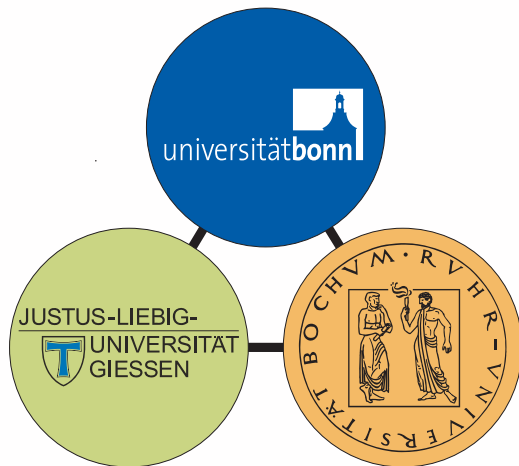


Light Baryon Spectroscopy

Christian S. Fischer

Justus Liebig Universität Gießen

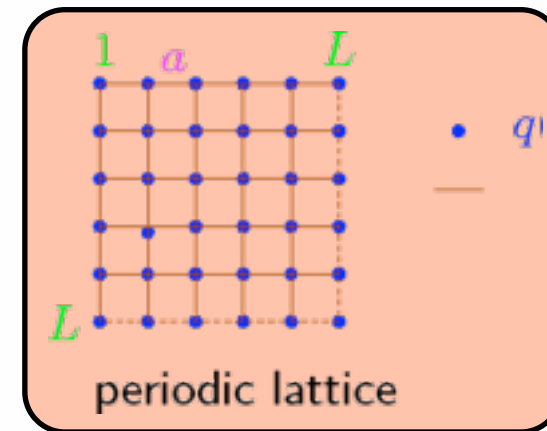


with

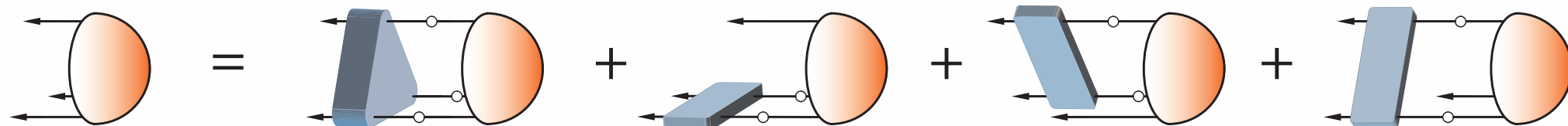
Gernot Eichmann, Helios Sanchis-Alepuz, Richard Williams

1.Introduction

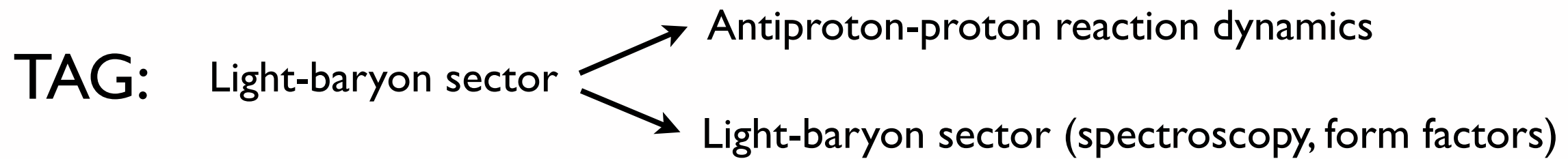
2.Results from Lattice-QCD



3.Results and perspective from DSE/Faddeev-approach



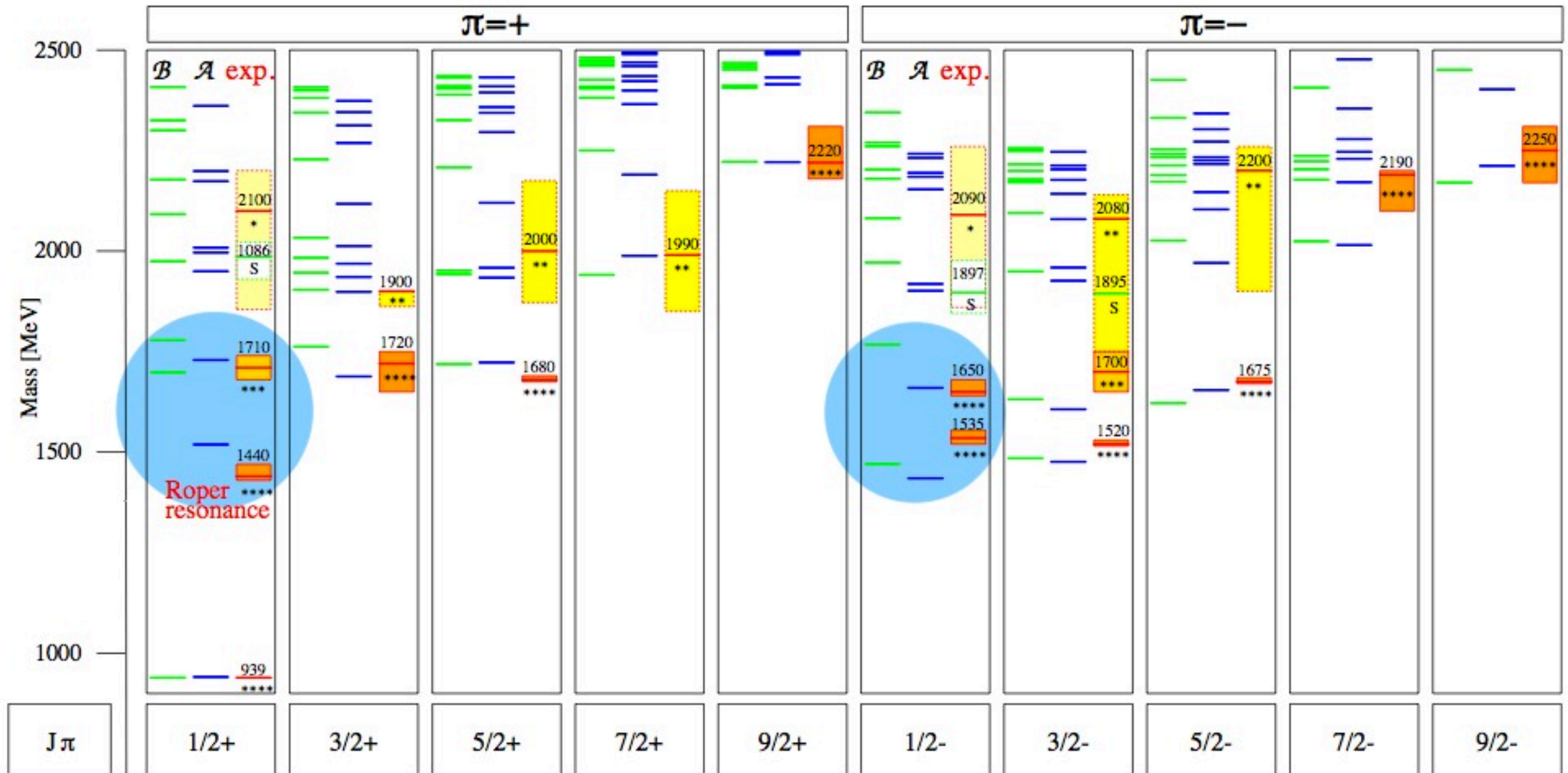
Light baryon spectroscopy



- Underlying QCD forces
 - two-body vs. three-body → Δ vs Y - configuration
 - confinement → Regge trajectories ?!
 - spin structure
 - meson cloud effects → GB-exchange vs QCD
- ‘Missing resonances’ → 3-quark vs. quark-diquark
- Heavy/heavy-light systems → Differences to light baryons
- Coupled-channel effects

Klemt, Richard, Rev.Mod.Phys. 82 (2010) 1095

Quark model



Loring, Metsch, Petry, EPJA 10 (2001) 395

- ‘missing resonances’ ?!
- parity doubling ?!
- level ordering: $N_{\frac{1}{2}}^{\pm}$ vs. $\Lambda_{\frac{1}{2}}^{\pm}$

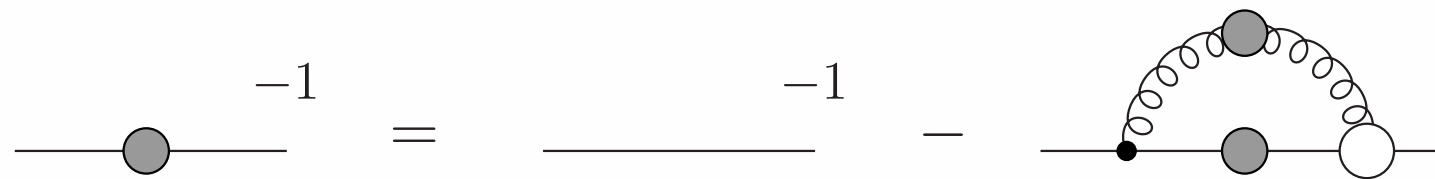
Properties of QCD: Dynamical mass generation

Dynamical quark masses
via weak and strong force



Yoichiro Nambu,
Nobel prize 2008

	u	d	s	c	b	t
$M_{\text{weak}} [MeV/c^2]$	3	5	80	1200	4500	176000
$M_{\text{strong}} [MeV/c^2]$	350	350	350	350	350	350
$M_{\text{total}} [MeV/c^2]$	360	360	450	1600	4900	176000



$$S^{-1}(p) = [i\not{p} + M(p^2)]/Z_f(p^2)$$

Properties of QCD: Dynamical mass generation

Dynamical quark masses
via weak and strong force



Yoichiro Nambu,
Nobel prize 2008

Input parameters in $N_f=2+1+1$ QCD

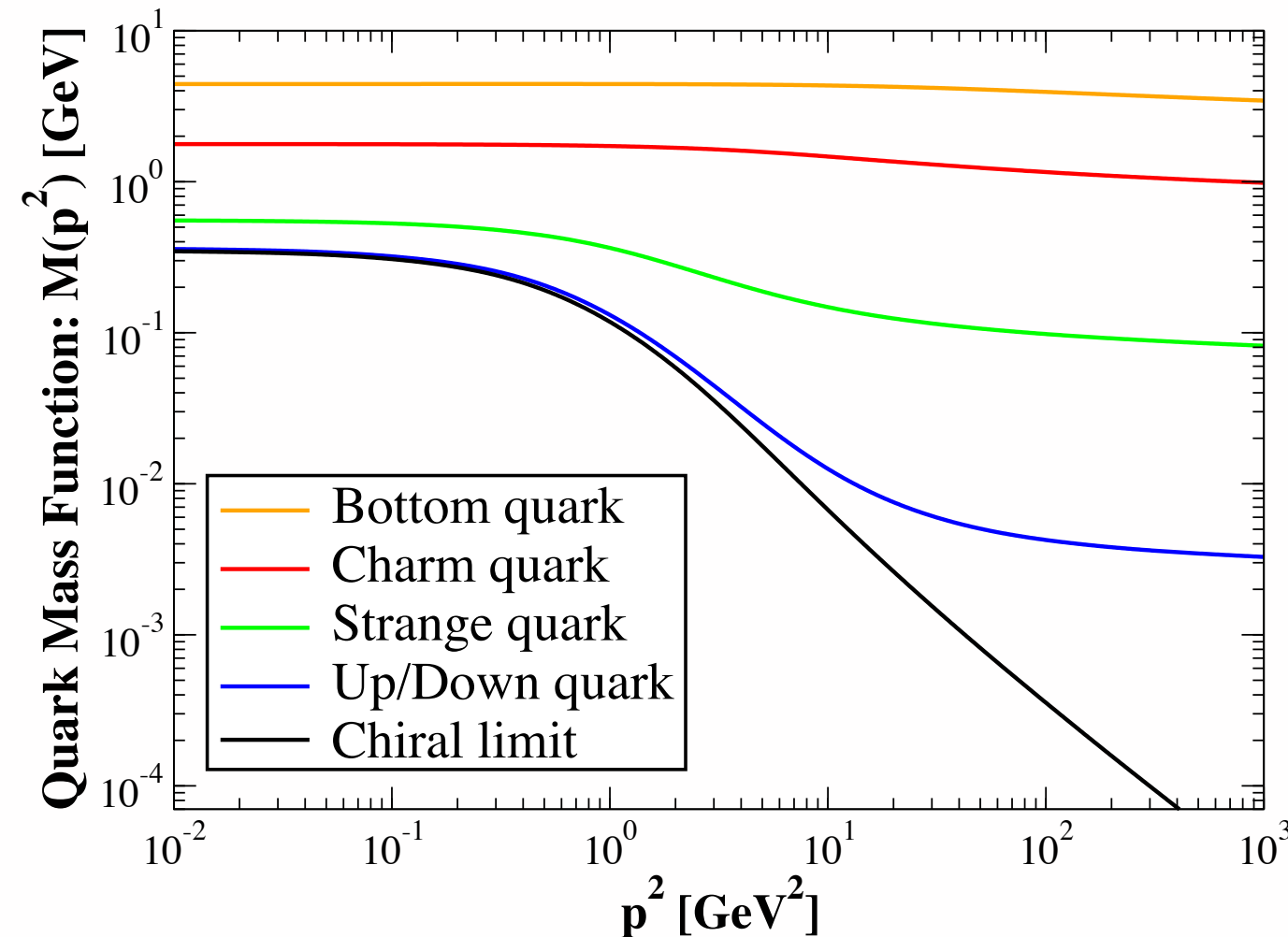
	u	d	s	c	b	t
$M_{\text{weak}} [MeV/c^2]$	3	5	80	1200	4500	176000
$M_{\text{strong}} [MeV/c^2]$	350	350	350	350	350	350
$M_{\text{total}} [MeV/c^2]$	360	360	450	1600	4900	176000

$$\text{Bare propagator} = \text{Bare propagator} + \text{Self-energy correction}$$

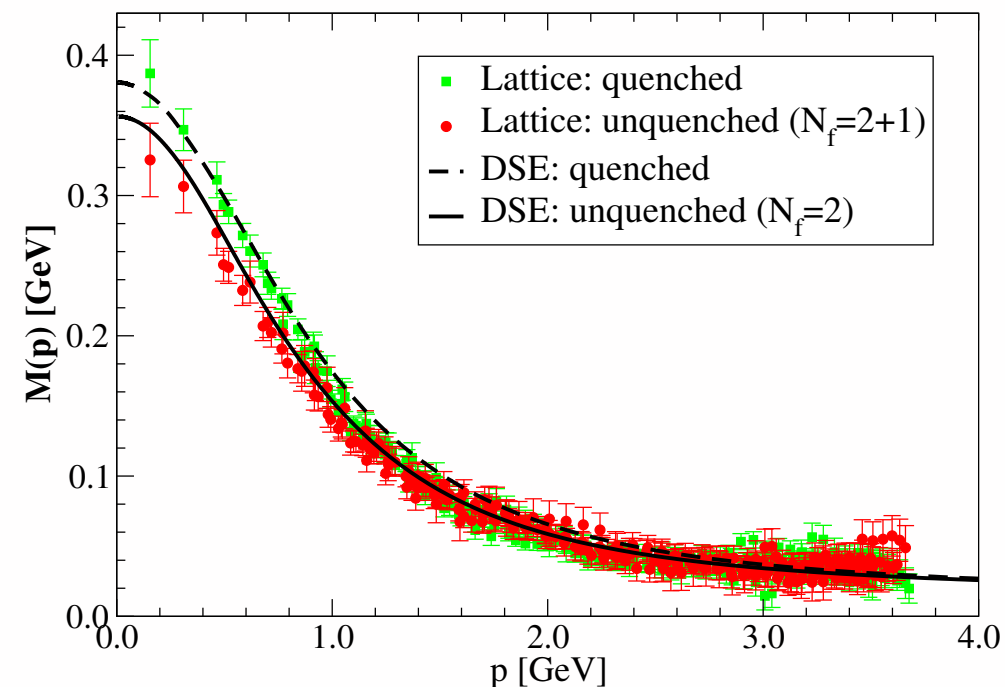
$$S^{-1}(p) = [i\not{p} + M(p^2)]/Z_f(p^2)$$

