

# Update on TDA measurements with $p\bar{p} \rightarrow \pi^0 e^+ e^-$ reaction based on EPJA referees' comments: Test of factorisation

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Electromagnetic Processes Session  
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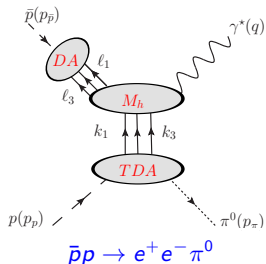
- 1 Introduction
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- 3 Summary of Previous Analysis
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- 5 Summary and Conclusions

# Transition Distribution Amplitudes

## TDA:

- New non-perturbative objects
  - Hard scale: high momentum transfer
  - Low transversal momentum for the  $\pi^0$
- Transition between a Baryon and a Meson
- Information about the Meson-cloud inside the proton
  - Fourier transform of a Matrix Element of a three-quark light-cone local operator
  - Generalization of GPDs

In CM of  $\overline{\text{PANDA}}$   
 $\pi^0$  backward  $\rightarrow$  emitted by  $p$   
 $\pi^0$  forward  $\rightarrow$  emitted by  $\bar{p}$



Experimentally accessible through  $\bar{p}p \rightarrow \gamma^*\pi^0 \rightarrow e^+e^+\pi^0$  which admits QCD collinear factorisation in terms of Distribution Amplitudes and Transition Distribution Amplitudes

Validity of QCD factorization and access to TDAs

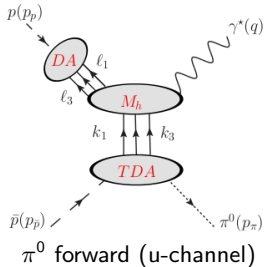
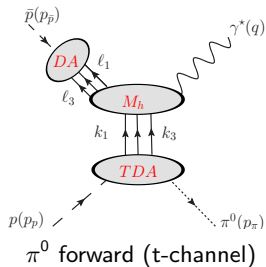
$\rightarrow$  kinematics accessible by  $\overline{\text{PANDA}}$

Studies based on: J. P. Lansberg et al., Phys Rev D 76, 111502(R) (2007)

# TDA's factorisation

Two subprocesses,  $p\bar{p} \rightarrow \gamma^*$  and  $\gamma^* \rightarrow e^+e^-$ , accept factorized description when:

- $q^2 \sim s$
- $t \ll q^2$  or  $u \ll q^2 \Rightarrow \pi^0$  emitted in  $\bar{p}$  direction (fw) or in the  $p$  direction (bw)



$$\mathcal{M}(\bar{p}p \rightarrow \gamma^* \pi^0) = \mathcal{M}_{\text{parton, parton}} \otimes (\text{DA}, \text{TDA})$$

$$\Rightarrow \left. \frac{d\sigma}{dt dq^2 d \cos \theta_\ell^*} \right|_{\Delta_T=0} = \frac{K}{s-4M^2} \frac{1}{(q^2)^5} (1 + \cos^2 \theta_\ell^*) \quad \text{with} \quad K = \frac{(4\pi\alpha_{\text{em}})^2 (4\pi\alpha_s)^4 f_M^4 |\mathcal{I}|^2}{64 \cdot 54^2 (2\pi)^3 f_\pi^2}$$

DA, TDA MODEL

SCALING

LEPTON PHASE-SPACE IN  $\gamma^*$  REST FRAME

Sent to EPJA:

- Analysis of **Signal Reconstruction Efficiency**
- Analysis of **Background Suppression**
- Study of the **Precision of Measurement of the Signal Cross Section**

Comments of the EPJA Referees:

- The analysis would be more complete if we include the **test of factorisation**
  - $q^2$  factorisation:

$$\frac{d\sigma}{dq^2} \sim \frac{1}{(q^2)^5}$$

- $\cos \theta^*$  factorisation:

$$\frac{d\sigma}{d \cos \theta^*} \sim (1 + 1 \cdot \cos^2 \theta^*)$$

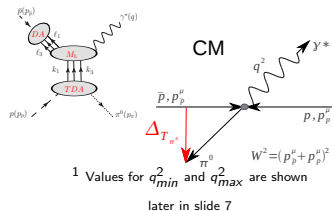
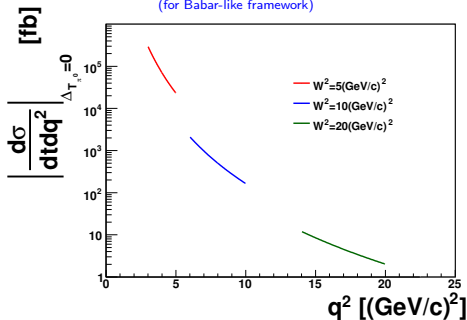
# Simulation of $\bar{p}p \rightarrow e^+e^-\pi^0$ and $\bar{p}p \rightarrow \pi^+\pi^-\pi^0$

