

TMD's in $p \uparrow l \rightarrow \pi + X$



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Outline

- ◇ SIDIS vs inclusive hadron production
- ◇ The Single Spin Asimmetry A_N
- ◇ Sivers contribution to A_N
- ◇ Transversity-Collins contribution to A_N
- ◇ Conclusions

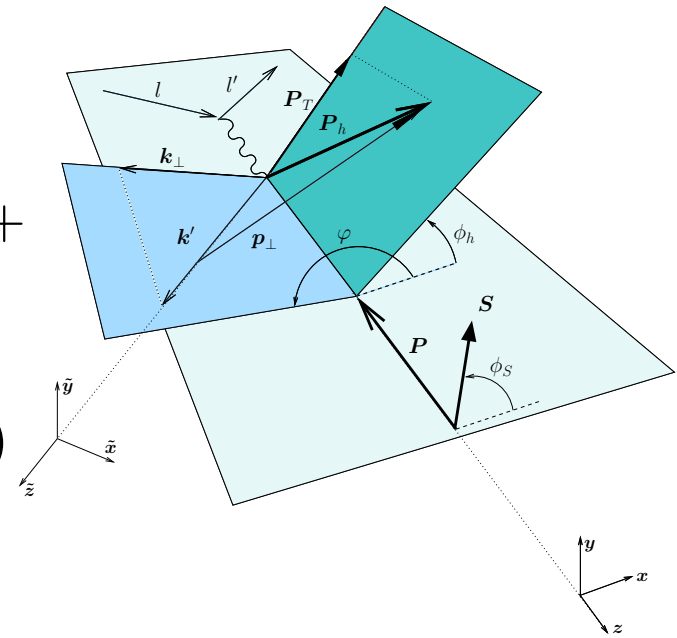
Polarized SIDIS

➤ Asymmetry A_{UT} in the γ^*p c.m. frame:

$$A_{UT} = \frac{d^6\sigma^{lp^\uparrow \rightarrow l'hX} - d^6\sigma^{lp^\downarrow \rightarrow l'hX}}{\frac{1}{2}[d^6\sigma^{lp^\uparrow \rightarrow l'hX} + d^6\sigma^{lp^\downarrow \rightarrow l'hX}]} \equiv 2 \frac{d\sigma^\uparrow - d\sigma^\downarrow}{d\sigma^\uparrow + d\sigma^\downarrow}$$

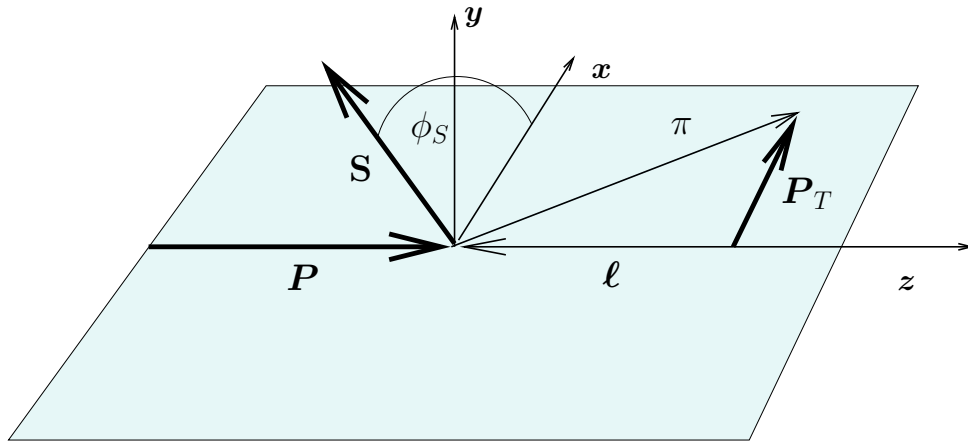
where $d^6\sigma^{lp^\uparrow \rightarrow l'hX} = d^6\sigma/dx_B dy dz_h d^2\mathbf{P}_T d\phi_h$

$$\begin{aligned} d\sigma^\uparrow - d\sigma^\downarrow \propto & \Delta^N f_{q/p^\uparrow} \otimes d\hat{\sigma} \otimes D_{h/q} \sin(\phi_h - \phi_S) + \\ & + \Delta_T q \otimes \Delta\hat{\sigma}^\uparrow \otimes \Delta^N D_{h/q^\uparrow} \sin(\phi_h + \phi_S) \\ & + h_{1T}^\perp \otimes \Delta\hat{\sigma}^\uparrow \otimes \Delta^N D_{h/q^\uparrow} \sin(3\phi_h - \phi_S) \end{aligned}$$



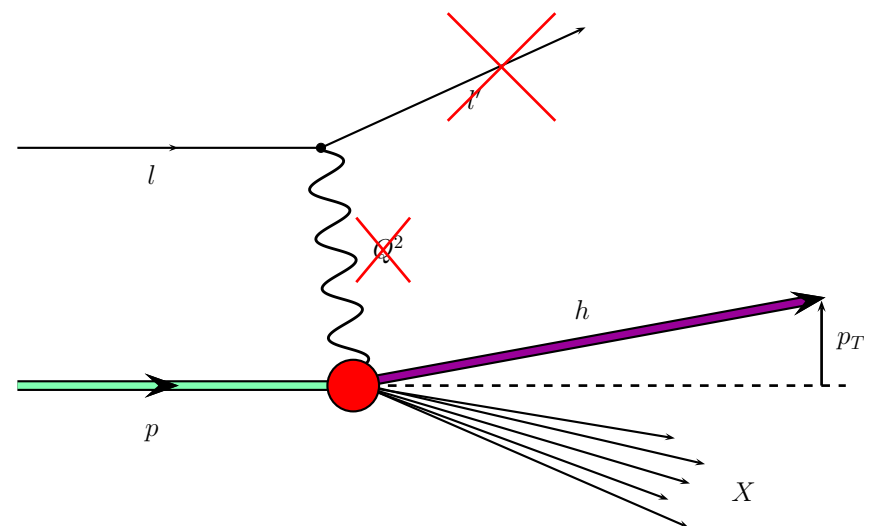
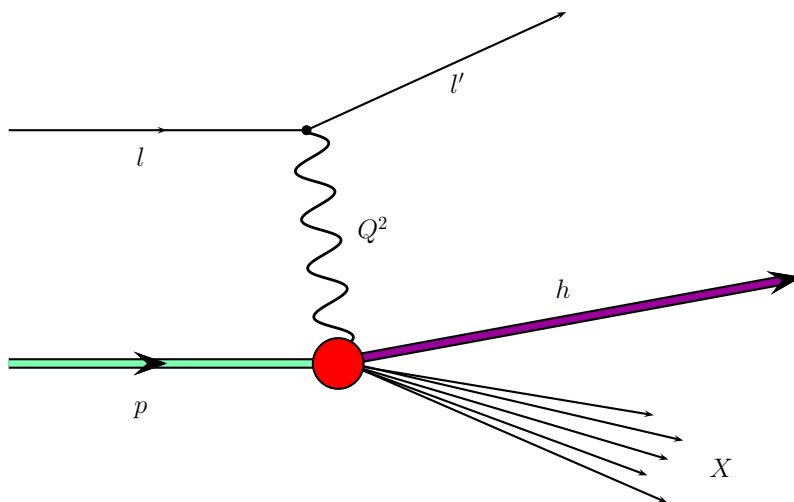
⇒ Separation of the Sivers and Collins effects

$$p \uparrow l \rightarrow h + X$$



- proton-lepton c.m. frame
- p is along the $+Z$ -axis,
- ϕ_S is the azimuthal of S_T
- h in the XZ plane
- Only h is detected

➤ If $P_T \gtrsim 1$ GeV then we are in a “perturbative” regime.



