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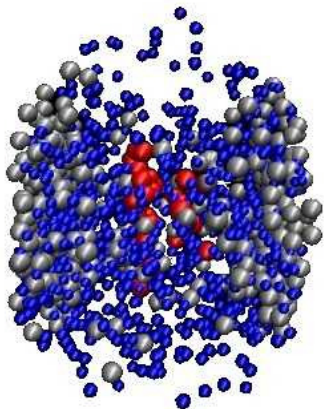
HIC
for **FAIR**
Helmholtz International Center

GOETHE
UNIVERSITÄT
FRANKFURT AM MAIN

Theory and HPC

Elena Bratkovskaya

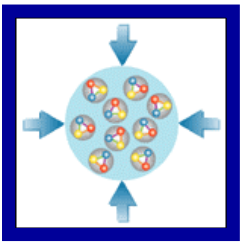
**Institut für Theoretische Physik & FIAS,
Uni. Frankfurt**



*HIC for FAIR Physics Day: HPC Computing,
FIAS, Frankfurt am Main*

11 November 2014





Physics at FAIR

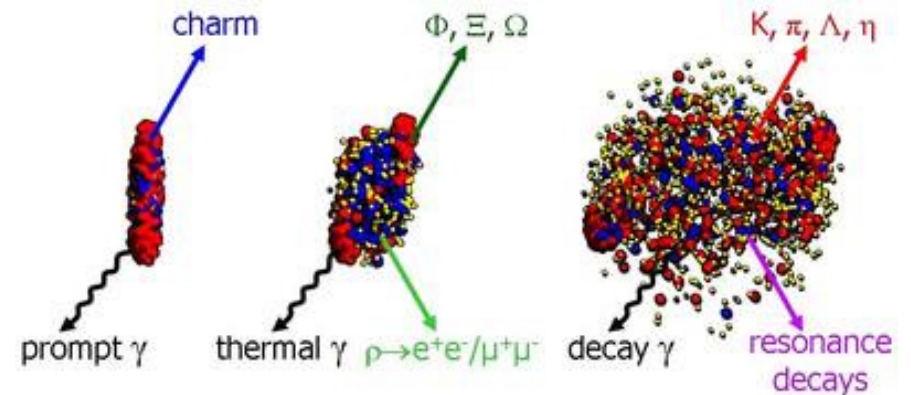
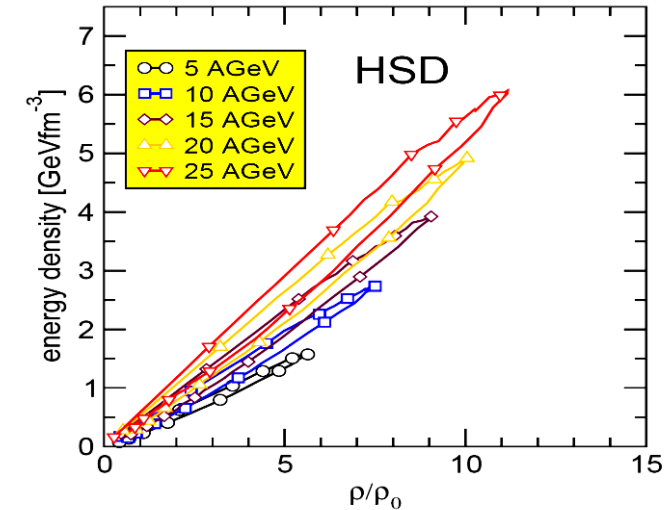
FAIR energies are well suited to study **dense and hot nuclear matter** :

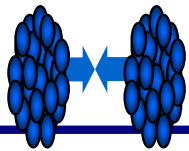
- a phase transition to QGP
- in-medium effects of hadrons
- chiral symmetry restoration

Way to study:

Experimental **energy scan** of different observables in order to find an **‘anomalous’** behavior by comparing with theory

→ **Dynamical models of HIC!**





Dynamical models for HIC

Macroscopic

Microscopic

hydro-models:

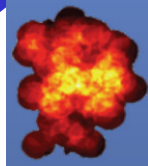
- description of QGP and hadronic phase by hydrodynamical equations for fluid
- **assumption of local equilibrium**
- EoS with phase transition from QGP to HG
- initial conditions (e-b-e, fluctuating)

ideal

(Jyväskylä, SHASTA, TAMU, ...)

viscous

(Romachkko, (2+1)D VISH2+1, (3+1)D MUSIC, ...)



Non-equilibrium microscopic transport models – based on many-body theory

Hadron-string models

(UrQMD, IQMD, HSD, QGSM ...)

Partonic cascades pQCD based

(Duke, BAMPS, ...)

Parton-hadron models:

- QGP: pQCD based cascade
- massless q, g
- hadronization: coalescence (AMPT, HIJING)

fireball models:

- no explicit dynamics: parametrized time evolution (TAMU)

,Hybrid'

- QGP phase: hydro with QGP EoS
- hadronic freeze-out: after burner - hadron-string transport model
- (,hybrid'-UrQMD, EPOS, ...)

- QGP: IQCD EoS
- massive quasi-particles (q and g with spectral functions) in self-generated mean-field
- dynamical hadronization
- HG: off-shell dynamics (applicable for strongly interacting systems)



Theoretical description of 'in-medium effects'

In-medium effects = changes of particle properties in the hot and dense baryonic medium; example – vector mesons, strange mesons

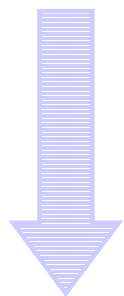
Many-body theory:

Strong interaction → large width = short life-time

→ broad spectral function → quantum object

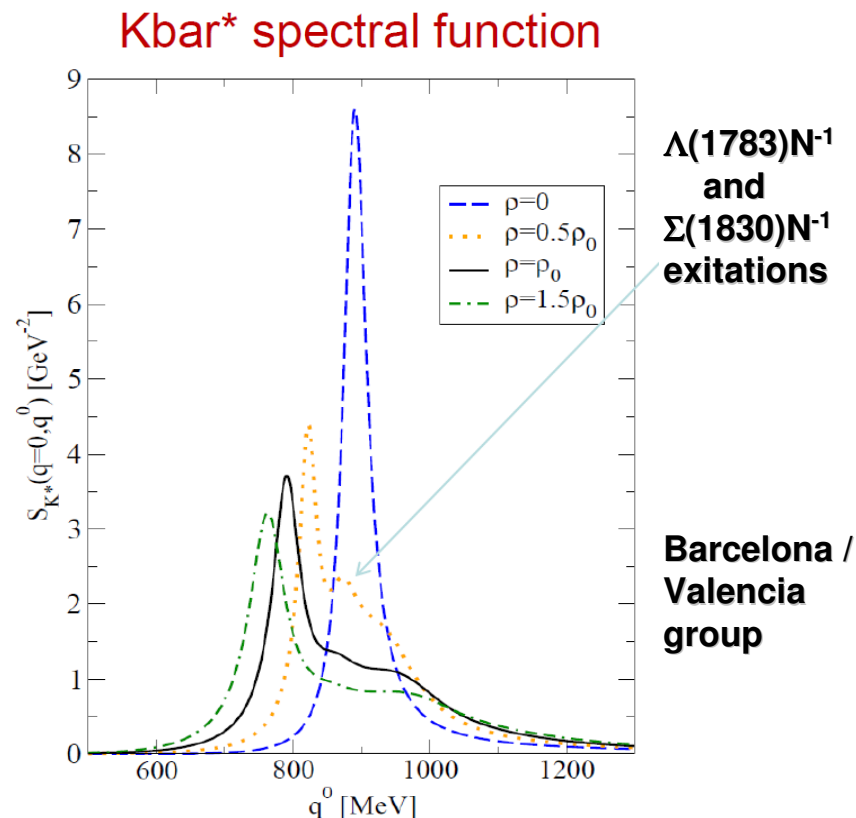
■ How to describe the **dynamics of broad strongly interacting quantum states in transport theory?**

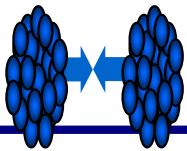
□ semi-classical BUU



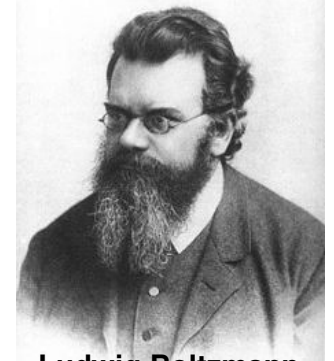
first order gradient expansion of quantum Kadanoff-Baym equations

□ generalized transport equations





Semi-classical BUU equation



Ludwig Boltzmann

Boltzmann-Uehling-Uhlenbeck equation (non-relativistic formulation)
 - propagation of particles in the **self-generated Hartree-Fock mean-field potential** $U(\vec{r},t)$ with an on-shell **collision term**:

$$\frac{\partial}{\partial t} f(\vec{r}, \vec{p}, t) + \frac{\vec{p}}{m} \vec{\nabla}_{\vec{r}} f(\vec{r}, \vec{p}, t) - \vec{\nabla}_{\vec{r}} U(\vec{r}, t) \vec{\nabla}_{\vec{p}} f(\vec{r}, \vec{p}, t) = \left(\frac{\partial f}{\partial t} \right)_{coll}$$

collision term:
 elastic and inelastic reactions

$f(\vec{r}, \vec{p}, t)$ is the **single particle phase-space distribution function**
 - probability to find the particle at position r with momentum p at time t

□ **self-generated Hartree-Fock mean-field potential:**

$$U(\vec{r}, t) = \frac{1}{(2\pi\hbar)^3} \sum_{\beta_{occ}} \int d^3 r' d^3 p V(\vec{r} - \vec{r}', t) f(\vec{r}', \vec{p}, t) + (Fock \text{ term})$$

□ **Collision term for 1+2→3+4 (let's consider fermions) :**

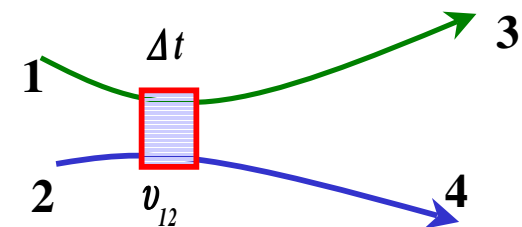
$$I_{coll} = \frac{4}{(2\pi)^3} \int d^3 p_2 d^3 p_3 \int d\Omega |v_{12}| \delta^3(\vec{p}_1 + \vec{p}_2 - \vec{p}_3 - \vec{p}_4) \cdot \frac{d\sigma}{d\Omega}(1+2 \rightarrow 3+4) \cdot P$$

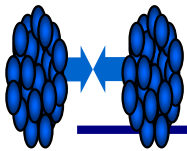
Probability including Pauli blocking of fermions:

$$P = \underline{f_3 f_4 (1 - f_1)(1 - f_2)} - \underline{f_1 f_2 (1 - f_3)(1 - f_4)}$$

Gain term: 3+4→1+2

Loss term: 1+2→3+4





Dynamical description of strongly interacting systems

□ **Semi-classical on-shell BUU:** applies for small collisional width, i.e. for a weakly interacting systems of particles

How to describe **strongly interacting systems?!**

□ **Quantum field theory** →

Kadanoff-Baym dynamics for resummed single-particle Green functions $S^<$

$$\hat{S}_{0x}^{-1} S_{xy}^< = \sum_{xz}^{ret} \odot S_{zy}^< + \sum_{xz}^< \odot S_{zy}^{adv}$$

(1962)

Green functions $S^</math>/self-energies Σ :$

Integration over the intermediate spacetime

$$iS_{xy}^< = \eta \langle \{ \Phi^+(y) \Phi(x) \} \rangle$$

$$S_{xy}^{ret} = S_{xy}^c - S_{xy}^< = S_{xy}^> - S_{xy}^a \quad \text{-retarded}$$

$$\hat{S}_{0x}^{-1} \equiv -(\partial_x^\mu \partial_\mu^x + M_0^2)$$

$$iS_{xy}^> = \langle \{ \Phi(y) \Phi^+(x) \} \rangle$$

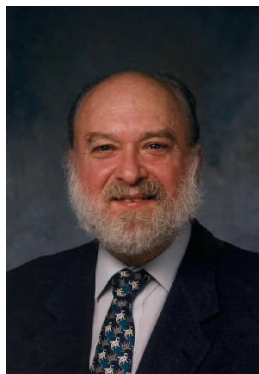
$$S_{xy}^{adv} = S_{xy}^c - S_{xy}^> = S_{xy}^< - S_{xy}^a \quad \text{-advanced}$$

$$iS_{xy}^c = \langle T^c \{ \Phi(x) \Phi^+(y) \} \rangle \quad \text{-causal}$$

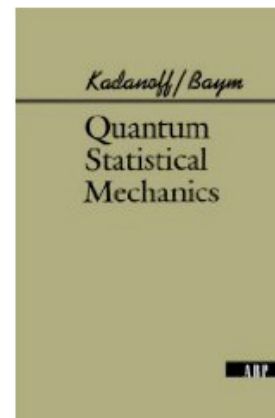
$$\eta = \pm 1 \text{ (bosons / fermions)}$$

$$iS_{xy}^a = \langle T^a \{ \Phi(x) \Phi^+(y) \} \rangle \quad \text{-anticausal}$$

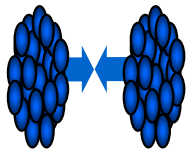
$$T^a(T^c) \text{ - (anti-)time - ordering operator}$$



Leo Kadanoff



Gordon Baym



From Kadanoff-Baym equations to generalized transport equations

After the **first order gradient expansion** of the **Wigner transformed Kadanoff-Baym equations** and separation into the real and imaginary parts one gets:

Generalized transport equations (GTE):

$$\diamond \{ P^2 - M_0^2 - \text{Re}\Sigma_{XP}^{\text{ret}} \} \{ S_{XP}^< \} - \boxed{\diamond \{ \Sigma_{XP}^< \} \{ \text{Re}S_{XP}^{\text{ret}} \}} = \frac{i}{2} [\Sigma_{XP}^> S_{XP}^< - \Sigma_{XP}^< S_{XP}^>]$$

collision term = ,gain' - ,loss' term

Backflow term incorporates the **off-shell** behavior in the particle propagation
! vanishes in the quasiparticle limit $A_{XP} \rightarrow \delta(p^2 - M^2)$

□ GTE: Propagation of the Green's function $iS_{XP}^< = A_{XP} N_{XP}$, which carries information not only on the **number of particles** (N_{XP}), but also on their **properties**, interactions and correlations (via A_{XP})

□ **Spectral function:**

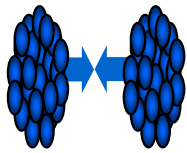
$$A_{XP} = \frac{\Gamma_{XP}}{(P^2 - M_0^2 - \text{Re}\Sigma_{XP}^{\text{ret}})^2 + \Gamma_{XP}^2/4}$$

$\Gamma_{XP} = -\text{Im}\Sigma_{XP}^{\text{ret}} = 2p_0\Gamma$ - **,width' of spectral function**
 = **reaction rate** of particle (at space-time position X)

4-dimensional generalization of the Poisson-bracket:

$$\diamond \{ F_1 \} \{ F_2 \} := \frac{1}{2} \left(\frac{\partial F_1}{\partial X_\mu} \frac{\partial F_2}{\partial P^\mu} - \frac{\partial F_1}{\partial P_\mu} \frac{\partial F_2}{\partial X^\mu} \right)$$

□ **Life time** $\tau = \frac{\hbar c}{\Gamma}$



General testparticle off-shell equations of motion

W. Cassing , S. Juchem, NPA 665 (2000) 377; 672 (2000) 417; 677 (2000) 445

□ Employ **testparticle Ansatz** for the real valued quantity $i S_{XP}^<$ -

$$F_{XP} = A_{XP} N_{XP} = i S_{XP}^< \sim \sum_{i=1}^N \delta^{(3)}(\vec{X} - \vec{X}_i(t)) \delta^{(3)}(\vec{P} - \vec{P}_i(t)) \delta(P_0 - \epsilon_i(t))$$

insert in generalized transport equations and determine equations of motion !

