

# Tests of nuclear properties with astronomical observations of neutron stars

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# Outline

Four examples of testing of nuclear physics with neutron stars

1) EOS from qLMXBs in globular clusters

(Heinke, WH+, arXiv:1406.1497)



Credit: HEASARC

2) EOS and superfluidity/superconductivity from Cassiopeia A NS

(WH+, in preparation)

3) EOS and superfluidity from pulsar glitches

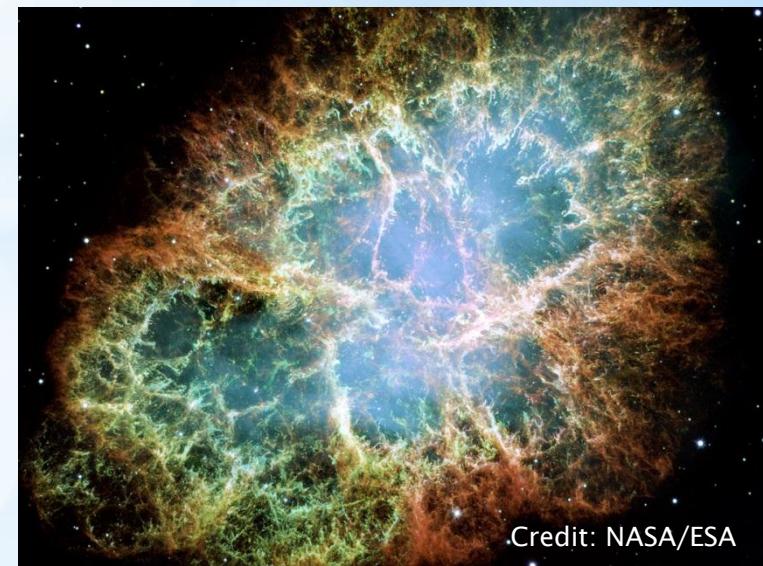
(Andersson, WH+, 2012)

4) Gravitational wave-induced r-modes

(WH+, 2011; Haskell, WH+, 2012; Andersson, WH+, 2014)

