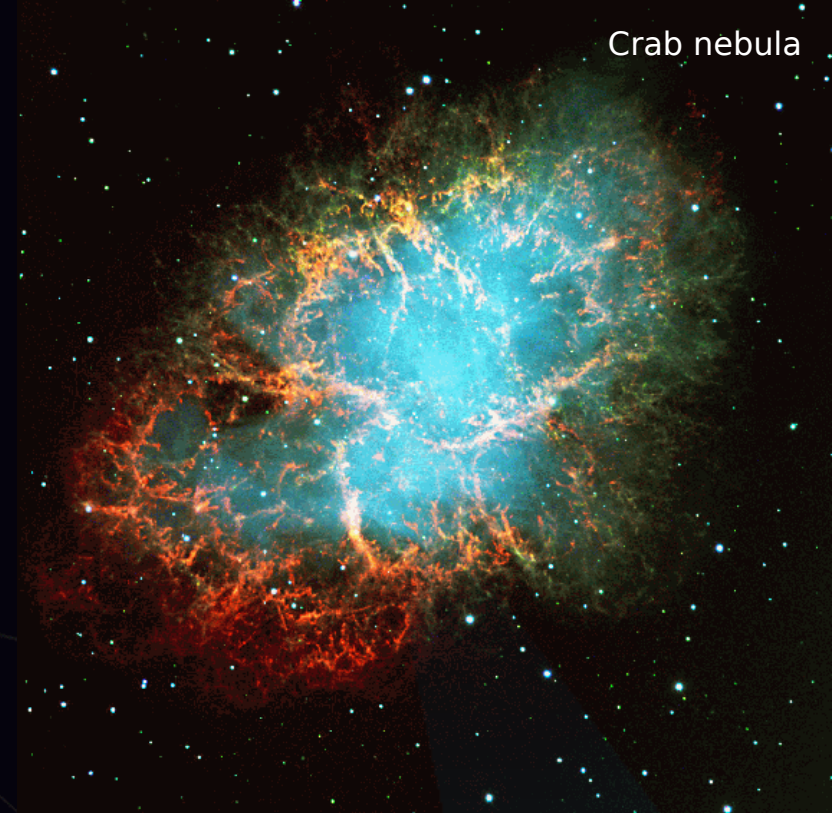




PHASES
of
DENSE MATTER
in
COMPACT STARS

Fridolin Weber
San Diego State University
California, USA

CBM Workshop, GSI, Darmstadt, 15-16 December 2005



Some facts about neutron stars:

$M \sim 1-2 M_{\text{sol}}$

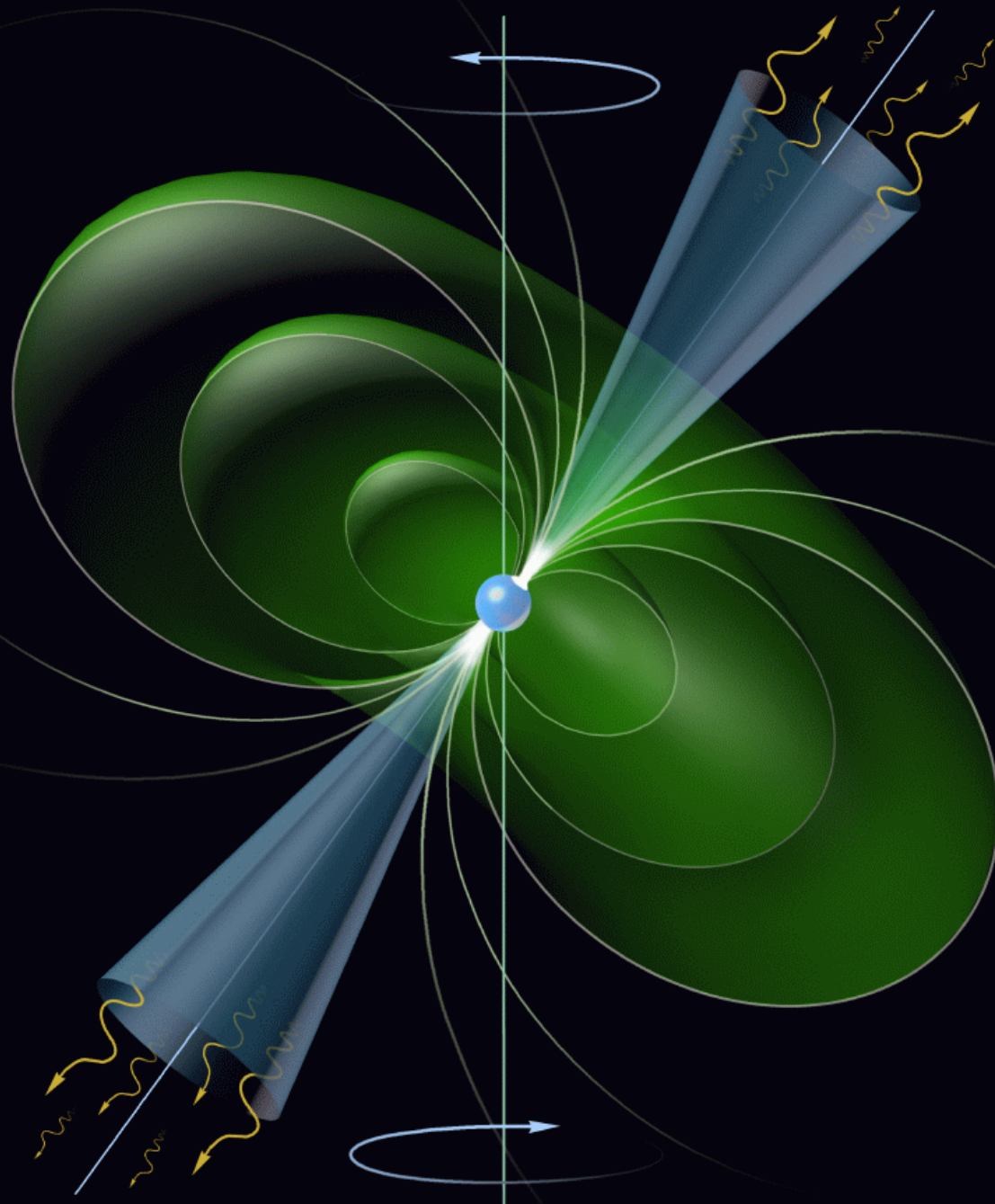
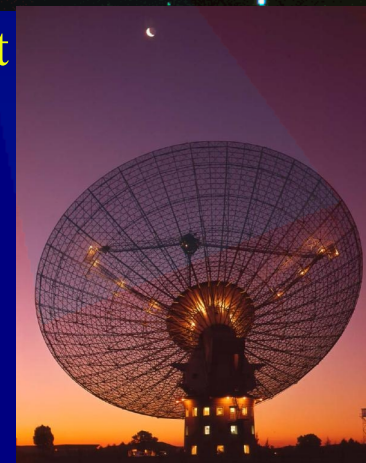
$R \sim 10 \text{ km}$

$B \sim 10^{12} \dots 10^{16} \text{ G}$

$\# \sim 10^9 - 10^{10}$

$P_{\text{min}} = 1.58 \text{ ms (630 Hz)}$

Ter5ad pulsar: $P = 1.39 \text{ ms (720 Hz)}$!



Rotating Neutron Star (Pulsar)

AGS

The multifaceted connection between CBM and Compact Star Physics

Bulk properties

$M, R, I, z, d_{\text{crust}}$
 $\omega, \Omega_{\text{lim}}, \Delta\Omega$
 $T, \varepsilon_v, \kappa, c$

Equation of state

Meson condensate
Hyperons
Strange quarks

Color-superconductivity

Gravitational radiation

Gamma-ray bursts

Soft gamma repeaters

True ground state of strong interaction
Strange quark matter

New types of astrophysical objects

Strange stars
Strange dwarfs
Strange MACHOS

Proto-neutron stars
(ν 's confined)

Pulsars

Superfast rotation
Backbending
Breaking behavior
Spin-up of iMSP

LMXBs

Crust thickness
Crust mass
Surface gravity
Pycnonuclear reactions

The Suspects



- Baryons (Σ , Λ , Ξ , Δ)

$$p_F \geq \sqrt{m_H^2 - m_n^2} \simeq 3 \text{ fm}^{-1} \Rightarrow \rho > 2\rho_0$$

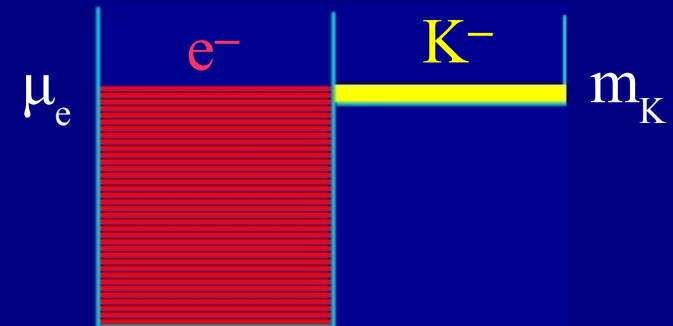
Ambartsumyan & Saakyan, 1960



- Boson condensates (π , K)

$$\rho > 3-5\rho_0$$

Brown & Weise, 1976
 Kaplan & Nelson, 1986
 Politzer & Wise, 1991
 Brown et al., 1992
 Waas, Rho, Weise 1997
 Schaffner-Bielich, 1998
 Mao 1999



- Quarks (u, d, s)

$$P_H(\mu^e, \mu^n) = P_Q(\mu^e, \mu^n) \Rightarrow \rho > 2-3\rho_0$$

Ivanenko & Kurdgelaidze, 1965
 Fritzsche, Gell-Mann & Leutwyler, 1973
 Collins & Perry, 1975
 Baym & Chin; Keister & Kisslinger, 1976
 Chapline & Nauenberg, 1977
 Glendenning, 1992

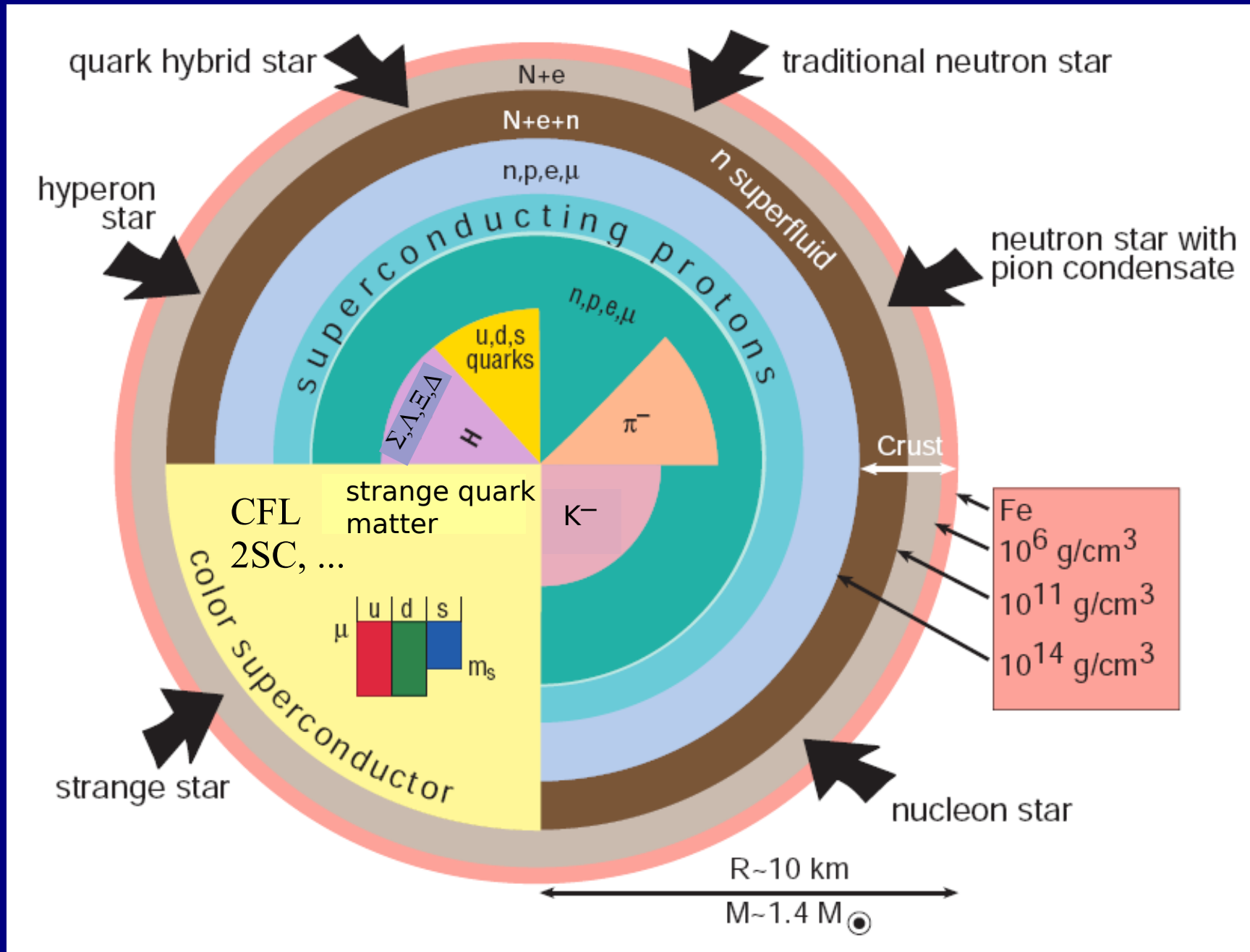
- H dibaryons

$$\rho > 4-5\rho_0$$

Glendenning & Schaffner-Bielich, 1998

“Neutron” Star Composition in 2005

(F. Weber, Prog. Part. Nucl. Phys. 54 (2005) 193-288)



Pulsar B in J0737-3039

M. Kramer et al. (astro-ph/0503386)

A $M_G = 1.25 M_{\text{sun}}$ neutron star!

