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COMPRESSED BARYONIC MATTER

Hadrons in dense and hot matter and Chiral Symmetry Restoration

- High baryonic density matter
 - From the high density side : color superconducting phase (di-quark condensation)
From the low density side : nucleonic (baryonic) matter (three-quark clustering), role of chiral symmetry (restoration) and color confinement implemented in effective theories
- In medium hadronic spectral functions
 - The rho meson and the axial-vector mixing : dilepton production
Fluctuations of the quark condensate : in-medium scalar-isoscalar modes

I. HADRONS IN MEDIUM

Observable consequences of in-medium chiral dynamics

- Order parameter at finite ρ_B, T
 - Dropping of the quark condensate

$$R = \frac{\langle\langle\bar{q}q\rangle\rangle(\rho_B, T)}{\langle\bar{q}q\rangle_{vac}} = 1 - \sum_h \frac{\rho_h \Sigma_h}{f_\pi^2 m_\pi^2} + \textit{higherorder}$$

In-medium hadronic spectral functions

- Evolution of the “centroids” (masses)

No universal link between condensate and observable evolutions (masses, f_π , etc...)

- Shape of the hadronic spectral functions

Softening/sharpening (σ) or broadening (K, ρ)

Relation with χ SR?

Simultaneous study of “chiral partners”

Vector (ρ) $\longleftrightarrow$ Axial (a_1)

$$\mathcal{V}_k^\mu = \bar{q} \gamma^\mu \frac{\tau_k}{2} q, \quad \longleftrightarrow \quad \mathcal{A}_k^\mu = \bar{q} \gamma^\mu \gamma_5 \frac{\tau_k}{2} q$$

II. *DILEPTON PRODUCTION*

- Dilepton production rate from hot and dense matter

$$\frac{dN_{l\bar{l}}}{d^4x d^4q} = -\frac{\alpha^2}{6\pi^3 M^2} \frac{1}{e^{\beta q^0} - 1} g_{\mu\nu} \left(\frac{1}{\pi} \textcolor{red}{Im} \Pi_V^{\mu\nu} \right)$$

Current-current correlator in the vector channel

$$\Pi_V^{\mu\nu}(q) = -i \int d^4x e^{iqx} \langle \langle \mathcal{V}^\mu(x), \mathcal{V}^\nu(0) \rangle \rangle (T, \rho_B)$$

Broadening and flatening of the rho meson spectral function

Lowering of the quark-hadron duality threshold $\iff$ radiation from a chiral symmetry restored phase

- Theoretical ideas and approaches

Density expansion, many-body approaches, transport codes,

QCD sum rules, Weinberg sum rules, ..

Dropping masses vs chiral partner mixing



II. *DILEPTON PRODUCTION*

- Many-body approaches

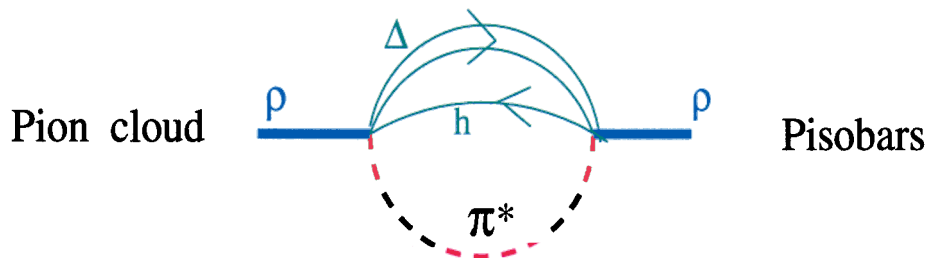
Effective hadronic theories : VDM + χ S + phenomenology (πN , ρN , photoabsorption, decay rates,...)

