

X(3872)-Scan Reloaded

PANDA CM Vienna

Charmonium Exotics Session

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Idea

- Nature of $X(3872)$
 - Need lineshape and width to understand structure
- Approach at PANDA
 - Fine scan around nominal mass
→ energy dependent cross section
- Analysis goals
 - Sensitivity of Γ measurement (conventional BW)
 - Sensitivity for virtual/bound state (molecular picture)
- Analysis strategy
 - Analysis of $X(3872) \rightarrow J/\psi(\ell^+\ell^-) \rho^0(\pi^+\pi^-)$ channel only
 - Full sim/reco → signal + background efficiencies ϵ_S and ϵ_B
 - Toy MC scan simulation with assumption for cross sections, integrated luminosities, BRs

Molecular Picture (Hanhart et al)

- Lineshapes from [Kalashnikova et al, Phys. Atom. Nucl. 73 (2010) 1592]
- Here only interested in $X(3872) \rightarrow J/\psi \pi^+ \pi^-$

$$\frac{d\text{Br}(B \rightarrow K \pi^+ \pi^- J/\psi)}{dE} = \mathcal{B} \frac{1}{2\pi} \frac{\Gamma_{\pi^+ \pi^- J/\psi}(E)}{|D(E)|^2}$$

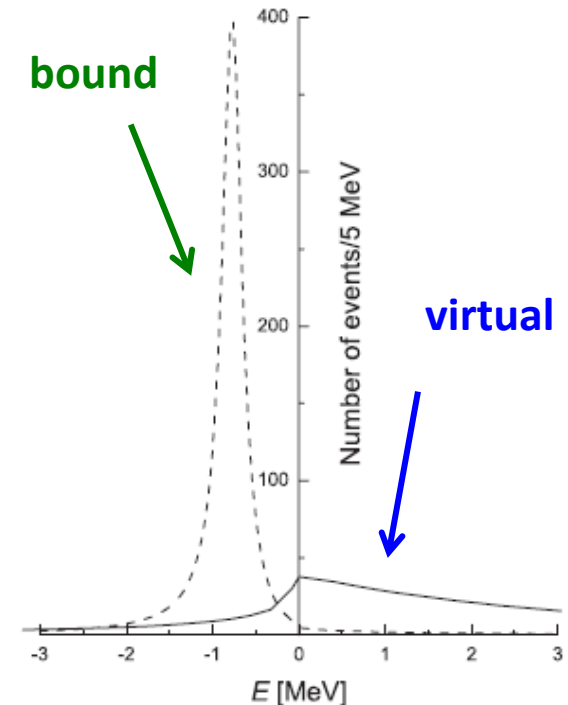
(assuming lineshape as in B decays)

$$D(E) = \begin{cases} E - E_f - \frac{g_1 k_1}{2} - \frac{g_2 k_2}{2} + i \frac{\Gamma(E)}{2}, & E < 0, \\ E - E_f - \frac{g_2 k_2}{2} + i \left(\frac{g_1 k_1}{2} + \frac{\Gamma(E)}{2} \right), & 0 < E < \delta, \\ E - E_f + i \left(\frac{g_1 k_1}{2} + \frac{g_2 k_2}{2} + \frac{\Gamma(E)}{2} \right), & E > \delta, \end{cases}$$

$$\Gamma(E) = \Gamma_{\pi^+ \pi^- J/\psi}(E) + \Gamma_{\pi^+ \pi^- \pi^0 J/\psi}(E) + \Gamma_0$$

$$\Gamma_{\pi^+ \pi^- J/\psi}(E) = f_\rho \int_{2m_\pi}^{M-m_{J/\psi}} dm \frac{q(m) \Gamma_\rho}{2\pi (m - m_\rho)^2 + \Gamma_\rho^2/4}$$

$$\Gamma_{\pi^+ \pi^- \pi^0 J/\psi}(E) = f_\omega \int_{3m_\pi}^{M-m_{J/\psi}} dm \frac{q(m) \Gamma_\omega}{2\pi (m - m_\omega)^2 + \Gamma_\omega^2/4}$$



Parameter E_f determines state to be **bound** or **virtual**

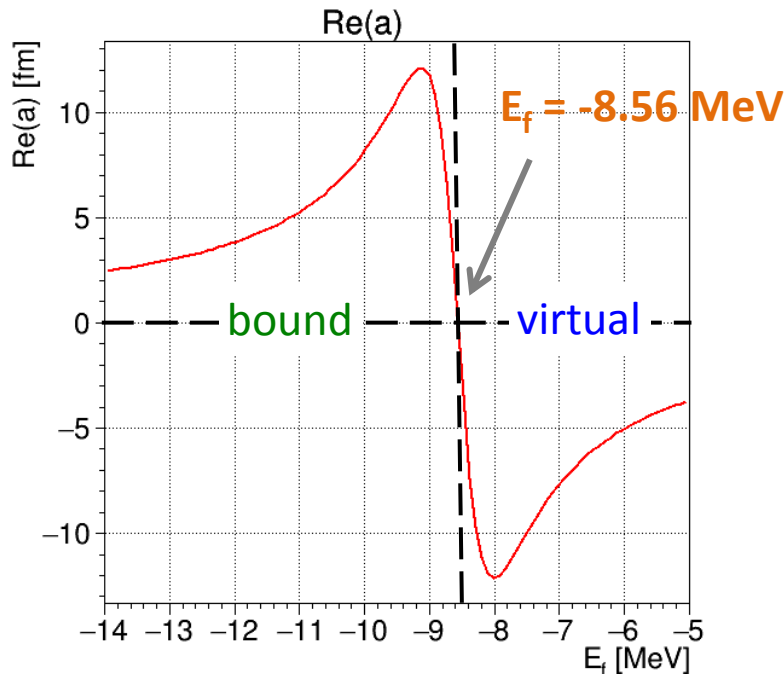
Lineshapes for different E_f

Scattering length $D^0 D^{0*}$:

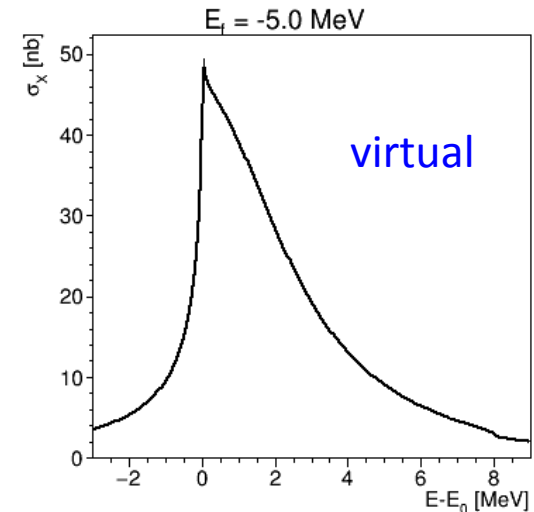
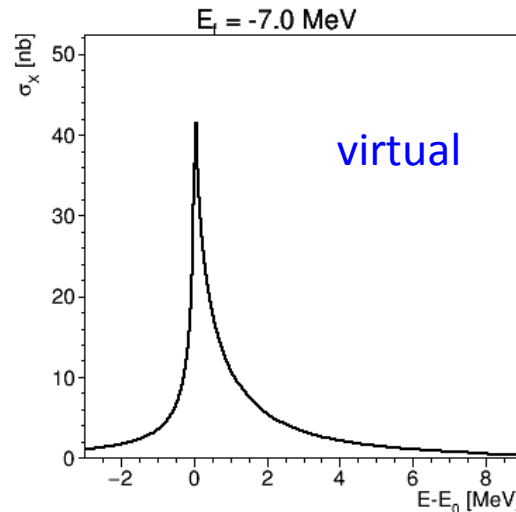
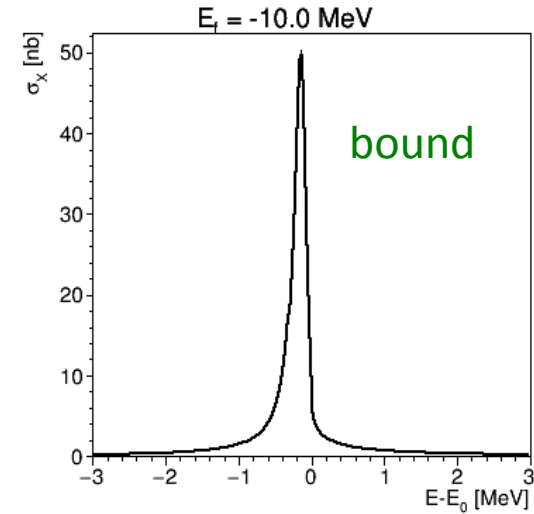
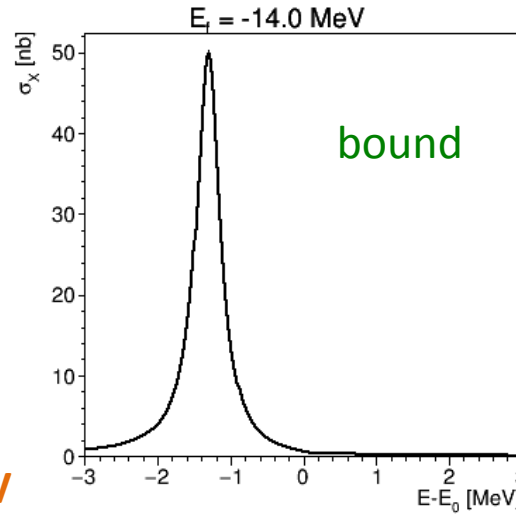
$$a = - \frac{\sqrt{2\mu_2\delta} + 2E_f/g + i\Gamma(0)/g}{(\sqrt{2\mu_2\delta} + 2E_f/g)^2 + \Gamma(0)^2/g^2}$$

$\text{Re}(a) > 0$: bound state

$\text{Re}(a) < 0$: virtual state



Always scaled to $f_{\text{max}} = 50$ nb here!



(with $f_p=0.00047$, $f_w=0.00271$, $g=0.137$, $\Gamma_0=1.0$ MeV)

Reconstruction Part

Parameters

	Parameter	Value
Branching Fractions	$\text{BR}(J/\psi \rightarrow e^+ e^-)$	5.97 %
	$\text{BR}(J/\psi \rightarrow \mu^+ \mu^-)$	5.96 %
	$\text{BR}(X \rightarrow J/\psi \rho^0)$	5 % (assumption)
Cross sections	$\sigma(\bar{p}p \rightarrow X)$	50 nb (assumption)
	$\sigma(\bar{p}p \rightarrow J/\psi \pi^+ \pi^- \text{ non-res})^*$	1.2 nb (theory)
	$\sigma(\bar{p}p \rightarrow \text{inelastic}) @ 3.872 \text{ GeV}$	46 mb
Luminosities	$L_{\text{HL}} (3.872 \text{ GeV})$	13683 (nb·d) ⁻¹
	$L_{\text{HR}} (3.872 \text{ GeV})$	1368 (nb·d) ⁻¹
	$L_{\text{HESRr}} (3.872 \text{ GeV})$	1170 (nb·d) ⁻¹
Resolutions	$\sigma_{\text{E,abs}}$ (<i>absolute energy positioning</i>)	100 keV (assumption)
	$\sigma_{\text{E,rel}}$ (<i>relative energy positioning</i>)	10 keV (assumption)
	$\sigma_{\text{E,beam}}(\text{HL})$	168 keV
	$\sigma_{\text{E,beam}}(\text{HR/HESRr})$	67 keV

*[PRD 77 (2008) 097501]

Software and Data

- Software
 - PandaRoot: Revision 28670
 - FairSoft: mar15p2
 - FairRoot: v15.03
- Data @ $E_{\text{cm}} = 3.872 \text{ GeV}$

Channel	#Events
$\bar{p}p \rightarrow J/\psi \rho^0 \rightarrow e^+e^- \pi^+\pi^-$	98k
$\bar{p}p \rightarrow J/\psi \rho^0 \rightarrow \mu^+\mu^- \pi^+\pi^-$	100k
$\bar{p}p \rightarrow J/\psi (\rightarrow e^+e^-) \pi^+\pi^- \text{ (NR)}$	100k
$\bar{p}p \rightarrow J/\psi (\rightarrow \mu^+\mu^-) \pi^+\pi^- \text{ (NR)}$	99k
DPM ($J/\psi \rightarrow e^+ e^-$ prefilter)	$\approx 10\text{M} = 9.58\text{G}$ generated
DPM ($J/\psi \rightarrow \mu^+ \mu^-$ prefilter)	$\approx 10\text{M} = 8.87\text{G}$ generated

Background Prefilter QA

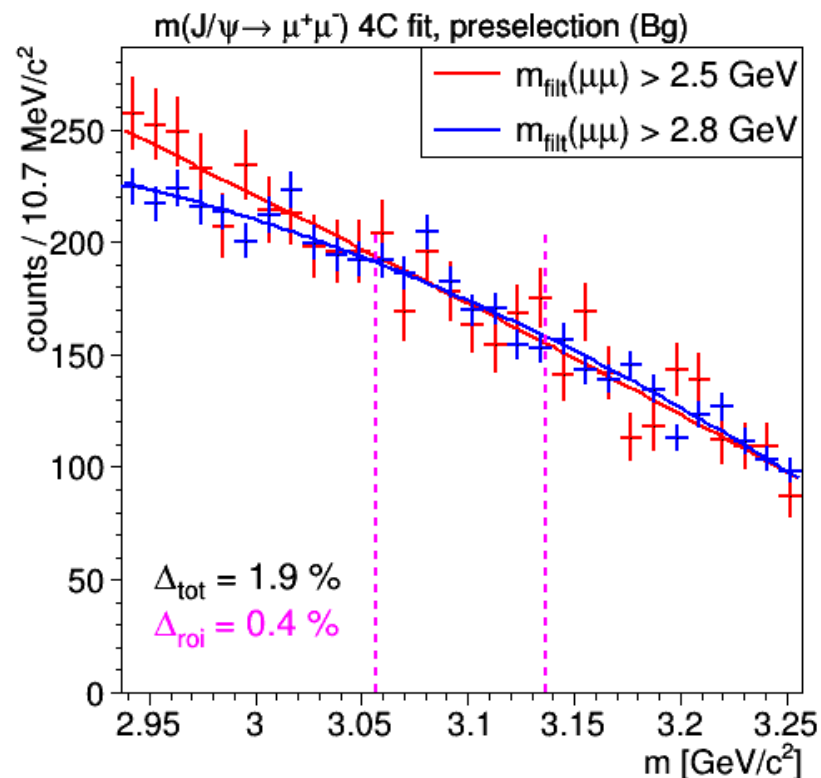
- Filtering criteria

- Require 4 charged tracks
- Require one 2-track combination : $m_{ee/\mu\mu} > 2.8 \text{ GeV}/c^2$
- Suppression factor e^+e^- : $\approx 1/1000$
- Suppression factor $\mu^+\mu^-$: $\approx 1/900$

- Check filter bias ($\mu\mu$ only)

- Cross check with criterion
 $m_{\mu\mu} > 2.5 \text{ GeV}/c^2$ (10M \rightarrow 2.6G)
- Slight difference at lower mass edge
- Total integral difference: 1.9%
- Difference in J/ ψ ROI: 0.4%

\Rightarrow Negligible effect!



