}(x) J_\nu^{em}(0) \rangle$$

- ▶ EM current of quarks

$$J_\mu^{em} = \sum_f e_f \bar{q}_f \gamma_\mu q_f$$



- ▶ gives the Born rate for emission from QGP

$$g^{\mu\nu} W_{\mu\nu}(q_0, \vec{q}) \simeq \sum_f e_f^2 \frac{3q^2 L(m_f)}{4\pi} \coth(\beta q_0/2)$$



- ▶ Consider e.g. **iso-vector** projection of the EM current J_μ^{em}

$$\begin{aligned} J_\mu^{em} &\rightarrow \frac{1}{2}(\bar{u}\gamma_\mu u - \bar{d}\gamma_\mu d) \\ &= V_\mu \end{aligned}$$

\implies coincides with the vector current of chiral symmetry

- ▶ use field-current identity (Sakurai); replace currents by fields
- in this case the vector-**isovector** ρ meson

$$j_\mu^{em} \rightarrow F_\rho m_\rho \rho_\mu$$

- ▶ so that, EM correlator $\langle T j^{em}(x) j^{em}(0) \rangle \propto \langle T \rho(x) \rho(0) \rangle$
 ρ -propagator
- ▶ imaginary part $\rightarrow W_{\mu\nu} = F_\rho^2 m_\rho^2 \text{Im} G_{\mu\nu}^\rho \propto \rho$ sp. fn.



- ▶ Adding the iso-scalar contribution and other flavours,

$$W_{\mu\nu} = F_\rho^2 m_\rho^2 \text{Im} G_{\mu\nu}^\rho + F_\omega^2 m_\omega^2 \text{Im} G_{\mu\nu}^\omega + \dots$$

$$\frac{dN_{l+l-}}{d^4x d^4q} = -\frac{\alpha^2}{3\pi^3} \frac{1}{q^2} \frac{1}{e^{\beta q_0} + 1} \sum_V F_V^2 m_V^2 A_V(q_0, \vec{q}, T, \mu_B)$$

⇒ dilepton production is given by the imaginary part of **in-medium** propagators (**spectral functions**) of vector mesons

- ▶ low mass dilepton emission \equiv vector meson spectroscopy



In-medium spectral function

- Interactions of ρ with medium is evaluated perturbatively by means of the **self-energy**

$$\text{wavy line} = \text{wavy line} + \text{wavy line} \text{---} \text{circle} \text{---} \text{wavy line} + \text{wavy line} \text{---} \text{circle} \text{---} \text{circle} \text{---} \text{wavy line} + \dots$$

$$\begin{aligned} G &= G^0 + G^0 \Pi G^0 + G^0 \Pi G^0 \Pi G^0 + \dots \\ &= \frac{G^0}{1 + \Pi G^0} = \frac{1}{p^2 - m^2 + \Pi} \end{aligned}$$

- spectral function**

$$A = \text{Im}G = \frac{\text{Im}\Pi}{(p^2 - m^2 + \text{Re}\Pi)^2 + (\text{Im}\Pi)^2}$$

- Real part gives in-medium **mass** & Imaginary part relates to **width**
- The spectral function at **finite momentum** is essential to study low mass lepton pair spectra
- requires good estimation of the vector meson **self-energy**



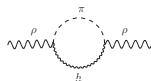
- ▶ We need to account for interactions with **mesons** and **baryons** in the hadronic medium (mesonic & baryonic loop diagrams)
- ▶ to evaluate them we need :
 - ▶ **effective interaction Lagrangian**
 - ▶ Massive Yang-Mills *Song et al PRD (1996)*
 - ▶ Hidden Local Symmetry *Bando et al PRL (1985)*
 - ▶ Chiral Perturbation Theory with massive spin-1 fields *Ecker et al PLB (1989)*
- ▶ **perturbative framework** → thermal field theory
 - ▶ imaginary time formalism (Matsubara)
 - ▶ real time formalism



