

A new era for jet studies in ultra-relativistic heavy-ion collisions

José Guilherme Milhano

CENTRA-IST (Lisbon) & CERN PH-TH

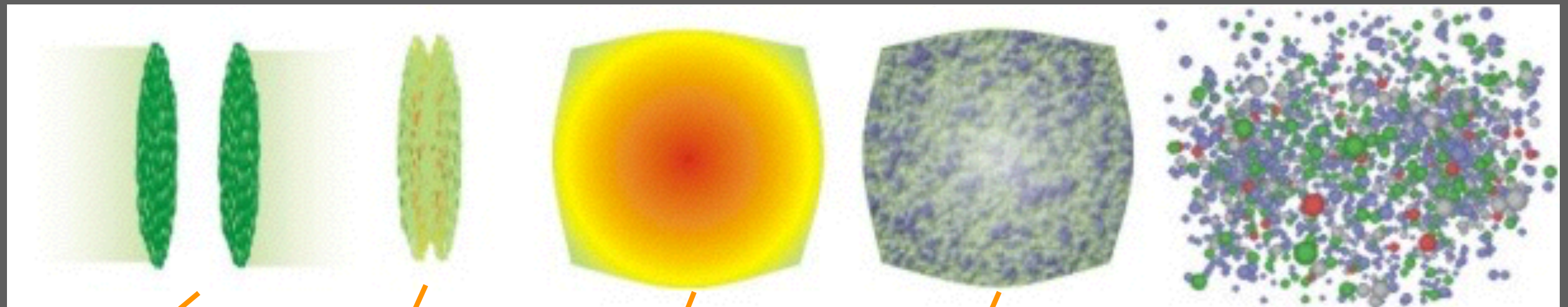
guilherme.milhano@cern.ch

$\sim 0.1 \text{ fm}/c$

$\sim 1 \text{ fm}/c$
[$\sim 10^{-24} \text{ s}$]

$\sim 10 \text{ fm}/c$

time



colliding [cold] nuclei
[initial condition]

pre-equilibrium
[collision]

Quark Gluon Plasma
[hot, dense and coloured]
[equilibrated/thermalized]
hydrodynamic expansion

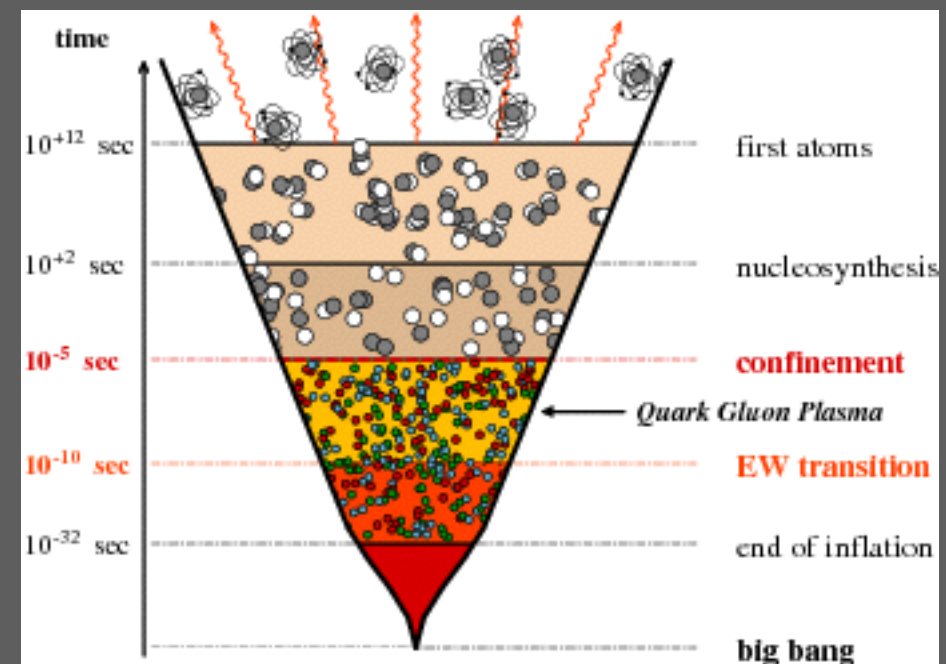
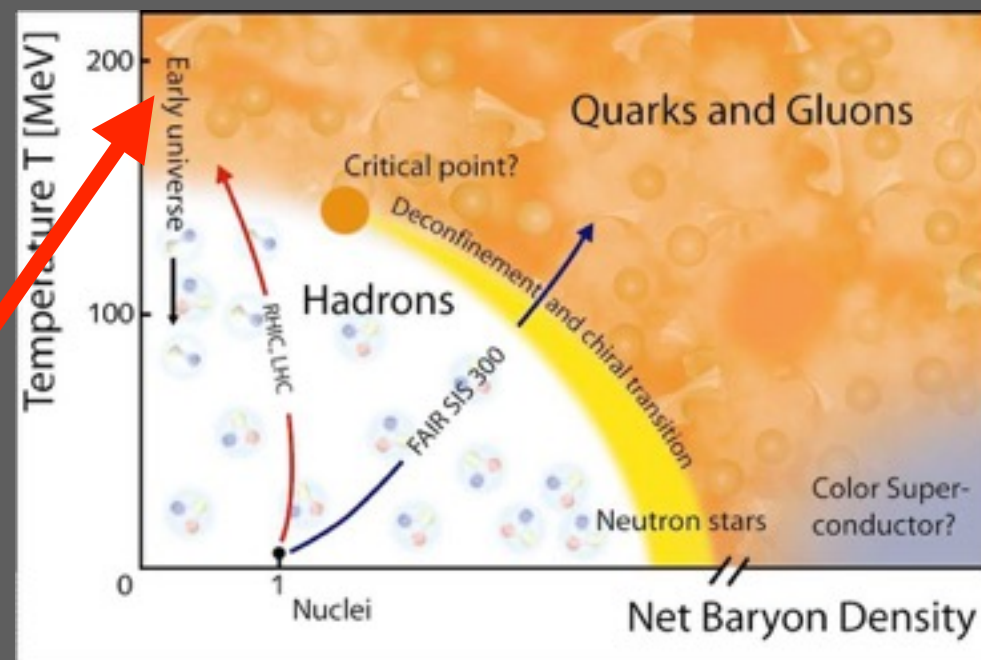
hadronization

hadrons
[back to cold nuclear matter]

from nuclei to QGP :: a heavy ion collision

quark gluon plasma

- an almost perfect liquid [the most perfect ever observed] of fundamental degrees of freedom [quarks and gluons] :: direct manifestation of collective behaviour in a fundamental non-abelian Quantum Field Theory [QCD]
- a unique, experimentally accessible and theoretically tractable, opportunity to further the understanding of nuclear matter in a novel regime [deconfined, yet strongly interacting, quarks and gluons] also of critical importance in the early history of the Universe



quark gluon plasma

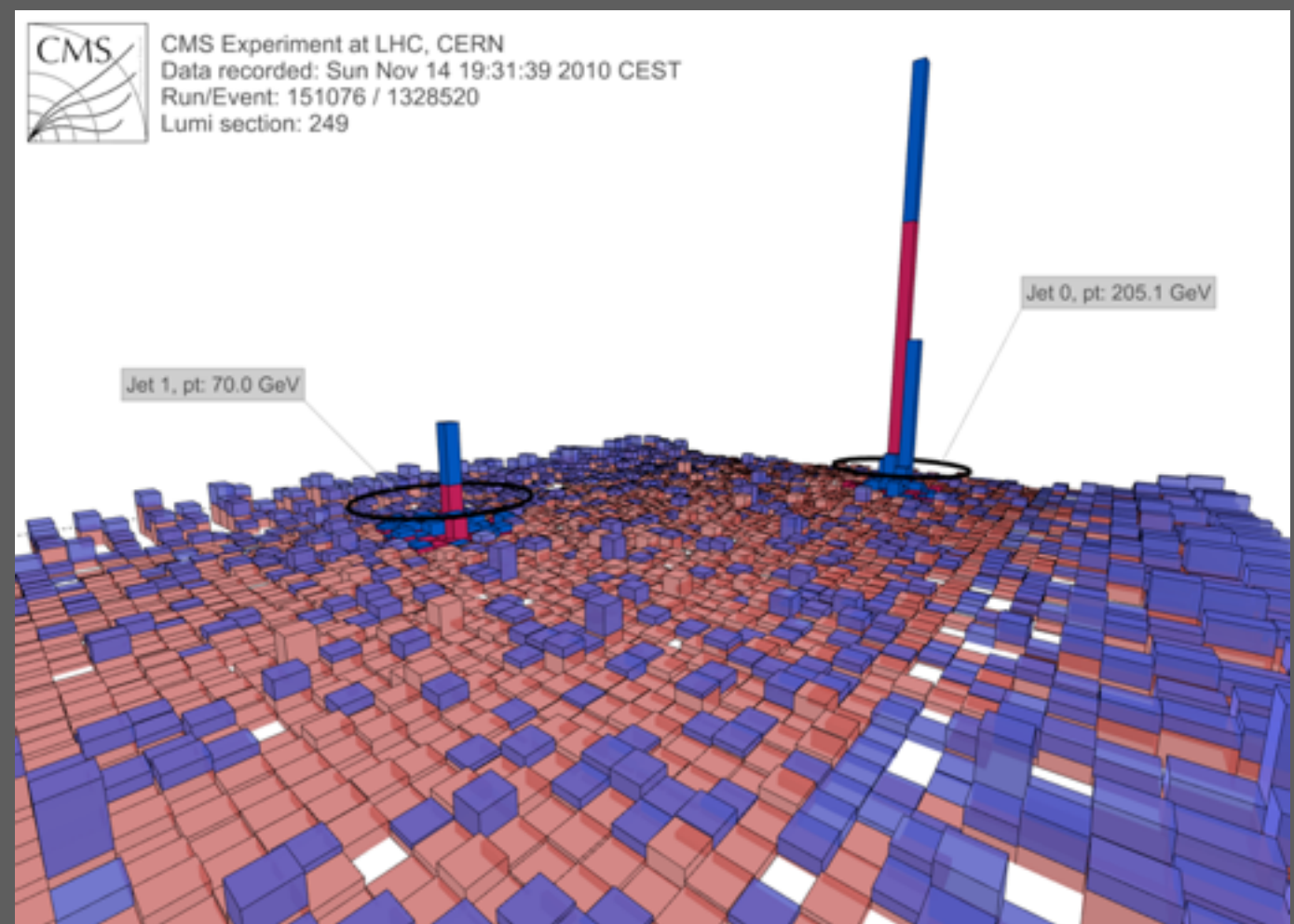
- 'discovered' and confirmed at the SPS, RHIC and LHC
- current focus on understanding of dynamics and precise measurement of properties :: must rely on self-generated probes [short-lived QGP]
- broadly two sets of handles
 - bulk [collective] observables :: flows, correlations, ... B Schenke Wed 11.00
K Redlich Wed 12.00
 - hard probes [detailed microscopic probes] M van Leeuwen Mon 10.00
 - EW [non-interacting benchmark]
 - quarkonia/heavy flavour S Masciocchi Tue 12.00
 - jets M van Leeuwen + this talk



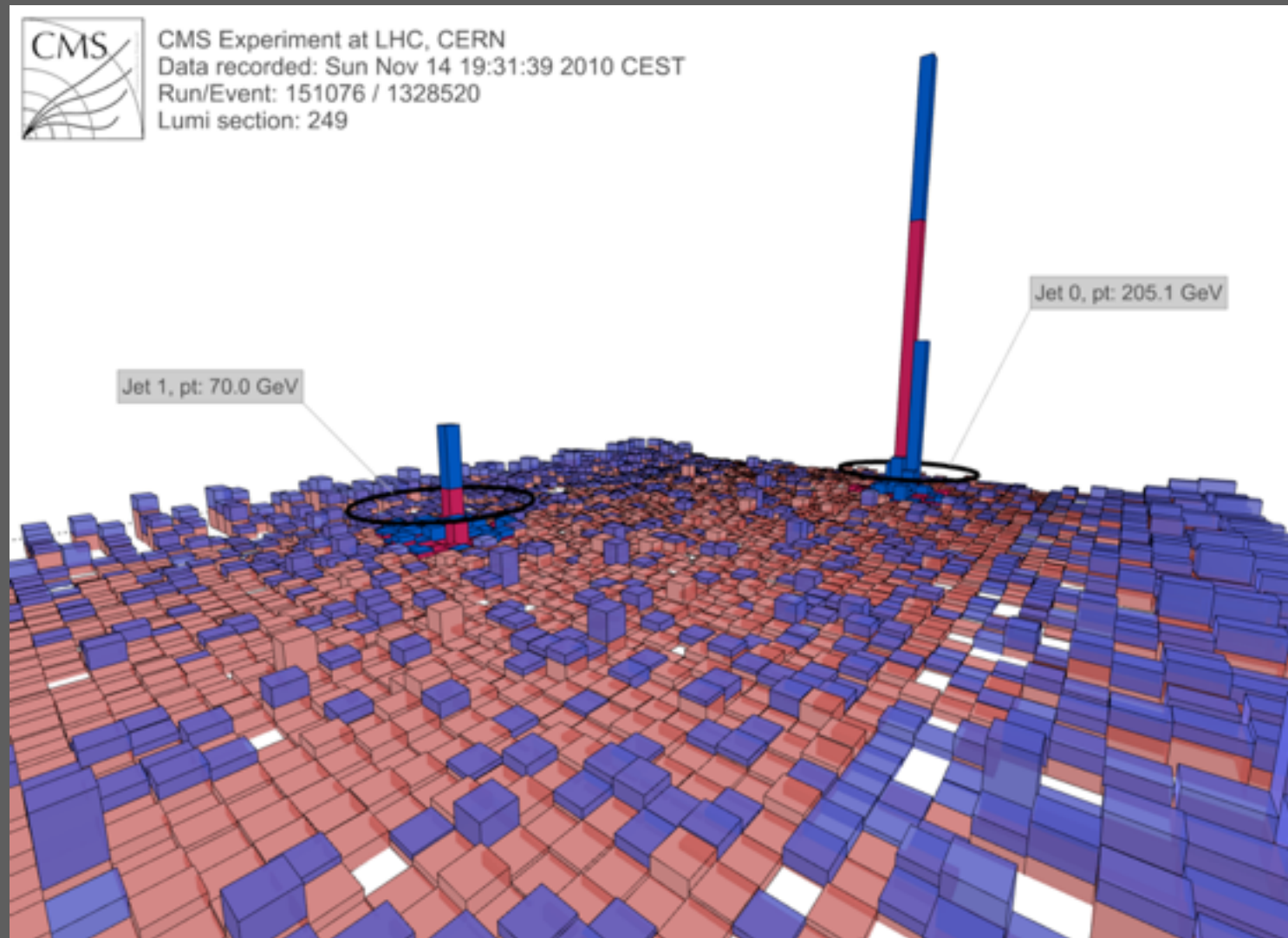
focus here on few key theoretical ideas

jet definition

collimated spray of hadrons resulting from the QCD branching of a hard [high- p_t] parton and subsequent hadronization of fragments and grouped according to given infra-red and collinear safe procedure [jet algorithm] and for given defining parameters [eg, jet radius]



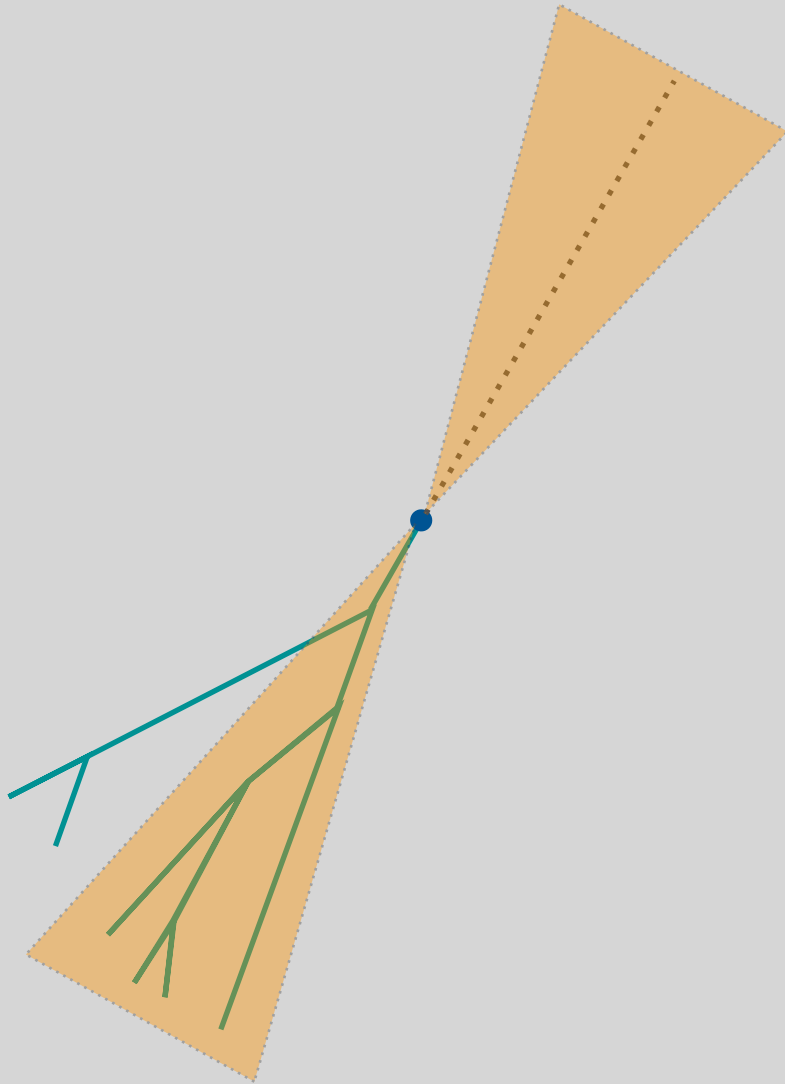
jets in heavy ion collisions



- major accomplished experimental challenge
 - jets can be systematically reconstructed above large [100 GeV in jet catchment area] and fluctuating [up to 20 GeV] background
- jets are very well understood in vacuum and modified [jet quenching] by the QGP they traverse
- jets are multi-scale probes [wealth of observables/properties sensitive to different QGP scales]

in-medium jet dynamics

jets in vacuum



vacuum jets under overall excellent theoretical control

- reliable baseline and template for inclusion of medium effects
- factorization of initial and final state

$$\sigma^{h_1 h_2 \rightarrow X}(p_1, p_2) = f_i^{h_1}(x_1, Q^2) \otimes f_j^{h_2}(x_2, Q^2) \otimes \sigma^{ij \rightarrow k}(x_1 p_1, x_2 p_2, Q^2) \otimes D_{k \rightarrow X}(z, Q^2)$$

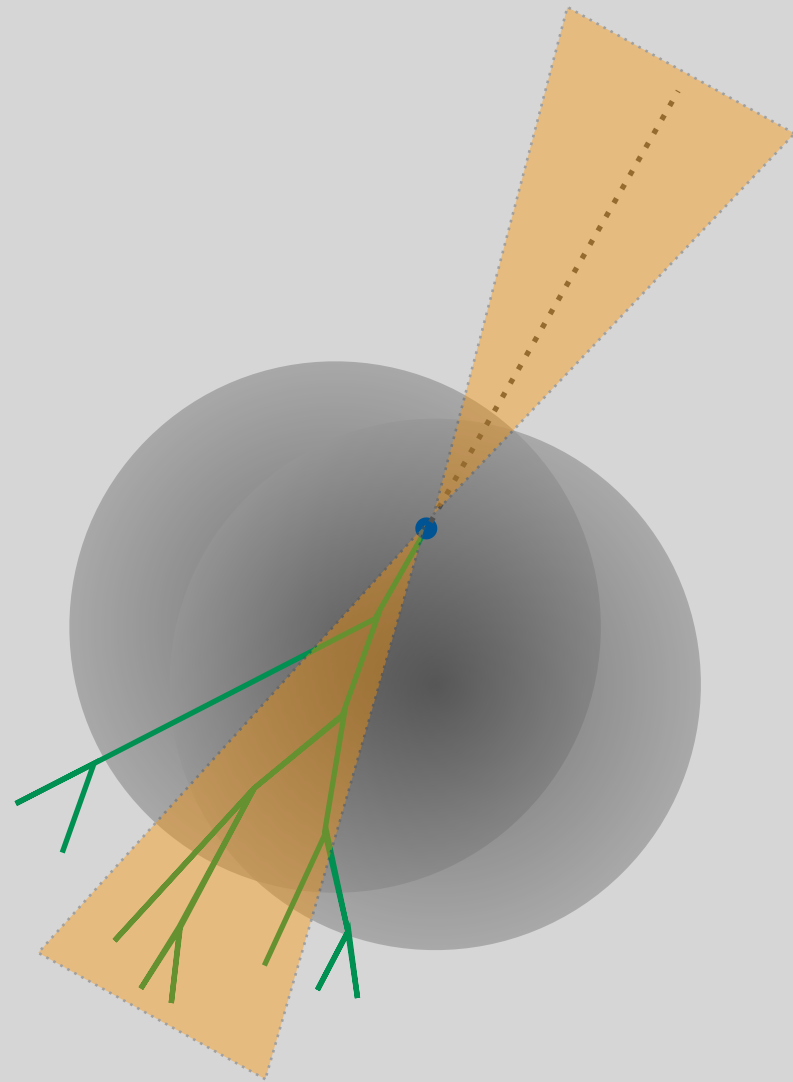
- branching pattern dictated by Altarelli-Parisi splitting functions

$$dw^{k \rightarrow l+m} = \frac{\alpha_s}{4\pi} \frac{d^2 k_{\perp}}{k_{\perp}^2} dz P_{lk}(z)$$

- AND coherence [interference] between emitters :: angular ordering [MLLA]

$$\frac{\partial}{\partial \log Q} D_i(x, Q) = \sum_j \int_x^1 \frac{dz}{z} \frac{\alpha_s(k_{\perp}^2)}{2\pi} \hat{P}_{ji}(z) D_j(x/z, zQ)$$

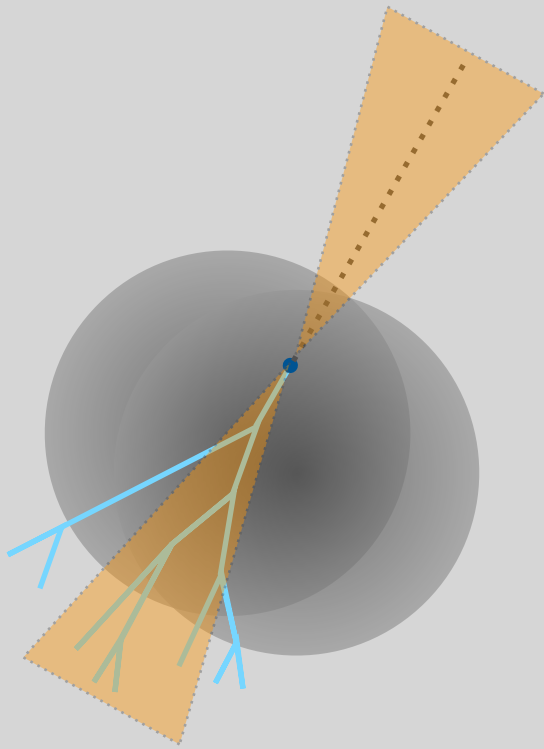
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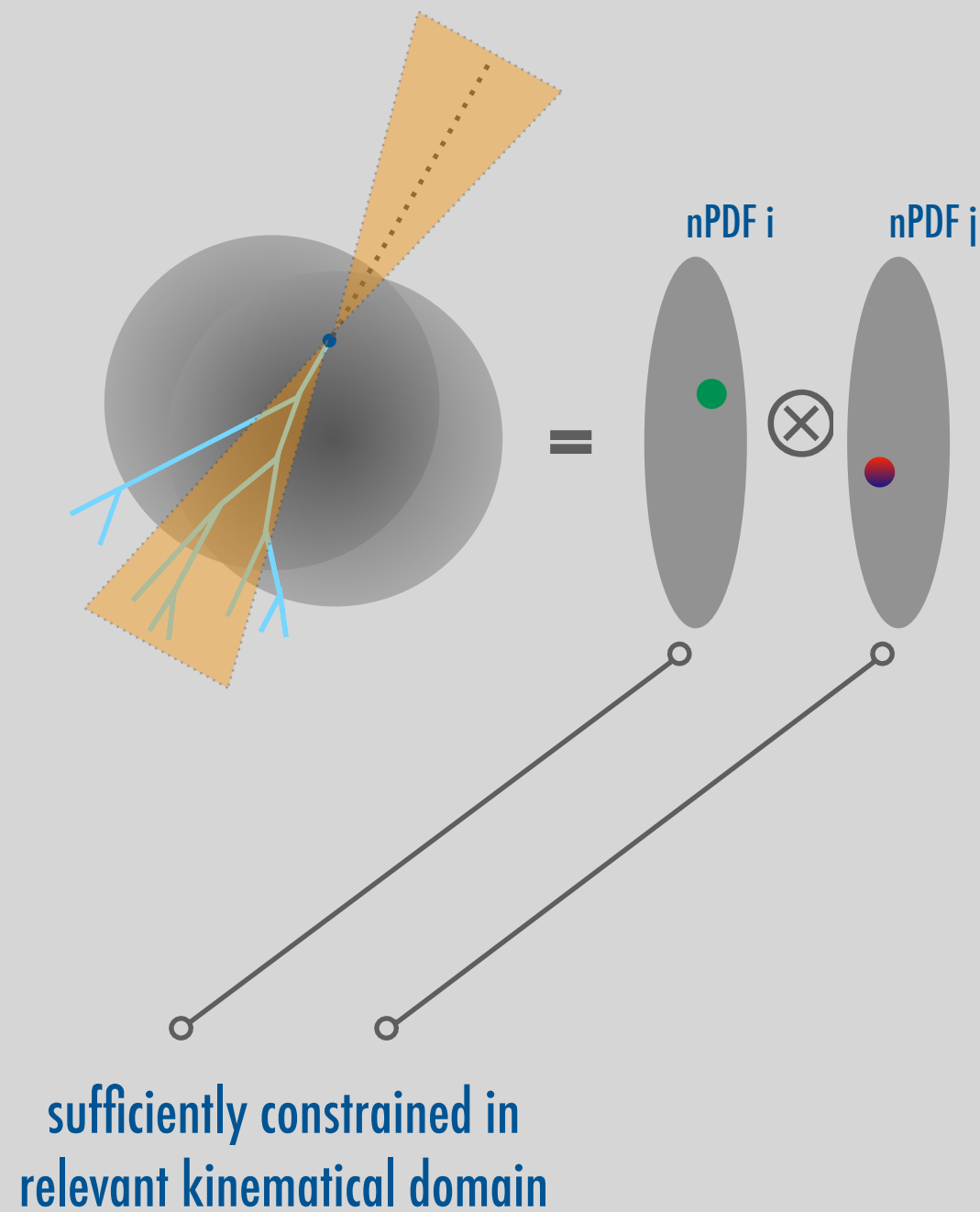
in HIC jets traverse sizable in-medium pathlength

jets in heavy ion collisions

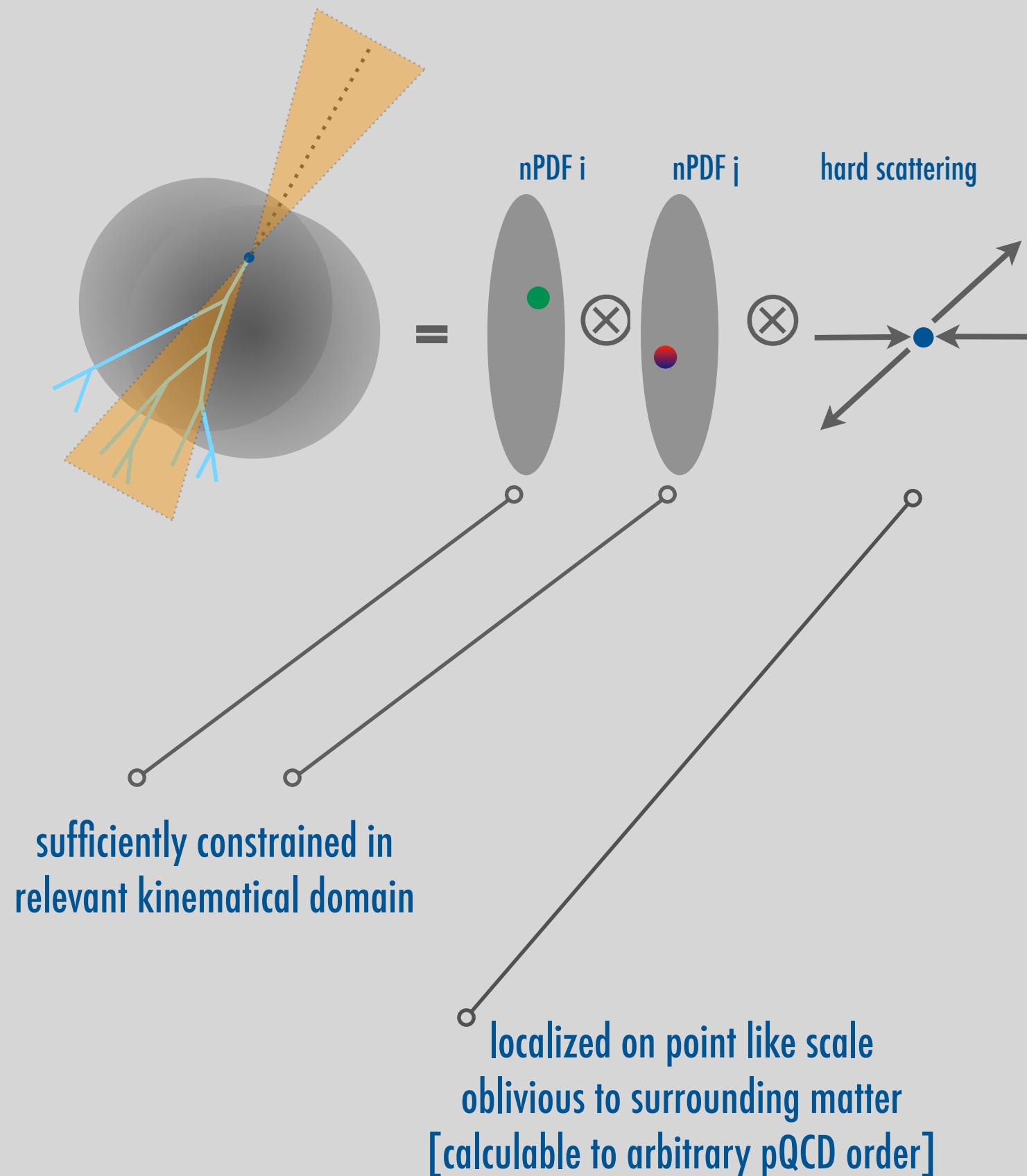
same factorizable structure [challengeable working hypothesis]