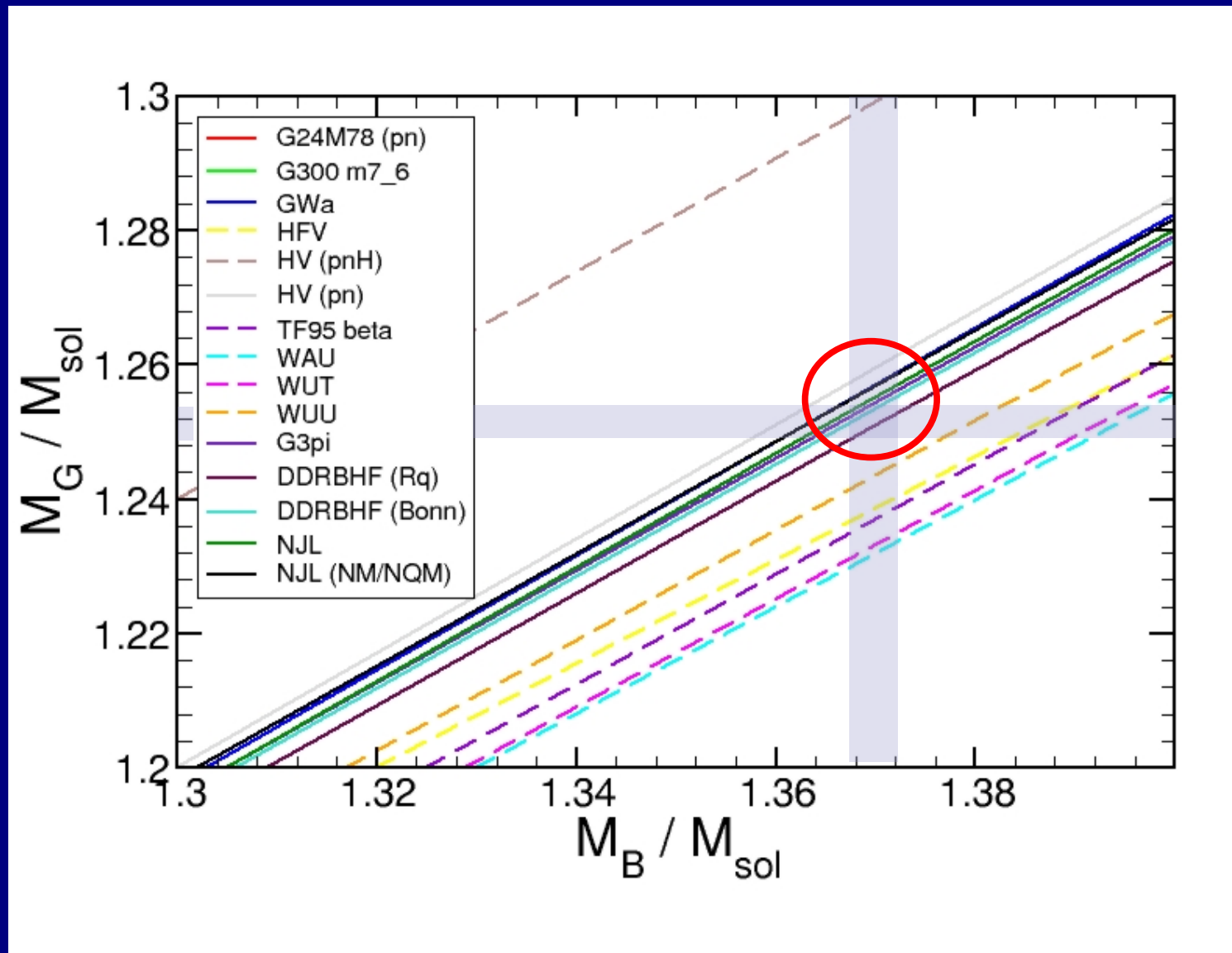
Remnant of a collapsed of ONeMg white dwarf?

Collapse because of e^- capture onto Mg @ $4.5 \times 10^9 \text{ g cm}^{-3}$

If this interpretation is correct, the star's baryon mass is

$$M_B = 1.37 M_{\text{sun}}$$

Constraints on EoS from Pulsar B in J0737-3039



Common Feature of the Success Models

1. $K \approx 240$ MeV, $m^*/m \approx 0.7$, $a_{\text{sym}} \approx 30$ MeV @ saturation

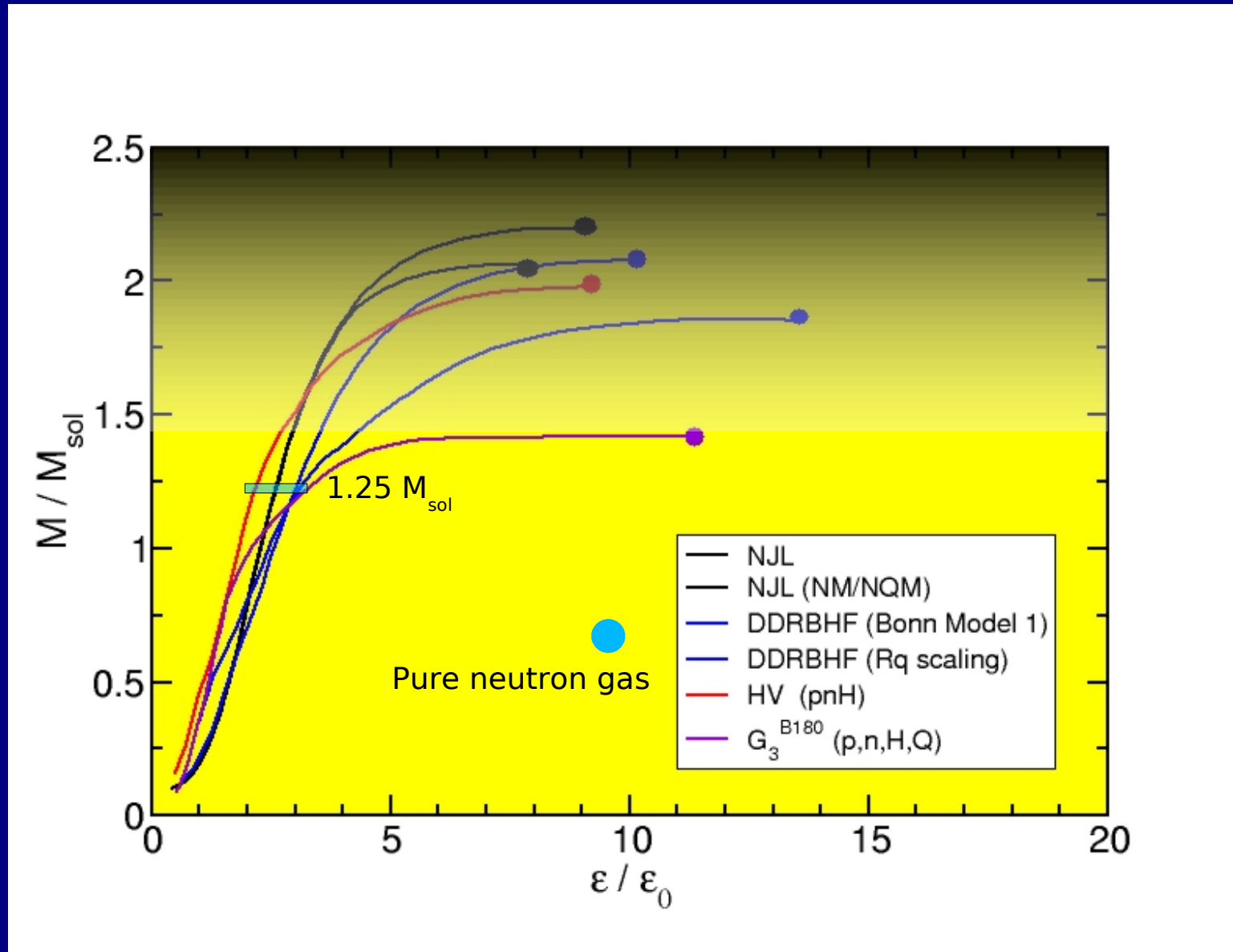
These values agree rather well with the latest values reported at Umesh Garg's workshop on "Nuclear Incompressibility", July 2005, Univ. Notre Dame, IN, USA

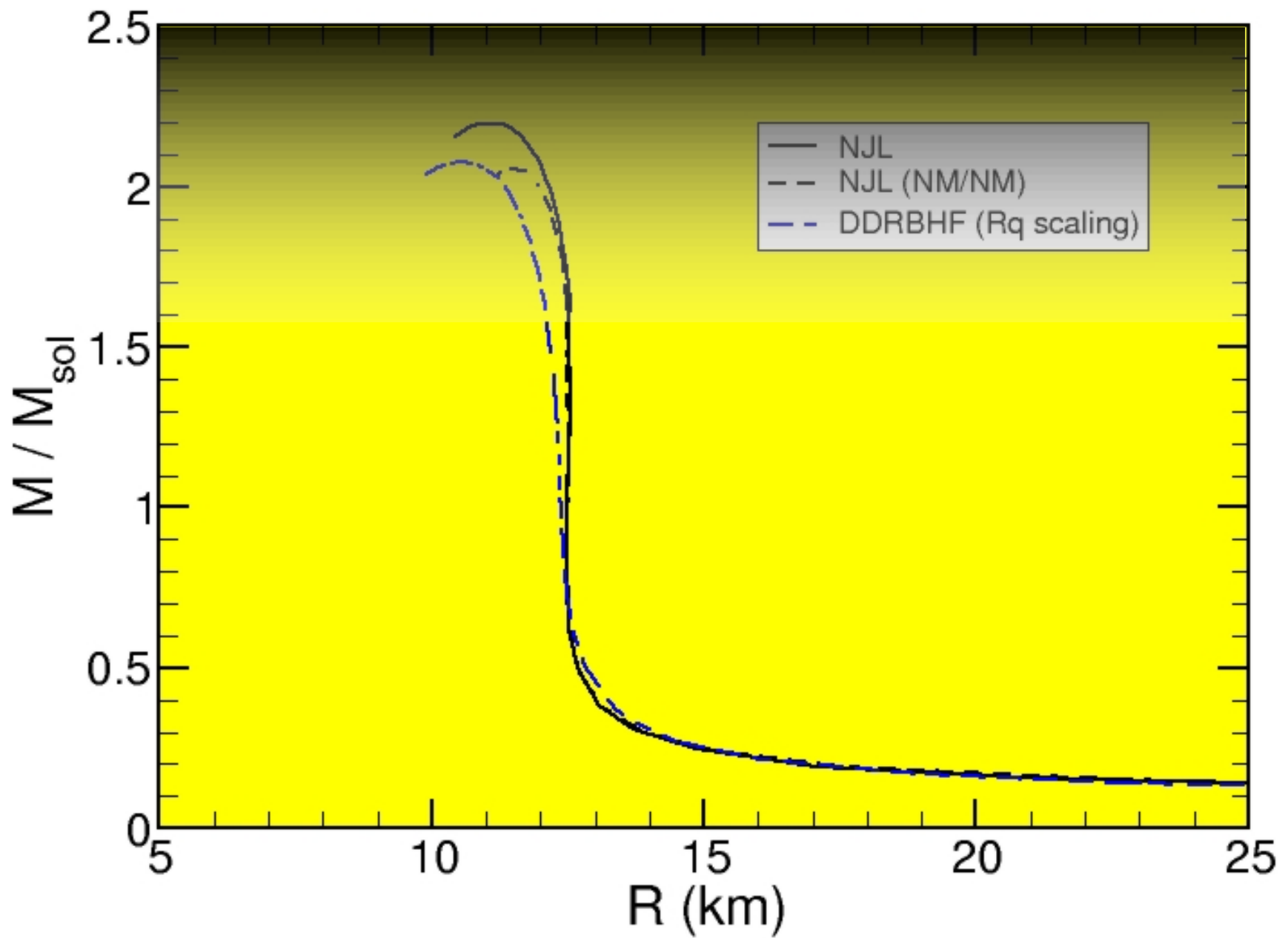
2. Protons and neutrons (in chemical equilibrium) only!

$$M/M_{\text{sol}} = 1.25 \quad \text{☞} \quad \epsilon_{\text{center}}/\epsilon_0 \sim 2 \text{ to } 3$$

$$M_{J0751+1807} = 2.1^{+0.4}_{-0.5} M_{\text{sol}} \quad (1.6 < M/M_{\text{sun}} < 2.5 \text{ at } 95\% \text{ confidence})$$

(Nice, Splaver, Stairs, Loehmer, Jessner, Kramer, Cordes, astro-ph/0508050)





The stellar composition
depends on the star's
mass

but also on the star's
frequency !