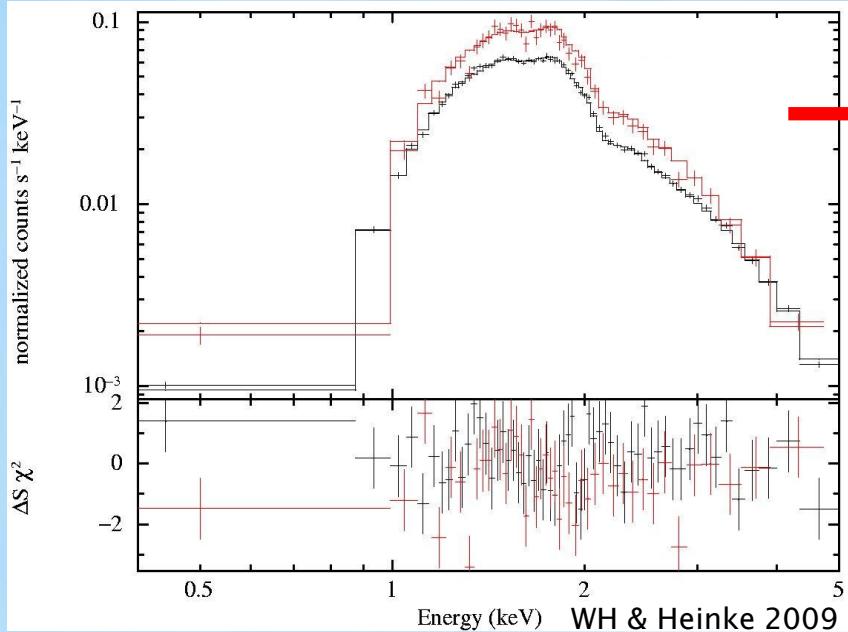


~50 km > 2×NS diameter

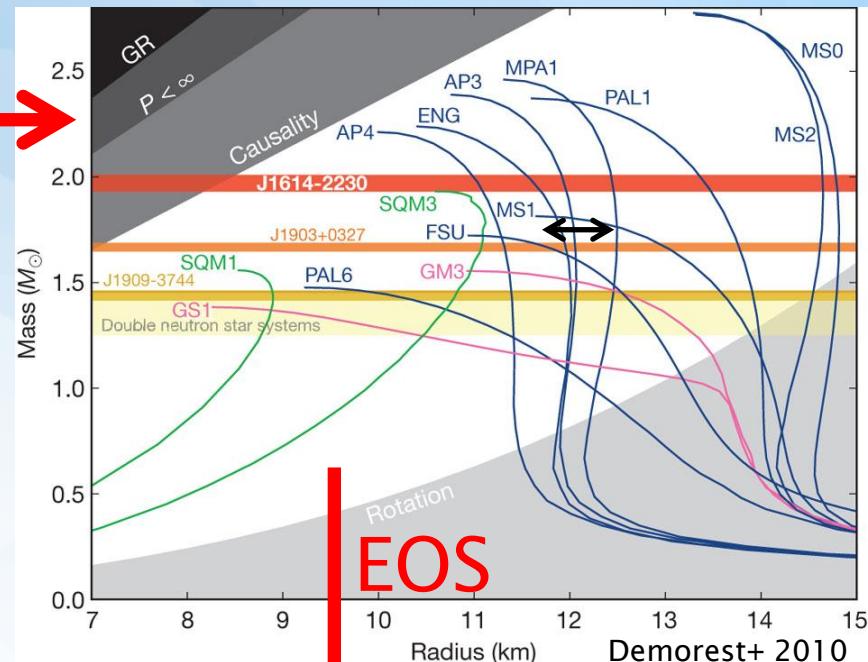


.Credit: NASA/ESA

# EOS from Neutron Star Surface Radiation



*M-R*

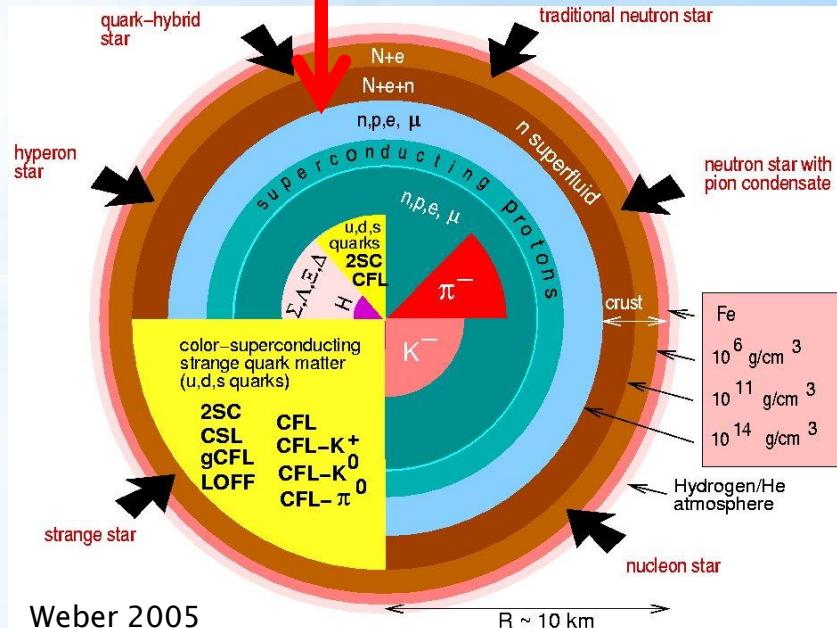


1) X-ray/UV/optical energy spectrum from telescopes (eg *Chandra*, *Hubble*, *XMM*)

2) Fit spectrum with model:

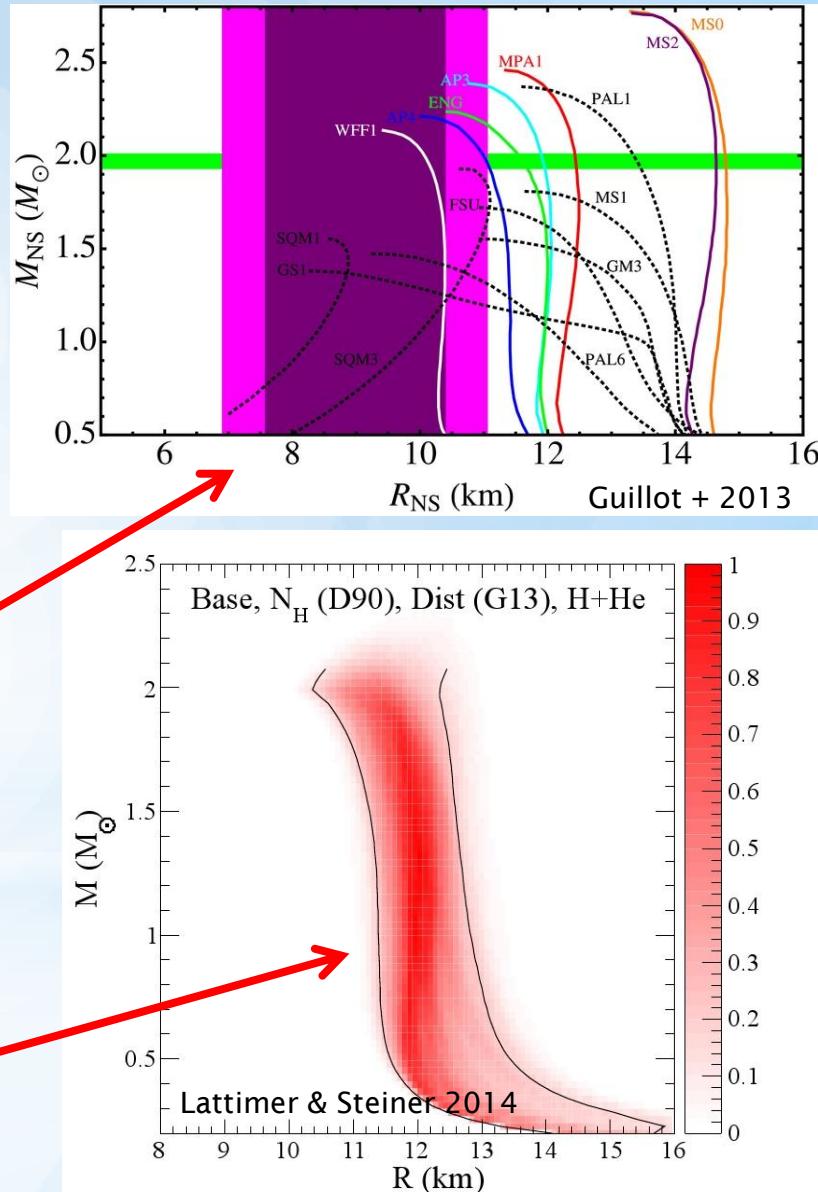
- blackbody:  $T$ ,  $R/d$
- atmosphere: redshift  $\propto M/R$ , surface gravity  $\propto M/R^2$ , composition, magnetic field

3) Constrain EOS



# Neutron star radii from quiescent low-mass X-ray binaries (qLMXBs) in globular clusters

- qLMXBs in globular clusters (GCs)
  - binary star system with NS accreting from low-mass companion, thus **X-ray bright**
  - globular cluster – mini-galaxy orbiting Milky Way with **well-determined distance**
  - spectral fit depends on  **$R/d$**
- Radius constraints using five qLMXB in GC
  - Guillot+ (2013):  $R = 9.1_{-1.5}^{+1.3}$  km
    - NGC 6397:  $R \approx 6.6 \pm 1.2$  km
    - $\omega$  Cen:  $R \approx 20.1 \pm 7.3$  km
    - other three:  $R \sim 10 \pm 3$  km
    - exclude NGC 6397:  $R = 10.7_{-1.4}^{+1.7}$  km
  - Lattimer & Steiner (2014):  $R \approx 12 \pm 1$  km



