

Slow Extraction of High Intensity Protons at BNL's AGS

K.A. Brown

kbrown@bnl.gov

*Collider Accelerator Department,
BNL*

The Slow Extraction Workshop, Darmstadt, Germany
June 1-3, 2016

Contents

Overview of C-AD Complex

AGS Performance History (fixed target programs)

Overview of AGS Slow Extraction

SEB Devices

Electrostatic Septum

AGS Main Magnet PS

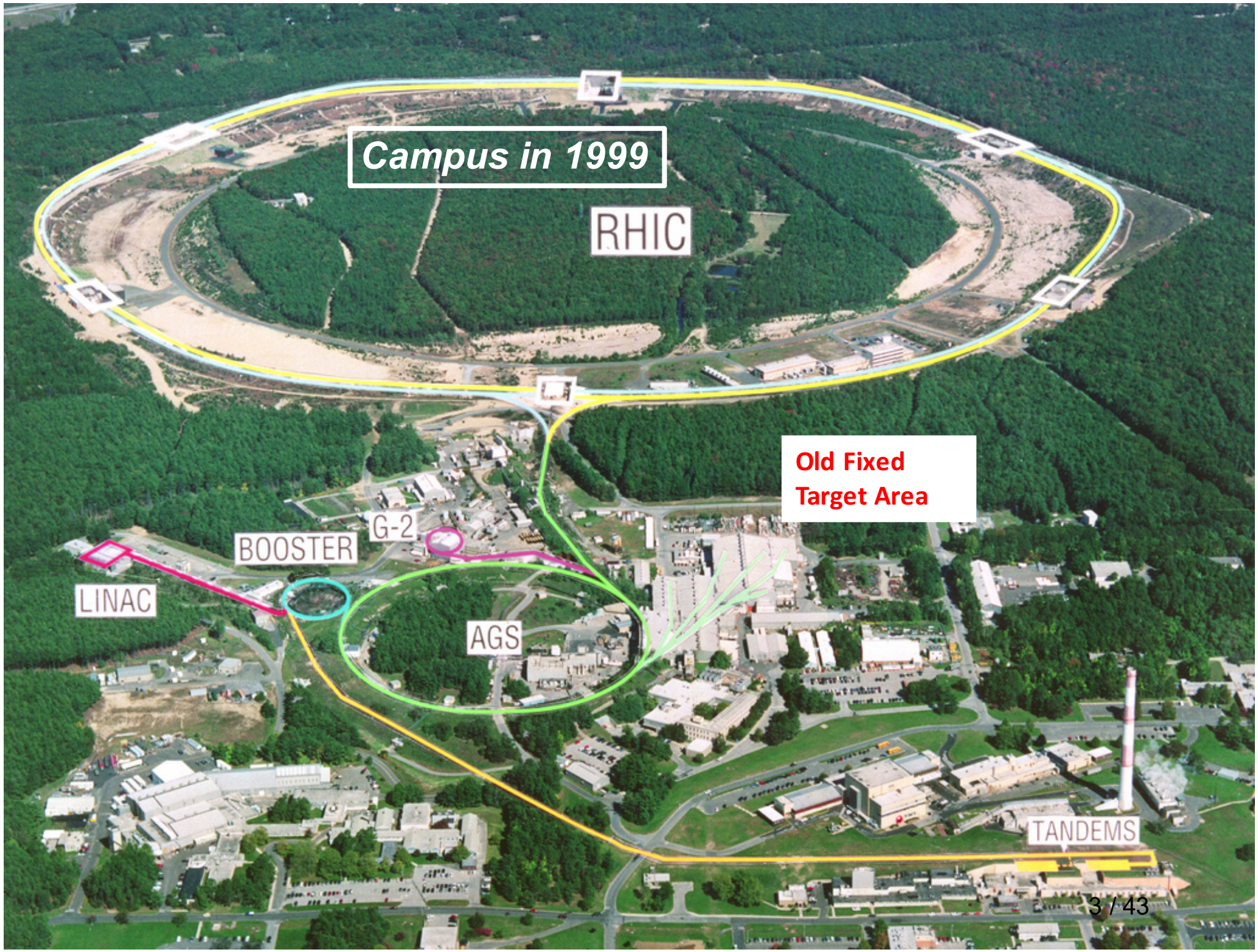
High Intensity Slow Extraction

Longitudinal Phase Space Dilution

Spill and ripple

Transport to target stations

Summary



Campus in 1999

RHIC

Old Fixed
Target Area

BOOSTER

G-2

LINAC

AGS

TANDEM

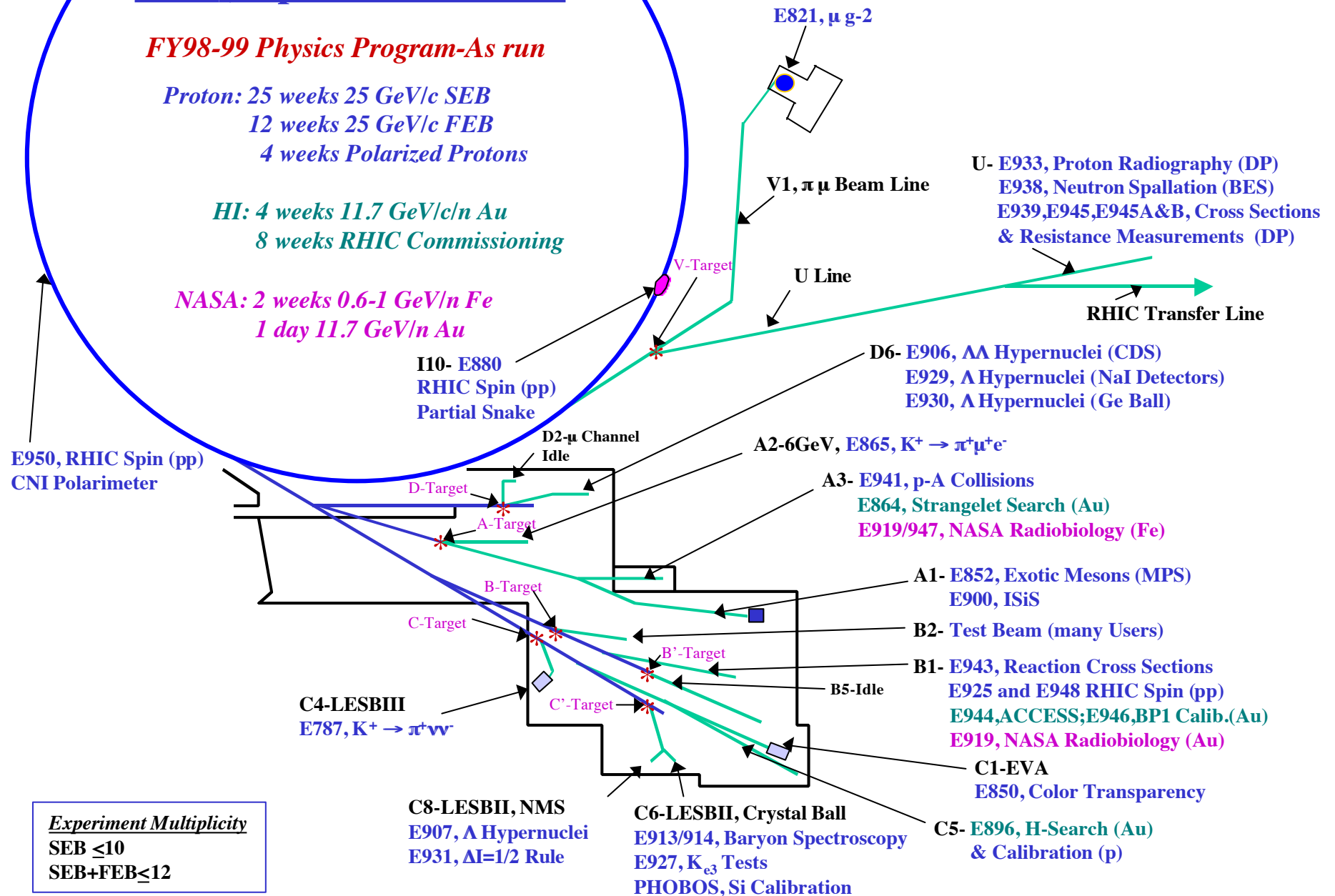
AGS Experimental Area

FY98-99 Physics Program-As run

*Proton: 25 weeks 25 GeV/c SEB
12 weeks 25 GeV/c FEB
4 weeks Polarized Protons*

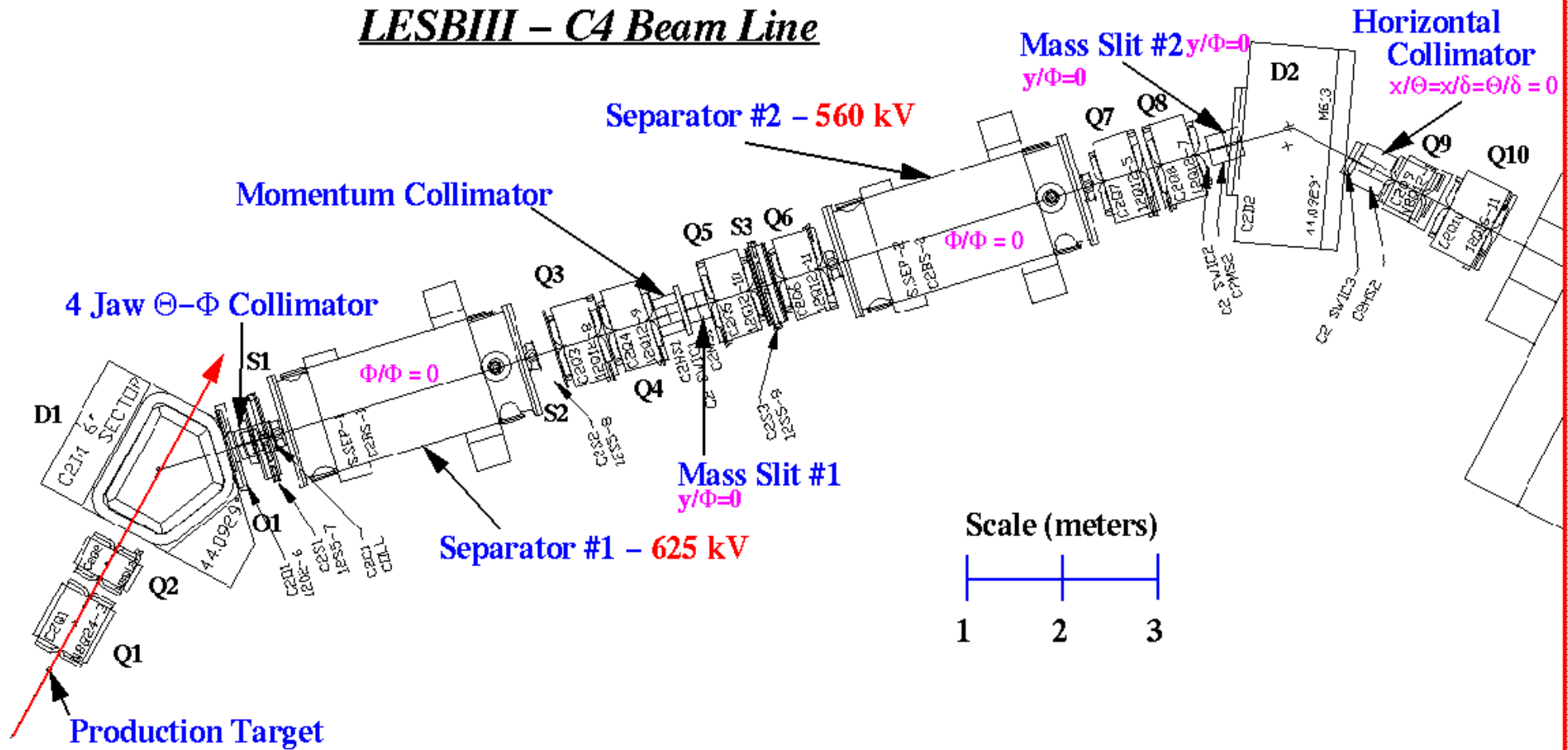
*HI: 4 weeks 11.7 GeV/c/n Au
8 weeks RHIC Commissioning*

*NASA: 2 weeks 0.6-1 GeV/n Fe
1 day 11.7 GeV/n Au*



Experiment Multiplicity
SEB ≤ 10
SEB+FEB ≤ 12

LESBIII – C4 Beam Line



1 billion 800 MeV K^+ / 10^{13} protons with 60 - 70% Purity ($\pi^+ / K^+ = 0.3 - 0.4$)

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Slow Extraction at the AGS

- March, 1968: first SE for HEP, $3Q_H=26$
 - Simple system with no ES septum
- 1972: 200 MeV LINAC (previous was 50 MeV), H⁺ injection to AGS
- 1979: first ES septum installed
- 1979: new multi-hall switchyard (3 lines)
- 1980's: pre-Booster era, H⁻ injection to AGS
 - Intensities $1.0 - 1.6 \times 10^{13}$ protons/pulse
 - Extraction momentum 25-29 GeV/c
 - Spills 1 – 2 sec., repetition periods 2.4 - 4.0 sec.
 - Extraction inefficiency 3 – 5 %
 - Began doing heavy ion experiments (NPP)
- 1990's: post-Booster era
 - Intensities $5.0 - 7.6 \times 10^{13}$ protons/pulse
 - Extraction momentum 25.5 GeV/c (to improve uptime)
 - Similar spills and rep periods, more optimization on duty factor
 - Extraction inefficiency 2 – 3 %
 - Problem! Higher losses in switchyard beam transport (more later)
- 2002: program ends. RHIC era.

AGS Performance

Proton Beams	FY94	FY95	FY96	FY97	FY98	FY99 (G-2)	FY00 (G-2)	FY01 (G-2)	FY02
Beam Energy (GeV)	24	24	24	24	24	24	24	24	24
Peak Beam Intensity (10^{12} #p/pulse)	40	63	62	62	72	58	61	63	76
Total Integrated (10^{20} protons)	0.3	1.1	0.9	0.4	0.9	0.4	0.5	0.6	0.7
Spill Length/Cycle Time (seconds)	1.0 / 3.0	1.6 / 3.6	1.6 / 3.6	1.6 / 3.6	2.8 / 5.1				2.4 / 5.4
Duty Cycle	26 %	44 %	44 %	44 %	55 %				44 %
Spill Structure (peak-average) /average	50 %	20 %	20 %	20 %	20 %				20 %

Note: Each year also included Heavy Ion operations.

G-2 Operations used Fast Beam to the U-line (now upstream end of AtR line)

G-2 Commissioning began FY97

Booster & AGS Performance: SEB

Imposed limits to lost beam power to maintain hands-on maintenance (ALARA).

•AGS SEB operation, 5.4 s AGS cycle time, 6 Booster cycles.

Achieved **19.6 Tp/sec, Booster Late** & **13.7 Tp/second, AGS Late**.

Table: SEB 10 Pulse Ave. Data (best performance)

	Intensity (Tp/cycle)*	Efficiency (%)	Beam Loss (Tp/cycle)	ALARA (Tp/cycle)	Loss (kW)	Loss/m (W/m)
Linac	177	-	-	-	-	
Booster Injected	125	71	52	54	0.31	1.5
Booster Extracted	106	86	18	18	0.5	2.5
AGS Injected	78	74	28	31.5	1.62	2.0**
Transition	76	98	2	3	0.26	0.3
After Transition	73	95	3	4.5	0.63	0.8
AGS Late	73	100	0	1.5	0	0

* 1 Tp = 1×10^{12} protons

** assumed lost in AGS

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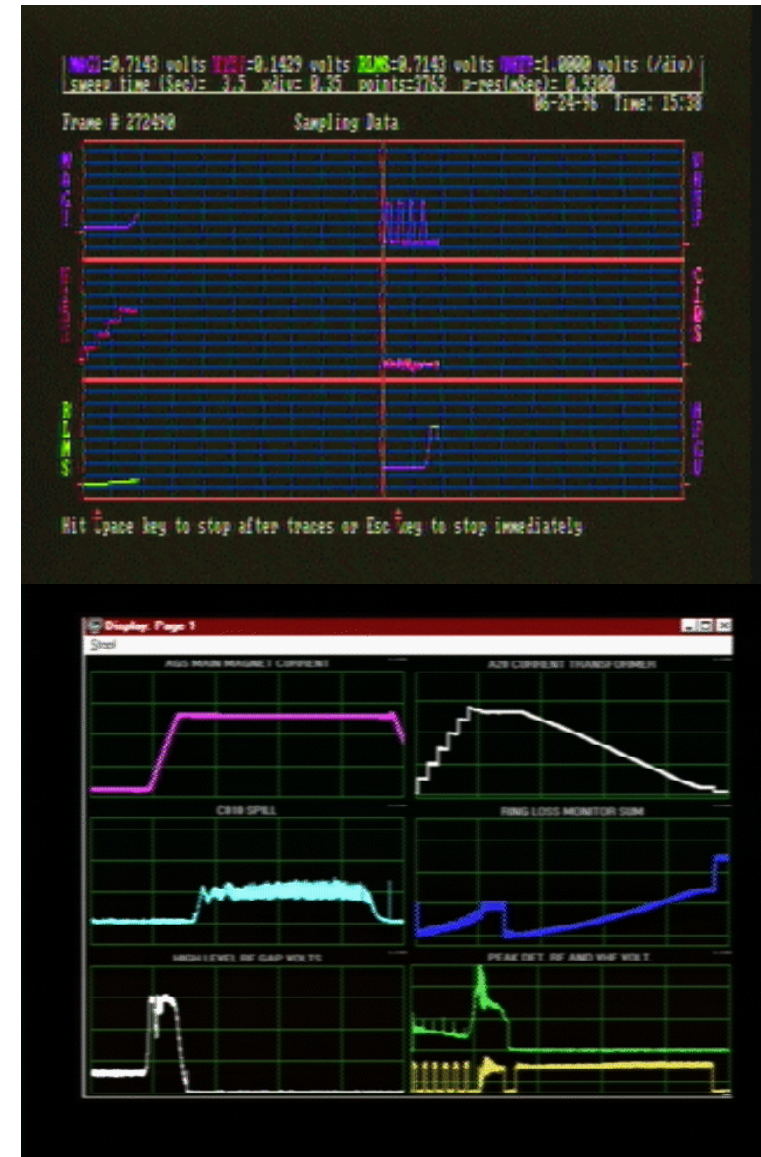
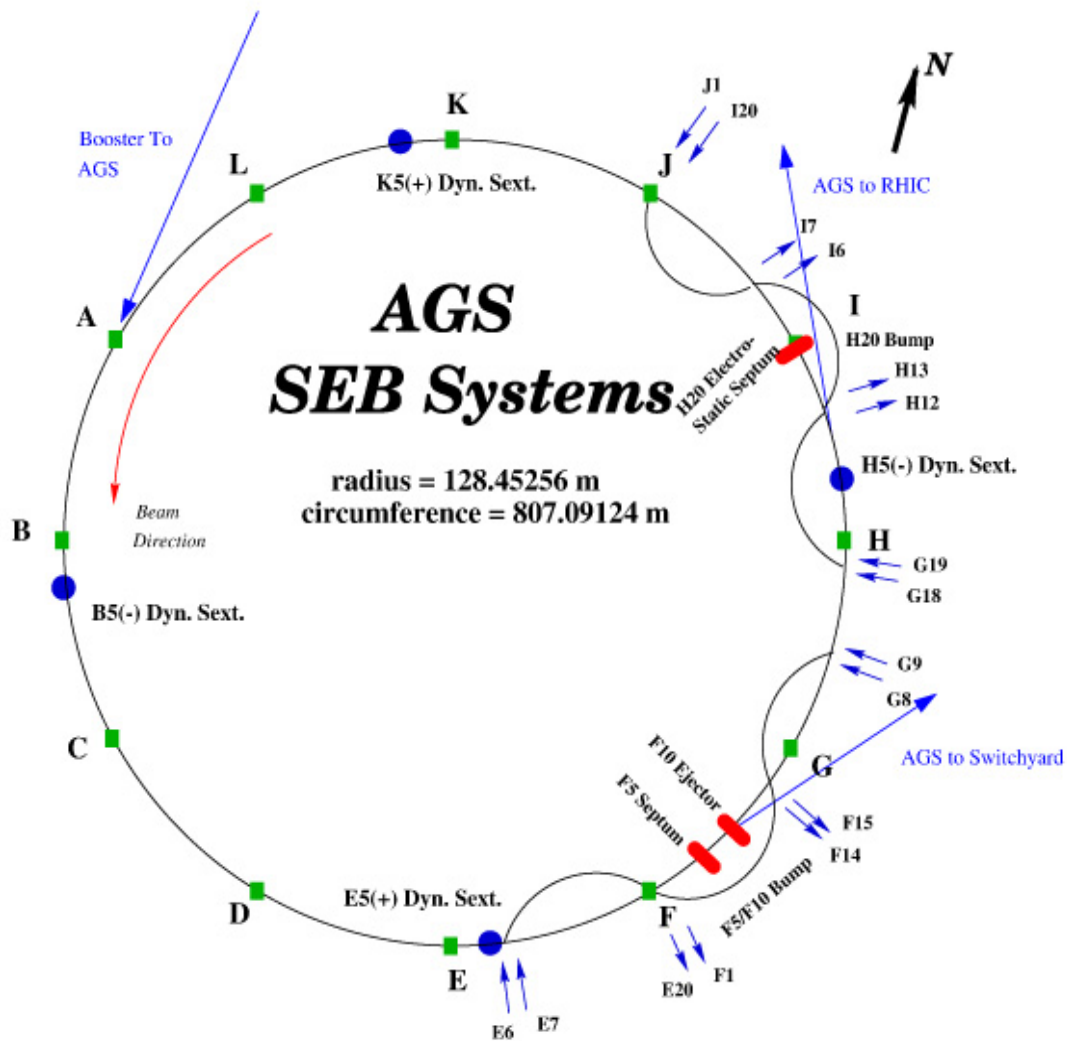
Longitudinal Phase Space Dilution

Spill and ripple

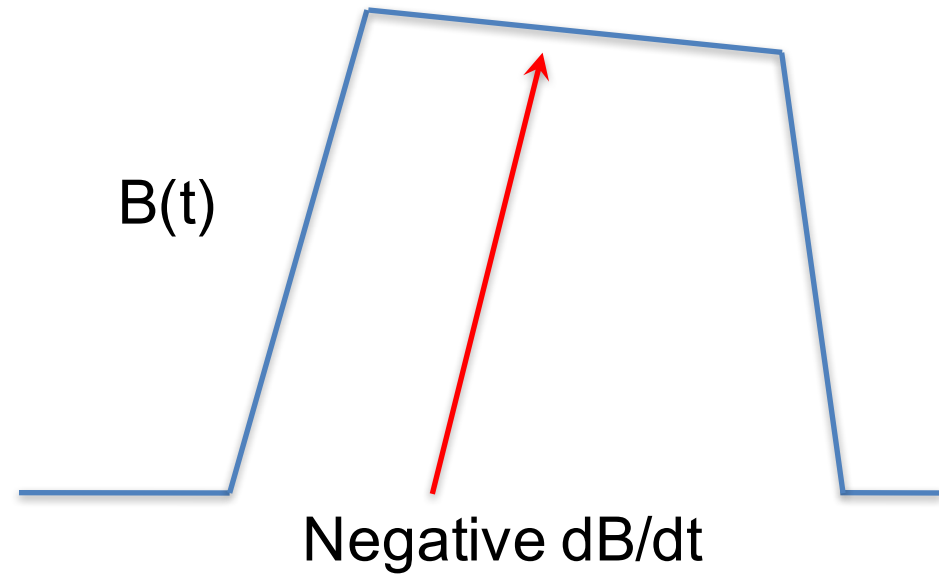
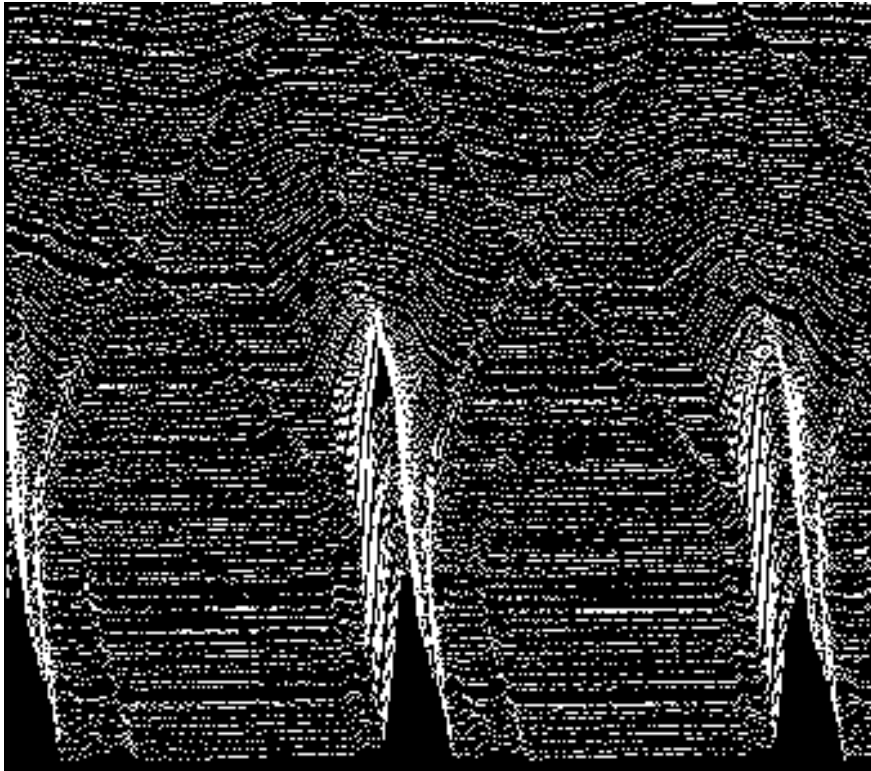
Transport to target stations