Einstein's Field Equations for Rotating Compact Objects

- Metric: $ds^2 = - e^{-2\nu} dt^2 + e^{2(\alpha+\beta)} r^2 \sin^2\theta (d\phi - N^\phi dt)^2 + e^{2(\alpha-\beta)} (dr^2 + r^2 d\theta^2)$

- Christoffel symbols:

$$\Gamma^\sigma_{\mu\nu} = g^{\sigma\lambda} (\partial_\nu g_{\mu\lambda} + \partial_\mu g_{\nu\lambda} - \partial_\lambda g_{\mu\nu}) / 2$$

- Riemann tensor:

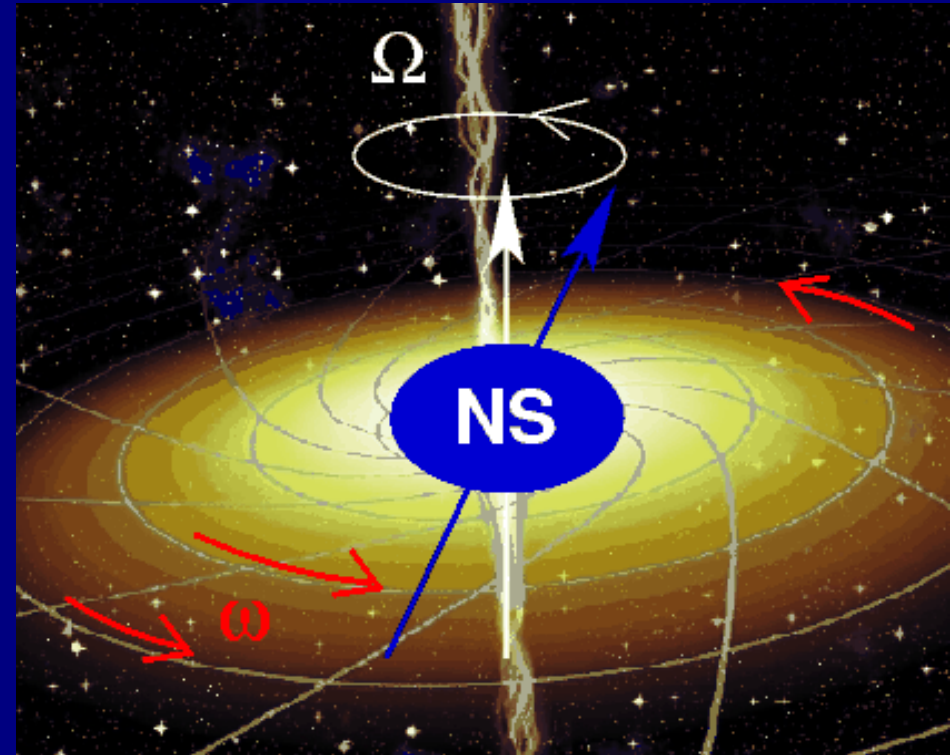
$$R^\tau_{\mu\nu\sigma} = \partial_\nu \Gamma^\tau_{\mu\sigma} - \partial_\sigma \Gamma^\tau_{\mu\nu} + \Gamma^\kappa_{\mu\sigma} \Gamma^\tau_{\kappa\nu} - \Gamma^\kappa_{\mu\nu} \Gamma^\tau_{\kappa\sigma}$$

- Ricci tensor: $R_{\mu\nu} = R^\tau_{\mu\sigma\nu} g^\sigma_\tau$

- Scalar curvature: $R = R_{\mu\nu} g^{\mu\nu}$

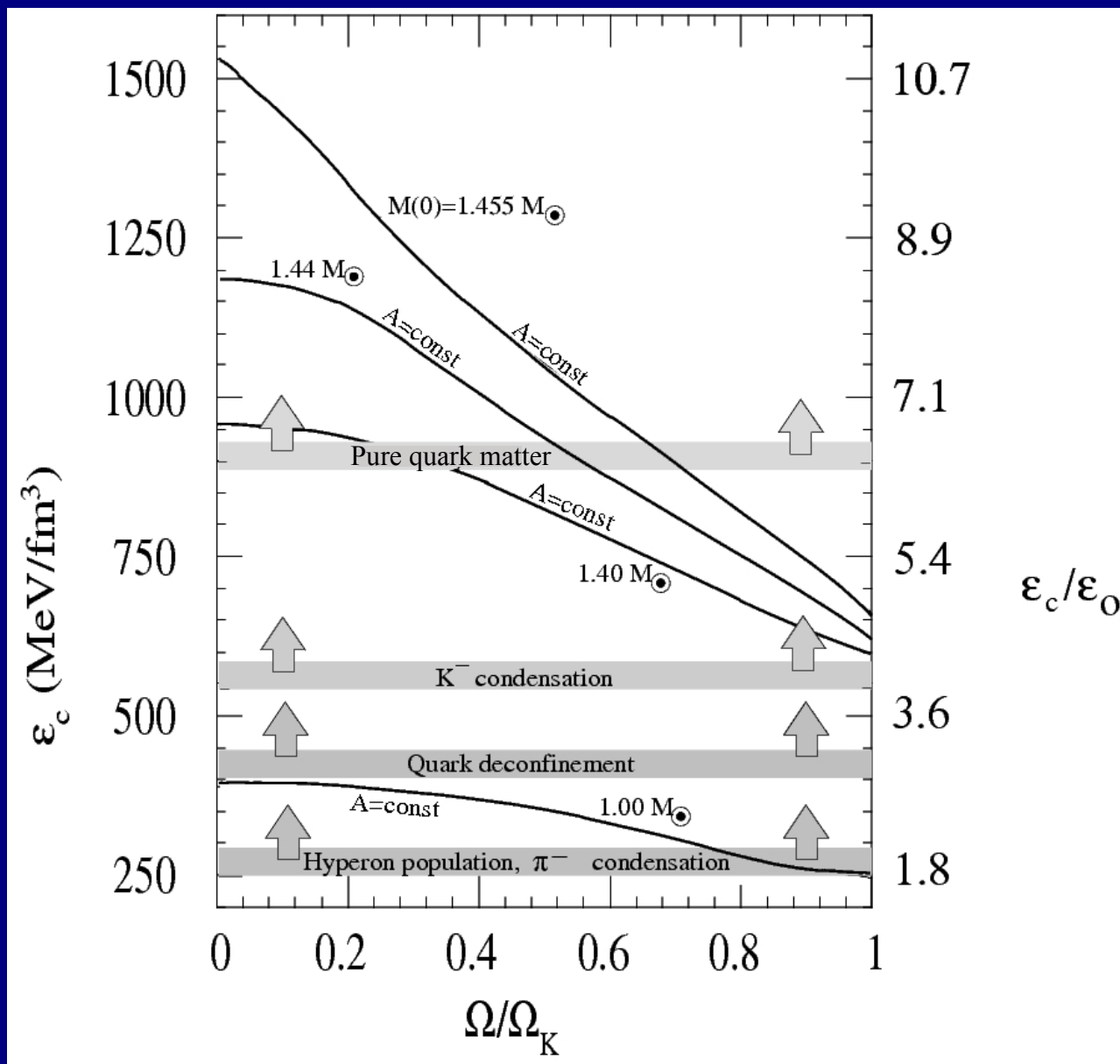
- Kepler frequency: $\Omega_K = r^{-1} e^{v-\alpha-\beta} U_K + N^\phi$

- Differential rotation/uniform rotation



► Stellar properties: $M, R_p, R_{eq}, I, z, \Omega_K, \omega$

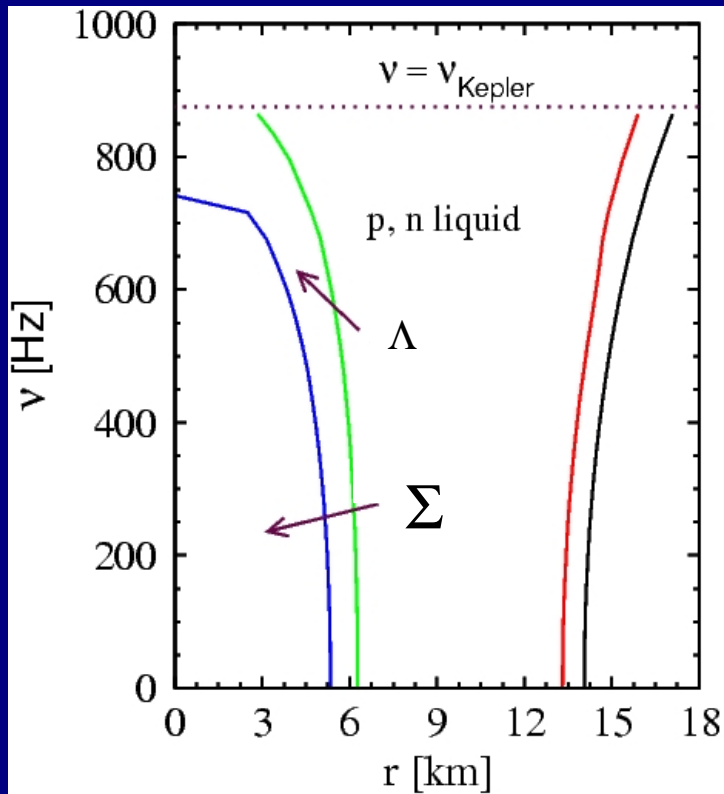
Composition of CBM in Neutron Stars depends on Spin Frequency!



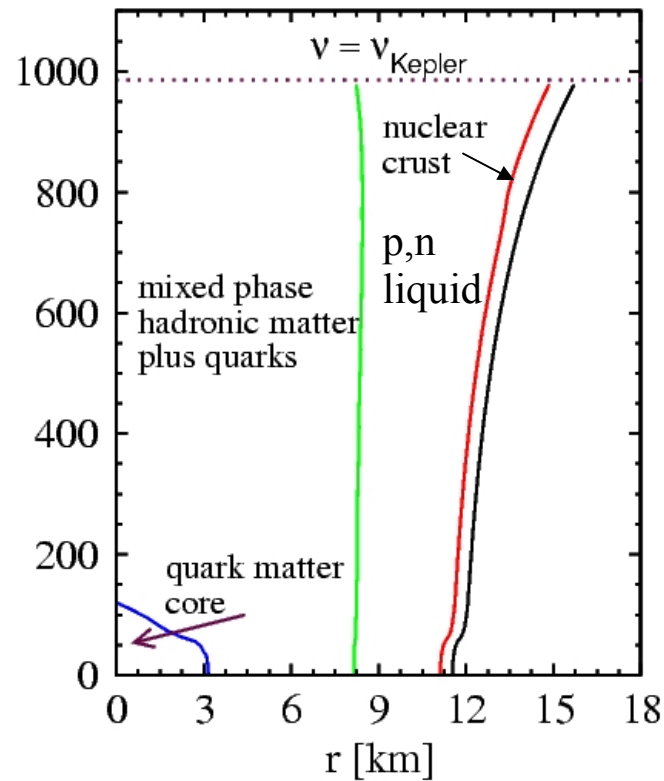
60% change!!