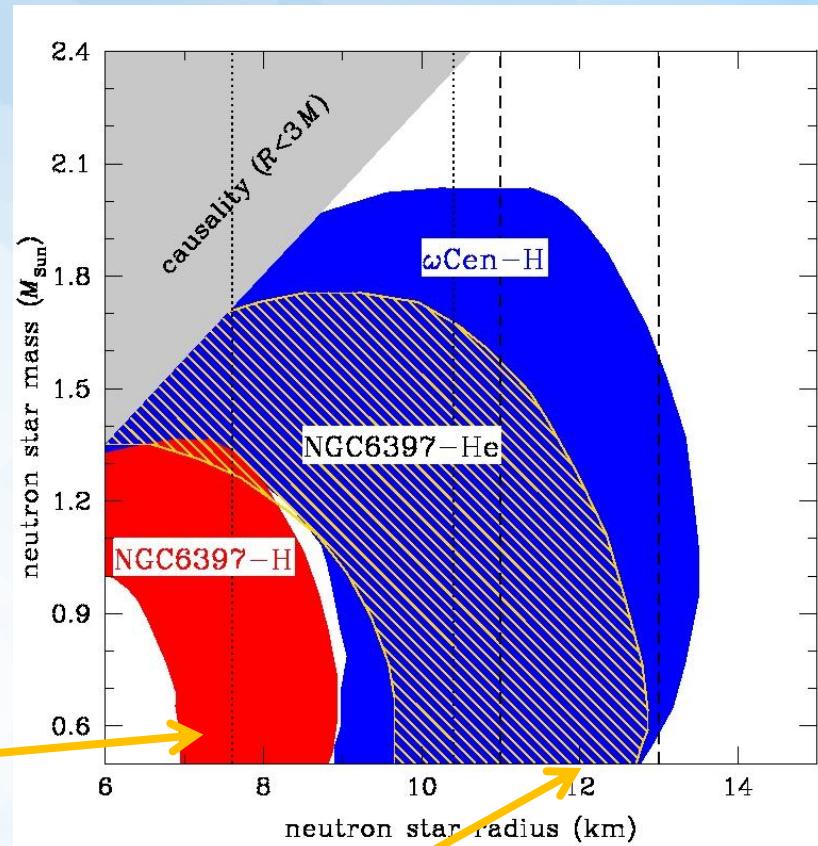
# Neutron star radii from qLMXBs in globular clusters

Heinke, WH+, arXiv:1406.1497

- NGC 6397
  - *Hubble* observations place upper limit on hydrogen on companion  
⇒ possible helium white dwarf  
⇒ **NS has helium surface (?)**

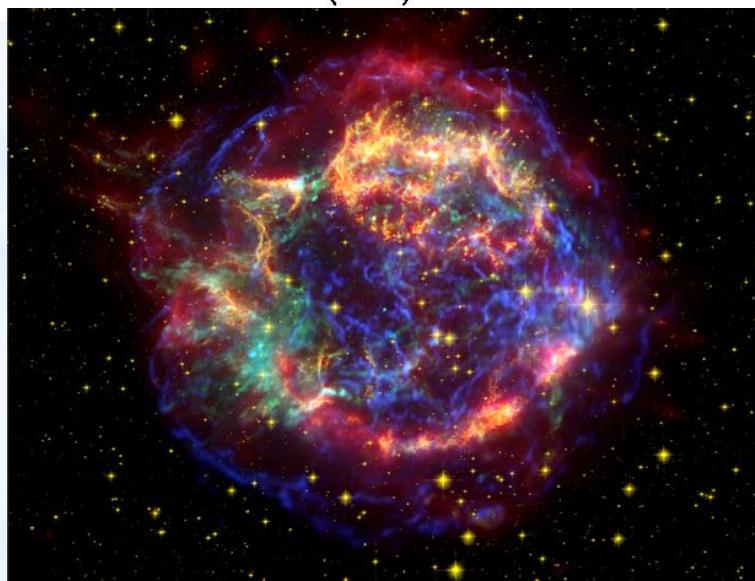
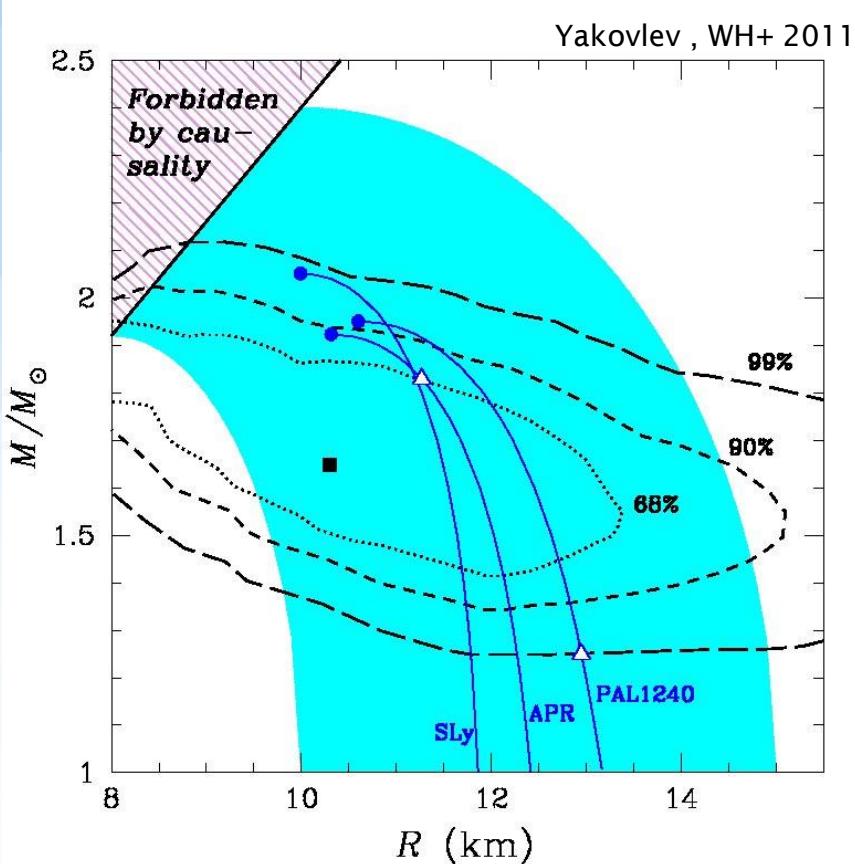
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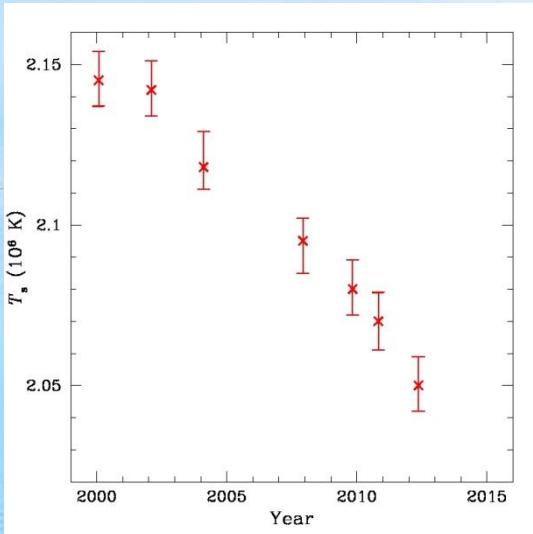
# Cassiopeia A neutron star and APR and BSk EOSs

