

"Beam Dynamics meets Diagnostics" Workshop 4-6 November 2015, Florence, Italy.

Session Storage Ring and lepton machines

Analytical and numerical non-linear beam dynamics optimization



Contents

Ultra-Low Emittance Ring

- Quick overview
- Challenges in term of beam dynamics
- Figures of Merit

Tools and methods for Optimization of nonlinear dynamics Focus: Single particle dynamics and transverse beam dynamics

- Tracking codes for storage rings
- Frequency Map Analysis (FMA)
- Momentum aperture & Touschek lifetime
- Resonance Driving Terms (RDTs)
- New optimization method via genetic algorithms (GA)
- **Conclusions and perspectives**





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Quick overview Challenges in term of beam dynamics Figures of Merit

LOW-EMITTANCE RINGS



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Ultra-Low Emittance Ring: reducing the horizontal emittance

Transverse emittance control

H-emittance given by lattice •

NCHROTRON

V-emittance control by coupling •

Light Sources	Colliders	Damping Rings								
High flux Spectral brightness High transverse coherence	Increase luminosity ~2 nm•rad (SuperB HER, superKEKB)	Low emittance for injecting in colliders								
5-500 pm•rad/1 pm•rad B > 10^{22} - 10^{23} ph/s/mm ² /	L > 10^{36} cm ⁻² s ⁻¹	ILC (500pm/2 pm•rad), CLIC (100 pm•rad/1 pm)								
mrad ² /0.1%BW										
$B \propto \frac{N_{ph}}{dt \epsilon_x \epsilon_z} 0.1\% \Delta \lambda / \lambda \qquad L \propto \frac{n_b f_{rev} N_1 N_2}{\epsilon_x k \beta^*}$										
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BRILLANCE = Figure of Merit for a new class of light Sources: Diffraction Limited Light Sources (DLSR)

$$B_n(\lambda) = \frac{F_n(\lambda)}{(2\pi)^2 (\Sigma_x \Sigma_z) (\Sigma'_x \Sigma'_z)}$$

$$F_{n} = \frac{\pi}{2} \alpha N_{u} Q_{n} (\frac{nK^{2}}{4+2K^{2}}) \frac{\Delta \omega}{\omega} \frac{I}{e}$$

$$\Sigma_{x,z} = \sqrt{\sigma_{r}^{2} + \sigma_{x,z}^{2}(e^{-})} \qquad \Sigma_{x,z}^{'} = \sqrt{\sigma_{r}^{'2} + \sigma_{x,z}^{'2}(e^{-})}$$

$$\varepsilon_{x,z} (e^{-}) = \sigma_{x,z} (e^{-}) \sigma_{x,z}^{'} (e^{-})$$

$$\sigma_{x,z} = \sqrt{\varepsilon_{x,z}} \beta_{x,z} \qquad \sigma_{x,z}^{'} = \sqrt{\frac{\varepsilon_{x,z}}{\beta_{x,z}}}$$

$$\varepsilon_r(\lambda) = \sigma_r(\lambda)\sigma'_r(\lambda) = \frac{\lambda}{4\pi}$$

Single electron emittance: Diffraction limit

(Gaussian beam)

8 pm rad - 10 keV

(cas le plus simple.)

Optimum brilliance is obtained when electron beam and photon beam ellipses match In both planes (specific β function for adaptation))

$$B_n(\lambda) = \frac{F_n(\lambda)}{4\pi^2(\varepsilon_x + \lambda_n/4\pi)(\varepsilon_z + \lambda_n/4\pi)}$$

$$e^{-\frac{x}{x}} vs.$$

$$vs. \qquad x$$
Electron-photons ellipse matching
Electron-photons ellipse matching
$$Electron-photons ellipse matching$$

$$f(x) = \frac{F_n(\lambda)}{4\pi^2(\varepsilon_x + \lambda_n/4\pi)(\varepsilon_z + \lambda_n/4\pi)}$$

Today's light source chart



Survey of low emittance lattices



Update from R. Bartolini LER 2014





Lattice Design for LER

Hybrid Multi Bend Achromat

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Linear lattice unit cell



Multi Bend Achromat

 $\epsilon_x = C_q \frac{\gamma^2}{J_x} \frac{\oint H(s)/\rho(s)^3 \, ds}{\oint 1/\rho(s)^2 \, ds}$ Magnets types



Nonlinear lattice

Chromatic Sextupoles (2)

Harmonic Sextupoles > 5-10

Octupoles (MAX-IV, ESRF-II, etc.)