Quark mass: flavor dependence

Typical solution:



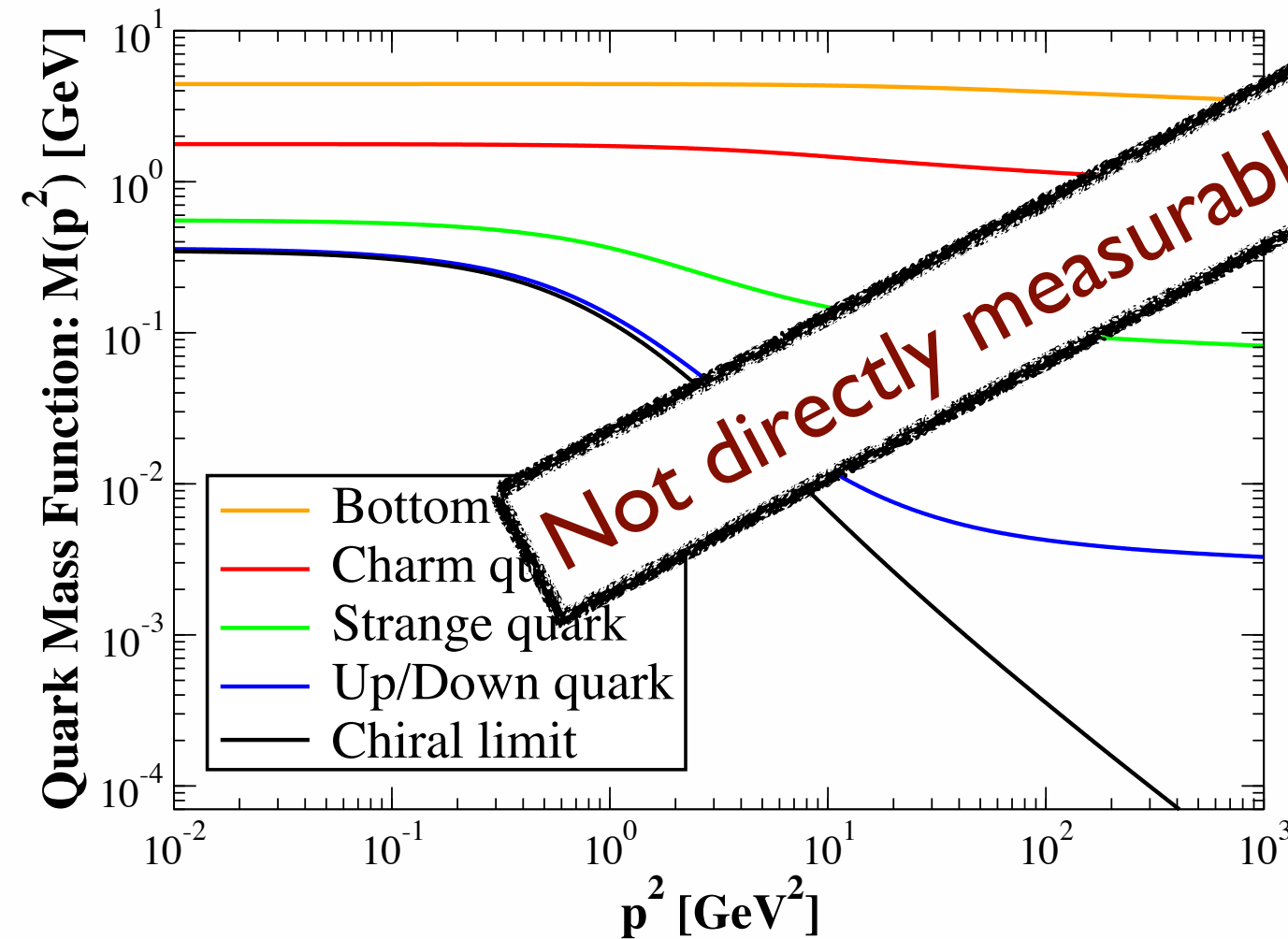
CF, JPG 32 (2006) R253



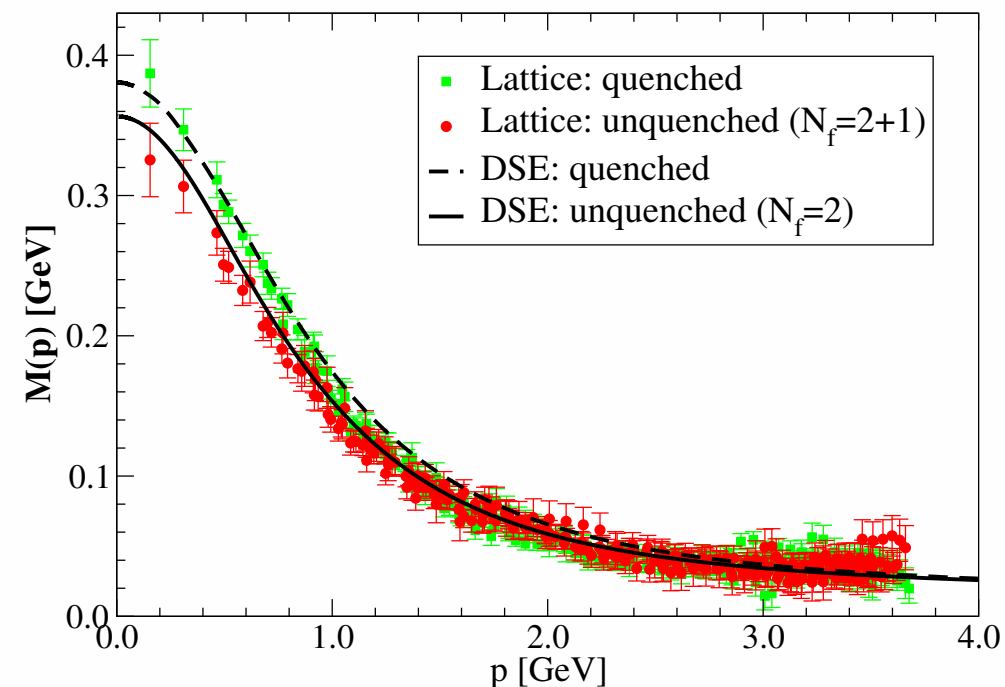
- $M(p^2)$: momentum dependent!
- Dynamical mass: $M_{\text{strong}} \approx 350 \text{ MeV}$
- Flavour dependence because of M_{weak}
- Chiral condensate: $\langle \bar{\Psi}\Psi \rangle \approx (250 \text{ MeV})^3$

Quark mass: flavor dependence

Typical solution:



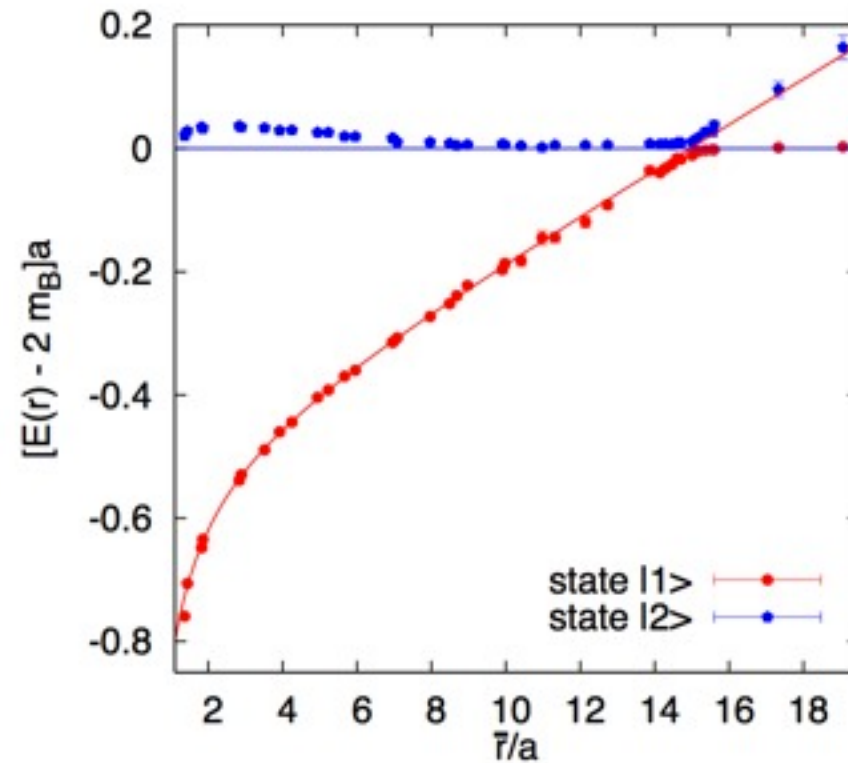
CF, JPG 32 (2006) R253



- $M(p^2)$: momentum dependent!
- Dynamical mass: $M_{\text{strong}} \approx 350 \text{ MeV}$
- Flavour dependence because of M_{weak}
- Chiral condensate: $\langle \bar{\Psi}\Psi \rangle \approx (250 \text{ MeV})^3$

Confinement

Color confinement:



Bali et al. [SESAM Collaboration], PRD 71 (2005) 114513

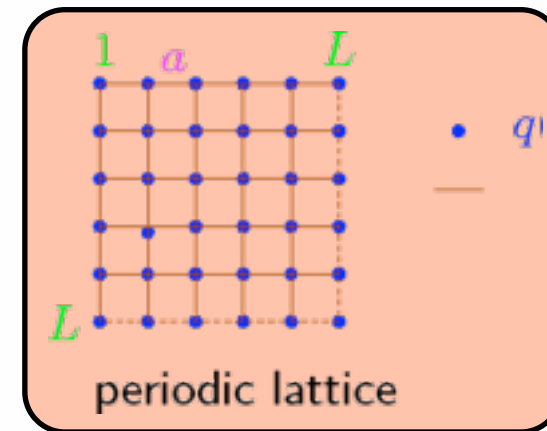


Strategies to deal with this situation:

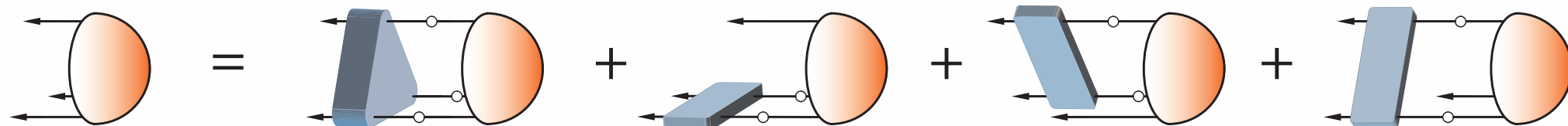
- Nonperturbative QCD: Lattice, Functional methods
- Effective theories with hadronic dof