Signal Reconstruction

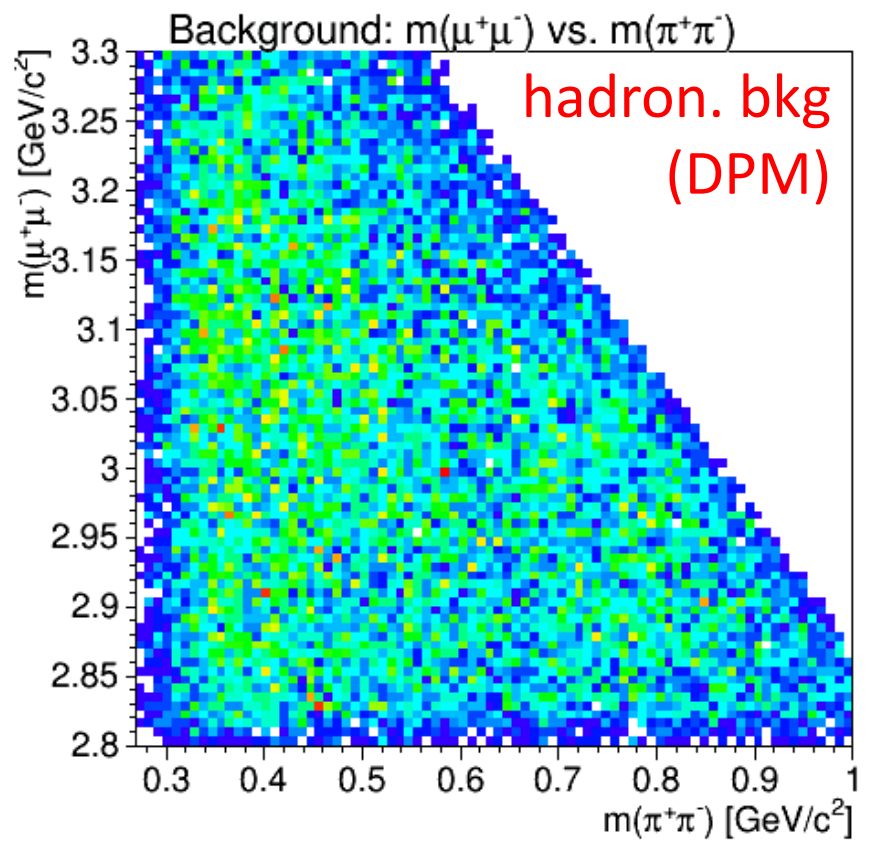
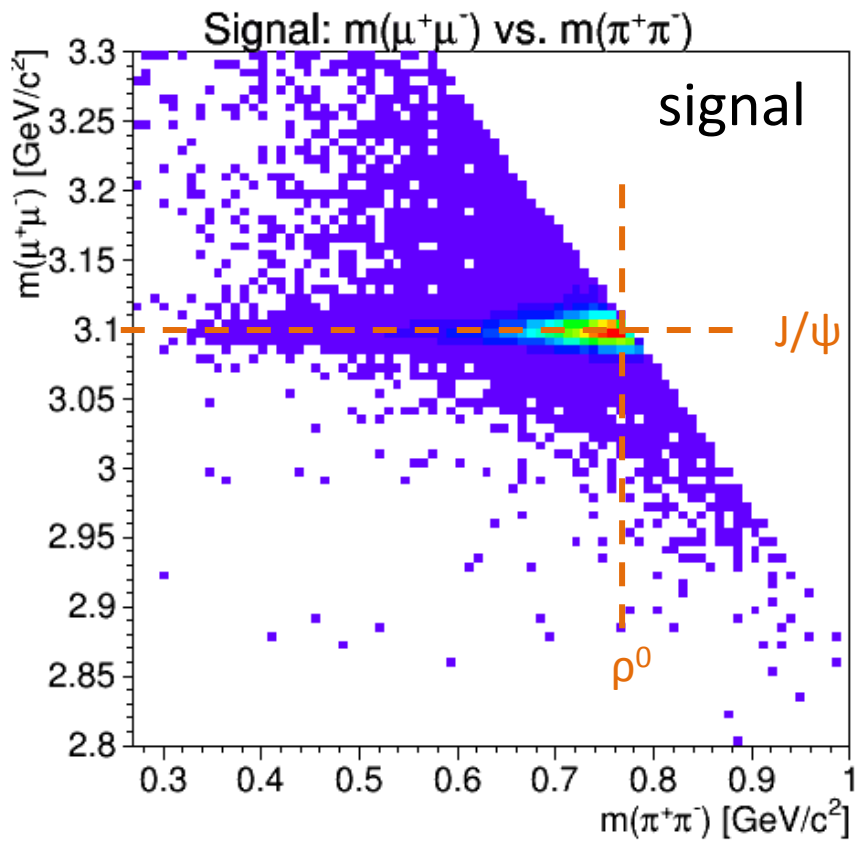
- Preselection e^+e^- :

- Particle Identification : **ElectronTight, PionAll**
(PidAlgoEmcBayes;PidAlgoDrc;PidAlgoDisc;PidAlgoStt;PidAlgoMdtHardCuts)
- $J/\psi \rightarrow e^+e^-$ mass window: **$2.0 < m(e^+e^-) < 3.4 \text{ GeV}/c^2$**
- $\rho^0 \rightarrow \pi^+\pi^-$ mass window: **$0.27 < m(\pi^+\pi^-) < 1.0 \text{ GeV}/c^2$**
- $\bar{p}p \rightarrow J/\psi \rho^0$ 4C fit : **$\chi^2 < 200$**

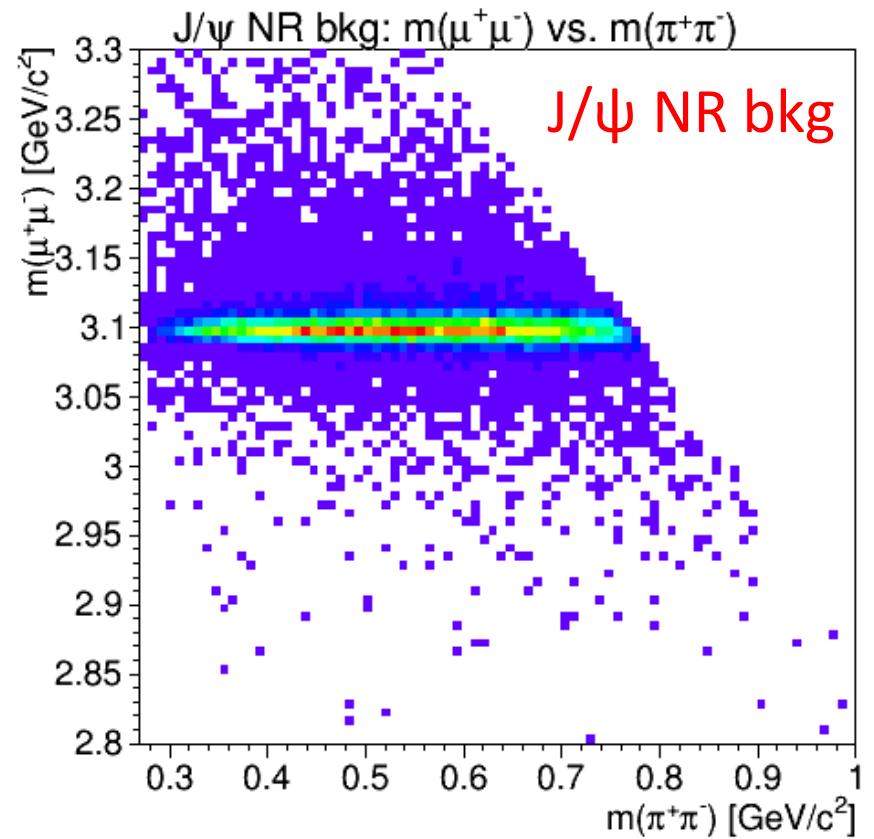
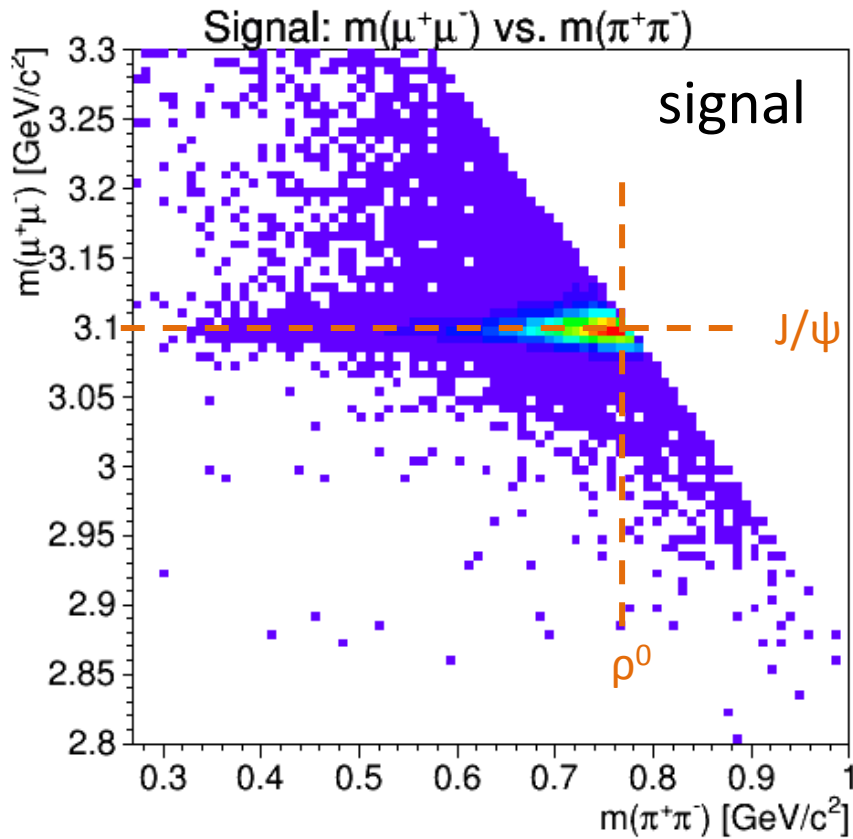
- Preselection $\mu^+\mu^-$:

- Particle Identification : **MuonTight, PionAll**
(PidAlgoEmcBayes;PidAlgoDrc;PidAlgoDisc;PidAlgoStt;PidAlgoMdtHardCuts)
- $J/\psi \rightarrow \mu^+\mu^-$ mass window: **$2.5 < m(\mu^+\mu^-) < 3.4 \text{ GeV}/c^2$**
- $\rho^0 \rightarrow \pi^+\pi^-$ mass window: **$0.27 < m(\pi^+\pi^-) < 1.0 \text{ GeV}/c^2$**
- $\bar{p}p \rightarrow J/\psi \rho^0$ 4C fit : **$\chi^2 < 100$**

Correlation $M(\ell^+\ell^-)$ vs. $M(\pi^+\pi^-)$

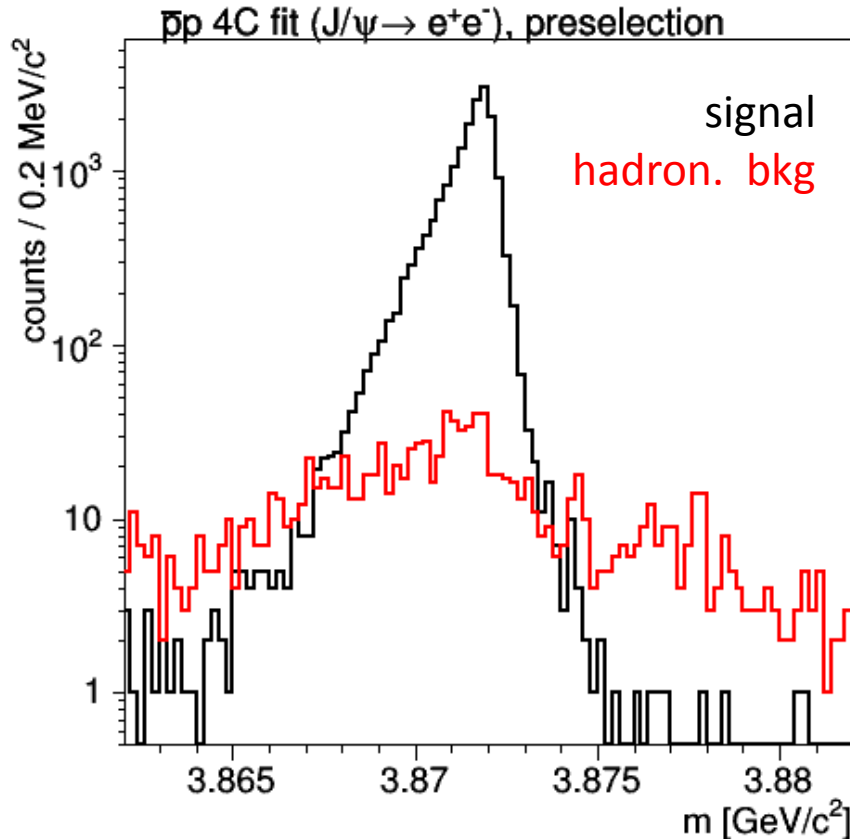


Correlation $M(\ell^+\ell^-)$ vs. $M(\pi^+\pi^-)$

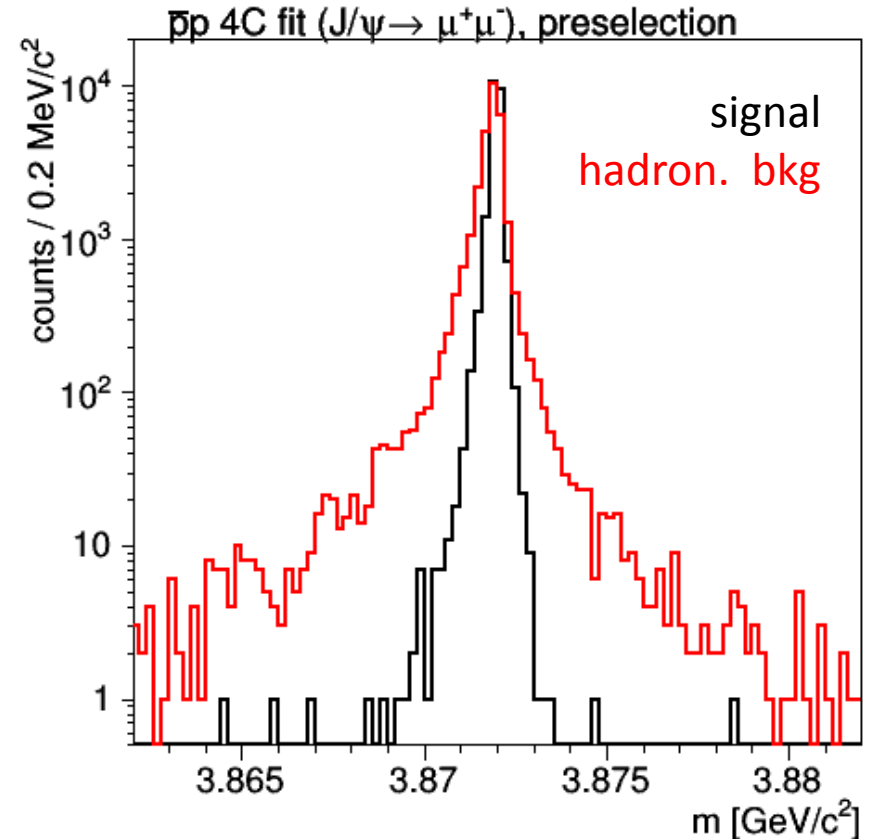


$\bar{p}p$ System after Preselection

$$\bar{p}p \rightarrow J/\psi \rho^0 \rightarrow e^+ e^- \pi^+ \pi^-$$



$$\bar{p}p \rightarrow J/\psi \rho^0 \rightarrow \mu^+ \mu^- \pi^+ \pi^-$$



Final Selection Criteria

- Final selection e^+e^-
 - Electron PID(e^\pm) > 0.95
 - $m(e^+e^-) > 2.7 \text{ GeV}/c^2$
 - $p(e^+e^-) > 4.6 \text{ GeV}/c$
 - $p_{\text{cm}}(e^+e^-) < 0.38 \text{ GeV}/c$
 - $\angle(p_{e^+}, p_{e^-}) < 2 \text{ rad}$
- Final selection $\mu^+\mu^-$
 - Muon PID(μ^\pm) > 0.99
 - $p_{\text{cm}}(\mu^+\mu^-) < 0.32 \text{ GeV}/c$
 - $p_{\text{cm}}(\mu^\pm) > 1.37 \text{ GeV}/c$

