

Resonant Structures in $J/\psi p$

The LHCb Pentaquark Candidates

Sebastian Neubert

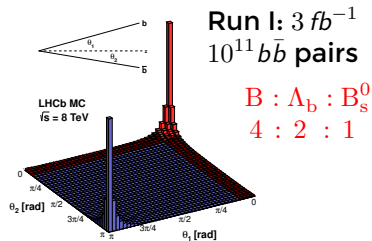
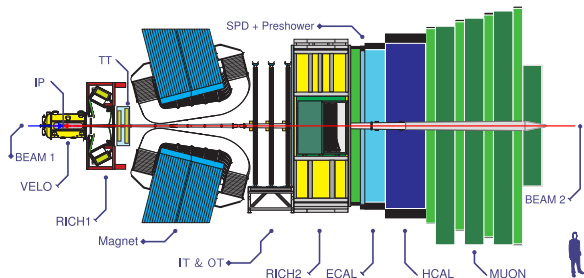
Heidelberg University

GSI 2015



The LHCb Experiment

- LHCb is a single-arm ($2 < \eta < 5$) spectrometer at the LHC
 - CP violation measurements, rare decays,
heavy flavor decays as source for exotic hadrons
 - Exploits the correlated production of $b\bar{b}$ pairs in the LHC environment



- Time-dependent analyses require good time resolution: ~ 40 fs (VELO)
- Flavor tagging, final state discrimination needs excellent particle ID (RICH)
- Highly efficient trigger: di-muons, displaced vertices (topological B-hadron), ..

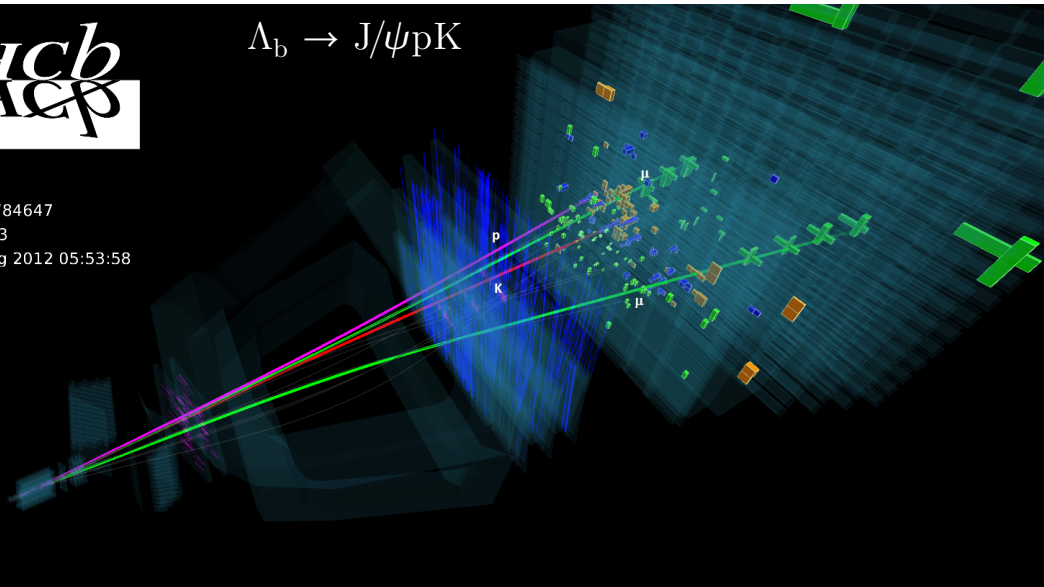


$$\Lambda_b \rightarrow J/\psi p K$$

Event 251784647

Run 125013

Thu, 09 Aug 2012 05:53:58



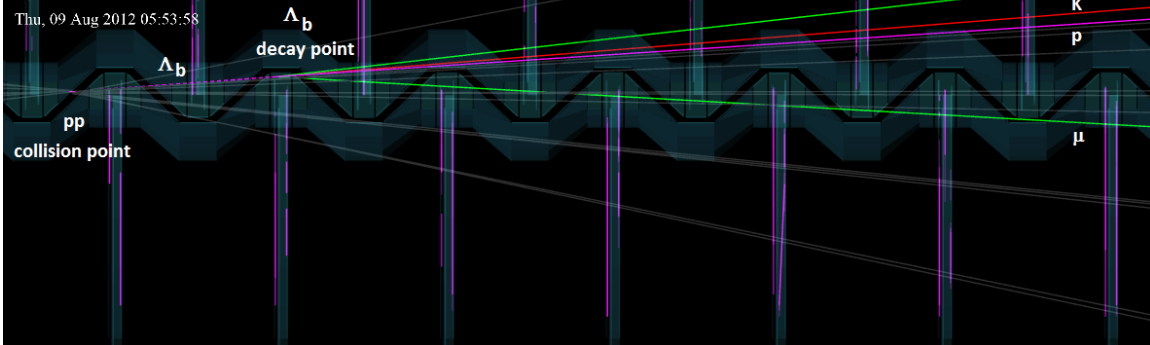


$$\Lambda_b \rightarrow J/\psi p K$$

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Run 125013

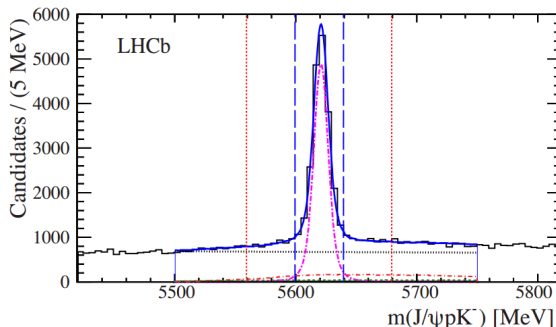
Thu, 09 Aug 2012 05:53:58





A Surprise in Λ_b Decays

- Initial goal: a precise measurement of the Λ_b **lifetime**
- 1 fb^{-1} of $\Lambda_b \rightarrow J/\psi p K$ + previous measurements: $\tau = 1.482 \pm 0.018 \pm 0.012\text{ ps}$
↪ PRL111(2013)102003





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 $\hookrightarrow \text{PRL111(2013)102003}$

$\hookrightarrow \text{arXiv:1509.00292}$

(to appear in Chin. Phys. C)

$$\sigma(\Lambda_b) \mathcal{B}(\Lambda_b \rightarrow J/\psi p K) =$$

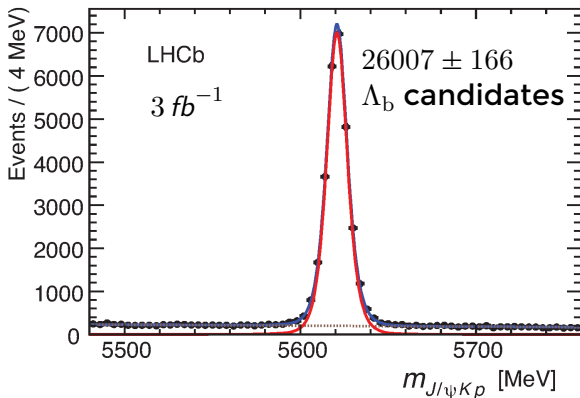
$$6.12 \pm 0.10 \pm 0.25 \text{ nb} \quad @7 \text{ TeV}$$

$$7.51 \pm 0.08 \pm 0.31 \text{ nb} \quad @8 \text{ TeV}$$

$$\mathcal{B}(\Lambda_b \rightarrow J/\psi p K) =$$

$$3.04 \pm 0.04 \pm 0.06 \pm 0.33^{+0.34}_{-0.27}$$

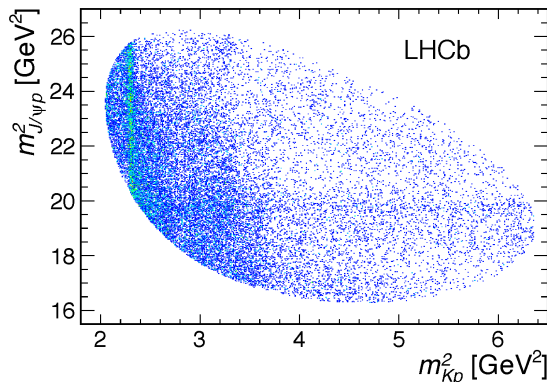
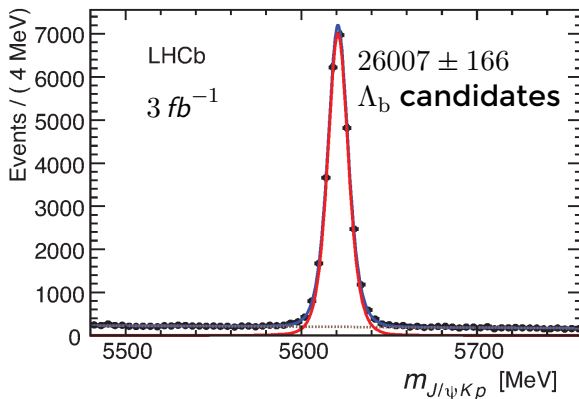
(additional systematic uncertainties
 from $B \rightarrow J/\psi K^*$ and f_{Λ_b}/f_d)





