

# Aktuelle Entwicklungen in der Theorie: Ab initio Beschreibung der Kerne

**Low-energy pion-nucleon dynamics**

**Chiral nuclear forces in the precision era**

**Nuclear lattice simulations: recent highlights**

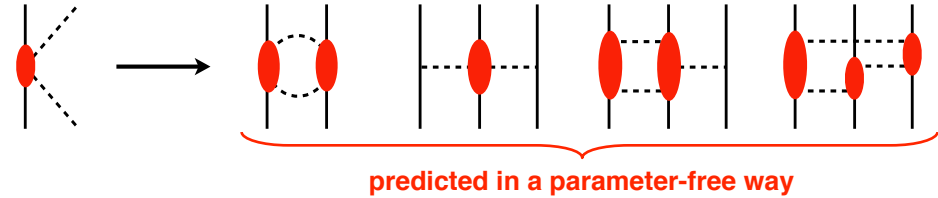
**Medium-mass nuclei and nuclear matter**

**Nuclear systems from lattice QCD**

**Summary**

# Low-energy pion-nucleon dynamics

Long-range nuclear forces are completely determined by the  $\chi$ -symmetry of QCD + experimental information on  $\pi N$  scattering



## Pion-nucleon Roy-Steiner equations

M. Hoferichter, J. Ruiz de Elvira, B. Kubis, U.-G. Meißner, PRL 115 (2015) 092301; arXiv:1510.06039 [hep-ph]

Integral equations in the form of dispersion relations which incorporate constraints from analyticity, unitarity & crossing symmetry

**Input:** S-,P-waves at high energy, inelasticities, D- and higher waves + scatt. lengths from hadronic atoms

**Output:** reliable results for S-,P-waves with systematic uncertainties; subthreshold coefficients, determination of the  $\sigma$ -term:

$$\sigma_{\pi N} = 59.1 \pm 3.5 \text{ MeV}$$

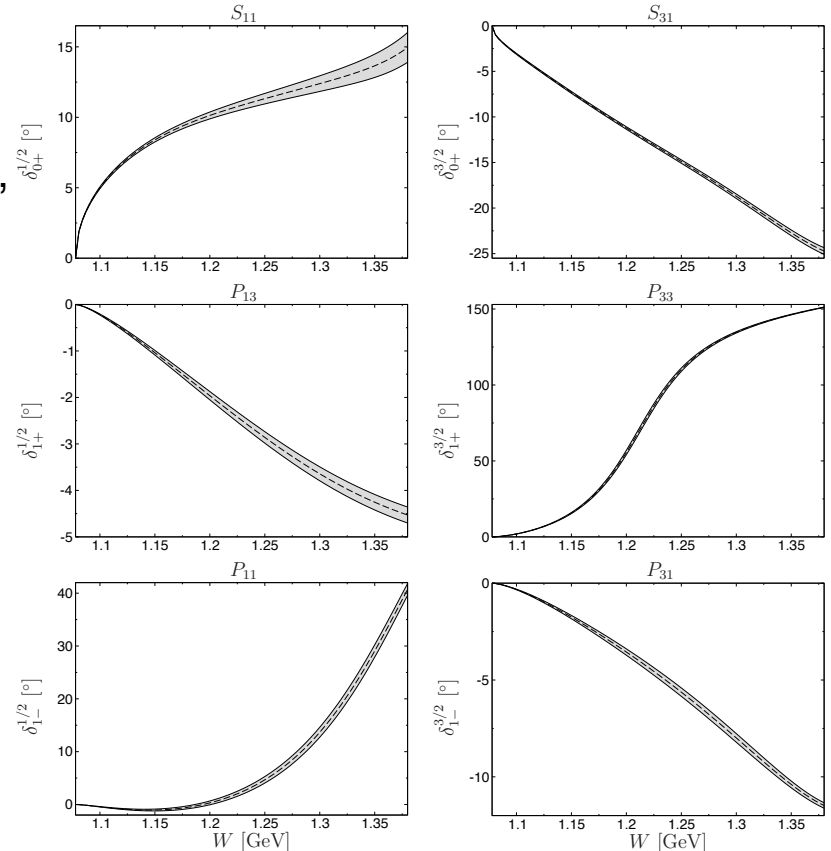
## ChPT for $\pi N$ , $\pi N \rightarrow \pi\pi N$ with/without $\Delta(1232)$

Siemens et al., PRC 89 (2014) 065211; to appear

## Baryon ChPT beyond the low-energy region

EE, J. Gegelia, U.-G. Meißner, D.-L. Yao, EPJ C75 (2015) 499

$\pi N$  phase shifts from the RS equations



# Chiral nuclear forces

	Two-nucleon force	Three-nucleon force	Four-nucleon force
LO ( $Q^0$ )			
NLO ( $Q^2$ )			
N <sup>2</sup> LO ( $Q^3$ )			
N <sup>3</sup> LO ( $Q^4$ )			
N <sup>4</sup> LO ( $Q^5$ )			

have been worked out

focus of intense research efforts...

Entem, Kaiser, Machleidt, Nosyk, PRC 91 (2015) 014002  
 EE, Krebs, Meißner, PRL 115 (2015) 122301