Coupling of the ρ to many-body excitations

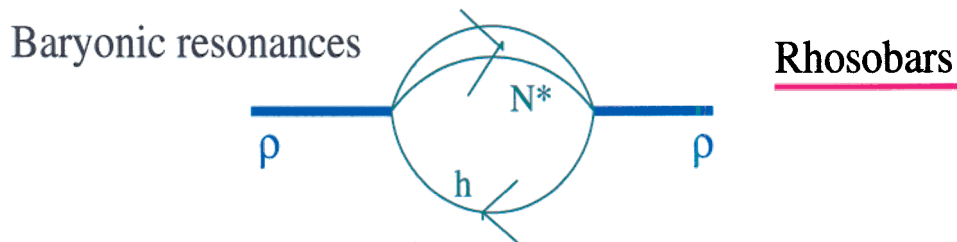
- TEMPERATURE EFFECTS : meson gas (Rapp-Gale)

$$\pi \rho \longleftrightarrow \omega a_1 \quad \text{Ch.SR}$$

- BARYONIC EFFECTS (Rapp-Wambach, GC et al, Friman et al, Peters et al)

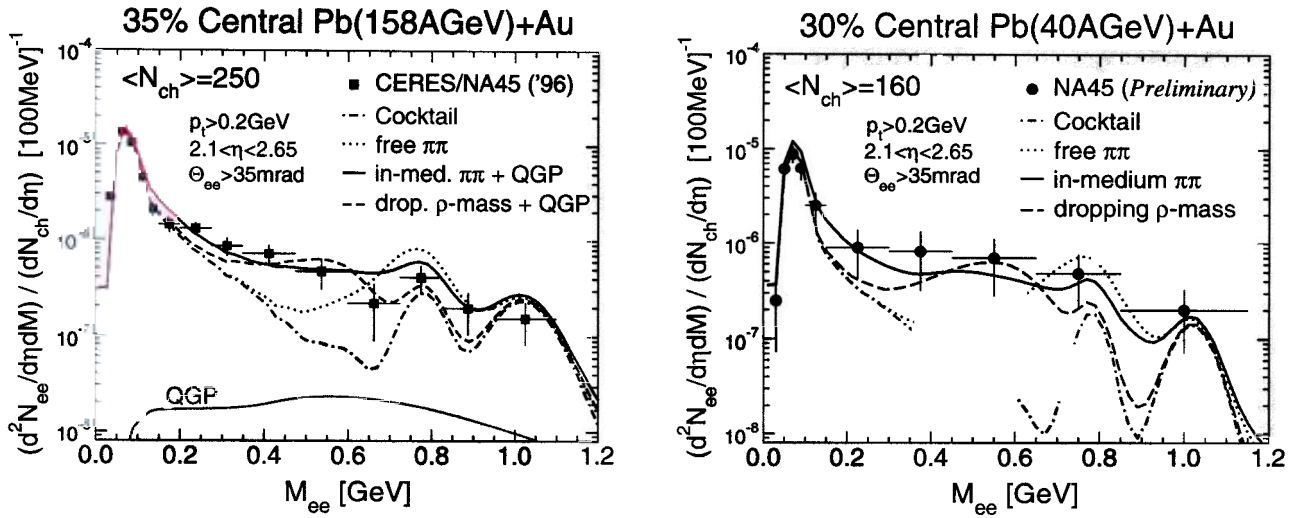


Vector (rho) - Axial baryonic current Ch. SR



Dominant S wave ($q=0$) $N_{13}^*(1520)$: Strong medium effect

II. DILEPTON PRODUCTION



- Brodening and flatening dominated by baryonic effects
- Stronger effect at lower SPS energy *i.e.* higher baryonic density
- (Partial) Connection with (partial) chiral symmetry restoration : mixing of vector and axial correlators : Linked to the pionic part of the in-medium chiral condensate
- What is the chiral status of the $N^*(1520)$? Linked to a nucleon structure problem

III. SCALAR ISOSCALAR MODES

- High baryonic density matter

One central question : in-medium behaviour of scalar-isoscalar modes ?