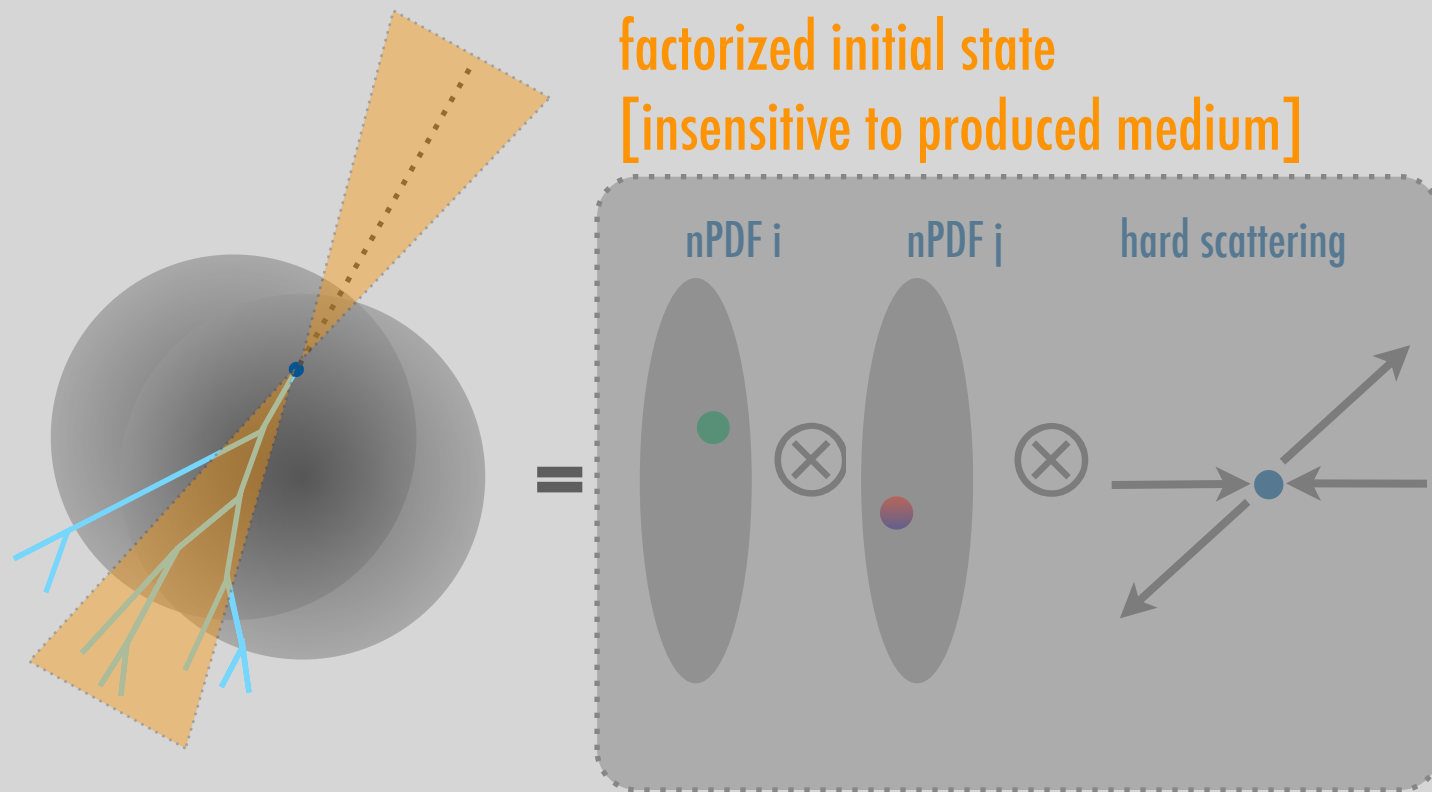
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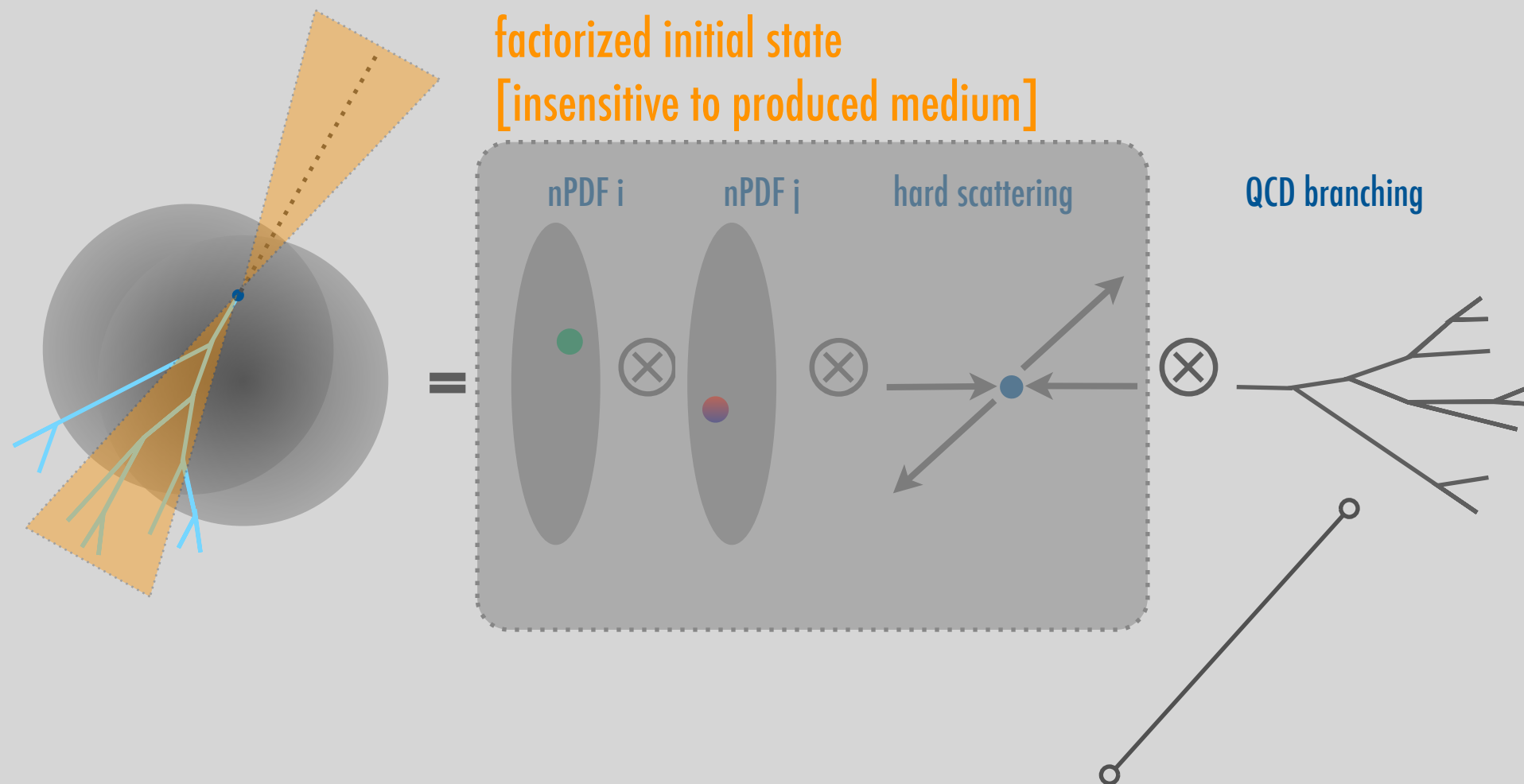
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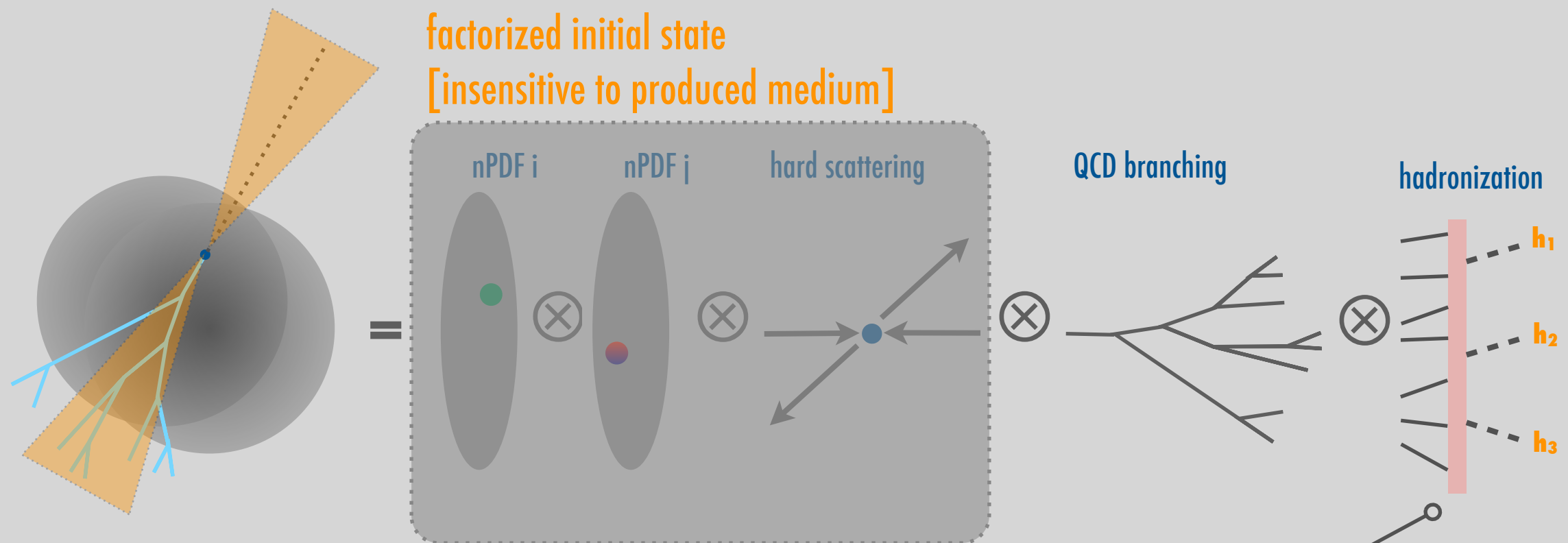
very well [and perturbatively] understood in vacuum

- coherence between successive splittings leads to angular ordering
- faithfully implemented in MC generators

medium modified

- induced radiation
- broadening of all partons traversing medium
- energy/momentum transfer to medium [elastic energy loss]
- strong modification of coherence properties
- modification of colour correlations

jets in heavy ion collisions



in vacuum

- effective description in MC [Lund strings, clusters, ...]
- FF for specific final state [jet, hadron class/species, ...]

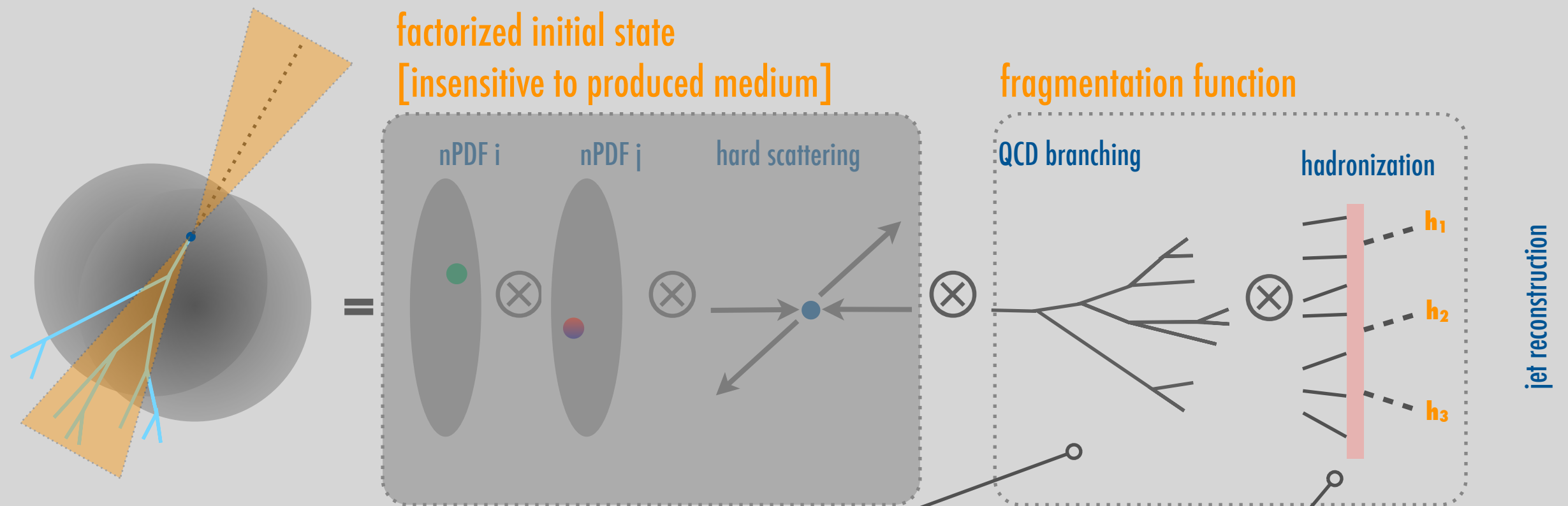
in medium

- time delayed [high enough p_T] thus outside medium
- colour correlations of hadronizing system changed

fragmentation outside medium = vacuum FFs ???

[however, many jet observables largely insensitive to hadronization]

jets in heavy ion collisions



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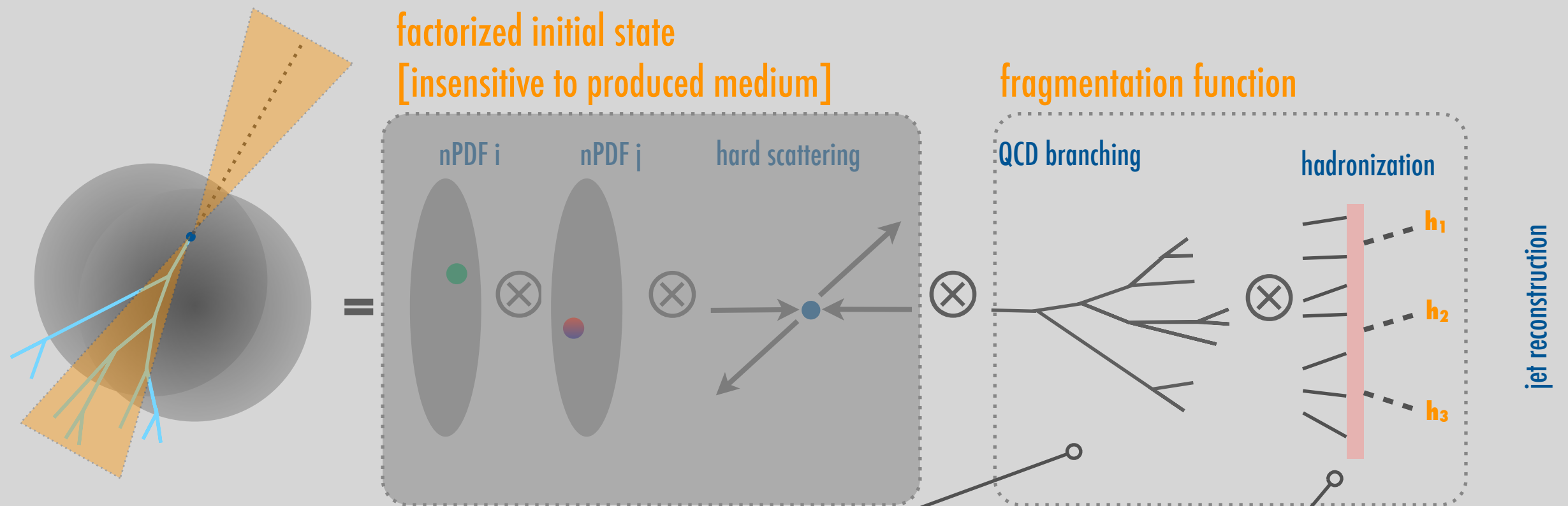
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jets in heavy ion collisions



jet quenching ::
observable consequences [in jet and jet-like hadronic observables] of the effect of the medium

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to establish **quenched jets**
as **medium probes** requires a full theoretical account of

- QCD *branching*
- *effect on hadronization [for hadrons]*

in the presence of a **generic medium**

and

a detailed assessment of the **sensitivity of observables**
to specific medium properties

:: probe ::

*physical object/process/observable under strict theoretical control
for which a definite relationship between its properties and those
of the probed system can be established*

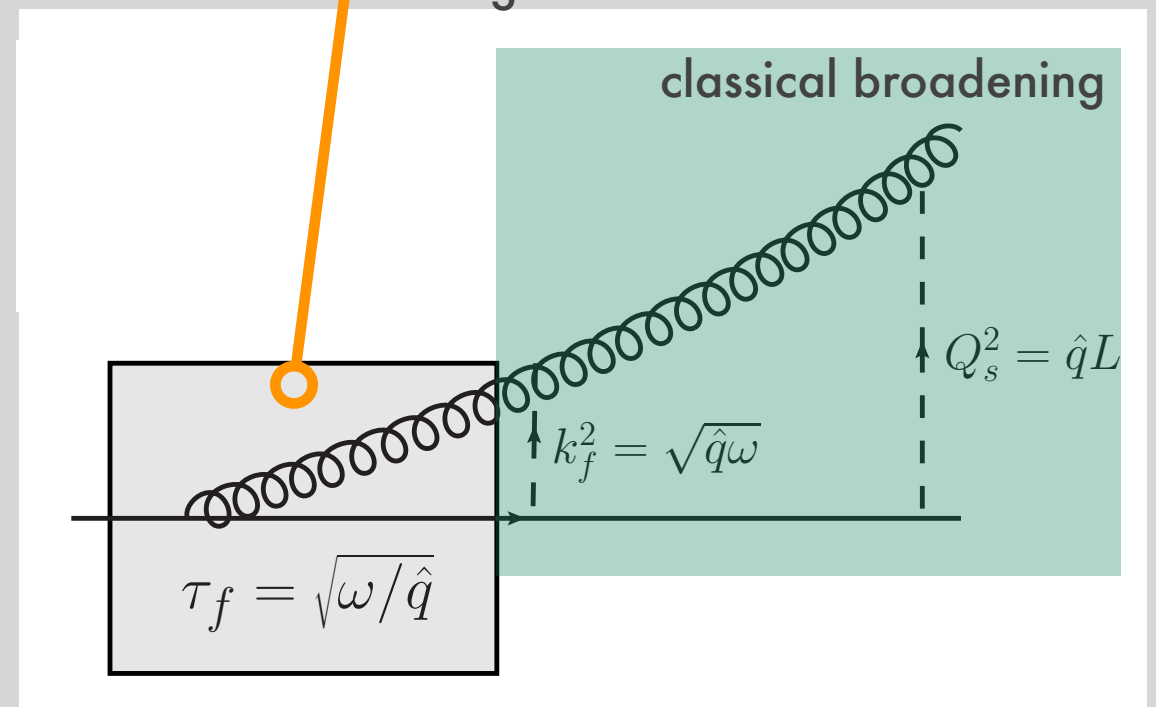
medium induced radiation and broadening

- interaction with QGP leads to enhanced splitting probability [more emissions] for each jet component [parton]
- classical [Brownian] broadening of all partons
- understood within several perturbative approaches

$$\mathcal{R}_q^{\text{med}} \approx 4\omega \int_0^L dt' \int \frac{d^2 \mathbf{k}'}{(2\pi)^2} \mathcal{P}(\mathbf{k} - \mathbf{k}', L - t') \sin\left(\frac{\mathbf{k}'^2}{2k_f^2}\right) e^{-\frac{\mathbf{k}'^2}{2k_f^2}}$$

quantum emission/broadening during formation time

$$\hat{q} \simeq \frac{\mu^2}{\lambda} \quad :: \text{transport coefficient}$$



large broadening

- in-medium formation time for small angle and soft gluons [vacuum] is very short

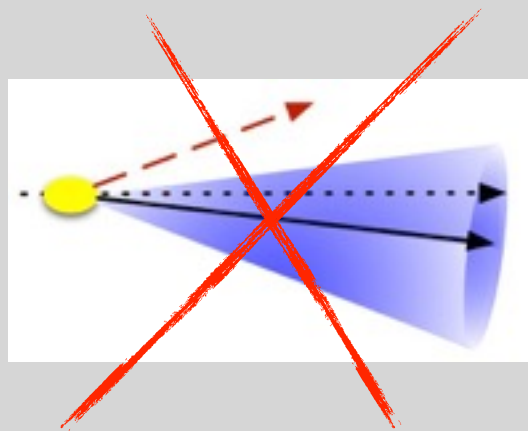
- democratic broadening is a large effect for soft partons
 - soft radiation decorrelated from jet direction/transported to large angles without disturbing back-to-back correlation
 - enhancement of soft fragments outside the jet
 - jet energy depletion driven by away transport of soft fragments NOT by rare out-of-cone semi-hard splitting

$$\tau \sim \frac{\omega}{k_{\perp}^2} \xrightarrow{\langle k_{\perp}^2 \rangle \sim \hat{q}\tau} \langle \tau \rangle \sim \sqrt{\frac{\omega}{\hat{q}}}$$

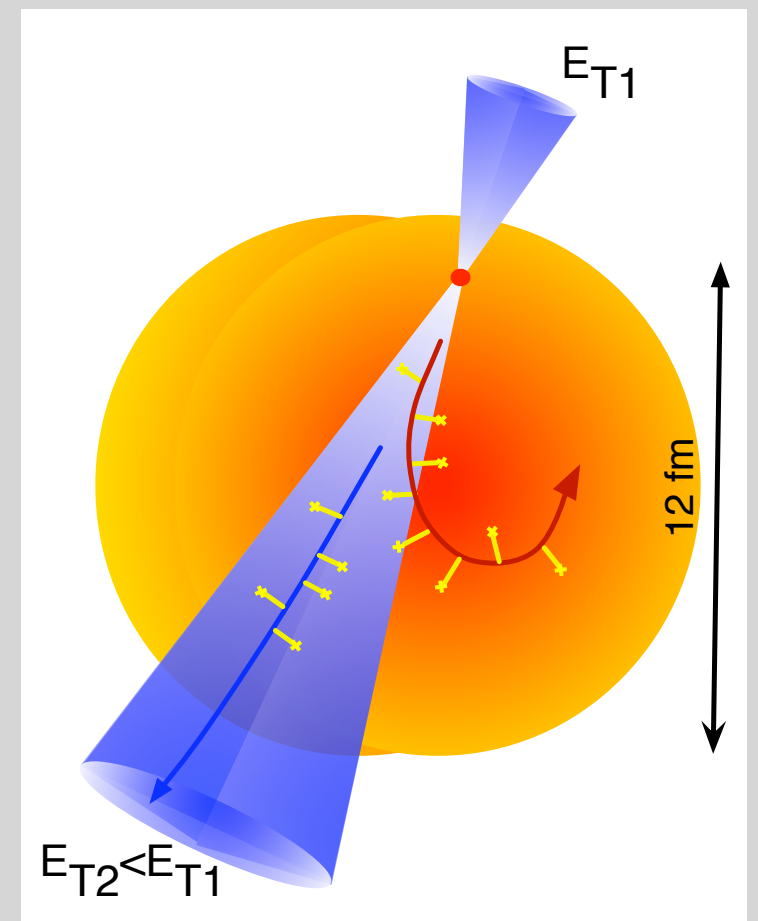
$$\langle k_{\perp} \rangle \sim \sqrt{\hat{q}L}$$

$$\omega \leq \sqrt{\hat{q}L}$$

an important lesson learnt from dijet asymmetry data



Casalderrey-Solana, Milhano, Wiedemann

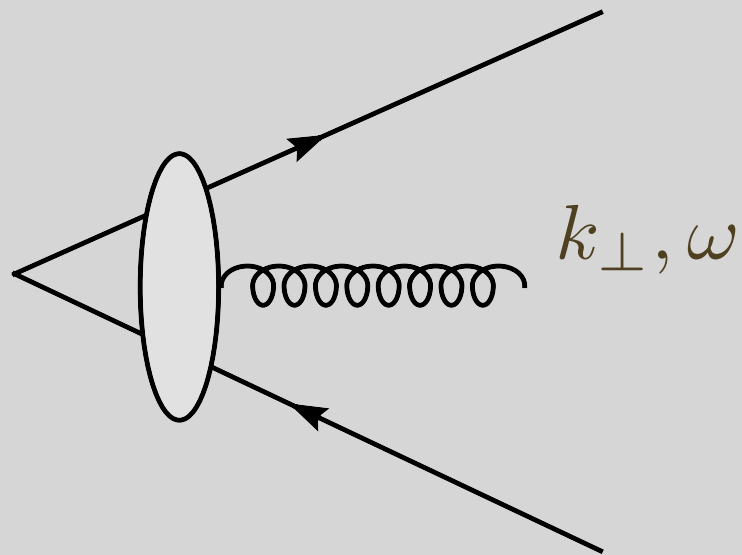


multiple emissions :: vacuum antennas

- bona fide description of multiple gluon radiation requires understanding of emitters interference pattern

multiple emissions :: vacuum antennas

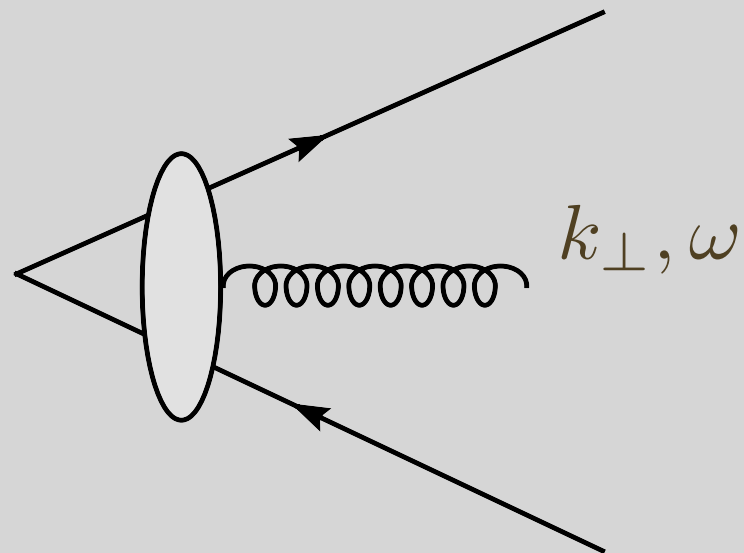
- bona fide description of multiple gluon radiation requires understanding of emitters interference pattern
- ↪ qqbar antenna [radiation much softer than both emitters] as a TH lab



multiple emissions :: vacuum antennas

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::vacuum::

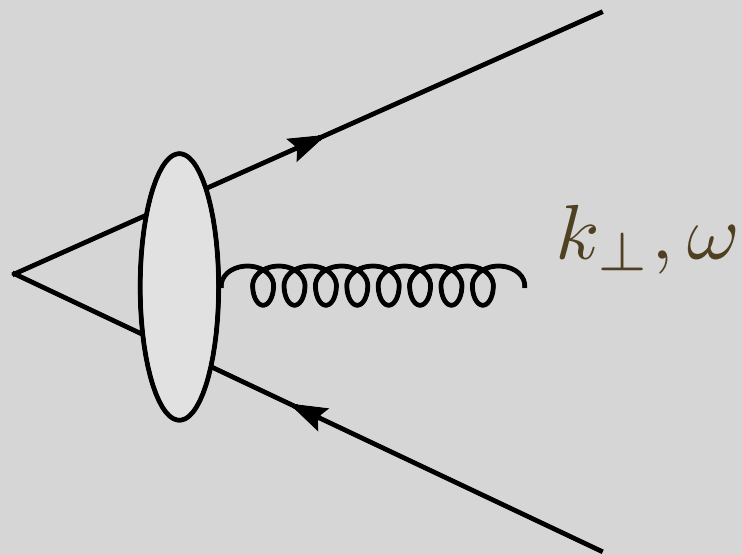
- transverse separation at formation time

$$r_{\perp} \sim \theta_{q\bar{q}} \tau_f \sim \frac{\theta_{q\bar{q}}}{\theta^2 \omega}$$

