

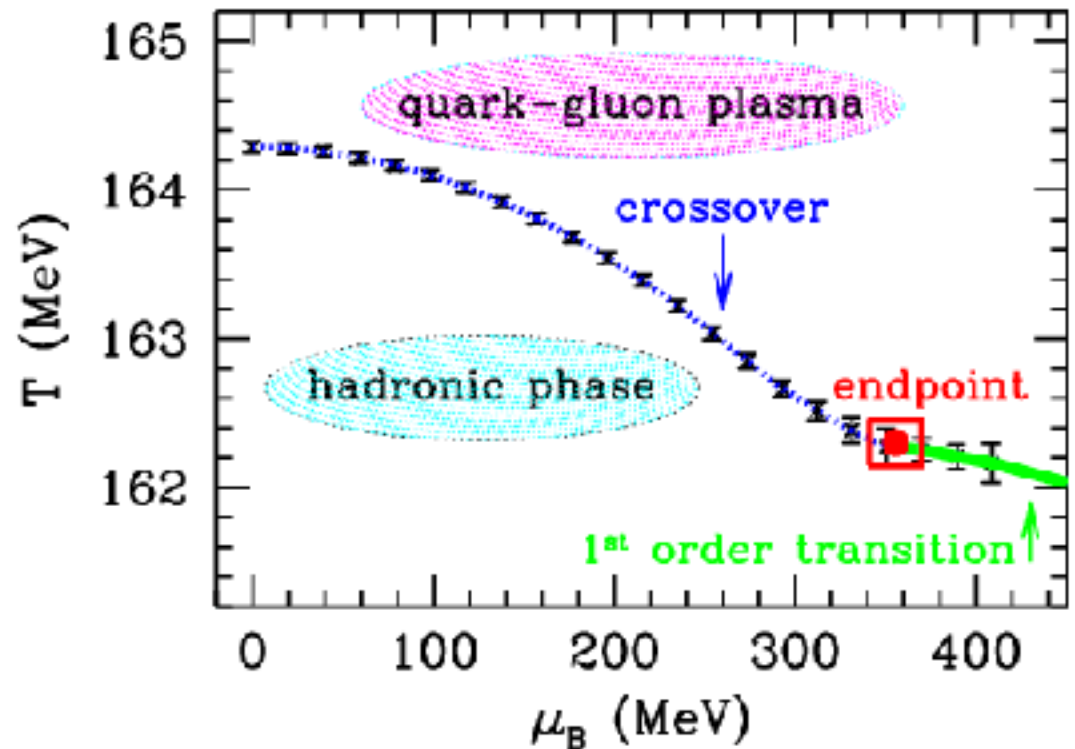
Chiral Hydrodynamics

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in collab. with Kerstin Paech

★ Critical Fluct. at endpoint ?

★ Change in bulk dynamics
left/right of endpoint ?



Fodor, Katz, JHEP '04

Large N:

$$SU(N) \rightarrow U(N)$$

$$V_{gl}(\ell) \sim m^2 \ell \ell^* + \dots$$

$$V_{qk}(\ell) \sim h(e^{\mu\ell} + e^{-\mu\ell^*})$$

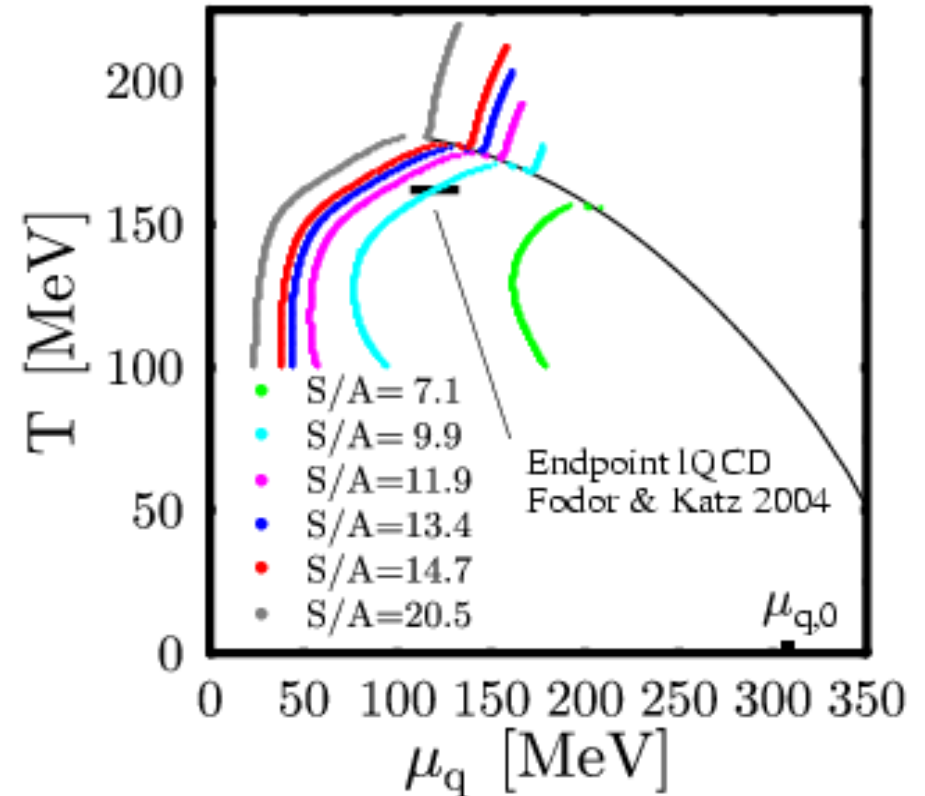
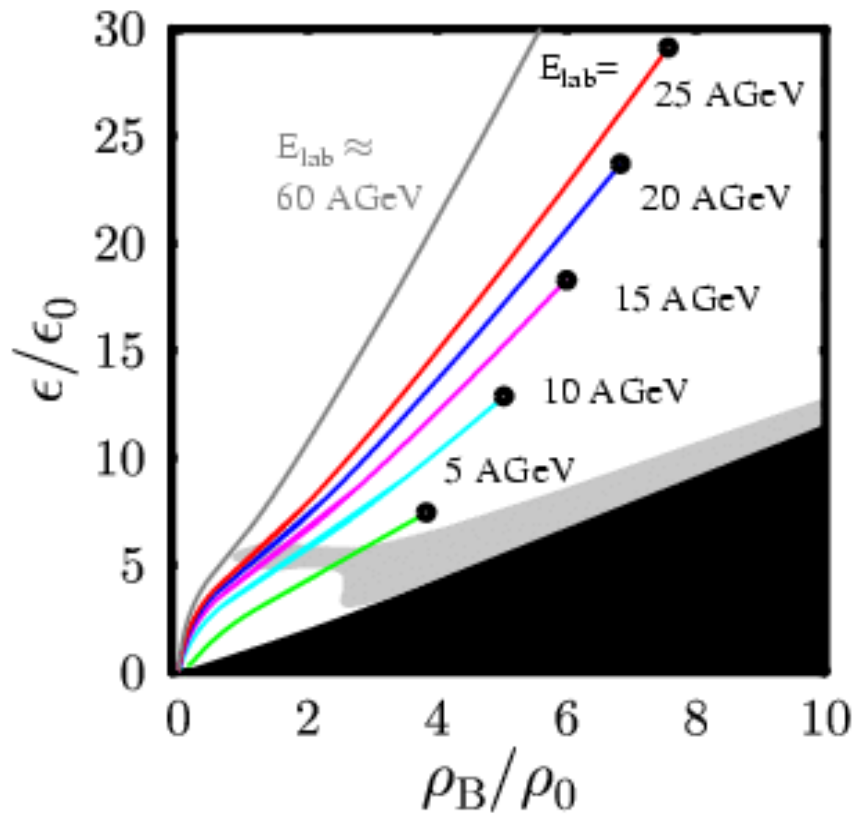
$$\ell = (1/N) \text{tr } L: \text{ Polyakov loop}$$