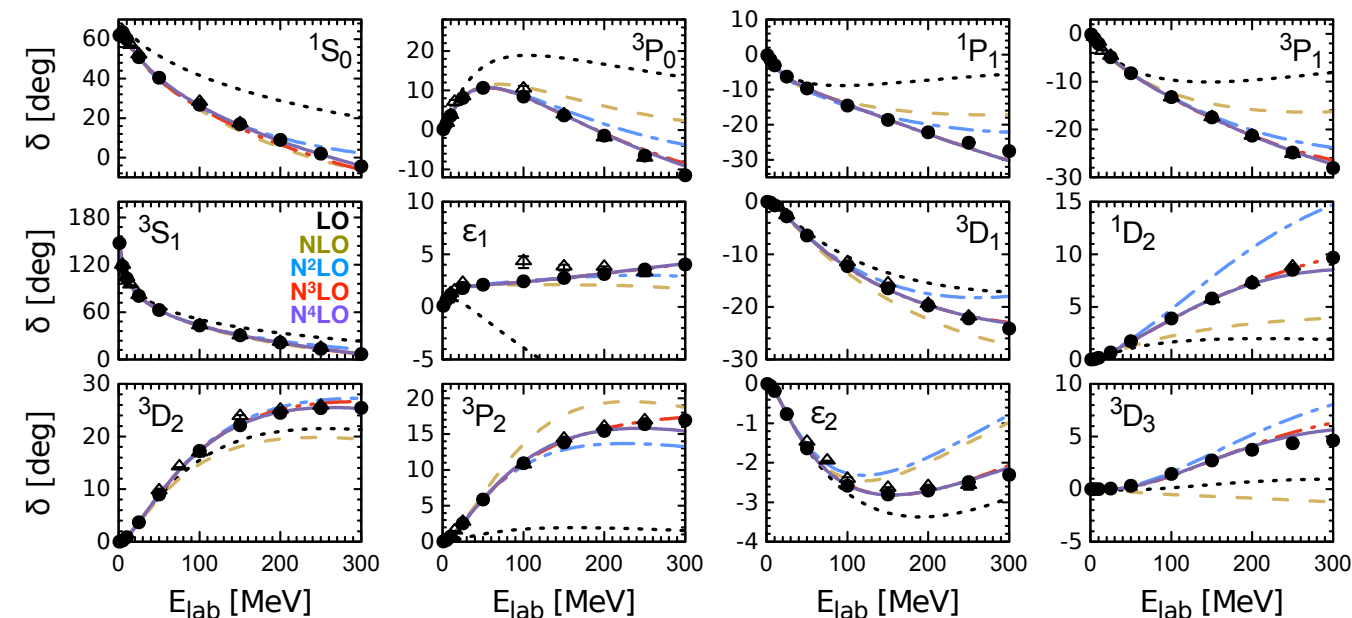
Why is it necessary/interesting to extend the  $\chi$ -expansion of the NN potential to  $Q^5$ ?

- no additional parameters (except for 1 IB term)  $\rightarrow$  testing the theory (long-range physics)
- there is evidence that  $\chi$ -expansion for the 3NF is not yet converged at  $Q^4$
- understanding fine details of the 3NF requires accurate and precise NN forces

# Chiral nuclear forces

## New state-of-the-art chiral NN potentials up to N<sup>4</sup>LO

EE, Krebs, Meißner, EPJA 51 (2015) 53; PRL 115 (2015) 122301



- improved UV regulator maintains the analytic structure of the amplitude
- all LECs in the long-range part are taken from  $\pi$ N scattering, no fine tuning!
- coupled with the novel approach for uncertainty quantification, provides **the tool for next-generation precision ab initio studies**

## Quality of the reproduction of the Nijmegen PWA („ $\chi^2_{\text{datum}}$ “)

$E_{\text{lab}}$ bin	LO [Q <sup>0</sup> ]	NLO [Q <sup>2</sup> ]	N <sup>2</sup> LO [Q <sup>3</sup> ]	N <sup>3</sup> LO [Q <sup>4</sup> ]	N <sup>4</sup> LO [Q <sup>5</sup> ]
neutron-proton phase shifts					
0–100	360	31	4.5	0.7	0.3
0–200	480	63	21	0.7	0.3
proton-proton phase shifts					
0–100	5750	102	15	0.8	0.3
0–200	9150	560	130	0.7	0.6
	2 LECs	+ 7 LECs + 2 IB LECs		+ 15 LECs	+ 1 IB LEC

# Uncertainty quantification

A simple algorithm for estimating uncertainty from the truncation of the chiral expansion:

EE, Krebs, Meißner, EPJA 51 (2015) 53

For any observable:  $X^{(i)}(p) = X^{(0)} + \underbrace{\Delta X^{(2)}}_{\sim Q^2 X^{(0)}} + \dots + \underbrace{\Delta X^{(i)}}_{\sim Q^i X^{(0)}}$  with  $Q = \max(p/\Lambda_b, M_\pi/\Lambda_b)$

*estimated from the error plots  $\Lambda_b \sim 600$  MeV*

Use the explicitly calculated  $\Delta X^{(i)}$  to estimate the uncertainty  $\delta X^{(i)}$  at order  $Q^i$ :

$$\delta X^{(0)} = Q^2 |X^{(0)}|,$$

$$\delta X^{(i)} = \max_{2 \leq j \leq i} (Q^{i+1} |X^{(0)}|, Q^{i+1-j} |\Delta X^{(j)}|)$$

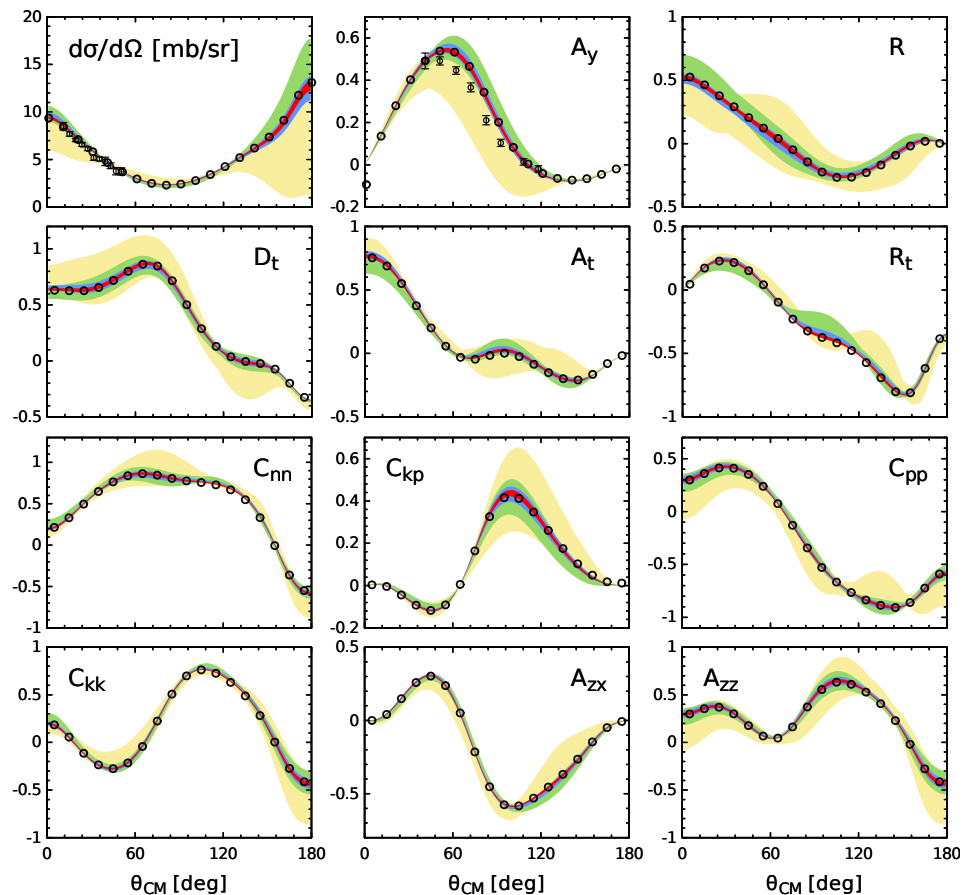
subject to the additional constraint

$$\delta X^{(i)} \geq \max_{j,k} (|X^{(j \geq i)} - X^{(k \geq i)}|).$$

- no reliance on the cutoff variation (not reliable)
- easily applicable to any observable (scattering, bound states, 3N, ...)
- error bars found to be consistent with 68% degree-of-belief intervals