1.Introduction

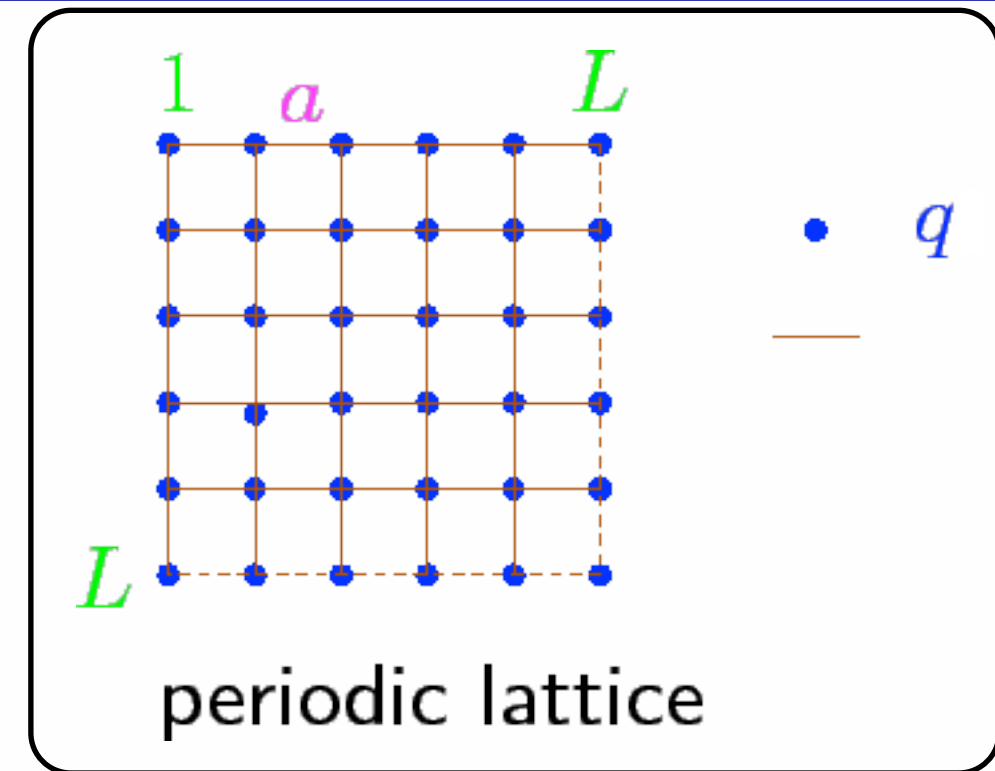
2.Results from Lattice-QCD



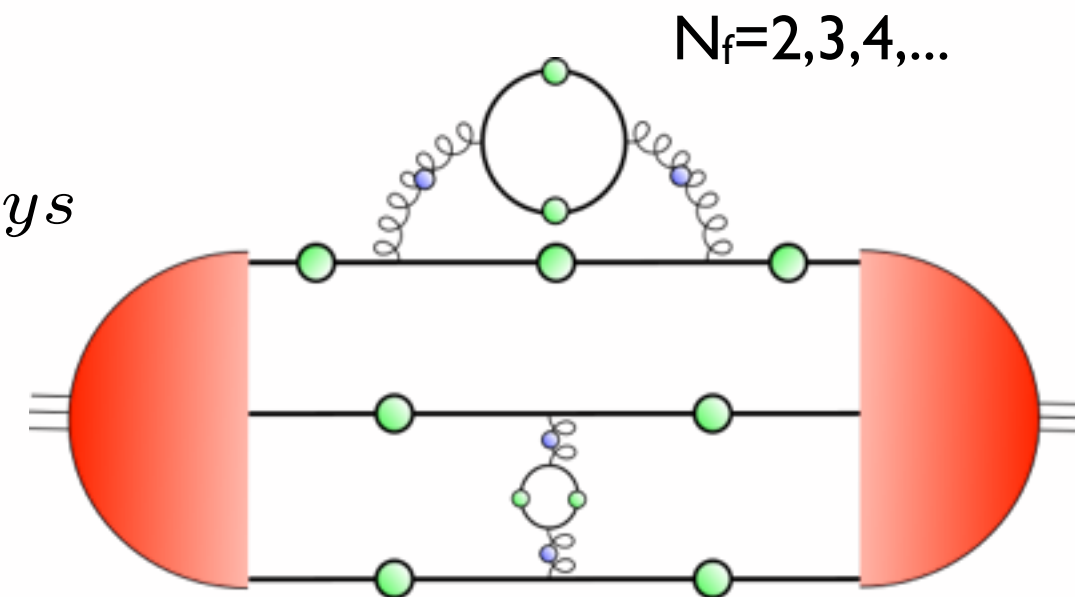
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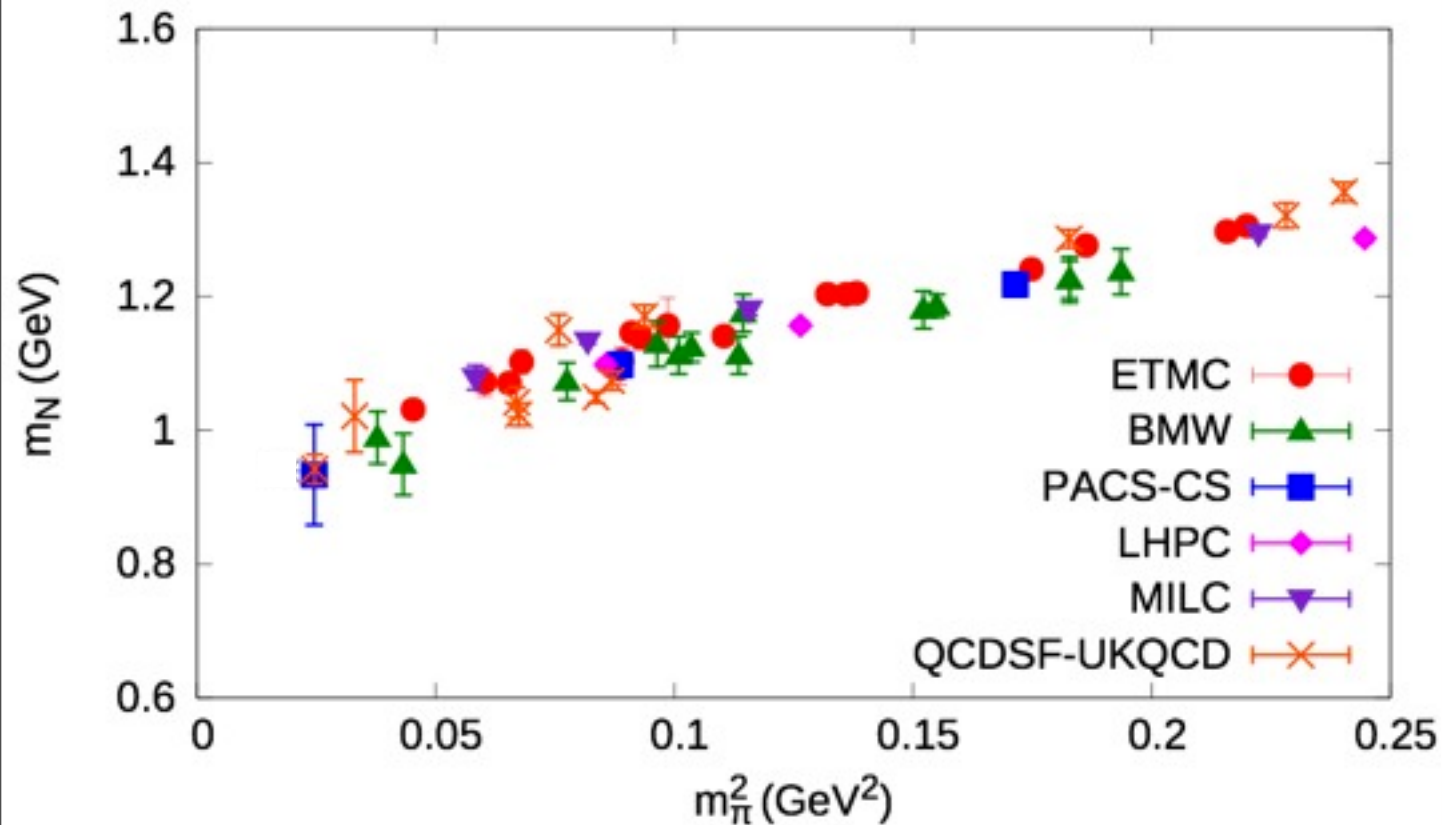
QCD on a space-time lattice



- Continuum extrapolation: $a \rightarrow 0$
- Volume extrapolation: $L \rightarrow \infty$
- Chiral extrapolation: $m_q \rightarrow m_q^{phys}$
- Valence vs. sea ('dynamical') quarks:
- # operators for a given channel
 - related to statistical error of results

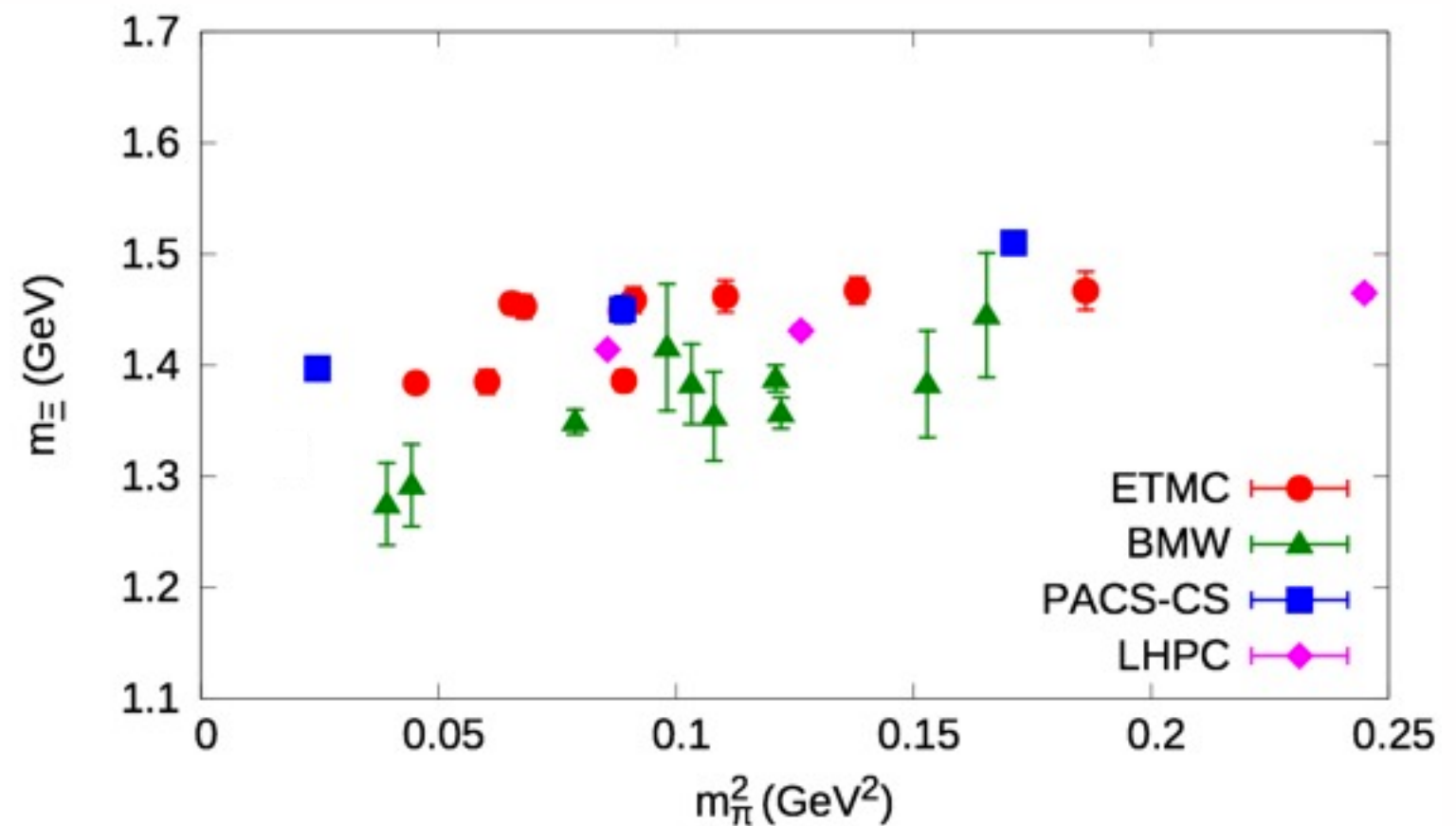


Extrapolation towards the physical point, $N_f=2+1+1$

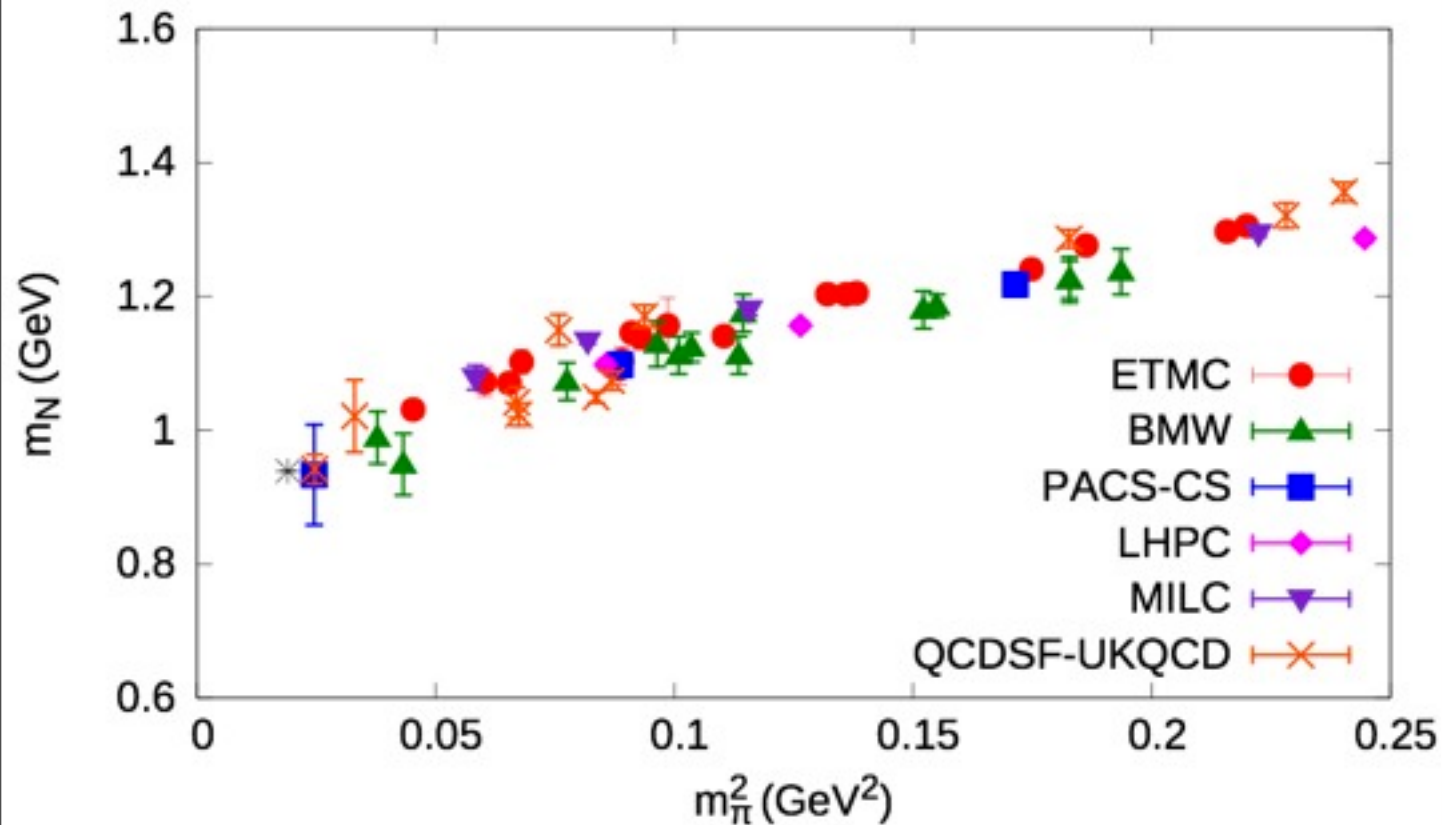


Alexandrou et al. (ETMC), PRD 90 (2014) 7

● m_N often used to set scale



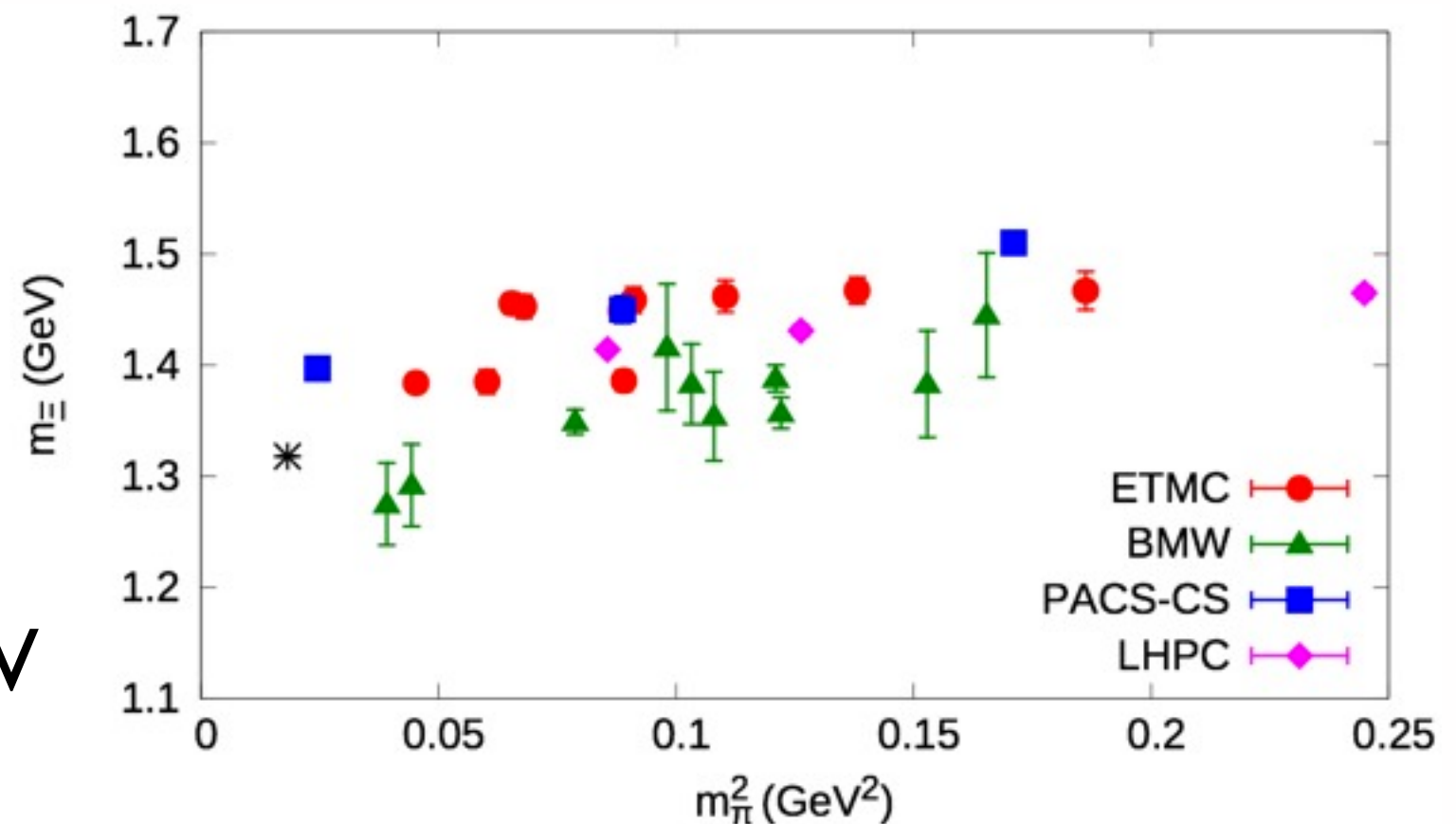
Extrapolation towards the physical point, $N_f=2+1+1$