Stellar Compositions ($M \sim 1.4 M_{\text{sun}}$)

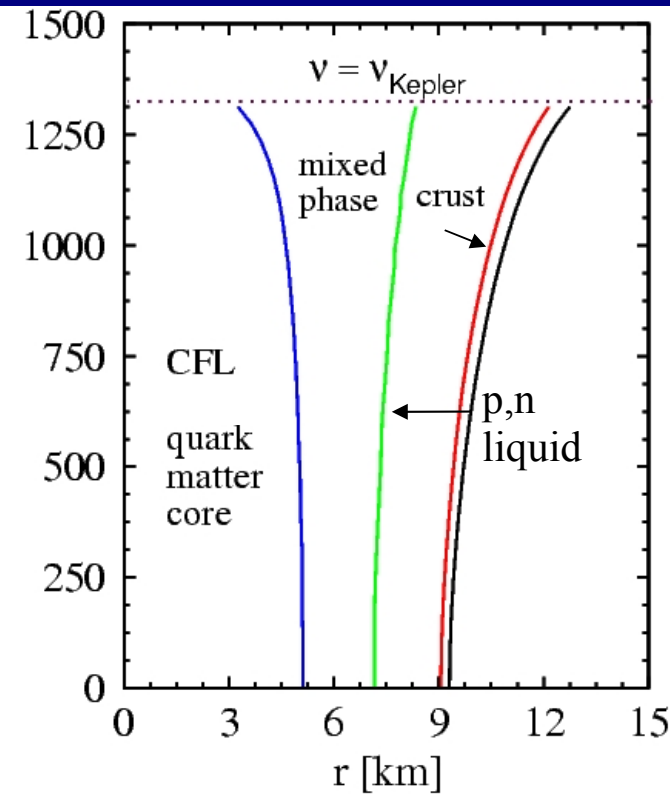
“Traditional” NS



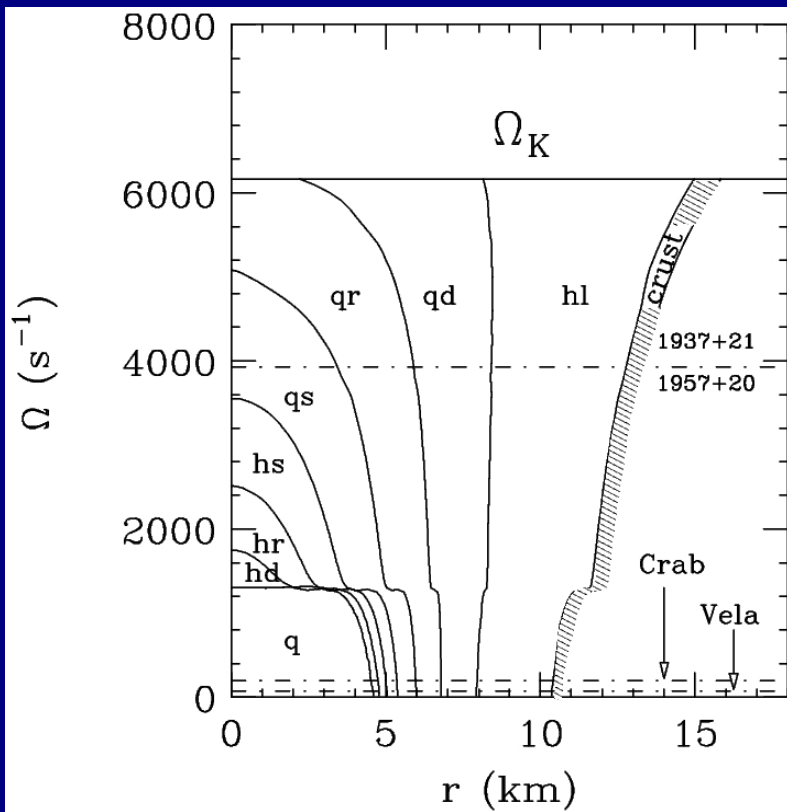
Quark-hybrid star



Quark-hybrid star

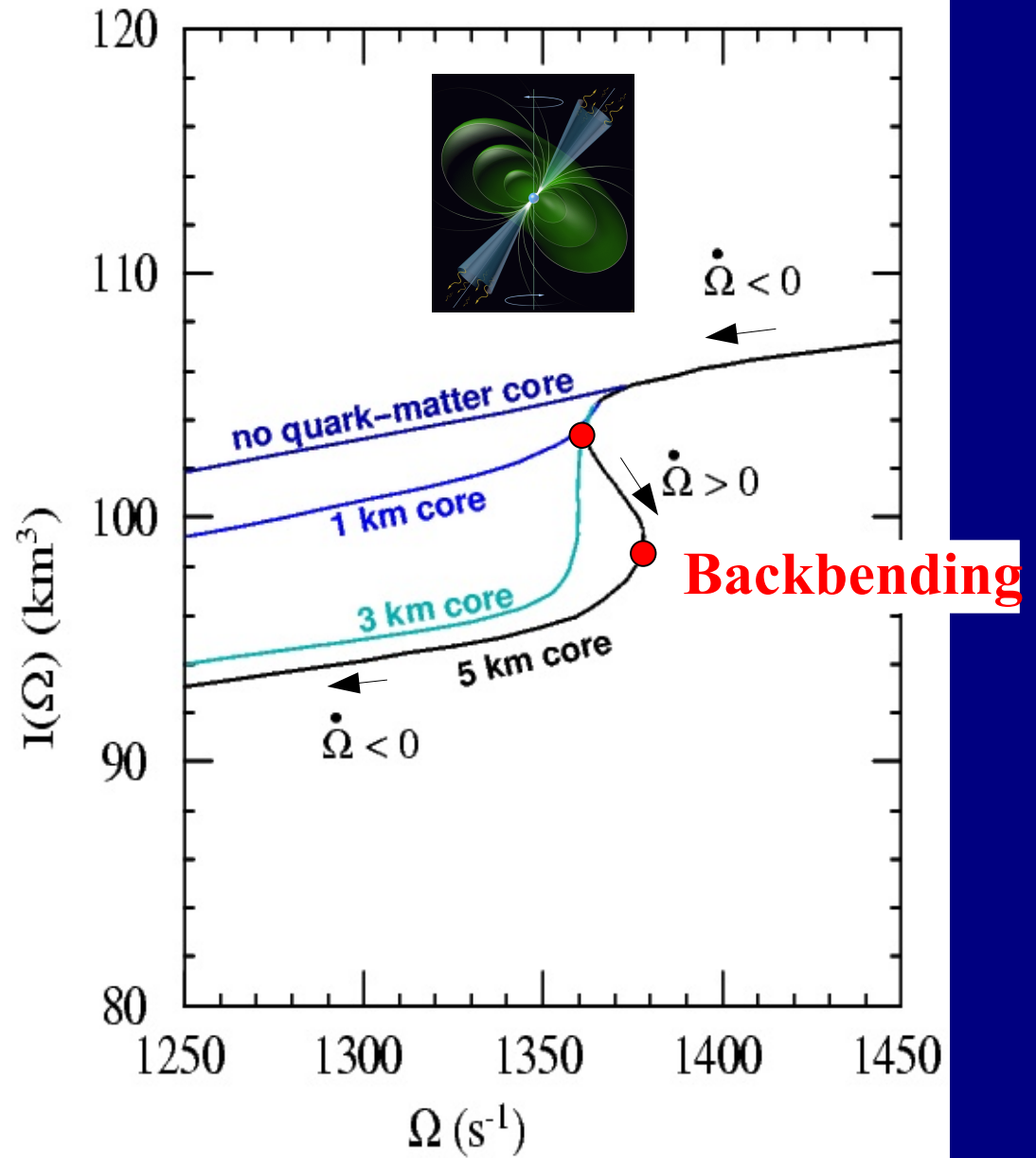


Moment of Inertia



Glendenning & Weber,
PRL 79 (1997) 1603;

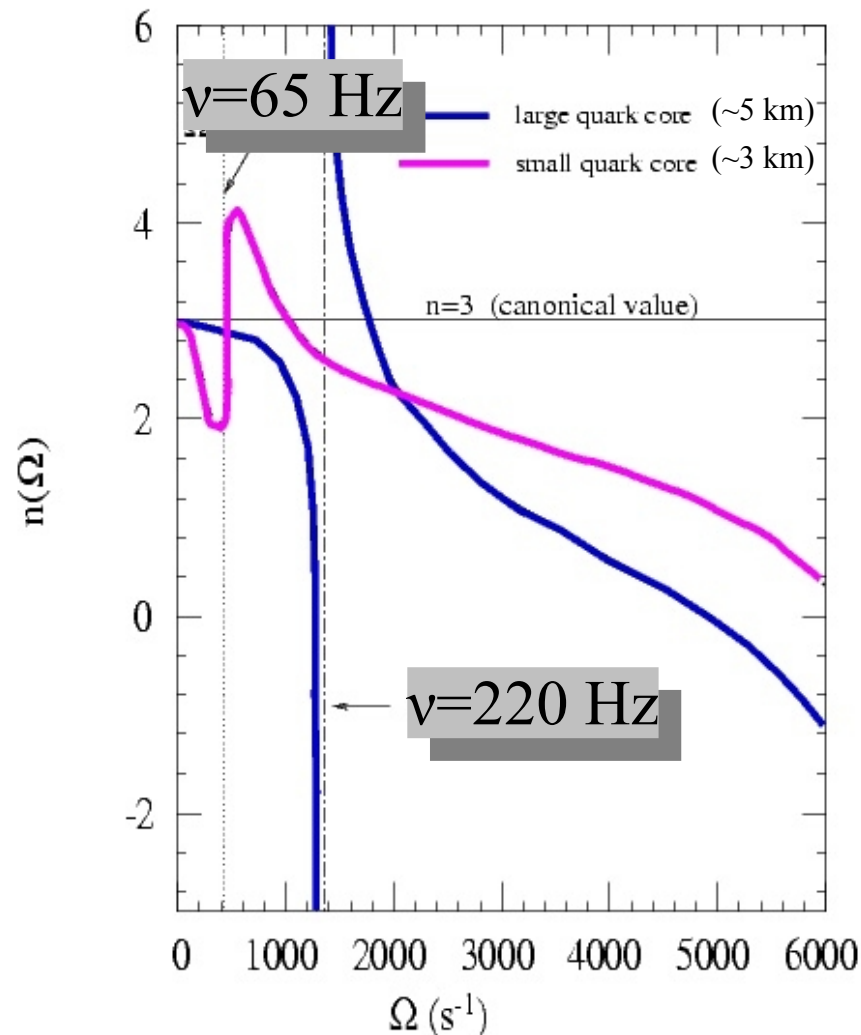
F. Weber, Prog. Nucl.
Part. Phys. 54 (2005)
193-288



Signal of Quark Matter in NSs

Braking index

$$n = \frac{\Omega \ddot{\Omega}}{\dot{\Omega}^2} = 3 - \frac{I'' \Omega^2 + 3 I' \Omega}{I' \Omega + 2 I}$$

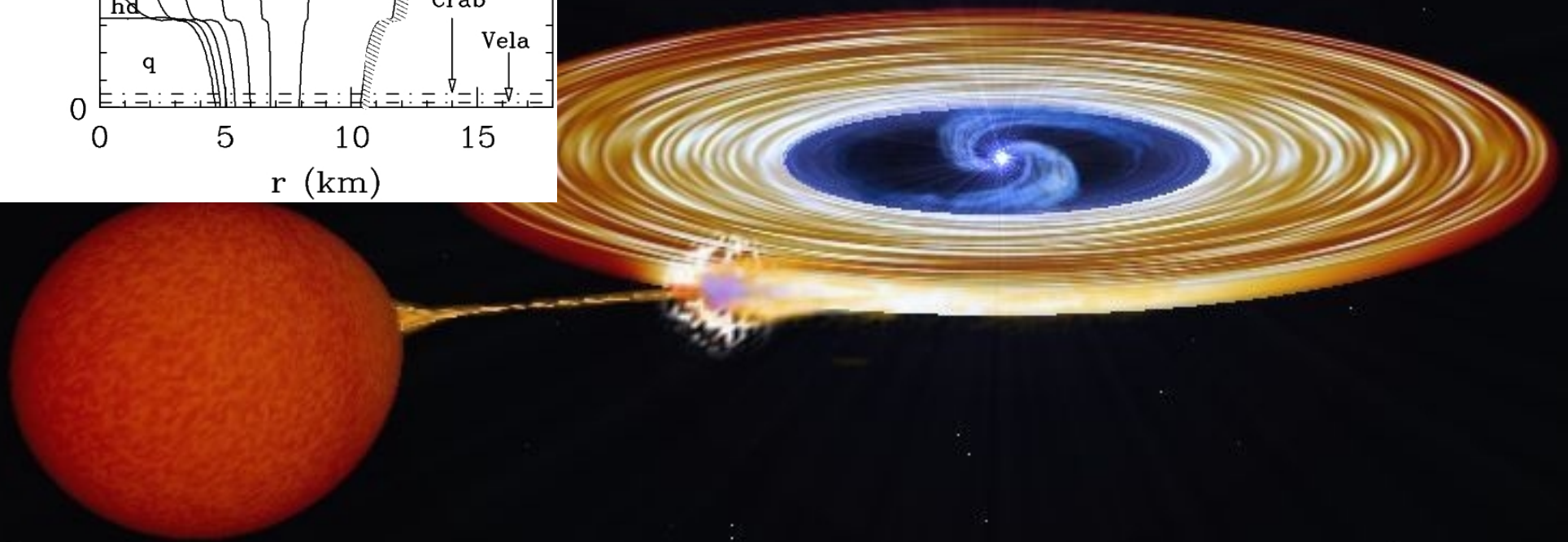
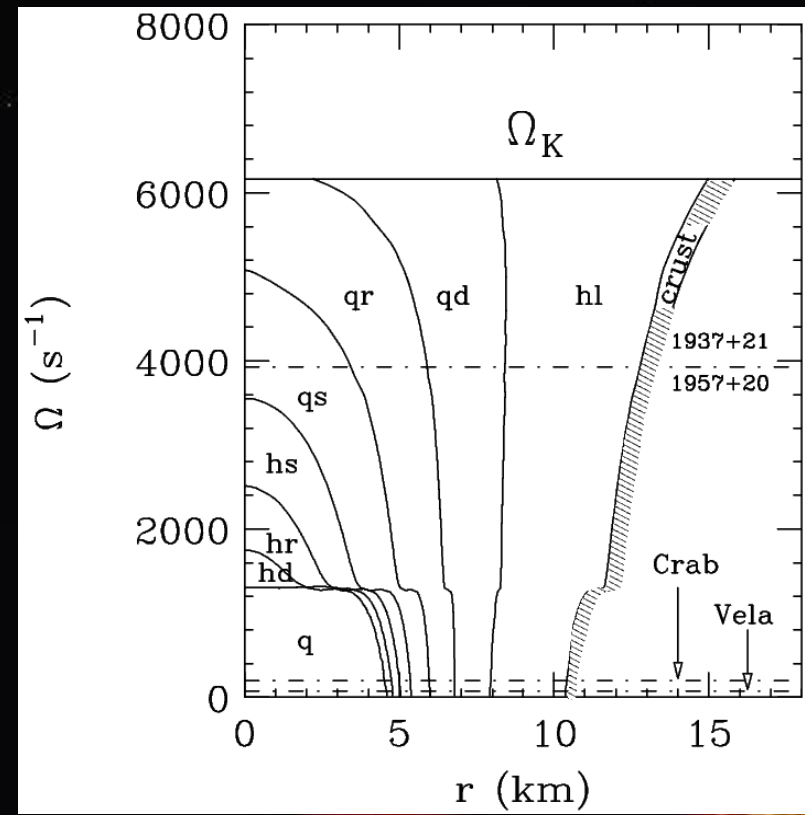