- Order parameter $\mathcal{M}^{ij} = \psi_R^j \psi_L^i$

$$\langle \mathcal{M}^{ij} \rangle \neq 0 \quad \mathcal{M} \rightarrow V_L \mathcal{M} V_R^\dagger$$

$$\mathcal{M} = \left(\frac{\bar{\psi} \psi}{2} \right) + i \vec{\tau} \cdot \left(i \bar{\psi} \gamma_5 \frac{\vec{\tau}}{2} \psi \right) \quad \sigma + i \vec{\tau} \cdot \vec{\pi}$$

- σ meson : amplitude fluctuation of the condensate
- pion : phase fluctuation of the condensate

But $\sigma \rightarrow \pi\pi$ Large σ width

- In-medium “ σ meson”
 - Chiral symmetry restoration : softening (hardening) of the spectral function (dropping of the sigma mass and chiral condensate)
 - Coupling of the sigma to in-medium $\pi\pi$: softening
 - Role of the nucleonic polarization or confinement ?

III. SCALAR ISOSCALAR MODES

Chiral effective theory

NJL type : $M \sim -2G \langle \bar{q}q \rangle(\rho, T)$

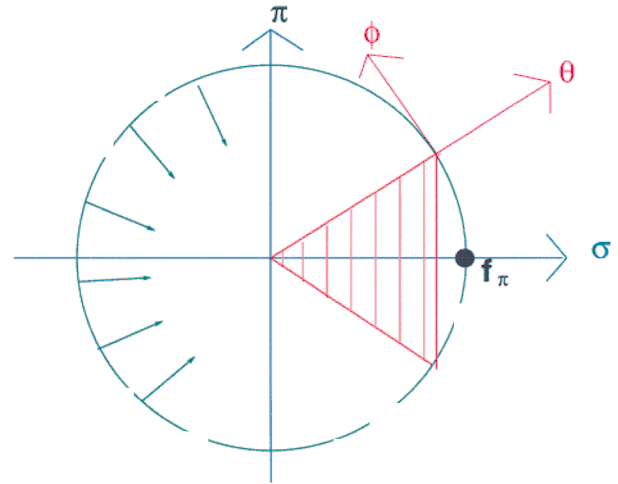
Hadronic theories : $\langle \sigma \rangle \sim \langle \bar{q}q \rangle(\rho, T)$

Alternative : $\sigma + i \tau \cdot \vec{\pi} = \Theta U \quad (\theta + f_\pi) e^{i \tau \cdot \vec{\phi}_\pi}$

- $\vec{\phi}$ New pion field : orthoradial soft mode
- • θ is chiral invariant : fluctuation of the chiral radius to be identified with the “sigma meson” of the Walecka model

$$R = 1 - \frac{\langle \phi_\pi^2 \rangle(\rho)}{2 f_\pi^2} \quad \frac{|\langle \theta \rangle|(\rho)}{f_\pi}$$

- Pionic fluctuation : $\langle \phi_\pi^2 \rangle$
- Shrinking of the chiral radius : $\langle \Theta \rangle$ decreases



Manifestations of χS Restoration

- Pionic fluctuations $\iff$ Axial-vector mixing
- Scalar field (Θ) $\iff$ Dropping of the masses

III. SCALAR ISOSCALAR MODES

In-medium spectral function or $T_{\pi\pi}^{I=J=0}$

- In-medium $\sigma\pi\pi$

Coupling of the sigma (with vacuum mass and couplings) to dressed pions

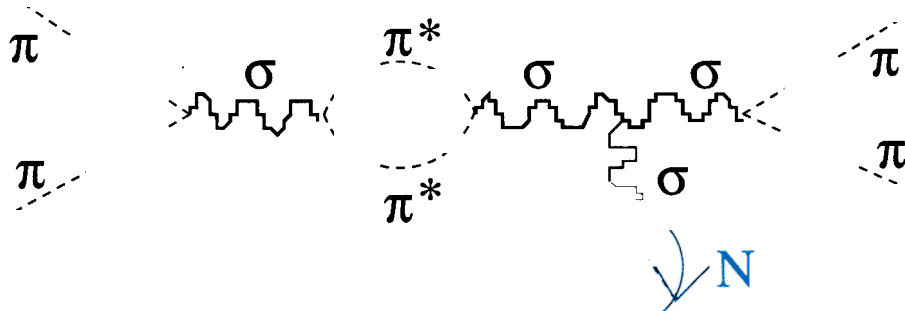
σ pole in the complex plan moves at lower energies with a reduced width (Oset et al) $\rightarrow$ Shift of the the invariant mass spectrum in $A(\gamma, \pi^0\pi^0)$ observed by the TAPS collaboration

