

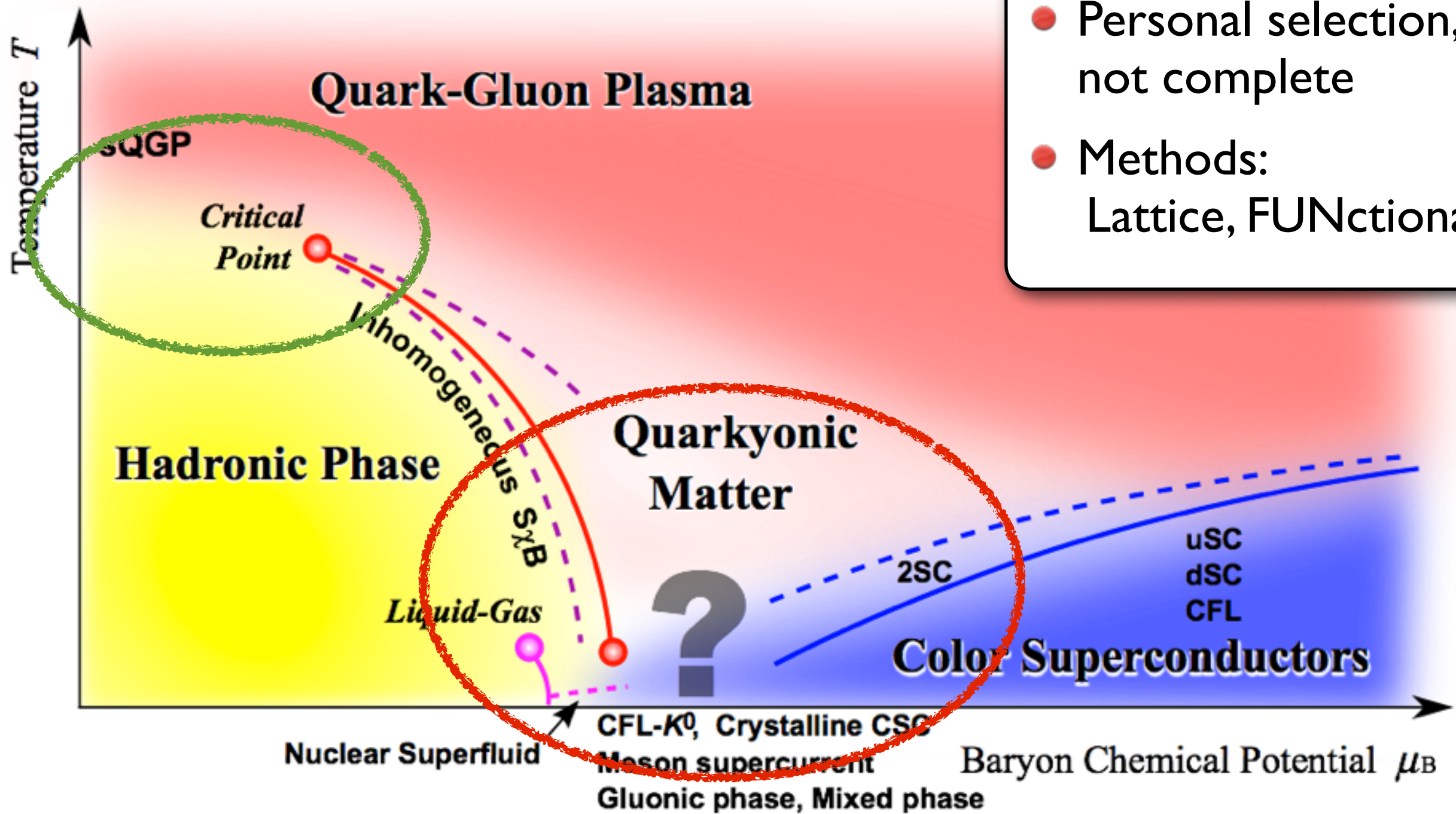
# Materie bei endlicher Temperatur und Dichte

Christian S. Fischer

Justus Liebig Universität Gießen

5th of December 2016

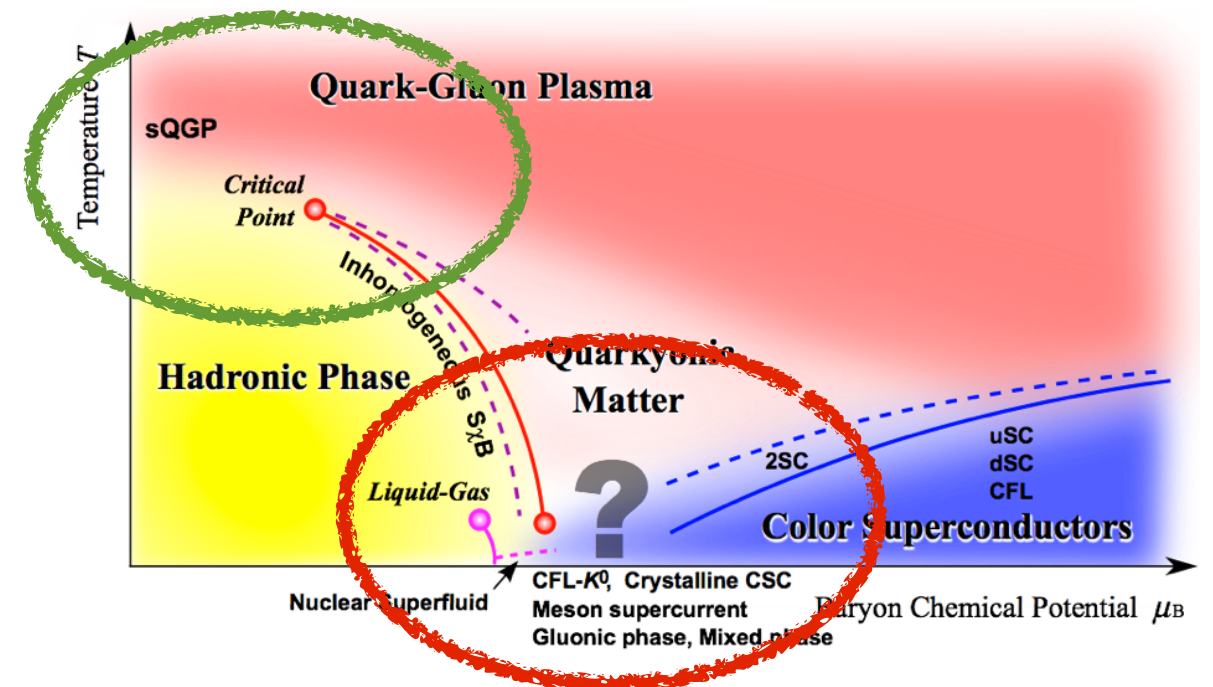
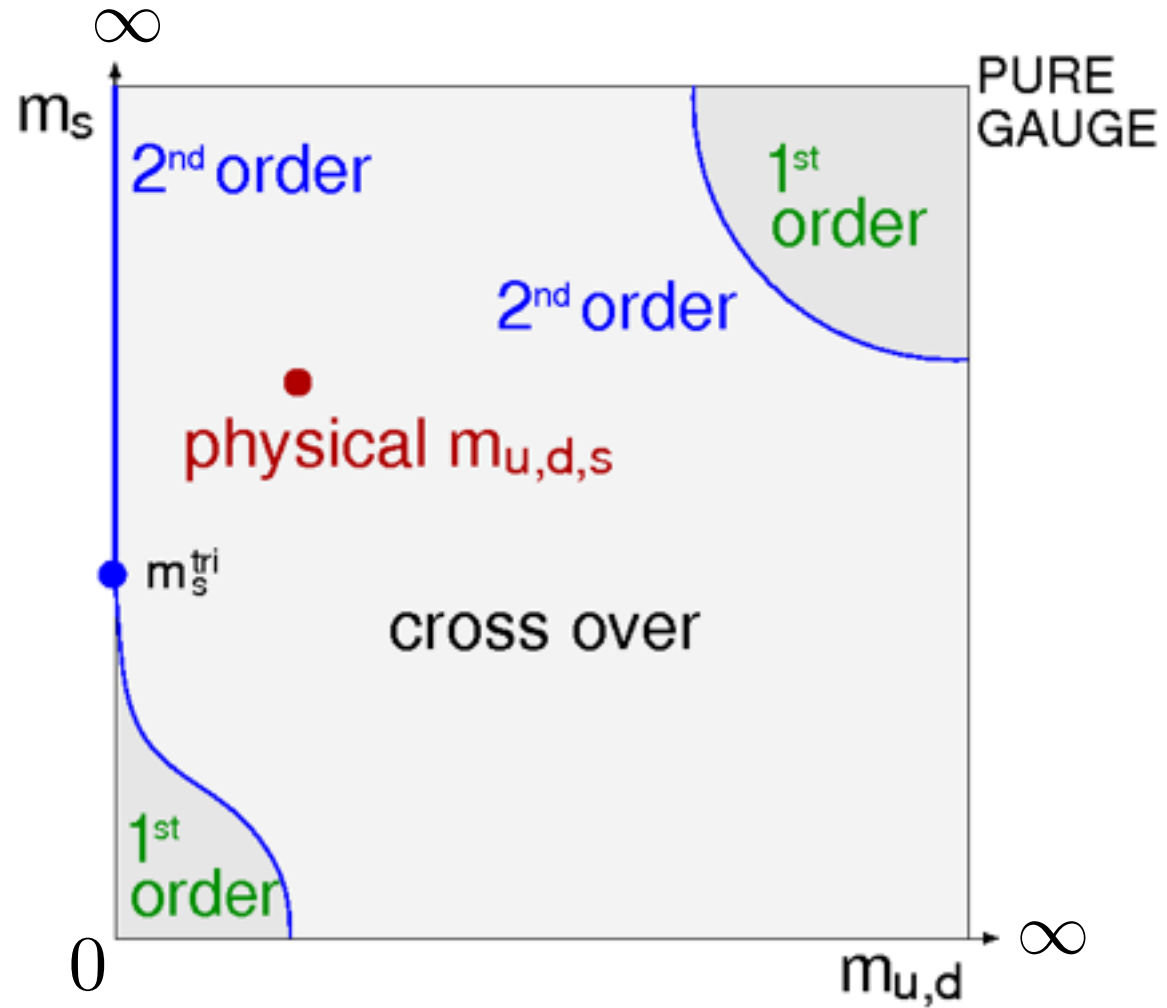
# QCD phase transitions I