A Surprise in Λ_b Decays

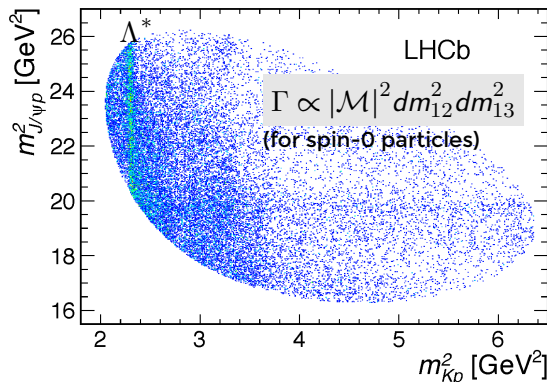
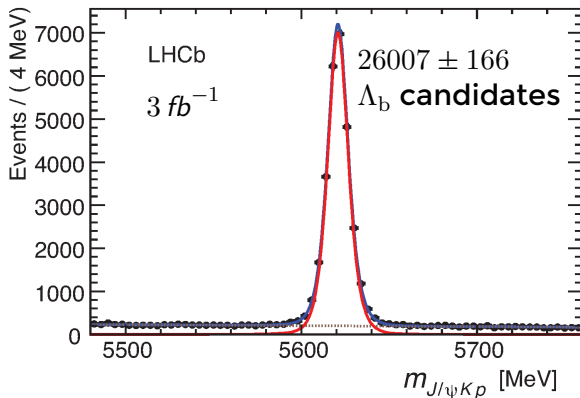
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- But looking closer at the $J/\psi\text{ } p\text{ } K$ Dalitz-Plot with a dataset of 3 fb^{-1} (Run I)





A Surprise in Λ_b Decays

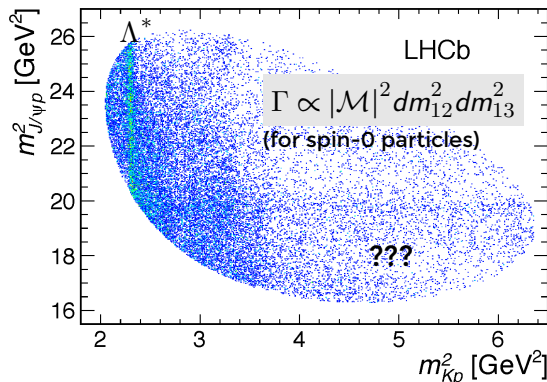
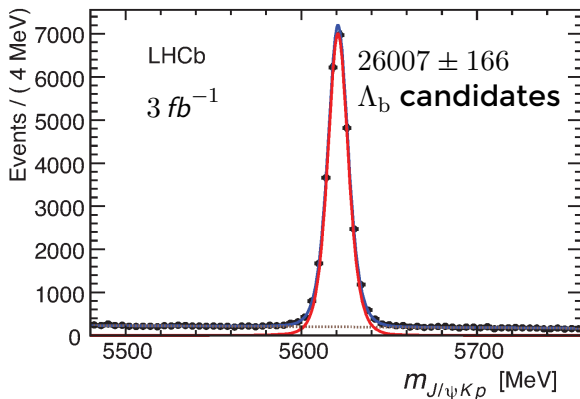
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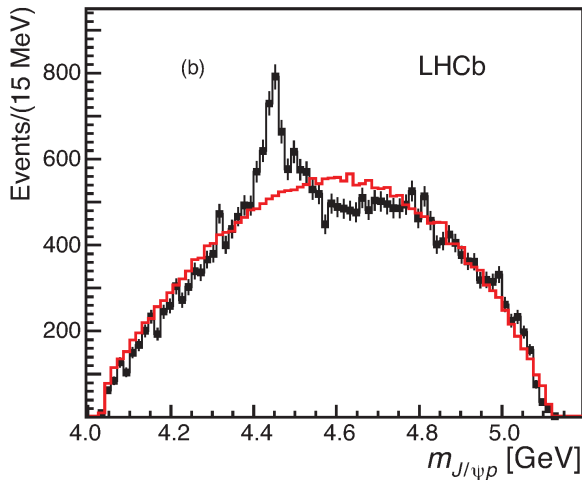
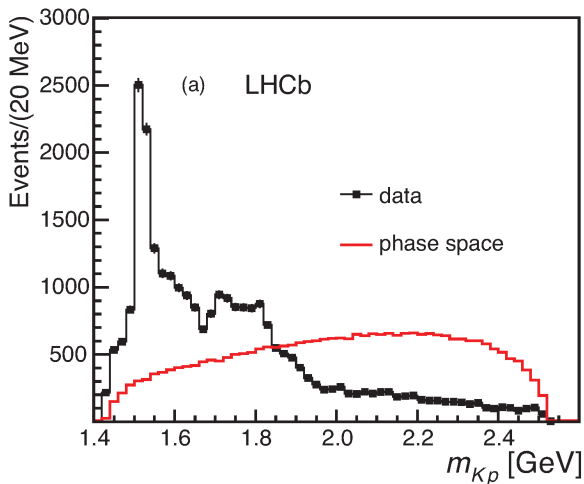
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2-Body Mass Spectra

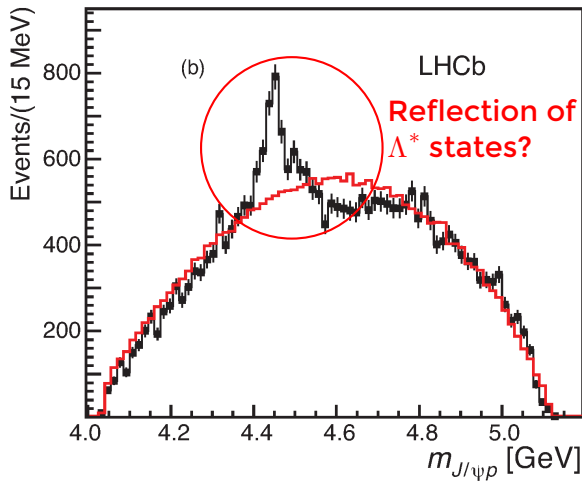
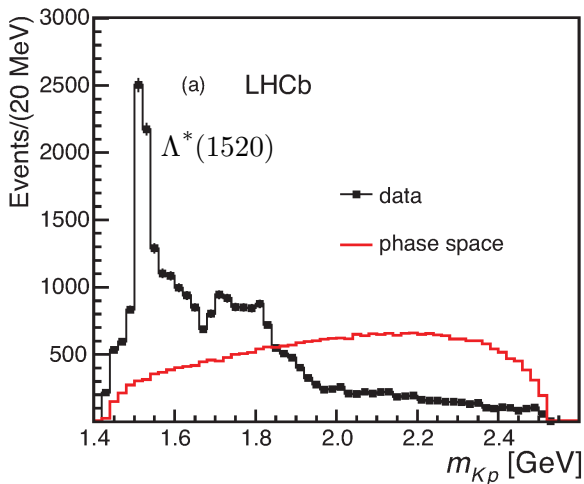
↪ PRL115(2015)072001





2-Body Mass Spectra

↪ PRL115(2015)072001





Known Λ^* States

2 Fit-Models used!

anchor →

State	J^P	PDG class	Mass (MeV)	Γ (MeV)	# Reduced	# Extended
$\Lambda^*(1405)$	$1/2^-$	****	$1405.1^{+1.3}_{-1.0}$	50.5 ± 2.0	3 ℓs couplings	4
$\Lambda^*(1520)$	$3/2^-$	****	1519.5 ± 1.0	15.6 ± 1.0	5	6
$\Lambda^*(1600)$	$1/2^+$	***	1600	150	3	4
$\Lambda^*(1670)$	$1/2^-$	****	1670	35	3	4
$\Lambda^*(1690)$	$3/2^-$	****	1690	60	5	6
$\Lambda^*(1710)$	$1/2^+$	*	1713 ± 13	180 ± 40	0	0
$\Lambda^*(1800)$	$1/2^-$	***	1800	300	4	4
$\Lambda^*(1810)$	$1/2^+$	***	1810	150	3	4
$\Lambda^*(1820)$	$5/2^+$	****	1820	80	1	6
$\Lambda^*(1830)$	$5/2^-$	****	1830	95	1	6
$\Lambda^*(1890)$	$3/2^+$	****	1890	100	3	6
$\Lambda^*(2000)$	?	*	≈ 2000	?	0	0
$\Lambda^*(2020)$	$7/2^+$	*	≈ 2020	?	0	0
$\Lambda^*(2050)$	$3/2^-$	*	2056 ± 22	493 ± 60	0	0
$\Lambda^*(2100)$	$7/2^-$	****	2100	200	1	6
$\Lambda^*(2110)$	$5/2^+$	***	2110	200	1	6
$\Lambda^*(2325)$	$3/2^-$	*	≈ 2325	?	0	0
$\Lambda^*(2350)$	$9/2^+$	***	2350	150	0	6
$\Lambda^*(2585)$	?	**	≈ 2585	200	0	6



Known Λ^* States

2 Fit-Models used!

anchor →

State	J^P	PDG class	Mass (MeV)	Γ (MeV)	# Reduced	# Extended									
$\Lambda^*(1405)$	$1/2^-$	2-body systems $\Lambda^* \rightarrow pK$ spin-spin and spin-orbit coupling $J = 1/2 \otimes 0 \otimes \ell$ $P = (+1) \times (-1) \times (-1)^\ell$ <table><tr><td>ℓ</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>J^P</td><td>$\frac{1}{2}^-$</td><td>$\frac{1}{2}^+, \frac{3}{2}^+$</td><td>$\frac{3}{2}^-, \frac{5}{2}^-$</td><td>$\frac{5}{2}^+, \frac{7}{2}^+$</td></tr></table> can you guess how this looks like for J/ψ p?	ℓ	0	1	2	3	J^P	$\frac{1}{2}^-$	$\frac{1}{2}^+, \frac{3}{2}^+$	$\frac{3}{2}^-, \frac{5}{2}^-$	$\frac{5}{2}^+, \frac{7}{2}^+$			couplings 4
ℓ	0		1	2	3										
J^P	$\frac{1}{2}^-$		$\frac{1}{2}^+, \frac{3}{2}^+$	$\frac{3}{2}^-, \frac{5}{2}^-$	$\frac{5}{2}^+, \frac{7}{2}^+$										
$\Lambda^*(1520)$	$3/2^-$		6												
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$\Lambda^*(1670)$	$1/2^-$		4												
$\Lambda^*(1690)$	$3/2^-$		6												
$\Lambda^*(1710)$	$1/2^+$		0												
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$\Lambda^*(1830)$	$5/2^-$		6												
$\Lambda^*(1890)$	$3/2^+$		6												
$\Lambda^*(2000)$	?		0												
$\Lambda^*(2020)$	$7/2^+$		0												
$\Lambda^*(2050)$	$3/2^-$	0													
$\Lambda^*(2100)$	$7/2^-$	6													
$\Lambda^*(2110)$	$5/2^+$	6													
$\Lambda^*(2325)$	$3/2^-$	0													
$\Lambda^*(2350)$	$9/2^+$	6													
$\Lambda^*(2585)$	?	6													