Furnstahl et al., PRC 92 (2015) 024005

proton-neutron scattering observables at  $E_{\text{lab}}=143$  MeV



# 3N force studies

With these tools, we are well equipped to tackle the 3N force problem.

Is there any clear evidence for missing 3N forces effects? **Yes!** Binder et al., arXiv: 1505.07218 [nucl-th]

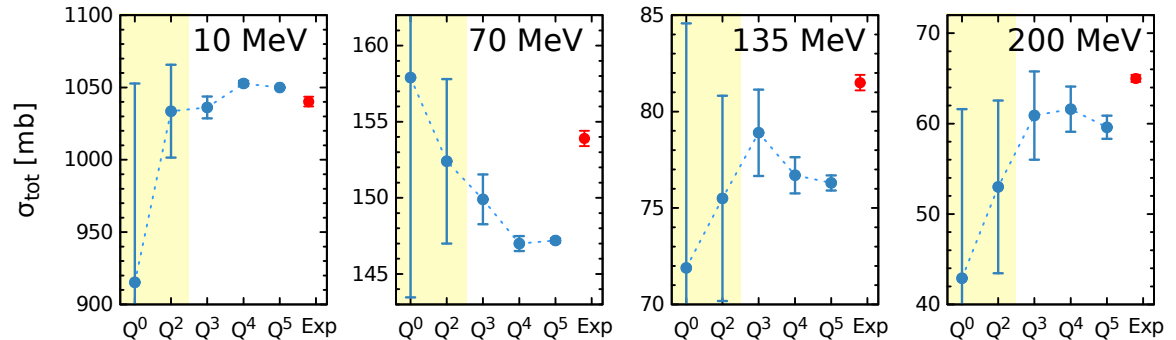
- Discrepancies between theory and data well outside the range of quantified uncertainties

→ unambiguous evidence for missing 3NF effects!

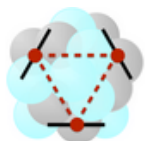
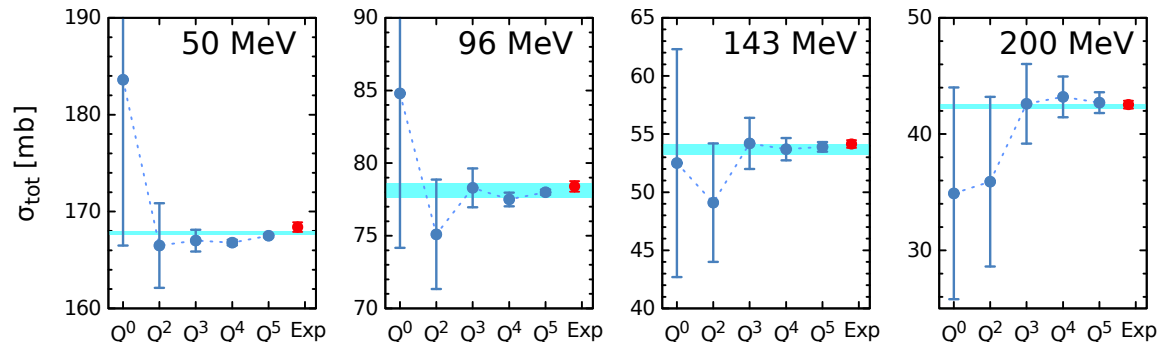
- The magnitude of the required 3NF contributions matches well the estimated size of  $N^2LO$  terms

→ consistent with the chiral power counting!

