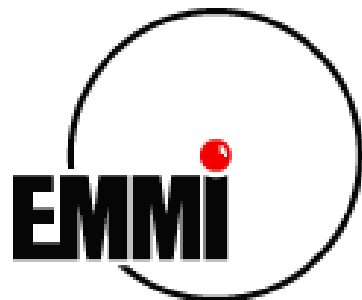


# Flavor fluctuations and their relevance to the understanding of hadronization

R. Bellwied (University of Houston)

Thanks to:

C. Ratti, S. Jena, D. McDonald (University of Houston)  
P. Alba, V. Mantovani (Torino University & INFN)  
M. Bluhm, M. Nahrgang (North Carolina & Duke)  
S. Borsanyi, Z. Fodor, S. Katz (Wuppertal & Budapest)



**EMMI Workshop: Imprints of the QGP**

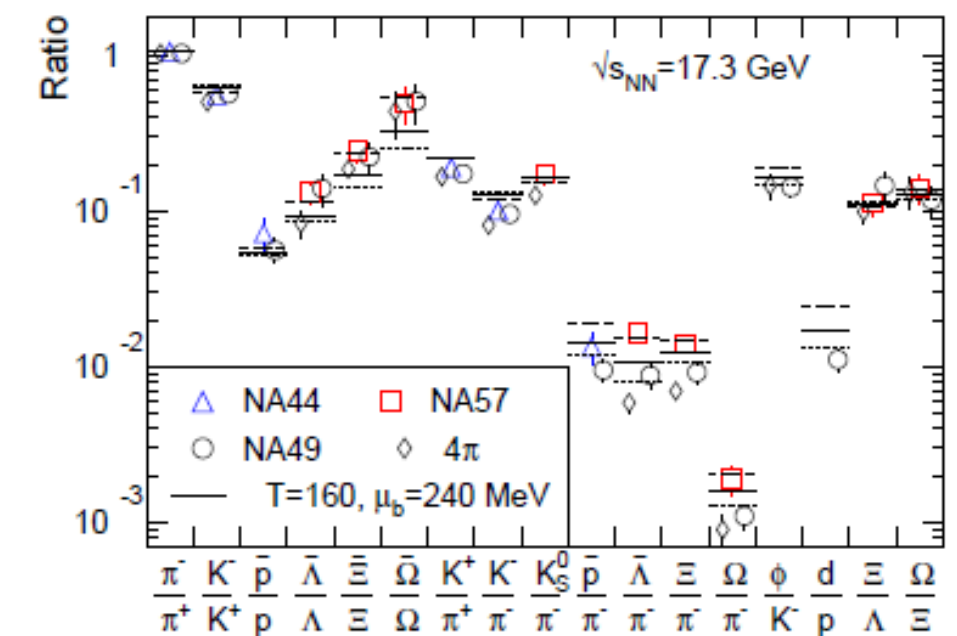
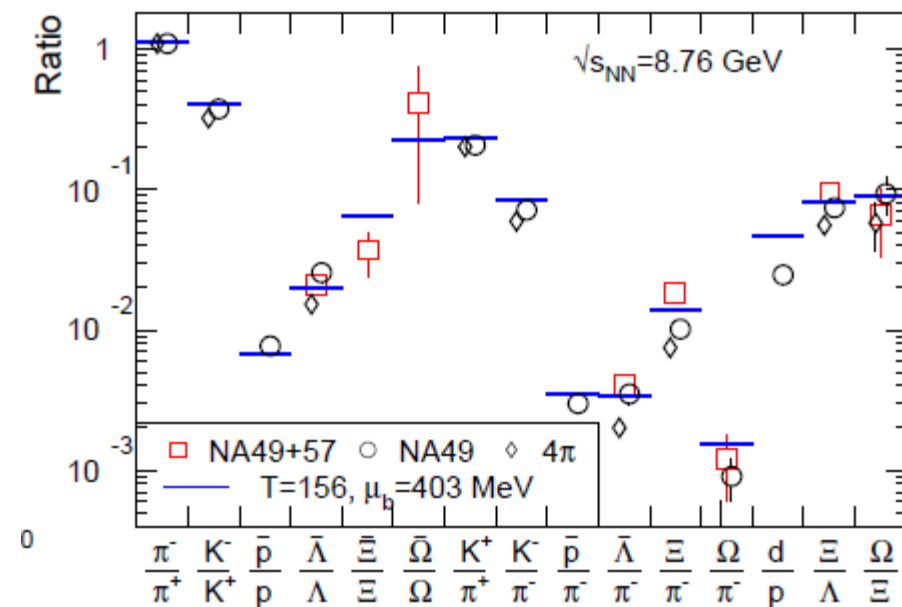
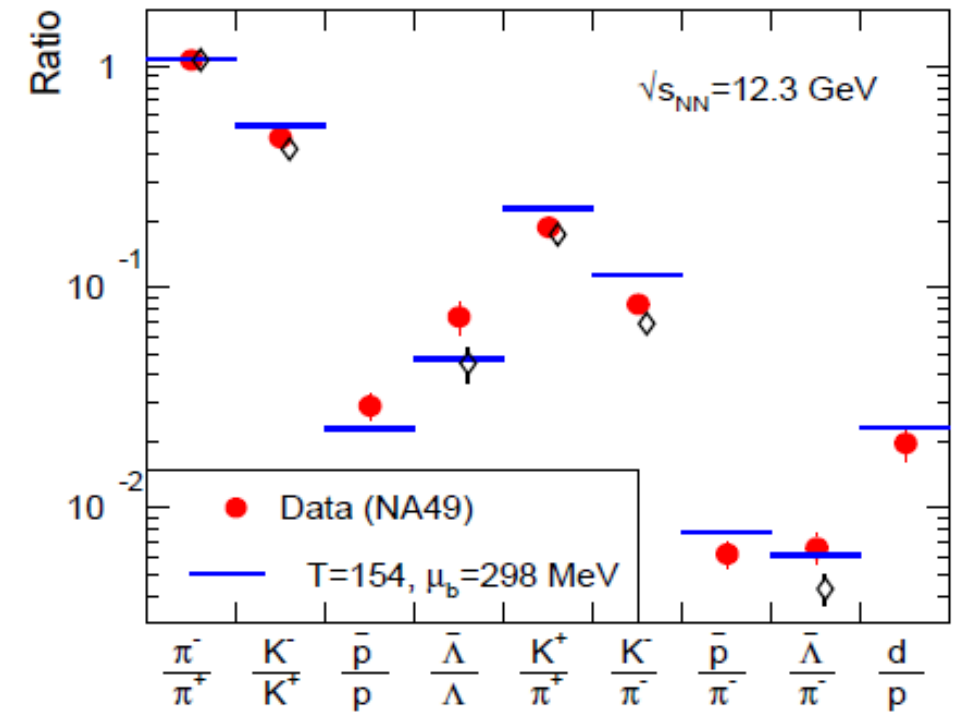
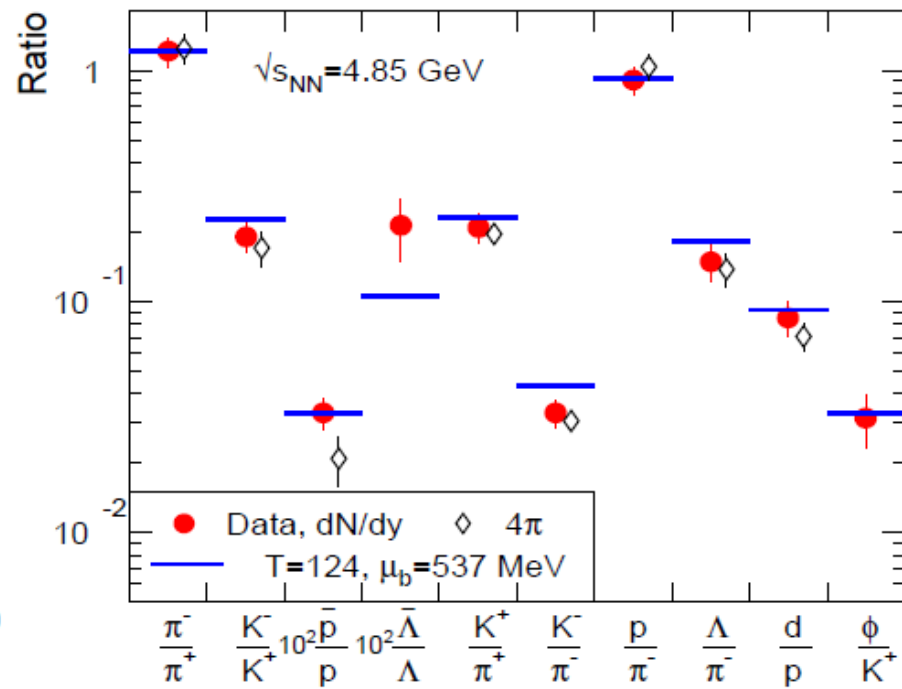
16-17 April 2015

MPI for Nuclear Physics & Heidelberg University

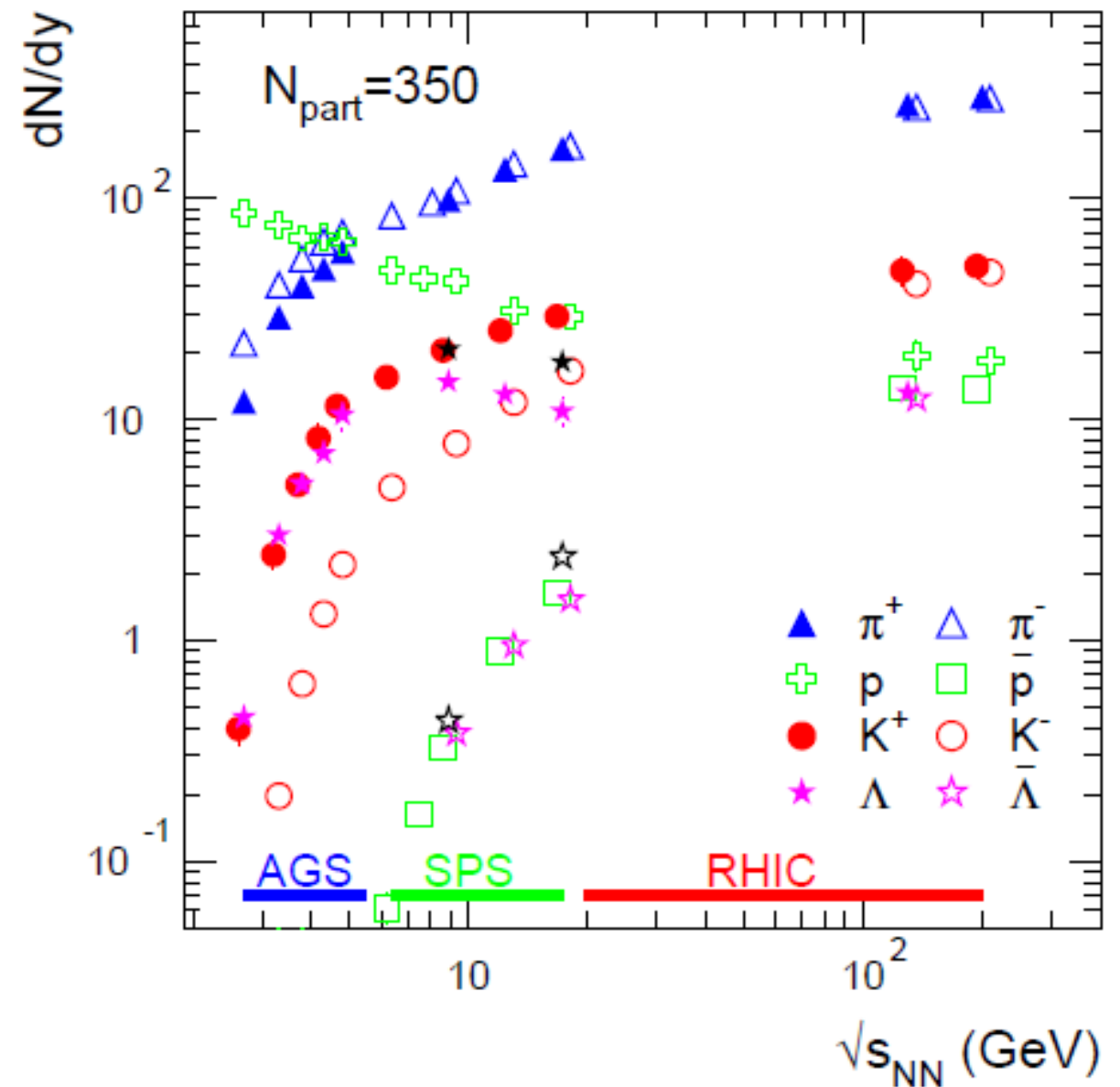
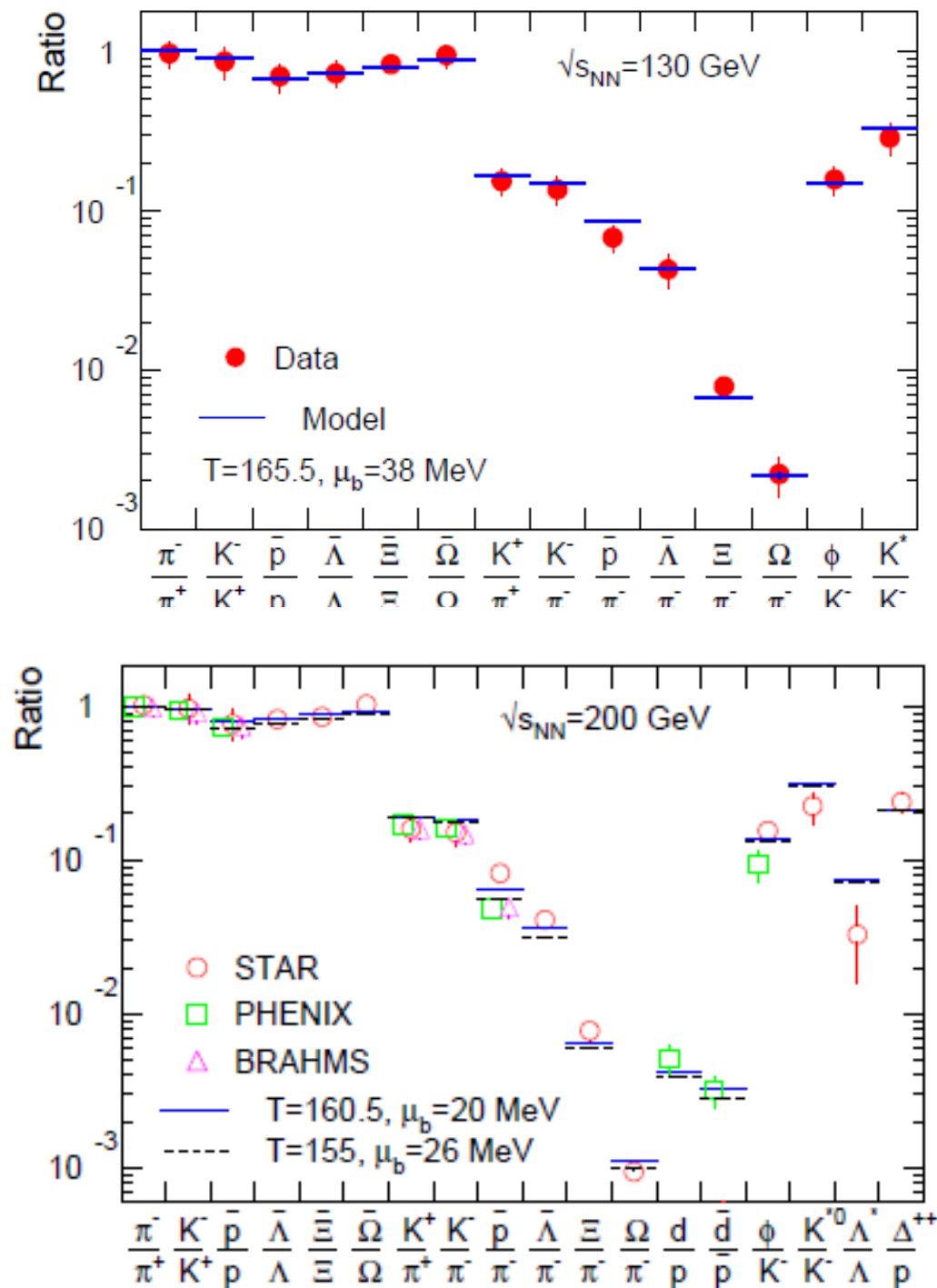
# Outline

- History of The Statistical Hadronization Model
- Recent input from lattice QCD on the issue of hadronization
- The role of flavor during the transition / HRG model input
- New measurements: fluctuations in addition to yields & ratios
- Experimental verification of lattice predictions
- Where do we go, what does it mean ?

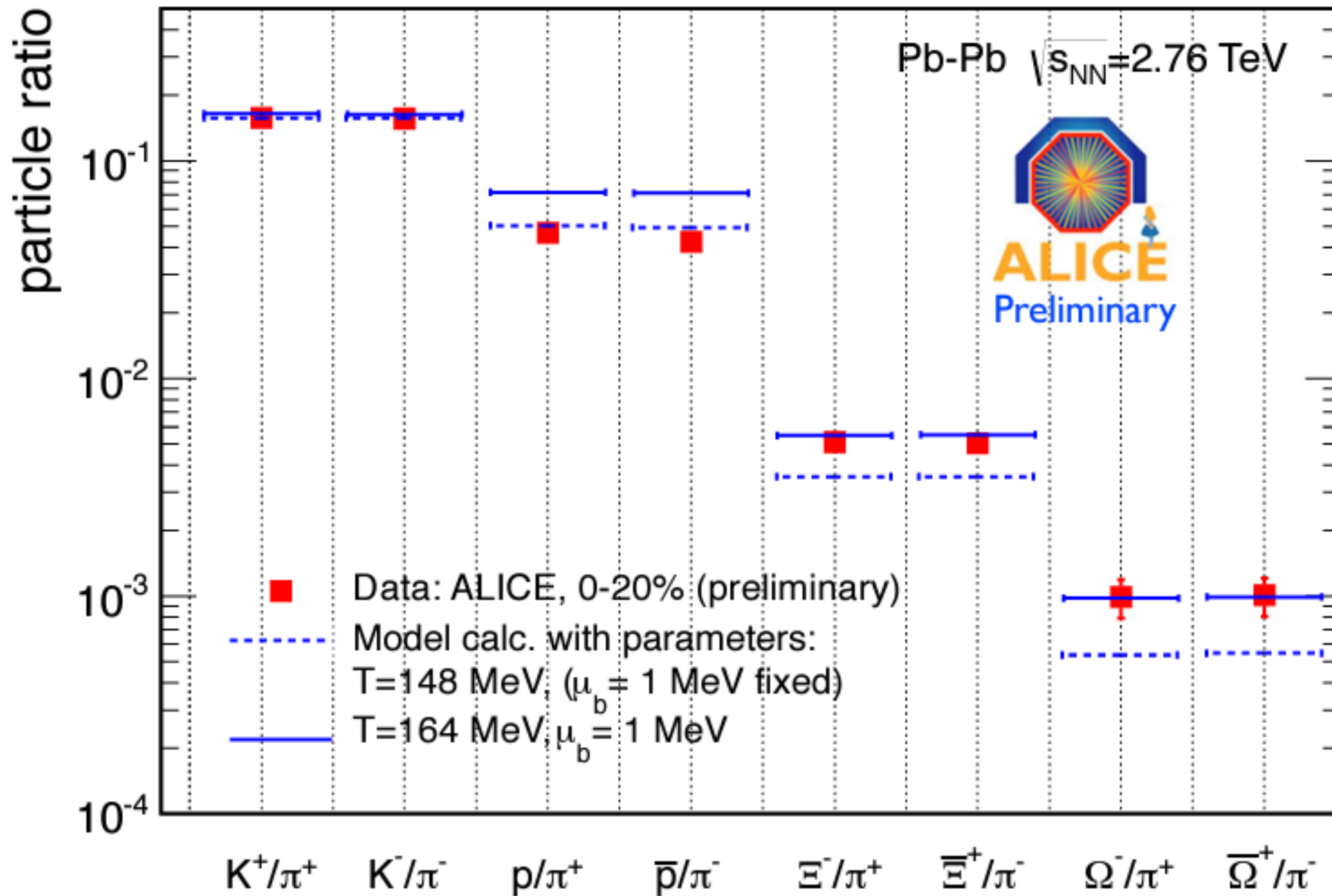
# The impressive success of SHM over many decades & energy regimes (JS, PBM, Xu, Wessels, Magestro, Andronic,....)