The single spin asymmetry A_N

➤ We can define the single spin asymmetry A_N :

$$A_{TU}(\phi_S) \equiv \frac{d\sigma(\phi_S) - d\sigma(\phi_S + \pi)}{\frac{1}{2}[d\sigma(\phi_S) + d\sigma(\phi_S + \pi)]}; \quad A_{TU}(\phi_S) = 2 |S_T| A_N \sin \phi_S$$

➤ Therefore A_N can be written as:

$$A_N = \sum_i \frac{1}{2 |S_T| \sin \phi_{Si}} A_{TU}^i$$

or weighting A_{TU} with $\sin \phi_S$:

$$A_N = \frac{1}{2 |S_T| [\sum_i \sin^2 \phi_{Si}]} \sum_i A_{TU}^{\sin \phi_{Si}}$$

The single spin asymmetry A_N

➤ Assuming the factorization, at born level, A_N can be written as:

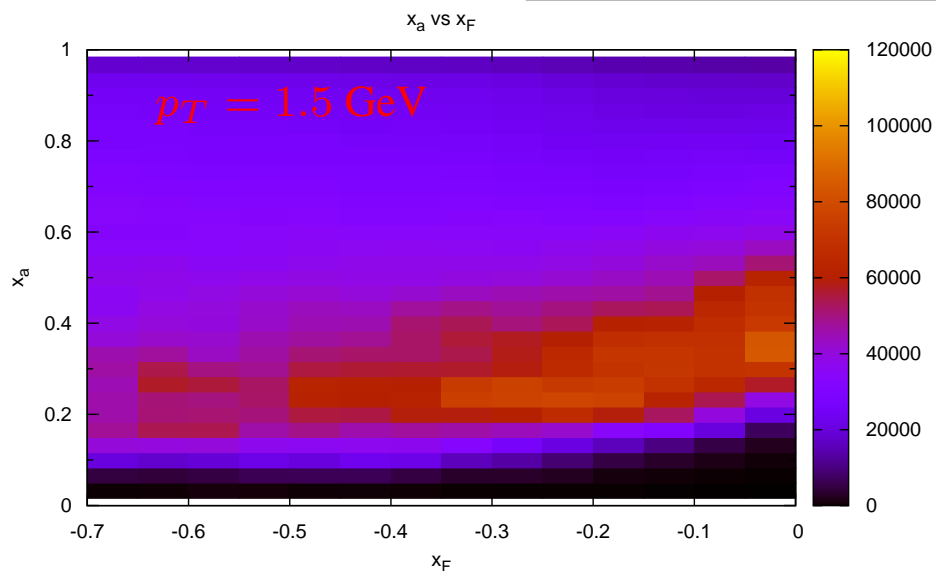
$$A_N \propto \frac{1}{2d\sigma_{unp}} \left[\Delta^N f_{q/p\uparrow} \otimes d\hat{\sigma} \otimes D_{h/q} + \Delta_{Tq} \otimes \Delta\hat{\sigma}^\uparrow \otimes \Delta^N D_{h/q\uparrow} + h_{1T}^\perp \otimes \Delta\hat{\sigma}^\uparrow \otimes \Delta^N D_{h/q\uparrow} \right]$$

- The Sivers and the Collins effect add up, h_{1T}^\perp contribution is negligible
- $d\sigma$ is differential in $d^3\mathbf{p}_h$ ($x_F = \frac{2p_L}{\sqrt{s}}$ and p_T): x_a integrated from x_a^{min} to 1

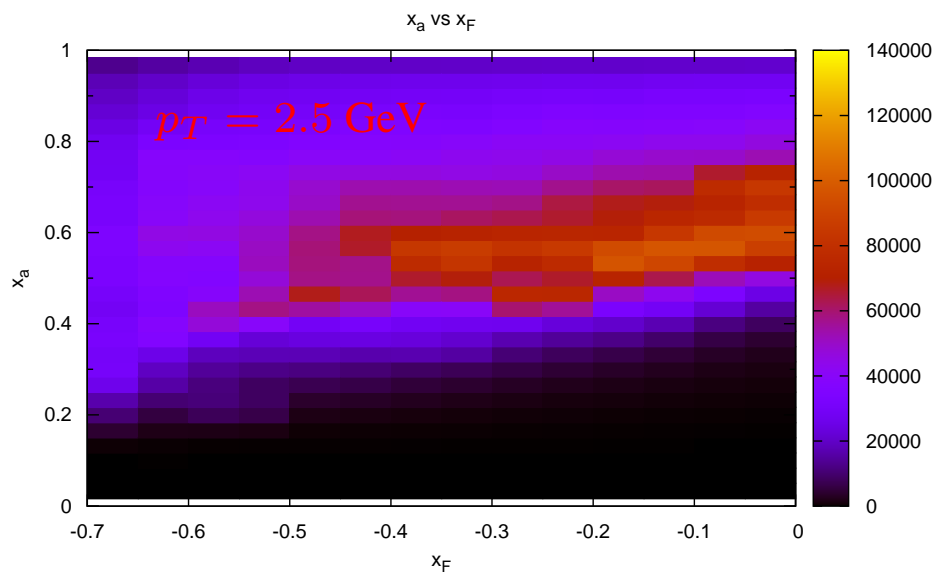
In collinear approximation: $x_a^{min} = \frac{\sqrt{(P_T^2 + P_L^2)} + P_L}{\sqrt{s}}$

➤ Possibility to extend the x_a region explored?? (consistently to exp. cuts)

Kinematics at HERMES:



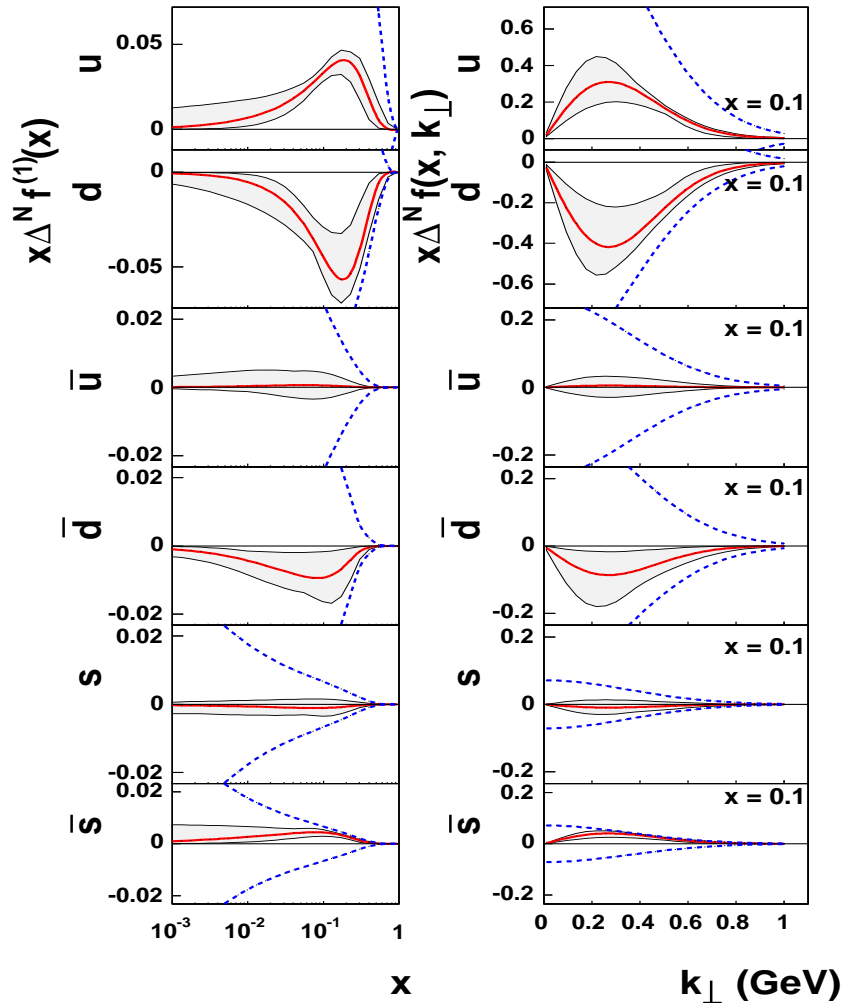
- x_a vs x_F at $\sqrt{s} = 7.24$ GeV and $p_T = 1.5$ GeV



- x_a vs x_F at $\sqrt{s} = 7.24$ GeV and $p_T = 2.5$ GeV

Estimation of A_N from the Sivers and the Collins effects

First moment of the Sivers functions



◇ For valence quarks:

- $\Delta^N f_{u/p^\uparrow} > 0$
- $\Delta^N f_{d/p^\uparrow} < 0$

◇ For sea quarks:

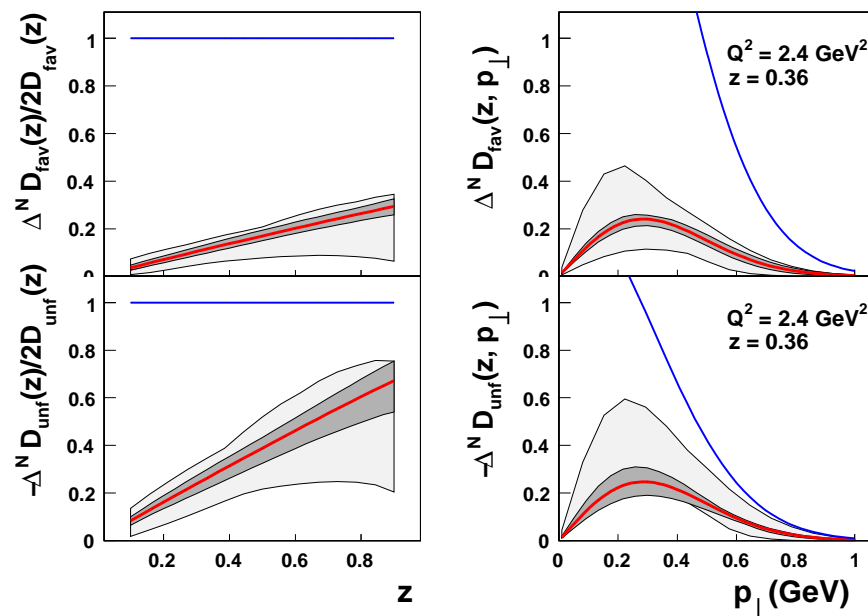
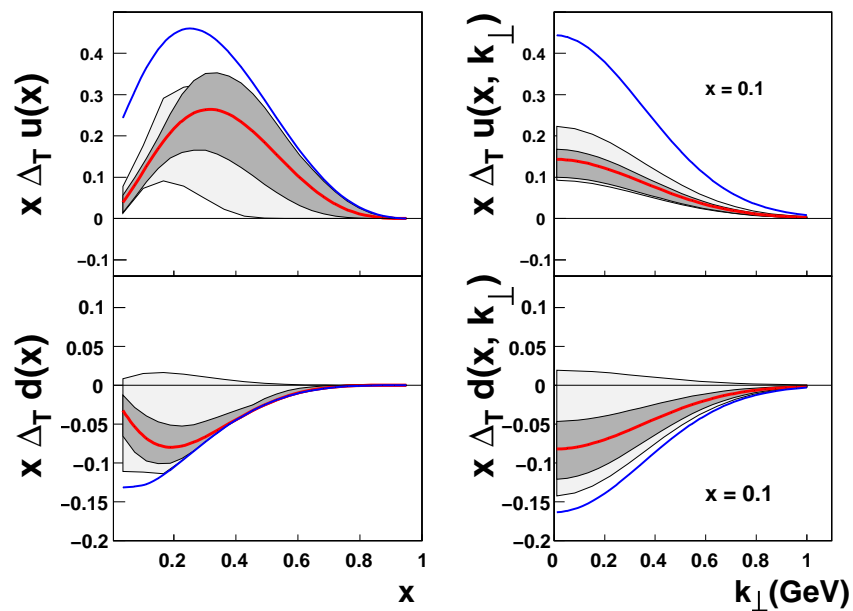
- $\Delta^N f_{\bar{s}/p^\uparrow} > 0$

$$\diamond \Delta^N f_q^{(1)}(x) \equiv \int d^2 \mathbf{k}_\perp \frac{k_\perp}{4m_p} \Delta^N f_{q/p^\uparrow}(x, k_\perp) = -f_{1T}^{\perp(1)q}(x)$$

Transversity and Collins functions

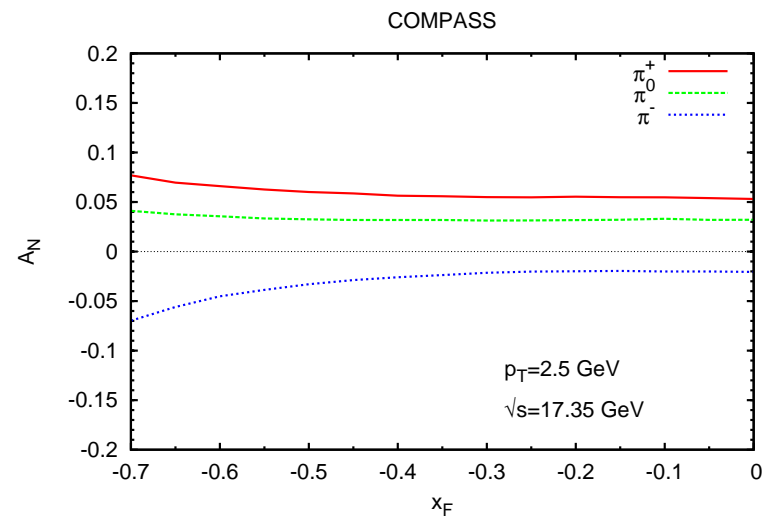
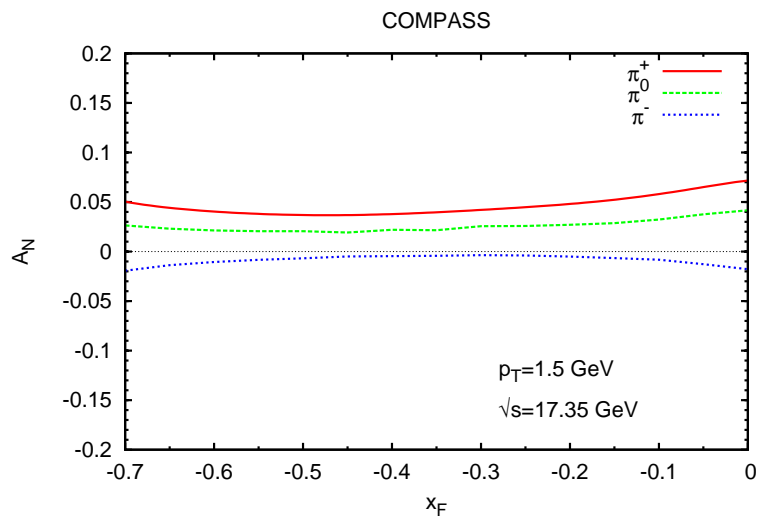
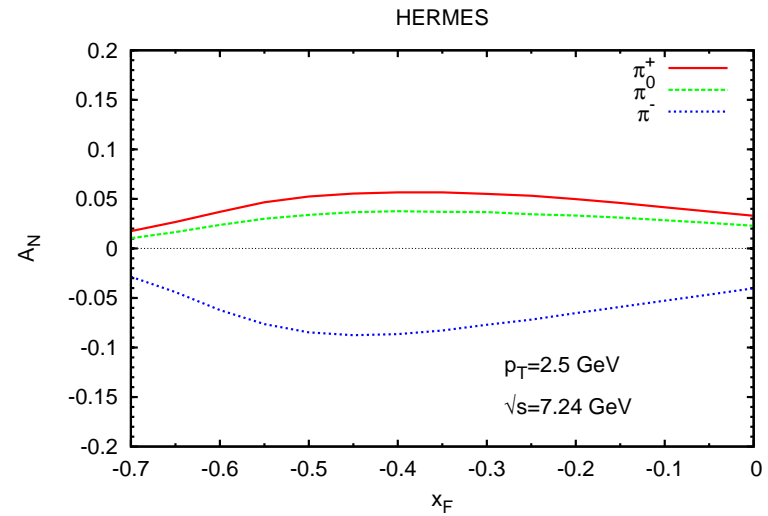
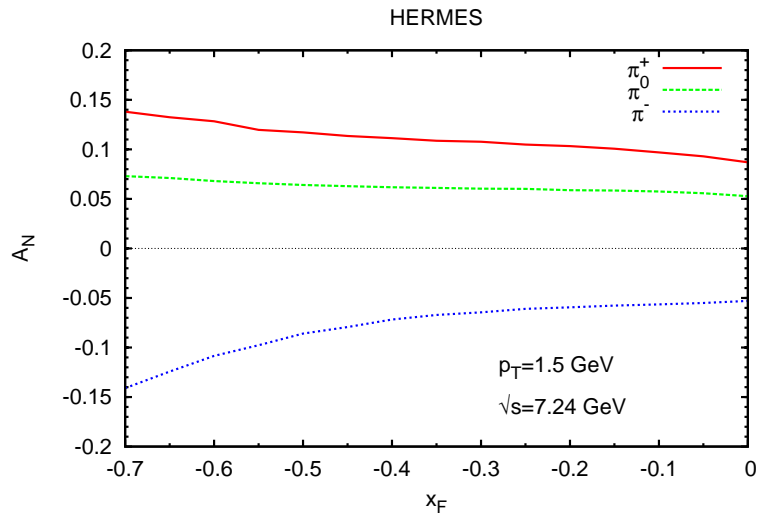
◇ Transversity: u and d