- Mass and radius from X-ray spectrum
  - redshift –  $M/R$
  - brightness –  $R^2$
  - surface gravity –  $M/R^2$
- Neutron star cooling
  - detailed EOS info (eg particle abundances)
  - superfluid & superconducting gap energies
- Detailed constraints from using specific EOS
  - APR ( $A18 + \delta v + UIX^*$ ) –  $M_{dU} > 1.96 M_{\text{sun}}$
  - BSk20
  - BSk21 –  $M_{dU} > 1.59 M_{\text{sun}}$

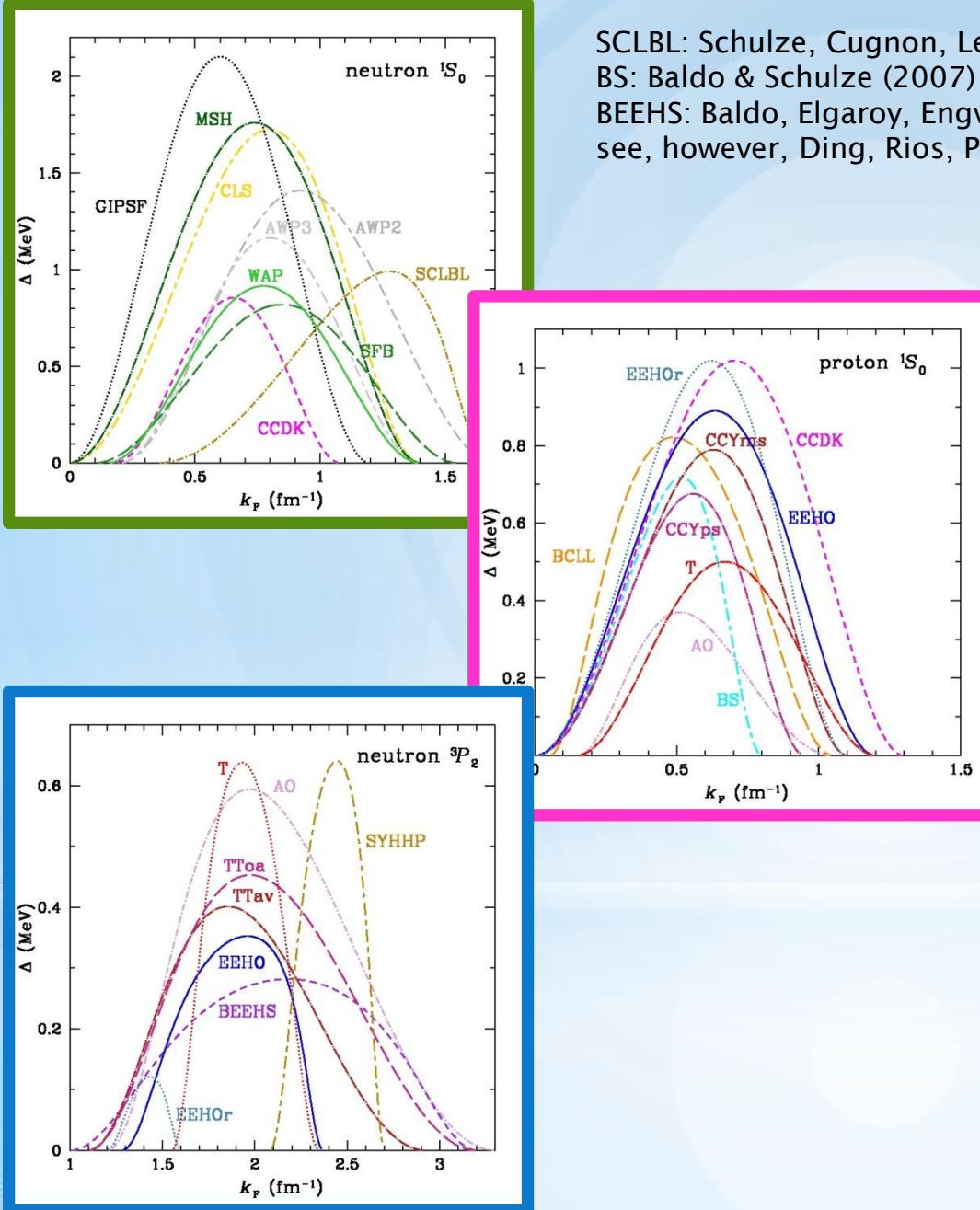


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# Superfluid and Superconductor Gap Energies