$$Z = \int dL \exp[-V_{gl}(\ell) - V_{qk}(\ell, \mu)]$$

$$\rightarrow \int dL \exp[-V_{gl}(\ell) - V_{qk}(\ell, \mu=0)]$$

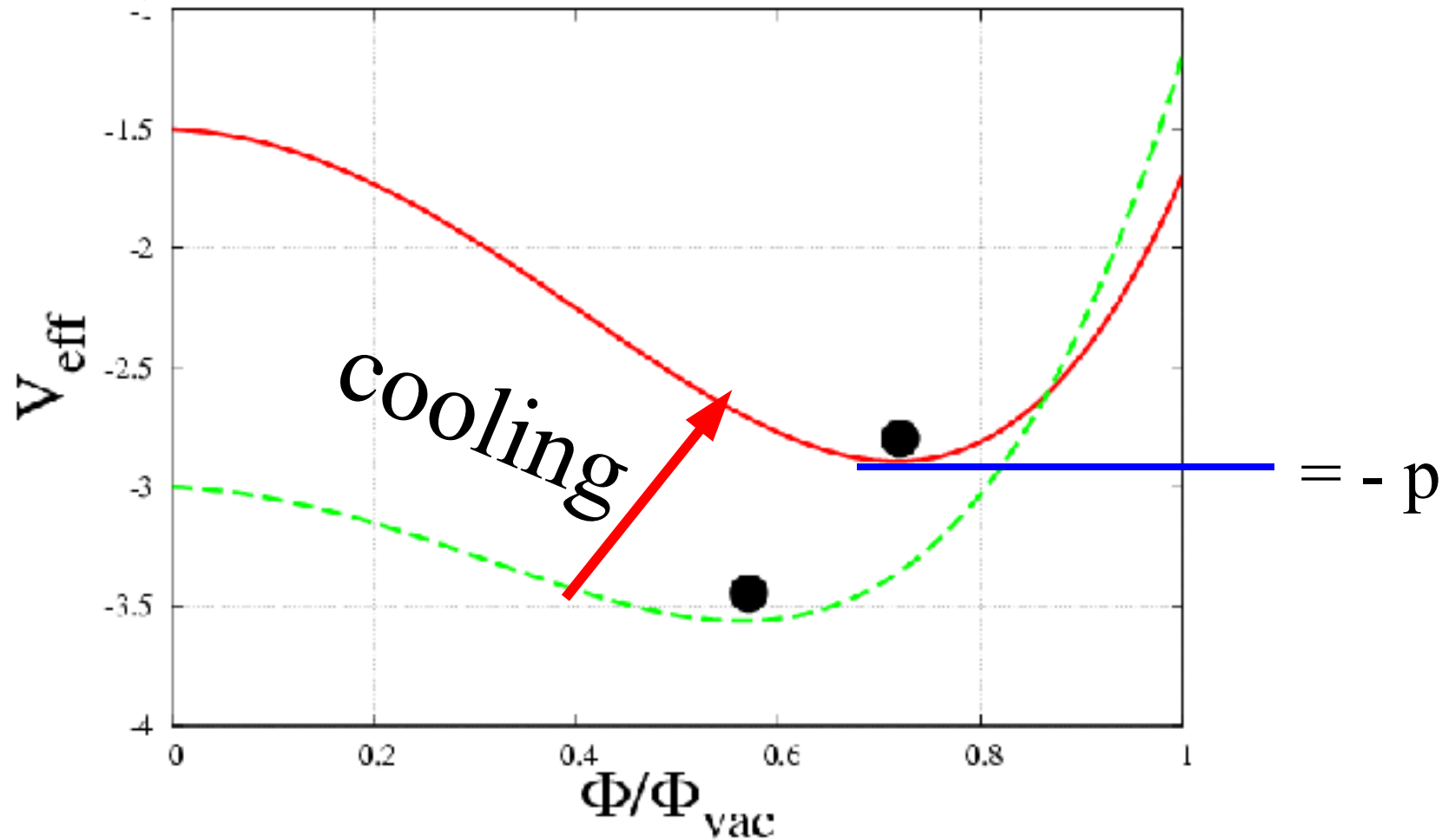
μ -effects are $O(1/N)$:

T_c depends weakly on μ



- ★ How does the transition to the broken state happen ?
 → real-time dynamics of order parameter

Cross over

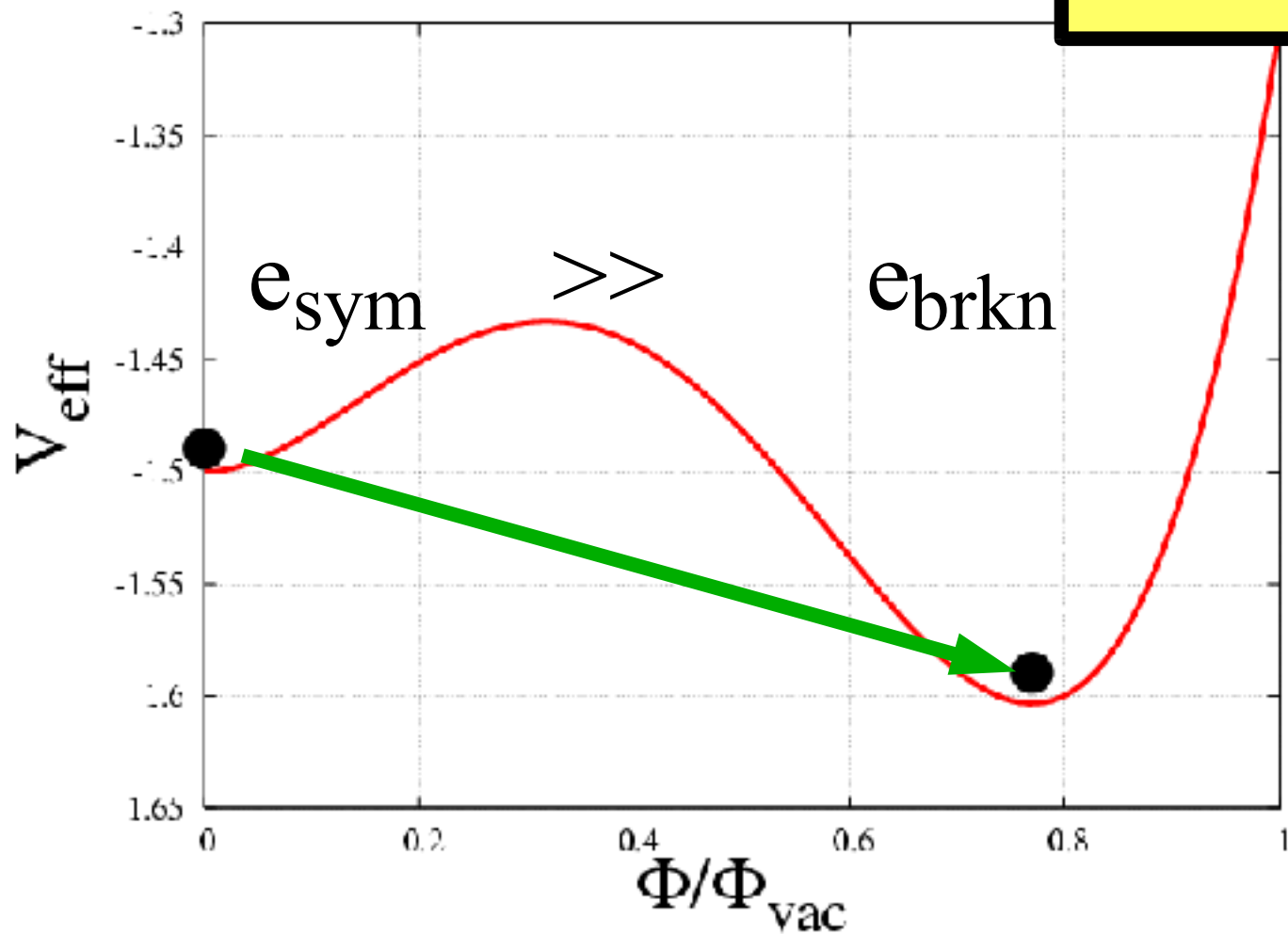
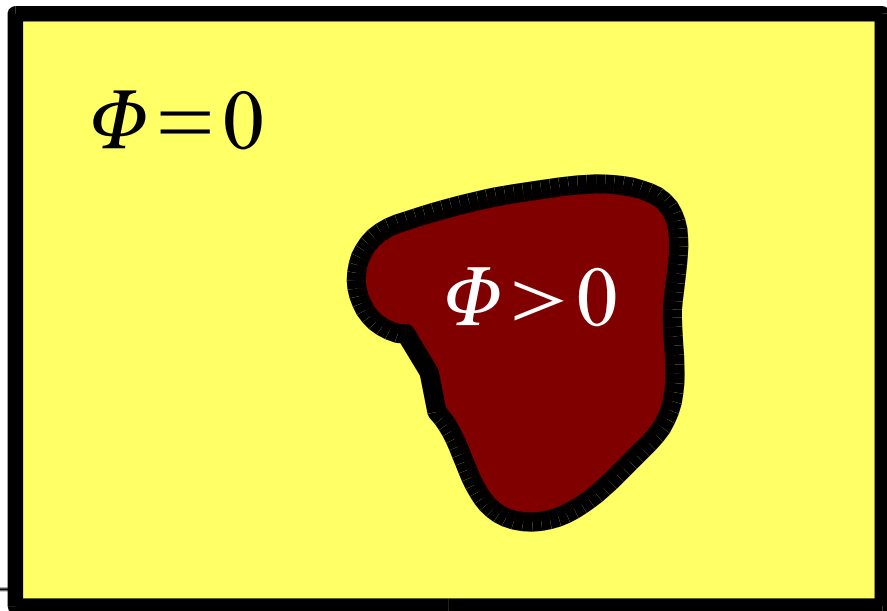