→ **General testparticle off-shell equations of motion**
for the time-like particles:

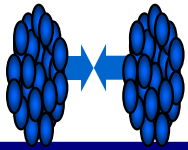
$$\frac{d\vec{X}_i}{dt} = \frac{1}{1 - C_{(i)}} \frac{1}{2\epsilon_i} \left[2\vec{P}_i + \vec{\nabla}_{P_i} \text{Re}\Sigma_{(i)}^{\text{ret}} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\Gamma_{(i)}} \vec{\nabla}_{P_i} \Gamma_{(i)} \right],$$

$$\frac{d\vec{P}_i}{dt} = -\frac{1}{1 - C_{(i)}} \frac{1}{2\epsilon_i} \left[\vec{\nabla}_{X_i} \text{Re}\Sigma_{(i)}^{\text{ret}} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\Gamma_{(i)}} \vec{\nabla}_{X_i} \Gamma_{(i)} \right],$$

$$\frac{d\epsilon_i}{dt} = \frac{1}{1 - C_{(i)}} \frac{1}{2\epsilon_i} \left[\frac{\partial \text{Re}\Sigma_{(i)}^{\text{ret}}}{\partial t} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\Gamma_{(i)}} \frac{\partial \Gamma_{(i)}}{\partial t} \right],$$

with $F_{(i)} \equiv F(t, \vec{X}_i(t), \vec{P}_i(t), \epsilon_i(t))$

$$C_{(i)} = \frac{1}{2\epsilon_i} \left[\frac{\partial}{\partial \epsilon_i} \text{Re}\Sigma_{(i)}^{\text{ret}} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\Gamma_{(i)}} \frac{\partial}{\partial \epsilon_i} \Gamma_{(i)} \right]$$



Collision term in off-shell transport models

Collision term for reaction 1+2->3+4:

$$I_{coll}(X, \vec{P}, M^2) = Tr_2 Tr_3 Tr_4 \underline{A(X, \vec{P}, M^2)} \underline{A(X, \vec{P}_2, M_2^2)} \underline{A(X, \vec{P}_3, M_3^2)} \underline{A(X, \vec{P}_4, M_4^2)}$$

$$\underline{|G((\vec{P}, M^2) + (\vec{P}_2, M_2^2) \rightarrow (\vec{P}_3, M_3^2) + (\vec{P}_4, M_4^2))|_{\mathcal{A},S}^2} \delta^{(4)}(P + P_2 - P_3 - P_4)$$

$$[\underbrace{N_{X\vec{P}_3M_3^2} N_{X\vec{P}_4M_4^2} \bar{f}_{X\vec{P}M^2} \bar{f}_{X\vec{P}_2M_2^2}}_{\text{,gain' term}} - \underbrace{N_{X\vec{P}M^2} N_{X\vec{P}_2M_2^2} \bar{f}_{X\vec{P}_3M_3^2} \bar{f}_{X\vec{P}_4M_4^2}}_{\text{,loss' term}}]$$

with $\bar{f}_{X\vec{P}M^2} = 1 + \eta N_{X\vec{P}M^2}$ and $\eta = \pm 1$ for bosons/fermions, respectively.

The trace over particles 2,3,4 reads explicitly

for fermions

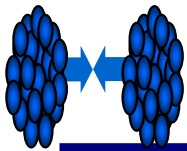
$$Tr_2 = \sum_{\sigma_2, \tau_2} \frac{1}{(2\pi)^4} \int d^3 P_2 \frac{dM_2^2}{2\sqrt{\vec{P}_2^2 + M_2^2}}$$

for bosons

$$Tr_2 = \sum_{\sigma_2, \tau_2} \frac{1}{(2\pi)^4} \int d^3 P_2 \frac{dP_{0,2}^2}{2}$$

additional integration

The transport approach and the particle spectral functions are fully determined once the **in-medium transition amplitudes G** are known in their **off-shell dependence!**



In-medium transition rates: G-matrix approach

Need to know in-medium transition amplitudes **G** and their off-shell dependence

$$|G((\vec{P}, M^2) + (\vec{P}_2, M_2^2) \rightarrow (\vec{P}_3, M_3^2) + (\vec{P}_4, M_4^2))|_{\mathcal{A}, \mathcal{S}}^2$$

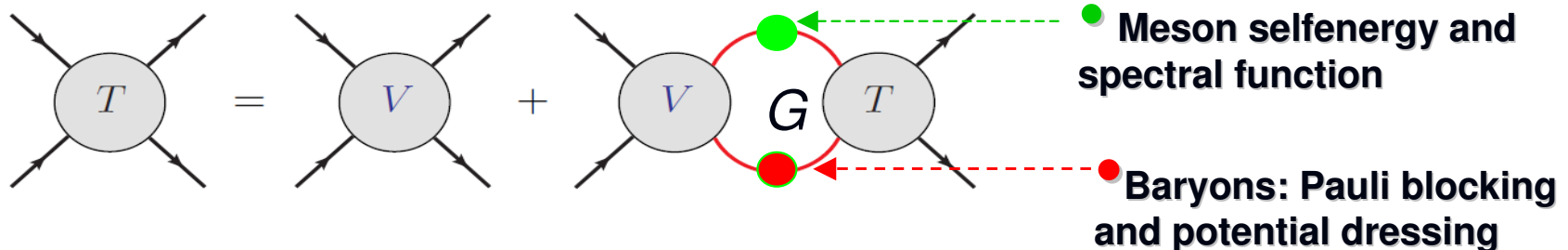


Coupled channel G-matrix approach

Transition probability :

$$P_{1+2 \rightarrow 3+4}(s) = \int d \cos(\theta) \frac{1}{(2s_1 + 1)(2s_2 + 1)} \sum_i \sum_\alpha G^\dagger G$$

with $G(p, \rho, T)$ - **G-matrix** from the solution of **coupled-channel equations:**



$$\blacksquare T_{ij}(\rho, T) = V_{ij} + V_{il} G_l(\rho, T) T_{lj}(\rho, T)$$

For strangeness:

D. Cabrera, L. Tolos, J. Aichelin, E.B., arXiv:1406.2570; W. Cassing, L. Tolos, E.B., A. Ramos, NPA727 (2003) 59

Collision width in off-shell transport model

□ **Total width** = collision width + decay width : $\Gamma = \Gamma_{coll} + \Gamma_{dec}$

In the **vacuum**: $\Gamma = \Gamma_{dec}$

□ **Example: Collision width** Γ_{coll} for 1+2->3+4 process – defined from the **loss term** of the collision integral I_{coll} :
(similar for the n<->m reactions!)

$$-I_{coll}(loss) = \Gamma_{coll}(X, \vec{P}, M^2) N_{X\vec{P} M^2}$$

$$\Gamma_{XP} = -Im\Sigma_{XP}^{ret} = 2p_0\Gamma$$

$$\Gamma_{coll}(X, \vec{P}, M^2) = Tr_2 Tr_3 Tr_4 A(X, \vec{P}, M^2) A(X, \vec{P}_2, M_2^2) A(X, \vec{P}_3, M_3^2) A(X, \vec{P}_4, M_4^2) \\ \times |G((\vec{P}, M^2) + (\vec{P}_2, M_2^2) \rightarrow (\vec{P}_3, M_3^2) + (\vec{P}_4, M_4^2))|_{AS}^2 \delta^4(P + P_2 - P_3 - P_4) N_{X\vec{P}_2 M_2^2} \bar{f}_{X\vec{P}_3 M_3^2} \bar{f}_{X\vec{P}_4 M_4^2}$$

❖ Collision width is defined by all possible interactions in the local cell

! **Assumptions used in transport calculations for V-mesons** (to speed up calculations):

- Collision width in **low density approximation**: $\Gamma_{coll} = \gamma \rho \langle v \sigma_{VN}^{tot} \rangle$
- replace $\langle v \sigma_{VN}^{tot} \rangle$ by averaged value $G = \text{const}$: $\Gamma_{coll} = \gamma \rho G$

(Works well – cf. low density approximation vs. the full dynamical calculation of Γ_{coll} in Ref. E.B., NPA696 (2001) 761)

Mean-field potential in off-shell transport model

- **Many-body theory:** Interacting relativistic particles have a **complex self-energy**:

$$\Sigma_{XP}^{ret} = \text{Re}\Sigma_{XP}^{ret} + i \text{Im}\Sigma_{XP}^{ret}$$

The neg. imaginary part $\Gamma_{XP} = -\text{Im}\Sigma_{XP}^{ret} = 2p_0\Gamma$ is related via $\Gamma = \Gamma_{coll} + \Gamma_{dec}$

to the inverse lifetime of the particle $\tau \sim 1/\Gamma$.

- The **collision width** Γ_{coll} is determined from the **loss term** of the collision integral I_{coll}

- By **dispersion relation** we get a contribution to the **real part of self-energy**:

$$\text{Re}\Sigma_{XP}^{ret}(p_0) = P \int_0^{\infty} dq \frac{\text{Im}\Sigma_{XP}^{ret}(q)}{(q-p_0)}$$

that gives a **mean-field potential** U_{XP} via:

$$\text{Re}\Sigma_{XP}^{ret}(p_0) = 2p_0 U_{XP}$$

→ the **complex self-energy** relates in a self-consistent way to the self-generated mean-field potential and collision width (inverse lifetime)

Detailed balance on the level of $2 \leftrightarrow n$: treatment of multi-particle collisions in transport approaches

W. Cassing, NPA 700 (2002) 618

Generalized collision integral for $n \leftrightarrow m$ reactions:

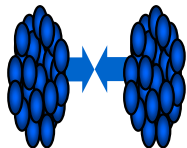
$$I_{coll} = \sum_n \sum_m I_{coll}[n \leftrightarrow m]$$

$$\begin{aligned}
 I_{coll}^i[n \leftrightarrow m] = & \\
 & \frac{1}{2} N_n^m \sum_\nu \sum_\lambda \left(\frac{1}{(2\pi)^4} \right)^{n+m-1} \int \left(\prod_{j=2}^n d^4 p_j A_j(x, p_j) \right) \left(\prod_{k=1}^m d^4 p_k A_k(x, p_k) \right) \\
 & \times A_i(x, p) W_{n,m}(p, p_j; i, \nu | p_k; \lambda) (2\pi)^4 \delta^4(p^\mu + \sum_{j=2}^n p_j^\mu - \sum_{k=1}^m p_k^\mu) \\
 & \times [\tilde{f}_i(x, p) \prod_{k=1}^m f_k(x, p_k) \prod_{j=2}^n \tilde{f}_j(x, p_j) - f_i(x, p) \prod_{j=2}^n f_j(x, p_j) \prod_{k=1}^m \tilde{f}_k(x, p_k)].
 \end{aligned}$$

$\tilde{f} = 1 + \eta f$ is Pauli-blocking or Bose-enhancement factors;
 $\eta=1$ for bosons and $\eta=-1$ for fermions

$W_{n,m}(p, p_j; i, \nu | p_k; \lambda)$ is a **transition probability**

→ huge CPU!



Antibaryon production in heavy-ion reactions

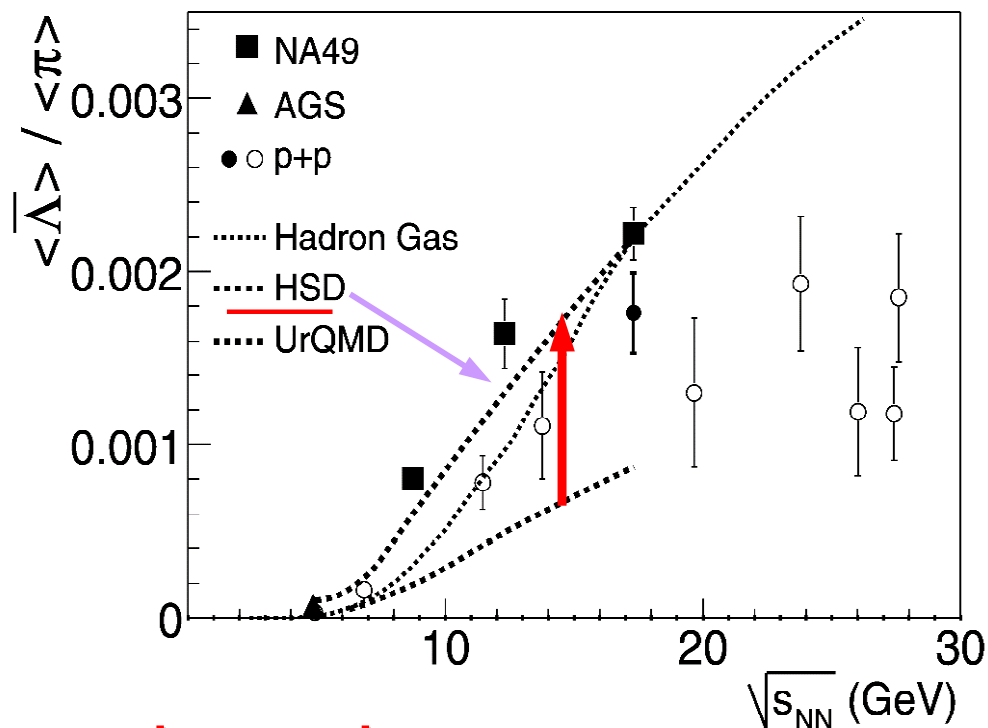
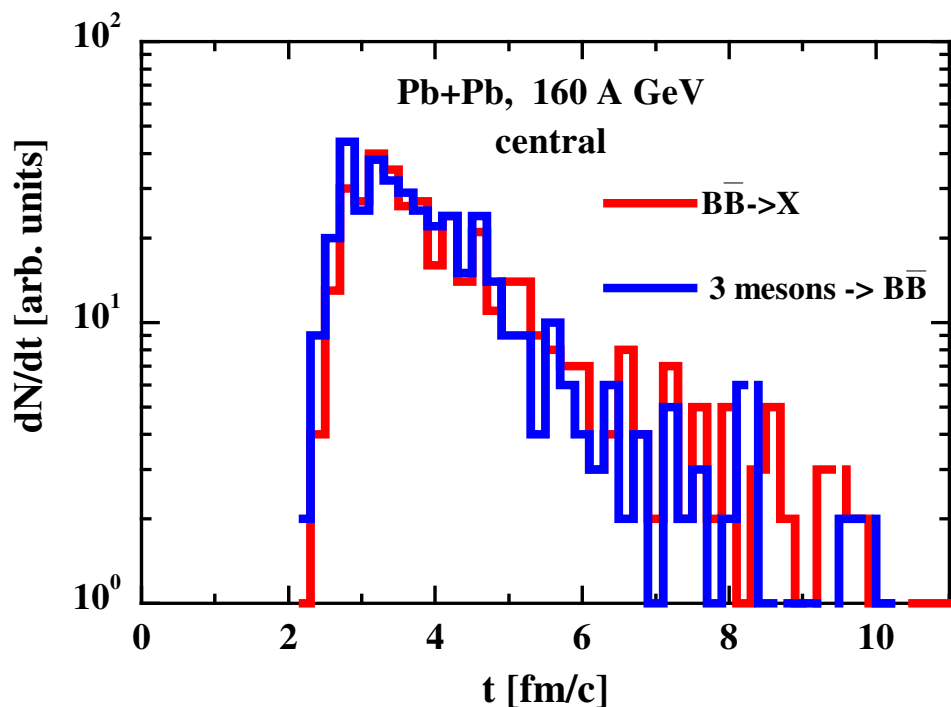
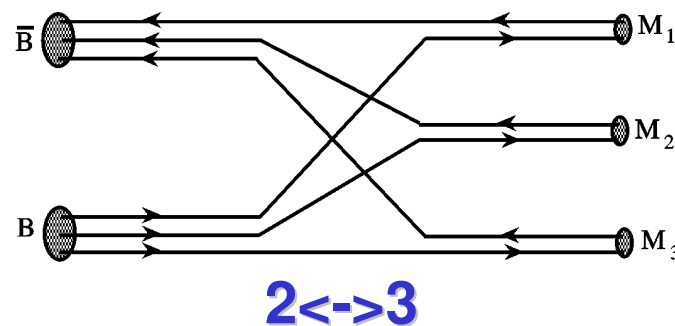
Multi-meson fusion reactions

$$m_1 + m_2 + \dots + m_n \leftrightarrow B + \bar{B}$$

($m = \pi, \rho, \omega, \dots$)

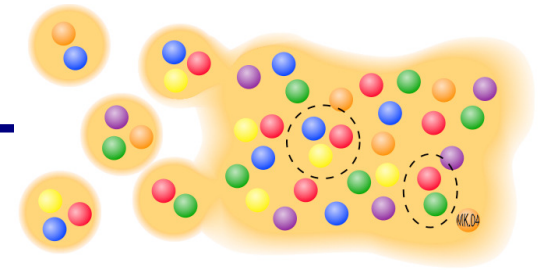
□ important for antiproton, antilambda dynamics !

