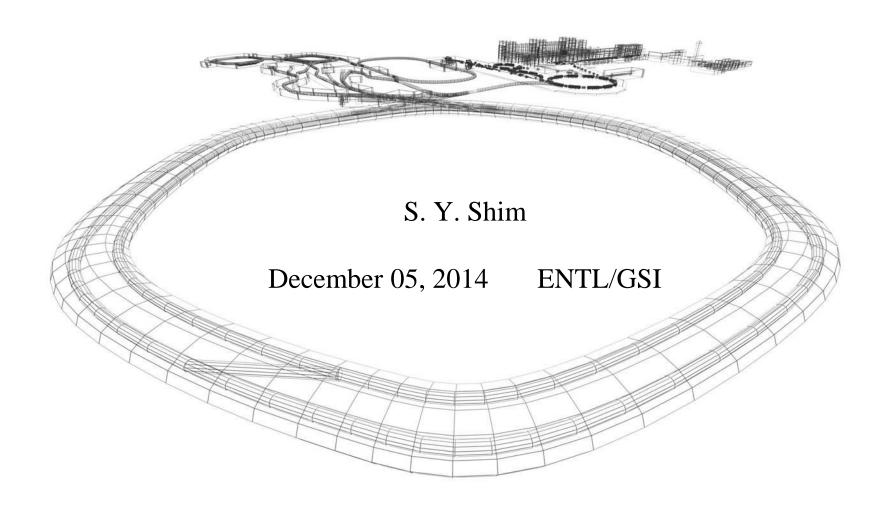
# Influence of Driving Current Ripple on CR Dipole Magnetic Field





#### Contents



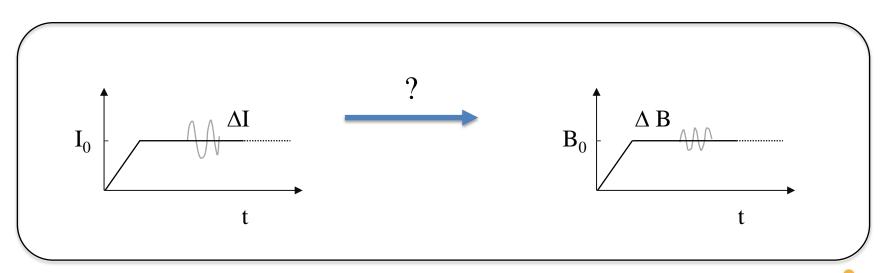
- 1. Motivation
- 2. Parametric conditions for simulation
- 3. CR dipole magnet geometry and FE model
- 4. DC operation property
- 5. Current ripple effect on magnetic field
  - Center of magnet, inside of magnet
  - Beam space average value
- 6. Summary and conclusion
- 7. Appendix
  - Material property Iron yoke BH curve with packing factor

#### Motivation



- The driving current unstability was reported considering the CR magnets circuit. And it may give a change of magnetic field.
- Therefore, we need to clarify the relation between rippling current and corresponding magnetic field.
- The proportional ratio  $\alpha$  can be expressed by following relation.