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$\Lambda^*(1710)$	$1/2^+$	*	1713 ± 13	1	Two Λ^* models	
$\Lambda^*(1800)$	$1/2^-$	***	1800			
$\Lambda^*(1810)$	$1/2^+$	***	1810		- Extended: Explore model space - Reduced: only keep non-vanishing components for final result - For the experts: Agreement checked by moments analysis	
$\Lambda^*(1820)$	$5/2^+$	****	1820			
$\Lambda^*(1830)$	$5/2^-$	****	1830			
$\Lambda^*(1890)$	$3/2^+$	****	1890			
$\Lambda^*(2000)$	?	*	≈ 2000			
$\Lambda^*(2020)$	$7/2^+$	*	≈ 2020			
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$\Lambda^*(2585)$	?	**	≈ 2585	200	0	6

Two Λ^* models

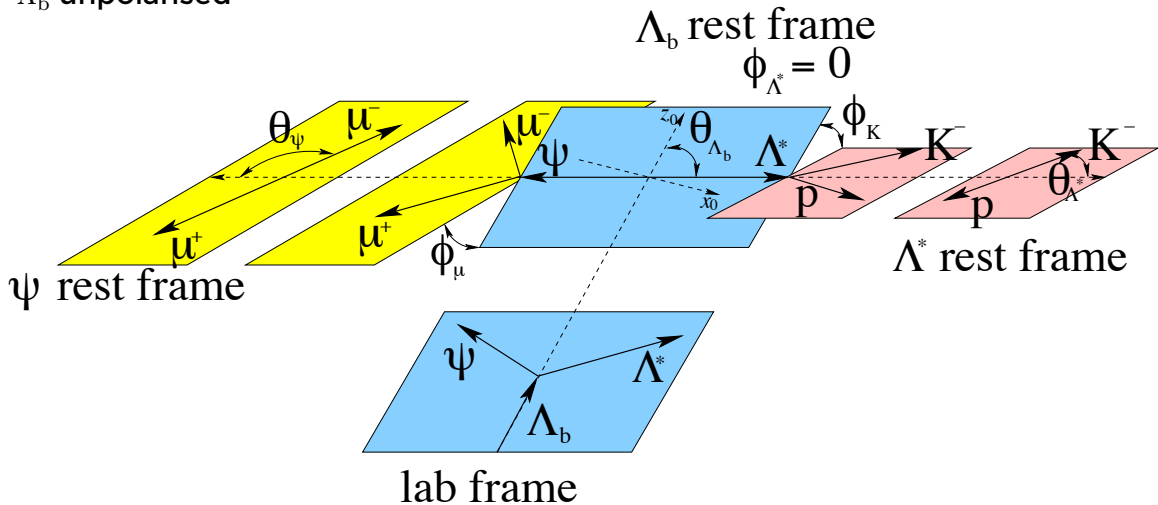
- Extended: Explore model space
- Reduced: only keep non-vanishing components for final result
- For the experts: Agreement checked by moments analysis



Isobarmodel Helicity Amplitudes for $\Lambda_b \rightarrow J/\psi \Lambda^*$

Matrix Element $\mathcal{M}^{\Lambda^*}$ parametrized as a function of 5 angles and one mass m_{pK}^2

Λ_b unpolarised





Isbarmodel Helicity Amplitudes for $\Lambda_b \rightarrow J/\psi \Lambda^*$

- **Angular structures** (no free parameters)
- **Helicity couplings** ← complex numbers, floating in fit
- **Λ^* resonant amplitudes** see next slide

$$\mathcal{M}^{\Lambda^*} = \sum_n R_n(m_{Kp}) \mathcal{H}_{\lambda_p}^{\Lambda_n^* \rightarrow Kp} \sum_{\lambda_\psi} e^{i\lambda_\psi \phi_\mu} d_{\lambda_\psi, \Delta\lambda_\mu}^1(\theta_\psi) \times$$

$$\sum_{\lambda_{\Lambda^*}} \mathcal{H}_{\lambda_{\Lambda^*}, \lambda_\psi}^{\Lambda_b \rightarrow \Lambda_n^* \psi} e^{i\lambda_{\Lambda^*} \phi_K} d_{\lambda_{\Lambda_b}, \lambda_{\Lambda^*} - \lambda_\psi}^{\frac{1}{2}}(\theta_{\Lambda_b}) d_{\lambda_{\Lambda^*}, \lambda_p}^{J_{\Lambda_n^*}}(\theta_{\Lambda^*})$$



Resonance parametrisation

Dynamical Terms $R_n(m_{Kp})$ given by

- Relativistic, single-channel Breit-Wigner amplitudes $BW(M_{Kp}|M_0^{\Lambda_n^*}, \Gamma_0^{\Lambda_n^*})$

$$BW(M|M_0, \Gamma_0) = \frac{1}{M_0^2 - M^2 - iM_0\Gamma(M)},$$

where

$$\Gamma(M) = \Gamma_0 \left(\frac{q}{q_0} \right)^{2\ell_{\Lambda^*}+1} \frac{M_0}{M} B'_{\ell_{\Lambda^*}}(q, q_0, d)^2.$$

- Angular-momentum barrier factors $B'_\ell(p, p_0, d)$

$$R_n(m_{Kp}) = B'_{\ell_{\Lambda_b}} \left(\frac{p}{M_{\Lambda_b}} \right)^{\ell_{\Lambda_b}} \times BW(M_{Kp}) \times B'_{\ell_{\Lambda_n^*}} \left(\frac{q}{M_{\Lambda_n^*}} \right)^{\ell_{\Lambda_n^*}}.$$

- special case $\Lambda(1405)$ is subthreshold: Flatté (K p and $\Sigma \pi$ channels)

$p(q)$ are momenta of the daughter particles in the rest-frame of the decaying particle.

$p_0(q_0)$ calculated on the nominal resonance mass

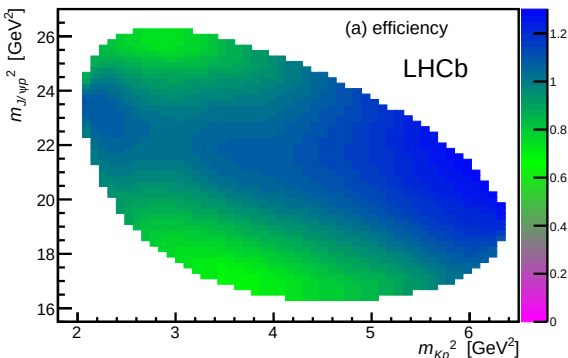


2 Fitters - XCheck of Background Treatment

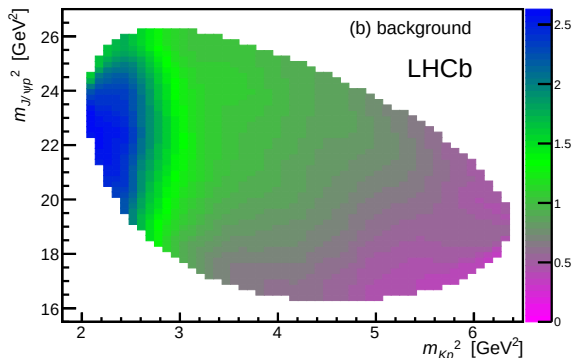
Log-likelihood fitters:

- **sFit** : subtract background with the sWeight method
- **cFit** : explicitly model background from sidebands (default)
- Missidentified B-meson decays vetoed $B \rightarrow J/\psi K \pi$ and $B_s^0 \rightarrow J/\psi K K$

Efficiency from MC



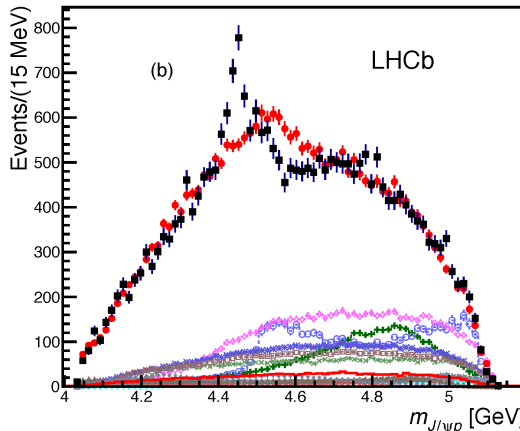
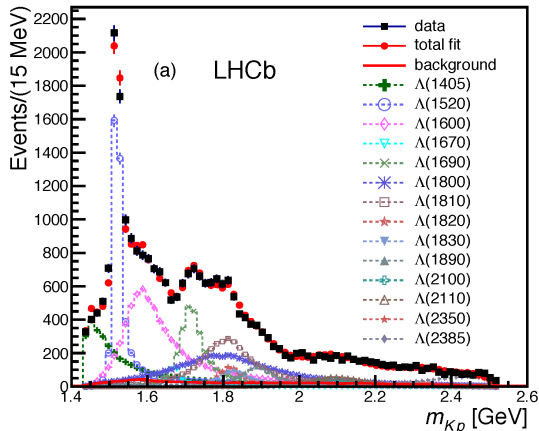
Background density shape (5.4%)