★ e varies smoothly with Φ

→ expect relatively homogeneous system

Thermal 1st-O transition

→ produce inhomogeneities !



Gell-Mann Levy Model

$$L = \bar{\Psi} \left[i \partial_\mu \gamma^\mu - g (\sigma + i \gamma_5 \vec{\tau} \vec{\pi}) \right] \Psi + \frac{1}{2} (\partial_\mu \Phi)^2 - U(\Phi)$$

$$U(\Phi) = \frac{\lambda}{4} (\Phi^2 - v^2)^2 - h \Phi_0$$

tilted “Mexican hat”
vacuum potential

$$\Phi^a = (\sigma, \vec{\pi}) \quad \text{O(4) chiral vector}$$

$T, \mu > 0$: q's constitute thermalized fluid:
integrate out the quarks (1 loop)

$$V_{eff} = U(\Phi) + V_T(\Phi)$$

$$V_T(\Phi) = T v_q \int \frac{d^3 p}{(2\pi)^3} \log \left(1 + e^{-\frac{E+\mu}{T}} \right) + \log \left(1 + e^{-\frac{E-\mu}{T}} \right)$$

EoM:
$$\partial_\mu \partial^\mu \Phi^a + \frac{\delta V_{eff}}{\delta \Phi^a} = 0$$

$$\partial_\mu (T_{fl}^{\mu\nu} + T_\Phi^{\mu\nu}) = 0 \quad , \quad \partial_\mu (\rho u^\mu) = 0$$