$$\frac{\Delta B}{B_0} = \alpha \frac{\Delta I}{I_0}$$



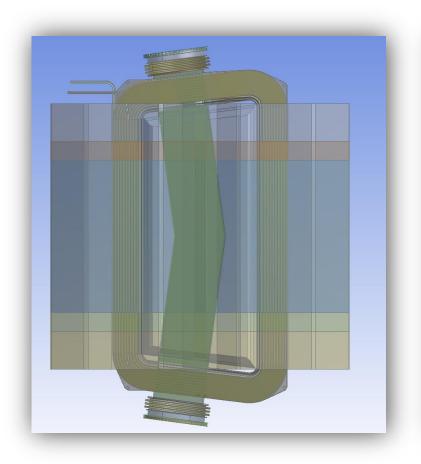
#### Parametric Condition

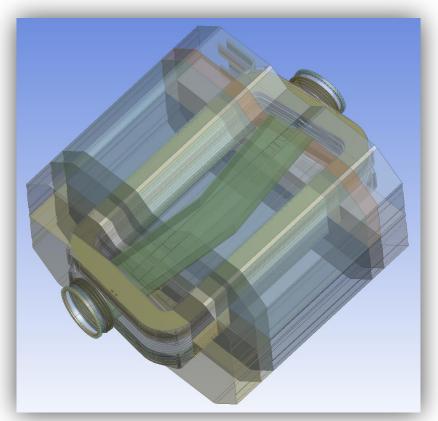


- The  $\alpha$  depends on not only frequency but also  $I_0$  and  $\Delta I$ .
- The frequency range of rippling current is  $10 \sim 10 \text{ kHz}$ .
- The maximum amplitude of current ripple is assumed to be  $\Delta I_{max}/I_0 = 10^{-4}$ .
- The desired field stability is  $\Delta B_{\text{max}}/B_0 \cong 10^{-6}$ .
- The operation field for Collect Ring is  $B_0 = 1.6$  T and corresponding applied current  $I_0$  is about 1.4 kA.



### Geometry of CR dipole magnet

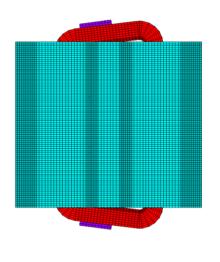


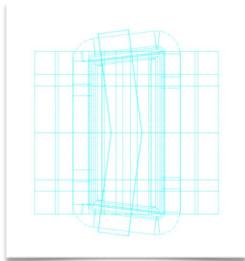




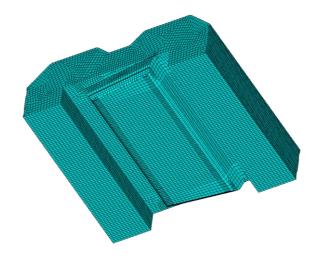
### FE model







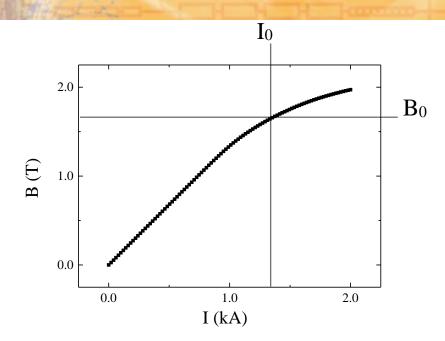


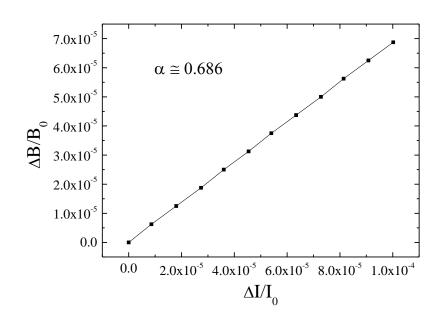




#### DC Property



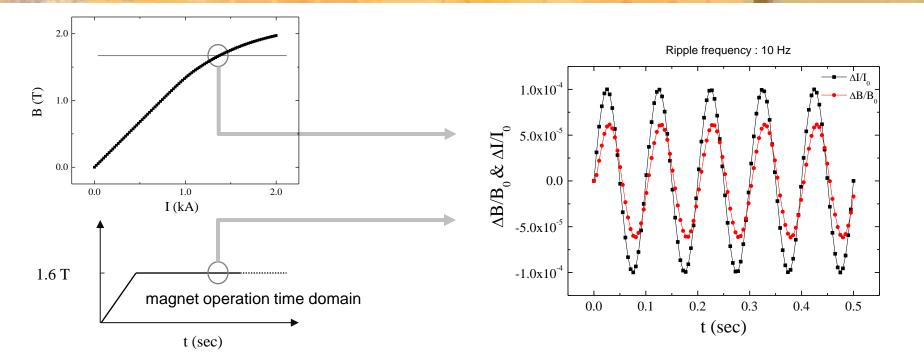




- This result shows field operation property as a function of DC current.
- It enables us to estimate the maximum  $\alpha$  as a reference value to interpret the results of AC ripple effect.
- The DC proportional parameter  $\alpha$  is 0.686.
- This curve depends on material property and is shown in Appendix 1.