Results with only Λ^* States

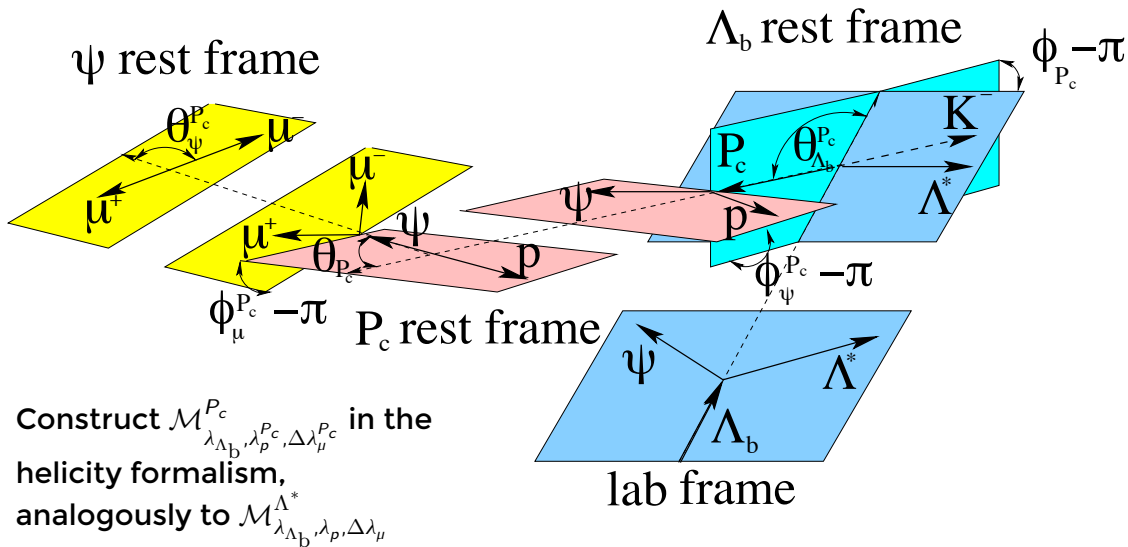
cFit with extended Λ^* model (14 states allowed):



- Adding two new Λ^* states with floating mass/width does not improve fit
- Λ^* reflections don't explain the structure in $m_{J/\psi p}$



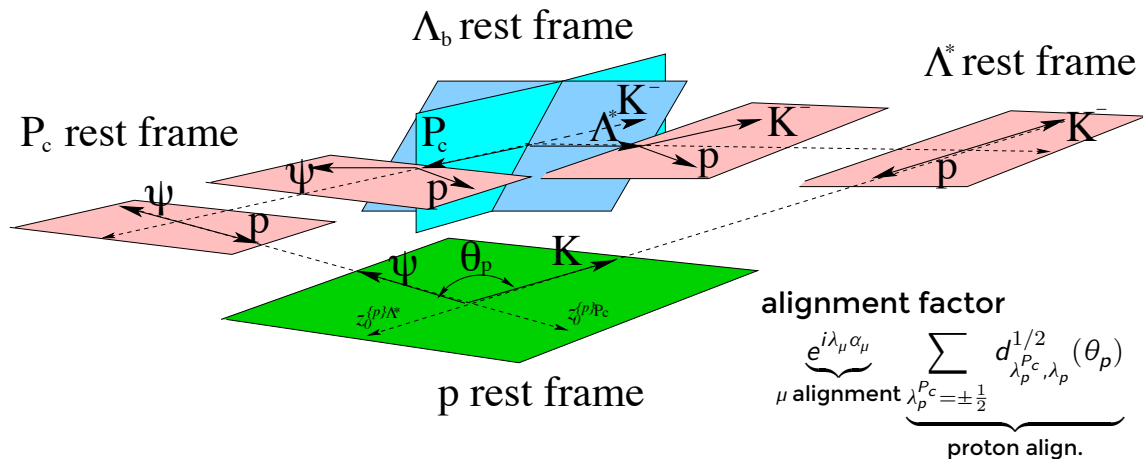
Adding Helicity Amplitudes for $\Lambda_b \rightarrow P_c K$





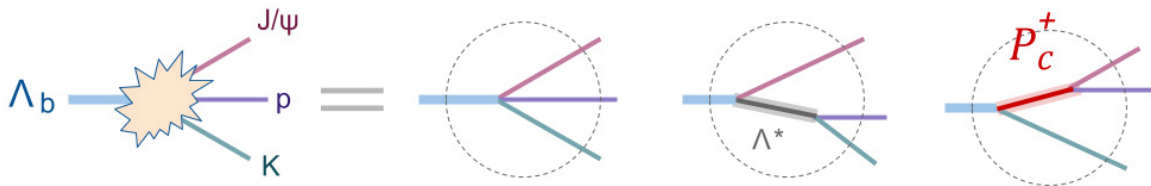
An important detail: Aligning reference frames

Helicities of final state particle have to be evaluated in the same reference system!





Interference between $\Lambda_b \rightarrow J/\psi \Lambda^*$ and $\Lambda_b \rightarrow P_c K$



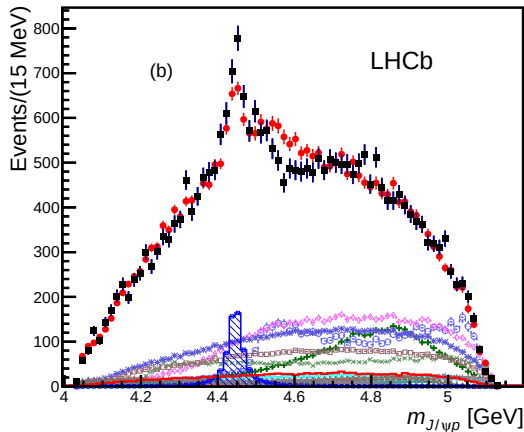
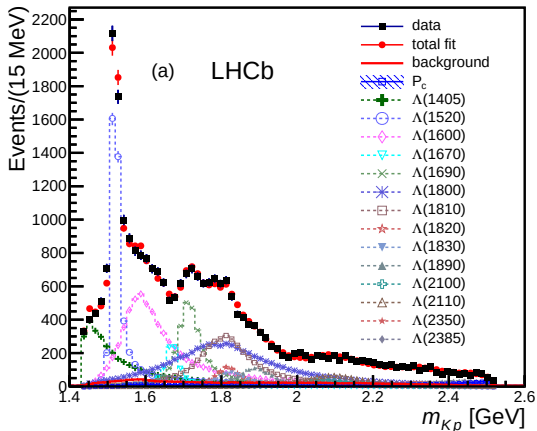
- Coherent sum over amplitudes, incoherent sum over external helicities

$$|\mathcal{M}|^2 = \sum_{\lambda_{\Lambda_b} = \pm \frac{1}{2}} \sum_{\lambda_p = \pm \frac{1}{2}} \sum_{\Delta\lambda_\mu = \pm 1} \left| \mathcal{M}^{\Lambda^*} + \underbrace{e^{i\lambda_\mu \alpha_\mu}}_{\mu \text{ alignment}} \underbrace{\sum_{\lambda_p^{P_c} = \pm \frac{1}{2}} d_{\lambda_p^{P_c}, \lambda_p}^{1/2}(\theta_p)}_{\text{proton align.}} \mathcal{M}^{P_c} \right|^2$$



Results with One J/ψ p Resonance

Extended Λ^* model + 1 J/ψ p resonance (floating mass and width, $J^P = 5/2^+$)

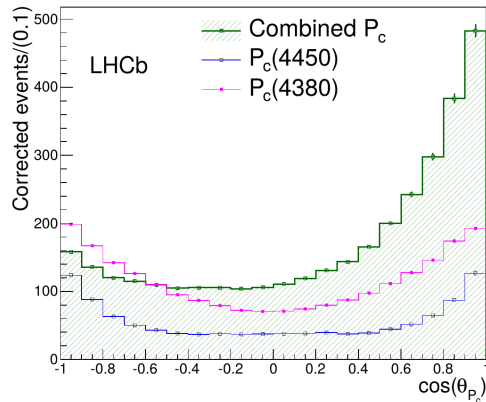
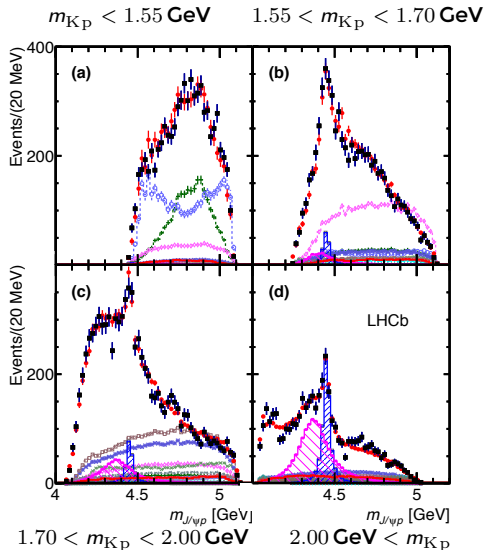


Improvement w.r.t to fit without P_c : $\sqrt{\Delta 2\mathcal{L}} = 14.7\sigma$



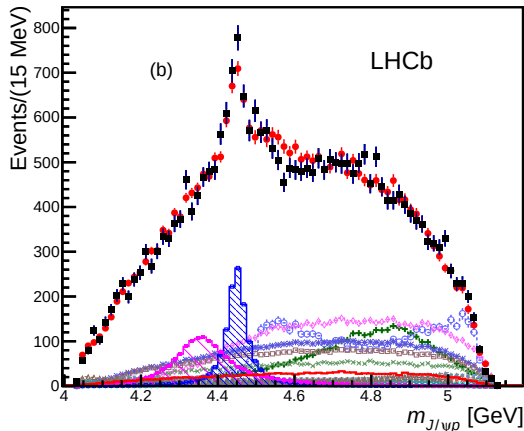
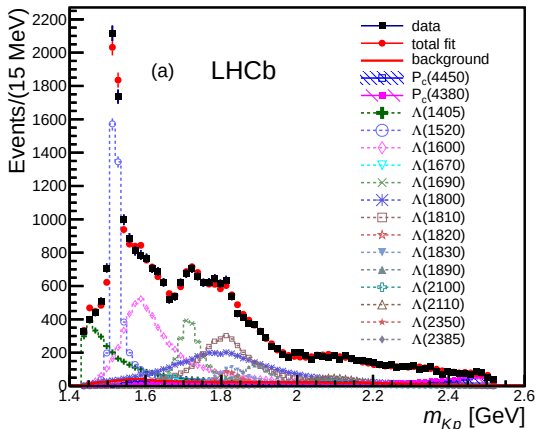
Why a second state with opposing parity?