- Chiral symmetry restoration

Softening (and sharpening) of a collective scalar-isoscalar mode *i.e.* the particle representing the amplitude fluctuation of the order parameter around the minimum of the effective potential

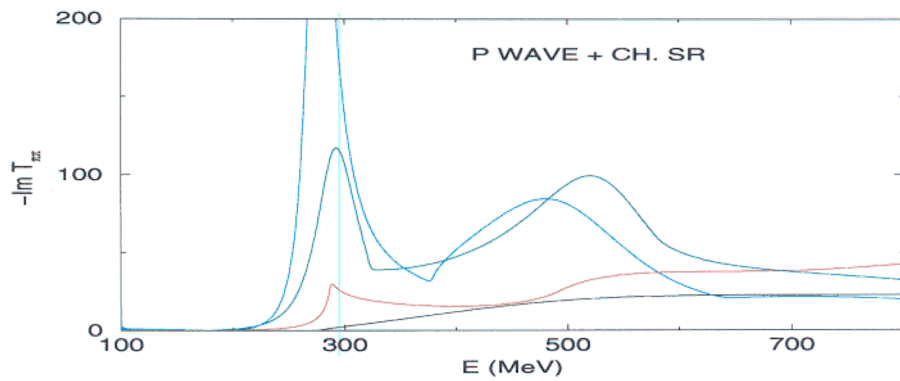
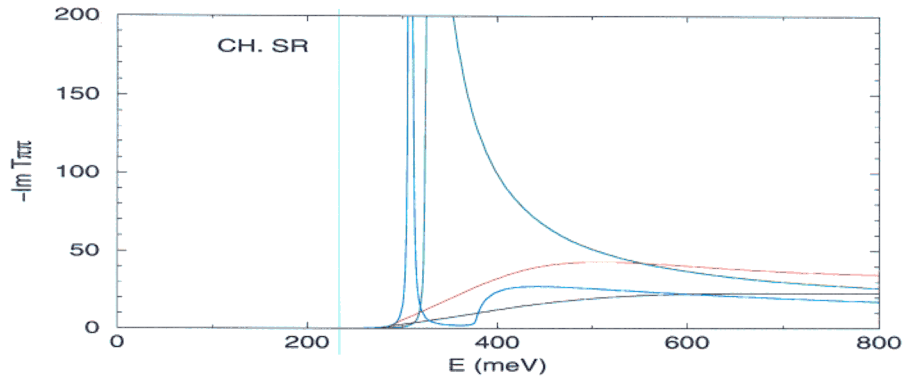
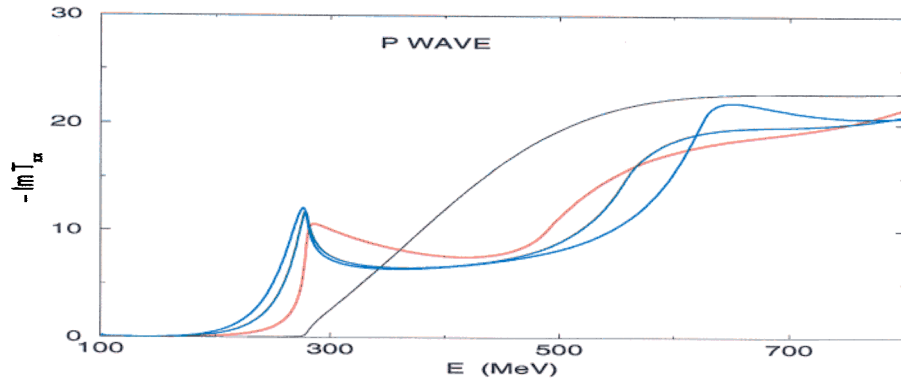
Precursor effect of χ SR : Sharp structure near the 2π threshold in σ and $\pi\pi$ strength function at ρ_d such that :

$$m_\sigma = 2 m_\pi \text{ (Hatsuda et al)}$$



III. SCALAR ISOSCALAR MODES

- Model calculation : In-medium $T_{\pi\pi}$ (Linear sigma model (NJL), $\pi\pi$ phase shifts)



