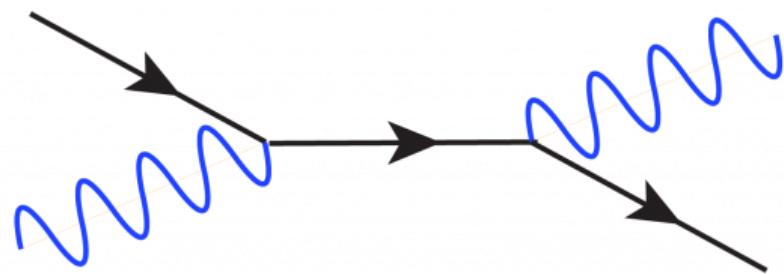


In-beam γ -ray spectroscopy using RIB

Selected Recent Results



EURORIB-15

Radioactive beams from in-flight and ISOL facilities

- γ -ray detectors coupled to charged particle detectors
- Coulomb Excitation and Transfer reaction as experimental method
- Excitation energy, spectroscopic factor, $B(E\lambda)$ and electromagnetic moment

In the last 7 years :

23 papers from safe coulex with RIB

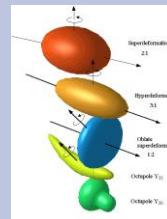
1 Nature

9 Phys. Rev. Lett.

12 Phys. Rev. C

1 Phys. Lett. B.

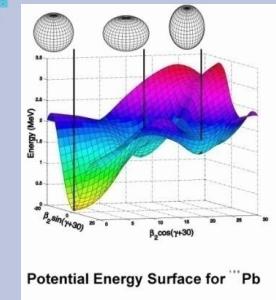
^{17}C N=20 collapse
 ^{43}S , ^{46}Ar N=28 collapse
Shape coexistence in Sr/Rb



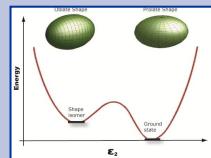
^{220}Rn and ^{224}Ra

Shape coexistence and exotic shapes

^{208}Pb



B(E2) in Sn, In and Cd



^{100}Sn

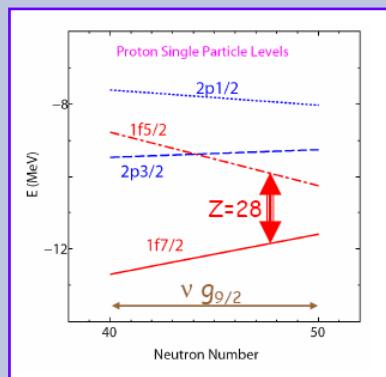
^{132}Sn

68-78Ni

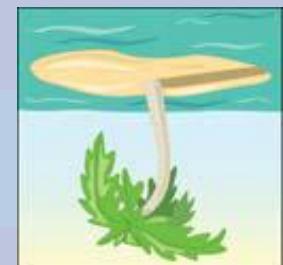
40-48Ca

Toward N=50 :

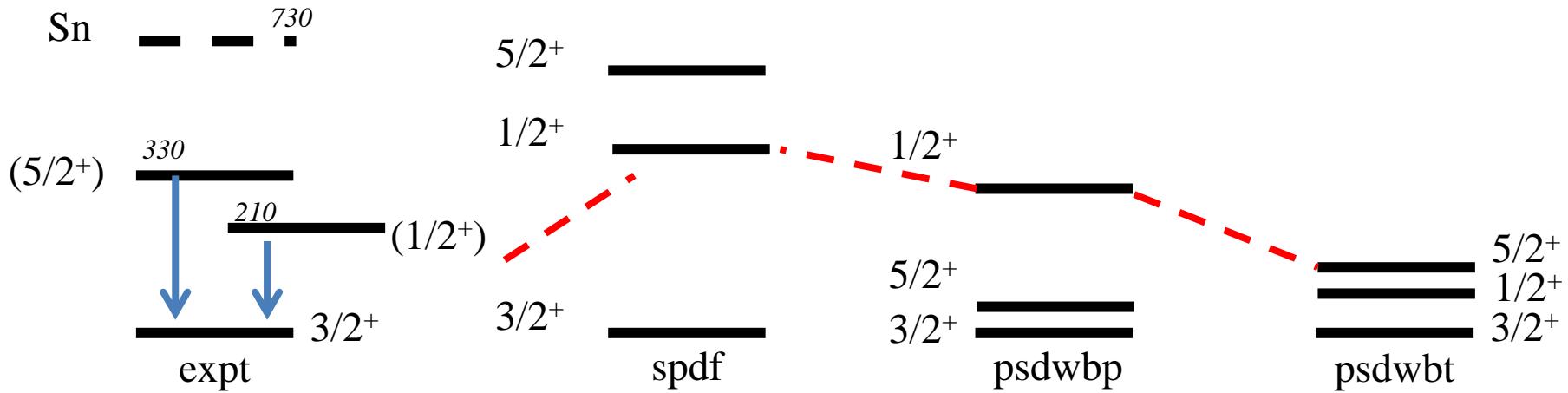
- Zn spectroscopy
- pf_{5/2} migration,
- sp and collectives states in Cu



- N=20 and N=28 shell erosion; island of inversion
- Enhancement of N=16



Spectroscopic information from transfer reaction and Coulex at SPIRAL1 and Rex-Isolde
Extend the knowledge to the n-rich $C \rightarrow ^{17}C$ spectroscopy

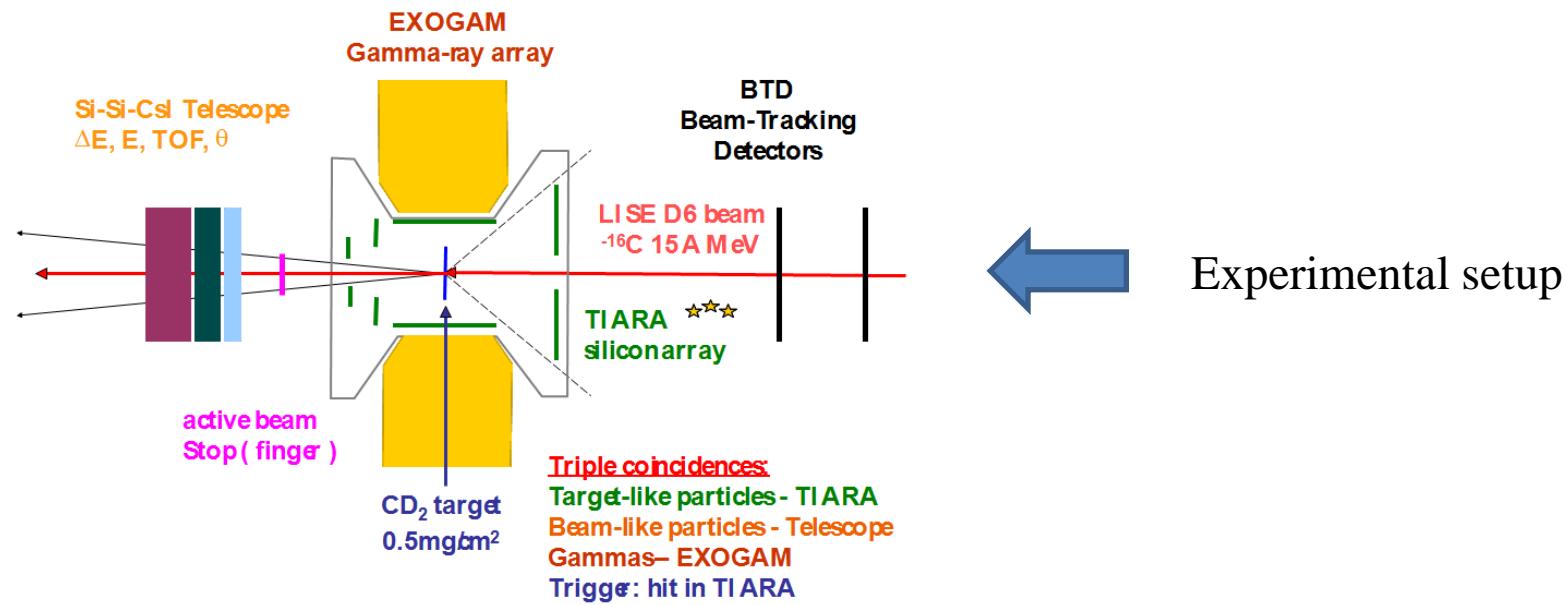
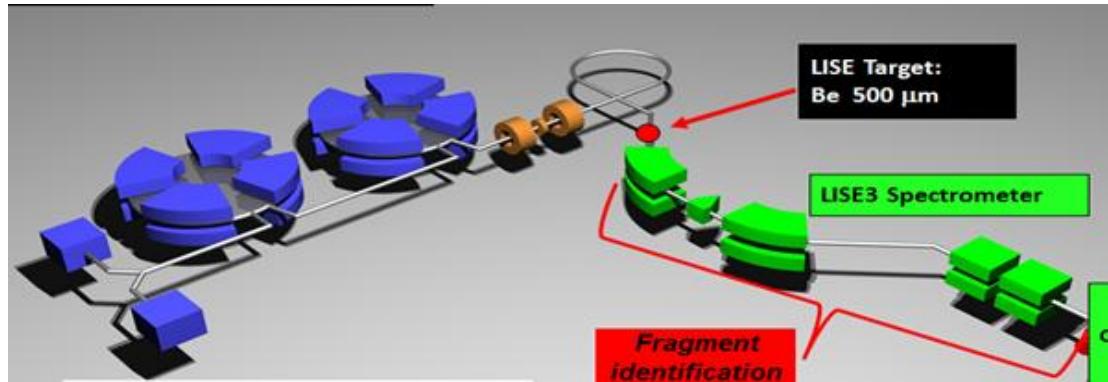


Objectives :

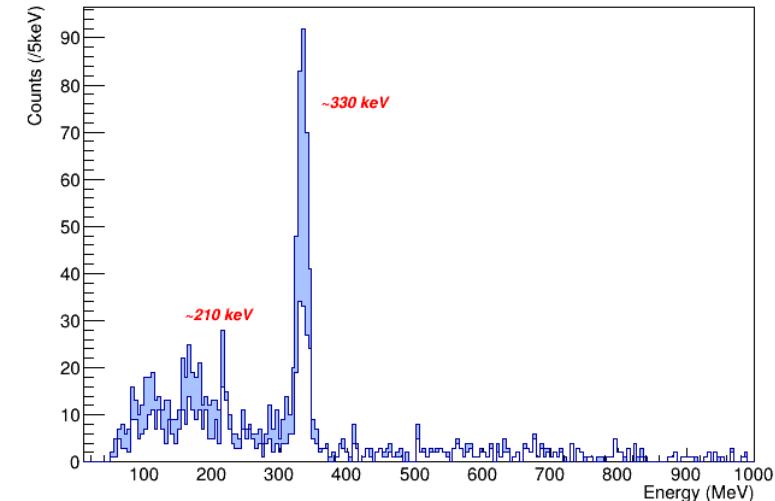
- ❖ Spin assignment of the 3 bound states
- ❖ Spectroscopic factor of the GS to constraint its micropscopical configuration
- ❖ Locate the $3/2^+$ unbound state $\rightarrow 0d_{3/2}$ as constraint for SM calculations