SCLBL: Schulze, Cugnon, Lejeune, Baldo, Lombardo (1996)

BS: Baldo & Schulze (2007)

BEEHS: Baldo, Elgaroy, Engvik, Hjorth-Jensen, Schulze (1998)

see, however, Ding, Rios, Polls+ 2014

- sf/sc characterized by energy  $\Delta(k_F)$  where  $k_F \propto n^{1/3}$
- Matter becomes sf/sc when  $T < T_c(\Delta)$
- 3 sf/sc (pairing) types in NS:
  - inner crust-core – n singlet  $^1S_0$
  - core – proton singlet  $^1S_0$
  - core – neutron triplet  $^3P_2$ - $^3F_2$
- Parameterize theoretical models by  
(see Kaminker et al 2001; Andersson et al 2005)

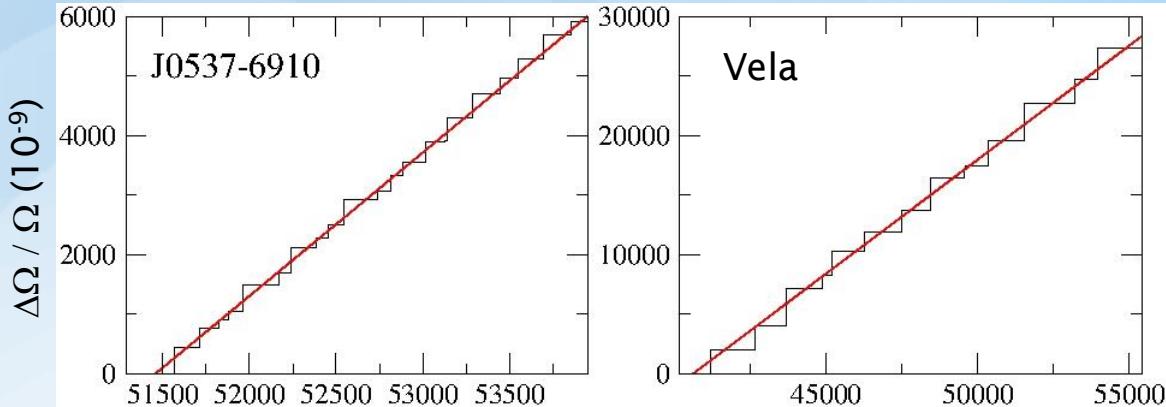
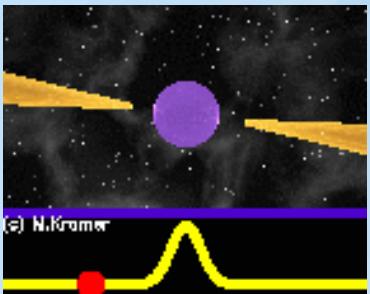
$$\Delta = \Delta_0 (k_F - k_0)^2 / [(k_F - k_0)^2 + k_1] \times (k_F - k_2)^2 / [(k_F - k_2)^2 + k_3]$$

- 9 neutron singlet models
- 9 proton singlet models
- 8 neutron triplet models

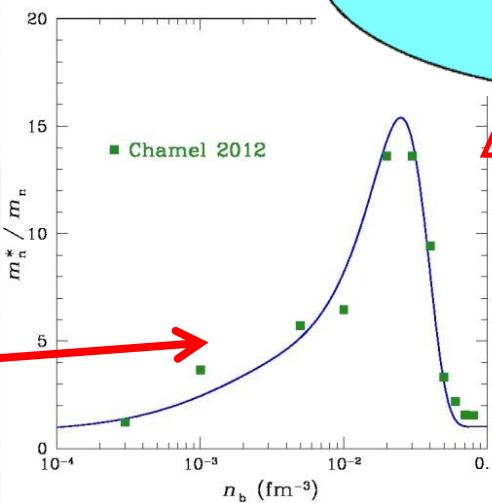
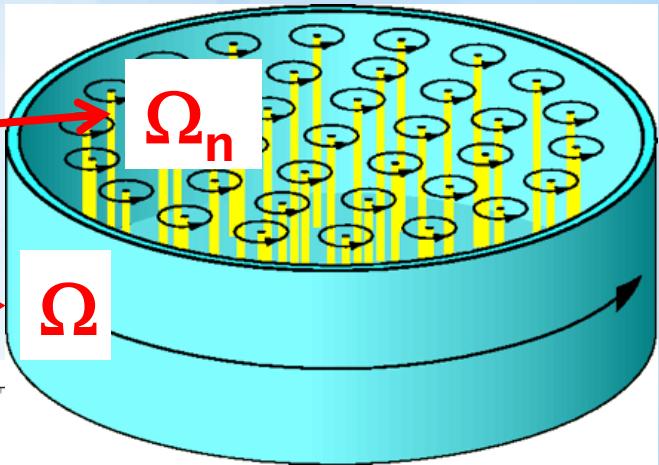
# Preliminary Conclusions

# Pulsar Glitches: The Crust is Not Enough

Andersson, WH+, PRL, 109, 241103 (2012); see also Chamel (2013)



- Track spin evolution of 11 pulsars
- Model: Two-component moment of inertia
  - 1. inner crust superfluid
    - no spin-down since vortices pinned
  - 2. outer crust (+ core)
    - spin-down by EM radiation  
⇒ glitch when  $\Delta\Omega / \Omega$  too big
- Requires angular momentum/moment of inertia reservoir
  - $I_{\text{crust}} / I_{\text{total}} \approx [-\Omega / (d\Omega/dt)] (\sum \Delta\Omega^i / \Omega) / t_{\text{obs}}$   
 $= 2 \tau_c A \langle m_n^* \rangle / m_n$   
**superfluid entrainment** (Chamel 2012)