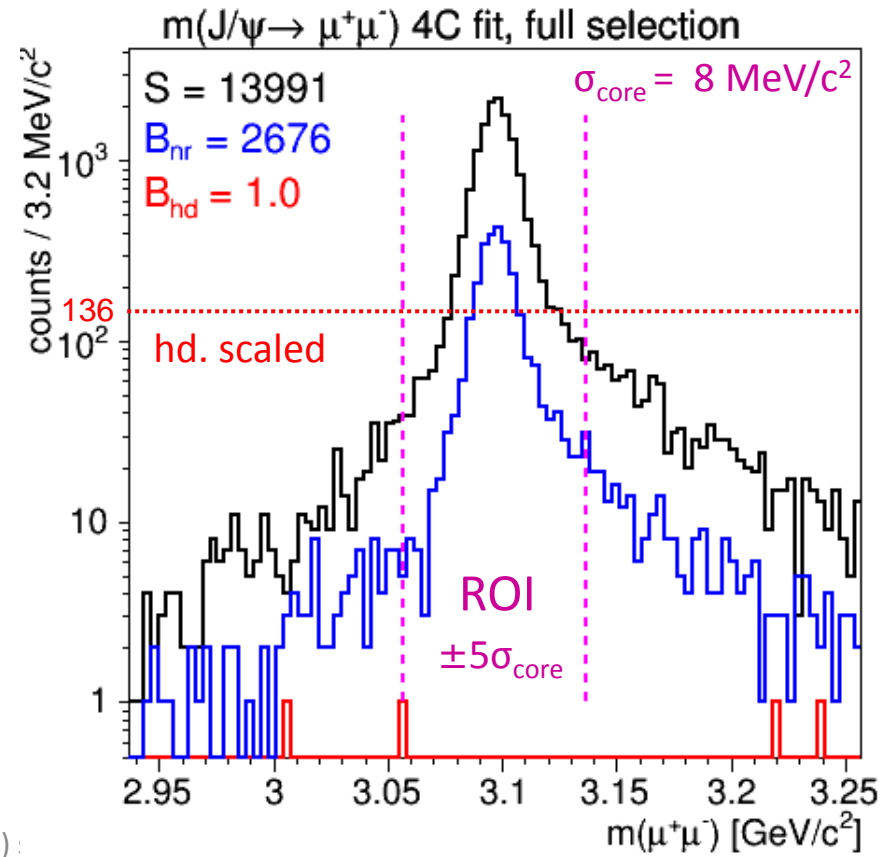
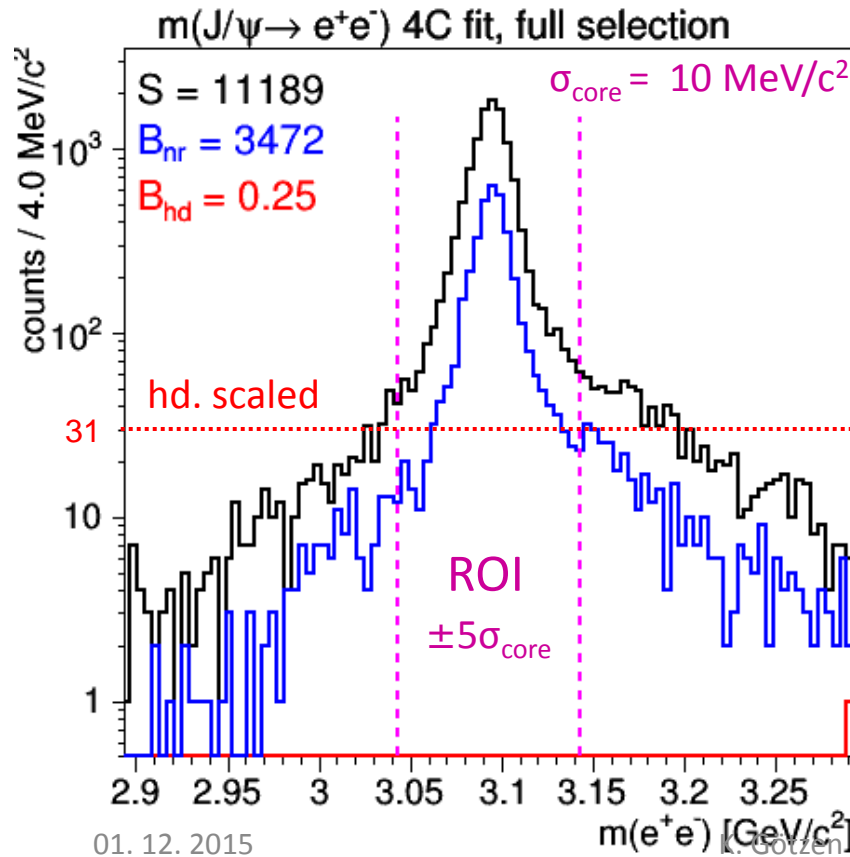
Final Selection Results

$$J/\psi \rightarrow e^+e^-$$

$\epsilon_S = 11.4\%$
 $\epsilon_{B,nr} = 3.5\%$, $\epsilon_{B,hd} = 2.6 \cdot 10^{-11}$
S:N = 4.6 : 1

$$J/\psi \rightarrow \mu^+\mu^-$$

$\epsilon_S = 14.0\%$
 $\epsilon_{B,nr} = 2.7\%$, $\epsilon_{B,hd} = 1.1 \cdot 10^{-10}$
S:N = 3 : 1



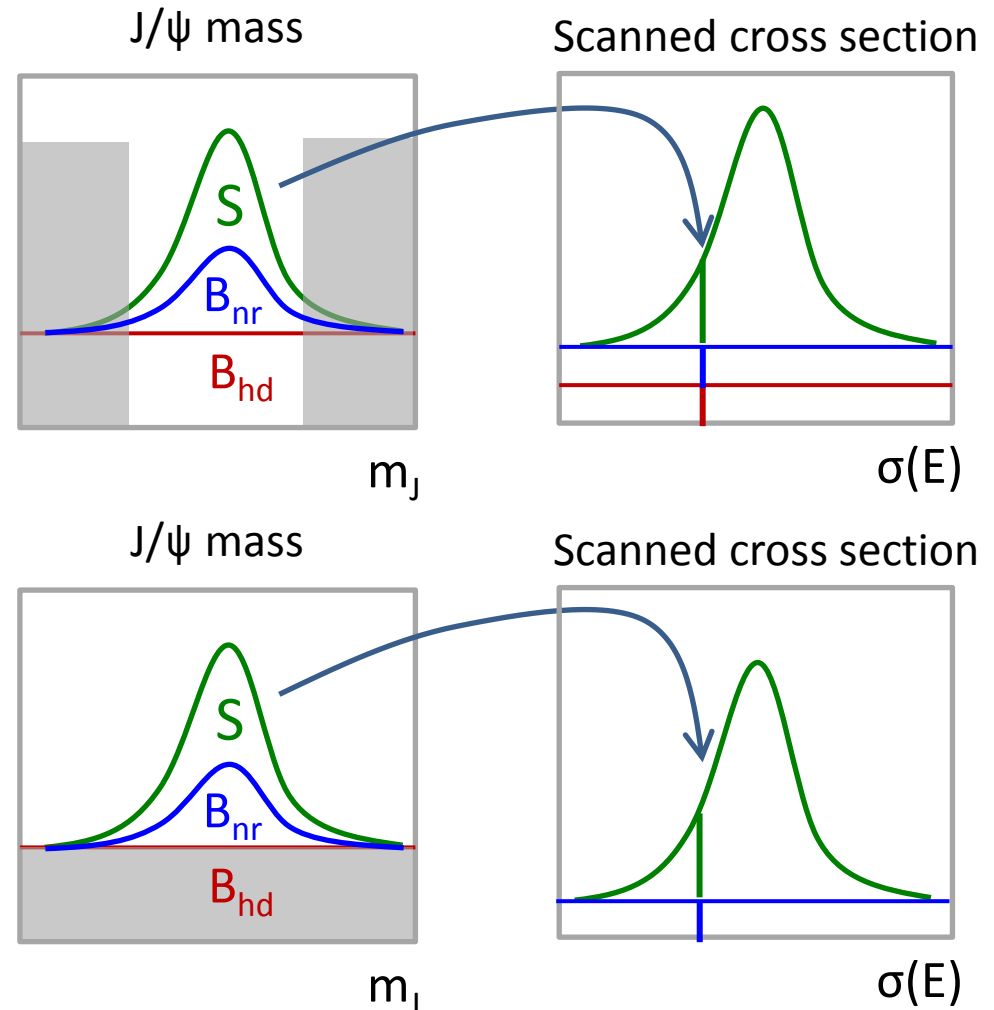
Energy Scan Part

Possible Approaches

Two obvious approaches possible to extract lineshape:

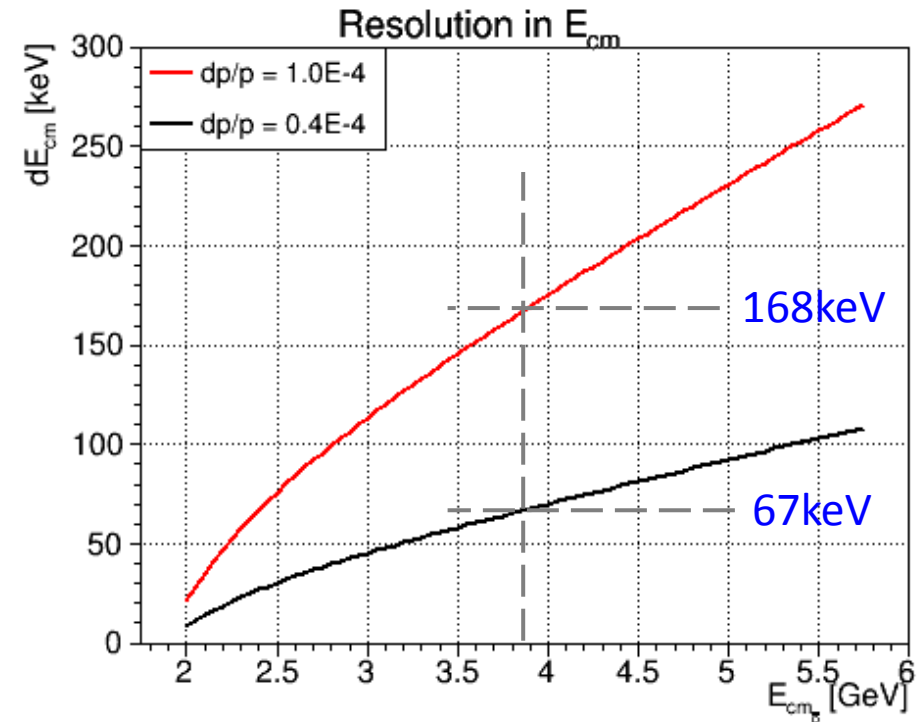
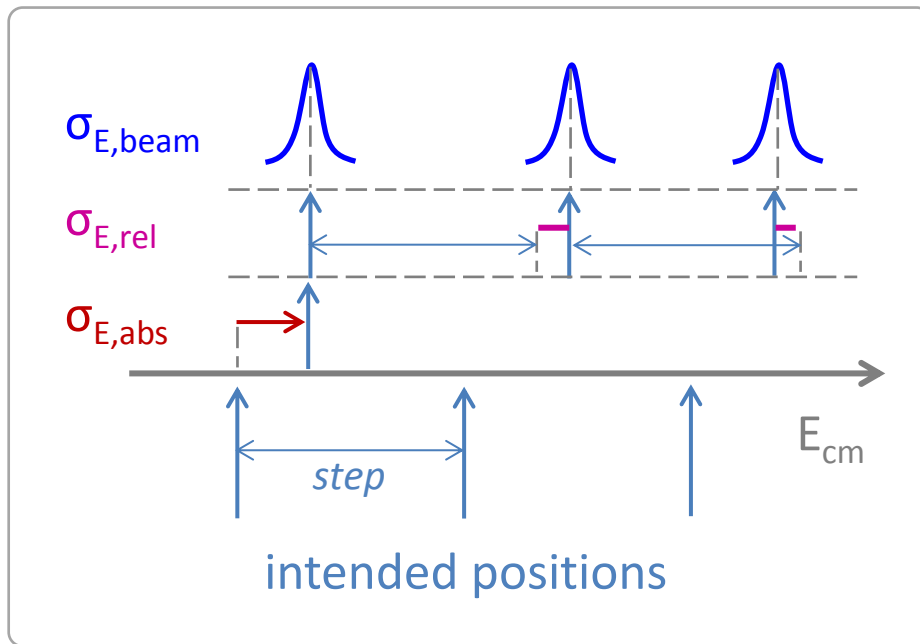
1. Cut on J/ψ and count
 - simple + robust
 - all backgrounds still in scanned lineshape
2. Fit signal in J/ψ mass
 - removes hadronic bkg
 - NR bkg still present

Show 2. method here
being slightly better than 1.