◇ Collins functions: favored and unfavored



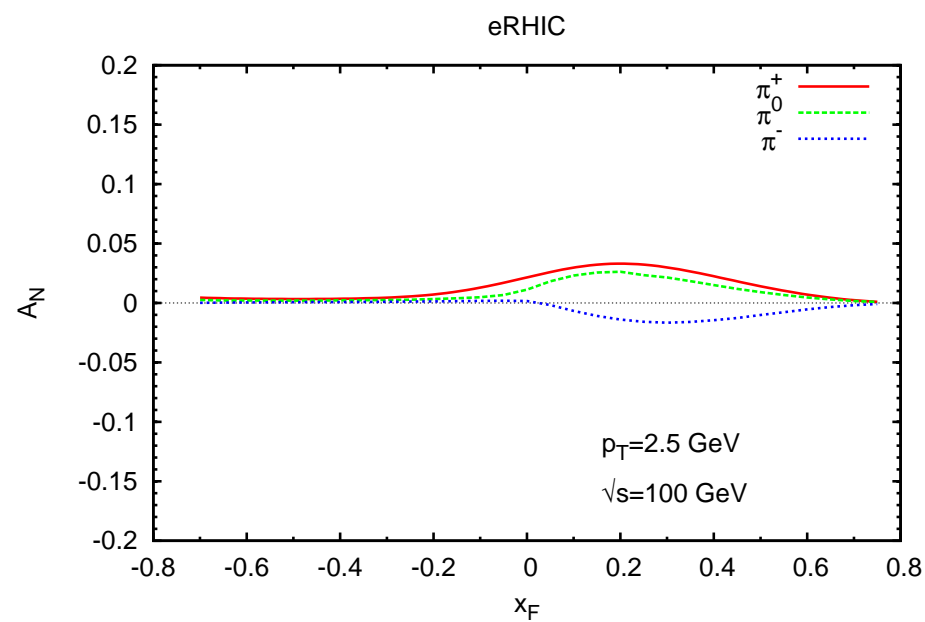
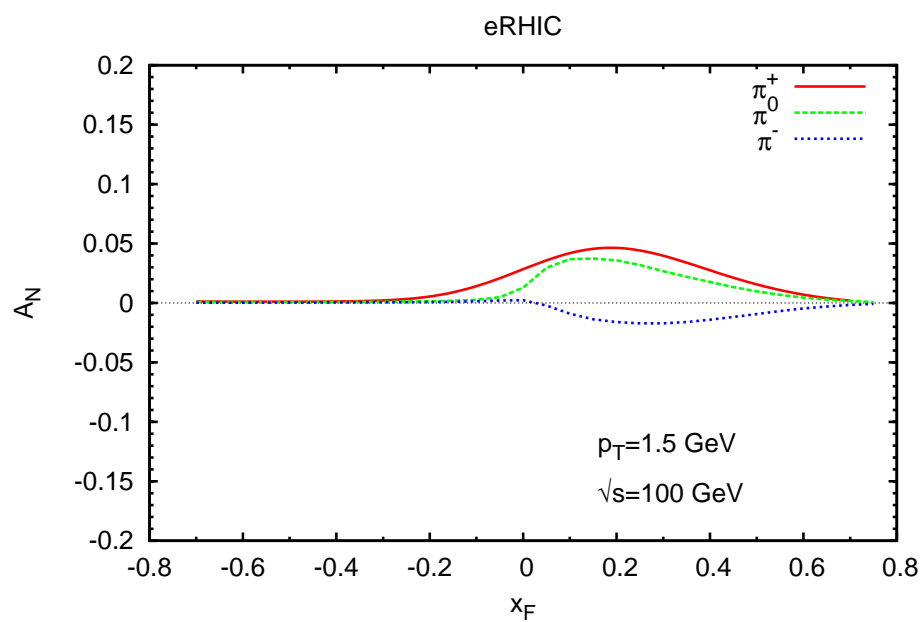
Sivers Effect at HERMES and COMPASS:

➤ Sivers effect



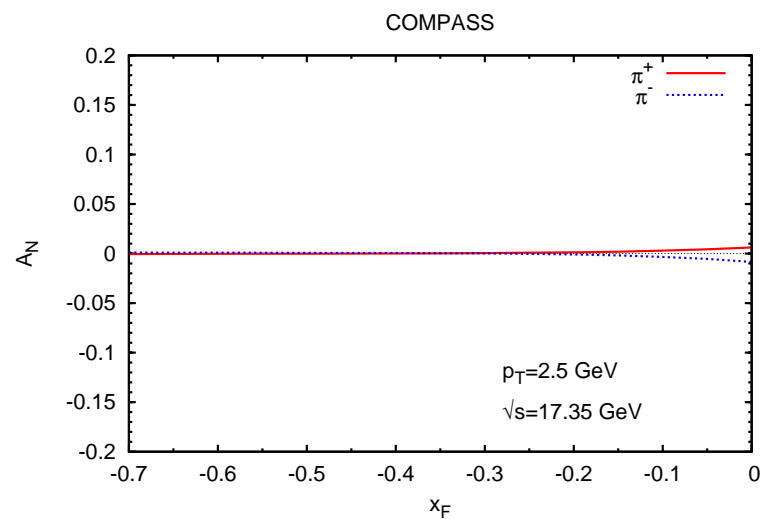
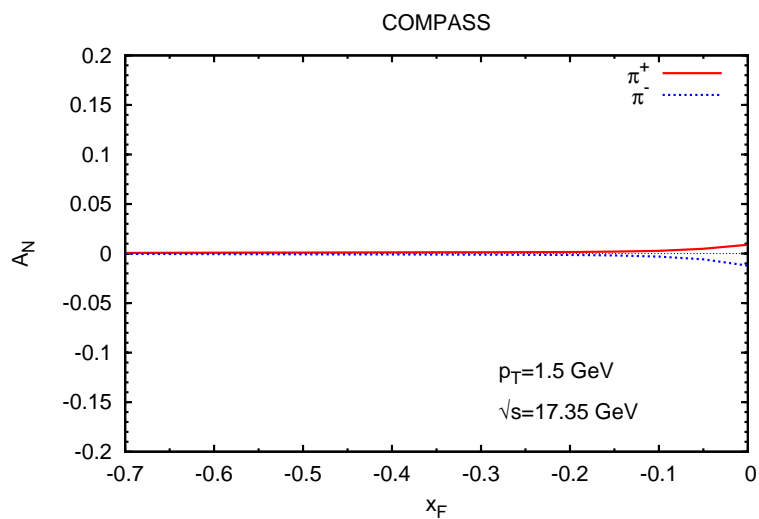
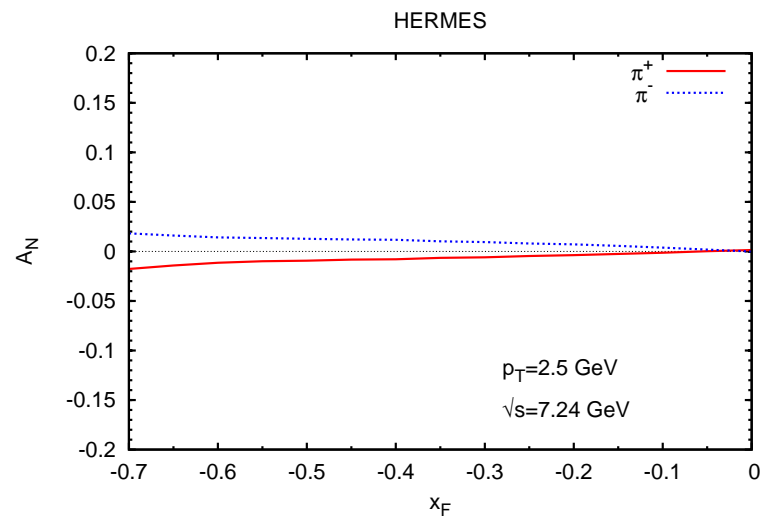
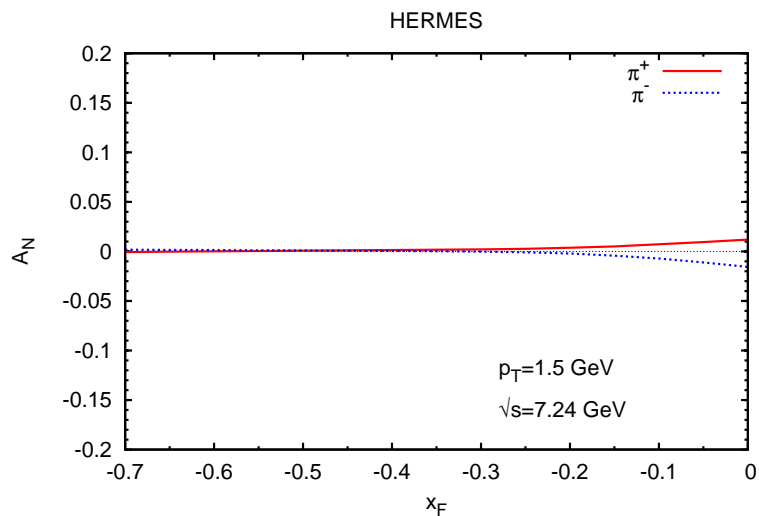
Sivers Effect at eRHIC:

➤ Sivers effect



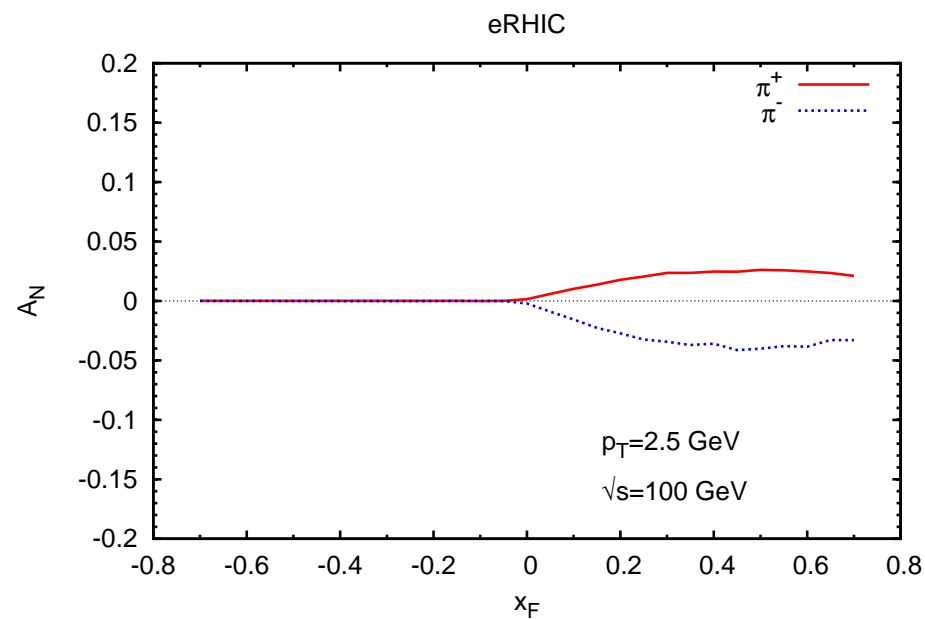
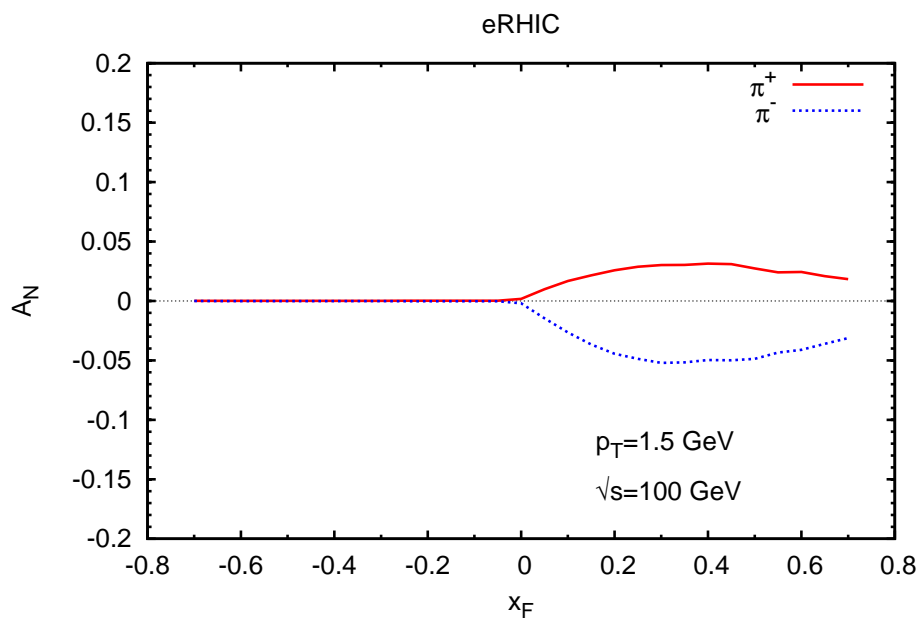
Collins Effect at HERMES and COMPASS:

➤ Collins effect



Collins Effect at eRHIC:

➤ Collins effect



Summary and Conclusions

- Inclusive hadron production in $p^\uparrow l$ scattering
- Factorization assumed: experimental test
- Different kinematical regions covered with respect to SIDIS
- Sivers effect can be large
- Transversity \otimes Collins effect small in some kinematical regions
- ...only preliminary results

Parametrizations:

➤ We assume a factorized gaussian smearing for the unpolarized PDF and FF:

$$\diamond f_{q/p}(x, k_{\perp}) = f_q(x) \frac{1}{\pi \langle k_{\perp}^2 \rangle} e^{-k_{\perp}^2 / \langle k_{\perp}^2 \rangle} \quad \diamond D_q^h(z, p_{\perp}) = D_q^h(z) \frac{1}{\pi \langle p_{\perp}^2 \rangle} e^{-p_{\perp}^2 / \langle p_{\perp}^2 \rangle}$$

$$\langle k_{\perp}^2 \rangle = 0.25 \text{ (GeV}/c)^2 \qquad \langle p_{\perp}^2 \rangle = 0.20 \text{ (GeV}/c)^2 .$$

$\langle k_{\perp}^2 \rangle$ and $\langle p_{\perp}^2 \rangle$ fixed as found in Ref. [1] by analysing the Cahn effect.