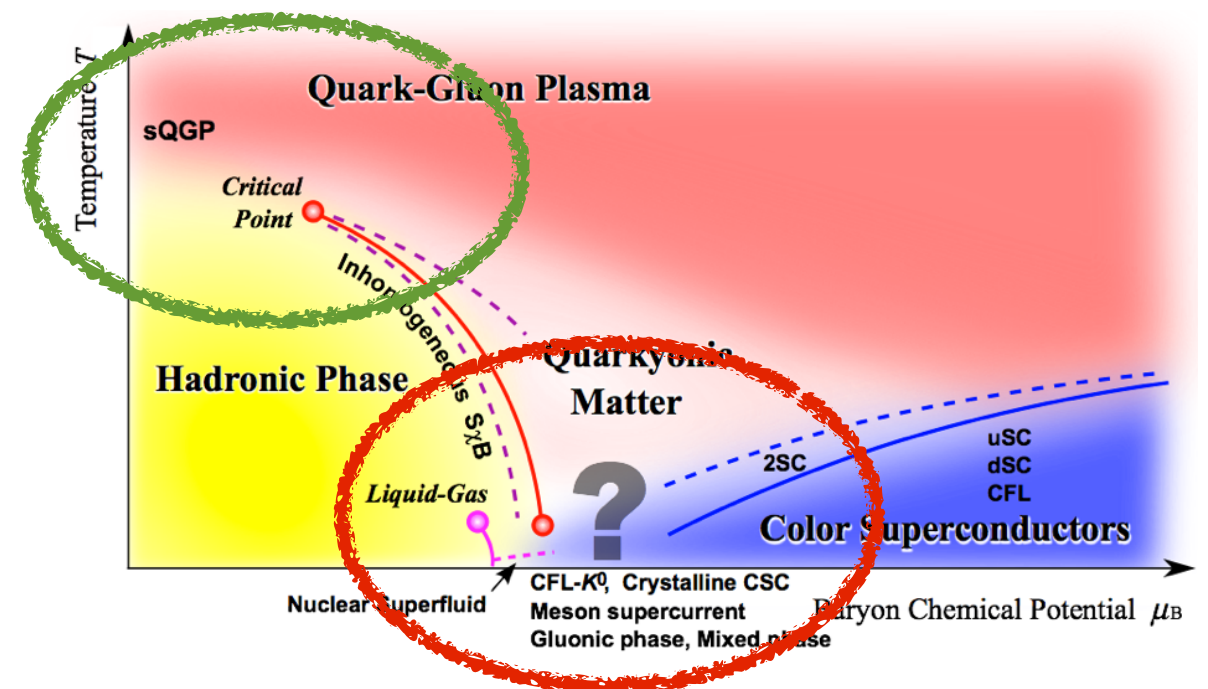
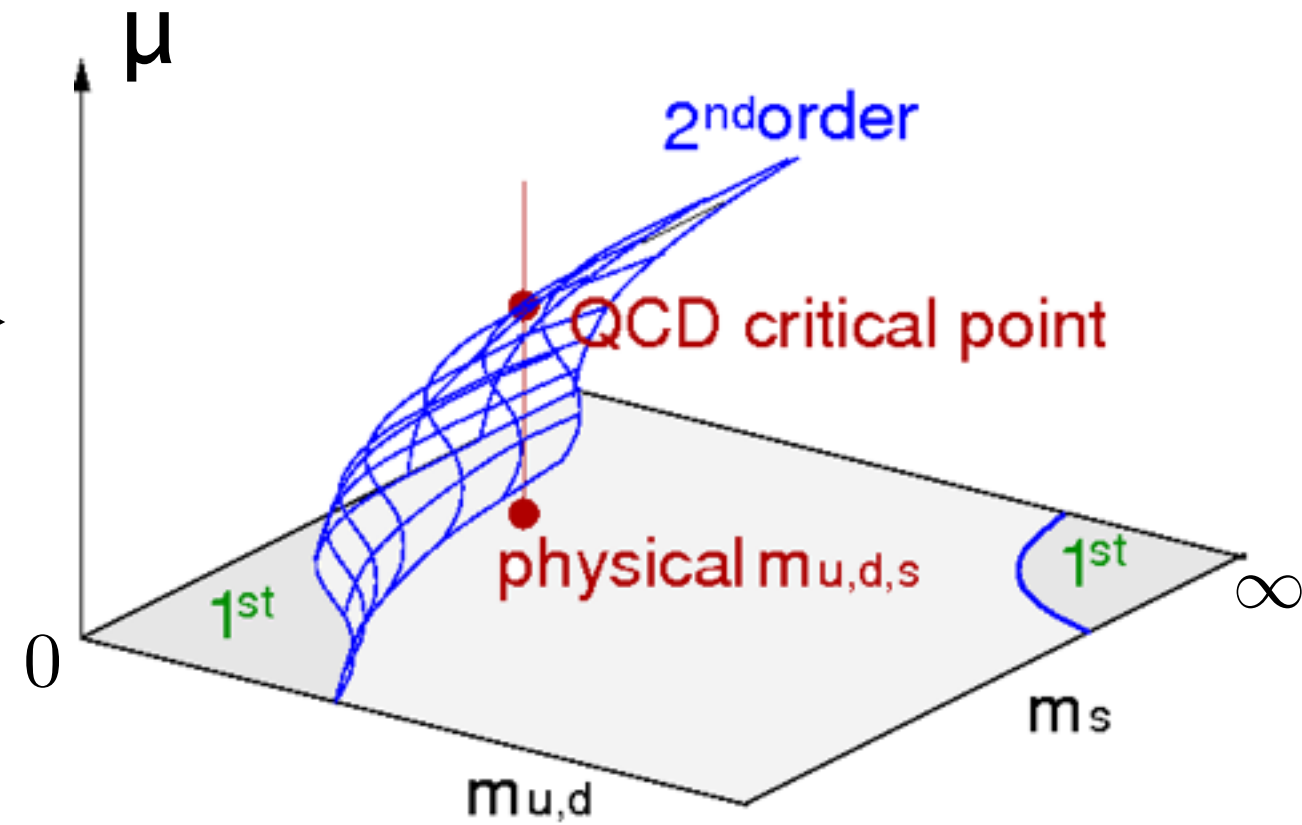
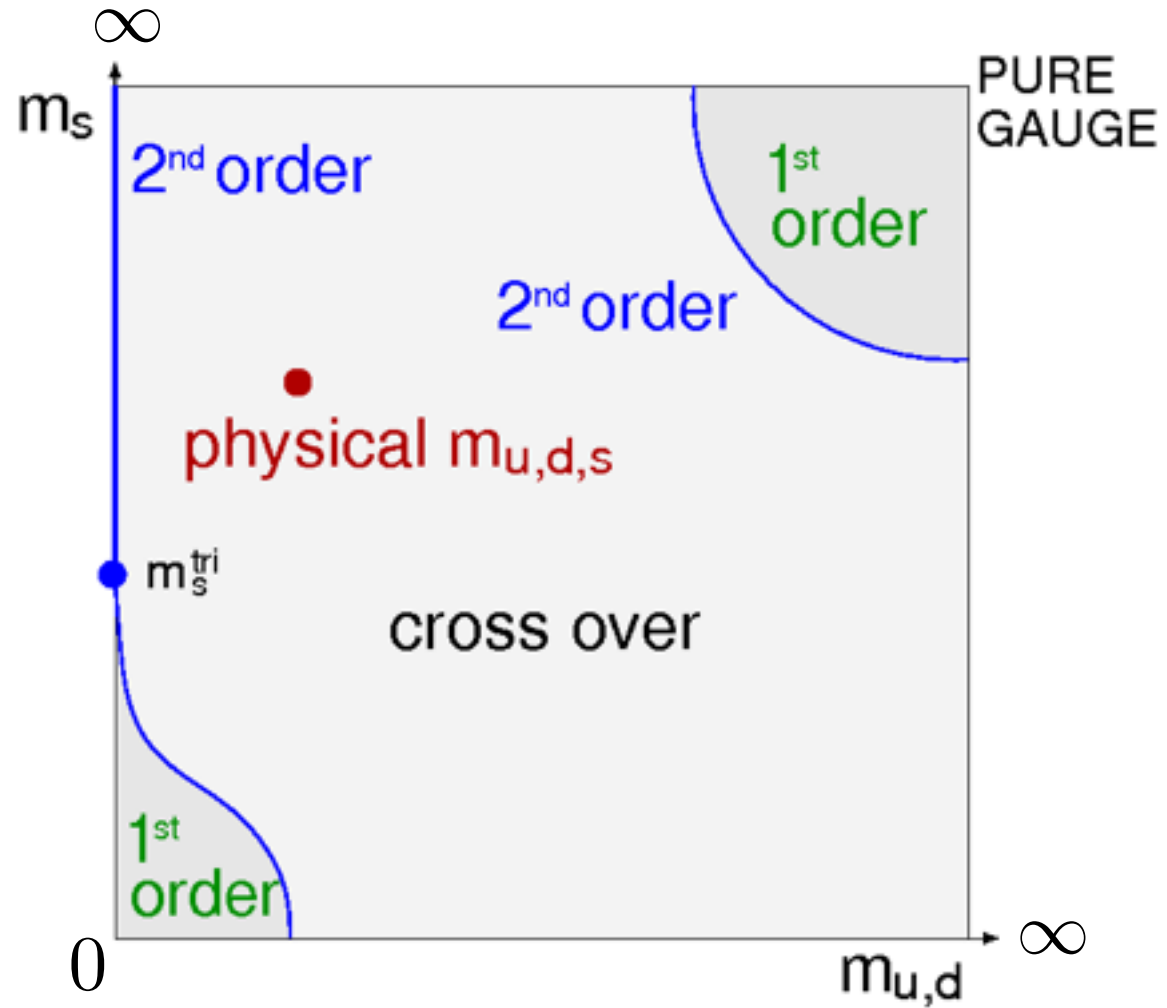
- Overview on progress in 2015
- Personal selection, not complete
- Methods: Lattice, FUNctional