total cross section in nD scattering calculated without 3NF



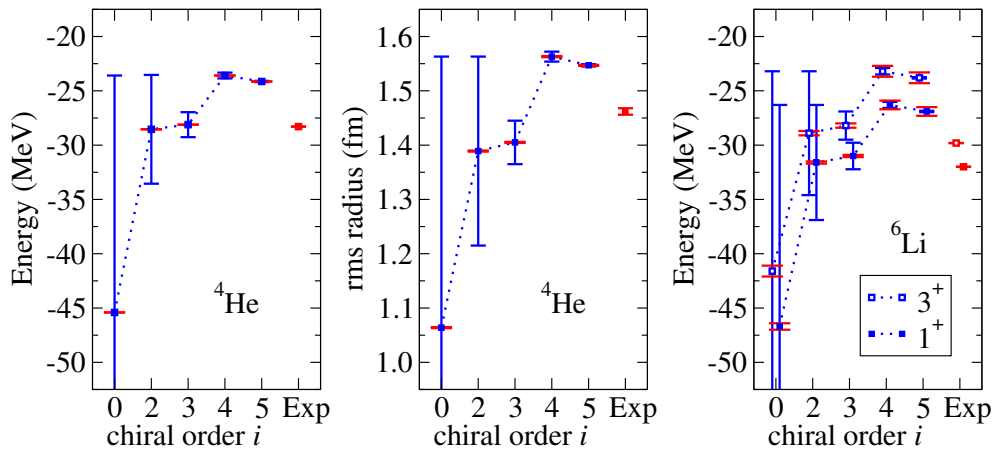
total cross section in np scattering



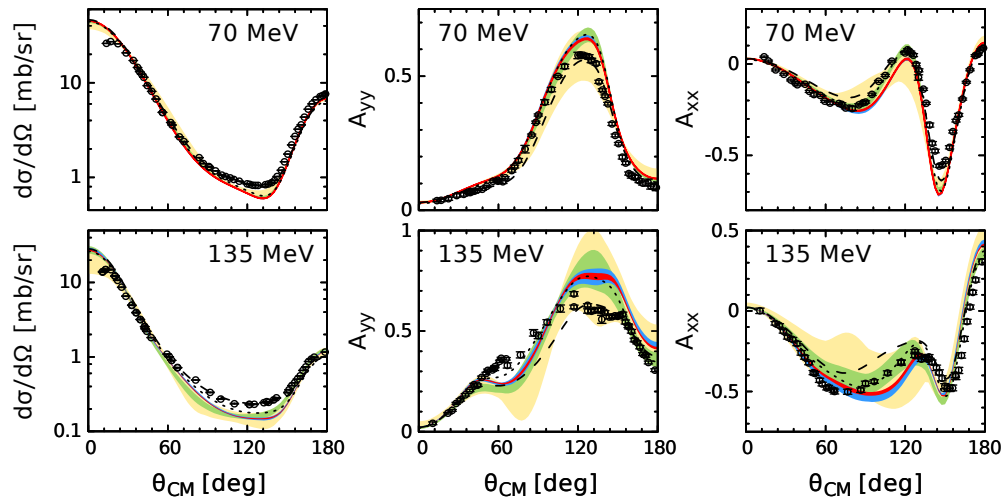
LENPIC: Low Energy Nuclear Physics International Collaboration



# 3N force studies



Similar pattern is observed for the properties of the light nuclei



Elastic  $nd$  scattering at intermediate energies:

The golden window to probe the (spin structure) of the 3NF



Next step: inclusion of the 3NF (LENPIC, work in progress)



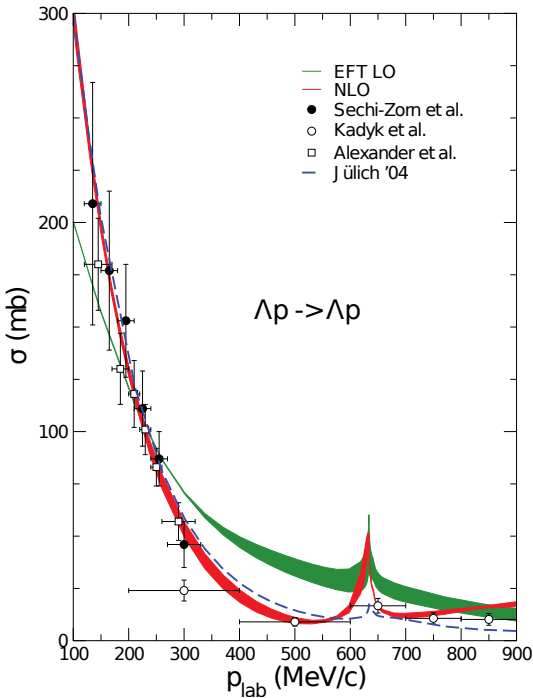
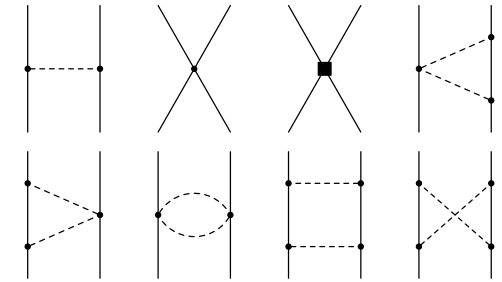
LENPIC: Low Energy Nuclear Physics International Collaboration



# Baryonic forces from SU(3) chiral effective field theory

J. Haidenbauer (FZJ), N. Kaiser (TUM), U.-G. Meißner (Bonn), S. Petschauer (TUM), W. Weise (ECT\*)

- ▶ extend successful SU(2)  $\chi$ EFT approach to nuclear forces to three flavors
- ▶ hyperon-nucleon interaction from SU(3)  $\chi$ EFT at NLO (one- and two-meson exchange + contact terms)

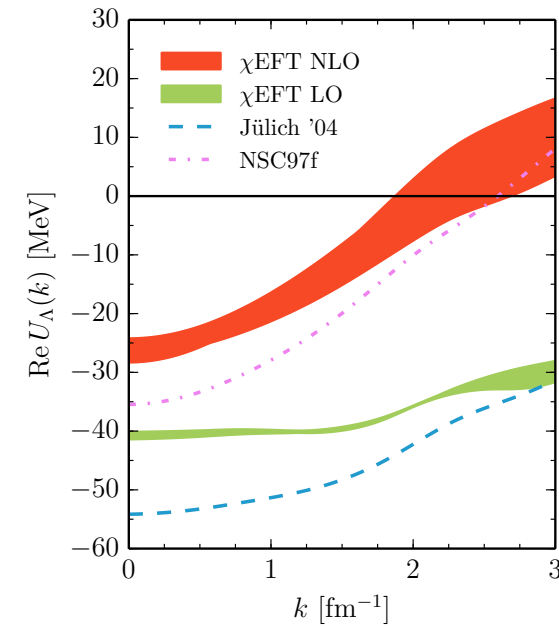


- ▶ good description of available  $YN$  scattering data

[Nucl.Phys. A915 (2013) 24-58]

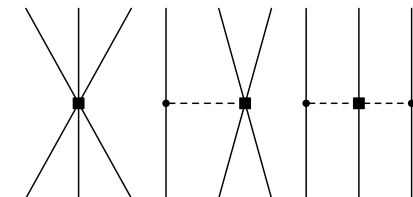
- ▶ G-matrix calculation of hyperon potentials in isospin-(a)symmetric nuclear matter
- weak  $\Lambda$ -nuclear spin-orbit
- repulsive  $\Sigma$ -nuclear potential

[arXiv:1507.08808]



- ▶ construction of leading three-baryon forces (e.g.  $\Lambda NN$ ) [arXiv:1511.02095]

- ▶ constants estimated via decuplet saturation (e.g.  $\Sigma^*$  for  $\Lambda NN$ )





# Nuclear systems from lattice $\chi$ EFT

## Nuclear lattice simulations:

A new ab initio approach to nuclei and nuclear reactions

D. Lee, EE, H. Krebs, T. Lähde, T. Luu, U.-G. Meißner, G. Rupak, ...

## Some recent highlights:

Ab initio calculation of the Hoyle state

EE, H. Krebs, D. Lee, U.-G. Meißner, PRL 106 (11) 192501; EE, H. Krebs, T.A.Lähde, D. Lee, U.-G. Meißner, PRL 109 (12) 252501

Viability of Carbon-based life as a function of light quark masses

EE, H. Krebs, T. A. Lähde, D. Lee, U.-G. Meißner, PRL 110 (13) 112502; EPJA 49 (13) 82

Ab initio calculation of the spectrum and structure of  $^{16}\text{O}$

EE, H. Krebs, T. A. Lähde, D. Lee, U.-G. Meißner, G. Rupak, PRL 112 (14) 102501

Lattice EFT for medium-mass nuclei („triangulation“ method for Euclidean-time extrapol.)