# The impressive success of SHM over many decades & energy regimes (JS, PBM, Xu, Wessels, Magestro, Andronic,....)



# SHM model comparison based on ratios including multi-strange baryons



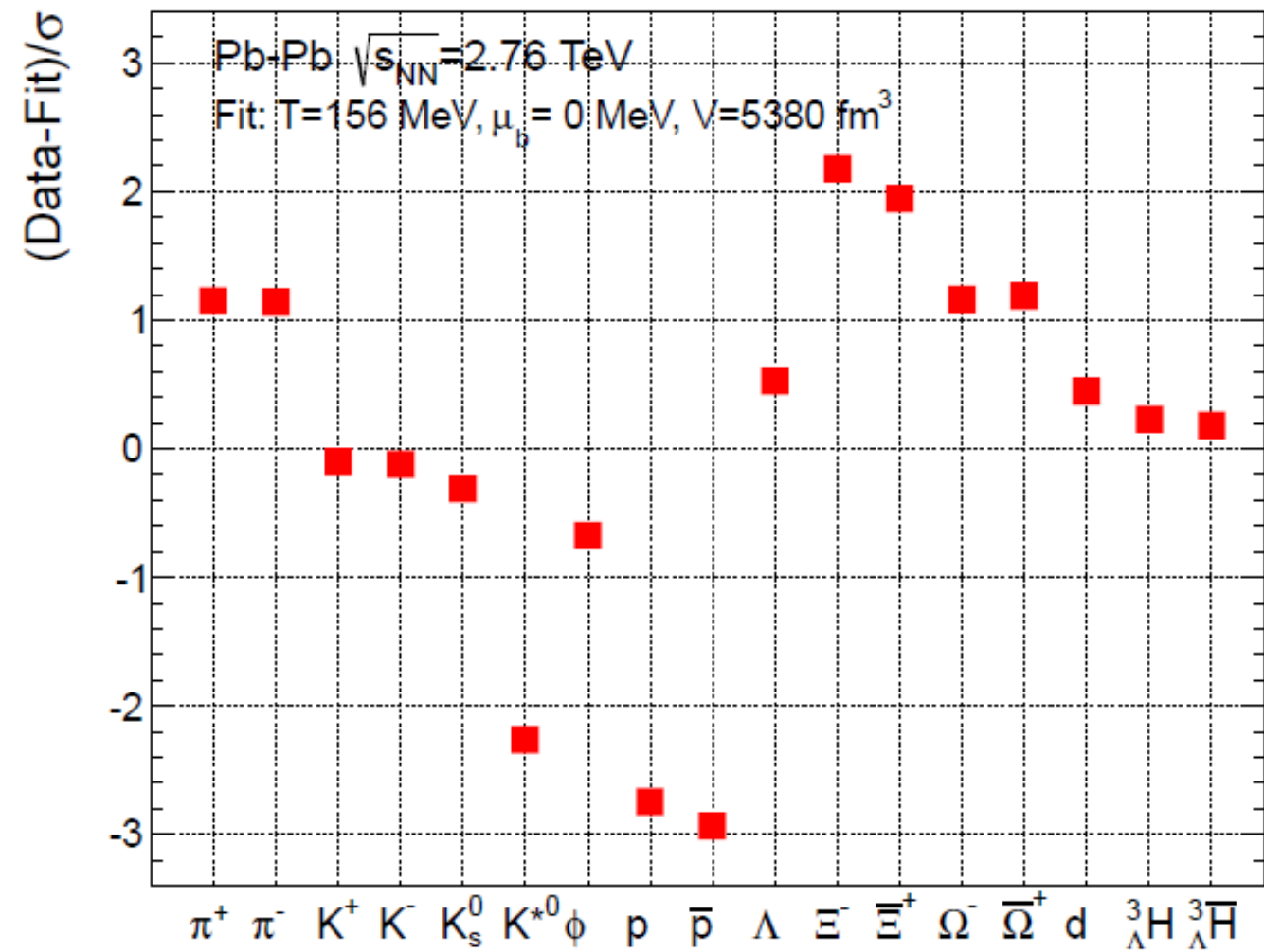
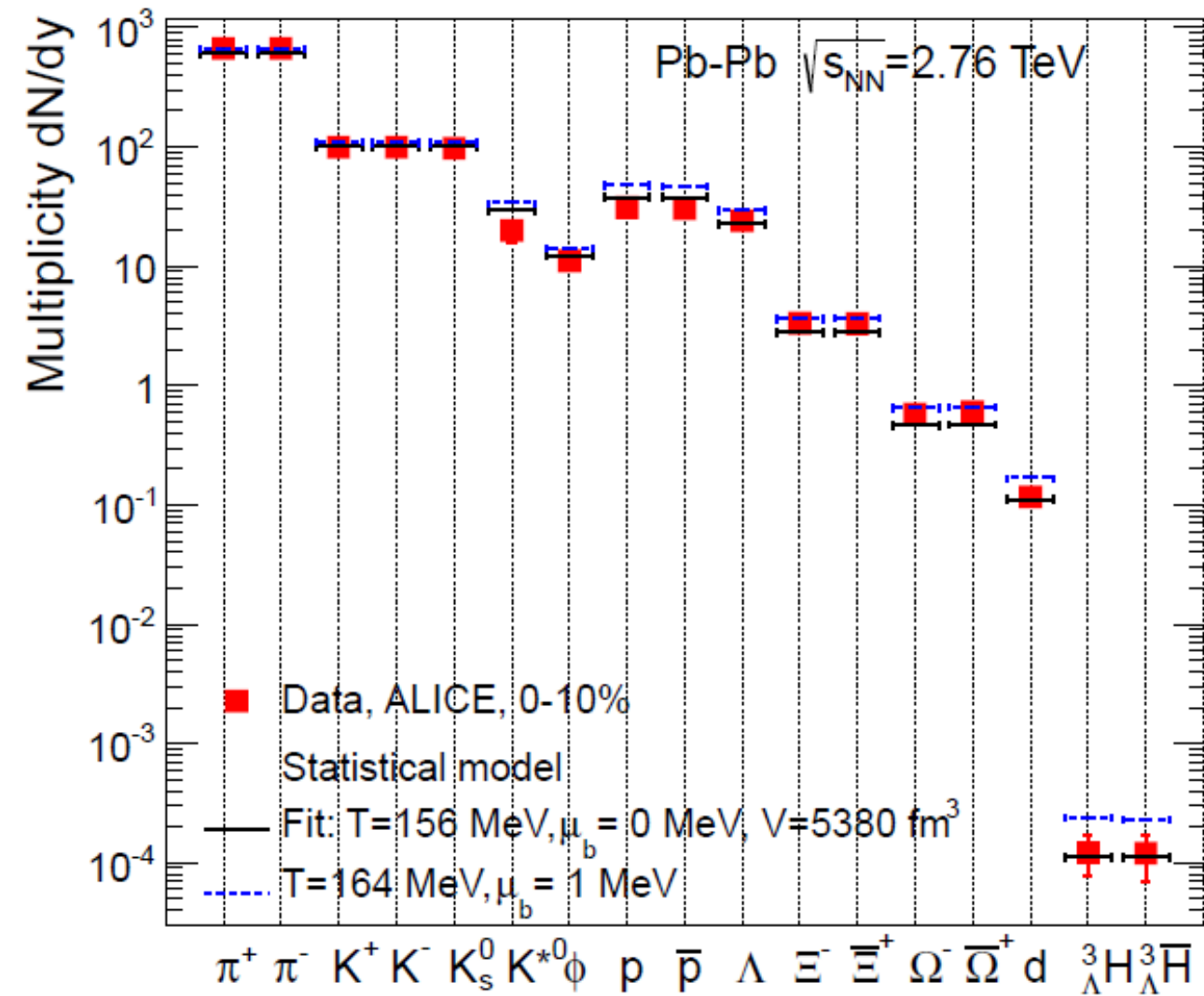
R. Preghenella  
for ALICE  
SQM 2012  
arXiv:1111.7080  
Acta Phys. Pol.

## Ratios or Yields ?:

Ratios are less sensitive to biases and do not require the volume parameter

Yields might be more sensitive to determine freeze-out parameters

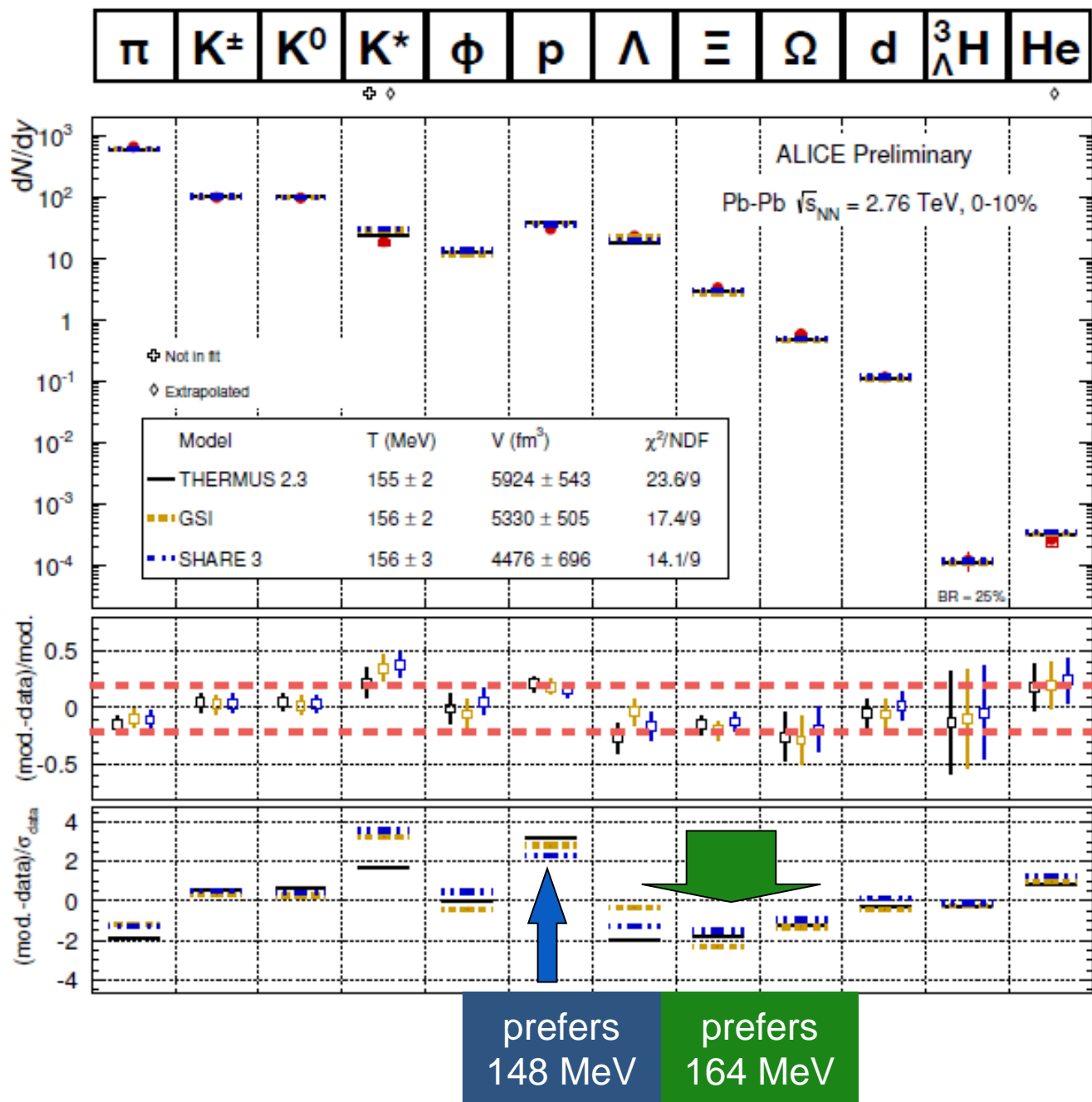
# The latest on the ALICE fits



J. Stachel, arXiv:1311.4662



# SHM model comparison based on yields including multi-strange baryons



This looks like a good fit, but it is not  $\chi^2/\text{NDF}$  improves from 2 to 1 when pions and protons are excluded.

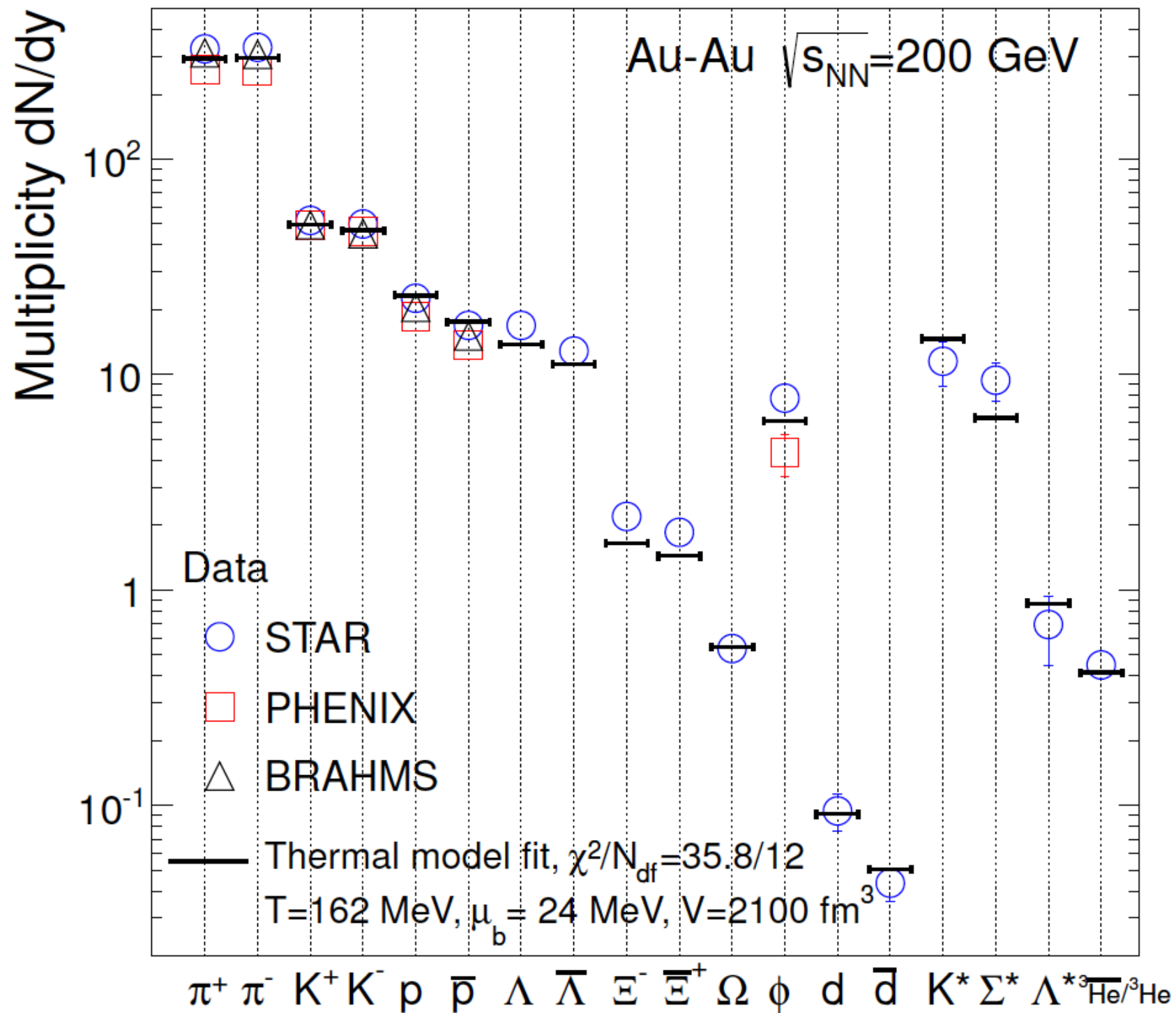
Fit to pions and protons alone yield a temperature of 148 MeV.

Several alternate explanations:

- Inclusion of Hagedorn states
- Non-equilibrium fits
- Baryon annihilation
- *Different  $T_{ch}$  for light and strange*

Is a common freeze-out surface that important? Is it supported by lattice QCD?

# The latest 200 GeV RHIC fits based on yields



A. Andronic et al.,  
 QM 2012  
 arXiv:1210.7724



Can we add something to this picture ?

Can we go beyond yields in a static model ?

Can we make a link to first principle calculations ?

In addition to SHM let us also look at lattice QCD and compare to hadron resonance gas features just below the phase transition (Redlich, Karsch, etc.)

***Lattice QCD is also a ‘static model’ assuming thermalization (grand-canonical ensemble), but it can be calculated at every temperature.***

In addition to yields let us also look at fluctuations of net-yields to the highest possible order (variance, skewness, kurtosis).

***Lattice QCD links susceptibilities to moments of the multiplicity distribution.***

# Relating susceptibilities to moments

In a thermally equilibrated system we can define susceptibilities  $\chi$  as 2<sup>nd</sup> derivative of pressure with respect to chemical potential (1<sup>st</sup> derivative of  $\rho$ ). Starting from a given partition function we define the fluctuations of a set of conserved charges as:

$$\frac{p}{T^4} = \frac{\ln \mathcal{Z}}{VT^3} \quad \chi_{lmn}^{BSQ} = \frac{\partial^{l+m+n} (p/T^4)}{\partial (\mu_B/T)^l \partial (\mu_S/T)^m \partial (\mu_Q/T)^n}$$

The fluctuations of conserved charges are related to the moments of the multiplicity distributions of the same charge measured in HIC.

$$\delta N = N - \langle N \rangle$$

mean:  $M = \langle N \rangle = VT^3 \chi_1,$

variance:  $\sigma^2 = \langle (\delta N)^2 \rangle = VT^3 \chi_2,$

skewness:  $S = \frac{\langle (\delta N)^3 \rangle}{\sigma^3} = \frac{VT^3 \chi_3}{(VT^3 \chi_2)^{3/2}},$

kurtosis:  $k = \frac{\langle (\delta N)^4 \rangle}{\sigma^4} - 3 = \frac{VT^3 \chi_4}{(VT^3 \chi_2)^2};$

Karsch, arXiv:1202.4173:  $\kappa_B \sigma_B^2 \equiv \frac{\chi_{4,\mu}^B}{\chi_{2,\mu}^B} = \frac{\chi_4^B(T)}{\chi_2^B(T)} \left[ \frac{1 + \frac{1}{2} \frac{\chi_6^B(T)}{\chi_4^B(T)} (\mu_B/T)^2 + \dots}{1 + \frac{1}{2} \frac{\chi_4^B(T)}{\chi_2^B(T)} (\mu_B/T)^2 + \dots} \right]$

Measurable ratios:

$$R_{32} = S\sigma = \frac{\chi_3^{(B,S,Q)}}{\chi_2^{(B,S,Q)}}$$

$$R_{42} = K\sigma^2 = \frac{\chi_4^{(B,S,Q)}}{\chi_2^{(B,S,Q)}}$$

To measure  $\mu_B$ :

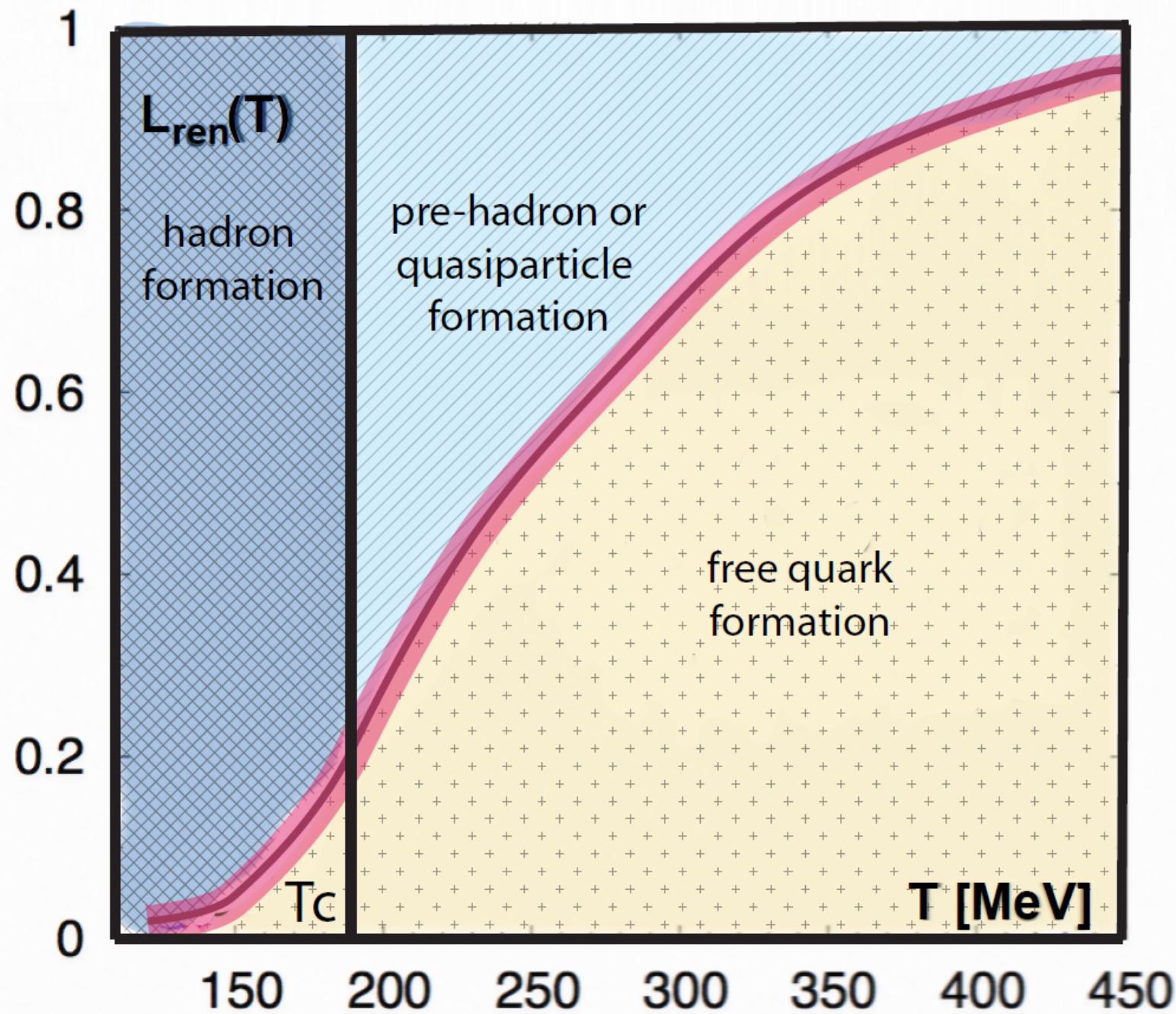
$$R_{12} = \frac{M}{\sigma^2} = \frac{\chi_1^{(B,S,Q)}}{\chi_2^{(B,S,Q)}}$$

To measure T:

$$R_{31} = \frac{S\sigma^3}{M} = \frac{\chi_3^{(B,S,Q)}}{\chi_1^{(B,S,Q)}}$$

# The impact of a crossover on the hadronization

A re-interpretation of the Polyakov Loop calculation in lattice QCD



- In a regime where we have a smooth crossover why would there be a single freeze-out surface ?
- In a regime where quark masses (even for the s-quark) could play a role why would there be single freeze-out surface ?

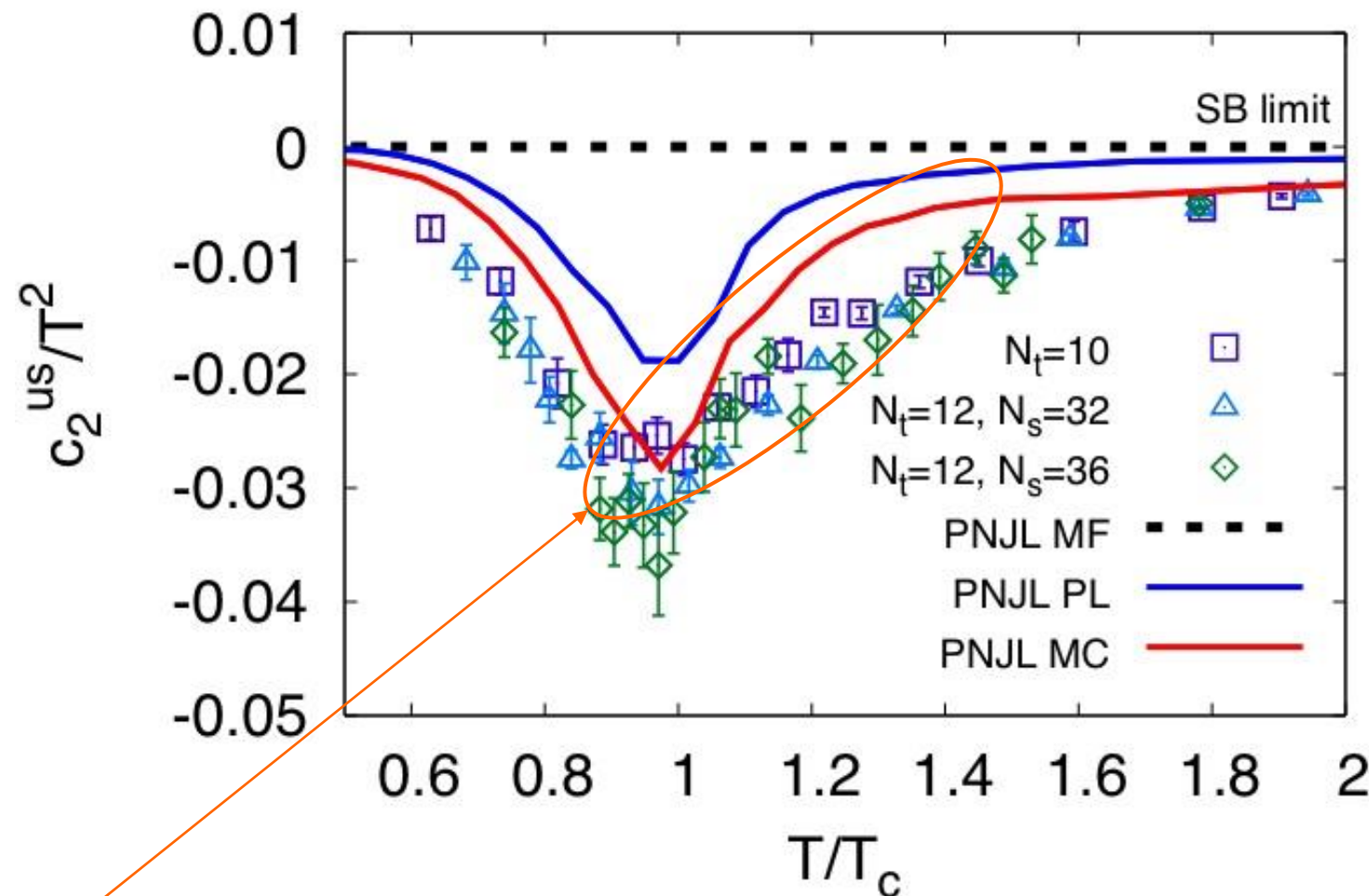
RB et al., PLB691 (2010) 208

Data: Bazavov et al., arXiv:1105:1131



# Indication of bound states in non-diagonal susceptibility correlators (*C. Ratti et al., PRD 85, 014004 (2012)*)

## Comparison of lattice to PNJL



### PNJL variations

PNJL-MF:

*pure mean field calculation*

PNJL-PL:

*mean field plus Polyakov loop fluctuations*

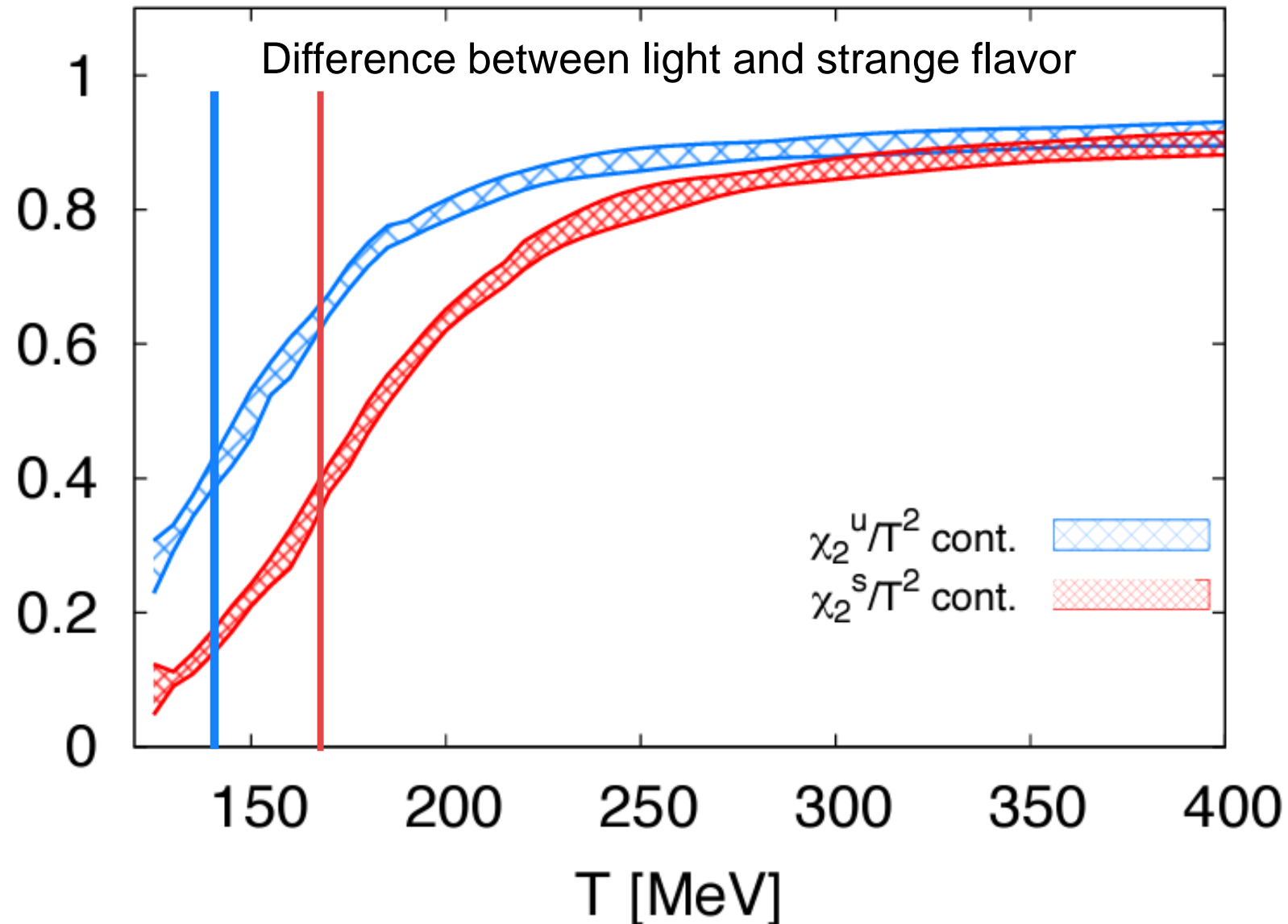
PNJL-MC:

*mean field plus all fluctuations (incl. chiral and Kaon condensate fluctuations)*

**Conclusion:** even the inclusion of *all possible fluctuations* is *not sufficient* to describe lattice data above  $T_c$ .