Glendenning, Pei, Weber,
PRL 79 (1997) 1603

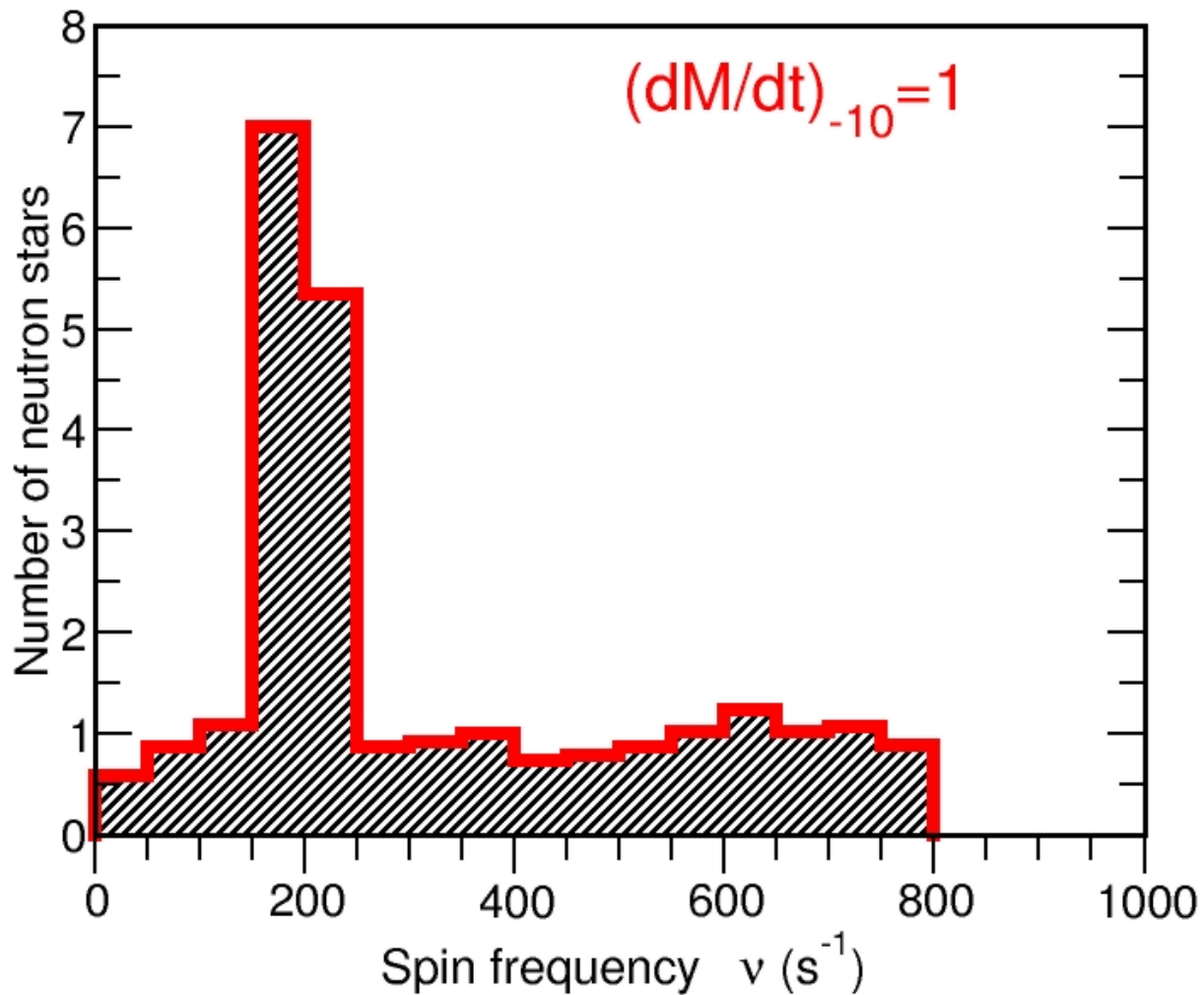
Weber, J. Phys. G: Nucl.
Part. Phys. 25 (1999) R195

Chubarian, Grigorian,
Poghosyan, Blaschke (2000)

Weber, Prog. Part. Nucl.
Phys. 54 (2005) 193

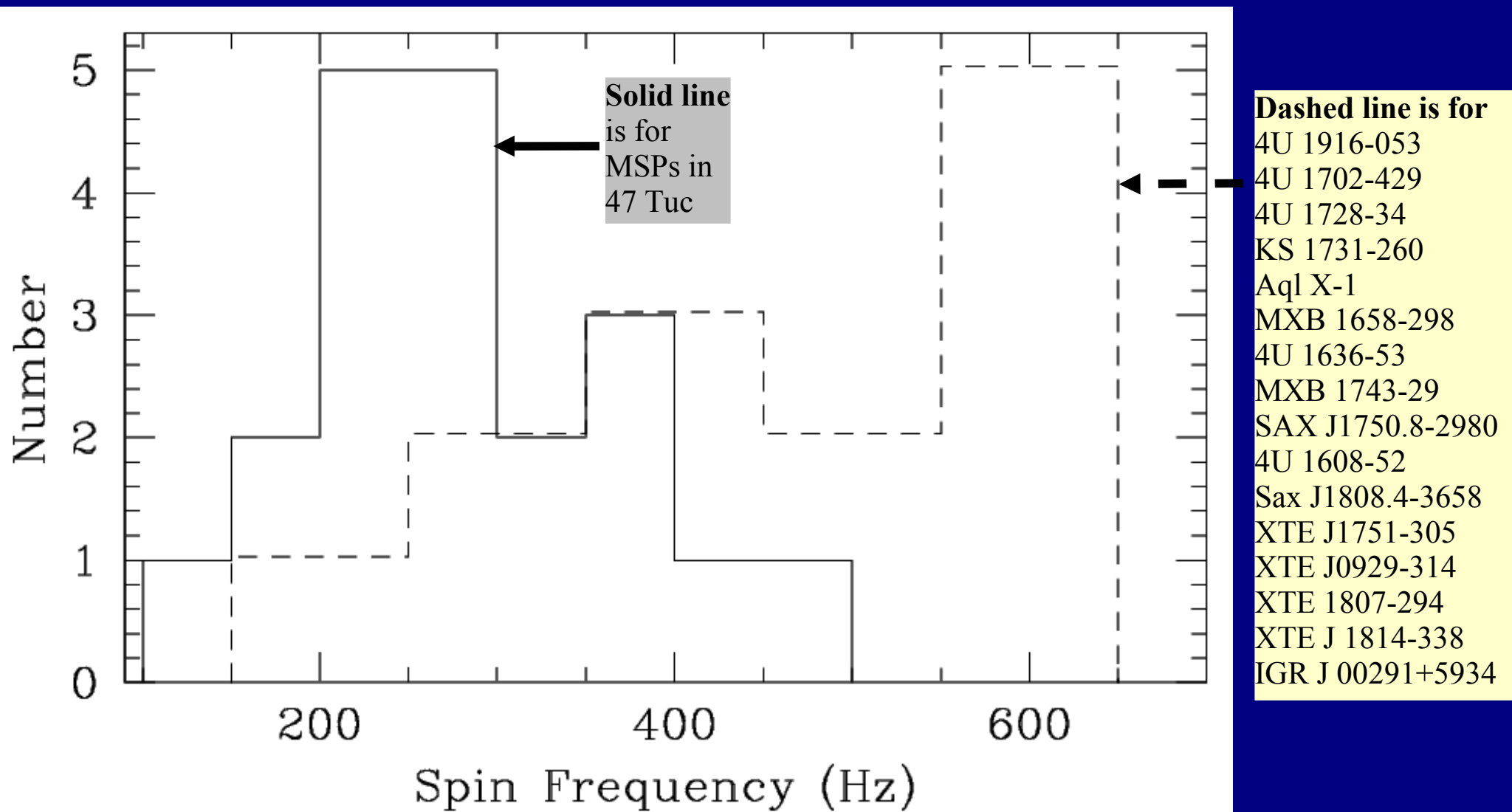


Pile-up of Neutron Stars



Histogram of Neutron Stars Spin Frequencies

(see L. Bildsten, astro-ph/0212004; R. Wijnands, astro-ph/0501264)



Rotation at Mass Shedding Frequency

Kepler frequency:

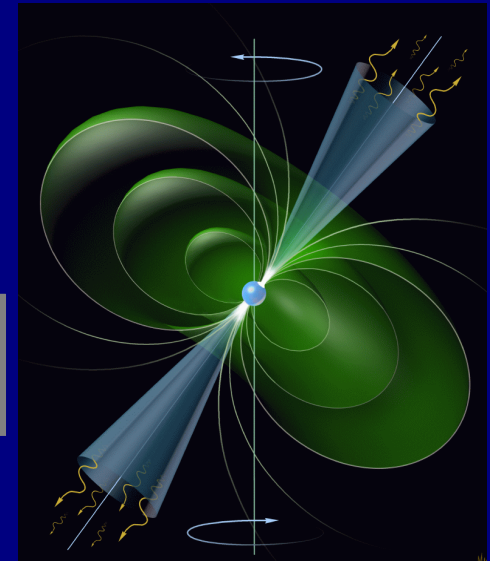
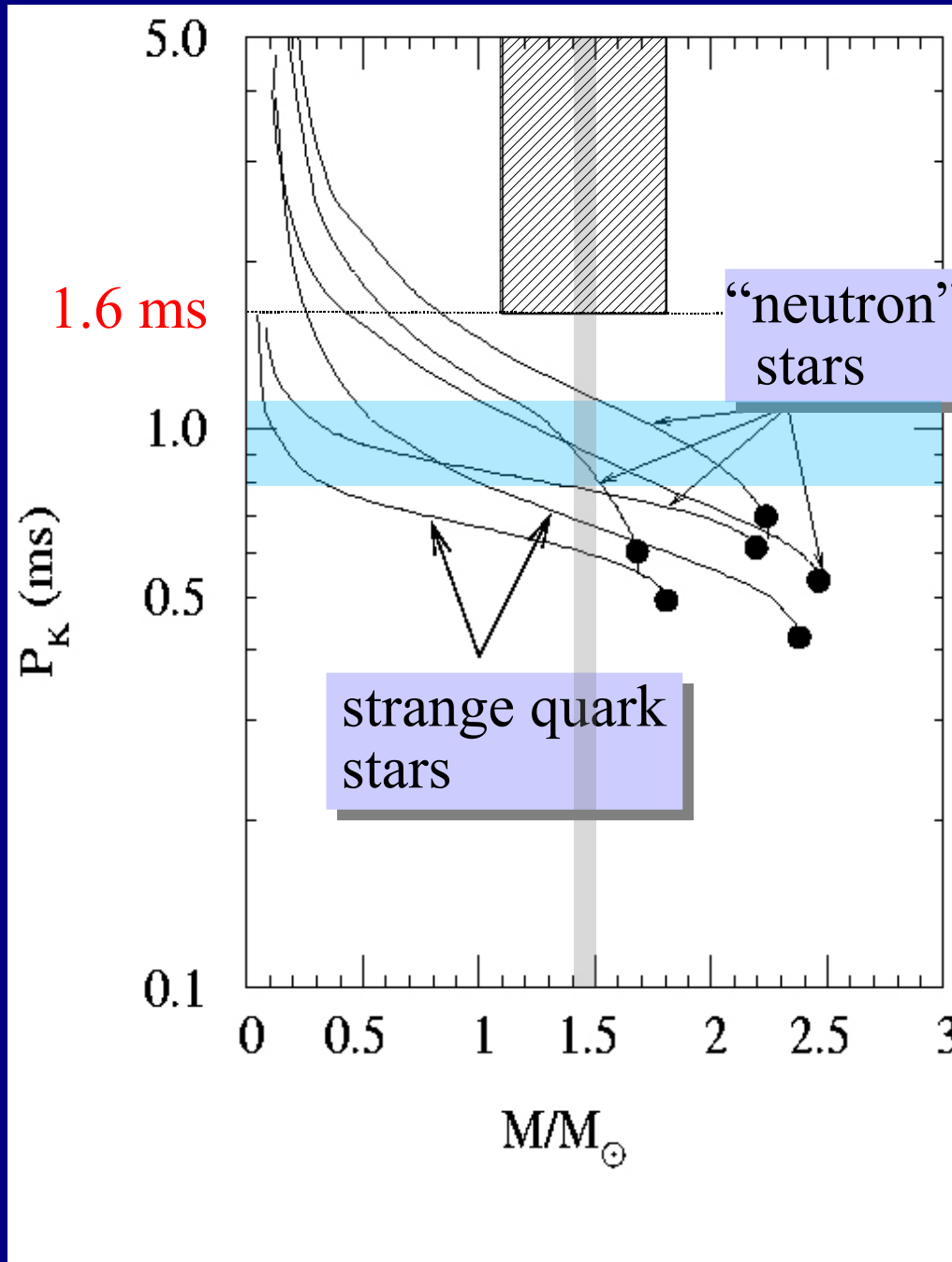
Einstein:

$$\Omega_K = r^{-1} e^{\nu-\alpha-\beta} U_K + N^\phi \text{ at } r=R_{eq}$$

► $P_K = 2\pi/\Omega_K$

(Newton:

$$P_K = 2\pi\sqrt{(R^3/M)}$$
)