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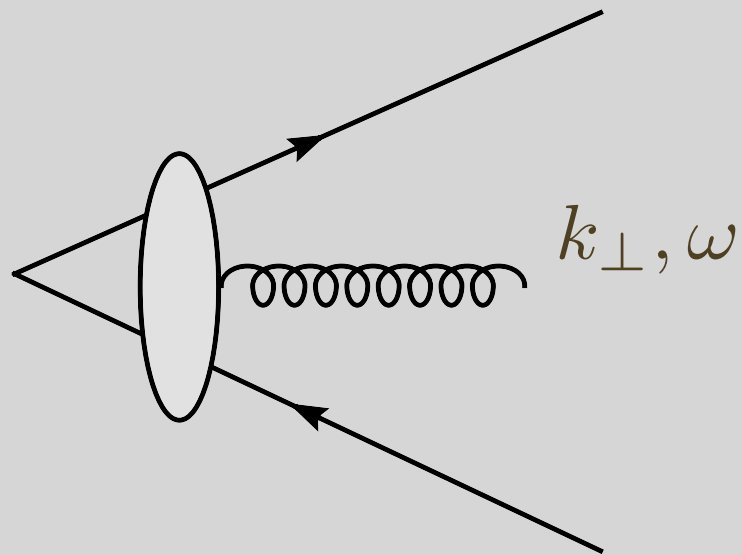
- wavelength of emitted gluon

$$\lambda_{\perp} \sim \frac{1}{k_{\perp}} \sim \frac{1}{\omega \theta}$$

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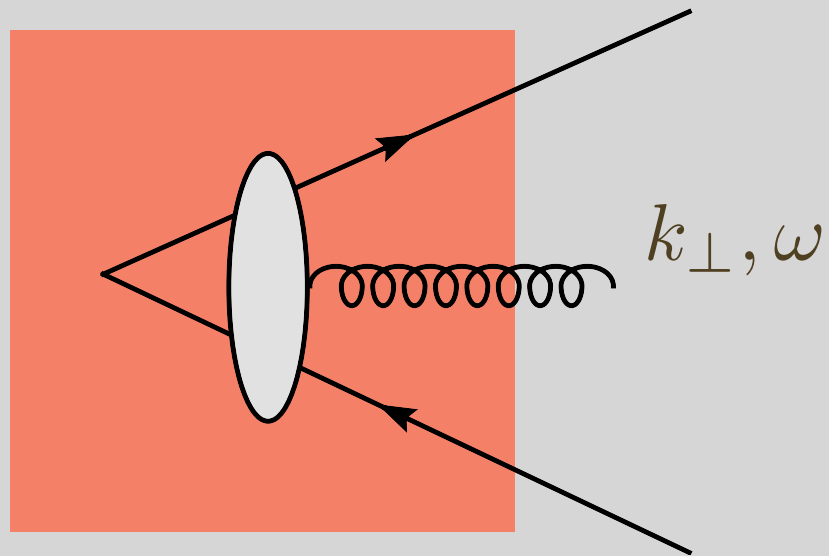
- wavelength of emitted gluon

$$\lambda_{\perp} \sim \frac{1}{k_{\perp}} \sim \frac{1}{\omega \theta}$$

for $\lambda_{\perp} > r_{\perp}$ emitted gluon cannot resolve emitters,
thus emitted coherently from total colour charge

large angle radiation suppressed :: angular ordering

medium antennas



MAJOR EFFORT

Mehtar-Tani, Salgado, Tywoniuk

Casalderrey-Solana & Iancu

Blaizot, Dominguez, Iancu, Mehtar-Tani

Mehtar-Tani, Milhano, Tywoniuk [review]

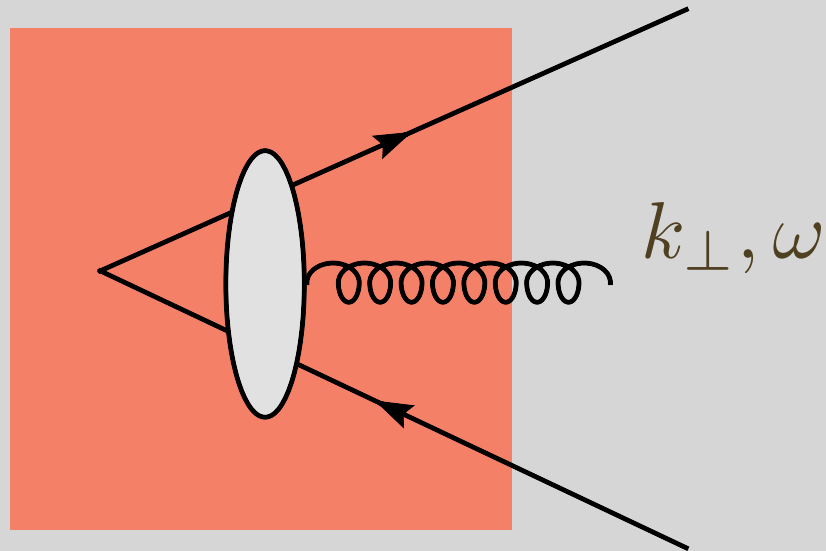
—○ new medium induced colour decorrelation scale

$$\Lambda_{med} \sim \frac{1}{k_{\perp}} \sim \frac{1}{\sqrt{\hat{q}L}}$$

—○ such that decorrelation driven by timescale

$$\tau_d \sim \left(\frac{1}{\hat{q}\theta_{q\bar{q}}^2} \right)^{1/3}$$

[de]coherence of multiple emissions



- qqbar colour coherence survival probability

$$\Delta_{med} = 1 - \exp \left\{ - \frac{1}{12} \hat{q} \theta_{q\bar{q}}^2 t^3 \right\} = 1 - \exp \left\{ - \frac{1}{12} \frac{r_{\perp}^2}{\Lambda_{med}^2} \right\}$$

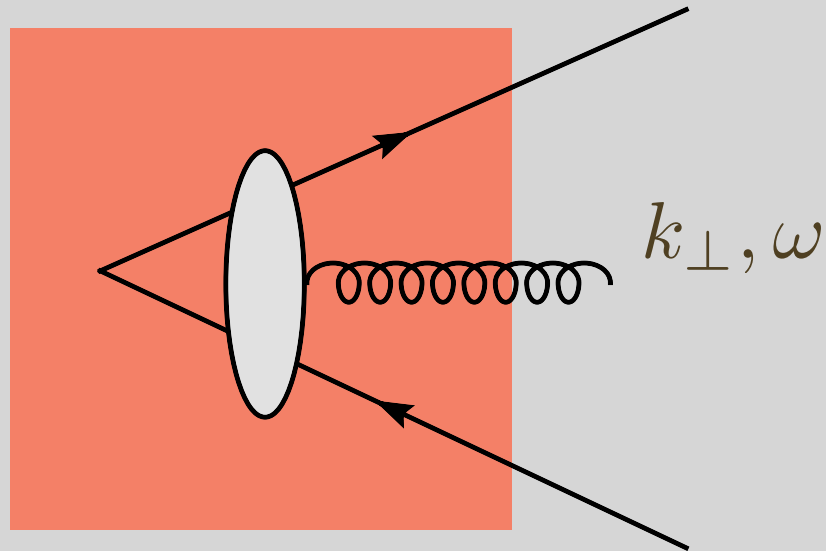
- time scale for decoherence

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- total decoherence when $L > \tau_d$

↪ colour decoherence opens up phase space for emission

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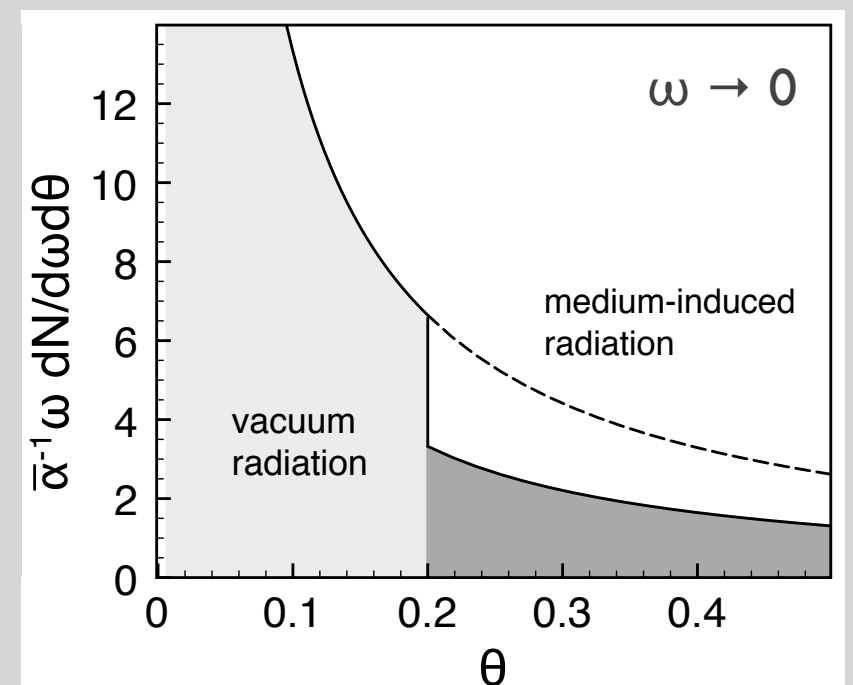
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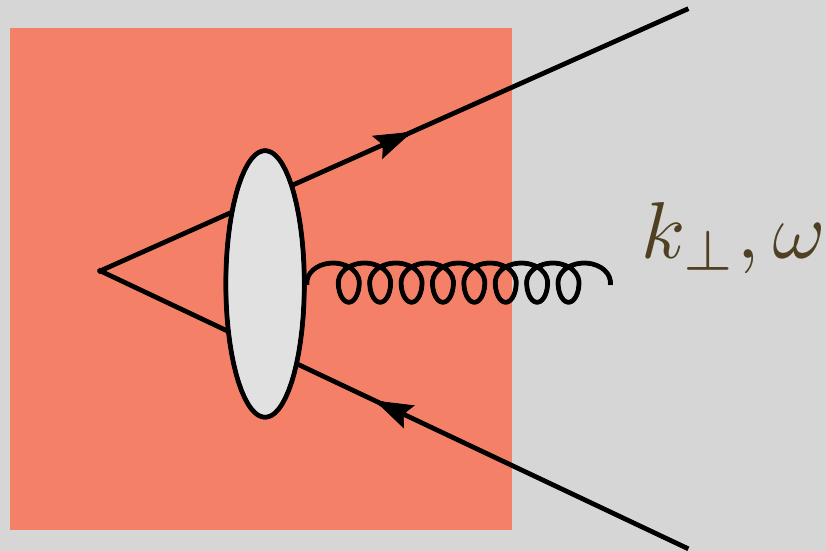
→ colour decoherence opens up phase space for emission

- large angle radiation [anti-angular ordering]
- geometrical separation [in soft limit]

$$dN_{q,\gamma^*}^{\text{tot}} = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{\sin \theta}{1 - \cos \theta} \left[\Theta(\cos \theta - \cos \theta_{q\bar{q}}) - \Delta_{med} \Theta(\cos \theta_{q\bar{q}} - \cos \theta) \right]$$



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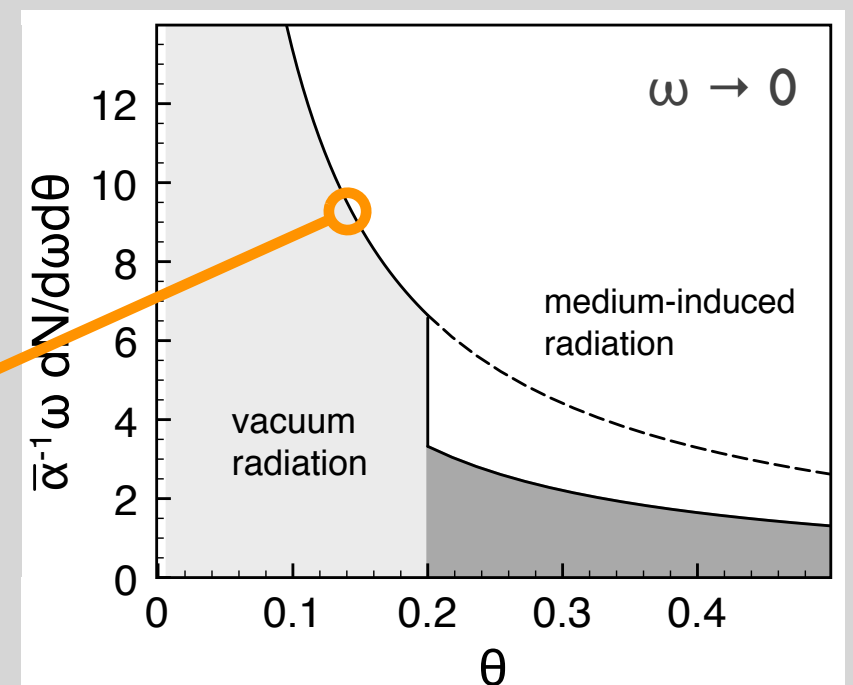
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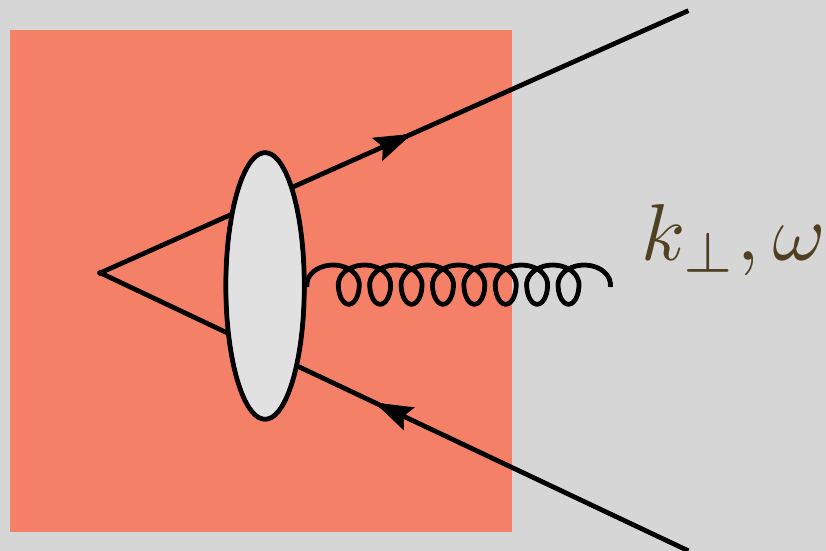
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$$\Delta_{med} \rightarrow 0$$

coherence



[de]coherence of multiple emissions



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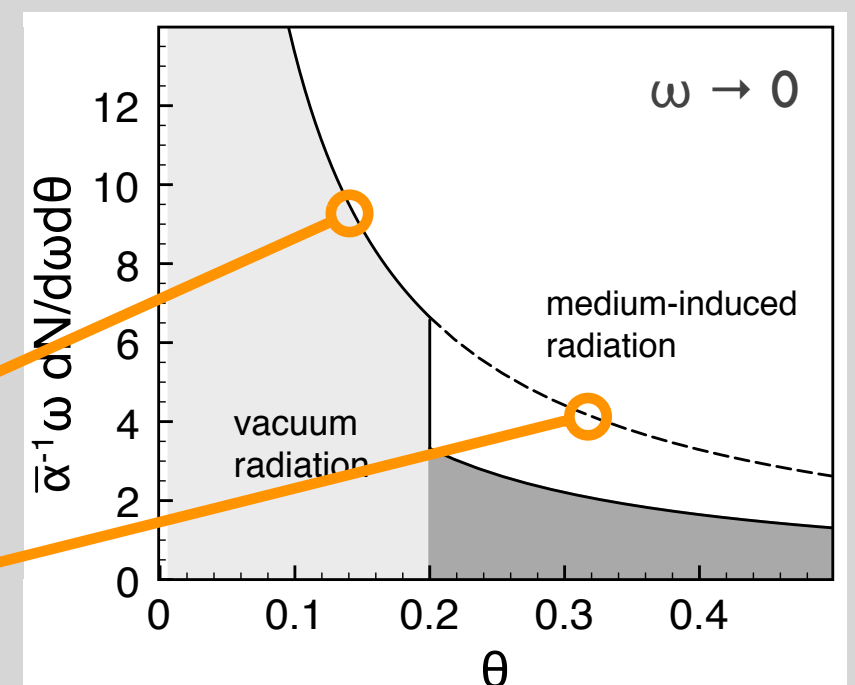
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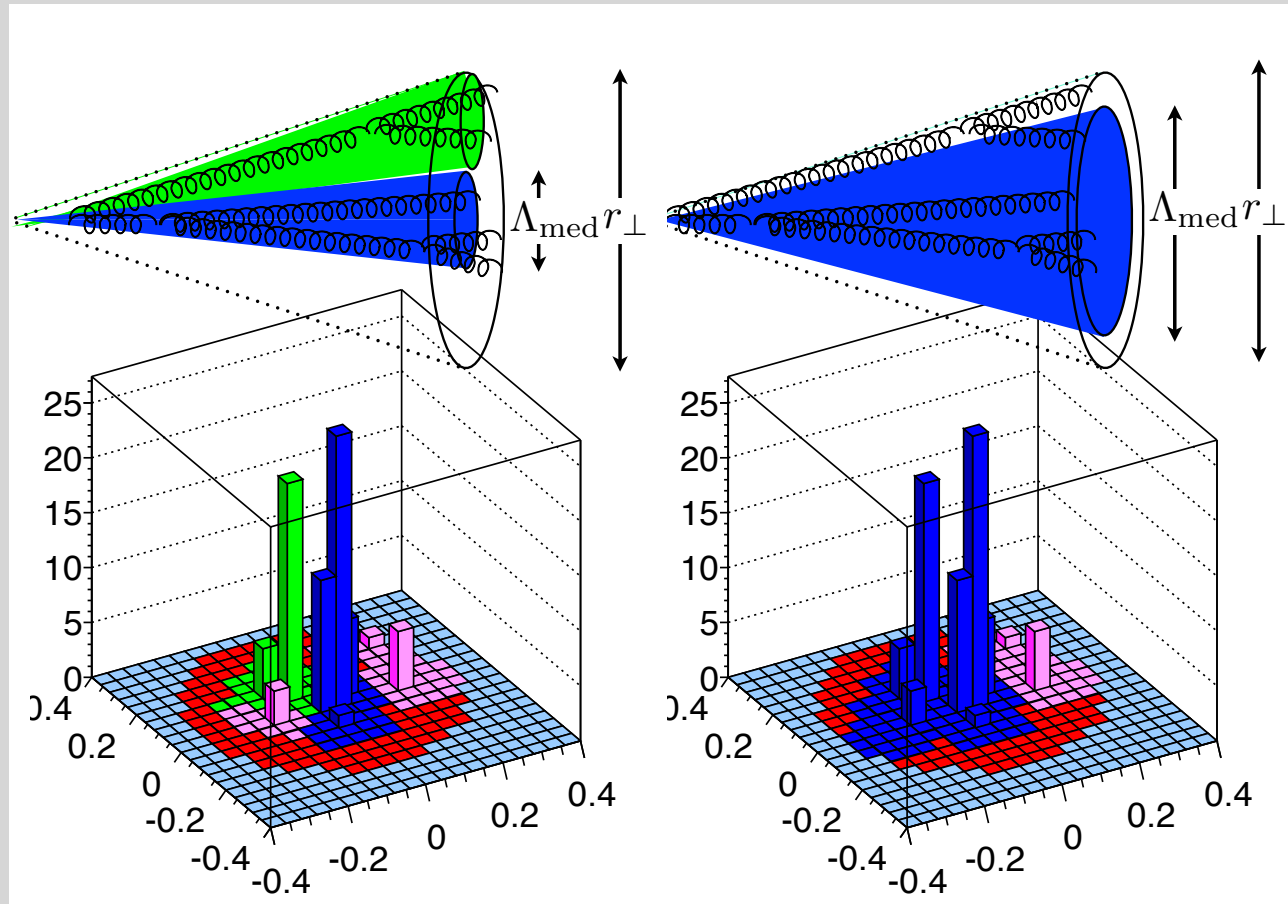
$$\Delta_{med} \rightarrow 1$$

decoherence



from antennas to jets

Casalderrey, Mehtar-Tani, Salgado, Tywoniuk

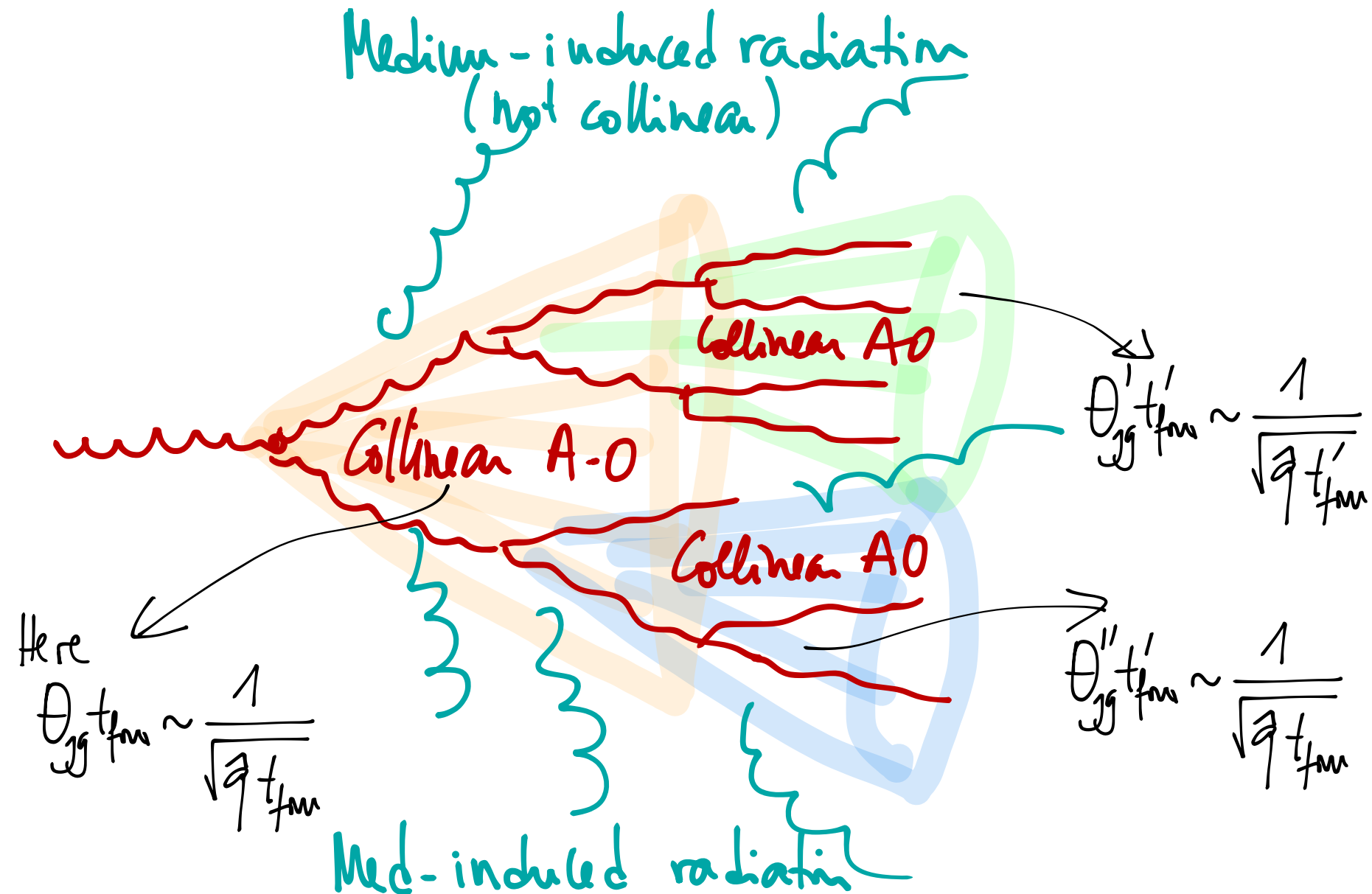


— $r_t < \Lambda_{\text{med}}$:: antenna unresolved by medium :: vacuum like

— $r_t > \Lambda_{\text{med}}$:: medium probes antenna :: strong suppression of interference :: independent radiation from each constituent

— in-medium jet dynamics driven by number of resolved charges

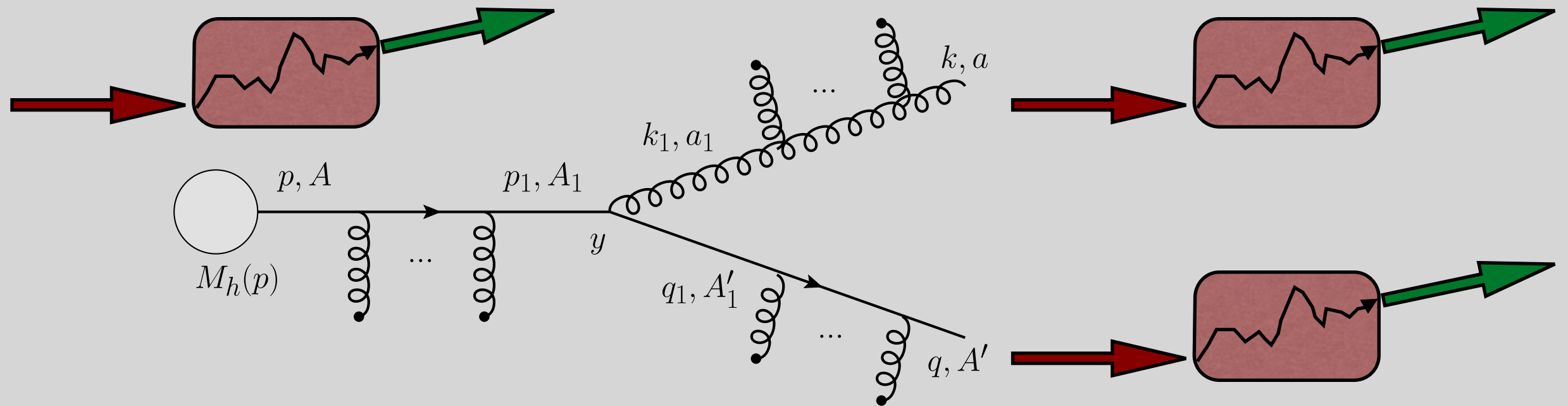
from antennas to jets



beyond antennas [full in-medium jet calculus]

Apolinário, Armesto, Milhano, Salgado
Blaizot, Dominguez, Iancu, Mehtar-Tani

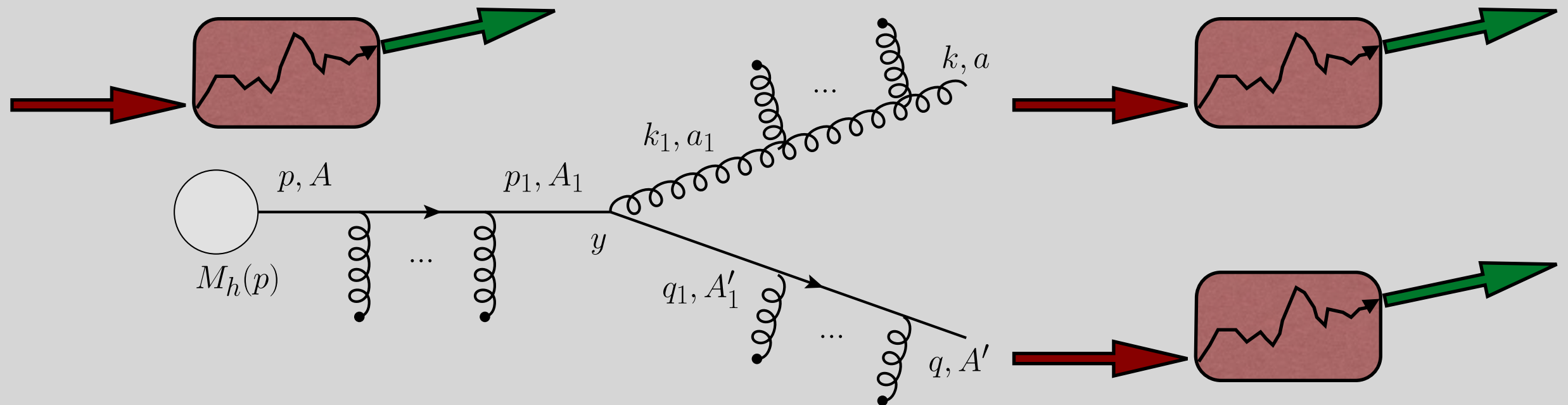
- compute in-medium splitting vertices for arbitrary momentum fraction of radiation



beyond antennas [full in-medium jet calculus]

Apolinário, Armesto, Milhano, Salgado
Blaizot, Dominguez, Iancu, Mehtar-Tani

- compute in-medium splitting vertices for arbitrary momentum fraction of radiation



- general decoherence features survive [just more complicated]
- in short formation time limit [equivalently infinite medium] full evolution equation derived :: not valid close to medium edge

life story of an in-medium jet

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- *prior to medium formation [$\tau^{\text{med}} \sim 0.1 \text{ fm}$]*
 - *hard skeleton defined [3-jet rates, hard frag, ...]*
 - *effect of Glasma ?*

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- *during medium traversal [$\sim \text{few fm}$] :: modification of formation times*
 - *enhanced [mostly soft] radiation*
 - *broadening [large for very soft]*
 - *breakdown of colour coherence*
 - *modification of colour correlations*
 - *E-p transfer to medium*

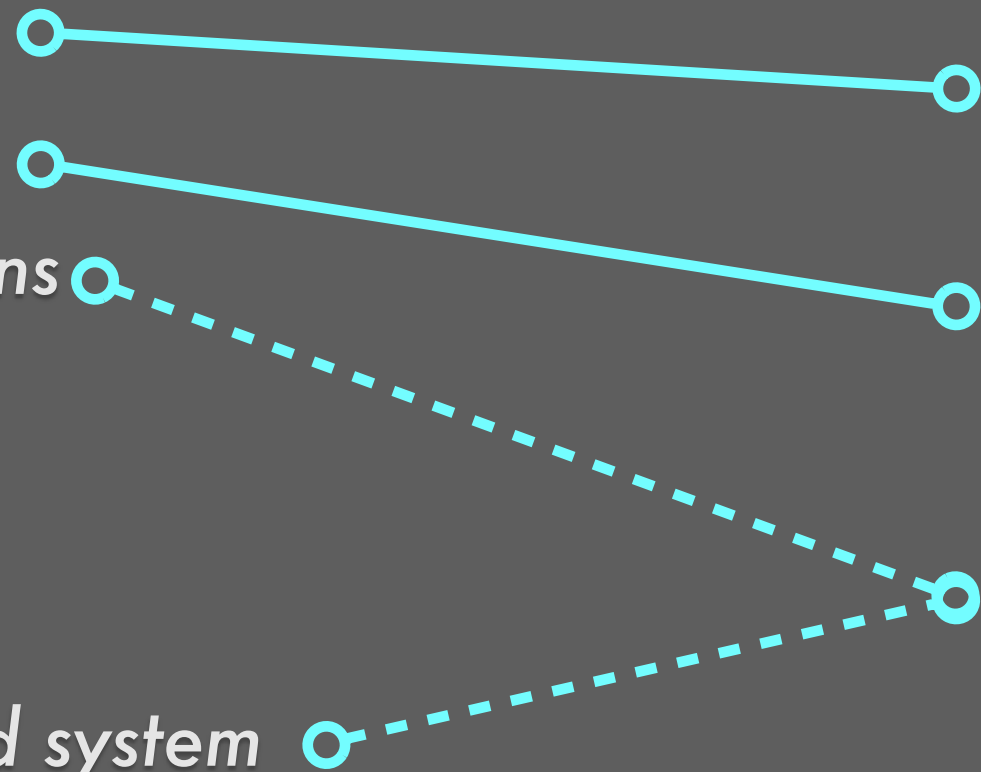
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 - *E-p transfer to medium*
- *after medium escape*
 - *vacuum branching*
 - *hadronization of colour modified system*

life story of an in-medium jet

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soft components at large angles



life story of an in-medium jet

very appealing pQCD based overall picture

BUT

the QGP is strongly coupled and its collective behaviour [flows] suggestive of the non-existence of scattering centres [quasi-particles]

still, parton branching is a perturbative process

are there quasi-particles ?