^{18}O beam at 65MeV/A

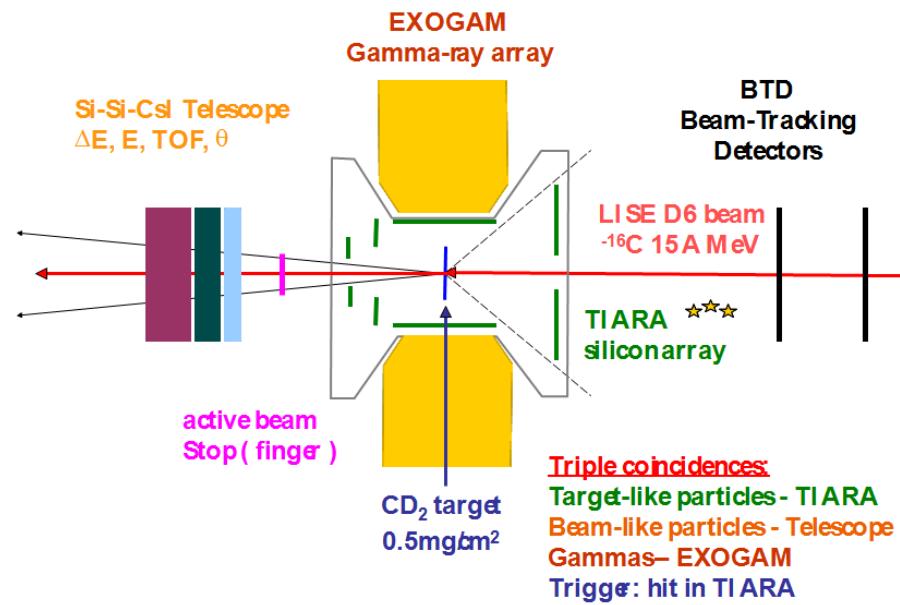
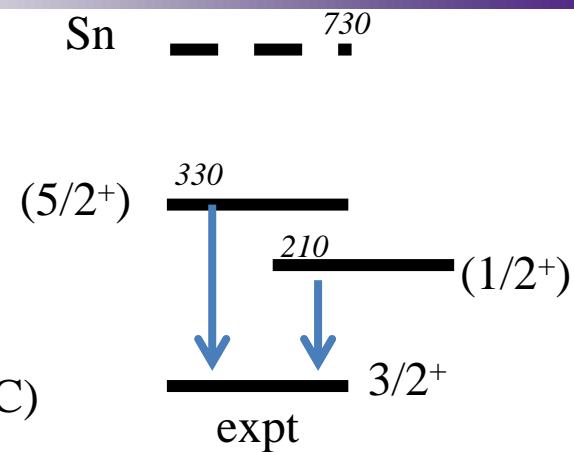
^{16}C secondary beam at 15MeV/A $\sim 4.10^4$ pps



γ spectrum

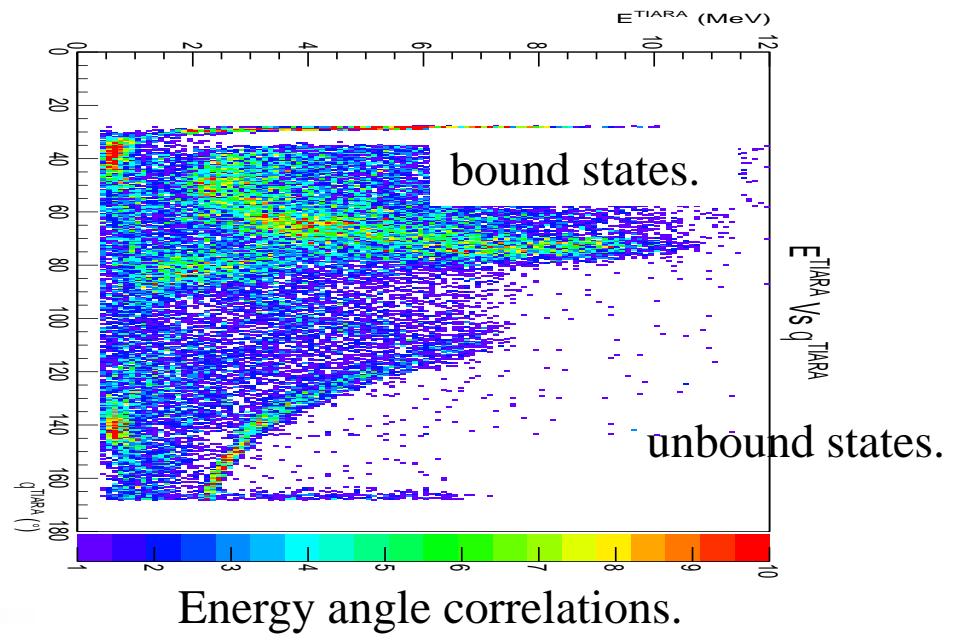
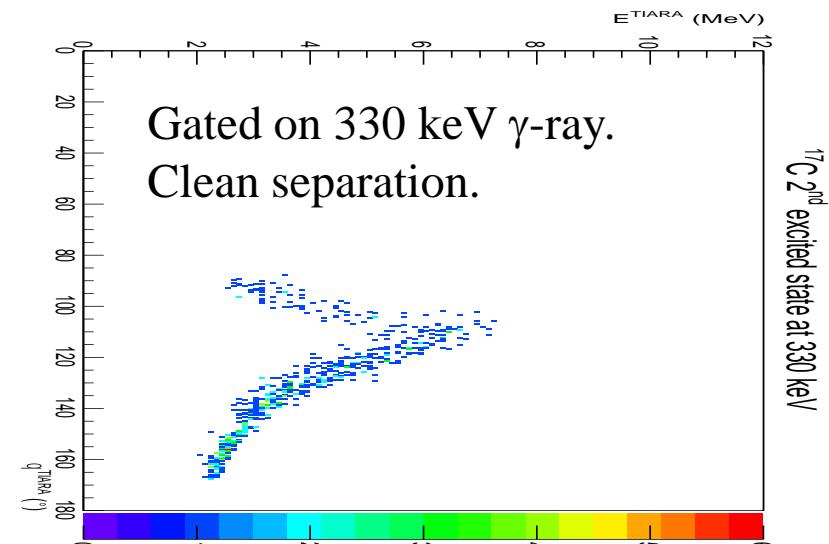
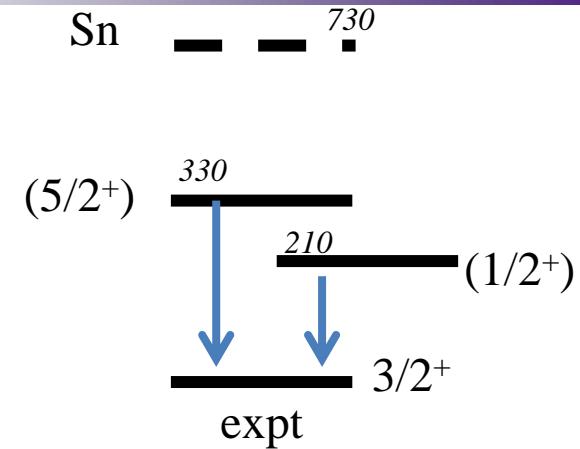
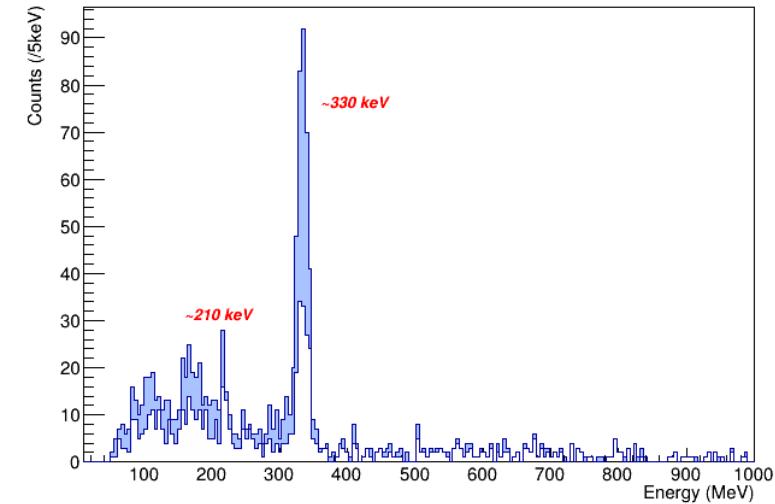


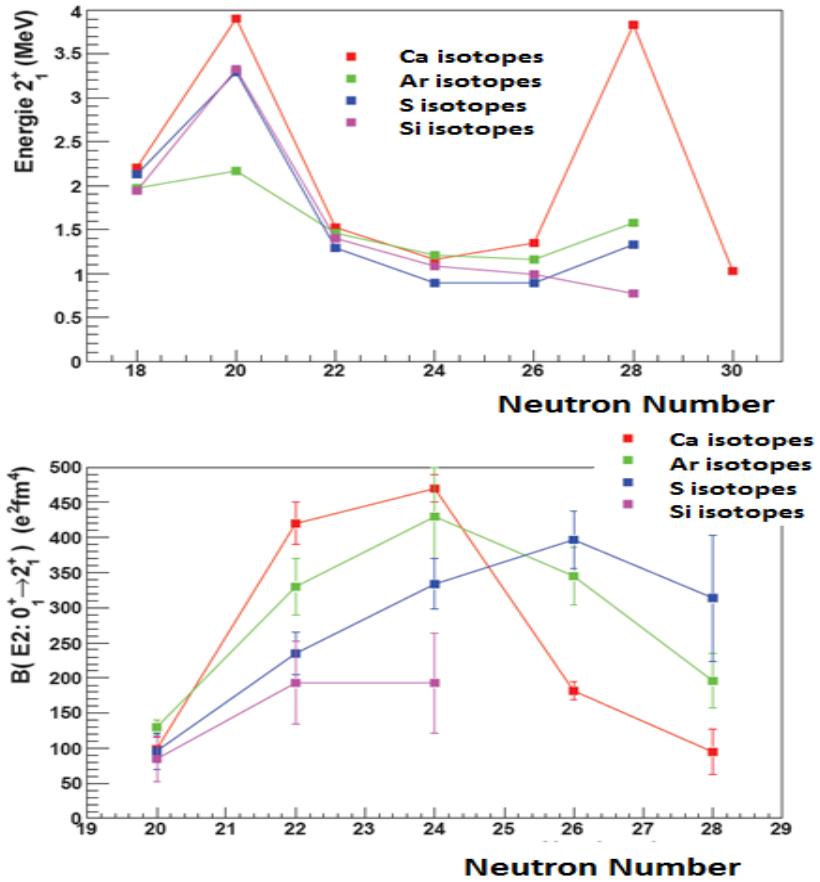
X. Pereira-López (USC/LPC)



- γ -rays to separate states ~ 100 keV apart that could not be separated in TIARA
- The 210 keV transition corresponds to an s-state which population decreases in the barrel.

γ spectrum





^{46}Ar

$$B(E2; 0^+ \rightarrow 2_1^+) = 196(39)e^2 fm^4$$

H. Scheit et al., Phys. Rev. Lett 77 (1996)

$$B(E2; 0^+ \rightarrow 2_1^+) = 218(39)e^2 fm^4$$

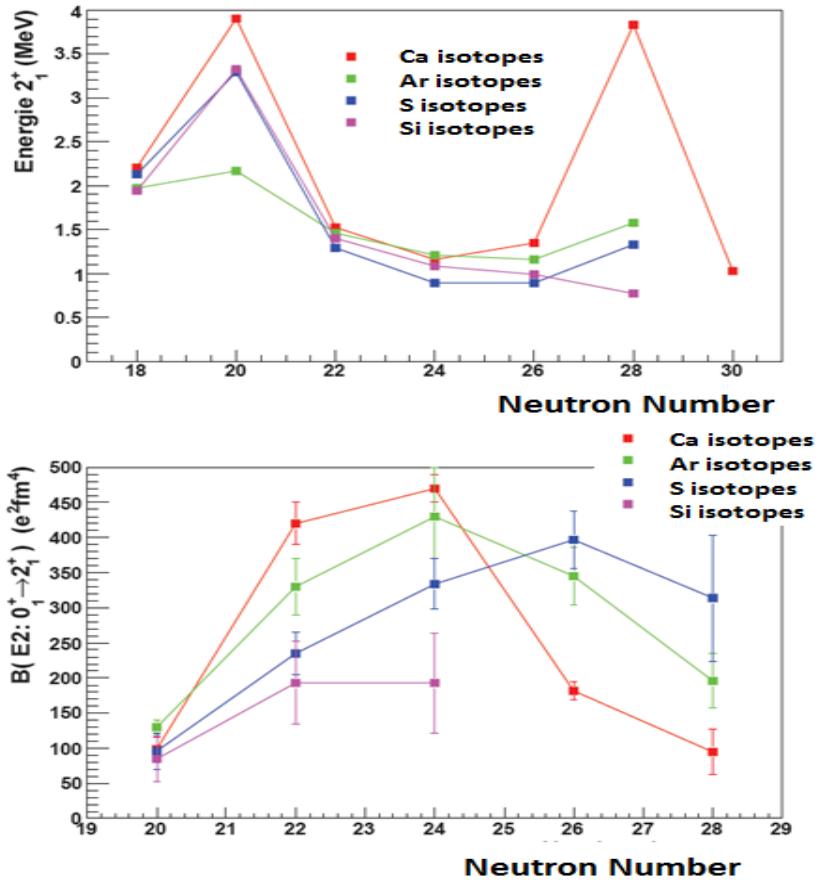
A. Gade et al., Phys. Rev. C 74 (2006)