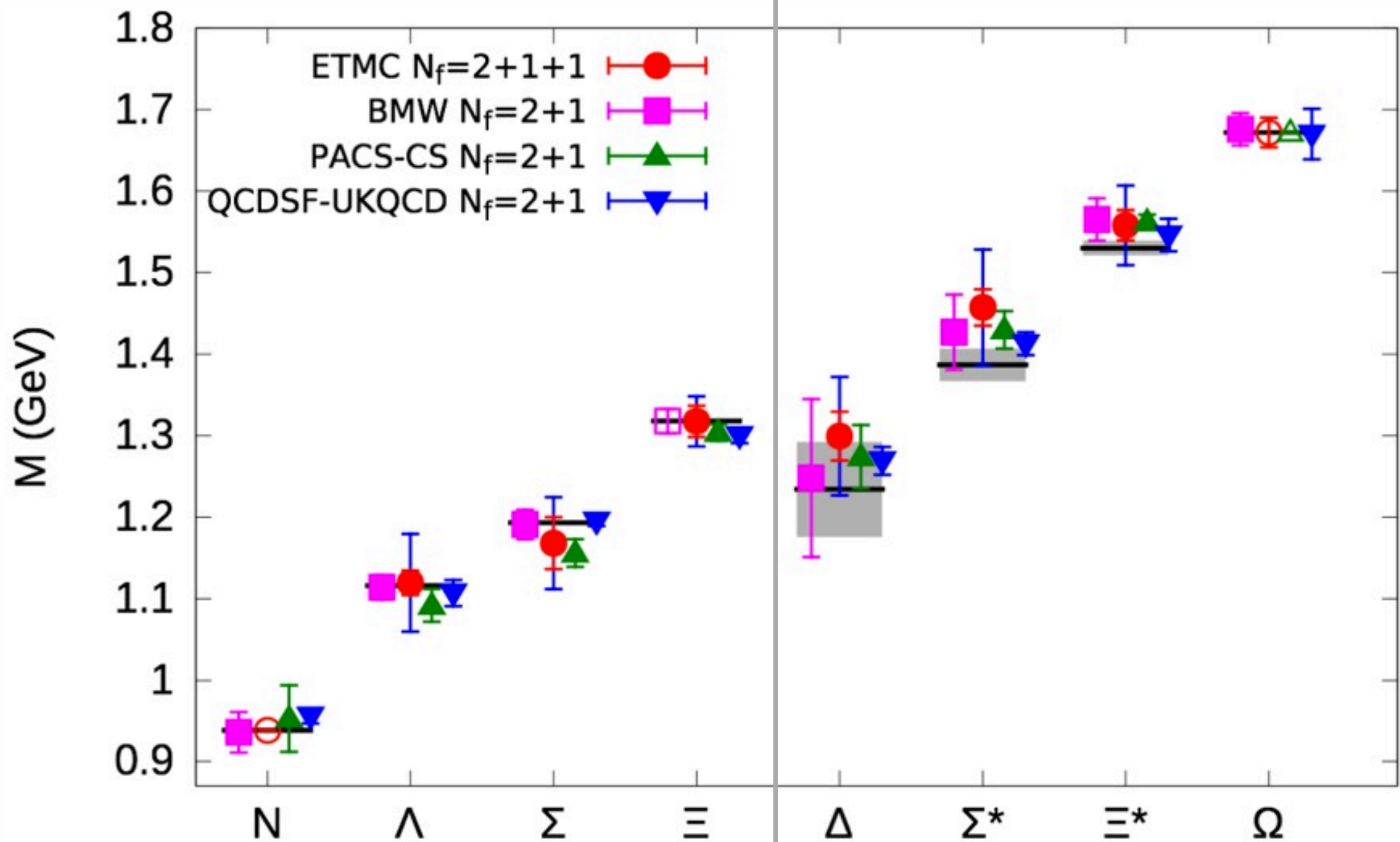
Alexandrou et al. (ETMC), PRD 90 (2014) 7