### Current Ripple Effect 1

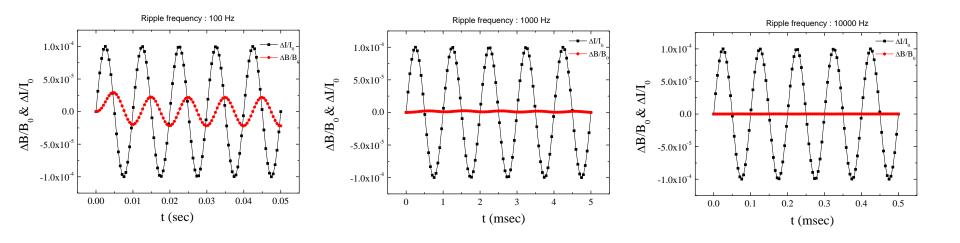


- The current ripple is produced in the range of  $10 \sim 10$  kHz at the reference field 1.6 T.
- The corresponding  $\alpha$  value is similar to that of DC current in 10 Hz.
- The result of higher frequency is shown in the next slide.



### Current Ripple Effect 2



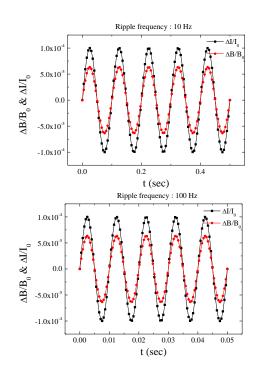


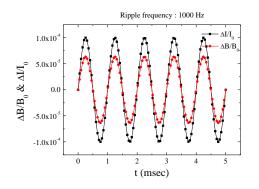
- The amplitude of field response is decreased by increasing ripple frequency.
- The reason of this field amplitude decreasing is secondary field by eddy current on the beam chamber. And it is confirmed by comparative simulation with and without beam chamber.

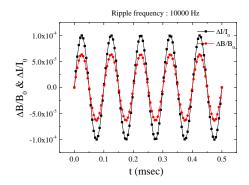


#### Without beam chamber





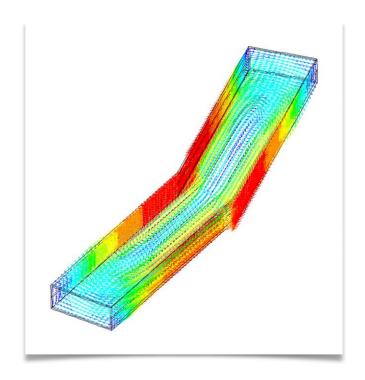




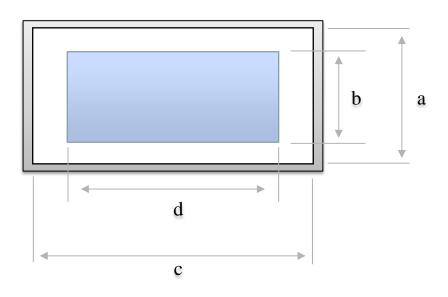
- The results are from the simulation without beam chamber.
- There is no frequency dependence of  $\Delta B/B_0$  without beam chamber.
- The secondary field by eddy current on the beam chamber is the origin of the high frequency shielding.



### Space for average calculation



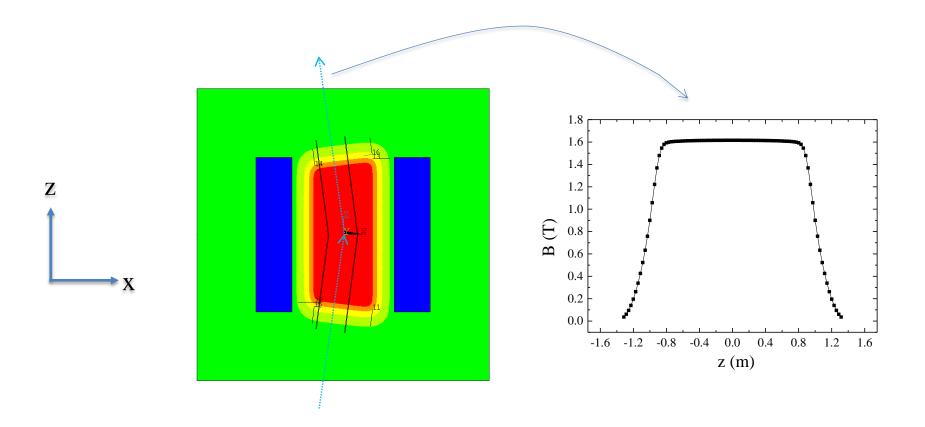
Eddy current density profile.