III. SCALAR ISOSCALAR MODES

Four-quark condensate

$$\langle 0 | (\bar{q}q)^2 | 0 \rangle = \langle 0 | \bar{q}q | 0 \rangle \langle 0 | \bar{q}q | 0 \rangle + \sum_n \langle 0 | \bar{q}q | n \rangle \langle n | (\bar{q}q) | 0 \rangle$$

$|n\rangle$ 2π scalar-isoscalar modes i.e. σ meson

• Model calculation

Effective linear sigma model with in-medium modified couplings (m_σ , f_π , m_π) from chiral symmetry restoration (NJL)

Unitarization : $\pi\pi$ loop with pion p-wave dressing from nuclear physics i.e. $\Delta - h$

$$\kappa_2(\rho) = \frac{\langle (\bar{q}q)^2 \rangle(\rho)}{\langle \bar{q}q \rangle^2(\rho)} = 1 + \frac{1}{f_\pi^2(\rho)} \int_0^{\Lambda_P} \frac{d\mathbf{P}}{(2\pi)^3} \int_0^\infty dE \left(\frac{-1}{\pi} \right) \text{Im} D_\sigma(E, \mathbf{P})$$

ρ/ρ_0	m_σ	m_π	f_π	$\Delta\kappa_2$
0	1000		93	0
0.5	890	140.3	87	0.33
1	795	143.1	79	0.88
1.5	649	148.7	69	1.39
2	510	161	56	3.74

III. SCALAR ISOSCALAR MODES

Matter stability in chiral theories

Energy density of dense nuclear matter

$$\epsilon(\rho, \sigma) = \sum_{p < p_F} \sqrt{p^2 + M_N^*(\langle \sigma \rangle)} + V(\langle \sigma \rangle) + C_V \rho^2$$

- NJL (Bentz, Thomas, Birse) : Nucleon $\equiv$ diquark-quark state. $M_q = g_q \langle \sigma \rangle$
- Chiral relativistic theories : $\sigma = \Theta \equiv$ chiral invariant scalar field. $M_N^* = g \langle \Theta \rangle$

NO STABILITY

Decrease of the curvature of the effective potential when $\langle \sigma \rangle$ drops

A sizeable $\frac{\partial^2 M_N}{\partial \sigma^2}$ can stabilize the matter

NEED OF CONFINEMENT EFFECT

NJL : Infrared cutoff

QMC : Polarization of the nucleon : Influence of the scalar field on the confined quark wave functions

IV. SCALAR-ISOSCALAR MODES

Model calculation

$$\mathcal{H} = N^\dagger \left(-i \vec{\alpha} \cdot \nabla + \beta M_N \left(1 + \frac{\theta}{f_\pi} + C \frac{\theta^2}{f_\pi^2} \right) \right) N$$

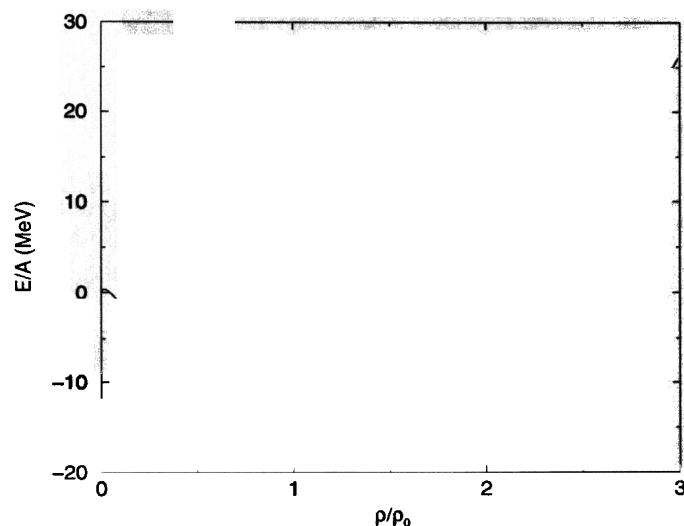
$$+ \frac{m_\theta^2}{8 f_\pi^2} \left((\theta + f_\pi)^2 - f_\pi^2 \right)^2 + g_\omega \omega N^\dagger N - \frac{1}{2} m_\omega^2 \omega^2$$

$$g_{\theta NN} = M_N / f_\pi \simeq 10, \quad m_\theta \simeq 800 \text{ MeV}$$

Extra θ^3, θ^4 terms constrained by chiral symmetry *i.e.* from the Mexican hat potential.