Signal:  $\bar{p}p \rightarrow e^+e^-\pi^0$

- $W^2=5 \text{ GeV}^2$  and  $10 \text{ GeV}^2$  ( $W^2=s$ )
- $\pi^0$  Forward and Backward  
→ 4 simulations
- $\frac{d\sigma}{dq^2}$  calculated for  $\pi$ -transverse momentum  $\Delta_{T_{\pi^0}} = 0$ ,
- extrapolated over a  $\Delta_{T_{\pi^0}} < 0.5 \text{ GeV}$  and  $[q_{min}^2, q_{max}^2]$ <sup>1</sup>

Input for the Event Generator

(for Babar-like framework)



Background:  $\bar{p}p \rightarrow \pi^+\pi^-\pi^0$

- No data
- The same angular distribution as the signal
- Considered to be  $10^6$  times higher

## Event selection: Combinations of $\pi^0 + e^+ + e^-$ candidates per event

- Particle identification cuts (PID):
  - Two charged tracks
  - One positive very tight electron and one negative very tight electron
  - Two photons reconstructing a  $\pi^0$
- Kinematical fit:
  - Used only to improve the quality of the data, but no cuts on CL or  $\chi^2$  are applied.

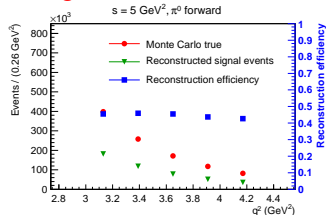
## Kinematic region selection (Factorization validity)

- $q^2$  cuts in the region in which the cross section is integrated

	$W^2 = 5 \text{ GeV}^2$	$W^2 = 10 \text{ GeV}^2$
Analysis limits	$3.8 < q^2 < 4.2$	$7.00 < q^2 < 8.00$
Expected Statistics ( $\mathcal{L} = 2 \text{ fb}^{-1}$ )	$\sim 3350$	$\sim 465$

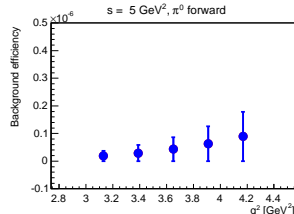
- $|\cos\theta_{\pi^0}| > 0.5 \Rightarrow \Delta_{T_{\pi^0}} < 0.5 \text{ GeV}$  (QCD factorisation)

## 1.- Signal Reconstruction Efficiency



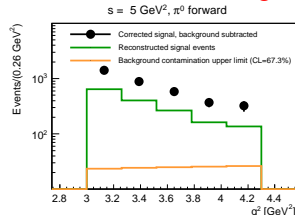
$\sim 45\% @ W^2 = 5 \text{ GeV}^2$  fw;  $33\% - 43\% @ W^2 = 5 \text{ GeV}^2$  bw;  
 $\sim 45\% @ W^2 = 10 \text{ GeV}^2$  fw;  $25\% - 40\% @ W^2 = 10 \text{ GeV}^2$  bw

## 2.- Background Efficiency



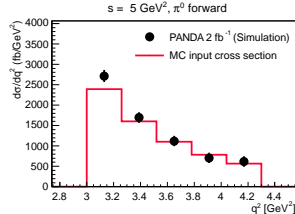
Background suppression:  $5 \cdot 10^7 - 10^7 @ W^2 = 5 \text{ GeV}^2$ ;  
 $10^8 - 6 \cdot 10^6 @ W^2 = 10 \text{ GeV}^2$

## 3.- Subtraction of Background



Background pollution: Few % @ low  $q^2$ ;  
 $< 20\% @$  higher  $q^2$

## 4.- Measured Cross Section



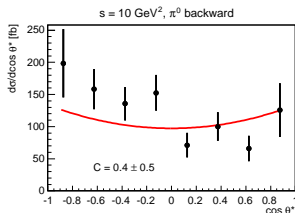
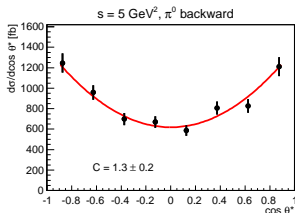
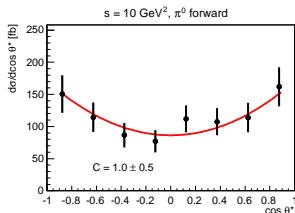
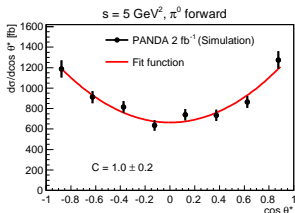
Precision:  $6\% - 21\% @ W^2 = 5 \text{ GeV}^2$ ;  
 $11\% - 90\% @ W^2 = 10 \text{ GeV}^2$ ;  $10\% - 60\% @ W^2 = 10 \text{ GeV}^2$



# New analysis: Test of factorisation, term on $(1 + \cos^2 \theta^*)$

$$\left. \frac{d\sigma}{dt dq^2 d \cos \theta^*} \right|_{\Delta_T=0} = \frac{K}{s-4M^2} \frac{1}{(q^2)^5} (1 + \cos^2 \theta^*) \Rightarrow \frac{d\sigma}{d \cos^2 \theta^*} \sim (1 + 1 \cdot \cos^2 \theta^*)$$