- The peaking structure in $m_{J/\psi p}$ is asymmetric as a function of m_{Kp} (or $\cos \theta_{P_c}$)
- This can be explained by interference of two states with opposing parity





Results with 2 J/ψ p Resonances

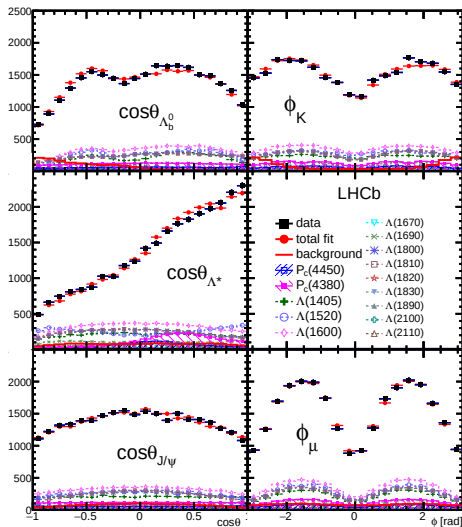


Improvement w.r.t to fit without P_c : $\sqrt{\Delta 2\mathcal{L}} = 18.7\sigma$
Adding further P_c states did not improve the fit significantly

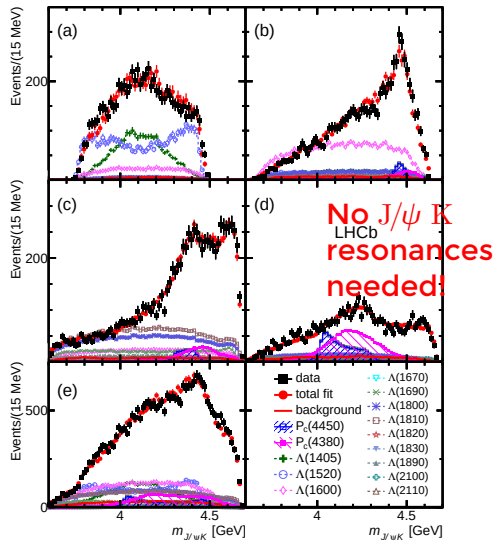


Fit describes data well in all variables

Angular distributions

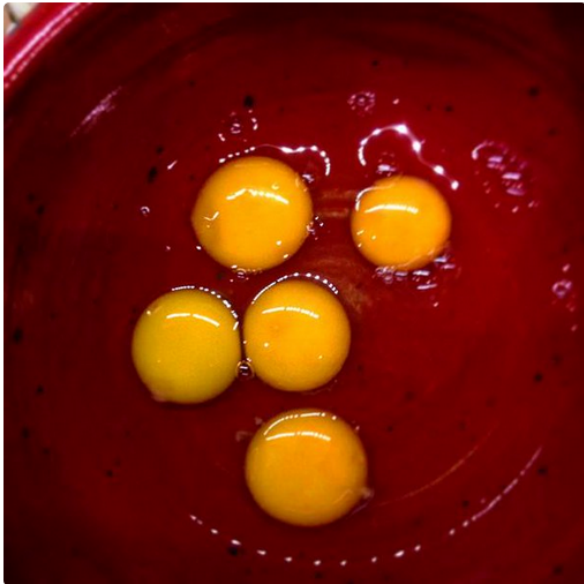


$m_{J/\psi K}$ in bins of m_{K^0}





amarsollier @amarsollier · Jul 13





Extracted Resonance Parameters

State	Mass [MeV]	Width [MeV]	fav. J^P	Fit fraction	Signi.
$P_c(4380)^+$	$4380 \pm 8 \pm 29$	$205 \pm 18 \pm 86$	$3/2^-$	$(8.4 \pm 0.7 \pm 4.2)\%$	9σ
$P_c(4450)^+$	$4449.8 \pm 1.7 \pm 2.5$	$39 \pm 5 \pm 19$	$5/2^+$	$(4.1 \pm 0.5 \pm 1.1)\%$	12σ

- Reduced fit model used for central values
- Significances evaluated on Toy-MC samples: $-2 \ln \mathcal{L}$ distributions consistent with χ^2 distribution $\rightarrow$ p-value
- Spin-parity assignment not conclusive:

Fit	$\Delta(-2 \ln \mathcal{L})$	P_c (Low) Mass	P_c (Low) Γ	P_c (High) Mass	P_c (High) Γ
$\frac{3}{2}^-, \frac{5}{2}^+$	0	4.3799 ± 0.0064	0.205 ± 0.011	4.4498 ± 0.0017	0.0387 ± 0.0037
$\frac{3}{2}^+, \frac{5}{2}^-$	0.9^2	4.3696 ± 0.0063	0.211 ± 0.012	4.4504 ± 0.0017	0.0492 ± 0.0040
$\frac{5}{2}^+, \frac{3}{2}^-$	2.3^2	4.3770 ± 0.0098	0.239 ± 0.024	4.4486 ± 0.0018	0.0444 ± 0.0053
$\vdots$					



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$\frac{3}{2}^-, \frac{5}{2}^+$	0	4.3799 ± 0.0064	0.205 ± 0.011	4.4498 ± 0.0017	0.0387 ± 0.0037
$\frac{3}{2}^+, \frac{5}{2}^-$	0.9^2	4.3696 ± 0.0063	0.211 ± 0.012	4.4504 ± 0.0017	0.0492 ± 0.0040
$\frac{5}{2}^+, \frac{3}{2}^-$	2.3^2	4.3770 ± 0.0098	0.239 ± 0.024	4.4486 ± 0.0018	0.0444 ± 0.0053
$\vdots$					

- Λ^* states fit-fractions:

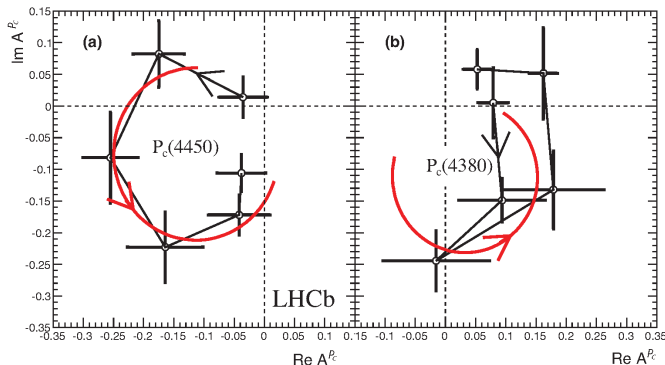
$$\Lambda(1405) \rightarrow pK \quad (15 \pm 1 \pm 6)\%$$

$$\Lambda(1520) \rightarrow pK \quad (19 \pm 1 \pm 4)\%$$



Extracting the Phase

- Replace the Breit-Wigner amplitude in the model with complex valued cubic spline A in 6 bins of $m^2(J/\psi p)$, centered around the P_c peaks from nominal fit



- Amplitude in complex plane
- Circular shape corresponds to resonant phase motion (anti-clockwise)
- In red: BW amplitude from nominal fit
- Offset in phase from reference amplitude(s)

Interpretations



Inspirations



Pentaquarks are not a new idea

Volume 8, number 3

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A SCHEMATIC MODEL OF BARYONS AND MESONS *

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Received 4 January 1964

If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" ¹⁻³, we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone ⁴). Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

Even if we consider the scattering amplitudes of strongly interacting particles on the mass shell only and treat the matrix elements of the weak, electromagnetic, and gravitational interactions by means

of $n_t - n_{\bar{t}}$ would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin $\frac{1}{2}$ and $z = -1$, so that the four particles d^- , s^- , u^0 and b^0 exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon b if we assign to the triplet t the following properties: spin $\frac{1}{2}$, $z = -\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" ⁶) q and the members of the anti-triplet as anti-quarks $\bar{q}$. Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. It is assuming that the lowest baryon configuration (qqq) gives just the representations **1**, **8**, and **10** that have been observed, while the lowest meson configuration $(q\bar{q})$ similarly gives just **1** and **8**.



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All previous searches have failed

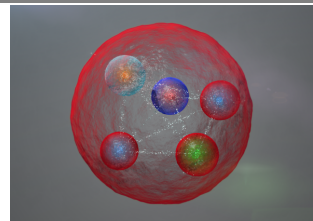
Historical account:
"On the conundrum of the pentaquark"

EPJ H37(2012)1



What causes these resonant structures in J/ψ p?

- Valence quark content: $uudc\bar{c}$
- What are the relevant degrees of freedom?