ideal fluid of quarks:
$$T_{fl}^{\mu\nu} = (e + p) u^\mu u^\nu - p g^{\mu\nu}$$

one-loop \rightarrow ideal gas of massive q's, $m_q = \sqrt{g^2 \Phi^2}$

$$p = p(e, \rho, \Phi)$$

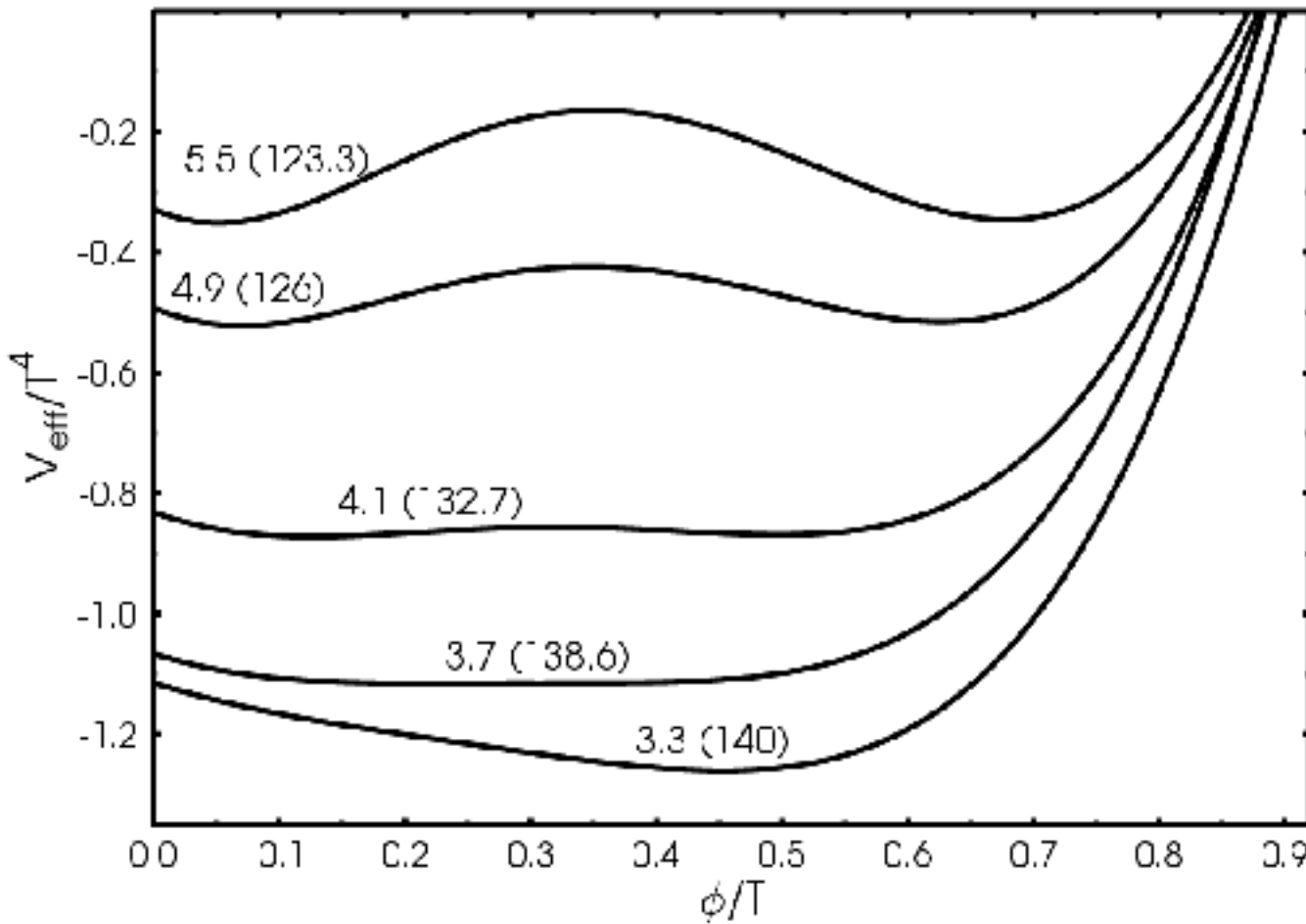
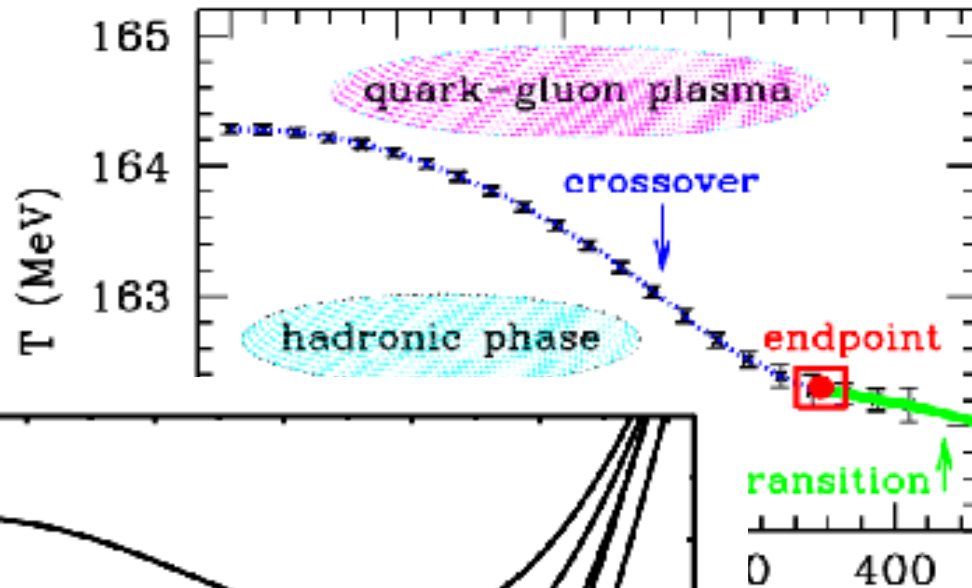
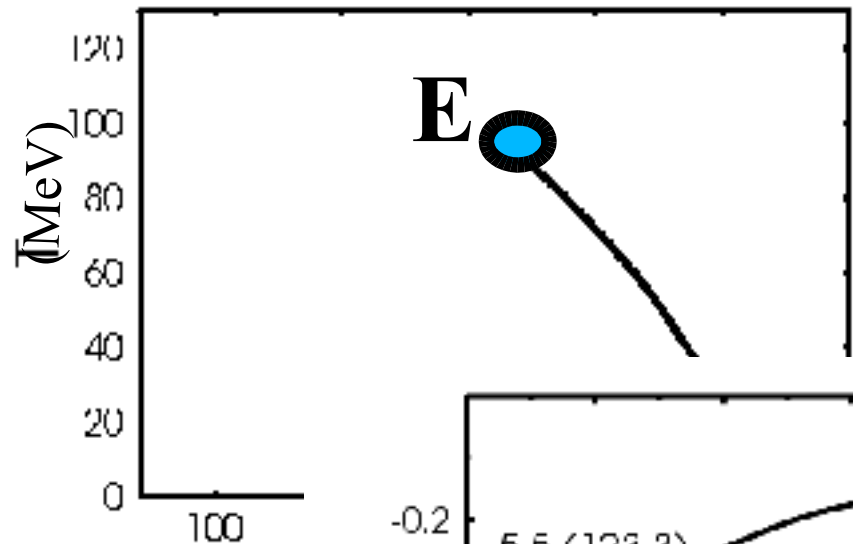
in equilibr. $\Phi = \Phi_0(T, \mu)$ is the minimum of $V_{eff}(T, \mu)$

Scavenius, Mishustin, '97, '98; D.T. Son, '00;

3D solution with classical order parameter fluctuations:

Kerstin Paech, PhD, Frankfurt Univ., '01-'05

The phase diagram for $m_{q,vac} \approx 310 \text{ MeV}$



E: Stephanov,]