Fit function:  $f(\cos^2 \theta) = D \cdot (1 + C \cdot \cos^2 \theta) \xrightarrow{\text{bin average}} g(x) = \frac{1}{a} \int_{x-a/2}^{x+a/2} D \cdot (1 + C \cdot x^2) dx$   
with  $x = \cos \theta$



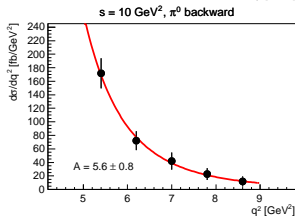
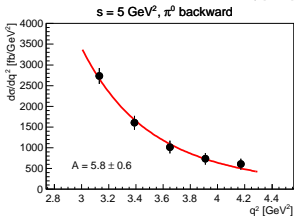
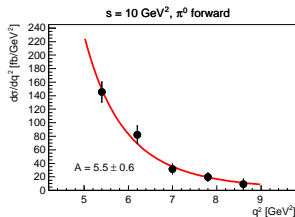
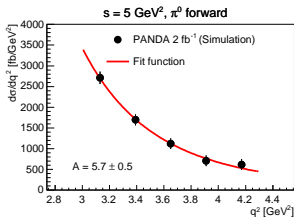
$$\rightarrow \langle C \rangle \pm \sigma_{n-1} = 0.925 \pm 0.377$$

Leaving out the fit for  $W^2 = 10 \text{ GeV}^2 \pi^0\text{-bw}$ :  $\langle C \rangle \pm \sigma_{n-1} = 1.1 \pm 0.17$

# New analysis: Test of factorisation, term on $\frac{1}{(q^2)^5}$ (I)

$$\left. \frac{d\sigma}{dt dq^2 d\cos\theta_\ell^*} \right|_{p_T=0} = \frac{K}{s-4M^2} \frac{1}{(q^2)^5} (1 + \cos^2\theta^*) \Rightarrow \frac{d\sigma}{dq^2} \sim \frac{1}{(q^2)^5}$$

Fit function:  $f(q^2) = B \frac{1}{(q^2)^A}$   $\xrightarrow{\text{bin average}}$   $g(x) = \frac{1}{a} \int_{x-a/2}^{x+a/2} B \frac{1}{x^A} dx$  with  $x = q^2$



$\rightarrow \langle A \rangle \pm \sigma_{n-1} = 5.65 \pm 0.13 \Rightarrow$  **Scaling factor systematically higher!!**

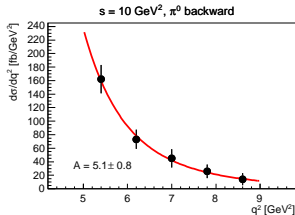
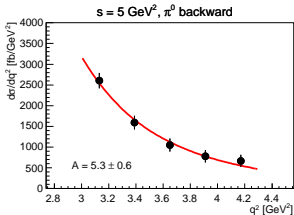
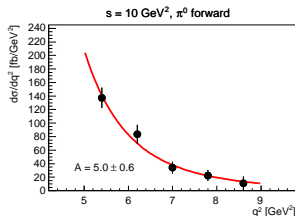
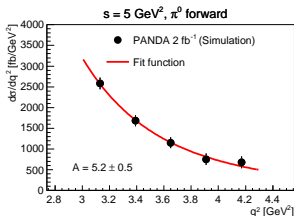
$\rightarrow$  Data have been reweighted keeping the same total measured cross section to correct the error in the event generator and refitted.

# New analysis: Test of factorisation, term on $\frac{1}{(q^2)^5}$ (II)

$$\left. \frac{d\sigma}{dt dq^2 d\cos\theta^*} \right|_{p_T=0} = \frac{K}{s-4M^2} \frac{1}{(q^2)^5} (1 + \cos^2\theta^*) \Rightarrow \frac{d\sigma}{dq^2} \sim \frac{1}{(q^2)^5}$$

Fit function:  $f(q^2) = B \frac{1}{(q^2)^A} \xrightarrow{\text{bin average}} g(x) = \frac{1}{a} \int_{x-a/2}^{x+a/2} B \frac{1}{x^A} dx$  with  $x = q^2$

Reweighted



$$\rightarrow \langle A \rangle \pm \sigma_{n-1} = 5.15 \pm 0.13$$

## Summary

- The Analysis have been extended following the comments of the referees.
- Thanks to that a mistake in the cuts for  $\cos \theta_{lab} < -0.83$  was found and corrected.
- A problem with the dependence of  $q^2$  in the event generator was also found.
- The dependence of  $q^2$  has been corrected reweighting the data and fitting again

## Conclusions:

- We can measure the factorization with an accuracy:
  - $\langle A \rangle \pm \sigma_{n-1} = 5.15 \pm 0.13$  for the scaling factor of  $\frac{1}{(q^2)^A}$ ,
  - and  $\langle C \rangle \pm \sigma_{n-1} = 0.925 \pm 0.377$  for the  $(1 + C \cdot \cos \theta^*)$  dependence.
- After correcting the small errors in the Analysis no changes in the conclusions of the paper have been found.

THANKS FOR LISTENING