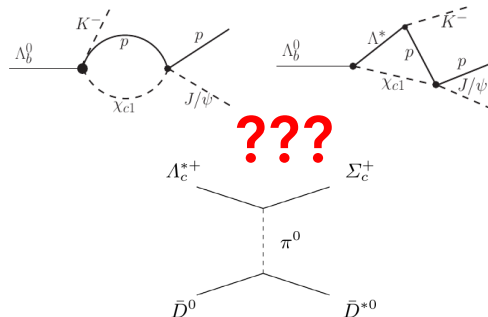


Challenges:

- Why two states with opposite parity?
- Small mass gap ≈ 100 MeV
- Narrow width of $P_c(4450)$

Proposed paradigms:

- Rescattering effects
- Meson-Baryon Molecules
- Pentaquarks in the Di-Quark model





Theory community reacting to $J/\psi p K$ (selection)

Rescattering effects:

$\chi_{c1}(1P)p$ rescattering	$\hookrightarrow$ arXiv:1507.04950
D^*, D_s^*, Σ_c triangle singularity	$\hookrightarrow$ arXiv:1507.06552
$P_c(4380)$ rescat, $P_c(4450)$ di-quark model	$\hookrightarrow$ arXiv:1507.07652
Anomalous triangle singularity	$\hookrightarrow$ arXiv:1507.05359

Mini Review on Meson-Baryon composite models: $\hookrightarrow$ arXiv:1509.02460

Molecules:

Chiral constituent quark model	$\hookrightarrow$ arXiv:1507.08046
Isospin exchange model	$\hookrightarrow$ arXiv:1506.06386
$D^* \Sigma_c$ molecule	$\hookrightarrow$ arXiv:1507.04249
Hadrocharmonium	$\hookrightarrow$ arXiv:1508.00888

Di-Quark Models:

Dynamical di-quark tri-quark picture	$\hookrightarrow$ arXiv:1507.05867
Strange and Nonstrange pentaquarks	$\hookrightarrow$ arXiv:1509.04898
QCD sum rules for $(qq)(qq)(\bar{q})$	$\hookrightarrow$ arXiv:1509.06436
Flavour SU(3) in di-quark model	$\hookrightarrow$ arXiv:1507.04980
P_c masses in di-quark model	$\hookrightarrow$ arXiv:1508.00356
Coloured constituents	$\hookrightarrow$ arXiv:1507.04694

	P_c^*				P_c	
	$\chi_{c1}p$	$\Sigma_c \bar{D}^*$	$\Lambda_c^* \bar{D}$	$J/\psi N^*$	$\Sigma_c^* \bar{D}$	$J/\psi N^*$
$J/\psi N$	✓	✓	✓	✓	✓	✓
$\eta_c N$	×	×	✓	×	×	×
$J/\psi \Delta$	×	✓	×	×	✓	×
$\eta_c \Delta$	×	✓	×	×	✓	×
$\Lambda_c \bar{D}$	✓	[×]	[✓]	×	[×]	×
$\Lambda_c \bar{D}^*$	✓	✓	[✓]	✓	✓	✓
$\Sigma_c \bar{D}$	✓	[×]	✓	×	[×]	×
$\Sigma_c^* \bar{D}$	✓	✓	[×]	✓		
$J/\psi N \pi$	×	✓	×	✓	✓	✓
$\Lambda_c \bar{D} \pi$	×	×	×	×	✓	×
$\Lambda_c \bar{D}^* \pi$	×	✓	×	×		
$\Sigma_c^+ \bar{D}^0 \pi^0$	×	✓	✓	×		

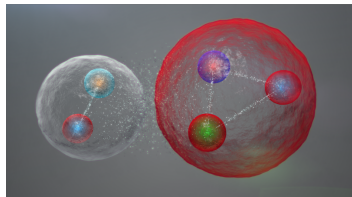
Production:

Bottom baryon decays	$\hookrightarrow$ arXiv:1509.03708
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Meson-Baryon degrees of freedom following $\hookrightarrow$ arXiv:1509.02460

- Proximity of thresholds makes two-body contributions unavoidable



Closeby thresholds		
[MeV]	$P_c(4380)^+$	$P_c(4450)^+$
Mass	$4380 \pm 8 \pm 29$	$4449.8 \pm 1.7 \pm 2.5$
$\Sigma_c^{*+} \bar{D}^0$	4382.3 ± 2.4	
$\chi_{c1}(1P) p$		4448.93 ± 0.07
$\Lambda_c^{+*} \bar{D}^0$		4457.09 ± 0.35
$\Sigma_c \bar{D}^{0*}$		4459.9 ± 0.5
$\Sigma_c \bar{D}^0 \pi^0$		4452.7 ± 0.5

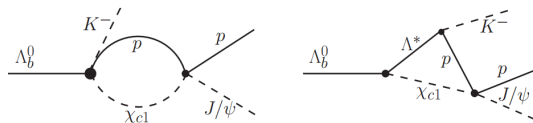
Channel	$\chi_{c1}(1P) p$	$\Lambda_c^{+*} \bar{D}$	$\Sigma_c^* \bar{D} / \Sigma_c \bar{D}^*$	$J/\psi N(1440/1520)$
Features	phase-motion of $P_c(4450)$		Pion exchange	opposite parity with S-wave for both states
Exp.Sign.	Decays to direct channels		Isospin $I = \frac{3}{2}$	150 MeV binding?

considered here: $J^P \in \left\{ \frac{3^\pm}{2}, \frac{5^\pm}{2} \right\}$

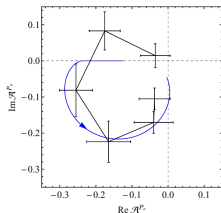


Testing Rescattering Models: $\Lambda_b \rightarrow \chi_{c1}(1P) p K$

■ Guo et al $\hookrightarrow$ arXiv:1507.04950

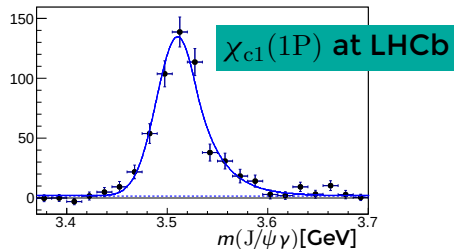
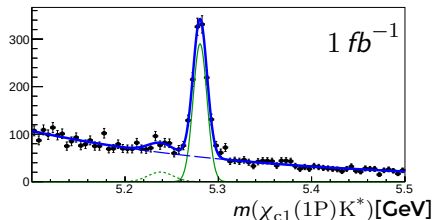


■ can explain $P_c(4450)$ phase motion



■ Rescattering would not explain a narrow enhancement right above $\chi_{c1}(1P) p$ threshold

$B \rightarrow \chi_{c1}(1P) K^*$
 $\hookrightarrow$ arXiv:1305.6511



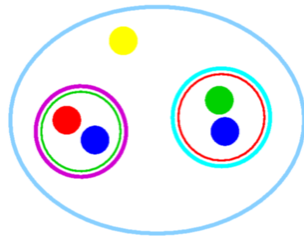


Pentaquarks in the Di-Quark Picture $\hookrightarrow$ arXiv:1507.04980

$$P = \{\bar{c}[cq]_s[qq]_s, \ell\}$$

- Opposite parity understood: additional orbital angular momentum ℓ
- One unit ℓ costs:
 $\delta m \approx m(\Lambda(1405)) - m(\Lambda(1116)) \approx 300 \text{ MeV}$
- Coupling spins to $s = 1$ in the light-light di-quark:
 $\delta m \approx m(\Sigma_c(2455)) - m(\Lambda_c(2286)) \approx 200 \text{ MeV}$

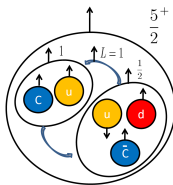
$P_c(4380)$	$\frac{3}{2}^-$	$\{\bar{c}[cq]_{s=1}[qq]_{s=1}, \ell = 0\}$
$P_c(4450)$	$\frac{5}{2}^+$	$\{\bar{c}[cq]_{s=1}[qq]_{s=0}, \ell = 1\}$



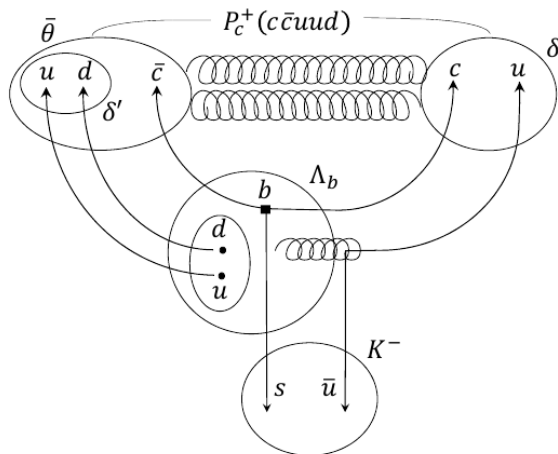
- Can explain the small mass gap!



■ $P_c(4450)$ as Di-quark + Antitri-quark



- Rapidly expanding system
- Can't hadronise by fluxtube breaking
- Decay through wavefunction overlap with daughters
- J/ψ as well as Λ_c^+ are compact
- **Explains narrow width!**



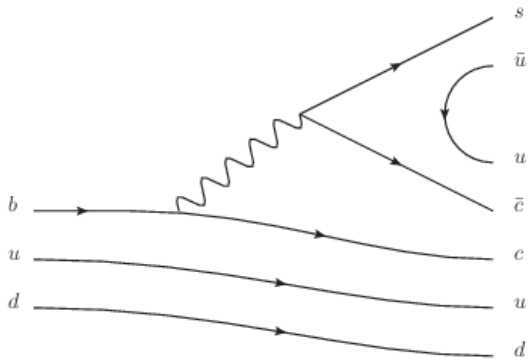
- Similar to model for $X(3872)$ ↪ arXiv:1406.7281



Pentaquark Isospin Multiplet?