W. Cassing, NPA 700 (2002) 618



→ approximate equilibrium of annihilation and recreation

From hadrons to partons



In order to study the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma** – we **need a consistent non-equilibrium (transport) model with**

- **explicit parton-parton interactions** (i.e. between quarks and gluons) beyond strings!

- **explicit phase transition** from hadronic to partonic degrees of freedom
- **IQCD EoS** for partonic phase

Transport theory: off-shell Kadanoff-Baym equations for the Green-functions $S_h^<(x,p)$ in phase-space representation for the **partonic and hadronic phase**



Parton-Hadron-String-Dynamics (PHSD)

QGP phase described by

Dynamical QuasiParticle Model (DQPM)

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;
NPA831 (2009) 215;
W. Cassing, EPJ ST 168 (2009) 3

A. Peshier, W. Cassing, PRL 94 (2005) 172301;
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

Dynamical QuasiParticle Model (DQPM) - Basic ideas:

DQPM describes QCD properties in terms of ,resummed‘ single-particle Green’s functions – in the sense of a two-particle irreducible (2PI) approach:

Gluon propagator: $\Delta^{-1} = P^2 - \Pi$ gluon self-energy: $\Pi = M_g^2 - i2\Gamma_g \omega$

Quark propagator: $S_q^{-1} = P^2 - \Sigma_q$ quark self-energy: $\Sigma_q = M_q^2 - i2\Gamma_q \omega$

- the resummed properties are specified by complex self-energies which depend on temperature:
 - the real part of self-energies (Σ_q, Π) describes a **dynamically generated mass** (M_q, M_g);
 - the imaginary part describes the **interaction width** of partons (Γ_q, Γ_g)
- space-like part of energy-momentum tensor $T_{\mu\nu}$ defines the potential energy density and the **mean-field potential** (1PI) for quarks and gluons (U_q, U_g)
- 2PI framework guaranties a consistent description of the system **in- and out-off equilibrium** on the basis of **Kadanoff-Baym equations** with proper states in equilibrium

A. Peshier, W. Cassing, PRL 94 (2005) 172301;
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

The Dynamical QuasiParticle Model (DQPM)

Properties of interacting quasi-particles: massive quarks and gluons (g, q, q_{bar}) with Lorentzian spectral functions :

$$(i = q, \bar{q}, g) \quad \rho_i(\omega, T) = \frac{4\omega\Gamma_i(T)}{(\omega^2 - \bar{p}^2 - M_i^2(T))^2 + 4\omega^2\Gamma_i^2(T)}$$

■ Modeling of the quark/gluon masses and widths → HTL limit at high T

■ quarks:

$$\text{mass: } M_{q(\bar{q})}^2(T) = \frac{N_c^2 - 1}{8N_c} g^2 \left(T^2 + \frac{\mu_q^2}{\pi^2} \right)$$

$$\text{width: } \Gamma_{q(\bar{q})}(T) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$$

■ gluons:

$$M_g^2(T) = \frac{g^2}{6} \left(\left(N_c + \frac{N_f}{2} \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

$$\Gamma_g(T) = \frac{1}{3} N_c \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$$

$N_c = 3, N_f = 3$

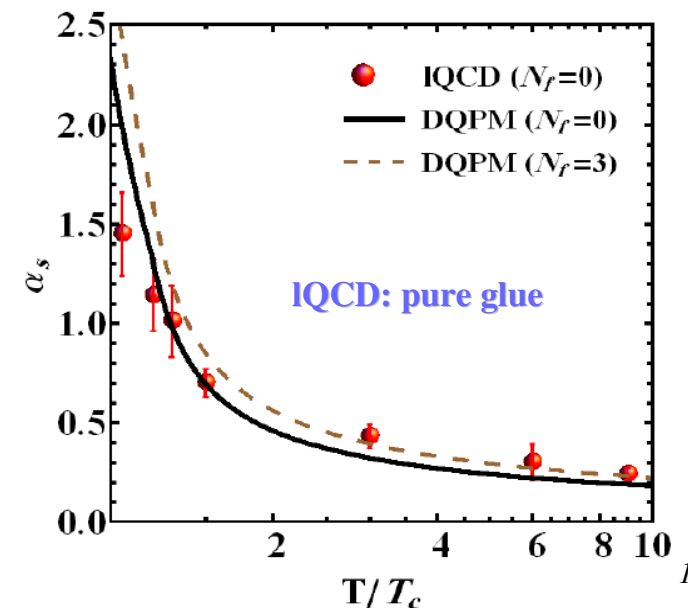
■ running coupling (pure glue):

$$\alpha_s(T) = \frac{g^2(T)}{4\pi} = \frac{12\pi}{(11N_c - 2N_f) \ln[\lambda^2(T/T_c - T_s/T_c)^2]}$$

□ fit to lattice (IQCD) results (e.g. entropy density)

with 3 parameters: $T_s/T_c = 0.46$; $c = 28.8$; $\lambda = 2.42$
(for pure glue $N_f = 0$)

DQPM: Peshier, Cassing, PRL 94 (2005) 172301;
Cassing, NPA 791 (2007) 365; NPA 793 (2007)



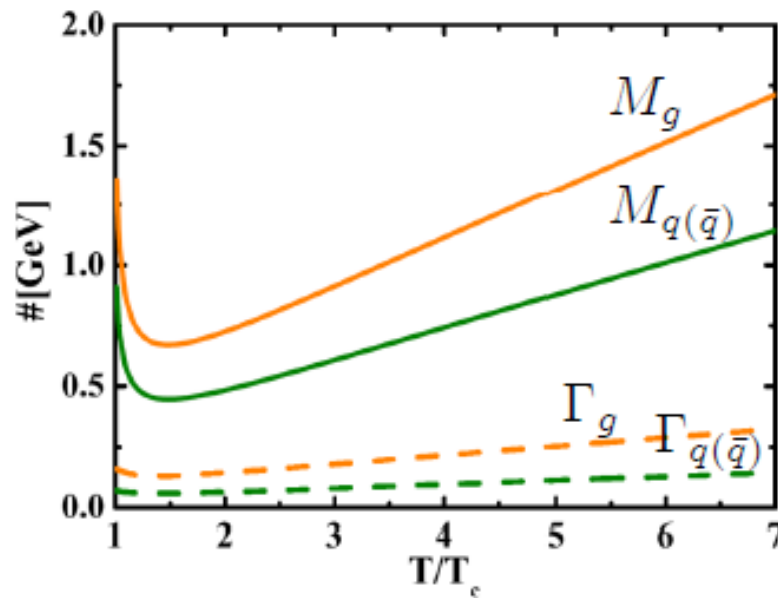
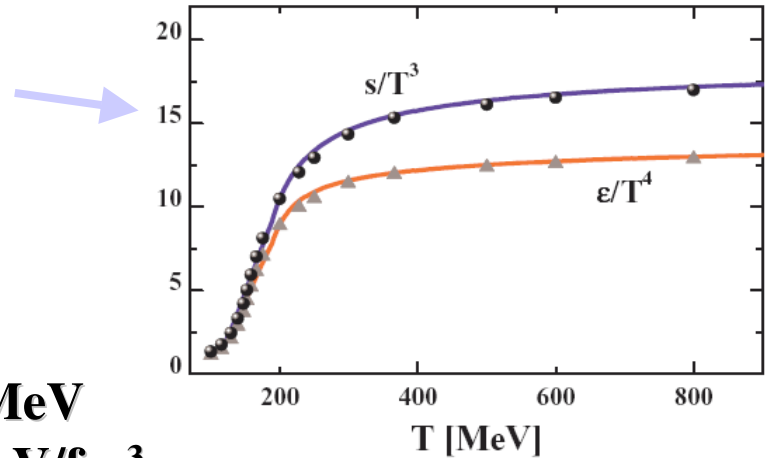
The Dynamical QuasiParticle Model (DQPM)

➤ **fit to lattice (IQCD) results** (e.g. entropy density)

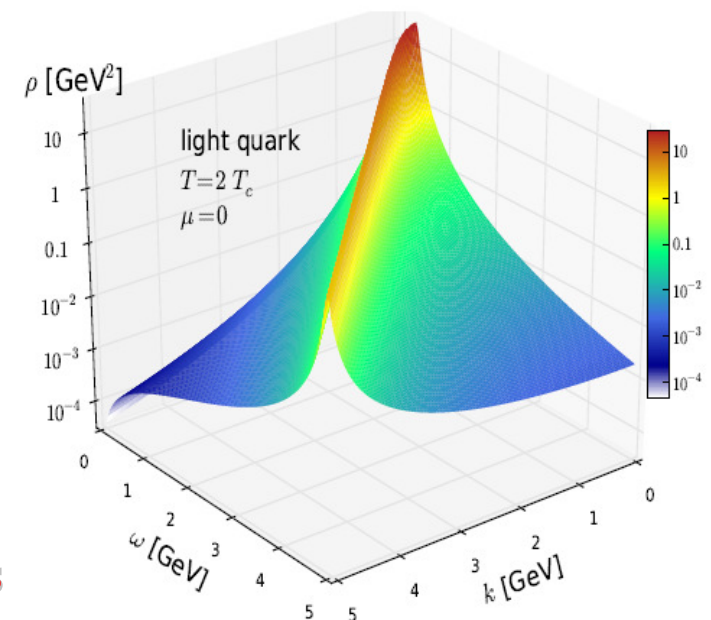
* BMW IQCD data S. Borsanyi et al., JHEP 1009 (2010) 073

➔ **Quasiparticle properties:**

■ **large width and mass for gluons and quarks**



$T_C=158 \text{ MeV}$
 $\epsilon_C=0.5 \text{ GeV/fm}^3$



- **DQPM matches well lattice QCD**
- **DQPM provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)**
- **DQPM gives transition rates for the formation of hadrons → PHSD**



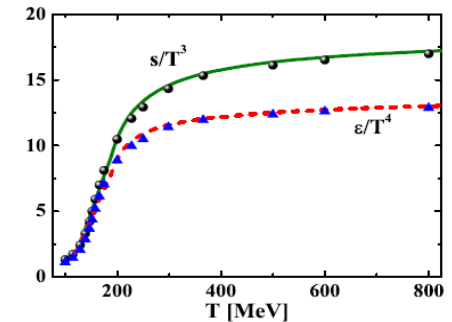
Parton Hadron String Dynamics

I. From hadrons to QGP:

- Initial A+A collisions:
 - string formation in primary NN collisions
 - strings decay to pre-hadrons (B - baryons, m – mesons)
- Formation of QGP stage by dissolution of pre-hadrons into massive colored quarks + mean-field energy based on the Dynamical Quasi-Particle Model (DQPM) which defines quark spectral functions, masses $M_q(\epsilon)$ and widths $\Gamma_q(\epsilon)$ + mean-field potential U_q at given ϵ – local energy density (related by lQCD EoS to T - temperature in the local cell)

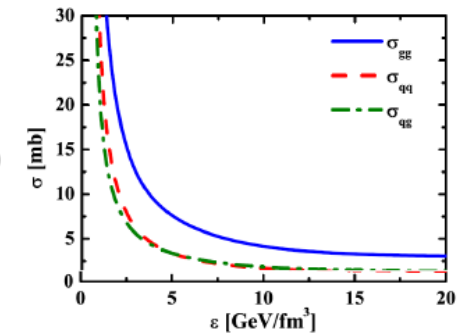


QGP phase:
 $\epsilon > \epsilon_{\text{critical}}$



II. Partonic phase - QGP:

- quarks and gluons (= ‚dynamical quasiparticles‘) with off-shell spectral functions (width, mass) defined by the DQPM
- in self-generated mean-field potential for quarks and gluons U_q, U_g
- EoS of partonic phase: ‚crossover‘ from lattice QCD (fitted by DQPM)
- (quasi-) elastic and inelastic parton-parton interactions: using the effective cross sections from the DQPM

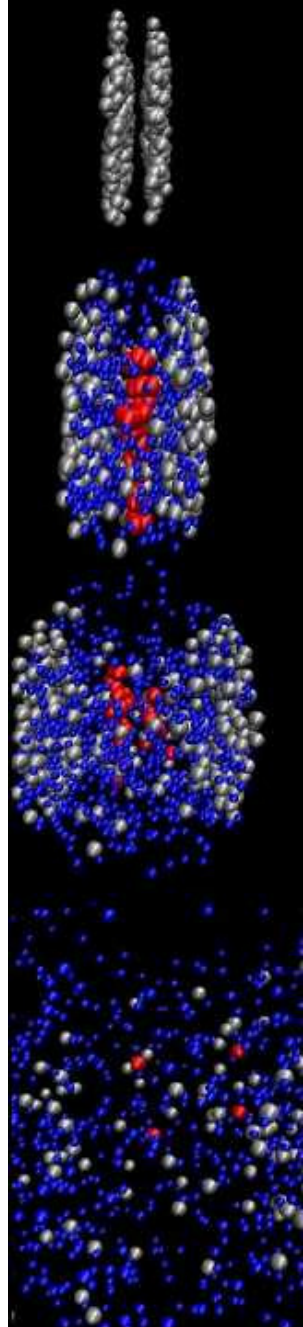


III. Hadronization: based on DQPM

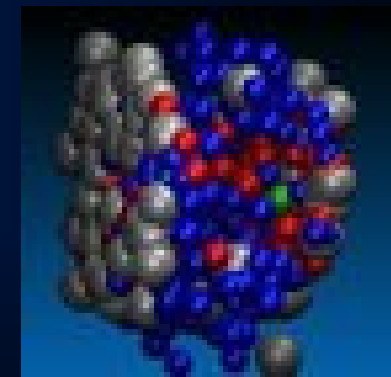
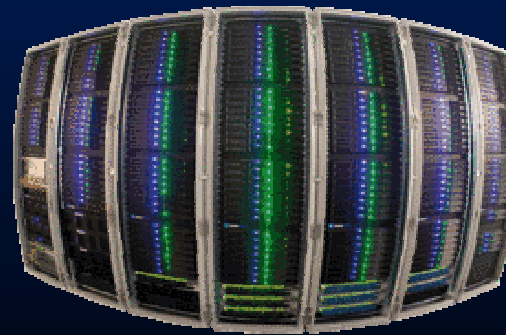
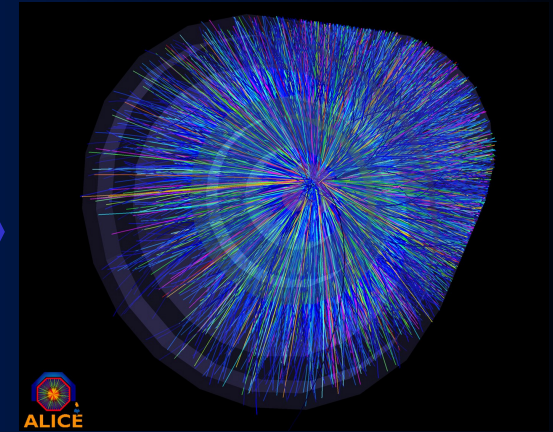
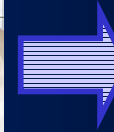
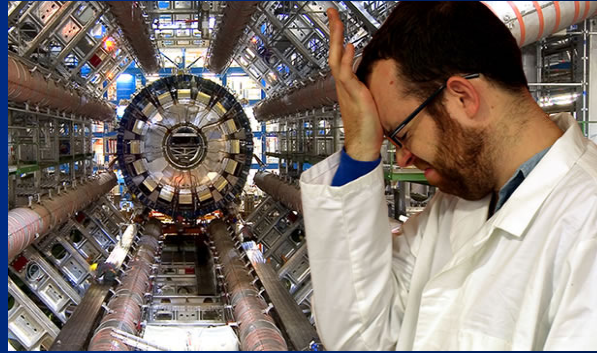
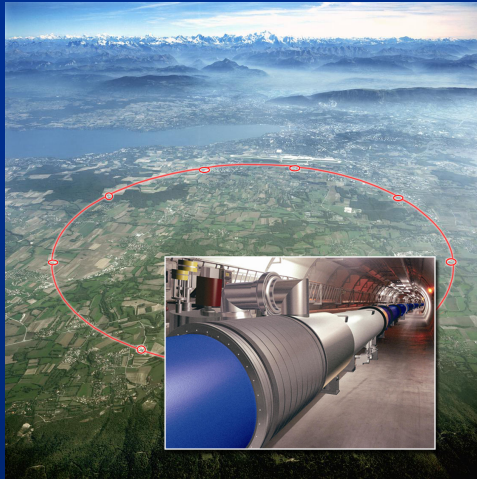
- massive, off-shell (anti-)quarks with broad spectral functions hadronize to off-shell mesons and baryons or color neutral excited states - ‚strings‘ (strings act as ‚doorway states‘ for hadrons)