$C \simeq 1$: Nucleon polarization (QMC model) needed!

Short range repulsion : g_ω^2 / m_ω^2 : $m_\omega \simeq 780 \text{ MeV}$, $g_\omega \simeq 6$

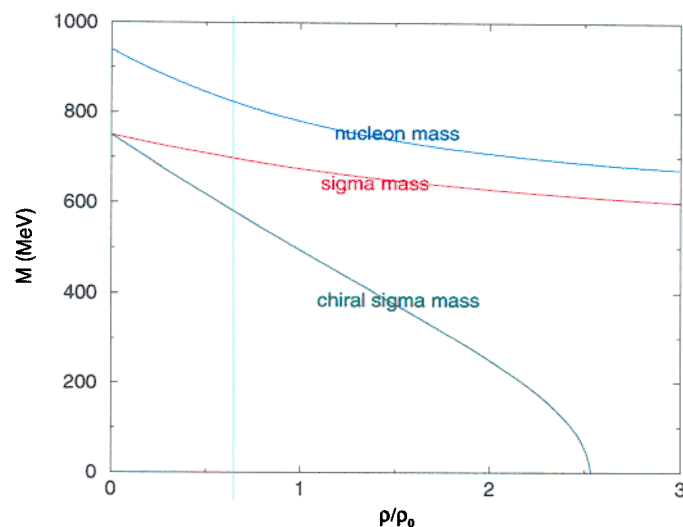


IV. SCALAR-ISOSCALAR MODES

- In-medium sigma mass

$$m_{\sigma}^{*2} = \frac{\partial^2 \epsilon}{\partial \Theta^2}$$

“Confining” term : $\frac{\theta^2}{f_{\pi}^2} + \frac{1}{3} \frac{\theta^3}{f_{\pi}^3}$
 $m_{\sigma} = 750 \text{ MeV}, \quad g_{\omega} = 6.8$

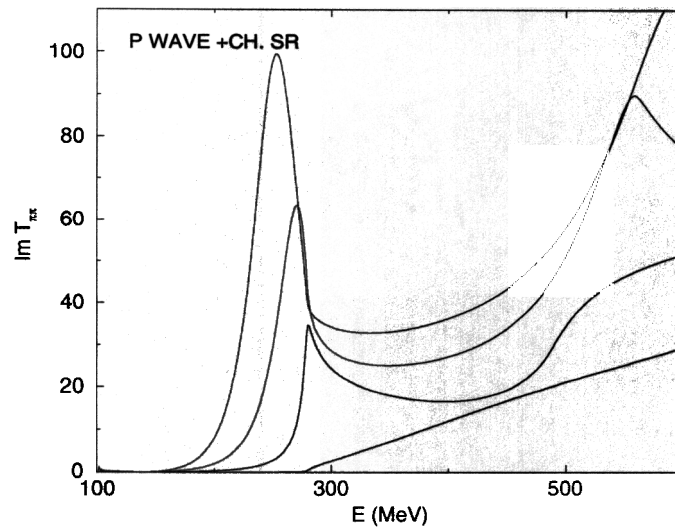
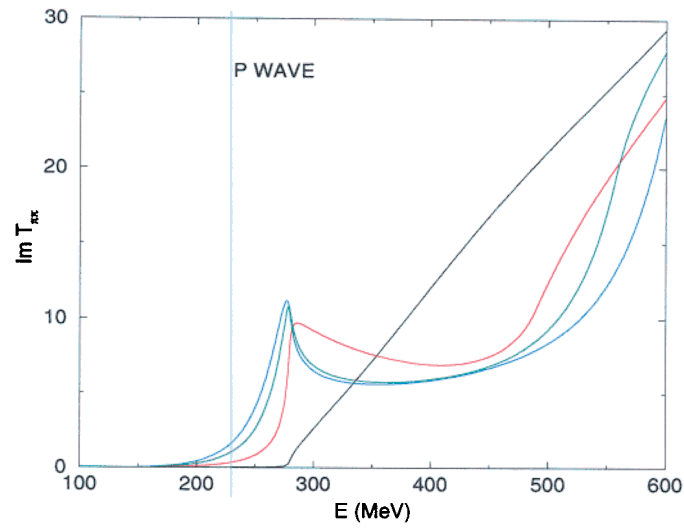