➤ Similarly for the Sivers function:

$$\Delta^N f_{q/p\uparrow}(x, k_{\perp}) = 2 \mathcal{N}_q(x) h(k_{\perp}) f_{q/p}(x, k_{\perp})$$

$$\mathcal{N}_q(x) = N_q x^{\alpha_q} (1-x)^{\beta_q} \frac{(\alpha_q + \beta_q)^{(\alpha_q + \beta_q)}}{\alpha_q^{\alpha_q} \beta_q^{\beta_q}} \leq 1, \quad h(k_{\perp}) = \sqrt{2} e \frac{k_{\perp}}{M_1} e^{-k_{\perp}^2 / M_1^2} \leq 1,$$

where N_q , α_q , β_q and M_1 (GeV/c) are free parameters

Fit of HERMES & COMPASS SIDIS data: Sivers functions

- ◇ GRV98 set for PDF's
- ◇ DSS set for FF's
- ◇ $\langle k_{\perp}^2 \rangle$ and $\langle p_{\perp}^2 \rangle$ from the Cahn Effect

➤ “Broken sea“ ansatz, 11 free parameters:

$$\begin{array}{ccc}
 N_u & & N_d \\
 N_{\bar{u}} & & N_{\bar{d}} \\
 N_s & & N_{\bar{s}} \\
 \alpha_u & \alpha_d & \alpha_{sea} \\
 \beta & & M_1
 \end{array}$$

$$\Delta^N f_{q/p\uparrow}(x, k_{\perp}) = 2 \mathcal{N}_q(x) h(k_{\perp}) f_{q/p}(x, k_{\perp})$$

$$\mathcal{N}_q(x) = N_q x^{\alpha_q} (1-x)^{\beta_q} \frac{(\alpha_q + \beta_q)^{(\alpha_q + \beta_q)}}{\alpha_q^{\alpha_q} \beta_q^{\beta_q}}$$

$$h(k_{\perp}) = \sqrt{2e} \frac{k_{\perp}}{M_1} e^{-k_{\perp}^2 / M_1^2}$$

$\chi^2/d.o.f = 1$		
$N_u = 0.35^{+0.078}_{-0.079}$	$N_d = -0.9^{+0.43}_{-0.098}$	$N_s = -0.24^{+0.62}_{-0.5}$
$N_{\bar{u}} = 0.037^{+0.22}_{-0.24}$	$N_{\bar{d}} = -0.4^{+0.33}_{-0.44}$	$N_{\bar{s}} = 1^{+0}_{-0.0001}$
$\alpha_u = 0.73^{+0.72}_{-0.58}$	$\alpha_d = 1.1^{+0.82}_{-0.65}$	$\alpha_{sea} = 0.79^{+0.56}_{-0.47}$
$\beta = 3.5^{+4.9}_{-2.9}$	$M_1^2 = 0.34^{+0.3}_{-0.16} \text{ GeV}^2$	

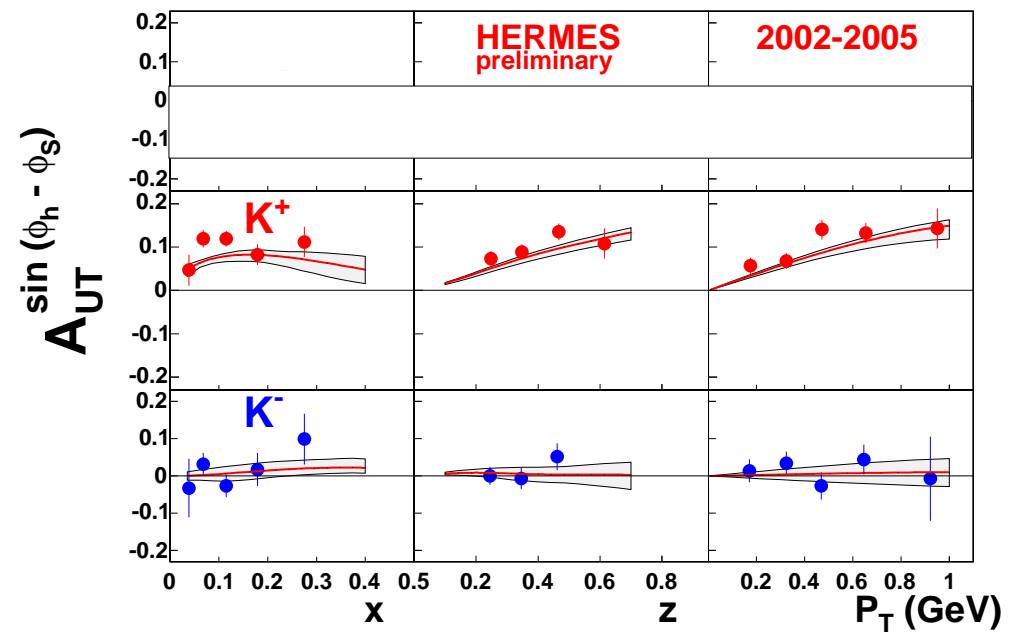
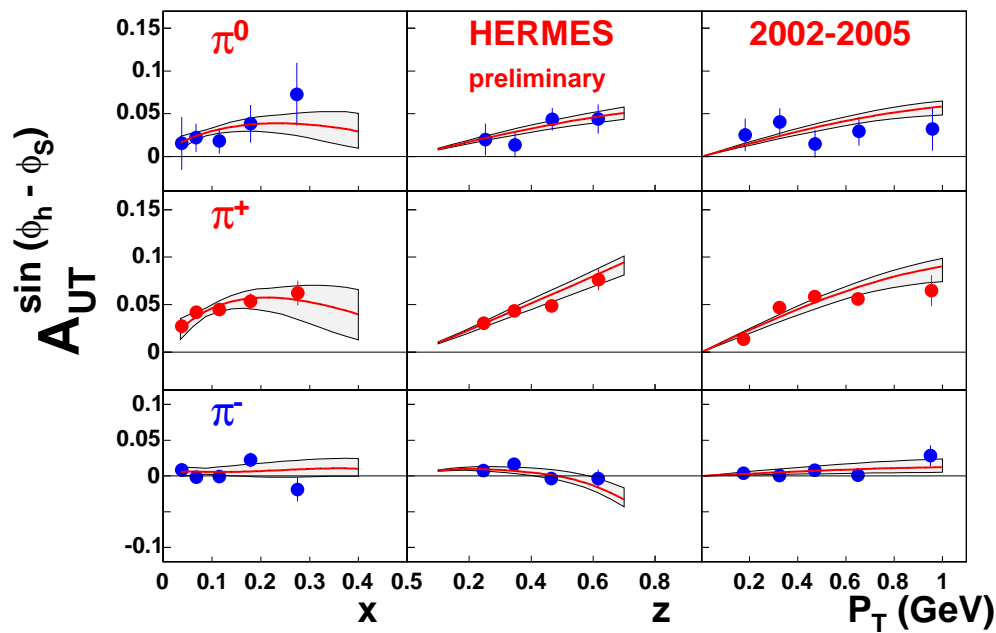
Fit: HERMES data

➤ HERMES data \diamond fit

$ep \rightarrow e\pi X$

$p_{lab} = 27.57 \text{ GeV}/c$

$ep \rightarrow eK X$



\diamond Diefenthaler, hep-ex/0612010 (2006)