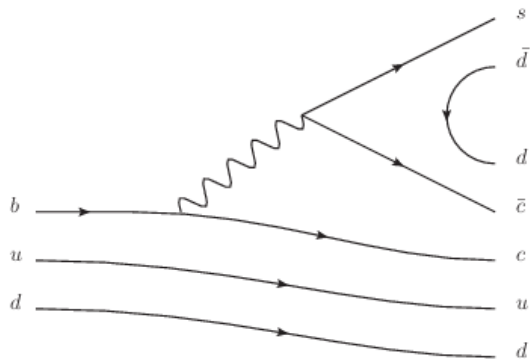
The observed pentaquark

$$\Lambda_b \rightarrow P_c^+ K \rightarrow J/\psi p K$$



Isospin partner: replacing $u\bar{u}$ with $d\bar{d}$

$$\Lambda_b \rightarrow P_c^0 K^0 \rightarrow J/\psi n K^0 \quad \text{or} \quad J/\psi p \pi^- K^0$$



**Neutron in the final state
or 4-body $J/\psi p \pi^- K_S^0$**



$\Lambda_b \rightarrow J/\psi \Lambda \phi$ and Friends

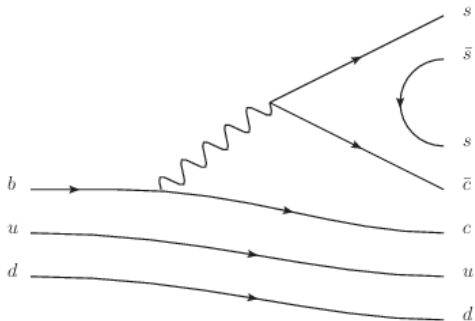
SU(3) Flavour Multiplet!?

Strange partner: replacing $u\bar{u}$ with $s\bar{s}$

$$\Lambda_b \rightarrow P_{cs}^0 \phi \rightarrow J/\psi \Lambda \phi$$

■ Each subsystem exotic

- $J/\psi \Lambda$: Strange Pentaquark
- $J/\psi \phi$: X(4140) ?
- $\Lambda \phi$: Spectrum unexplored



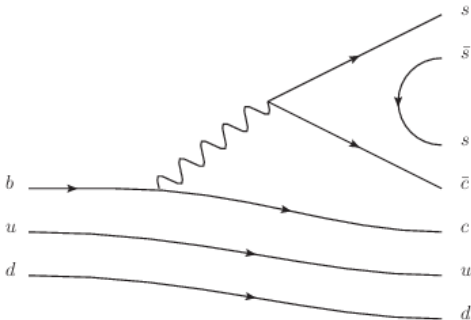


$\Lambda_b \rightarrow J/\psi \Lambda \phi$ and Friends

SU(3) Flavour Multiplet!?
 Strange partner: replacing $u\bar{u}$ with $s\bar{s}$

$$\Lambda_b \rightarrow P_{cs}^0 \phi \rightarrow J/\psi \Lambda \phi$$

- Each subsystem exotic
 - $J/\psi \Lambda$: Strange Pentaquark
 - $J/\psi \phi$: $X(4140)$?
 - $\Lambda \phi$: Spectrum unexplored



Di-quark model suggestions

Maiani et al $\hookrightarrow$ arXiv:1507.04980

Process	$\mathbb{P} \in 10 \oplus 8$
$\Lambda_b \rightarrow K J/\psi p$	$\mathbb{P}_8(\bar{c}[cq]_{s=1}[q'q'']_{s=0,1}, \ell = 0, 1)$
$\Lambda_b \rightarrow \pi J/\psi \Sigma(1385)$	$\mathbb{P}_{10}(\bar{c}[cq]_{s=0,1}[q's]_{s=0,1})$
$\Xi_b^- \rightarrow K J/\psi \Sigma(1385)$	$\mathbb{P}_{10}(\bar{c}[cs]_{s=0,1}[ss]_{s=1})$
$\Omega_b^- \rightarrow \phi J/\psi \Omega^-(1672)$	$\mathbb{P}_{10}(\bar{c}[cq]_{s=0,1}[ss]_{s=1})$

A Program for Baryon Spectroscopy



$P_c(4380)$ & $P_c(4450)$: a New Sector in Baryon Spectroscopy?

What are they?

Are there more of their kind?



$P_c(4380)$ & $P_c(4450)$: a New Sector in Baryon Spectroscopy?

What are they?

- Observe $P_c \rightarrow J/\psi p$ as subsystems in different final states
 - $\Lambda_b \rightarrow J/\psi p \pi$
 - $\Upsilon \rightarrow J/\psi p \bar{p}$
 - $\Lambda_b \rightarrow J/\psi p \pi K_S^0$
- Confirmation by other experiments urgently needed!
- Search for new decay modes of P_c
 - $\Lambda_b \rightarrow \chi_{c1}(1P) p K$
 - $\Lambda_b \rightarrow \Lambda_c^+ \bar{D}^0 K$

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$P_c(4380)$ & $P_c(4450)$: a New Sector in Baryon Spectroscopy?

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Are there more of their kind?

- Explore a possible multiplet of pentaquarks
 - $\Lambda_b \rightarrow J/\psi p \pi K_S^0$
 - $\Lambda_b \rightarrow J/\psi \Lambda \phi$
 - Triply charged baryons?

All modes unobserved so far!



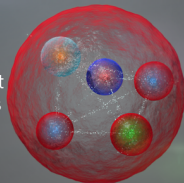
Summary: First observation of J/ψ p resonances

- Full amplitude analysis of $3\text{ fb}^{-1} \Lambda_b \rightarrow J/\psi p K$ at LHCb
↪ PRL115(2015)072001
- Two states of opposite parity required
 - $P_c(4380)^+$: $m = 4380 \pm 8 \pm 29$, $\Gamma = 205 \pm 18 \pm 86$, $J^P = 3/2^-$ **or** $5/2^+$
 - $P_c(4450)^+$: $m = 4449.8 \pm 1.7 \pm 2.5$, $\Gamma = 39 \pm 5 \pm 19$, $J^P = 5/2^+$ **or** $3/2^-$
- Resonant phase motion extracted
 - Consistent with Breit-Wigner for $P_c(4450)$
 - $P_c(4380)$: More complicated (but counter-clockwise phase motion)
- No $J/\psi K$ resonances needed, No extra Λ^* needed
- Program to confirm and search for new states
- Confirmation from other experiments needed!

nature

The LHCb result
leaves little doubt
that **pentaquarks**
are real

bit.ly/pentaquarks



Backup



Systematic Uncertainties

Source	M_0 (MeV)		Γ_0 (MeV)		Fit fractions (%)			
	low	high	low	high	low	high	$\Lambda^*(1405)$	$\Lambda^*(1520)$
Extended vs. reduced	21	0.2	54	10	3.14	0.32	1.37	0.15
Λ^* masses & widths	7	0.7	20	4	0.58	0.37	2.49	2.45
Proton ID	2	0.3	1	2	0.27	0.14	0.20	0.05
$10 < p_p < 100$ GeV	0	1.2	1	1	0.09	0.03	0.31	0.01
Non-resonant	3	0.3	34	2	2.35	0.13	3.28	0.39
Separate sidebands	0	0	5	0	0.24	0.14	0.02	0.03
J^P ($3/2^+$, $5/2^-$) or ($5/2^+$, $3/2^-$)	10	1.2	34	10	0.76	0.44		
$d = 1.5 - 4.5$ GeV^{-1}	9	0.6	19	3	0.29	0.42	0.36	1.91
$\ell_{\Lambda_b}^{P_c} \Lambda_b \rightarrow P_c^+ (\text{low/high}) K^-$	6	0.7	4	8	0.37	0.16		
$\ell_P P_c^+ (\text{low/high}) \rightarrow J/\psi p$	4	0.4	31	7	0.63	0.37		
$\ell_{\Lambda_b}^{\Lambda_c^*} \Lambda_b^* \rightarrow J/\psi \Lambda^*$	11	0.3	20	2	0.81	0.53	3.34	2.31
Efficiencies	1	0.4	4	0	0.13	0.02	0.26	0.23
Change $\Lambda^*(1405)$ coupling	0	0	0	0	0	0	1.90	0
Overall	29	2.5	86	19	4.21	1.05	5.82	3.89
sFit/cFit cross check	5	1.0	11	3	0.46	0.01	0.45	0.13



Pre Selection

Table : Pre-selection requirements used. The stripping line is FullDSTDiMuonJpsi2MuMuDetachedLine.

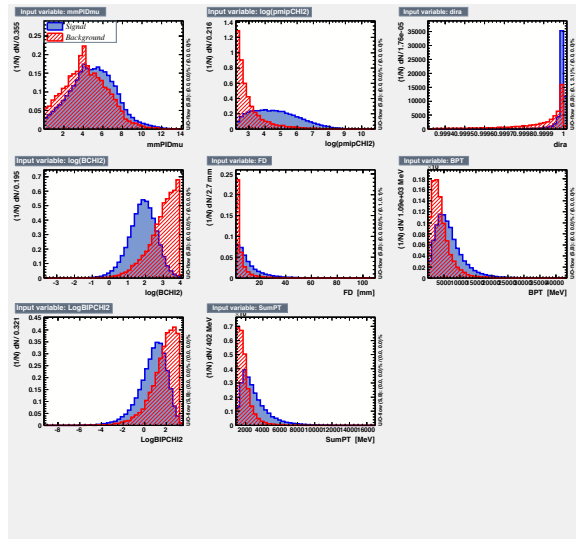
#	Selection variables	Requirements
1	All tracks χ^2/ndof	< 4
2	Muon PID	$\text{DLL}(\mu - \pi) > 0$
3	PT of muon	$> 550 \text{ MeV}$
4	PT of hadron	$> 250 \text{ MeV}$
5	J/ψ vertex χ^2	< 16
6	J/ψ mass window	$-48 < m(\mu^+\mu^-) - m(J/\psi) < 43 \text{ MeV}$
7	Hadron χ_{IP}^2	> 9
8	K^- ID	$\text{DLL}(K - \pi) > 0$ and $\text{DLL}(p - K) < 3$
9	p ID	$\text{DLL}(p - \pi) > 10$ and $\text{DLL}(p - K) > 3$
10	pK^- vertex χ^2	$\text{DOCA } \chi^2 < 16$
11	Λ_b χ_{IP}^2	< 25
12	Λ_b vertex χ^2/ndof	< 10
13	Λ_b flight distance	$> 1.5 \text{ mm}$
14	Λ_b pointing, $\cos \theta_p$	> 0.999
15	Trigger	HLT1 and HLT2 TOS on J/ψ (see text)
16	Clone track rejection on hadron	Ghost probability < 0.2