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—○ do hard probes have finite mean free paths?

↪ all pQCD based approaches assume so

↪ in AdS/CFT [strong coupling] constructions

- heavy quarks propagate without mean free path :: lost energy goes into Mach cone and wake
- light quarks/jets propagate towards thermalization :: no collinear structure [hedgehog jets]

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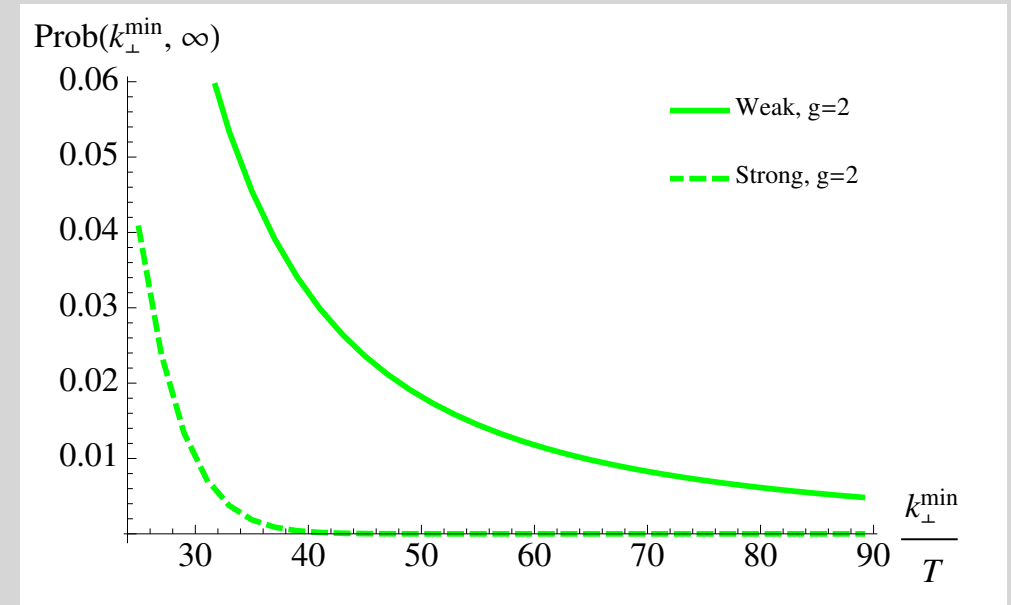
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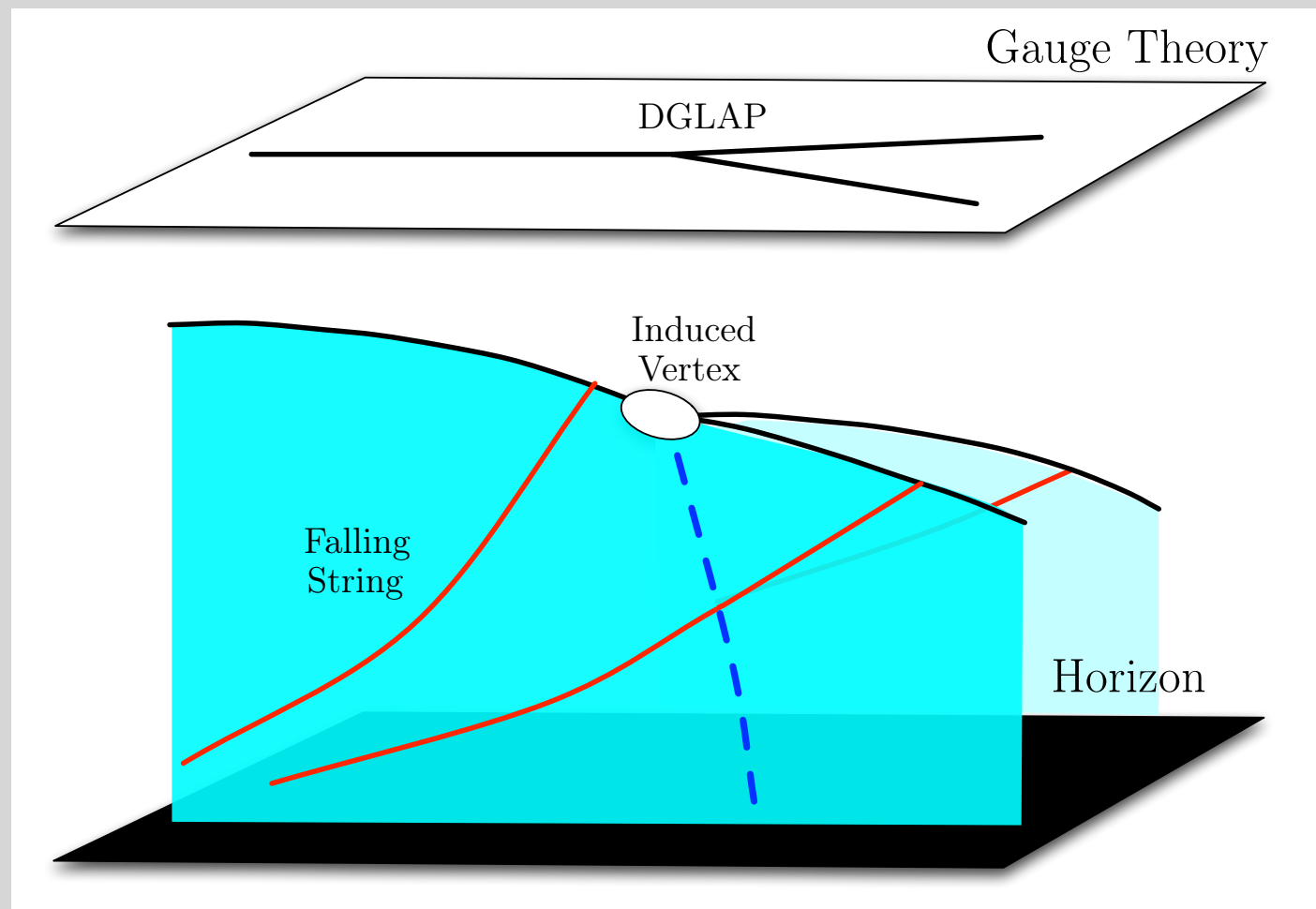
—○ probability of large broadening larger for pQCD [$\sim 1/k_{\perp}^4$] than for strong coupled [gaussian]

↪ rare, yet unmeasured, but measurable events



hybrid strong/weak coupling model

Can Gulan, Casalderrey-Solana, Milhano, Pablos, Rajagopal

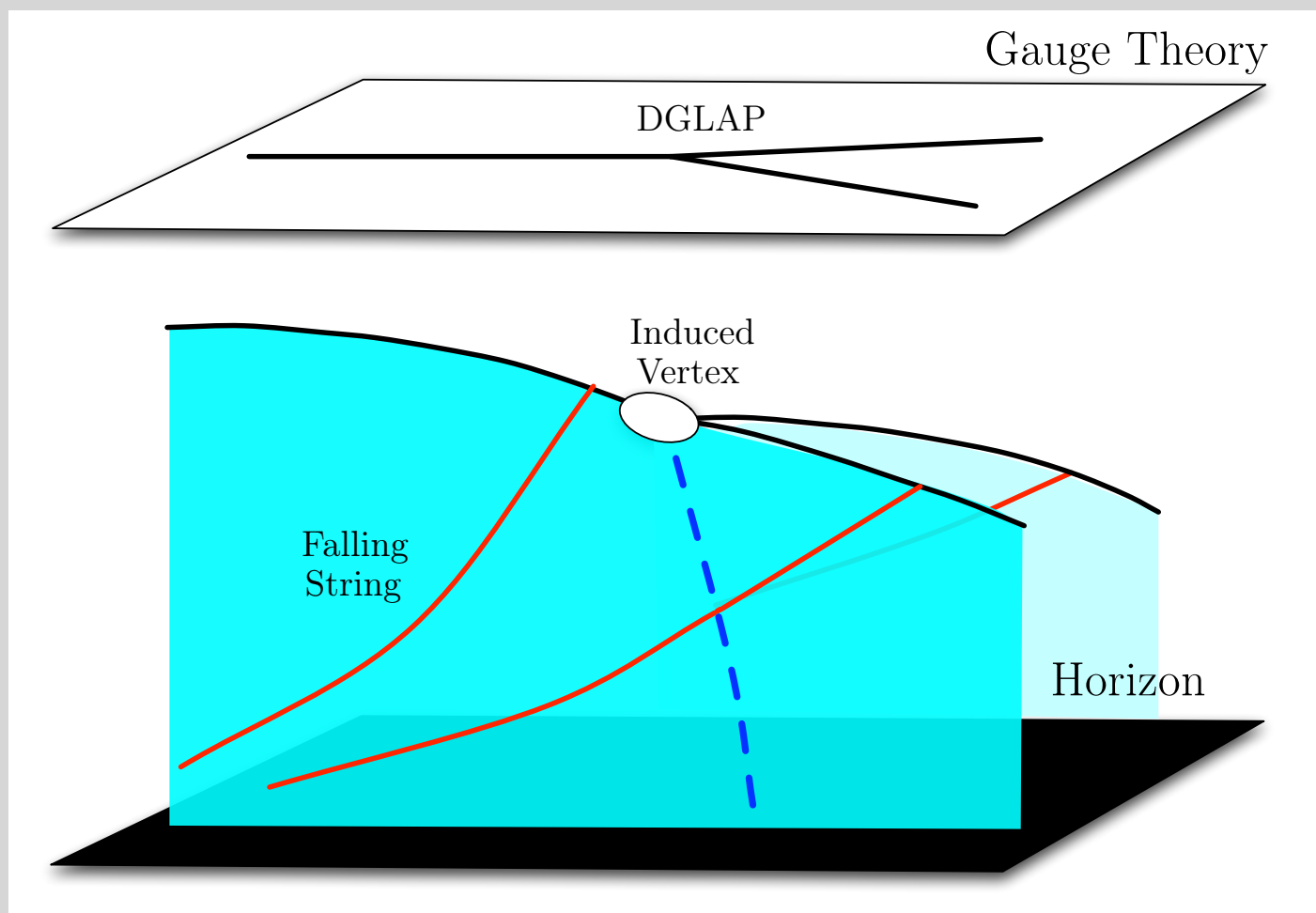


$$\left. \frac{dE}{dx} \right|_{\text{strongly coupled}} = -\frac{4}{\pi} E_{\text{in}} \frac{x^2}{x_{\text{stop}}^2} \frac{1}{\sqrt{x_{\text{stop}}^2 - x^2}}, \quad x_{\text{stop}} = \frac{1}{2\kappa_{\text{sc}}} \frac{E_{\text{in}}^{1/3}}{T^{4/3}}$$

single free parameter
[accounts for QCD/N=4 SYM differences]

hybrid strong/weak coupling model

Can Gulan, Casalderrey-Solana, Milhano, Pablos, Rajagopal



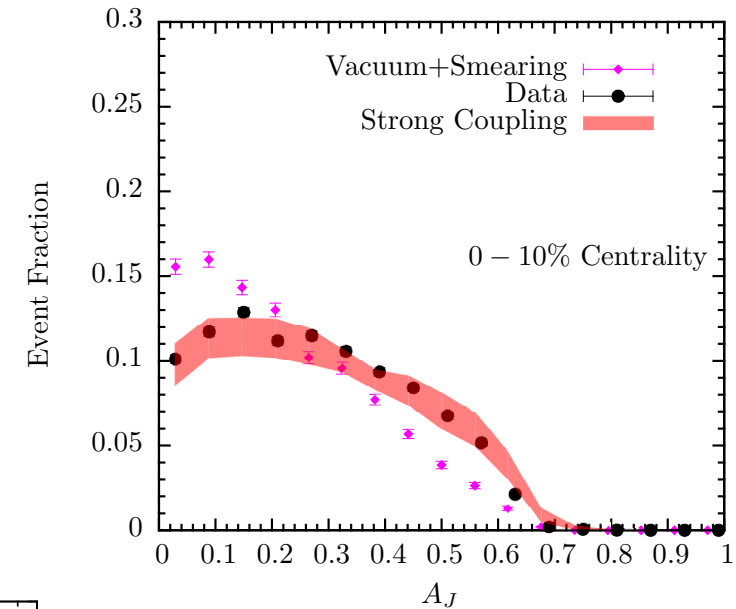
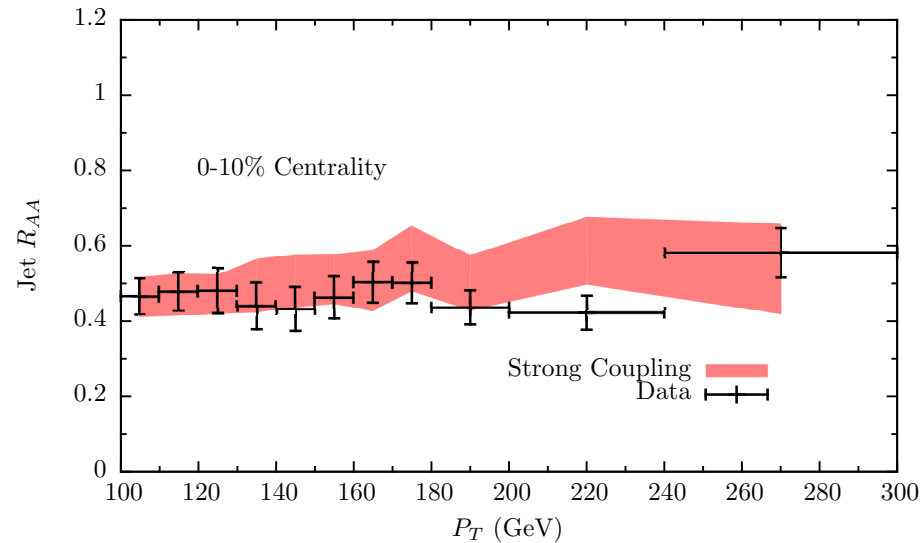
- vacuum jets [no medium induced radiation] where each parton loses energy non-perturbatively [as given by a holographic AdS-CFT calculation]

$$\left. \frac{dE}{dx} \right|_{\text{strongly coupled}} = -\frac{4}{\pi} E_{\text{in}} \frac{x^2}{x_{\text{stop}}^2} \frac{1}{\sqrt{x_{\text{stop}}^2 - x^2}}, \quad x_{\text{stop}} = \frac{1}{2\kappa_{\text{sc}}} \frac{E_{\text{in}}^{1/3}}{T^{4/3}}$$

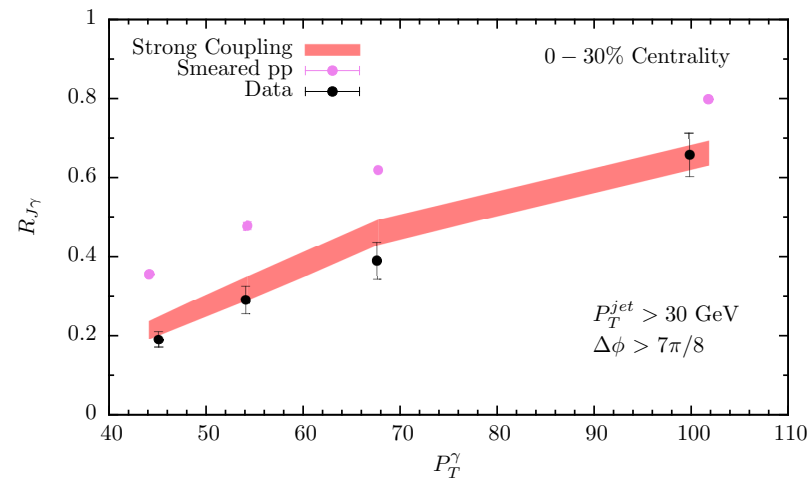
single free parameter
[accounts for QCD/N=4 SYM differences]

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5 observables
and centrality dependence
all described with
single parameter

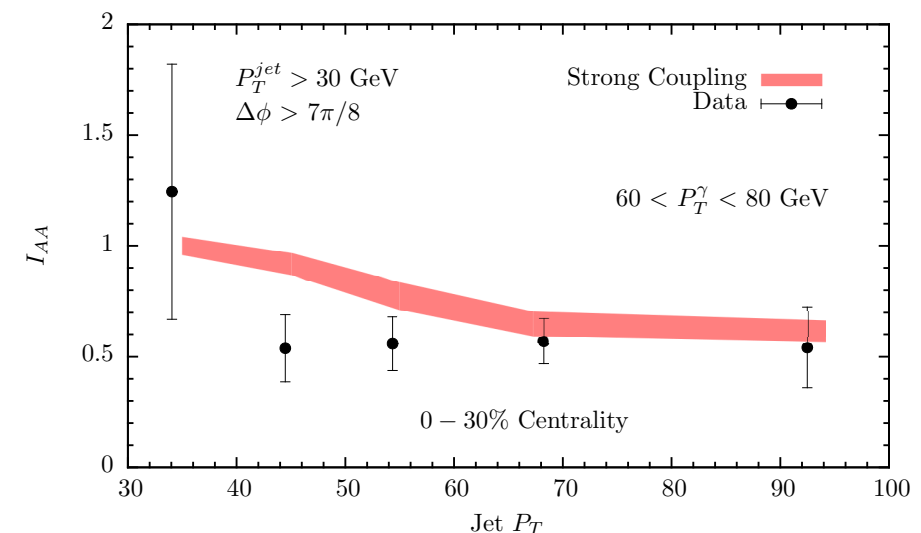
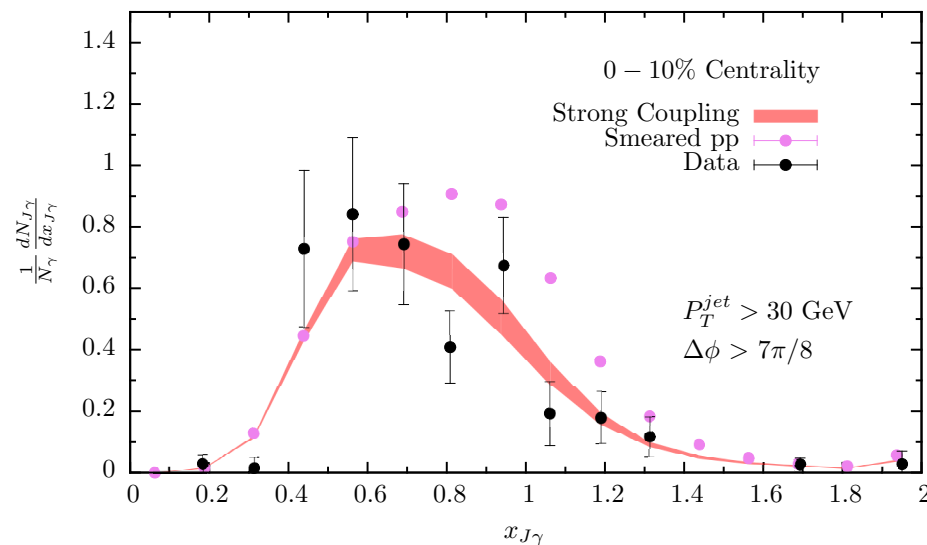


Bands in all plots correspond to

$$0.32 < \kappa_{sc} < 0.41$$

$\mathcal{O}(1)$ as expected.

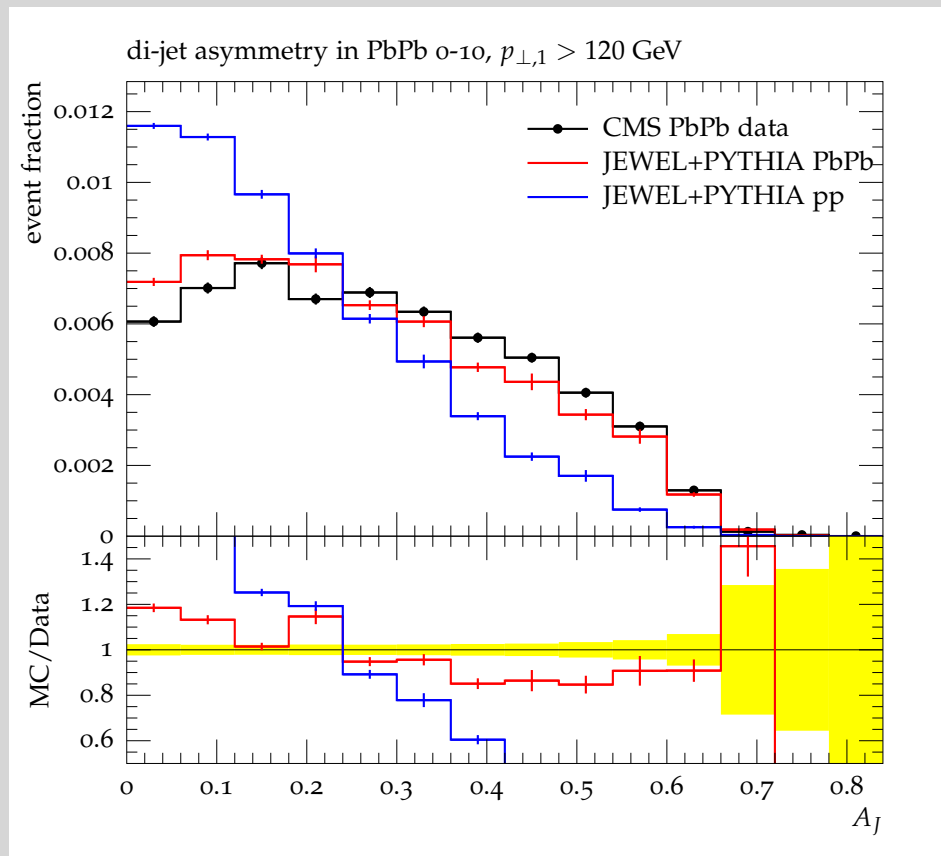
$$x_{stop}^{QCD} \sim (2 - 3)x_{stop}^{\mathcal{N}=4}$$



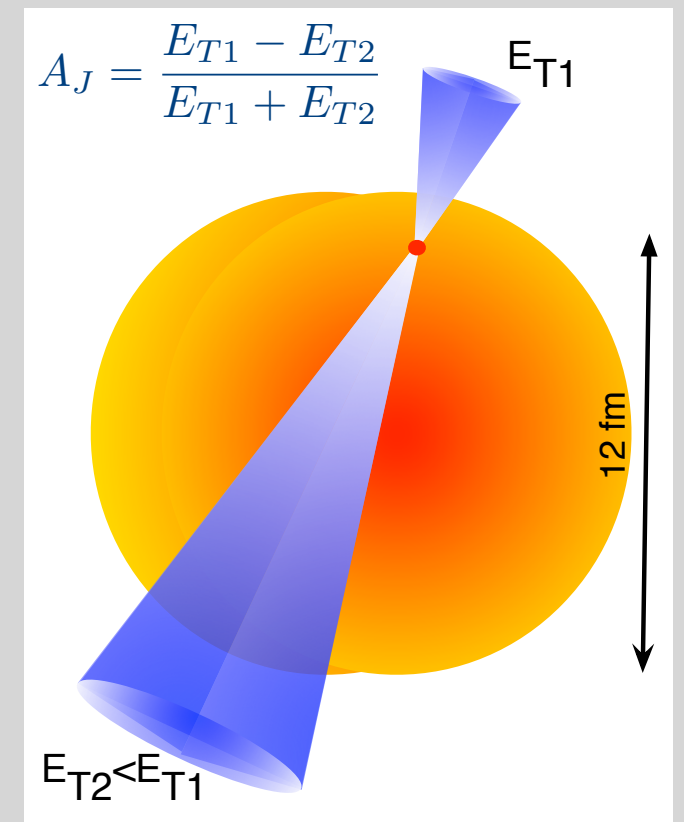
understanding sensitivity
[a non-trivial example towards a new era]

dijet asymmetry

Milhano, Zapp

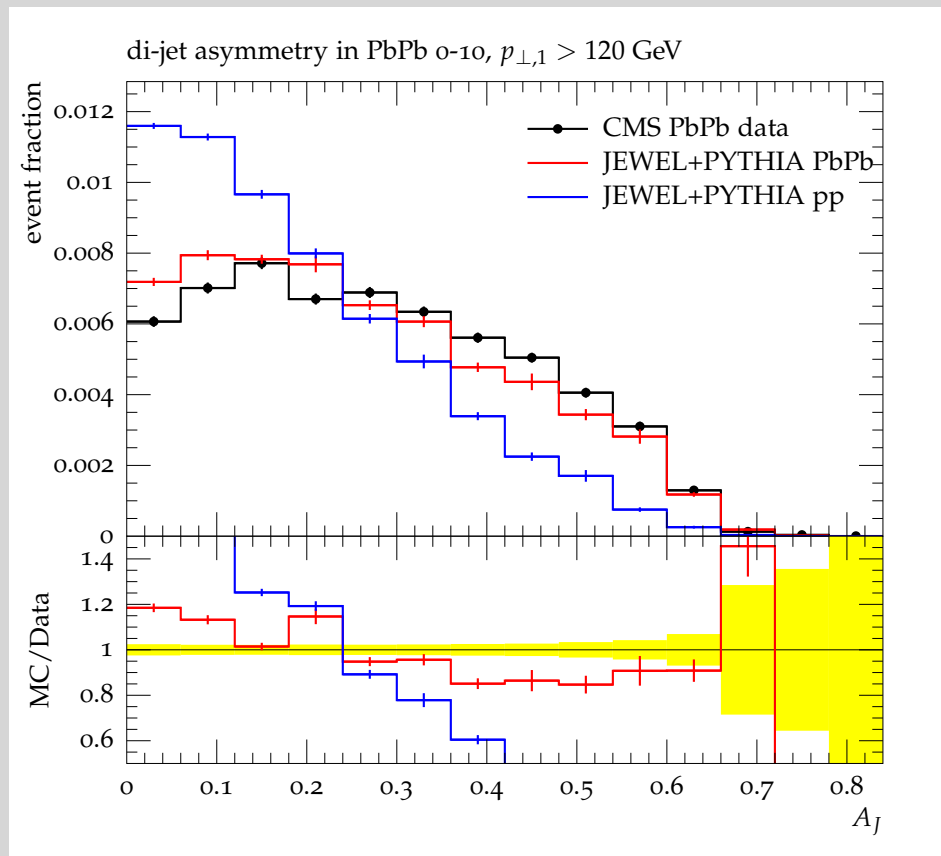


*imbalance of jet energy within a cone of radius R for
'back-to-back' di-jets*

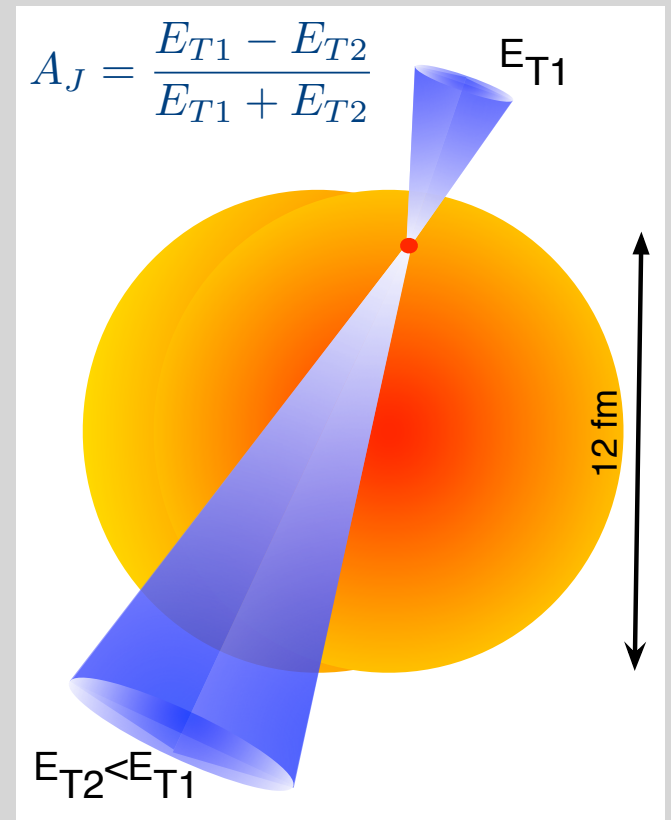
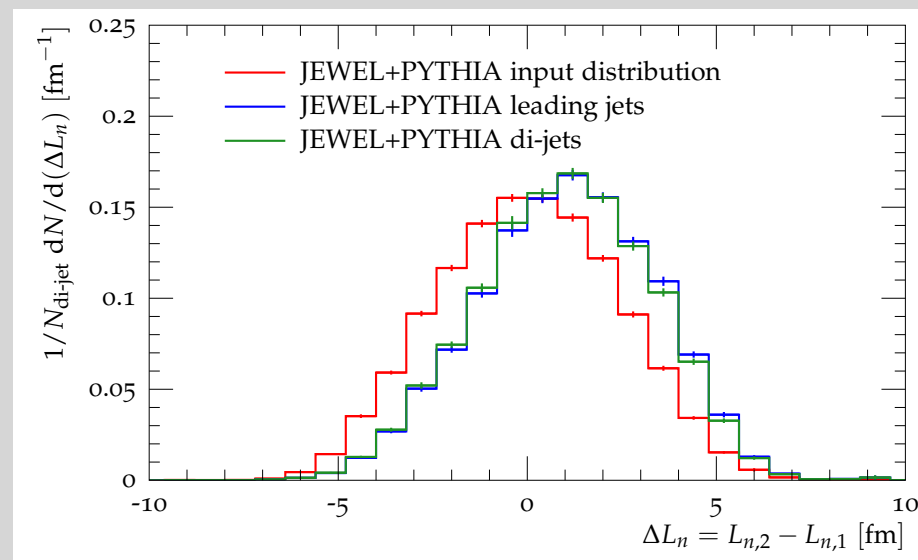