*There has to be a contribution from bound states*

# Indication of flavor dependence in diagonal susceptibility correlators

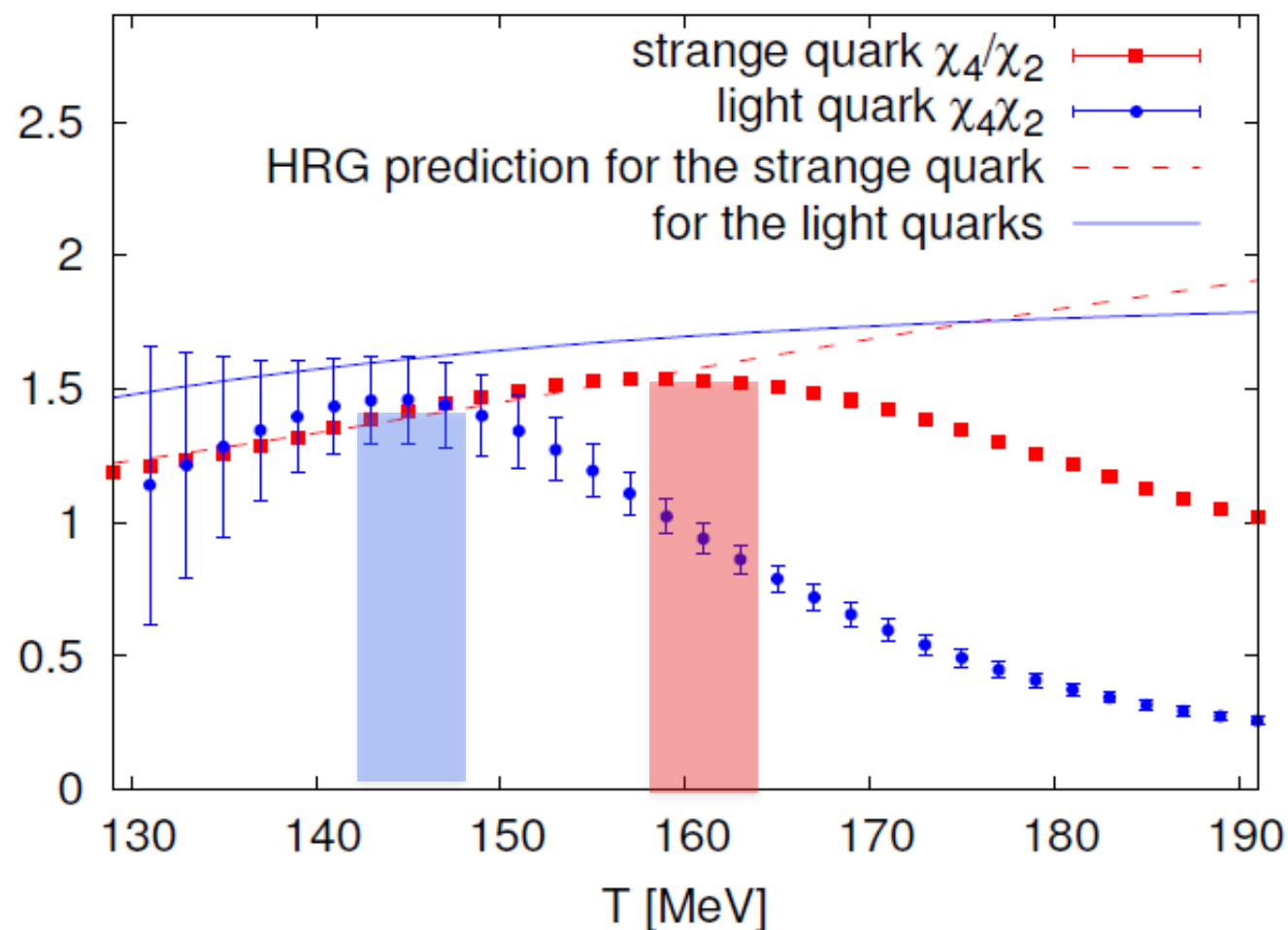


C. Ratti et al., PRD 85, 014004 (2012)  
R. Bellwied, arXiv:1205.3625

# And finally: Direct determination of freeze-out parameters from first principles (lattice QCD)

$$\kappa_B \sigma_B^2 \equiv \frac{\chi_{4,\mu}^B}{\chi_{2,\mu}^B} = \frac{\chi_4^B(T)}{\chi_2^B(T)} \left[ \frac{1 + \frac{1}{2} \frac{\chi_6^B(T)}{\chi_4^B(T)} (\mu_B/T)^2 + \dots}{1 + \frac{1}{2} \frac{\chi_4^B(T)}{\chi_2^B(T)} (\mu_B/T)^2 + \dots} \right]$$

Susceptibility ratios are a model Independent measure of the chemical freeze-out temperature near  $\mu=0$ . (Karsch, arXiv:1202.4173)



- In a regime where we have flavor (quark mass) dependent susceptibility ratios there might be no single freeze-out surface

R. Bellwied & WB Collab., PRL (2013), arXiv:1305.6297



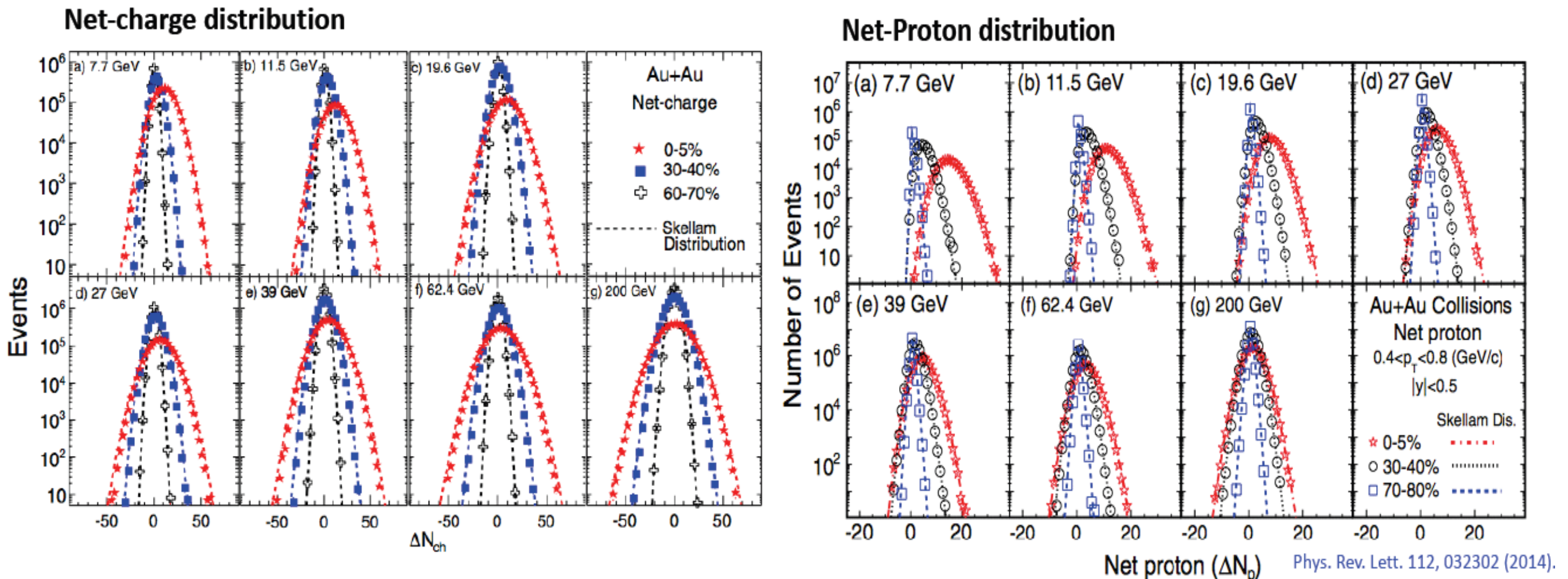
# Experimental verification

Yields of strange particles should be enhanced relative to yields of non-strange particles (the new strangeness enhancement)

Higher order fluctuations of conserved charges should be sensitive to the freeze-out temperature.

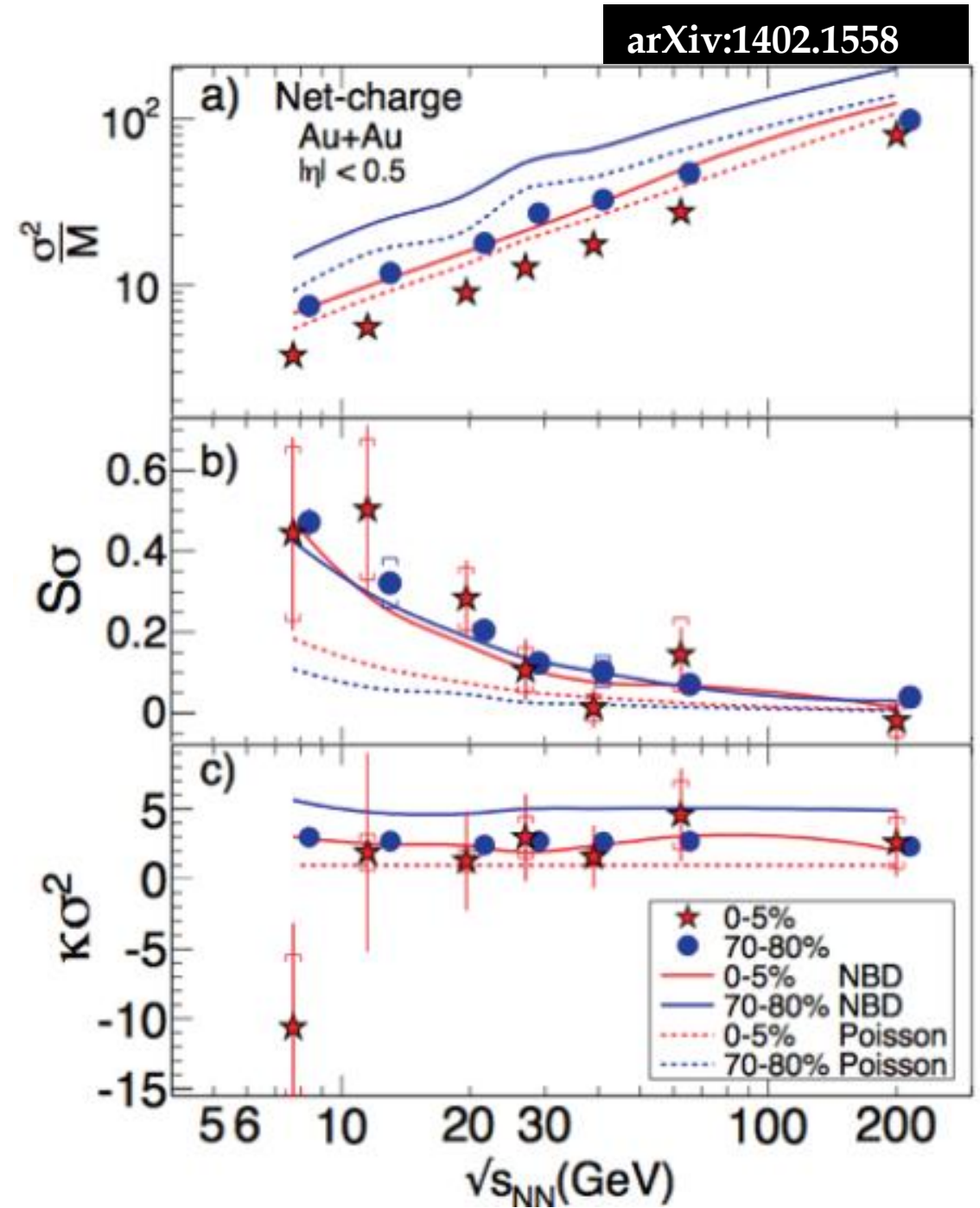
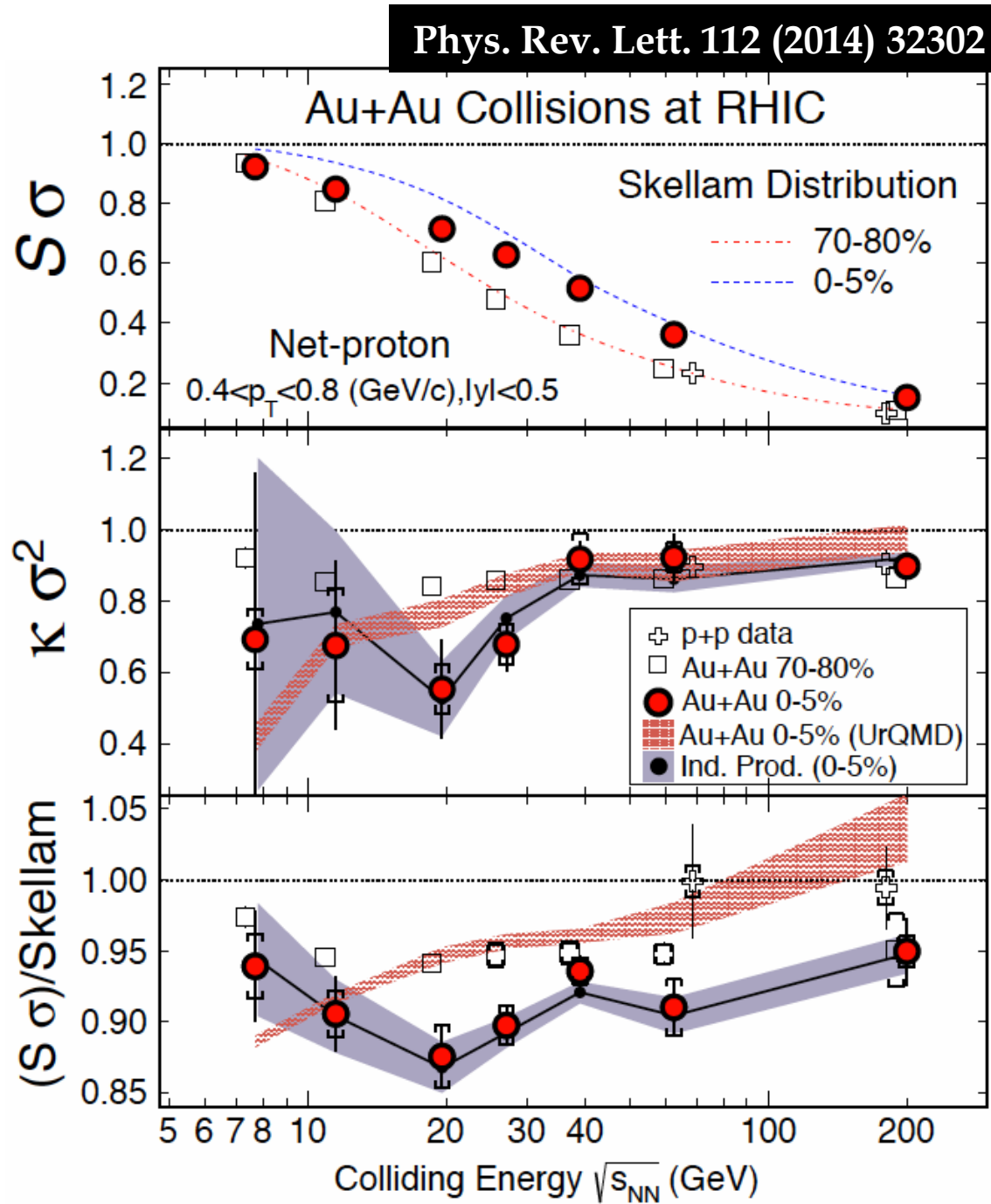
A closer look at RHIC measurements

# Measure net-distributions and calculate moments in STAR

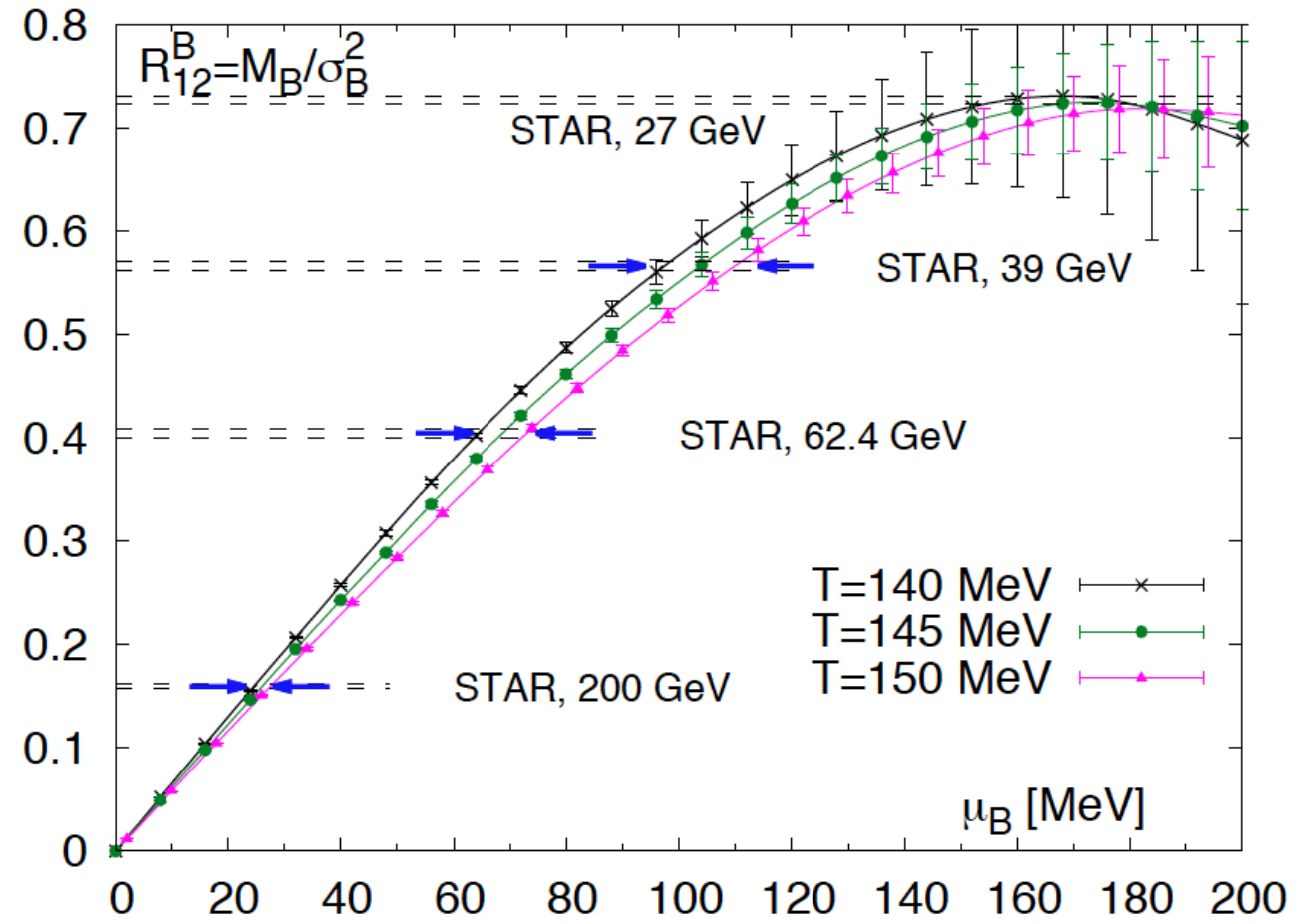
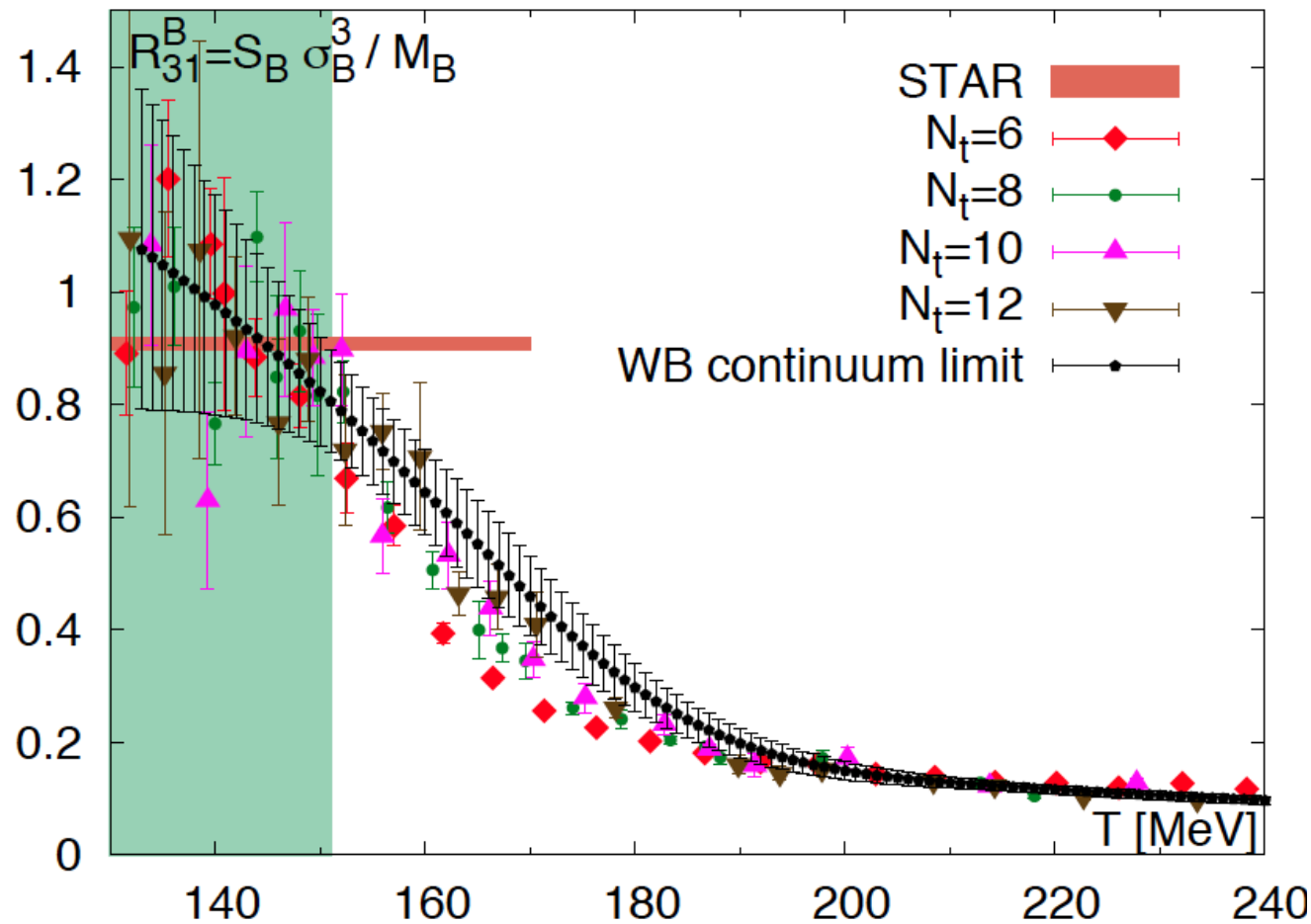


STAR distributions: the means shift towards zero from low to high energy  
Then: calculate moments (c1-c4: mean, variance, skewness, kurtosis)

# Higher moment ratios for net-charge and net-proton distributions



# Freeze-out parameters from lattice comparison to STAR data



(WB collaboration, PRL (2014) arXiv:1403.4576)

Maximum chemical freeze-out temperature:  $151 \pm 4$  MeV  
 (for  $\sqrt{s} > 39$  GeV based on net-protons)



# But can one simply compare lattice susceptibility results to experimental fluctuation measurements ?

The following criteria need to be met:

- one needs a grand-canonical ensemble (intrinsic in lattice QCD conditions, but only reached in limited acceptance in experiment). In full acceptance a conserved charge cannot fluctuate.