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Overview of AGS Slow Extraction

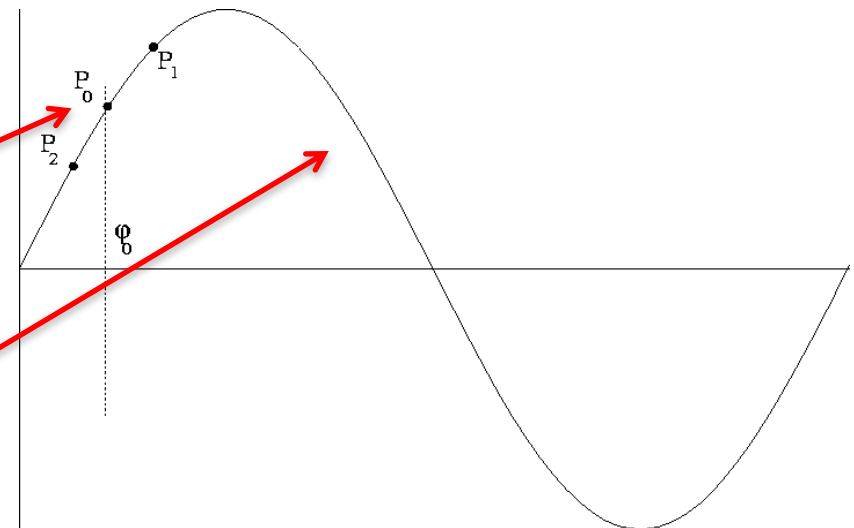


Extraction Method: Chromatic SE

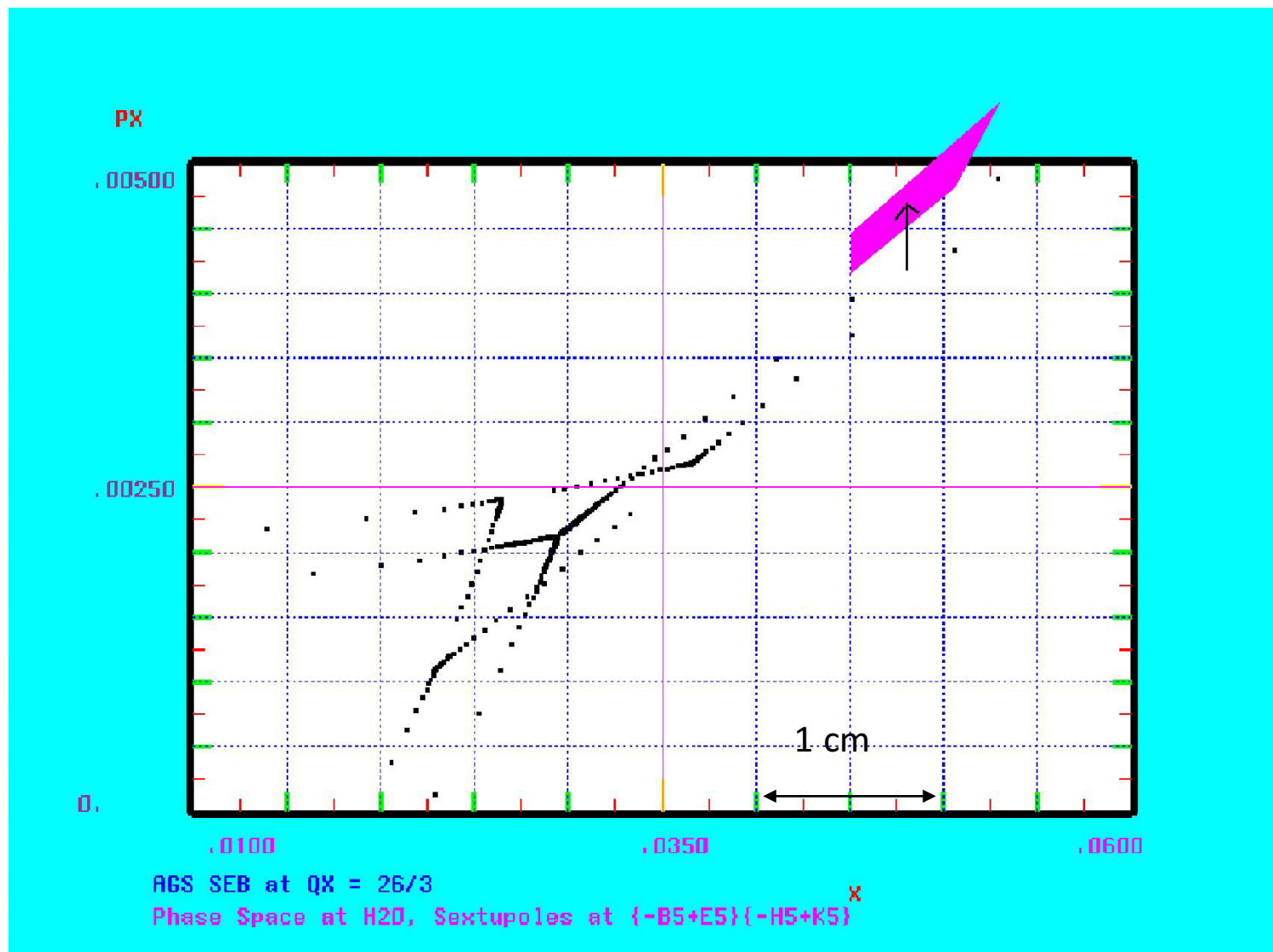


To increase dp/p , phase back
Drive dp/p to as high as 0.5%

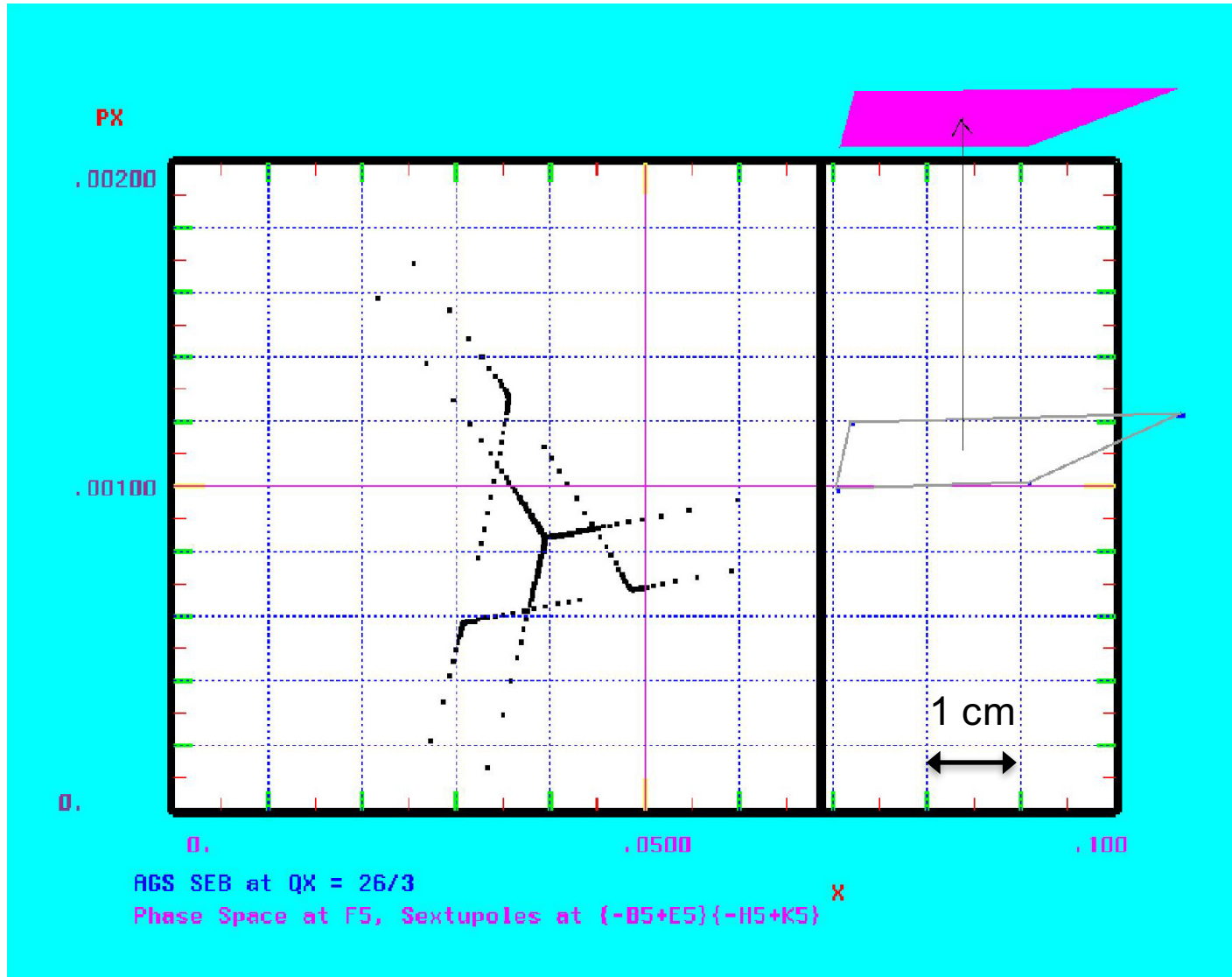
After γ_{tr} accel. on (-) slope



Slow Extraction: ES Phase Space



Slow Extraction: Thin MS Phase Space



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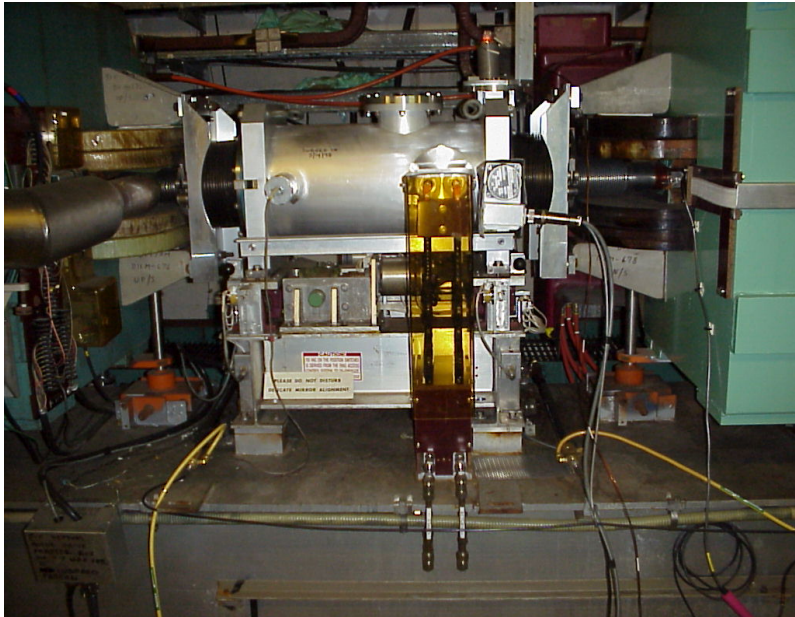
Summary

SEB Device Parameters

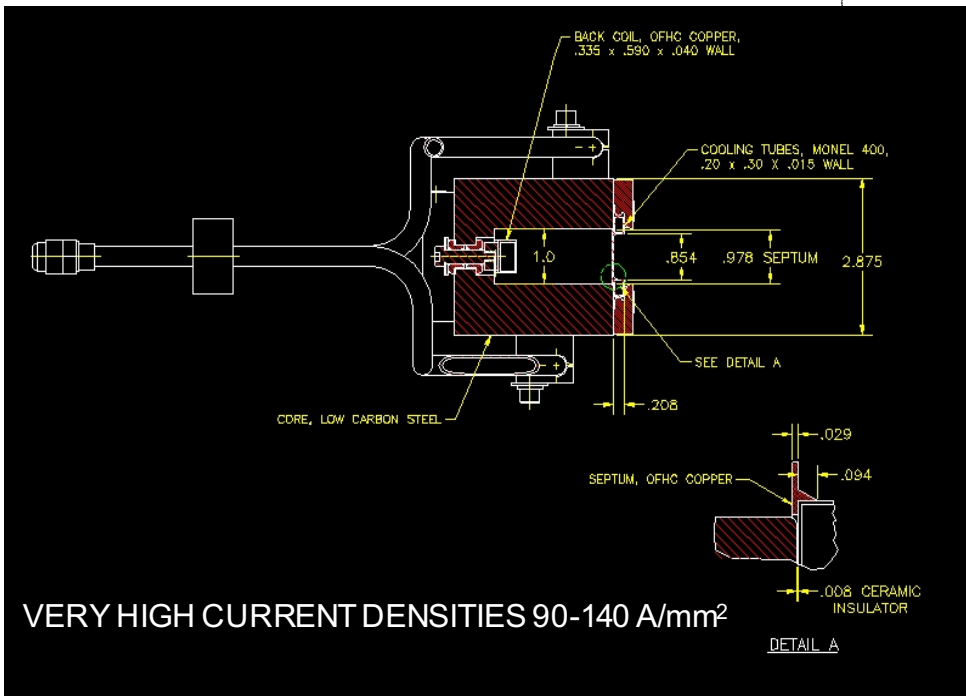
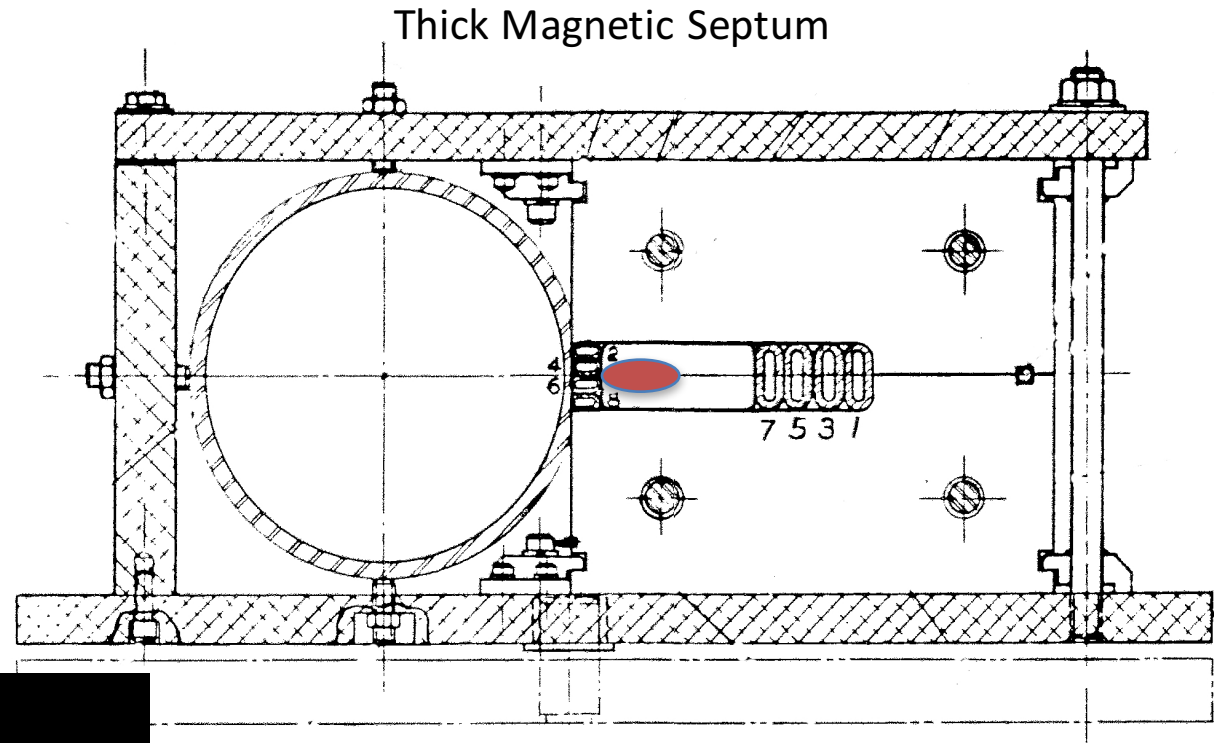
	Elect. Septum	Thin Septum	Thick Septum
β_x [m]	12.0 – 19.9	22.1	19.9 – 12.0
β_y [m]	19.9 – 12.0	10.5	12.0 – 19.9
Vert. Gap [mm]	20.0	17.8 (25.4)	19.1
Horiz. Gap [mm]	10.0	44.45	38.1
Length [m]	2.30	0.667	0.81+1.22=2.03
N turns		1	4
Septum w [mm]	0.051 / 3.175 space WRe 1.58 wide foil	0.76	13.5 / 15.85
Deflect. [mrad]	0.43	1.1	18.5
Field B/E	80 kV/cm	1.5 kG	9.5 kG

All US/DS remotely movable

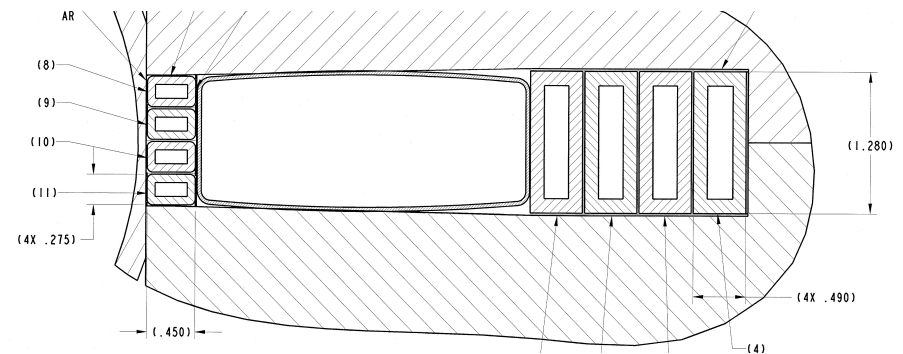
SEB Devices : Septa



Thin Magnetic Septum in Place.



VERY HIGH CURRENT DENSITIES 90-140 A/mm²



SEB Devices : Electrostatic Septum

Properties of Foil Septum

Material : 75% Tungsten and 25% Rhenium

Special property: Ductile in High Temperature

Foil thickness .051 mm

Foil Width 1.5 mm

Foil Spacing 3.175 mm

Number of foils 1000

Gap = 1cm

Length = 2.5 meter

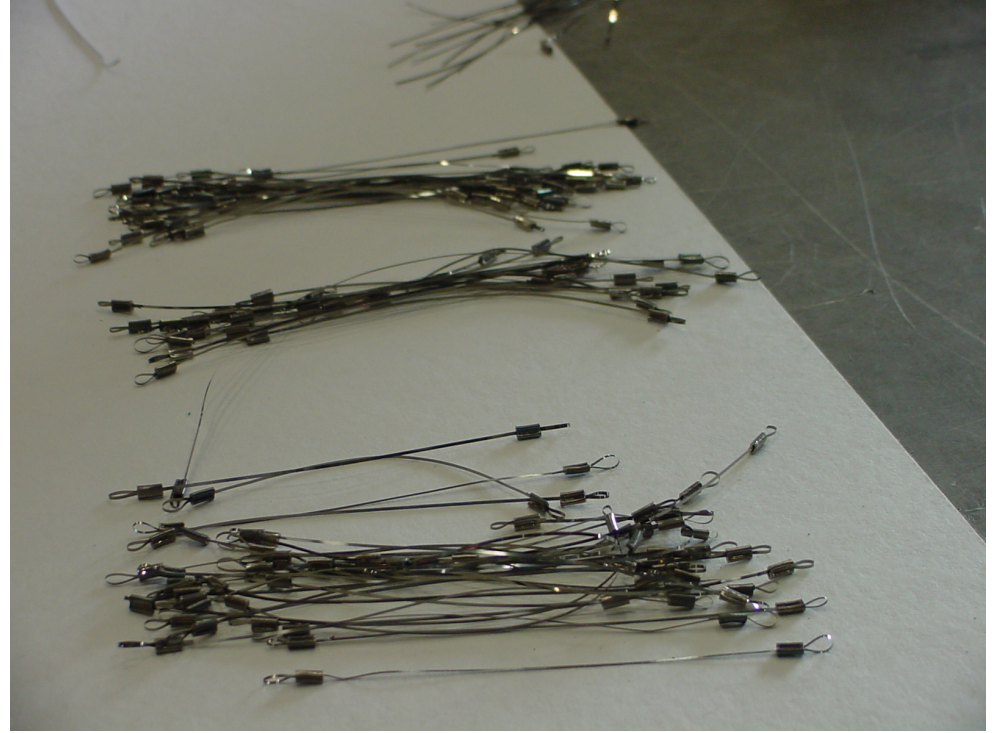
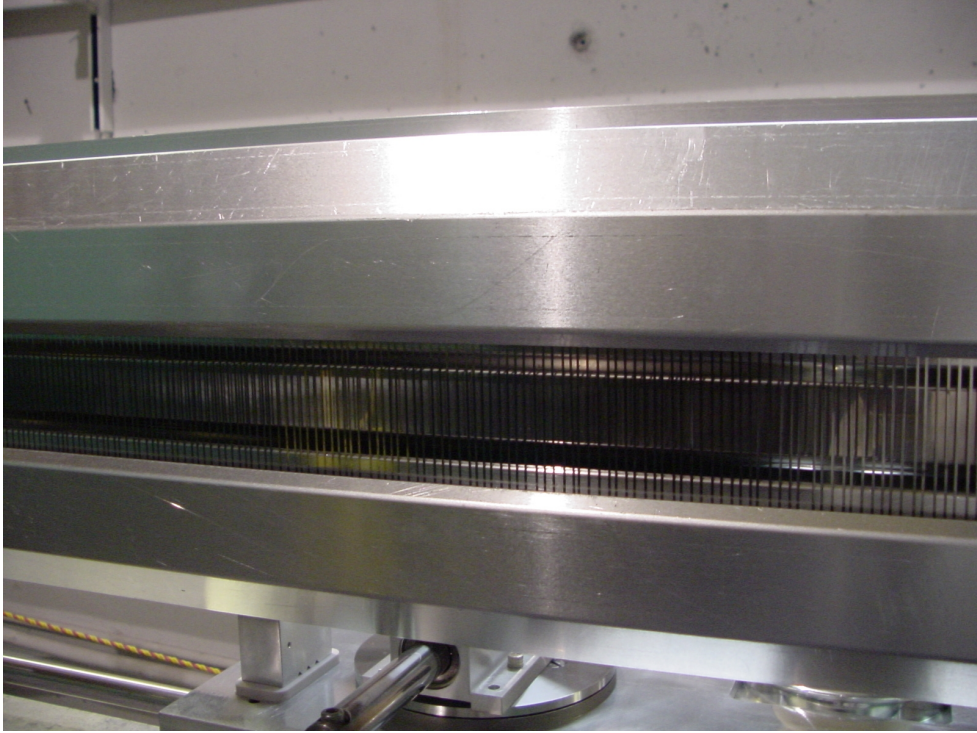
Operating voltage 56 kV