Higher multipoles



7BA

9BA

HMBA

From Simple to Complex and Compact lattices ALS case



Simple lattice with **2 independent families** of sextupole magnets to lattices with many families or individual of sextupoles, n-poles (octupole, ...) → strong nonlinearities



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Criteria for optimization



Criteria for optimization and limitations



Optimization tool progress of the last decades



Non-linear dynamics What is included in the Model? Tracy II & MADX/PTC track exact (SOLEIL)

- Systematic multipole errors
 - Large momentum acceptance, large dispersion function \rightarrow high order multipoles
- From magnetic measurements:
 - Add true m-poles (both systematic and non systematic)
 - Dipole: fringe field, gradient error, edge tilt errors
 - Quad .: fringe field
- Beam based
 - Multipoles deduced from turn by turn measurement, off-axis field integrals
 - Coupling errors
- Insertion devices
 - Taylor expansion
 - Radia kick maps
 - Sorting magnets: Genetics algo.

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Collective effects

NCHROTRON



- Tracking codes for storage rings
- Frequency Map Analysis (FMA): concept true for model and online measurements

TOOLS AND FOR OPTIMIZATION OF NONLINEAR DYNAMICS



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Tracking codes for numerical simulations

- Long term tracking based on symplectic integrators
 - Implicit or explicit schemes
- Popularized by Ruth and Forest 1983-1990, use of Lie Algebra (Neri, 1988), Yoshida techniques (1990), Channel and Scovel (1990), Mclachlan (1995), Sanz-Serna (1998), Laskar integrators (2001)

SABAC

- Preserves energy, bounded errors,
- Phase stability
- Used by MADX/PTC, Tracy, OPA, LEGO, ELEGANT, etc.



A brief History of Frequency Map Analysis (FMA)

- For many centuries, the motion of planets in the Solar System was considered as perfectly regular.
- In 1988, J. Laskar (Paris Observatory) published evidence of chaotic motion in the Solar Systems using a new method called Frequency Map Analysis (FMA).
- FMA was successively applied to the study of dynamics systems such as (short list)
 - Stability of Earth Obliquity and climate stabilization (Laskar, Robutel, 1993)
 - Standard application (Laskar, Floeschlé, Celleti, 1992, Laskar and Carletti 2000)
 - Galactic Dynamics (Papaphilippou et Laskar, 1996 and 1998)
 - Accelerator beam dynamics: lepton and hadron storage rings (Dumas, Laskar, 1993, Laskar, Robin, 1996, Papaphilippou, 1999, ...)



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Computing a frequency map





Frequency Map Analysis: ALS and BESSY-II

6.75

Qy

P. Kuske (BESSY-II)

BESSY-II with harmonic sextupole

magnets, chromaticity, coupling

6.75

Qu

ALS linear lattice corrected to 0.5% rms β -beating

FM computed including residual β-beating and coupling errors

NCHROTRON



- fringe fields: dipole, quadrupole (and sextupole) magnets
- systematic octupole components in quadrupole magnets
- decapoles, skew decapoles and octupoles in sextupole magnets

Courtesy C. Steier (ALS) P. Kuske (BESSY-II)

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Off momentum dynamics



The SOLEIL energy acceptance of the bare machine is large : +/- 4%. **Agreement of a few percents (typically a factor two 20 years ago)** Complete optimized linear and non-linear model



Resonance Driving Terms (RDTs)

ANALYTICAL OPTIMIZATION



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The "standard method" for sextupole optimization