● m_N often used to set scale

● $m_\Xi = 1.318(19)(23)(9)$ GeV

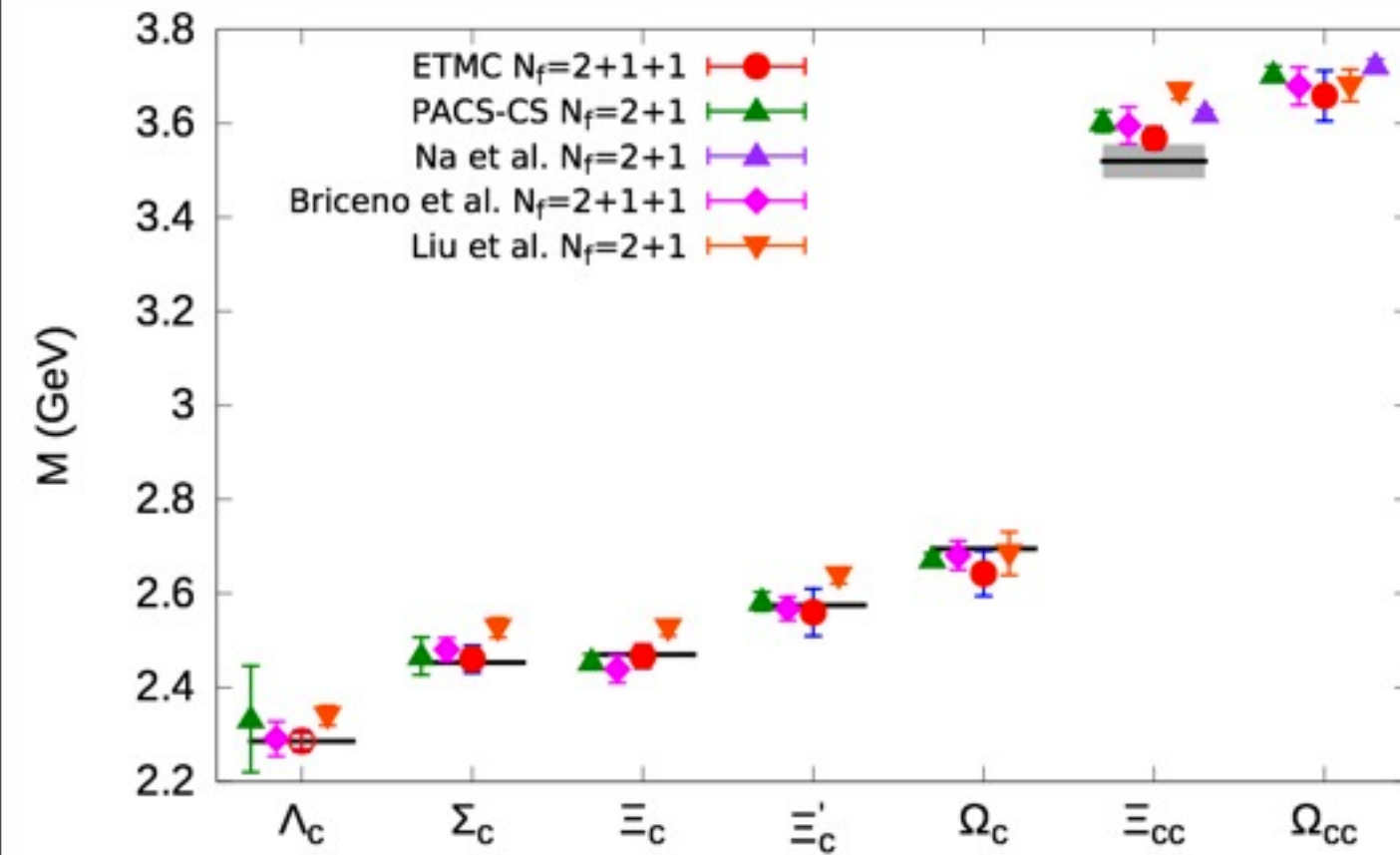


Ground states

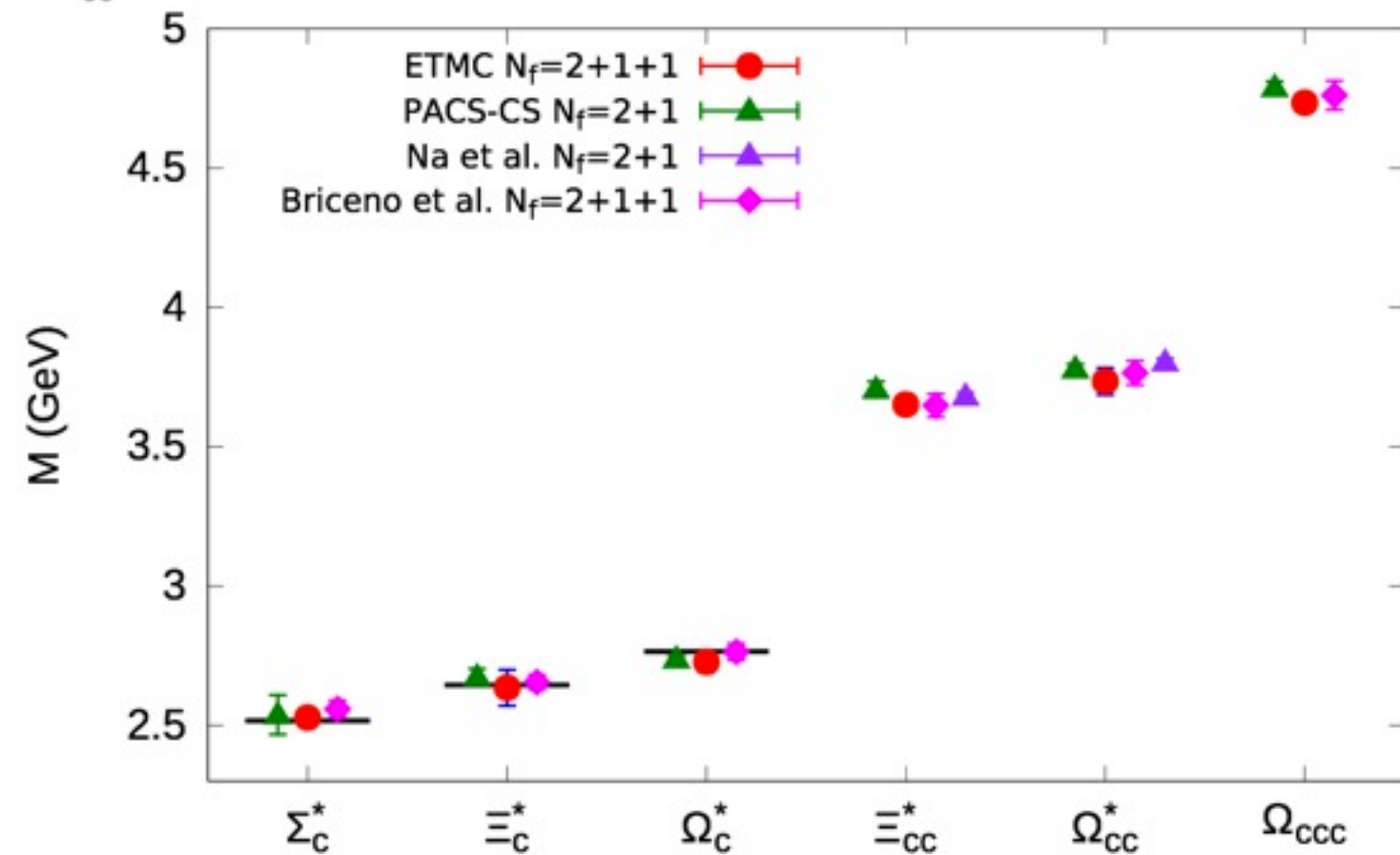


Alexandrou et al. (ETMC), PRD 90 (2014) 7

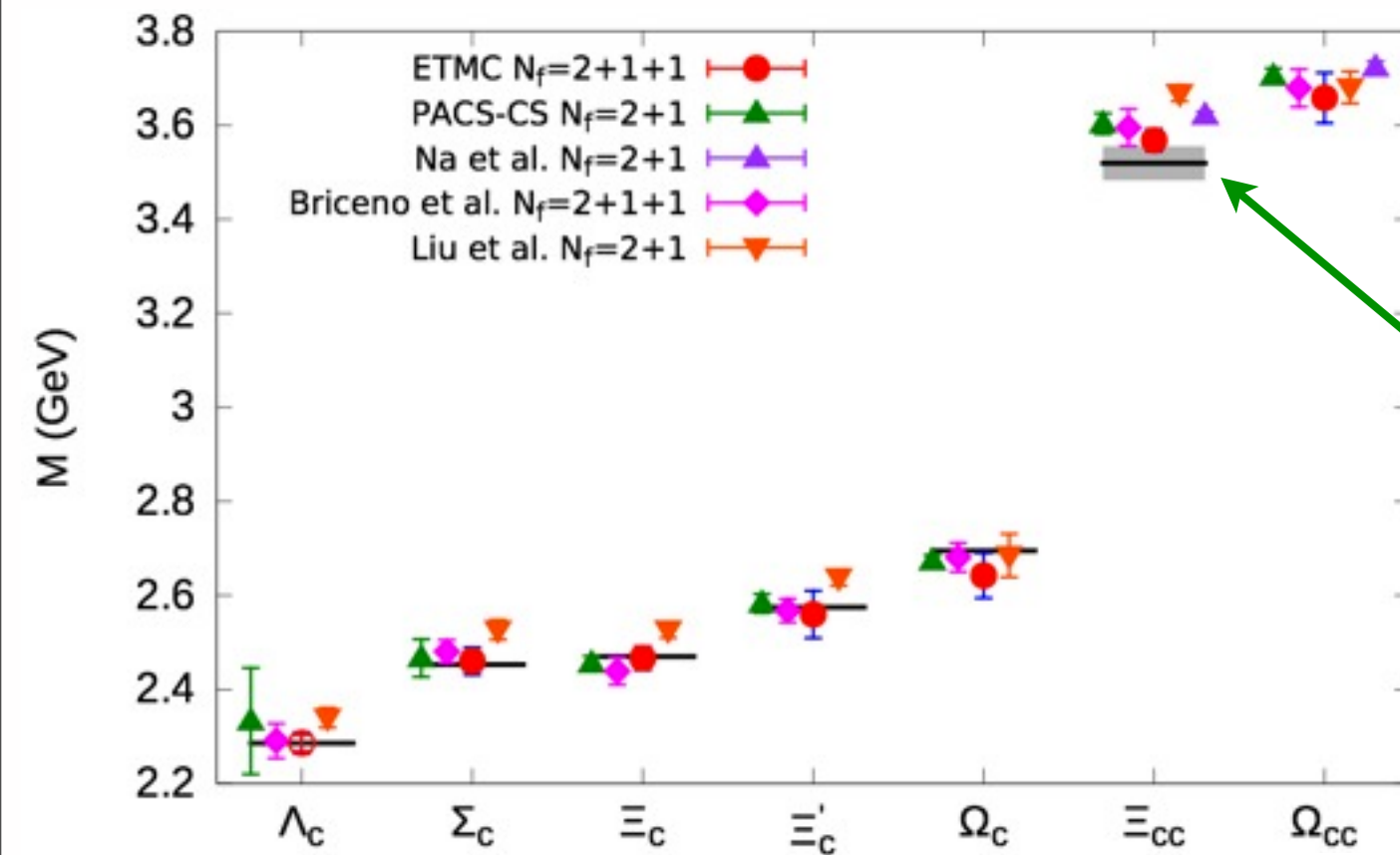
Ground states - charm sector



Alexandrou et al. (ETMC), PRD 90 (2014) 7

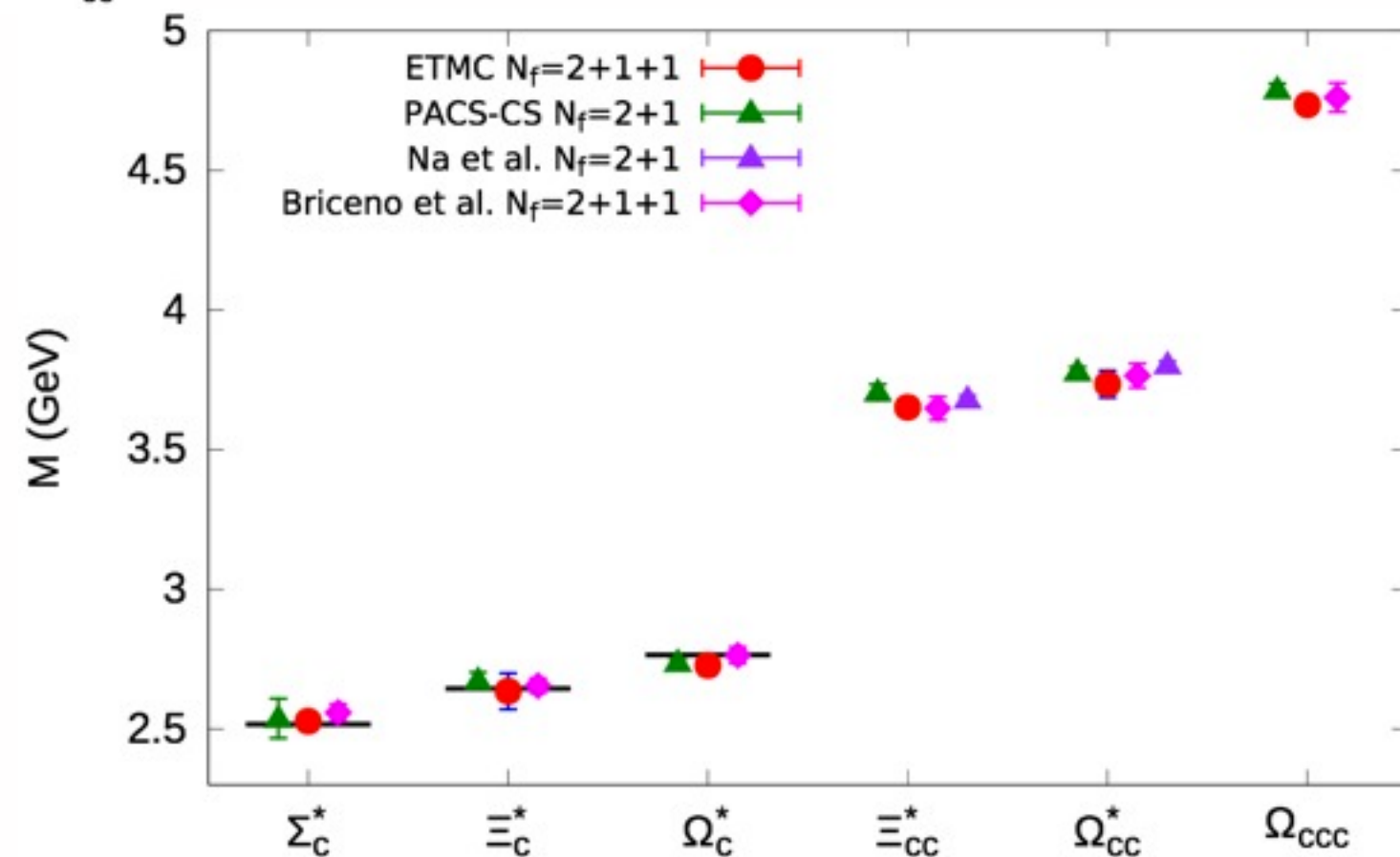


Ground states - charm sector

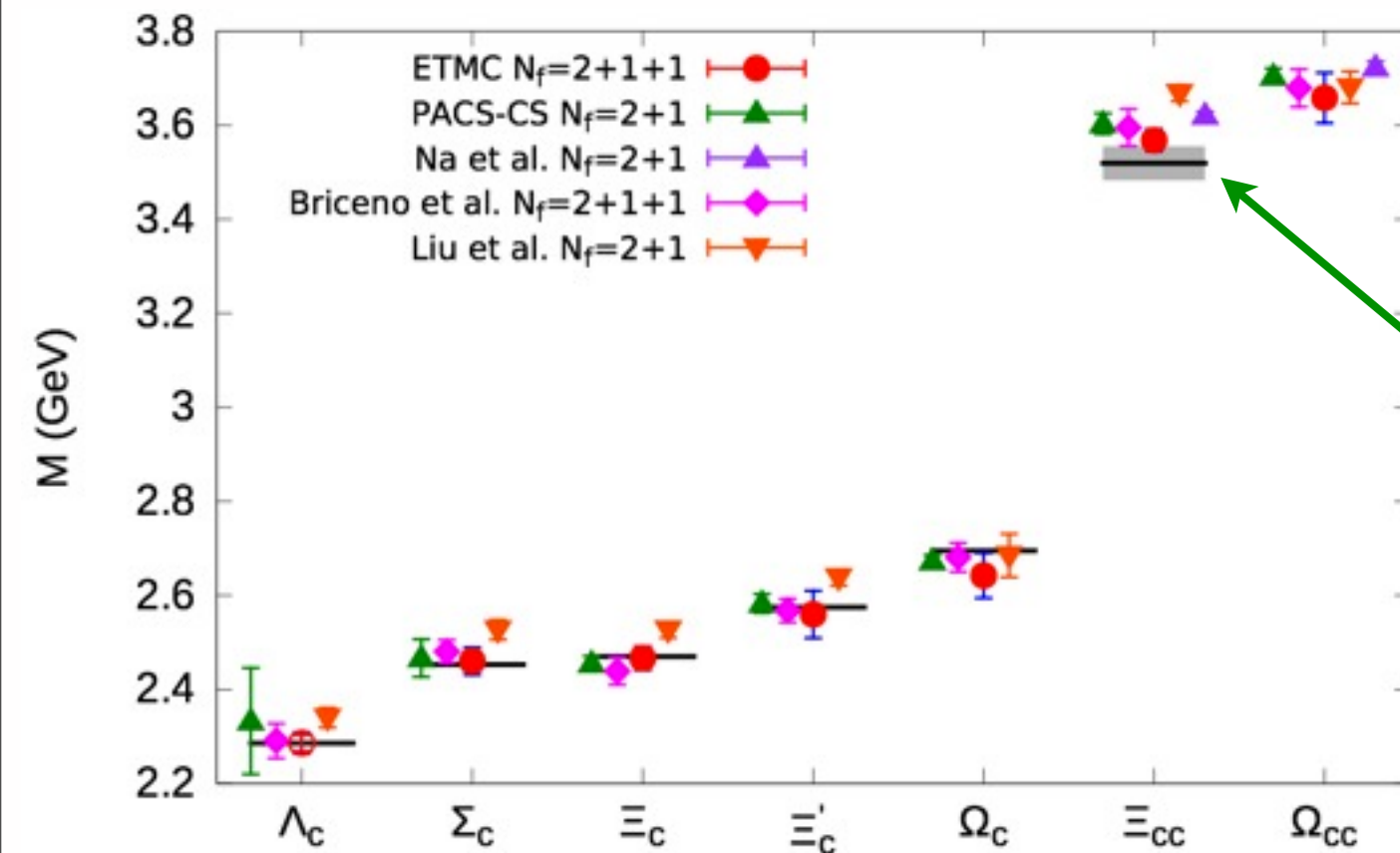


Ξ_{cc} measured by SELEX,
not found by others

Alexandrou et al. (ETMC), PRD 90 (2014) 7



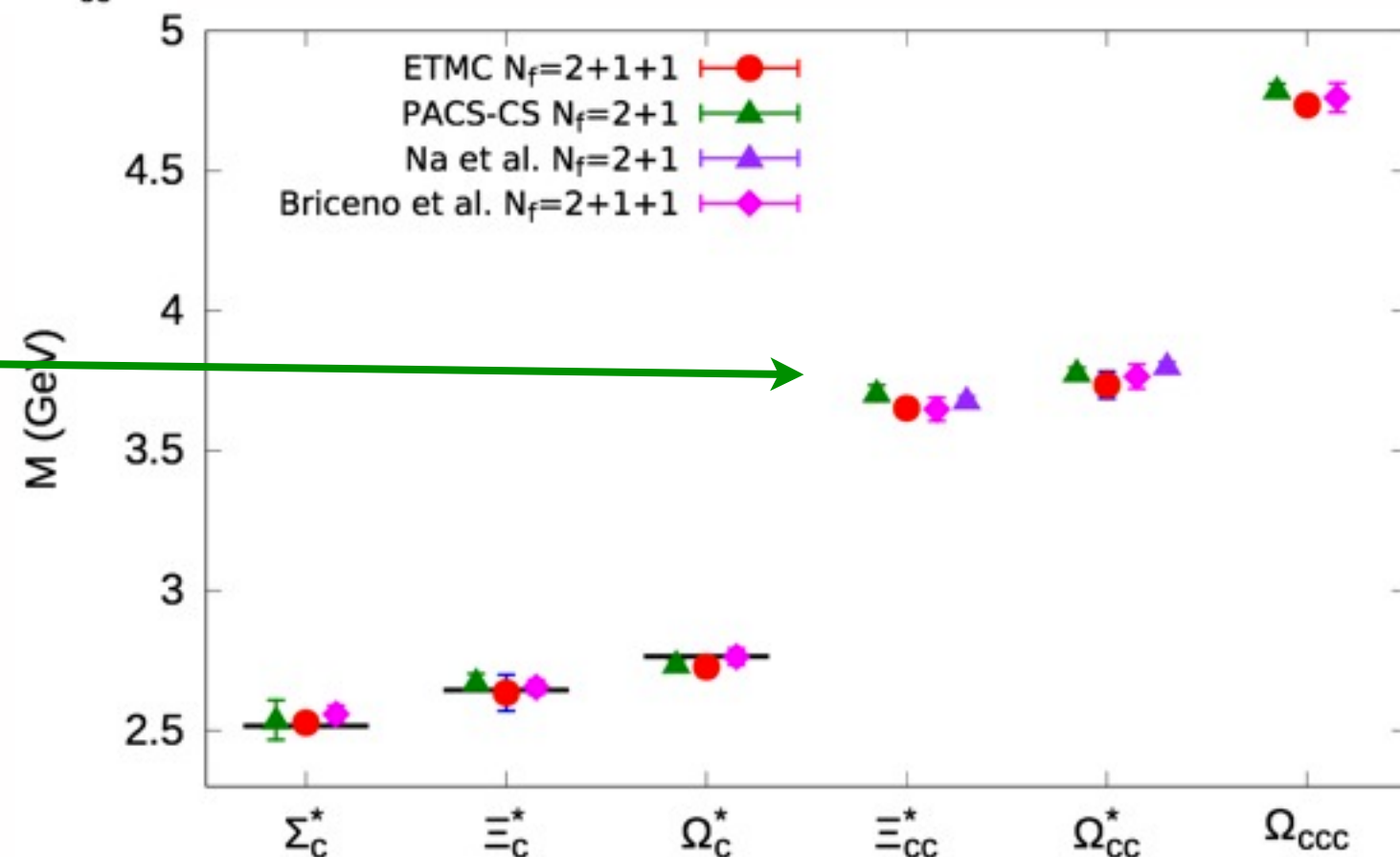
Ground states - charm sector



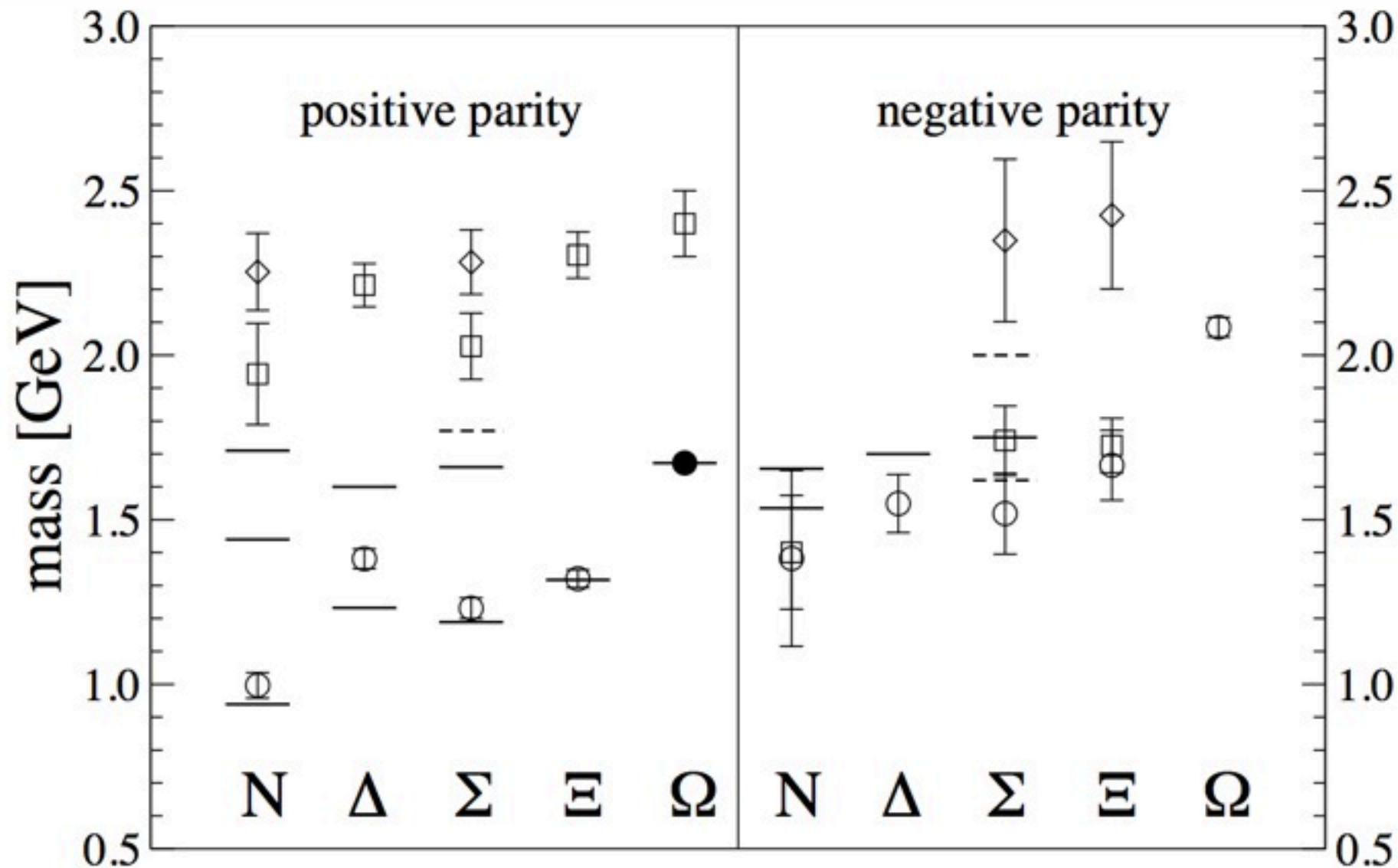
Ξ_{cc} measured by SELEX,
not found by others

Alexandrou et al. (ETMC), PRD 90 (2014) 7

Predictions !