BDT Classifier

BDT variables:

- minimum DLL($\mu - \pi$) of the μ^+ and μ^- (mmPIDmu);
 - minimum of the χ^2_{IP} of the K^- and the p [log(pmipCHI2)];
 - Λ_b (DIRA);
 - $\Lambda_b \chi^2_{IP} \log(\text{BCHI2})$;
 - Λ_b FD;
 - PT of the Λ_b (BPT);
 - Λ_b vertex χ^2 (LogBIPCHI2);
 - PT sum of the K^- and p (SumPT).
- **Trained on signal MC and sideband data for bkg**
 - **Cut optimized by maximising $S/\sqrt{S+B}$ in data, subsequently tightened to reduce background across DP**





ℓS Couplings

- The angular momentum barrier should suppress decays with high orbital angular momentum.
- Express helicity couplings through ℓS -couplings $B_{\ell S}$ using Clebsch-Gordan coefficients

$$\mathcal{H}_{\lambda_B, \lambda_C}^{A \rightarrow B C} = \sum_{\ell} \sum_S \sqrt{\frac{2\ell+1}{2J_A+1}} \times B_{\ell, S} \times \underbrace{\begin{pmatrix} J_B & J_C & S \\ \lambda_B & -\lambda_C & \lambda_B - \lambda_C \end{pmatrix}}_{\text{Spin-Spin coupling}} \times \underbrace{\begin{pmatrix} \ell & S & J_A \\ 0 & \lambda_B - \lambda_C & \lambda_B - \lambda_C \end{pmatrix}}_{\text{Spin-Orbit coupling}}$$

- Limit the allowed range of ℓ in the fit model
- Automatically implements parity conservation in strong decays by choice of ℓ



Efficiency corrected Signal PDF

- Ω = 6 kinematical variables (m_{Kp} + 5 angles)
- $\vec{\omega}$ = fit parameters (couplings, masses, widths)

$$\frac{d\mathcal{P}}{d\Omega} \equiv \mathcal{P}_{\text{sig}}(\Omega|\vec{\omega}) = \frac{1}{CI(\vec{\omega})} |\mathcal{M}(\Omega|\vec{\omega})|^2 \Phi(\Omega) \epsilon(\Omega)$$

- Phase space volume element
- efficiency
- With the normalisation calculated by MC-integration over accepted MC events

$$I(\vec{\omega}) \equiv \int \mathcal{P}_{\text{sig}}(\Omega) d\Omega \propto \frac{\sum_j w_j^{\text{MC}} |\mathcal{M}(\Omega_j|\vec{\omega})|^2}{\sum_j w_j^{\text{MC}}},$$

- weights w_j^{C} account for differences in Λ_b production kinematics and PID between simulation and data



Interference between $\Lambda_b \rightarrow J/\psi \Lambda^*$ and $\Lambda_b \rightarrow P_c K$

- Coherent sum over amplitudes, incoherent sum over external helicities
- Set Λ_b polarisation to 0

$$|\mathcal{M}|^2 = \sum_{\lambda_{\Lambda_b} = \pm \frac{1}{2}} \sum_{\lambda_p = \pm \frac{1}{2}} \sum_{\Delta\lambda_\mu = \pm 1} \left| \mathcal{M}^{\Lambda^*} + \underbrace{e^{i\lambda_\mu \alpha_\mu}}_{\mu \text{ alignment}} \underbrace{\sum_{\lambda_p^{P_c} = \pm \frac{1}{2}} d_{\lambda_p^{P_c}, \lambda_p}^{1/2}(\theta_p)}_{\text{proton align.}} \mathcal{M}^{P_c} \right|^2$$

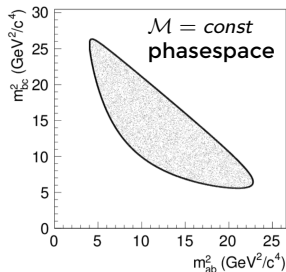


Reminder: 3-body decays and Dalitz-Plots

all particles spin 0:

$$X \rightarrow ABC$$

$$\Gamma \propto |\mathcal{M}|^2 dm_{AB}^2 dm_{BC}^2$$



plots by Antimo Palano

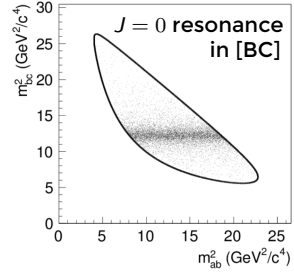
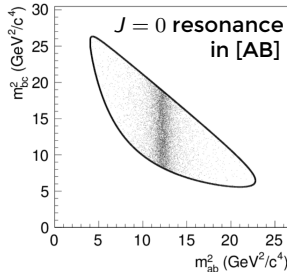
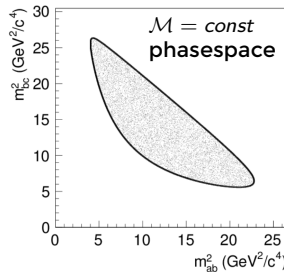


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plots by Antimo Palano

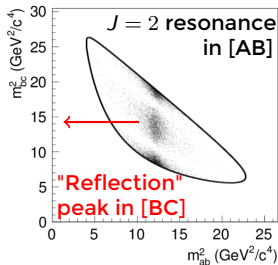
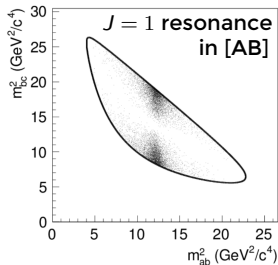
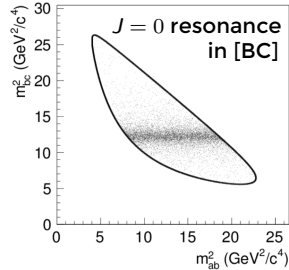
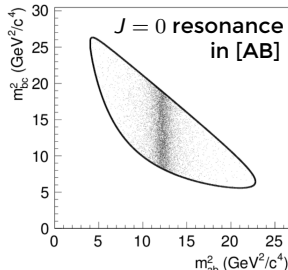
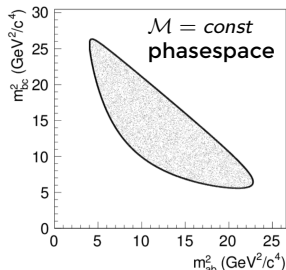


Reminder: 3-body decays and Dalitz-Plots

all particles spin 0:

$$X \rightarrow ABC$$

$$\Gamma \propto |\mathcal{M}|^2 dm_{AB}^2 dm_{BC}^2$$



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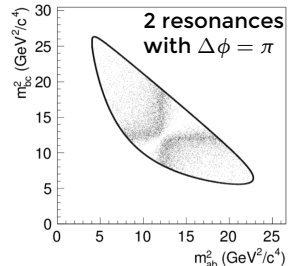
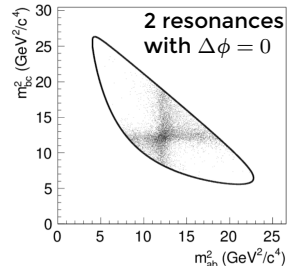
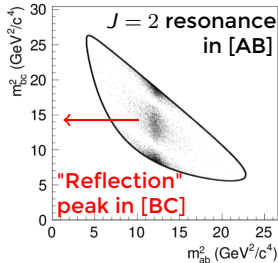
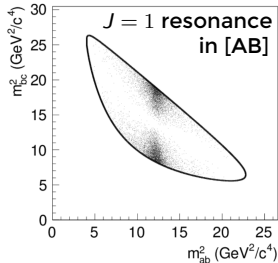
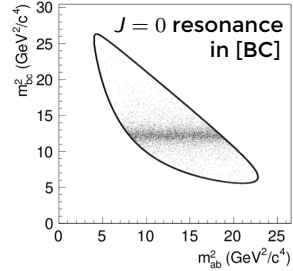
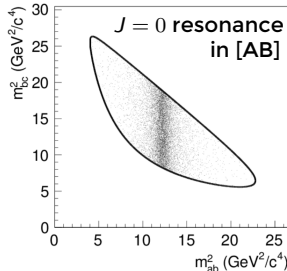
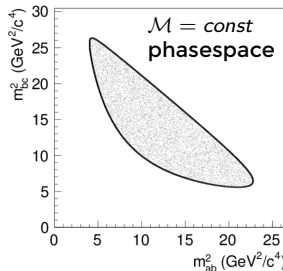


Reminder: 3-body decays and Dalitz-Plots

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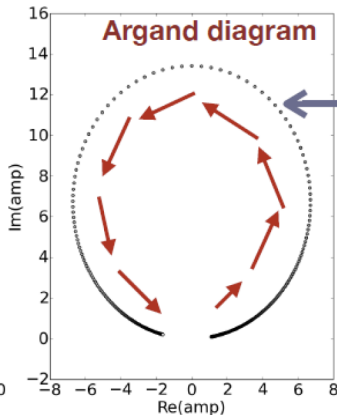
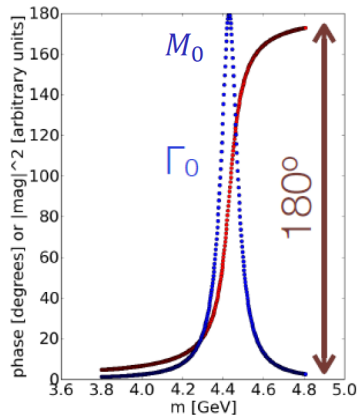
$$\Gamma \propto |\mathcal{M}|^2 dm_{AB}^2 dm_{BC}^2$$



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Phasemotion of Breit-Wigner Resonances



- Circular trajectory in complex plane is characteristic of resonance
- Circle can be rotated by arbitrary phase
- Phase change of 180° across the pole