J. Bengtsson, *The sextupole scheme for the SLS: an analytic approach,* Internal report SLS-TME-TA-1997-12

a) get the sextupole [+quadrupole] Hamiltonian:

$$\Rightarrow \int_{\text{cell}} [H_2(s) + H_3(s)] \, ds = \sum h_{jklmp} \text{ with } \text{Resonances}$$

$$h_{jklmp} \propto \sum_n^{N_{\text{sext}}} (b_3 L)_n \, \beta_{xn}^{\frac{j+k}{2}} \, \beta_{yn}^{\frac{l+m}{2}} \, D_n^p \, e^{i\{(j-k)\phi_{xn} + (l-m)\phi_{yn}\}}$$

$$\text{Resonant Driving } - \left[\sum_n^{N_{\text{quad}}} (b_2 L)_n \, \beta_{xn}^{\frac{j+k}{2}} \, \beta_{yn}^{\frac{l+m}{2}} \, e^{i\{(j-k)\phi_{xn} + (l-m)\phi_{yn}\}} \right]_{p \neq 0}$$

$$h = \sum_{n}^{N_{\text{sext}}} V_n e^{i\Phi_n} \ [+\dots \text{ quads for } p \neq 0 \dots]$$

Sextupole_n \leftrightarrow complex vector: Length $V_n = V_n (b_3, L, \beta_x, \beta_y, D)$ Angle $\Phi_n = \Phi_n (\phi_x + \phi_y)$ • $\Phi_n = 0 \forall n \rightarrow$ tune shifts • $\Phi_n \neq 0 \rightarrow$ resonances Laurent S. Nadolski Beam Dynamics meets Diagnotics, 4-6 Nov 2015 24 ... 9 first order sextupole terms: adjust 2 real, suppress 7 complex...

First order sextupole [+quadrupole] Hamiltonian

- \bullet 2 phase independant terms \rightarrow chromaticities:
 - $\begin{aligned} h_{11001} &= +J_x \delta \left[\sum_{n}^{N_{sext}} (2b_3 L)_n \beta_{xn} D_n \sum_{n}^{N_{quad}} (b_2 L)_n \beta_{xn} \right] &\to \xi_x \\ h_{00111} &= -J_y \delta \left[\sum_{n}^{N_{sext}} (2b_3 L)_n \beta_{yn} D_n \sum_{n}^{N_{quad}} (b_2 L)_n \beta_{yn} \right] &\to \xi_y \end{aligned}$
- 7 phase dependant terms \rightarrow resonances: $h^N := h$ for N cells, $N \rightarrow \infty \implies$



... still not the end: 13 more terms in 2nd order: 5 real, 8 complex (Pandora's box has a false bottom!)

Second order sextupole [+first order octupole] Hamiltonian

 $\sum_{n} \sum_{m} (b_3 L)_n (b_3 L)_m \times (\beta_n, \phi_n \beta_m, \phi_m \ldots) + \left[\sum_{q} (b_4 L)_q \times (\beta_q, \phi_q \ldots) \right]$

- 3 phase independant terms \rightarrow amplitude dependant tune shifts: $\frac{\partial Q_x}{\partial J_x} \quad \frac{\partial Q_x}{\partial J_y} = \frac{\partial Q_y}{\partial J_x} \quad \frac{\partial Q_y}{\partial J_y}$
- 2 phase independant off-momentum terms \rightarrow second order chromaticities:

$$\xi_{x/y}^{(2)} = \frac{\partial^2 Q_{x/y}}{\partial \delta^2}$$

- 8 phase dependant terms
 - \rightarrow octupolar resonances:

$$\begin{array}{ll} h_{40000} \to 4Q_{x} & h_{31000} \to 2Q_{x} \\ h_{00400} \to 4Q_{y} & h_{20110} \to 2Q_{x} \\ h_{20200} \to 2Q_{x} + 2Q_{y} & h_{00310} \to 2Q_{y} \\ h_{20020} \to 2Q_{x} - 2Q_{y} & h_{01110} \to 2Q_{y} \end{array}$$