Parkes radio telescope

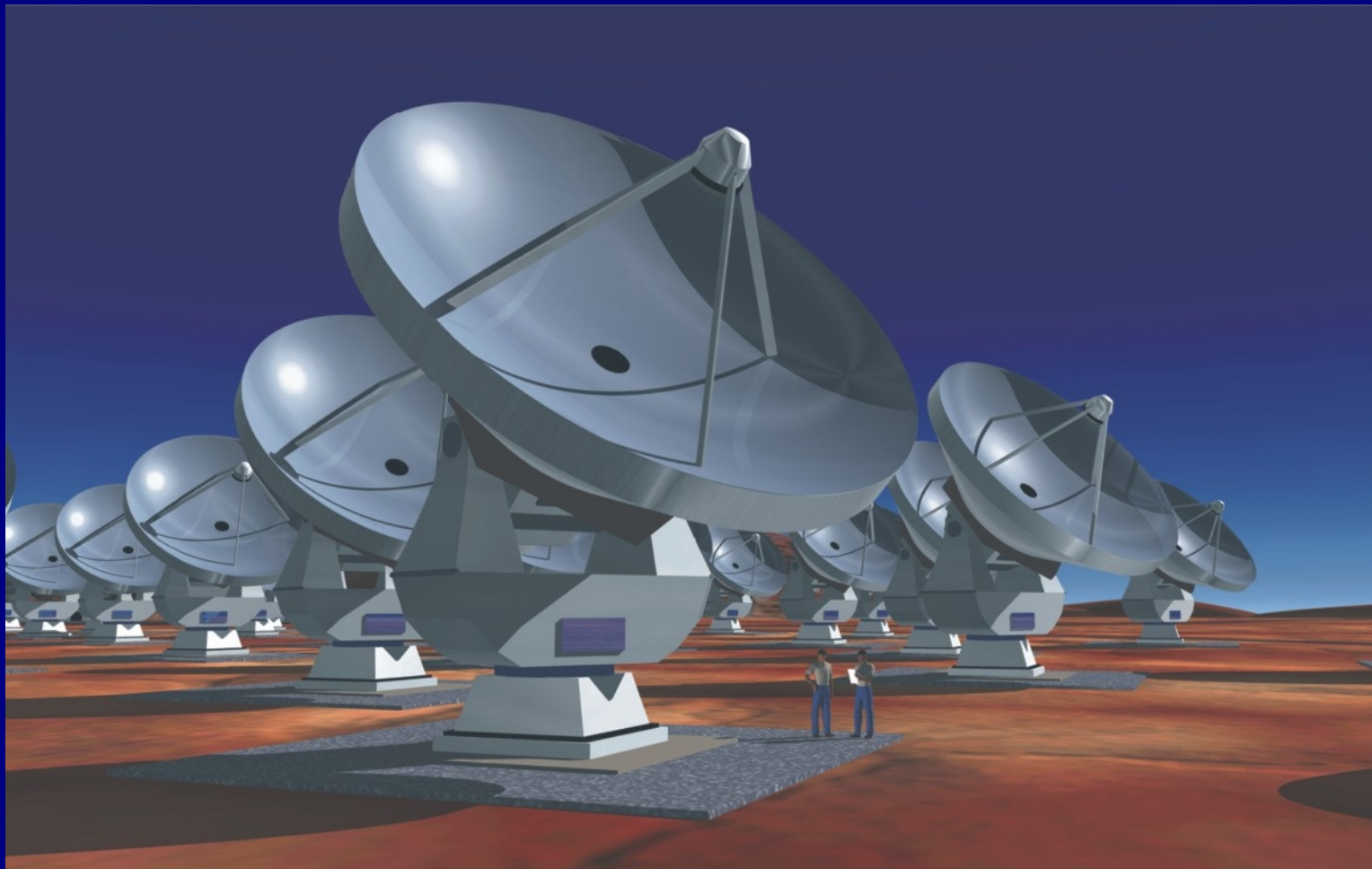
Most exciting future ahead: SKA (Square Kilometer Array)

Sensitivity ~100 times higher than the VLA sensitivity

~ **20,000** pulsars expected to be discovered

~ **1000 MSPs**

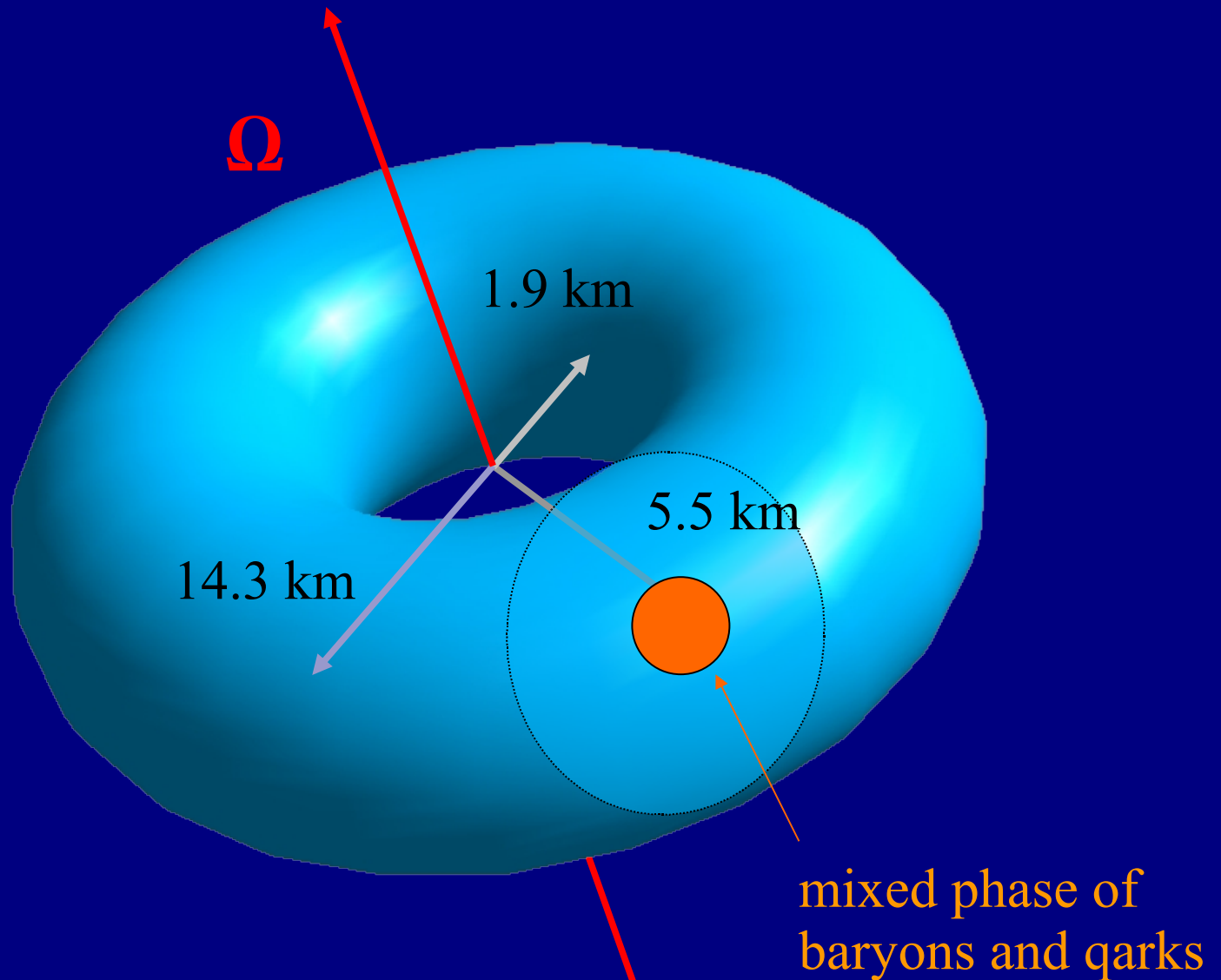
Operations start ~2016



ALMA
Antennas

Differentially Rotating Stellar Objects

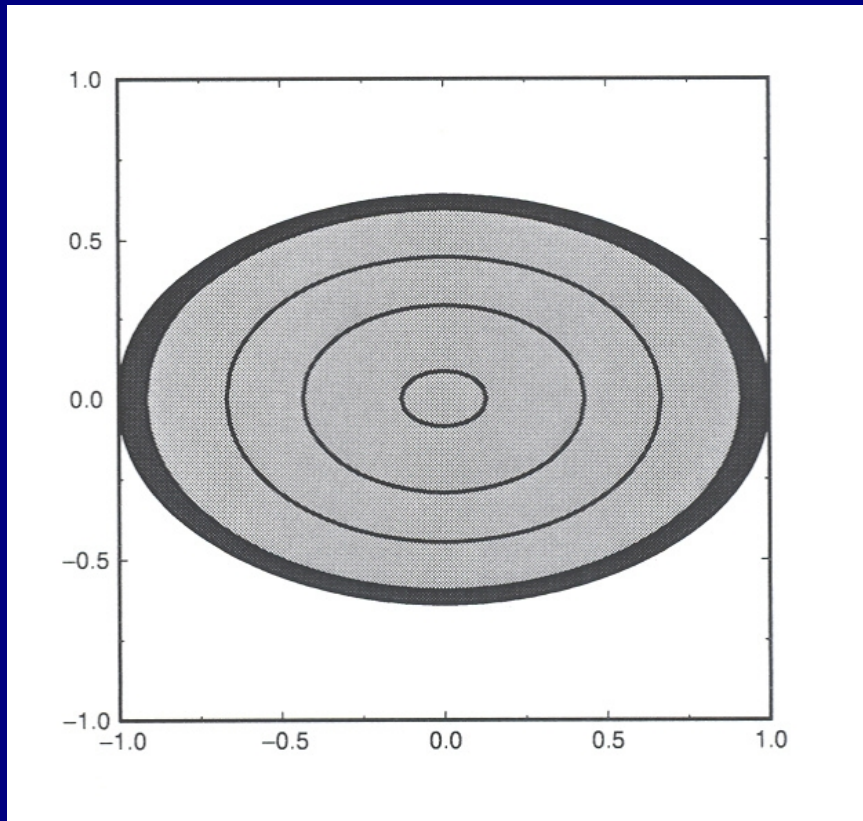
$$M = 1.4 M_{\text{sun}}$$
$$\nu_{\text{eq}} = 290 \text{ Hz}$$
$$\nu_{\text{c}} = 140 \nu_{\text{eq}}$$



Open issue: dynamical stability; secular stability

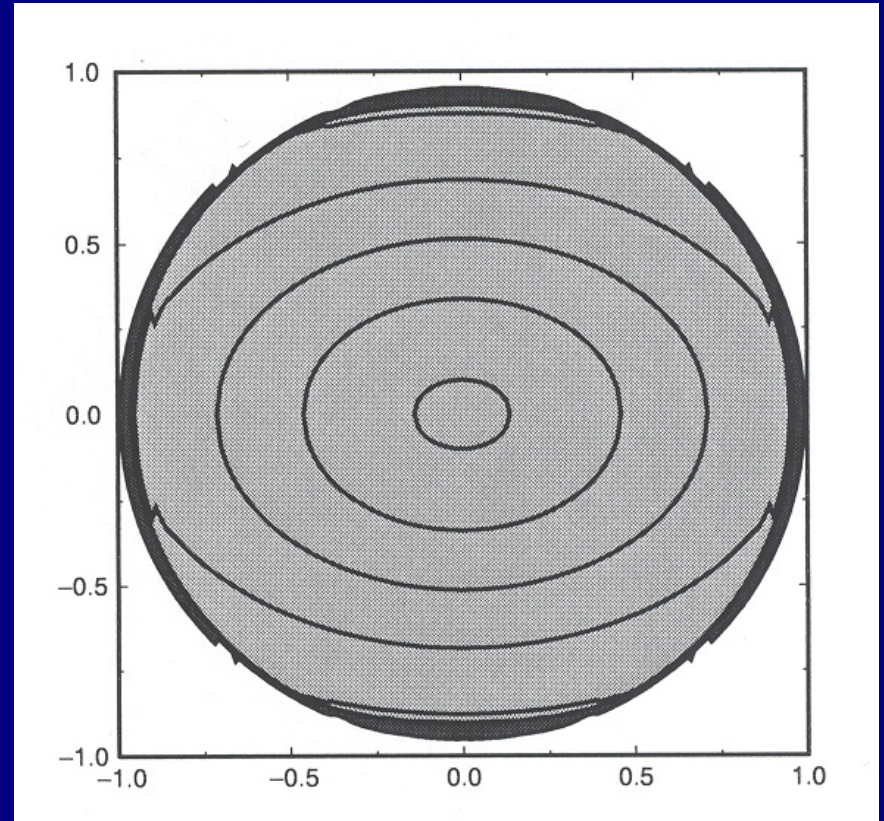
Differentially Rotating Strange Stars

($M=1.40 M_{\text{sol}}$, $B^{1/4}=145 \text{ MeV}$)