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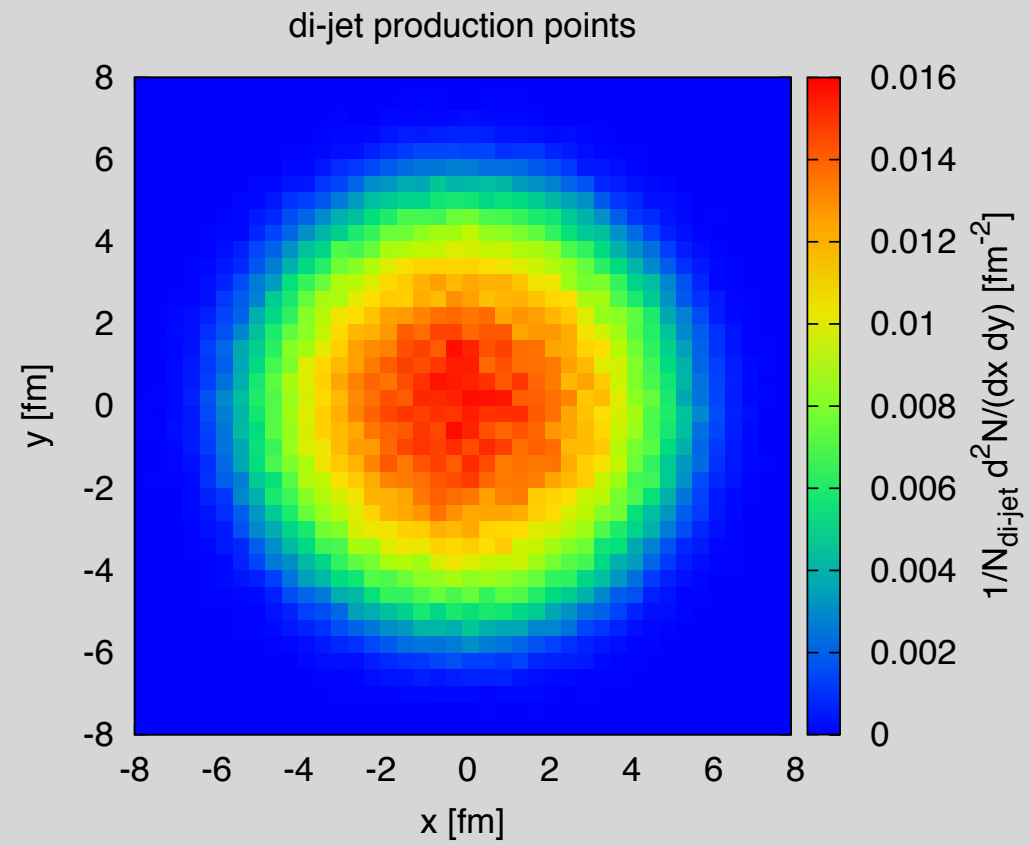


—○— most naive guess :: medium-induced asymmetry is sensitive to difference in traversed QGP by leading and recoiling jets



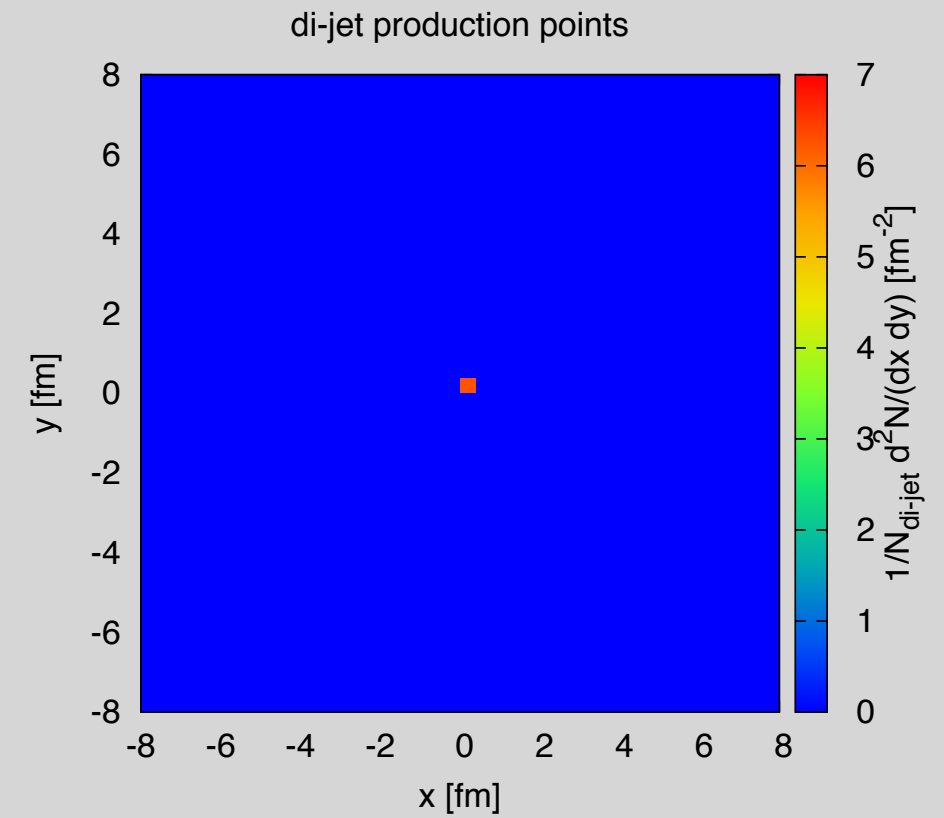
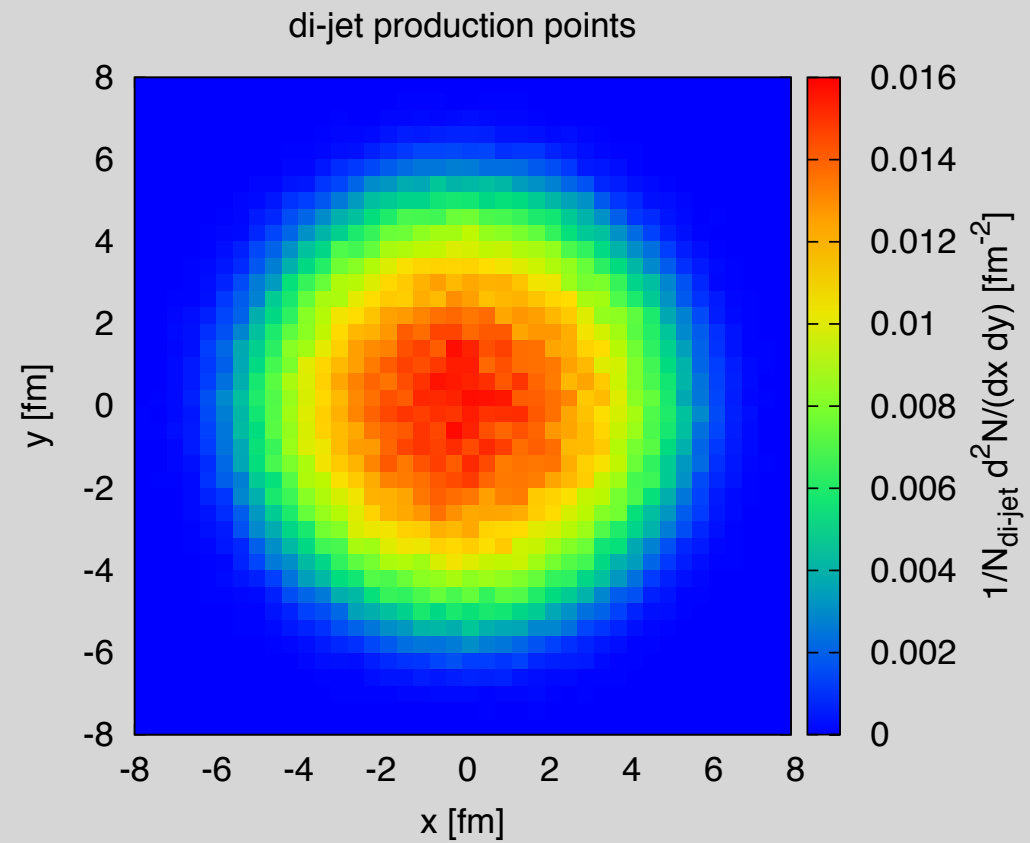
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a sanity check



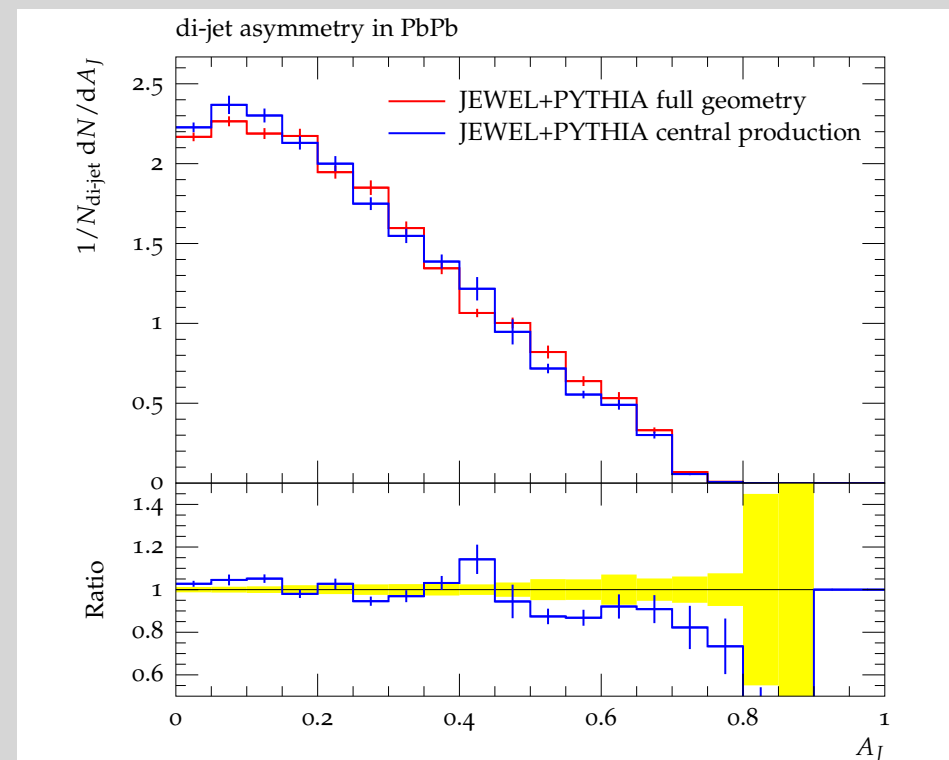
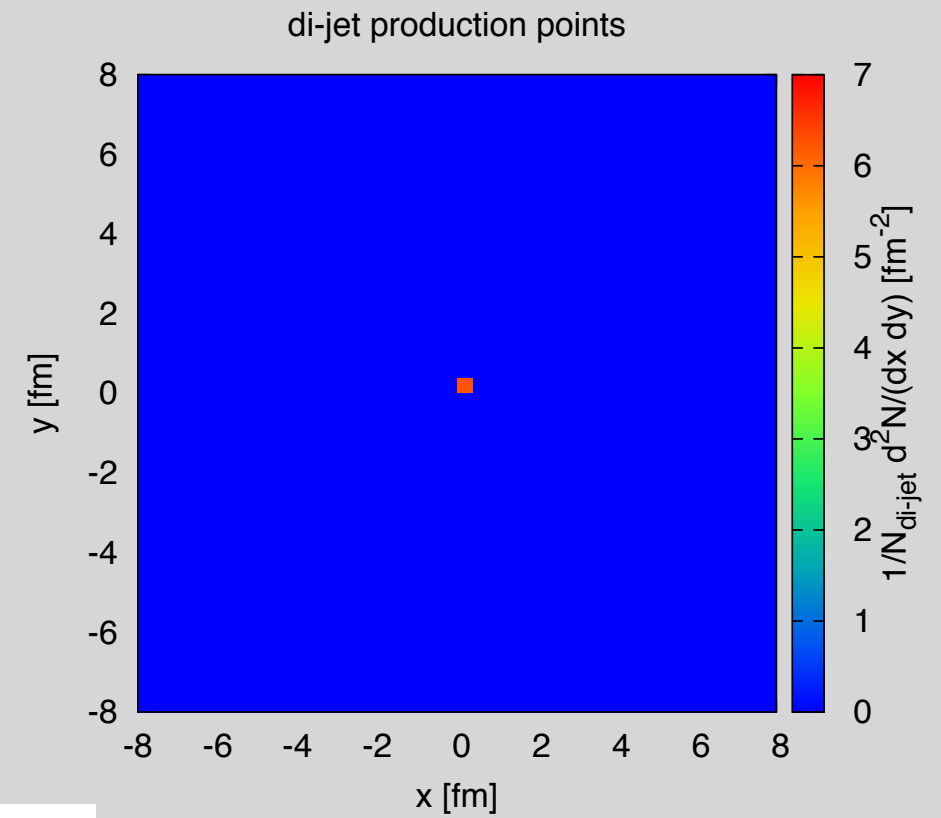
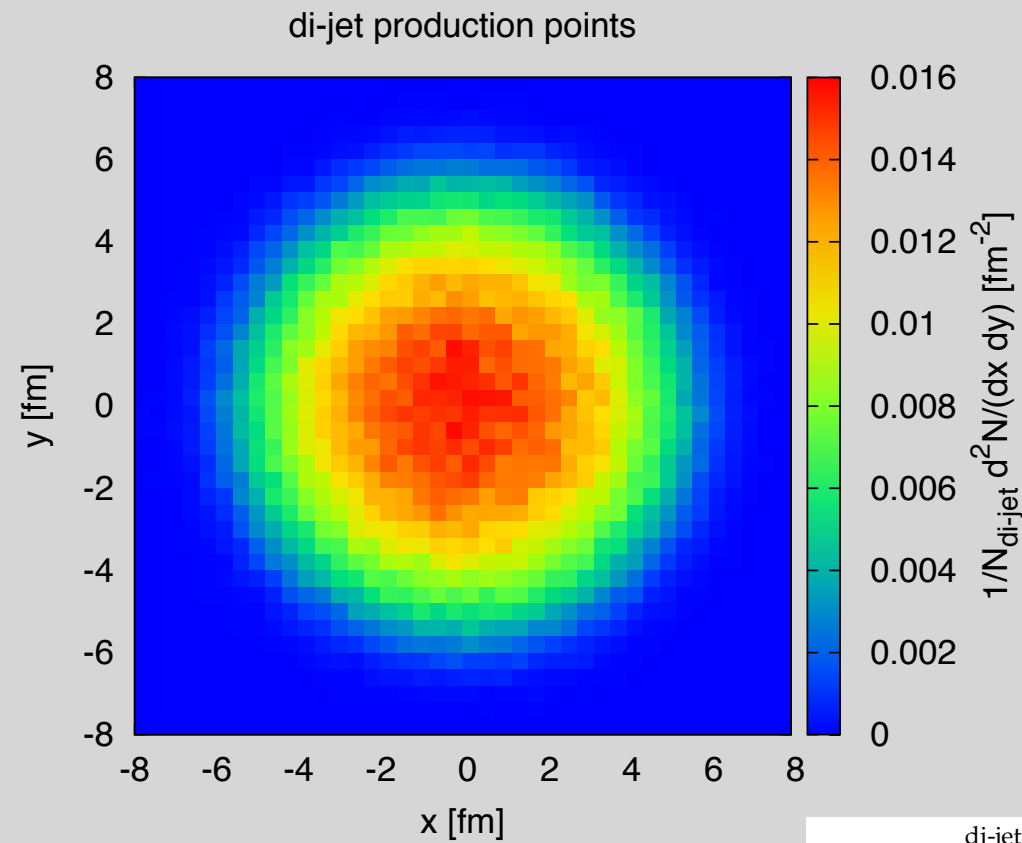
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Milhano, Zapp



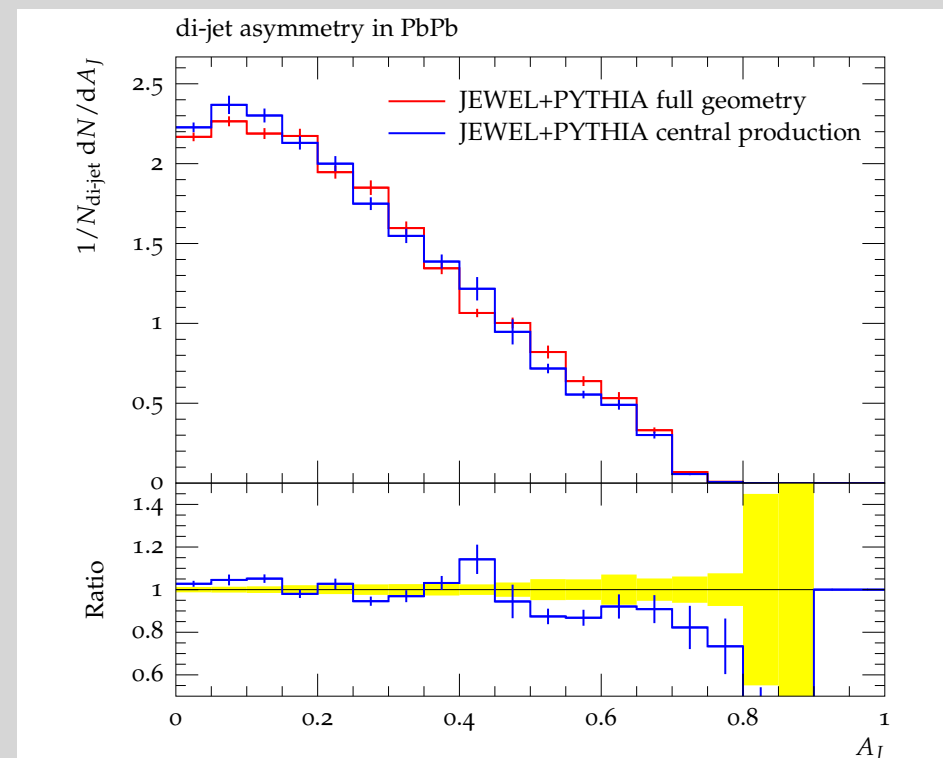
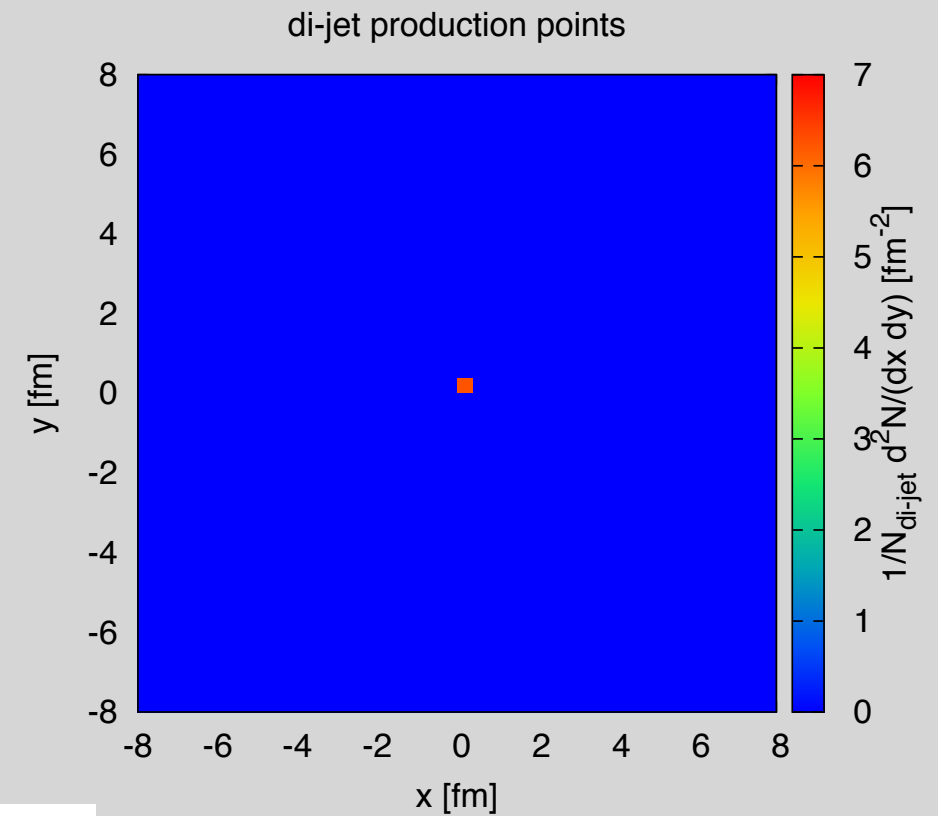
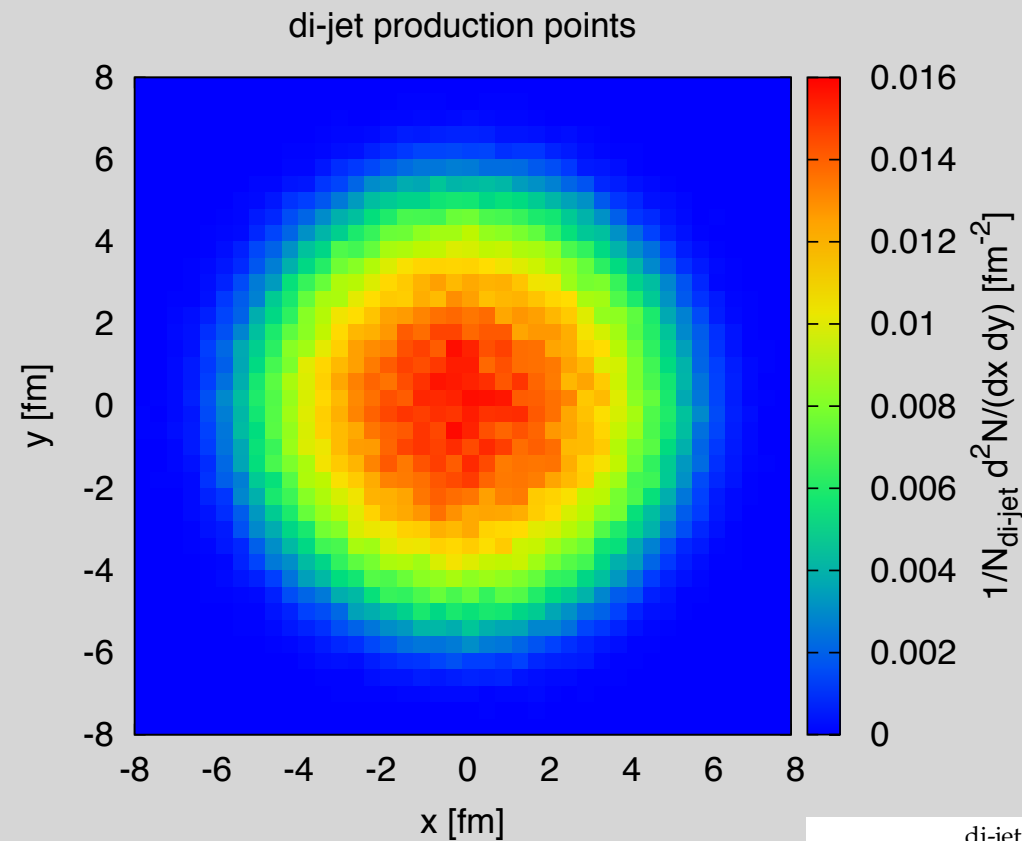
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Milhano, Zapp



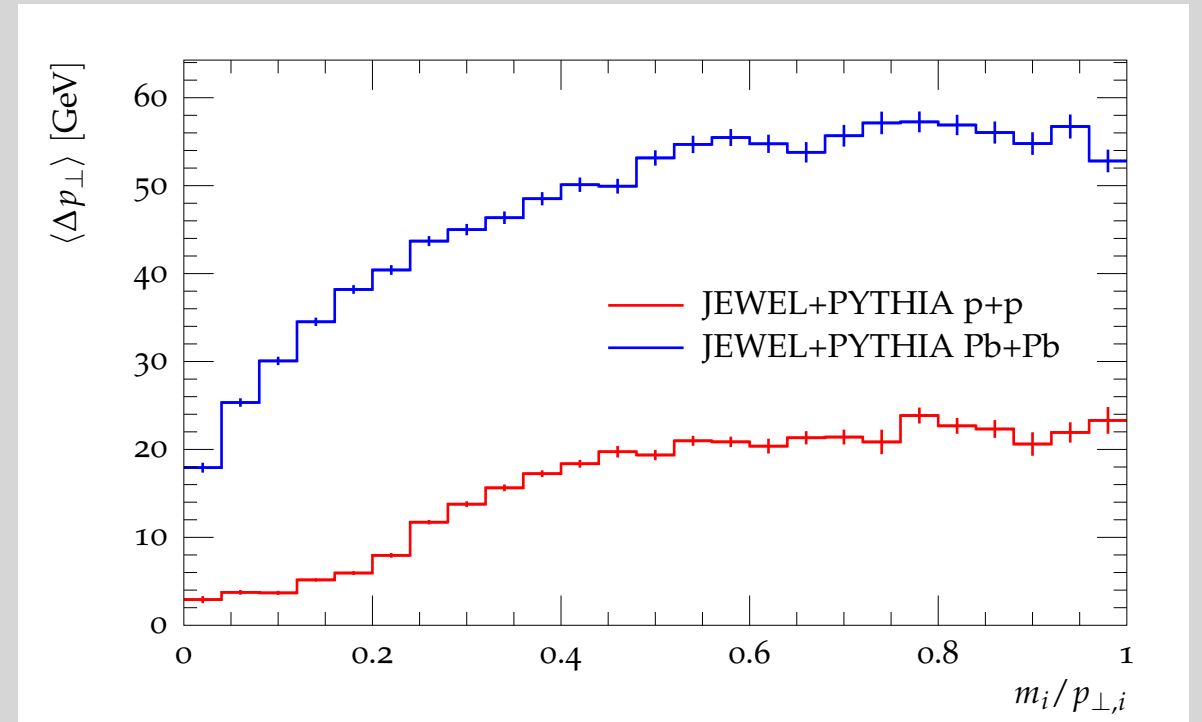
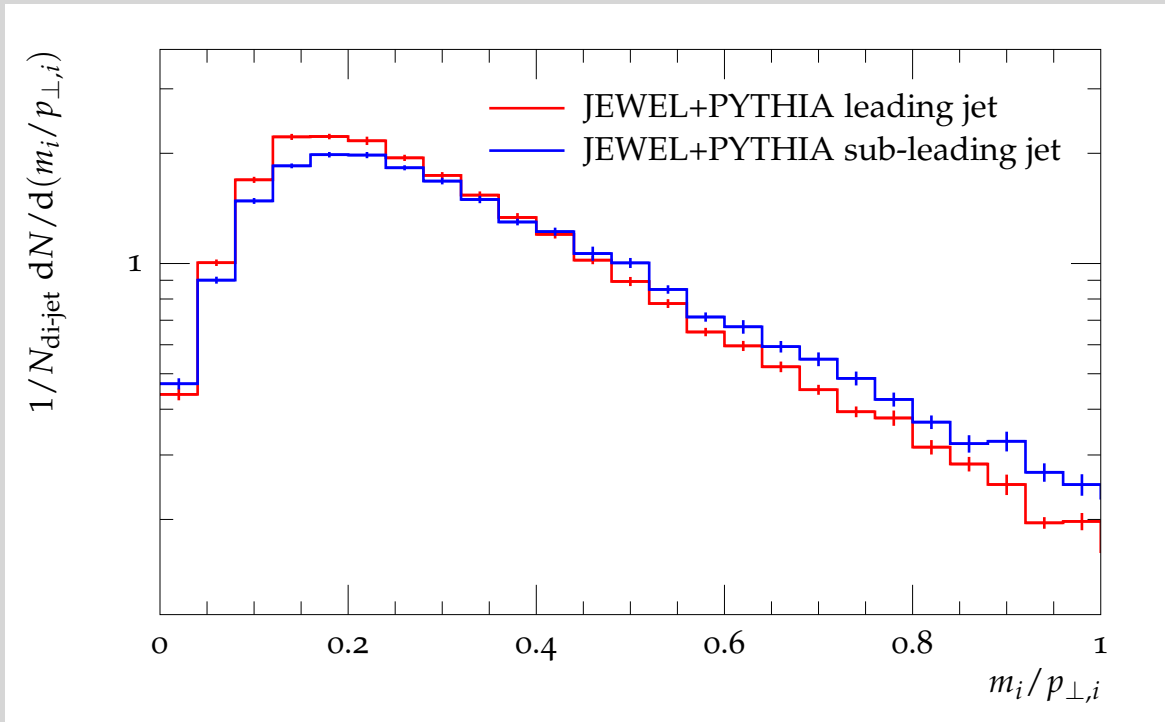
a sanity check

Milhano, Zapp



asymmetry is not driven by path-length differences

what then?