Fukushima, Hatsuda, Rept. Prog. Phys. 74 (2011) 014001

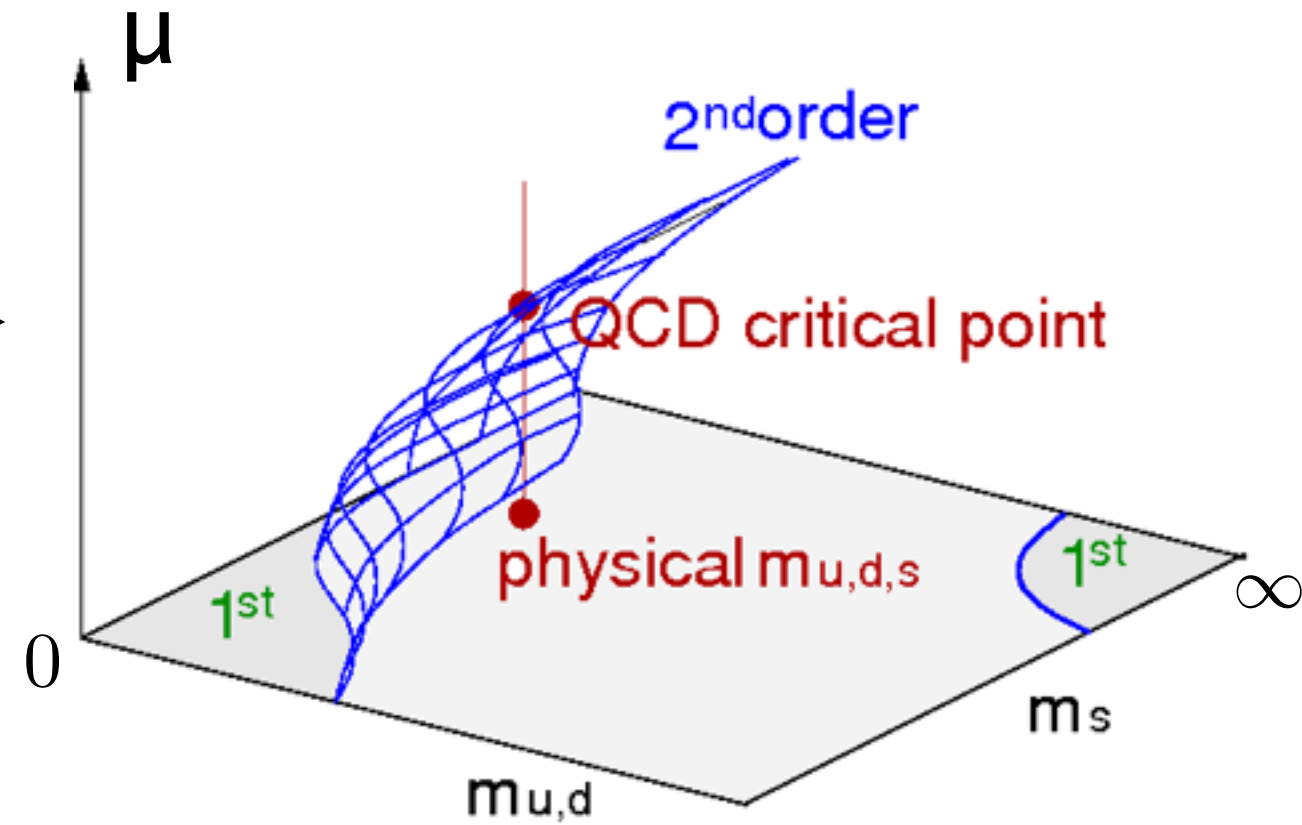
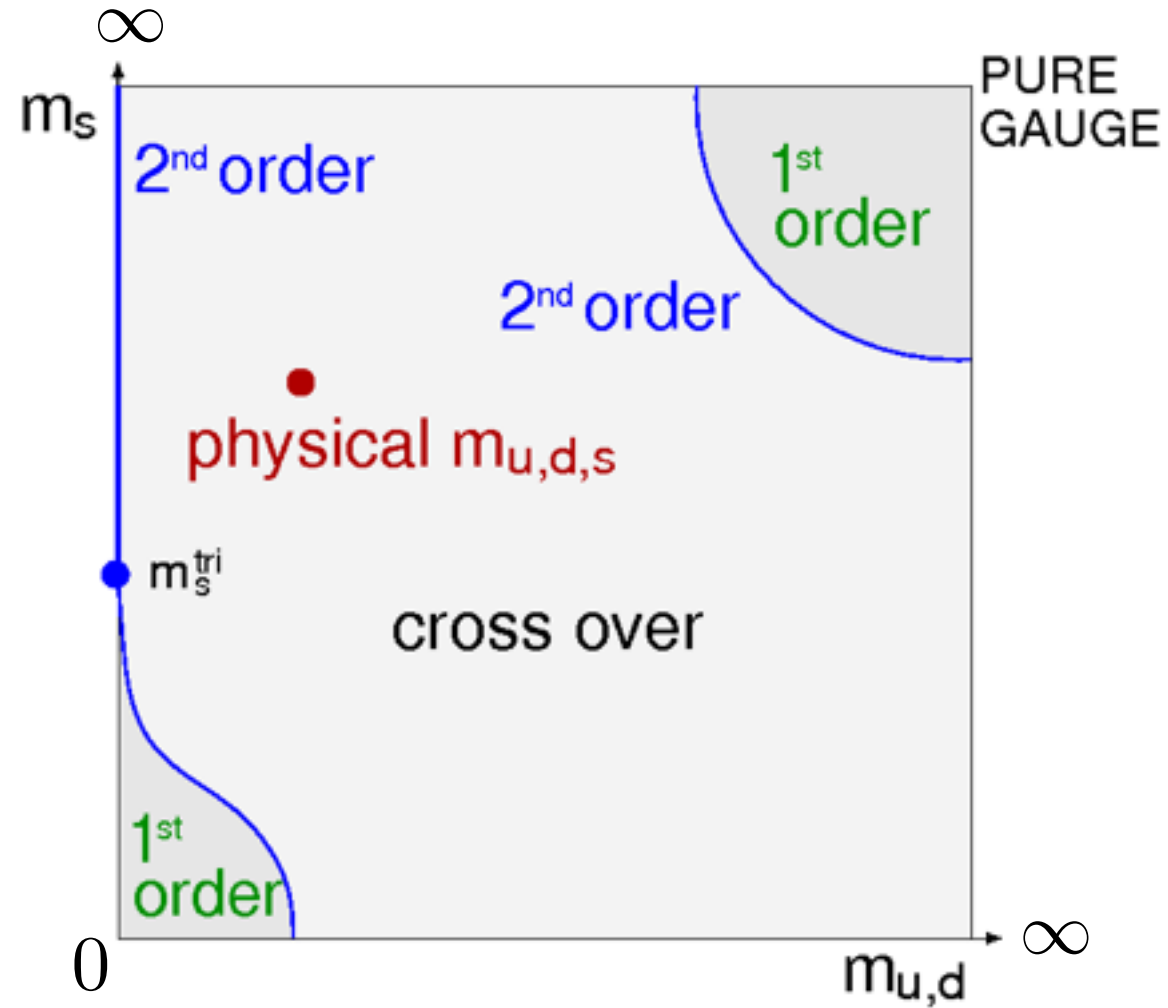
# Existence and properties of critical end point (CEP)



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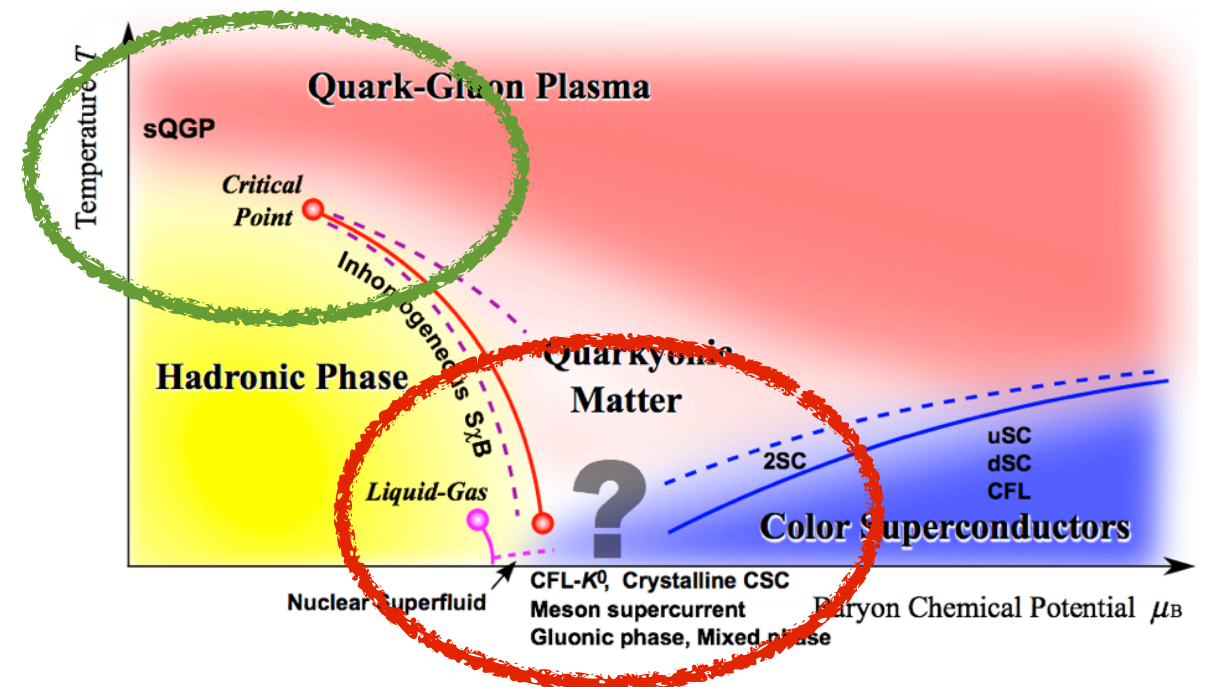