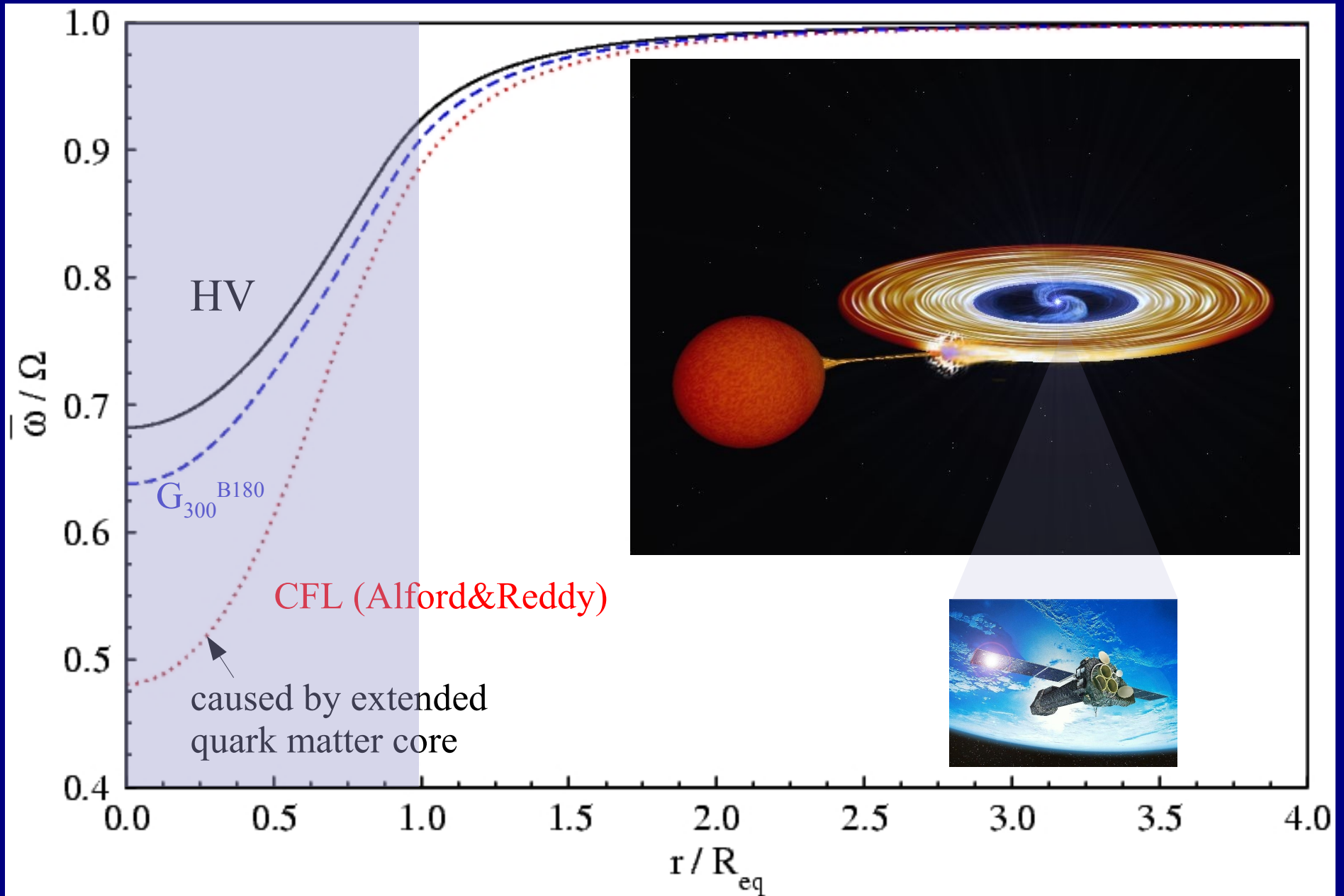
Rigid body rotation

$$\Omega_s/\Omega_c = 1 \quad (1000 \text{ Hz})$$



$$\Omega_s/\Omega_c = 1/2$$

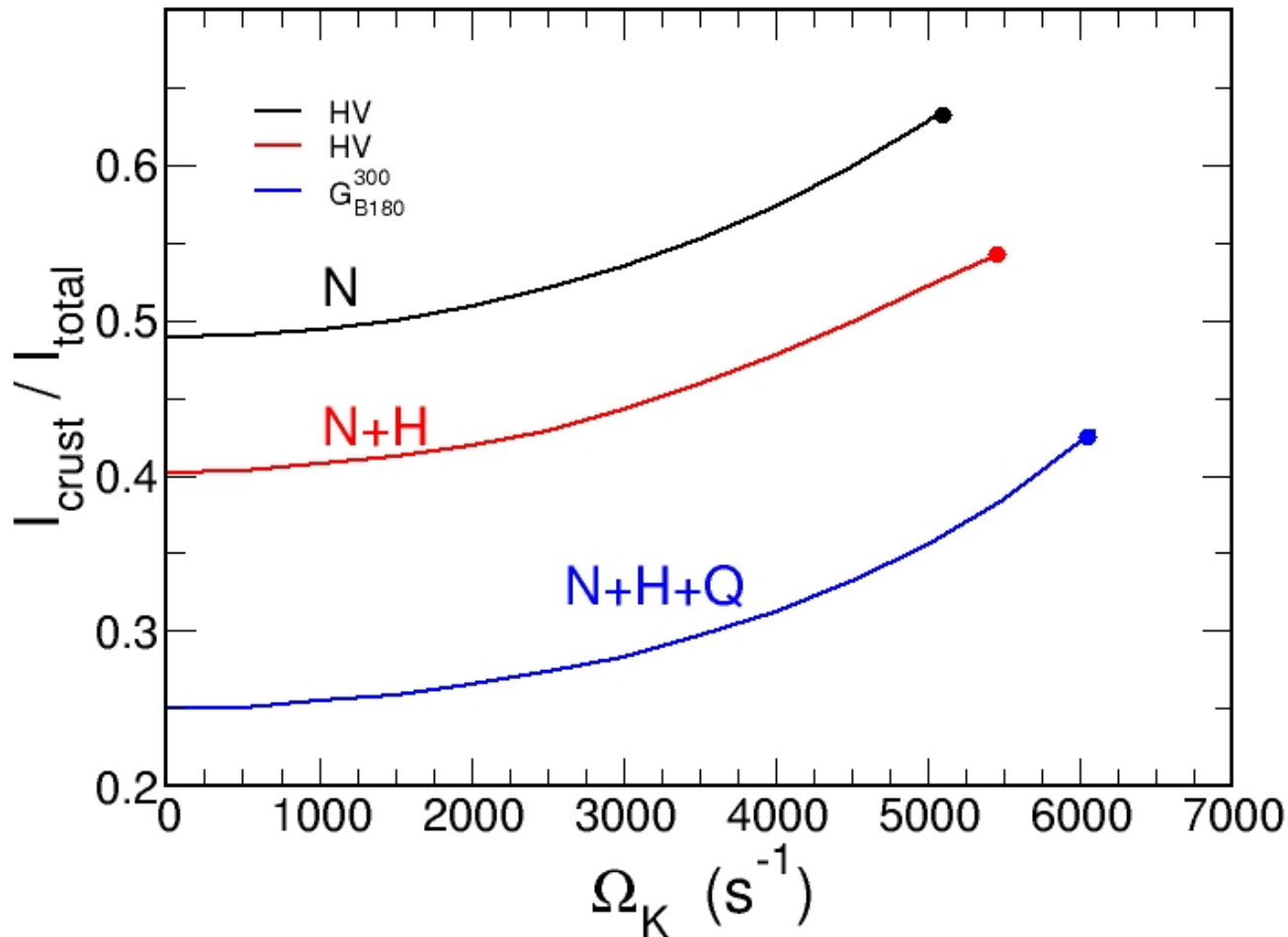
Frame Dragging of the LIFs



Crustal Moment of Inertia

$$I = \Omega^{-1} \int_V dr d\theta d\phi \sqrt{-g} T_\phi^t$$

$M = 1.40 M_{\text{sol}}$

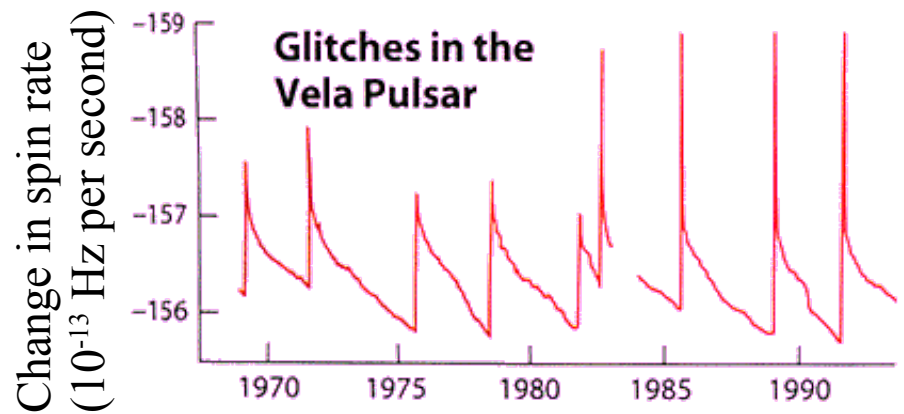
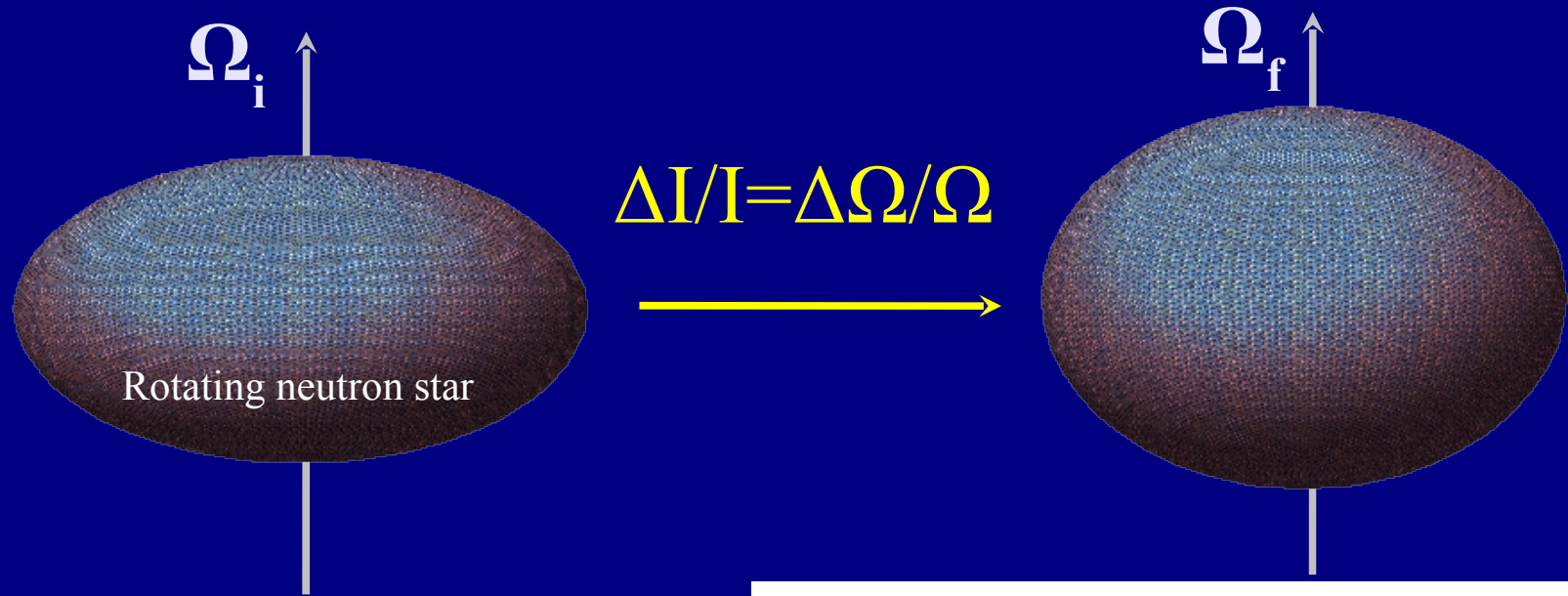