Lifetime measurement

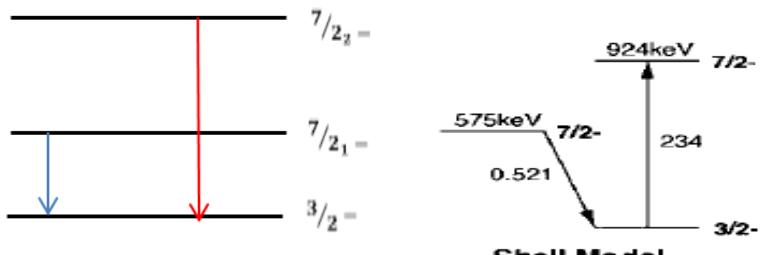
Isotope	E_γ (keV)	$J_i^\pi \rightarrow J_f^\pi$	τ (ps)	$B(E2)$ ($e^2 fm^4$)
^{44}Ar	1158	$2^+ \rightarrow 0^+$	5.9(2.0)	67_{-17}^{+44}
	1588	$4^+ \rightarrow 2^+$	$3.9_{-2.9}^{+3.6}$	21_{-10}^{+60}
	693	$6^+ \rightarrow 4^+$	>40	<128
^{46}Ar	1552	$2^+ \rightarrow 0^+$	$0.8_{-0.4}^{+0.3}$	114_{-32}^{+67}

D. Mengoni et al., Phys. Rev. C 82 (2010)

The N=28 Shell erosion



^{43}S

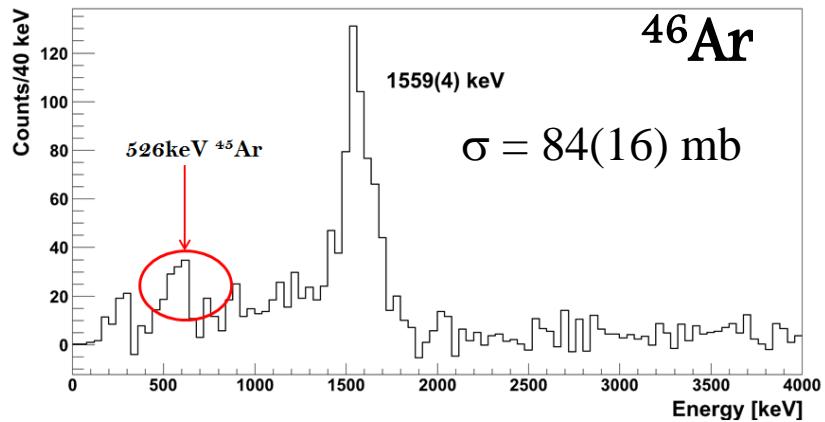


Adopted level scheme for ^{43}S

L.Gaudemroy et al, Phys.Rev.Lett 102(2009)

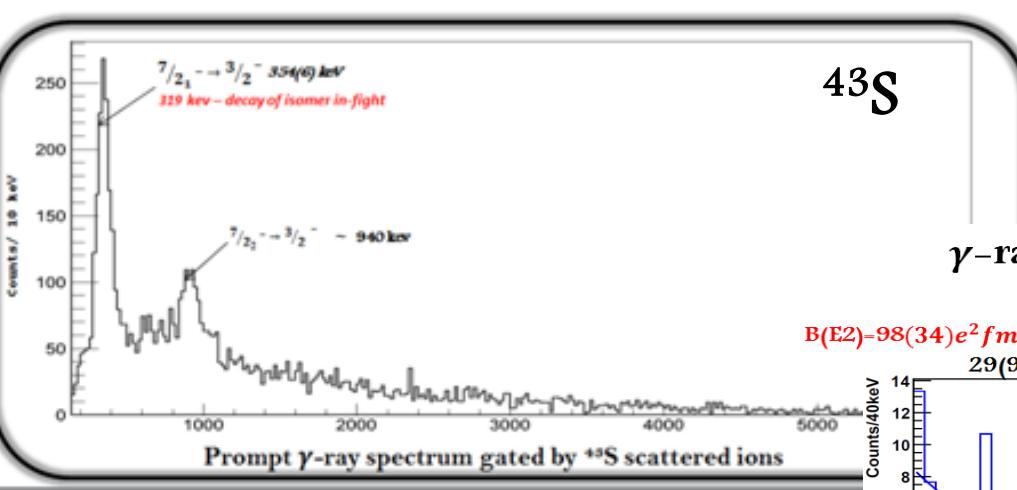
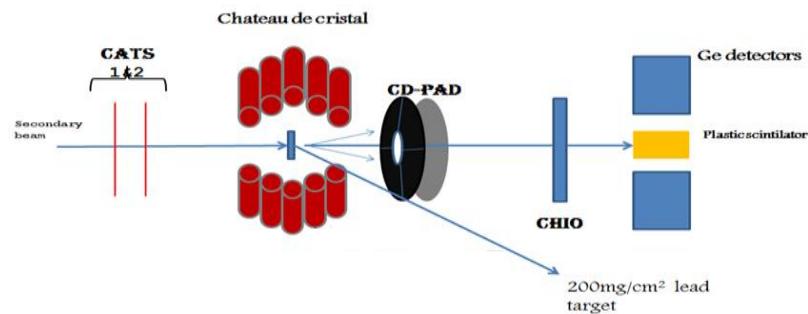
Nucleus	E/A (MeV)	E_γ (keV)	$B(E2\uparrow)$ ($e^2 fm^4$)
^{35}Al	43.8	1006 (19)	142 (52)
^{37}Si	45.1	1437 (27)	101 (45)
^{39}P	46.3	976 (17)	97 (30)
^{41}S	47.4	449 (8) 904 (16)	167 (65) 232 (56)
^{43}S	42.0	≈ 940	175 (69)
^{45}Cl	43.0	929 (17)	87 (24)

R.Ibbotson et al. Phys.Rev.C 59(1999)



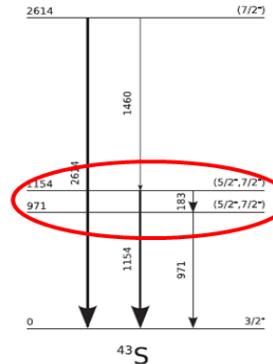
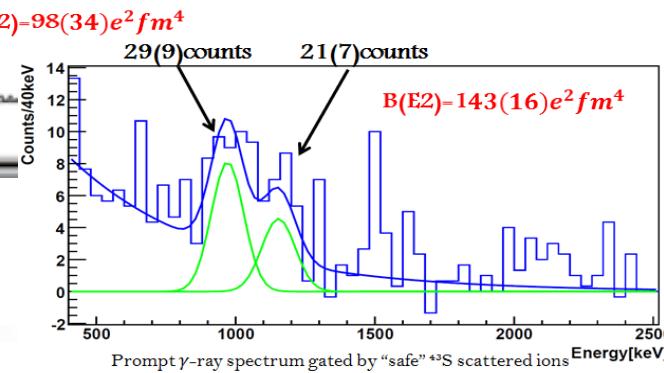
Prompt gamma-ray spectra gated by ^{46}Ar scattered ions
conditioned on the safe angle up to 3.25^0

$$B(E2) = 269(31) e^2 \text{fm}^4$$

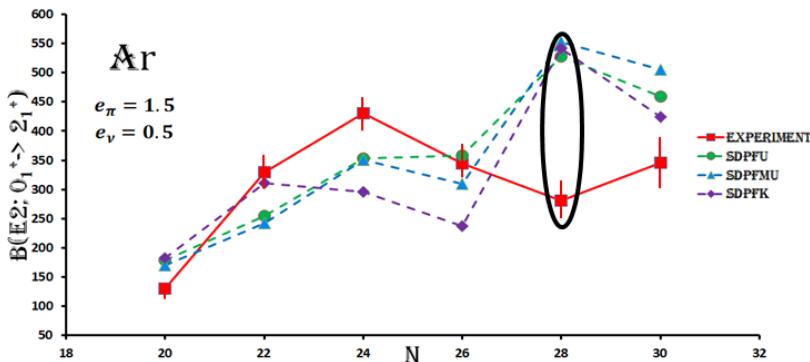


S. Calinescu IFIN-HH

γ -ray spectrum of ^{43}S : the assumption of two states

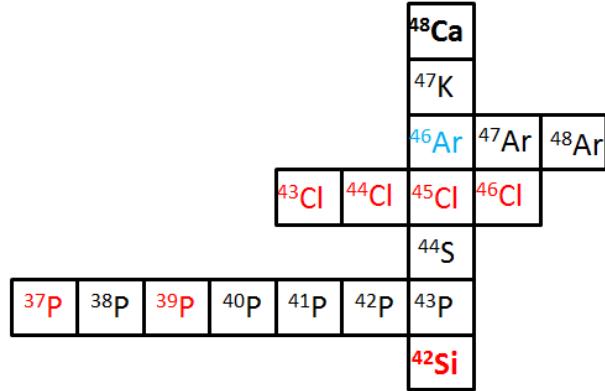


Shell model predictions for the Ar isotopic chain



Predicted level schemes for ^{46}Ar using NuShellX code by A.Brown

- All three interactions manage to reproduce the energy of the 2^+ state
- Global agreement between the experimental $B(E2)$ values and the theoretical predictions, except for $^{46}\text{Ar}!!$



In ^{46}Ar , the $B(E2, 0^+ \rightarrow 2^+) = 269(31)\text{e}^2\text{fm}^4$ is in agreement with previous Coulex excitations measurements. Further supports the semi-magic character of ^{46}Ar and confirms the puzzling deviation to SM calculations

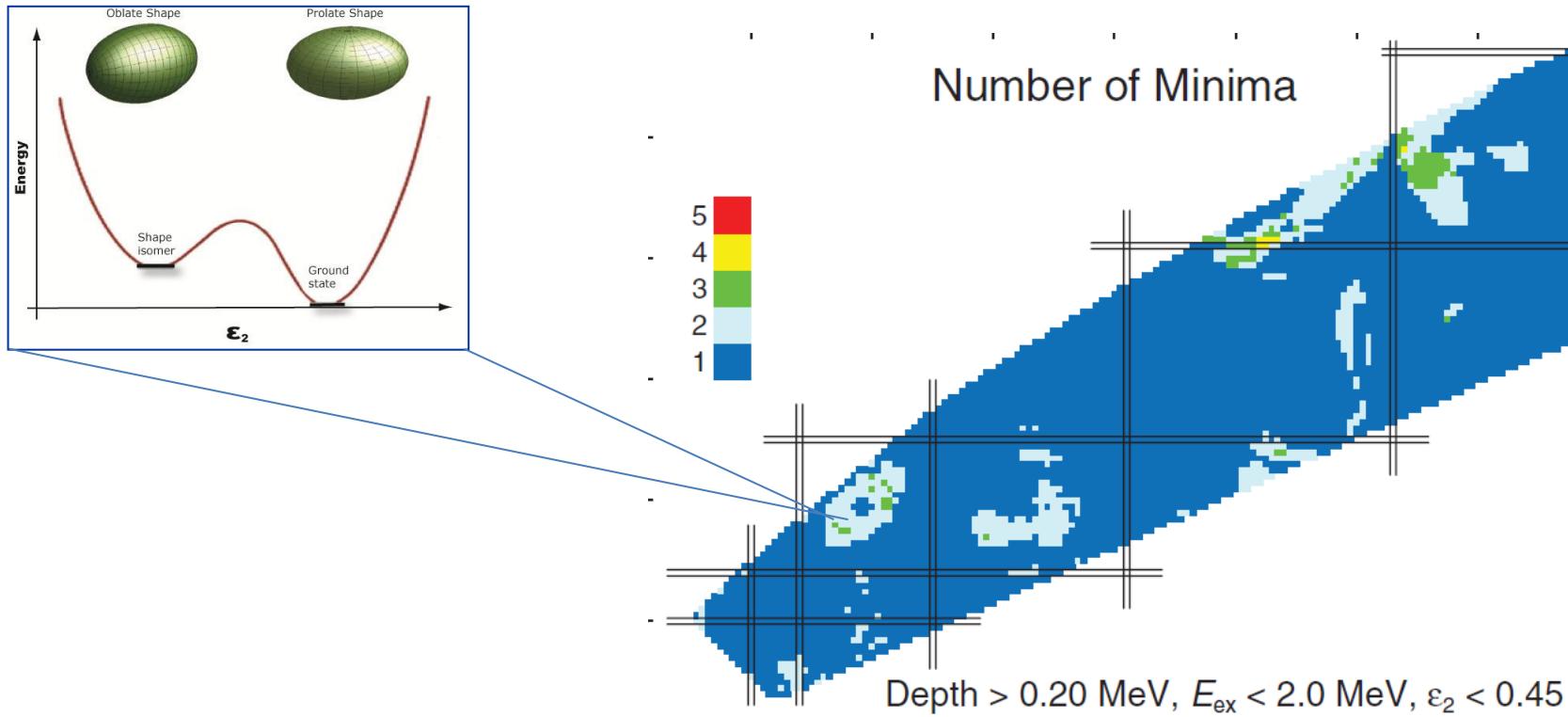
In ^{43}S the 971 keV and 1154 keV states have corresponding $B(E2)$ of $98(34)\text{e}^2\text{fm}^4$ and $143(16)\text{e}^2\text{fm}^4$