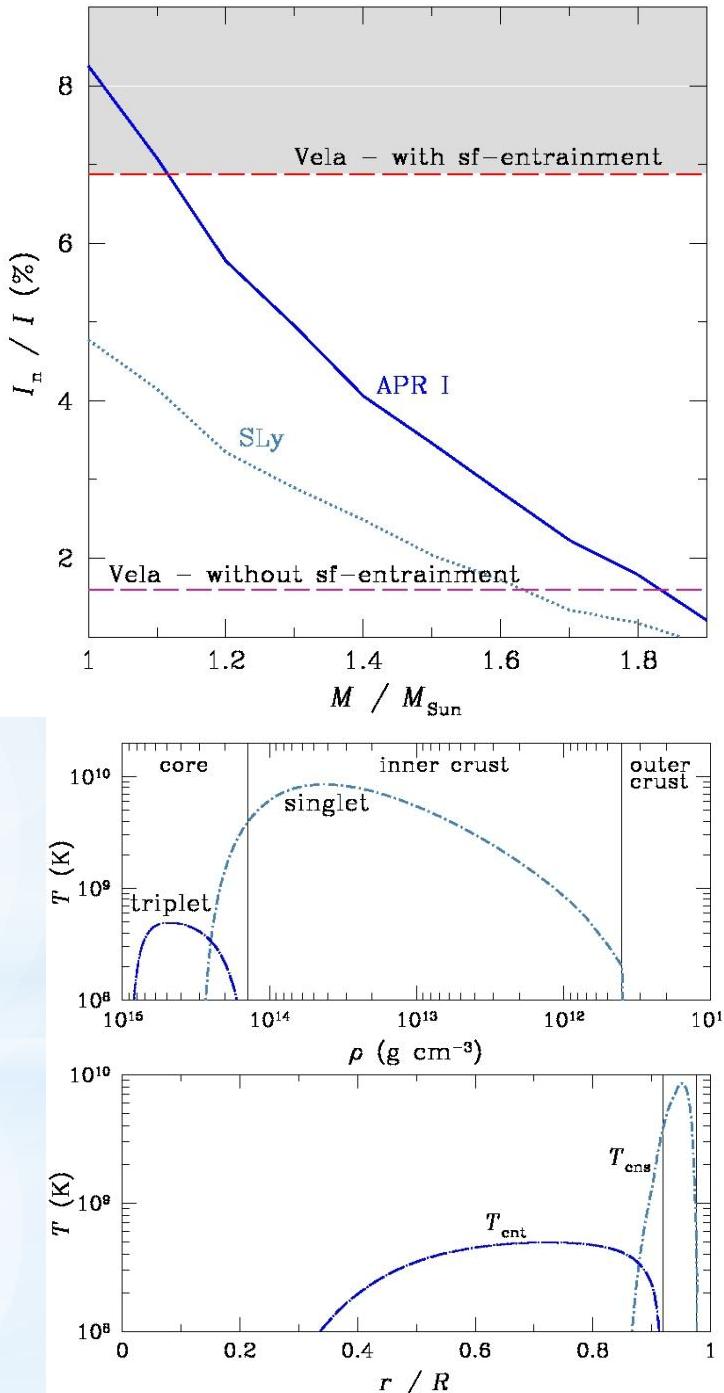


$$\Delta\Omega \propto \Omega_n - \Omega$$

# The Crust is Not Enough

Andersson, WH+, PRL, 109, 241103 (2012)

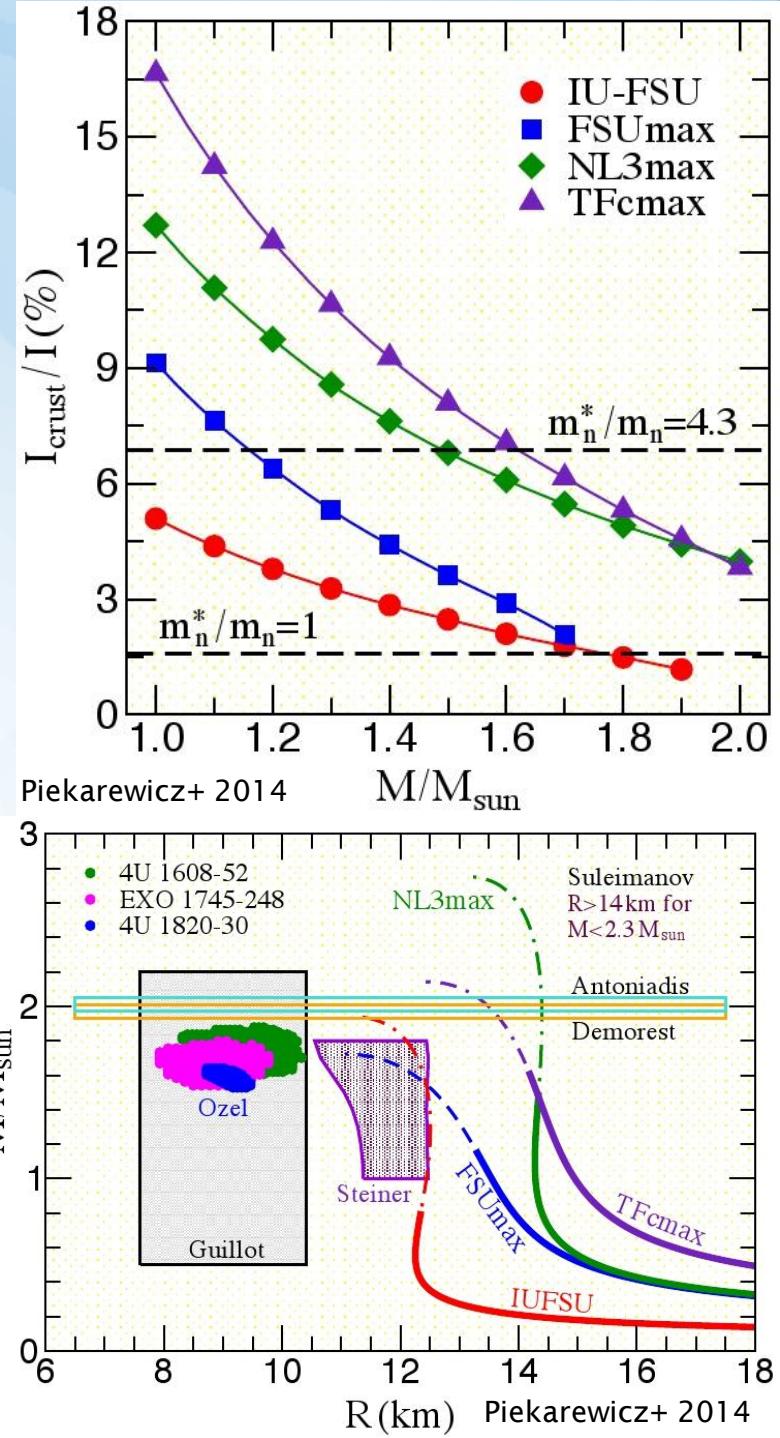
- Superfluid entrainment increases neutron effective mass (Chamel 2012)
- Glitches need mom of inertia reservoir 4-8%  
e.g., Vela: 7%
- NS models provide < 8 %
- Possible solutions:
  - stiff EOS and low NS mass
  - crust superfluid extends into core ( $\propto L$ )  
(see eg Hooker, Newton, Li 2013)
  - core superfluid
  - crust EOS and superfluid effective mass  
(see De La Mota talk)
  - crust may be enough: extremely stiff EOS  
(Piekarewicz, Horowitz+ 2014; Steiner, Newton+ 2014)