IV. Hadronic phase: hadron-string interactions – off-shell HSD

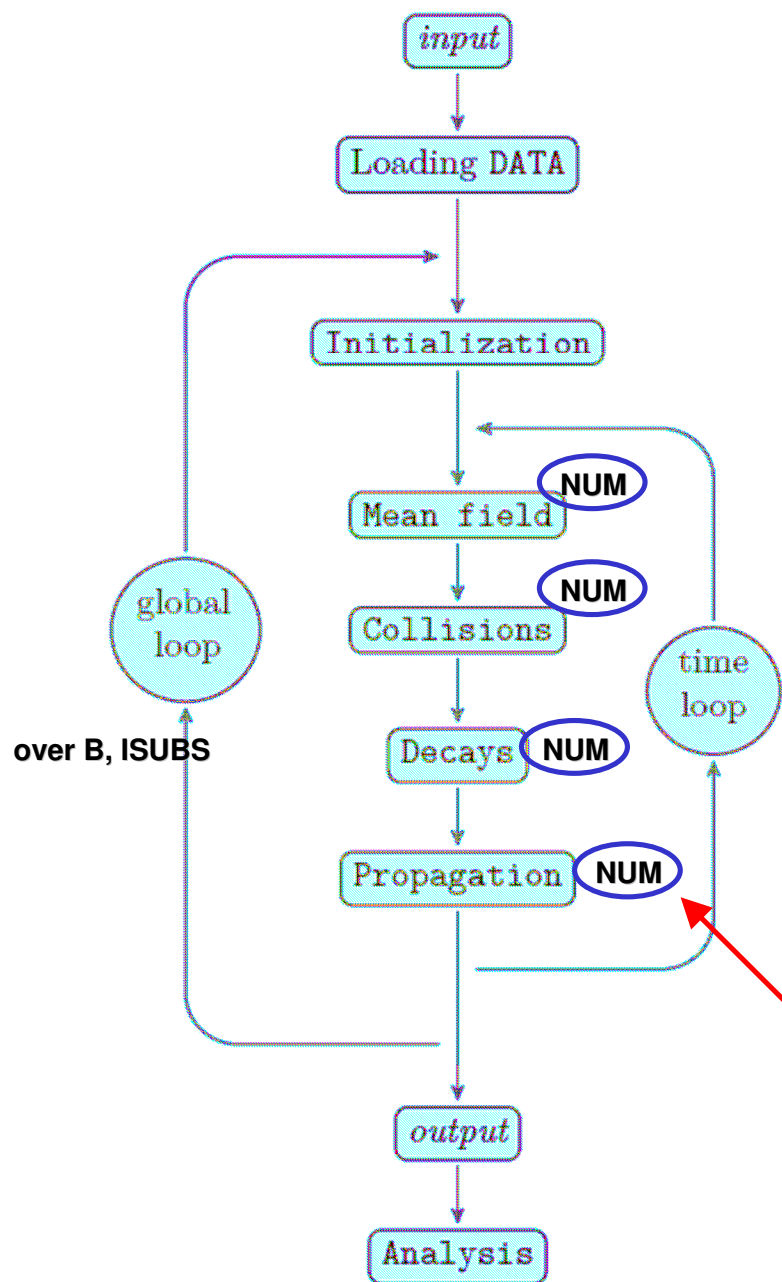


PHSD – ‚femto‘ accelerator





PHSD code: structure



Input file (*input*) for Au+Au @ 200 GeV - 30-40%

197,	MASSTA:	target mass
79,	MSTAPR:	protons in target
197,	MASSPR:	projectile mass
79,	MSPRPR:	protons in projectile
21300.,	ELAB:	lab energy per nucleon
8.7,	BMIN:	minimal impact parameter [fm]
8.7,	BMAX:	maximal impact parameter [fm]
1.,	DBIMP:	impact parameter step [fm]
25,	NUM:	number of parallel events
1,	ISUBS:	number of subsequent runs
4567,	ISEED:	initial random seed [integer]
0,	ICHARM:	charm degrees of freedom =0 no, =1 yes
0,	IDILEPT:	=0 no dileptons, =1 electron pair, =2 muon pair
0,	ICQ:	=0 free, =1 drop. mass, =2 broad., =3 drop.+broad.
1,	IGLUE:	=1 with partons, =0 w/o partons
40.,	FINALT:	final time of calculation [fm/c]
0,	IHARD:	=1 compute hard collisions, =0 no
10,	ILOW:	output level

HSD mode

PHSD is the parallel ensembles code!!!

loop over **NUM** – parallel ensembles or ,events‘:

□ needed for the smooth description of the mean-field properties as energy density or baryon density

➔ possible parallelization



PHSD running time \leftrightarrow HPC

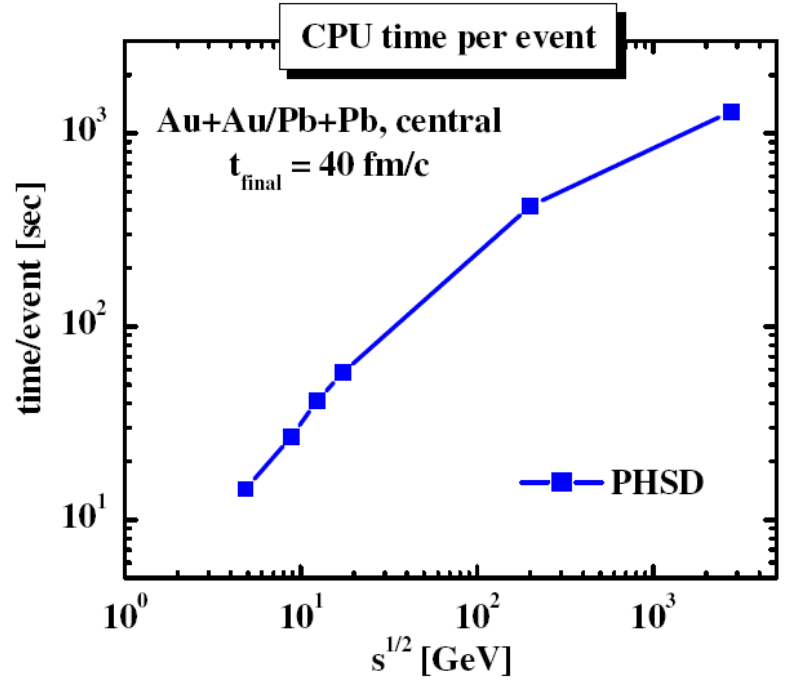
PHSD mode: Au+Au/Pb+Pb, central, $t_{\text{final}} = 40 \text{ fm/c}$

Elab, AGeV	$S^{1/2}$, GeV	CPU time, h	NUM	CPU time/NUM
10.7	4.86	0.2	50	14.4sec
40	8.86	0.75	100	27sec
80	12.4	1.15	100	41.4sec
158	17.3	0.8	50	57.6sec
21300	200	1.75	15	7min
4060000	2760	1.8	5	21.6min

from V. Konchakovski



NUM – the number of parallel ensembles/events

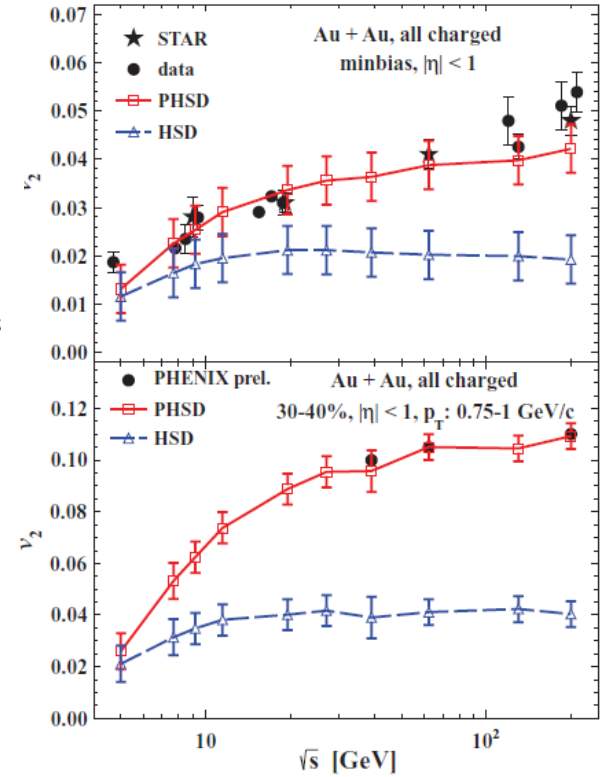
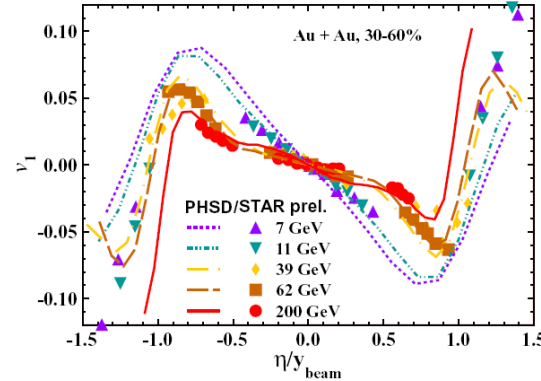
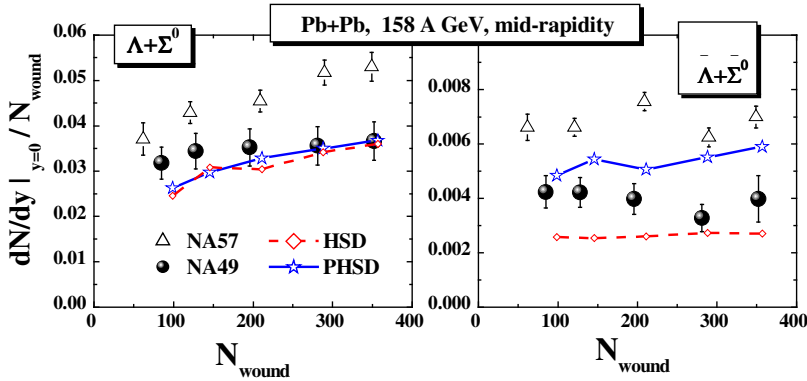


→ CPU time per event grows with energy
 → PHSD mode (for RHIC, LHC) – more time consuming than HSD

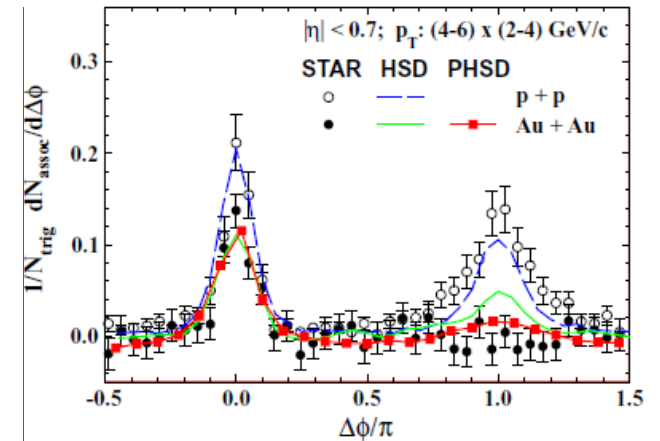
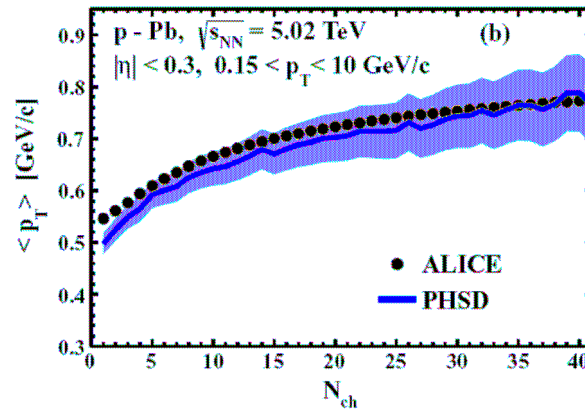
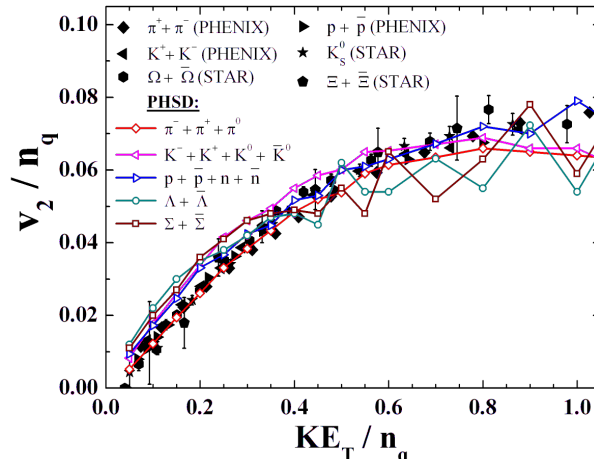
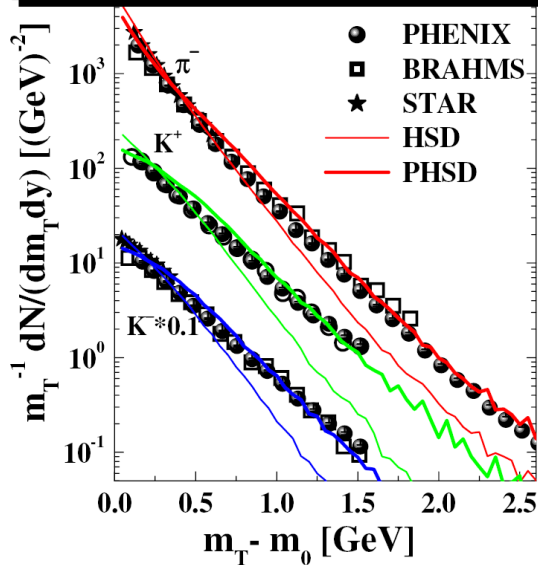
PHSD is the open source code for the FAIR experiments:
<http://fias.uni-frankfurt.de/~brat/PHSD/index4.html>



PHSD for HIC (highlights)



Au+Au @ $\sqrt{s} = 200$ GeV, 5% central, $|\eta| < 0.5$

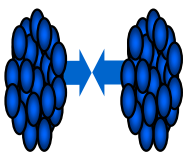


PHSD provides a consistent description of p+A and HIC dynamics

The most CPU costly observables (some examples)



(Multi-)strange particles in Au+Au



Multi-strange baryon production

Multi-strange hyperons (Ξ , Ω) are promising probes to study:

- in-medium effects at low bombarding energy
- QGP properties at high energy density

□ **Elementary production:**

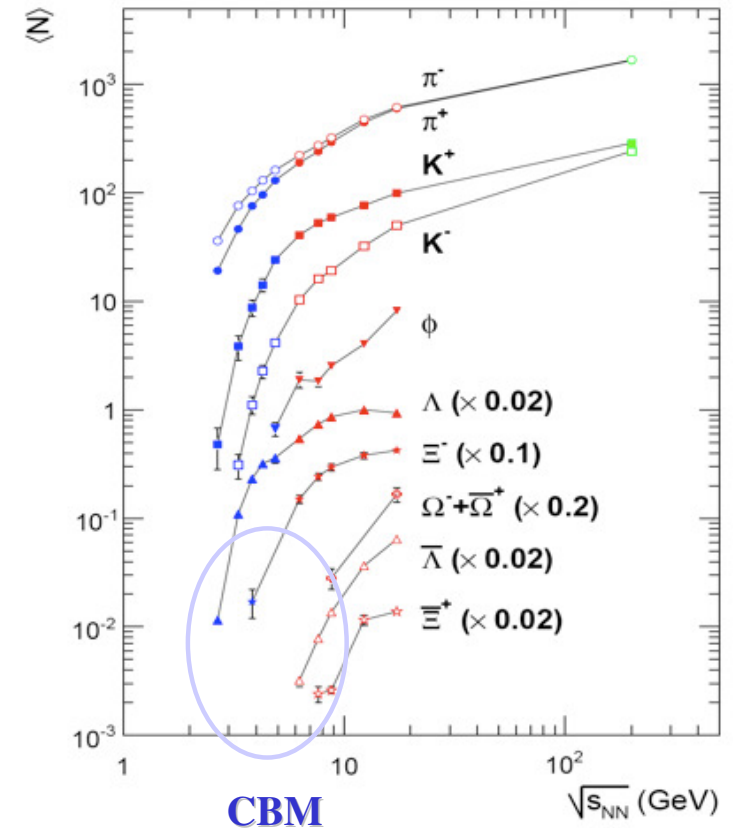


□ **In heavy-ion reactions:** sub-threshold channels,

e.g.