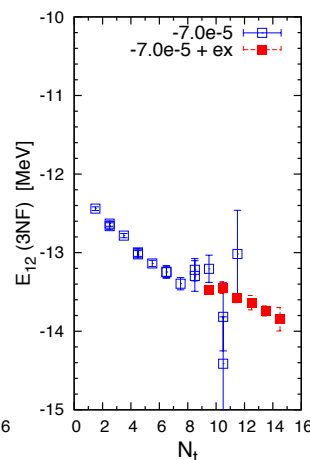
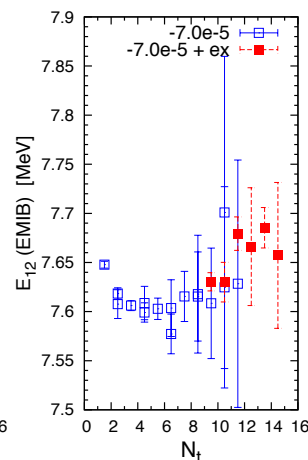
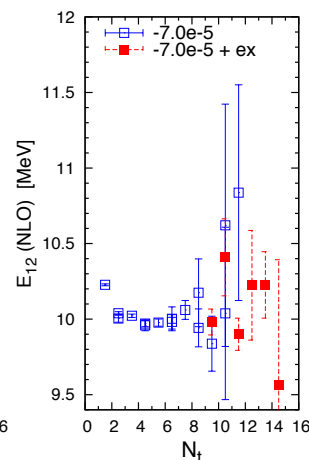
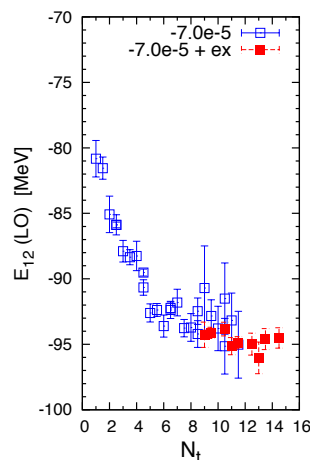
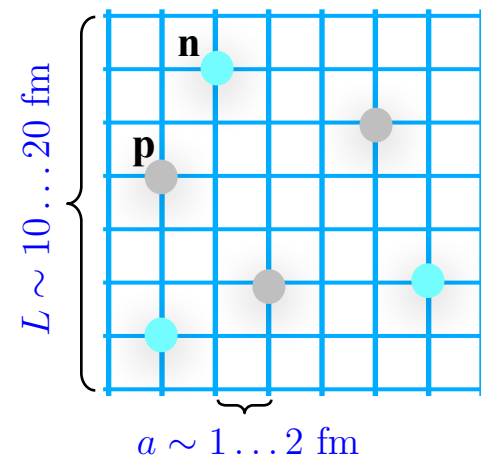
T. A. Lähde, EE, H. Krebs, D. Lee, U.-G. Meißner, G. Rupak, PLB 732 (14) 110

$E_{8\text{Be, old}} = -55(2) \text{ MeV}$

$E_{8\text{Be, new}} = -56.4(2) \text{ MeV}$

Symmetry-sign extrapol.

T.A. Lähde, T. Luu, D. Lee, U.-G. Meißner, EE, H. Krebs, G. Rupak, EPJ A51 (15) 92



# Nuclear systems from lattice $\chi$ EFT

nature

International weekly journal of science

## Ab initio alpha-alpha scattering

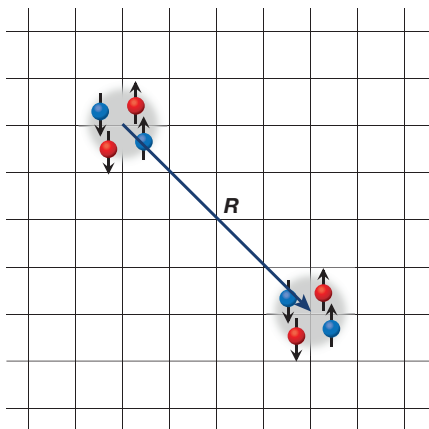
Serdar Elhatisari<sup>1</sup>, Dean Lee<sup>2</sup>, Gautam Rupak<sup>3</sup>, Evgeny Epelbaum<sup>4</sup>, Hermann Krebs<sup>4</sup>, Timo A. Lähde<sup>5</sup>, Thomas Luu<sup>1,5</sup> & Ulf-G. Meißner<sup>1,5,6</sup>

Nature 528, 111–114 (03 December 2015) | doi:10.1038/nature16067

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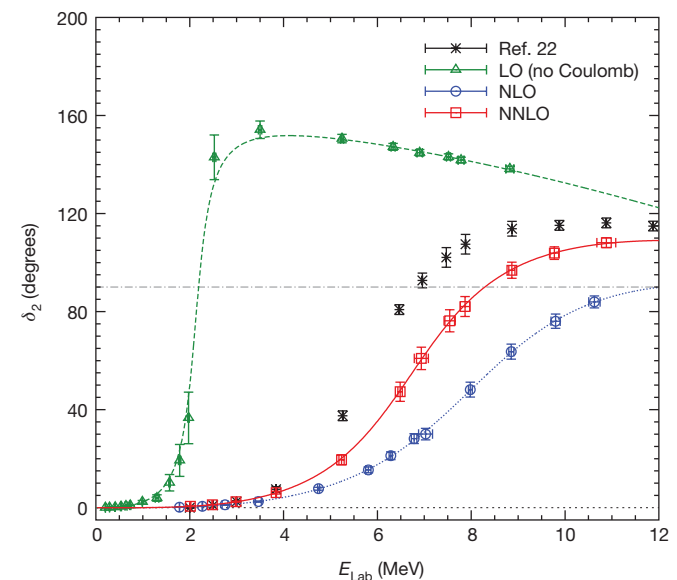
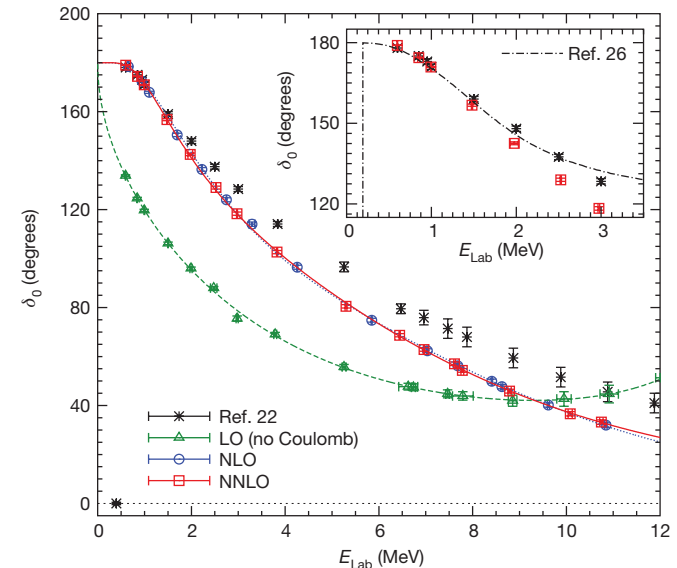
First ab initio calculation of alpha-alpha scattering!