- asymmetry is driven by fragmentation fluctuations [how many constituents in a jet] which are mostly due to vacuum-like fragmentation
- direct sensitivity to 'number of emitters'
- much more interesting than the naive guess

outlook

- *in just over ten years jet studies in heavy ion collisions have gone from 'an idea' to a robust experimental reality*
- *recent efforts have established a clear pathway to reliably compute jet dynamics in QGP*
- *detailed probing programme in its beginnings*
 - *time to think hard about 'new' observables [measurable and calculable]*
 - *direct sensitivity to formation times*
 - *sensitivity to different time and spacial scales*
 - *isolation of 'pure' sample of strongly modified jets where*

backups

jets in vacuum [recombination algorithms]

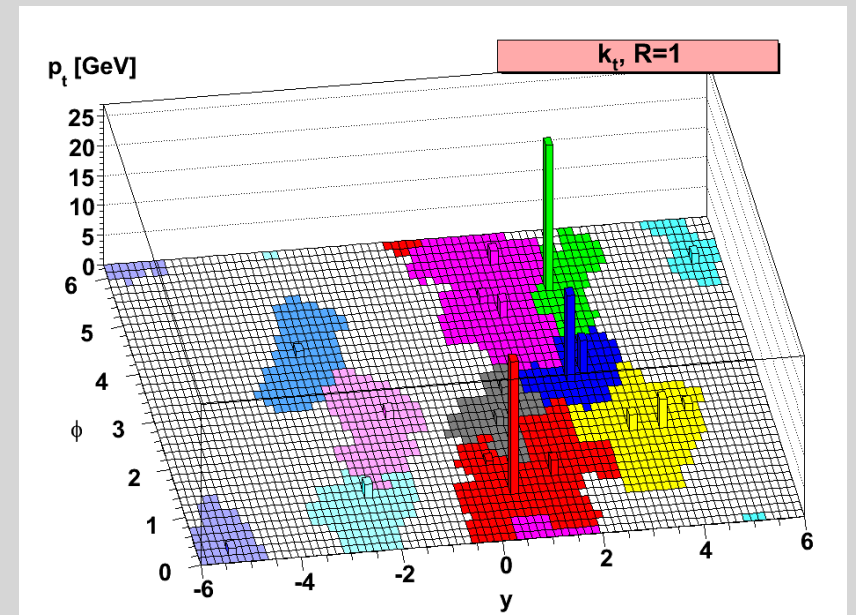
$$d_{ij} = \min(p_{ti}^{2p}, p_{tj}^{2p}) \frac{\Delta R_{ij}^2}{R^2}$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

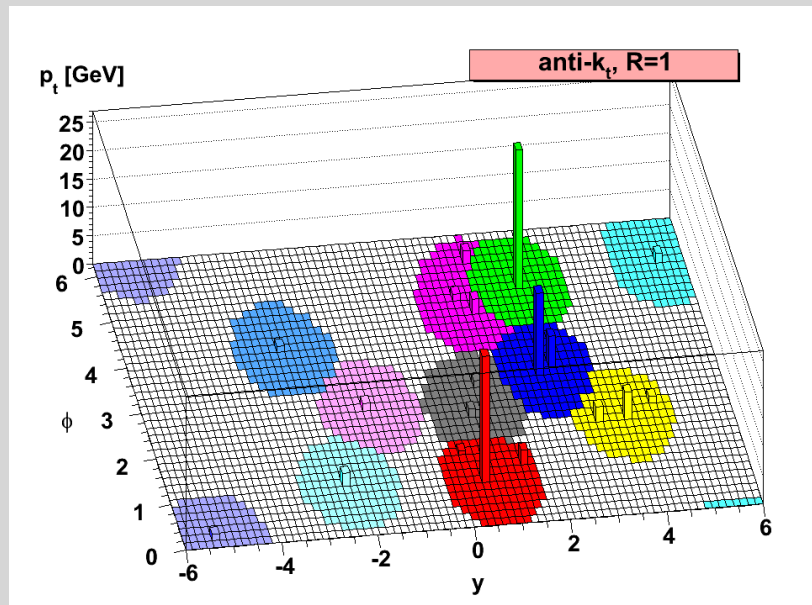
$p = 1$

:: k_t [from soft to hard] ::

:: preserves information on shower structure ::



Cacciari, Salam, Soyez [0802.1189]



$p = -1$

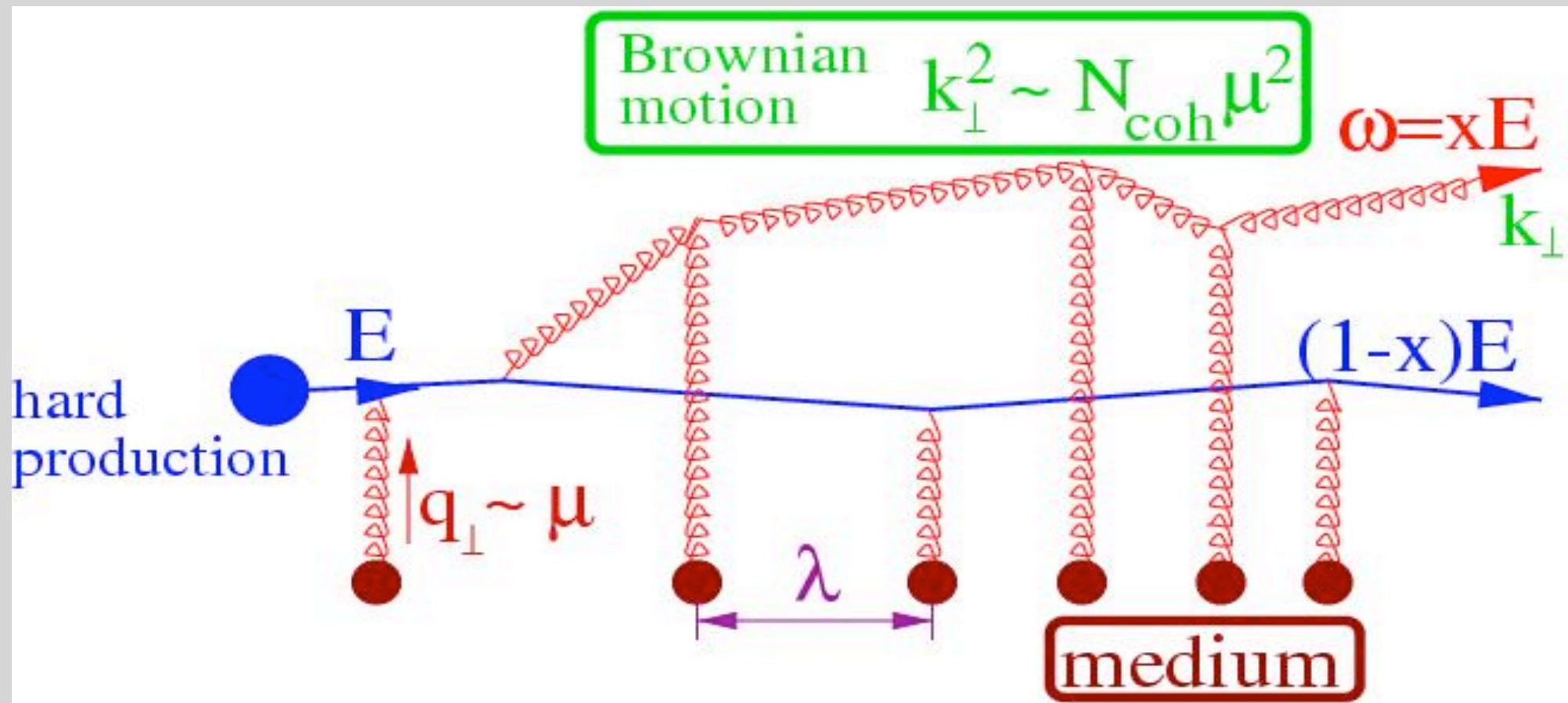
:: $\text{anti-}k_t$ [from hard to soft] ::

:: robustness in large background situations ::

additional handle [yet to be explored in heavy ions]

:: different jet definitions [recombination sequence] yield different jet populations

single emission [BDMPS-Z]



$$\hat{q}(t) \equiv \alpha_s n(t) \int_{|\mathbf{q}| < q^*} d\mathbf{q}^2 \, q^2 \gamma(q^2)$$

$$\hat{q} \simeq \frac{\mu^2}{\lambda}$$

medium induced radiation

medium induced radiation

- single gluon emission understood in 4 classes of pQCD-based formalisms
 - ↪ **Baier-Dokshitzer-Mueller-Peigné-Schiff-Zakharov**
 - ↪ **Gyulassy-Levai-Vitev**
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 - ↪ **Higher-Twist** [Guo and Wang]

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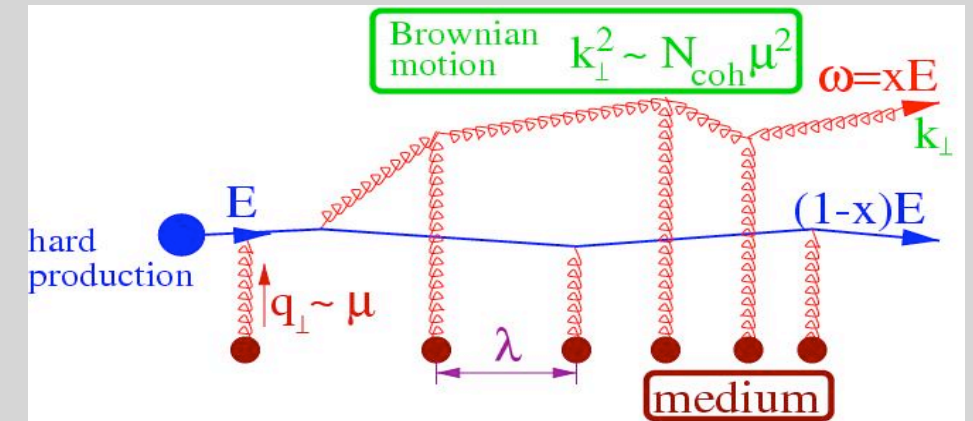
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- Monte Carlo implementations [HIJING, Q-PYTHIA/Q-HERWIG, JEWELL, YaJEM, MARTINI]

single emission [BDMPS-Z]

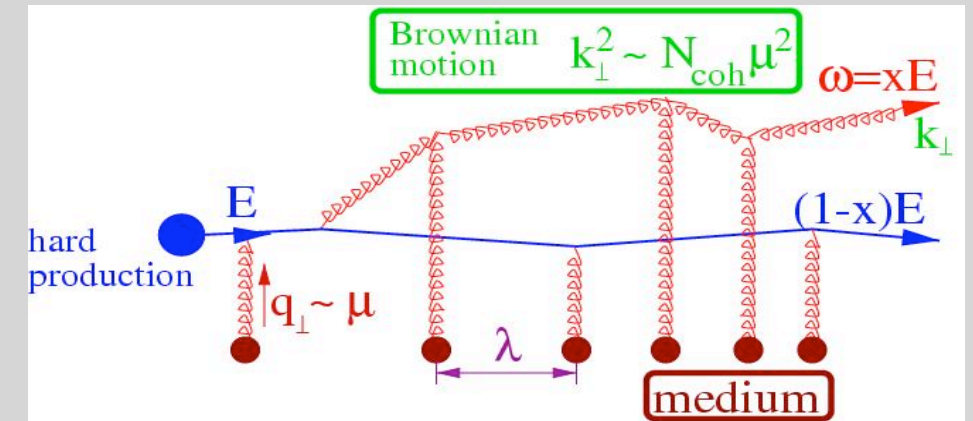


$$\hat{q} \simeq \frac{\mu^2}{\lambda}$$

single emission [BDMPS-Z]

—○ Brownian motion

$$\langle k_{\perp}^2 \rangle \sim \hat{q}L$$



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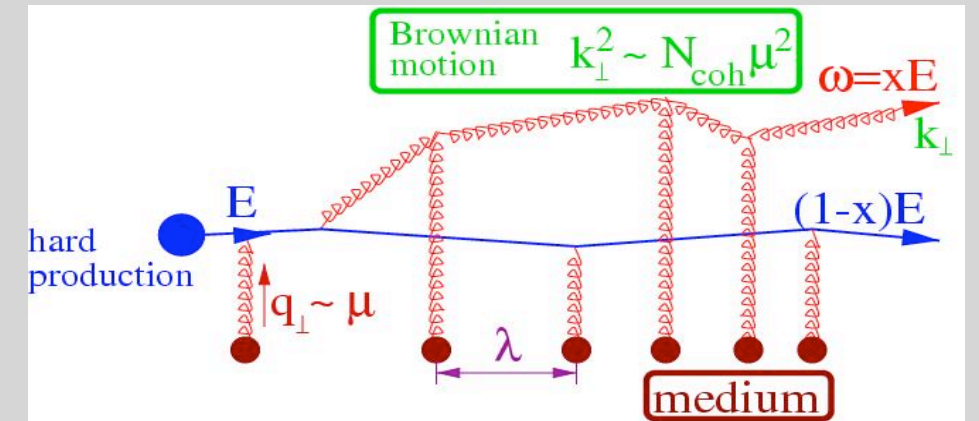
—○ Brownian motion

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—○ accumulated phase

$$\left\langle \frac{k_{\perp}^2 L}{\omega} \right\rangle \sim \frac{\hat{q}L^2}{\omega} \sim \frac{\omega_c}{\omega} \longrightarrow \text{characteristic gluon energy}$$

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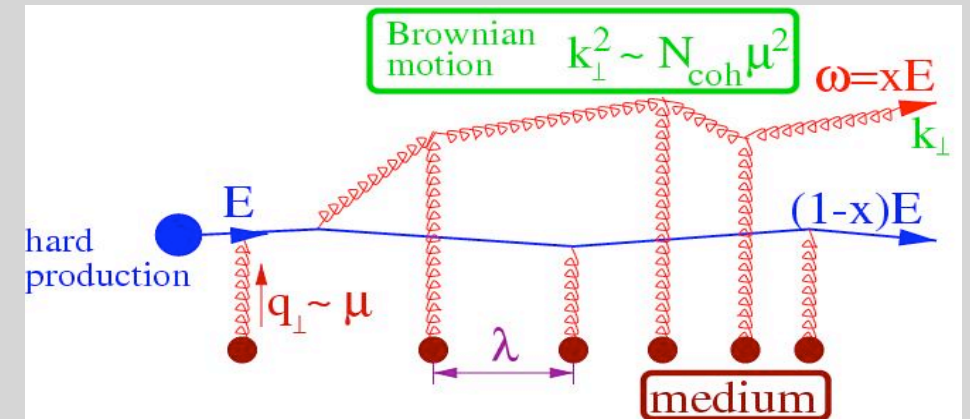
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- number of coherent scatterings

$$N_{coh} \sim \frac{t_{coh}}{\lambda}$$

$$t_{coh} \sim \frac{\omega}{k_{\perp}^2} \sim \sqrt{\frac{\omega}{\hat{q}}}$$

$$k_{\perp}^2 \sim \hat{q} t_{coh}$$



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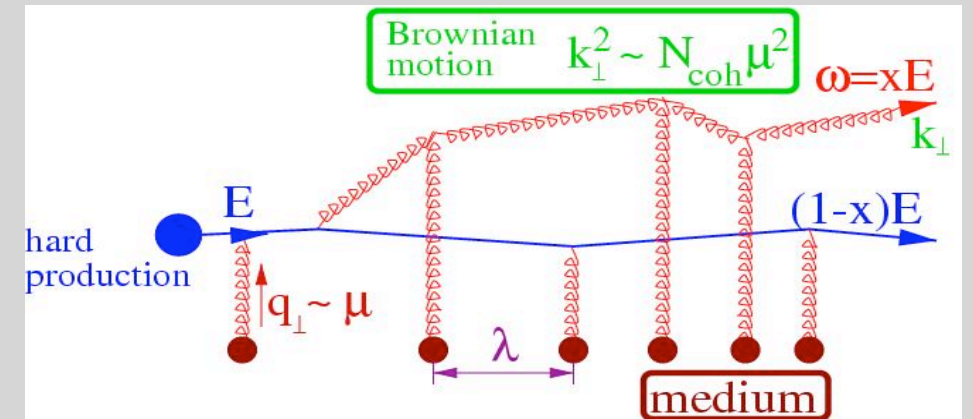
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$$k_{\perp}^2 \sim \hat{q} t_{coh}$$

- gluon energy distribution

$$\omega \frac{dI_{med}}{d\omega dz} \sim \frac{1}{N_{coh}} \omega \frac{dI_1}{d\omega dz} \sim \alpha_s \sqrt{\frac{\hat{q}}{\omega}} \longrightarrow \text{non-abelian LPM}$$



single emission [BDMPS-Z]

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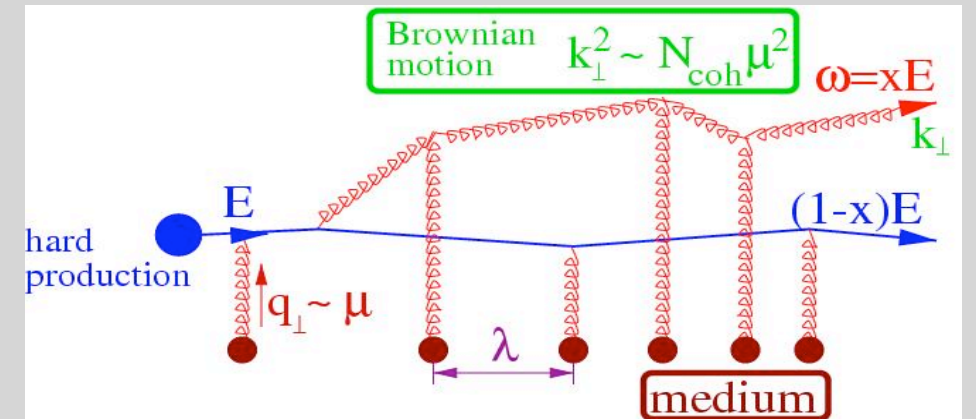
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—○ average energy loss

$$\Delta E = \int_0^L dz \int_0^{\omega_c} \omega d\omega \frac{dI_{med}}{d\omega dz} \sim \alpha_s \omega_c \sim \alpha_s \hat{q} L^2$$



beyond back the envelope [path-integral]

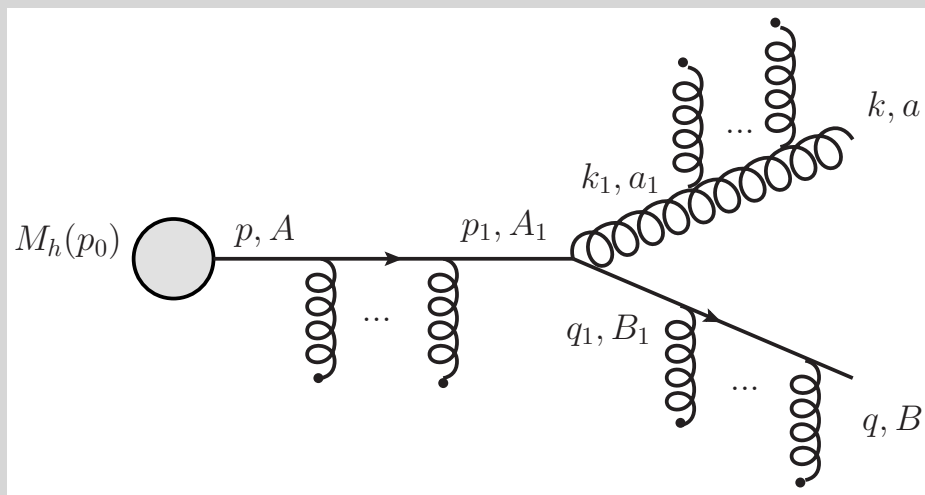
—○ eikonal trajectory of parton propagating in medium

$$W_{\alpha_f \alpha_i}(x_{f+}, x_{i+}; \mathbf{r}(\xi)) = \mathcal{P} \exp \left\{ ig \int_{x_{i+}}^{x_{f+}} d\xi A_- (\xi, \mathbf{r}(\xi)) \right\}$$

—○ off[but close to]-eikonal trajectory

$$G_{\alpha_f \alpha_i}(x_{f+}, \mathbf{x}_f; x_{i+}, \mathbf{x}_i | p_+) = \int_{\mathbf{r}(x_{i+})=\mathbf{x}_i}^{\mathbf{r}(x_{f+})=\mathbf{x}_f} \mathcal{D}\mathbf{r}(\xi) \exp \left\{ \frac{ip_+}{2} \int_{x_{i+}}^{x_{f+}} d\xi \left(\frac{d\mathbf{r}}{d\xi} \right)^2 \right\} W_{\alpha_f \alpha_i}(x_{f+}, x_{i+}; \mathbf{r}(\xi))$$

—○ observables computed from medium averages of Gs [from medium field 2-pt correlators]

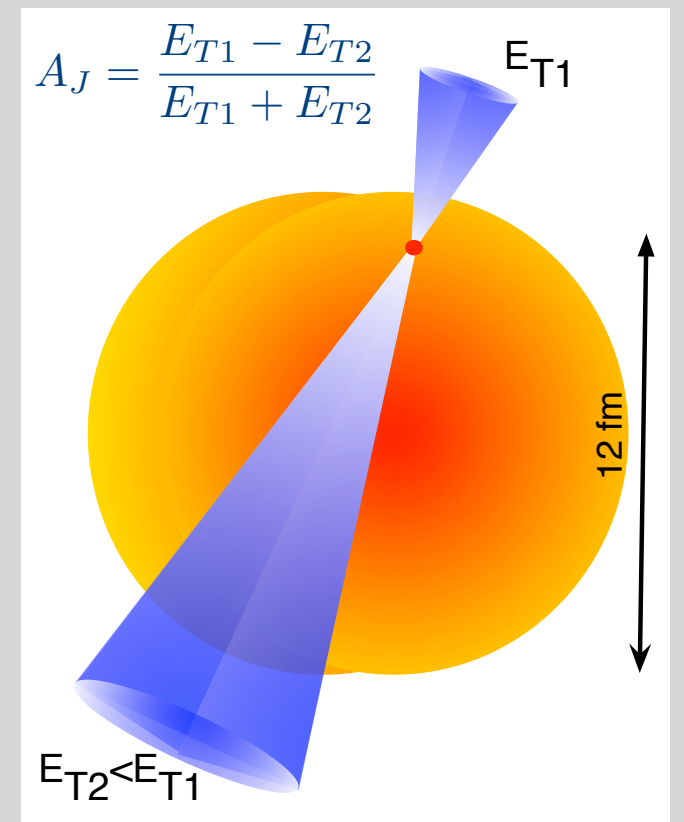


—○ BDMPS: quark eikonal, gluon soft and [slightly] off-eikonal

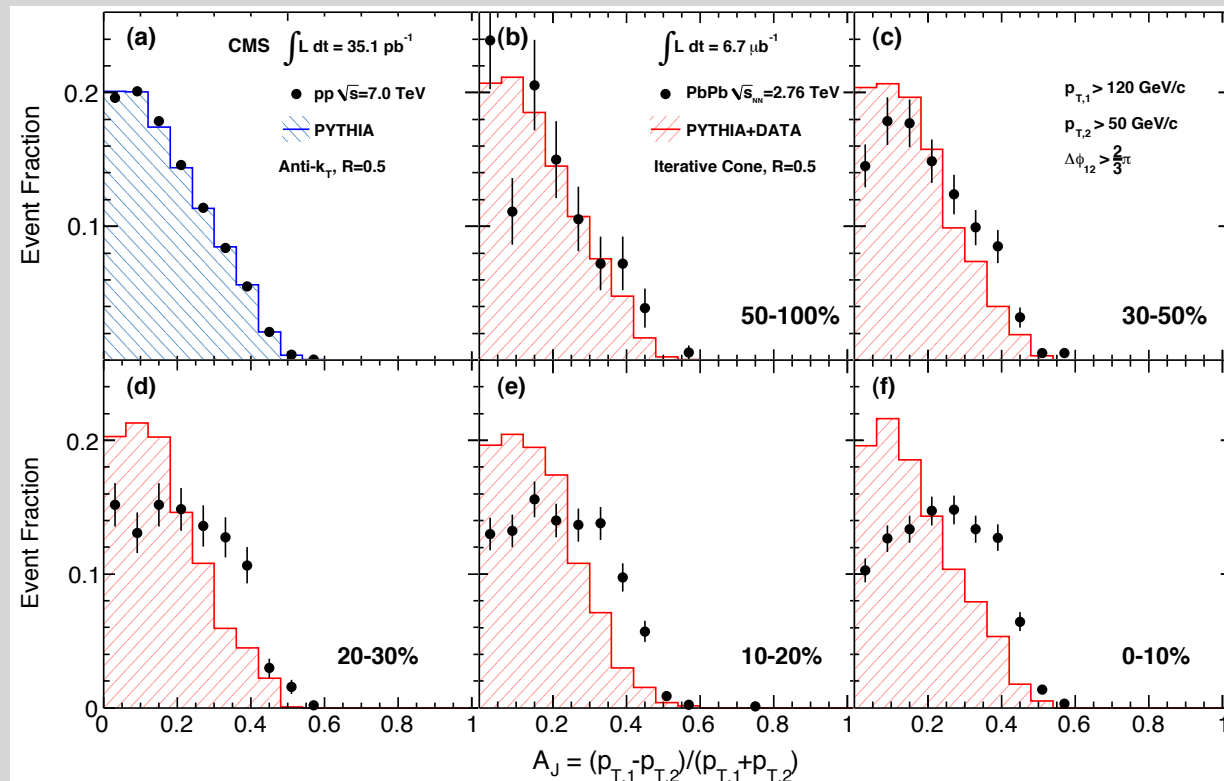
large broadening [a lesson from data]

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*imbalance of jet energy within a cone of radius R for
'back-to-back' di-jets*

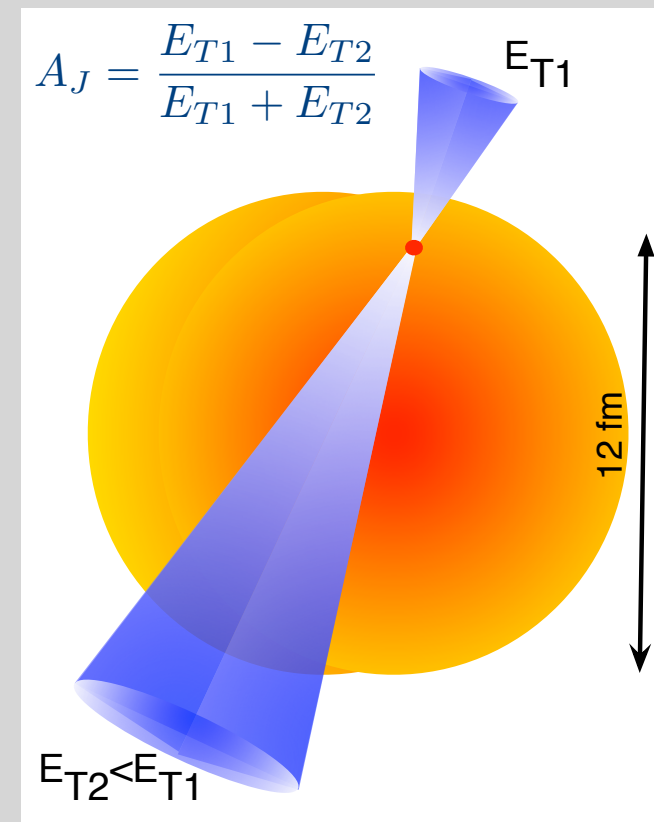


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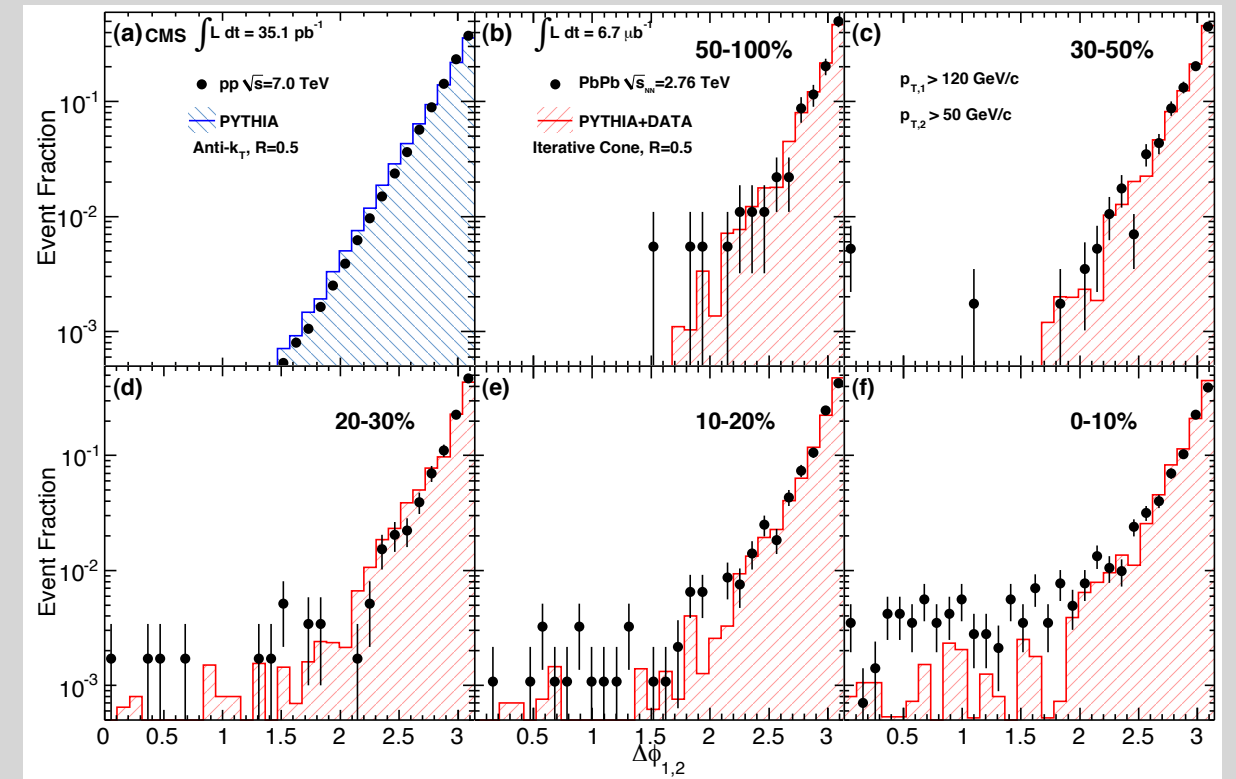
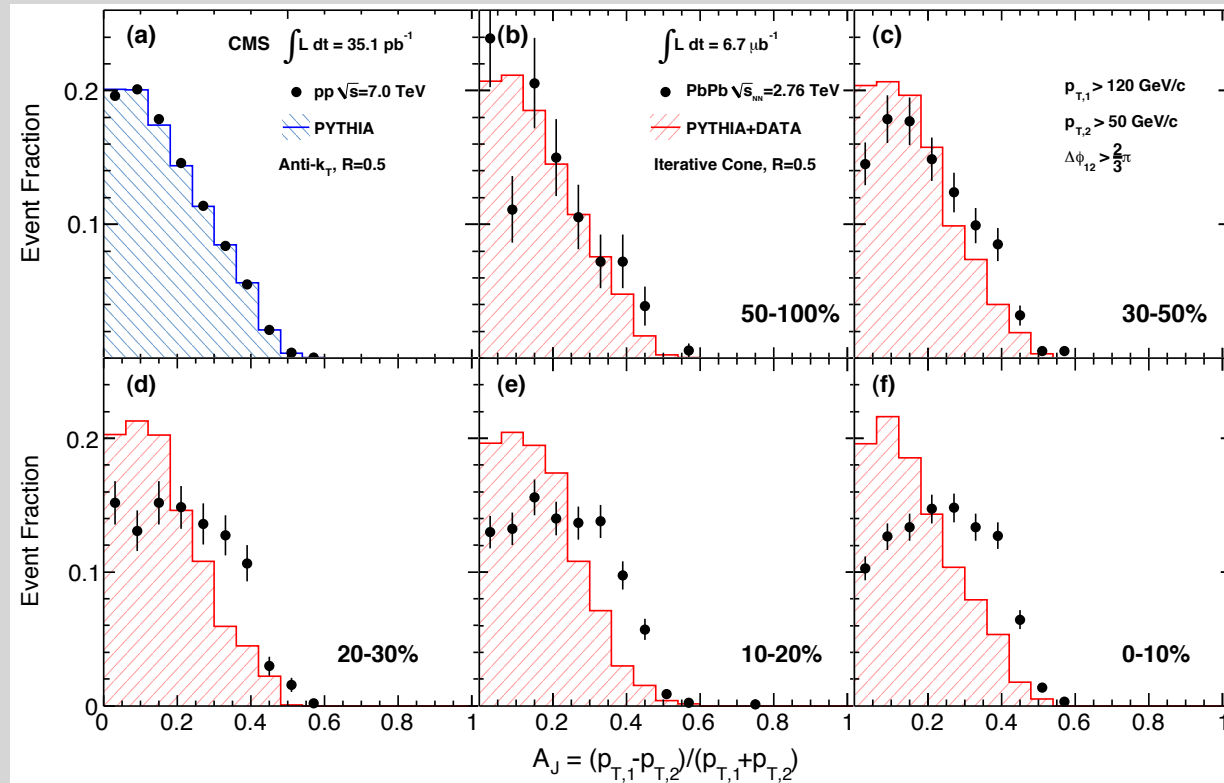