ρ self-energy: meson loops

- ▶ The one-loop self energy is given by

$$\Pi(E, \vec{q}) = i \int \frac{d^4 k}{(2\pi)^4} N(q, k) D_\pi(k) D_h(q - k)$$



$$h = \pi, \omega, h_1, a_1$$

where
$$D(k) = \underbrace{\frac{1}{k^2 - m^2 + i\epsilon}}_{\text{vacuum}} - \underbrace{2i\pi n \delta(k^2 - m^2)}_{\text{medium}}$$

vacuum + medium

- ▶ The vertex factors in $N(q, k)$ are obtained from :

$$\begin{aligned} \mathcal{L}_{int} = & -\frac{2G_\rho}{m_\rho F_\pi^2} \partial_\mu \vec{\rho}_\nu \cdot \partial^\mu \vec{\pi} \times \partial^\nu \vec{\pi} && \rho - \pi - \pi \\ & + \frac{g_1}{F_\pi} \epsilon_{\mu\nu\lambda\sigma} (\partial^\nu \omega^\mu \vec{\rho}^\lambda - \omega^\mu \partial^\nu \vec{\rho}^\lambda) \cdot \partial^\sigma \vec{\pi} && \rho - \omega - \pi \\ & - \frac{g_2}{F_\pi} h_1^\mu (\partial_\mu \vec{\rho}_\nu - \partial_\nu \vec{\rho}_\mu) \cdot \partial^\nu \vec{\pi} && \rho - h_1 - \pi \\ & + \frac{g_3}{F_\pi} (\partial_\mu \vec{\rho}_\nu - \partial_\nu \vec{\rho}_\mu) \cdot \vec{a}_1^\mu \times \partial^\nu \vec{\pi} && \rho - a_1 - \pi \end{aligned}$$



Self-energy in medium

- ▶ In vacuum only the first diagram of (a) contributes
- ▶ in the medium there are **eight** possibilities

$$\text{Im}\Pi(q_0, \vec{q}) = -\pi \int \frac{d^3 k}{(2\pi)^3 4\omega_\pi \omega_h} \times$$

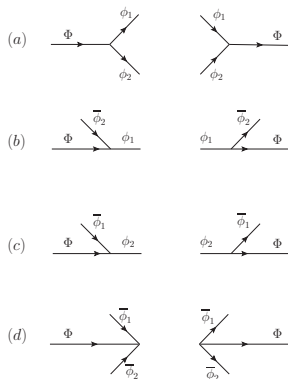
$$\left[N_1 \left\{ (1 - f^{(0)}(\omega_\pi) - f^{(0)}(\omega_h)) \delta(q_0 - \omega_\pi - \omega_h) \right. \right.$$

$$+ (f^{(0)}(\omega_\pi) - f^{(0)}(\omega_h)) \delta(q_0 - \omega_\pi + \omega_h) \left. \right\} +$$

$$N_2 \left\{ (f^{(0)}(\omega_h) - f^{(0)}(\omega_\pi)) \delta(q_0 + \omega_\pi - \omega_h) \right.$$

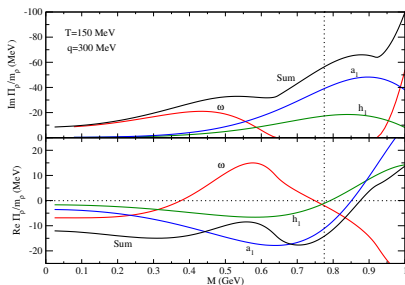
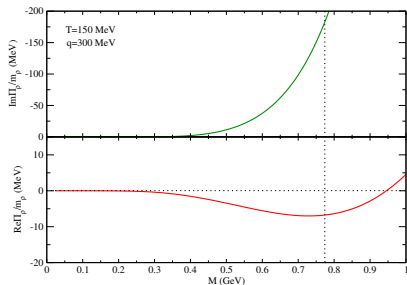
$$\left. - (1 - f^{(0)}(\omega_\pi) - f^{(0)}(\omega_h)) \delta(q_0 + \omega_\pi + \omega_h) \right\}]$$

- ▶ for positive q^2 and q_0 the diagrams (a) and (c) contribute (shown by the boxed terms)



S.Mallik and SS EPJC 61 (2009) 489

meson-loop contributions



contribution from $\pi - \pi$ loop to
real and imaginary parts

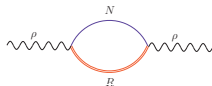
additional contributions from
the $\pi - \omega$, $\pi - h_1$ and $\pi - a_1$
loops

S. Ghosh, S.S & S. Mallik, EPJC (2010)



ρ self-energy: Baryons

- Baryon contribution is included through RN loops; $R \rightarrow$ 4-star baryon resonances