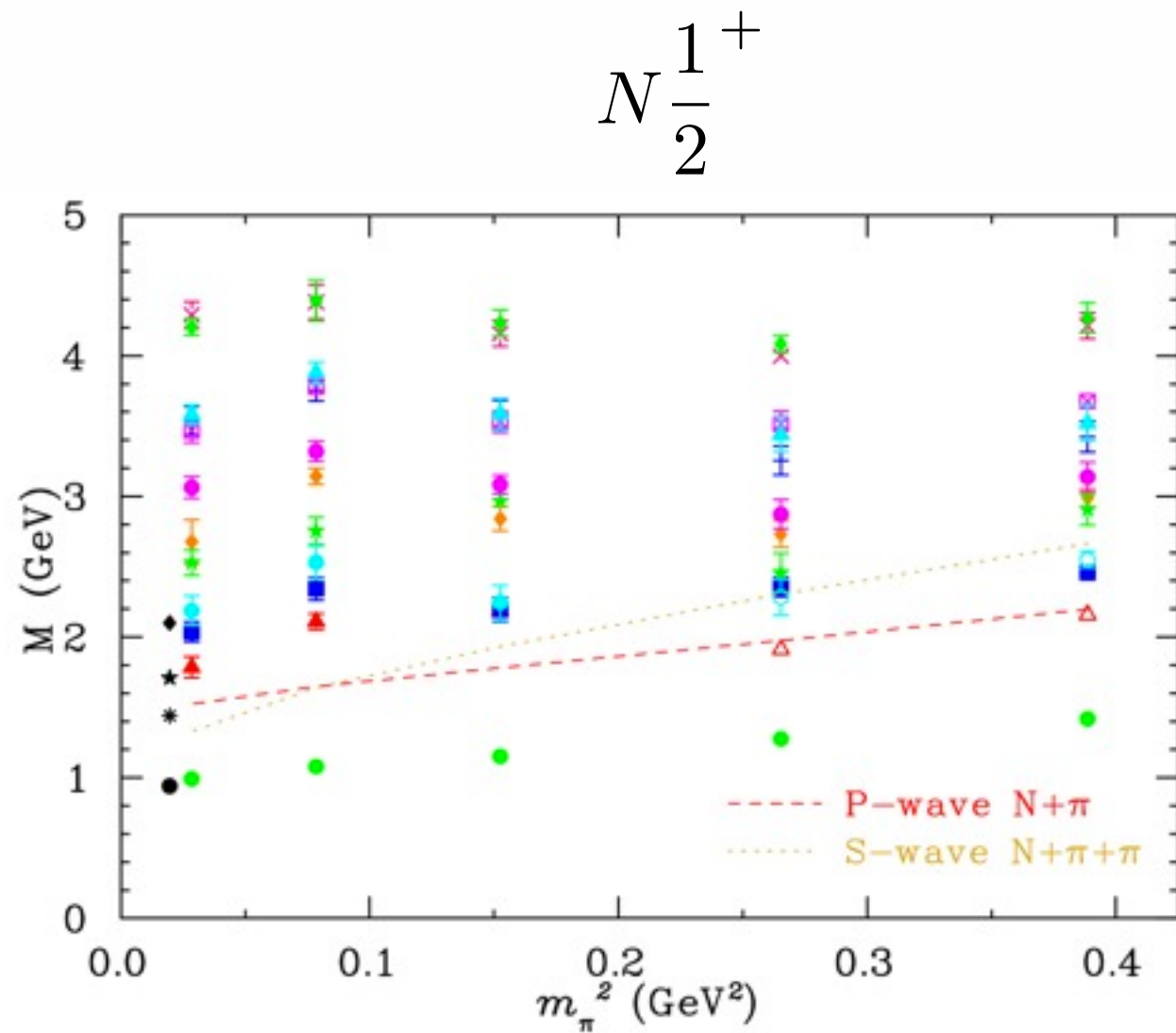
Excited states, $N_f=2$



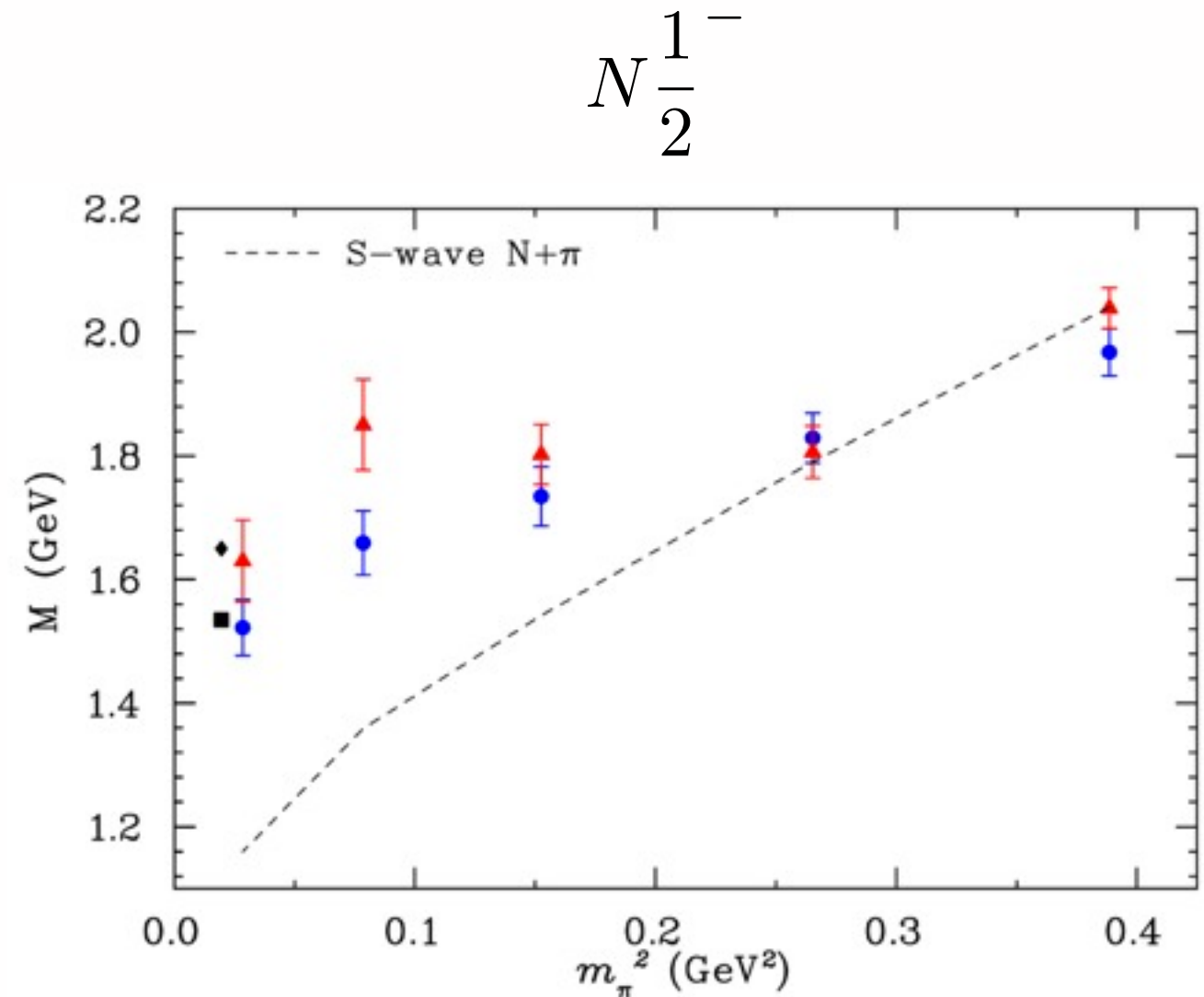
Engel et al. (BGR), PRD82 (2010) 034505

- Diquark-Quark-pattern ruled out
- No sign of parity doubling
- Large pion mass, $m_\pi=322$ MeV, extrapolated:
 - Positive parity: excited states systematically too large
 - Negative parity: ground states systematically too low

Positive/negative parity octet states



Mahbub et al. (CSSM), PLB707 (2012) 389

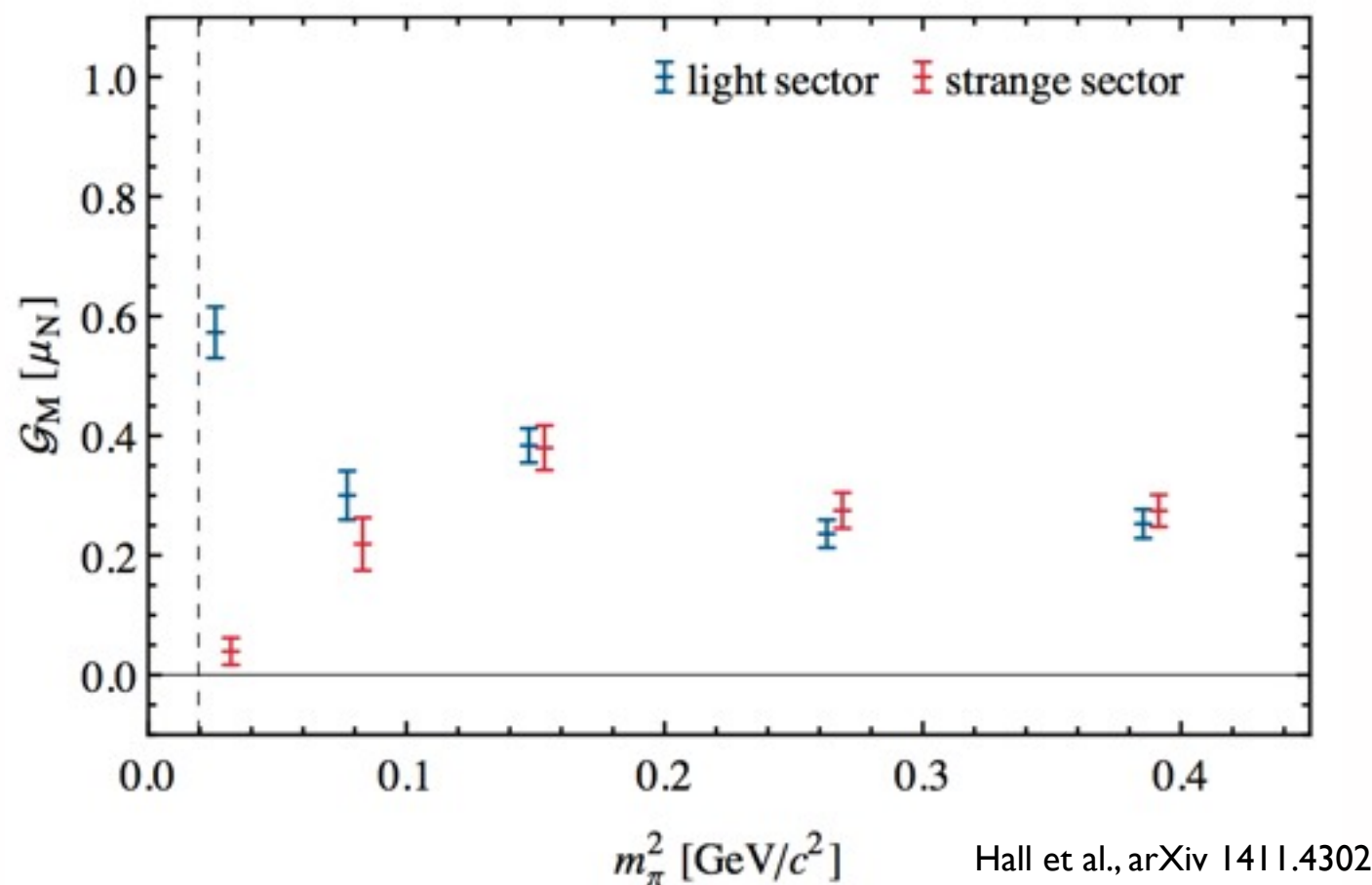
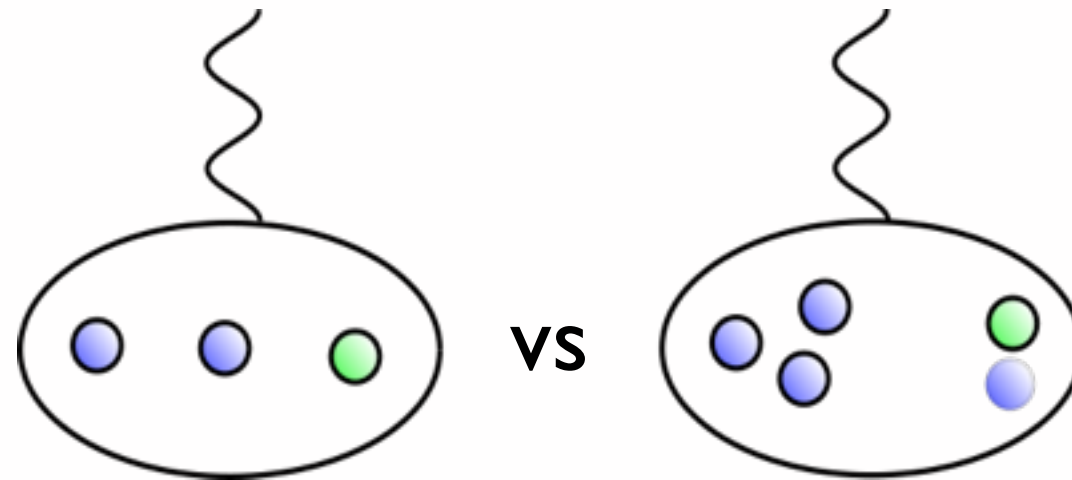


Mahbub et al. (CSSM), PRD87 (2013) 1

- $m_{\pi}=156 \text{ MeV}$
- considerable 'chiral curvature'
- small operator basis...