Conditioning Voltage 64 kV

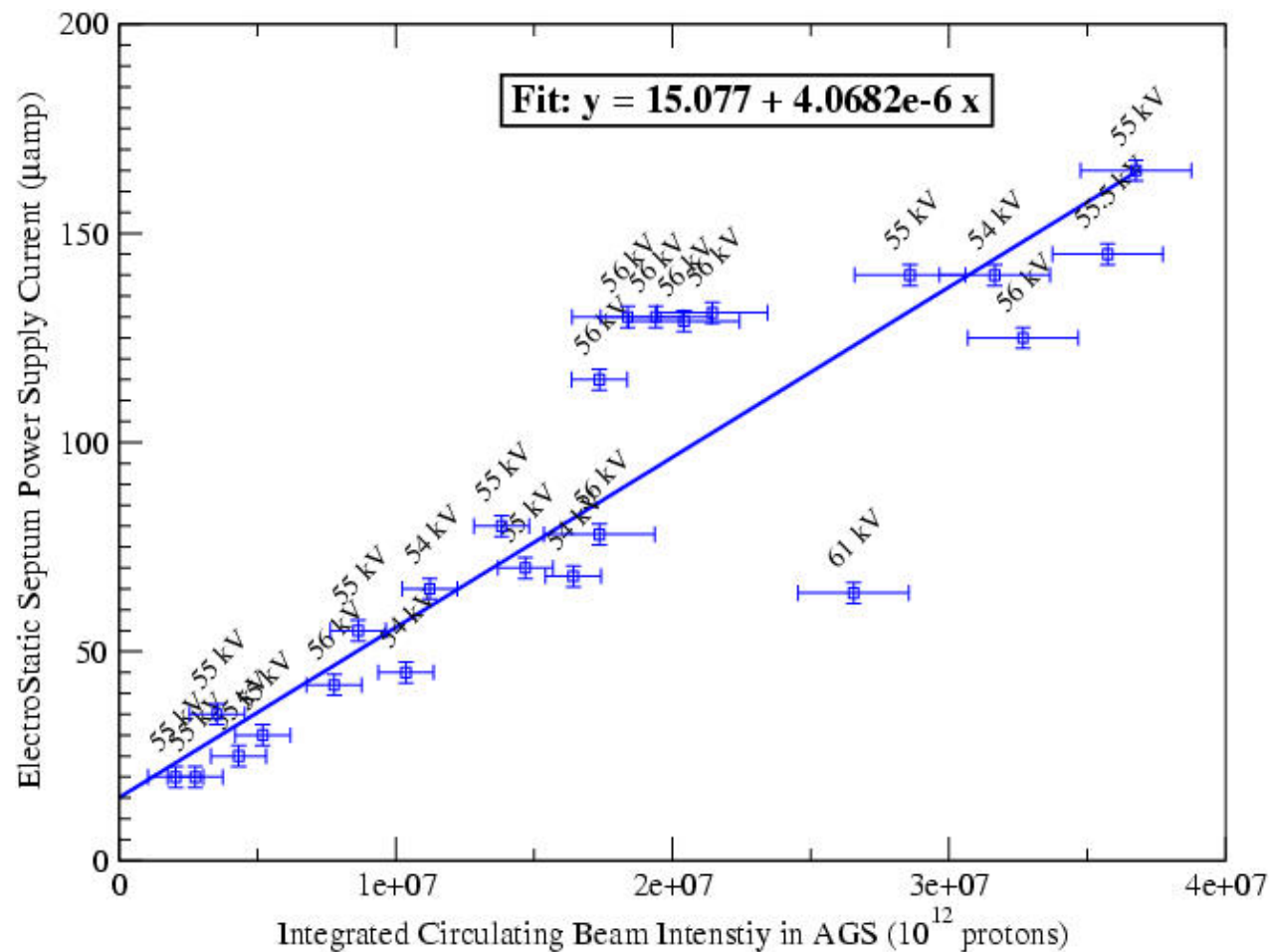
Operating Vacuum 10^{-8} Torr



Foils on Septum



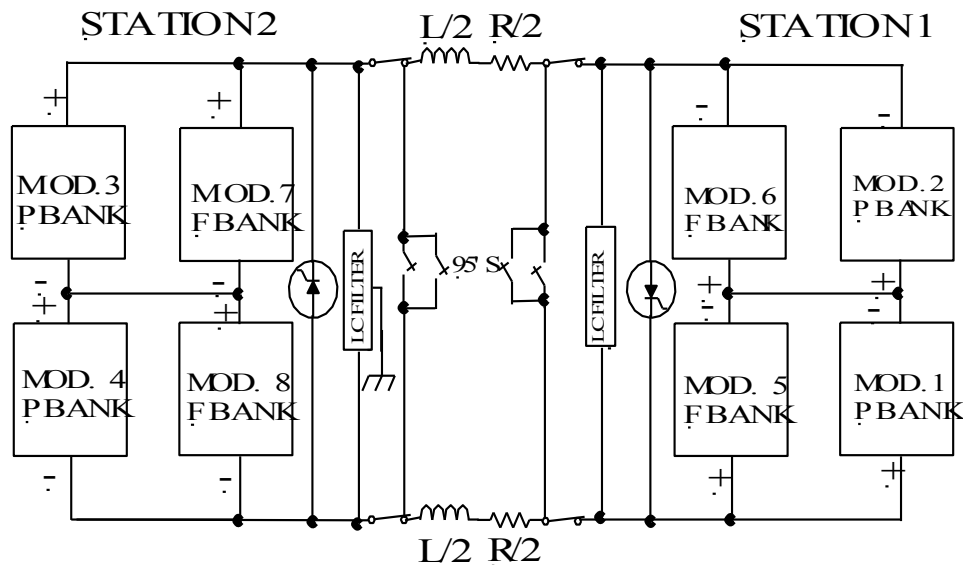
AGS High Intensity & ES Operation



Contents

Overview of C-AD Complex
AGS Performance History (fixed target programs)
Overview of AGS Slow Extraction
SEB Devices
Electrostatic Septum
AGS Main Magnet PS
High Intensity Slow Extraction
Longitudinal Phase Space Dilution
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AGS Magnet Power Supply Configuration.

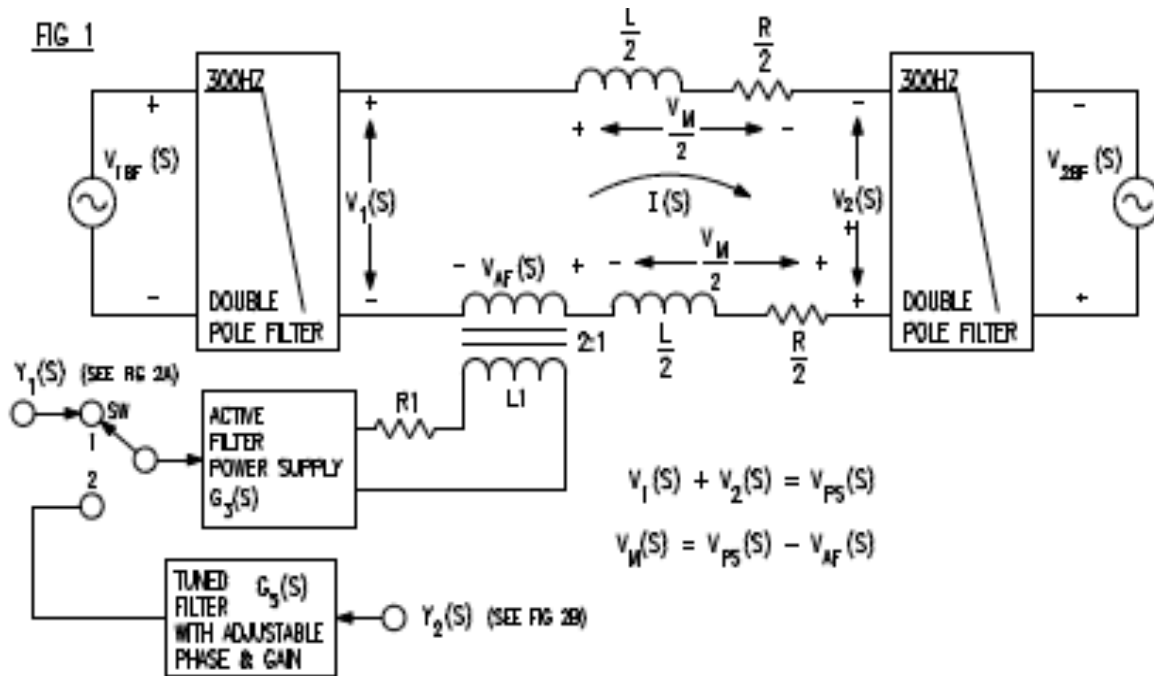


- 2 stations
- each with F-bank and P-bank power supplies in parallel.
- 24 pulse thyristor control rectifiers
- F-bank operate at ± 1900 Volt maximum, and 6000 Amp, and it is used during the flat-tops of the AGS cycles.
- P-bank operates at ± 9000 Volt maximum, and 6000 Amp, and it is used during ramping

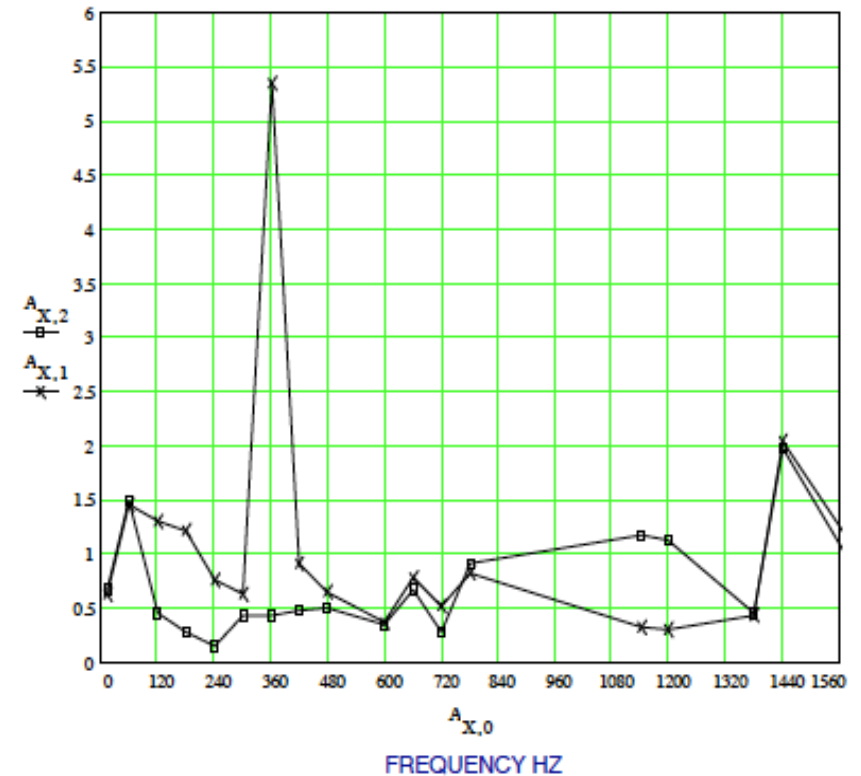
- Each PS is 12 phase
- Magnets are powered in two strings, alternating top/bottom coils on separate power supplies
- Field ripple fundamental is therefore 24 phase
- This ensures minimum ripple during the flat-tops, an essential condition for a slowly extracted beam.

Active Ripple Filter

FIG 1



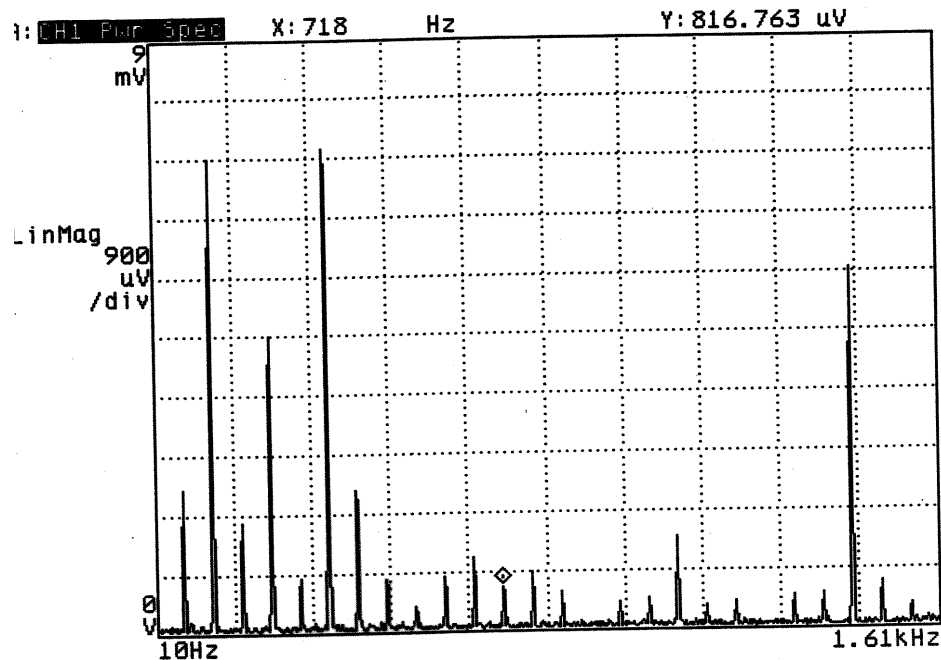
1. $A_{X,1}$ IS THE RIPPLE WITHOUT THE ACTIVE FILTER CORRECTION
2. $A_{X,2}$ IS THE RIPPLE USING THE ACTIVE FILTER CORRECTION, WITH SWITCH (SW) IN POSITION 2 (SEE FIG. 2). TUNED FILTER WAS TUNED TO CORRECT 120 HZ, 180 HZ, 240 HZ, 360 HZ, 720 HZ.



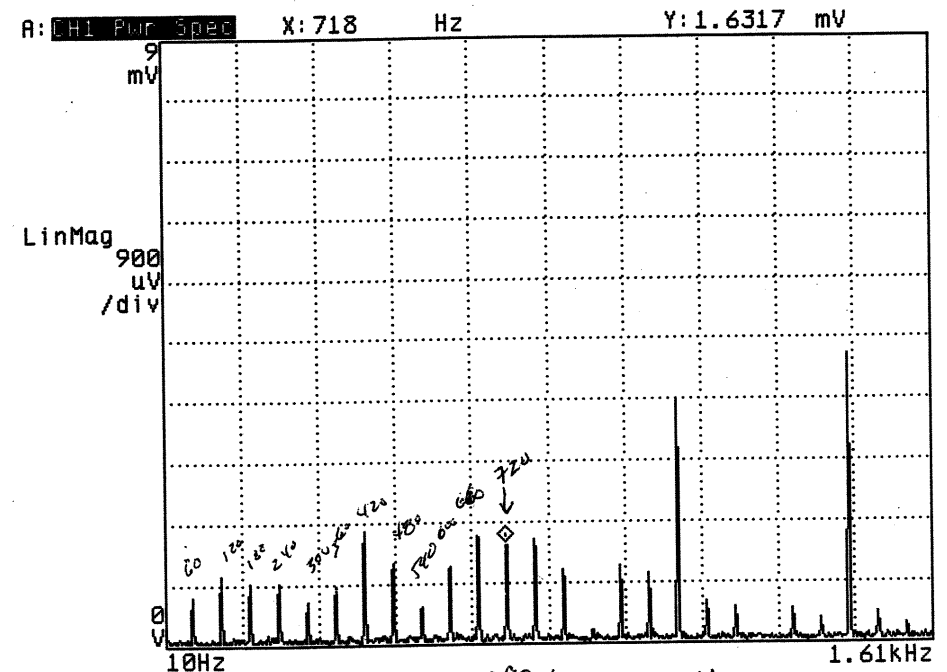
Active Filter Effect on Spill 60 Hz Harmonics

ACTIVE FILTER OFF/sh2 - u1 - p# 11050805

Scale Trace: A Ref Lvl: 0
Per Div: 900 u Ref Pos: Bottom
Date: 11-03-97 Time: 09:57:00 AM



Scale Trace: A Ref Lvl: 0
Per Div: 900 u Ref Pos: Bottom
Date: 11-03-97 Time: 09:57:00 AM



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Overview of AGS Slow Extraction

SEB Devices

Electrostatic Septum

AGS Main Magnet PS

High Intensity Slow Extraction

Longitudinal Phase Space Dilution

Spill and ripple

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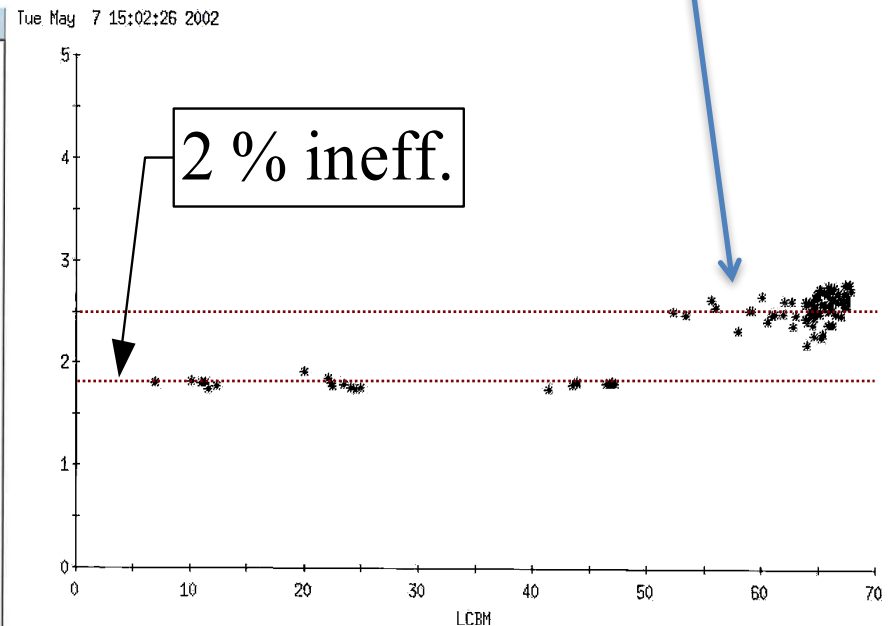
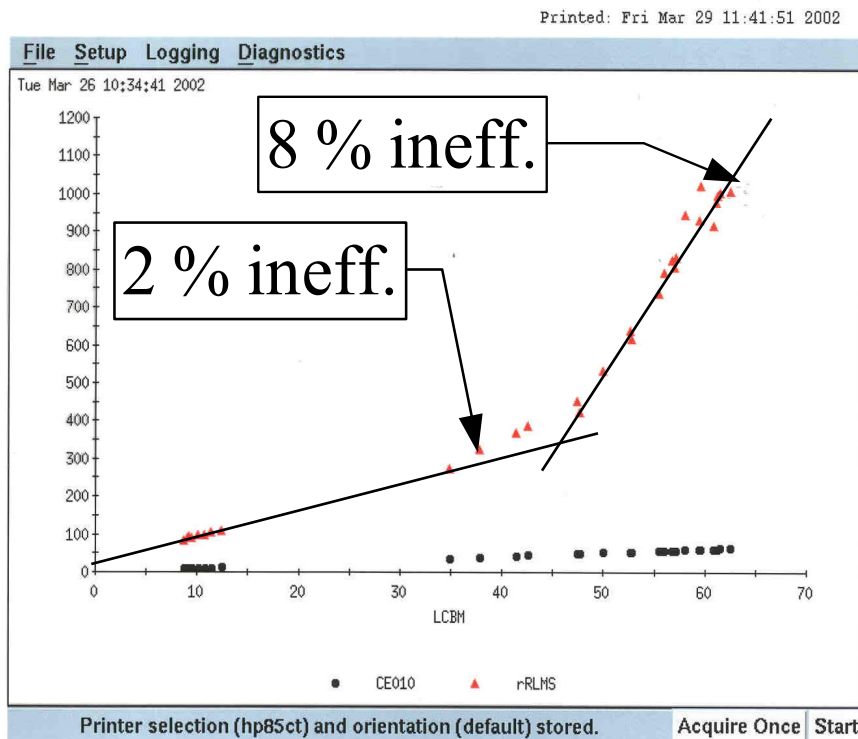
Summary

High Intensity Slow Extraction

70 TP Slow extracted beam observations.

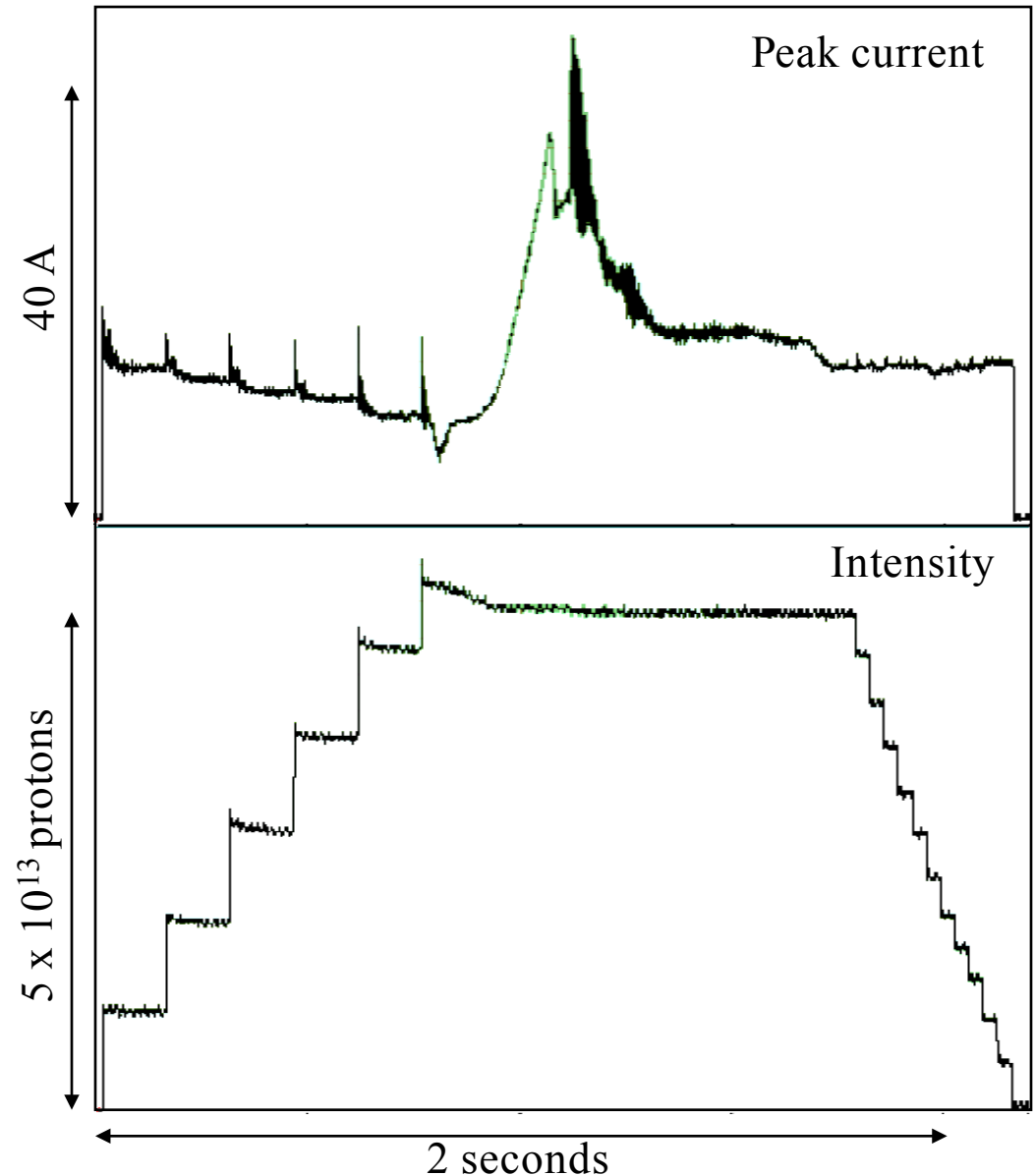
Vertical Chromaticity is kept positive after transition.

Negative Horizontal Chromaticity is a problem at high intensity.



AGS performance for high intensity

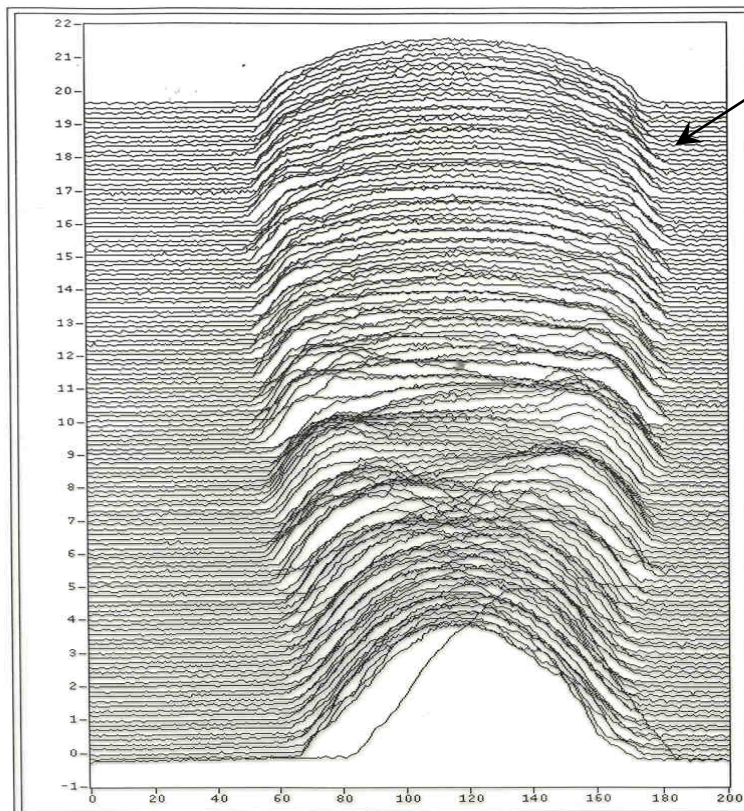
- 6 single bunch transfers from Booster
- Peak intensity reached: 76×10^{12} ppp
- Bunch area: 3 eVs at injection
10 eVs at extraction
- Intensity for g-2 ops: $50\text{-}60 \times 10^{12}$ ppp
- Strong space charge effects during accumulation in AGS
- 2nd order transition energy jump limits available momentum aperture.
- Chromatic mismatch at transition causes emittance dilution
- Dilution needed for beam stability



Longitudinal Phase Space Dilution

Keeping peak beam current low. Trade off with larger longitudinal emittance.