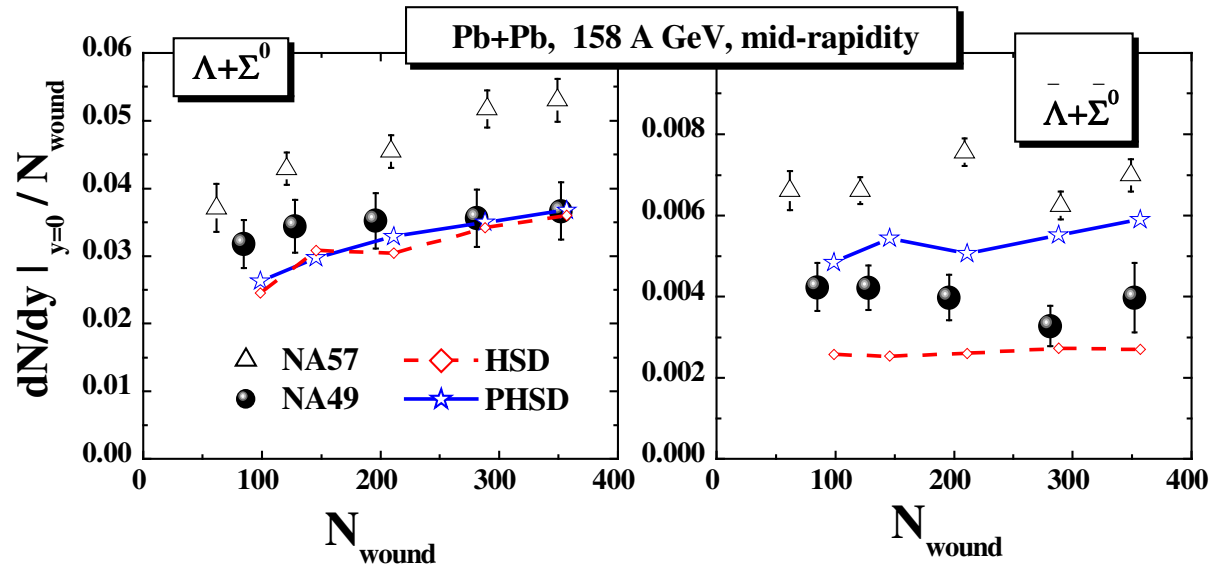


Production through these channels highly depends on baryon density (and its fluctuations)



Centrality dependence of (multi-)strange (anti-)baryons

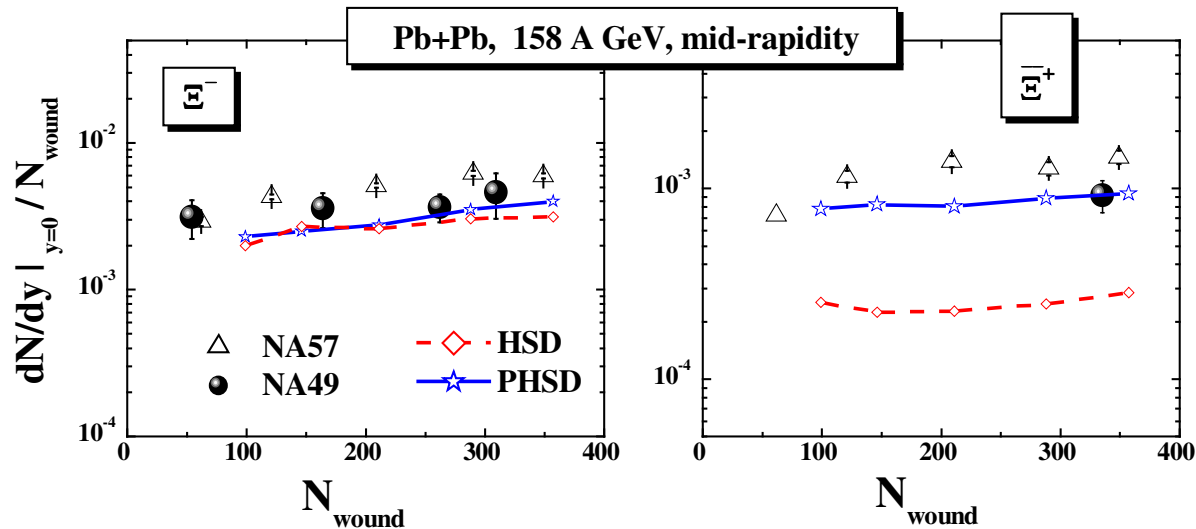
strange
baryons
 $\Lambda + \Sigma^0$



strange
antibaryons

$\bar{\Lambda} + \bar{\Sigma}^0$

multi-strange
baryon
 Ξ^-

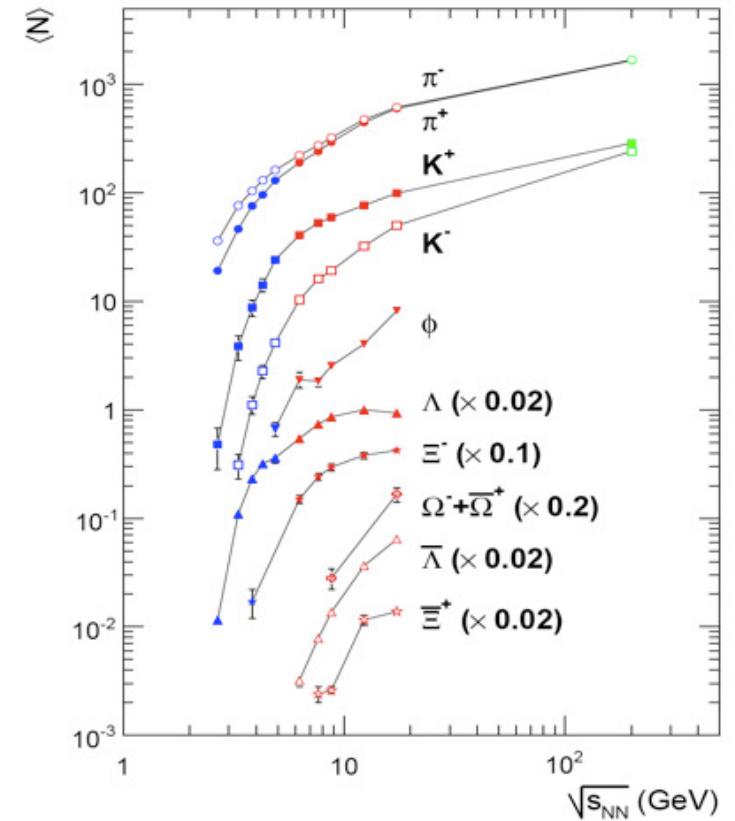
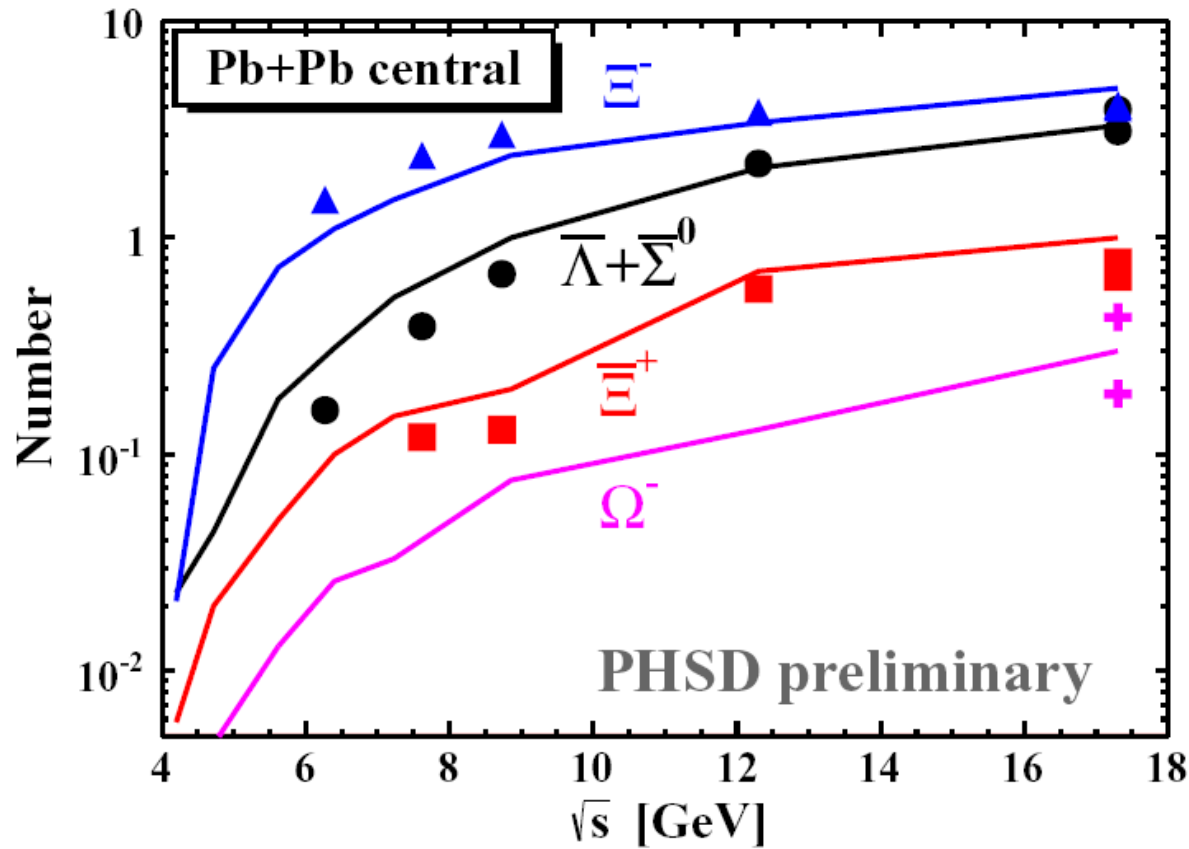


multi-strange
antibaryon

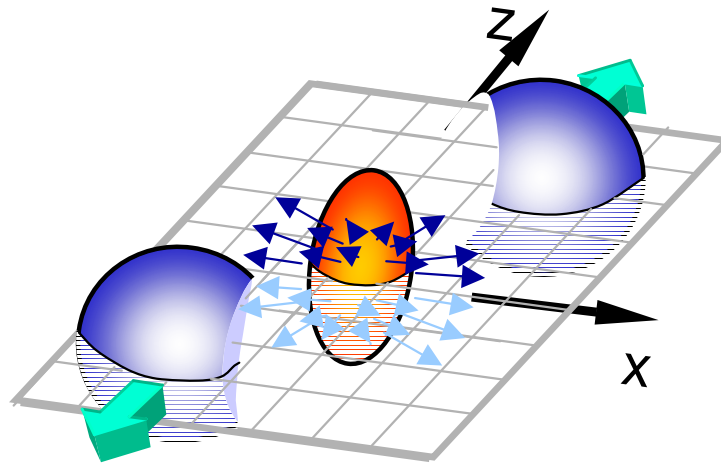
Ξ^+

→ enhanced production of (multi-) strange antibaryons in PHSD

Excitation function of (multi-)strange (anti-)baryons



**Collective flow:
anisotropy coefficients (v_1, v_2, v_3, v_4)
in A+A**



Anisotropy coefficients

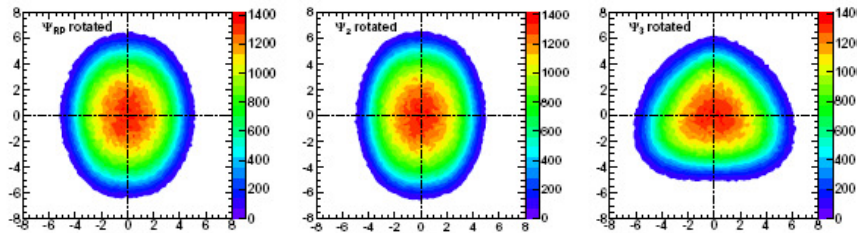
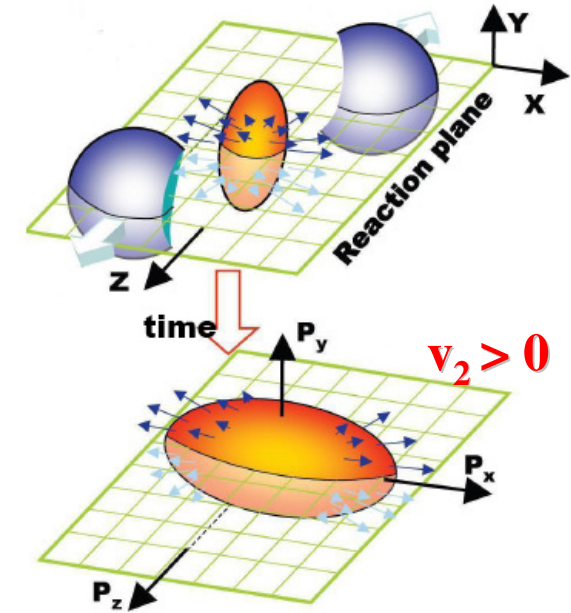
Non central Au+Au collisions :

□ interaction between constituents leads to a **pressure gradient** => spatial asymmetry is converted to an asymmetry in momentum space => **collective flow**

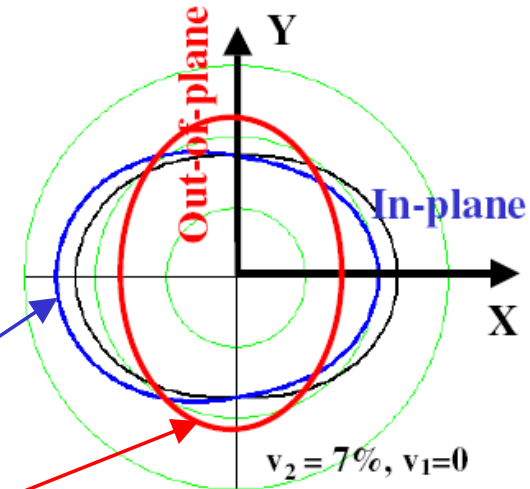
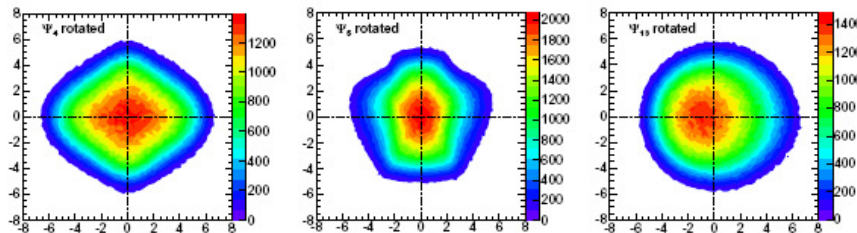
$$\frac{dN}{d\varphi} \propto \left(1 + 2 \sum_{n=1}^{+\infty} v_n \cos[n(\varphi - \psi_n)] \right)$$

$$v_n = \langle \cos n(\varphi - \psi_n) \rangle, \quad n = 1, 2, 3, \dots$$

v_1 : directed flow
 v_2 : elliptic flow
 v_3 : triangular flow.....



from S. A. Voloshin, arXiv:1111.7241



$v_2 > 0$ indicates **in-plane** emission of particles

$v_2 < 0$ corresponds to a **squeeze-out** perpendicular to the reaction plane (**out-of-plane** emission)