Further investigation by safe Coulex from the on-going SPIRAL1-upgrade ^{41}S , $^{37-39}\text{P}$, $^{43-45}\text{Cl}$

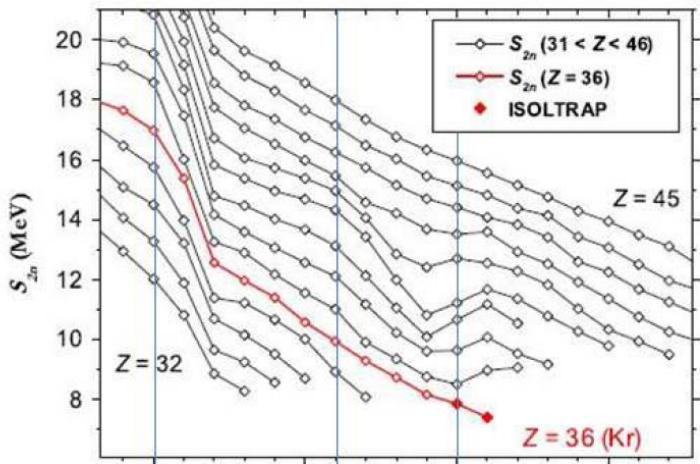
Shapes

- 1) Shape coexistence and shape change
- 2) Octupole correlations *L. P. Gaffney et al, Nature 497, 199 (2013)*

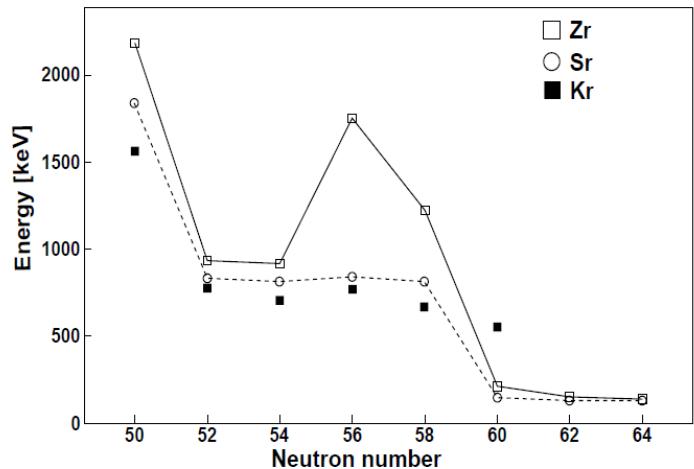
P. Möller et al Phys. Rev. Lett 103, 212501 (2009)



Shape Transition at N=60



S. Naimi et al., Phys. Rev. Lett. 105, 032502 (2010).

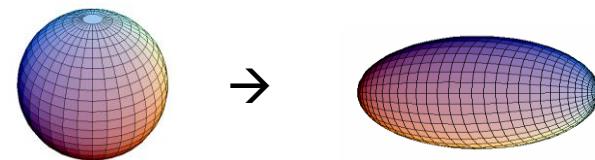


M. Albers et al., Phys. Rev. Lett. 108, 062701 (2012)

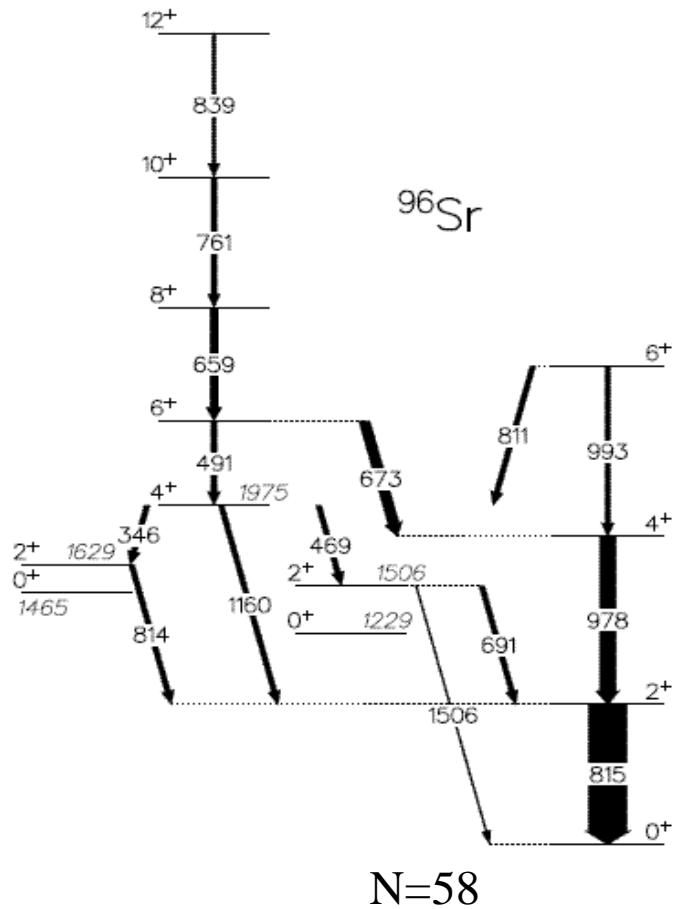
- The n-rich nuclei between $Z=37$ and $Z=42$ present at $N=60$ one of the most impressive deformation change in the nuclear chart

Point to a specific $\pi-\nu$ combinaison

+ 2v

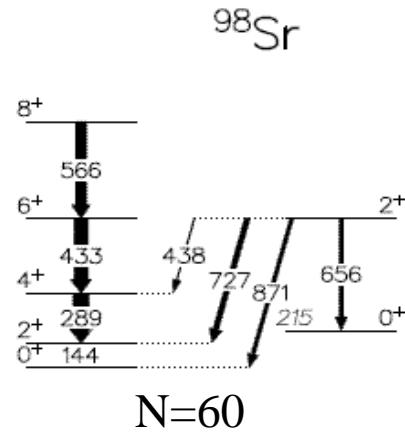


Shape coexistence

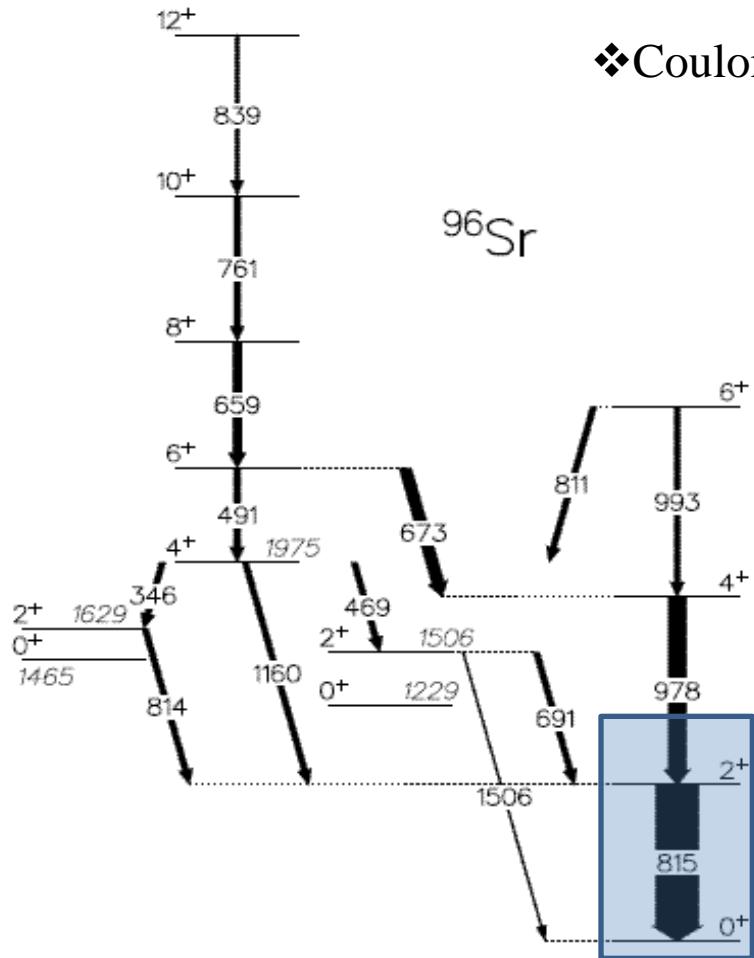


- B(E2)'s connecting states to probe the collectivity and the mixing of configurations
- Q_0 to determine the deformation

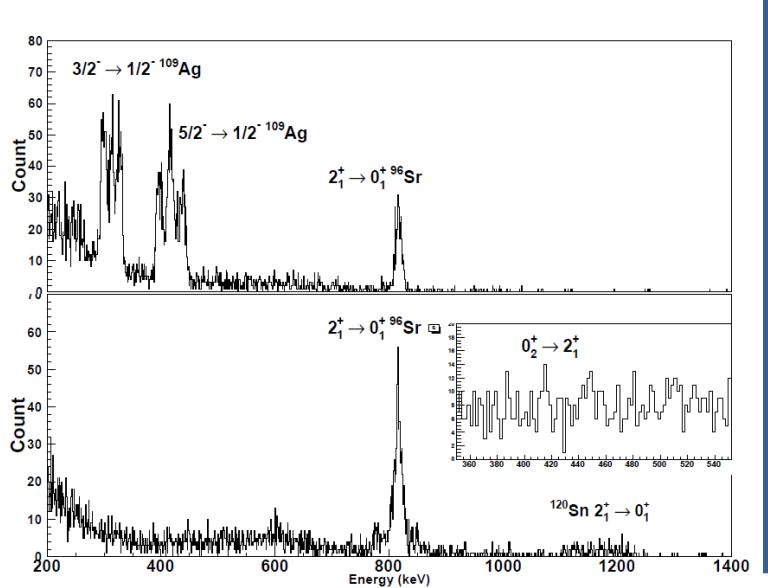
Coulomb excitation of RIB



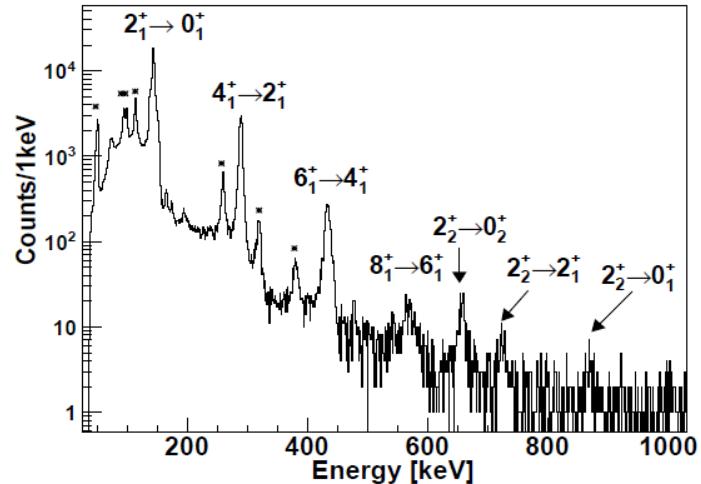
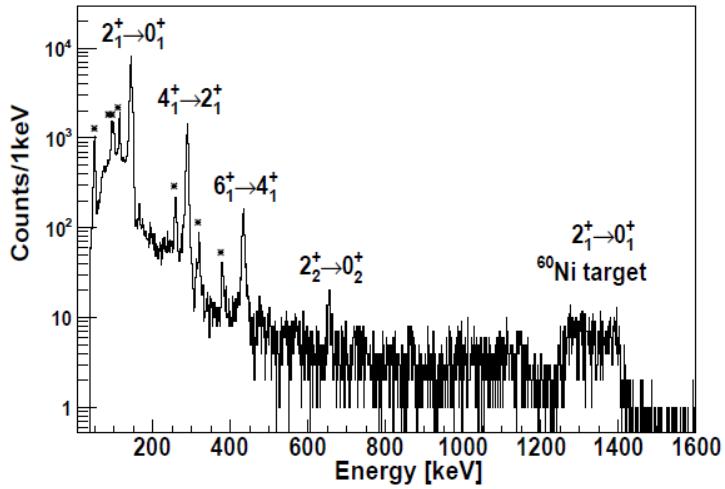
Coulomb excitation results