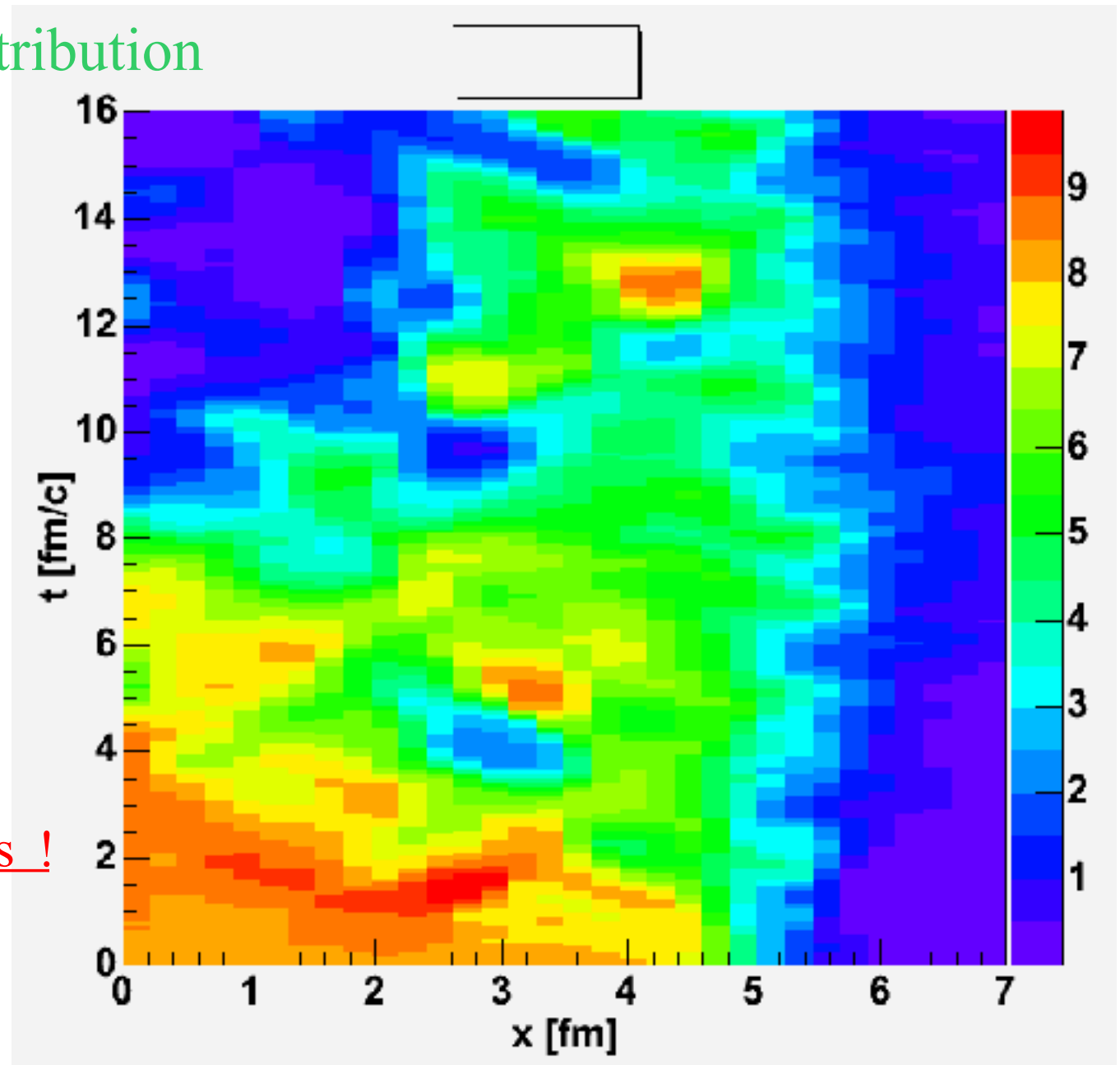
IEP 0404 ('04)

First-order transition, computed dynamically

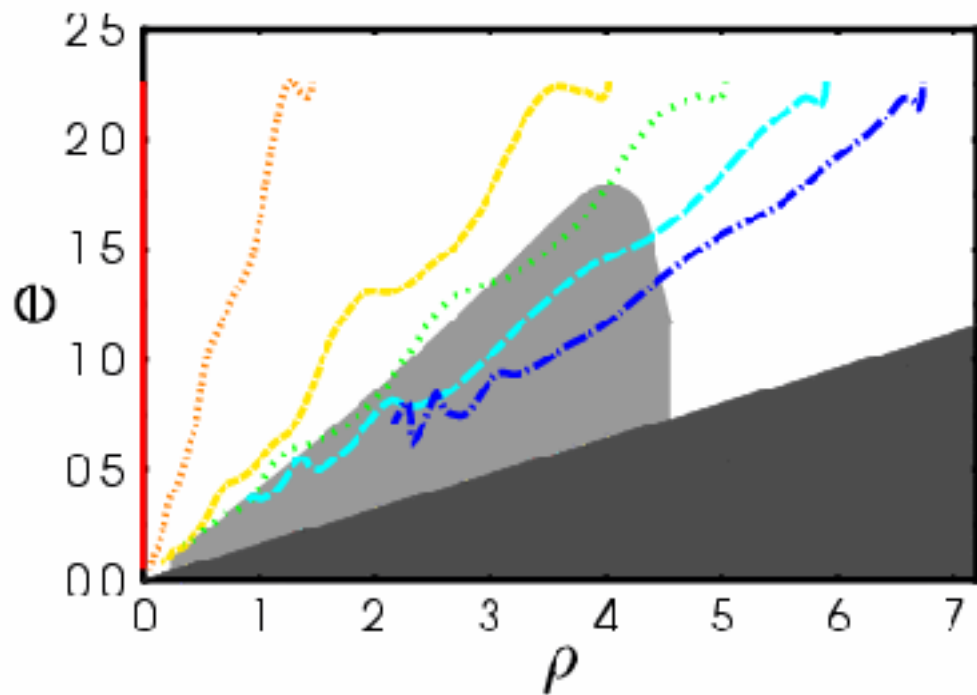
Energy density distribution

- ★ Hot & Dense Spots
- ★ Voids ...