(very nice overview paper by V. Koch, arXiv: 0810.2520)

- one needs to take into account acceptance, efficiency, detector effects
- one needs to estimate the effect from measuring only a subset of the conserved charge (e.g. protons instead of baryon number)

The easiest method: build all caveats into a statistical hadronization model (HRG) and show equivalence between HRG and lattice QCD

# Experimental constraints and how to deal with them in the HRG

- ◆ Effects due to volume variation because of finite centrality bin width
- ◆ Finite reconstruction efficiency
- ◆ Spallation protons
- ◆ Canonical vs Grand Canonical ensemble
- ◆ Proton multiplicity distributions vs baryon number fluctuations
- ◆ Final-state interactions in the hadronic phase [J.Steinheimer et al., PRL \(2013\)](#)



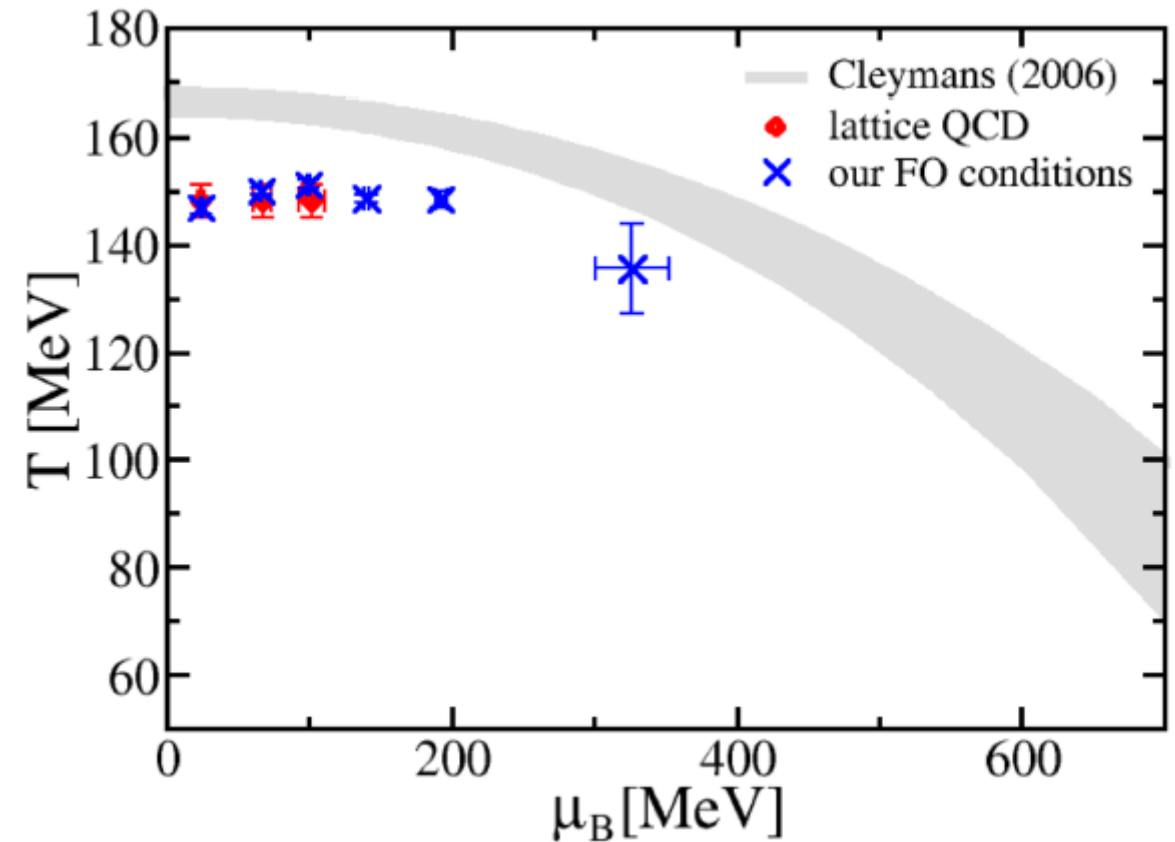
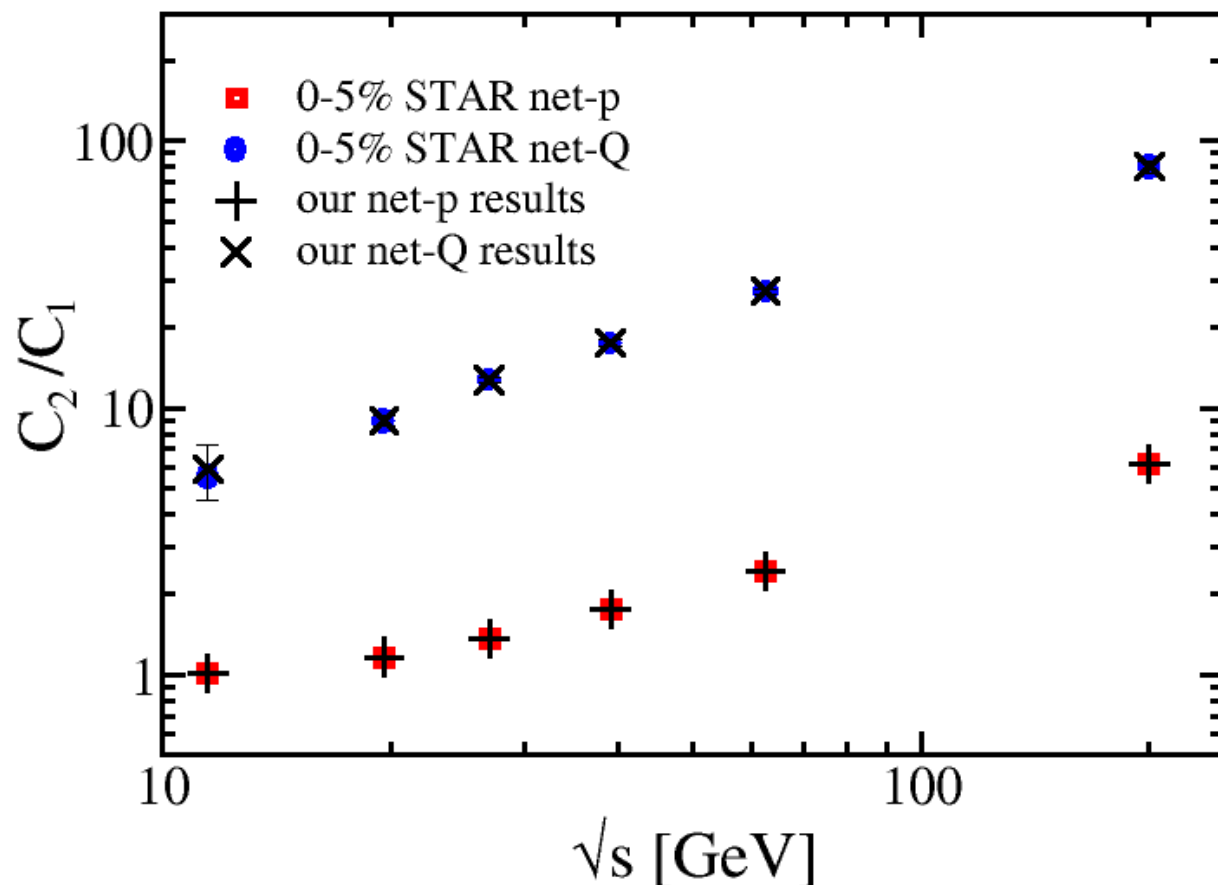
# Experimental constraints and how to deal with them in the HRG

- ◆ Effects due to volume variation because of finite centrality bin width
  - ⇒ Experimentally corrected by centrality-bin-width correction method
- ◆ Finite reconstruction efficiency
  - ⇒ Experimentally corrected based on binomial distribution [A. Bzdak, V. Koch, PRC \(2012\)](#)
- ◆ Spallation protons
  - ⇒ Experimentally removed with proper cuts in  $p_T$
- ◆ Canonical vs Grand Canonical ensemble
  - ⇒ Experimental cuts in the kinematics and acceptance [V. Koch, S. Jeon, PRL \(2000\)](#)
- ◆ Proton multiplicity distributions vs baryon number fluctuations
  - ⇒ Numerically very similar once protons are properly treated [M. Asakawa and M. Kitazawa, PRC \(2012\)](#), [M. Nahrgang et al., 1402.1238](#)
- ◆ Final-state interactions in the hadronic phase [J. Steinheimer et al., PRL \(2013\)](#)
  - ⇒ Consistency between different charges = fundamental test

# HRG analysis of STAR results (charge & proton)

Alba, Bellwied, Bluhm, Mantovani, Nahrgang, Ratti (PLB (2014), arXiv:1403.4903)

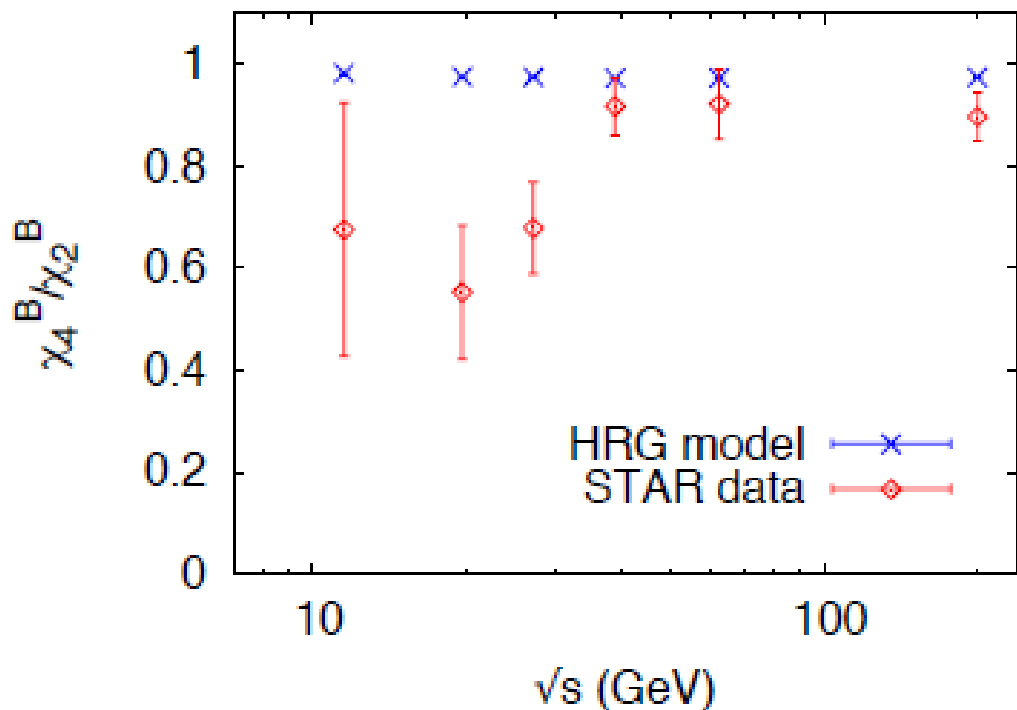
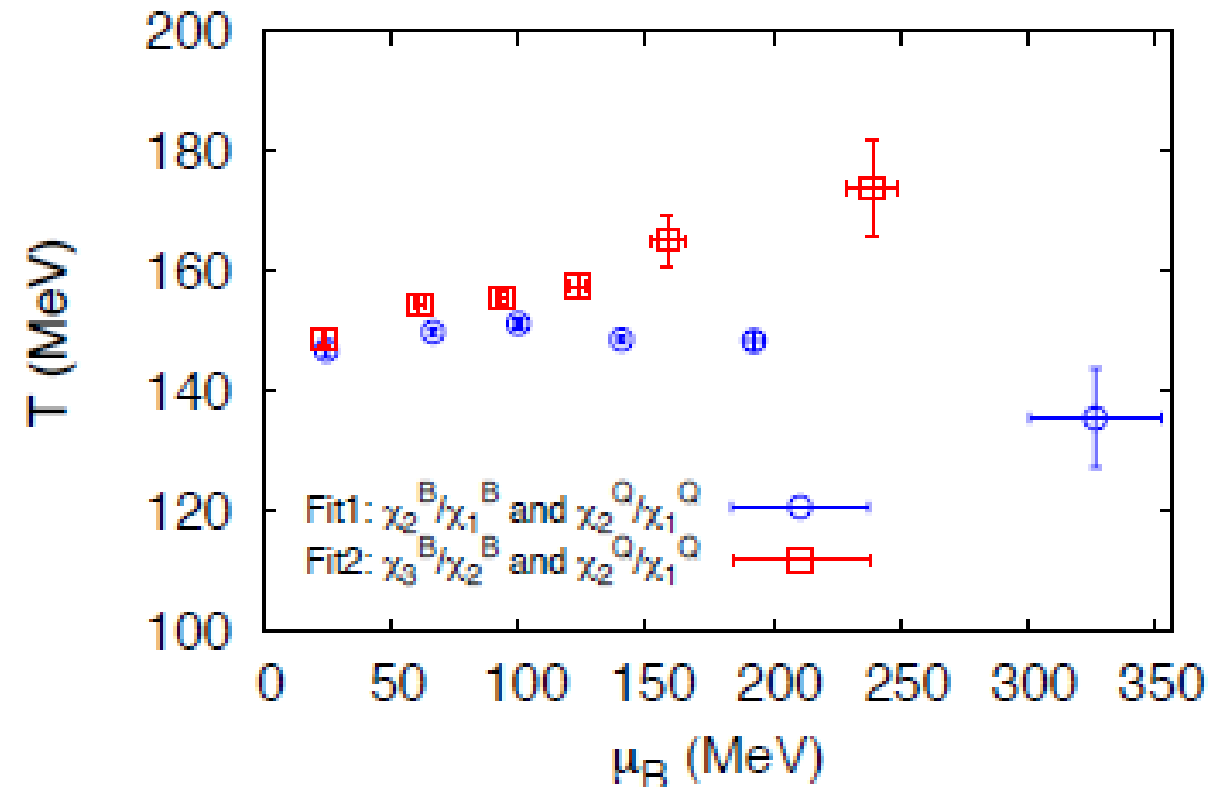
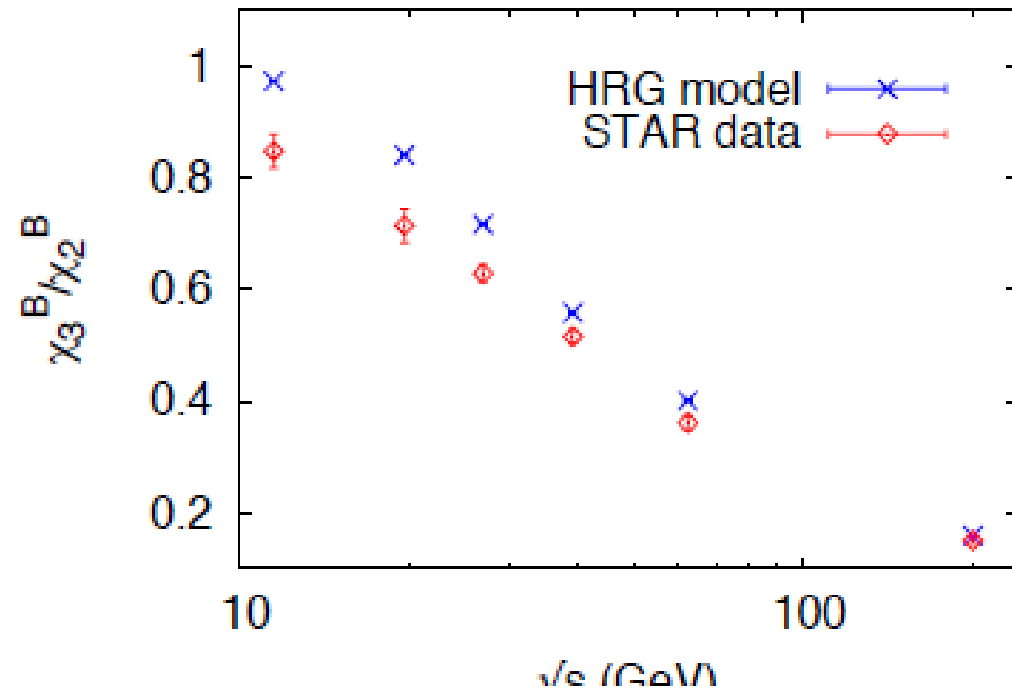
HRG in partial chemical equilibrium (resonance and weak decays) & PDG up to 2 GeV/c<sup>2</sup> & experimental cuts & isospin randomization (Nahrgang et al., arXiv:1402.1238)



$\sqrt{s}$ [GeV]	$\mu_{B, ch}$ [MeV]	$T_{ch}$ [MeV]
11.5	$326.7 \pm 25.9$	$135.5 \pm 8.3$
19.6	$192.5 \pm 3.9$	$148.4 \pm 1.6$
27	$140.4 \pm 1.4$	$148.5 \pm 0.7$
39	$99.9 \pm 1.4$	$151.2 \pm 0.8$
62.4	$66.4 \pm 0.6$	$149.9 \pm 0.5$
200	$24.3 \pm 0.6$	$146.8 \pm 1.2$

Remarkable consistency, pointing to lower freeze-out temperature for particles governing net-charge ( $\pi, p$ ) and net-protons ( $p$ )

# Problems with higher moments



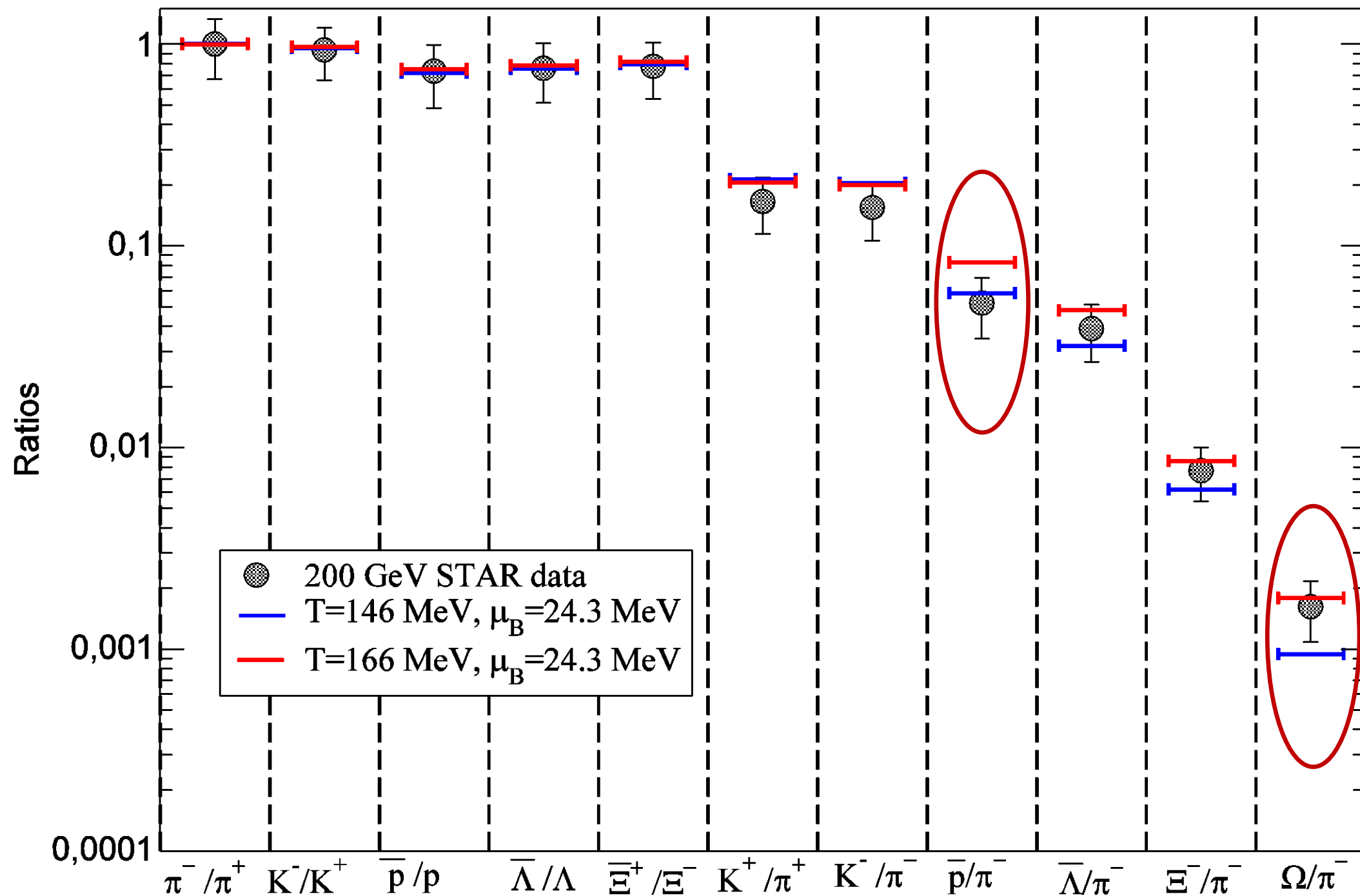
HRG overshoots the  $\chi_3/\chi_2$  at lower energies and cannot explain the ‘dip’ in  $\chi_4/\chi_2$ . Temperature dependence on collision energy becomes ‘unphysical’.