Very weak density dependence : “confinement” compensates chiral dropping

The scalar susceptibility (scalar quark density fluctuations) $\chi_S \sim 1/m_{\sigma}^{*2}$ does not increase but seems to saturate in the range $2 - 3 \rho_0$

IV. SCALAR-ISOSCALAR MODES

- $\pi\pi$ Strength function : Parameter set 1



Main effect : Dropping of the condensate

$$\lambda_{\sigma\pi\pi} = \frac{m_{\sigma}^{*2}}{\langle\Theta\rangle} m_{\pi}^2$$

IV. SCALAR SUSCEPTIBILITY

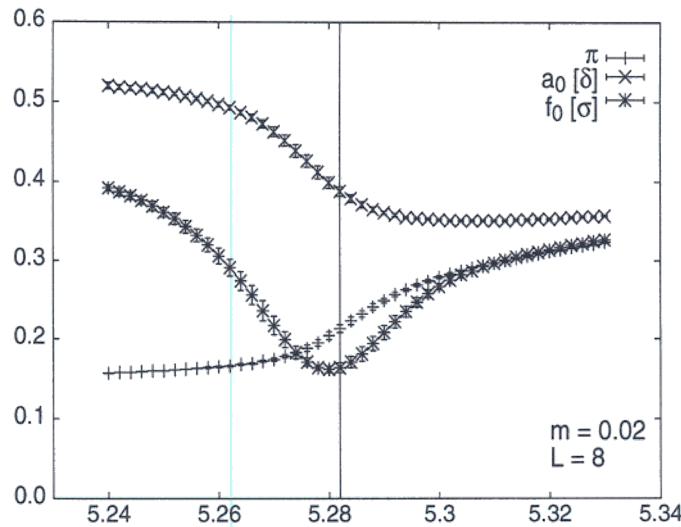
Scalar susceptibility

Define the Scalar susceptibility from the scalar correlator
i.e. the correlator of the scalar quark density fluctuations :

$$\chi_s = \frac{\partial \langle \bar{q} q \rangle}{\partial m} = \int dt d\vec{r} \langle \langle \delta \bar{q} q(0,0), \delta \bar{q} q(\vec{r},t) \rangle \rangle$$

$$\delta \bar{q} q(\vec{r},t) = \bar{q} q(\vec{r},t) - \langle \bar{q} q \rangle$$

- Thermal susceptibility (from lattice, Karsch et al)
- Near the phase transition the scalar susceptibility (fluctuations of the order parameter) becomes large
- Above the critical point : degeneracy between the chiral partners π and σ



SCALAR SUSCEPTIBILITY

Finite density susceptibilities (M)

$$\rightarrow \frac{\langle \bar{q} q \rangle_{vac}}{f_\pi} \sigma(\vec{r},$$

$$\bar{q} i \gamma_5 \frac{\vec{\tau}}{2} q(\vec{r}, t) \rightarrow \frac{\langle \bar{q} q \rangle_{vac}}{f_\pi} \vec{\Phi}(\vec{r}, t)$$

- Scalar susceptibility
- Quark density fluctuations carried by the scalar field σ

$$\chi_S = \frac{\langle \bar{q} q \rangle_{vac}^2}{f^2} \int dt d\vec{r} \langle \langle \delta\sigma(0, 0), \delta\sigma(\vec{r}, t) \rangle \rangle$$

$$\chi_S = \frac{\langle \bar{q} q \rangle_{vac}^2}{f^2} Re D_\sigma(\omega = 0, \mathbf{q} = 0)$$