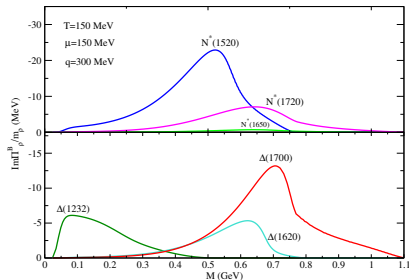
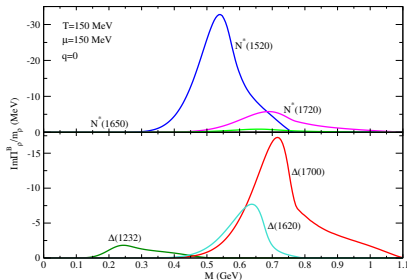
$$\Pi(q) = i \int \frac{d^4 p}{(2\pi)^4} \text{Tr}[\Gamma_{\mu\alpha} S(p, m_N) \Gamma_{\nu\beta} S^{\beta\alpha}(p - q, m_R)]$$

- The ρNR interaction vertices $\Gamma_{\mu\nu}$ are obtained from:

$$\begin{aligned} \mathcal{L} &= g_{RN\rho} [\bar{\psi}_R \sigma^{\mu\nu} \rho_{\mu\nu} \psi_N + h.c.] & J_R^P &= \frac{1}{2}^+ [N(940)] \\ \mathcal{L} &= g_{RN\rho} [\bar{\psi}_R \sigma^{\mu\nu} \gamma^5 \rho_{\mu\nu} \psi_N + h.c.] & J_R^P &= \frac{1}{2}^- [N^*(1650), \Delta(1620)] \\ \mathcal{L} &= g_{RN\rho} [\bar{\psi}_R^\mu \gamma^\nu \gamma^5 \rho_{\mu\nu} \psi_N + h.c.] & J_R^P &= \frac{3}{2}^+ [N^*(1720), \Delta(1232)] \\ \mathcal{L} &= g_{RN\rho} [\bar{\psi}_R^\mu \gamma^\nu \rho_{\mu\nu} \psi_N + h.c.] & J_R^P &= \frac{3}{2}^- [N^*(1520), \Delta(1700)] \end{aligned}$$



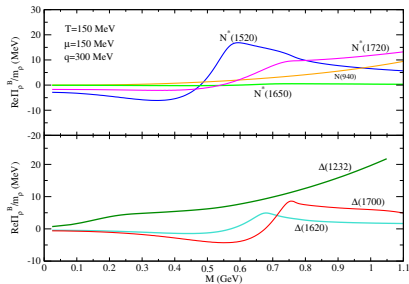
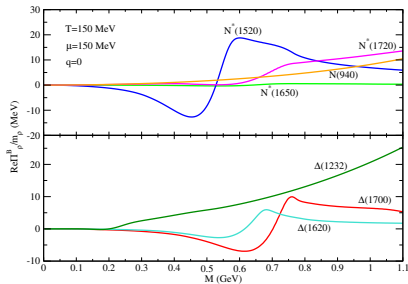
Imaginary parts



- baryonic loops significantly contribute to the spectral strength in the low mass region

S. Ghosh & S.S. NPA (2011)



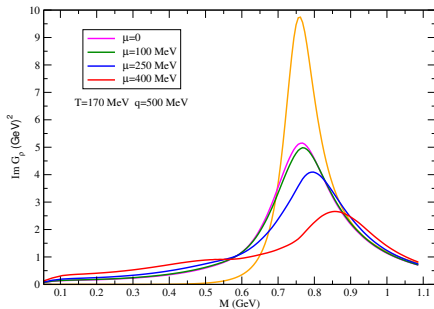
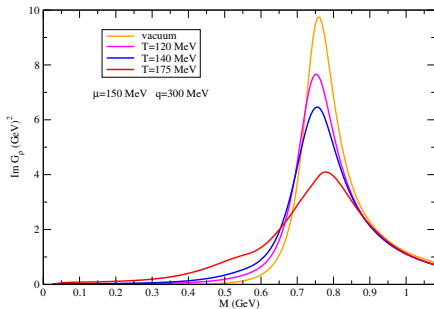


- ▶ The real parts from baryonic loops make a small positive contribution

S. Ghosh & S.S. NPA (2011)



The ρ spectral function

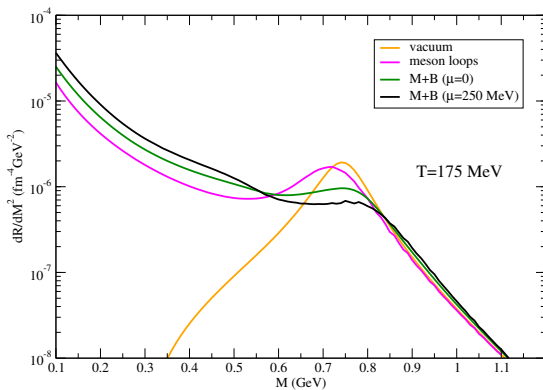


- ρ spectral function from meson and baryon loops:

$$A_\rho = \frac{\text{Im}\Pi_\rho}{(\rho^2 - m^2 + \text{Re}\Pi_\rho)^2 + (\text{Im}\Pi_\rho)^2}; \quad \Pi_\rho = \sum_{h=\pi, \omega, h_1, a_1} \Pi_{\pi h} + \sum_{R=N, N^*, \Delta} \Pi_{NR}$$