Uncertainty Assumptions for Scan

- Beam related energy resolution: $\sigma_{E,\text{beam}} = 67(\text{HR}) / 168(\text{HL}) \text{ keV}$
- Absolute positioning resolution: $\sigma_{E,\text{abs}} = 100 \text{ keV (shift)}$
- Relative positioning resolution: $\sigma_{E,\text{rel}} = 10 \text{ keV } (\sim \text{error in } E_{\text{cm}})$



Procedure for Individual Scan

- **Scan procedure**

- Set parameter P (Γ or E_f) in signal function
- Define scan region, number of points, $L_{\text{int}} / \text{point}$
- Scale unfolded function $\sigma_S(E)$ to $\sigma_{S,\text{max}} = 50\text{nb}$ and adapt convoluted function $\sigma_S'(E) \rightarrow \sigma_{S',\text{max}} \leq 50\text{nb}$
- For each energy scan point (E_{cm})

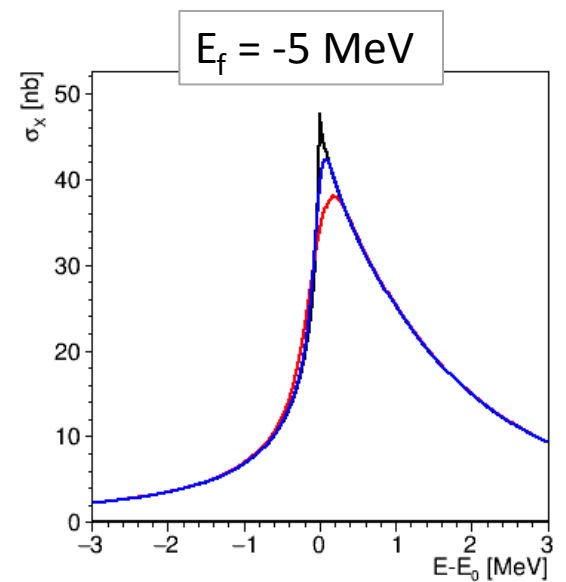
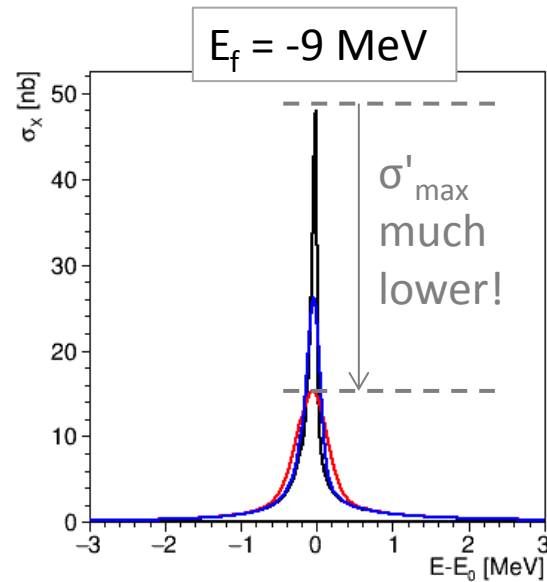
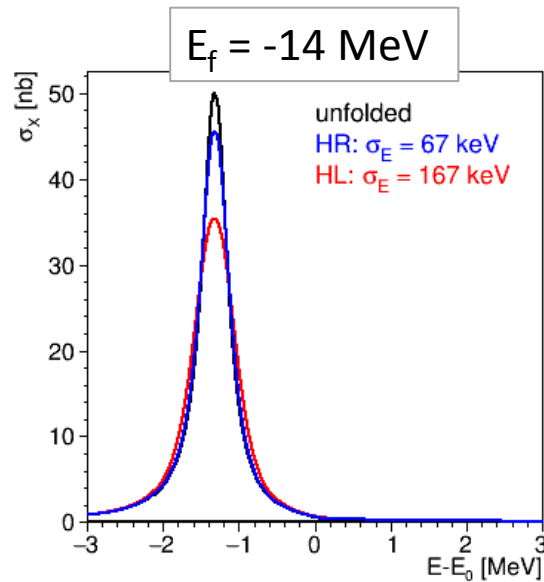
1. Modify energy $E_{\text{cm}} \rightarrow E_{\text{cm}}'$ due to $\sigma_{E,\text{abs}}$ and $\sigma_{E,\text{rel}}$
(Uncertainty for i -th scan point $\Delta E_{\text{cm},i} = \sqrt{i} \cdot \sigma_{E,\text{rel}}$)
2. Compute expected $S_0 / B_{\text{hd},0} / B_{\text{nr},0}$ based on $\sigma_S'(E_{\text{cm}}') / \sigma_{B,\text{hd}} / \sigma_{B,\text{nr}}$
3. Generate Poissonians $S / B_{\text{hd}} / B_{\text{nr}}$ from expected numbers
4. Generate J/ψ data with $S+B_{\text{nr}}$ signal and B_{hd} background events
5. Do unbinned ML fit to extract $N_{J/\psi} \pm \Delta N_{\text{lo}} - \Delta N_{\text{hi}} \rightarrow$ Scan graph at E_{cm}

- Fit graph with signal + background function \rightarrow parameter P

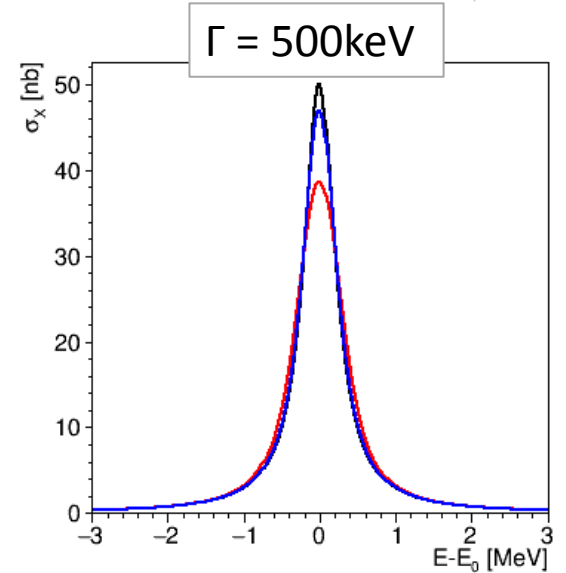
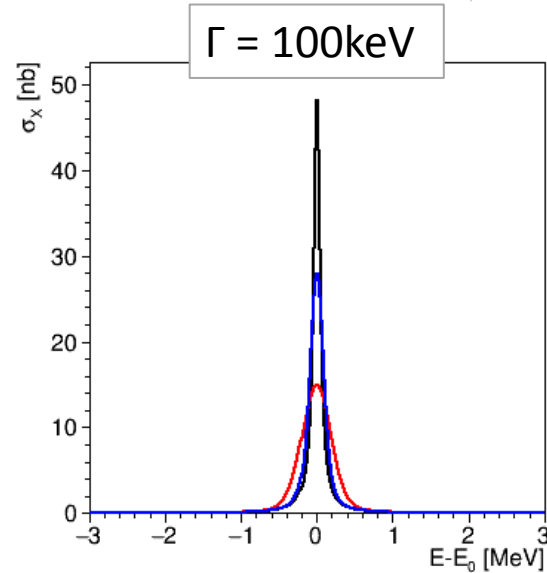
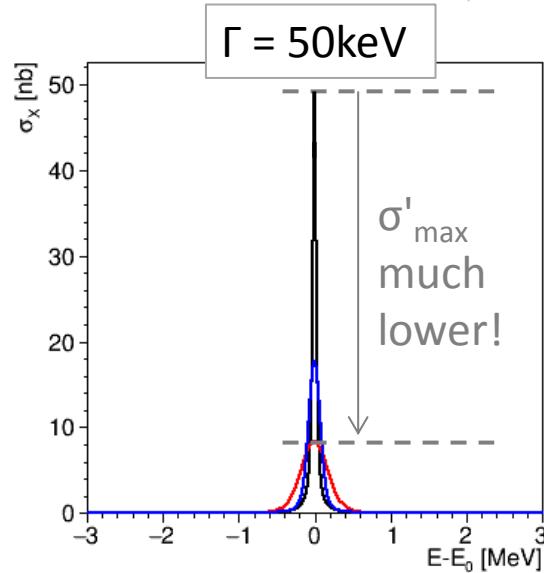
- Repeat N times to determine root-mean-square & bias of P

Lineshape Examples

Molecule

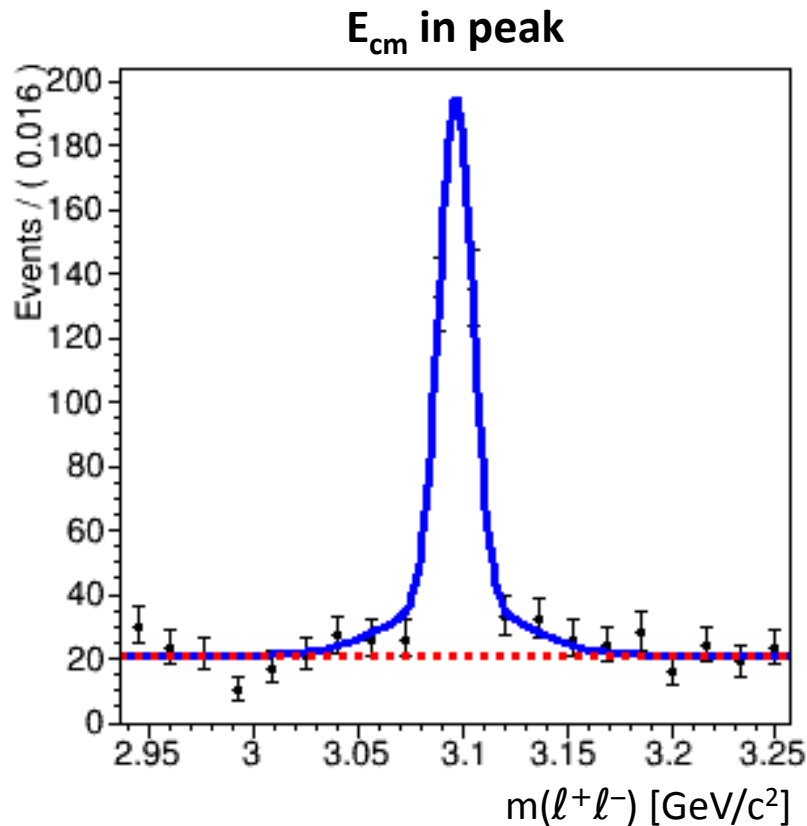


Breit-Wigner

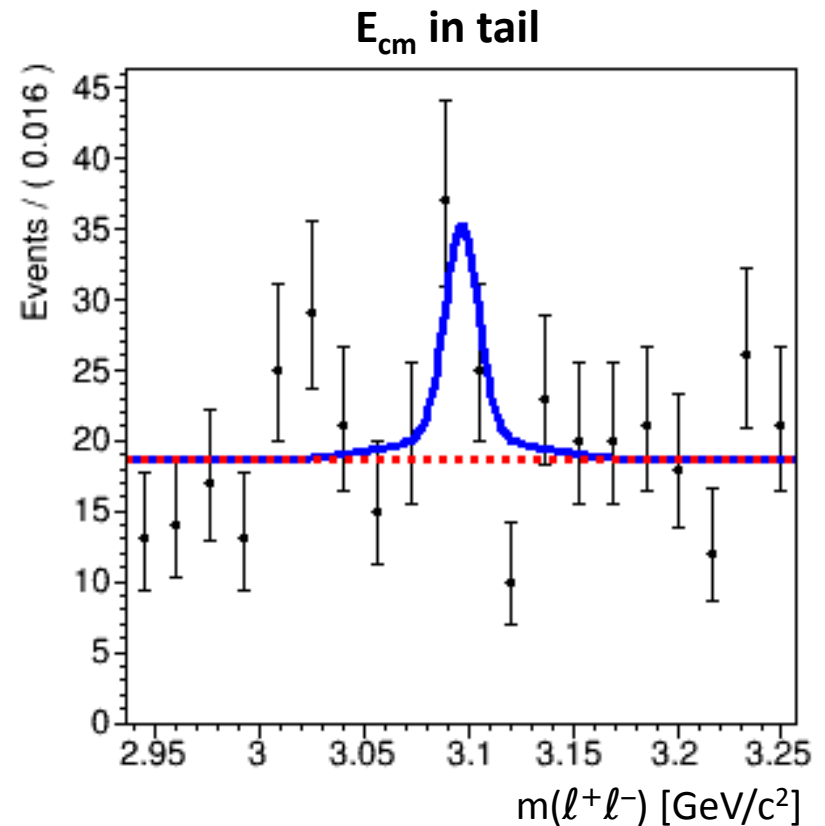


Generated J/ψ Plots Examples

- Signal pdf like in true reco; **hadr. background flat**
- **Scale** efficiencies from ROI to full window width ($\epsilon_S \times 1.1$, $\epsilon_B \times 4$)