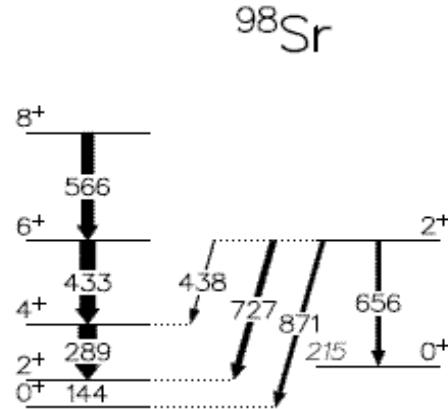
❖ Coulomb excitation of ^{96}Sr at 2.8 MeV/A –REX-ISOLDE



Coulomb excitation results



- ❖ Coulomb excitation of ^{98}Sr at 2.8 MeV/A
- ❖ Ground state and non-yrast states populated

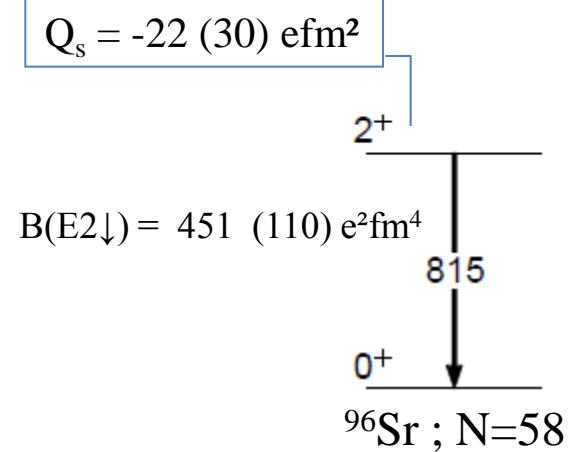


E. Clément et al , in preparation

E. Clément et al. EPJ Web of Conferences **62**, 01003 (2013)

❑ ^{96}Sr : The Electric spectroscopic Q_0 is small as its $B(E2)$ is rather large

- Vibrator character
- Weak quadrupole deformation



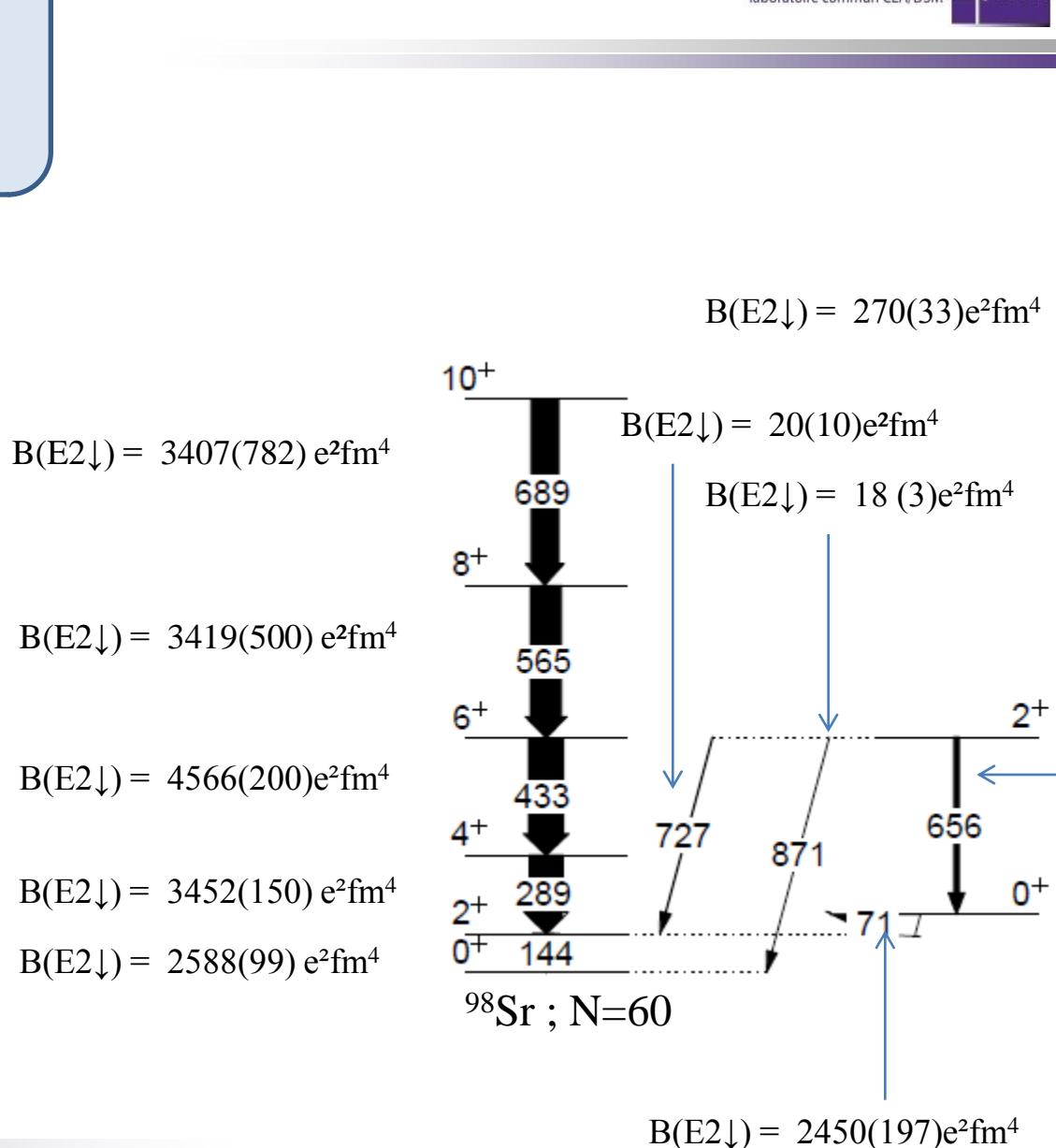
$$B(E2\downarrow) = 3407(782) \text{ e}^2\text{fm}^4$$

$$B(E2\downarrow) = 3419(500) \text{ e}^2\text{fm}^4$$

$$B(E2\downarrow) = 4566(200) \text{ e}^2\text{fm}^4$$

$$B(E2\downarrow) = 3452(150) \text{ e}^2\text{fm}^4$$

$$B(E2\downarrow) = 2588(99) \text{ e}^2\text{fm}^4$$



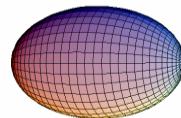
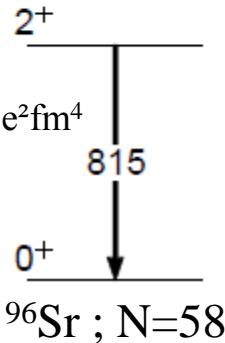
□ ^{96}Sr : The Electric spectroscopic Q_0 is small as its $B(E2)$ is rather large

- Vibrator character
- Weak quadrupole deformation

□ ^{98}Sr

- The ground state band is a rotor
- Excited configuration similar to ^{96}Sr

$$Q_s = -22(30) \text{ efm}^2$$



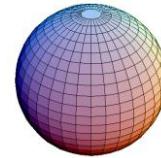
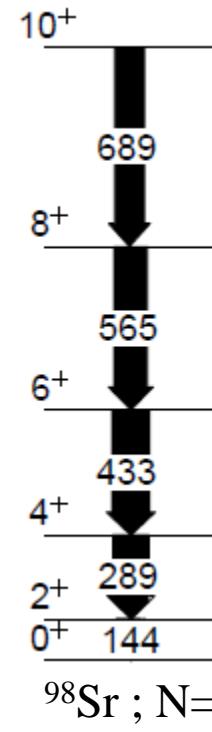
$$\beta \sim 0.4$$