Front Panel



Bunch Dilution using
93.15 MHz VHF cavity

The cavity:

- a shorted quarter wave TEM mode cavity
- 30 kV of gap voltage for less than 10 kW of drive power.
- When not in operation it was switched to a low-impedance state by a PIN diode switch.
- Harmonics 268, 272
- Phase modulated between 6.7 to 7.3 kHz

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High Intensity & Spill Structure

25-Apr-02
15:08:31

VHF OFF

REMOTE ENABLE

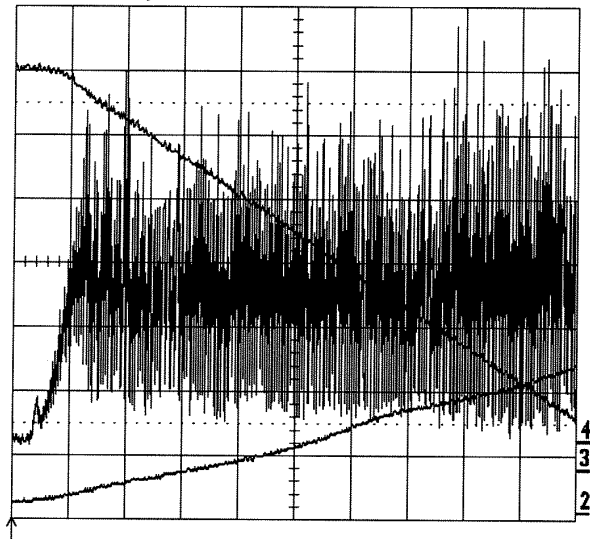
GO TO
LOCAL

2
.2 s
1.00 V

3
.2 s
0.50 V

4
.2 s
1.00 V

.2 s
1 2 V 50Ω
2 1 V 50Ω
3 .5 V DC
4 1 V DC



25 kS/s

□ STOPPED

Ext10 DC 4.70 V 50Ω

25-Apr-02
15:09:08

VHF ON

REMOTE ENABLE

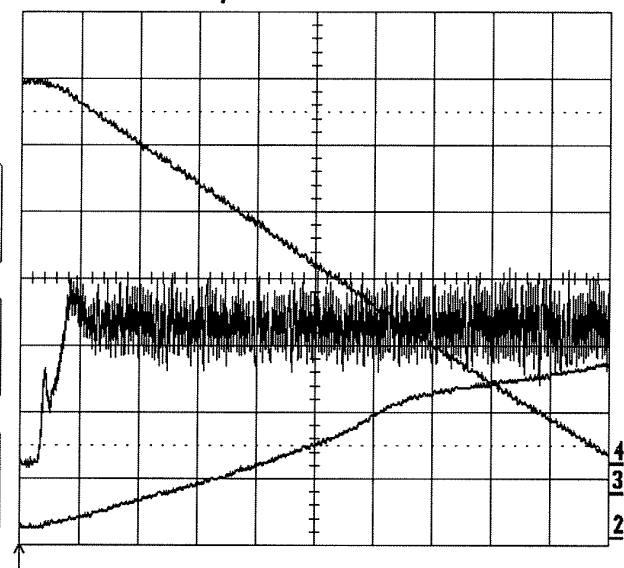
GO TO
LOCAL

2
.2 s
1.00 V

3
.2 s
0.50 V

4
.2 s
1.00 V

.2 s
1 2 V 50Ω
2 1 V 50Ω
3 .5 V DC
4 1 V DC

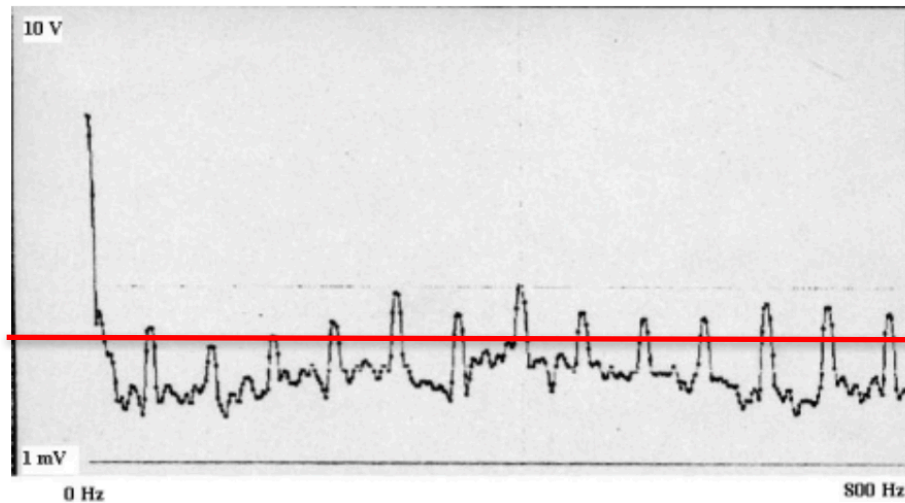


25 kS/s

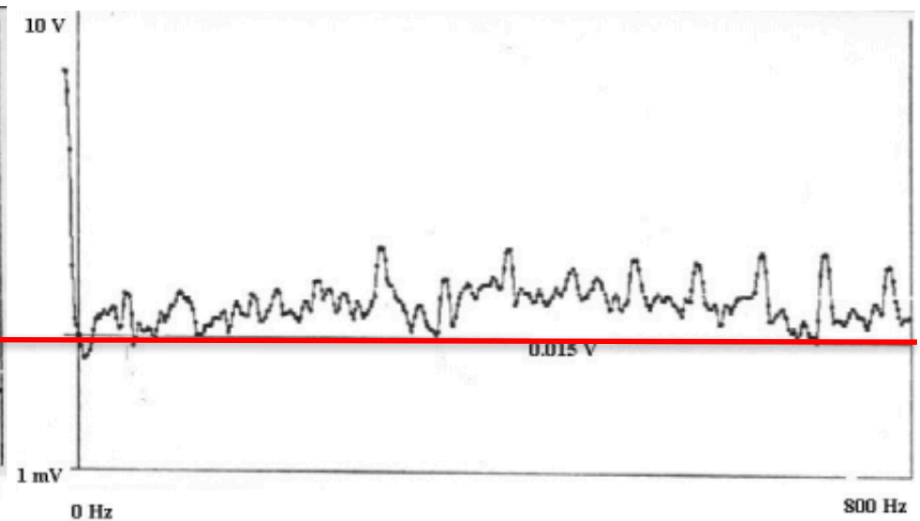
□ STOPPED

Ext10 DC 4.70 V 50Ω

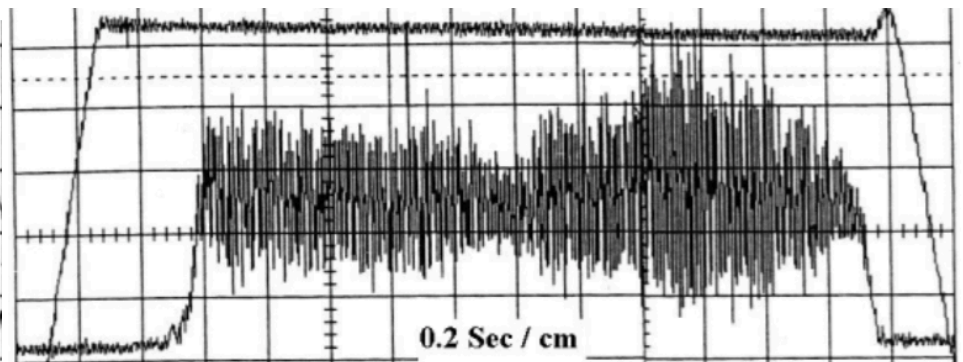
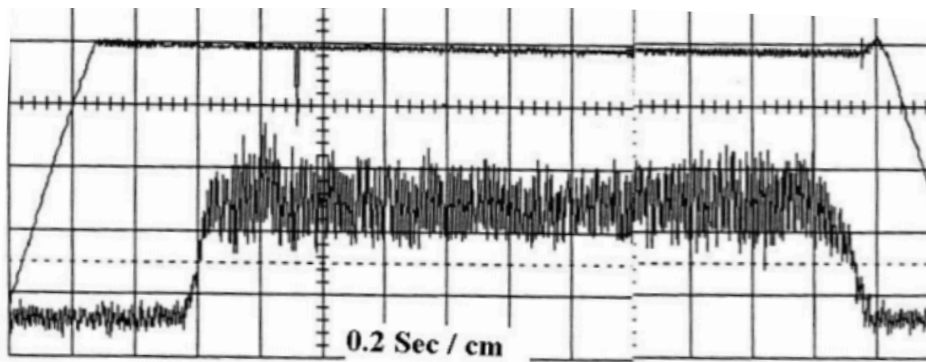
High Intensity & Spill Structure



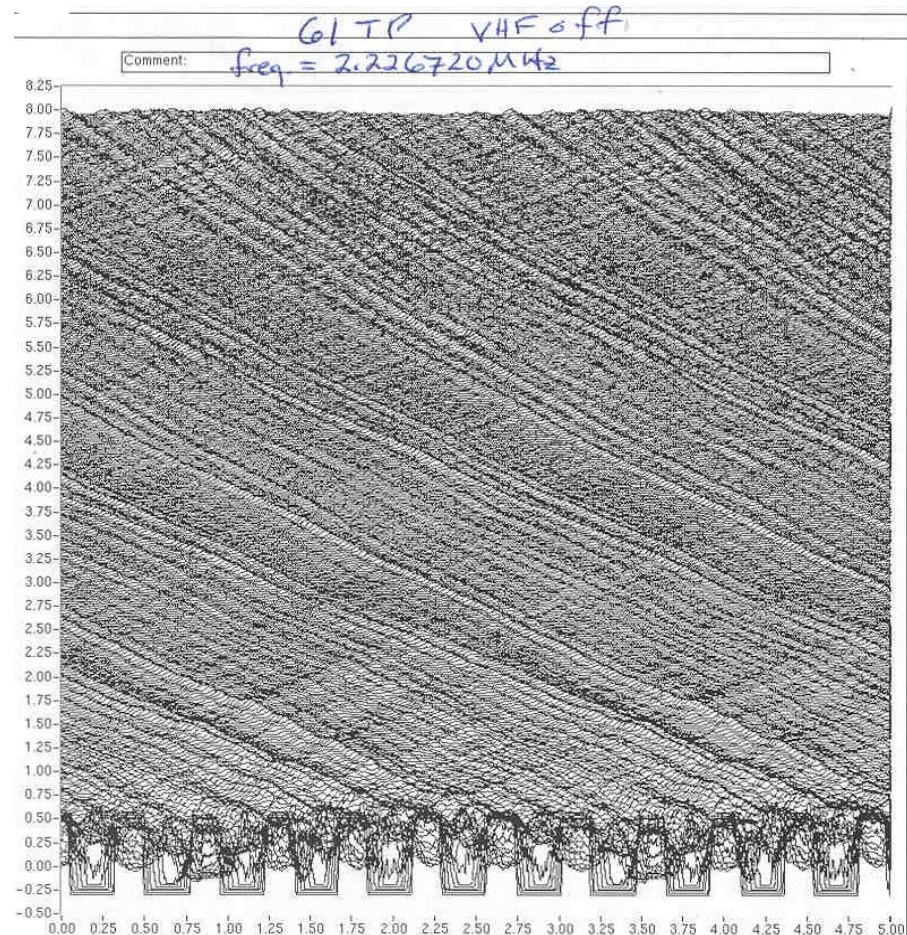
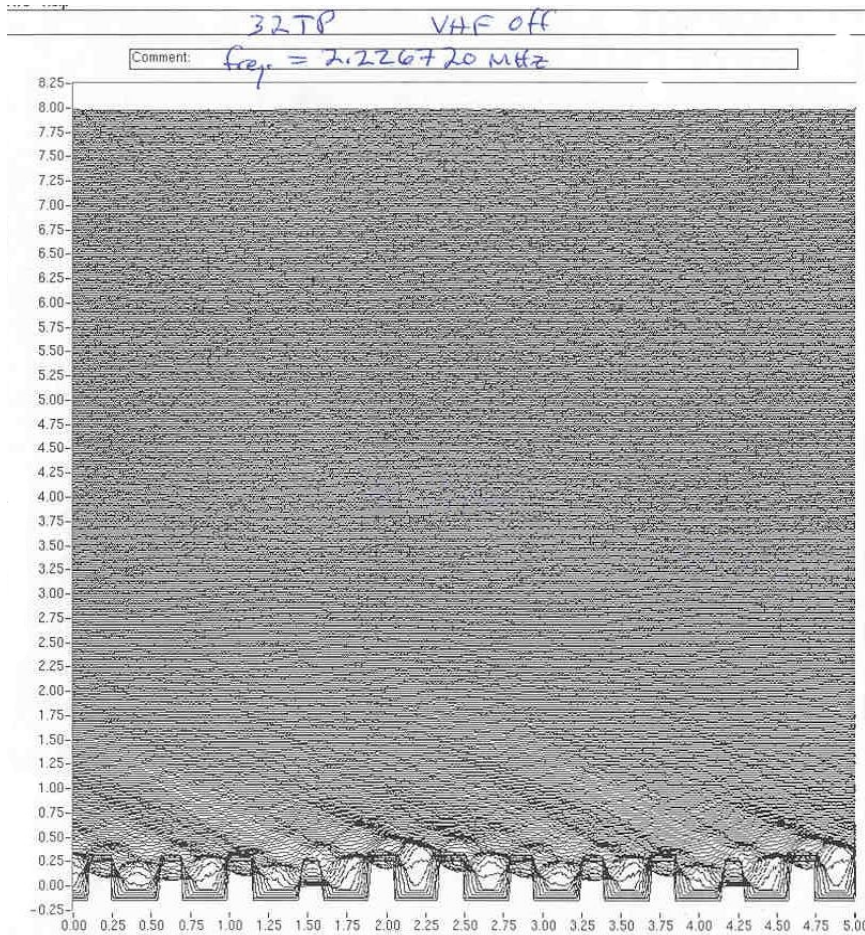
Spill – 20 TP / 2 Sec



Spill – 50 TP / 2 Sec



Wall Current Monitor View



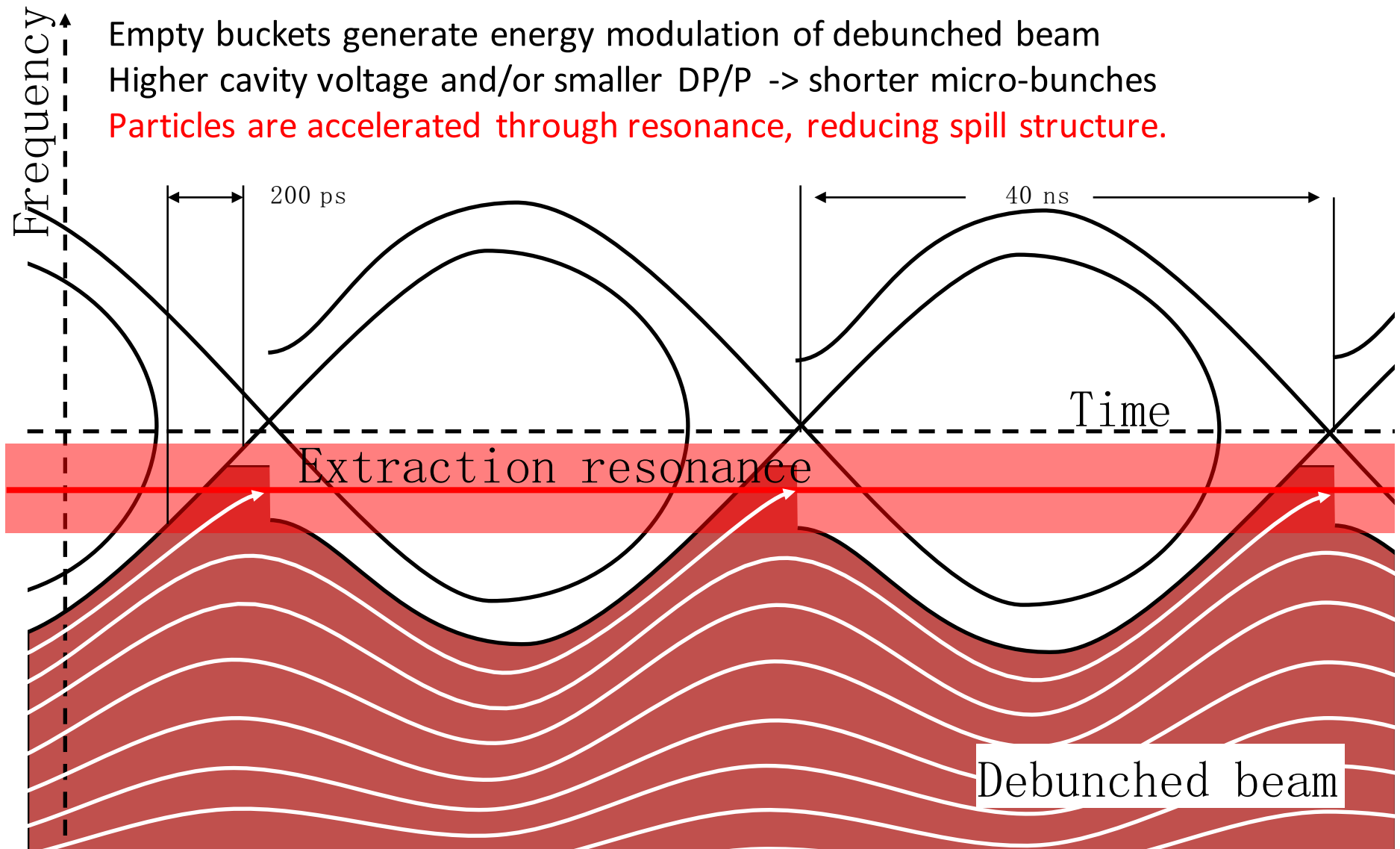
Worry's/Conjectures?

How are such solitons formed, if that is what they are?

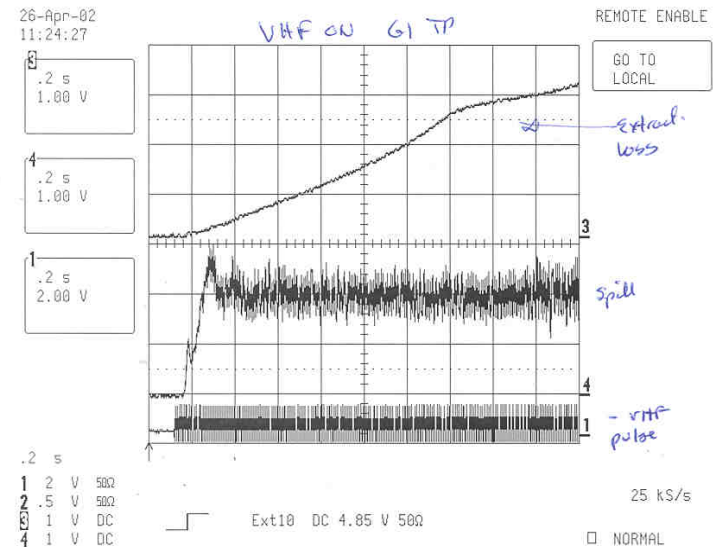
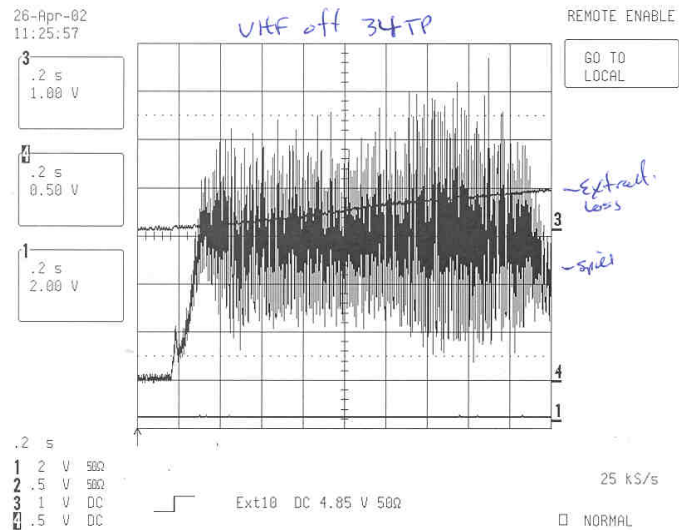
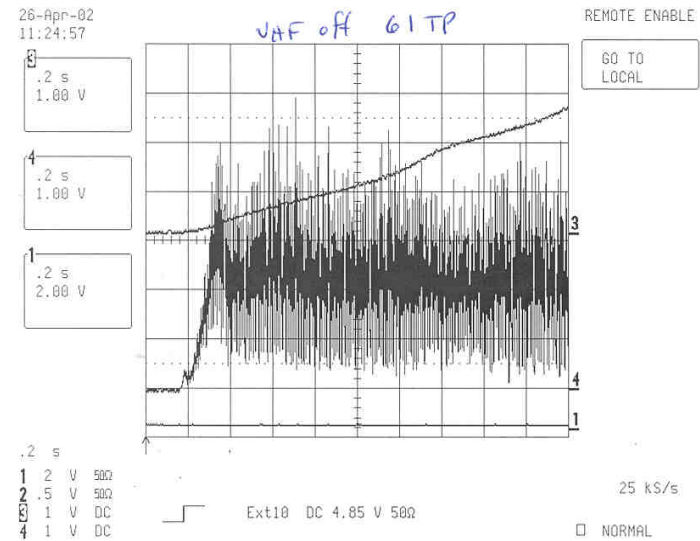
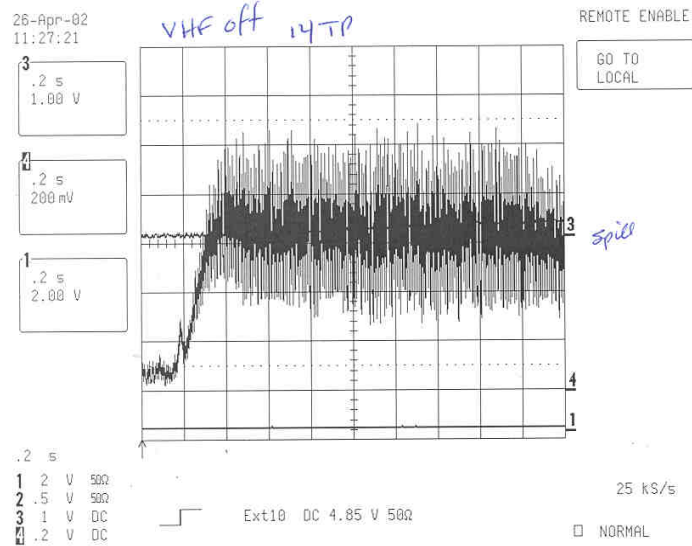
What kind of impedance drives the phenomena?

(Keil-Schnell just as/after RF voltage is dropped to zero?)