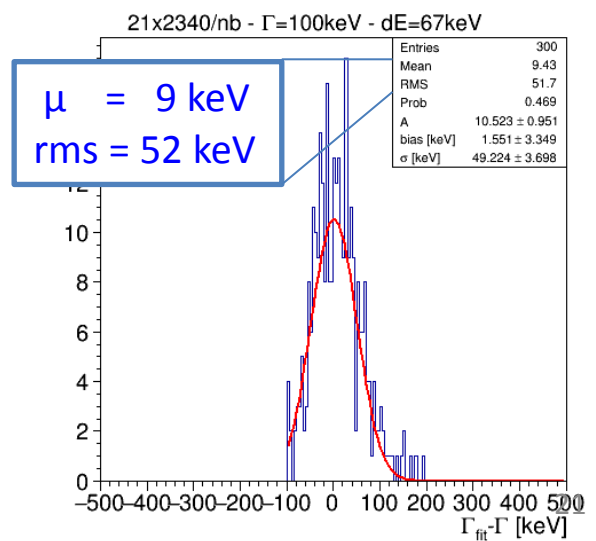
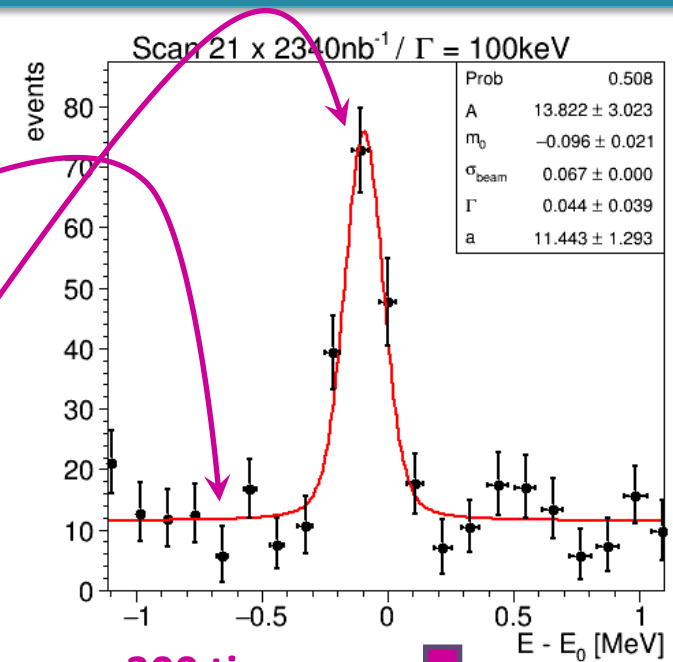
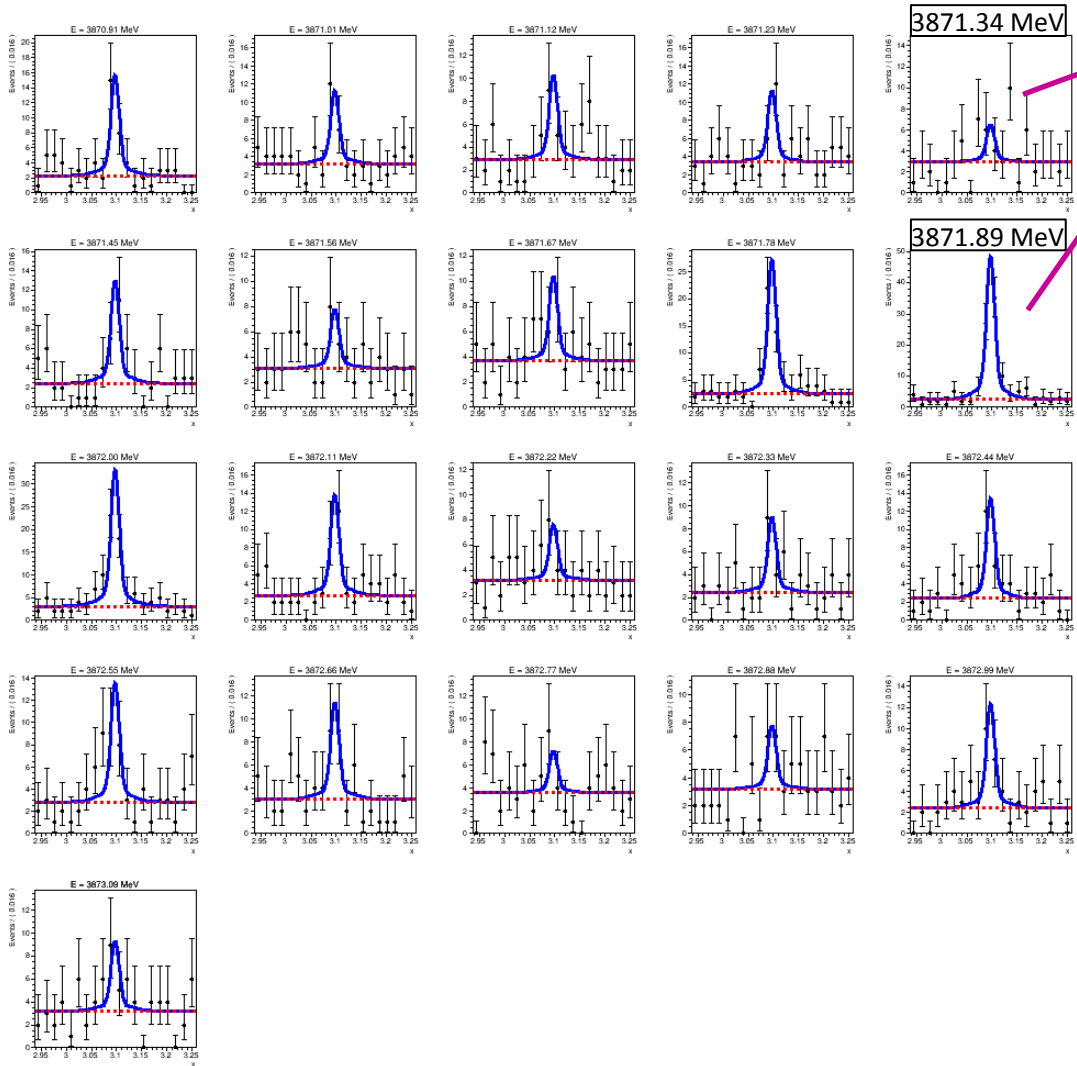
$$S = 275.8 \begin{matrix} + 16.8 \\ - 16.7 \end{matrix}$$



$$S = 26.1 \begin{matrix} + 9.7 \\ - 9.0 \end{matrix}$$

Illustration for Scan

BW, 21 x 2d in HESRr mode



Investigated Scenarios

- Luminosity modes ($E_{\text{cm}} = 3.872$ GeV): $N_L = 3$

Mode	HL	HR	HESRr
$L_{\text{int}} [(\text{nb}\cdot\text{d})^{-1}]$	13683	1368	1170

- Parameter settings: $N_P = 8$

BW	Γ [keV]	50	70	100	130	180	250	500	800
Molecule	$-E_f$ [MeV]	14	12	10	9	8	7	6	5

- Investigated scenarios: $N_S = 5$ Mainly show results for this one

Scan time [month]	1.5	2	2	2	10
Points \times days	21 x 2	21 x 3	31 x 2	61 x 1	61 x 5

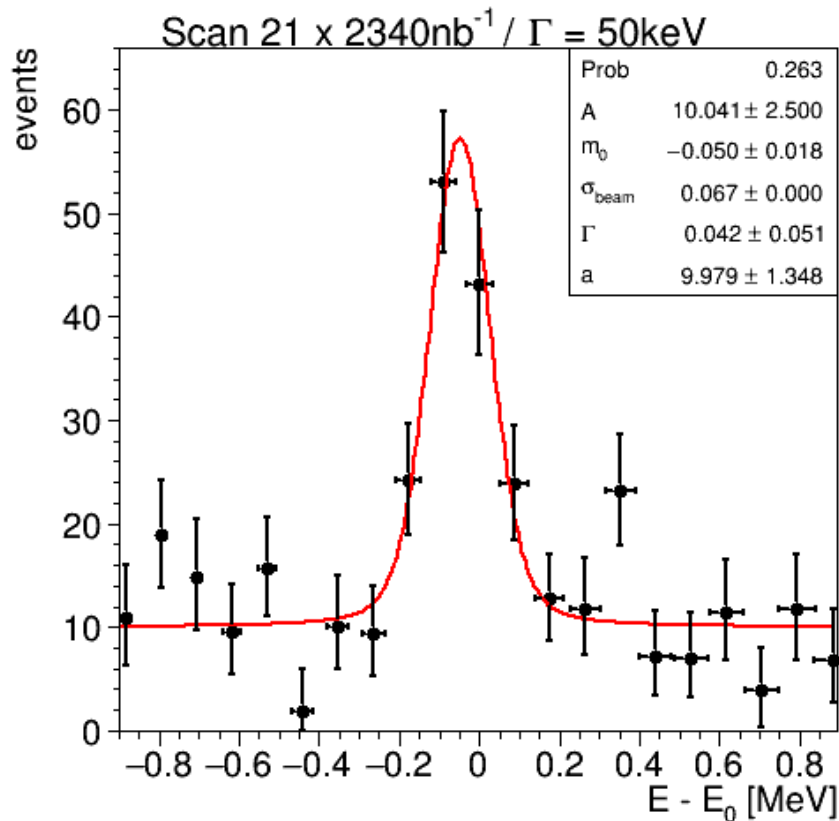
- Toy MC fits: $N_{\text{MC}} = 100 \dots 300$ ($N_{\text{tot}} \approx 50000$)

Physics mode	Breit-Wigner Γ	Molecule E_f
Number of fits	150 ... 300 / setup	100 / setup