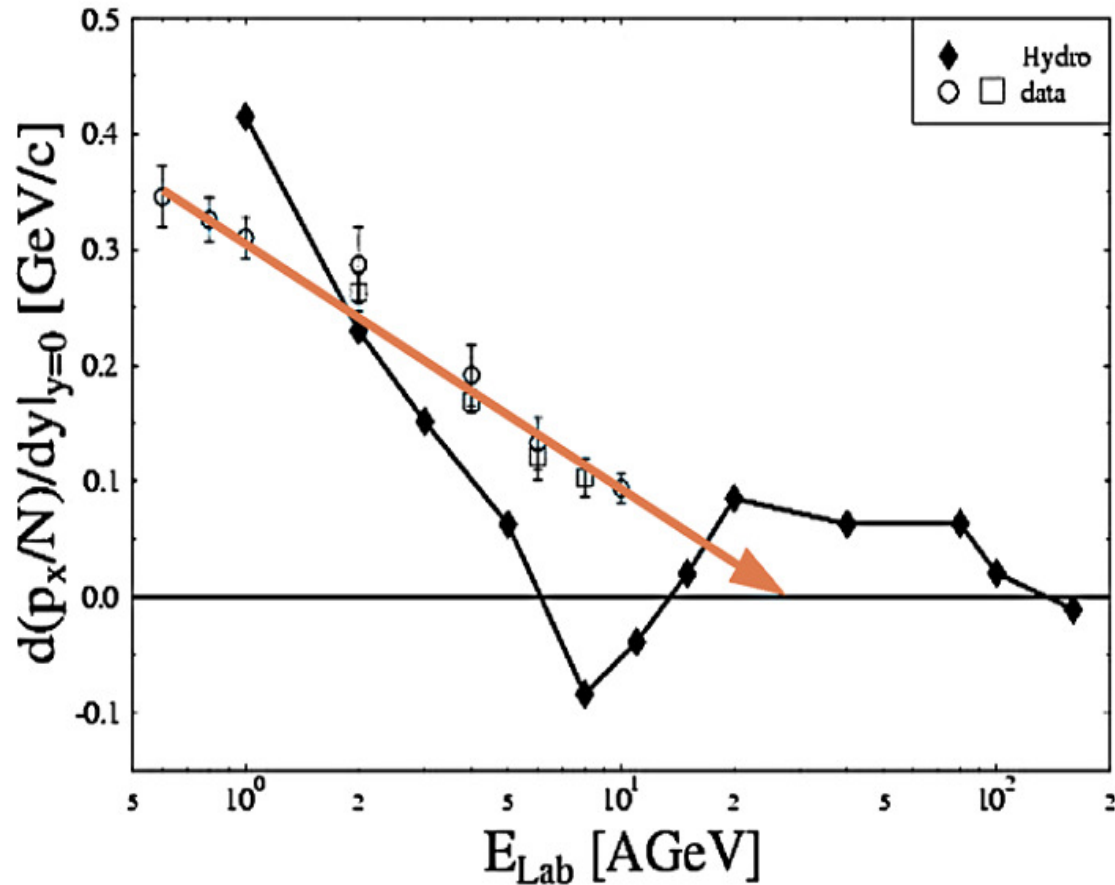
$v_2 = 7\%, v_1 = 0$

$v_2 = 7\%, v_1 = -7\%$

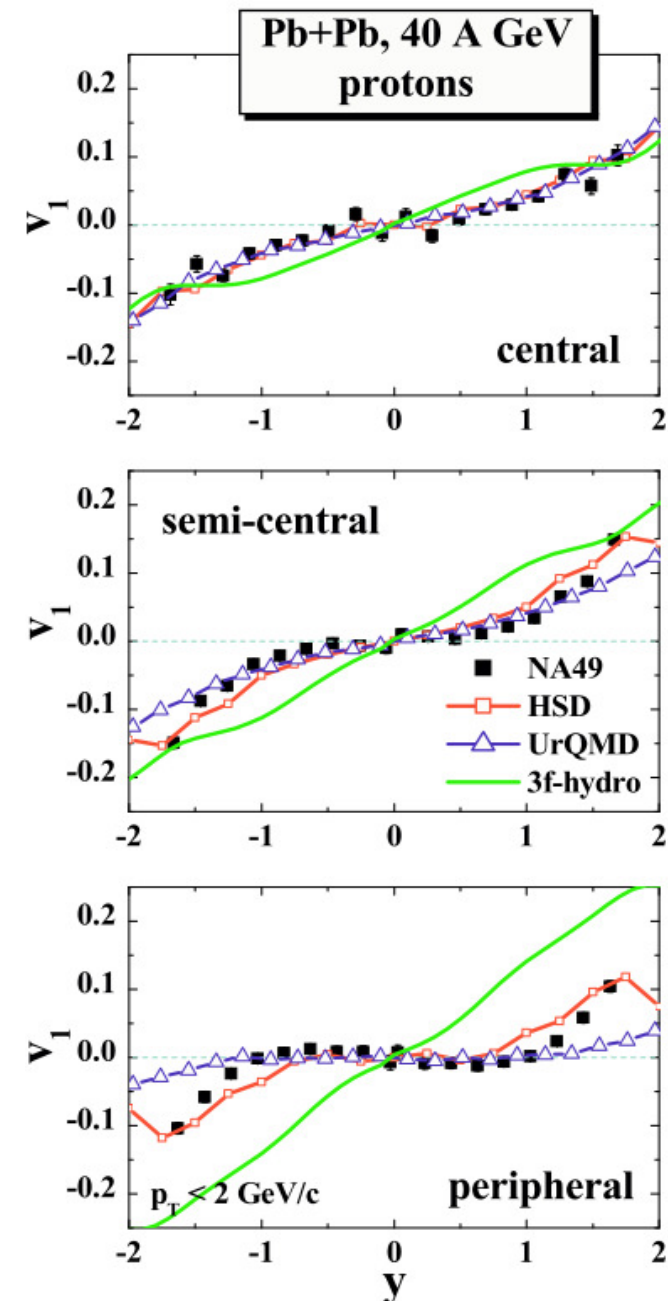
$v_2 = -7\%, v_1 = 0$

Directed flow signals of the Quark–Gluon Plasma

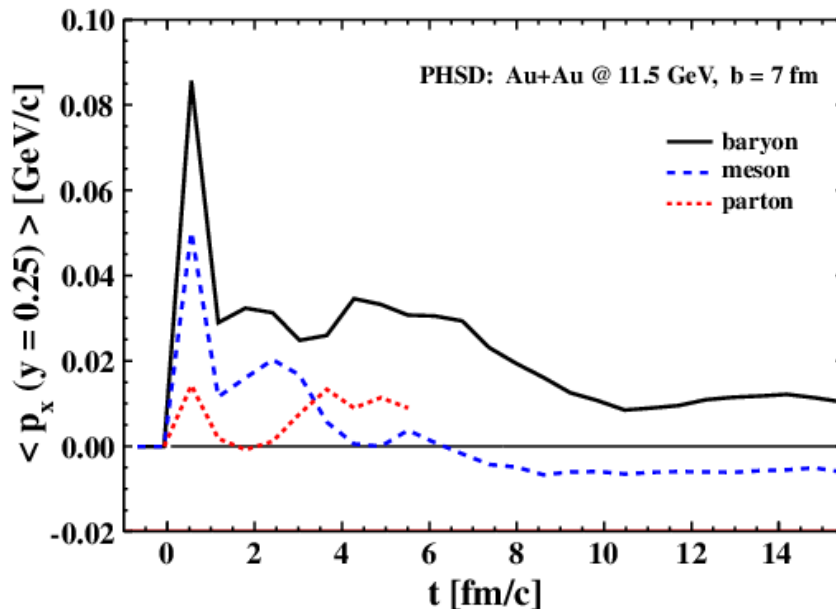
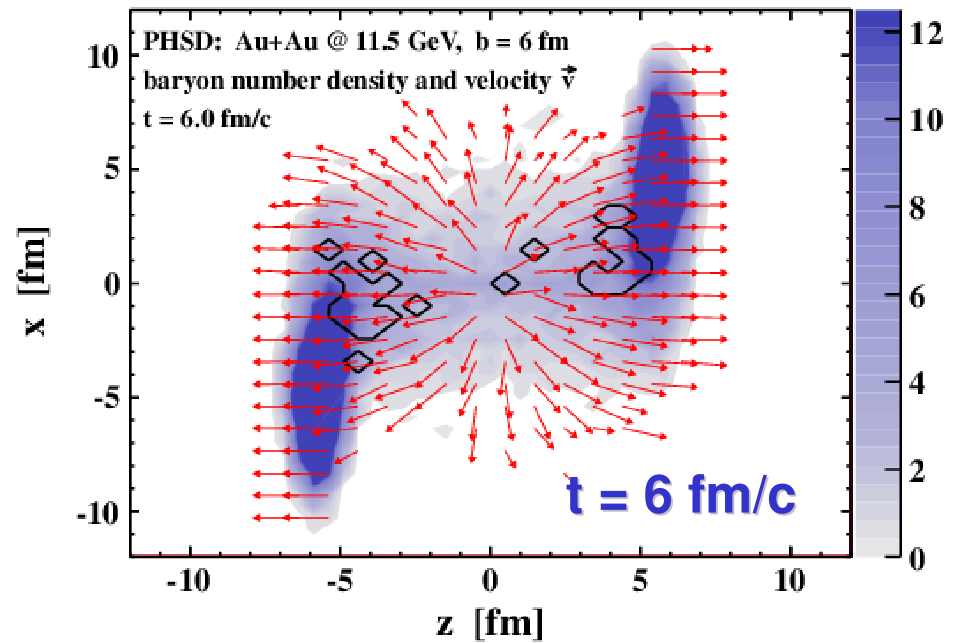
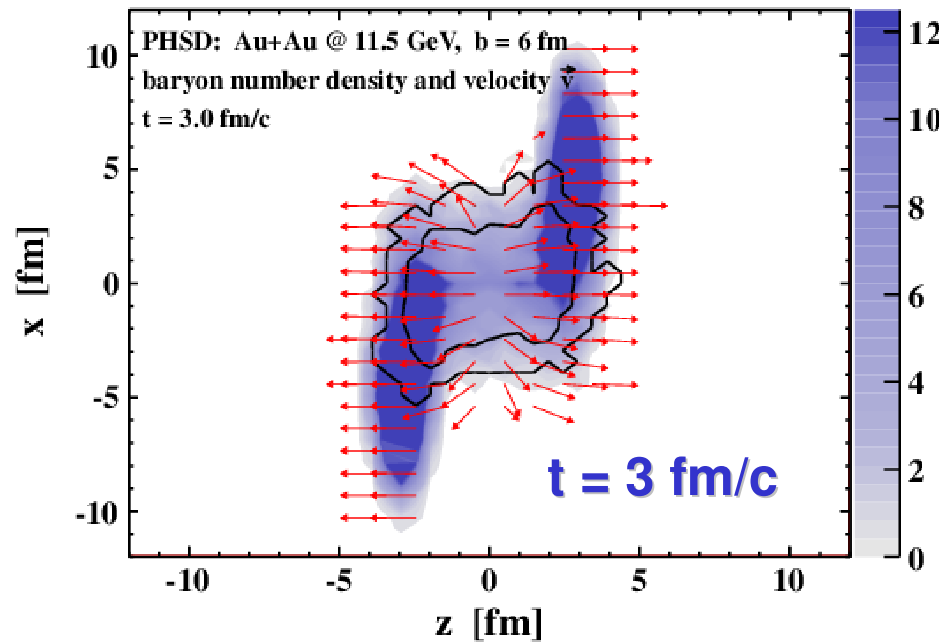
H. Stöcker, Nucl. Phys. A 750, 121 (2005)



- Early hydro calculation predicted the “softest point” at $E_{lab} = 8$ AGeV
- A linear extrapolation of the data (arrow) suggests a collapse of flow at $E_{lab} = 30$ AGeV

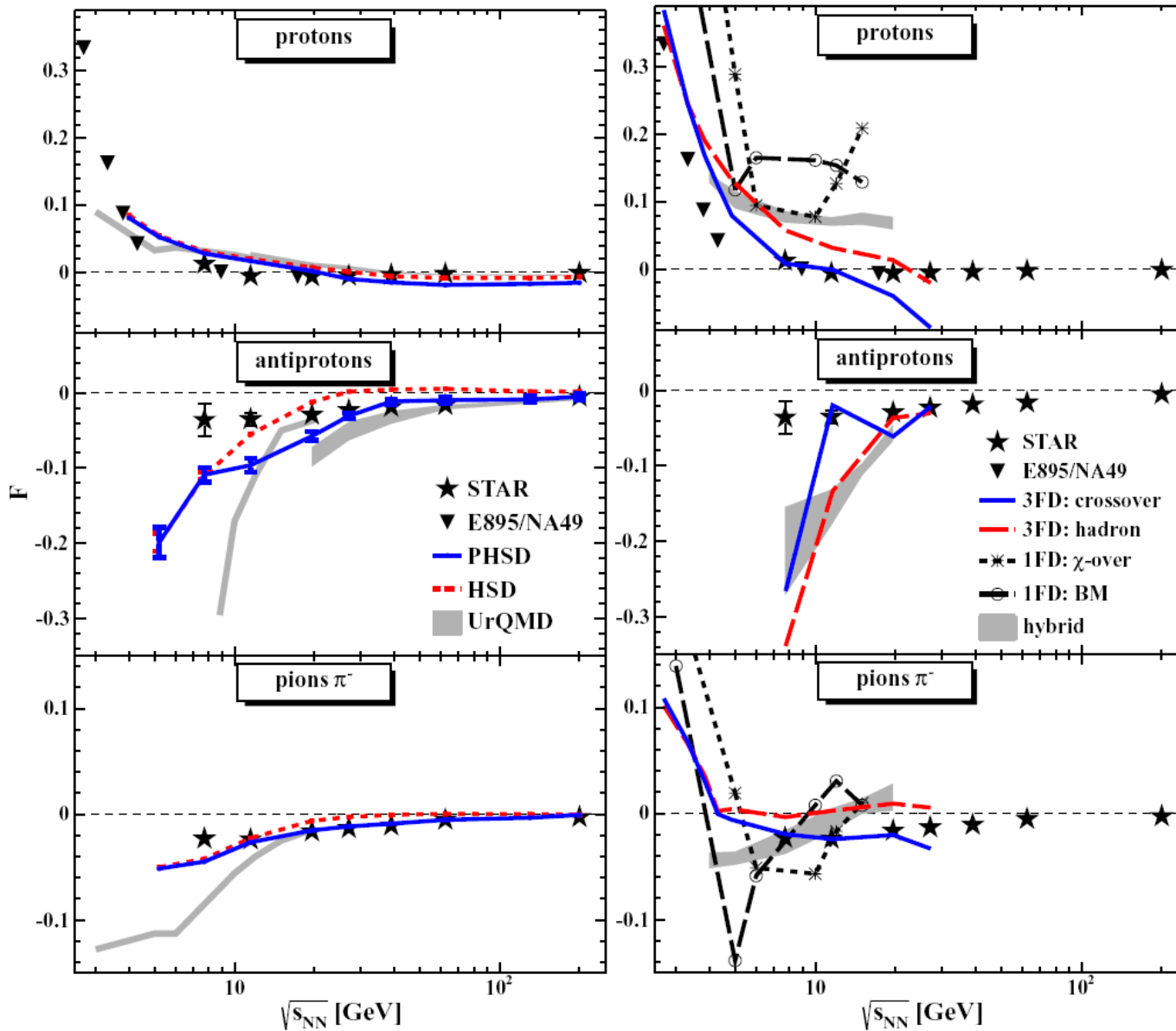
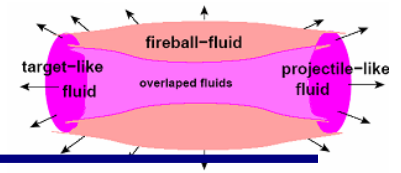


PHSD: snapshot of the reaction plane



- **Color scale:** baryon number density
Black levels: QGP- parton density 0.6 and 0.01 fm^{-3}
Red arrows: local velocity of baryon matter
- **Directed flow v_1 is formed at an early stage** of the nuclear interaction
- **Baryons are reaching positive and mesons – negative value of v_1**

Excitation function of v_1 slopes



• The slope of $v_1(y)$ at midrapidity:

$$F = \left. \frac{dv_1}{dy} \right|_{y=0}$$

Models:

- HSD, PHSD
- 3D-Fluid Dynamic approach (3FD)
- UrQMD
- Hybrid-UrQMD
- 1FD-hydro with chiral cross-over and Bag Model (BM) EoS

➔ smooth crossover?!