$$Q_s = -95(100) \text{ efm}^2$$

$$Q_s = -121(13) \text{ efm}^2$$

$$Q_s = -187(8) \text{ efm}^2$$

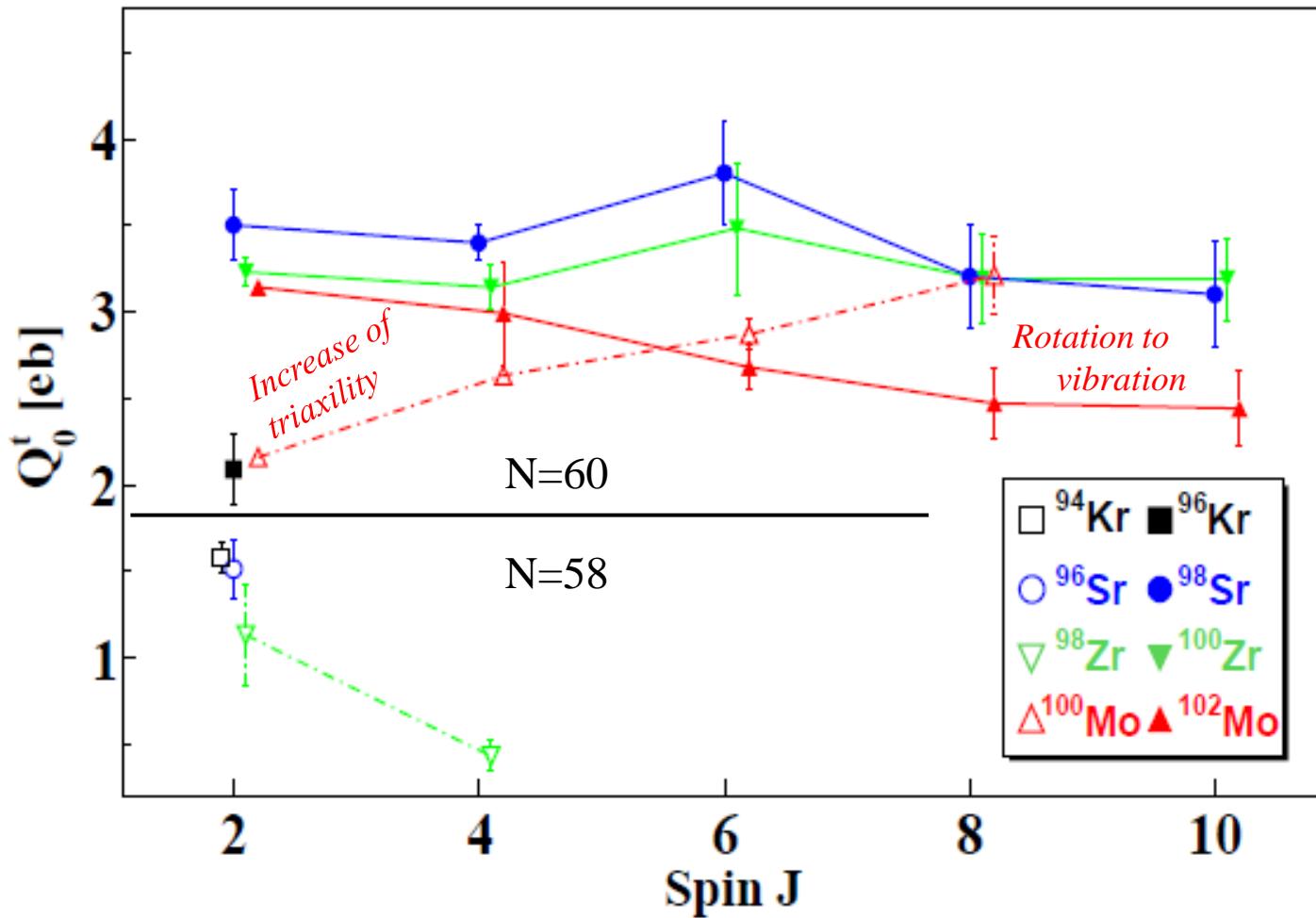
$$Q_s = -52(14) \text{ efm}^2$$

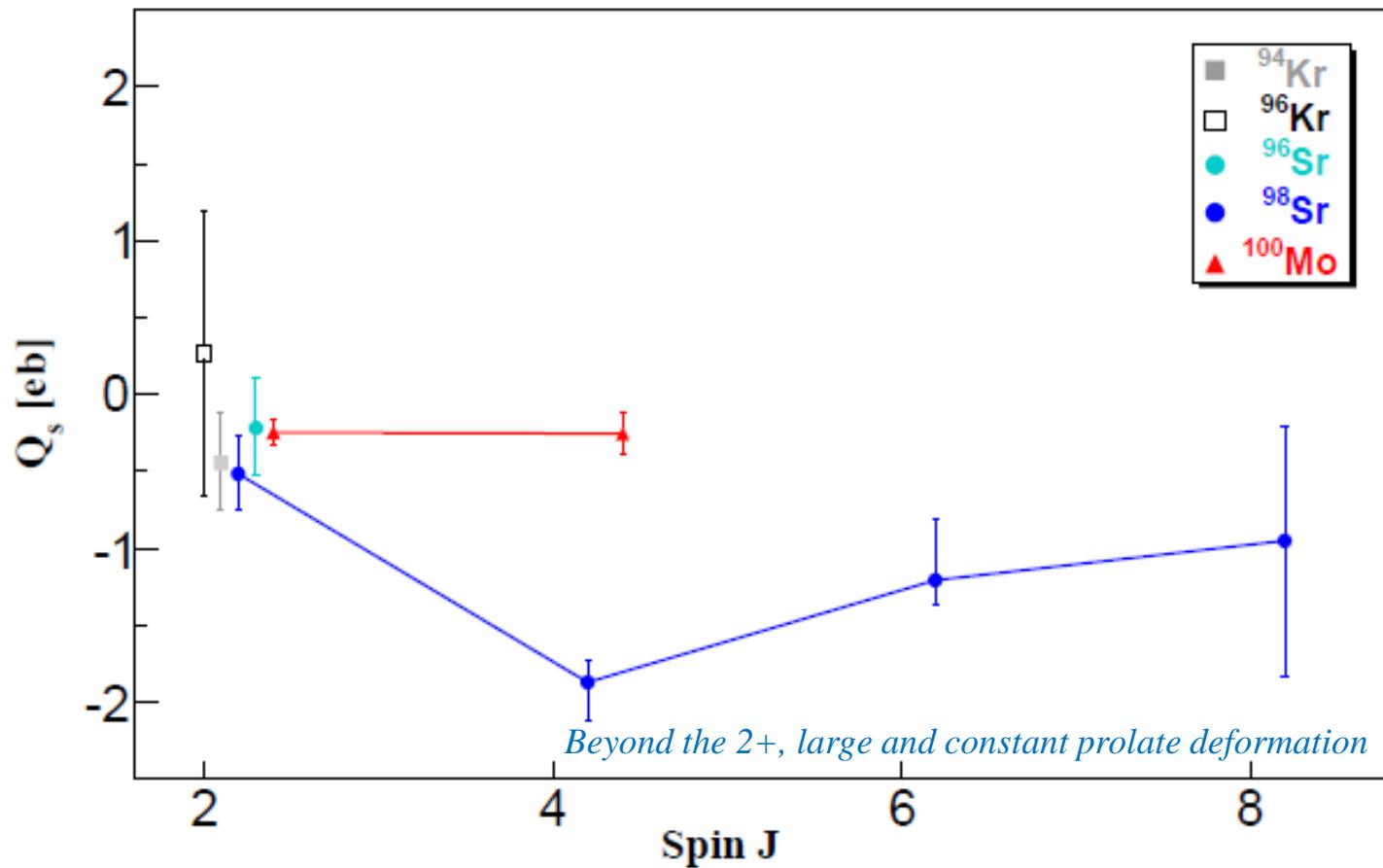


$$|\beta| < 0.1$$

$$Q_s = 2(20) \text{ efm}^2$$

Systematic of Transitional Quadrupole moment around N=60



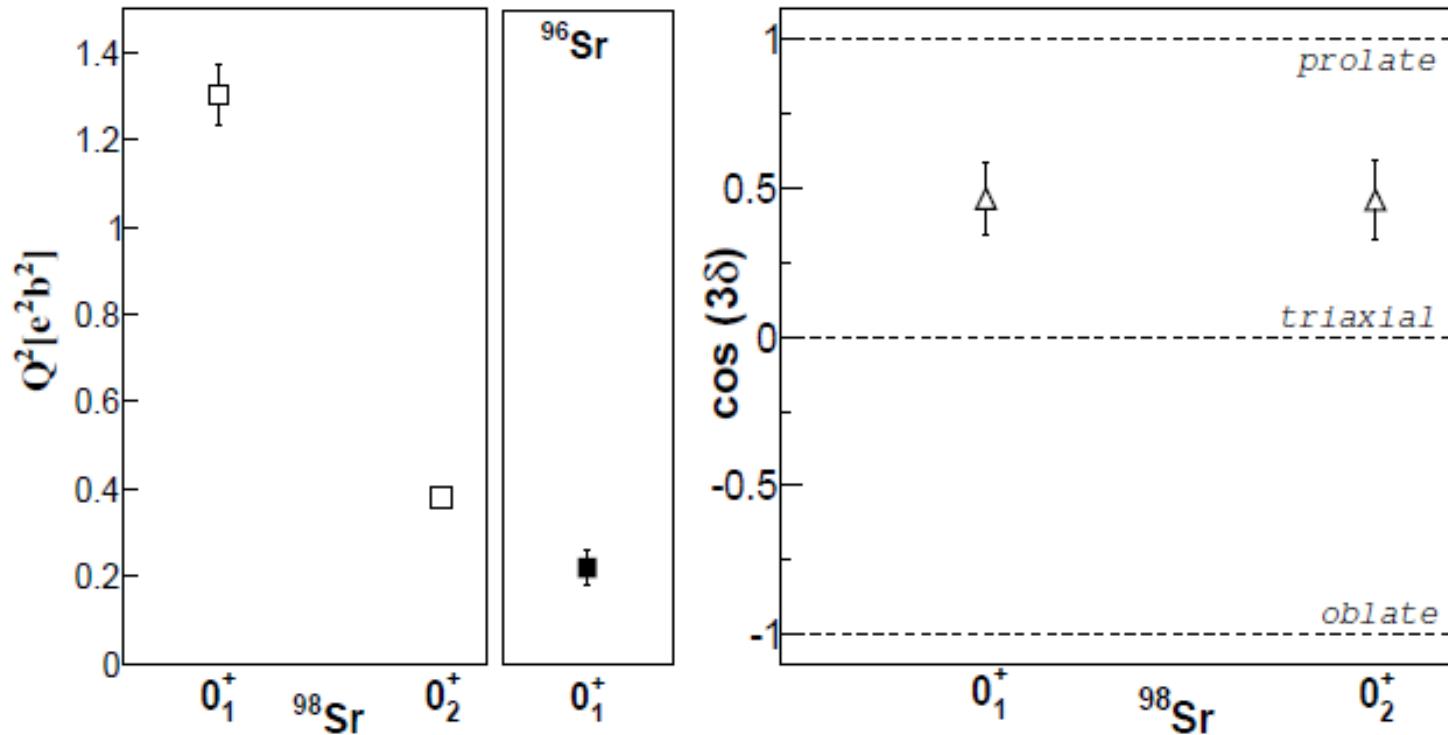


K. Wrzosek-Lipska et al. Phys. Rev. C 86, 064305 (2012).

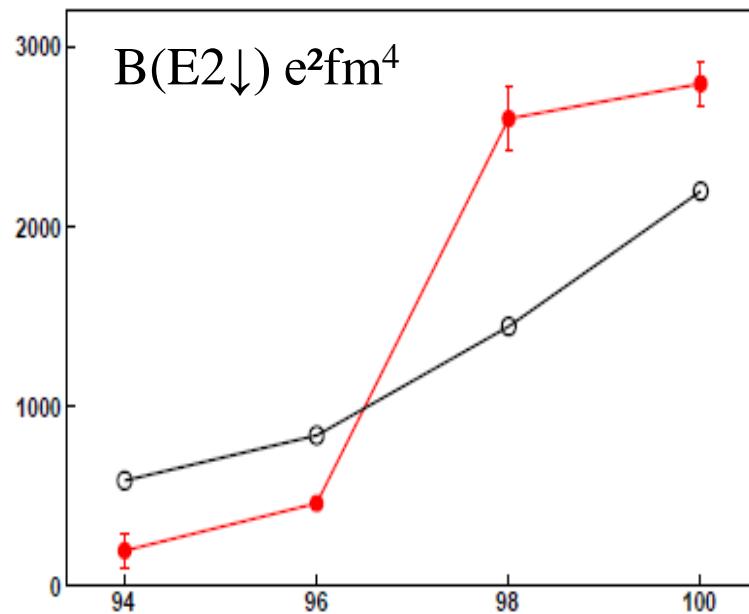
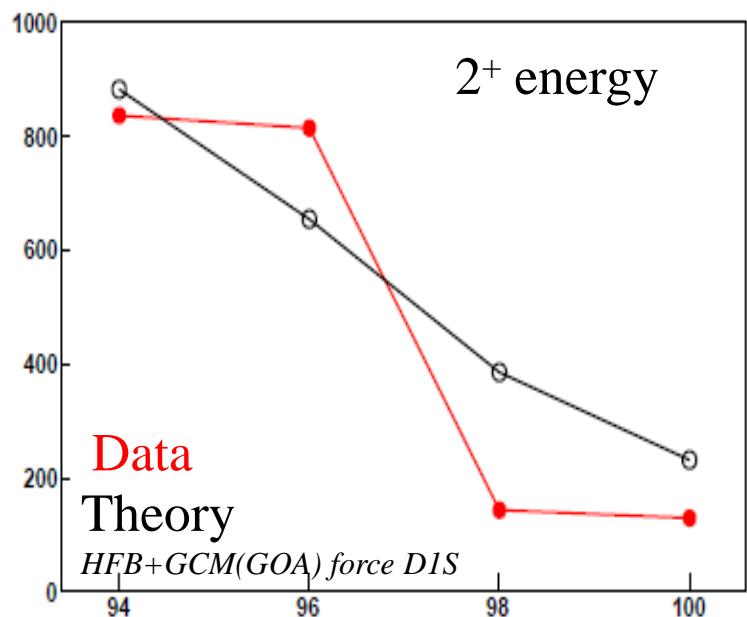
M. Albers et al., Phys. Rev. Lett. 108, 062701 (2012)

E. Clément et al , in preparation

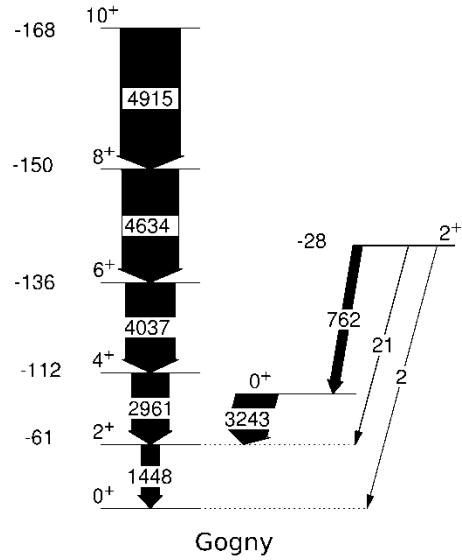
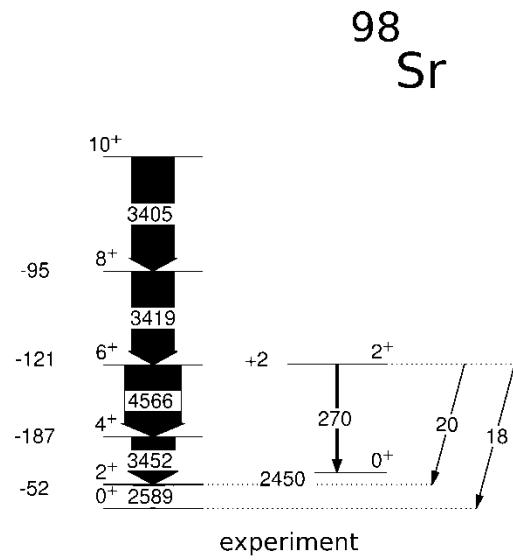
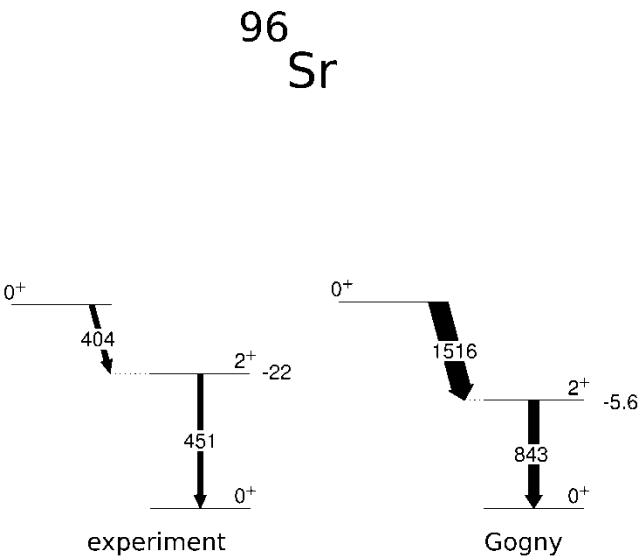
- Deformation of the 0^+ states analyzed with the Quadrupole Sum Rules formalism
- Sums of quadrupole E2 matrix elements give $Q^2 \sim |\beta_2|$ and $\cos(3\delta) \sim \gamma$