# Existence and properties of critical end point (CEP)



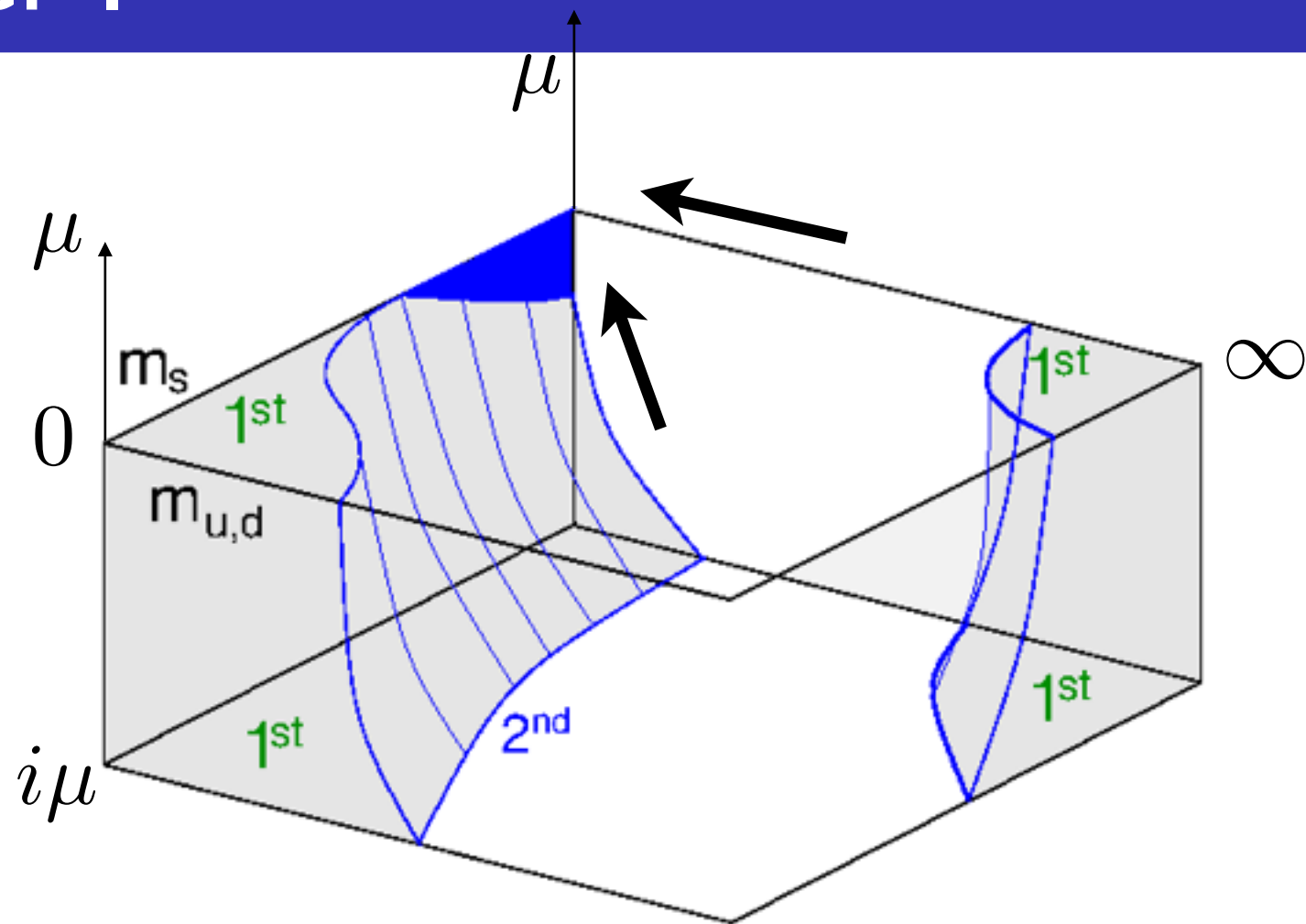
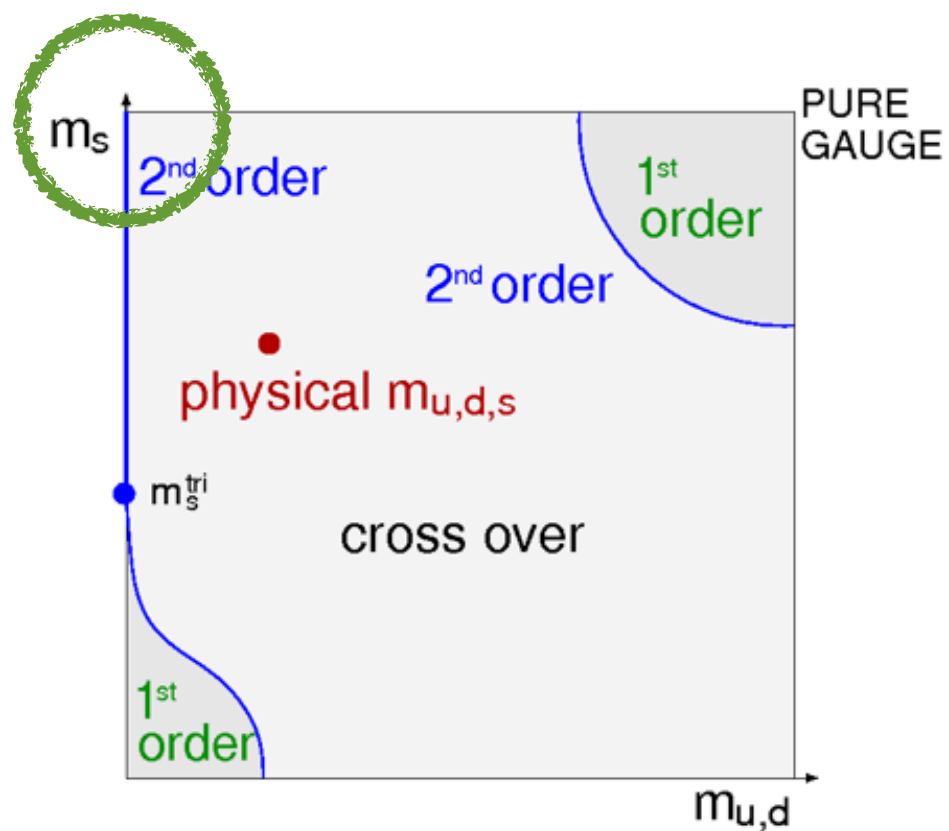
## Open questions:

- existence and location of CEP
- inhomogeneous phases
- observables:  $\eta/s$





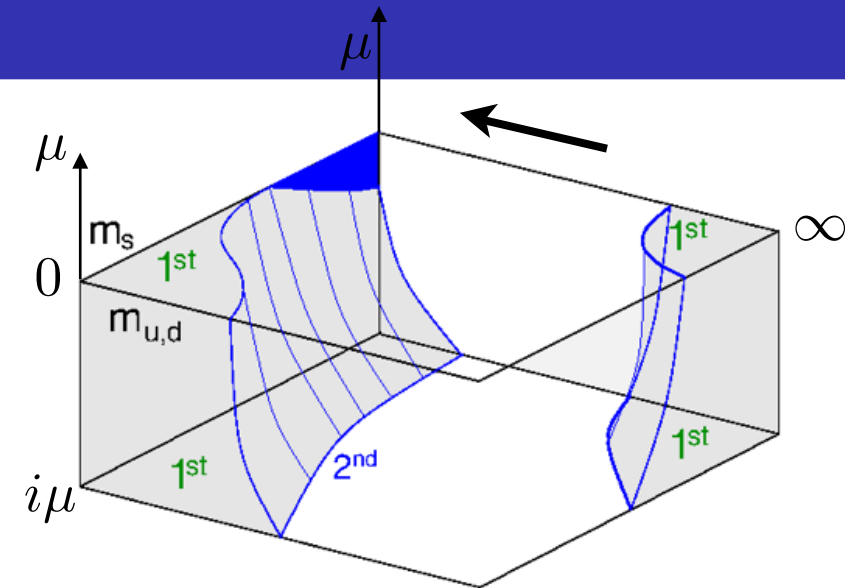
# The chiral $N_f=2$ - corner I



- $N_f=2$ : QCD chiral symmetries: 1st or 2nd order
- connected to axial  $U_A(1)$ -symmetry
  - not restored at  $T \approx T_c$  : 2nd order  $O(4)$
  - restored at  $T \approx T_c$  : 1st or 2nd order  $U(2) \times U(2)$

# The chiral $N_f=2$ - corner II

Dick, Karsch, Laermann, Mukherjee and Sharma, PRD 91 (2015) 9,094504



## Lattice method:

- restoration of  $U_A(1)$  makes  $\pi$  and  $\delta$  degenerate

$$\chi_\pi - \chi_\delta \xrightarrow{V \rightarrow \infty} \int_0^\infty d\lambda \frac{4m^2 \rho(\lambda, m)}{(\lambda^2 + m^2)^2} \quad \text{for } m_{u,d} \rightarrow 0$$

$\rho$  : eigenvalue density of overlap quark operator

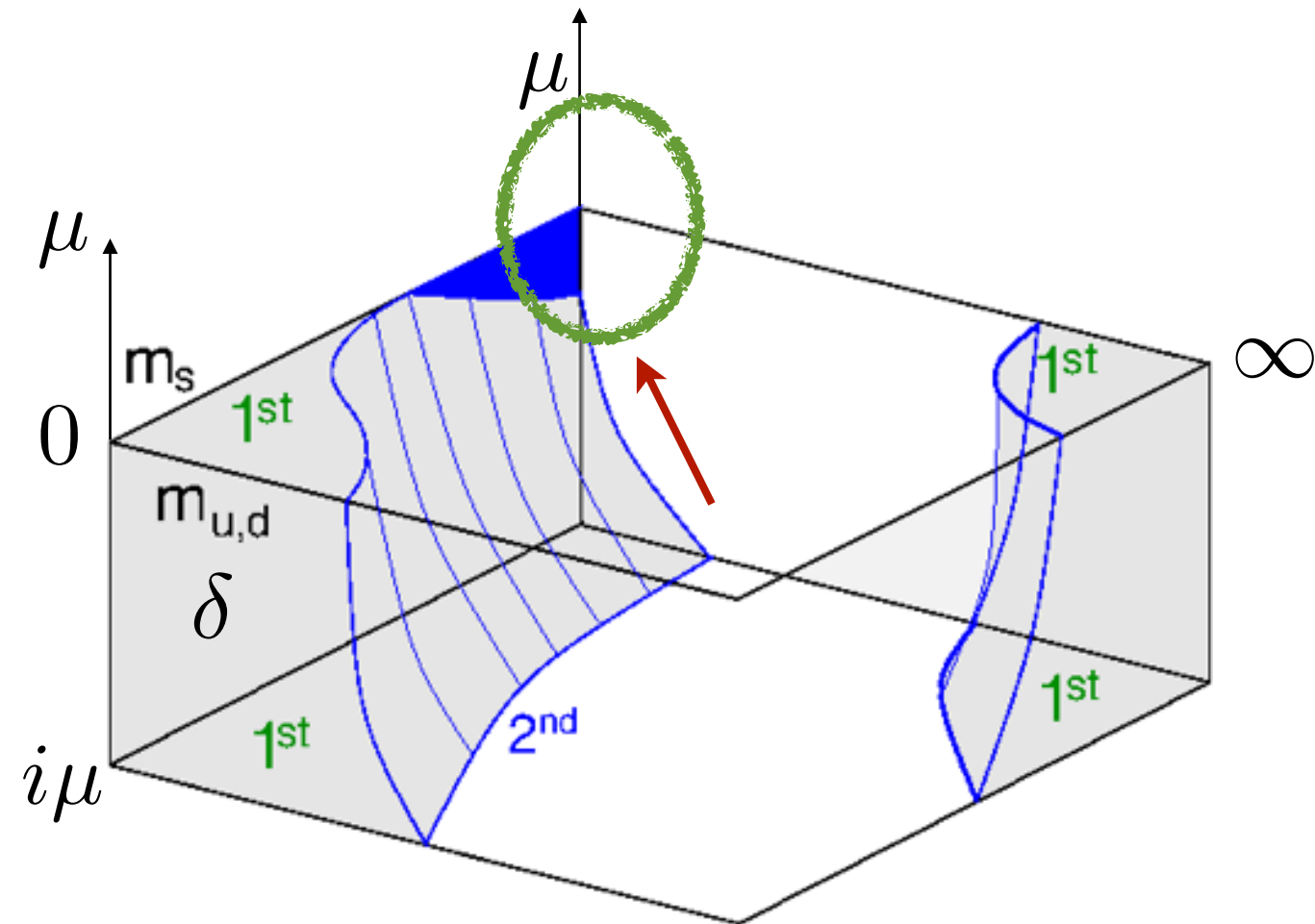
## Result:

- $\rho(0, 0) \neq 0$  up to  $T = 1.5T_c$
- axial  $U_A(1)$ -symmetry is **not** restored: **2nd order  $O(4)$**

# The chiral $N_f=2$ - corner III

## Lattice method:

- staggered or Wilson fermions
- map out critical line →



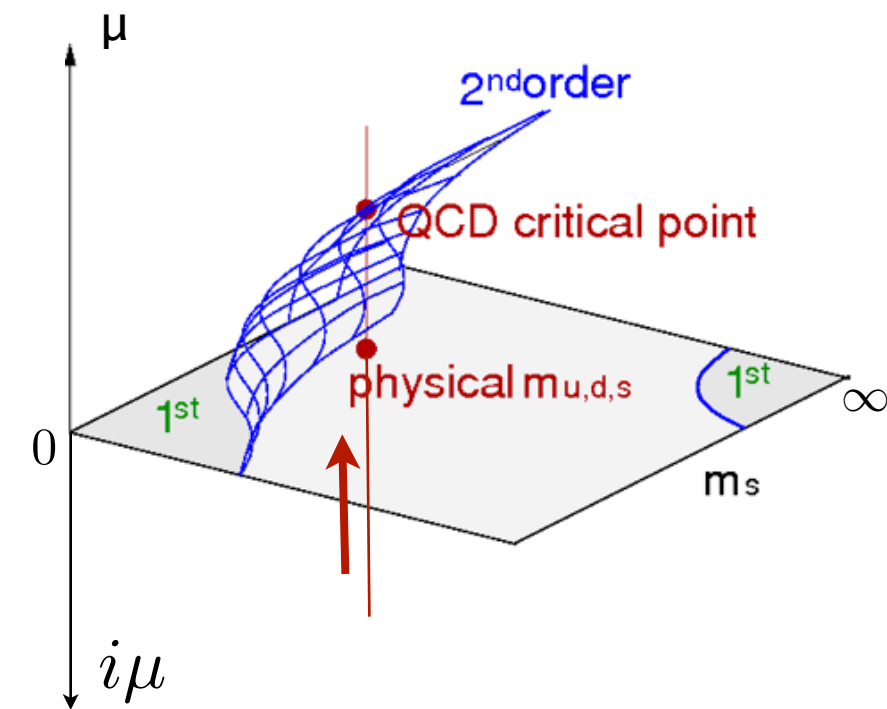
## Results:

- $N_T=4$ : tricritical point at **real  $\mu$** , i.e. **chiral  $N_f=2$  is 1st order**
- $N_T=6$ : chiral 1st order region shrinks...

Bonati, de Forcrand, D'Elia, Philipsen and Sanfilippo, PRD 90 (2014) 7  
Cuteri, Czaban, Philipsen and Pinke, arXiv:1511.03105 [hep-lat]



# Chiral transition line from analytic continuation

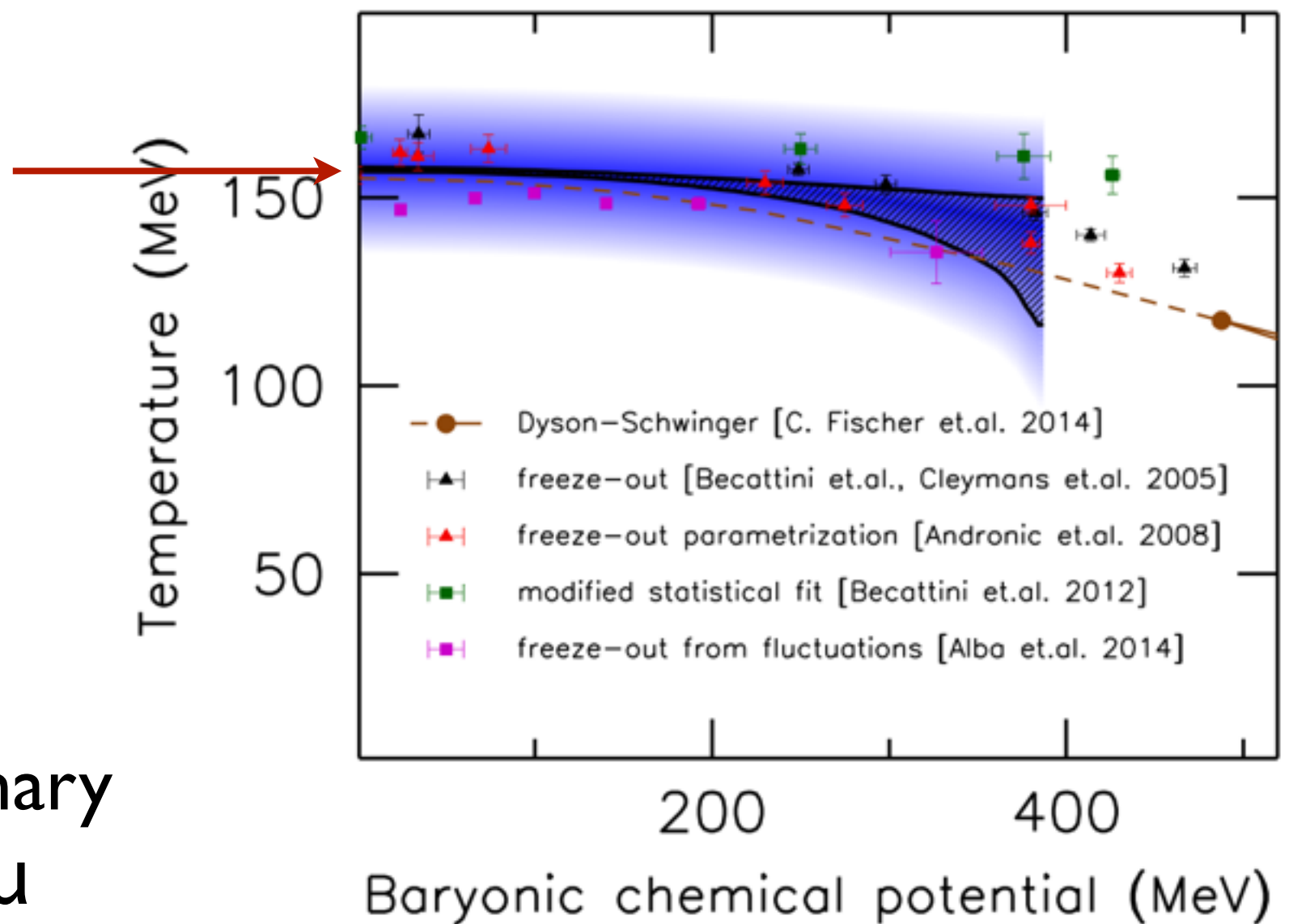


## Lattice method:

- Calc. boundary at imaginary and extrapolate to real  $\mu$
- Control systematics

## Results:

- Larger curvature than previous results (but: different definitions and error budget)



Bellwied, Borsanyi, Fodor, Günther, Katz, Ratti and Szabo, PLB B 751 (2015) 559

# Freeze out line from lattice QCD

Basic idea:

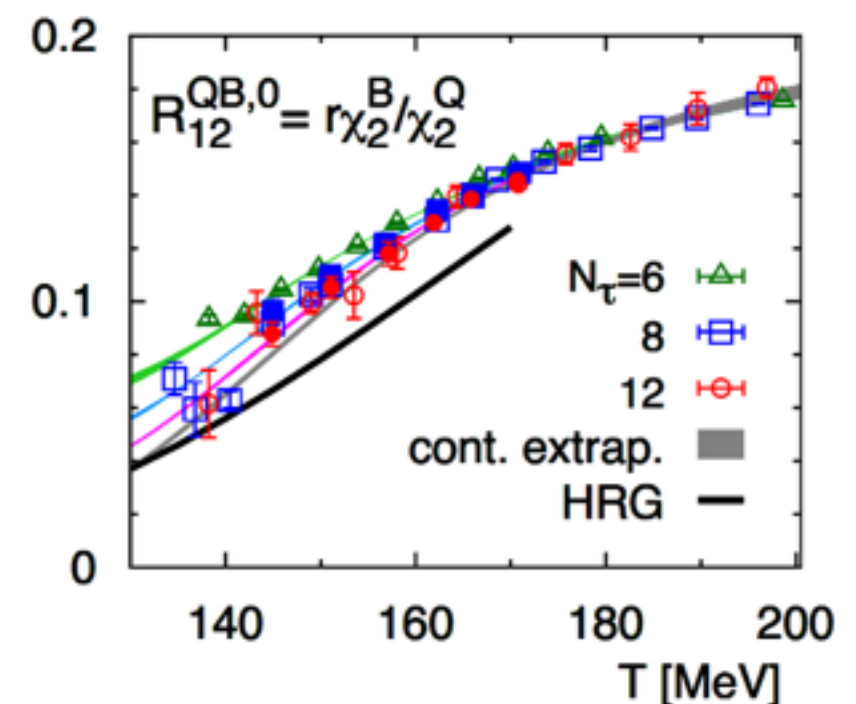
- Constrain freeze-out line by baryon number and electric charge fluctuations

$$T_f(\mu_B) = T_{f,0} \left( 1 - \kappa_2^f \left( \frac{\mu_B}{T_{f,0}} \right)^2 - \dots \right)$$

$$R_{12}^{QB} = R_{12}^{QB,0} + \left( R_{12}^{QB,2} - \kappa_2^f T_{f,0} \frac{dR_{12}^{QB,0}}{dT|_{T_{f,0}}} \right) \hat{\mu}_B^2$$

$$\text{with } R_{12}^{QB}(T, \mu) = \frac{\chi_1^Q}{\chi_1^B} \frac{\chi_2^B}{\chi_2^Q}$$