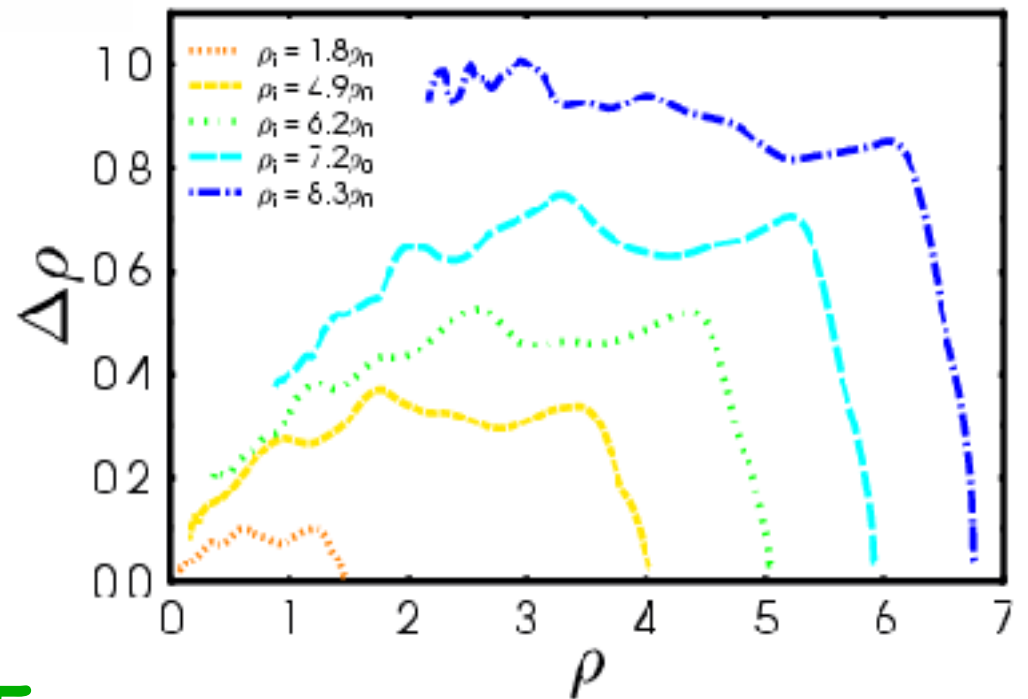
→ 1st-O transitions
lead to inhomogeneities !



K. Paech, H. Stöcker, AD: PRC 68 (2003)



$$e_1 - 2.8 e_0$$



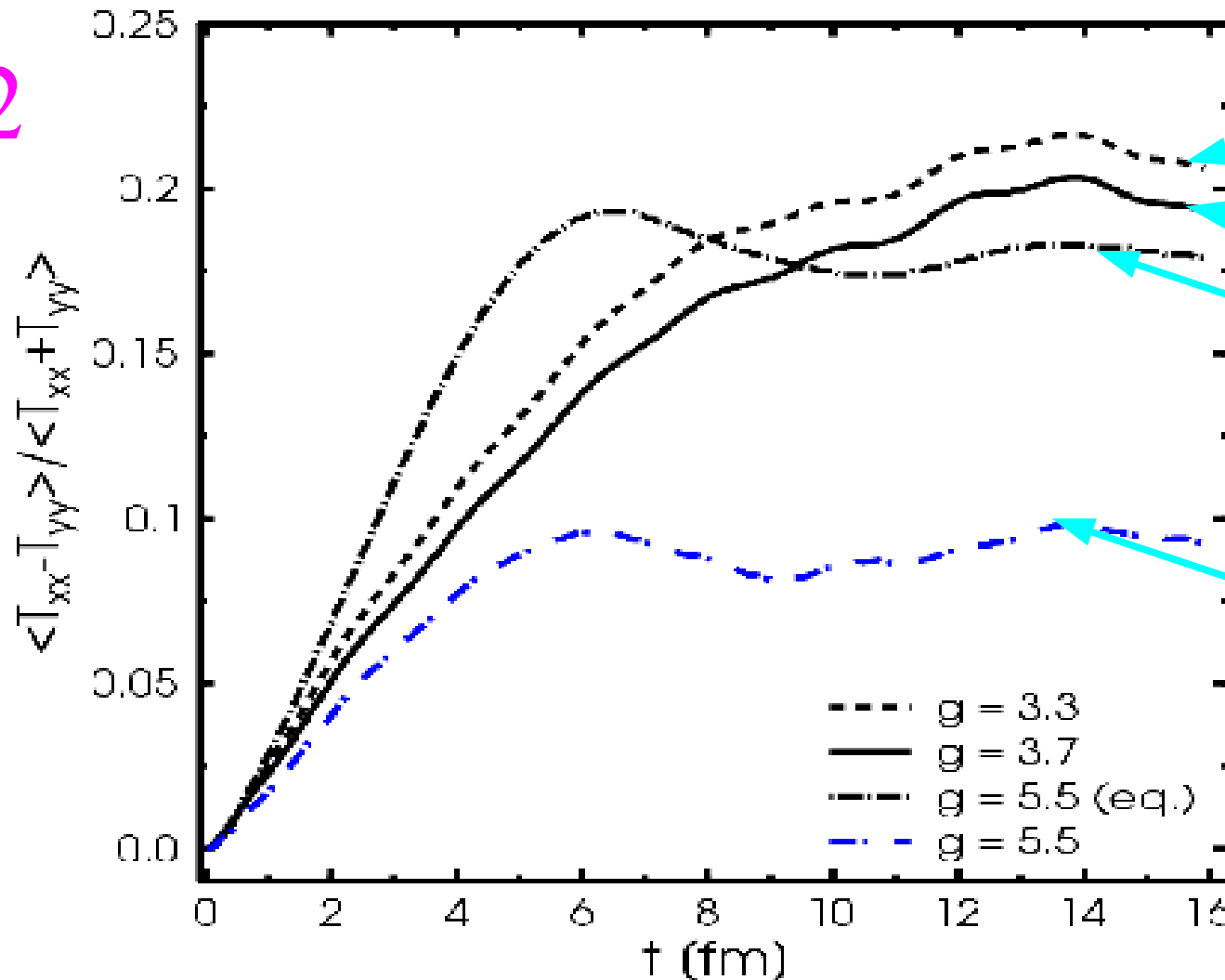
Kerstin Paech, PLB '05

Observables
for CBM @ FAIR ?