Possible reasons:

- overestimate of isospin randomization
- onset of critical behavior in  $\chi_3$  and  $\chi_4$

Important lesson: lower moments carry significant information with much smaller error bar (might be already sufficient)

# Difference: SHM-T and HRG-T in particle ratio fits

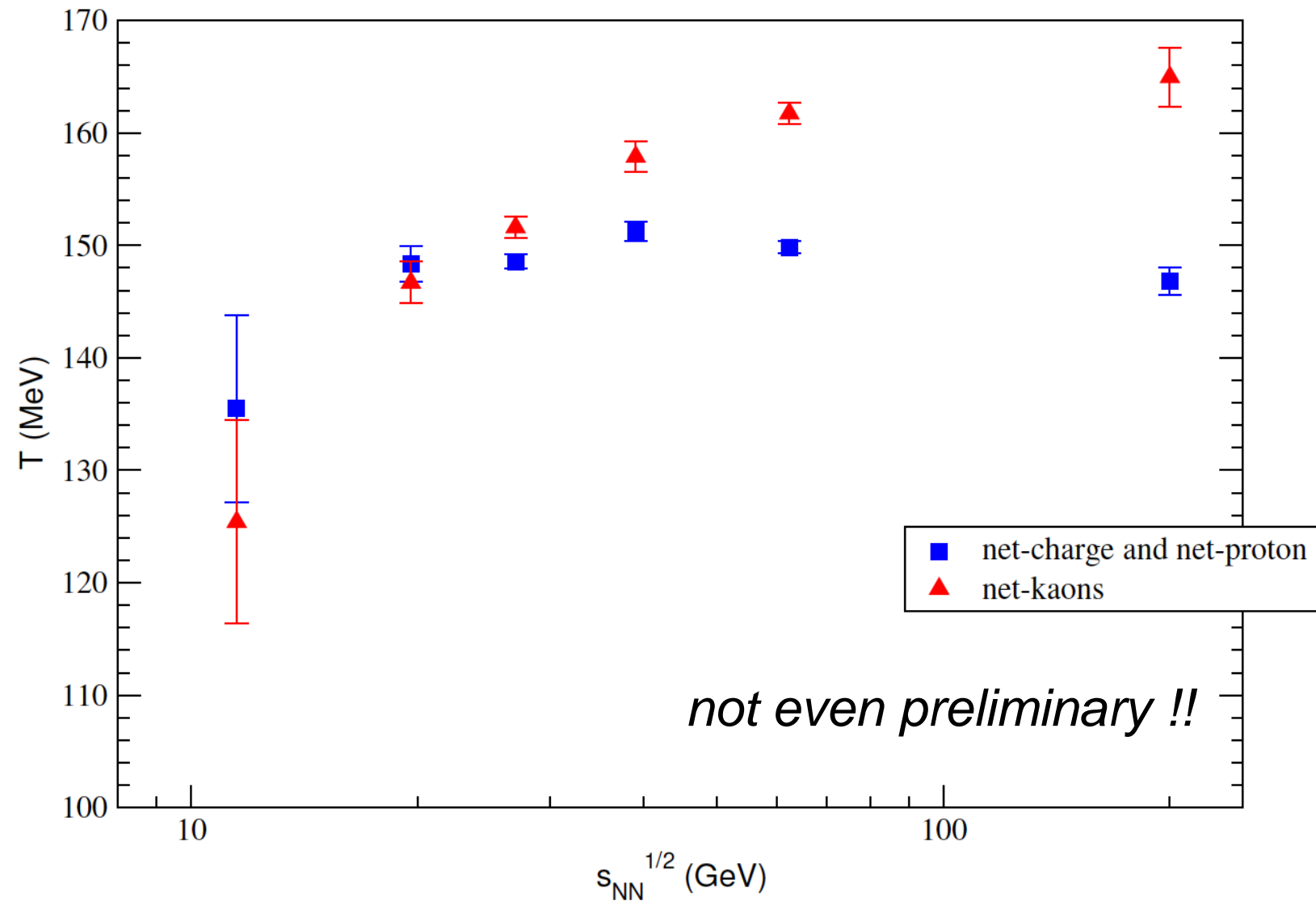
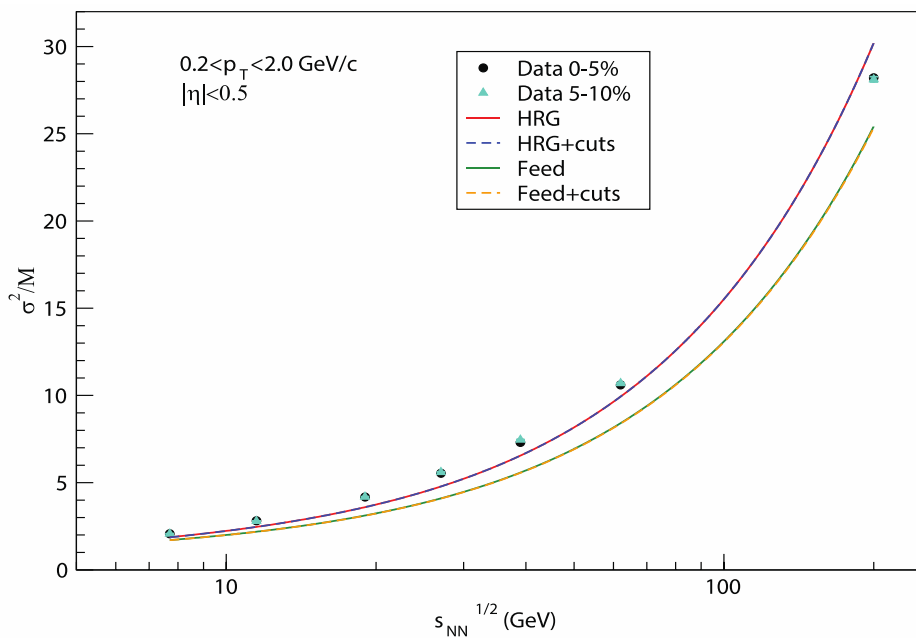
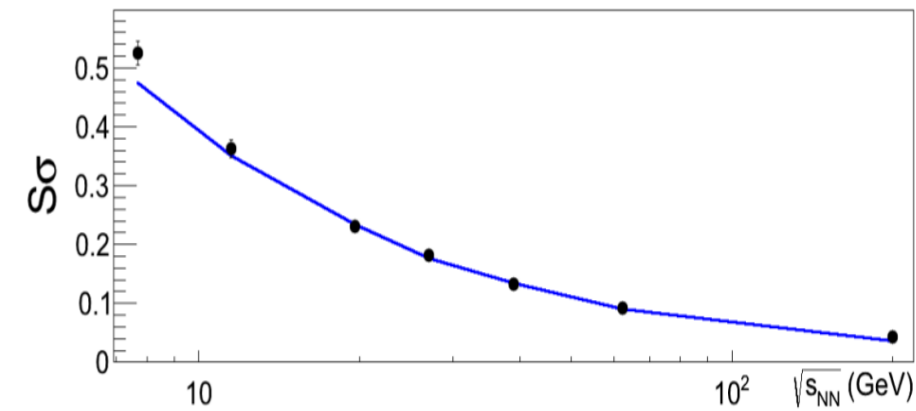
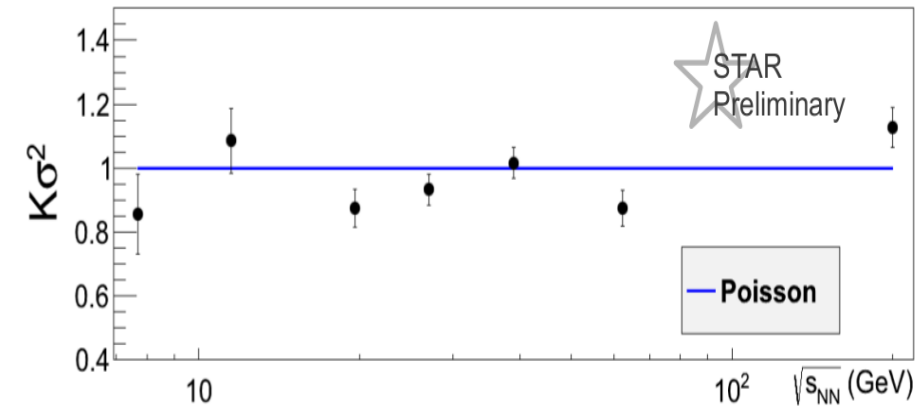


Main deviations in pure strange and light baryon state. Consistent with ALICE

We need corrected net-strange fluctuations (kaons not sufficient ?)

STAR has shown uncorrected kaons at QM (D. McDonald and A. Sarkar)

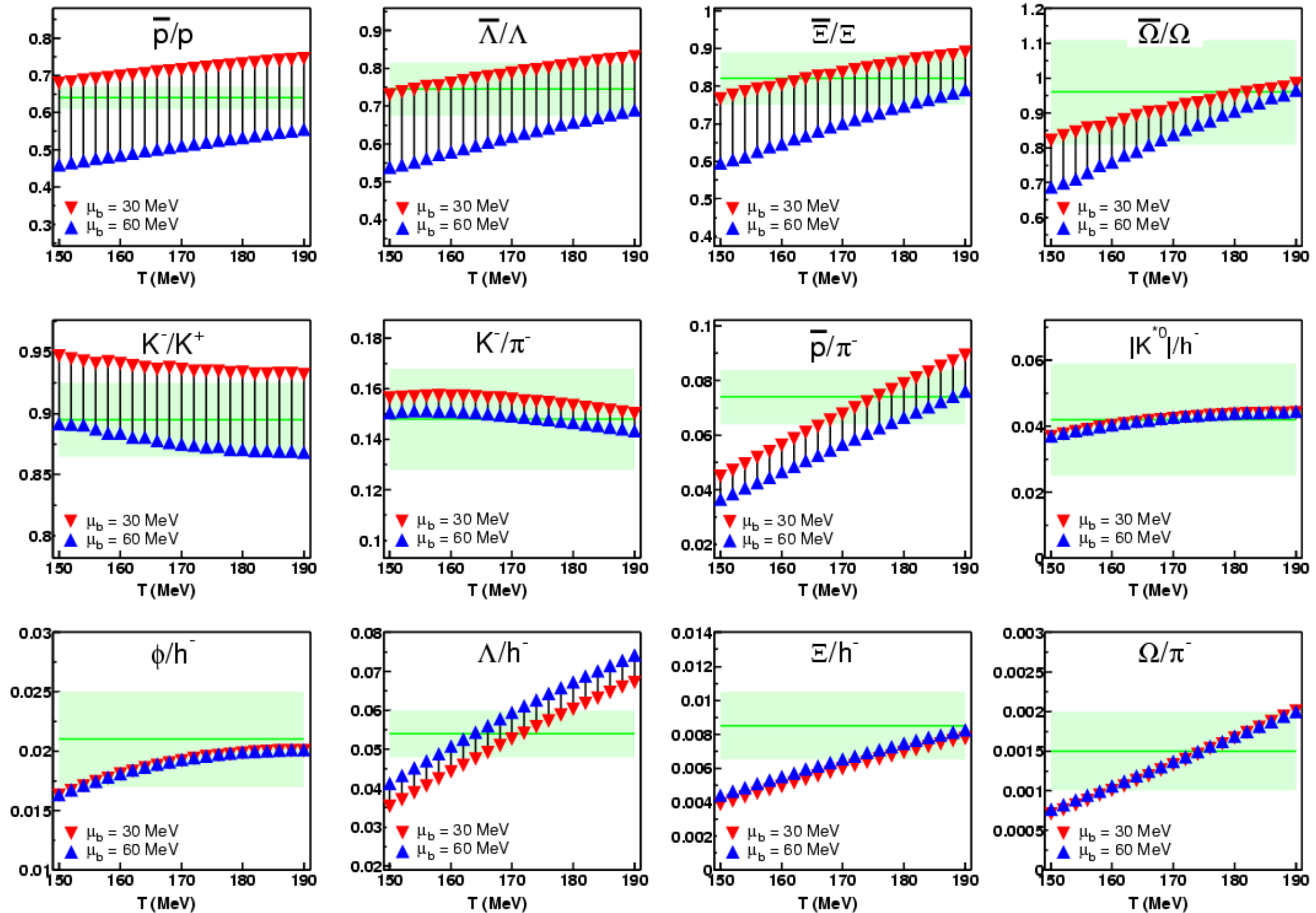
# If we play with uncorrected data.....



It only shows the sensitivity of the measurement

**Do not conclude any relevant physics prior to efficiency corrections**

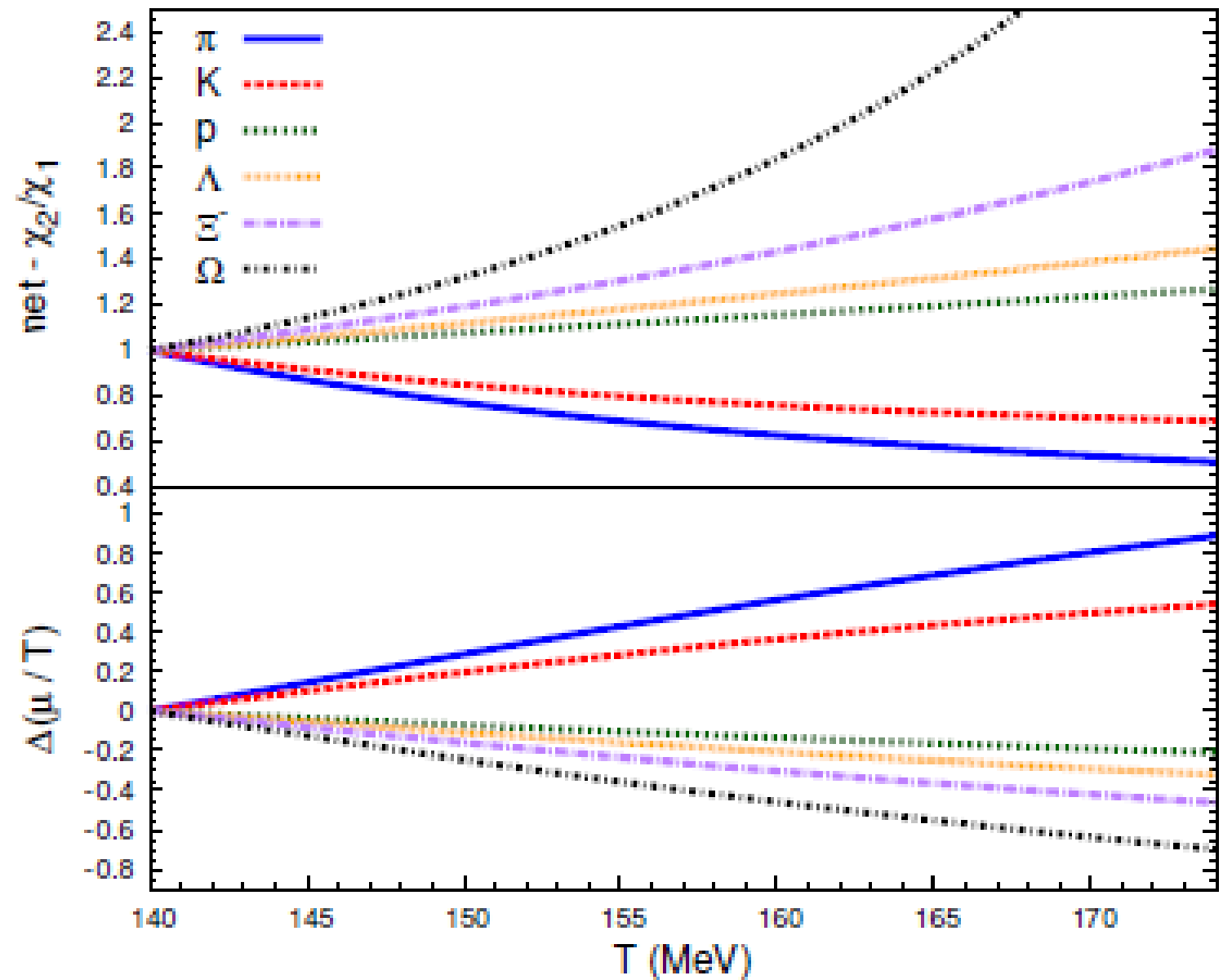
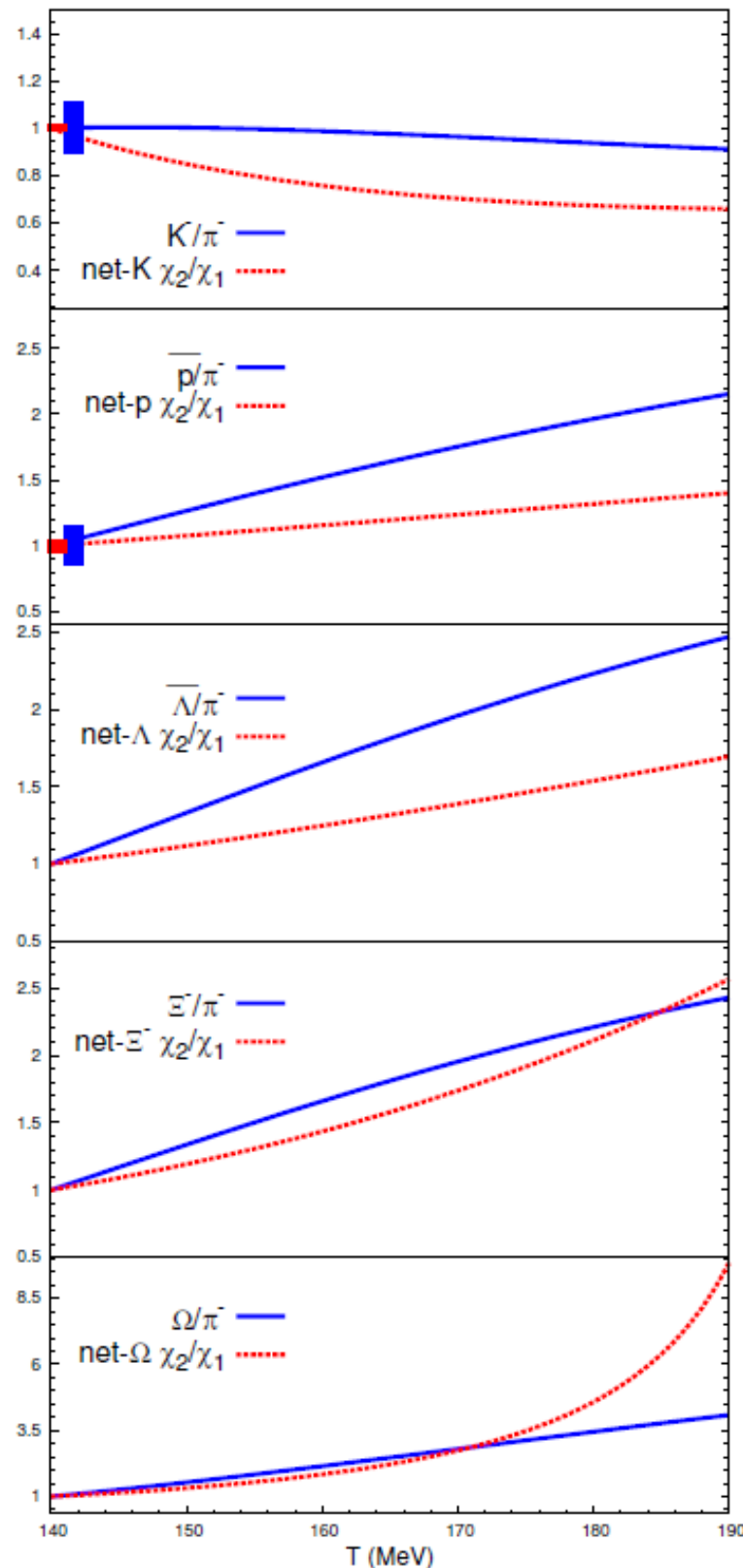
# The sensitivity of yields to the freeze-out parameters



D. Magestro, J. Phys G28 (2002) 1745; updated July 21

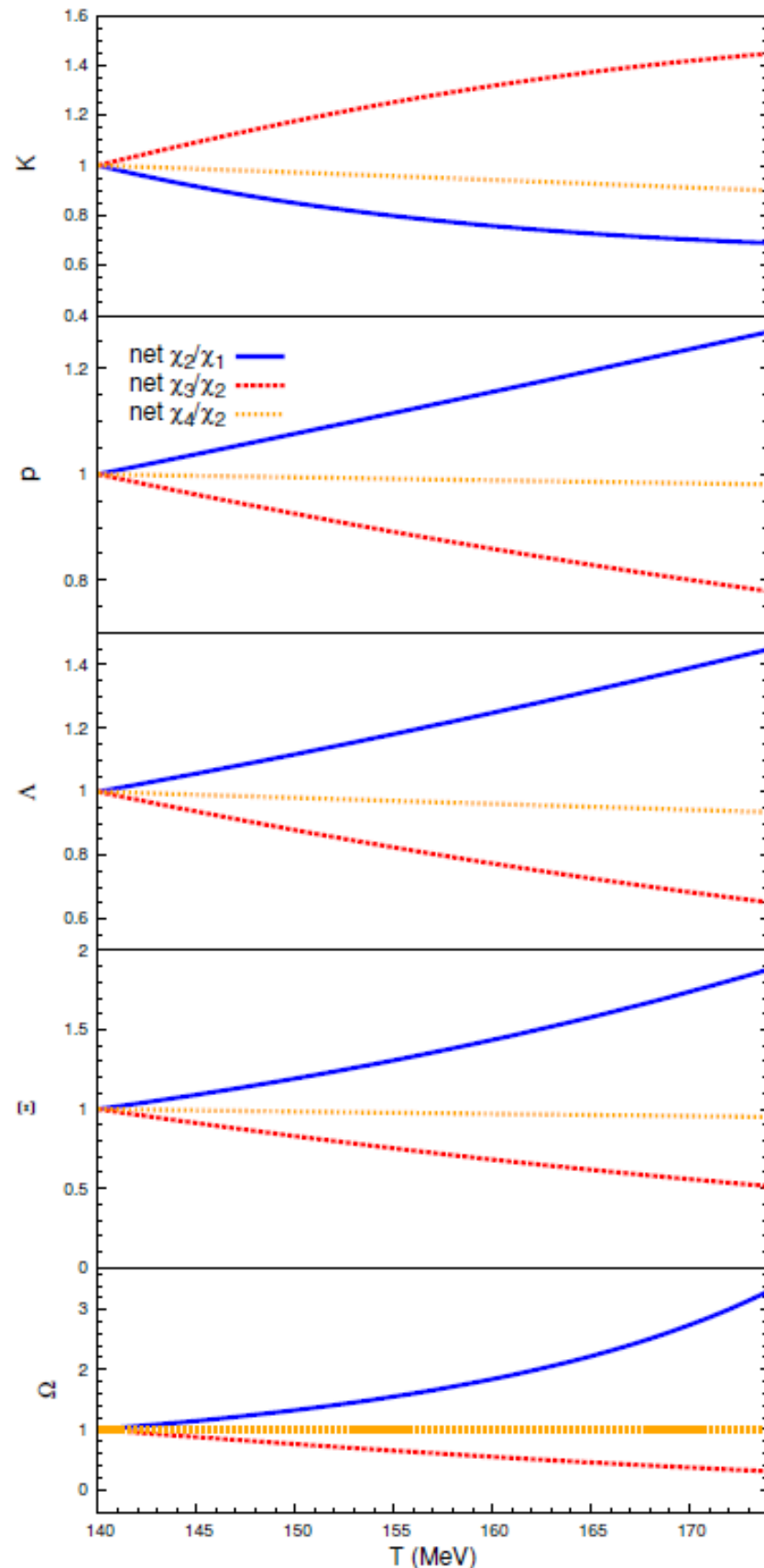


# The sensitivity of fluctuations to freeze-out parameters



HRG model calculations: Alba, Bellwied, Bluhm, Mantovani, Nahrgang, Ratti (arXiv:1504.03262)

# Do we need higher order measurements ?



Temperature sensitivity varies for moment ratios. Higher order ratios seem less sensitive and more prone to critical effects.