extract  $\kappa_2^f$   
from lattice QCD  
and/or experiment

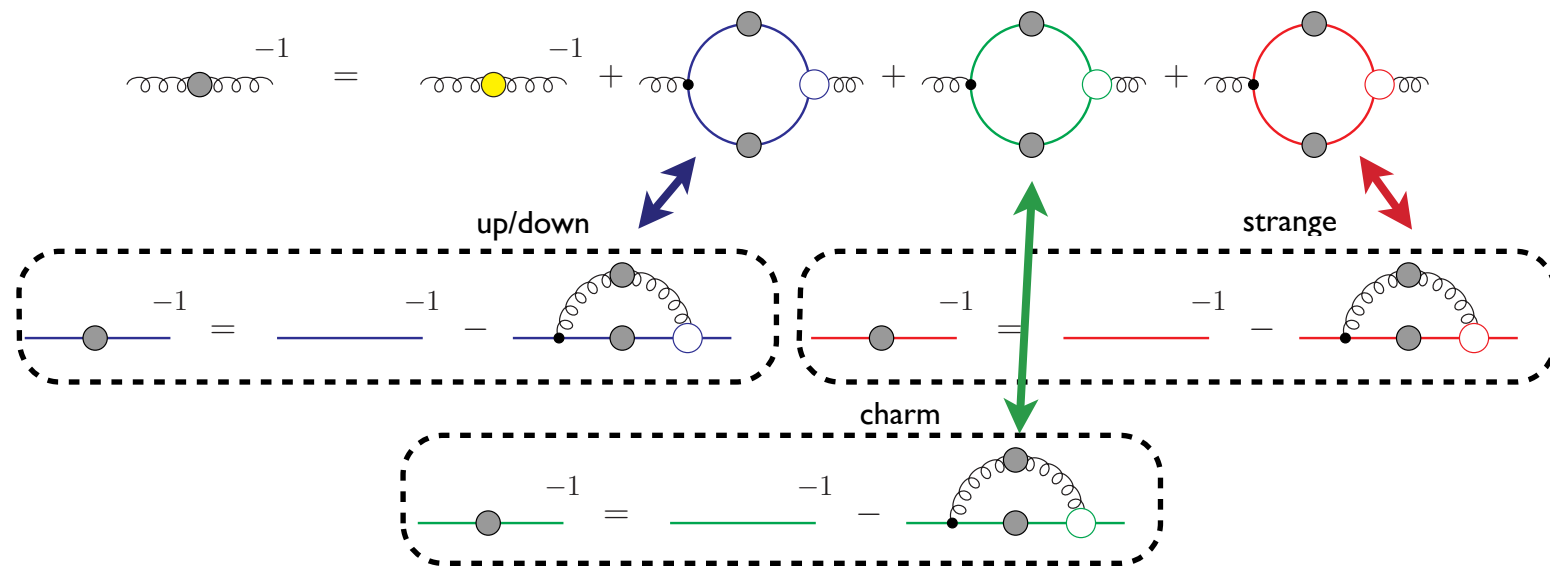


Results:

- Small curvature up to  $\sqrt{s_{NN}} \geq 27\text{GeV}$  *i.e.*  $\mu_B \leq 150\text{MeV}$

Bazavov, Ding, Hegde, Kaczmarek, Karsch, Laermann *et al.*, arXiv:1509.05786 [hep-lat]

# Chiral transition line from functional methods

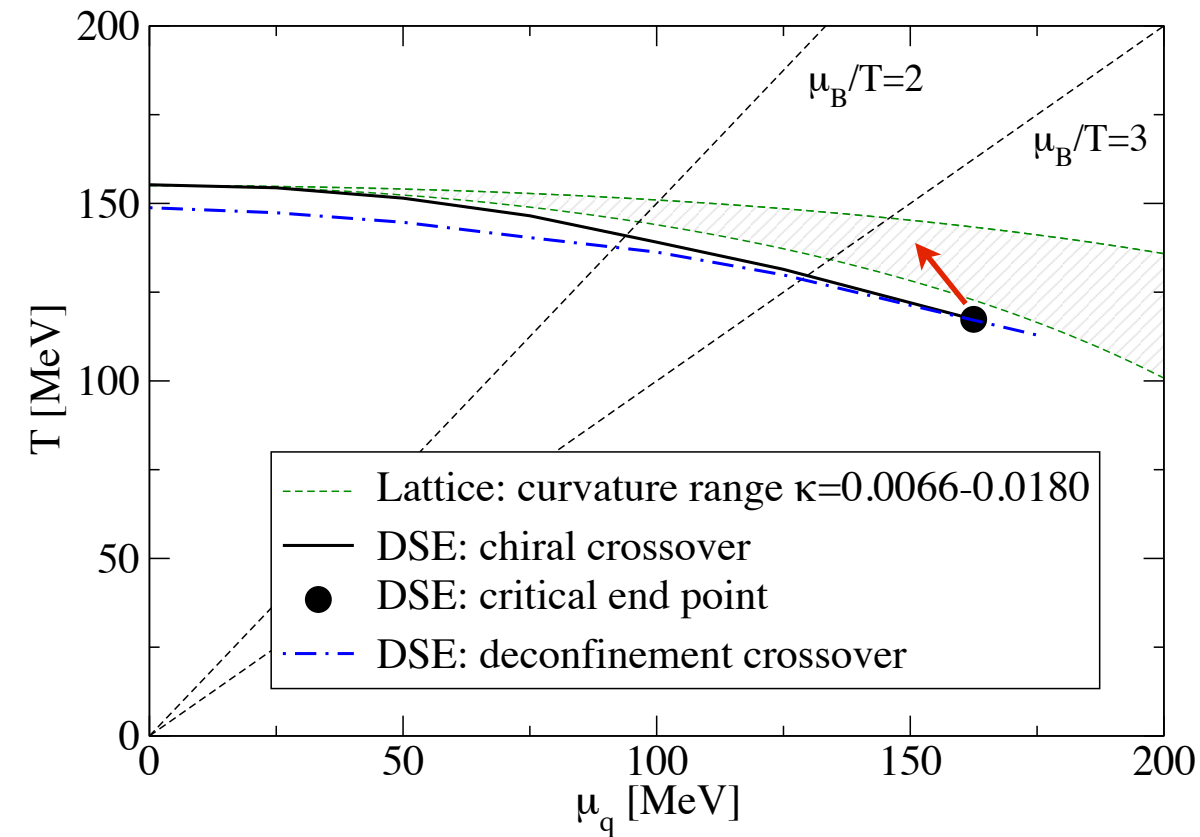
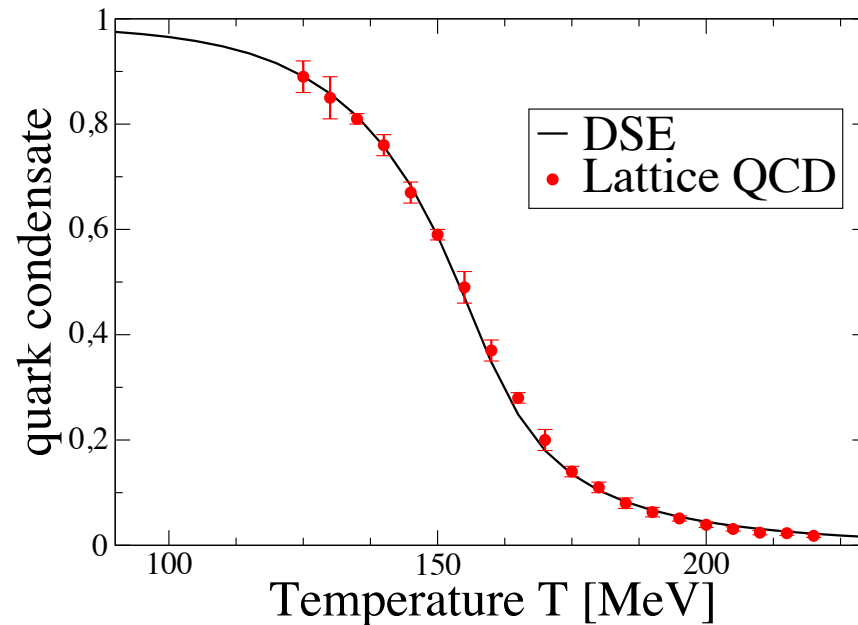


## Functional method: DSEs

- Use lattice results at  $\mu=0$  as input (quenched glue) and crosscheck (chiral condensate)

Fischer, Luecker and Welzbacher, PRD 90 (2014) 3,034022  
Eichmann, Fischer and Welzbacher, arXiv:1509.02082 [hep-ph]