Tool for sextupole optimization (OPA)

Analytical expressions for 1st and 2nd Hamiltonian modes. (*J.Bengtsson*)

Numeric differentiation for 1st,2nd,3rd chromaticity

 $\frac{\Sigma \ (b_3 l \)^2}{\text{included in}}$ included in minimization

ICHROTRO

	🍪 Chroma												
		Target	Value			Weigh	t	inc	ξI	Name		K [1/m2]	lock
	CrX lin	5.00	4.90			0.0	+		☑	SD	<< <	-4.978	> >> res off 🗹
	Cr¥ lin	5.00	5.06			0.0	÷			SE	<< <	-2.002	> >> res off
d	Qx	H21000	29.92			- 7.0	+		•	SF	<< <	4.652	> >> res off 🗹
	3Qx	H30000	5.57			- 7.0	+			SLA	<< <	-7.104	> >> res off
	Qx	H10110	28.12			7.0	±			SLB	<< <	2.860	> >> res off
	Qx-2Qy	H10020	8.00			7.0	<u>+</u>			SMA	<< <	-3.760	> >> res off
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-	dQyy	0.00	-627.70			- 8.0	+				w. /	11. /	
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	4Qx	H40000	2196.30			- 3.0	+				And I		
	2 Qx	H20110	4036.61			- 3.0	+					We	
	2Qy	H11200	8725.54			4.0	+		-				
	2Qx-2Qy	H20020	32673.46		<u> </u>	- 3.0	+			and the second sec			
	2Qx+2Qy	H20200	10592.53			- 3.0	+			- Ser /			
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		Laurent S. N	ladolski	Beam Dyna	amics mee	ets Dia	and	ICS.	4-1	6 Nov. 20)15		27
		0						1	ŧ.	m			

Cancellation of All Geometric 3rd and 4th at design level **Resonances Driven by Strong Sextupoles** except $2v_x - 2v_y$

PEPX lattice

Key: Phase advance between sextupoles



Frequency Analysis of betatron motion

Example: Spectral Lines for tracking data for the Diamond lattice



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Comparison real lattice to model linear and nonlinear optics

Courtesy R. Bartolini

Frequency Maps and amplitudes and phases of the spectral line of the betatron motion can be used to compare and correct the real accelerator with the model



BINCHNOINON

Optimization:

Parameter space large (ten-hundreds of parameters) How to ensure the optimal solution was found? Analytical is often a first step in the optimization process Subtleties of beam dynamics (on/off-momentum, symmetry)

- 1. Exhaustive search for all stable solutions
- 2. Genetic Algorithm based optimization

NUMERICAL OPTIMIZATION



Lattice optimization

GLASS – Global Linear Analysis of All Stable Solutions

•Scan for optimum lattice solution for highly periodic lattices (few parameters)

D. Robin, et al., Physical Review Special Topics 024002 (2008)

•A billion of lattices scanned with 3 quadrupole and 2 sextupole families

•After 1 day of computation, 1 million of stable solutions

- •Then compute main properties of these solutions to build up a large exhaustive database
- •Solutions sorted by emittance values, tunes, DA sizes,
- momentum apertures but also brilliance

Give a global view of the lattice, very practical



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Genetics Algorithms based optimization

- Exhaustive and global scanning is not possible in a finite for most 3GLSs
- Indeed large number of parameters (~tens families of quadrupoles, of sextupoles, individual. Power supplies)
- Genetic algorithms are a very promising solution
 - 1. Based on direct tracking or real tracking
 - 2. Open new optimization windows
 - 3. Give solutions never thought about
 - 4. Beam-based checked
- Early work started since around 10 years at APS and followed by over laboratories and starts to give practical results in simulation and/or online.
- APS (M. Borland et al), ALS, BNL, SIRIUS, SOLEIL, SLS, ... (all facilities)



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Genetic algorithm based optimizations for accelerators

• Evolutionary algorithms (1971-today)