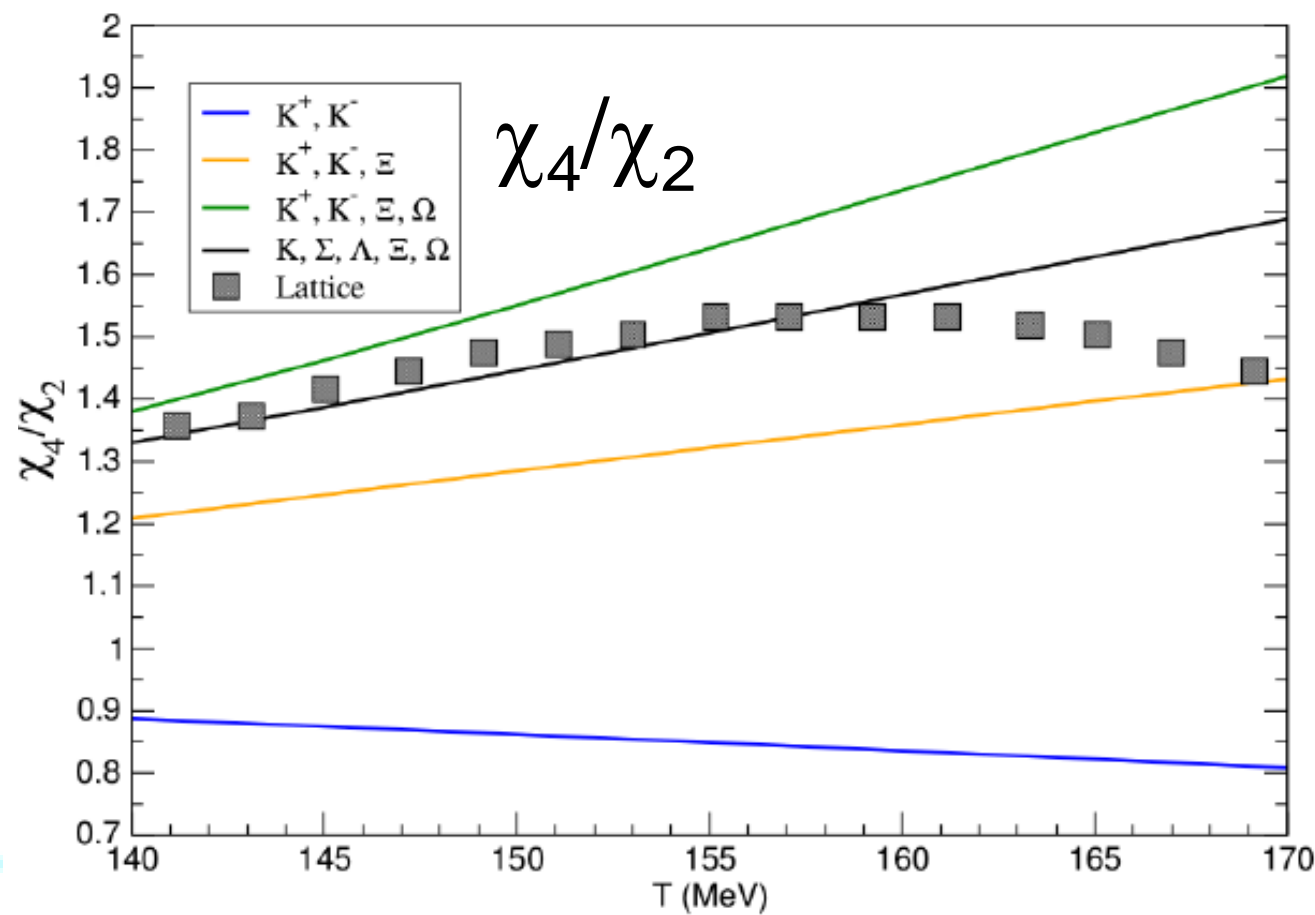
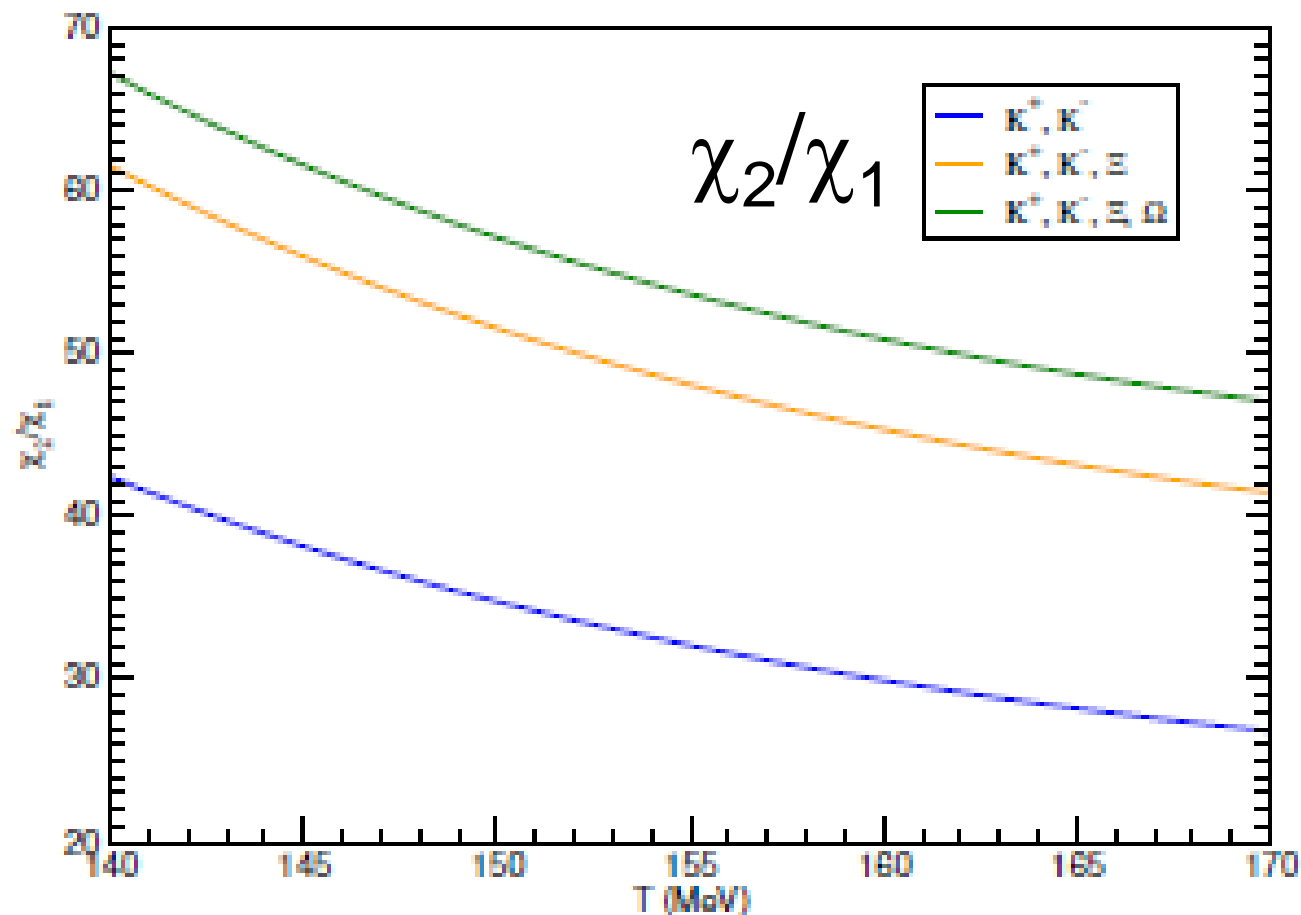
But in order to compare to lattice QCD we need full 'strangeness' and even/even ratios (i.e.  $c_4/c_2$  is the ultimate measurement)

*We need the complete strange particle spectrum for  $\chi_4/\chi_2$*

arXiv:1504.03262

Can we just measure a subset of states to determine strangeness freeze-out temperature in HRG ?

HRG calculations are very sensitive to particle composition



Temperature sensitivity varies for moment ratios  
 We need complete strange particle spectrum for  $\chi_4/\chi_2$   
 For  $\chi_2/\chi_1$  just kaons are sufficient

arXiv:1504.03262

# So what can happen between 148 and 164 MeV ?

A 20 MeV drop can be translated into a 2 fm/c time window  
Strangeness wants to freeze-out, light quarks do not

Can there be measurable effects ?

Can there be a mixed phase of degrees of freedom

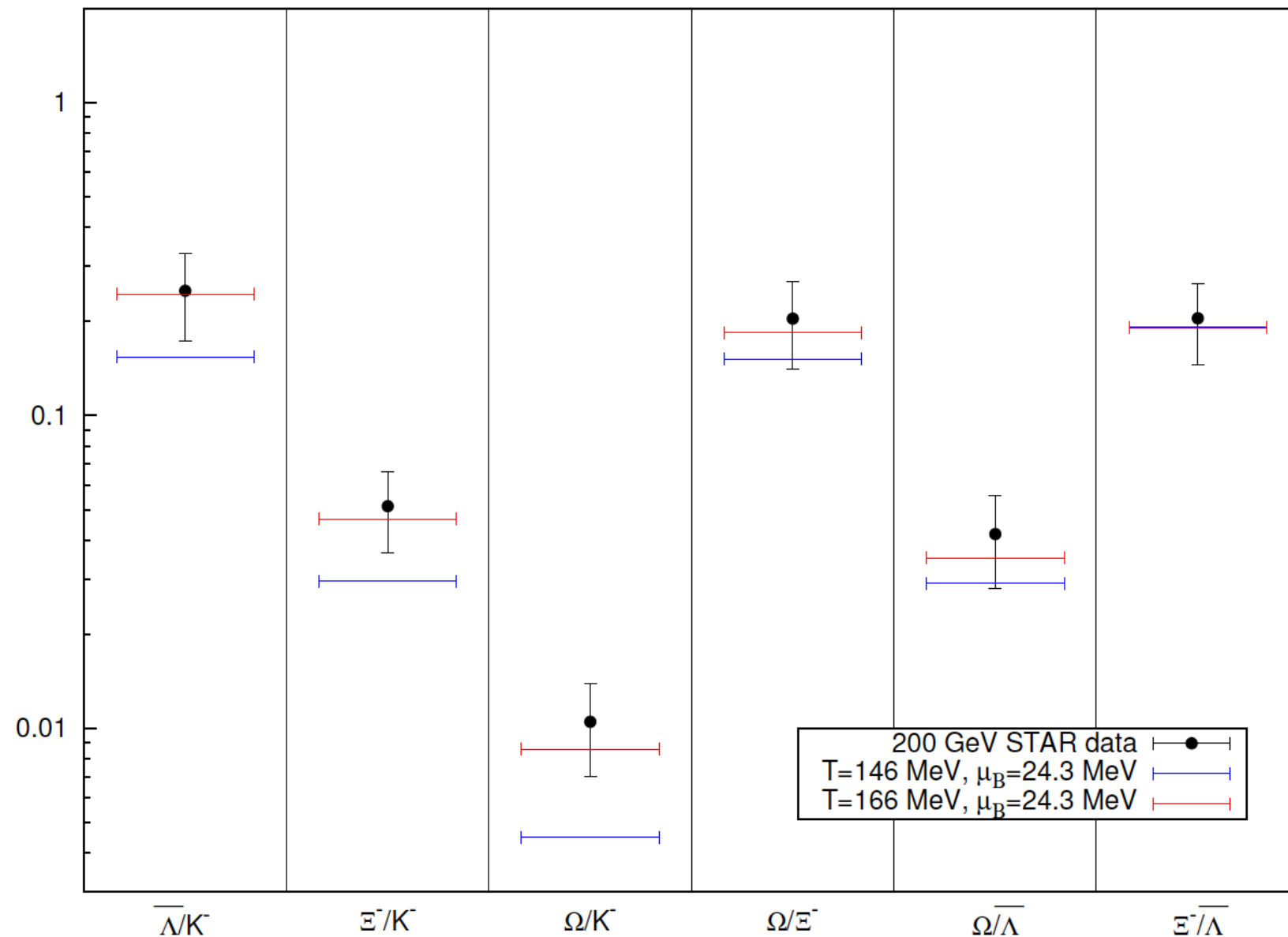
Can there be implications for the cosmological evolution of matter ?

Three options *from the mundane to the exotic:*

- 1.) a new strangeness enhancement
- 2.) higher strange states based on excited states in Quark Model
- 3.) exotic quark configurations

# A new strangeness enhancement

By comparing strange mesons to strange baryons we see that strange baryons are consistently enhanced at the higher T compared to the lower T.



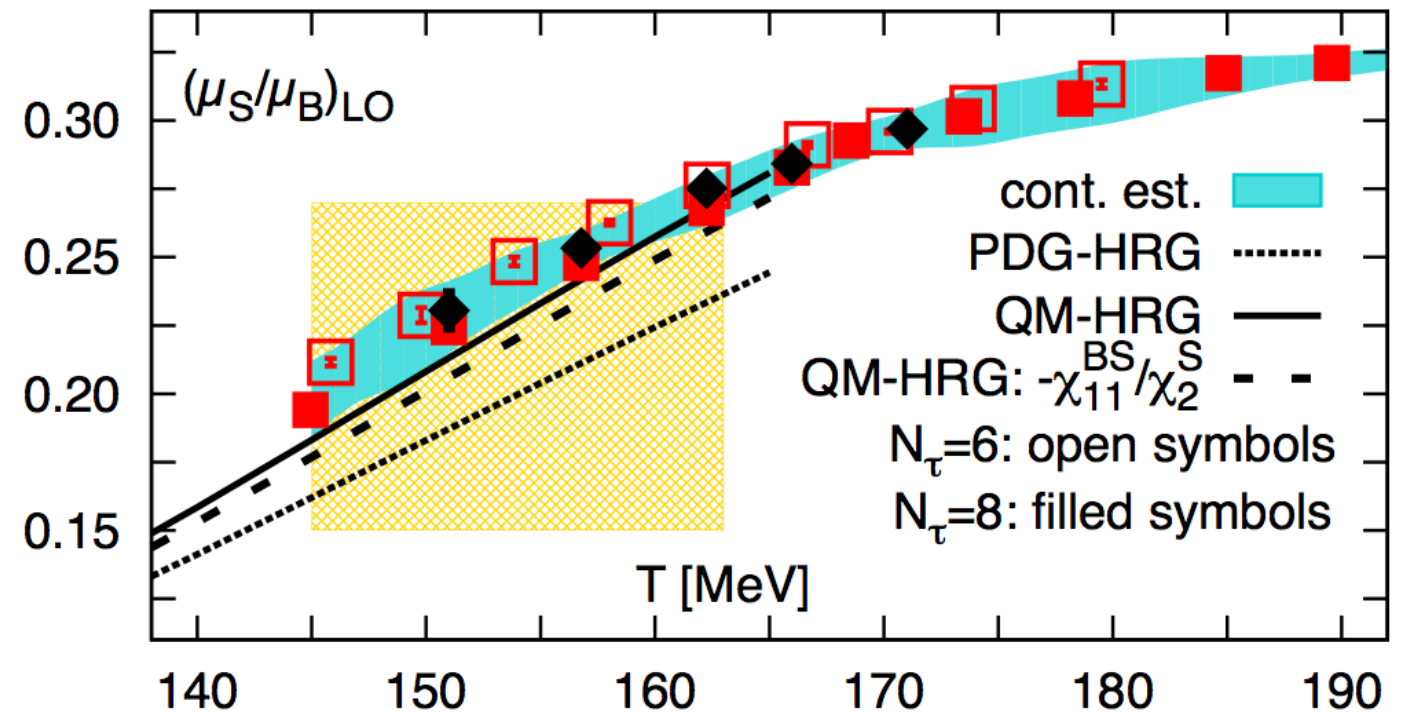
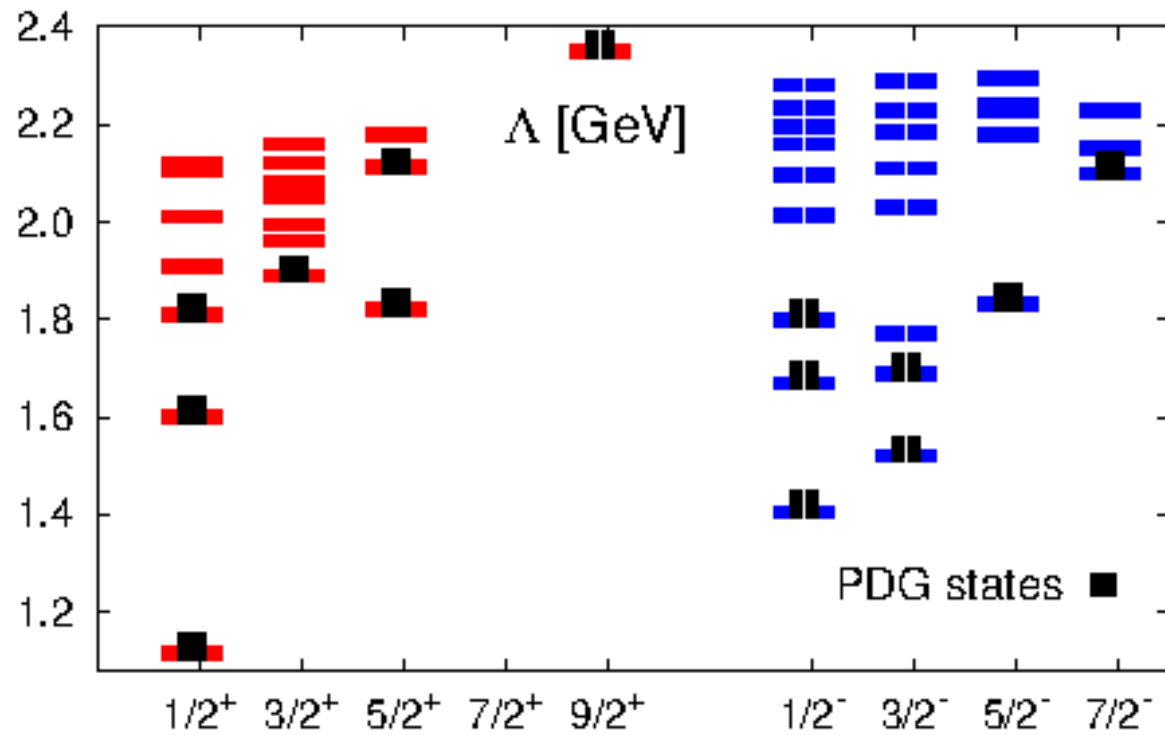
Enhancement factors from 146 to 166 MeV:

(assuming  $V=5570$  fm<sup>3</sup> and  $V=1760$  fm<sup>3</sup>, respectively)

**$\Lambda$  yield increases by 20%,  $\Xi$  yield increases by 30%,  $\Omega$  yield increases by 44%**

# Excited states within the Quark Model

Not yet seen higher mass states from Quark Model calculations seem to improve agreement between HRG and lattice for the  $\chi_{BS}$  correlator (Bazavov et al., PRL (2014), arXiv:1404.6511)



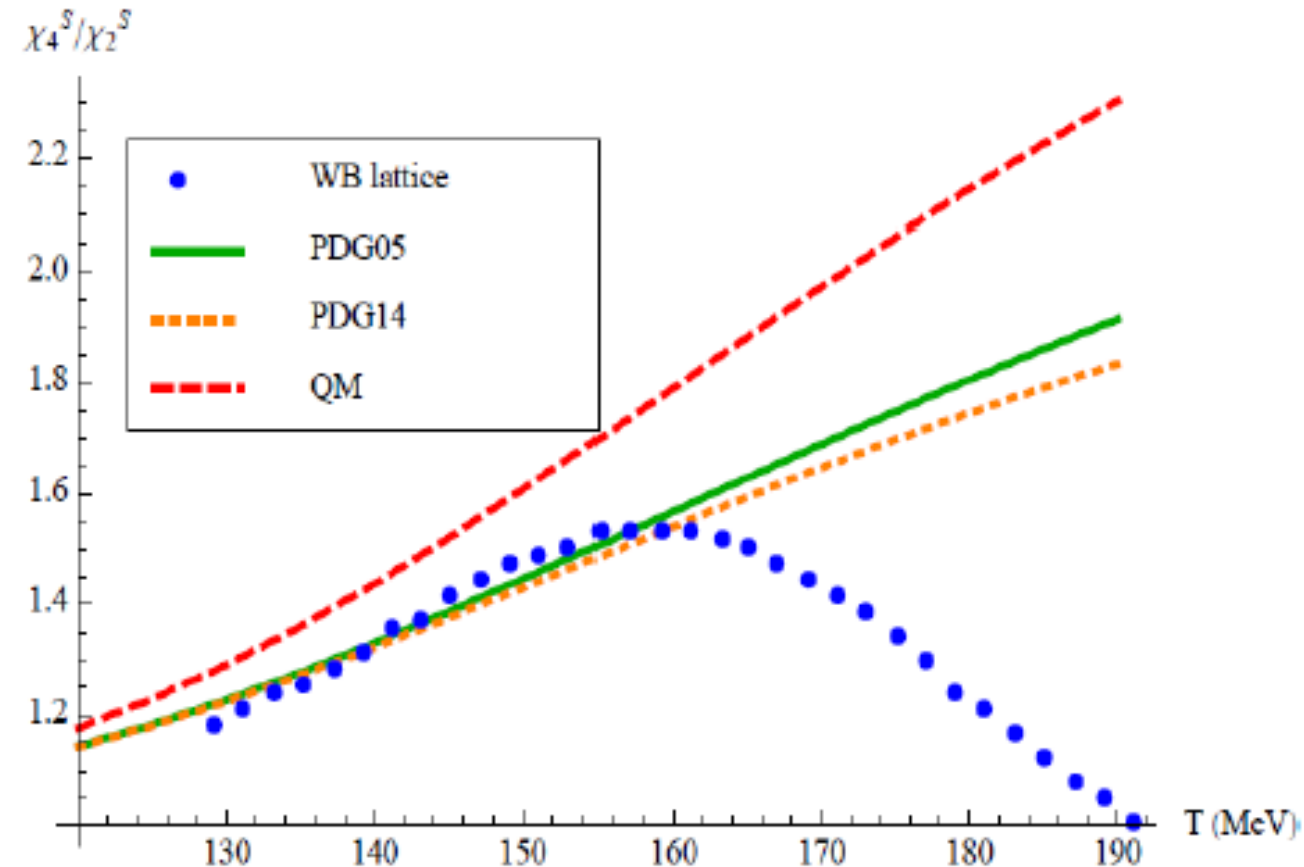
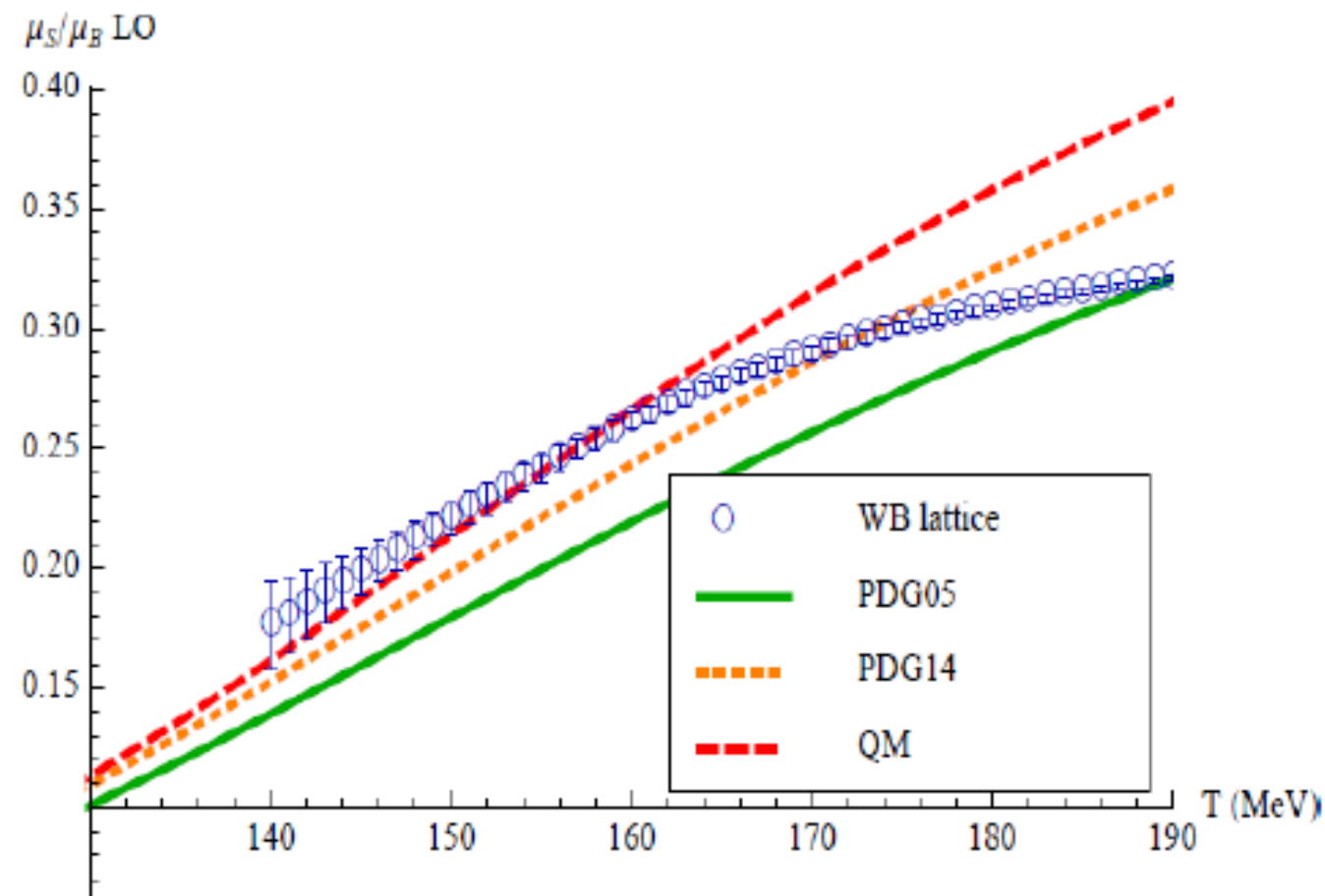
But those effects need to be consistently applied to all correlators that are possibly affected by higher lying strange states.