—○ significant enhancement of asymmetry

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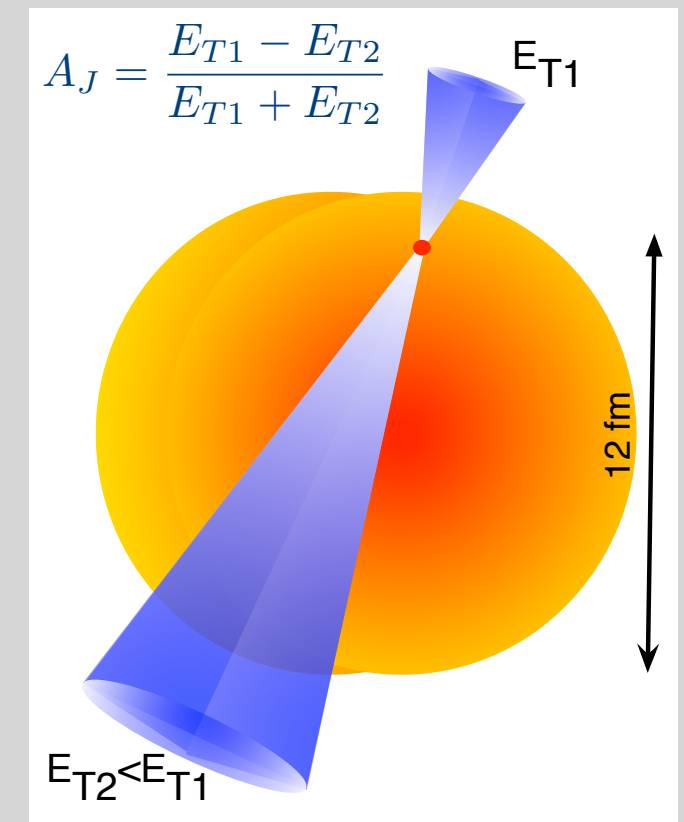


large broadening [a lesson from data]

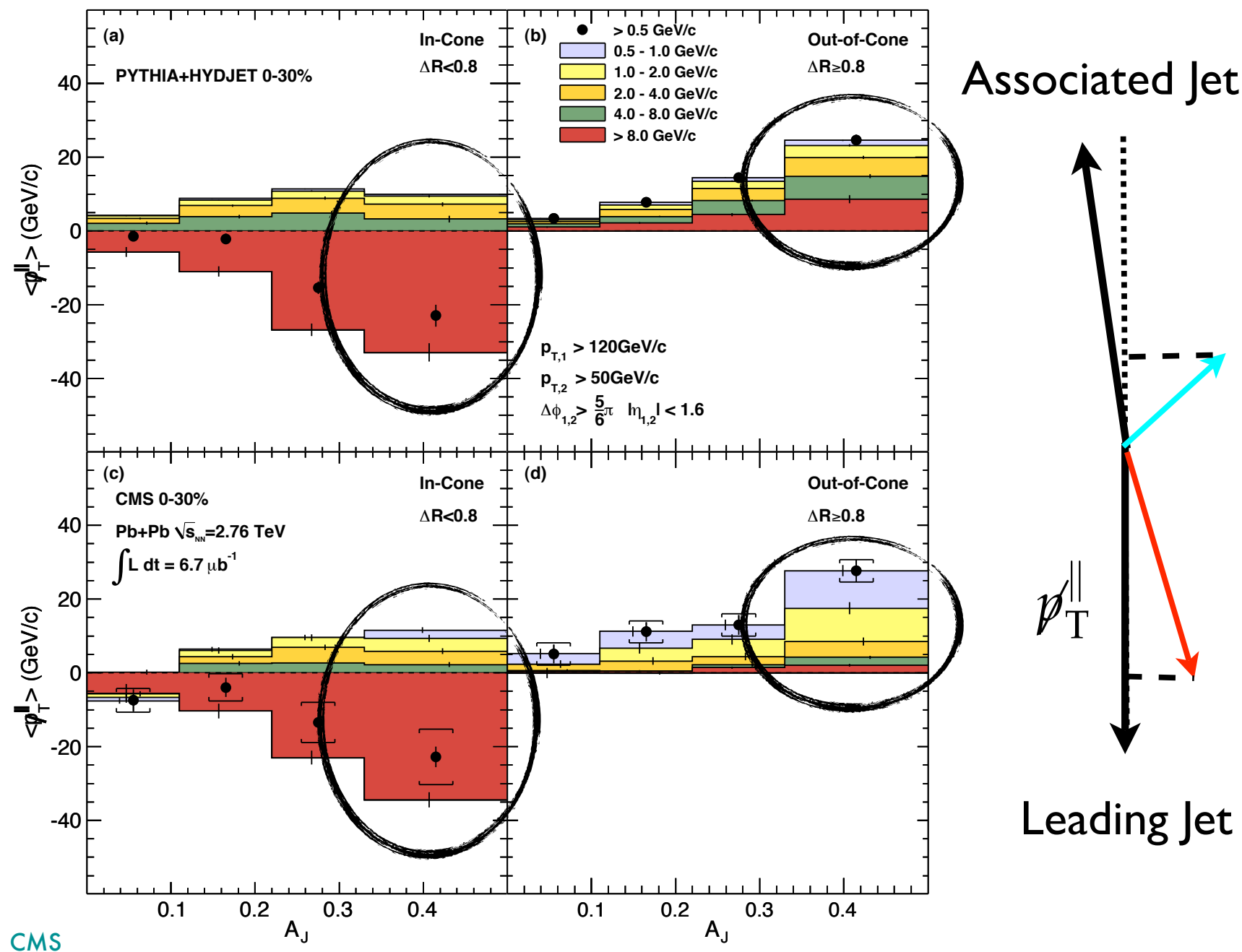


- significant enhancement of asymmetry
- no disturbance of azimuthal distribution

imbalance of jet energy within a cone of radius R for 'back-to-back' di-jets



large broadening [a lesson from data]



—○ energy lost from jet cone recovered in soft fragments at large angles

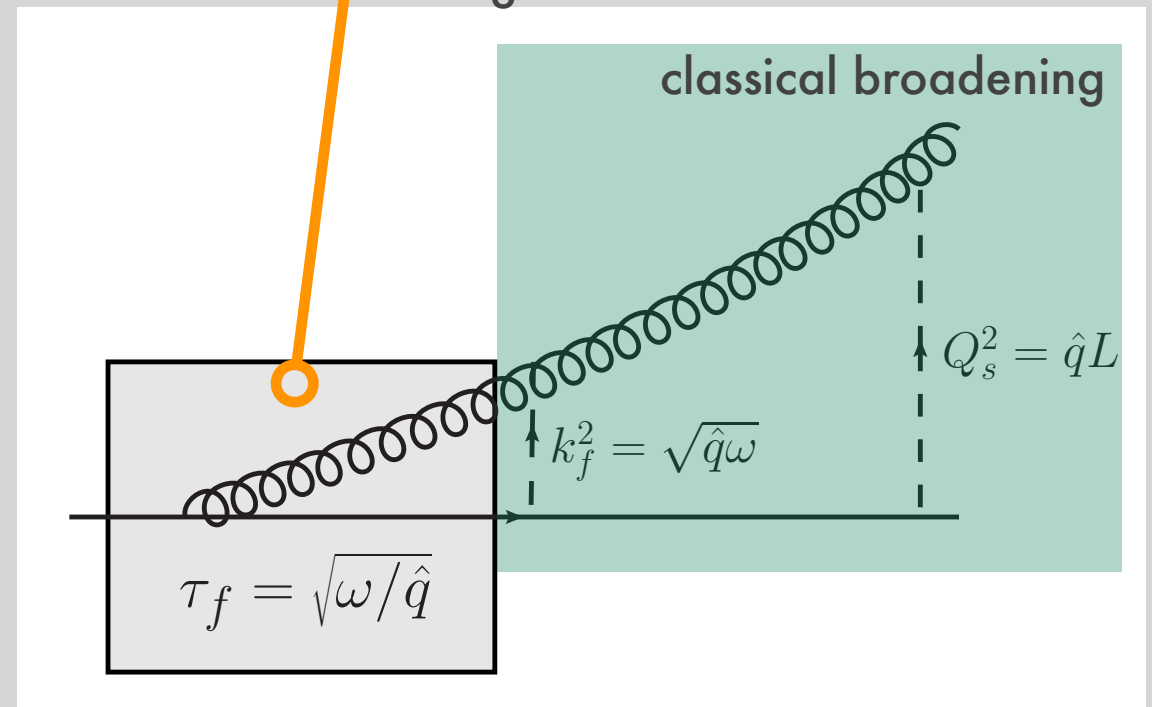
$$\not{p}_T^{\parallel} = \sum_i -p_T^i \cos(\phi_i - \phi_{\text{Leading Jet}})$$

large broadening

—○ medium induced radiation off a single quark in a dense medium **BDMPS-Z** revisited

$$\mathcal{R}_q^{\text{med}} \approx 4\omega \int_0^L dt' \int \frac{d^2 \mathbf{k}'}{(2\pi)^2} \mathcal{P}(\mathbf{k} - \mathbf{k}', L - t') \sin\left(\frac{\mathbf{k}'^2}{2k_f^2}\right) e^{-\frac{\mathbf{k}'^2}{2k_f^2}}$$

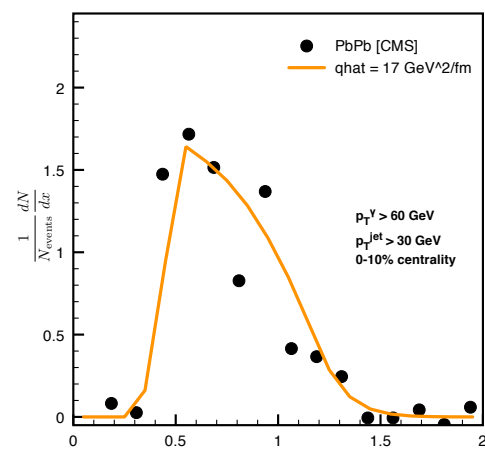
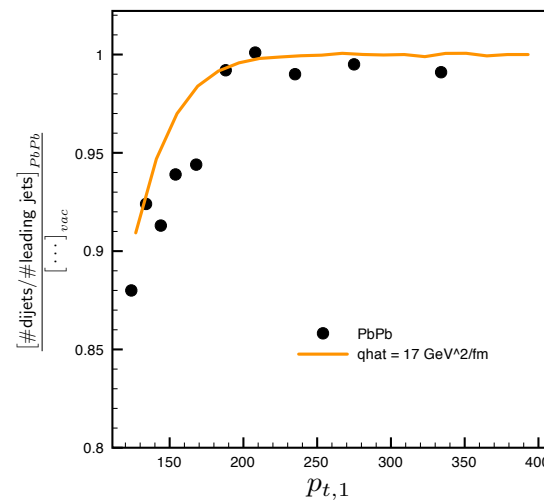
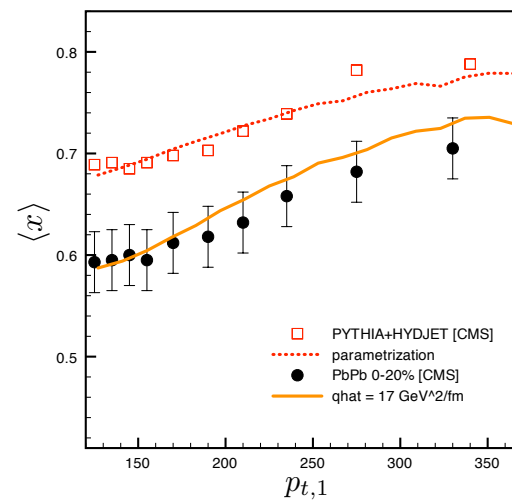
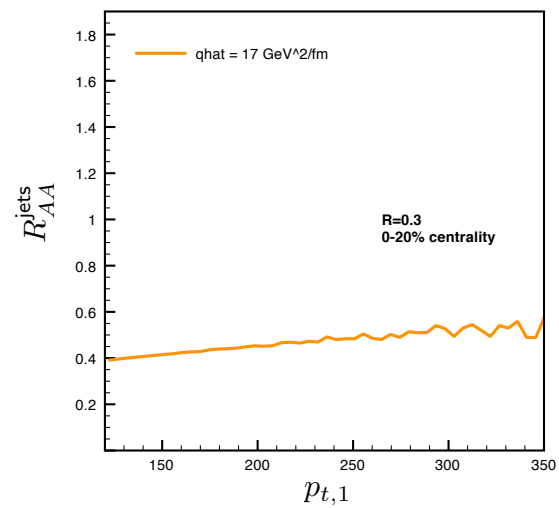
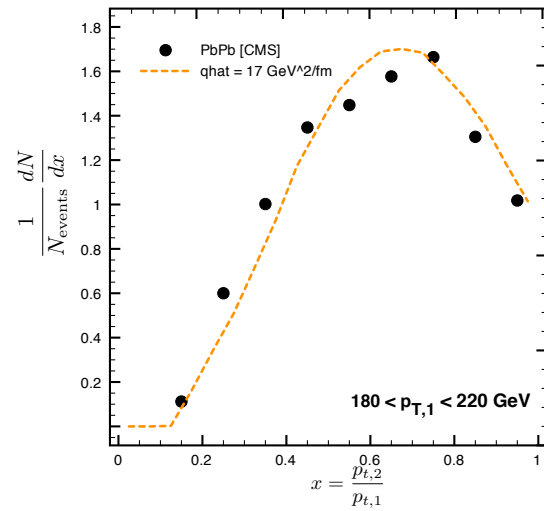
quantum emission/broadening
during formation time



AN IMPORTANT LESSON FROM DATA

large broadening [beyond quasi-eikonal] is a prominent dynamical mechanism for jet energy loss [dijet asymmetry]

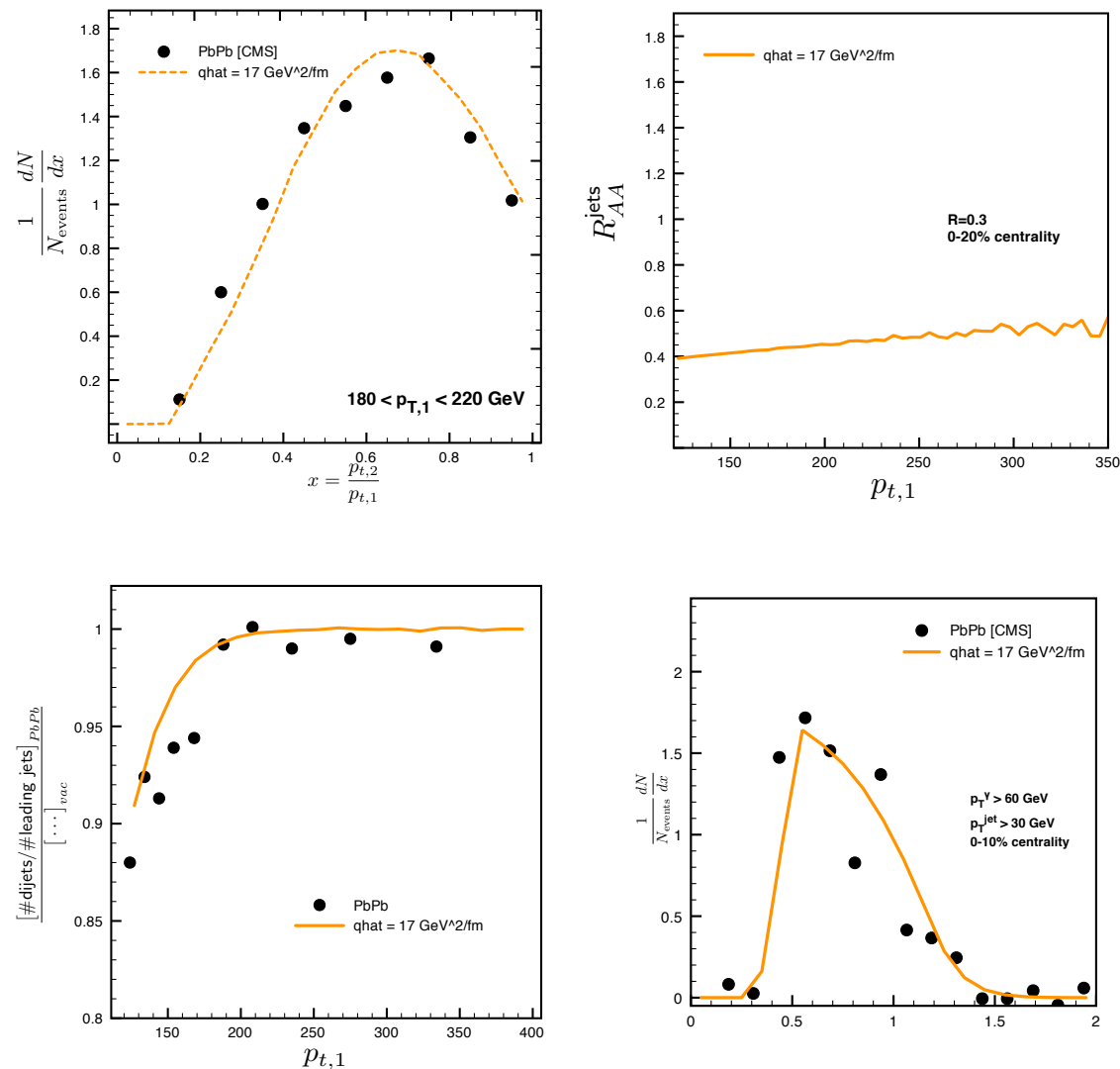
large broadening



HP 2012

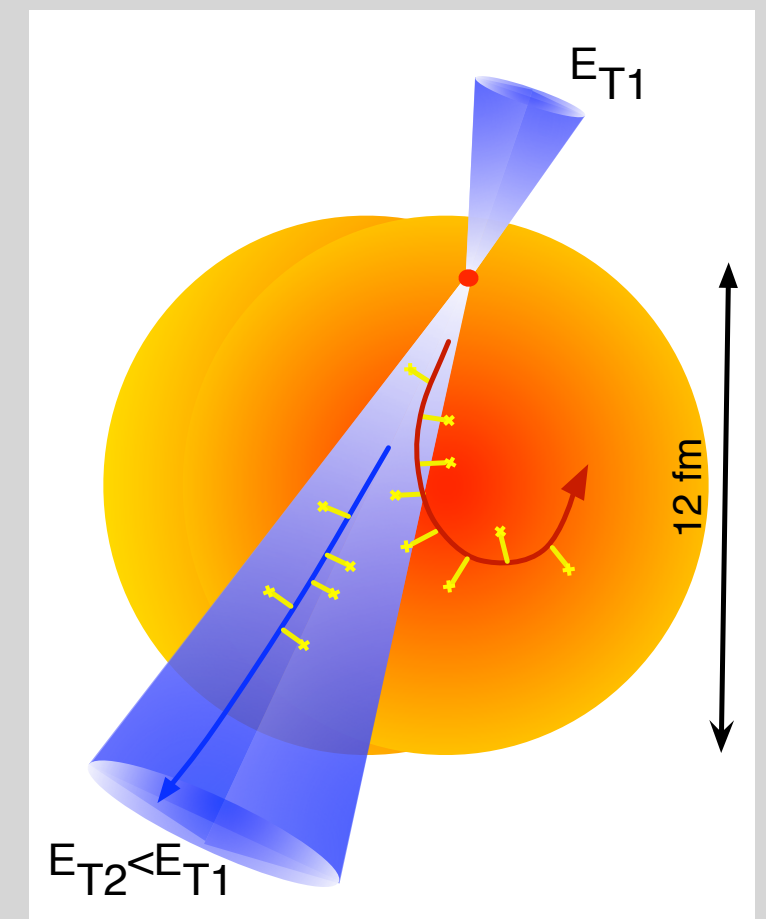
very reasonable phenomenological approach that remains unsubstantiated by a first principle calculation

large broadening



HP 2012

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interplay of branching and hadronization

—○ colour of all jet components rotated by interaction with medium

↪ colour correlations modified with respect to vacuum case

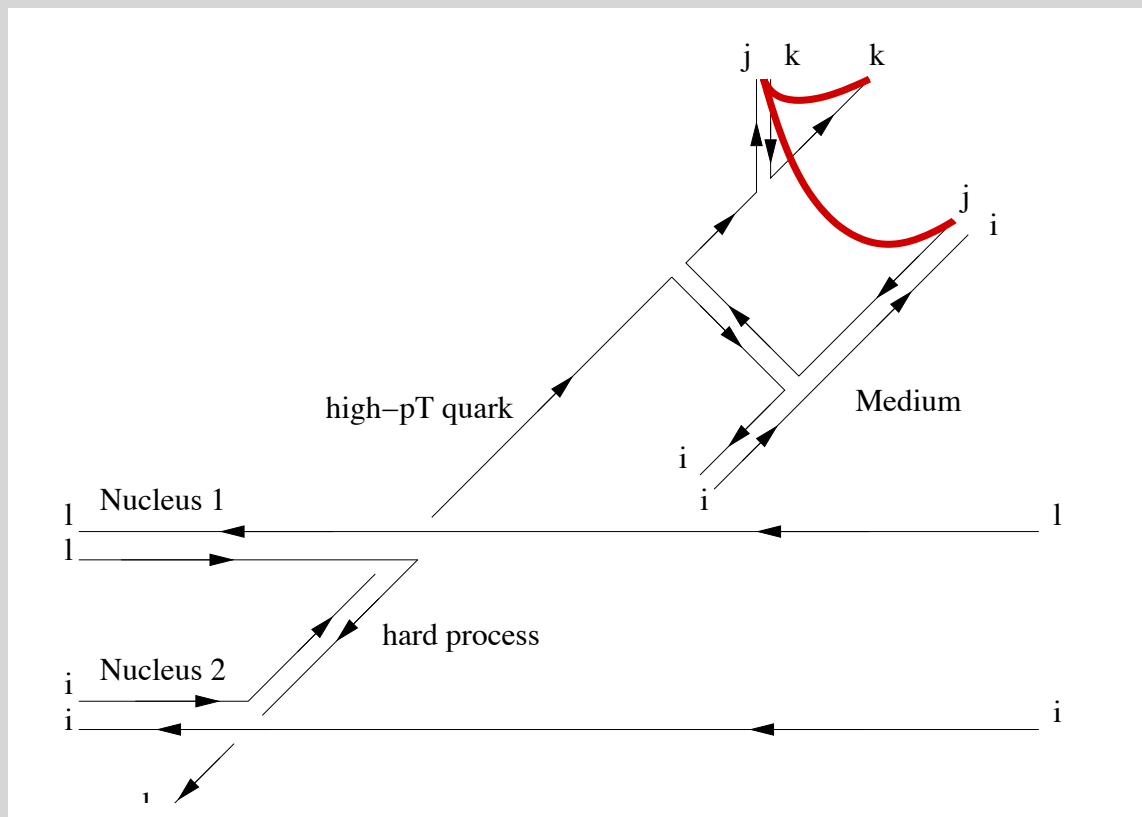
- theoretically controllable within a standard framework [opacity expansion]

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no medium interaction after radiation

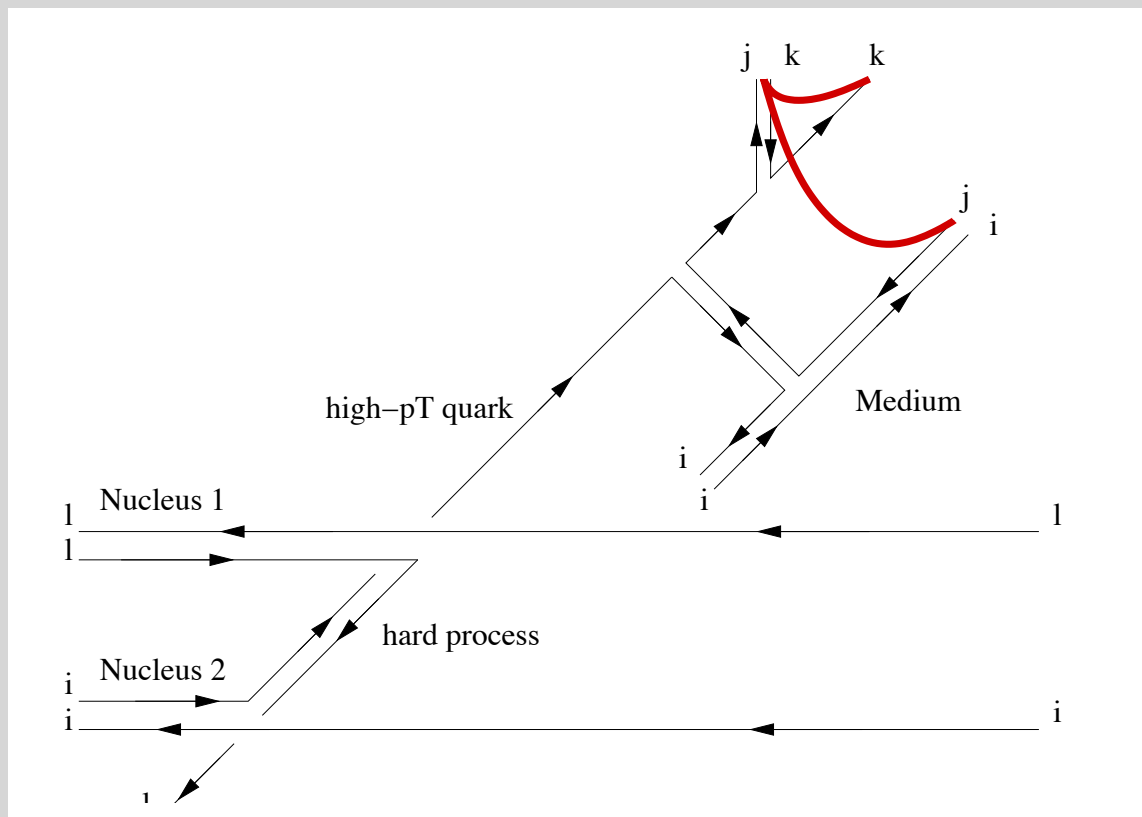
- colour properties of hadronizing system vacuum-like
- radiated gluon belongs to system