Used lattice EFT to extract the effective Hamiltonian for two interacting  $\alpha$ -clusters  
(adiabatic projection method [A. Rokash et al., PRC 92 (15) 054612])



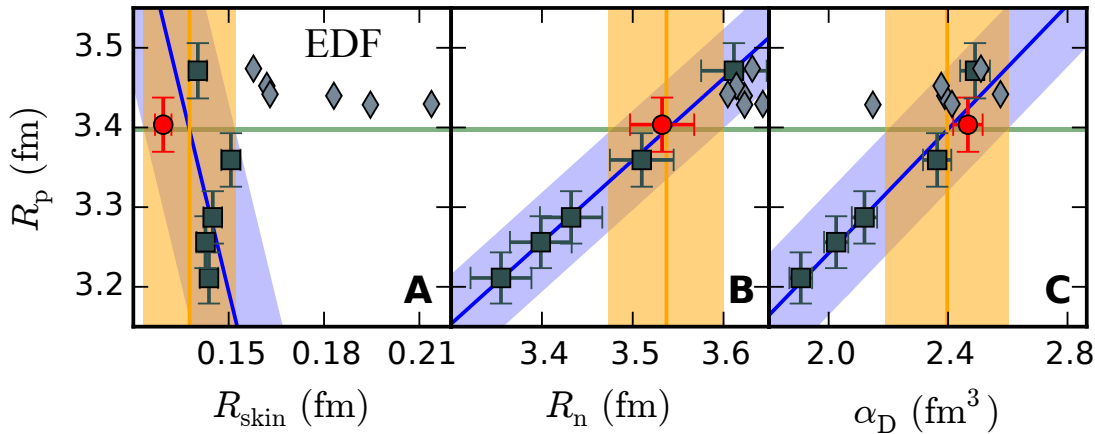
Phase shifts obtained employing a hard spherical wall boundary at asymptotically large distances

Promising scaling with respect to the number of particles as  $\sim (A_1 + A_2)^2$



# Frontier of ab initio calculations from Achim Schwenk, TU Darmstadt

- First NN+3N prediction of the **neutron skin**, **weak form factor**, **dipole polarizability** of  $^{48}\text{Ca}$



## Neutron and weak-charge distributions of the $^{48}\text{Ca}$ nucleus

G. Hagen<sup>1,2\*</sup>, A. Ekström<sup>1,2</sup>, C. Forssén<sup>1,2,3</sup>, G. R. Jansen<sup>1,2</sup>, W. Nazarewicz<sup>1,4,5</sup>, T. Papenbrock<sup>1,2</sup>, K. A. Wendt<sup>1,2</sup>, S. Bacca<sup>6,7</sup>, N. Barnea<sup>8</sup>, B. Carlsson<sup>3</sup>, C. Drischler<sup>9,10</sup>, K. Hebeler<sup>9,10</sup>, M. Hjorth-Jensen<sup>4,11</sup>, M. Miorelli<sup>6,12</sup>, G. Orlandini<sup>13,14</sup>, A. Schwenk<sup>9,10</sup> and J. Simonis<sup>9,10</sup>



Neutron skin smaller than previously thought! Hagen et al., Nature Phys.

- **In-Medium Similarity Renormalization Group**

First nonperturbative derivation of shell-model interactions from NN+3N interactions

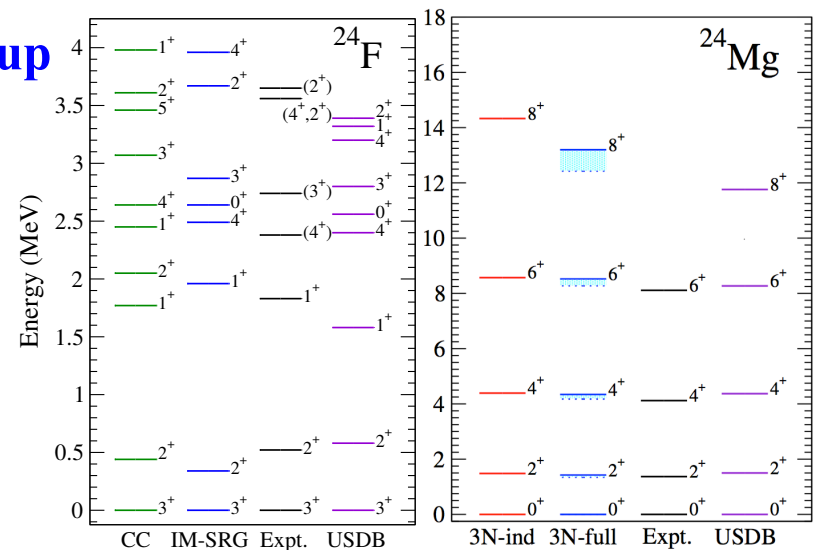
Bogner et al., PRL 113, 142501 (2014)