Still, the idea of preferred strange bound state production in a particular temperature window is intriguing and could ultimately lead to generation even of exotic multi-quark configurations



# Do we really need not yet measured states ?

## What happens from PDG-2008 to PDG-2014 ?

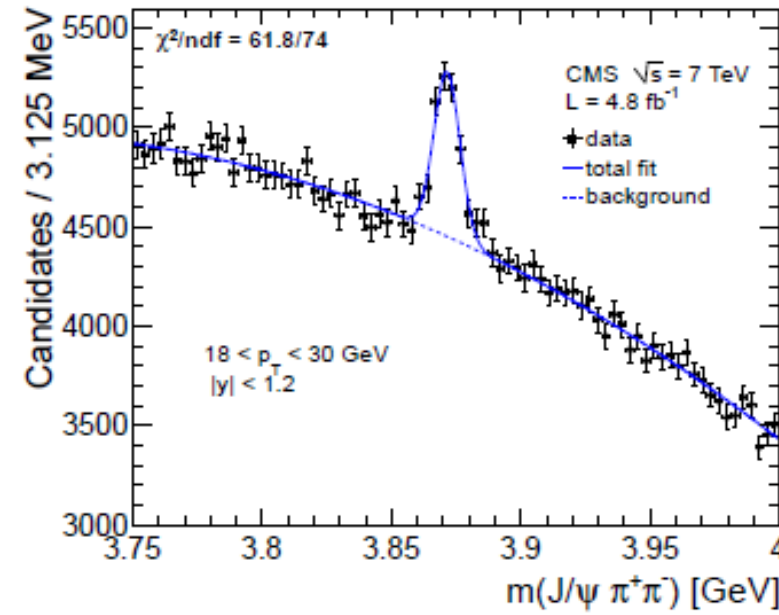
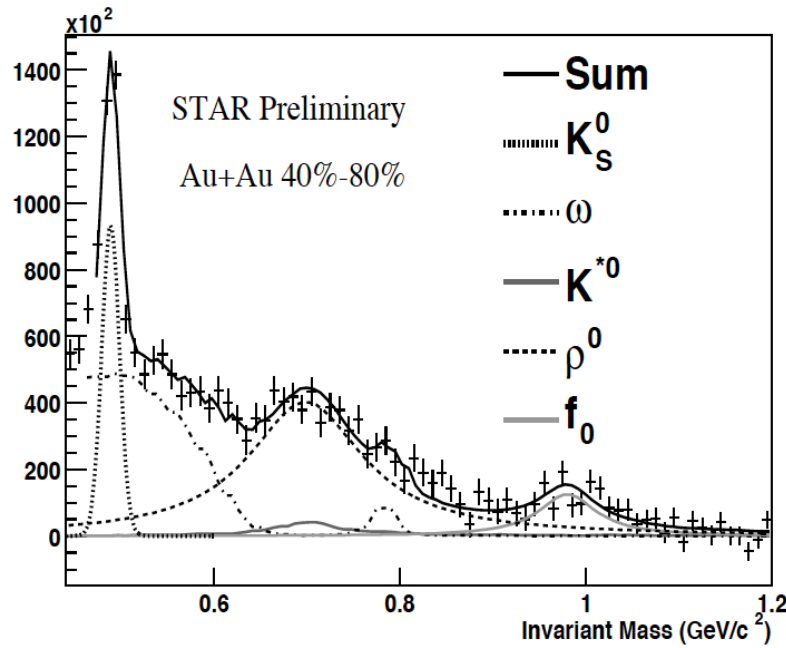


Although, new states from the Quark Model (QM) improve the leading order ratio, they worsen the agreement with the higher moment ratio on the lattice ( $c_4/c_2$ ).

It is true that the states available in PDG-2005 are not sufficient to describe both ratios equally well, but the inclusion of newly measured higher mass strange resonances as listed in PDG-2014 seem to be sufficient to reach a good agreement between lattice and data.

# Exotic states within the Standard Model

Exotic states measured at RHIC and the LHC (strange and charm sector)

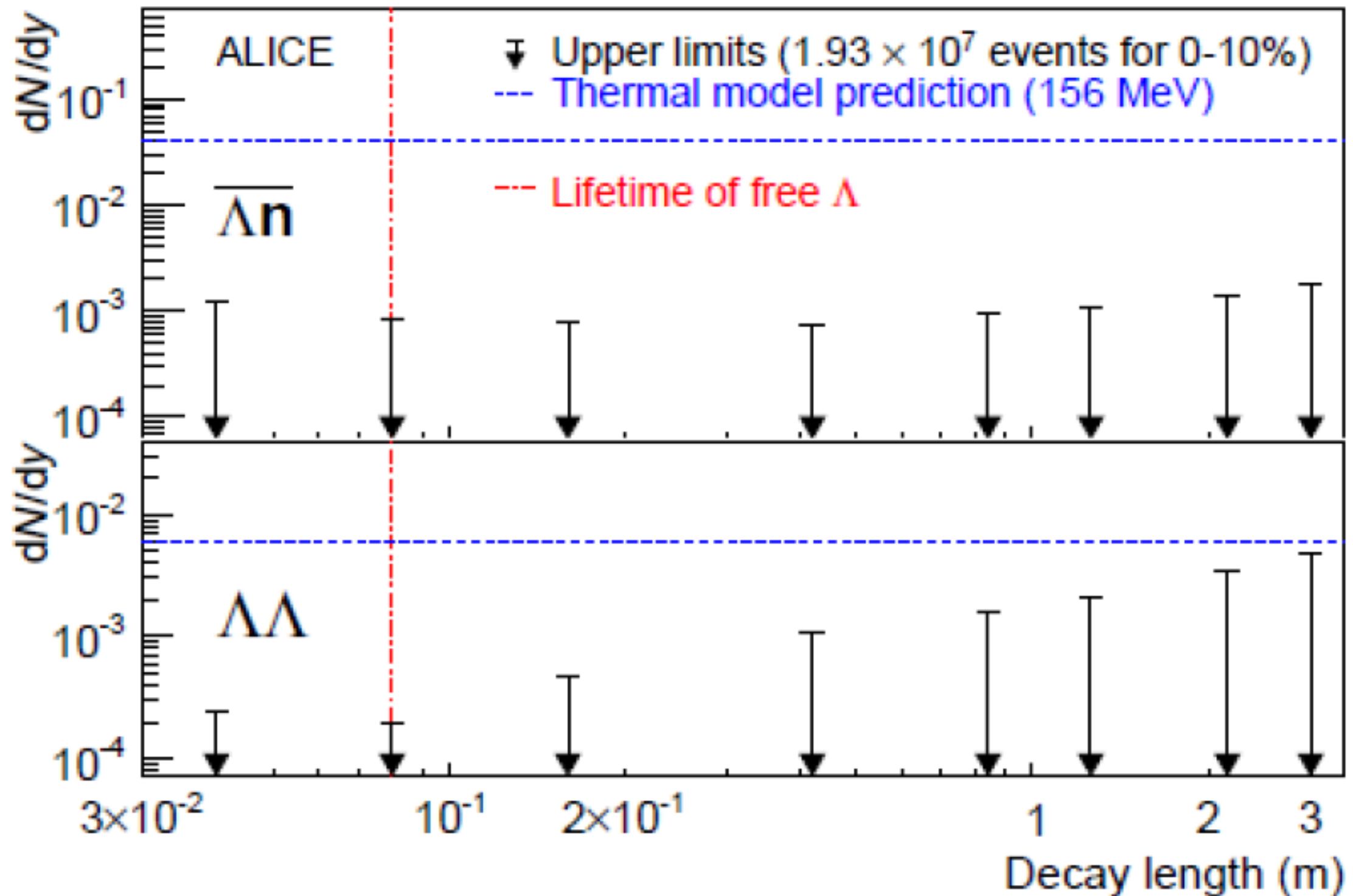


ExHIC Collaboration (2011):

Particle	$m$ (MeV)	$g$	$I$	$J^P$	$2q/3q/6q$	$4q/5q/8q$	Mol.	RHIC				LHC				
								$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.	$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.	
<b>Mesons</b>																
$f_0(980)$	980	1	0	$0^+$	$q\bar{q}, s\bar{s}(L=1)$	$q\bar{q}s\bar{s}$	$\bar{K}K$	3.8, 0.73( $s\bar{s}$ )	0.10	13	5.6	10, 2.0 ( $s\bar{s}$ )	0.28	36	15	
$a_0(980)$	980	3	1	$0^+$	$q\bar{q}(L=1)$	$q\bar{q}s\bar{s}$	$\bar{K}K$	11	0.31	40	17	31	0.83	$1.1 \times 10^2$	46	
$K(1460)$	1460	2	$1/2$	$0^-$	$q\bar{s}$	$q\bar{q}q\bar{s}$	$\bar{K}KK$	—	0.59	3.6	1.3	—	1.6	9.3	3.2	
$D_s(2317)$	2317	1	0	$0^+$	$c\bar{s}(L=1)$	$q\bar{q}c\bar{s}$	$DK$	$1.3 \times 10^{-2}$	$2.1 \times 10^{-3}$	$1.6 \times 10^{-2}$	$5.6 \times 10^{-2}$	$8.7 \times 10^{-2}$	$1.4 \times 10^{-2}$	0.10	0.35	
$T_{cc}^{1a}$	3797	3	0	$1^+$	—	$qqc\bar{c}$	$\bar{D}\bar{D}^*$	—	$4.0 \times 10^{-5}$	$2.4 \times 10^{-5}$	$4.3 \times 10^{-4}$	—	$6.6 \times 10^{-4}$	$4.1 \times 10^{-4}$	$7.1 \times 10^{-3}$	
$X(3872)$	3872	3	0	$1^+, 2^-^c$	$c\bar{c}(L=2)$	$q\bar{q}c\bar{c}$	$\bar{D}\bar{D}^*$	$1.0 \times 10^{-4}$	$4.0 \times 10^{-5}$	$7.8 \times 10^{-4}$	$2.9 \times 10^{-4}$	$1.7 \times 10^{-3}$	$6.6 \times 10^{-4}$	$1.3 \times 10^{-2}$	$4.7 \times 10^{-3}$	
$Z^+(4430)^b$	4430	3	1	$0^-^c$	—	$q\bar{q}c\bar{c}(L=1)$	$D_1\bar{D}^*$	—	$1.3 \times 10^{-5}$	$2.0 \times 10^{-5}$	$1.4 \times 10^{-5}$	—	$2.1 \times 10^{-4}$	$3.4 \times 10^{-4}$	$2.4 \times 10^{-4}$	
$T_{cb}^{0a}$	7123	1	0	$0^+$	—	$qqc\bar{b}$	$\bar{D}B$	—	$6.1 \times 10^{-8}$	$1.8 \times 10^{-7}$	$6.9 \times 10^{-7}$	—	$6.1 \times 10^{-6}$	$1.9 \times 10^{-5}$	$6.8 \times 10^{-5}$	
<b>Baryons</b>																
$\Lambda(1405)$	1405	2	0	$1/2^-$	$qqqs(L=1)$	$qqqs\bar{q}$	$\bar{K}N$	0.81	0.11	1.8–8.3	1.7	2.2	0.29	4.7–21	4.2	
$\Theta^+(1530)^b$	1530	2	0	$1/2^+^c$	—	$qqqq\bar{s}(L=1)$	—	—	$2.9 \times 10^{-2}$	—	1.0	—	$7.8 \times 10^{-2}$	—	2.3	
$\bar{K}KN^a$	1920	4	$1/2$	$1/2^+$	—	$qqqs\bar{s}(L=1)$	$\bar{K}KN$	—	$1.9 \times 10^{-2}$	1.7	0.28	—	$5.2 \times 10^{-2}$	4.2	0.67	
$\bar{D}N^a$	2790	2	0	$1/2^-$	—	$qqqq\bar{c}$	$\bar{D}N$	—	$2.9 \times 10^{-3}$	$4.6 \times 10^{-2}$	$1.0 \times 10^{-2}$	—	$2.0 \times 10^{-2}$	0.28	$6.1 \times 10^{-2}$	
$\bar{D}^*N^a$	2919	4	0	$3/2^-$	—	$qqqq\bar{c}(L=2)$	$\bar{D}^*N$	—	$7.1 \times 10^{-4}$	$4.5 \times 10^{-2}$	$1.0 \times 10^{-2}$	—	$4.7 \times 10^{-3}$	0.27	$6.2 \times 10^{-2}$	
$\Theta_{cs}^a$	2980	4	$1/2$	$1/2^+$	—	$qqqs\bar{c}(L=1)$	—	—	$5.9 \times 10^{-4}$	—	$7.2 \times 10^{-3}$	—	$3.9 \times 10^{-3}$	—	$4.5 \times 10^{-2}$	
$BN^a$	6200	2	0	$1/2^-$	—	$qqqq\bar{b}$	$BN$	—	$1.9 \times 10^{-5}$	$8.0 \times 10^{-5}$	$3.9 \times 10^{-5}$	—	$7.7 \times 10^{-4}$	$2.8 \times 10^{-3}$	$1.4 \times 10^{-3}$	
$B^*N^a$	6226	4	0	$3/2^-$	—	$qqqq\bar{b}(L=2)$	$B^*N$	—	$5.3 \times 10^{-6}$	$1.2 \times 10^{-4}$	$6.6 \times 10^{-5}$	—	$2.1 \times 10^{-4}$	$4.4 \times 10^{-3}$	$2.4 \times 10^{-3}$	
<b>Dibaryons</b>																
$H^a$	2245	1	0	$0^+$	$qqqqss$	—	$\Xi N$	$3.0 \times 10^{-3}$	—	$1.6 \times 10^{-2}$	$1.3 \times 10^{-2}$	$8.2 \times 10^{-3}$	—	$3.8 \times 10^{-2}$	$3.2 \times 10^{-2}$	
$\bar{K}NN^b$	2352	2	$1/2$	$0^-^c$	$qqqqqs(L=1)$	$qqqqq\bar{q}s\bar{q}$	$\bar{K}NN$	$5.0 \times 10^{-3}$	$5.1 \times 10^{-4}$	0.011–0.24	$1.6 \times 10^{-2}$	$1.3 \times 10^{-2}$	$1.4 \times 10^{-3}$	0.026–0.54	$3.7 \times 10^{-2}$	
$\Omega\Omega^a$	3228	1	0	$0^+$	$ssssss$	—	$\Omega\Omega$	$3.2 \times 10^{-5}$	—	$1.5 \times 10^{-5}$	$6.4 \times 10^{-5}$	$8.6 \times 10^{-5}$	—	$4.4 \times 10^{-5}$	$1.9 \times 10^{-4}$	
$H_c^{++a}$	3377	3	1	$0^+$	$qqqqsc$	—	$\Xi_c N$	$3.0 \times 10^{-4}$	—	$3.3 \times 10^{-4}$	$7.5 \times 10^{-4}$	$2.0 \times 10^{-3}$	—	$1.9 \times 10^{-3}$	$4.2 \times 10^{-3}$	
$\bar{D}NN^a$	3734	2	$1/2$	$0^-$	—	$qqqqq\bar{q}q\bar{c}$	$\bar{D}NN$	—	$2.9 \times 10^{-5}$	$1.8 \times 10^{-3}$	$7.9 \times 10^{-5}$	—	$2.0 \times 10^{-4}$	$9.8 \times 10^{-3}$	$4.2 \times 10^{-4}$	
$BNN^a$	7147	2	$1/2$	$0^-$	—	$qqqqq\bar{q}q\bar{b}$	$BNN$	—	$2.3 \times 10^{-7}$	$1.2 \times 10^{-6}$	$2.4 \times 10^{-7}$	—	$9.2 \times 10^{-6}$	$3.7 \times 10^{-5}$	$7.6 \times 10^{-6}$	

# Unfortunately little evidence for strange exotic states

Unsuccessful searches for H-Dibaryon and  $\Lambda n$  states in ALICE



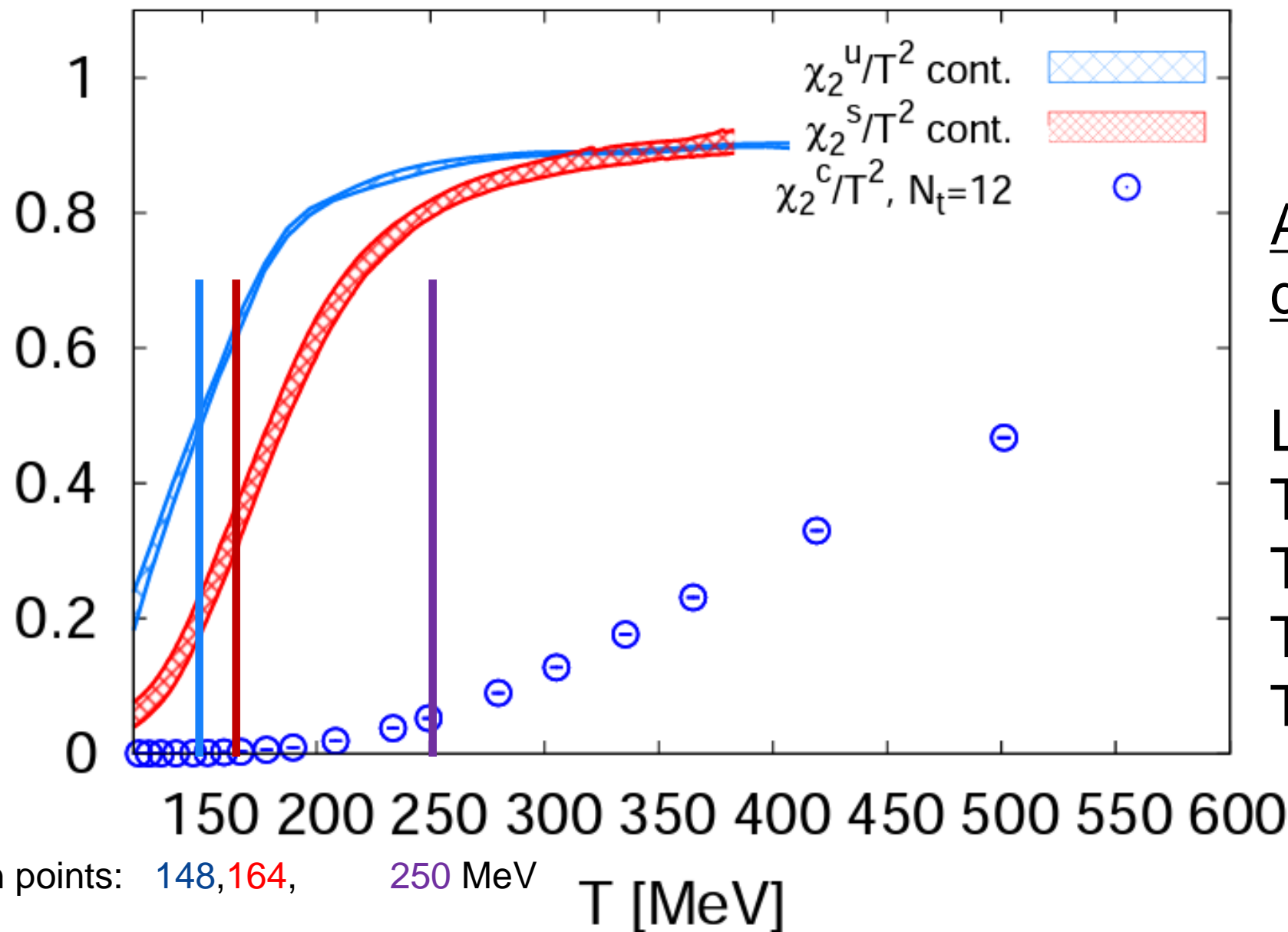
# Summary / Conclusions

- High precision (continuum limit) lattice QCD susceptibility ratios indicate *flavor separation in the crossover from the partonic to the hadronic matter*.
- There are hints, when comparing to hadron resonance gas and PNJL calculations, that this could lead to a short phase during the crossover in which strange particle formation is dominant.
- If the abundance of strange quarks is sufficiently high (LHC) this could lead to *enhancements in the strange hadron yields (evidence from ALICE)* and it could lead to *strangeness clustering (exotic states: dibaryons, strangelets)*.
- It could also lead to evidence for *higher mass strange Hagedorn states* (as predicted by Quark Model (for the low mass part of the spectrum))
- A new experimental verification method for flavor separation can be devised by measuring the higher moments of the strangeness production in comparison to light quark production.
- The translation of lattice susceptibility ratios to higher moments of measured multiplicity distributions is not trivial but possible. It needs exact mapping of the measurable states.
- The question remains whether any separation of flavor hadronization requires pure flavor states (e.g.  $p$  vs.  $\Omega$ ), as indicated by HotQCD charm study

# Backup slides

# Lattice QCD flavor susceptibility predictions

And then there was charm.....amazing if thermal.....



C. Ratti et al., QM 2012

A mixed phase of degrees of freedom ?

LHC evolution:

$T_{\text{init}} \sim 650$  MeV

$T_{\text{dyn.part.}} = 650-250$  MeV

$T_{\text{mixed}} = 250-150$  MeV

$T_{\text{hadr}} < 150$  MeV

....clearly a quark mass effect, but is it relevant for the hadronization behavior of the flavor ?



# Is the charm curve relevant at the LHC ?

Only if charm is in chemical equilibrium at  $T = 250$  MeV and at least in part thermally produced

Charm is predominantly produced in first collisions (gluon-gluon interactions)

But, assuming  $T_{\text{init}} \sim > 600$  MeV and  $T_{\text{ch}} = 250$  MeV, there might be finite contribution from equilibrated phase.