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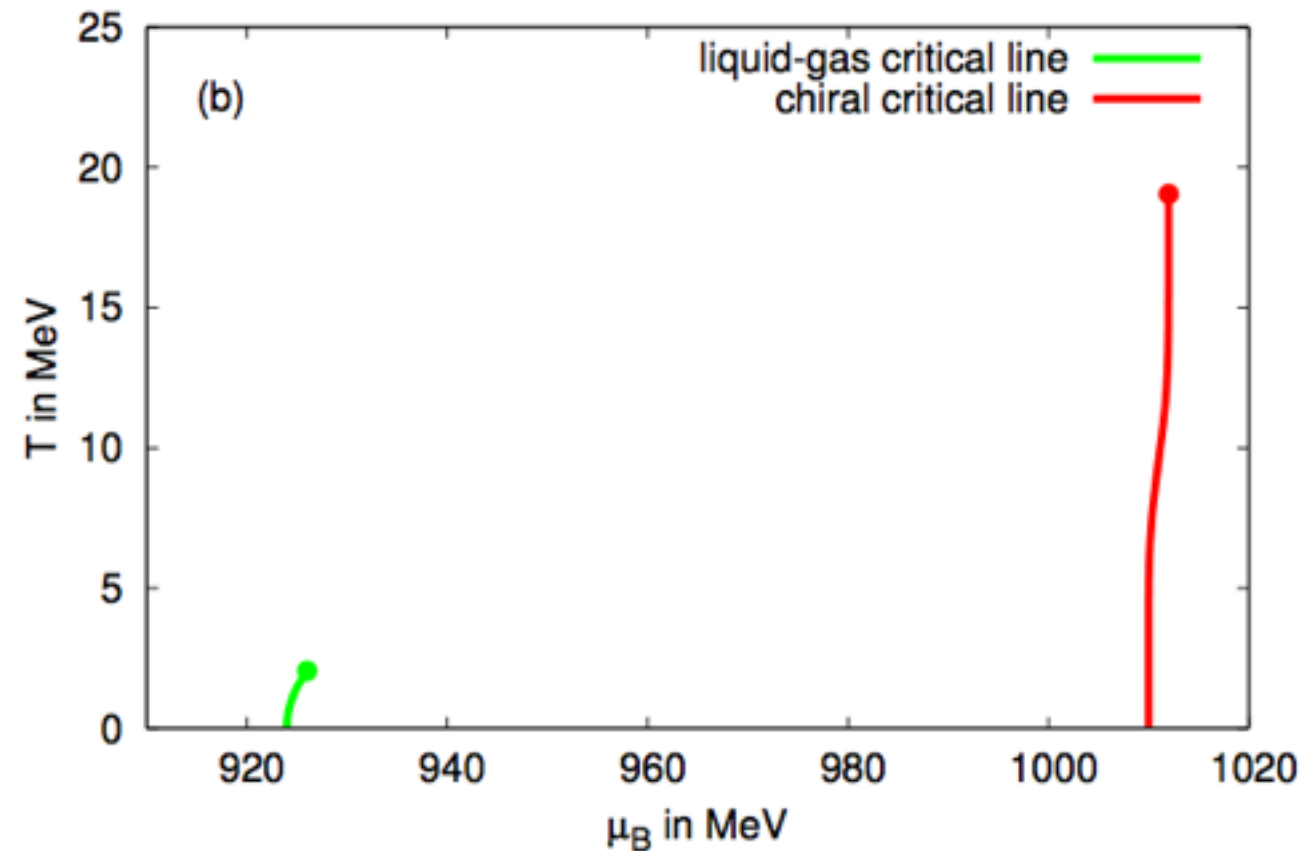
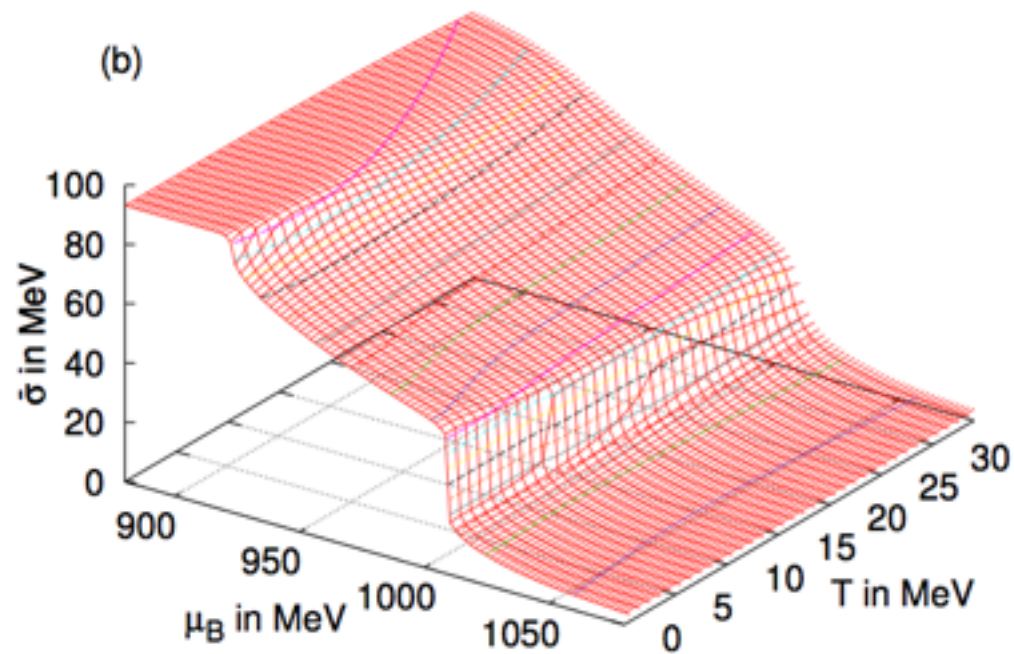
## Results:

- CEP at large chemical potential
- Baryon effects: curvature may decrease (exploratory calc.)

Fischer, Luecker and Welzbacher, PRD 90 (2014) 3,034022

Eichmann, Fischer and Welzbacher, arXiv:1509.02082 [hep-ph]

# Nuclear matter beyond mean field



## FRG-treatment of ‘Mirror model’:

- Baryons multiplets together with parity partners:  
finite baryon masses in chiral limit
- Interaction via meson exchanges

## Results:

- See both, liquid-gas and chiral transition
- Qualitatively stable wrt. fluctuations

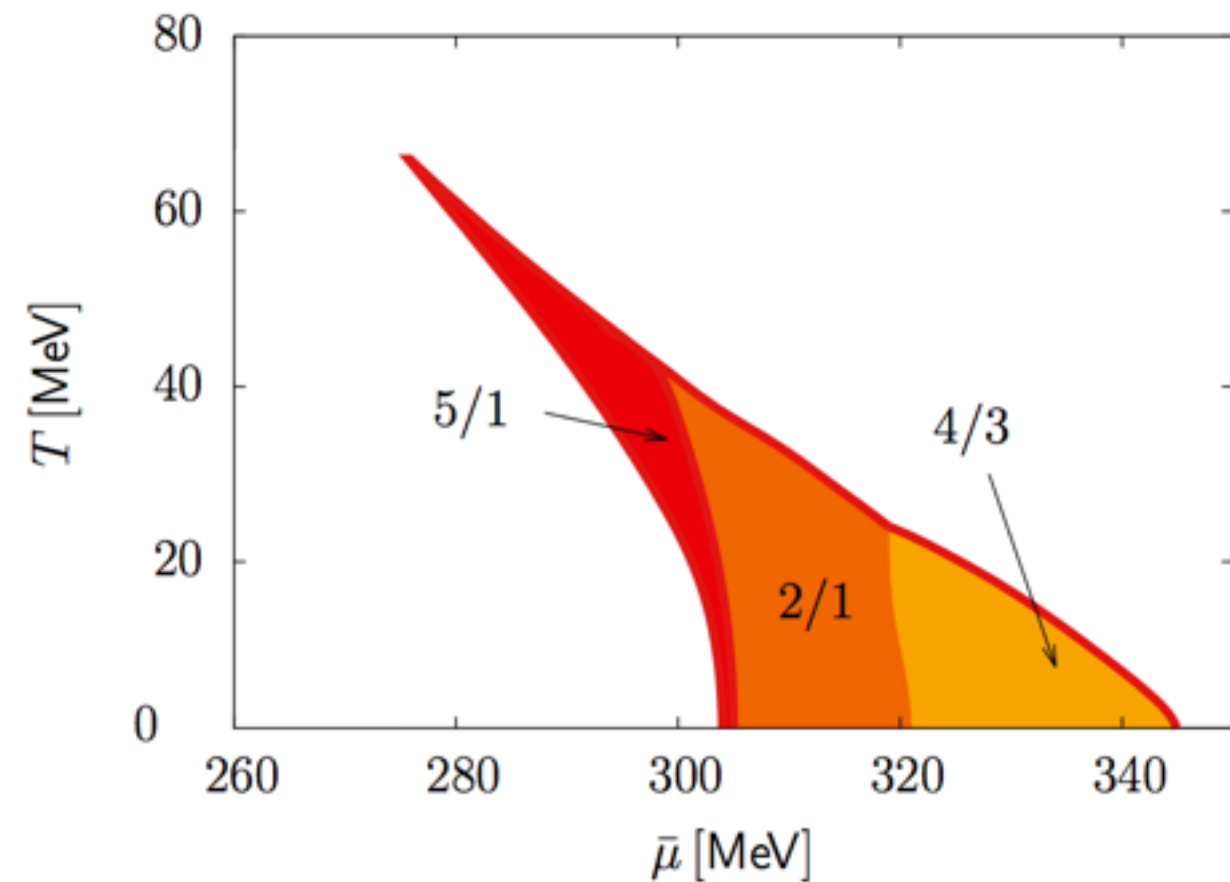
Weyrich, Strodthoff and von Smekal, PRC 92 (2015) 1, 015214



# Inhomogeneous phases

## Basic idea:

- allow for spatially varying chiral condensates
- potential impact on transport and cooling in compact stars



## Mean field NJL-model:

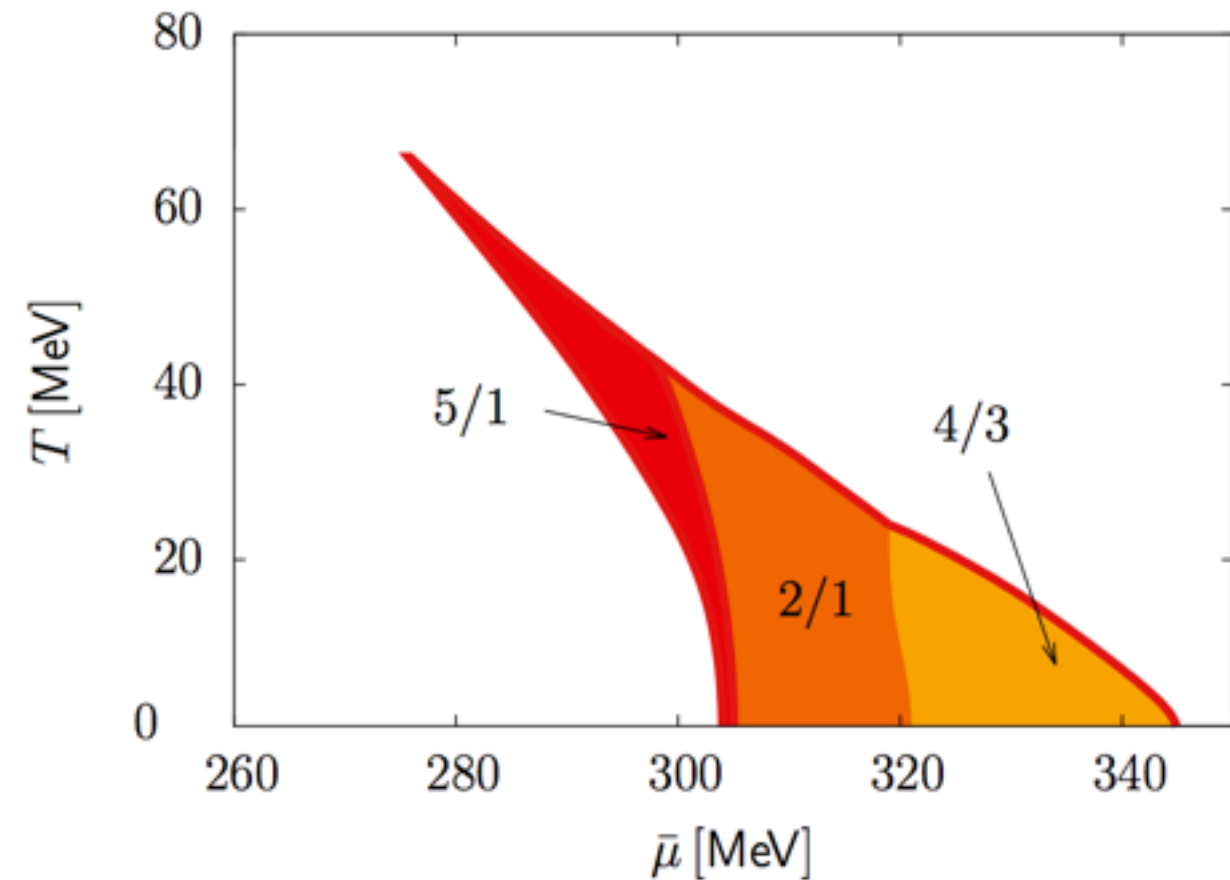
- Compact stars: charge neutrality and beta-equilibrium implies isospin imbalance