Scan Examples Breit Wigner

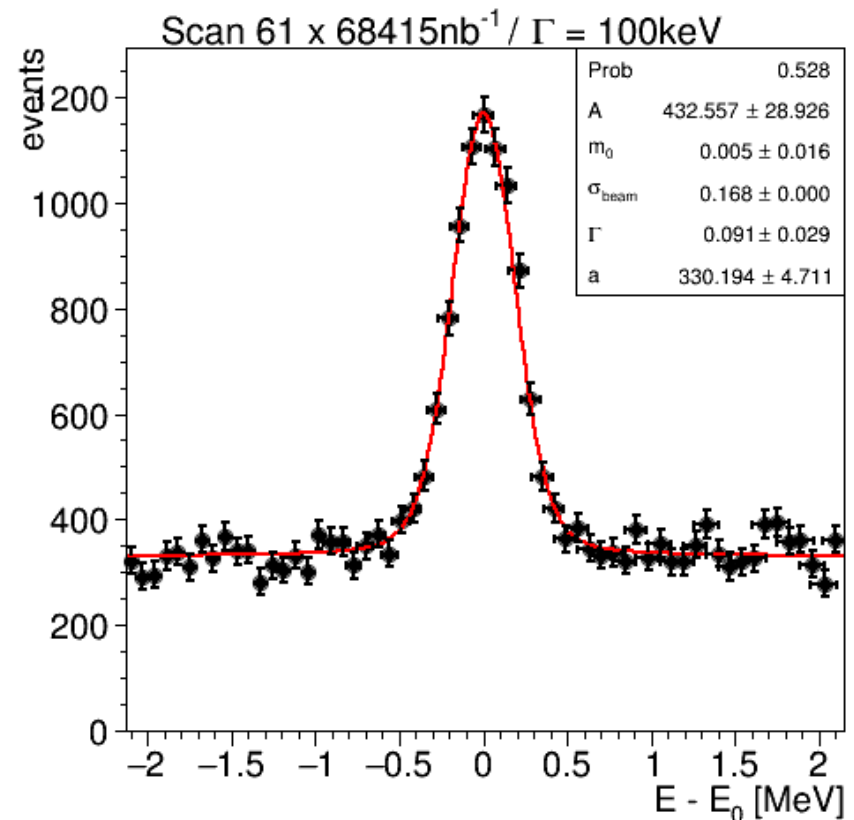
HESRr: 21 x 2 days

$\Gamma = 50 \text{ keV}$



HL: 61 x 5 days

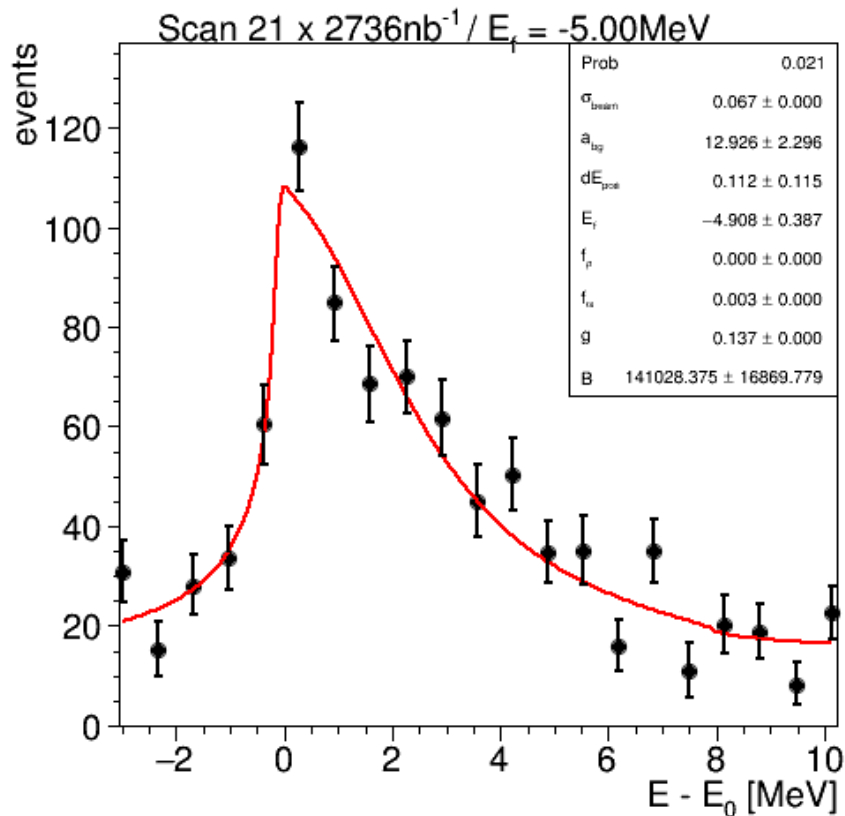
$\Gamma = 100 \text{ keV}$



Scan Examples Molecule Lineshape

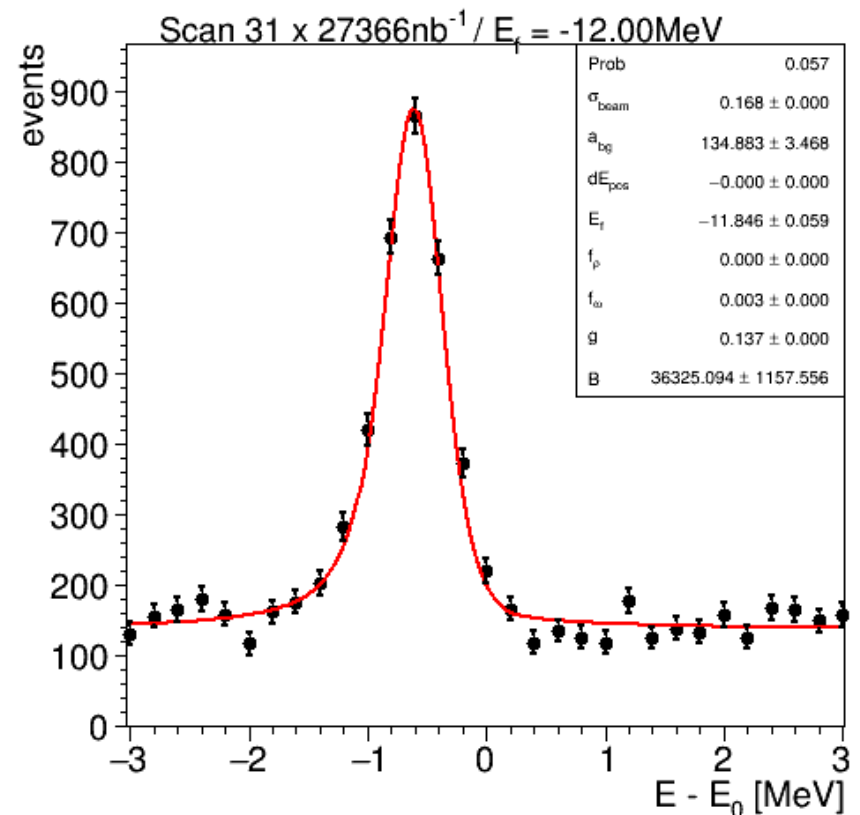
HR: 21 x 2 days

$E_f = -5$ MeV



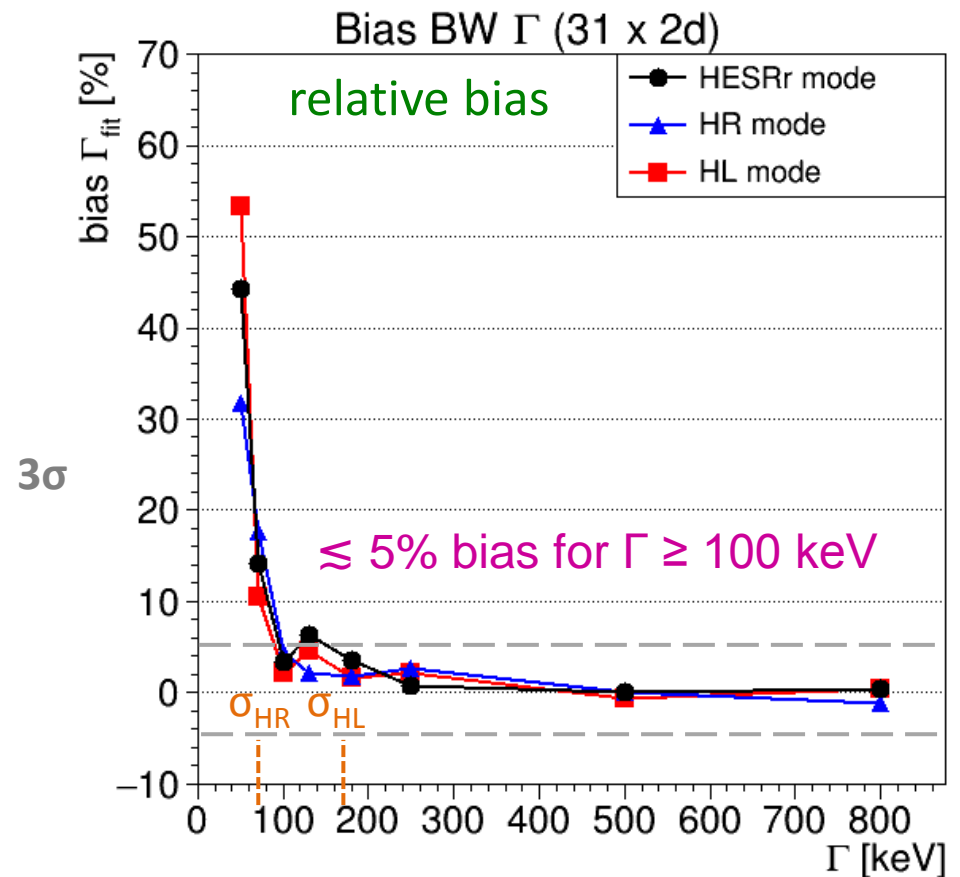
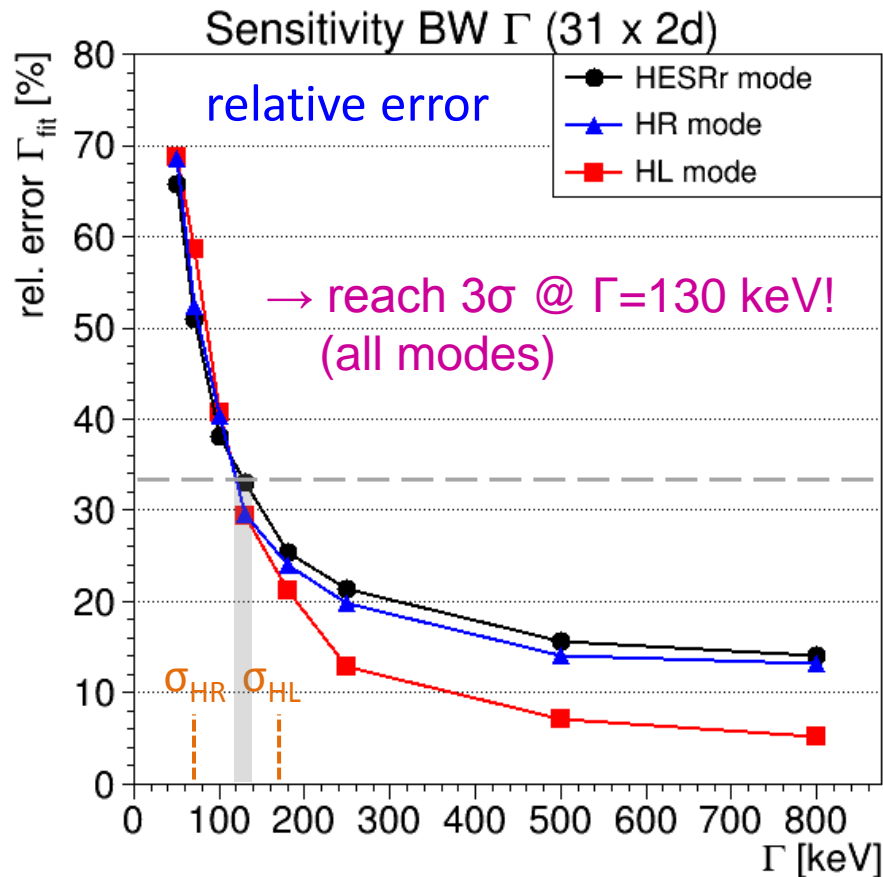
HL: 31 x 2 days

$E_f = -12$ MeV



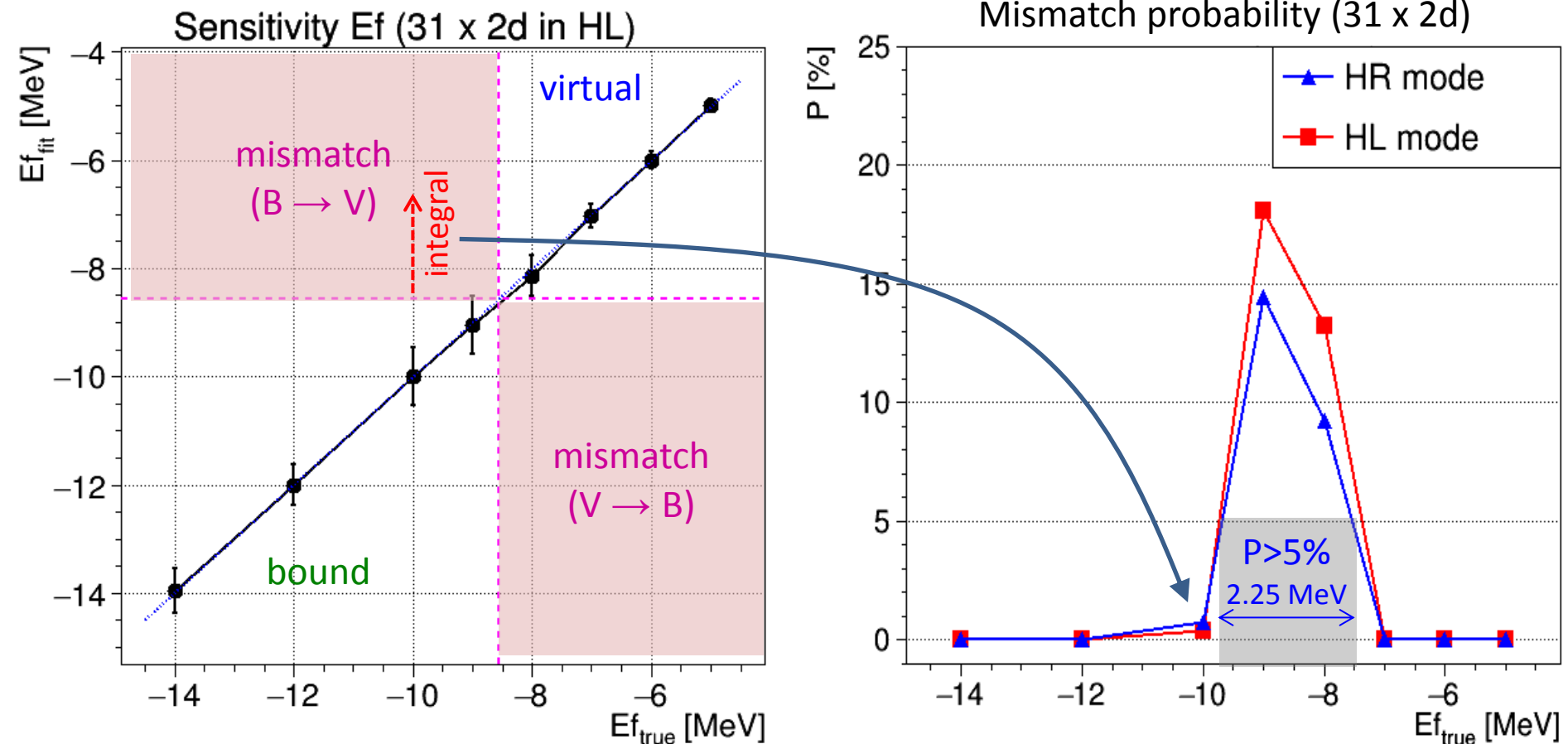
Sensitivities Breit-Wigner Γ (31 x 2d)

- Extract standard deviation and bias from toy MC fits (ML)
- Show **relative error** $\text{rms}_{\text{fit}}/\bar{\Gamma}_{\text{fit}}$ and **bias** $(\bar{\Gamma}_{\text{fit}} - \Gamma)/\Gamma$ in [%]



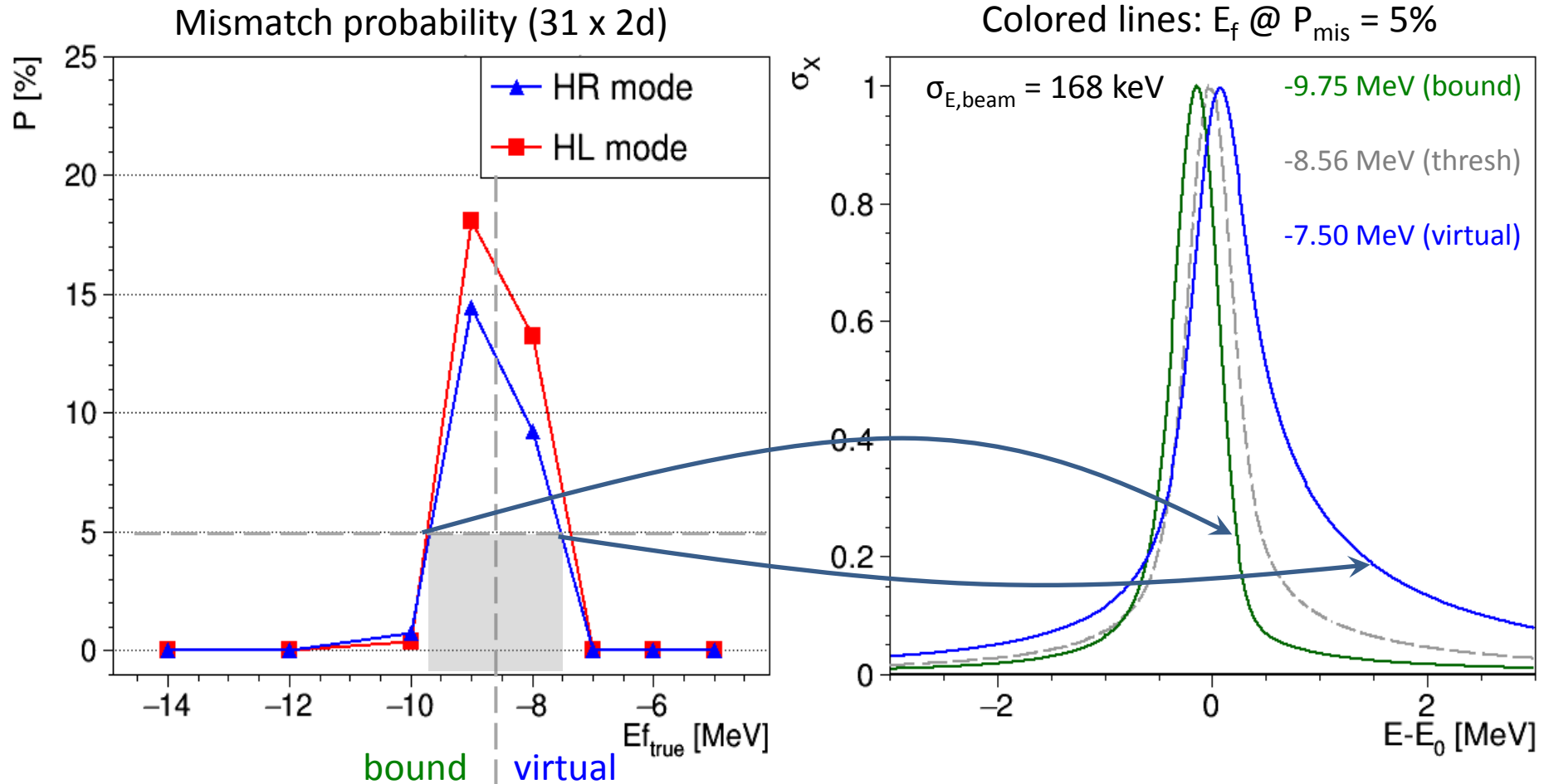
Sensitivities Molecule Lineshapes (31 x 2d)

- Extract standard deviation and bias from toy MC fits
- How well can **virtual** and **bound** state be distinguished?
- Uncertainty = σ_{Gaussian} \rightarrow **Integrate** in **mismatch region**



Probability of Mismatch (31x2d)

- How do the lineshapes look like?



Summary

- Investigation of X(3872)-Scan at PANDA in various scenarios
- Determined sensitivity for BW width measurement
 - Reach $\Gamma/\sigma_\Gamma > 3$ at $\Gamma \gtrsim 130$ keV (2 months data)
 - For $\Gamma \geq 100$ keV bias $\Delta\Gamma/\Gamma \leq 5\%$ (")
 - HL mode superior for $\Gamma > 180$ keV
- Determined sensitivity for molecular lineshape measurement
 - Possible to distinguish bound/virtual state
 - Outside $\Delta E_f = 2.25$ MeV trans. region $P > 95\%$ for correct id.
 - HL and HR modes seem comparable
- Further steps
 - Improve suppression of $J/\psi \pi^+\pi^-$ NR background
 - Start writing analysis document

BACKUP

Background Prefilter

- Reasonable S/N sensitivity: need huge amount of BG
- Example calculation:
 - Signal: $\sigma_S = 50 \text{ nb}$, $BR_{J/\psi} = 0.06$, $BR_X = 0.05$, $\epsilon_S = 20\%$
 - Background: $\sigma_B = 46 \text{ mb}$ (inelastic @ $E_{\text{cm}} = 3.872 \text{ GeV}$)

$$\frac{S}{N} = \frac{\sigma_S \cdot \epsilon_S}{\sigma_B \cdot \epsilon_B} \cdot BR_{J/\psi} \cdot BR_X \stackrel{!}{\geq} 1$$

$$\Rightarrow \epsilon_B < \frac{\sigma_S \cdot \epsilon_S}{\sigma_B} \cdot BR_{J/\psi} \cdot BR_X = 6.5 \cdot 10^{-10}$$

$$\Rightarrow N_B > 1/\epsilon_B = 1.5 \cdot 10^9$$

- Neither feasible nor efficient to simulate completely
- Use `FairFilteredPrimaryGenerator` to filter already at generator level