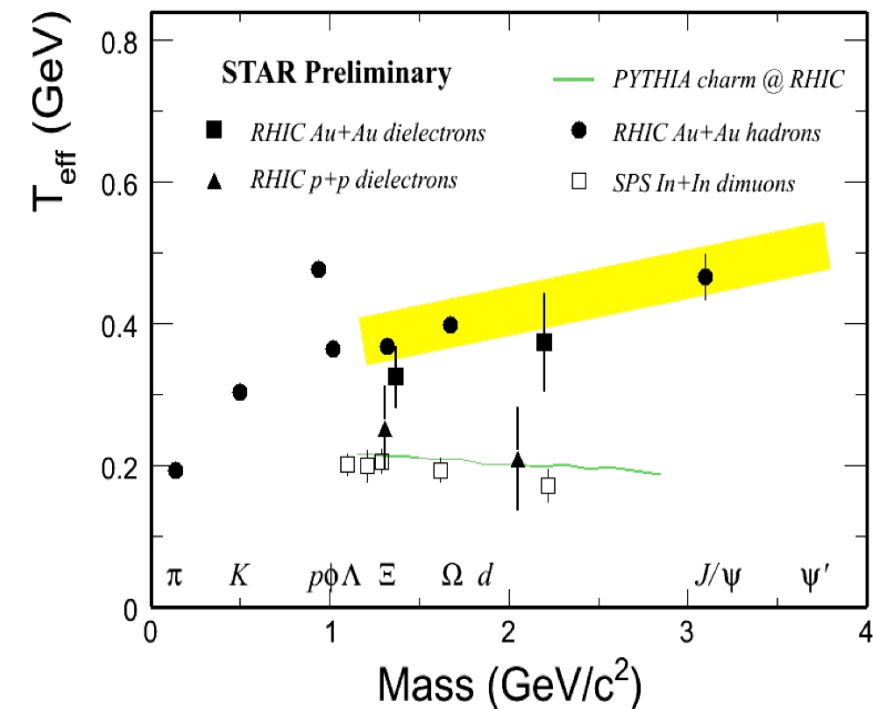
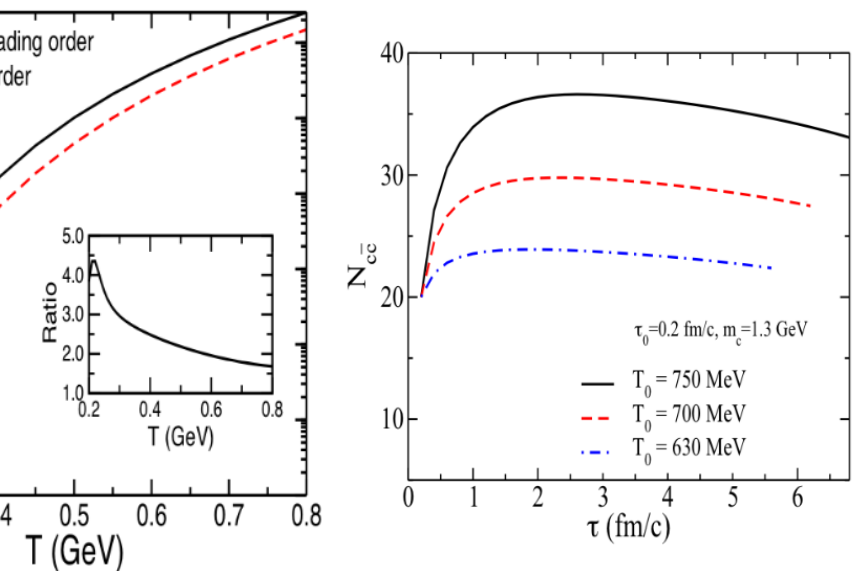
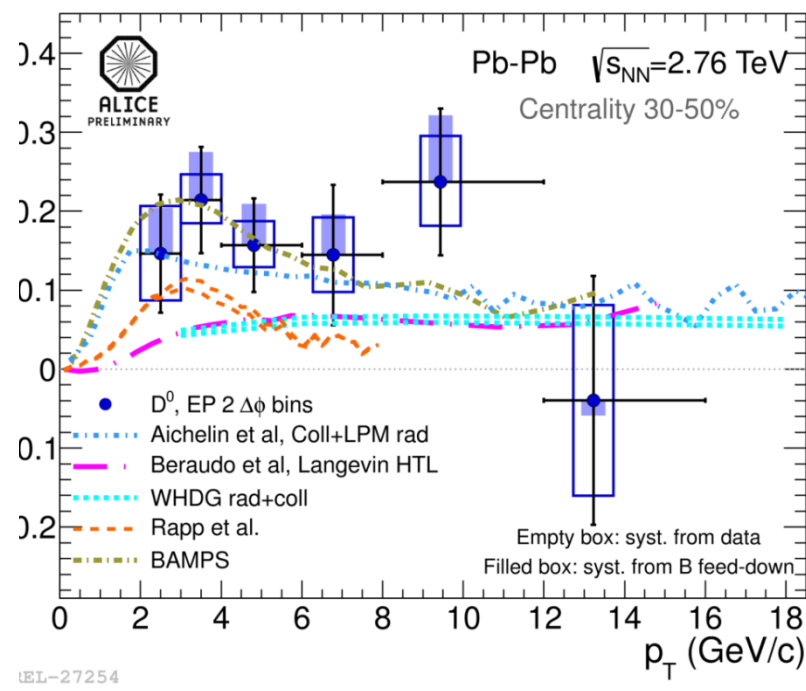
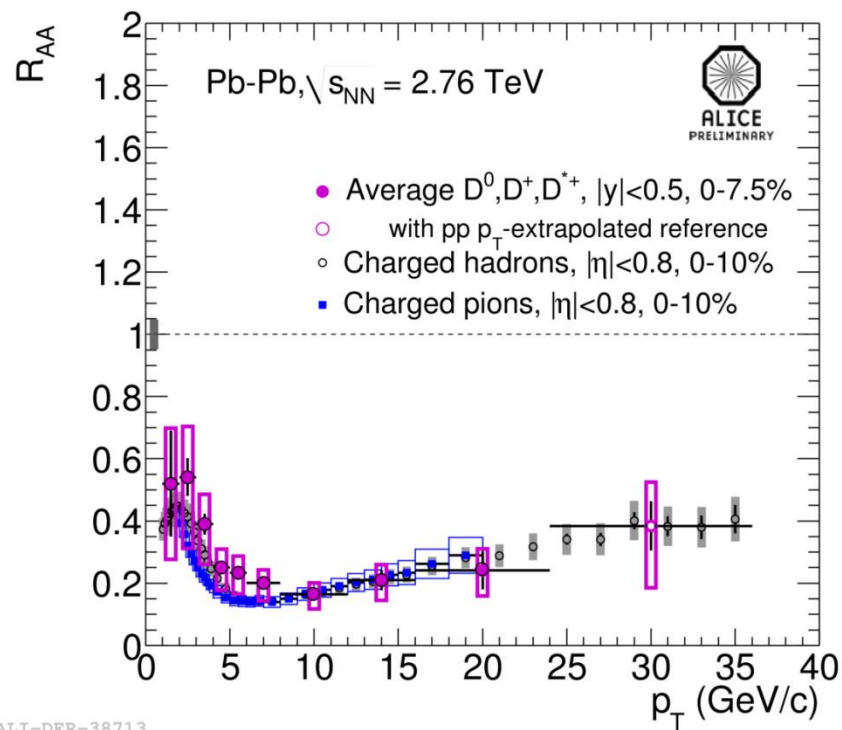
## Theory:

Redlich, Stachel, et al.: thermal production is negligible

Rafelski et al.: charm is over-abundant (hep-ph/0605307)

Zhang, Ko, Liu: thermal production significant (arXiv:0709.1684)

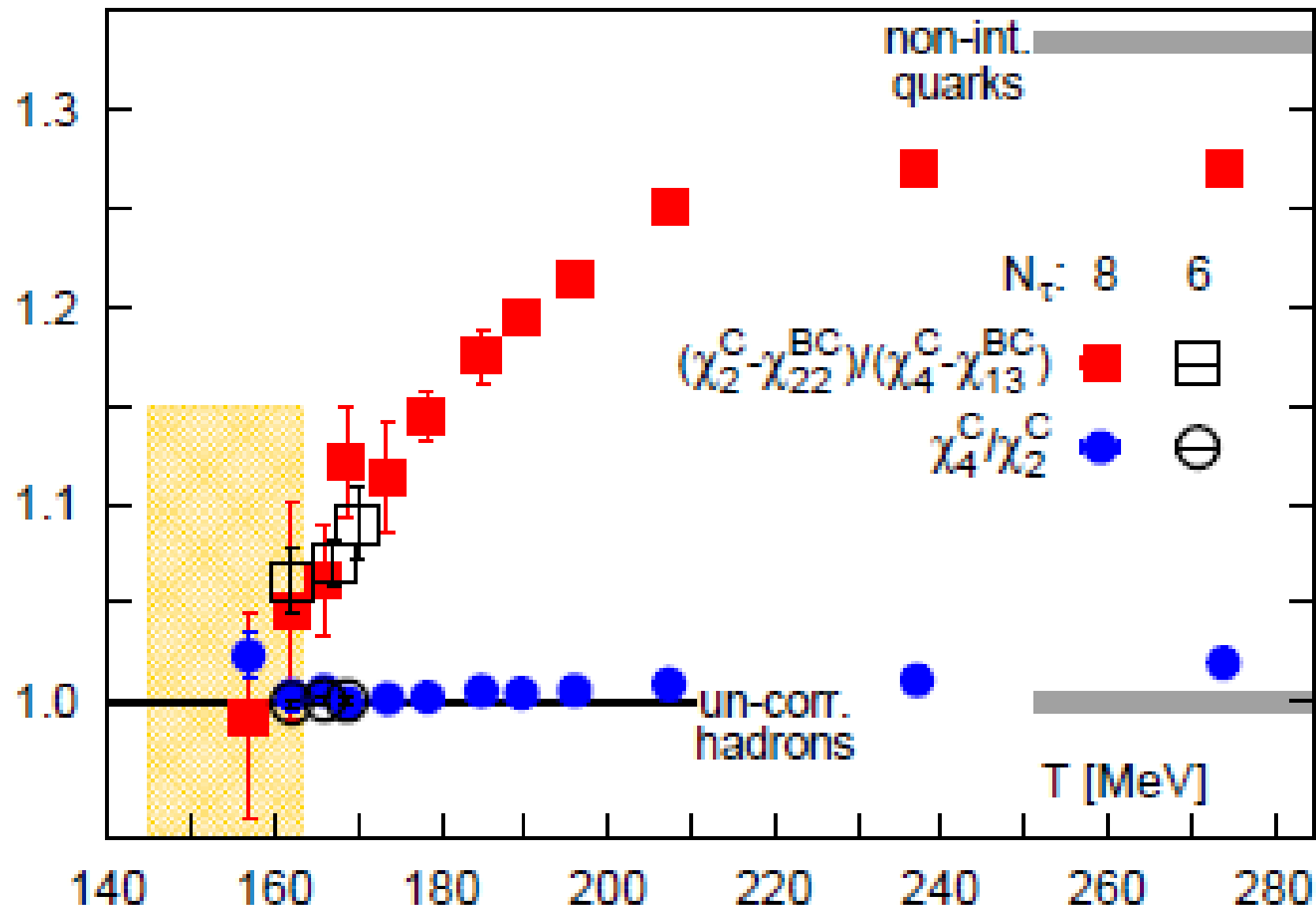
## Experiment: Charm $v_2$ & $R_{\Delta\Delta}$ : hints of equilibration



Even if charm is not thermally produced but thermalizes along the way then the yields might not be affected but the  $p_T$ -spectrum should still show the effect.

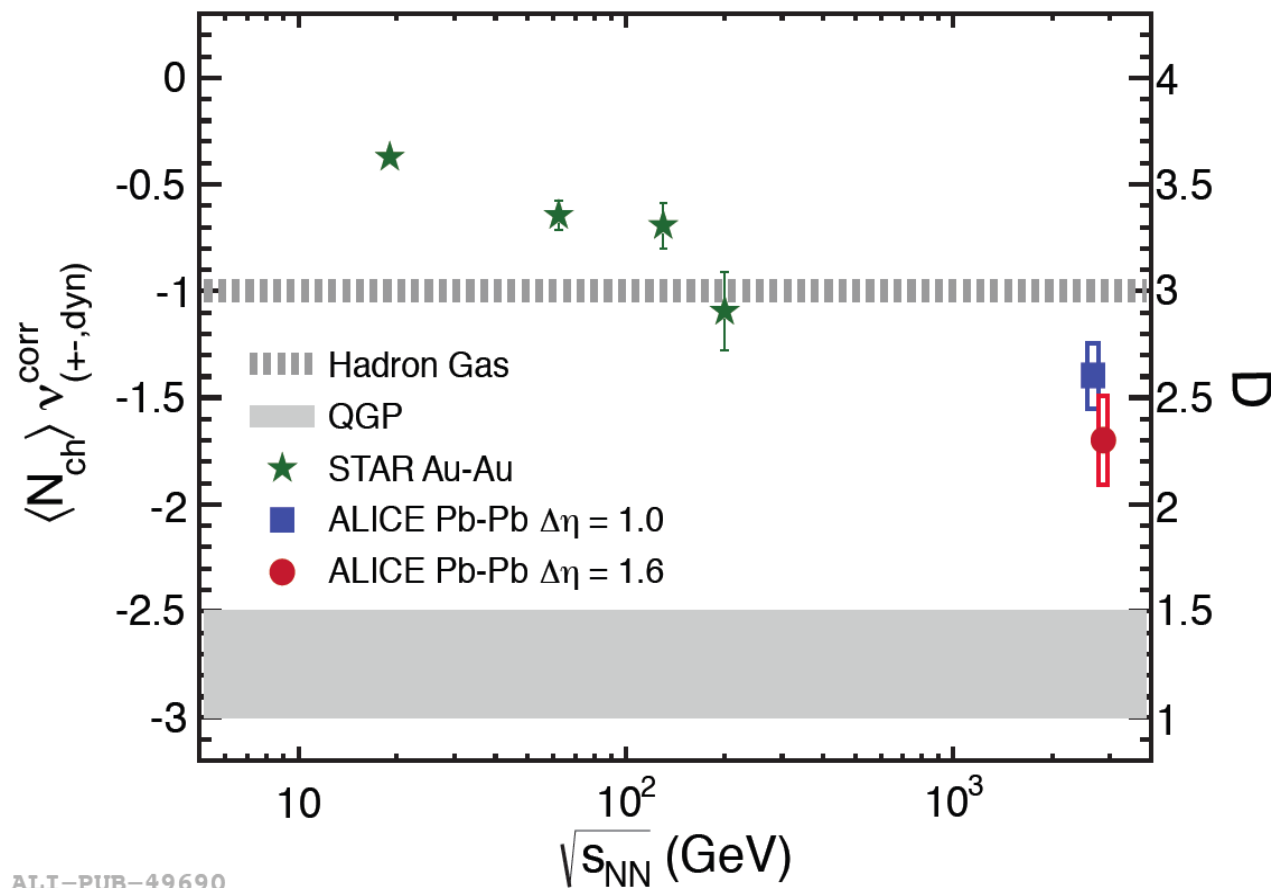


# Interesting study by HotQCD

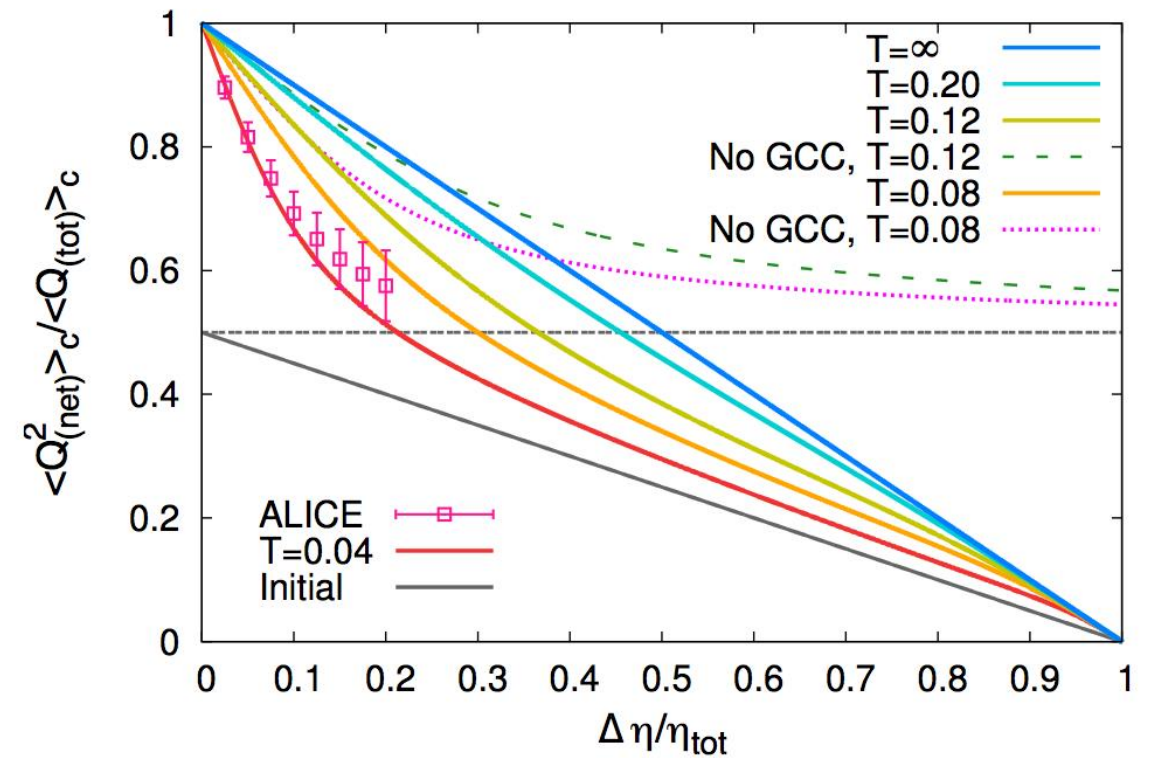


Open charm mesons have transition temperature similar to light quark hadrons (arXiv:1404.4043)

# On the issue of global charge conservation



ALICE, PRL 110, 152310 (2013)

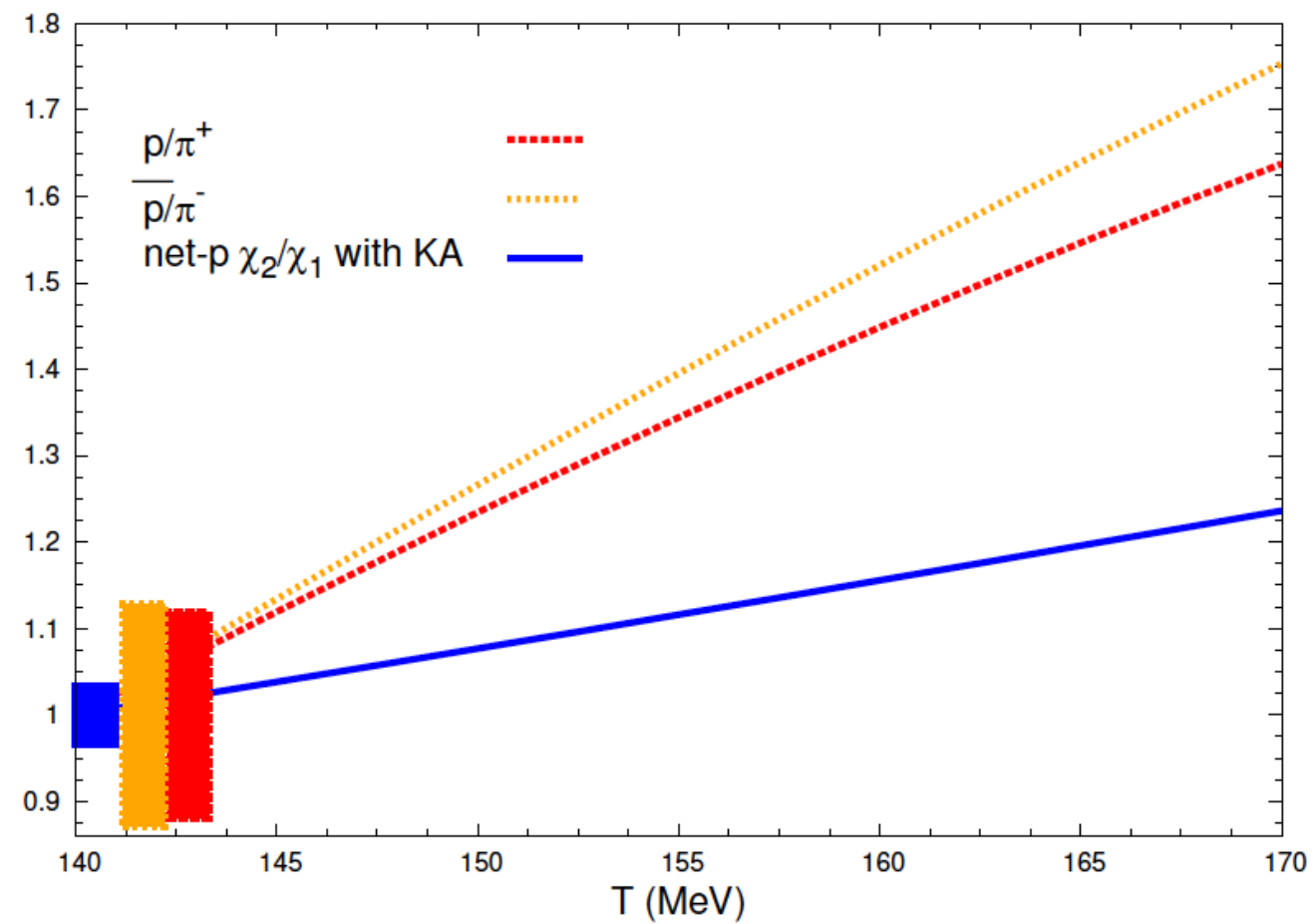
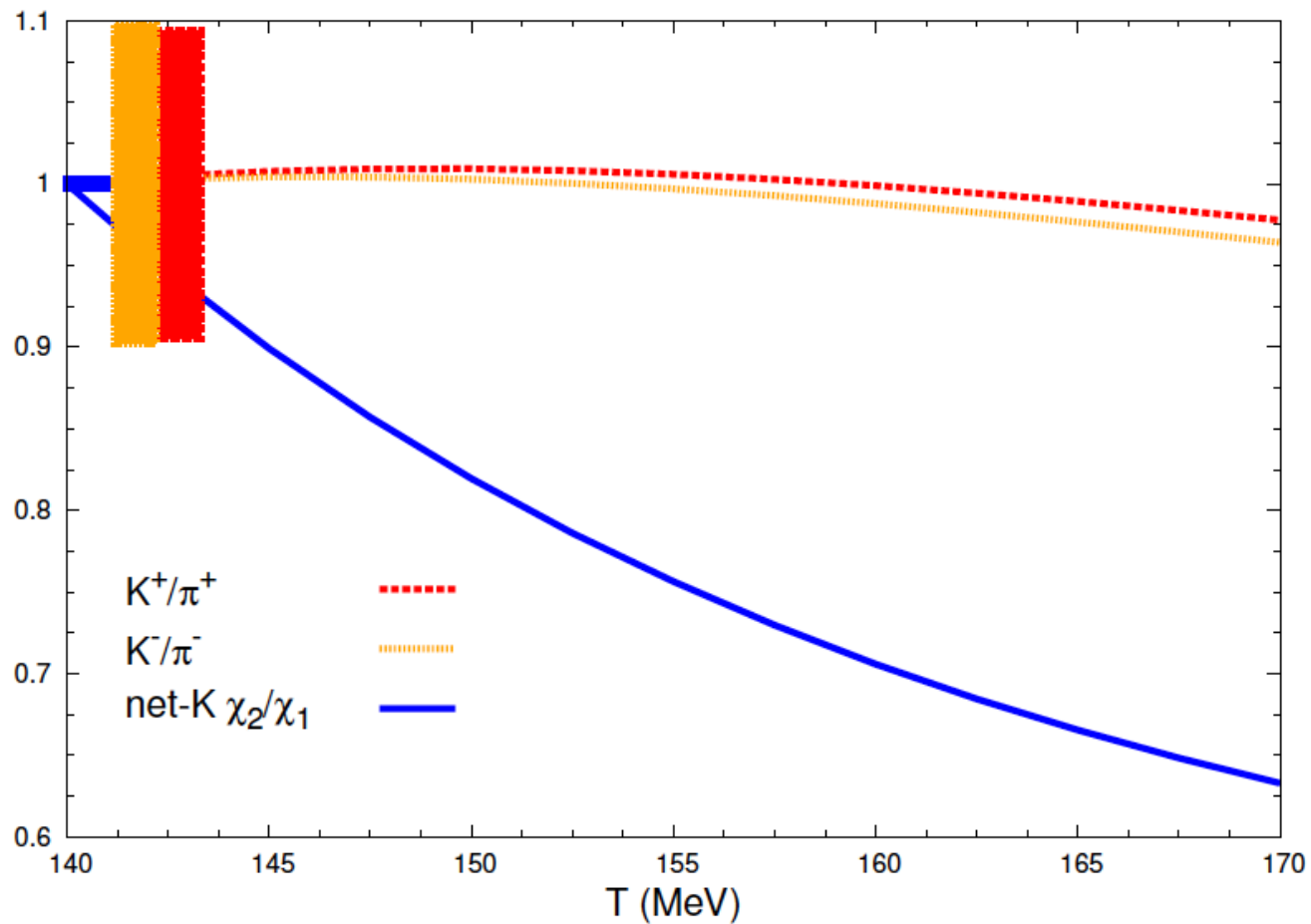


Sakaida, Asakawa, Kitazawa, arXiv:1409.6866

The pseudo-rapidity coverage in STAR and ALICE is such that GCC effect are negligible

# Kaons fluctuations show a remarkable sensitivity to the chemical freeze-out temperature

Comparing the temperature sensitivity of particle ratios and lower moment fluctuation ratios for kaons and protons in a HRG model



arXiv:

# Experimental error bars on particle ratios

(are the too big and why are they bigger than the fluctuation uncertainties ?)

**STAR has presented detailed uncertainty evaluations, separately for  $\pi, k, p$  and  $V0$ 's:**

For  $p, k, p$  PRC (2008), arXiv:0808.2041

For all strange baryons: PRL (2006), nucl-ex/0606014

## **Included in systematics for $\pi, k, p$ :**

PID uncertainties (all  $dE/dx$  and TOF cross check), small  $p_T$  coverage, Fit function uncertainties

## **Not included for $\pi, k, p$ :**

Lambda feed-down correction (obtained from Andronic plot (points larger than error bars)), proton background uncertainty (spallation)

General uncertainty between 10-15%

## **Included in systematics for $V0$ :**

Feed-down correction,  $V0$  cuts, magnetic field settings,  $p_T$  dependence

## **Not included for $V0$ :**

Fit function variation ( $p_T$ -coverage around 60-70%) yields probably an additional 10% uncertainty

General uncertainty: ~20%

Since fluctuation measurements are not extrapolated their uncertainties can be smaller.  
Ultimately all uncertainties that were used are as published by STAR