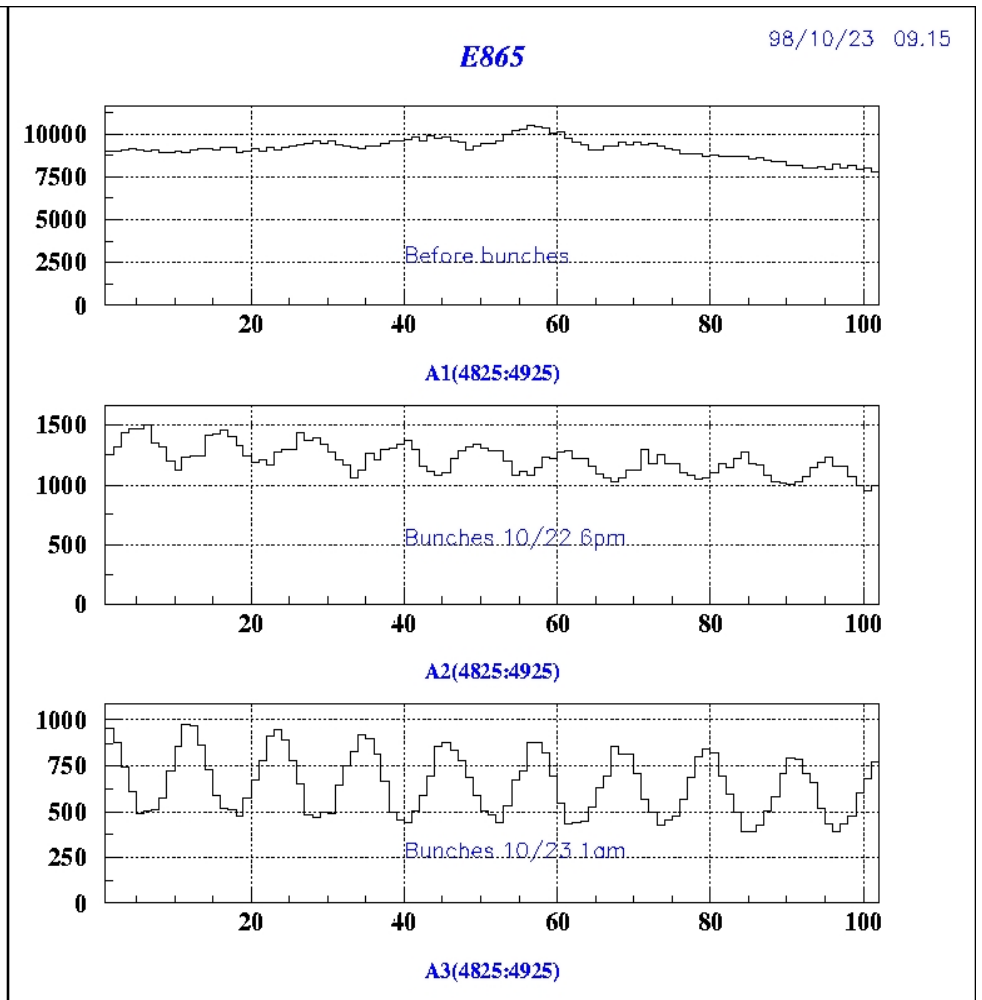
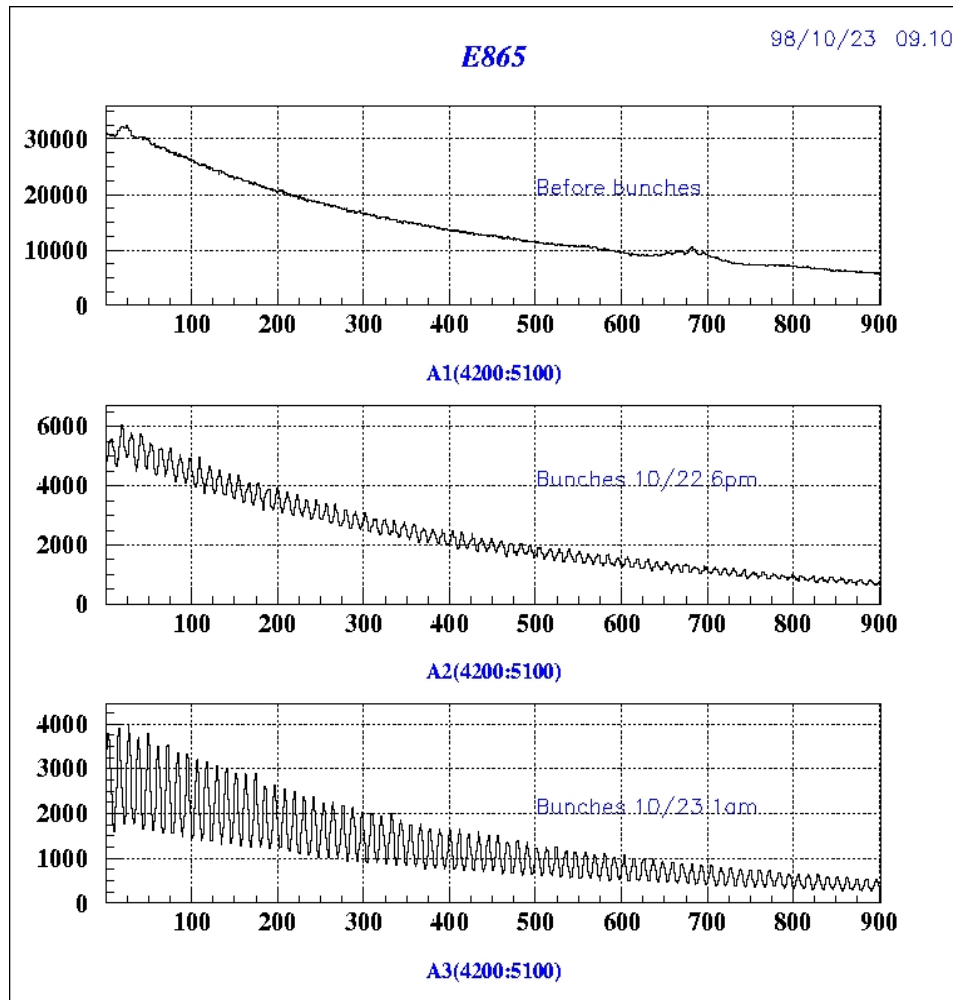
RF Phase Displacement slow extraction



Spill and Ripple



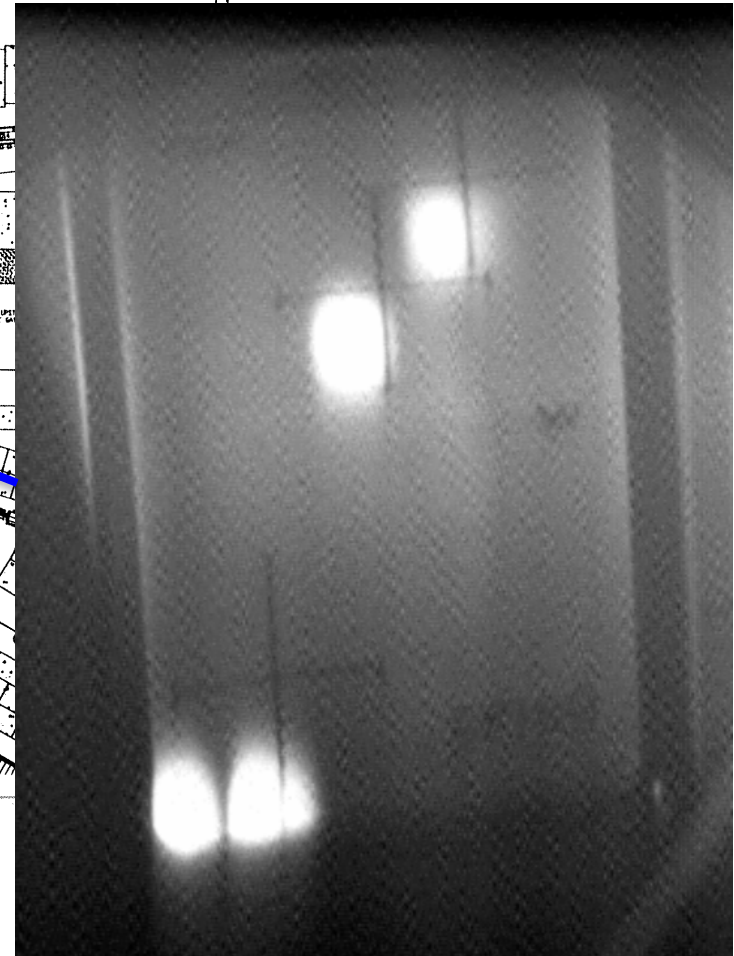
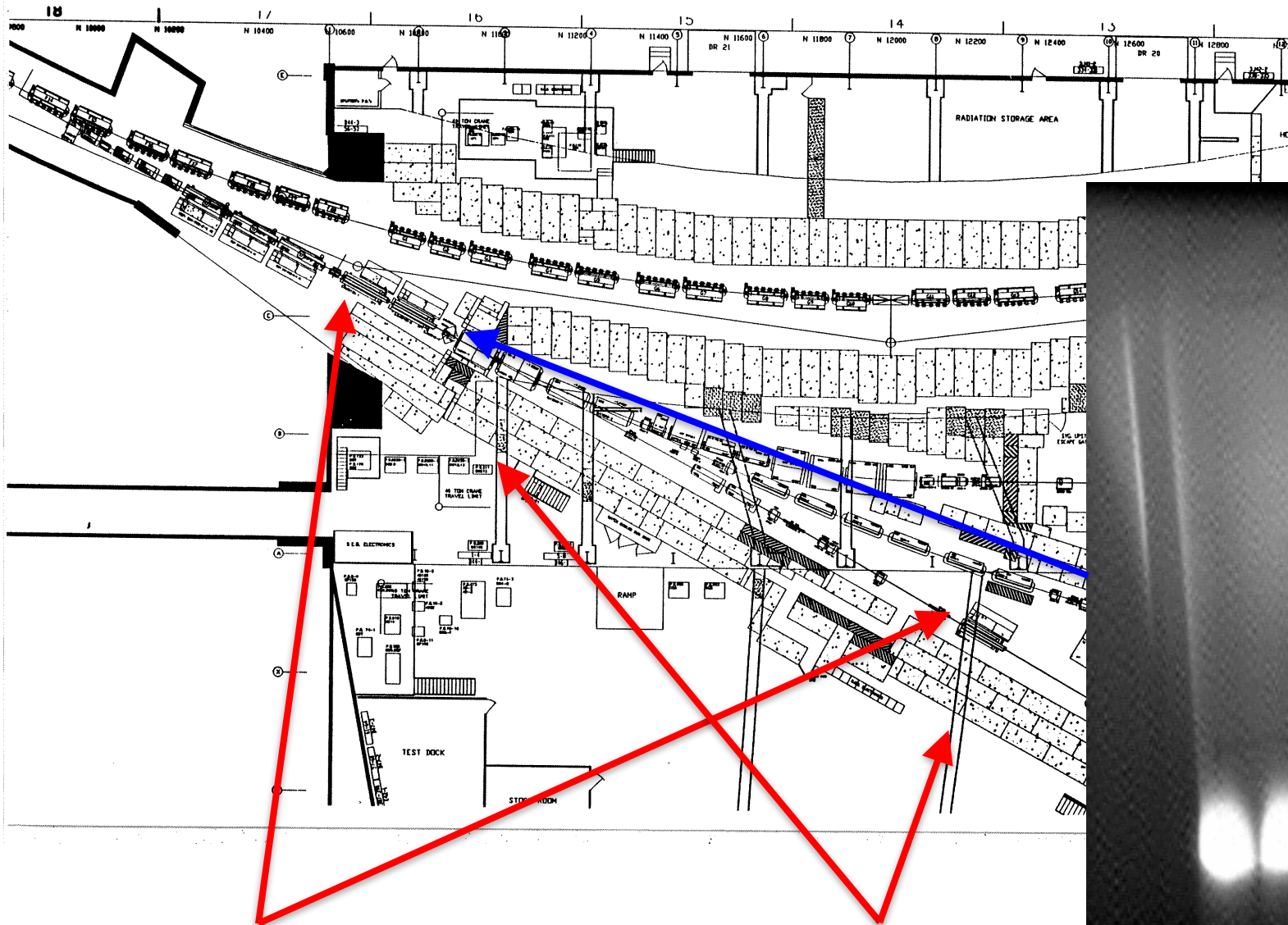
Beam Transport



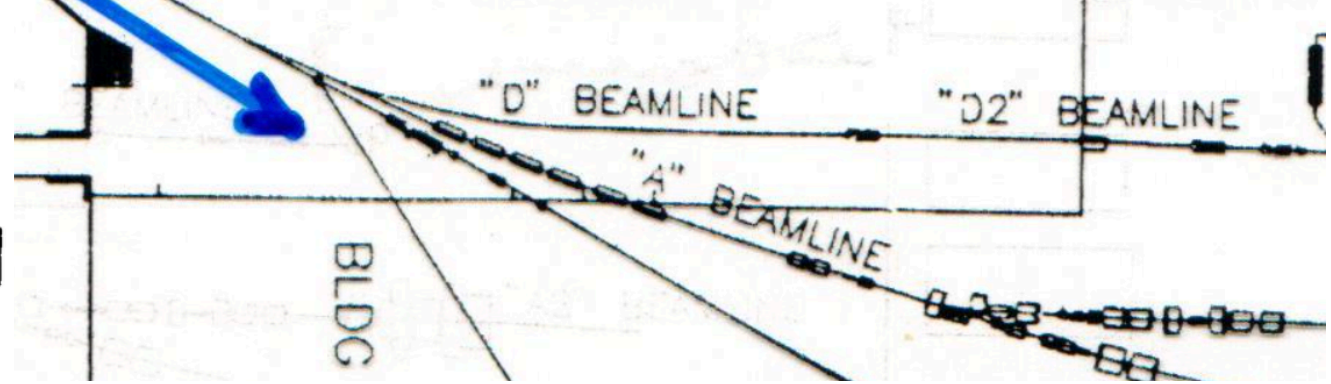
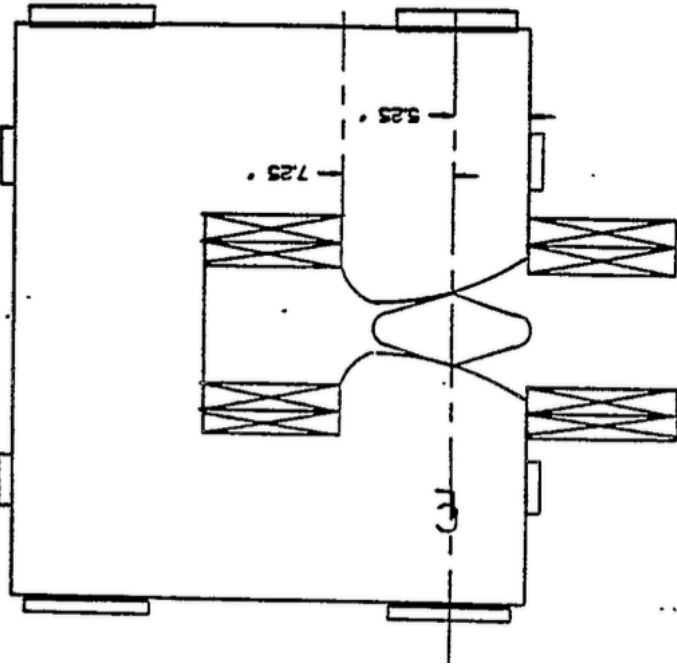
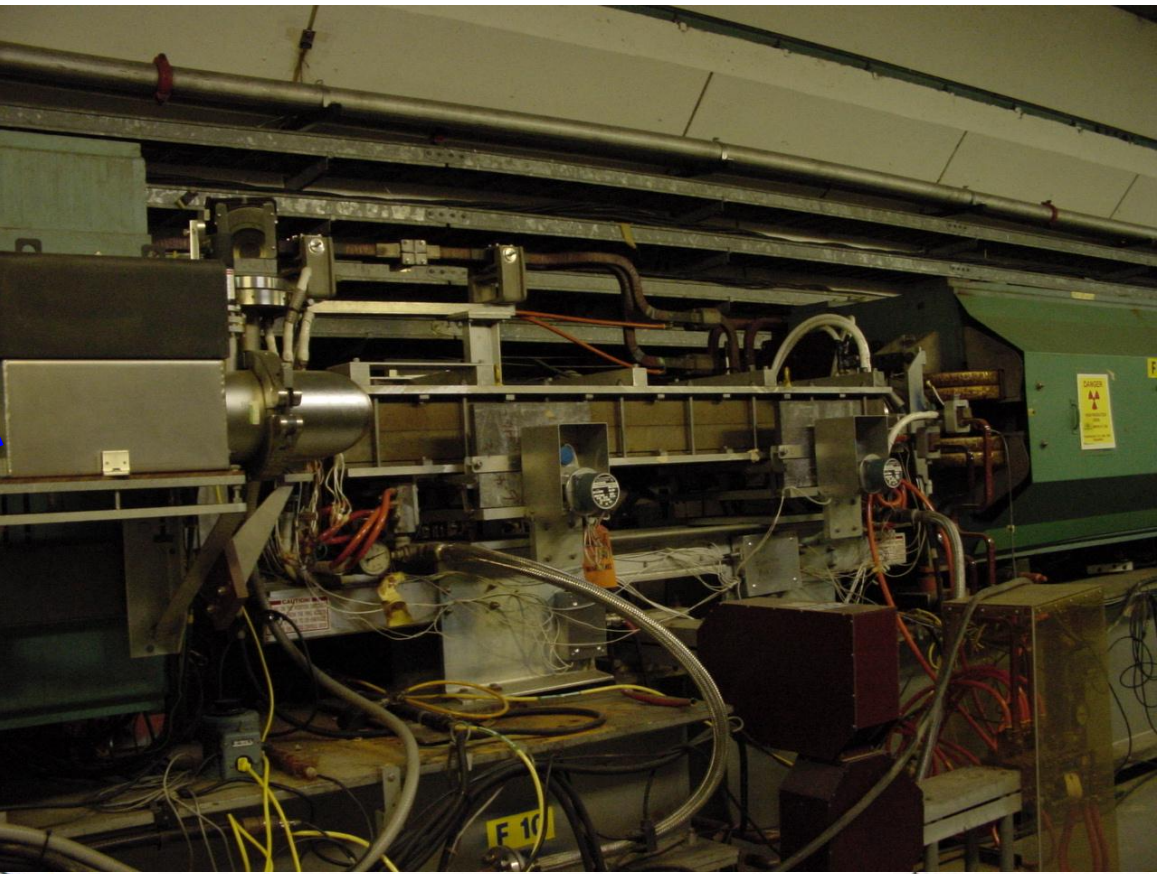
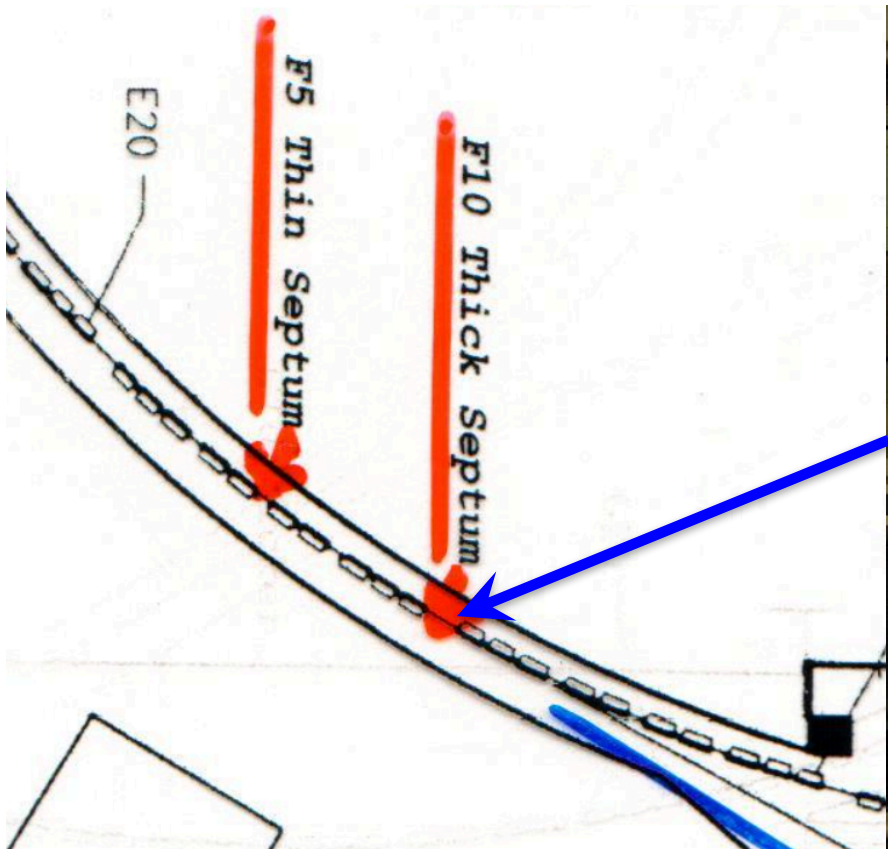
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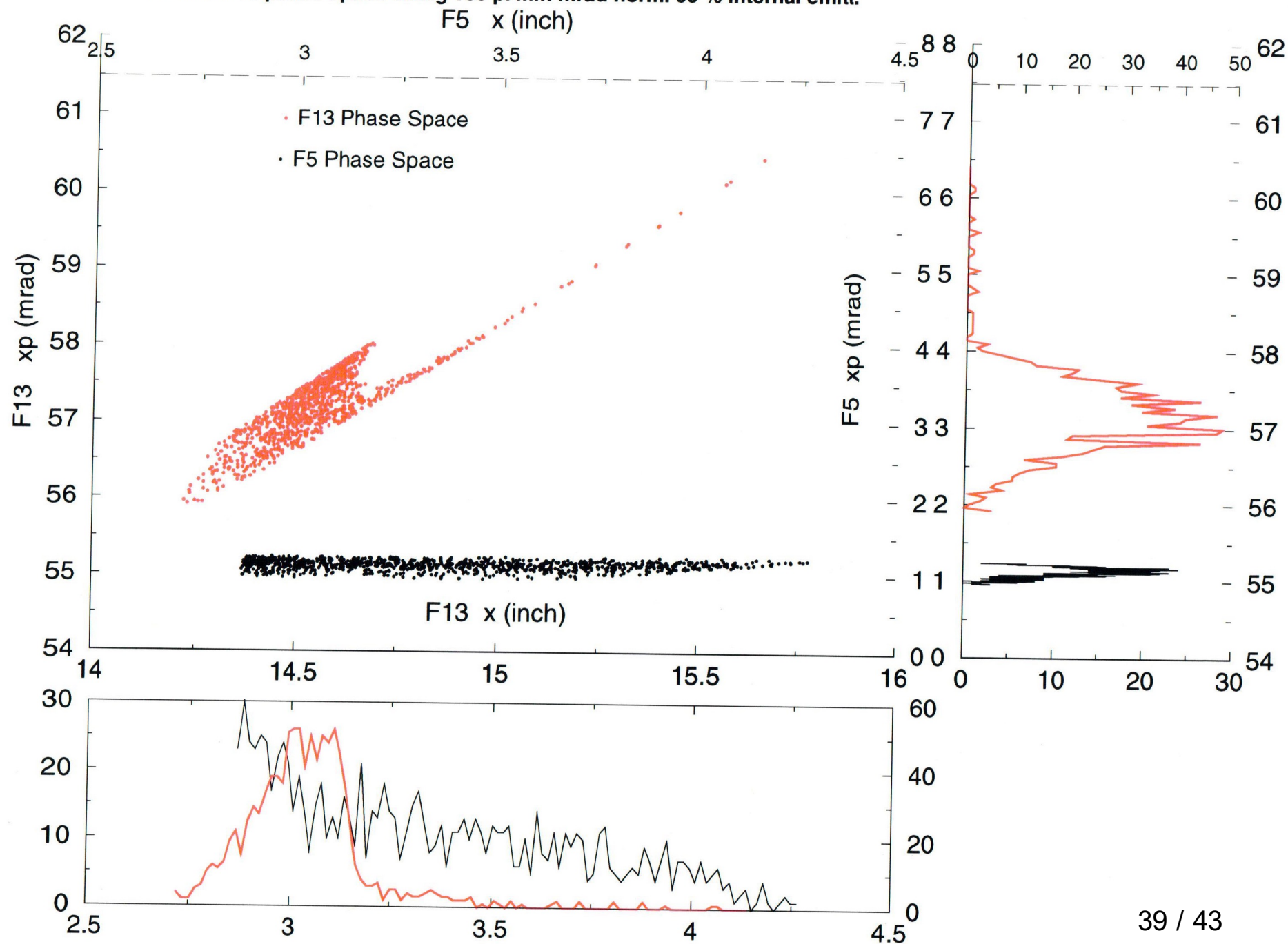
Switchyard: Two Post-Booster Problems



High Beam Losses & Outside Radiation Monitor Alarms/Trips

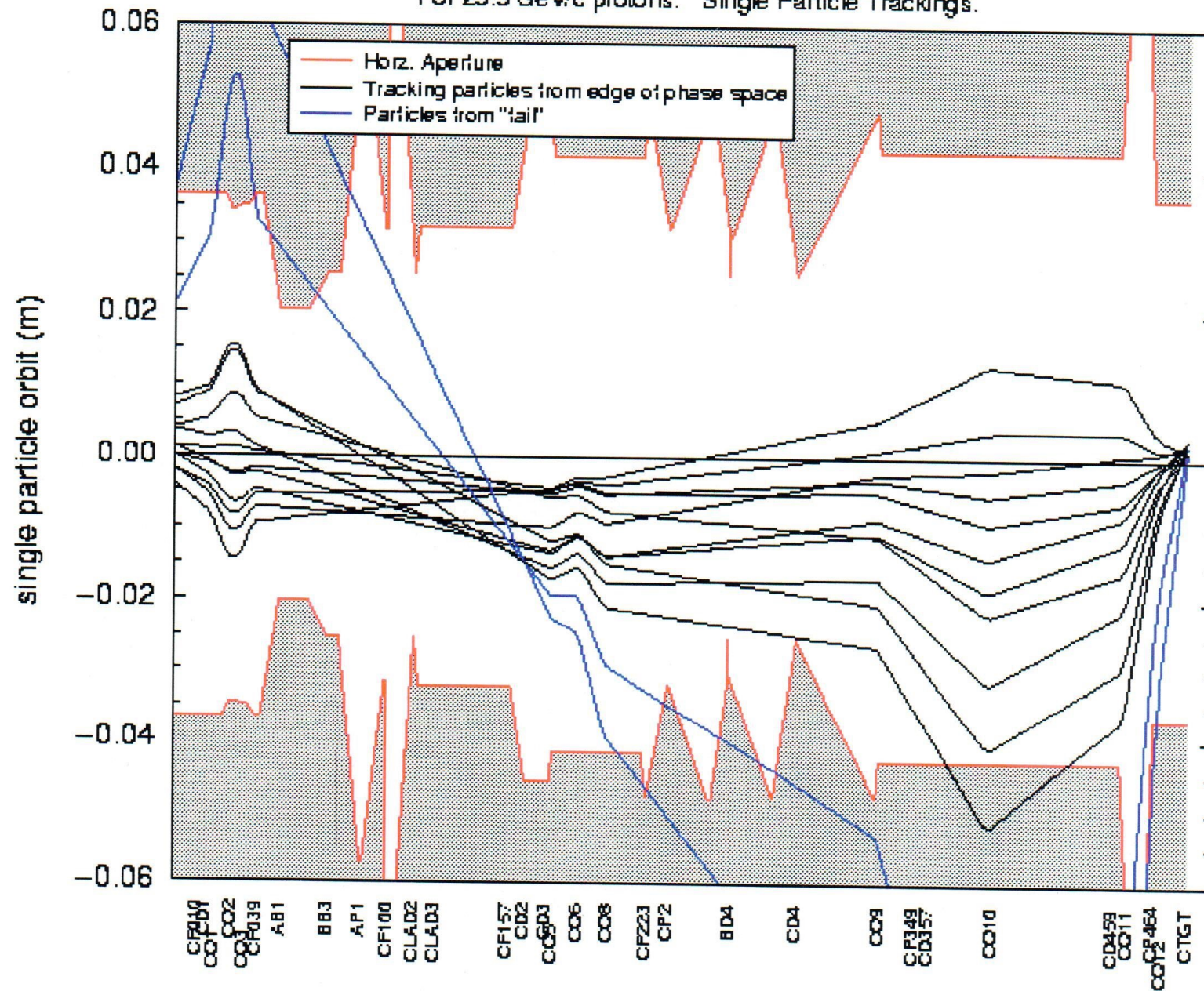


F5 and F13 phase space using 100 pi mm mrad norm. 95 % internal emitt.