Final Selection $J/\psi \rightarrow e^+e^-$ Channel

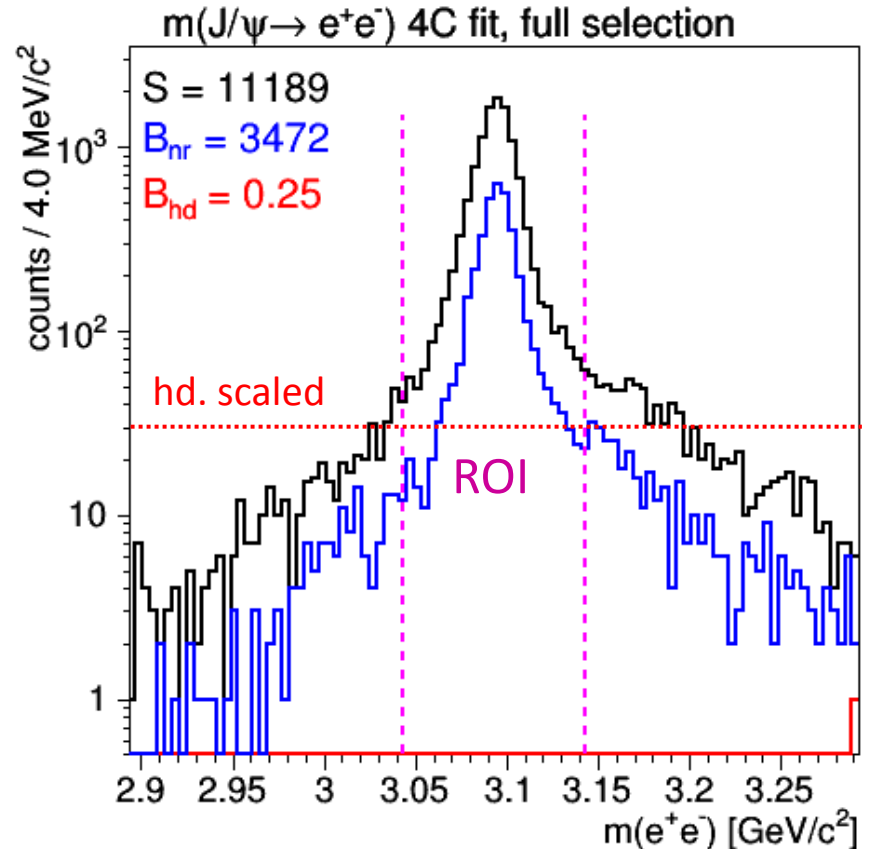
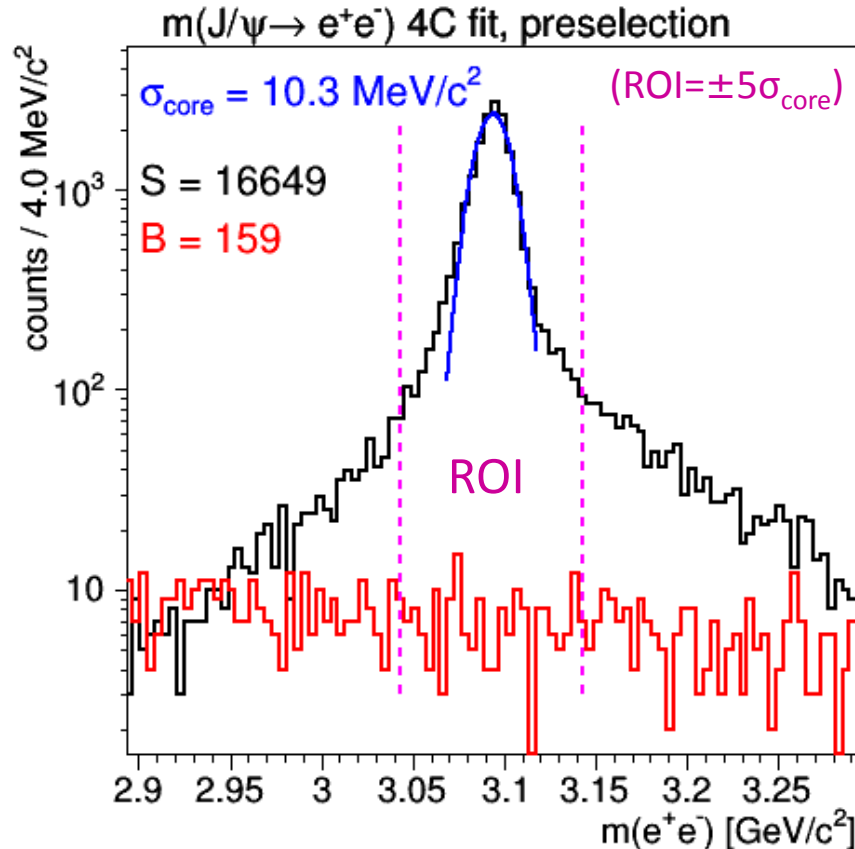
Preselection

$\epsilon_S = 16.6\%$
 $\epsilon_{B,nr} = \epsilon_S, \epsilon_{B,hd} = 1.7 \cdot 10^{-8}$
 $S:N = 1 : 32$



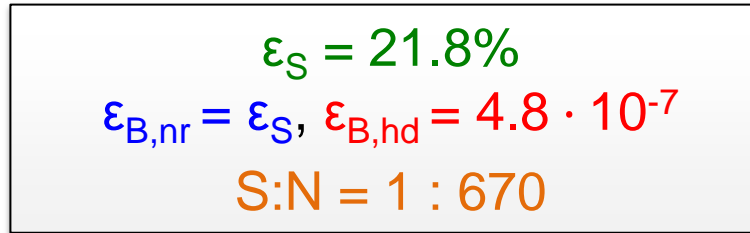
Final Selection

$\epsilon_S = 11.4\%$
 $\epsilon_{B,nr} = 3.5\%, \epsilon_{B,hd} = 2.6 \cdot 10^{-11}$
 $S:N = 4.6 : 1$

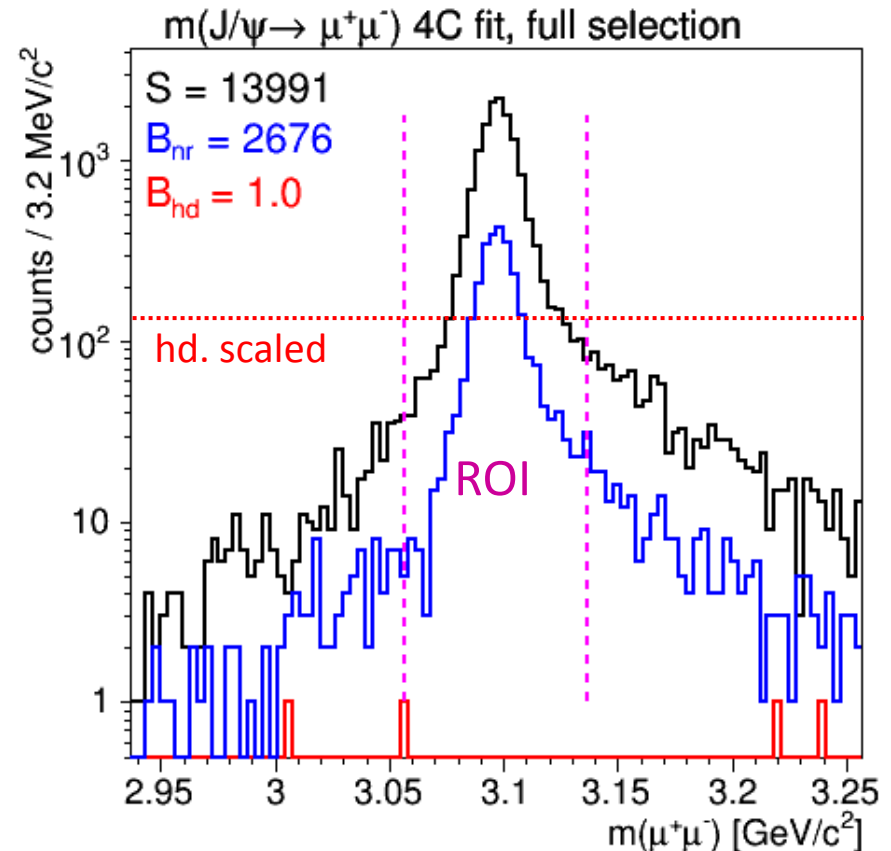
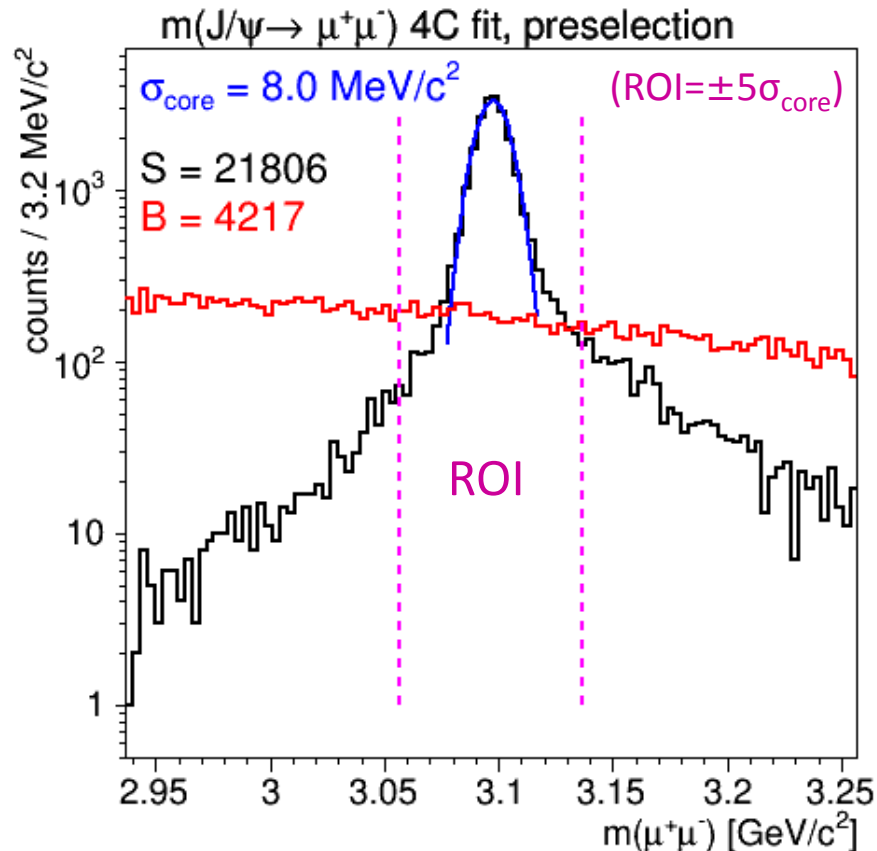
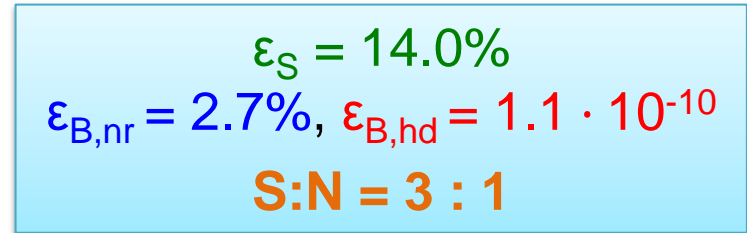