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# R-mode oscillations and X-ray detection(?)

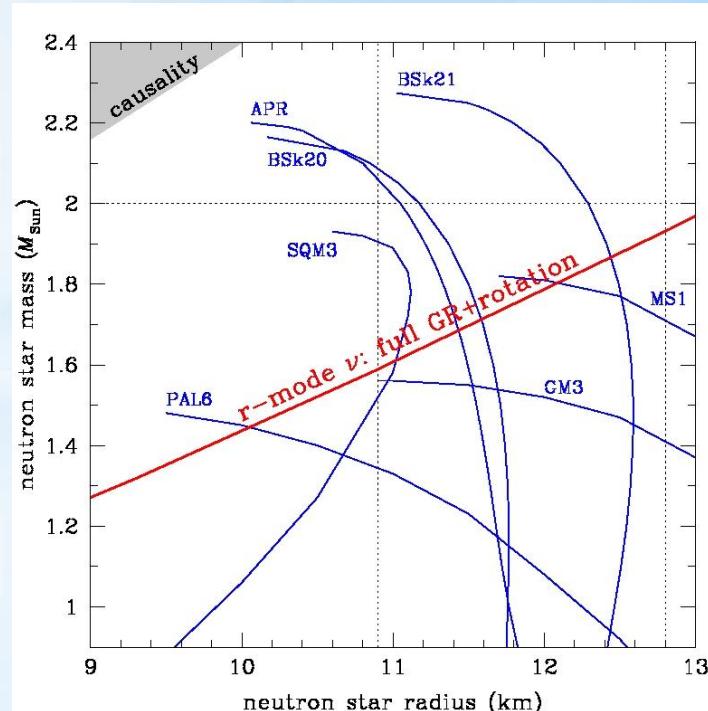
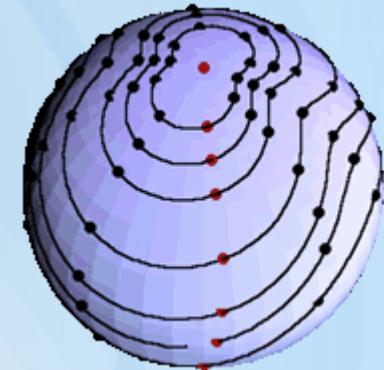
- Fluid oscillations in rotating stars with quadrupolar (corotating) frequency

$$\nu = (2/3) \times \Omega_s$$

- Observed in NS XTE J1751-305  
(Strohmayer & Mahmoodifar 2014)

$$\nu = 0.5727597 \times \Omega_s$$

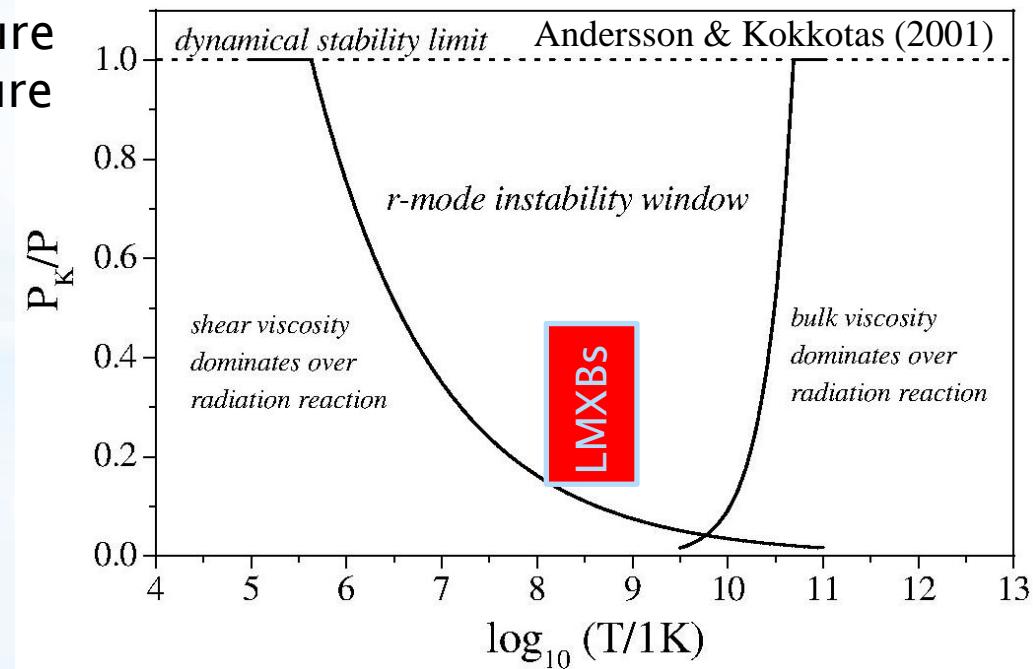
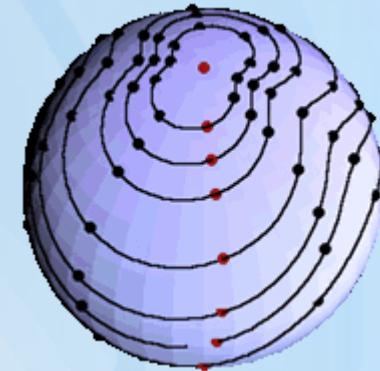
- Andersson, WH+, MNRAS, 442, 1786 (2014):
  - Relativistic corrections to mode frequency
  - Observed oscillation amplitude and spin evolution inconsistent with r-mode theory