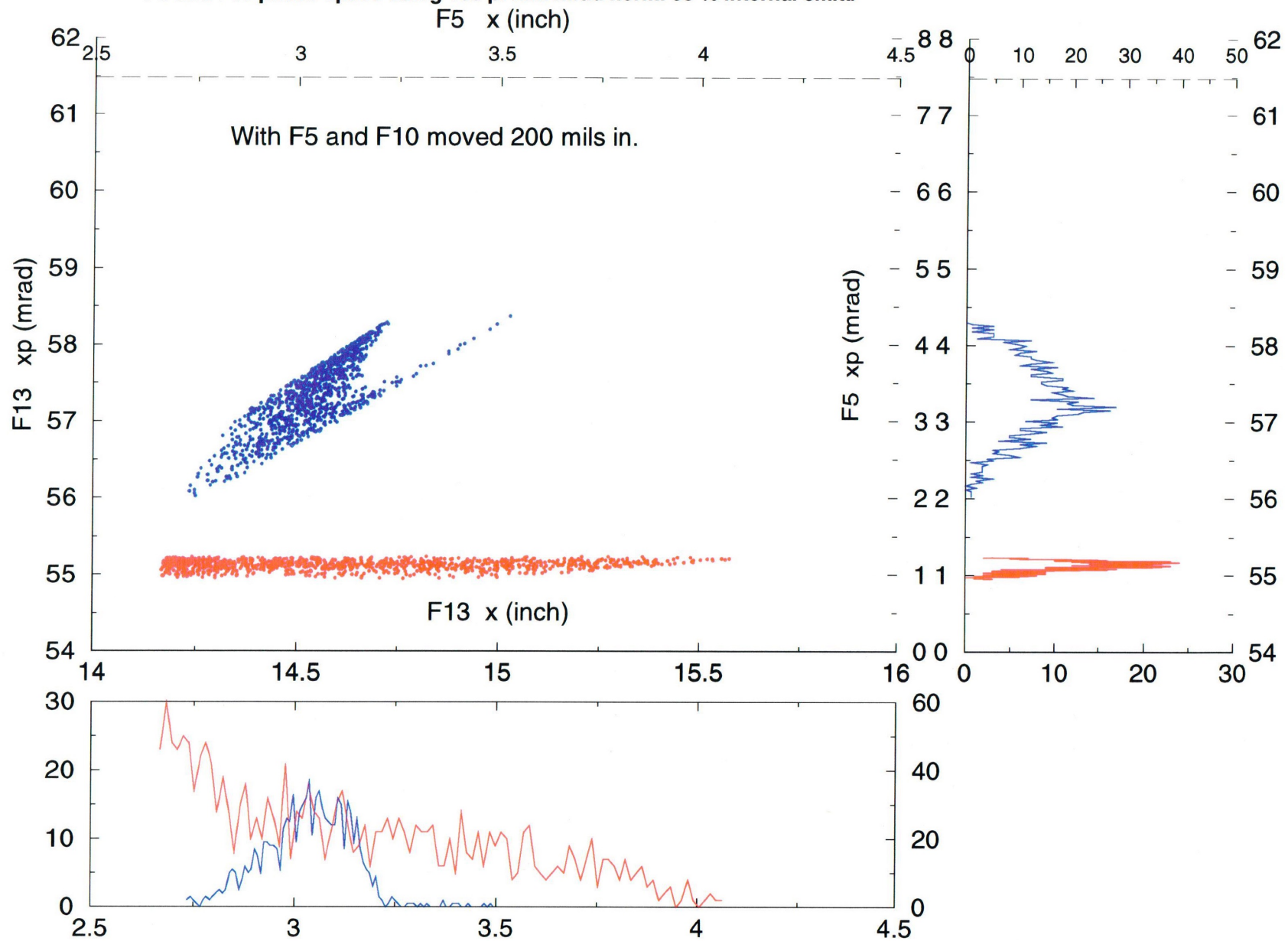


Mad Model of C Line

For 25.5 GeV/c protons. Single Particle Trackings.



F5 and F13 phase space using 100 pi mm mrad norm. 95 % internal emitt.



Measured emittance with High Intensity

Circulating Beam Emittances

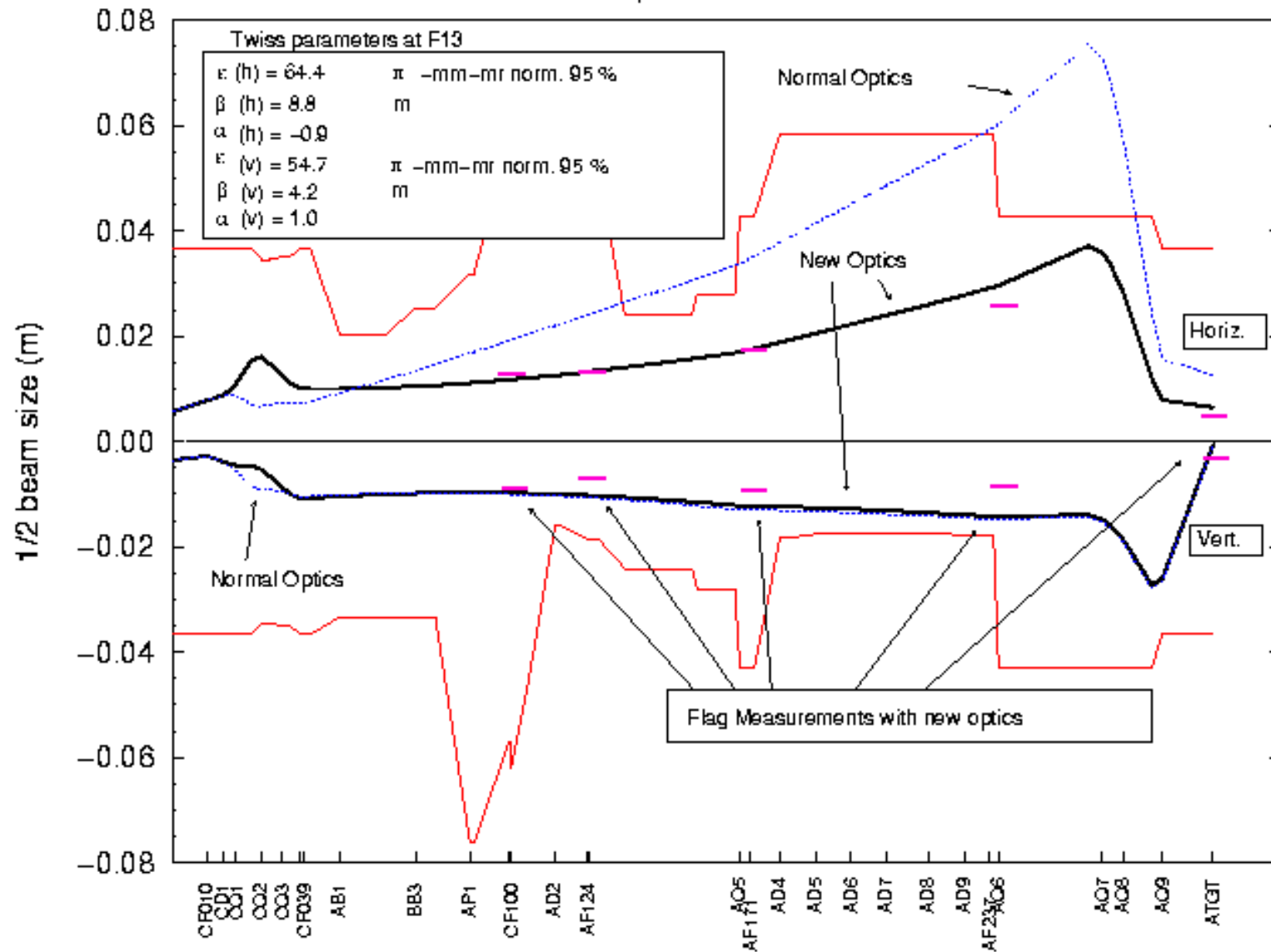
	$\epsilon_H^{99\%,N}$ (π mm-mrad)	$\epsilon_V^{99\%,N}$ (π mm-mrad)
Pre-Booster (1980) 200 MeV injection	49	60
Post-Booster (1997) 1.94 GeV injection	99	85

Extracted Beam Emittances

	$\epsilon_x^{95\%,N}$	β_x [m]	α_x	$\epsilon_y^{95\%,N}$	β_y [m]	α_y
1980	31.9	57.6	-6.64	38.8	3.25	0.87
1997	64.4	8.77	-0.92	54.7	4.18	1.01

Beam Transport

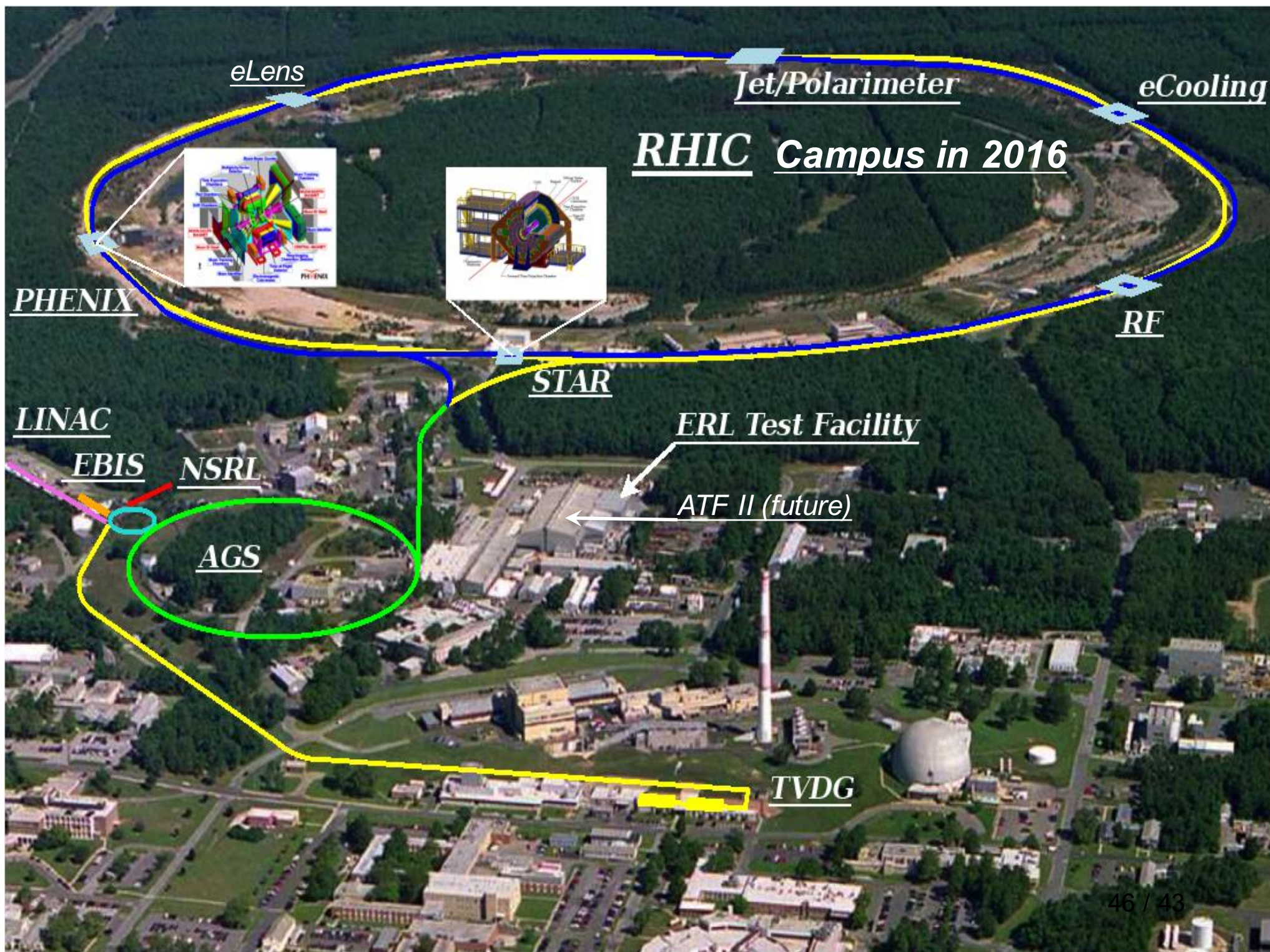
For 25.2 GeV/c protons 5/96 Measured Emitt.



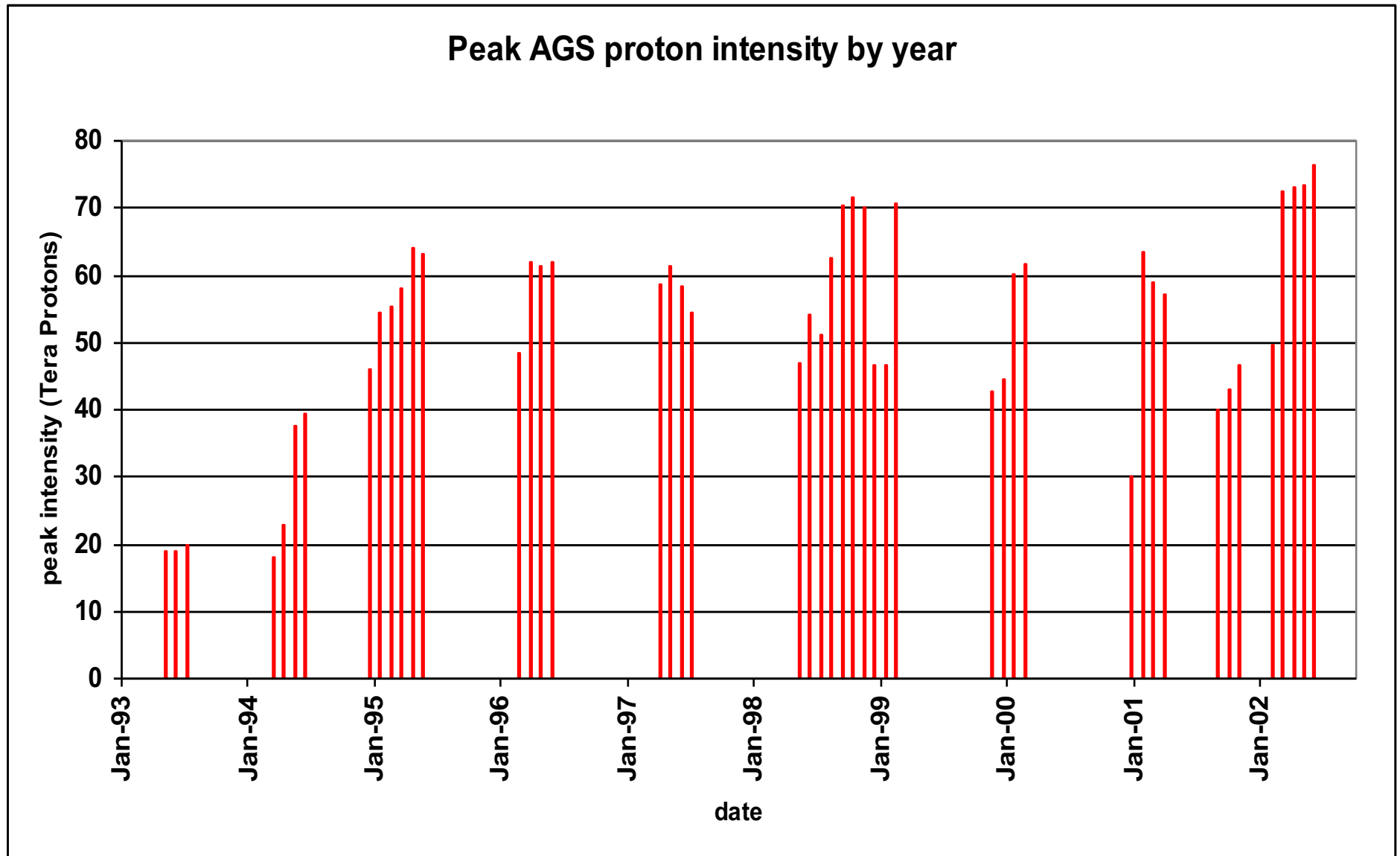
Summary

1. High Intensity History & Experience with the AGS SEB spans 35 years
2. Longitudinal Phase Space Dilution to reduce peak current
3. Collective Effects on Losses and Spill Structure
4. Positive Vertical Chromaticity was required
5. Positive Horizontal Chromaticity was needed at high intensity for further reducing inefficiency – but not implemented
6. RF Phase Displacement using a high frequency RF cavity was important for achieving low ripple, high duty factor beam spills
7. Electrostatic septum current increased over time/int. intensity
8. Tails/Halo created losses
9. Booster brought higher intensity, but also brought larger emittance beams, requiring a change in the switchyard optics.

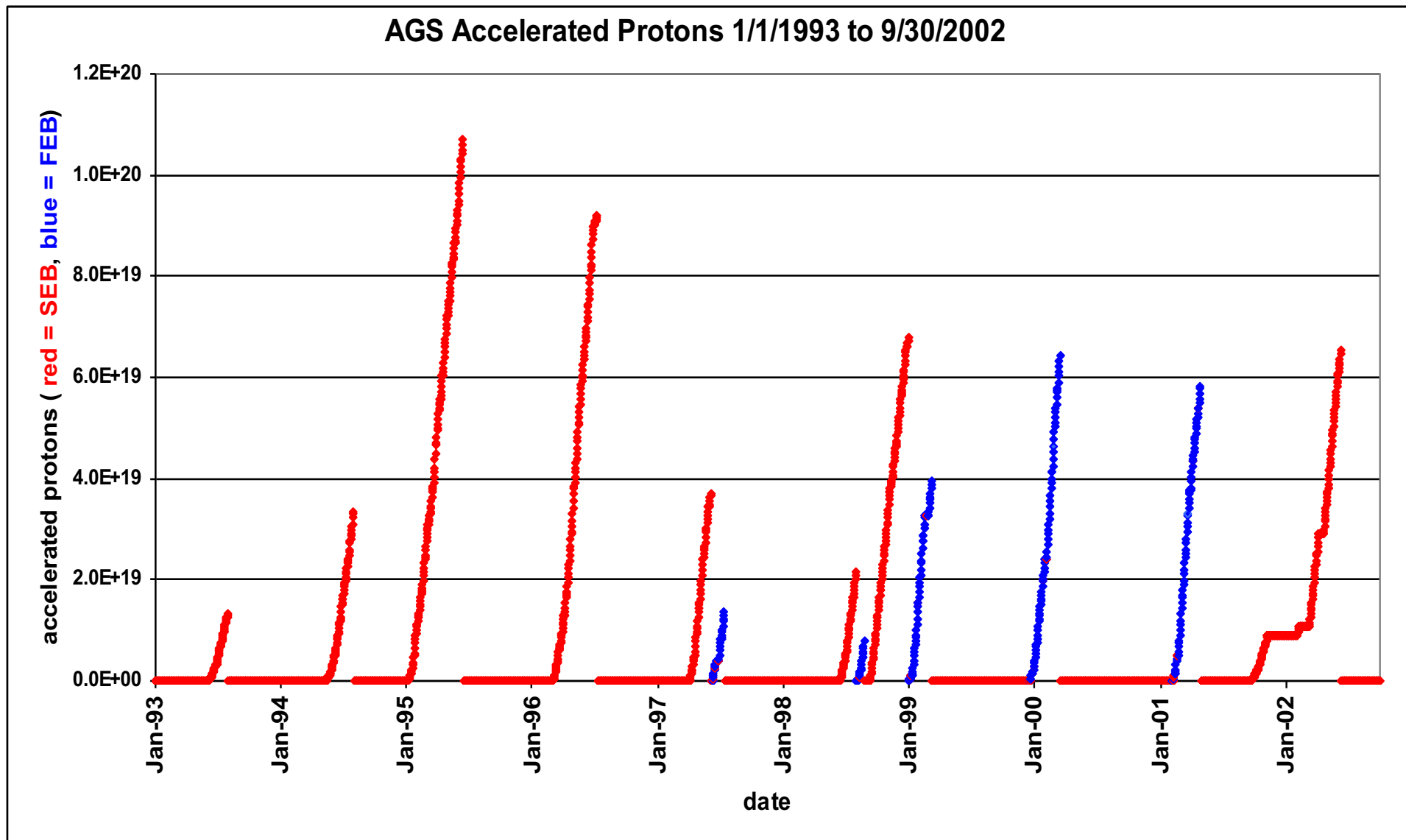
Backup Slides



Peak Intensities by Year



Integrated Intensity per Run



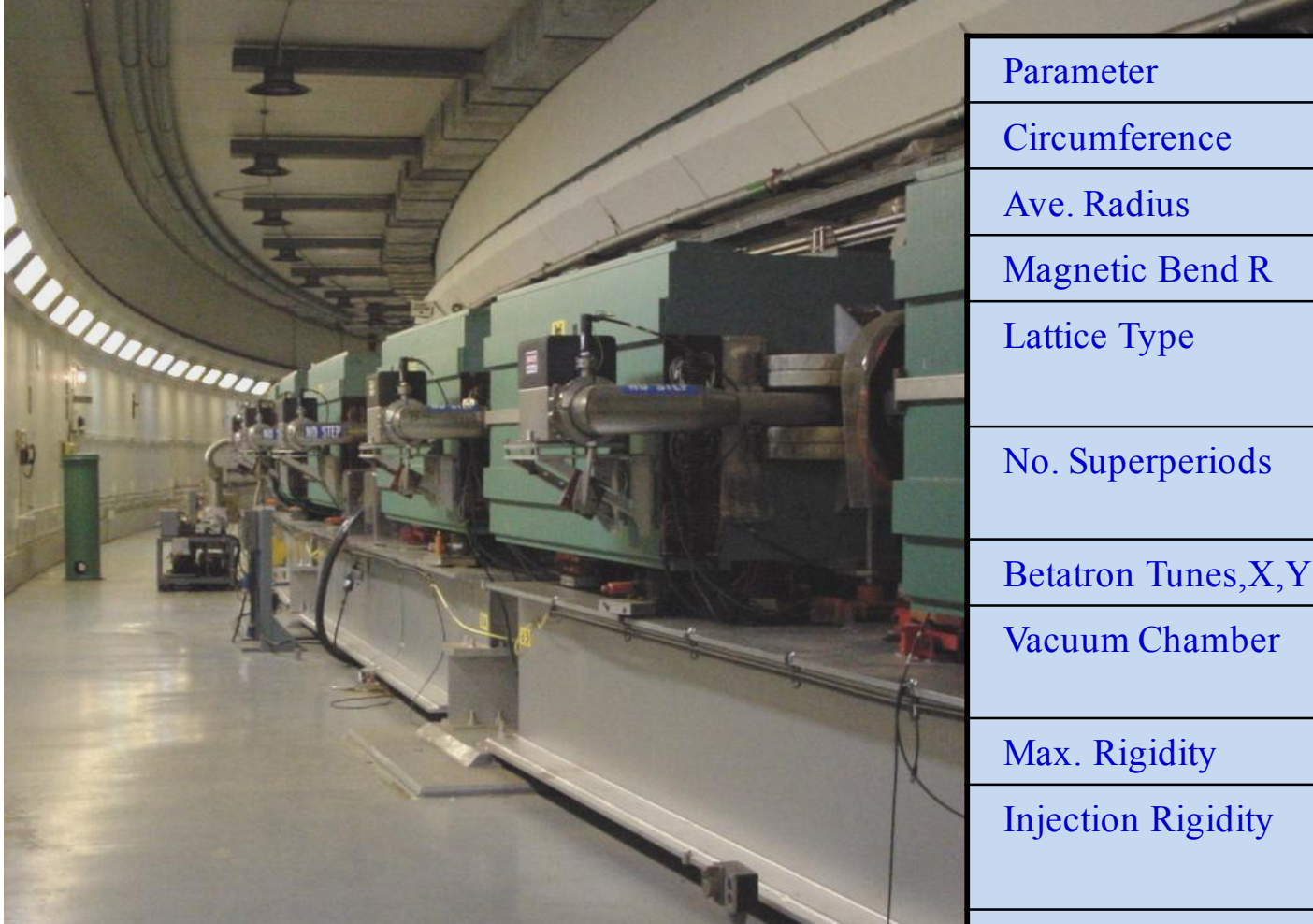
Sample of Physics program from 1998

AGS Beams, July 98

Beam	GeV/c	$\delta p/p$ (% fwhm)	Prod. Angle (deg)	$\Delta\Omega$ (msr)	Flux / 10^{13} 24 GeV/c protons on target						GeV/c	Purity	Remarks
					K^+	K^-	p	\bar{p}	π^+	π^-			
<i>Separated Charged Particle Beams</i>													
C4	≤ 0.83	4	0	12.0	4.6×10^6	1.5×10^6	1.5×10^9	1.0×10^6	6.0×10^9	6.0×10^9	0.80	$\pi^+/K^+ = 0.4$	L = 18 m – "LESBIII" $\sim 1 \times 10^6$ stopped $K^+/10^{13}$ protons
C6,C8	≤ 0.75	5	5	10.0	1.0×10^6	3.3×10^5	3.3×10^8	4.6×10^4	2.0×10^9	2.0×10^9	0.70	$\pi^-/K^- = 5$ $\pi^+/K^+ = 1$	L = 15 m – "LESBII"
D6	≤ 1.9	6	5	1.6	5.5×10^6	2.3×10^6	3.0×10^8	1.1×10^6	4.9×10^8	4.1×10^8	1.80	$\pi^-/K^- = 0.8$ $\pi^-/\bar{p} = .07$	L = 31 m – "2GEV"
<i>Unseparated Charged Particle Beams</i>													
A1*	5–28	3	0	0.2	1.9×10^6	2.9×10^4	5.0×10^9	2.3×10^3	3.0×10^7	1.0×10^7	18		L = 130 m to MPS – "HEUB"
A2	< 6.5	5	3.5	0.75	5.8×10^7	1.9×10^7	6.9×10^8	6.3×10^6	1.3×10^9	8.8×10^8	6		L = 34 m – "6GEV"
A3*	1–28	4	0	0.1			6.0×10^8		1.0×10^8	4.0×10^7	14		Primarily HI "OR" with A1
B1*	5–28	3	0	0.05			3.0×10^8		3.0×10^7	2.0×10^7	14		HI/Test Beam "OR" with B5
B1'	0.5–28	8	3	.001			3.0×10^4		6.0×10^4	4.0×10^4	5		L = 56 m – Test Beam
B2	< 9	5	6	0.5	3.4×10^5	1.2×10^5	8.5×10^6	9.5×10^4	1.2×10^7	9.0×10^7	4		L = 40 m – Test Beam
C1	1–20	5	0	0.8	3.0×10^7	3.5×10^6	1.0×10^9	0.7×10^6	3.5×10^8	1.6×10^8	13		L = 100 m – "OR" with C5
C5*	1–28	2	0	0.15			1.0×10^8				13		L = 81 m – "OR" with C1
<i>Neutral Beam</i>													
B5	2–20		1–4.5	0.1			K_L^0 flux = 1.3×10^8 @ 3.75°				2–20	$n/K_L^0 = 20$	L = 10 m – "OR" with B1
<i>Muon Channel</i>													
D2	0.025–0.15	9 (π) 30 (μ)	135 (π)	24 (π)			μ^+ flux = 2.0×10^6 Surface μ^+ flux = 2.0×10^6						L = 12 m Inactive, not yet commissioned
<i>Neutrino Beam</i>													
U							ν flux = $2.0 \times 10^{10}/m^2$ (Wide Band) $\bar{\nu}$ flux = $1.4 \times 10^{10}/m^2$ (Wide Band)						Not Presently Available FEB Flux avg. over 1.5 m R. $\langle E \rangle = 1.4$ GeV/c ² Wide Band
<i>g–2 π–μ Transfer Line</i>													
V1	< 3.0	0.6	0				π^+ flux = 1.7×10^8 μ^+ flux = 7×10^5				3.0		L = 120, for injection to g–2 ring commissioned in 1996

* These 0^0 beam lines can be used for full energy polarized protons and/or heavy ion beams

AGS Parameters



Parameter	Value
Circumference	807.091 m
Ave. Radius	128.453 m
Magnetic Bend R	85.3785 m
Lattice Type	Combined Function, FODO
No. Superperiods	12 (20 magnets each)
Betatron Tunes,X,Y	8.72, 8.80
Vacuum Chamber	78 x 173 mm Dipoles
Max. Rigidity	110 Tm
Injection Rigidity	9.076 Tm (1.94 GeV protons)
Acceleration Rate (max)	2.5 T/s

Booster & AGS Performance: FEB

Imposed limits to lost beam power to maintain hands-on maintenance (ALARA).