The ratio of area for finding average  $\alpha$  is b/a = 6/10, d/c = 11/15

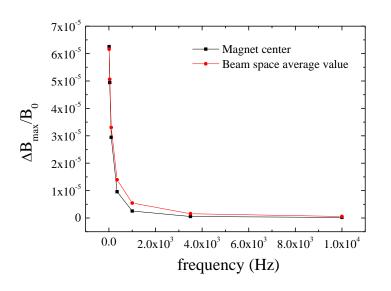


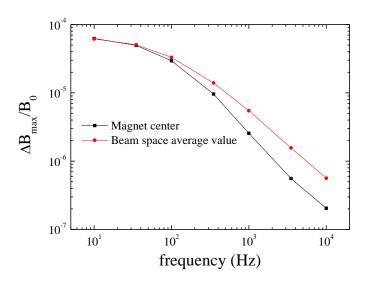
### Static field profile on beam axis





### ΔB/B<sub>0</sub> according to Ripple Frequency



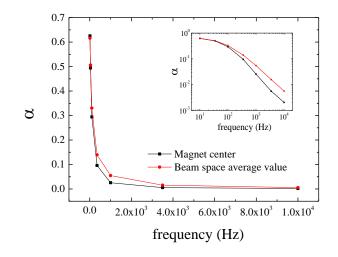


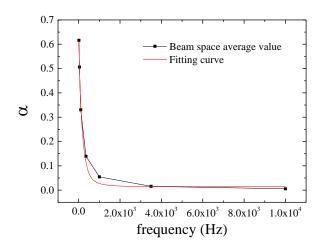
- The figures show the  $\Delta B_{max}/B_0$  as a function of current ripple frequency.
- The  $\Delta B/B_0$  has a rapid decreasing with increasing frequency in the low frequency region.



### Proportional Variable $\alpha(f)$







• We can estimate functional expression with curve fitting procedure and the result shown below.

$$\frac{\Delta B}{B_0} = \alpha(f) \frac{\Delta I}{I_0} \longrightarrow \alpha(f) \cong a + b \times c^f$$

$$a \cong 0.015$$

$$b \cong 0.65$$

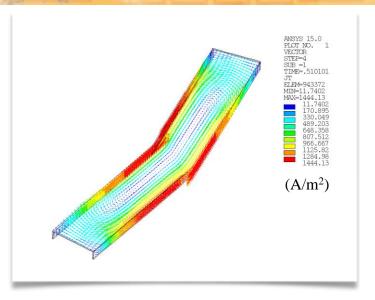
$$c \cong 0.99205$$

- The  $\alpha$  is close to the value of DC result with decreasing f down to zero.
- The  $\alpha$  is less than  $1.0 \times 10^{-2}$  with frequency of higher than  $\sim 2$  kHz and  $\sim 5$  kHz at the center of magnet and considered beam space, respectively.

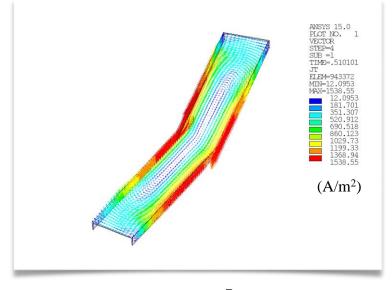


#### Beam chamber resistivity





 $\rho_{ref} = 7.5067 \times 10^{-7} \ \Omega m$ 



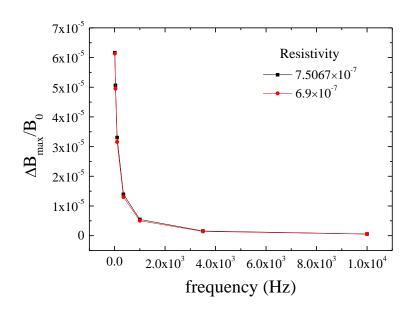
$$\rho = 6.9 \times 10^{-7} \ \Omega \mathrm{m}$$