S. Ghosh & S.S. NPA (2011)

Dilepton emission rate



$$\frac{dN_{l\bar{l}}}{d^4x dM^2 q_T dq_T dy} = -\frac{\alpha^2}{3\pi^3 q^2} \frac{1}{e^{\beta q_0} + 1} F_\rho^2 m_\rho^2 A_\rho(q_0, \vec{q}, T, \mu_B)$$

S.S. & S.Ghosh (2013)



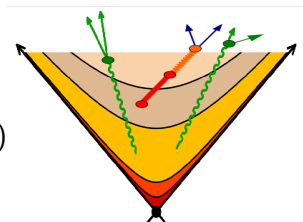
Space-time evolution

- ▶ QGP \rightarrow Hadron gas \rightarrow chem. freeze-out \rightarrow thermal freeze-out
- ▶ The total yield is obtained as

$$\frac{dN}{d^4Q} = \int d^4x \frac{dN}{d^4x d^4Q}(E^*(x), T(x))$$

$$E^* = u^\mu Q_\mu$$

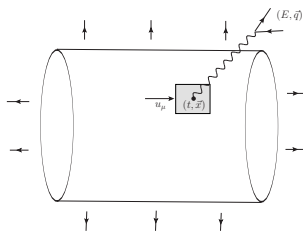
$$= \gamma_T [M_T \cosh(y - \eta) + q_T v_T \cos \phi]$$



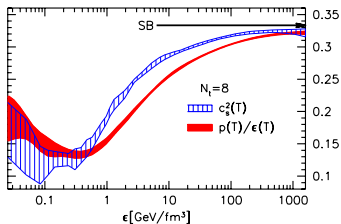
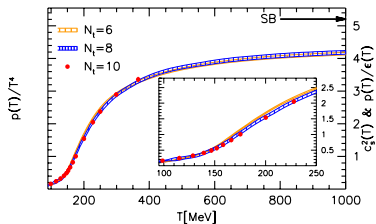
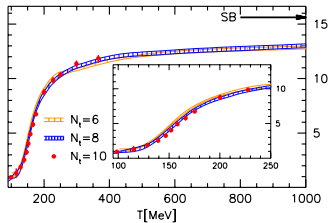
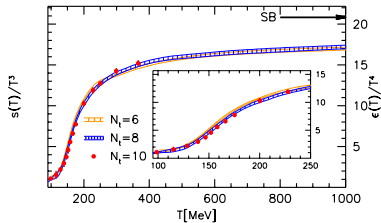
- ▶ $v_T = v_T(x, y, \tau, \eta)$ and $T = T(x, y, \tau, \eta)$ are obtained from

$$\partial_\mu T^{\mu\nu} = 0; \quad T^{\mu\nu} = (\epsilon + p)u^\mu u^\nu - g^{\mu\nu} p$$

using the **Equation of State** : $p = p(\epsilon)$
e.g from lattice



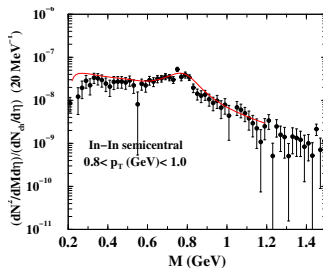
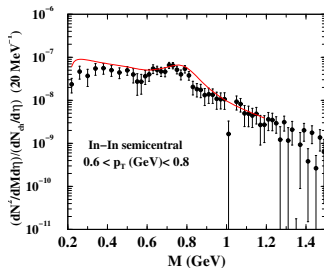
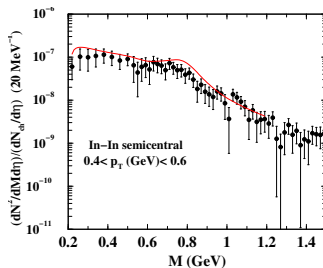
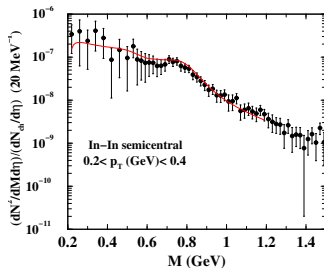
Lattice Equation of State