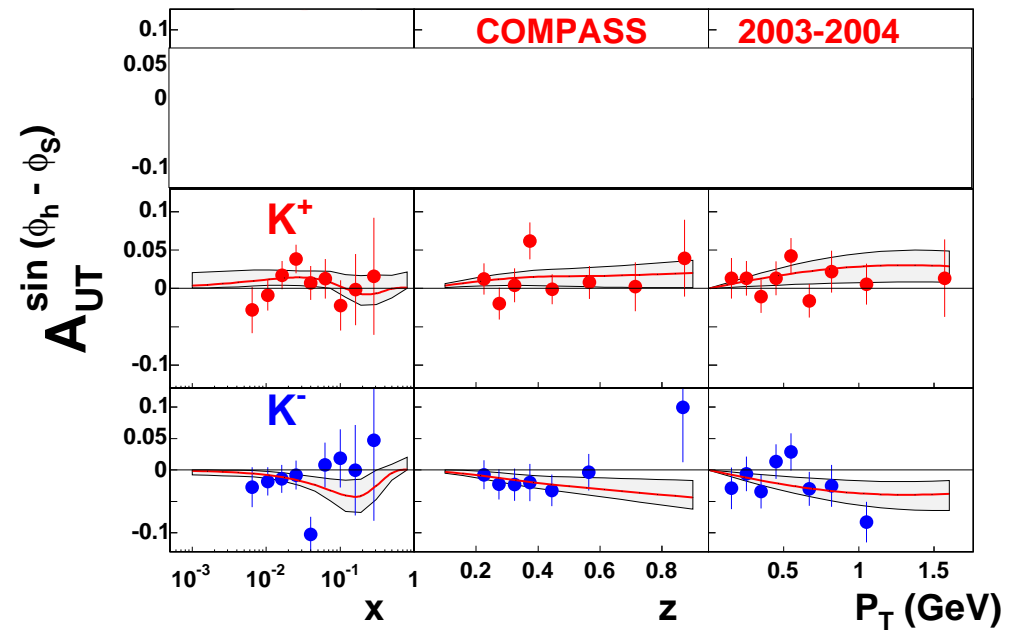
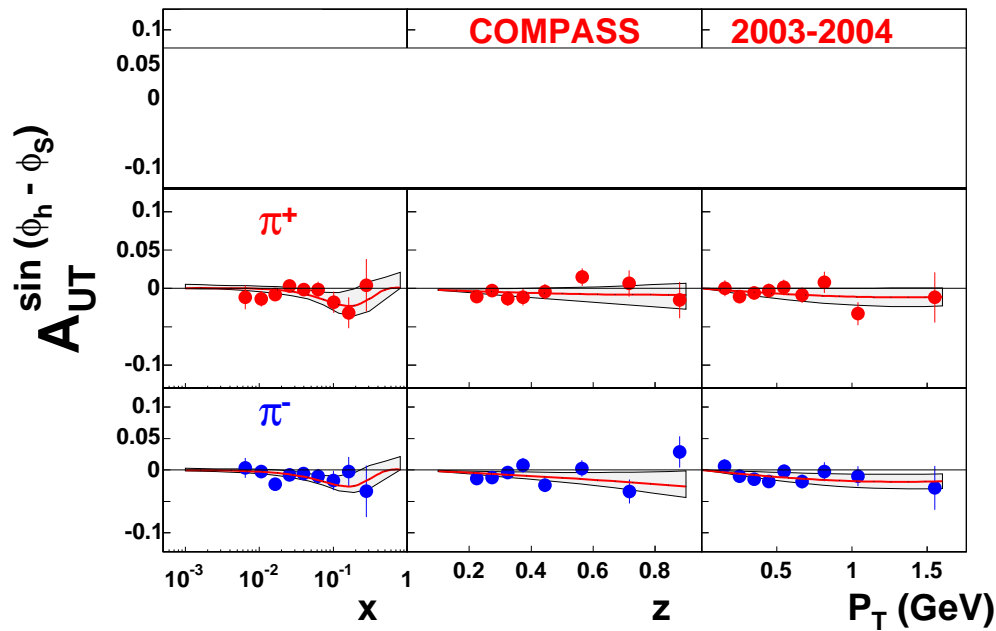
Fit: COMPASS data

➤ COMPASS data \diamond fit

$$\mu D \rightarrow \mu \pi X$$

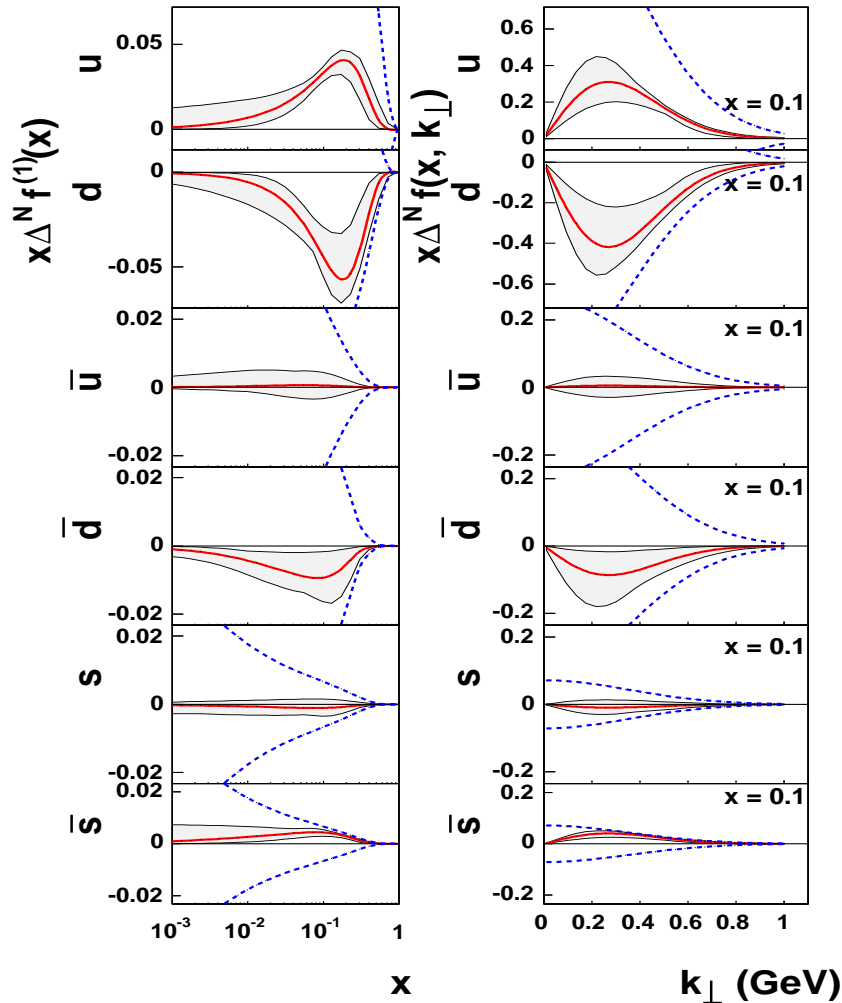
$$p_{lab} = 160 \text{ GeV}/c$$

$$\mu D \rightarrow \mu K X$$



\diamond A. Martin (COMPASS), Czech. J. Phys. 56, F33 (2006)

First moment of the Sivers functions



◇ For valence quarks:

- $\Delta^N f_{u/p^\uparrow} > 0$
- $\Delta^N f_{d/p^\uparrow} < 0$

◇ For sea quarks:

- $\Delta^N f_{\bar{s}/p^\uparrow} > 0$

◇
$$\Delta^N f_q^{(1)}(x) \equiv \int d^2 \mathbf{k}_\perp \frac{k_\perp}{4m_p} \Delta^N f_{q/p^\uparrow}(x, k_\perp) = -f_{1T}^{\perp(1)q}(x)$$

Parametrizations of the Transversity and the Collins function

➤ We assume a factorized gaussian smearing for $\Delta_T q(x)$ and $\Delta^N D_{\pi/q\uparrow}$:

$$\diamond \Delta_T q(x, k_\perp) = \frac{1}{2} \mathcal{N}_q^T(x) [f_{q/p}(x) + \Delta q(x)] \frac{1}{\pi \langle k_\perp^2 \rangle} e^{-k_\perp^2 / \langle k_\perp^2 \rangle}$$

$$\diamond \Delta^N D_{\pi/q\uparrow}(z, p_\perp) = 2 \mathcal{N}_q^C(z) h(p_\perp) D_{\pi/q}(z) \frac{1}{\pi \langle p_\perp^2 \rangle} e^{-p_\perp^2 / \langle p_\perp^2 \rangle}$$

where:

$$\mathcal{N}_q^T(x) = N_q^T x^{\alpha_q} (1-x)^{\beta_q} \frac{(\alpha_q + \beta_q)^{(\alpha_q + \beta_q)}}{\alpha_q^{\alpha_q} \beta_q^{\beta_q}}$$