Nowakowski, Buballa, Carignano and Wambach, arXiv:1506.04260 [hep-ph] Buballa and Carignano, Prog. Part. Nucl. Phys. 81 (2015) 39

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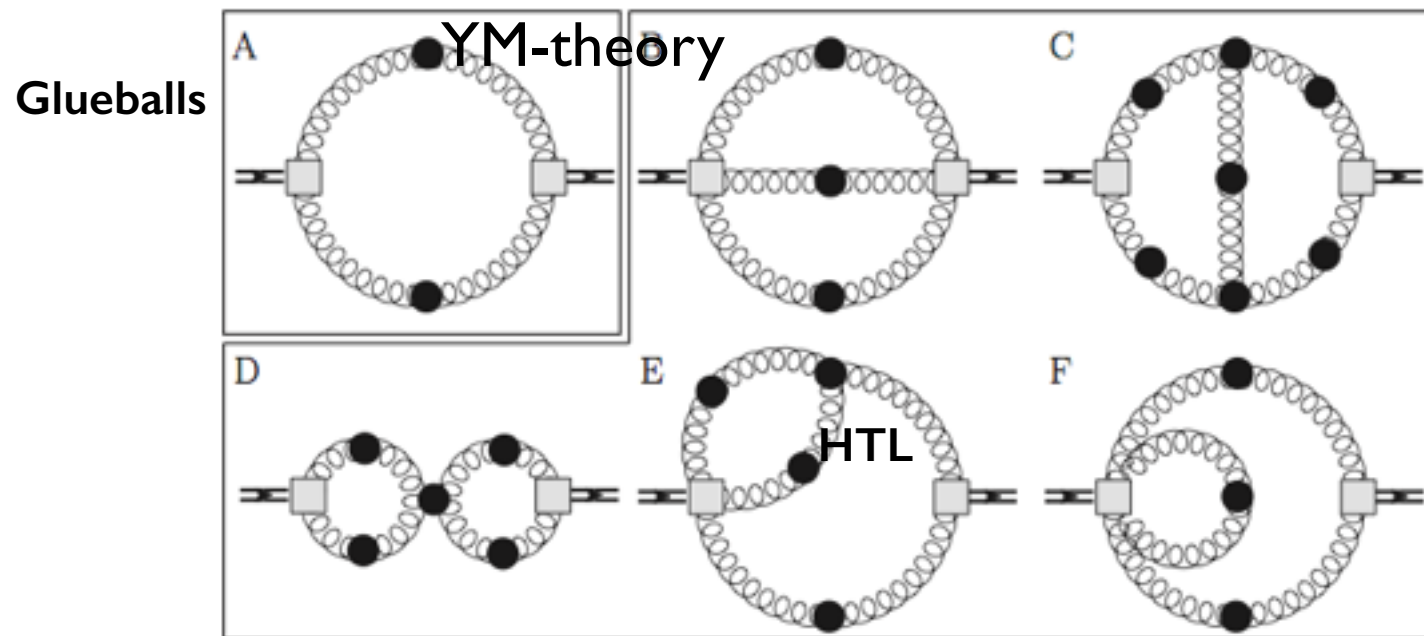
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## Results:

- Stable inhomogeneous regime

Nowakowski, Buballa, Carignano and Wambach, arXiv:1506.04260 [hep-ph] Buballa and Carignano, Prog. Part. Nucl. Phys. 81 (2015) 39

# Transport coefficients: $\eta/s$



## Functional method:

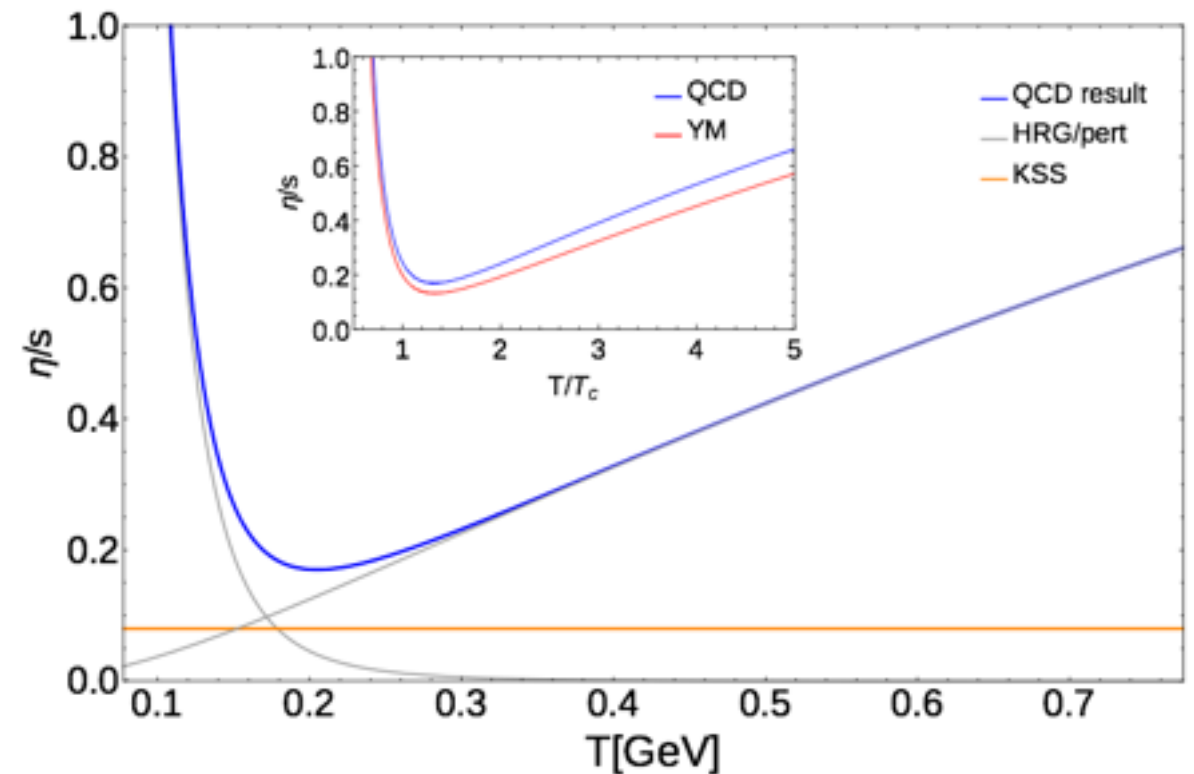
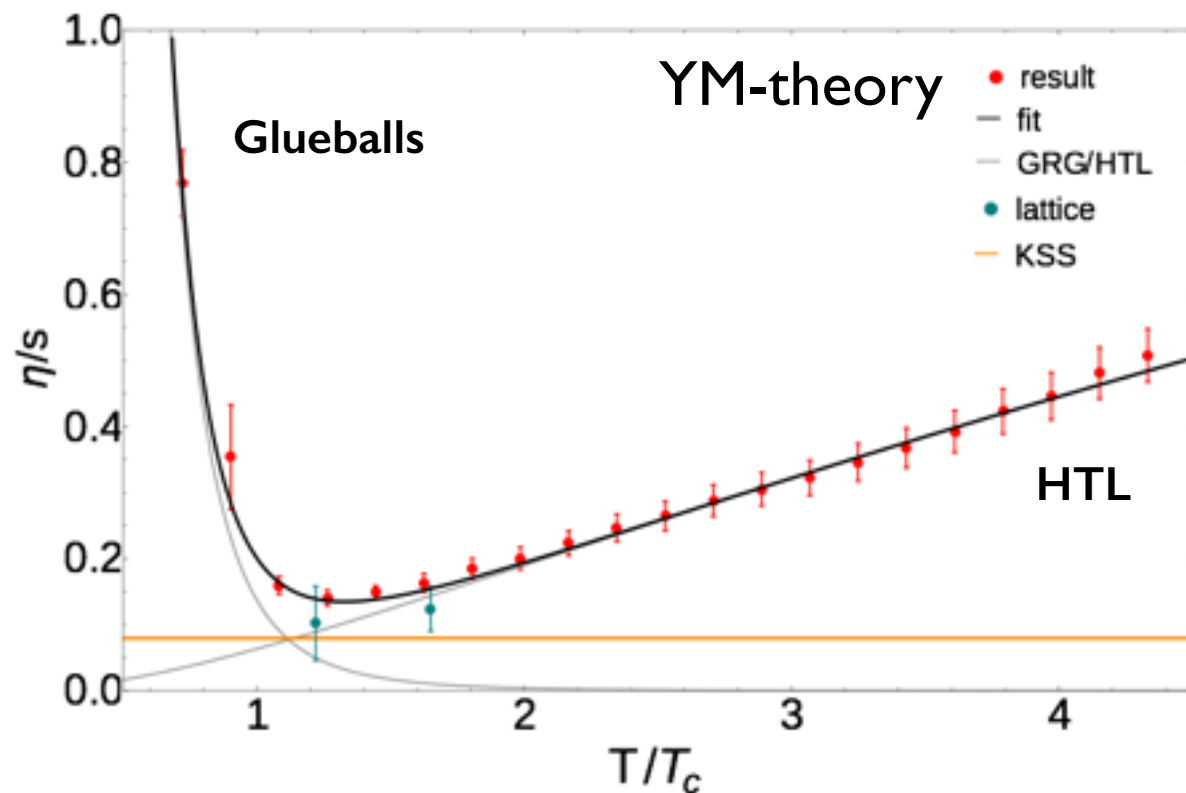
- Calc. gluon spectral function and running coupling
- Kubo formula to determine  $\eta/s$

## Results:

- Good agreement DSE vs lattice at pure YM
- First estimate for QCD using perturbative quark corrections

Christiansen, Haas, Pawłowski and Strodthoff, PRL 115 (2015) 11, 112002

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