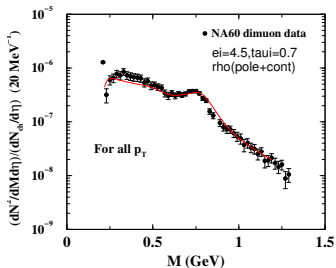
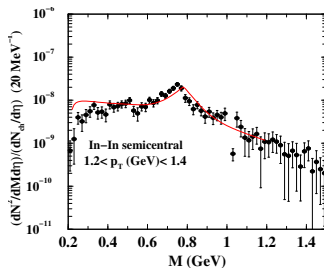
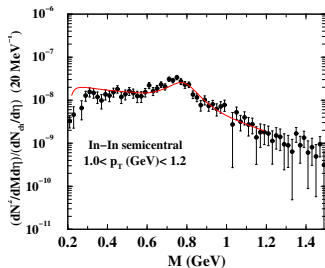
S. Borsanyi et al JHEP (2010)



Dimuon mass spectra from In-In collisions @ SPS



Dimuon mass spectra from In-In collisions @ SPS



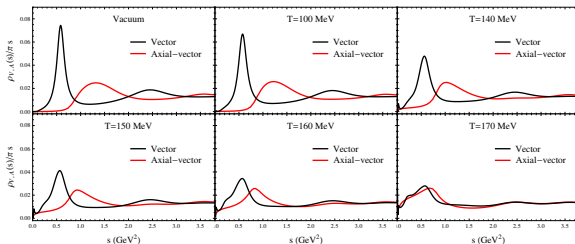
Conclusions and Outlook : observing χ SR using dileptons

- ▶ comprehensive agreement with data at several p_T and M provides confidence about the **vector spectral function**
- ▶ consistent with a scenario where the ρ spectral function is significantly broadened
- ▶ to check for χ SR we need to obtain the **axial-vector (a_1) spectral function** :-
 - ▶ Start from a microscopic theory (chiral effective theory)
 - ▶ should reproduce the **vacuum** axial-vector spectral function
 - ▶ obtain the in-medium spectral function
 - ▶ no experimental verification forthcoming \implies **check consistency with in-medium Weinberg Sum Rules**
 - ▶ test if the vector and axial-vector spectral functions conform to any of the **scenarios of χ SR**



Conclusions and Outlook : schematic study

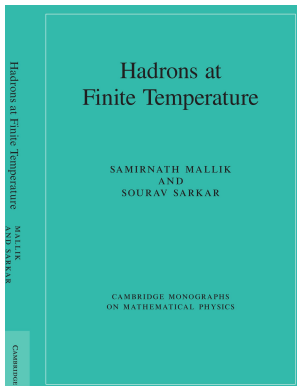
- ▶ Connecting dileptons and χ SR using ansatz a_1 sp-fn (Rapp 2014)
 - ▶ the a_1 resonance is parametrised with Breit-Wigner functions
 - ▶ in-medium modification of a_1 implemented through 4-parameter ansatz compatible with Weinberg Sum Rules



- ▶ scheme to be scrutinized by microscopic calculations
- ▶ Status: calculation of the a_1 spectral function is challenging even in vacuum (existing schemes do not lead to measured sp-fn)



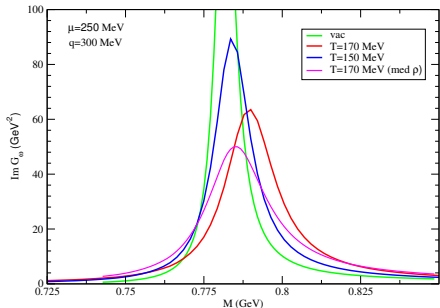
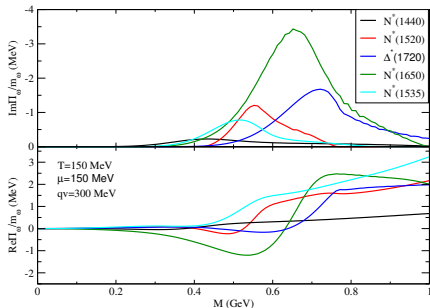
Theoretical details are discussed in the upcoming book



Thanks



The ω spectral function



- meson loop: $\rho - \pi$
- baryon loop: $N - R$,
[$R = N^*(1440), N^*(1520), N^*(1535), N^*(1650), \Delta(1720)$]