- Sharp (in-medium) sigma $D_\sigma(r) = e^{-m_\sigma^* r}/r \rightarrow \chi_S \sim 1/m_\sigma^{*2}$
infinite range fluctuations
- Scalar density fluctuations transmitted by the sigma meson, relayed by the nucleons i.e. coupling to NN^{-1} . $\iff$ increase the range of the fluctuations

$$D_\sigma = D_\sigma^0 + D_\sigma^0 \Pi_{SS} D_\sigma^0$$

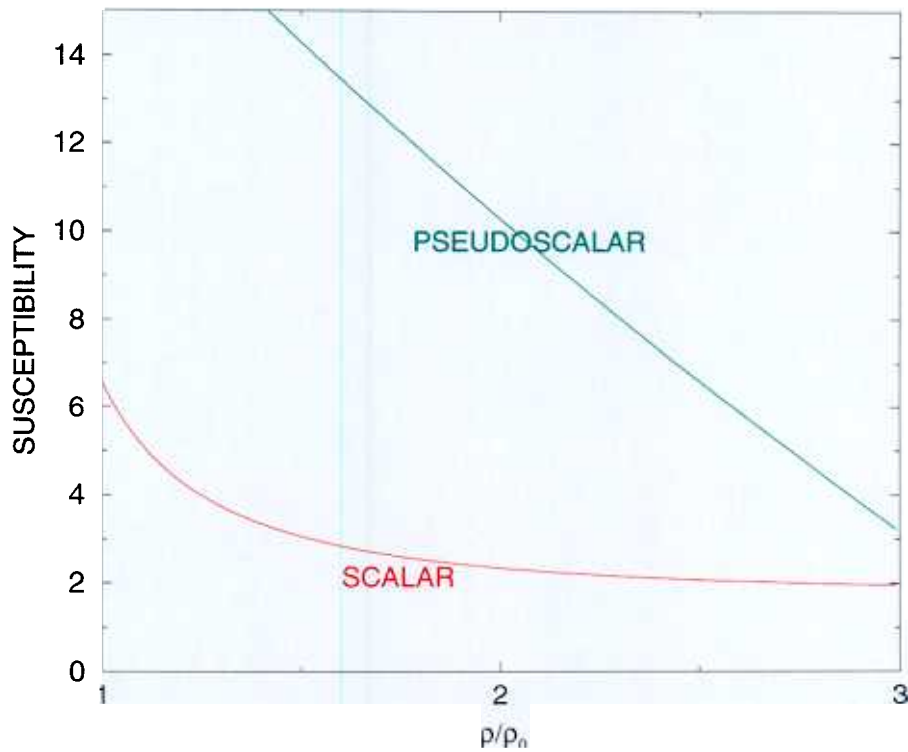
$$D_\sigma = D_\sigma^0 \left(1 + \frac{g_S^2}{m_\sigma^2} \frac{9}{K} \right)_{\rho=\rho_0}$$

IV. SCALAR SUSCEPTIBILITY

- Model calculation

$$D_\sigma = D_\sigma^0 \frac{m_\sigma^2}{m_\sigma^{*2}} \left(1 + \frac{g_S^{*2}}{m_\sigma^{*2}} \Pi(0, 0) \right)$$

$$\Pi(0, 0) = \frac{(-2 M_N^* k_F / \pi^2)}{1 - \left(\frac{g_V^2}{m_V^2} - \frac{g_S^{*2}}{m_\sigma^{*2}} \right) (-2 M_N^* k_F / \pi^2)}$$



- Dilepton production : Broadening of the vector meson spectral function driven by baryonic effect. Connection to chiral restoration only partially understood
- Study of high baryonic density matter : Need for a consistent description incorporating :
 - In-medium chiral dynamics (coupling to the condensate)
 - baryon (nucleon) structure and confinement
- Support from lattice at finite density (spectral functions, susceptibilities,...)