- AGS FEB operation, 2.77 s cycle AGS cycle time, 6 Booster cycles

Achieved **30 Tp/sec, Booster Late** & **22 Tp/sec, AGS Late**

Table: FEB 10 Pulse Ave. Data (best performance, not sustainable operation)

	Intensity (Tp/cycle)	Efficiency (%)	Beam Loss (Tp/cycle)	ALARA (Tp/cycle)	Loss (kW)	Loss/m (W/m)
Linac	115	-	-	-	-	-
Booster Injected	89	77	27	27.7	0.31	1.5
Booster Extracted	83	93	6	9.2	0.33	1.6
AGS Injected	66	78	18	16.3	2.0	2.5**
Before Transition	62.3	94	3.7	1.5	0.9	1.1
After Transition	61.6	99	0.6	2.3	0.2	0.2
AGS Late	61.4	99.5	0.3	0.8	0.25	0.3

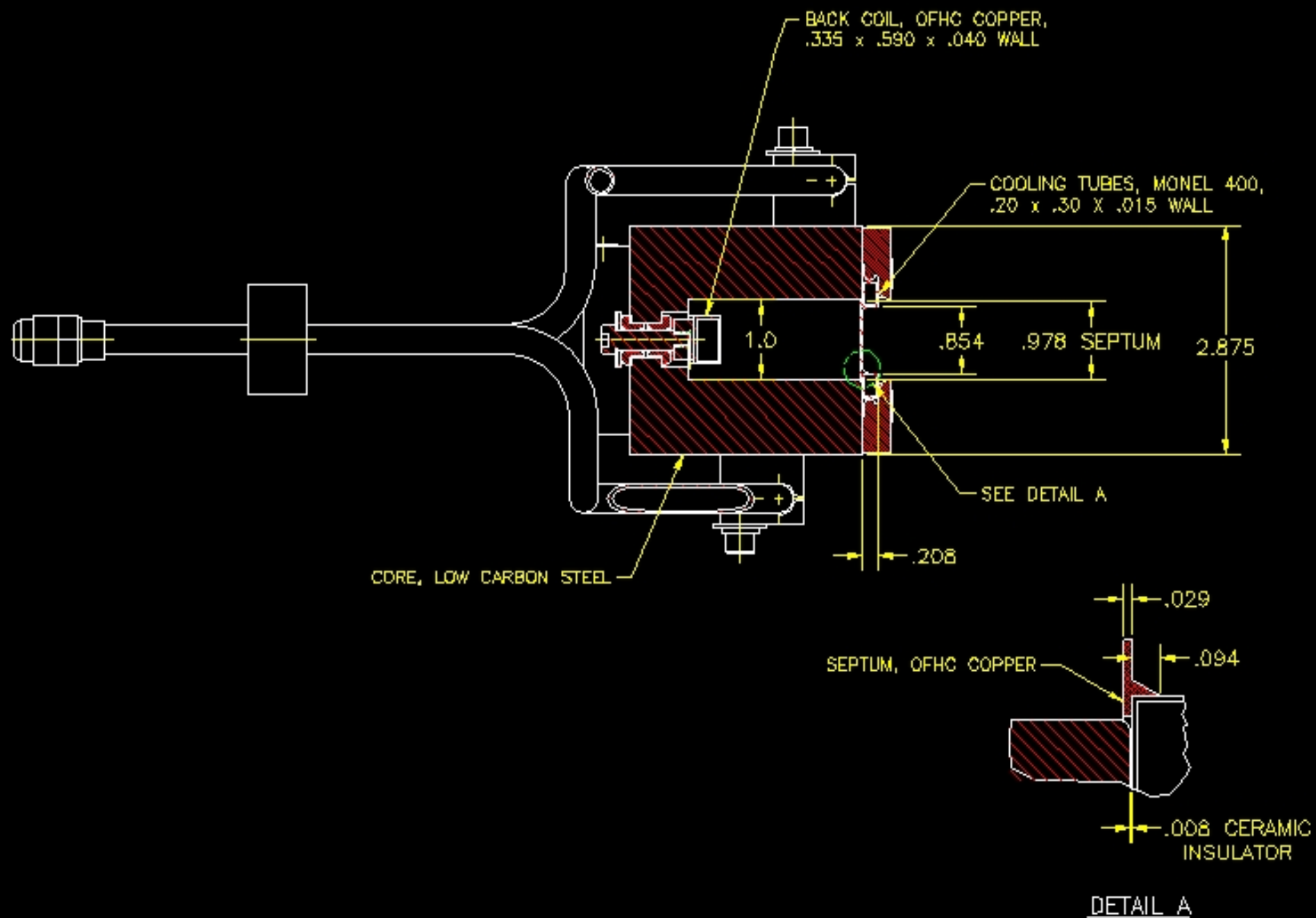
** assumed lost in AGS

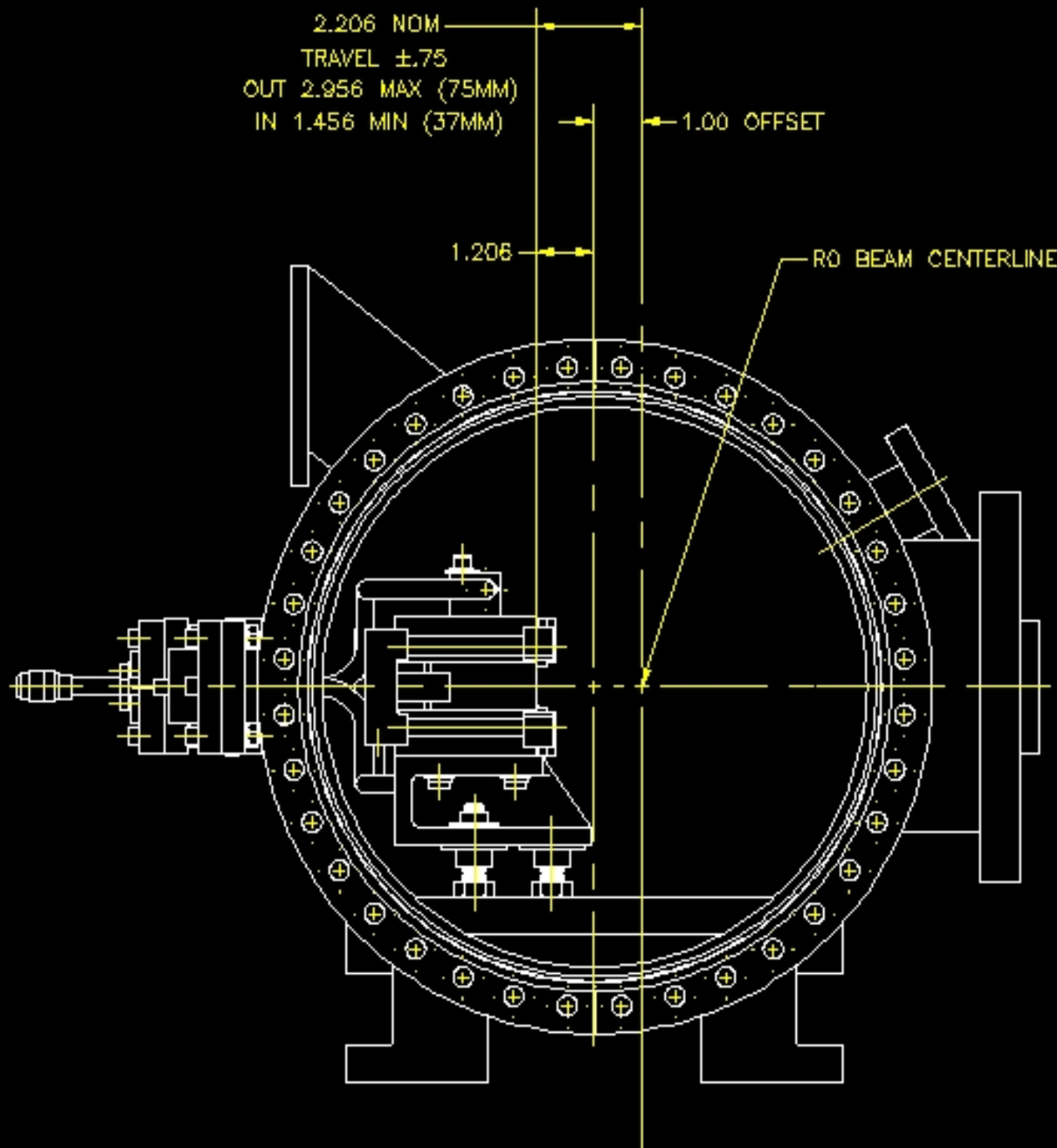
Naming Conventions & P.S. Families

- 12 Superperiods, labeled A – L; 20 magnets/superperiod
 - 12 Long magnets = 94 inches, bend ~ 1.6 degrees
 - 8 Short magnets = 79 inches, bend ~ 1.4 degrees
 - All are combined function, strong focusing
- 2 Tune control families
 - Horiz. Focusing – 1/superperiod at #17 straight sections
 - Vert. Focusing – 1/superperiod at #3 straight sections
- 2 Chromaticity control families
 - Horiz. – 1/superperiod at #13 straight sections
 - Vert. – 1/superperiod at #7 straight sections
- Skew quadrupoles – 1 string, 6 magnets every other superperiod
 - B17, D17, F17, H17, J17, L17
- Drive sextupoles – 1 string (+ - + -) = don't affect chrom.
- Orbit deformation bumps – two sets, using backleg windings
 - One for electrostatic septum
 - One for two magnet septa

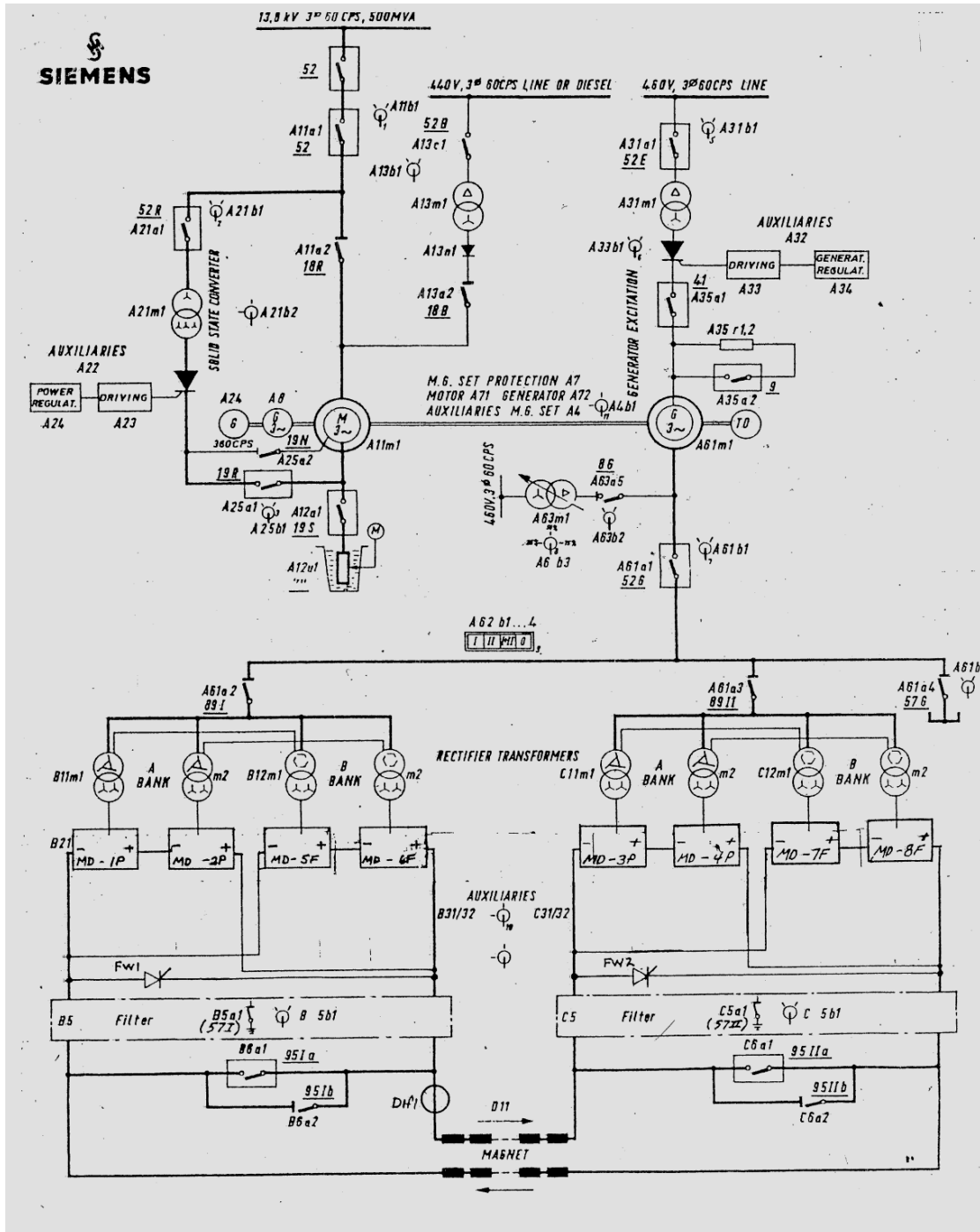
Slow Extraction Parameters

Parameter	Value	Units
Peak Intensity	76.0	10^{12} protons/pulse
Extraction Efficiency	97-98	%
Rep Period/Flatop Length	4-8/2-6	Seconds
Spill Lengths	1.8 – 5.8	Seconds
Working Point	8.667 / 8.78	Horiz./Vert. Tune
Chromaticity	-2.5 / 0.05	Horiz./Vert. Chrom.
Extraction Momentum	25.5	GeV/c



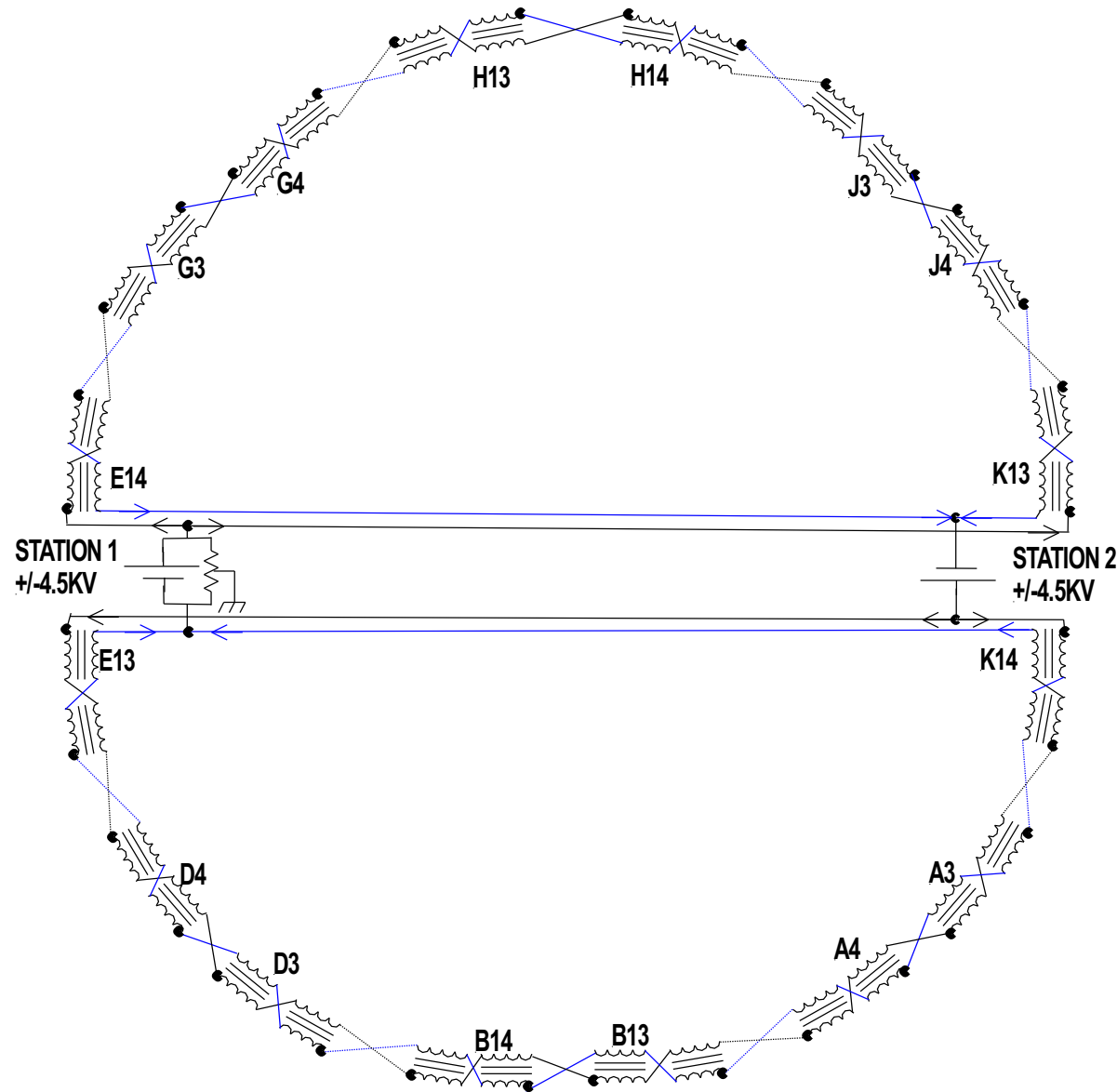


AGS MMPS BLOCK DIAGRAM



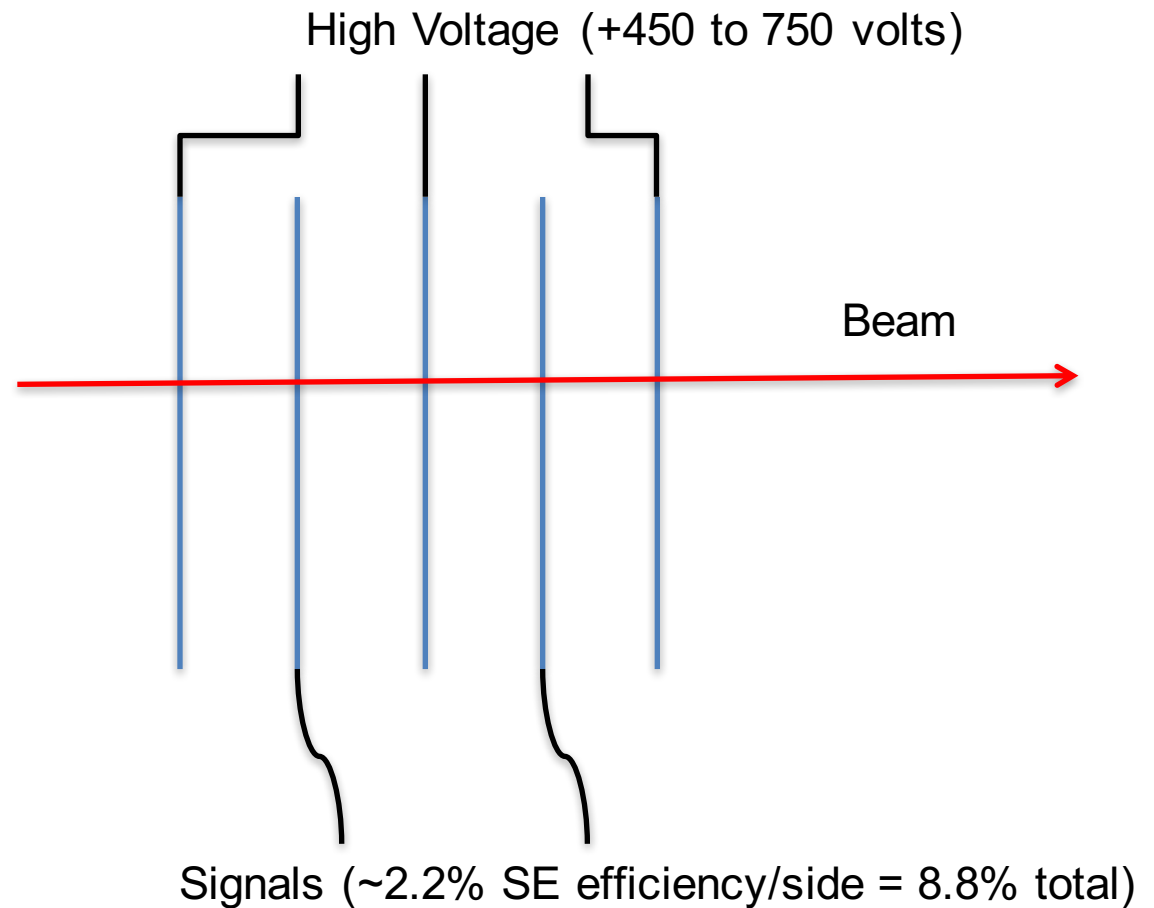
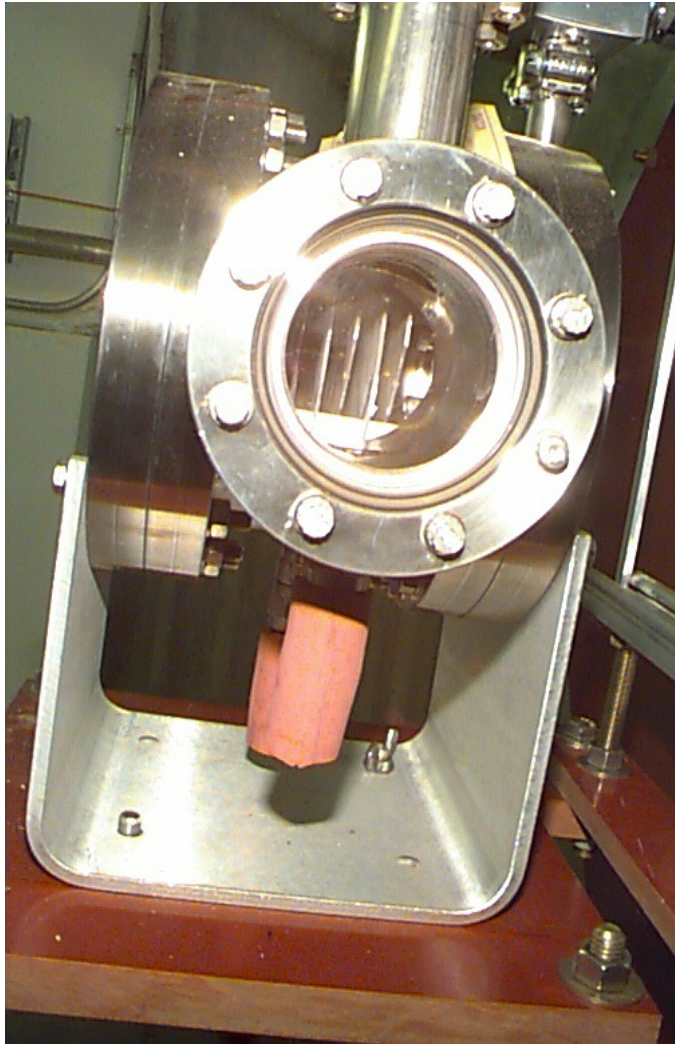
- AGS MMPS 6000 Amps, ± 9000 Volts (SCR) power supply.
- Maximum AGS magnets average power 5 MW.
- Two stations of power supplies ± 4500 Volts and 6000 Amps each.
- The grounding of the power supply is done in the middle of station 1 or 2 through a resistive network.
- With this grounding configuration, the maximum magnet voltage to ground will not exceed 2500 Volts.