☞ Pulsar glitches

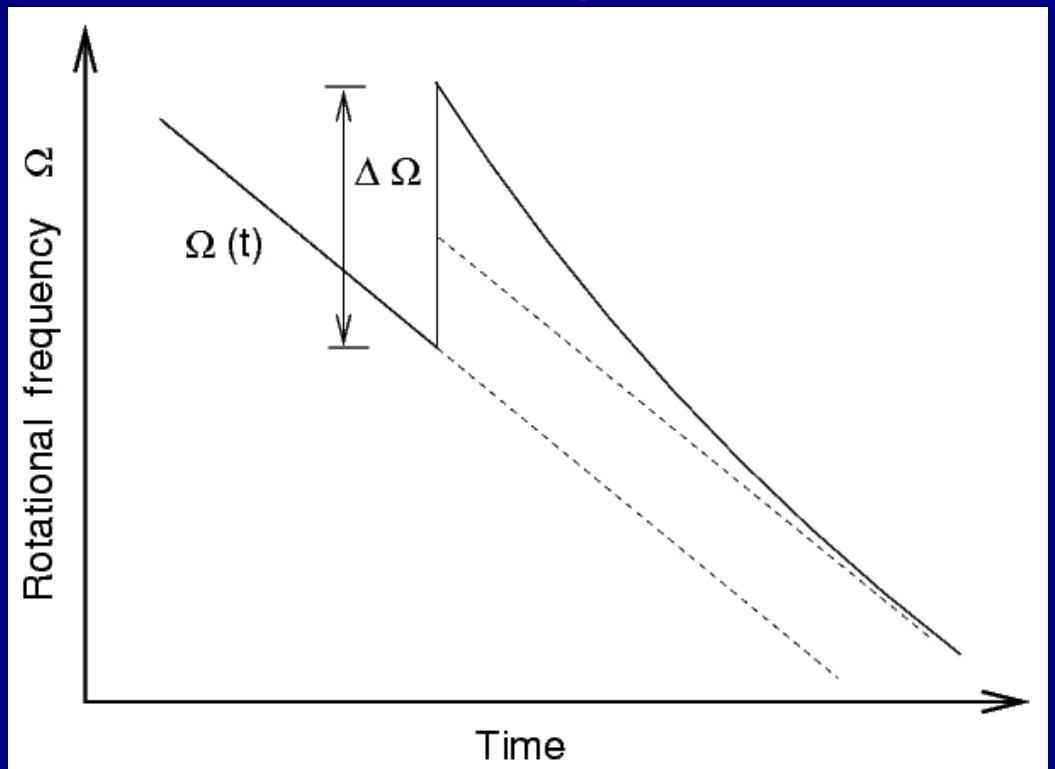
☞ Post-glitch behavior

☞ JINA physics

Pulsar Glitches

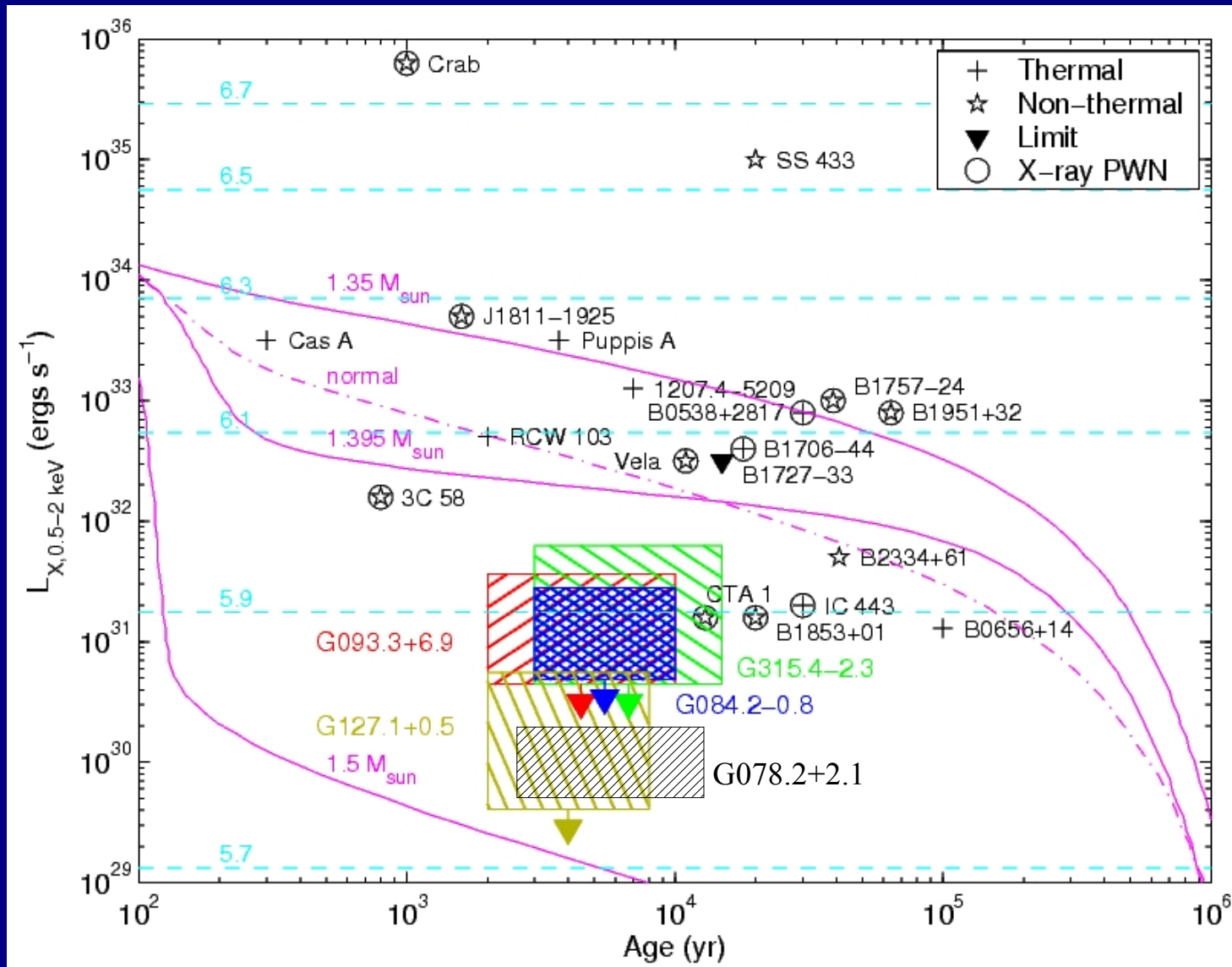


Source: www.kosmologika.net/Stars/



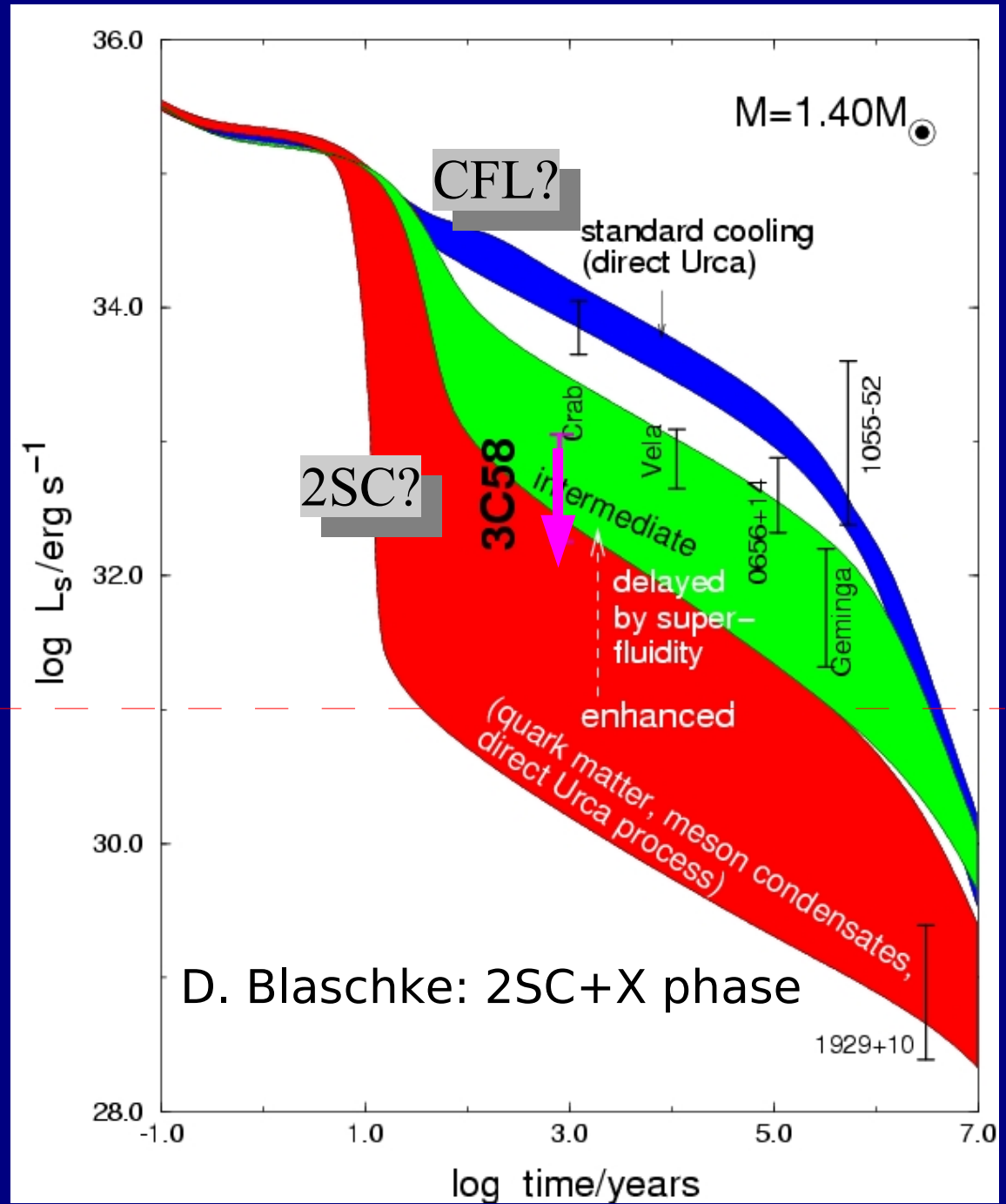
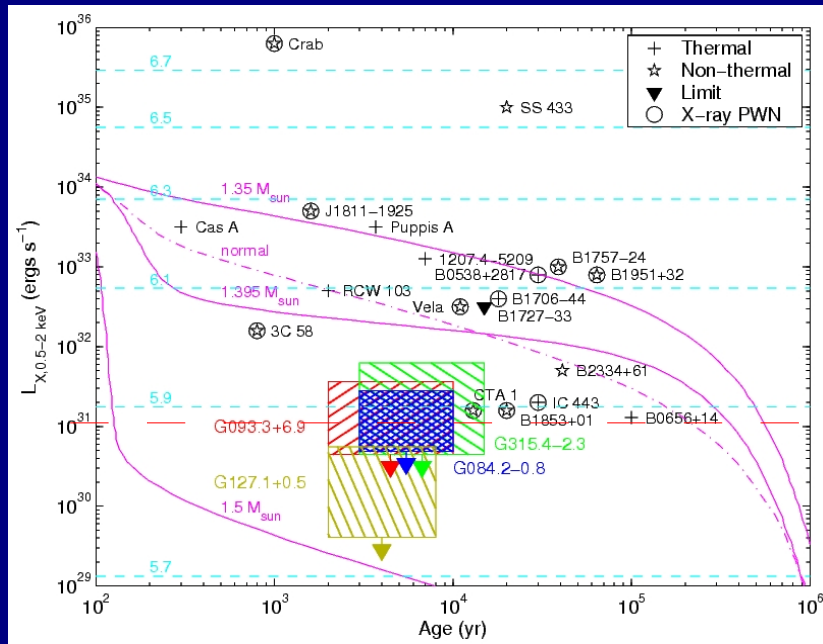
Searching for Young Neutron Stars in SNRs

Kaplan et al. (2004)



Non-detection in G084.2-08, G093.3-6.9, G127.1+0.5, G078.2+2.1
→ strong constraints on cooling (?)

“Neutron” Star Cooling



Summary

- Compact stars/Astrophysical settings offer the unique opportunity to explore the properties of CBM, i. e. a portion of the phase diagram of nuclear matter that cannot be probed by RHIC.
- The list of hot research topics includes:
 1. Modern theories of (ultra) dense matter
 2. Fundamental building blocks (true ground state)
 3. Equation of state
 4. Properties of matter subjected to high density radiation fields, magnetic fields, electric fields
 4. Making of the elements, . . .
- We just began to scratch the surface – a most exciting future is ahead driven by unprecedented advanced in observational astronomy!