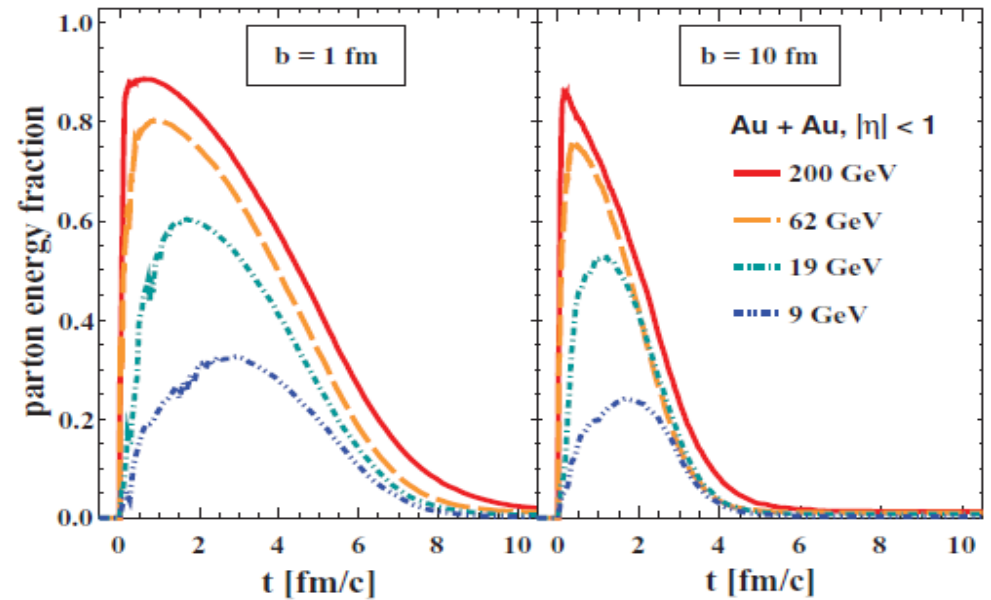
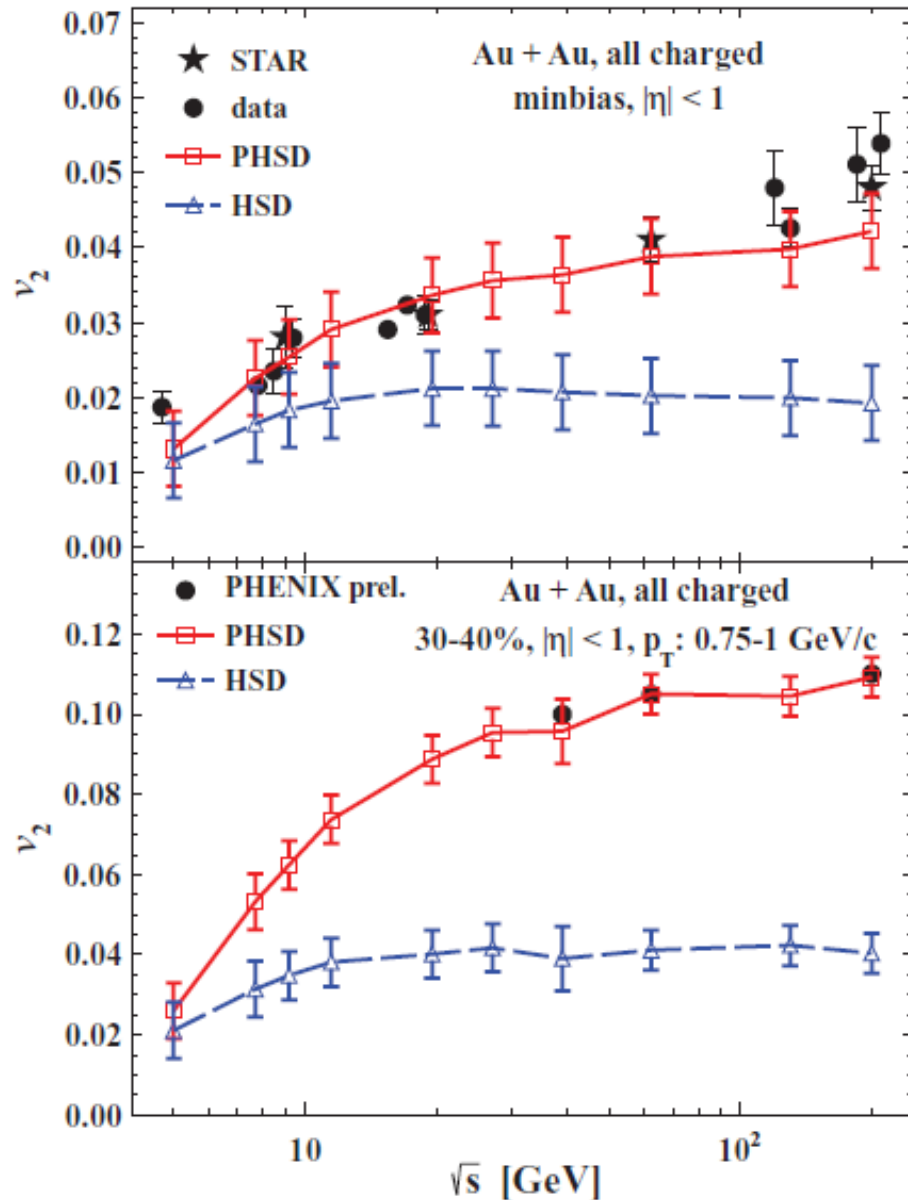
STAR Collaboration, arXiv:1401.3043

PHSD/HSD and 3D-fluid hydro: V. Konchakovski, W. Cassing, Yu. Ivanov, V. Toneev, PRC(2014), arXiv:1404.2765

Hybrid-UrQMD/Hydro: J. Steinheimer, J. Auvinen, H. Petersen, M. Bleicher, H. Stöcker, PRC 89 (2014) 054913



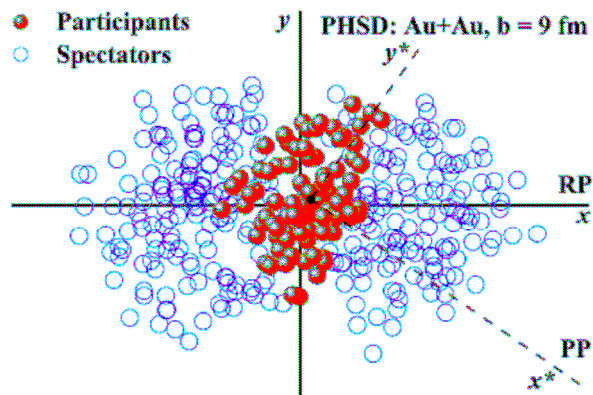
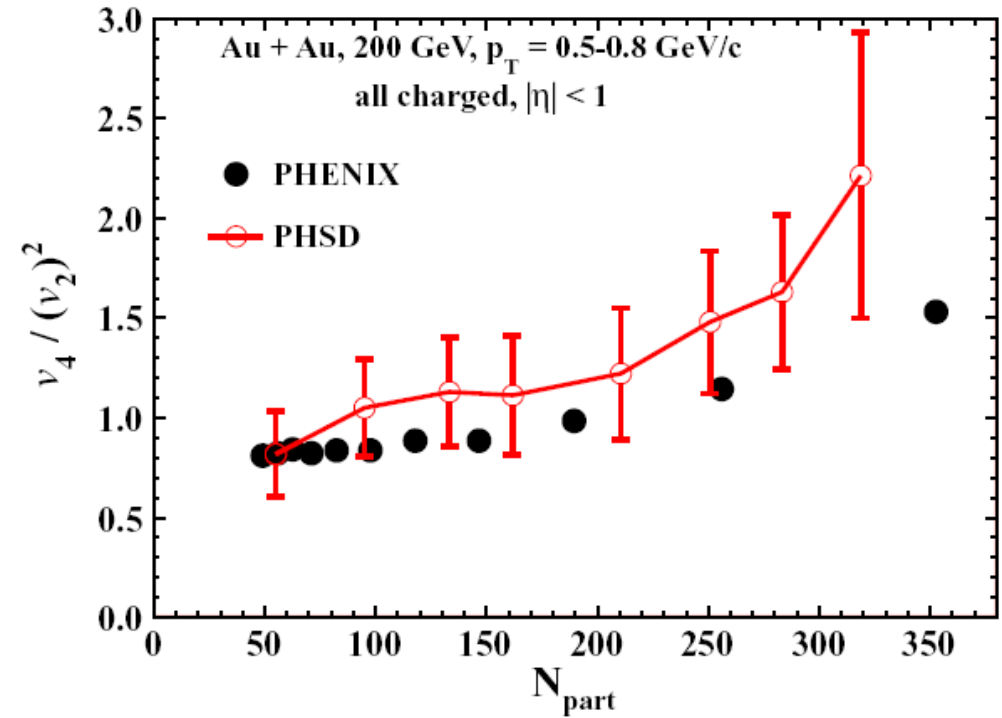
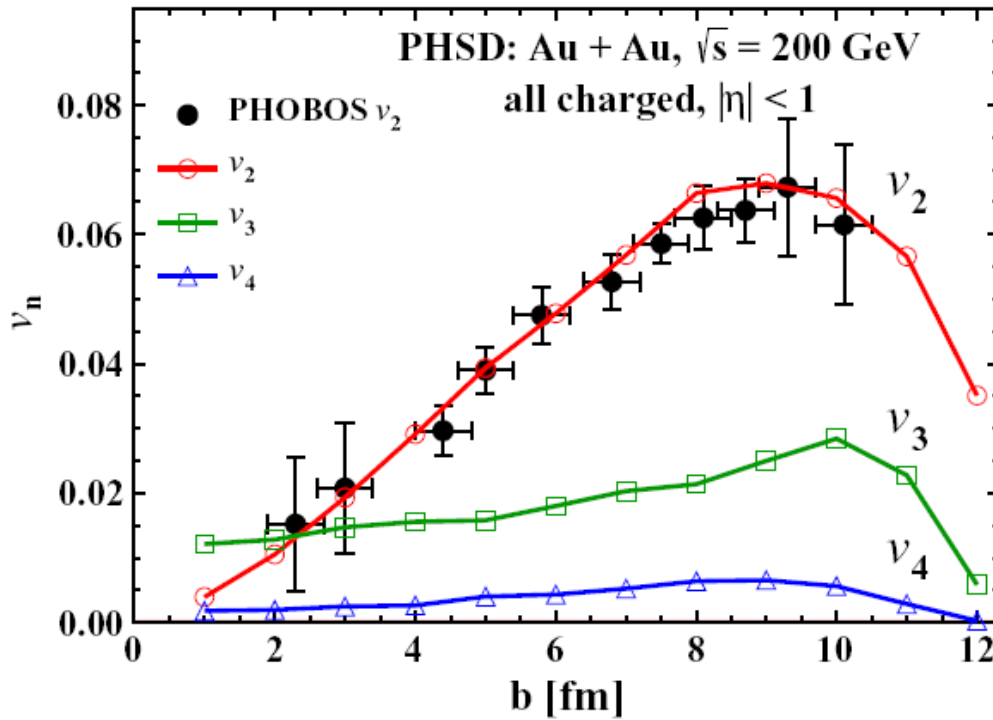
Elliptic flow v_2 vs. collision energy for Au+Au



- v_2 in PHSD is larger than in HSD due to the repulsive scalar mean-field potential $U_s(\rho)$ for partons
- v_2 grows with bombarding energy due to the increase of the parton fraction



Flow coefficients versus centrality at RHIC



□ increase of v_2 with impact parameter but flat v_3 and v_4

Fluctuations and correlations

Lattice QCD: Critical Point

Fluctuations of the **quark number density (susceptibility)** at $\mu_q > 0$

[F. Karsch et al.]

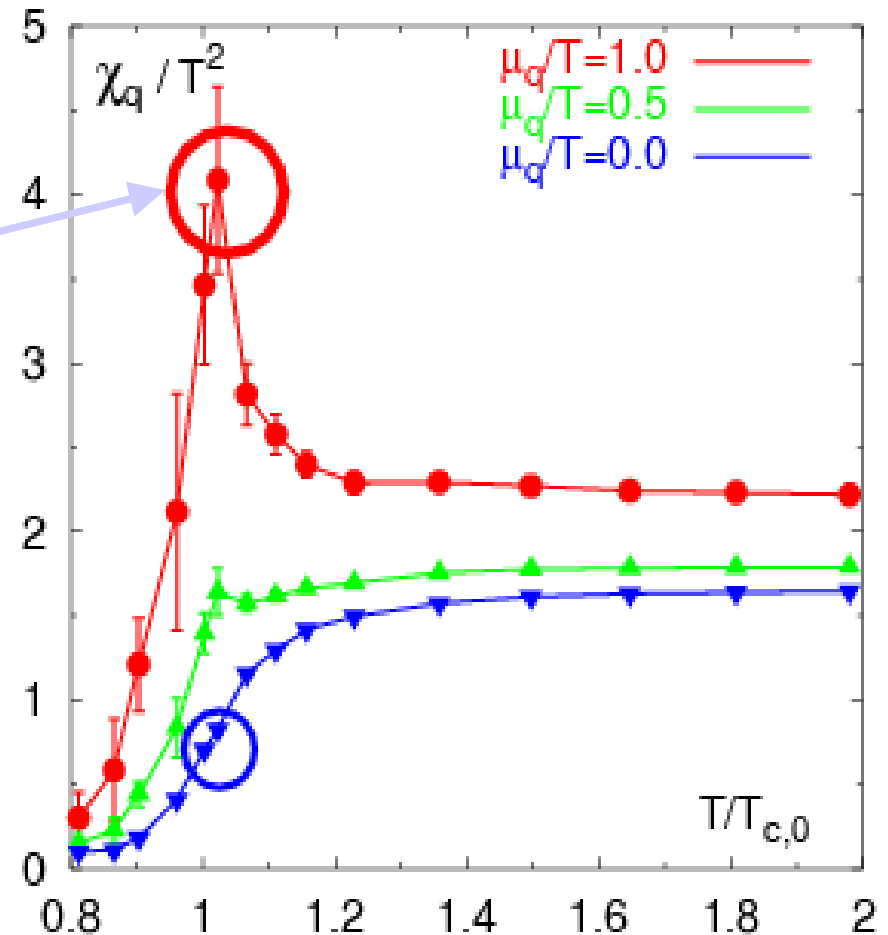
$$\frac{\chi_q}{T^2} = \left[\frac{\partial^2}{\partial (\mu_q / T)^2} \frac{P}{T^4} \right]_{T_{fixed}}$$

Lattice QCD predictions:

χ_q (quark number density fluctuations) will diverge at the **critical chiral point** =>

Experimental observation – look for **non-monotonic behavior** of the observables near the critical point :

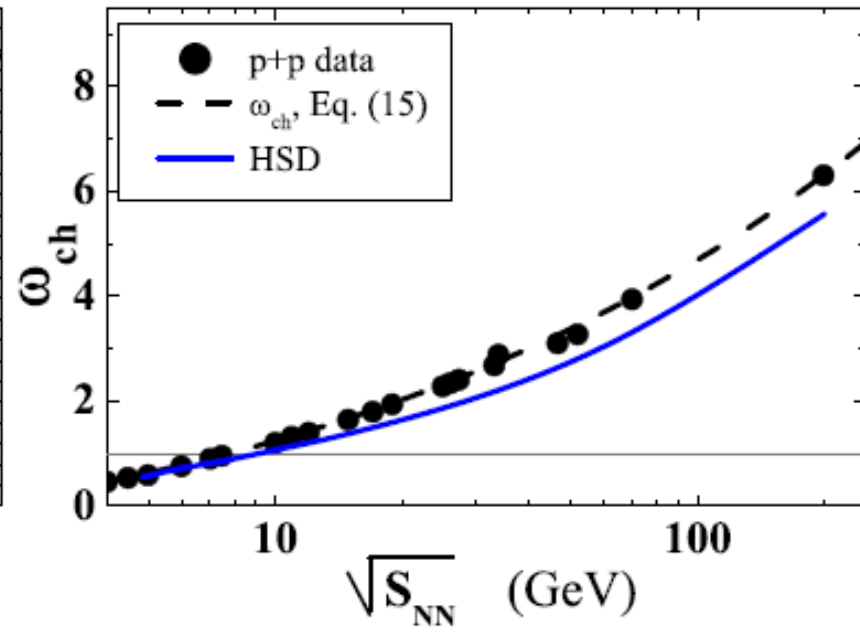
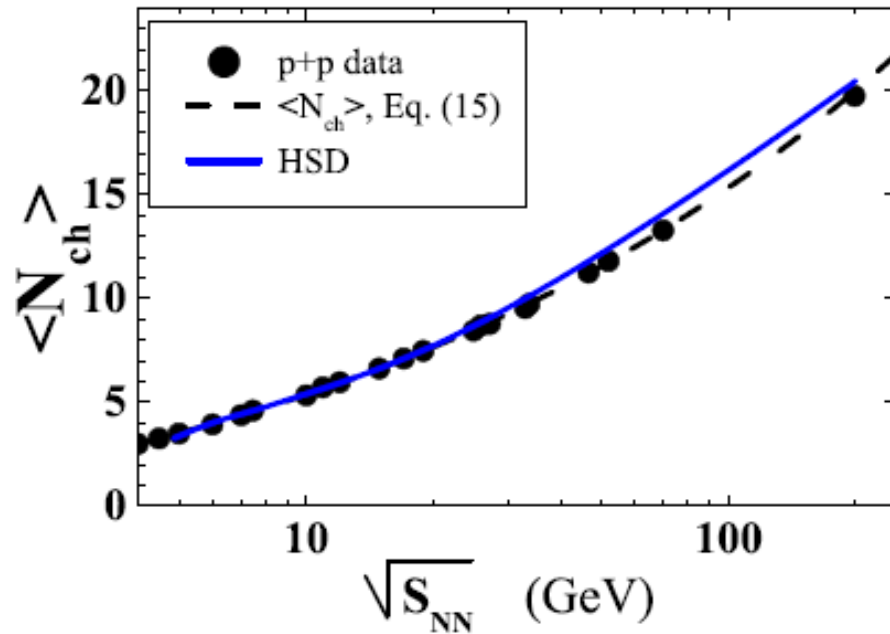
- baryon number fluctuations
- charge number fluctuations
- multiplicity fluctuations
- particle ratio fluctuations (K/π , K/p , ...)
- mean p_T fluctuations
- 2 particle correlations
- ...