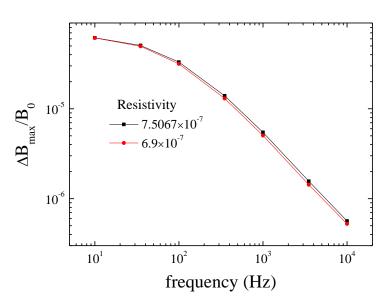
- The field shield effect is due to the eddy current in the beam chamber. Therefore, the resistivity of the beam chamber can be a parameter which can affect magnetic field ripple.
- To get more reasonable interpretation for this simulation, additional calculation has been done with another low resistivity of  $6.9 \times 10^{-7} \Omega m$ .



### Resistivity effect



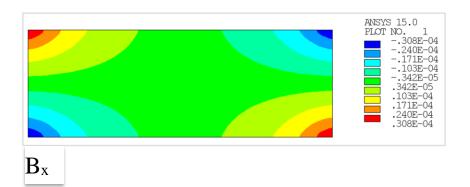


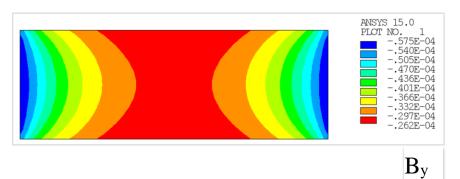


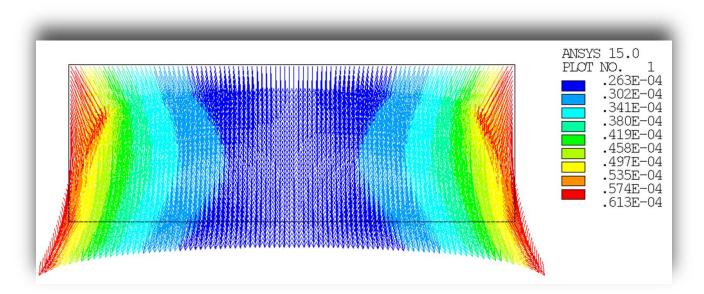
•  $\Delta f$  is  $\sim 400$  Hz at  $\Delta B_{\text{max}}/B_0 = 10^{-6}$ .



## Eddy current induced magnetic field inside beam chamber - 10 kHz









unit: Tesla 17

### Summary & Conclusion

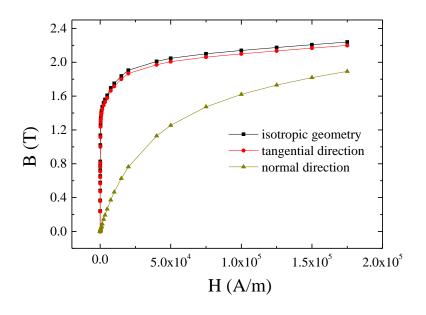


- To find the current ripple effect on magnetic field, the variable  $\alpha$  is needed to be clarified.
- The  $\alpha$  variable reaches to  $10^{-2}$  around 2 kHz and 5.5 kHz around the center of magnet and beam space, respectively.
- The reason of this field shielding effect is the magnetic field by eddy current in beam chamber.
- The eddy current on the rectangular shaped beam chamber generates not only dipole but also all other higher odd-number multipoles. The eddy current density is ~ 25 times lower than that of SIS100 dipole beam chamber. Even though the different geometry and eddy current profile, we can expect negligibly small higher odd-number multipoles.
- Result of resistivity dependence can be used for the practical interpretation after having confirmation of real material parameters of CR dipole construction.



#### Appendix 1 - Material property





$$\mu_n = \frac{\mu_0 \mu}{p\mu_0 + (1 - p) \mu}$$
$$\mu_t = p\mu + (1 - p) \mu_0$$

- $\mu_n$  and  $\mu_t$  is magnetic permeability of laminated material with normal and tangential direction, respectively.
- The 98 % packing factor, p = 0.98, is considered for this simulation.
- We can produce FE model which has laminated yoke property with un-laminated iron yoke FE model after applying this curve.