The $\Lambda(1405)$ as a $\bar{K}N$ -molecule

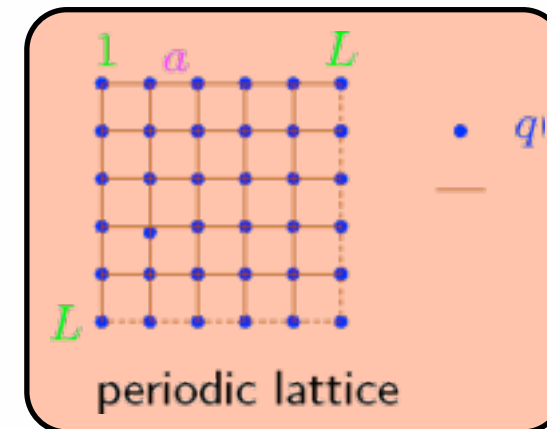
- Basic idea: calculate flavour contributions to magnetic form factors



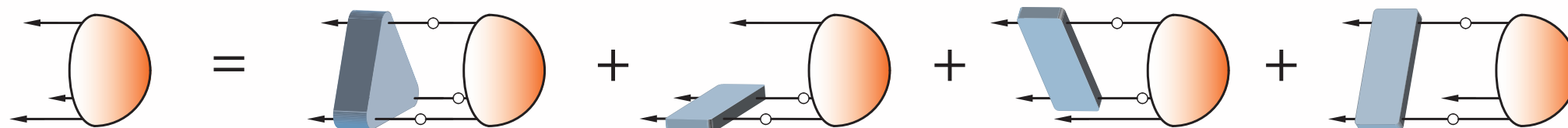
- looks like $\bar{K}N$ -molecule !
- caveat: operator basis

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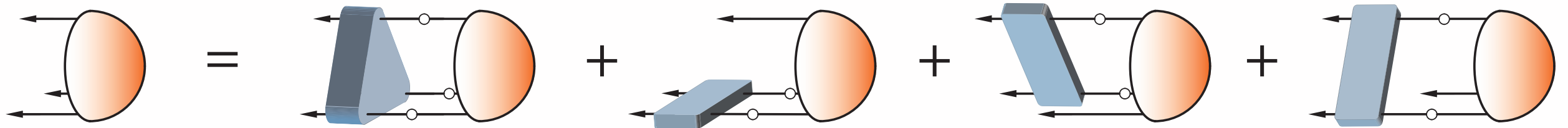
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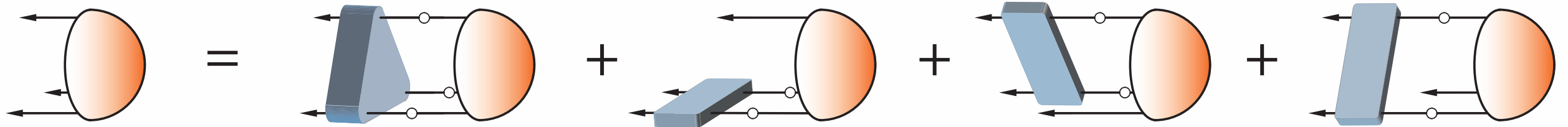


Faddeev - equation



- two and three-body forces:
 - dominance of two-body forces: quark-diquark picture
 - three-body forces relevant ? most likely yes...
- relativistic bound state:
 - 64 tensor structures for nucleon: s, p, d - wave
 - 128 tensor structures for Delta: s, p, d, f - wave

Faddeev - equation



- irreducible three-body forces
- two-body interactions:
 - non-perturbative **one-gluon exchange**
 - **meson exchange**
 - two-body forces **beyond one-particle exchange**
- numerically expensive but manageable !

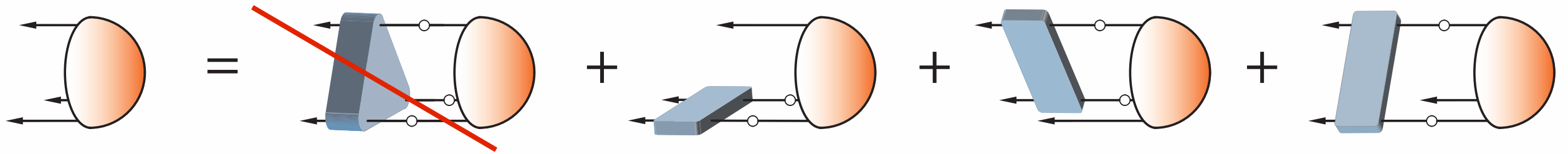
Sanchis-Alepuz, Williams, work in progress...

Eichmann, Alkofer, Krassnigg, Nicmorus, PRL 104 (2010)

Sanchis-Alepuz, CF, Kubrak, PLB 733 (2014)

CF, Sanchis-Alepuz, Williams, work in progress...

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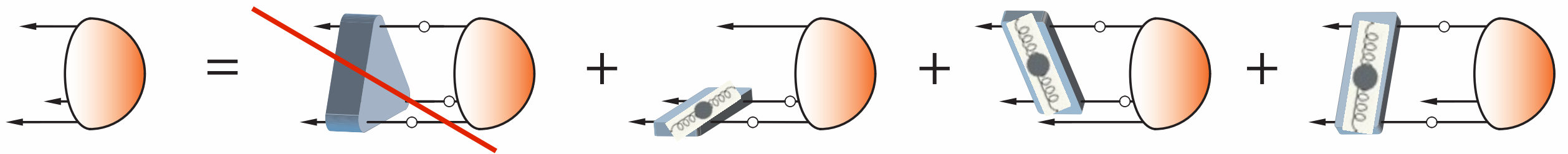
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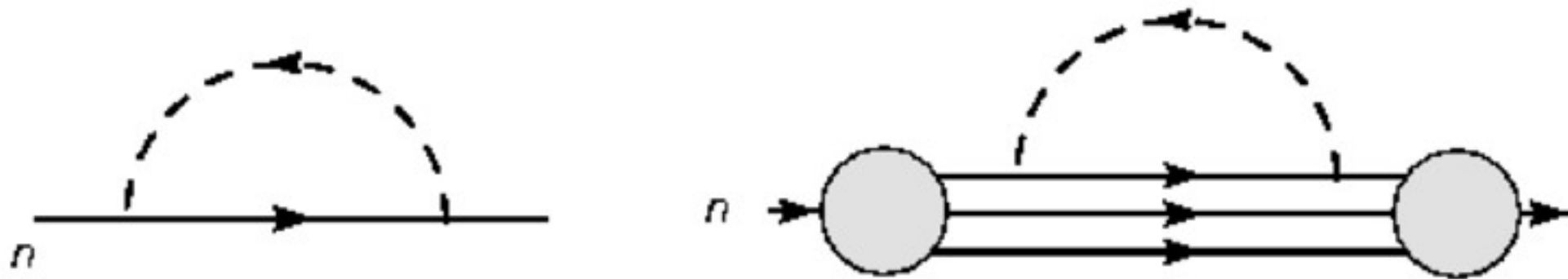
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Eichmann, Alkofer, Krassnigg, Nicmorus, PRL 104 (2010)

Sanchis-Alepuz, CF, Kubrak, PLB 733 (2014)

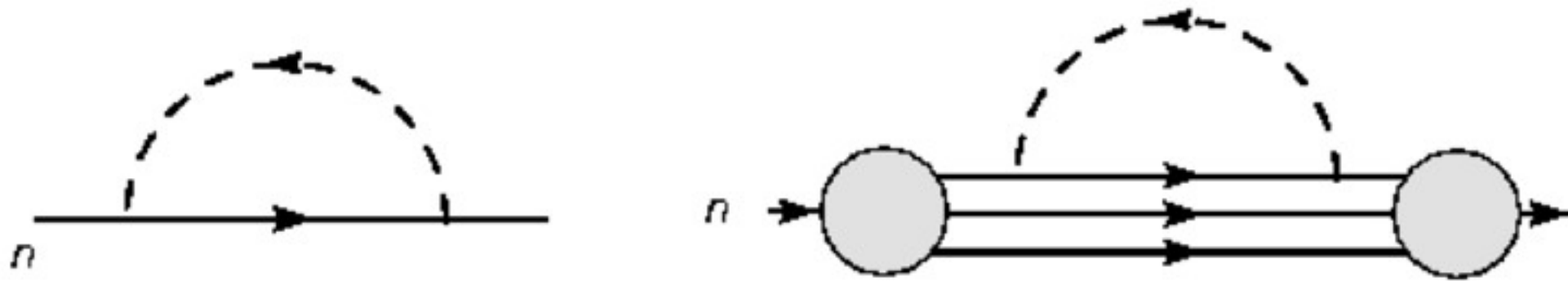
CF, Sanchis-Alepuz, Williams, work in progress...

Pion cloud effects

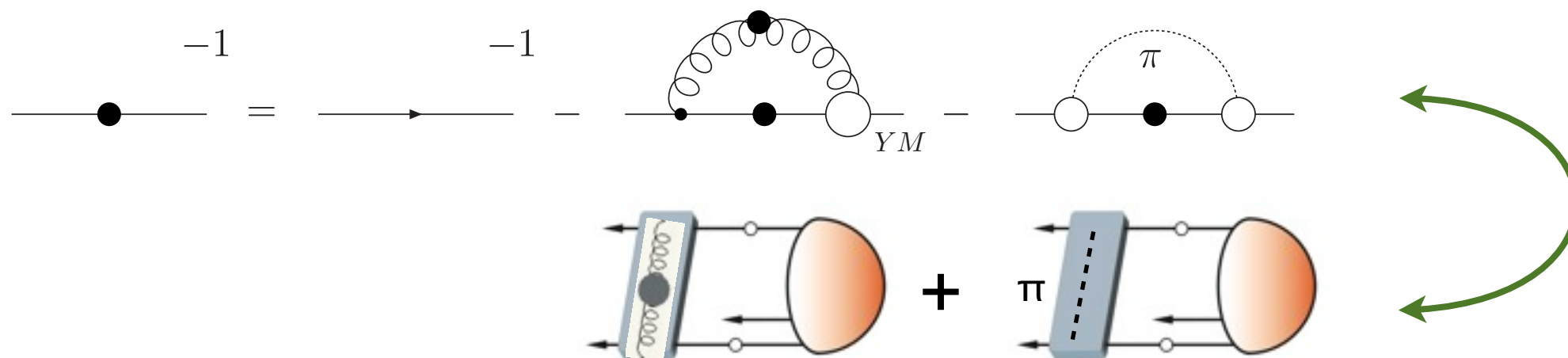


- Hadron level: π N-contributions to nucleon self-energy
- Quark-level: π -contributions to quark self-energy and interactions

Pion cloud effects



- Hadron level: πN -contributions to nucleon self-energy
- Quark-level: π -contributions to quark self-energy and interactions



Pion not an elementary field!

Derived from DSE for quark-gluon interaction!

CF, Nickel and Wambach, PRD 76 (2007) 094009

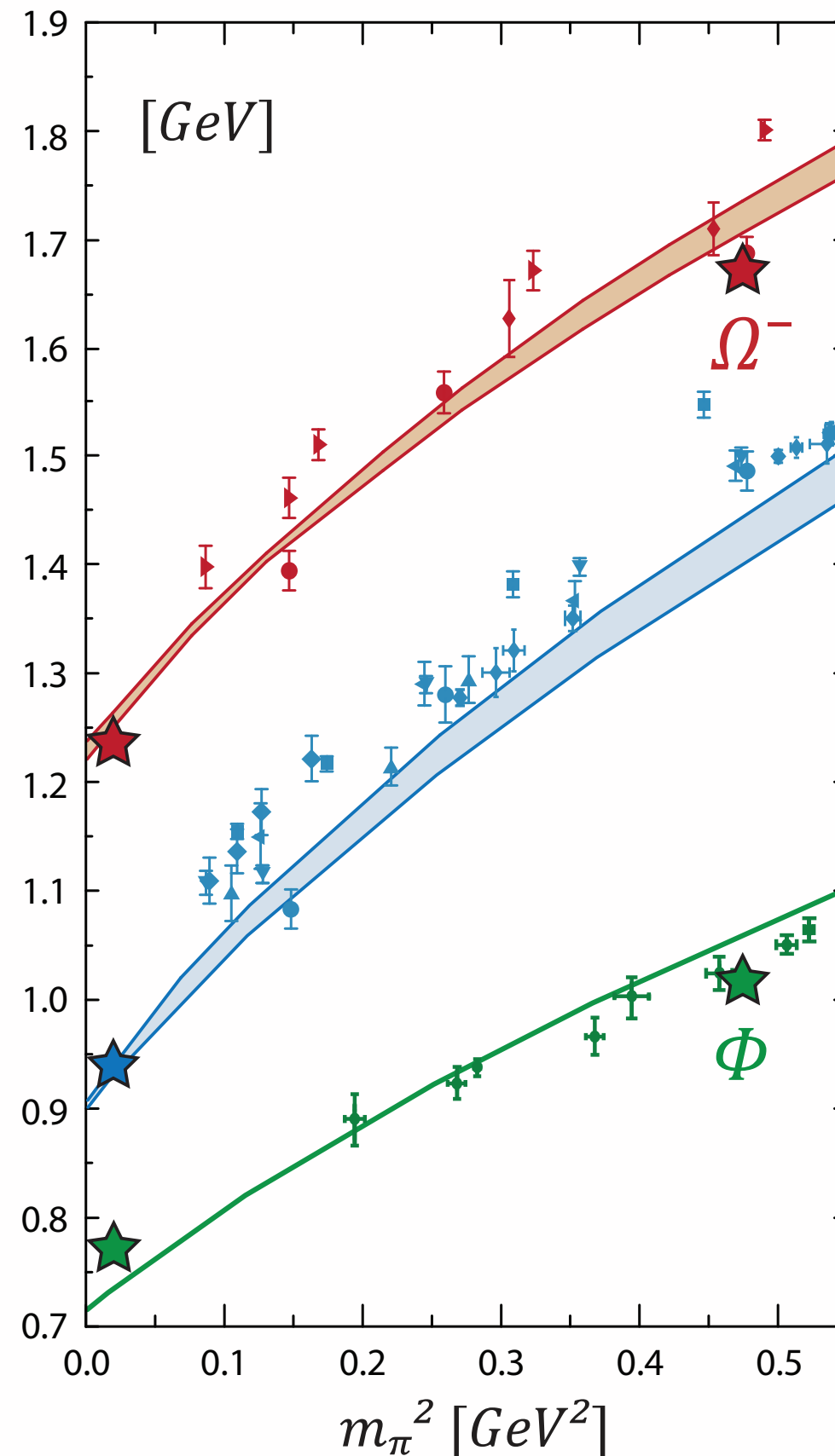
Baryon masses - gluon exchange only

- first covariant three-body calculations !
- grosso modo: consistent description of mesons and baryons
- wave functions contain sizable p-wave contributions

Eichmann, Alkofer, Krassnigg, Nicmorus, PRL 104 (2010)

Eichmann, PRD 84 (2011)

Sanchis-Alepuz, Eichmann, Villalba-Chavez, Alkofer, PRD (2012)



Delta:

Sanchis-Alepuz et al.,
PRD 84 (2011)

Nucleon:

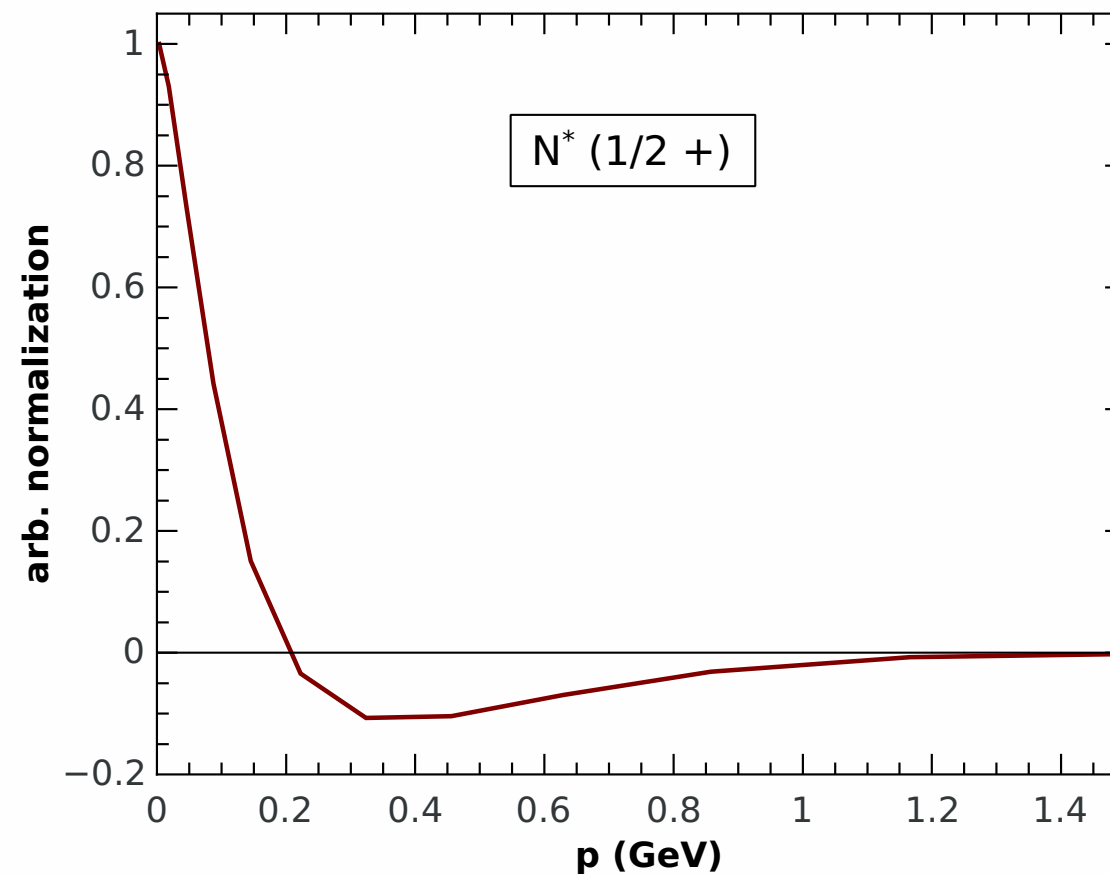
Eichmann et al.,
PRL 104 (2010),
PRD 84 (2011)

ρ -meson:

Maris & Tandy,
PRC 60 (1999)

Baryon resonances - gluon exchange only

Roper: $M_{N^*} = 1.26 - 1.41 \text{ GeV}$



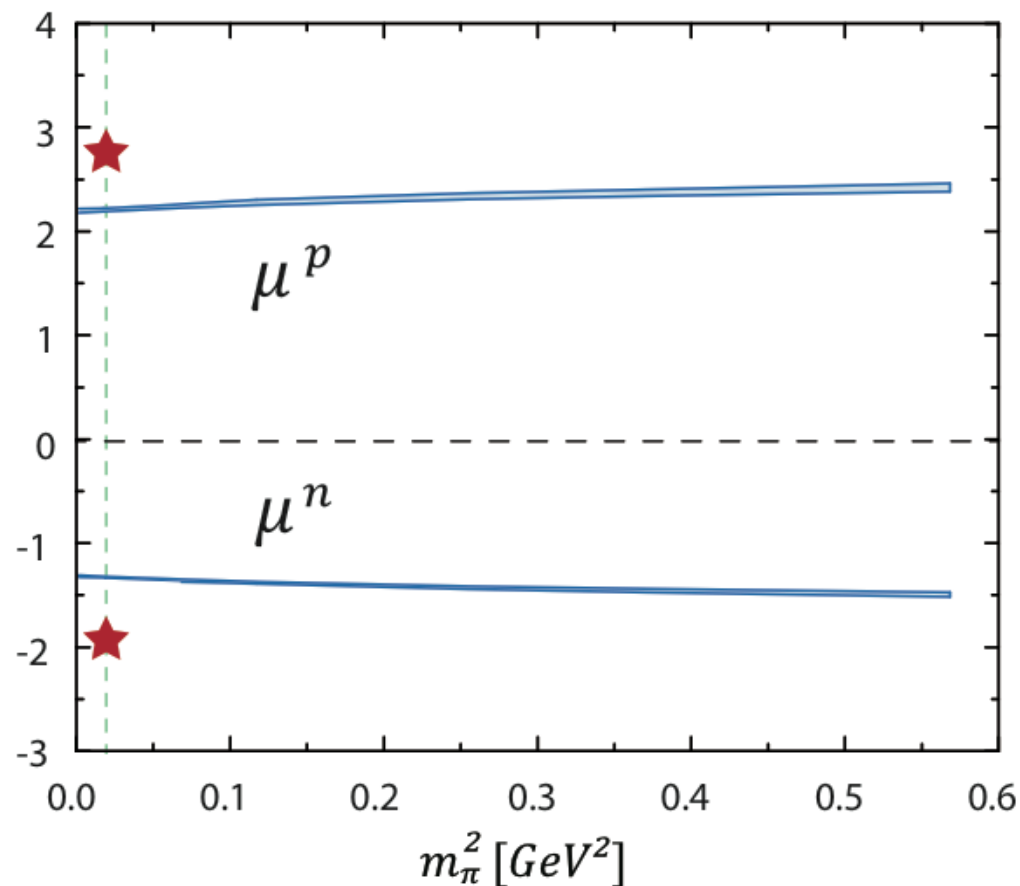
Sanchis-Alepuz, CF, in preparation

Preliminary: almost pure s-wave

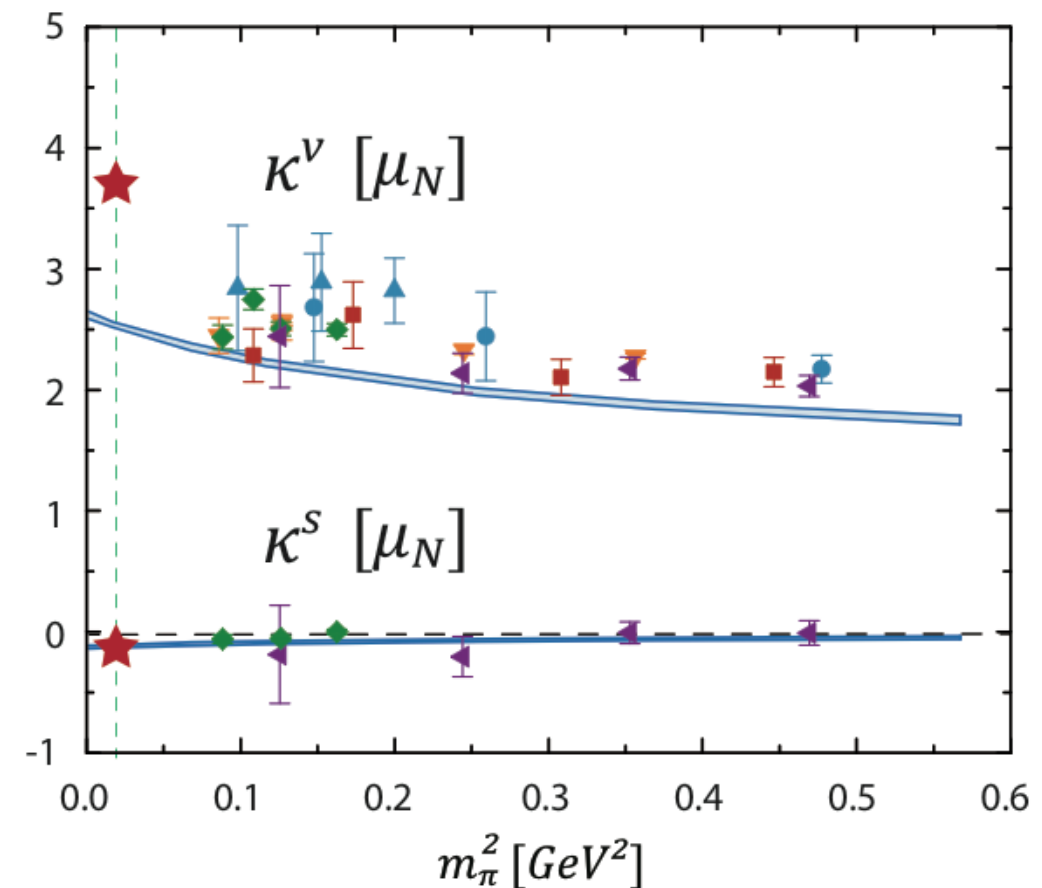
- $N_{\frac{1}{2}}^{\pm}$ same level ordering as in quark model

Magnetic moments - gluon exchange only

Magnetic moments (p, n):



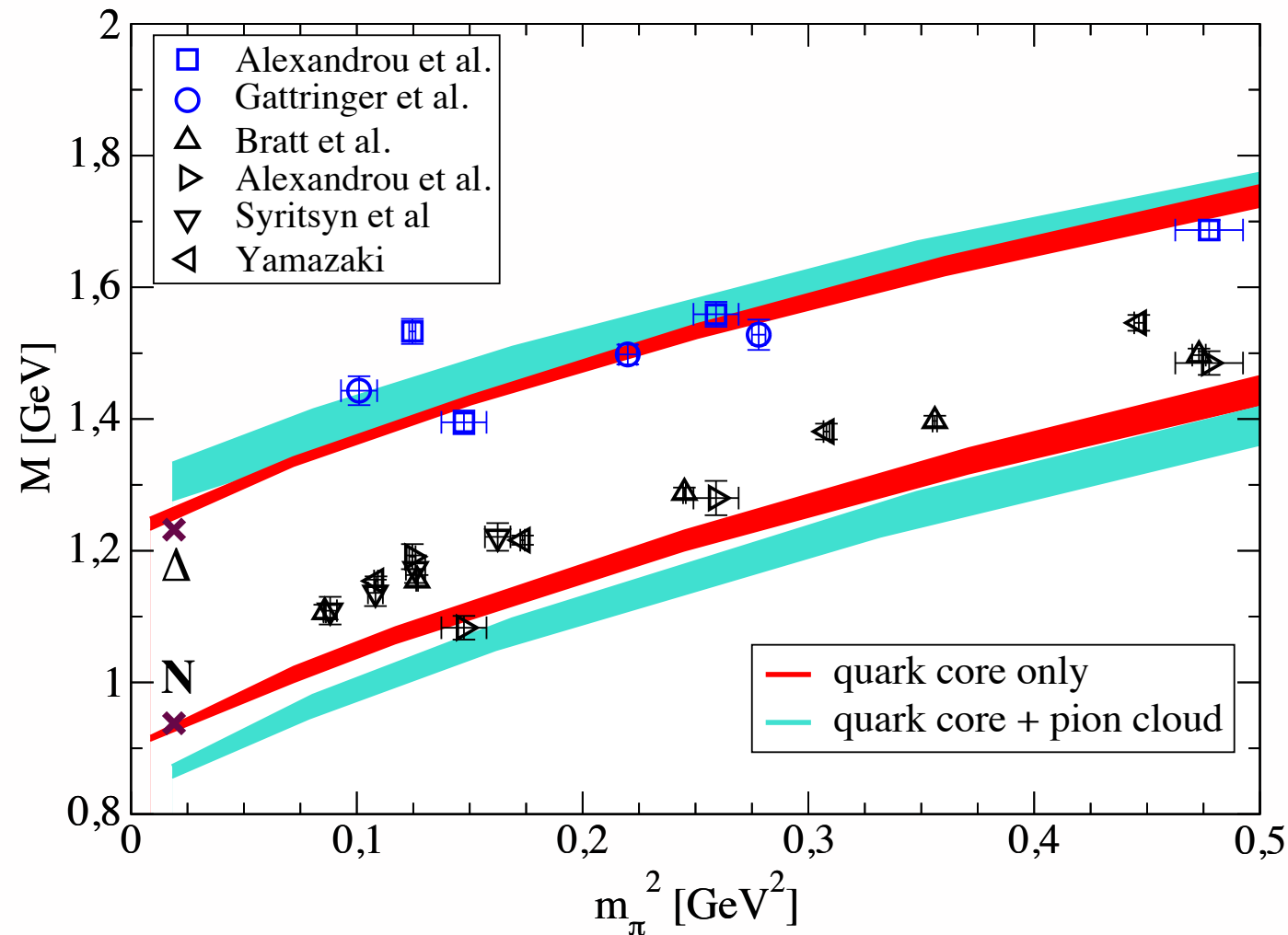
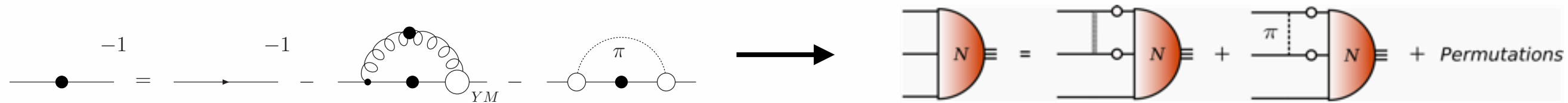
Isovector (p-n), isoscalar (p+n):



- missing **pion cloud** effects in isovector moment κ^v
- no **pion cloud** effects in isoscalar moment κ^s

Eichmann, PRD 84 (2011)

Baryon masses- including pion cloud



Sanchis-Alepuz, CF, Kubrak, PLB 733 (2014) [1401.3183]

- fix Λ by f_π , vary η s.t. f_π still ok
- effects of the order of 50-100 MeV
- missing: gluon self-interaction effects

$$\alpha(k^2) = \pi \eta^7 \left(\frac{k^2}{\Lambda^2} \right) e^{-\eta^2 \left(\frac{k^2}{\Lambda^2} \right)} + \alpha_{UV}(k^2)$$

Pion cloud effects in baryons: structure

	Nucleon			Delta			
	s-wave	p-wave	d-wave	s-wave	p-wave	d-wave	f-wave
quark core	75	24	1	61	31	7	0,2
quark core plus pion cloud	75	24	1	60	31	8	0,2

$$\sigma_{\pi N} = 30(3) \text{ MeV} \quad (\text{quark core only})$$

$$\sigma_{\pi N} = 31(3) \text{ MeV} \quad (\text{quark core} + \text{pion cloud})$$

Sanchis-Alepuz, CF, Kubrak, PLB 733 (2014) [1401.3183]

- pion cloud does not change shape of nucleon: **uniform skin**
- sigma-term probably too small...

Lots of interesting physics still to be explored !!

Agenda for DSE/BSE/Faddeev framework:

- Electromagnetic form factors with pion cloud
- Three-body forces
- Compton scattering

Other activities of our group related to PANDA:

- Light and heavy mesons
- Tetraquarks
- *Glueballs: to be published, arXiv:xxxxx*