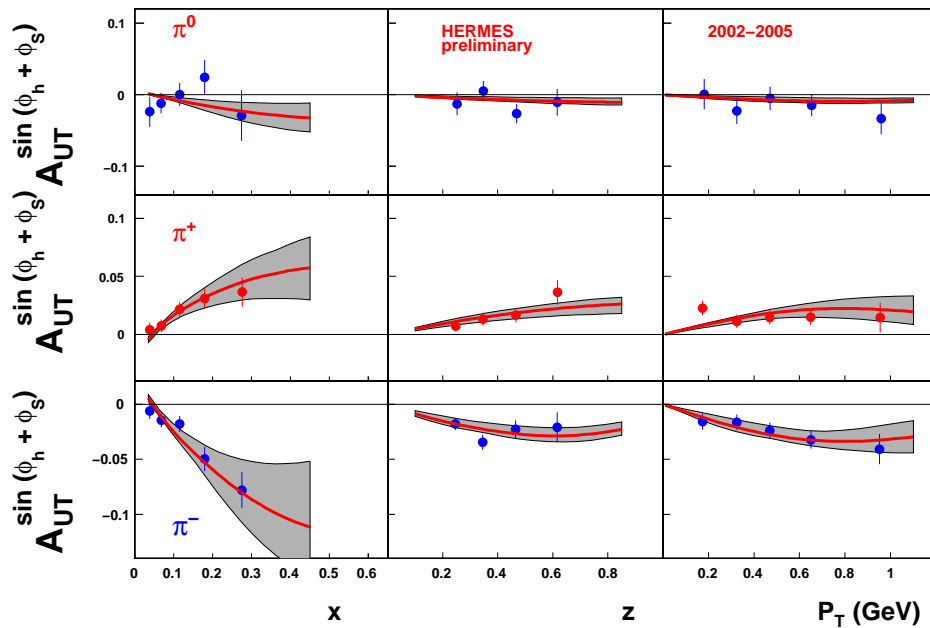
$$\mathcal{N}_q^C(x) = N_q^C x^\gamma (1-x)^\delta \frac{(\gamma + \delta)^{(\gamma + \delta)}}{\gamma^\gamma \delta^\delta} \quad h(p_\perp) = \sqrt{2} e \frac{p_\perp}{M_h} e^{-p_\perp^2 / M_h^2}$$

$N_u^T = 0.64 \pm 0.34$	$N_d^T = -1.00 \pm 0.02$
$\alpha = 0.73 \pm 0.51$	$\beta = 0.84 \pm 2.30$
$N_{fav}^C = 0.44 \pm 0.07$	$N_{unf}^C = -1.00 \pm 0.06$
$\gamma = 0.96 \pm 0.08$	$\delta = 0.01 \pm 0.05$
$M_h^2 = 0.91 \pm 0.52 \text{ GeV}^2$	

Fit: HERMES & COMPASS data

➤ HERMES data \diamond fit

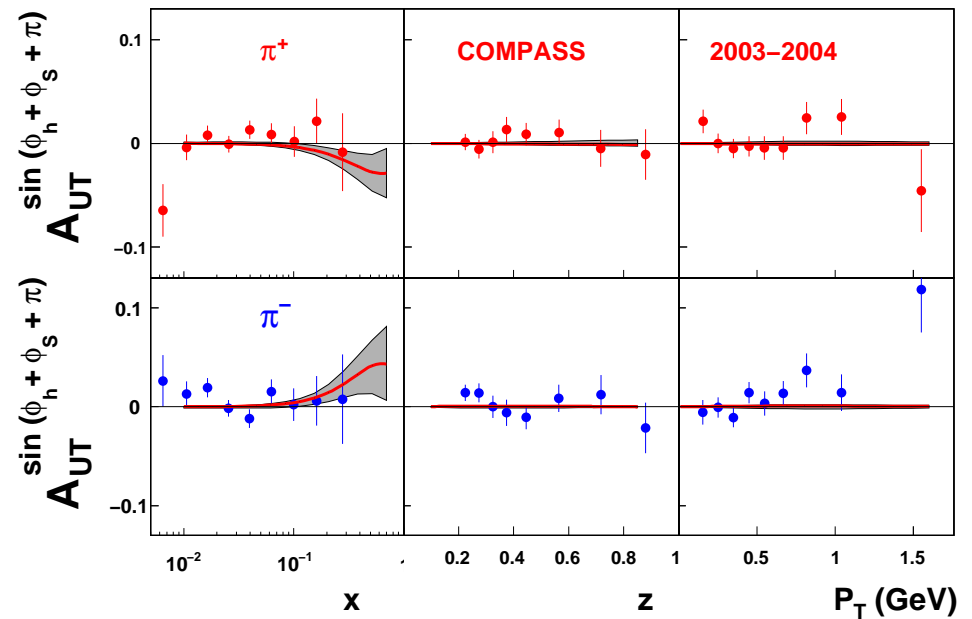
$ep \rightarrow e\pi X$ $p_{lab} = 27.57 \text{ GeV}/c$



\diamond M. Diefenthaler, (2007), arXiv:0706.2242

➤ COMPASS data \diamond fit

$\mu D \rightarrow \mu\pi X$ $p_{lab} = 160 \text{ GeV}/c$



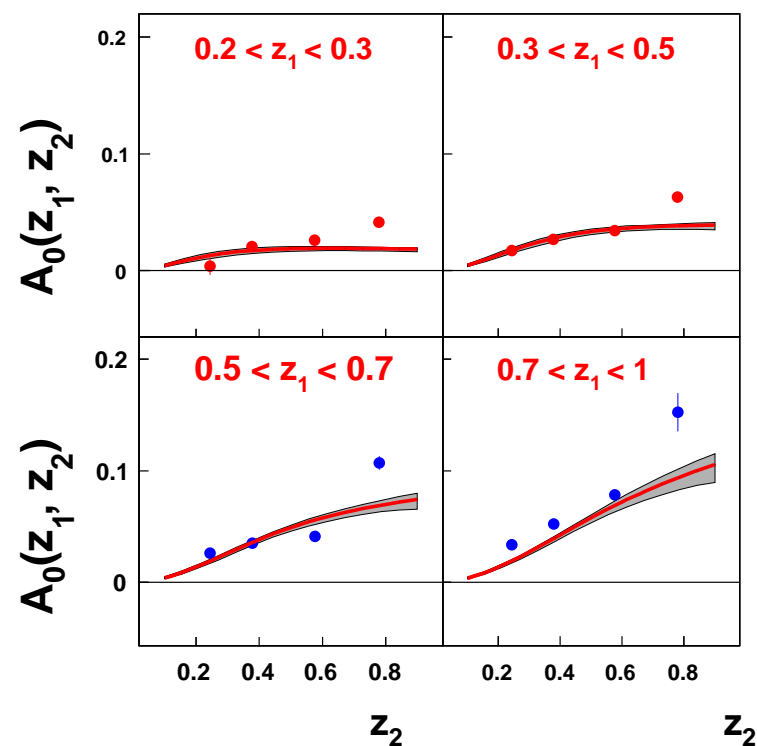
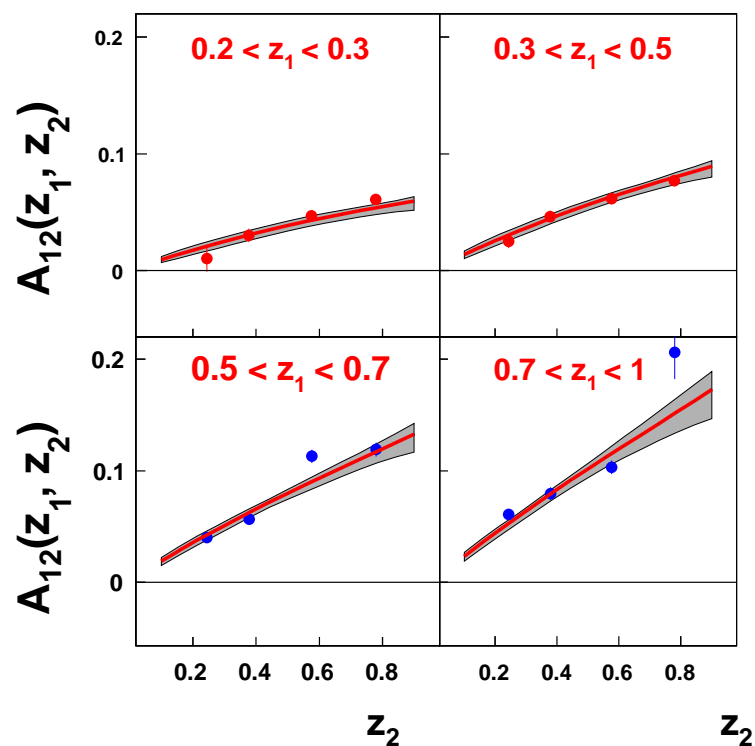
\diamond M. Alekseev et al., (2008), arXiv:0802.2160

Fit: BELLE data

➤ BELLE data \diamond fit

$$e^+e^- \rightarrow \pi\pi X$$

$$\sqrt{s} = 10.58 \text{ GeV}/c$$



\diamond R. Seidl et al., Phys. Rev. D78

Transversity and Collins functions

Transversity: u and d

Collins functions: favored and unfavored