# R-mode instability and emission of gravitational waves

- Fluid oscillations in rotating stars
- Generically unstable  
(Andersson 1998; Friedman & Morsink 1998):
  - GW emission drives r-mode growth
  - Viscosity damps r-mode
    - shear viscosity at low temperature
    - bulk viscosity at high temperature
  - R-mode (in)stability criterion

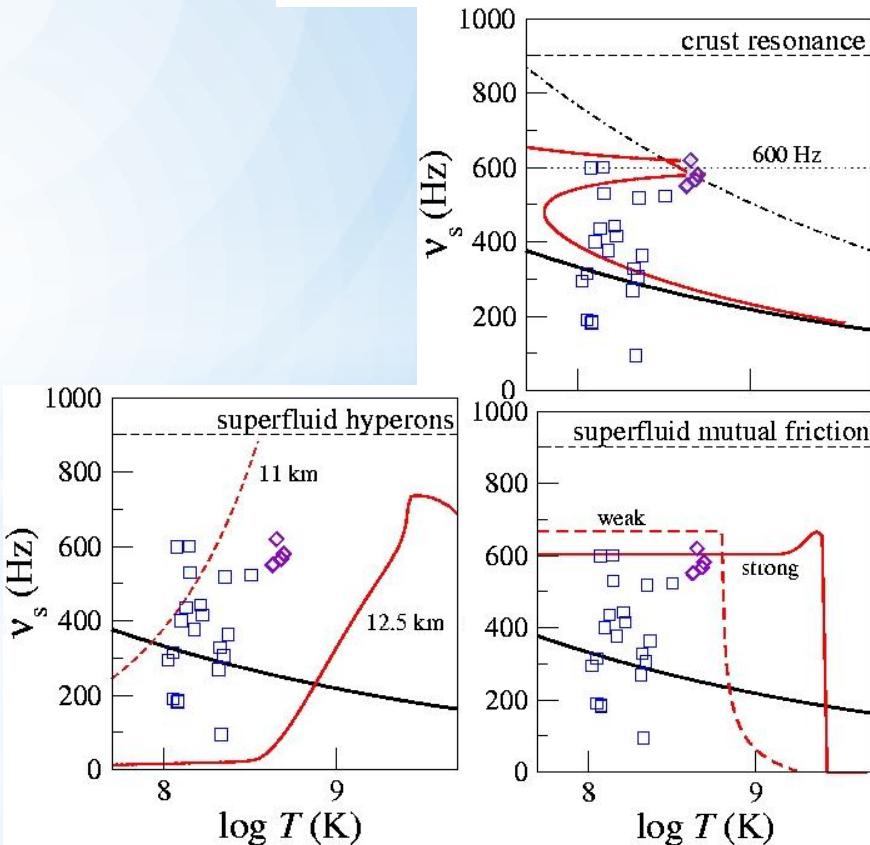
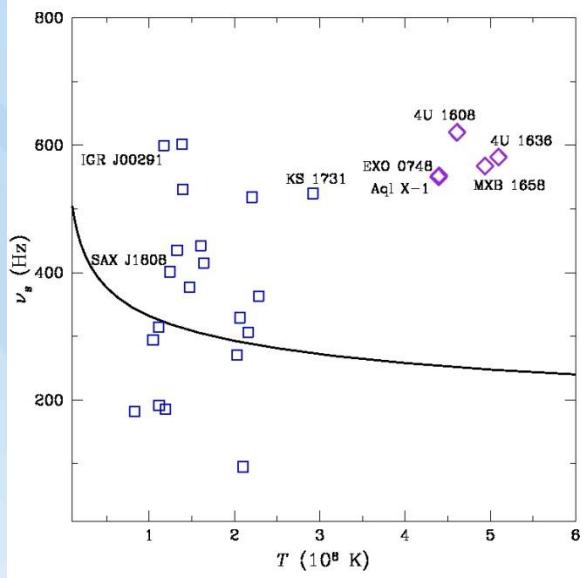
$$t_{\text{gw}}(v_s) = t_{\text{visc}}(v_s, T)$$



# Physics of r-mode instability

WH+, PRL, 107, 101101 (2011);  
Haskell, WH+, MNRAS, 424, 93 (2012)

- Instability window for GWs is uncertain
- GW sources counter to expectations
- Rich physics arena
  - core temperature estimates:
    - envelope composition
    - thermal conductivity
    - neutrino emission
  - window shape:
    - crust-core transition/elasticity  
(see eg Wen, Newton, Li 2012; Vidana 2012;  
De La Mota talk)
    - superfluidity (critical temperature,  
hyperons, mutual friction)
    - EOS (strange matter, quarks)
    - magnetic field (damping and strength)
    - non-linearity and saturation



# Summary

- Neutron stars are unique astronomical tool for nuclear physics (EOS and sf/sc gaps)
  - quiescent low-mass X-ray binaries
  - Cas A X-ray spectra and cooling
  - radio pulsar glitches
  - r-modes and gravitational waves
- Request for astrophysically-useful parameterization of nuclear properties
- **By studying the big and far, we can understand the small and near.**