Multiplicity fluctuations in p+p

- **Scaled variance - multiplicity fluctuations** in some acceptance (charge, strangeness, etc.):

$$\omega = \frac{\text{Var}(N)}{\langle N \rangle} = \frac{\langle N^2 \rangle - \langle N \rangle^2}{\langle N \rangle}$$

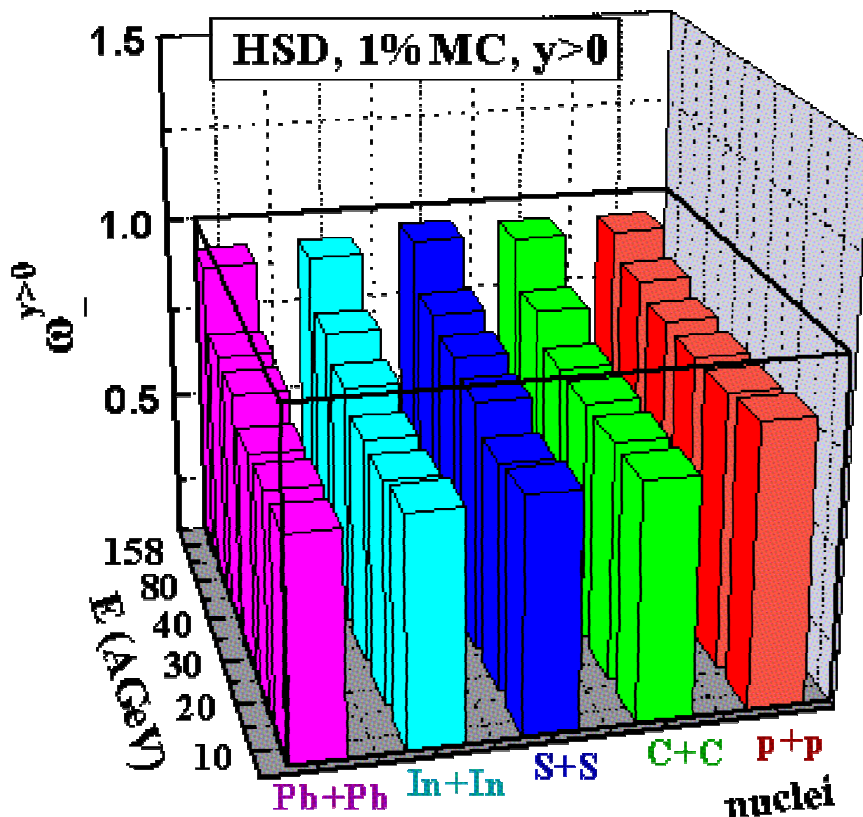


- The excitation functions of N_{ch} and charge multiplicity fluctuations ω_{ch} from **HSD** are approximately in line with experimental data

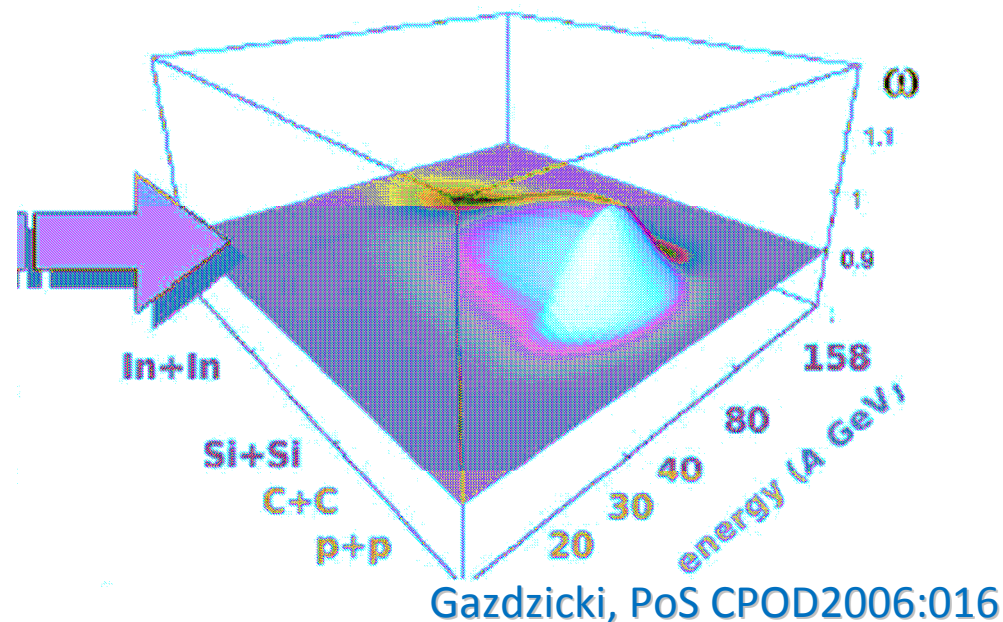
Multiplicity fluctuations in HSD: 1%MC

Konchakovski, Lungwitz, Gorenstein, Bratkovskaya, Phys. Rev. C78 (2008) 024906

rapidity $y > 0$



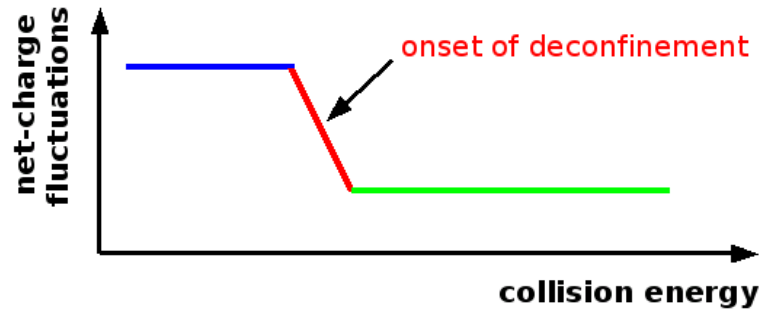
□ Multiplicity fluctuations for 1%MC practically do not **depend on atomic mass for $y > 0$** and only slightly grow with increasing collision energy.



□ **HSD (and UrQMD) show a plateau** on top of which the SHINE Collaboration expects to find increasing multiplicity fluctuations as a "signal" for the critical point !

Charge fluctuations

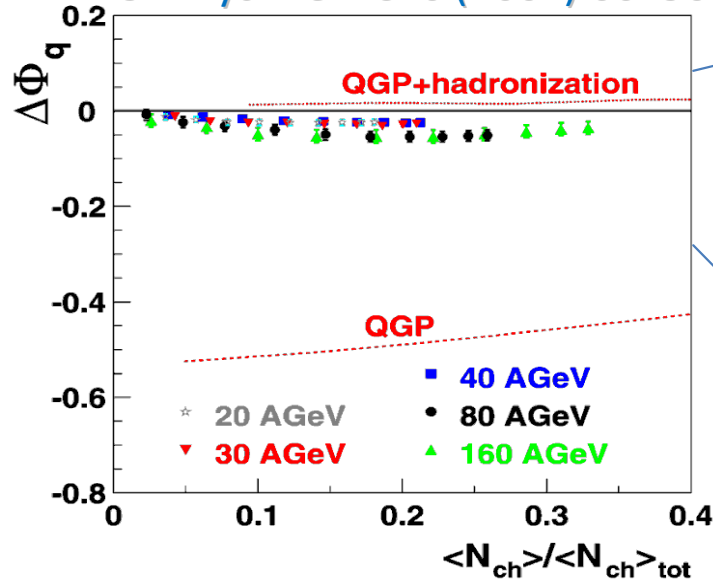
- sensitive to the **EoS** at the early stage of the collision and to its changes in the deconfinement phase transition region



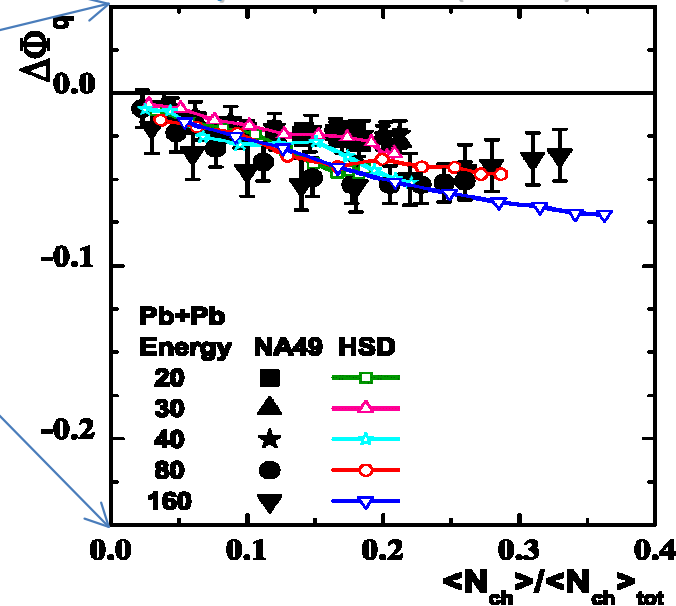
Jeon, Koch, PRL85 (2000) 2076
Asakawa, Heinz, Muller PRL85 (2000) 2072

- net-charge fluctuations are smaller in QGP than in a hadron gas

NA49: Phys. Rev. C70 (2004) 064903

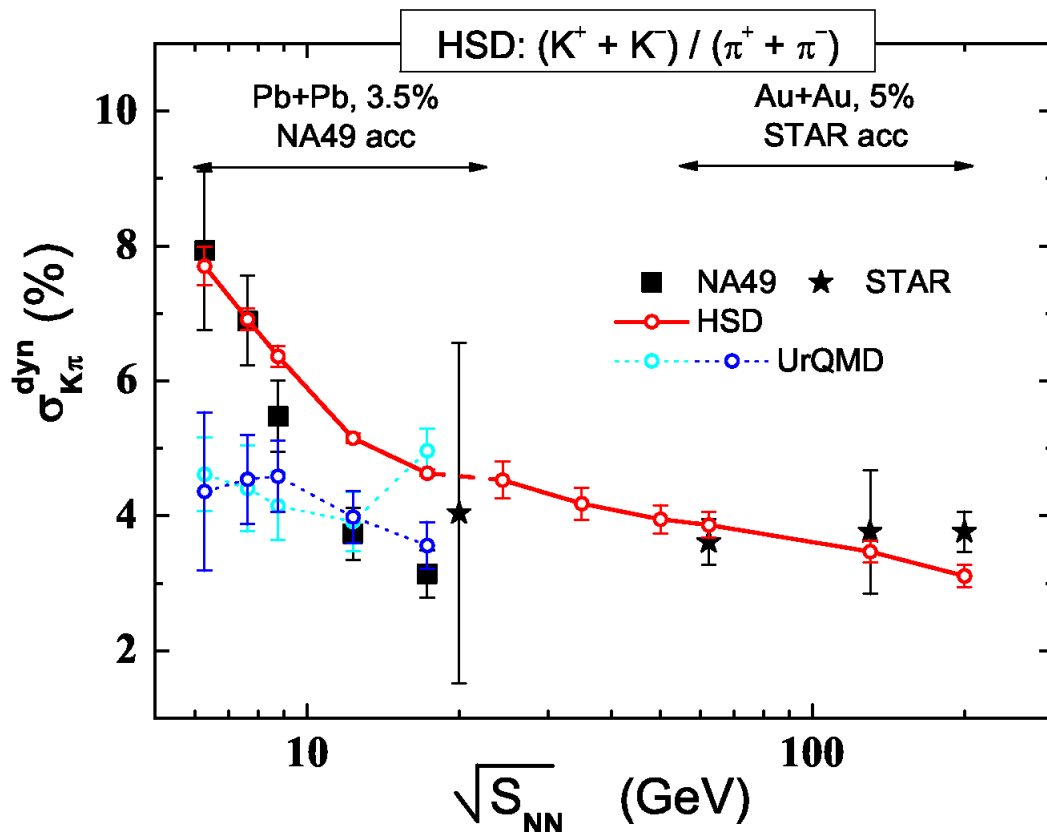


HSD: Phys. Rev. C74 (2006) 64911



- The **decay of resonances** strongly modifies the initial QGP fluctuations!

K/ π -ratio fluctuations: Transport models vs Data



HSD: Phys. Rev. C 79 (2009) 024907

UrQMD: J. Phys. G 30 (2004) S1381, PoS CFRNC2006,017

NA49: 0808.1237

STAR: 0901.1795

$$\sigma^2 \equiv \frac{\langle \Delta(N_A/N_B)^2 \rangle}{\langle N_A/N_B \rangle^2}$$

■ In GCE for ideal Boltzman gas:

$$\sigma^2 = \frac{1}{\langle N_A \rangle} + \frac{1}{\langle N_B \rangle}$$

• **Exp. data** show a plateau from top SPS up to RHIC energies and an increase towards lower SPS energies

→ **evidence for a critical point at low SPS energies ?**

• **but** the HSD (without QGP!) results shows the same behavior →

• K/ π -ratio fluctuation is **driven by hadronic sources** → No evidence for a critical point in the K/ π ratio ?

• K/ π ratio fluctuation is **sensitive to the acceptance!**

Outlook - Perspectives

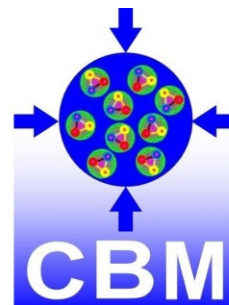
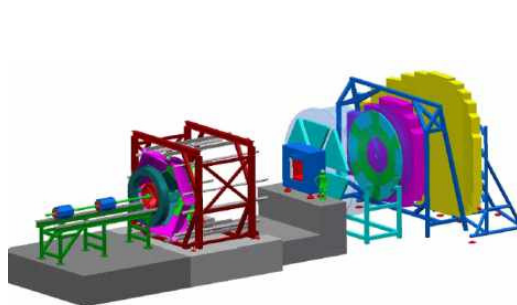
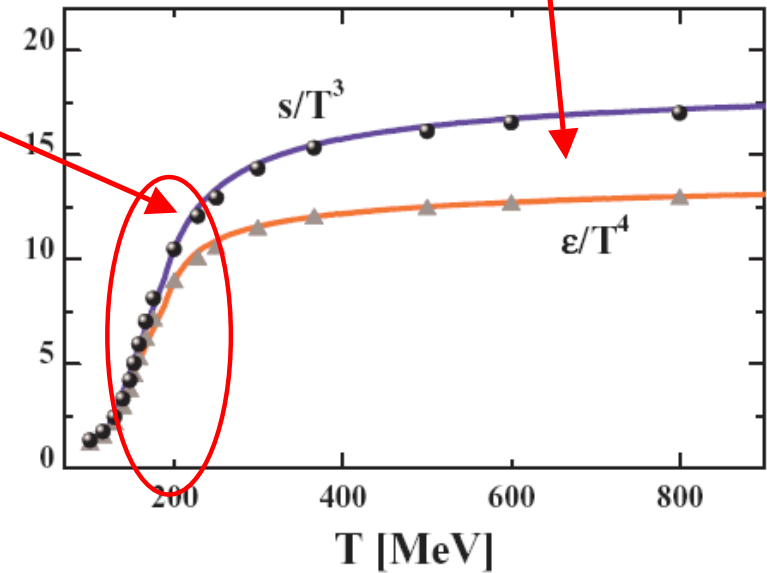
What is the stage of matter close to T_c and large μ :

- 1st order phase transition?
- ‚Mixed‘ phase = interaction of partonic and hadronic degrees of freedom?

Open problems:

- How to describe a **first-order phase transition** in transport models?
- How to describe parton-hadron interactions in a **‚mixed‘ phase**?

Lattice EQS for $m=0$
 \rightarrow ‚crossover‘, $T > T_c$





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