Various classes of algorithms

- Single/multi-objective types
- Dominant/non dominant sorting (SPEA2, PESA, NGSA-II, ...)
- Pareto front optimality
 - Multi-objective Genetic Algorithm (MOGA)
 - Multi-objective Particle Optimization Algorithm (MOPSOA) 1995
- Modern GA implementation (OPAL)

Interesting Recent PhD dissertations

- O. Roudenko, Application des algorithmes évolutionnaires aux problèmes d'optimisation multi-objectif avec contraintes pastel-00000967 (2010).
 - Y. Ineichen, Toward Massively Parallel Multi-Objective Optimization With Application To Particle Accelerators DISS. ETH NO. 21114 (2013)



Principal of GA

Objectives: MA, DA, emiitance... Begin The general form of an optimization problem Optimization Initialize Population t=0 **Minimize**/Maximize $f_m(x)$, $m = 1, 2, \ldots, M;$ $g_j \ge 0,$ j = 1, 2, ..., J; $h_k(x) = 0,$ k = 1, 2, ..., K;subject ± (1) No Condition ? Evaluation V Yes $x_i^{(L)} \leq x_i \leq x_i^{(U)}, \quad i = 1, 2, \dots, N;$ Assign Fitness Stop Constraints: beta-function. Variables: strength of phase advance, Reproduction quadrupoles and tunes. sextupoles chromaticities t=t+1 Crossover high x_2^* Pareto front Mutation Lifetime x_1^* **Contradictory objectives x**4 $|x_0^*|$ **Optimal solution** low \dagger low Dyn. Apert. high aurent S. Nadolski Y. Ineichen ETH-Diss 21114, 2013 37 NCHROTRON

CPU, GPU farms

ALS Simultaneous Linear and Nonlinear Optimization



Online optimization for nonlinear dynamics

Diagnostics: proxies for dynamic aperture and lifetime

- Injection efficiency
- Lifetime
- Beam loss rate

▶ ...



Robust Conjugate Direction Search (RCDS)

- SPEAR 3

- Applied to coupling, top-off transient, LCLS undulator taper, etc...
- X. Huang, J. Corbett, J. Safranek, J. Wu, NIMA (2013)
- Dynamic aperture increase >3.5 mm X. Huang et al., PRSTAB 18, 084001 (2015)

ESRF (N. Carmignani, LER2015)

- 16 bunch operation: Improvement of lifetime 16.5 \rightarrow 20 h
- Single bunch in hybrid mode: bunch current threshold 4 \rightarrow 8 mA/bunch



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Conclusion and perspectives

• Nonlinear beam dynamics optimization is still a challenging task

• Theory

- Mature and modern tools
- Refined and accurate models (based on magn. measurements, alignment)

• Beam based Experiments and quality of diagnostics (ease of use)

- Mandatory to cross-check/benchmark our model vs experiment
 - Model upgrade, unexpected effects, difficult to model quantities, etc.
- <u>Online capability to explore nonlinear dynamics (tune shift, DA, MA, etc.)</u>
 - BPMs are our eyes
 - Single, collective beam dynamics
 - TbT BPMs, Bunch per Bunch
 - Small/large beam charge, off-axis beam position, many/few turns
 - Online optimization (RDTs, GA, Injection, Lifetime)
 - <u>Continuous monitoring (feedback, alive machine with insertion devices free</u> controlled by users for instance)



Tribute to Michel SOMMER

We have the very big sadness to announce you the death of Michel SOMMER, arisen on August 4th, 2015, at the age of 80.

He was an accelerator physicist of international renown, expert in electron beam dynamics in storage rings and in synchrotron radiation production.

He was working in the French LURE laboratory, and was involved in the design, construction and operation of many storage rings in France : ACO, DCI, ESRF, Super-ACO, SOLEIL, but also in other countries : Italy, Germany, Brazil, Taiwan, Korea, Jordan...

Above all, Michel Sommer was an open and cultivated man.





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Thank you for your attention