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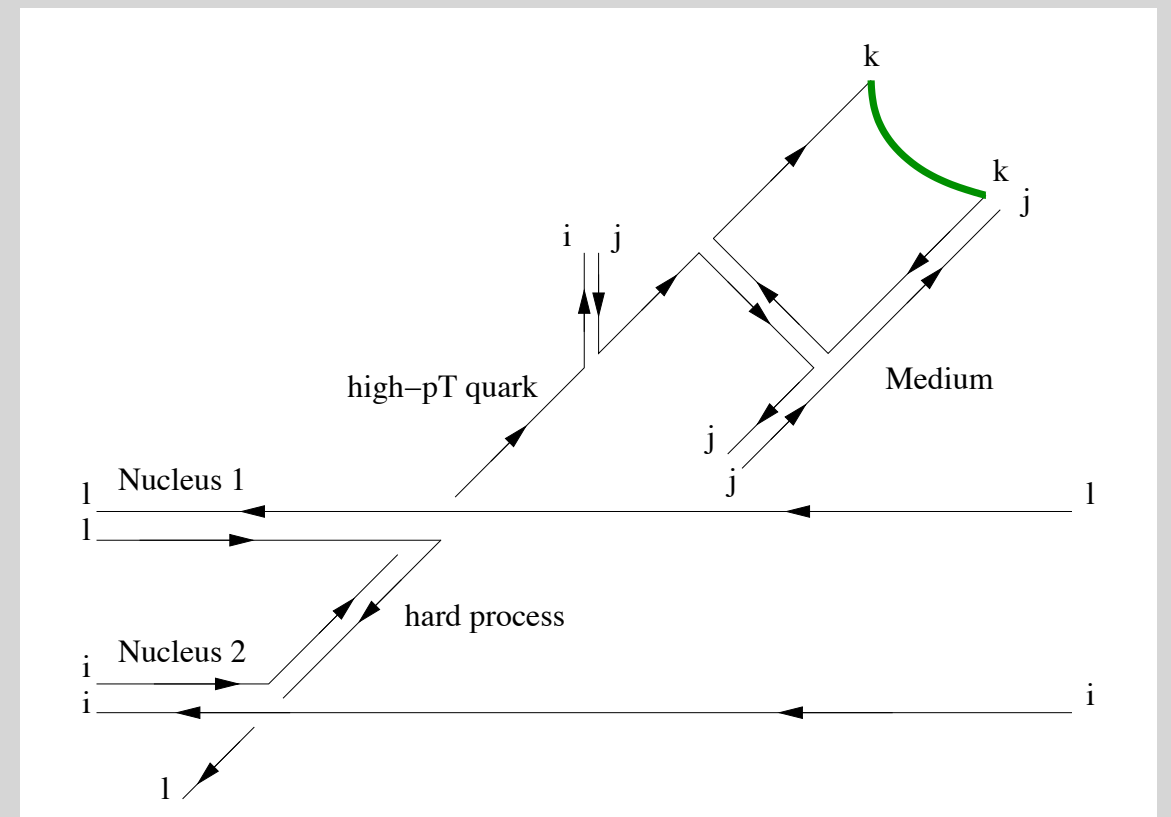
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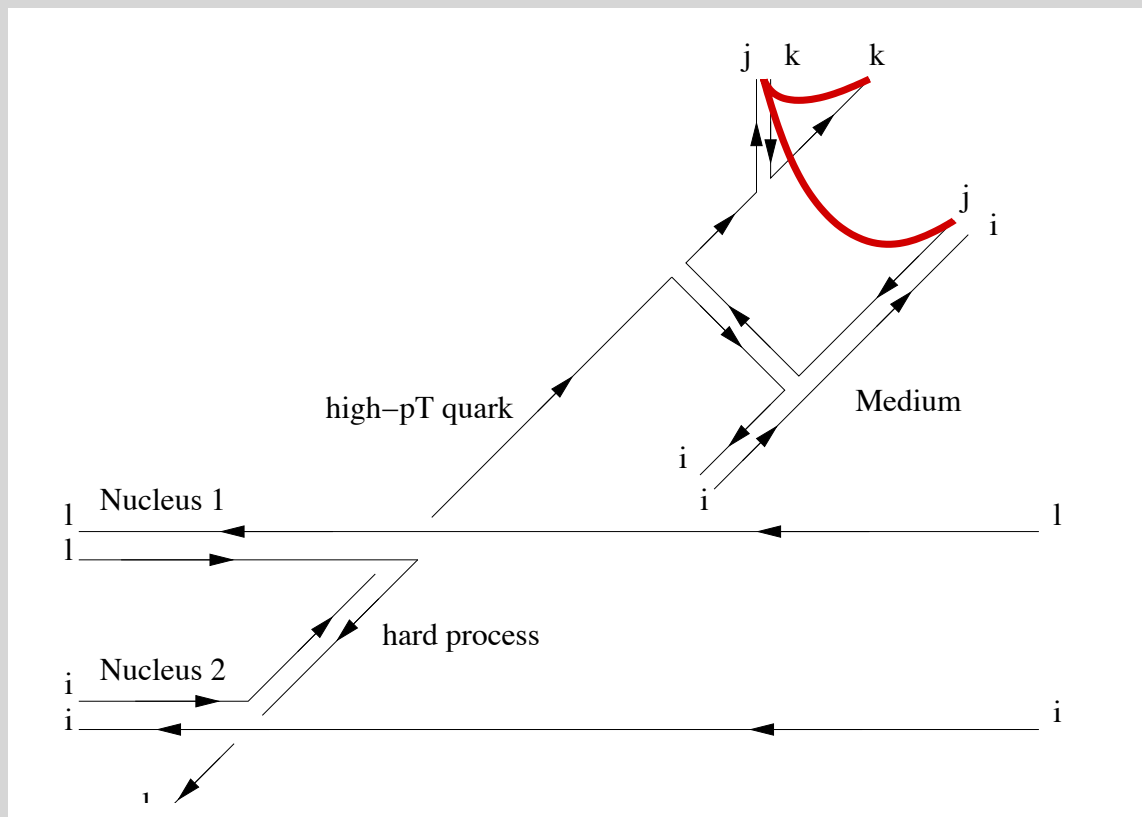


medium interaction after radiation

- colour properties of hadronizing system modified
- radiated gluon LOST

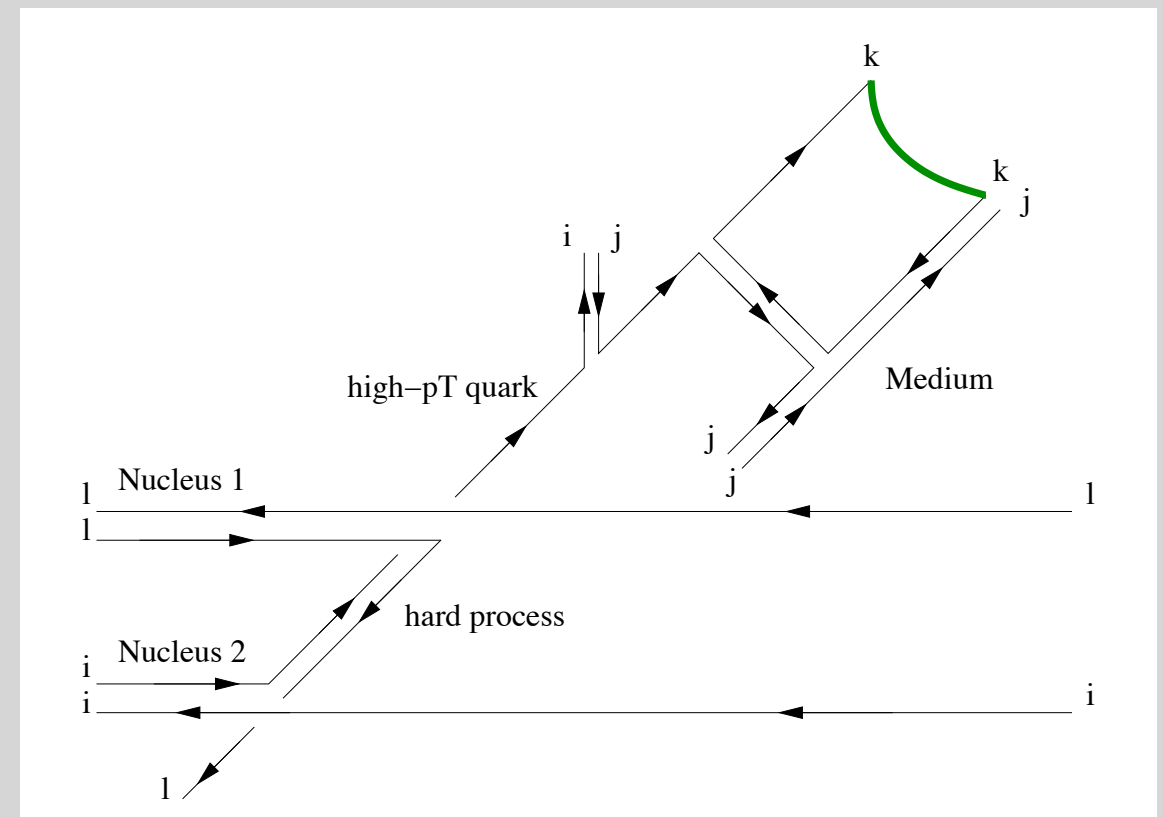
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- radiated gluon belongs to system



medium interaction after radiation

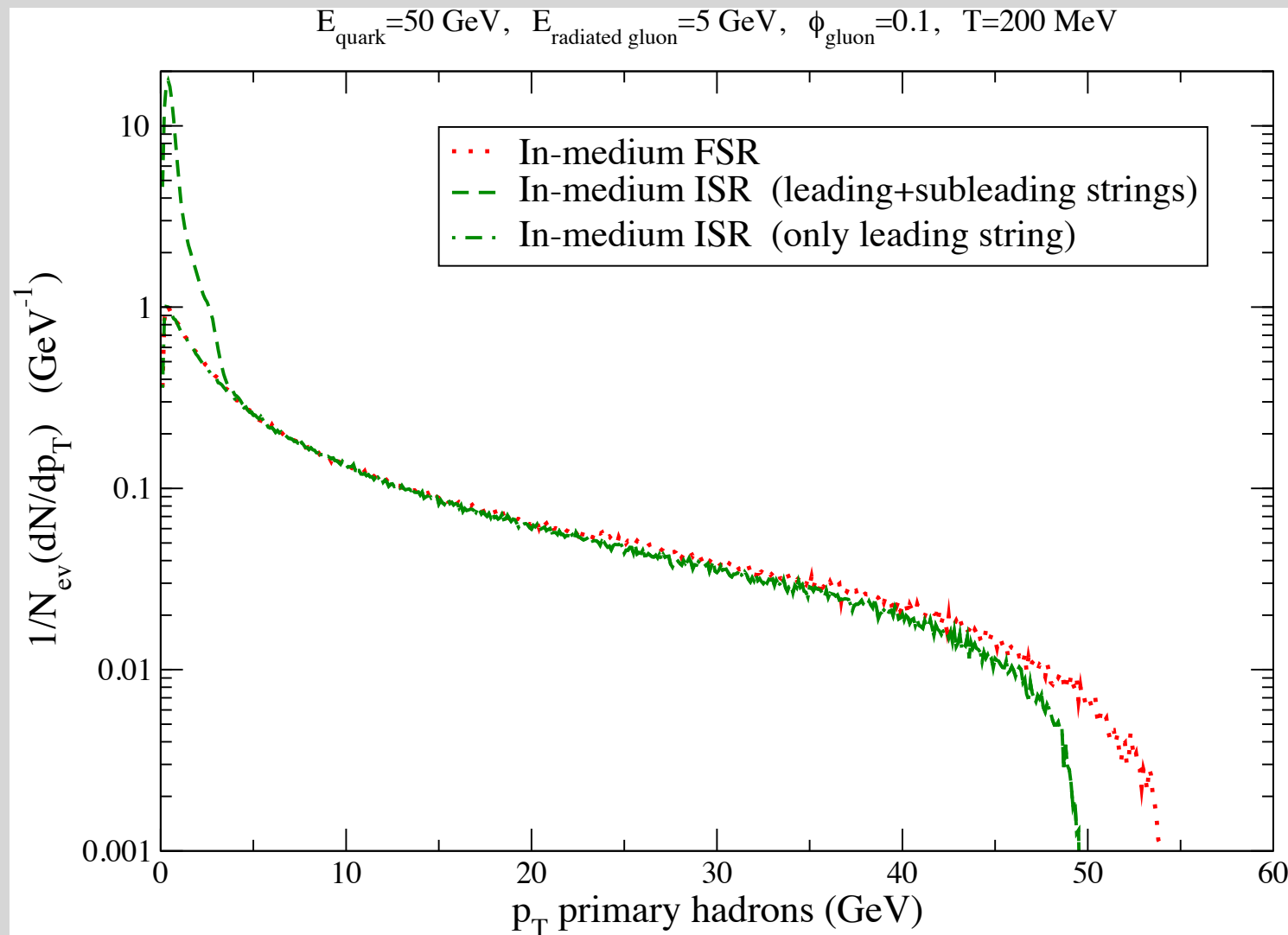
- colour properties of hadronizing system modified
- radiated gluon LOST

first steps towards fully colour differential framework

interplay of branching and hadronization

—○ colour correlations modified with respect to vacuum case

↪ essential input for realistic hadronization schemes



generic [robust] effects:

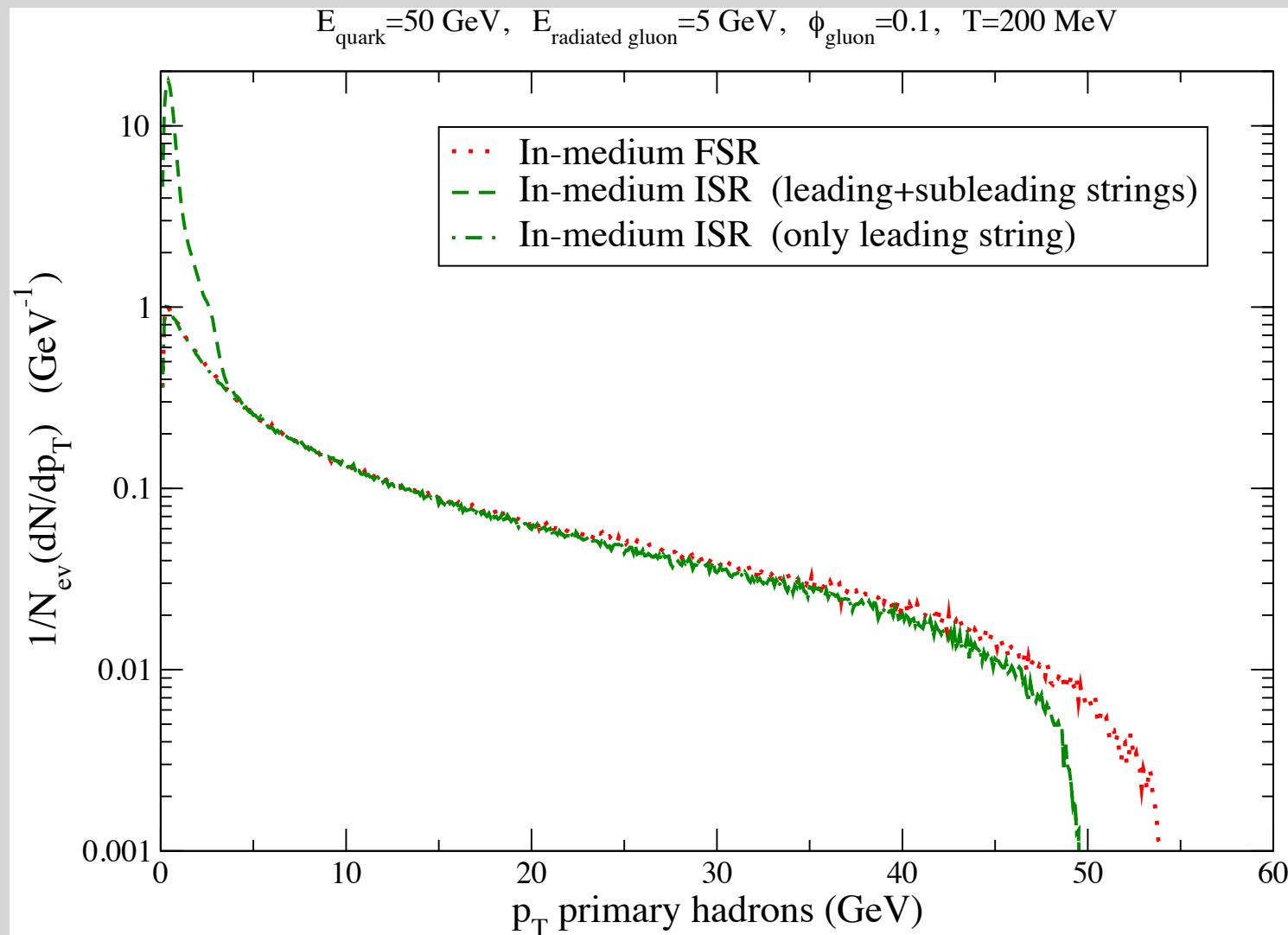
- softening of hadronic spectra
- lost hardness recovered as soft multiplicity
- at work even if radiative energy loss kinematically unviable
- survives branching after medium escape

modification of jet hadrochemistry
Aurenche & Zakharov [1109.6819]

interplay of branching and hadronization

—○ colour correlations modified with respect to vacuum case

↪ essential input for realistic hadronization schemes



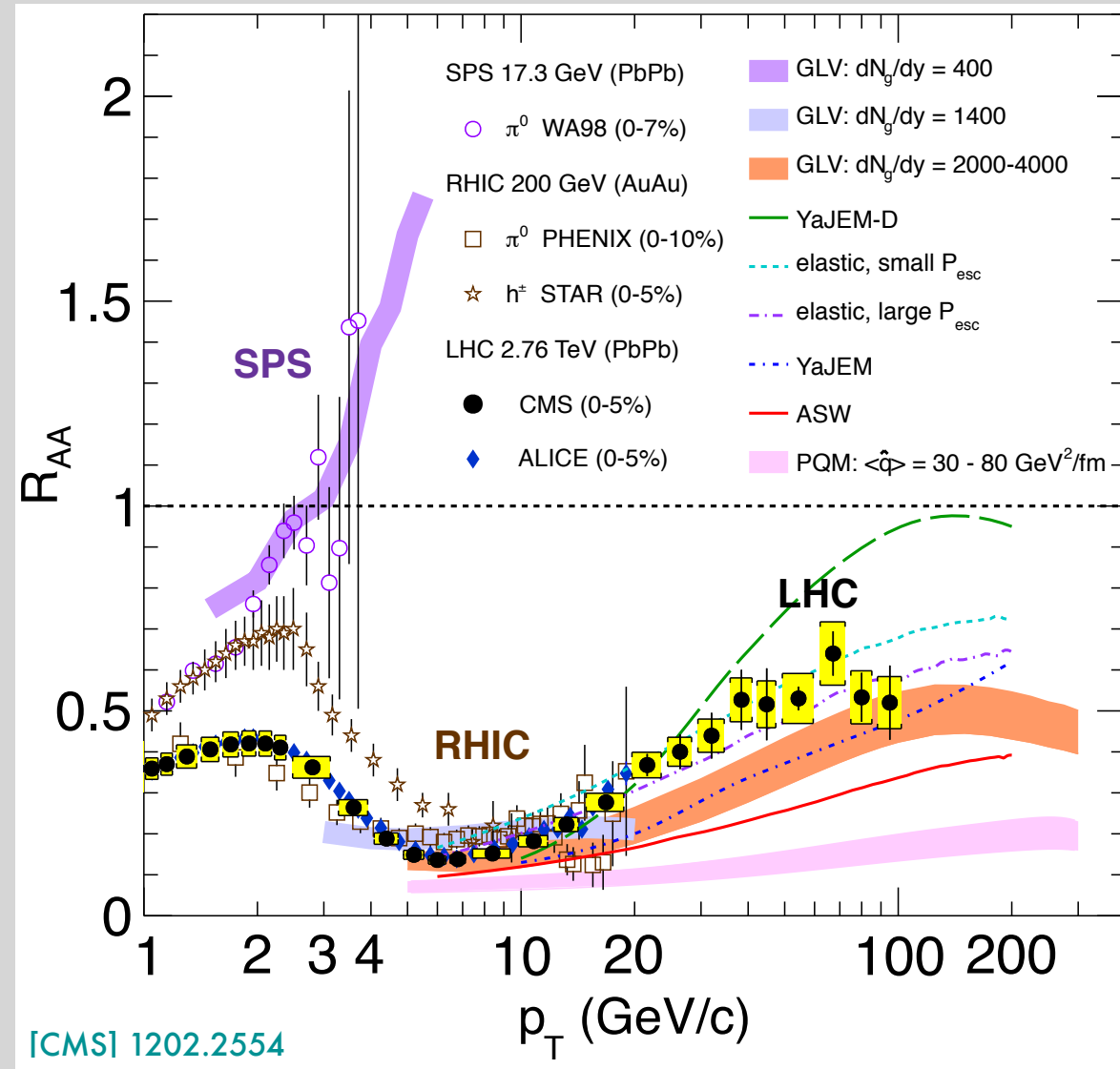
generic [robust] effects:

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modification of jet hadrochemistry
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fragmentation in vacuum NOT the same as using vacuum FFs

sensitivity :: hadron spectra

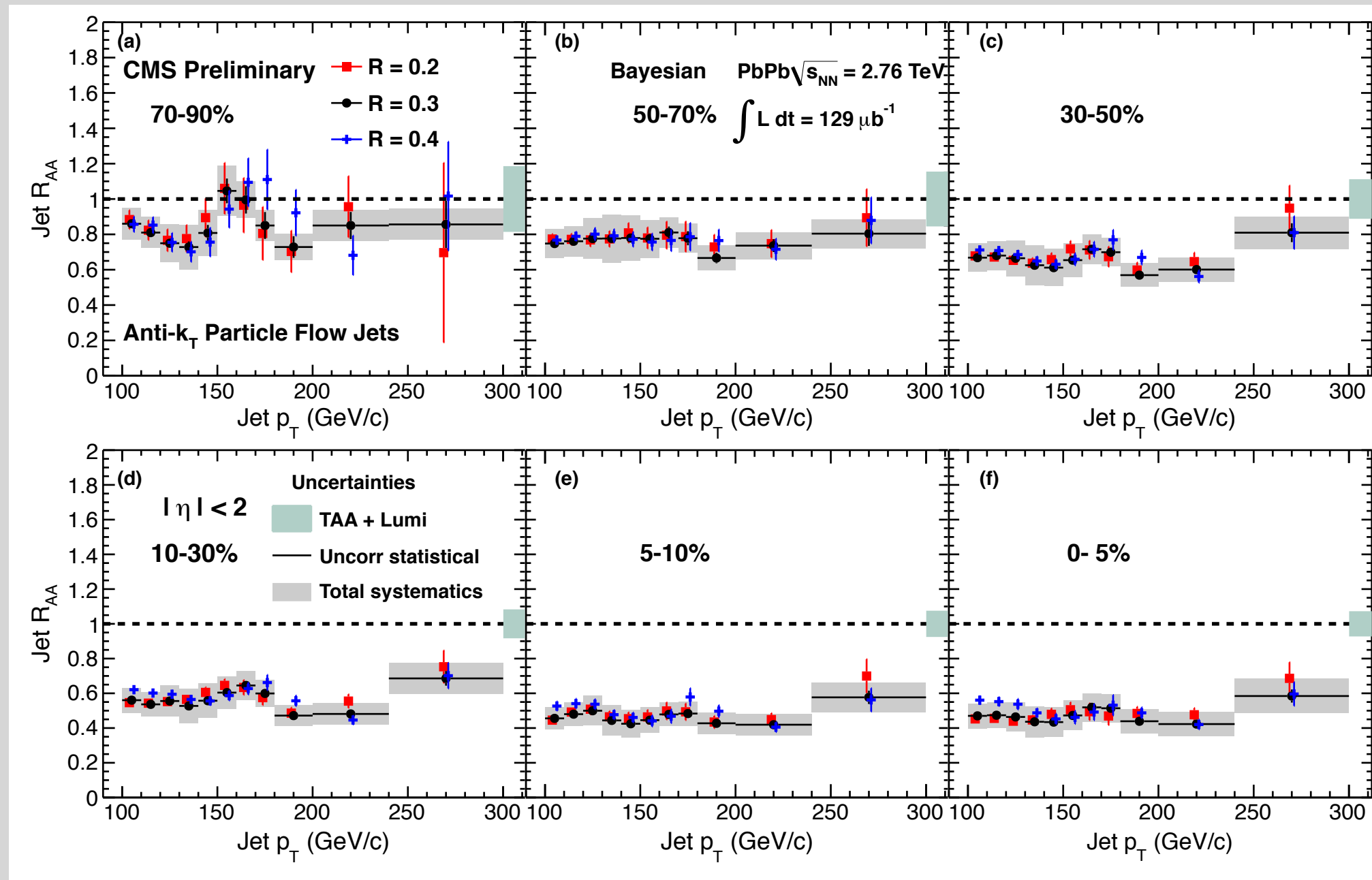


$$R_{AA}(p_T) = \frac{(1/N_{evt}^{AA}) d^2 N_{ch}^{AA} / d\eta dp_T}{\langle N_{coll} \rangle (1/N_{evt}^{pp}) d^2 N_{ch}^{pp} / d\eta dp_T}$$

- clear and strong suppression of all hadronic yields
- ↪ photons/ Z^0 unsuppressed
- ↪ centrality [path-length] dependence

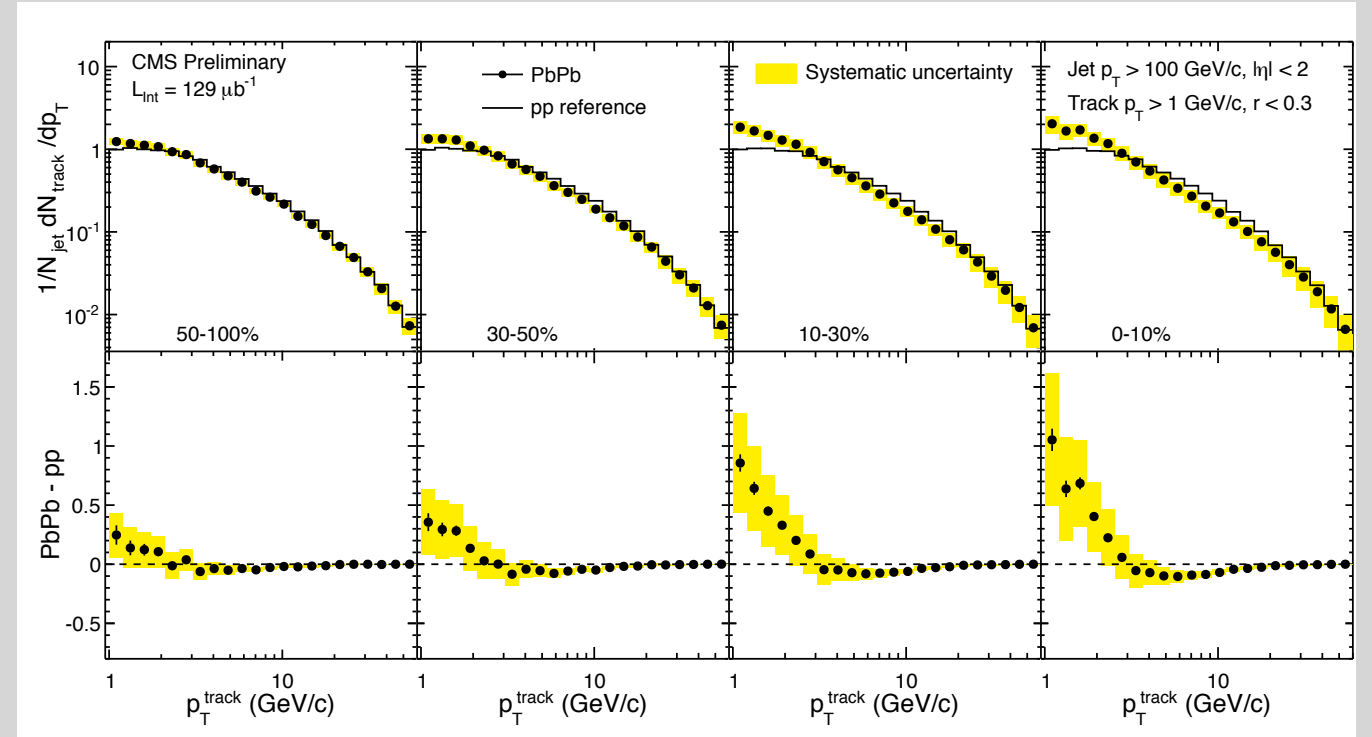
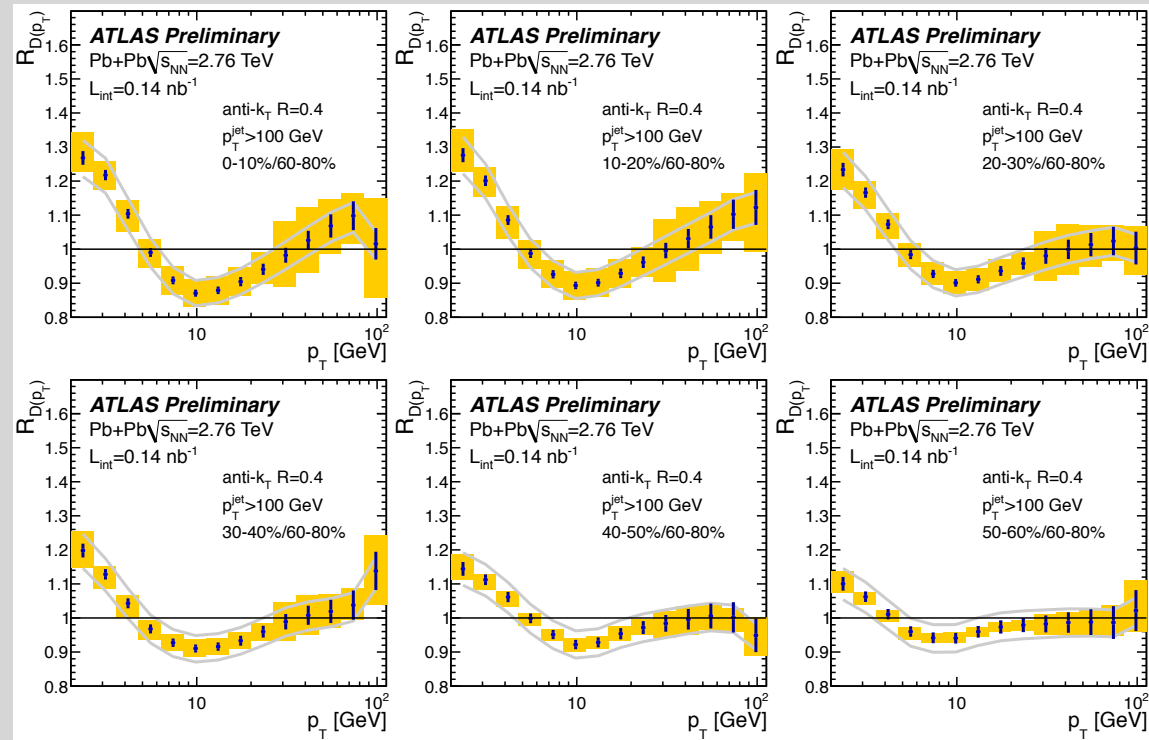
- sensitive to induced radiation, also to hadronization modifications, but NOT to broadening

sensitivity :: jet R_{AA}



- just counts fraction of unmodified jets [steeply falling jet spectrum]
- [recall] dijet asymmetry sensitive to broadening, same for photon jet [advantage of known initial energy, but statically limited]

sensitivity :: fragmentation functions



—○ sensitivity to medium-induced radiation, broadening, hadronization

↪ remarkably similar to vacuum jets [most branching occurs after medium escape; branching within unresolved systems also vacuum like]