Comparison with theory :

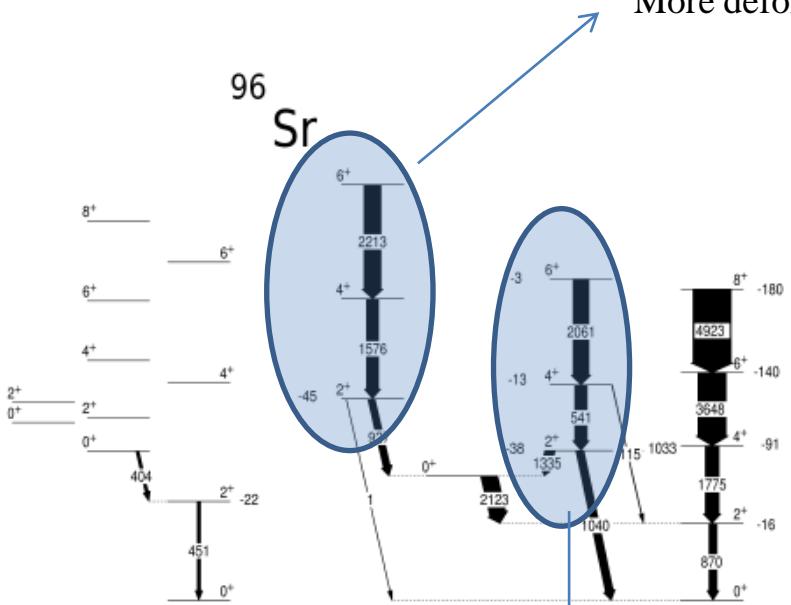


Comparison with theory :



Comparison with theory :

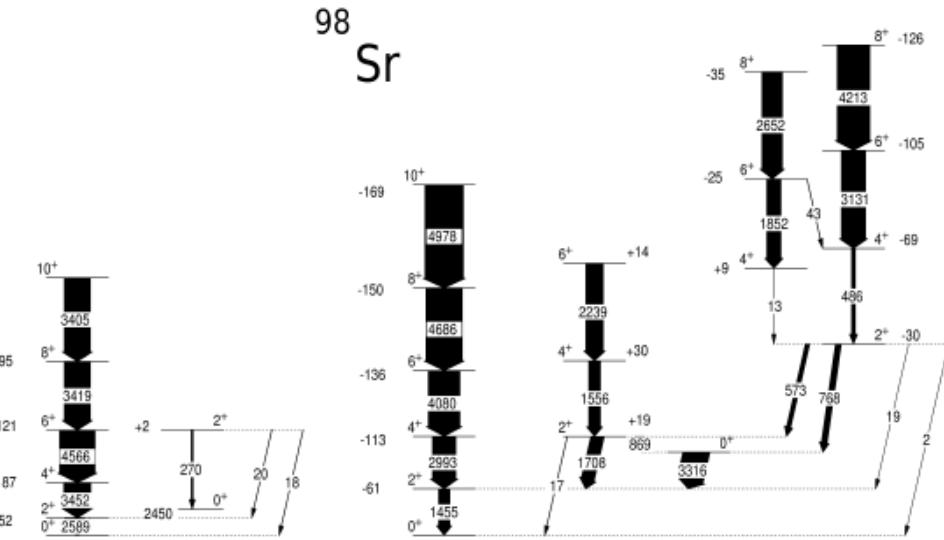
More deformed with a larger contribution of K=0.



experiment

Gogny

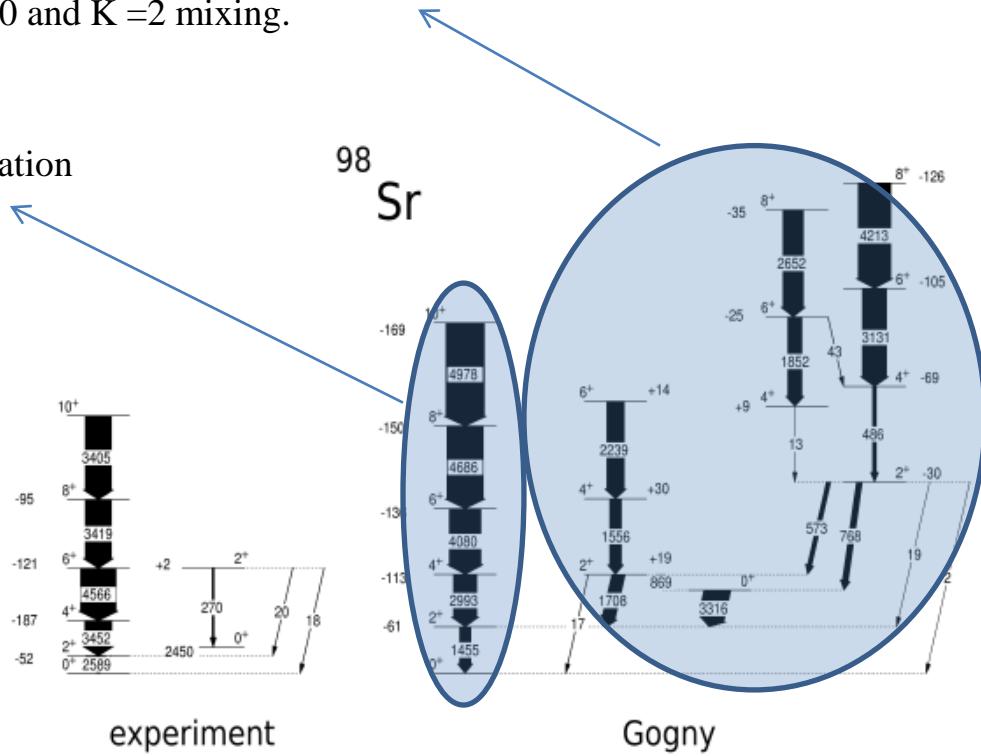
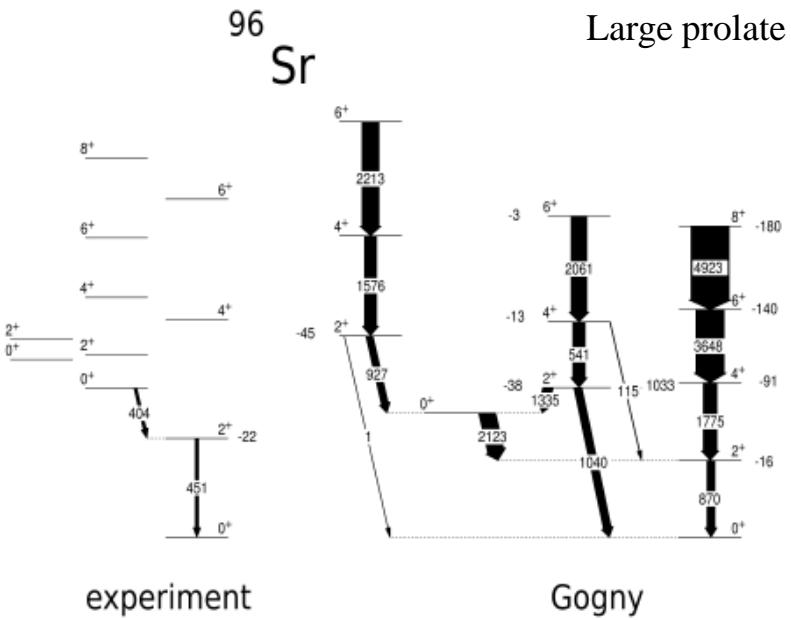
Large B(E2) values and small Qs.
 Contribution of the triaxial degree of freedom
 K=0 component below 50%



experiment

Gogny

Similarly to the Kr case, a clear classification of the states and the assignment of non-yrast bands is difficult, due to γ softness and K=0 and K =2 mixing.



- The first theoretical excited band, predicted to be mainly of K=2 character
 - Probably calculated too low in excitation energy since it is not observed experimentally.
 - Large calculated $B(E2, 2^+_2 \rightarrow 2^+_1)$ value and the relative proximity of the three 2^+ states suggest a very complex mixing between bands in the calculation.

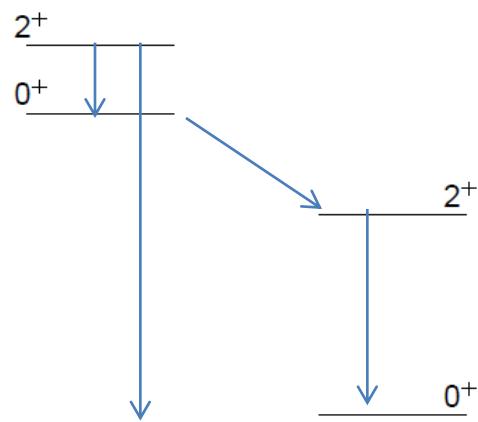
Shape coexistence in a two-state mixing model

$$\begin{array}{l}
 \boxed{|I_1\rangle = +\cos\theta_I |I_{\text{pr}}\rangle + \sin\theta_I |I_{\text{ob}}\rangle} \\
 \boxed{|I_2\rangle = -\sin\theta_I |I_{\text{pr}}\rangle + \cos\theta_I |I_{\text{ob}}\rangle}
 \end{array}$$

Pure states

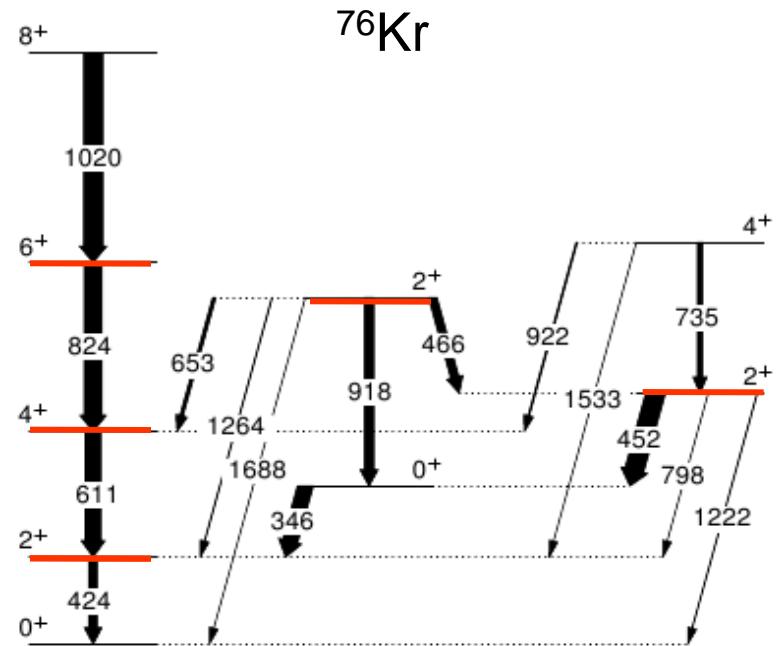
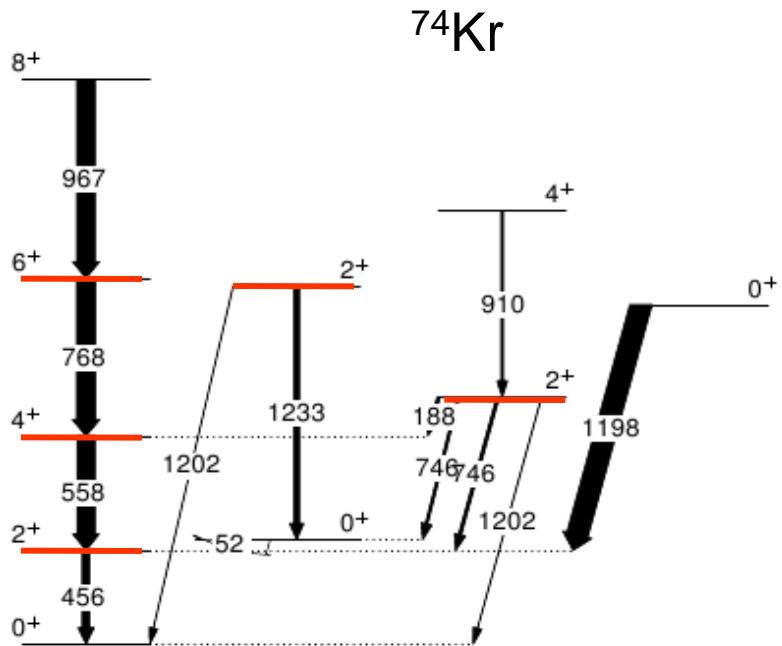
Perturbed states