First ab initio description of deformed nuclei

Stroberg et al., 1511.02802

- **Quantum Monte Carlo** with local chiral 3N

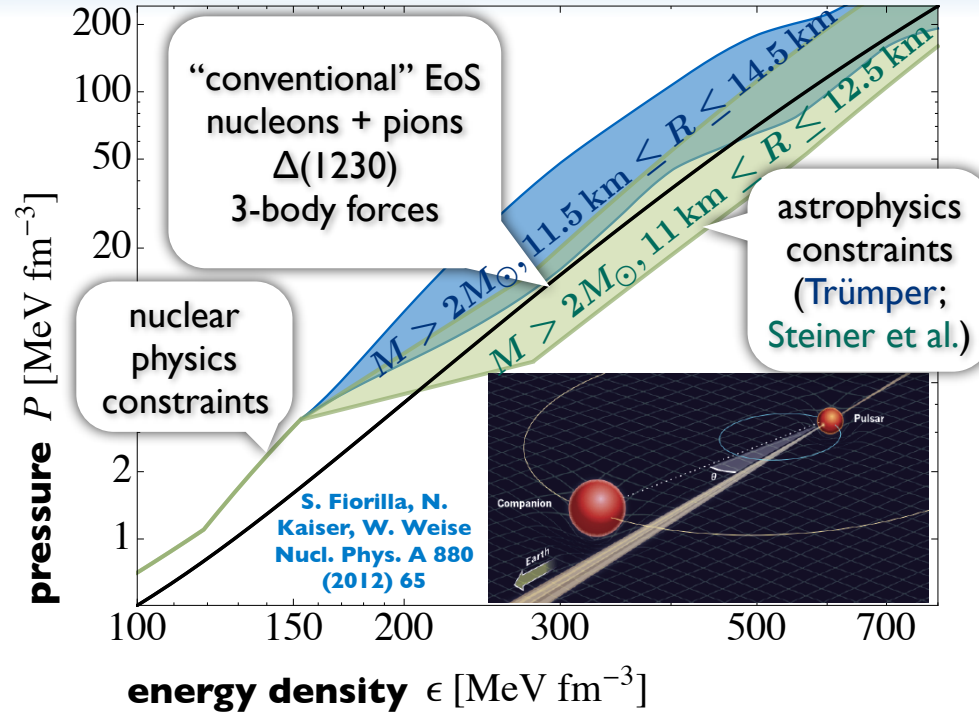
Lynn, Tews et al., 1507.05561, 1509.0347



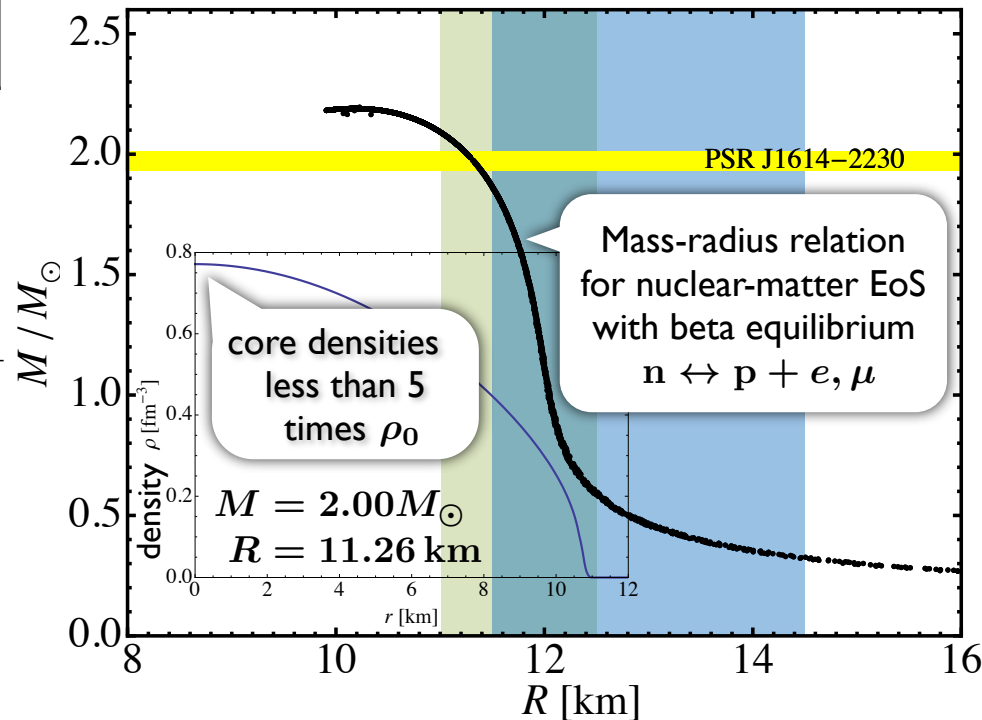
# Neutron-Star Matter

from Norbert Kaiser, TUM

T. Hell, N. Kaiser, B. Röttgers, S. Schulteß, W. Weise  
PRC 90 (2014) 045801



- Very precise measurement of a neutron star (PSR J1614-2230) P.B. Demorest et al.,  
Nature, 467, 1081 (2010)  
 $M = (1.97 \pm 0.04) M_{\odot}$
- Sets new constraints on the equation of state (EoS) of nuclear matter
- Inclusion of neutron star constraints plus **Chiral Effective Field Theory** at lower density



- Mass-radius relation R.C. Tolman (1939)  
J.R. Oppenheimer, G.M. Volkoff (1939)

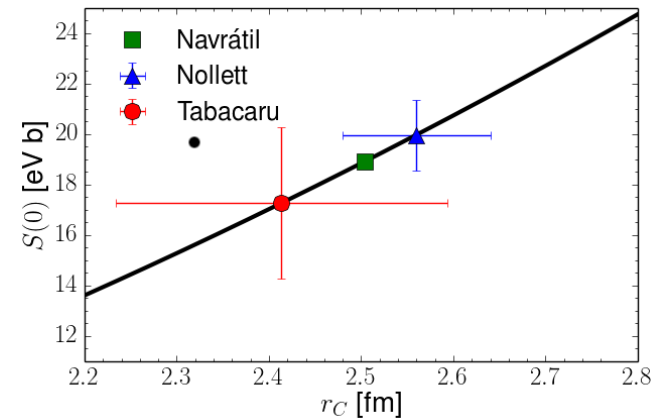
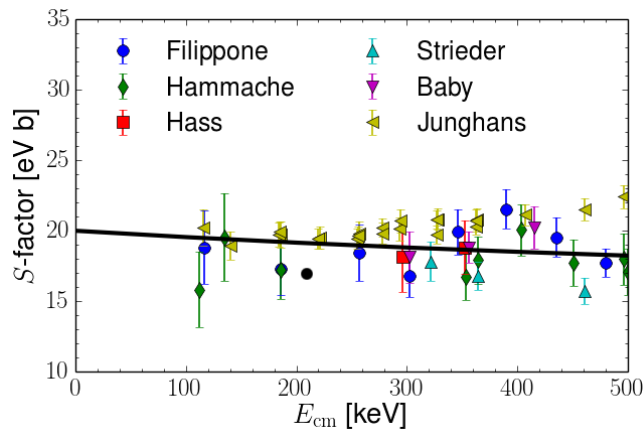
$$\frac{dP(r)}{dr} = -\frac{\mathcal{G} [\epsilon(r) + P(r)] [M(r) + 4\pi r^3 P(r)/c^2]}{c^2 r [r - 2\mathcal{G}M(r)/c^2]}$$