Flow must be affected

Geometry of field fluctuations uncorrelated to reaction plane

v_2



cross over

crit. endpoint

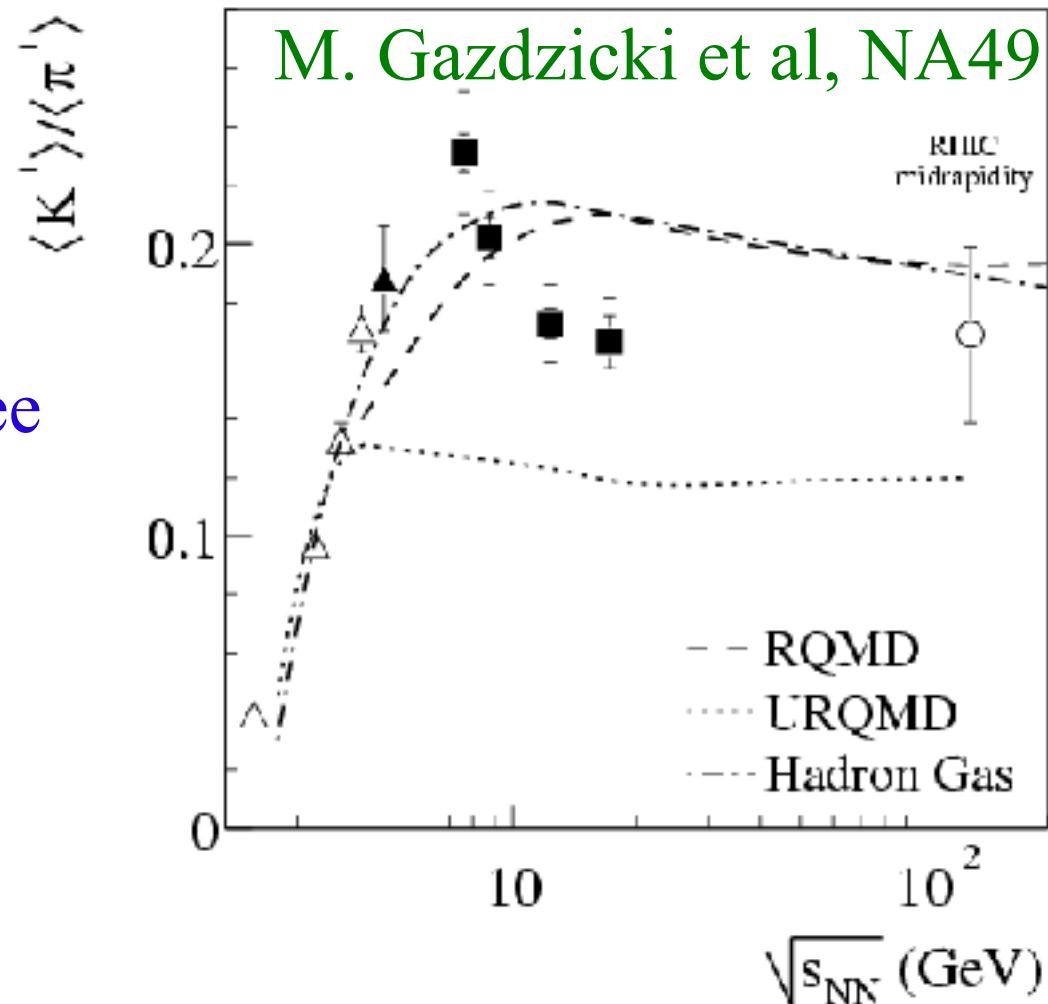
equilib. 1st-O transition

dynamical 1st-O transition

Density Perturbations on the f.o. surface might reflect in hadron “chemistry” !

for example, K^+/π^+ @ SPS is not reproduced well by homog. hadron gas:

even though T, μ are free fit parameters !



★ inhomog. f.o. surface, simple model:

L. Portugal, D. Zschiesche + A.D., '05

take T, μ as Gaussian random variables,

$$P[T] \sim \exp -\frac{(T - \bar{T})^2}{2 \delta T^2} \quad P[\mu] \sim \exp -\frac{(\mu - \bar{\mu})^2}{2 \delta \mu^2}$$

This is the distribution on the f.o. surface in each event!

Do not confuse with EbyE fluctuations !

(If # of “domains” is large, EbyE flucs $\rightarrow 0$)

$$N_i = Vol_3 \times \bar{\rho}_i(\bar{T}, \bar{\mu}, \delta T, \delta \mu)$$
$$\bar{\rho}_i(\bar{T}, \bar{\mu}, \delta T, \delta \mu) = \int dT P[T] \int d\mu P[\mu] \rho_i(T, \mu)$$
$$\neq \rho_i(\bar{T}, \bar{\mu}) \quad \text{!}$$

Also check coalescence of nuclei: d, t, α !

Summary

- ★ Real-Time dynamics of 1st-O transition needs to be studied
- ★ Aside from critical fluctuations, changes in bulk evolution may also reflect the crossing of E
- ★ Relatively clean experim. observables
 - Flow
 - Inhomog. predicted for 1st-O, affects flow (v_i), hadron ratios etc

Theory/Modeling permits lots of improvement, examples:

- More realistic EoS/endpoint: include more hadrons
- Quantitative initial conditions from 3-fluid hydro or hadron transport models
- Freeze-out
- Integrate out “hard” field flucs also to 1-loop
- ...