Extract **mixing** and **shape** parameters from set of experimental **matrix elements**.



$$\tan\theta_0 = A \pm \sqrt{A^2 + 1}, \quad A = \frac{M_{11}^2 + M_{21}^2 - M_{12}^2 - M_{22}^2}{2(M_{11}M_{12} + M_{21}M_{22})}$$

$$\tan\theta_2 = \frac{M_{11}\tan\theta_0 + M_{12}}{M_{21}\tan\theta_0 + M_{22}},$$



E. Clément et al. Phys. Rev. C 75, 054313 (2007)

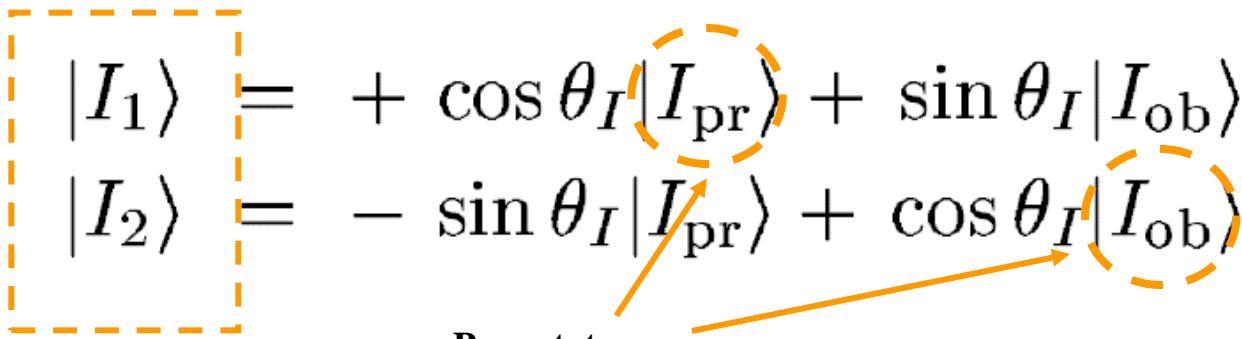
In ^{74}Kr and ^{76}Kr , a prolate ground state coexists with an oblate excited configuration and they are strongly interaction

Shape coexistence in a two-state mixing model

$$\begin{array}{l}
 \boxed{|I_1\rangle} = +\cos\theta_I |I_{\text{pr}}\rangle + \sin\theta_I |I_{\text{ob}}\rangle \\
 |I_2\rangle = -\sin\theta_I |I_{\text{pr}}\rangle + \cos\theta_I |I_{\text{ob}}\rangle
 \end{array}$$

Pure states

Perturbed states



Extract **mixing** and **shape** parameters from set of experimental **matrix elements**.

- **Energy perturbation of 0^{+}_2 states**

E. Bouchez et al. Phys. Rev. Lett **90** (2003)

	${}^{76}\text{Kr}$	${}^{74}\text{Kr}$	${}^{72}\text{Kr}$
$\cos^2\theta_0$	0.73(1)	0.48(1)	0.10(1)

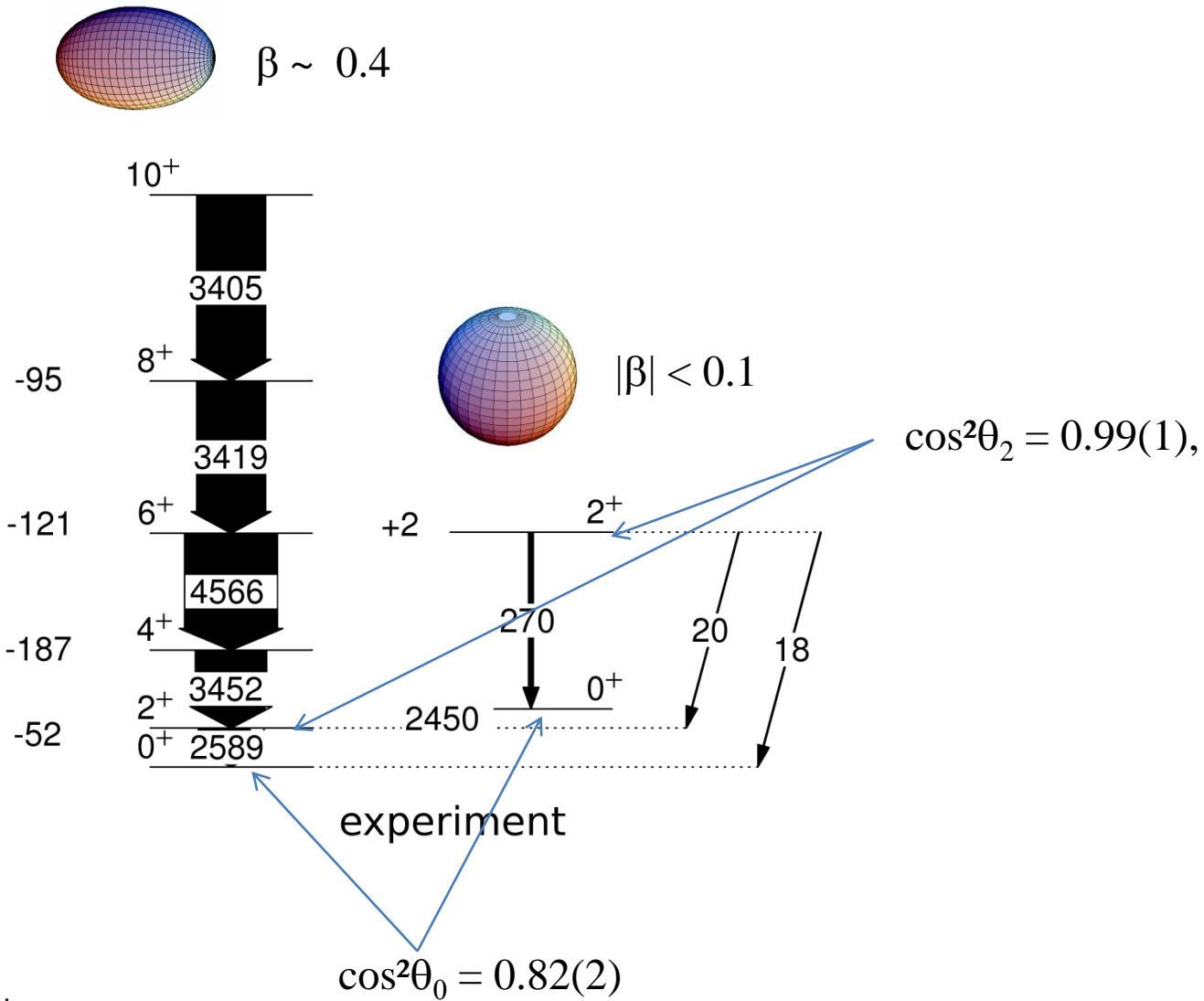
- **Full set of matrix elements :**

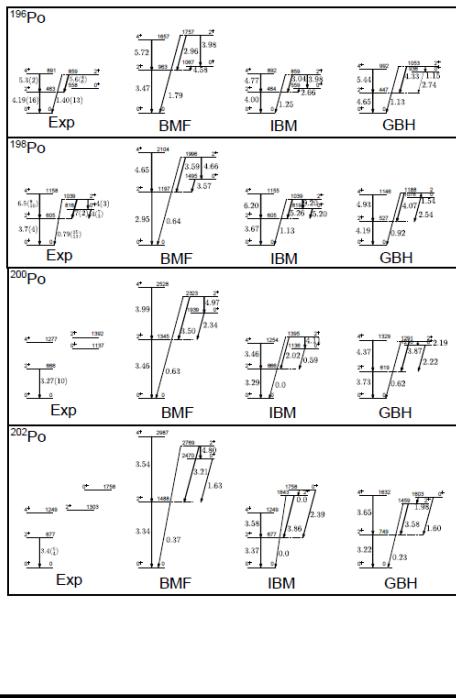
E. Clément et al. Phys. Rev. C **75**, 054313 (2007)

	${}^{76}\text{Kr}$	${}^{74}\text{Kr}$	${}^{72}\text{Kr}$
$0.69(4)$	0.48(2)	*	*
*	0.6	0.5	

- **Excited Vampir approach:**

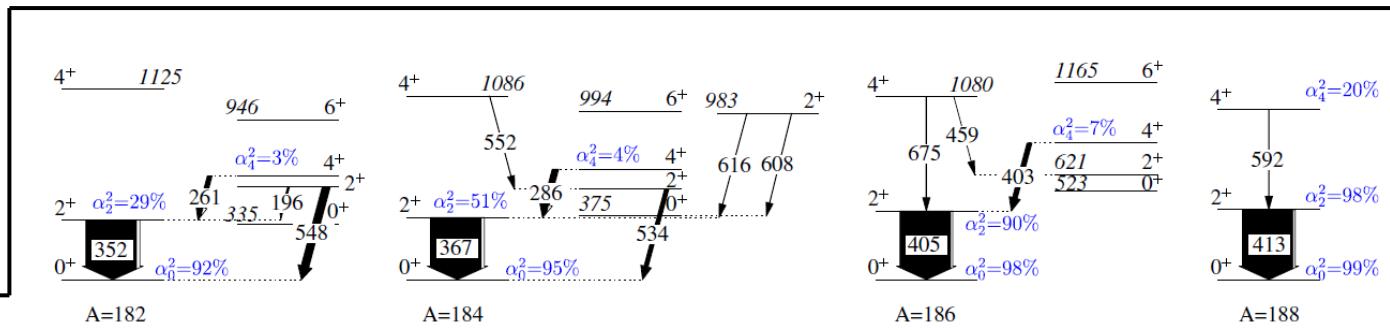
A. Petrovici et al., Nucl. Phys. A **665**, 333 (00)





Isotope	α_{0+}^2	α_{2+}^2
^{194}Po	12 %	29 %
^{196}Po	85 %	50 %
^{198}Po	94 %	69 %
^{200}Po	97 %	92 %
^{202}Po	99 %	88 %

N. Kesteloot et al submitted to PRC



N. Bree et al, PRL 112, 162701 (2014)

- Over long isotopic chains, the two level mixing model shows that intrinsic configurations remain and the measured values are the results of the mixing amplitude
- True for Kr, Po and Hg so far → Sr, Zr, Pb ?

Conclusion

- In-beam γ -ray spectroscopy with RIB provides fundamental information in the study of the nuclear structure far from stability
- Post-accelerated RIB at the suitable energies allow high quality spectroscopic measurement

Where to look :

At N=28 and N=20 new post-accelerated RIB for Transfer and Coulex data

RIB in the 3rd island of inversion : post accelerated beam of Co, Fe in the vicinity of N=40

Large isotopic chain for the shape coexistence , triple shape coexistence in the Pb, Sr/Zr chain