- ▶ Conventional (baryonic and mesonic) degrees of freedom are sufficient to describe massive neutron stars
- ▶ no “exotic” matter needed (or excluded)

# EFT for Proton Halos

from Hans-Werner Hammer, TU Darmstadt

- Delicate interplay between strong and Coulomb interaction
  - ⇒ two fine tunings required to obtain shallow halo states
  - ⇒ proton halos are rarer in nature than neutron halos
- Range corrections in proton halos  
Ryberg, Forssen, Hammer, Platter, arXiv:1507.08675
- Explore universal correlations between observables
- S-factor for  ${}^7\text{Be}(p, \gamma){}^8\text{B}$  and charge radius of  ${}^8\text{B}$  are correlated



Ryberg, Forssen, Hammer, Platter, Eur. Phys. J. A **50** (2014) 170

# Nuclear physics from lattice QCD

- Lattice QCD results for light nuclei start to emerge (at high  $M_\pi$ )
- Controversial results: more binding [NPLQCD, Yamazaki et al.] versus no binding at all [HAL QCD]

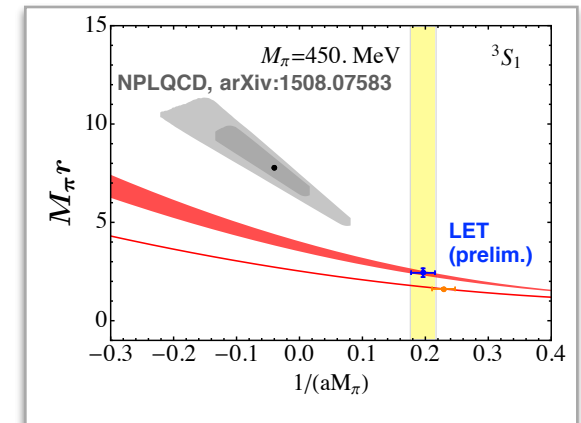
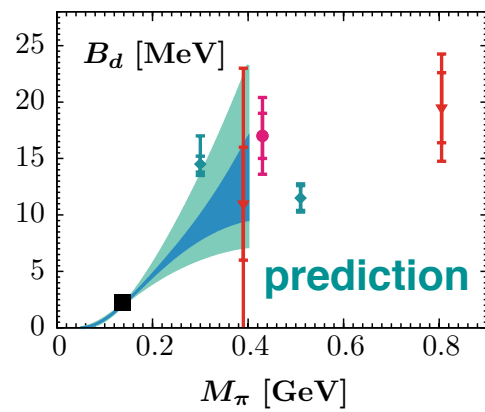
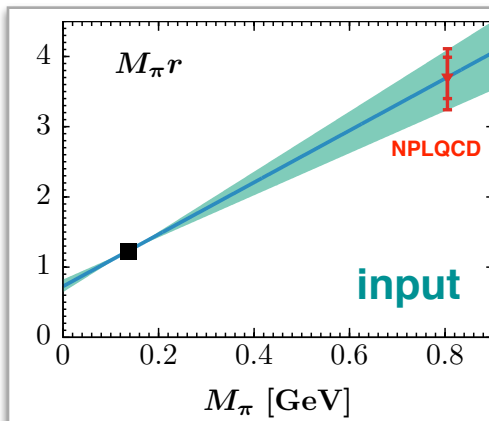
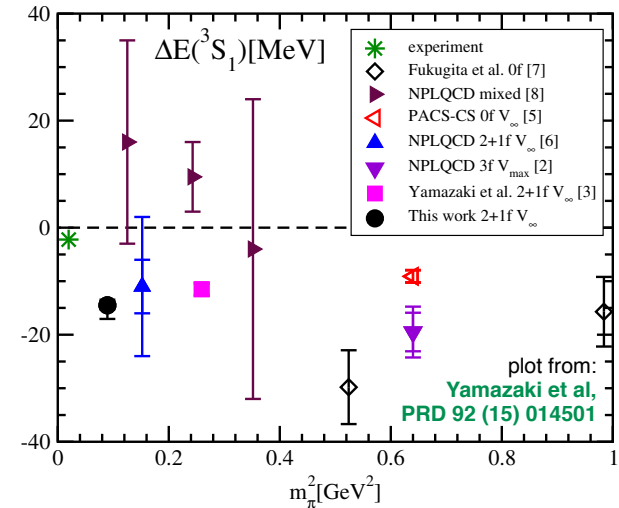
→ consistency checks are needed!

- $\pi$ -less EFT & extrapolations in the # of nucl. [Barnea et al.'15]
- **Low-energy theorems:** long-range interactions imply correlations between coefficients in the effective range expansion

- model-independent; no reliance on the  $\chi$ -expansion
  - good predictive power in  ${}^3S_1$  for physical  $M_\pi$
  - can be extended to heavier  $M_\pi$
- [Baru et al., PRC99 (15) 014001]



	$a$ [fm]	$r$ [fm]	$v_2$ [fm <sup>3</sup> ]	$v_3$ [fm <sup>5</sup> ]	$v_4$ [fm <sup>7</sup> ]
LO LET	input	1.60	-0.05	0.82	-5.0
NLO LET	input	input	0.06	0.70	-4.0
Nijmegen PWA	5.42	1.75	0.04	0.67	-4.0



# Summary

**New generation of accurate and precise chiral nuclear forces**

**+ Reliable approach to uncertainty quantifications**

**+ Exciting progress in ab initio methods**

**(Nuclear lattice simulations, Coupled cluster, In-Medium SRG, Green Function Monte Carlo, ...)**

**+ Growing computational resources**

**Low energy nuclear theory is entering precision era:**

**Reliable ab initio few- and many-body calculations based on chiral EFT with quantified theoretical uncertainties.**