AGS Magnet Power Supply Configuration.



- The AGS ring consists of 240 magnets hooked up in series.
- The total resistance R is 0.28 ohms and the total inductance L , is 0.8 henries.
- There are 12 super-periods, A through L, of 20 magnets each.

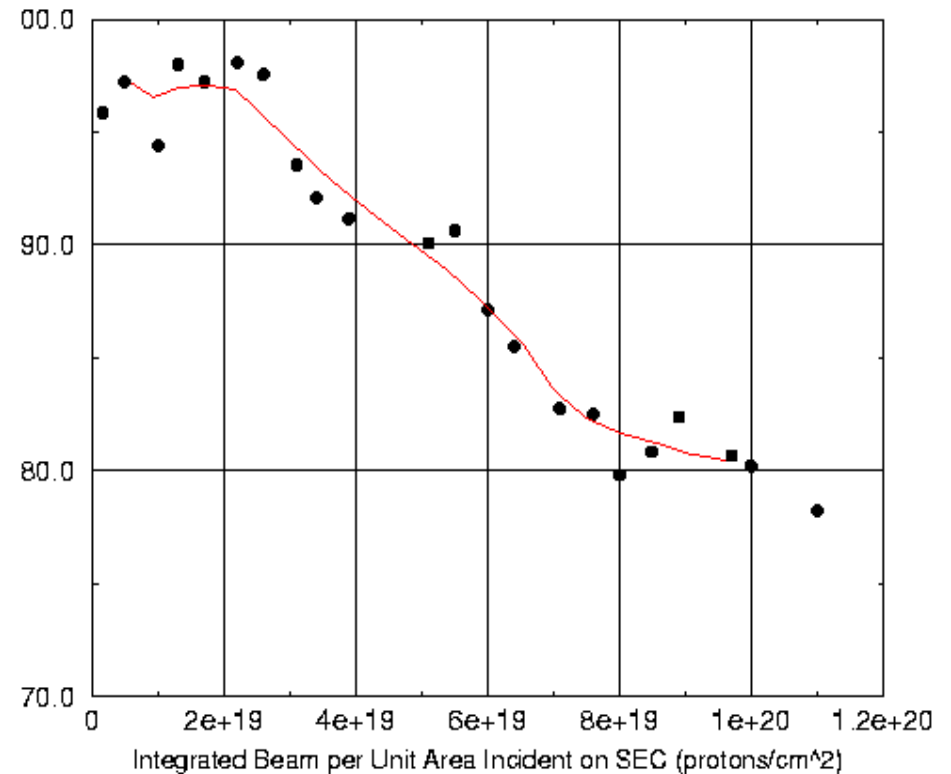
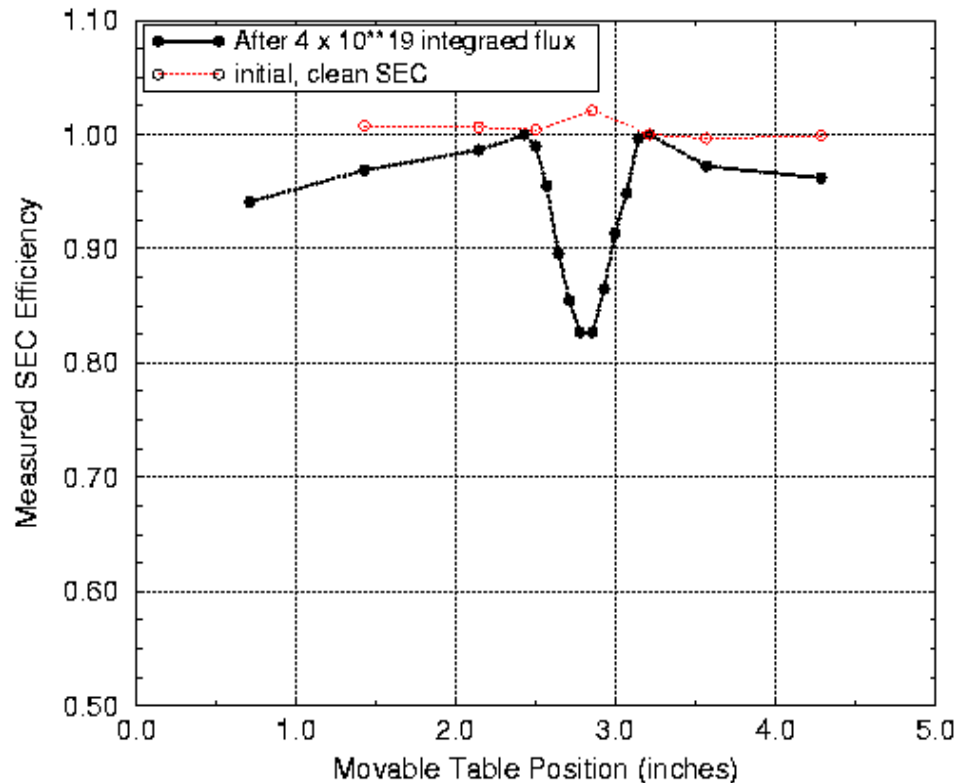
Measuring Extracted Beam Intensity

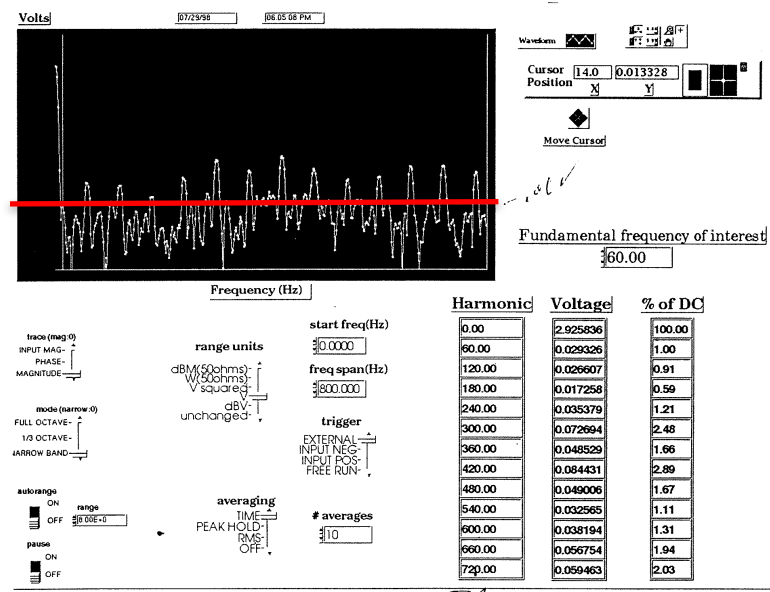
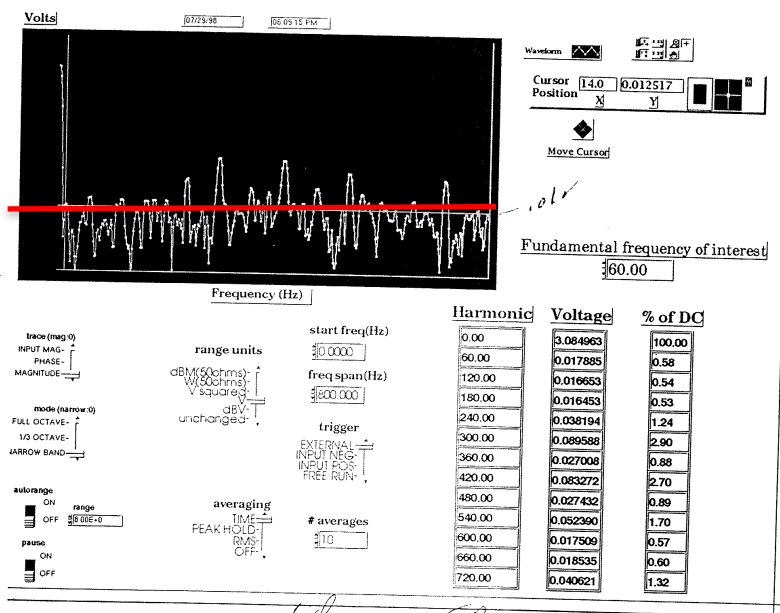
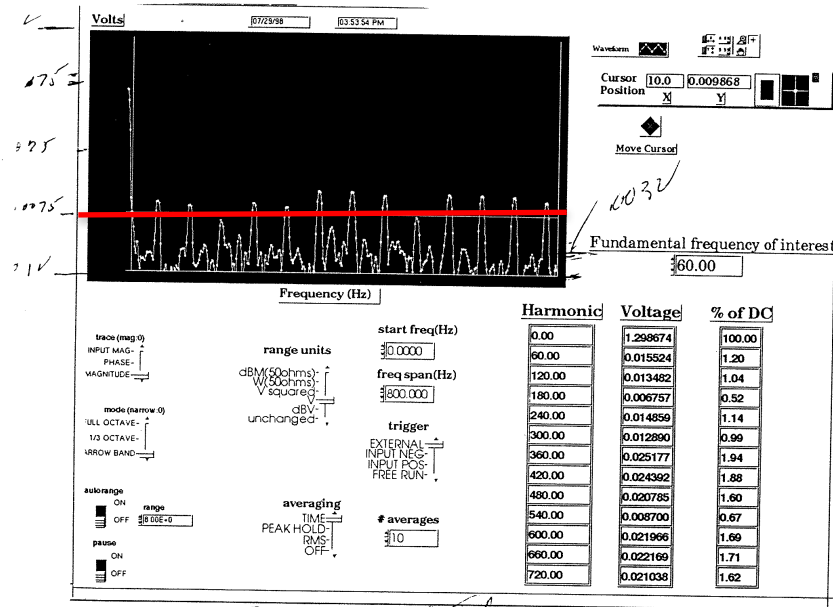
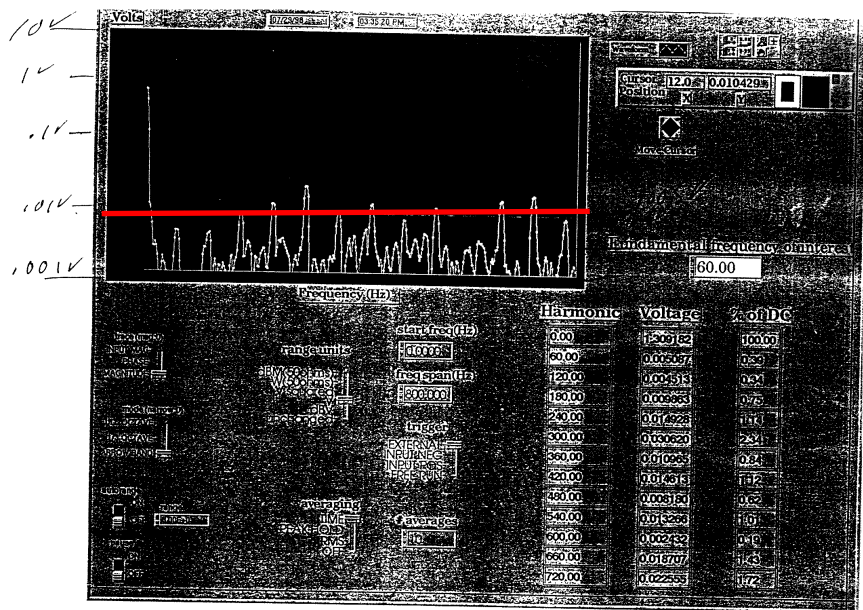


Secondary Emission Chambers

Measuring Extracted Beam Intensity

Secondary Emission degradation





Spill and Ripple

Time Structure Formalism

definitions:

Q = horizontal betatron tune

ξ = horizontal chromaticity = $\frac{dQ/Q}{dp/p}$

I_m = current in the Main Dipoles and Quadrupoles

N = number of particles ($\frac{dN}{dQ}$ represents the particle distribution in tune space

T = period over which particles are extracted

Low frequency duty factor:

$$D_f = \frac{[f_T S(t) dt]^2}{T f_T [S(t)]^2 dt} \Rightarrow \left(\frac{f_{av}}{f_{rms}}\right)^2 \text{ in general}$$

where

$$S(t) = \frac{dN}{dt} = \frac{dN}{dQ} \frac{dQ}{dt}$$

if there is no ripple,

$$S(t) = \frac{dN}{dQ} \dot{Q}_0$$

where \dot{Q}_0 is the rate at which particles move into resonance.

$$\dot{Q}_0 = \frac{Q\xi}{I_m} \frac{dI_m}{dt}$$

Spill and Ripple

If there is ripple on the magnet power supplies;

$$S(t) = \frac{dN}{dQ}(\dot{Q}_0 + \dot{Q}_v)$$

where \dot{Q}_v is the variations in the rate at which particles move into resonance.

$$\dot{Q}_v = \frac{Q\xi}{I_m L_m} \sum_h V_h$$

L_m is the total inductance of the main dipoles and quads and V_h is the sum of the 60 Hz harmonics amplitudes (in volts).

Reducing Time structure using RF Phase Displacement

$$S(t) = \frac{dN}{dQ} \dot{Q}_0 \left(1 + \frac{\dot{Q}_v}{\dot{Q}_0}\right)$$

For 1 particular frequency we can write the duty factor as

$$D_f = \frac{1}{1 + \frac{1}{2}\left(\frac{\dot{Q}_v}{\dot{Q}_0}\right)^2} = \frac{1}{1 + \frac{1}{2}\left(\frac{\omega \delta Q}{v_0}\right)^2}$$

where

ω = frequency

δQ = relative ampl. of that freq. in tune space

v_0 = speed that beam crosses resonance

$$v_0 = \frac{\Delta p}{p} \frac{1}{T}$$

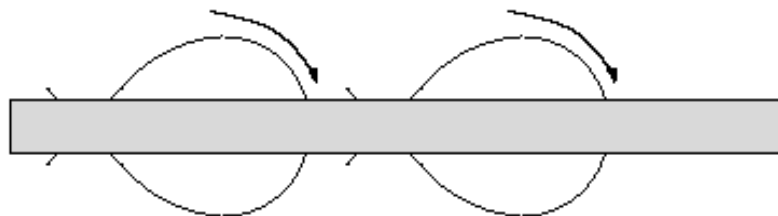
Spill and Ripple

D_f is increased by

1. decreasing δQ

2. increasing v_0

One way to increase v_0 is to increase $\frac{\Delta p}{p}$. To further increase it we use RF phase displacement, using a high frequency RF cavity. In this case RF buckets are centered on the resonance.



The buckets are empty and beam is forced between them.

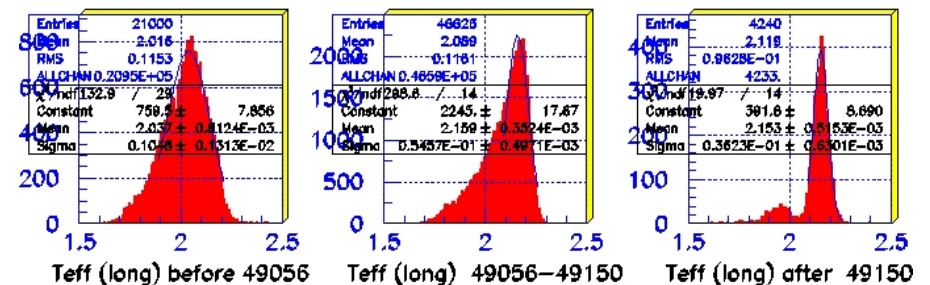
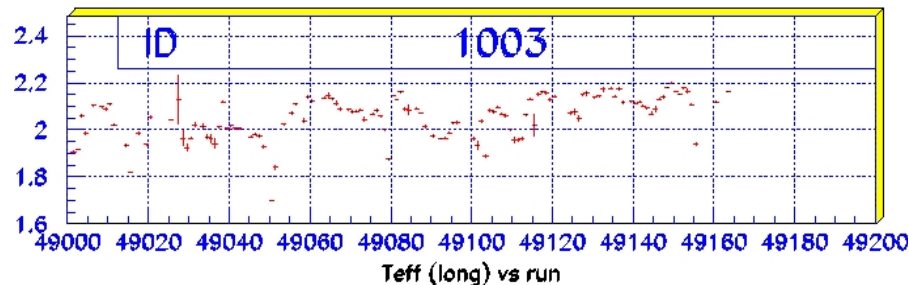
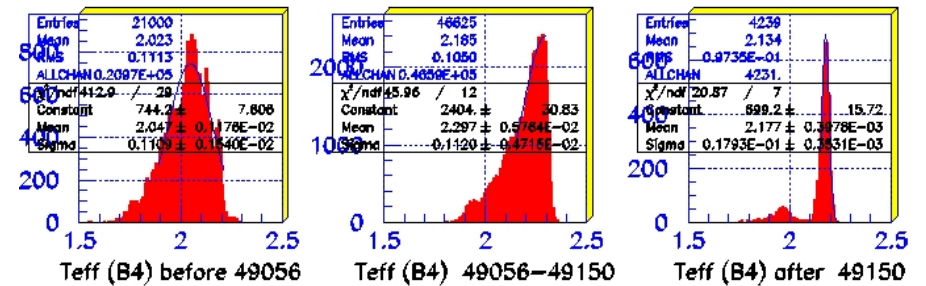
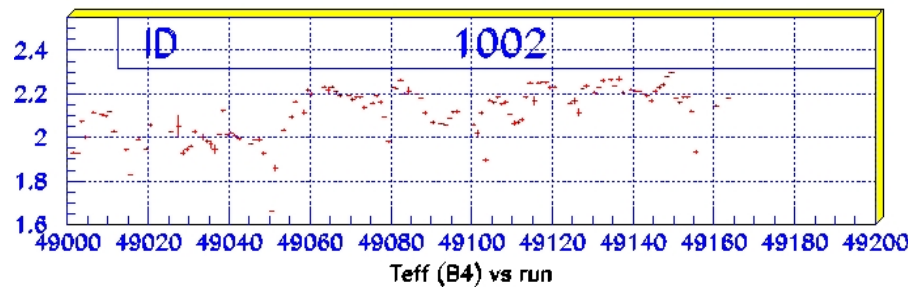
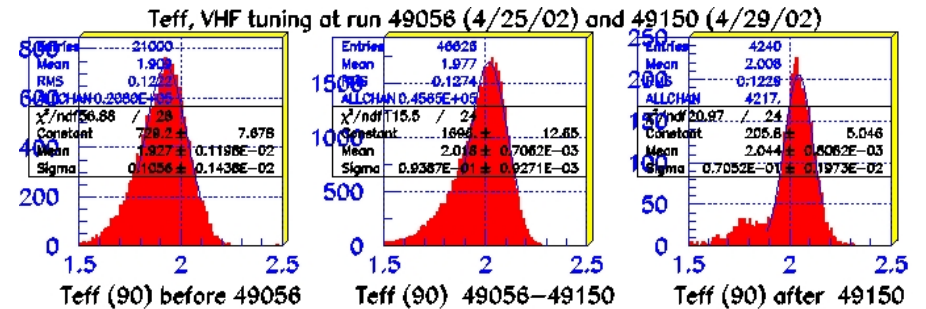
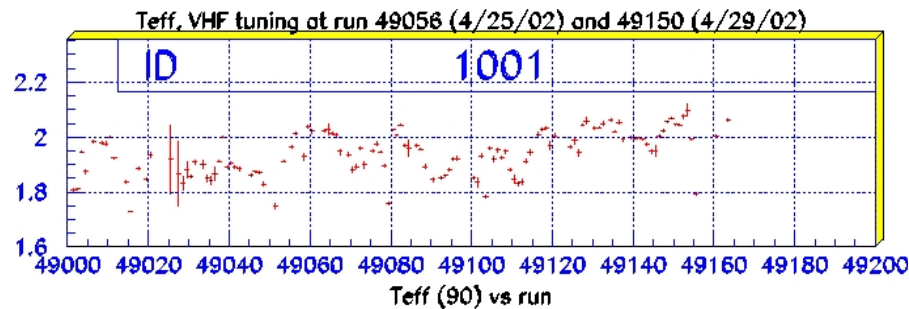
Now,

$$D_f = \frac{1}{1 + \frac{RB\rho T}{V\frac{\Delta p}{p}}(\omega\delta Q)^2}$$

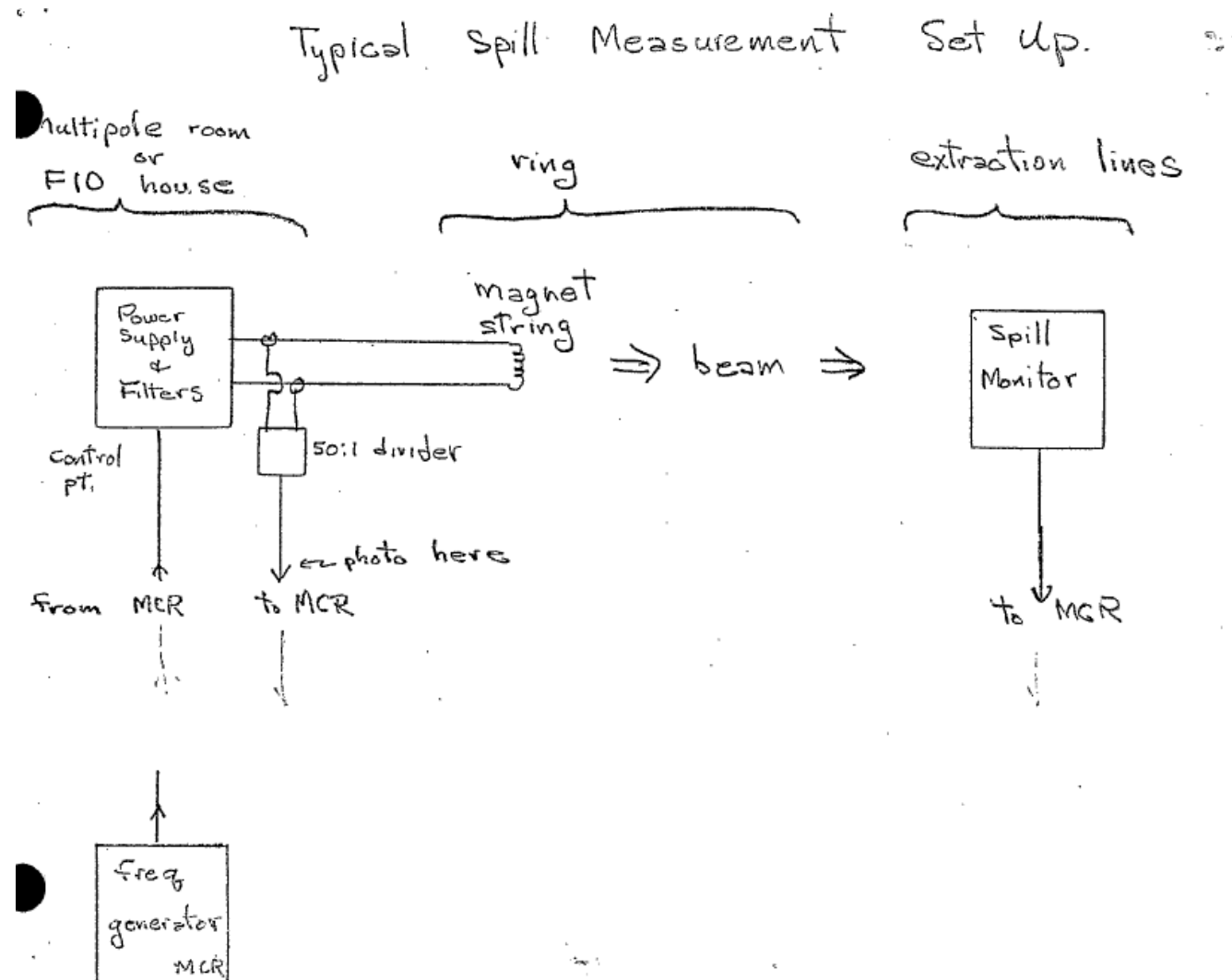
Without RF phase displacement, a 100 % modulated spill has $D_f = 0.67$. In this case,

$$\omega\delta Q \geq \frac{\Delta p}{p} \frac{1}{T}$$

Improved Effective Spill Length



Transfer Function Measurements



Transfer Function Measurements