Final Selection $J/\psi \rightarrow \mu^+\mu^-$ Channel

Preselection

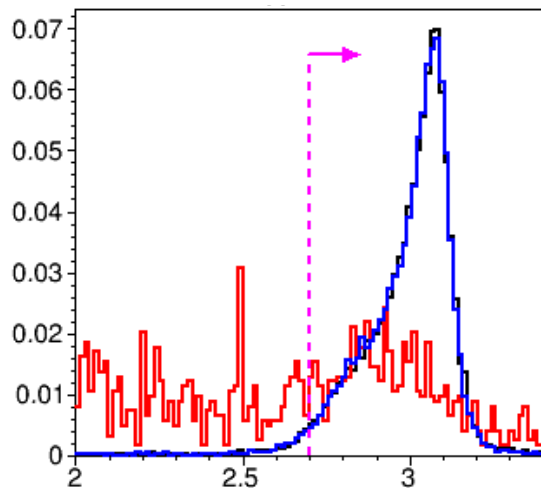


Final Selection

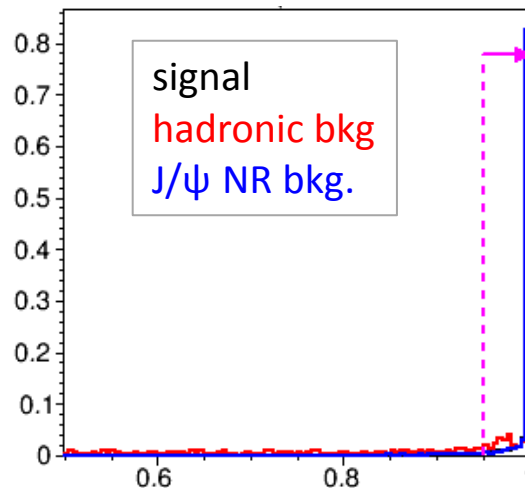


Criteria for $J/\psi \rightarrow e^+e^-$ Channel

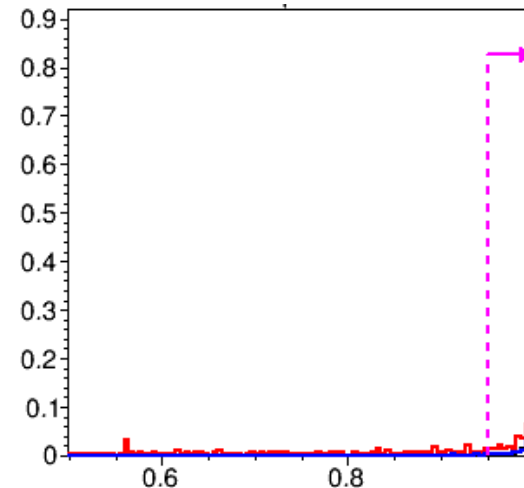
$m(e^+e^-) > 2.7 \text{ GeV}/c^2$



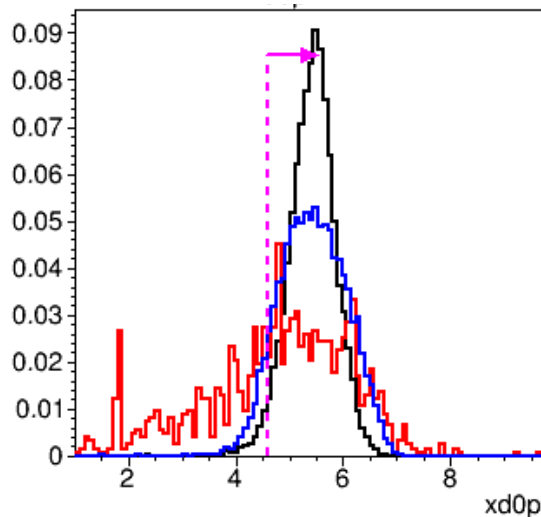
$\text{PID}(e^+) > 0.95$



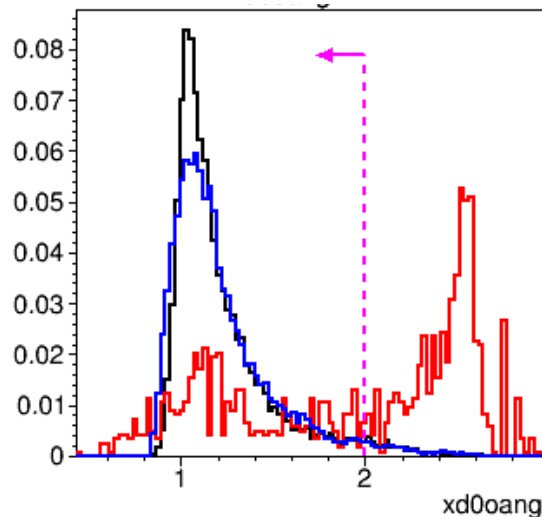
$\text{PID}(e^-) > 0.95$



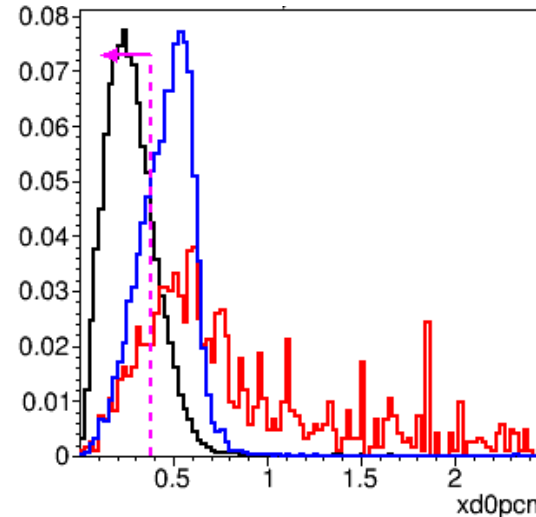
$p(e^+e^-) > 4.6 \text{ GeV}/c$



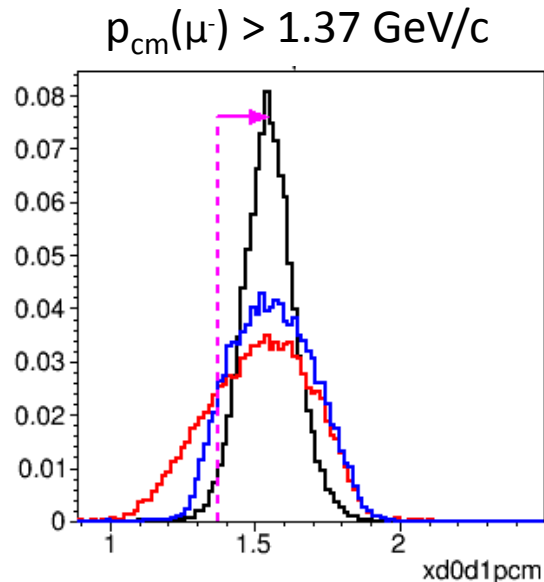
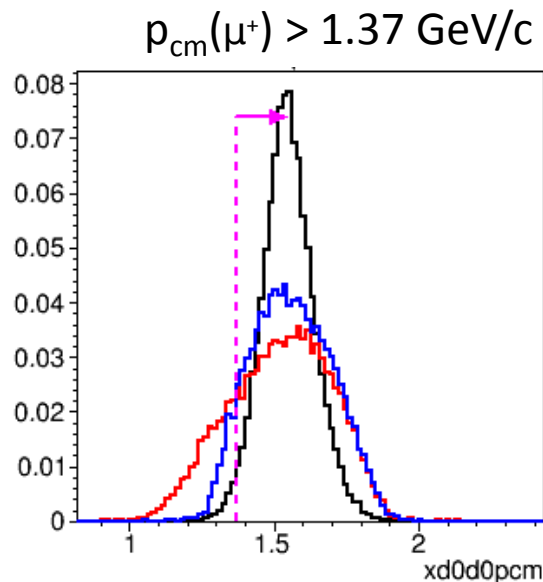
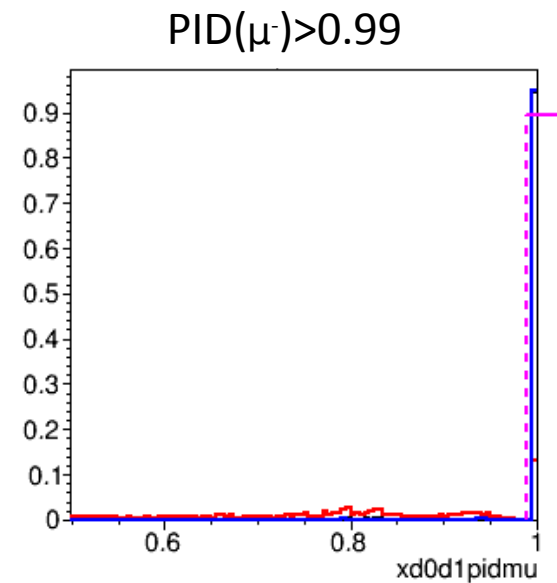
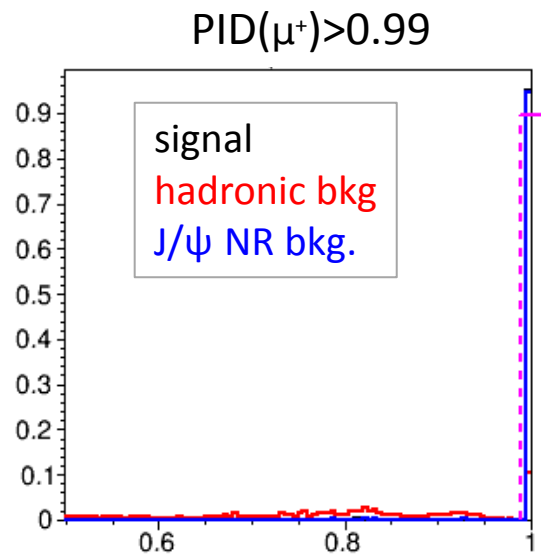
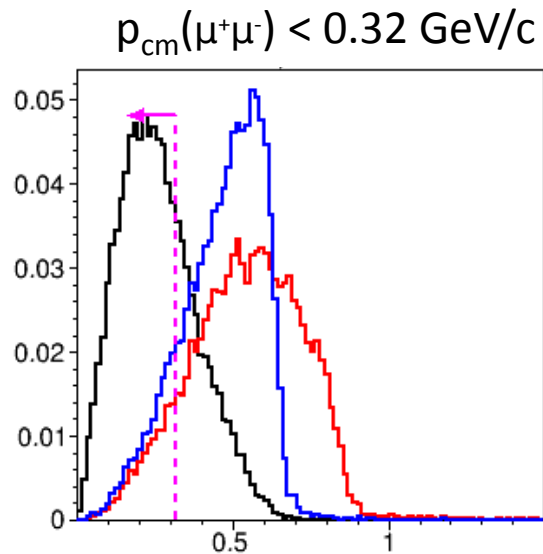
$\Delta(p_{e^+}, p_{e^-}) < 2 \text{ rad}$



$p_{\text{cm}}(e^+e^-) < 0.38 \text{ GeV}/c$



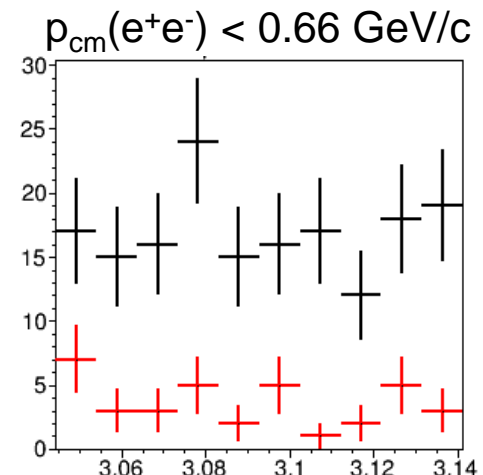
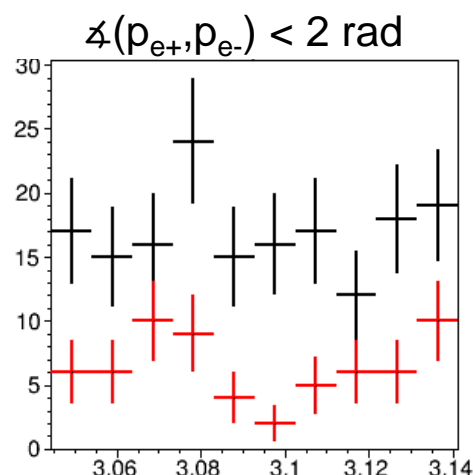
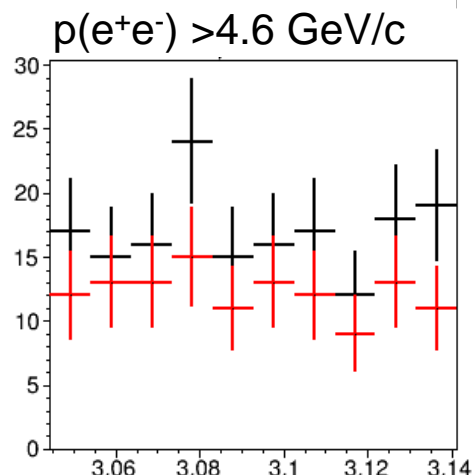
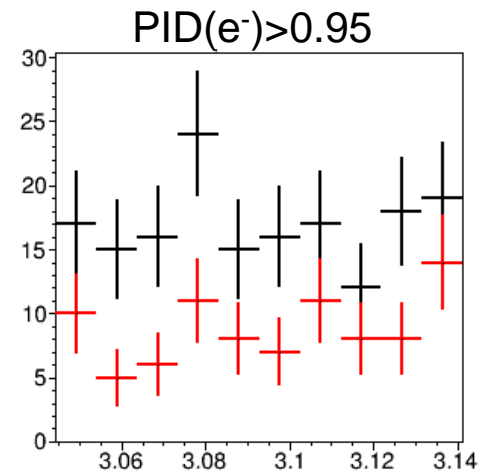
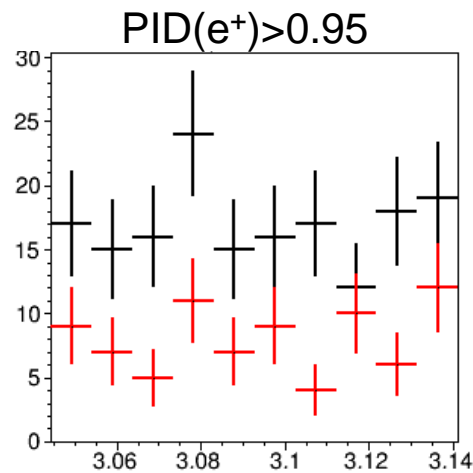
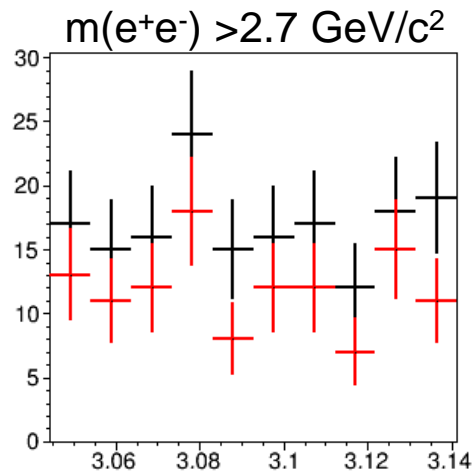
Criteria for $J/\psi \rightarrow \mu^+\mu^-$ Channel



Flatness Check of Cuts

- We want to interpolate background in ROI
 - Cuts should not distort background shape!

preselection
after cut

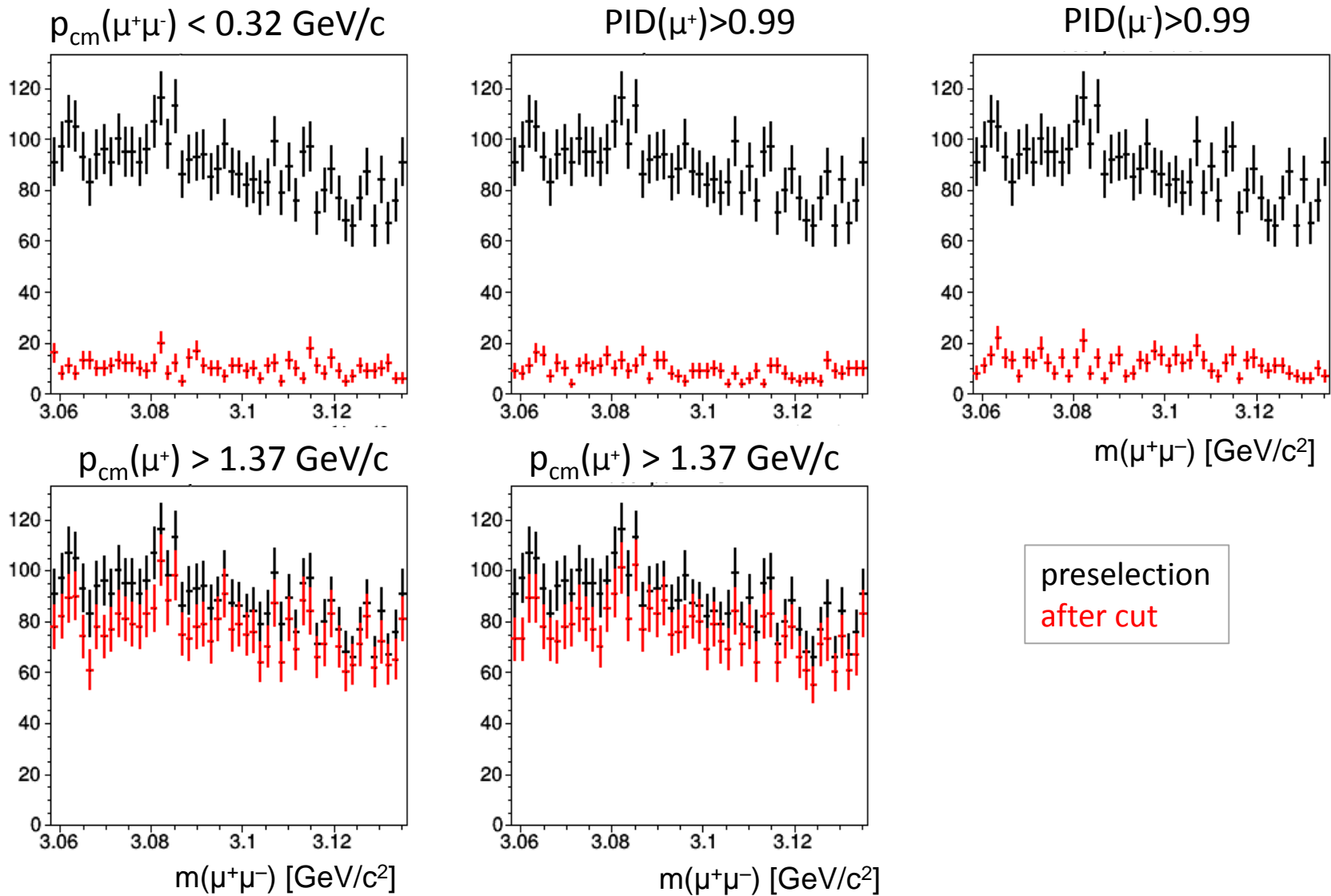


$m(e^+e^-) [\text{GeV}/c^2]$

$m(e^+e^-) [\text{GeV}/c^2]$

$m(e^+e^-) [\text{GeV}/c^2]$

Flatness Check of Cuts



Sensitivities Molecule Lineshapes (31 x 2d)

- Extract standard deviation and bias from toy MC fits
- How well can **virtual** and **bound** state be distinguished?

